

Species scale, worldsheet CFTs and emergent geometry

Christian Aoufia

based on 2405.03683 [CA, Ivano Basile, Giorgio Leone]



SUSY24, Madrid, 13/06/2024

(see Alberto's parallel)

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However, it's crucial to know what happens when we give it up, and even more so in String Theory

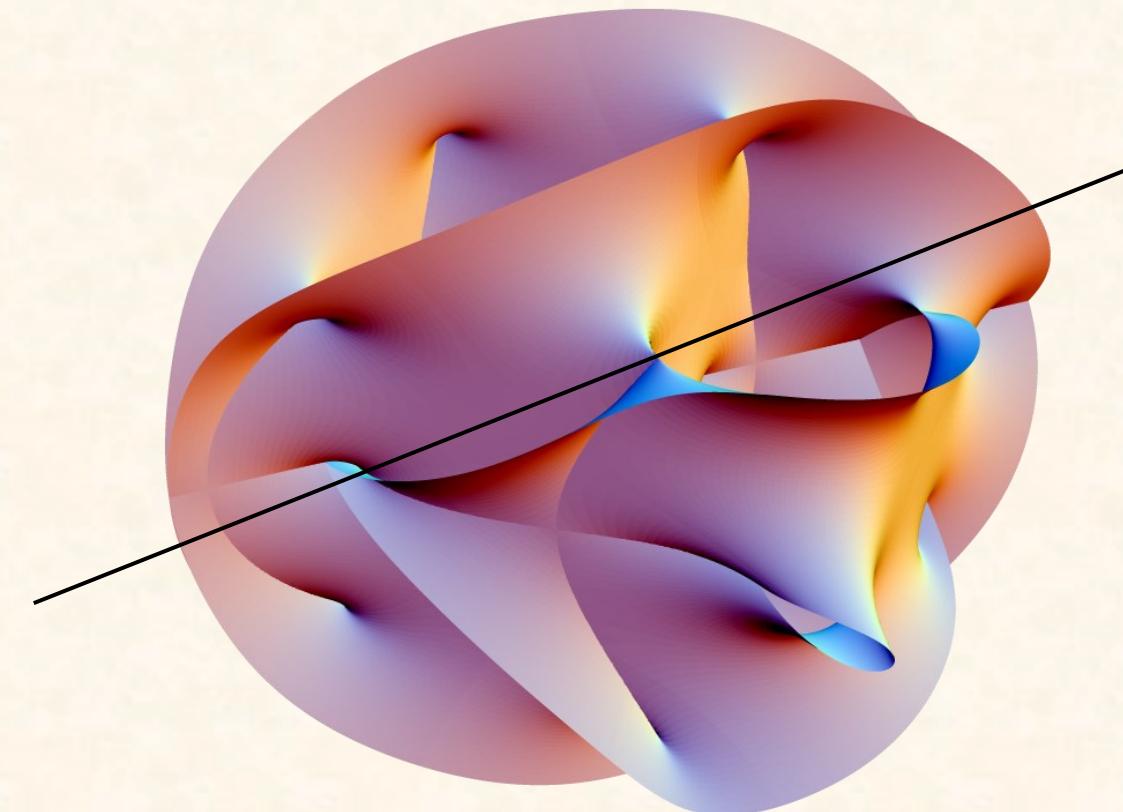
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Here we will try to do even more!

~~SUSY~~

+



Does string theory need extra dimensions¹ ?

1) *in the «classical sense» and asymptotically far in moduli space.*

The known story: worldsheet sigma model

- ⊕ Polyakov action:

$$\mathcal{S} = \frac{1}{2\pi\alpha'} \int d^2\sigma \, G_{\mu\nu}(X) \partial X^\mu \bar{\partial} X^\nu$$

The known story: worldsheet sigma model

- + Polyakov action:

$$\mathcal{S} = \frac{1}{2\pi\alpha'} \int d^2\sigma G_{\mu\nu}(X) \partial X^\mu \bar{\partial} X^\nu \quad \text{«geometric»}$$

«*spacetime metric*»

