

# Local supersymmetry and non-relativistic limits of M-theory

Chris Blair (IFT UAM-CSIC)

SUSY24, IFT UAM-CSIC, 13/06/2024

Based on:

[arXiv:2104.07579](https://arxiv.org/abs/2104.07579) with A. D. Gallegos, N. Zinnato

Work in progress with E. Bergshoeff, J. Lahnsteiner, J. Rosseel

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## **Three lies about supersymmetry**

Absorbed during my Masters many supermoons ago

Don't take this slide too seriously...

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3. 11-dimensional supergravity is unique

Today I will only discuss number 3 (explicitly) and 1 (implicitly)

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## 11-d SUGRA is the unique max SUGRA in max dimension

'Unique' assumes Lorentz invariance

$$S = \int d^{11}x \sqrt{-G} \left( R - \frac{1}{48} F^2 \right) - \frac{1}{6} C \wedge F \wedge F + \text{fermionic}$$

$F_4 = dC_3$        $\Psi_\mu$

$$\delta G_{\mu\nu} \sim \bar{\epsilon} \gamma_{(\mu} \Psi_{\nu)}$$

$$\delta C_{\mu\nu\rho} \sim \bar{\epsilon} \gamma_{[\mu\nu} \Psi_{\rho]}$$

$$\delta \Psi_\mu \sim D_\mu \epsilon + (F \cdot \gamma)_\mu \epsilon$$



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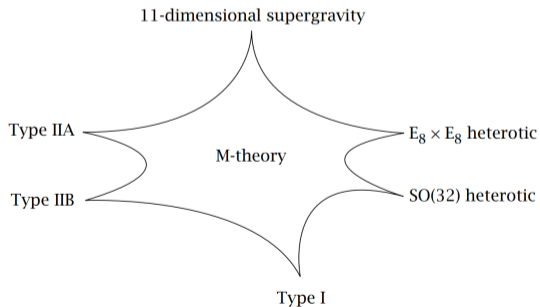
11-d SUGRA: low energy limit of M-theory

Other limits?

**Decoupling limits: focus on simpler sub-sectors.** Can encode surprising amounts of info e.g.

AdS/CFT, Matrix Theory

Examples: **non-relativistic limits**



## Non-relativistic decoupling limits

Can be taken for particles, strings and branes

### o) Point particles

$$S = -mc \int d\tau \sqrt{-\eta_{\mu\nu} \dot{x}^\mu \dot{x}^\nu} + qc \int d\tau A_\mu \dot{x}^\mu$$

$$ds^2 = -c^2 dt^2 + \delta_{ab} dx^a dx^b$$

Special case: BPS  $m = q$ ,  $A_\mu = (c, 0, 0, 0)$

→ cancels rest mass divergence

$$S \rightarrow \frac{1}{2} m \int dt \dot{x}^a \dot{x}^b$$

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Two generalisations:

– extended objects

in string/M-theory [Gomis, Ooguri; Danielsson, Guijosa, Kruczenski 2000]

– curved backgrounds  $ds^2 = (-c^2 \tau_\mu \tau_\nu + \delta_{ab} e^a_\mu e^b_\nu) dx^\mu dx^\nu$ ,  $A_\mu = c\tau_\mu + a_\mu$

unifying modern perspective [CB, Lahnsteiner, Obers, Yan 2023 + WIP]

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## 2) Membranes

$$S = -T \int d^3\sigma \sqrt{-\det G} + T \int C_3$$

$$ds^2 = (c^2 \eta_{AB} \tau^A_\mu \tau^B_\nu + c^{-1} \delta_{ab} e^a_\mu e^b_\nu) dx^\mu dx^\nu$$

$$C_{\mu\nu\rho} = -c^3 \epsilon_{ABC} \tau^A_\mu \tau^B_\nu \tau^C_\rho + C_{\mu\nu\rho}$$

$$A = 0, 1, 2$$

$$a = 3, \dots, 10$$

Units: s.t.  $T \sim 1/\ell_p^3$  fixed,  $c$  dimensionless parameter

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# Taking the membrane decoupling limit in SUGRA

This leads to a non-relativistic SUGRA theory

## Limit of bosons

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[CB, Gallegos, Zinnato 2021]

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$$\Lambda^{\hat{a}}_{\hat{b}} = (\Lambda^A_B, \Lambda^a_b, c^{-3/2} \lambda^a_A)$$

$$\text{SO}(1, 10) \rightarrow \text{SO}(1, 2) \text{ SO}(8) \quad \text{boosts}$$

