

$$\mathcal{O}_{HG} = H^\dagger H G_{\mu\nu}^A G^{A\mu\nu}$$

$$\mathcal{O}_{HB} = H^\dagger H B_{\mu\nu} B_{\mu\nu}$$

$$\mathcal{O}_{HD} = (H^\dagger D_\mu H)^2$$

$$\mathcal{O}_{ll} = (\bar{l}_p \gamma_\mu l_q)$$

$$\mathcal{O}_{lq}^{(1)} = (\bar{l}_p \gamma_\mu l_q) (q_r \gamma^\mu q_s)$$

Mapping the SMEFT one-loop structure of linear SM extensions

John Gargalionis, Jérémie Quevillon, Pham Ngoc Hoa Vuong, Tevong You

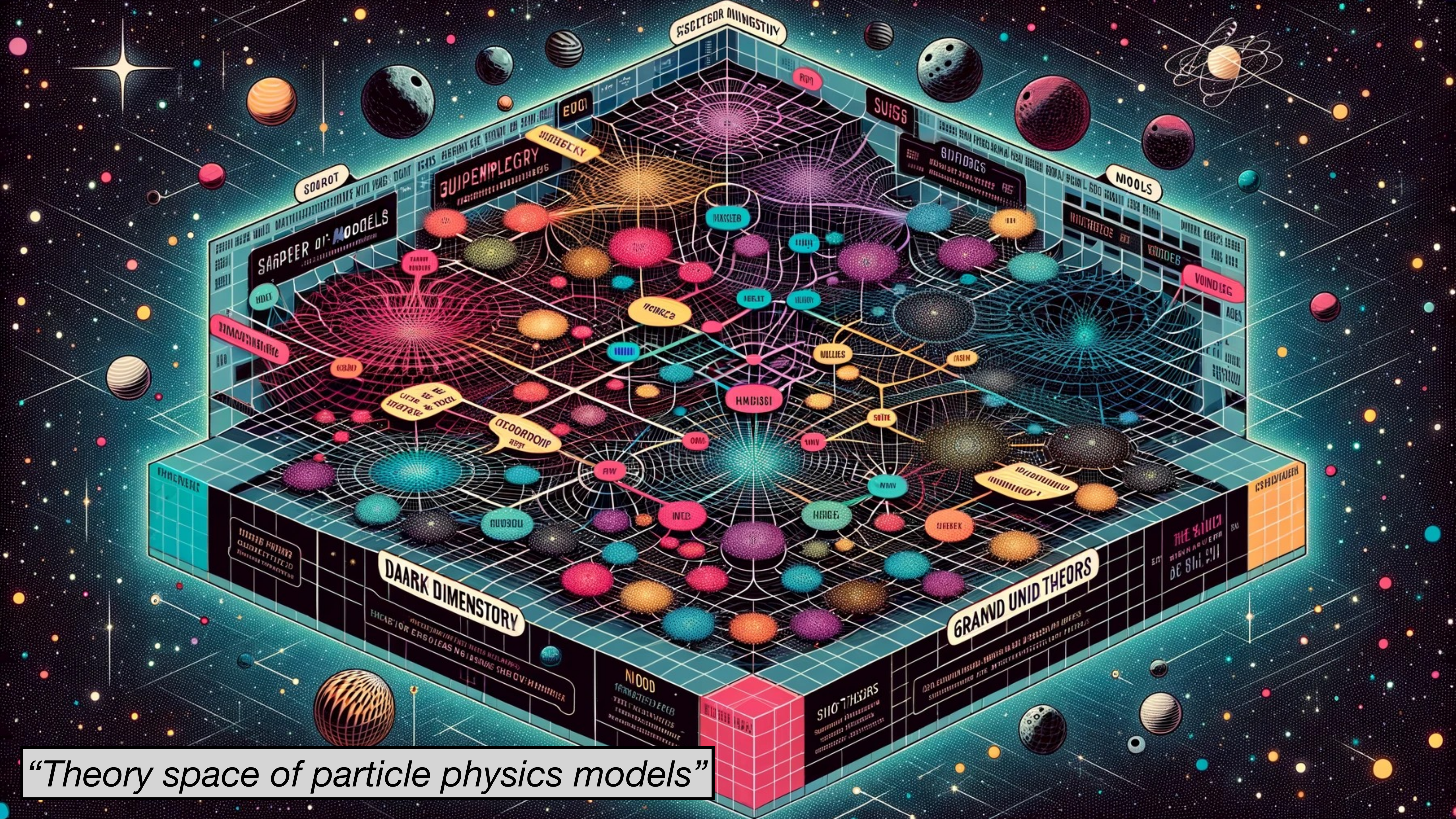
[arXiv: 24XX.XXXXX]



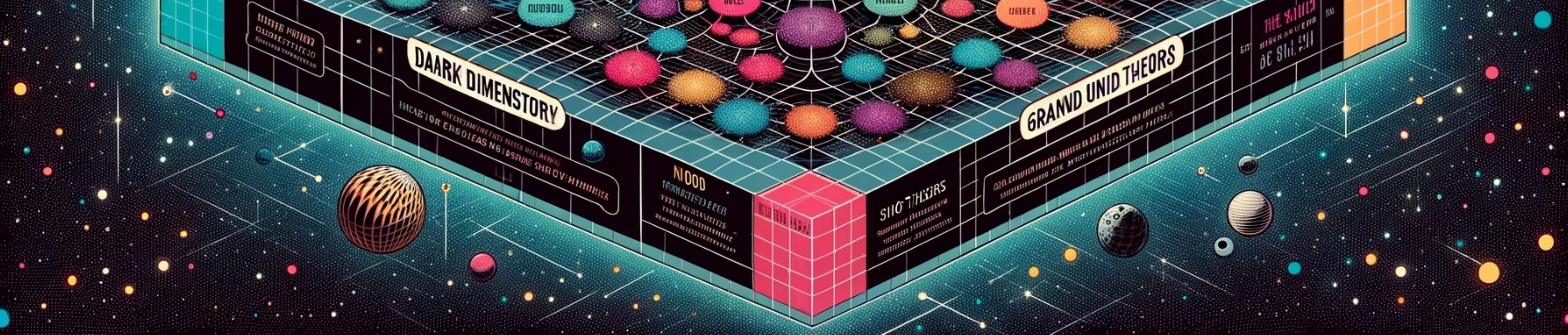
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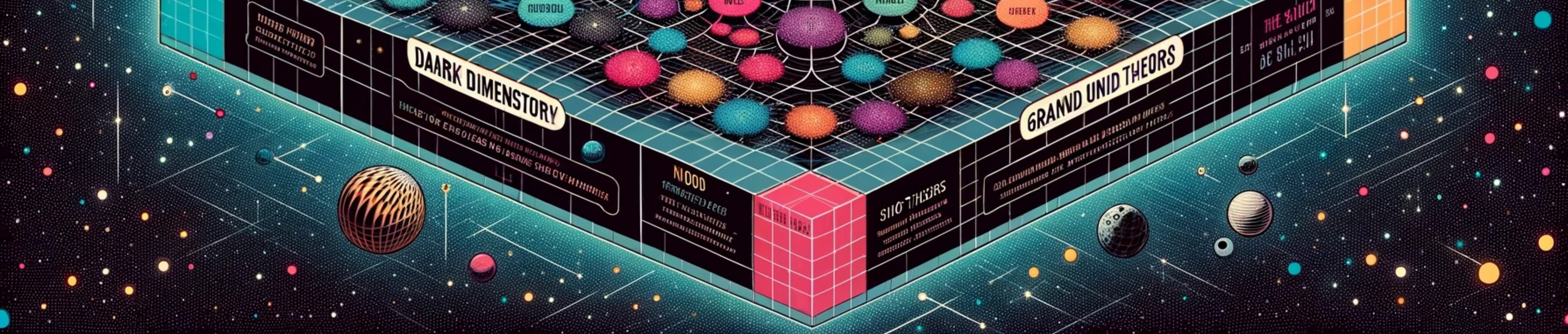