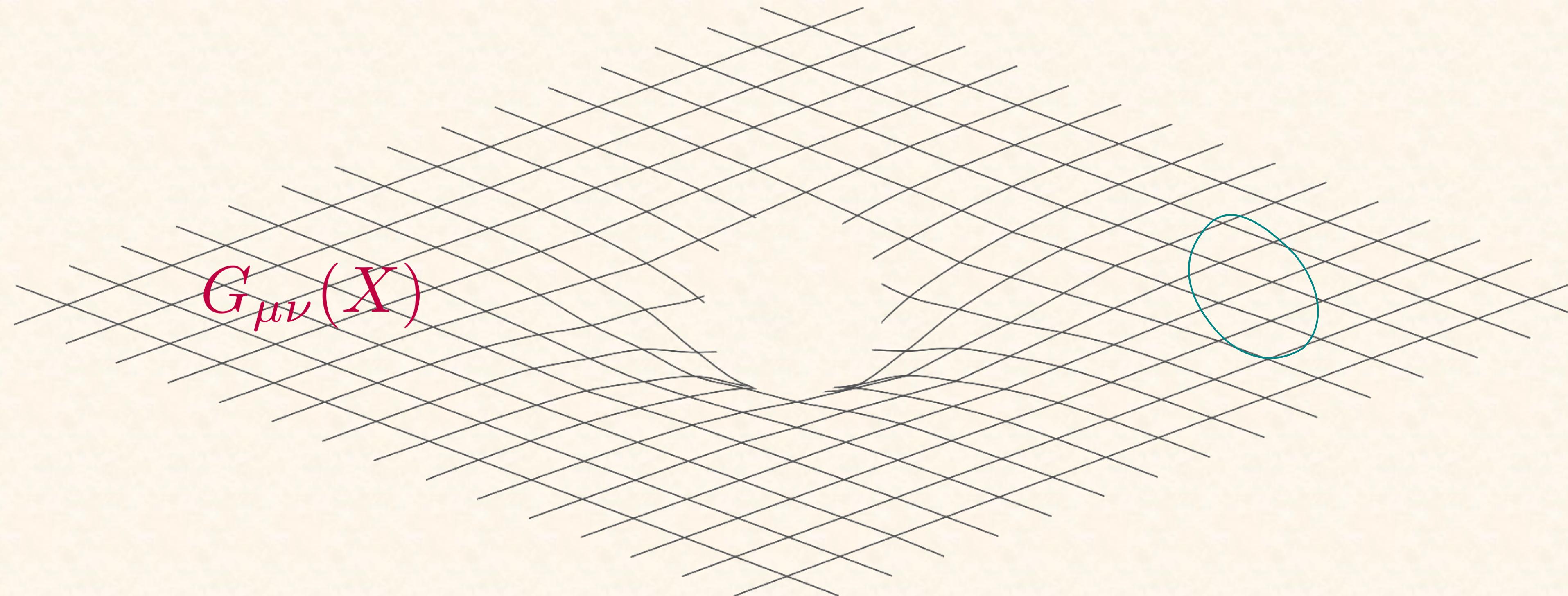
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«*target space metric*»

«*worldsheet coordinates*»

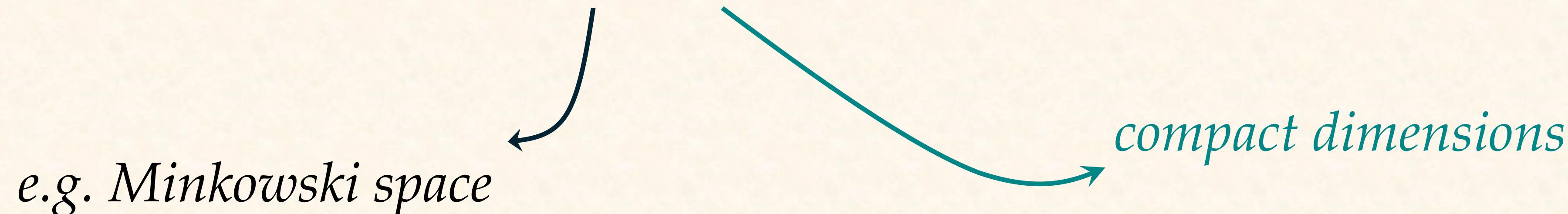
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«*2d CFT fields*»



The known story: worldsheet sigma model

- ⊕ Consider a spacetime of type $\mathcal{M}_d \times \mathcal{N}$.



The known story: worldsheet sigma model

- ⊕ Consider a spacetime of type $\mathcal{M}_d \times \mathcal{N}$.
- ⊕ Consistency of the worldsheet theory demands that

c central charge of CFT on \mathcal{N} proportional to number of compact dimensions.
(«*internal CFT*»)

The known story: worldsheet sigma model

- ⊕ Consider a spacetime of type $\mathcal{M}_d \times \mathcal{N}$.
- ⊕ c central charge of CFT on \mathcal{N} proportional to number of compact dimensions.
- ⊕ The action looks like

$$\mathcal{S}(\textcolor{red}{t}) = \frac{1}{2\pi\alpha'} \int d^2\sigma G_{ab}^{\mathcal{N}}(X, \textcolor{red}{t}) \partial X^a \bar{\partial} X^b$$