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## Limit of fermions

$$\Psi_\mu = c^{1/2} \psi_{-\mu} + c^{-1} \psi_{+\mu}$$

$$\gamma_{012} \Psi_{\pm\mu} = \pm \psi_{\pm\mu}$$

c.f. non-rel string limit and  $\mathcal{N} = 1$  SUGRA in 10d

[Bergshoeff et al 2021]

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## Fermionic symmetries

$$\text{SUSY } \epsilon = c^{1/2} \epsilon_- + c^{-1} \epsilon_+$$

## Expanding SUSY must lead to emergent symmetries and constraints

Use the power expansion

$$S = c^3 S_3 + c^0 S_0 + c^{-3} S_{-3} + \dots$$

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Divergent action:  $S_3 \sim - \int f_{abcd}^{(-)} f^{(-)abcd}$

$$f_4 = dc_3, f_{abcd} = e^\mu{}_a \dots f_{\mu\nu\rho\sigma}$$
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**Upshot:**

$\delta_3 S_0 = 0 \Rightarrow$  emergent fermionic symmetry of  $S_0$

$\delta_0 S_0 = -\delta_3 S_{-3} \Rightarrow S_0$  invariance needs  $\delta_3 \equiv 0 \Rightarrow$  constraints



## Constraints beget constraints

Max SUSY or half-max SUSY?

$$\delta_3(\text{bosons}) = 0$$

$$\delta_3(\text{fermions}) \neq 0$$

$$\begin{aligned} \epsilon_+ \times T_{ab}{}^A \\ \epsilon_- \times T_a{}^{\{AB\}}, f_{Aabc}, f_{abcd}^{(+)} \end{aligned}$$

$$T_{\mu\nu}{}^A = 2\partial_{[\mu}\tau^A{}_{\nu]}$$

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**Option 1: Half-maximal SUSY**  $\epsilon_+ \neq 0, \epsilon_- = 0$

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**Option 1: Half-maximal SUSY**  $\epsilon_+ \neq 0, \epsilon_- = 0$

$$T_{ab}{}^A = 0 \xrightarrow{\delta_0} f_{abcd} = 0$$

**Option 2: Maximal SUSY**  $\epsilon_{\pm} \neq 0$

$$T_{ab}{}^A, T_a{}^{\{AB\}}, f_{Aabc}, f_{abcd}^{(+)} = 0 \xrightarrow{\delta_0} \text{fermionic curvatures} \xrightarrow{\delta_0} \text{bosonic curvatures} \xrightarrow{\delta_0} \dots$$
$$\partial\tau \xrightarrow{\delta_0} \partial\psi_{\pm} \xrightarrow{\delta_0} \partial^2\tau \xrightarrow{\delta_0} \partial^2\psi_{\pm} \xrightarrow{\delta_0} \partial^3\tau \xrightarrow{\delta_0} \dots ???$$

## A maximally SUSY solution exists

It may be easier to find solutions than the theory itself...

	0	1	2	3	4	5	6	7	8	9	10
Non-rel membrane limit	×	×	×	-	-	-	-	-	-	-	-
M2 solution	×	-	-	×	×	-	-	-	-	-	-

Holographically dual to non-rel limit of a 3d SCFT (ABJM) [Lambert-Smith 2024]

$$\tau^0 = \mathcal{H}^{-1/3} dx^0 \quad \tau^\alpha = \mathcal{H}^{1/6} dx^\alpha$$

$$\alpha = 1, 2$$

$$e^m = \mathcal{H}^{-1/3} dx^m \quad e^l = \mathcal{H}^{1/6} dx^l$$

$$m = 3, 4$$

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$$c_{034} = \mathcal{H}^{-1} \quad \lambda_{abcd} = 0$$

$$\mathcal{H} = \mathcal{H}(x^1, x^2)$$

$$= ((x^1)^2 + (x^2)^2)^{-3} \text{ for M2 near horizon}$$

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All physical curvatures zero  $\rightarrow$  all (possible) constraints obeyed

$\exists$  Killing spinor solution with 32 independent parameters using both SUSY and emergent fermionic shift symmetry

# Non-relativistic supersymmetry in 11 dimensions is a complicated beast

Despite many constraints, it seems that it is a non-trivial theory

## Membrane non-relativistic limit:

half-maximal SUSY  $\leftrightarrow$  simple constraints

maximal SUSY  $\leftrightarrow$  complicated constraints

... but  $\exists$  (surprisingly) non-trivial interesting solution

$\rightarrow$  dimensional reduction and type II maximal SUGRA?

$\rightarrow$  new novel holographic dualities?

$\rightarrow$  this limit is U-dual to M-theory on a null circle  $\rightarrow$  Matrix Theory

## Five-brane non-relativistic limit:

further non-uniqueness of non-relativistic 11-d SUGRA

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**Thanks for listening!**