“Theory space of particle physics models”



$$H \sim (1, 2, \frac{1}{2}), \quad Q \sim (3, 2, \frac{1}{6}), \quad \bar{u} \sim (\bar{3}, 1, -\frac{2}{3}), \quad \bar{d} \sim (\bar{3}, 1, \frac{1}{3}), \quad L \sim (1, 2, -\frac{1}{2}), \quad \bar{e} \sim (1, 1, 1)$$

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_{p,q} c_{pq}^{(5)} (L_p L_q) H H + \sum_{i=1}^{2499} \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{d=6} + \dots$$



Bottom-up approach



UV/IR dictionary



Top-down approach

$$H \sim (1, 2, \frac{1}{2}), \quad Q \sim (3, 2, \frac{1}{6}), \quad \bar{u} \sim (\bar{3}, 1, -\frac{2}{3}), \quad \bar{d} \sim (\bar{3}, 1, \frac{1}{3}), \quad L \sim (1, 2, -\frac{1}{2}), \quad \bar{e} \sim (1, 1, 1)$$

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_{p,q} c_{pq}^{(5)} (L_p L_q) H H + \sum_{i=1}^{2499} \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{d=6} + \dots$$

Linear SM extensions

Granada dictionary: de Blas, Criado, Pérez-Victoria, Santiago arXiv:1711.10391
 MatchingTools: Criado arXiv:1710.06445

- Patterns of **minimal tree-level deviation** from the SM can be understood in terms of **linear SM extensions**

$$\mathcal{L}_{\text{int}} \sim \text{SM} \cdot \text{SM} \cdot X + \text{SM} \cdot \text{SM} \cdot \text{SM} \cdot X + \dots$$

- **48 exotic multiplets** generating $d = 6$ operators at tree level
- Catalogued in the Granada dictionary
- Fermions are **vector-like** or Majorana

| Name | \mathcal{S} | \mathcal{S}_1 | \mathcal{S}_2 | φ | Ξ | Ξ_1 | Θ_1 | Θ_3 |
|-------|-------------------------|-------------------------|-------------------------|------------------------|------------------------|-------------------------|------------------------|------------------------|
| Irrep | $(1, 1)_0$ | $(1, 1)_1$ | $(1, 1)_2$ | $(1, 2)_{\frac{1}{2}}$ | $(1, 3)_0$ | $(1, 3)_1$ | $(1, 4)_{\frac{1}{2}}$ | $(1, 4)_{\frac{3}{2}}$ |
| Name | ω_1 | ω_2 | ω_4 | Π_1 | Π_7 | ζ | | |
| Irrep | $(3, 1)_{-\frac{1}{3}}$ | $(3, 1)_{\frac{2}{3}}$ | $(3, 1)_{-\frac{4}{3}}$ | $(3, 2)_{\frac{1}{6}}$ | $(3, 2)_{\frac{7}{6}}$ | $(3, 3)_{-\frac{1}{3}}$ | | |
| Name | Ω_1 | Ω_2 | Ω_4 | Υ | Φ | | | |
| Irrep | $(6, 1)_{\frac{1}{3}}$ | $(6, 1)_{-\frac{2}{3}}$ | $(6, 1)_{\frac{4}{3}}$ | $(6, 3)_{\frac{1}{3}}$ | $(8, 2)_{\frac{1}{2}}$ | | | |

Table 1. New scalar bosons contributing to the dimension-six SMEFT at tree level.

| Name | N | E | Δ_1 | Δ_3 | Σ | Σ_1 | | |
|-------|------------------------|-------------------------|-------------------------|-------------------------|------------------------|-------------------------|------------------------|--|
| Irrep | $(1, 1)_0$ | $(1, 1)_{-1}$ | $(1, 2)_{-\frac{1}{2}}$ | $(1, 2)_{-\frac{3}{2}}$ | $(1, 3)_0$ | $(1, 3)_{-1}$ | | |
| Name | U | D | Q_1 | Q_5 | Q_7 | T_1 | T_2 | |
| Irrep | $(3, 1)_{\frac{2}{3}}$ | $(3, 1)_{-\frac{1}{3}}$ | $(3, 2)_{\frac{1}{6}}$ | $(3, 2)_{-\frac{5}{6}}$ | $(3, 2)_{\frac{7}{6}}$ | $(3, 3)_{-\frac{1}{3}}$ | $(3, 3)_{\frac{2}{3}}$ | |

Table 2. New vector-like fermions contributing to the dimension-six SMEFT at tree level.

Tree-level UV/IR dictionary

Granada dictionary: de Blas, Criado, Pérez-Victoria, Santiago arXiv:1711.10391
 MatchingTools: Criado arXiv:1710.06445

Top-down

UV

IR

| Fields | Operators |
|-----------------|---|
| \mathcal{S} | $\mathcal{O}_{\phi 4}, \mathcal{O}_{\phi}, \mathcal{O}_{\phi\Box}, \mathcal{O}_{\phi B}, \mathcal{O}_{\phi\bar{B}}, \mathcal{O}_{\phi W}, \mathcal{O}_{\phi\bar{W}}, \mathcal{O}_{\phi G}, \mathcal{O}_{\phi\bar{G}}, \mathcal{O}_{e\phi}, \mathcal{O}_{d\phi}, \mathcal{O}_{u\phi}$ |
| \mathcal{S}_1 | \mathcal{O}_{ll} |
| \mathcal{S}_2 | \mathcal{O}_{ee} |
| φ | $\mathcal{O}_{le}, \mathcal{O}_{qu}^{(1)}, \mathcal{O}_{qu}^{(8)}, \mathcal{O}_{qd}^{(1)}, \mathcal{O}_{qd}^{(8)}, \mathcal{O}_{ledq}, \mathcal{O}_{quqd}^{(1)}, \mathcal{O}_{lequ}^{(1)}, \mathcal{O}_{\phi}, \mathcal{O}_{e\phi}, \mathcal{O}_{d\phi}, \mathcal{O}_{u\phi}$ |
| Ξ | $\mathcal{O}_{\phi 4}, \mathcal{O}_{\phi}, \mathcal{O}_{\phi D}, \mathcal{O}_{\phi\Box}, \mathcal{O}_{\phi WB}, \mathcal{O}_{\phi W\bar{B}}, \mathcal{O}_{e\phi}, \mathcal{O}_{d\phi}, \mathcal{O}_{u\phi}$ |
| Ξ_1 | $\mathcal{O}_{\phi 4}, \mathcal{O}_5, \mathcal{O}_{ll}, \mathcal{O}_{\phi}, \mathcal{O}_{\phi D}, \mathcal{O}_{\phi\Box}, \mathcal{O}_{e\phi}, \mathcal{O}_{d\phi}, \mathcal{O}_{u\phi}$ |
| Θ_1 | \mathcal{O}_{ϕ} |
| Θ_3 | \mathcal{O}_{ϕ} |
| ω_1 | $\mathcal{O}_{qq}^{(1)}, \mathcal{O}_{qq}^{(3)}, \mathcal{O}_{lq}^{(1)}, \mathcal{O}_{lq}^{(3)}, \mathcal{O}_{eu}, \mathcal{O}_{ud}^{(1)}, \mathcal{O}_{ud}^{(8)}, \mathcal{O}_{quqd}^{(1)}, \mathcal{O}_{lequ}^{(1)}, \mathcal{O}_{lequ}^{(3)}, \mathcal{O}_{duq}, \mathcal{O}_{qqq}, \mathcal{O}_{duu}$ |
| ω_2 | \mathcal{O}_{dd} |
| ω_4 | $\mathcal{O}_{uu}, \mathcal{O}_{ed}, \mathcal{O}_{duu}$ |
| Π_1 | \mathcal{O}_{ld} |
| Π_7 | $\mathcal{O}_{lu}, \mathcal{O}_{qe}, \mathcal{O}_{lequ}^{(1)}, \mathcal{O}_{lequ}^{(3)}$ |
| ζ | $\mathcal{O}_{qq}^{(1)}, \mathcal{O}_{qq}^{(3)}, \mathcal{O}_{lq}^{(1)}, \mathcal{O}_{lq}^{(3)}, \mathcal{O}_{qqq}$ |
| Ω_1 | $\mathcal{O}_{qq}^{(1)}, \mathcal{O}_{qq}^{(3)}, \mathcal{O}_{ud}^{(1)}, \mathcal{O}_{ud}^{(8)}, \mathcal{O}_{quqd}^{(1)}, \mathcal{O}_{quqd}^{(8)}$ |
| Ω_2 | \mathcal{O}_{dd} |
| Ω_4 | \mathcal{O}_{uu} |
| Υ | $\mathcal{O}_{qq}^{(1)}, \mathcal{O}_{qq}^{(3)}$ |
| Φ | $\mathcal{O}_{qu}^{(1)}, \mathcal{O}_{qu}^{(8)}, \mathcal{O}_{qd}^{(1)}, \mathcal{O}_{qd}^{(8)}, \mathcal{O}_{quqd}^{(8)}$ |