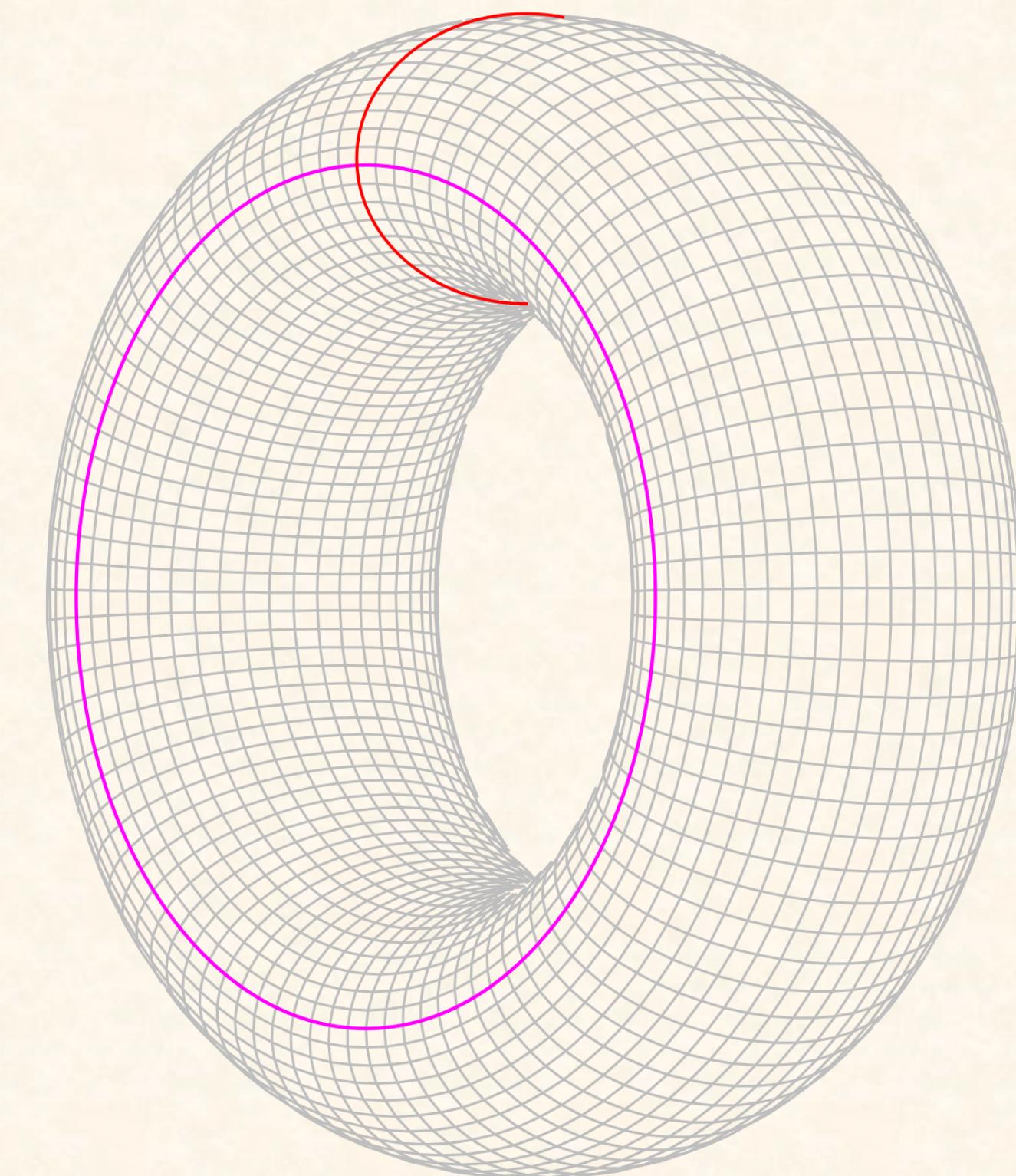
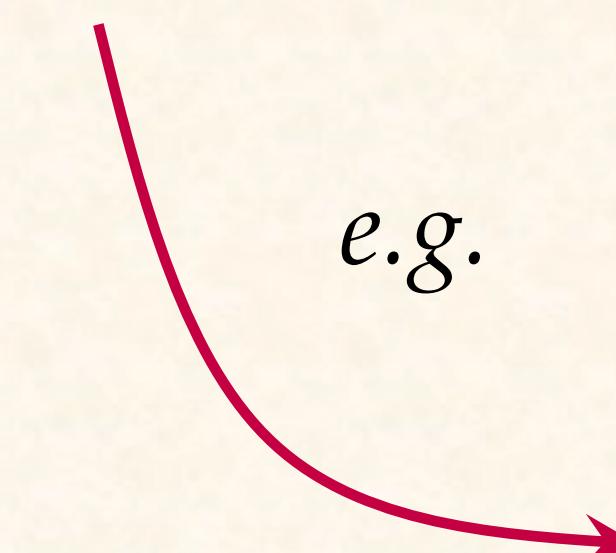
«moduli fields»

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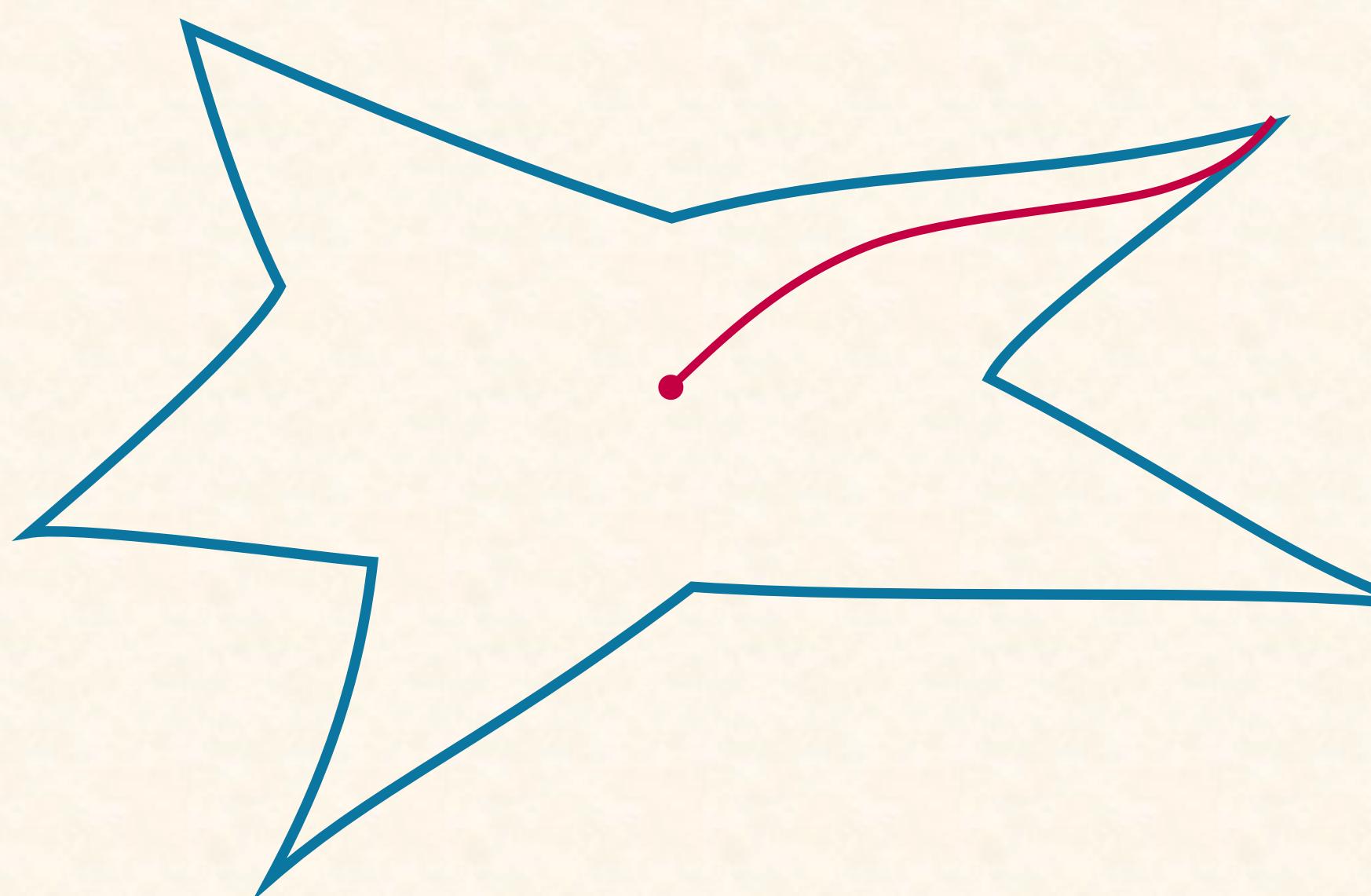
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- ⊕ The moduli fields t parametrize **marginal deformations** of the CFT on \mathcal{N} .



*«moduli space»
(conformal manifold)*

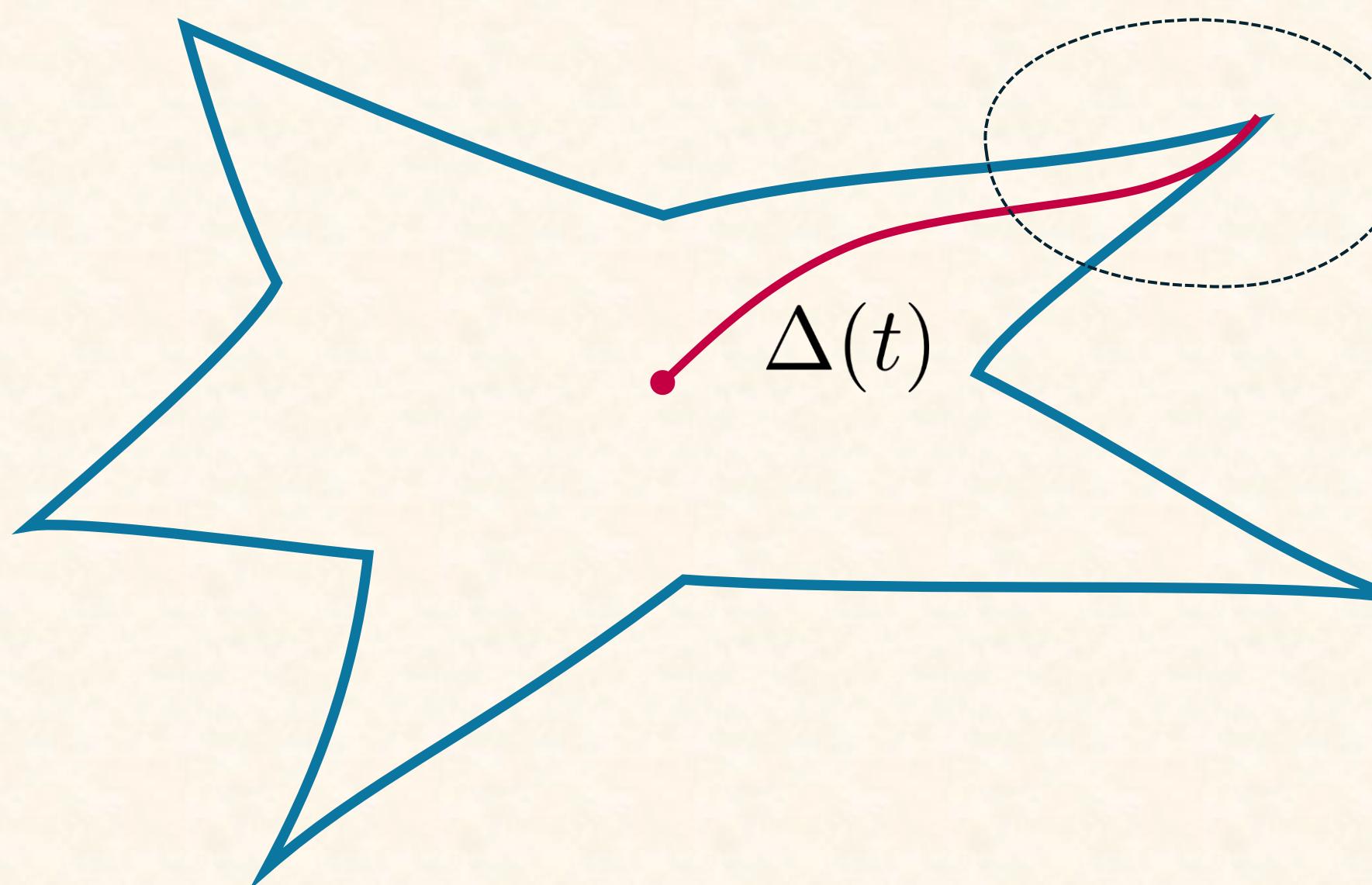
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infinite distance limits (Zamolodchikov metric)