Table 7. Operators generated by the heavy scalar fields into the dimension-six SMEFT at tree level.

D.3 Four-fermion Operators

D.3.1 $(\bar{L}L)(\bar{L}L)$

$$(C_U)_{ijkl} = \frac{(y_{S_1})_{rjl}^*(y_{S_1})_{rik}}{M_{S_1}^2} + \frac{(y_{\Xi_1})_{rki}(y_{\Xi_1})_{rlj}^*}{M_{\Xi_1}^2} - \frac{(g_B^l)_{rkl}(g_B^l)_{rij}}{2M_{B_r}^2} - \frac{(g_W^l)_{rkj}(g_W^l)_{ril}}{4M_{W_r}^2} + \frac{(g_W^l)_{rkl}(g_W^l)_{rij}}{8M_{W_r}^2}, \quad (D.11)$$

$$(C_{qq}^{(1)})_{ijkl} = \frac{(y_{\omega_1}^{qq})_{rik}(y_{\omega_1}^{qq})_{rlj}^*}{2M_{\omega_1}^2} + \frac{3(y_{\zeta}^{qq})_{rki}(y_{\zeta}^{qq})_{rlj}^*}{2M_{\zeta}^2} + \frac{(y_{\Omega_1}^{qq})_{rik}(y_{\Omega_1}^{qq})_{rjl}}{4M_{\Omega_1}^2} + \frac{3(y_{\Upsilon})_{rlj}(y_{\Upsilon})_{rki}^*}{4M_{\Upsilon}^2} - \frac{(g_B^q)_{rkl}(g_B^q)_{rij}}{2M_{B_r}^2} - \frac{(g_G^q)_{rkj}(g_G^q)_{ril}}{8M_{G_r}^2} + \frac{(g_G^q)_{rkl}(g_G^q)_{rij}}{12M_{G_r}^2} - \frac{3(g_H)_{rkj}(g_H)_{ril}}{32M_{H_r}^2}, \quad (D.12)$$

$$(C_{qq}^{(3)})_{ijkl} = -\frac{(y_{\omega_1}^{qq})_{rki}(y_{\omega_1}^{qq})_{rjl}^*}{2M_{\omega_1}^2} - \frac{(y_{\zeta}^{qq})_{rki}(y_{\zeta}^{qq})_{rjl}^*}{2M_{\zeta}^2} + \frac{(y_{\Omega_1}^{qq})_{rik}(y_{\Omega_1}^{qq})_{rlj}}{4M_{\Omega_1}^2} + \frac{(y_{\Upsilon})_{rki}^*(y_{\Upsilon})_{rjl}}{4M_{\Upsilon}^2} - \frac{(g_W^q)_{rkl}(g_W^q)_{rij}}{8M_{W_r}^2} - \frac{(g_G^q)_{rkj}(g_G^q)_{ril}}{8M_{G_r}^2} + \frac{(g_H)_{rkl}(g_H)_{rij}}{48M_{H_r}^2} + \frac{(g_H)_{rkj}(g_H)_{ril}}{32M_{H_r}^2}, \quad (D.13)$$

Bottom-up

| Name | \mathcal{S} | \mathcal{S}_1 | \mathcal{S}_2 | φ | Ξ | Ξ_1 | Θ_1 | Θ_3 |
|-------|---------------|-----------------|-----------------|------------------------|------------|------------|------------------------|------------------------|
| Irrep | $(1, 1)_0$ | $(1, 1)_1$ | $(1, 1)_2$ | $(1, 2)_{\frac{1}{2}}$ | $(1, 3)_0$ | $(1, 3)_1$ | $(1, 4)_{\frac{1}{2}}$ | $(1, 4)_{\frac{3}{2}}$ |

| Name | ω_1 | ω_2 | ω_4 | Π_1 | Π_7 | ζ |
|------|------------|------------|------------|---------------------|------------------------|-------------------------|
| | | | | $(2)_{\frac{1}{6}}$ | $(3, 2)_{\frac{7}{6}}$ | $(3, 3)_{-\frac{1}{3}}$ |
| | | | | | Φ | |
| | | | | $(3)_{\frac{1}{3}}$ | $(8, 2)_{\frac{1}{2}}$ | |

| | Δ_3 | Σ | Σ_1 |
|--|-------------------------|------------|---------------|
| | $(1, 2)_{-\frac{3}{2}}$ | $(1, 3)_0$ | $(1, 3)_{-1}$ |

| | Q_5 | Q_7 | T_1 | T_2 |
|--|-------------------------|------------------------|-------------------------|------------------------|
| | $(3, 2)_{-\frac{5}{6}}$ | $(3, 2)_{\frac{7}{6}}$ | $(3, 3)_{-\frac{1}{3}}$ | $(3, 3)_{\frac{2}{3}}$ |

28 pages...

UV

to the dimension-six SMEFT at tree level.

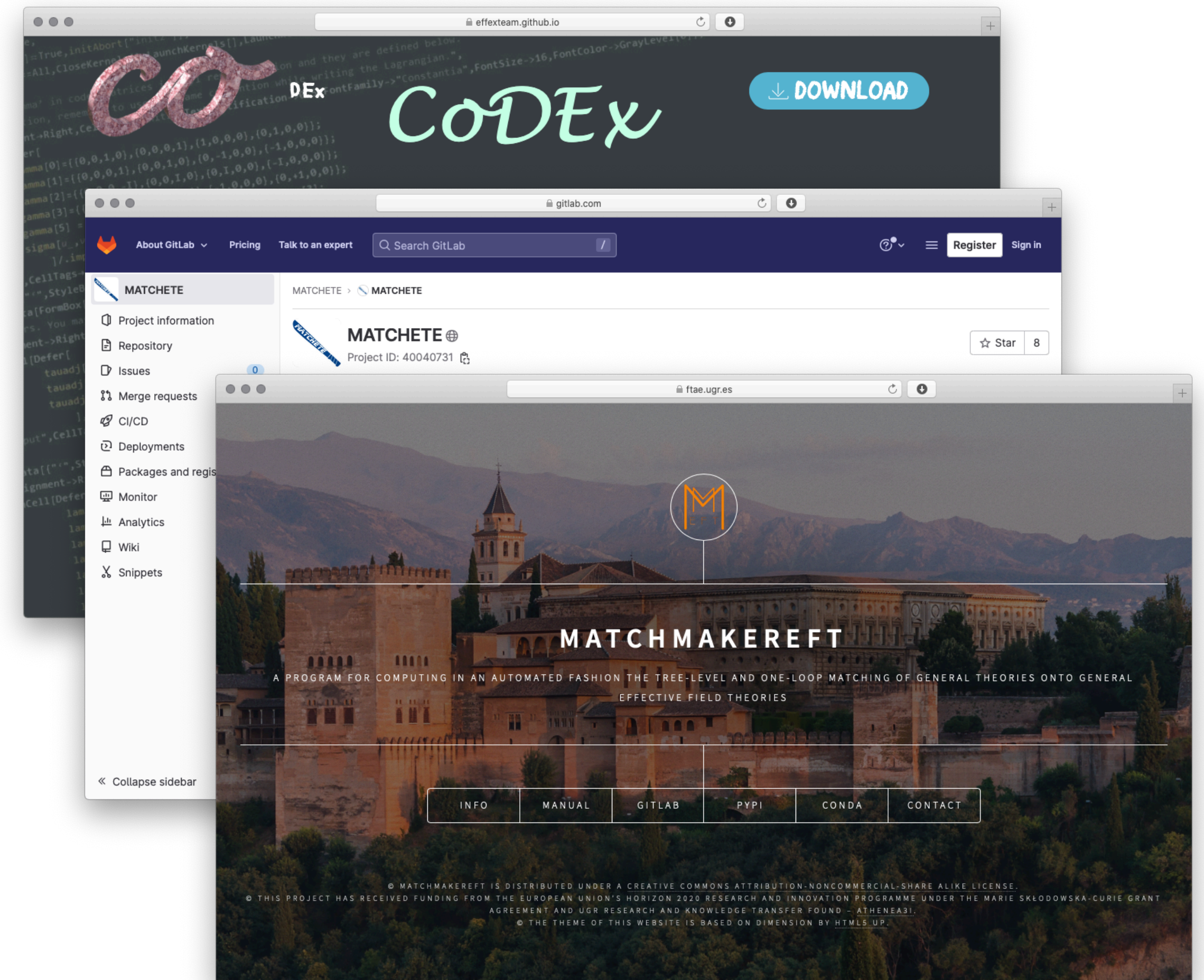
ing to the dimension-six SMEFT at tree level.