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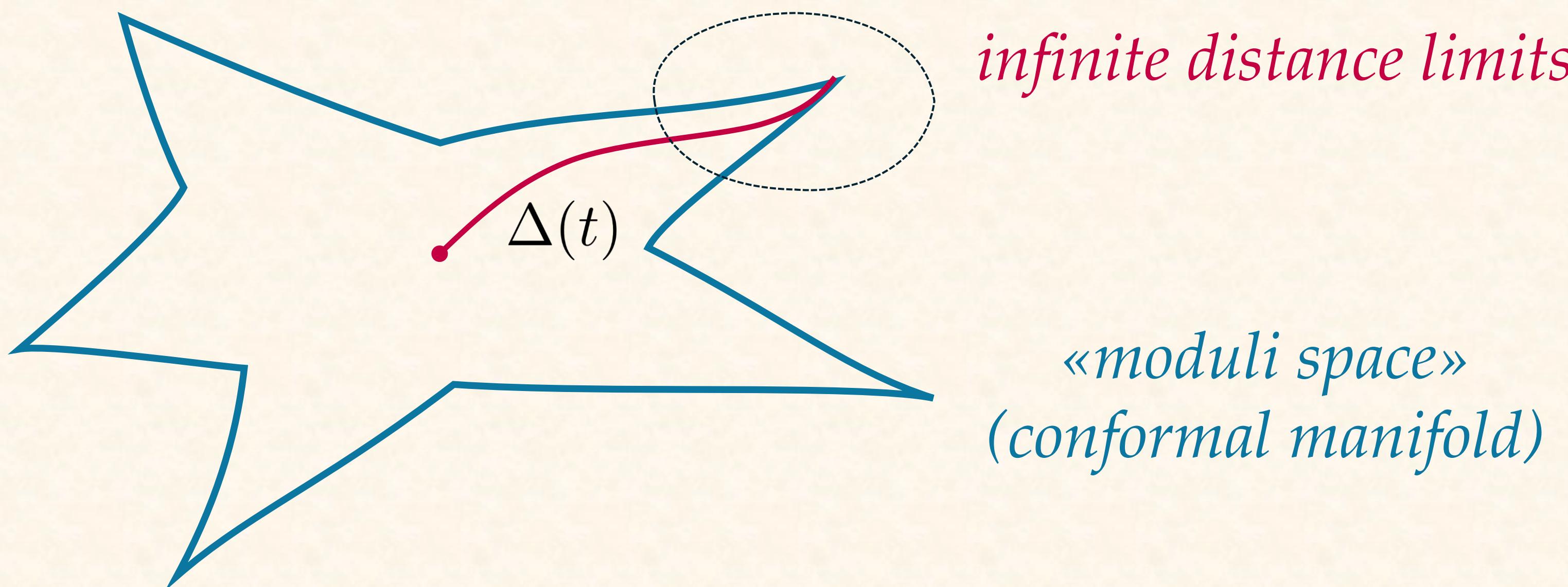
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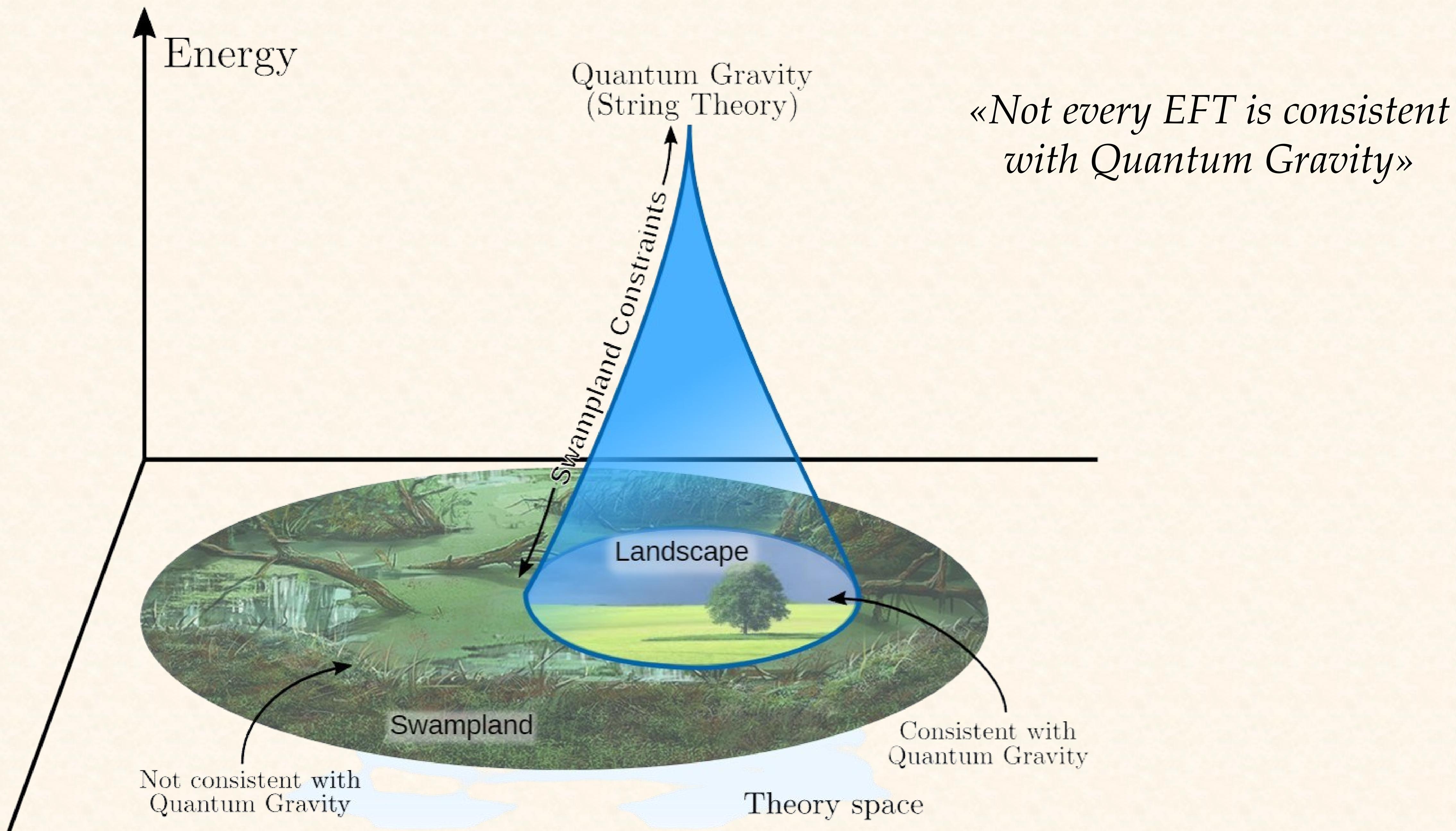
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Mandatory Swampland Slide