One-loop tools

Impressive recent progress in automating one-loop matching:

- CoDeX implements UOLEA results
- MatchMakerEFT implements diagrammatic matching
- Matchete uses functional techniques (built upon SuperTracer)

CoDeX: Bakshi Chakraborty, Patra arXiv:1808.04403
UOLEA results: Drozd, Ellis, Quevillon, You arXiv:1512.03003
Ellis, Quevillon, You, Zhang arXiv:1604.02445
Ellis, Quevillon, Vuong, You, Zhang arXiv:2006.16260
Larue, Quevillon arXiv:2303.10203
MatchMakerEFT: Carmona, Lazopoulos, Olgoso, Santiago arXiv:2112.10787
SOLD: Guedes, Olgoso, Santiago arXiv:2303.16965
Matchete & SuperTracer: Fuentes-Martín, Koenig, Pagès, Thomsen, Wilsch arXiv:2212.04510, arXiv:2012.08506



Going past tree level

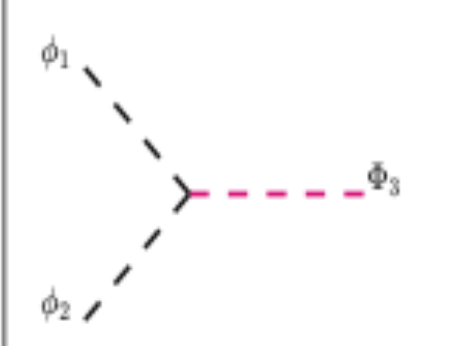
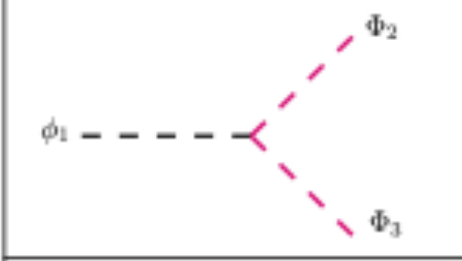
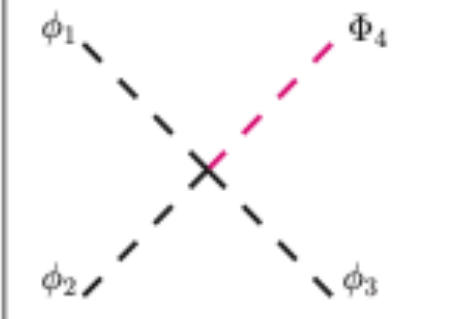
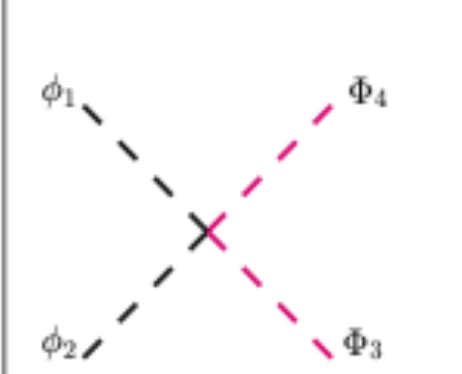
- Loop-level completions of dimension-5 Weinberg operator known up to three loops, for dimension-7 analogue up to one
 Cepedello, Esser, Hirsch, Sanz arXiv:2207.13714
- Methods extended to general loop-level studies of *e.g.* four-fermion operators
- Diagram-topology analysis of one-loop contributions to all dimension-6 and dimension-8 operators
- SOLD provides complete one-loop dictionary for subset of operators at dimension 6. Mathematica package for results
 Guedes, Olgoso, Santiago arXiv:2303.16965

Results in terms of exotic quantum numbers

Bonnet, Hirsch, Ota, Winter arXiv:1204.5862
 Aristizabal Sierra, Degee, Dorame, Hirsch arXiv:1411.7038
 Cepedello, Fonseca, Hirsch arXiv:1807.00629

Bakshi, Chakraborty, Prakash, Rahaman, Spannowsky arXiv:2103.11593
 Naskar, Prakash, Rahaman arXiv:2205.00910