[Vafa '05]



[van Beest, Calderon-Infante, Mirfendereski, Valenzuela '21]

Emergent String Conjecture (ESC)

[Lee,Lerche,Weigand '19]

- ⊕ Swampland Distance Conjecture (SDC) [Ooguri, Vafa '06; Perlmutter, Rastelli, Vafa, Valenzuela '21]

$$\Delta(\textcolor{red}{t}) \rightarrow \infty \quad \Rightarrow \quad \frac{m}{M_{\text{Pl}}} \sim e^{-\lambda \Delta}$$

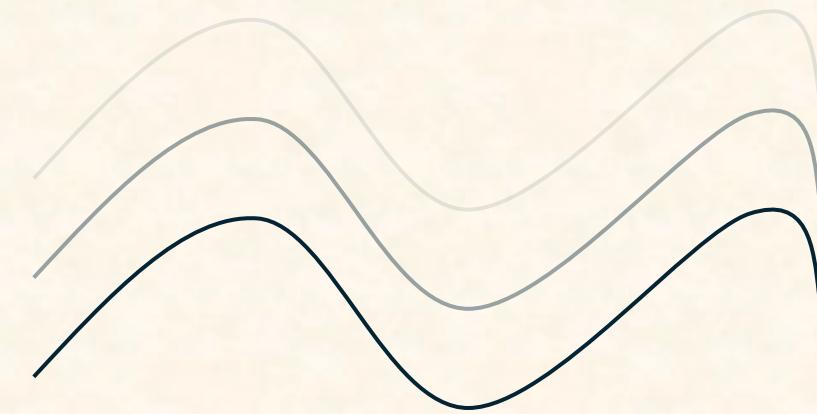
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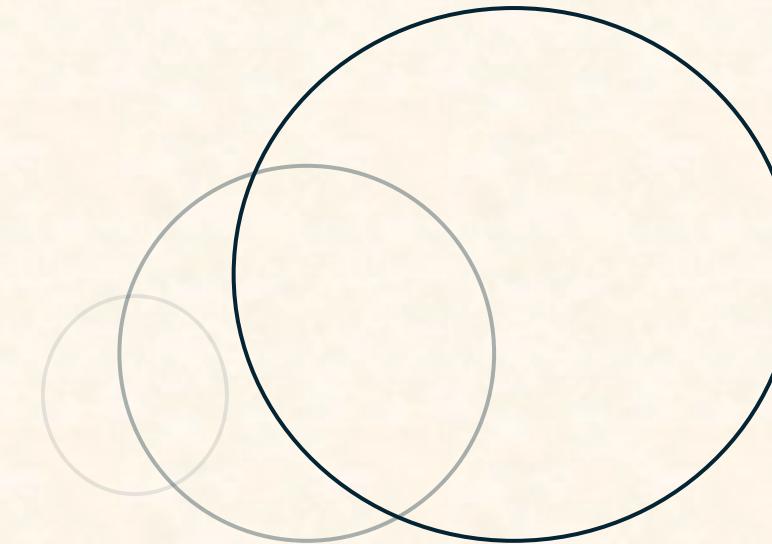
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- ⊕ Emergent String Conjecture: towers can only be of two types



or



«(critical) String tower»