E.g. Scalar interactions allowed @ one-loop and dimension 6

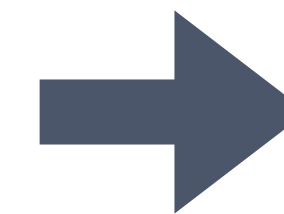
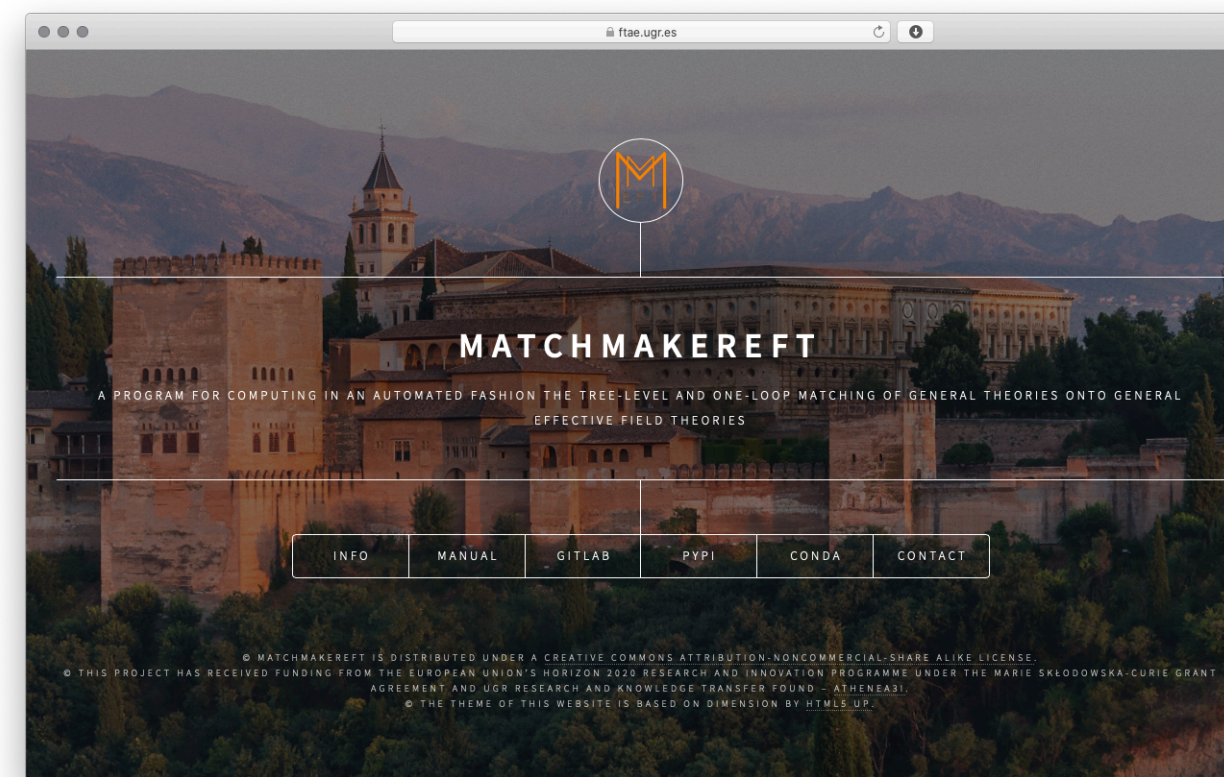
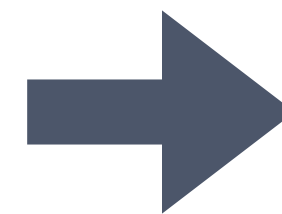
| Vertex | S. No. | Light fields | Heavy field(s) |
|---|---------|---|--|
|  | V1-(i) | $\phi_1 = \phi_2 = H_{(1,2,\frac{1}{2})}$ or $H_{(1,2,-\frac{1}{2})}^\dagger$ | $\Phi_3 \in \{(1, 3, \pm 1), (1, 1, \pm 1)\}$ |
| | V1-(ii) | $\phi_1 = H, \phi_2 = H^\dagger$ | $\Phi_3 \in \{(1, 3, 0), (1, 1, 0)\}$ |
|  | V2 | $\phi_1 = H$ or H^\dagger | $\Phi_2 \in (R_{C_2}, R_{L_2}, Y_2), \Phi_3 \in (R_{C_3}, R_{L_3}, Y_3)$ with $R_{C_2} \otimes R_{C_3} \equiv 1, R_{L_2} \otimes R_{L_3} \equiv 2$ and $Y_2 + Y_3 = \pm \frac{1}{2}$. |
|  | V3-(i) | $\phi_1 = \phi_2 = \phi_3 = H$ or H^\dagger | $\Phi_4 \in \{(1, 4, \pm \frac{3}{2}), (1, 2, \pm \frac{3}{2})\}$ |
| | V3-(ii) | $\phi_1 = \phi_2 = H, \phi_3 = H^\dagger$ | $\Phi_4 \in \{(1, 4, \pm \frac{1}{2}), (1, 2, \pm \frac{1}{2})\}$ |
|  | V4-(i) | $\phi_1 = H, \phi_2 = H^\dagger$ | $\Phi_3 \in (\{1, R_C\}, \{1, R_L\}, \{0, Y\}), \Phi_4 = \Phi_3^\dagger$ |
| | V4-(ii) | $\phi_1 = \phi_2 = H$ or H^\dagger | $\Phi_3 \in (R_{C_3}, R_{L_3}, Y_3), \Phi_4 \in (R_{C_4}, R_{L_4}, Y_4)$ with $R_{C_3} \otimes R_{C_4} \equiv 1, R_{L_3} \otimes R_{L_4} \equiv 1$ or 3 and $Y_3 + Y_4 = \pm 1$. |

Our approach: overview

Linear SM extensions are a physically motivated subset of toy models that parametrise tree-level deviation from the SM

Primary aim: Use these tools to extend results for the **linear SM extensions** to the **one-loop level**

Extend Lagrangian sufficient to generate dimension-6 operators at one loop



MatchMakerParser: Parses Mathematica to Python, writes classes for each multiplet

Lagrangian

- Similar assumptions to tree-level dictionary: limit ourselves to scalars and vector-like and Majorana fermions. **Our Lagrangian matches the conventions of the tree-level dictionary**
- We don't consider mixed terms
- For one-loop matching, only need to alter scalar interactions

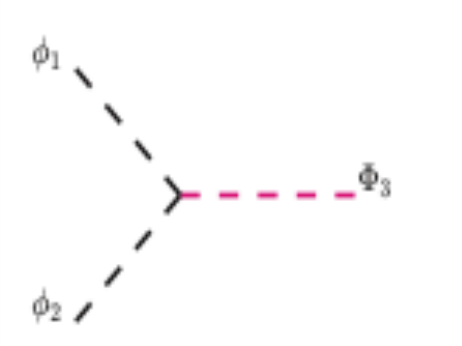
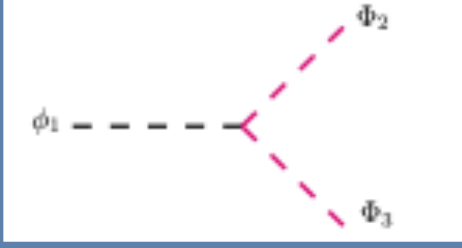

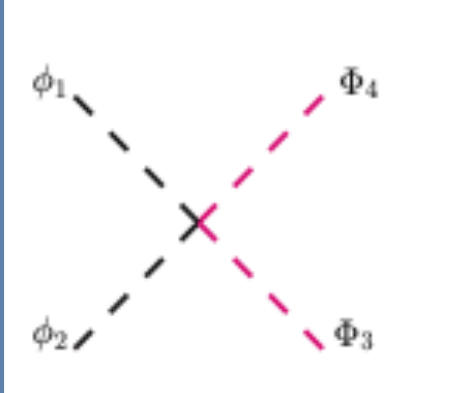
$$\Delta\mathcal{L} = \sum_S \hat{\lambda}'_S (H^\dagger H)(S^\dagger S) + \hat{\lambda}'_\varphi (H^\dagger \varphi)(\varphi^\dagger H) + \sum_{i \in \{1,3\}} \hat{\lambda}'_{\Theta_i} (\Theta_i^\dagger T_4^a \Theta_i)(H^\dagger \sigma^a H)$$

$$+ \sum_{i \in \{1,7\}} \hat{\lambda}'_{\Pi_i} (\Pi_i^\dagger H)(H^\dagger \Pi_i) + \hat{\lambda}'_\Phi \text{Tr}[(\Phi^\dagger \cdot \lambda H)(H^\dagger \Phi \cdot \lambda)]$$

$$+ \sum_{S \in \{\zeta, \Upsilon\}} \hat{\lambda}'_S f_{abc} (S^{a\dagger} S^b)(H^\dagger \sigma^c H)$$

$$+ \left\{ \hat{\lambda}''_{\Theta_1} \frac{8}{3\sqrt{5}} (\Theta_1^I \epsilon_{IJ} [T_4^a]^J_K \Theta_1^K)(H^\dagger \sigma^a \tilde{H}) + \hat{\lambda}''_\Phi \text{Tr}[(H^\dagger \Phi \cdot \lambda)(H^\dagger \Phi \cdot \lambda)] + \text{h.c.} \right\}$$