«Kaluza-Klein (KK) tower»

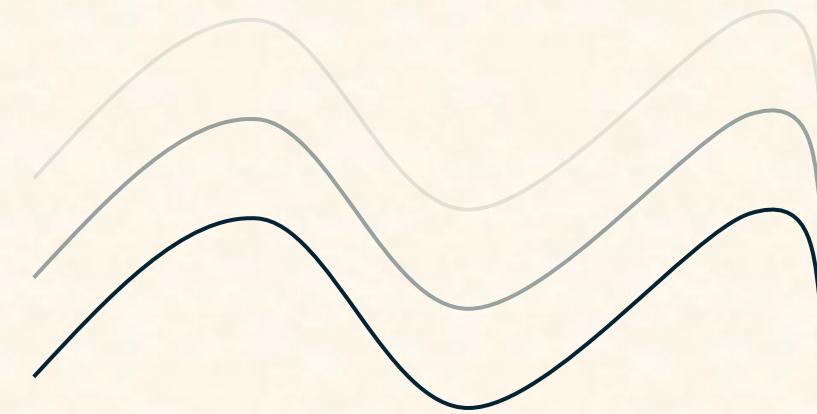
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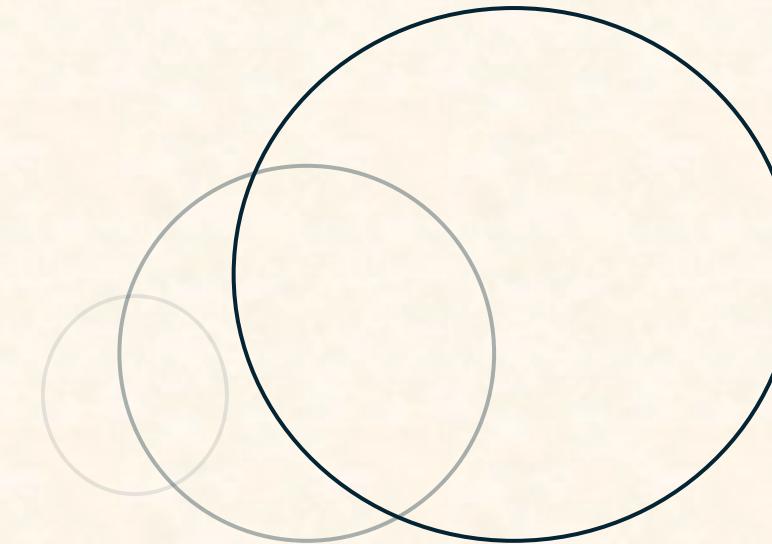
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probed by worldsheet theory on N

\Rightarrow *every infinite distance limit is «geometric»*

(see Veronica and Ignacio's parallels)

However, the worldsheet theory can be more general
than a non-linear sigma model...

«non-geometric models»

(e.g. asymmetric orbifolds, i.e. left and right moving excitations of a string move in different spacetimes)

(not clear if they are all perturbatively connected to geometric ones)

[Kawai, Lewellen, Tye '86; Narain, Sarmadi, Vafa '87; Lerche, Lust, Schellekens '87; Antoniadis, Bachas, Kounnas '87;
Antoniadis, Bachas '88; Gepner '1988; Green, Hubsch '88; Kamaza, Suzuki '89; Vafa, Warner '89; Witten '93; Kachru, Vafa '95;
Angelantonj, Bainchi, Pradisi, Sagnotti, Stanev '96; Blumenhagen, Wisskirchen '98; Israël and V. Thiéry '14;
Hull, Israël, Sarti '17; Gkountoumis, Hull, Stemerdink, Vandoren '23; baykara, hamada, Tarazi, Vafa '23; Baykara, Tarazi, Vafa '24]

*Given a generic worldsheet internal CFT,
possibly non-geometric and non-supersymmetric...*

Does geometry «emerge» at infinite distance?

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(spoiler: yes!)

Worldsheet CFT and emergent geometry

- Take a generic (internal) CFT¹, and compute its (reduced) torus partition function