Bakshi, Chakraborty, Prakash, Rahaman, Spannowsky
arXiv:2103.11593

| Vertex | S. No. | Light fields | Heavy field(s) |
|---|---------|---|--|
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|  | V2 | $\phi_1 = H$ or H^\dagger | $\Phi_2 \in (R_{C_2}, R_{L_2}, Y_2), \Phi_3 \in (R_{C_3}, R_{L_3}, Y_3)$ with $R_{C_2} \otimes R_{C_3} \equiv 1, R_{L_2} \otimes R_{L_3} \equiv 2$ and $Y_2 + Y_3 = \pm \frac{1}{2}$. |
|  | V3-(i) | $\phi_1 = \phi_2 = \phi_3 = H$ or H^\dagger | $\Phi_4 \in \{(1,4,\pm \frac{3}{2}), (1,2,\pm \frac{3}{2})\}$ |
| | V3-(ii) | $\phi_1 = \phi_2 = H, \phi_3 = H^\dagger$ | $\Phi_4 \in \{(1,4,\pm \frac{1}{2}), (1,2,\pm \frac{1}{2})\}$ |
|  | V4-(i) | $\phi_1 = H, \phi_2 = H^\dagger$ | $\Phi_3 \in (\{1, R_C\}, \{1, R_L\}, \{0, Y\}), \Phi_4 = \Phi_3^\dagger$ |
| | V4-(ii) | $\phi_1 = \phi_2 = H$ or H^\dagger | $\Phi_3 \in (R_{C_3}, R_{L_3}, Y_3), \Phi_4 \in (R_{C_4}, R_{L_4}, Y_4)$ with $R_{C_3} \otimes R_{C_4} \equiv 1, R_{L_3} \otimes R_{L_4} \equiv 1$ or 3 and $Y_3 + Y_4 = \pm 1$. |

Reading the Lagrangian and parsing th

- Written a lightweight wrapper around FeynRules to encode Lagrangians with less boilerplate code and more consistency checks
- A simple implementation of missing PythonForm to parse results from MatchMaker
- Outputs are Python classes with coefficients as methods.

```

class GranadazetaMatchingResult
    def __init__(self, name='
    super().__init__(name, scale)
    self.Mzeta = 1
    self.yqlzeta = np.ones((3, 3))
    self.yqlzetabar = np.ones((3, 3))
    self.yqqzeta = np.ones((3, 3))
    self.yqqzetabar = np.ones((3, 3))
    self.lambdaHatzeta = 1
    self.lambdaHatzetabar = 1
    self.lambdaHatPrimezeta = 1
    self.lambdaHatPrimezetabar = 1
    self.nonvanishing = ['alpha03G', 'alpha03W', 'alpha0HG', 'alpha0HW', 'alpha0HB', 'alpha0HWB', 'alpha0HBox', 'alpha0HD', 'alpha0H', 'alpha0uG', 'alpha

def alpha03G(self, ):
    return 1/1920 * (self.g3)**(3) * (self.Mzeta)**(-2) * self.oneLoopOrder * (np.pi)**(-2)

def alpha03Gt(self, ):
    return 0

def alpha03W(self, ):
    return 1/480 * (self.g2)**(3) * (self.Mzeta)**(-2) * self.oneLoopOrder * (np.pi)**(-2)

def alpha03Wt(self, ):
    return 0

def alpha0HG(self, ):
    return -1/128 * (self.g3)**(2) * self.lambdaHatzeta * (self.Mzeta)**(-2) * self.oneLoopOrder * (np.pi)**(-2)

def alpha0HGt(self, ):
    return 0

def alpha0HW(self, ):

```

```

In [10]: from python.Granadazeta_matching import GranadazetaMatchingResult
In [11]: zeta_matching = GranadazetaMatchingResult(scale=1e3)
In [12]: zeta_matching.alpha0HD()
Out[12]: -0.0063515302515737395
In [13]:

```

$$\zeta \sim (3,3)_{-1/3}$$

Connection to Python ecosystem

Wilson: Aebischer, Kumar, Straub arXiv:1804.05033
flavio: Straub arXiv:1810.08132

MatchingDB: Criado gitlab.com/jccriado/matchingdb

- Plans to put one-loop dictionary on PyPI for easy use with other tools
- Limited searching and querying ability, looking into other export options

```
import wilson
import flavio

from oneloopdict import ZetaMatching

SCALE = 1e3

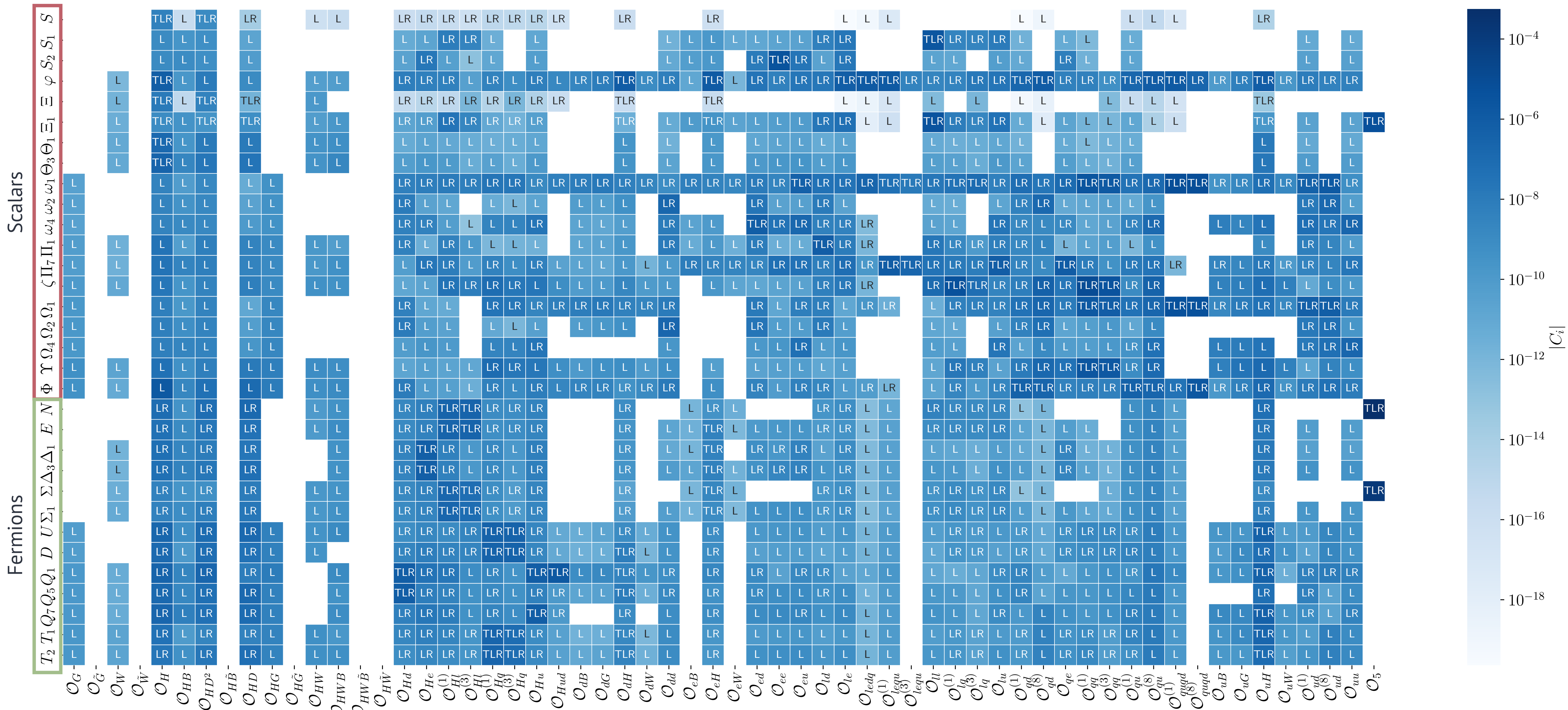
# Get coefficients
zeta_matching = ZetaMatching(scale=SCALE)
coefficients = zeta_matching.coefficient_dictionary

# Calculate!
zeta_wilson = wilson.Wilson(coefficients, scale=SCALE, eft="SMEFT", basis="Warsaw")
prediction = flavio.np_prediction("a_mu", zeta_wilson)
```