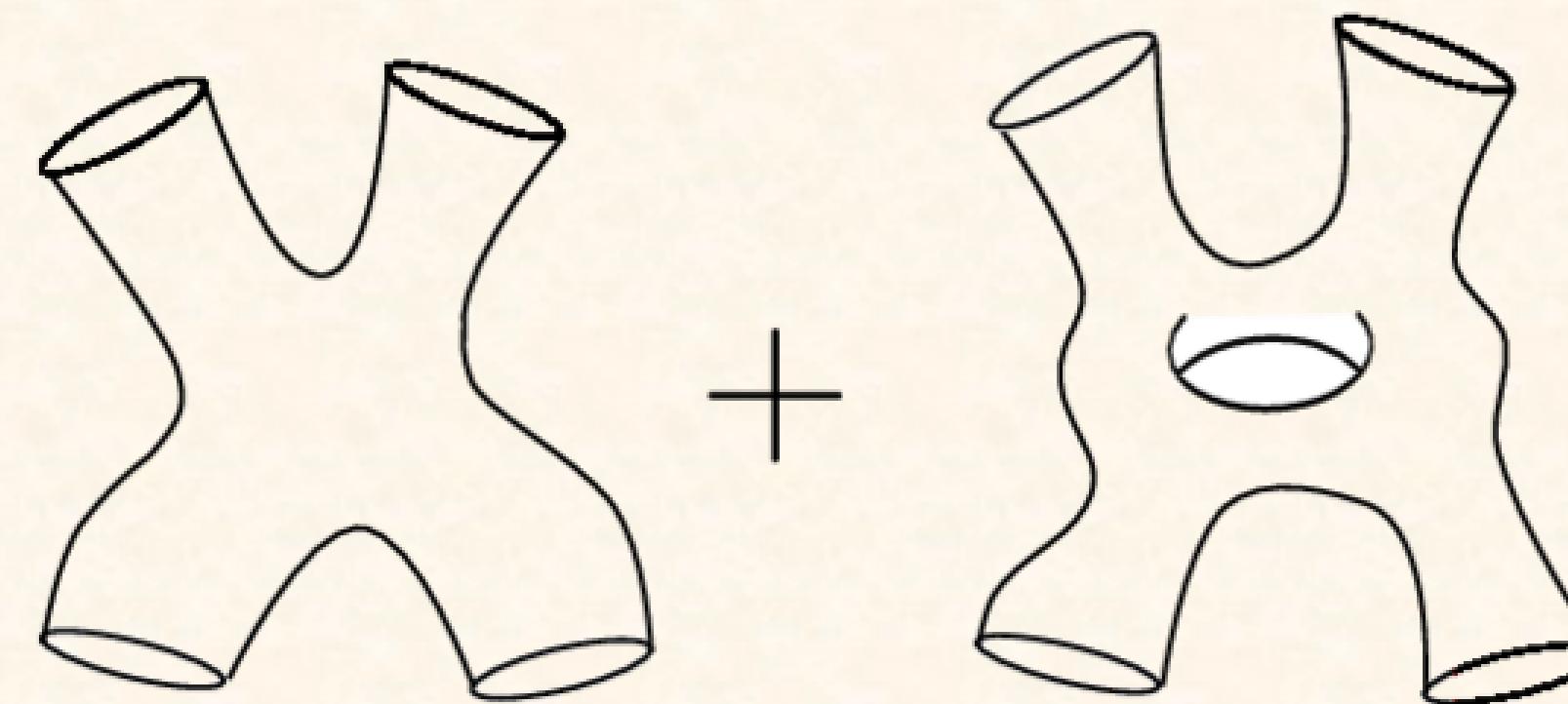
$$Z(\textcolor{red}{t}) = \int_{\mathcal{F}} d\mu \mathcal{Z}_{T^2}(\textcolor{red}{t})$$

↓
«fundamental domain»

«modulus» ←

$$\alpha = 2^{-6} \left(\frac{\ell_s}{\ell_{\text{Pl}}} \right)^{8-d} \left(2\zeta(3) \left(\frac{\ell_s}{\ell_{\text{Pl}}} \right)^{d-2} + 2\pi Z(t) \right)$$

1-loop Wilson coefficient of \mathcal{R}^4



1) $c_L = c_R = c$

Worldsheet CFT and emergent geometry

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- ⊕ The (modular) integrand contains information about the spectrum dependence on t

$$\mathcal{Z}_{T^2}(t) \equiv y^{c/2} \sum_{j, \Delta} e^{2\pi i j x} e^{-2\pi \Delta(t) y}$$

«conformal weights» of CFT states

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Assume SDC: $\Delta_{\text{light}}(t) \sim \frac{\Delta^*}{t}$ as $t \rightarrow \infty$ + $\Delta_{\text{heavy}}(t) \rightarrow \infty$ as $t \rightarrow \infty$

(*bonus: in the paper, derive presence
of a tower from diverging Wilson coefficient*)

exponential decay: [Ooguri, Wang '24]

(*bonus: in the paper, relax this assumption to include
parametrically constant conformal weights*)

Then, compare with the geometric case...

$$Z(t) \stackrel{t \gg 1}{\sim} t^{c/2} \equiv \Delta_{\text{gap}}(t)^{-c/2} \quad \text{vs} \quad Z_{\text{geometric}} \stackrel{\mathcal{V} \gg 1}{\sim} \mathcal{V} \equiv \Delta_{\text{gap}}^{-c/2}$$

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The Wilson coefficient is:

$$\alpha_{\text{1-loop}} \stackrel{t \gg 1}{\sim} \left(\frac{M_{\text{Pl}}}{M_s} \right)^{8-(c+d)} \left(\frac{m_{\text{gap}}}{M_{\text{Pl}}} \right)^{-c} = \left(\frac{\Lambda_{\text{sp}}}{M_{\text{Pl}}} \right)^{-6}$$

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They are the same!

In this sense, starting from a generic CFT, geometry «emerges» at infinite distance.

Take home message

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- ⊕ It is important to understand what happens in the non-geometric and non-susy string landscape;
- ⊕ Abandoning geometry, and focusing on pure CFT quantities, we were able to show that *asymptotically* in moduli space, a certain Wilson coefficient in the EFT scales as in the geometric case (*and much more in the paper ☺*);

Thank you!