$\zeta \sim (3,3)_{-1/3}$

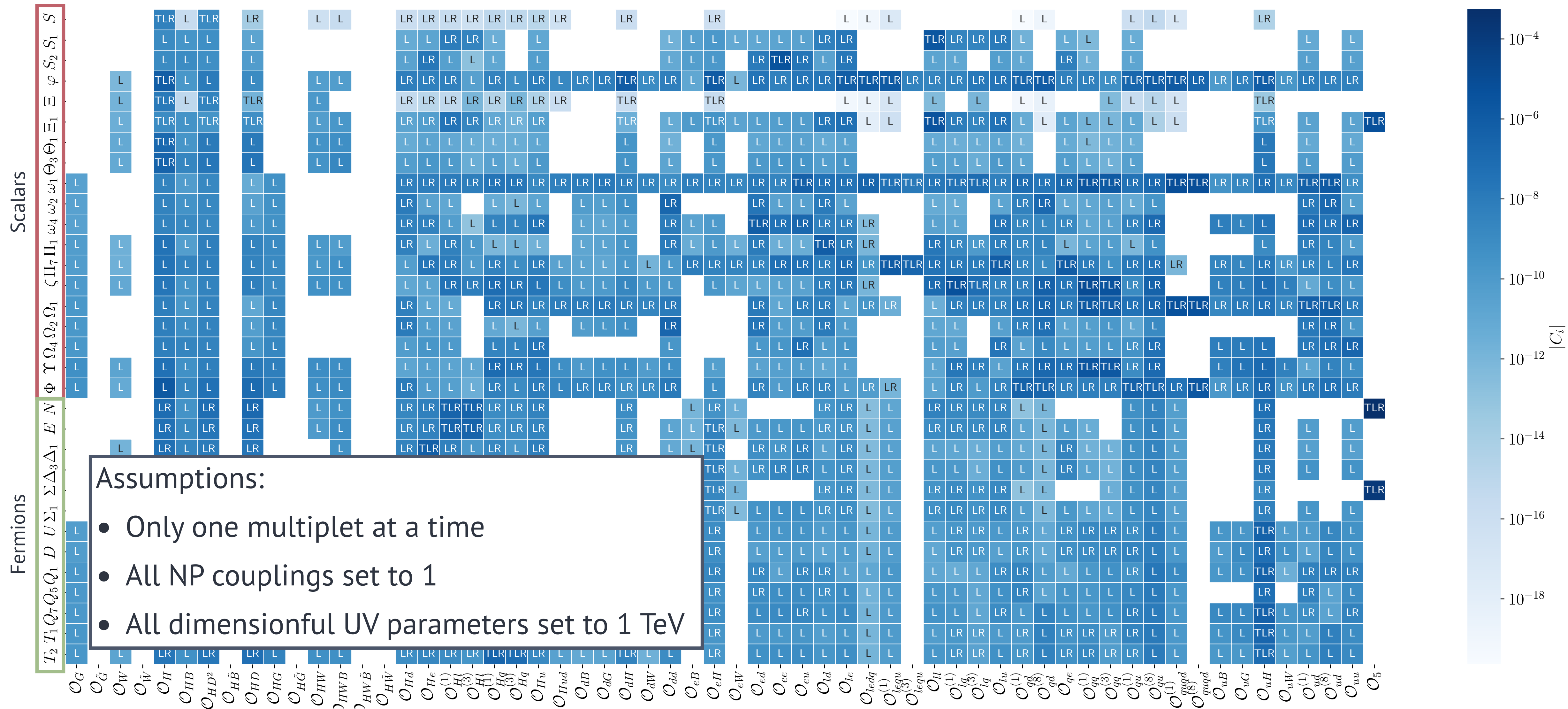
T L R

Tree generated
Loop generated
R GE induced



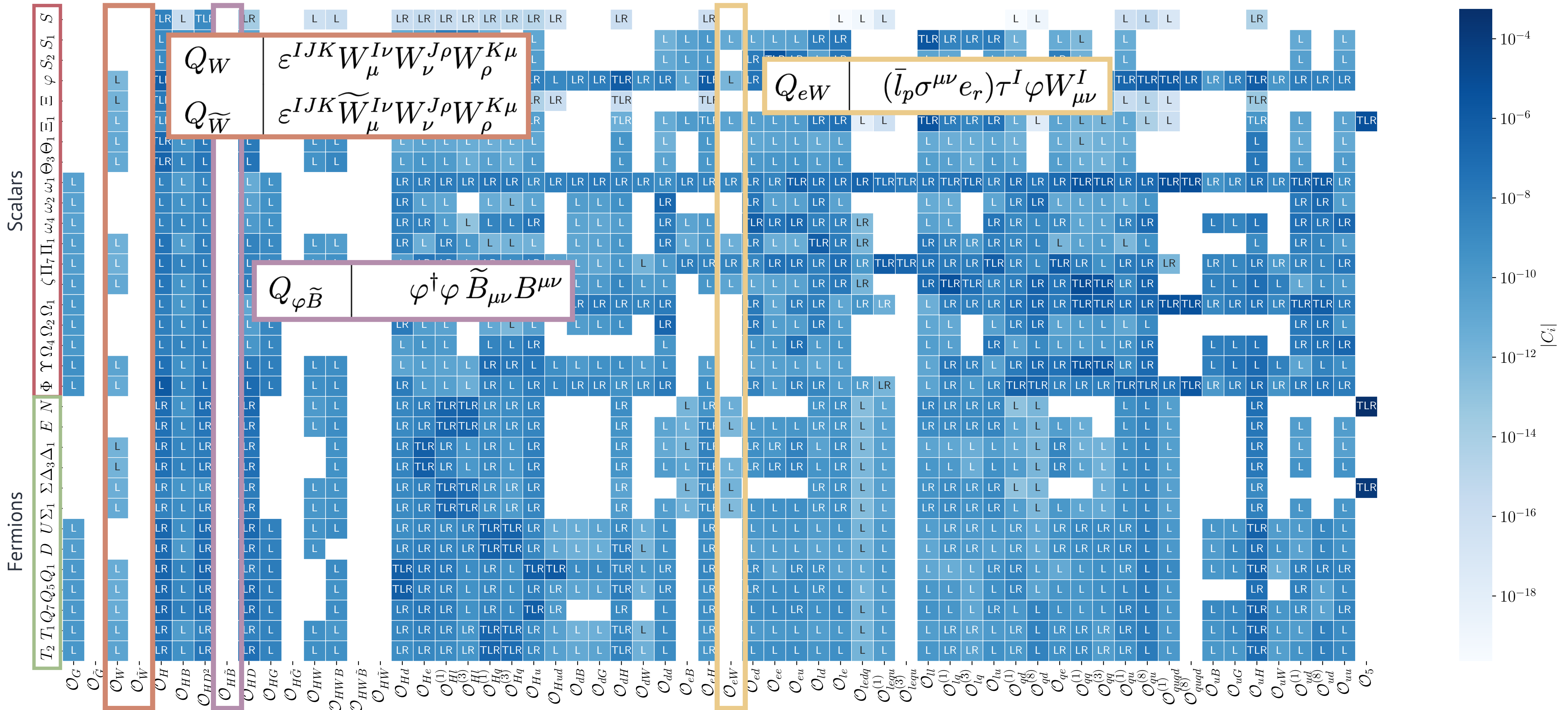
T L R

T tree generated
L loop generated
R GE induced



T L R

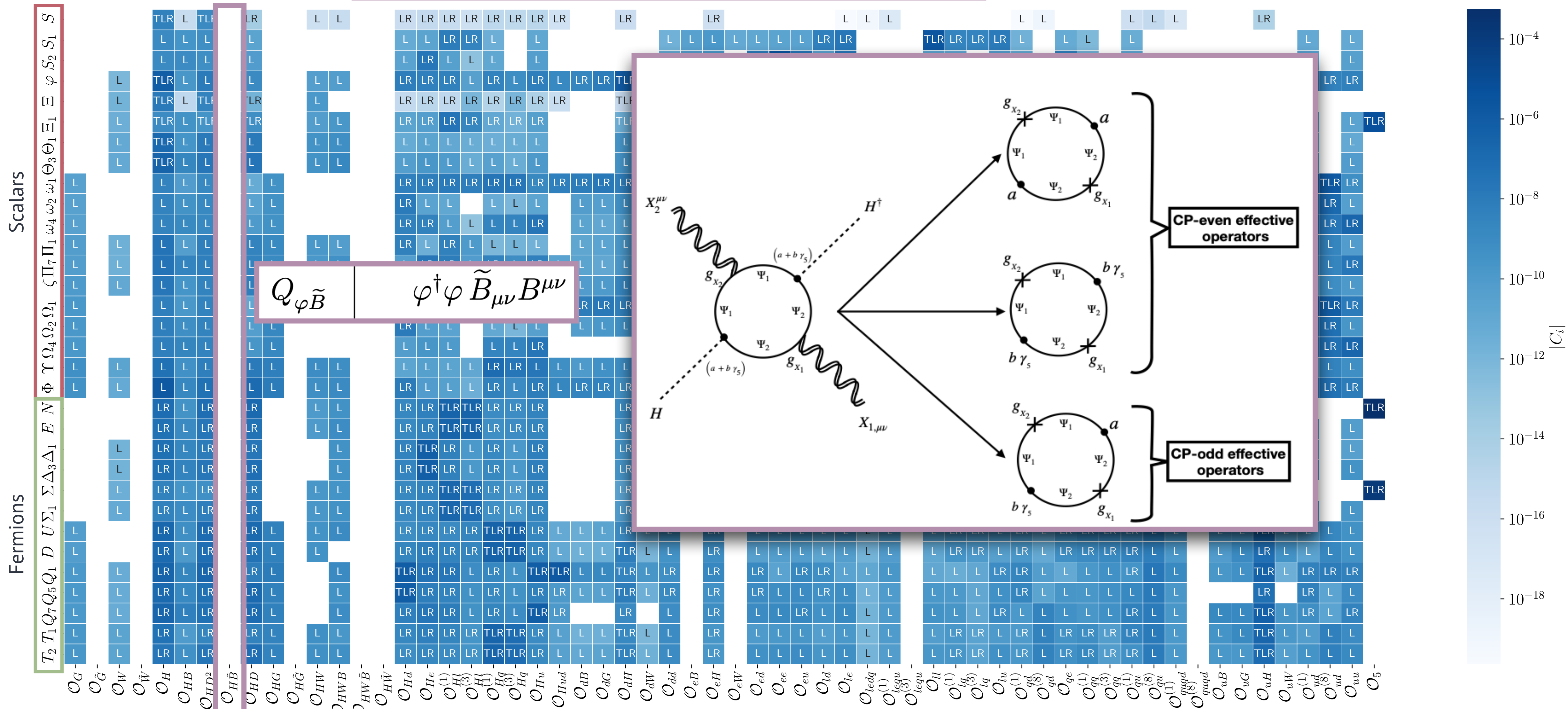
T ree generated
L oop generated
R GE induced



TLR

Tree generated
Loop generated
R GE induced

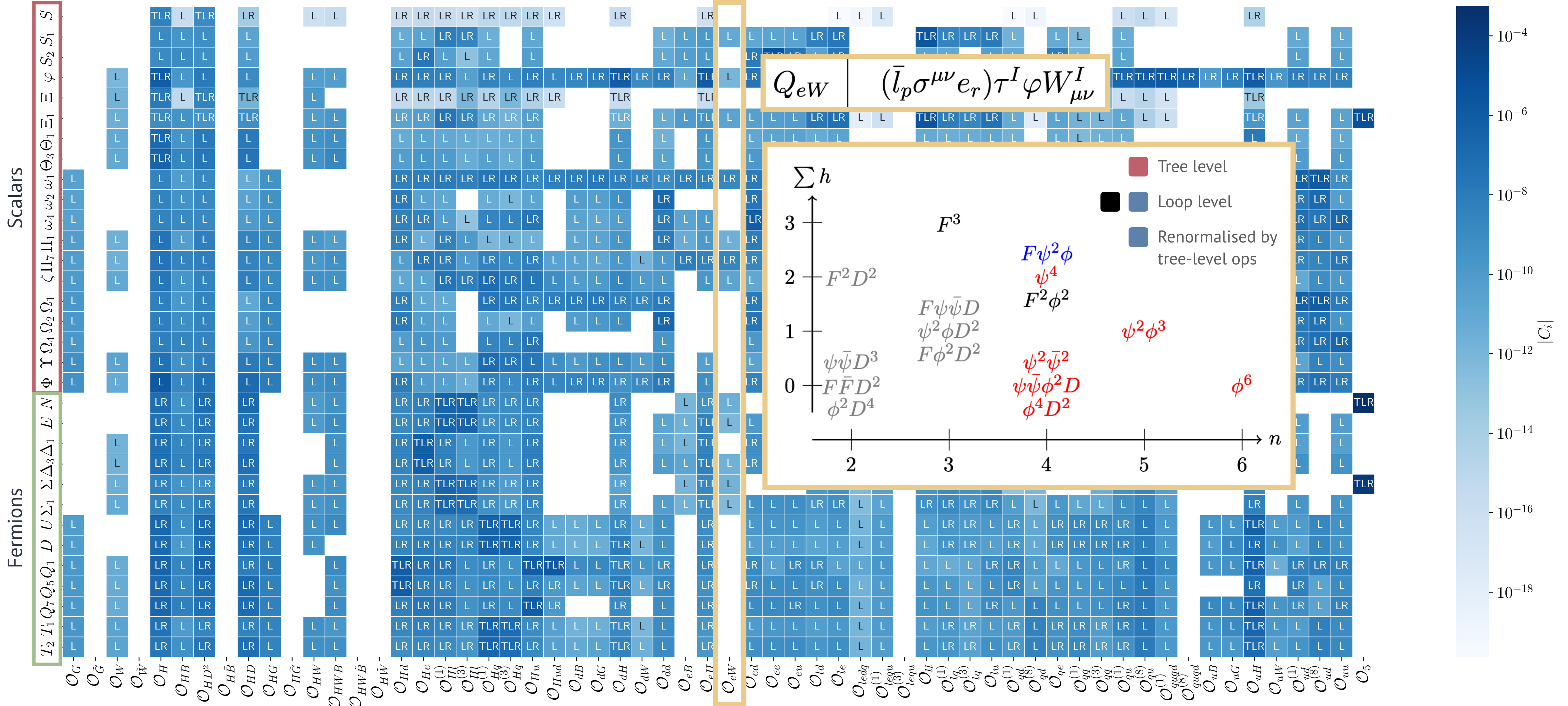
Other CP-odd bosonic operators can be generated at one loop, require **two** exotic multiplets



Operators of the form $F\psi^2\phi^2$ are renormalised by four-fermion operators

Tree generated
Loop generated
R GE induced

T L R



$$\mathcal{O}_{HG} = H^\dagger H G_{\mu\nu}^A G^{A\mu\nu}$$

Conclusions and outlook

$$\mathcal{O}_{HB} = H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

$$\mathcal{O}_{HD} = (H^\dagger D_\mu H)^2$$

- Computational tools are essential for the publishing and querying of UV/IR dictionaries going forward
- We use MatchMakerEFT and our MatchMakerParser to present our UV/IR dictionary for the linear SM extensions at one loop
- Useful tool for phenomenological analyses and general studies

$$\mathcal{O}_{ll} = (\bar{l}_p \gamma_\mu l_q)$$

$$\mathcal{O}_{lq}^{(1)} = (\bar{l}_p \gamma_\mu l_q) (\bar{q}_r \gamma^\mu q_s)$$

$$\mathcal{O}_{lq}^{(3)}$$

$$\mathcal{O}_{HG} = H^\dagger H G_{\mu\nu}^A G^{A\mu\nu}$$

$$\mathcal{O}_{HB} = H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

$$\mathcal{O}_{HD} = (H^\dagger D_\mu H)^2$$

$$\mathcal{O}_{ll} = (\bar{l}_p \gamma_\mu l_q)$$

$$\mathcal{O}_{lq}^{(1)} =$$

$$\mathcal{O}_{lq}^{(3)}$$

¡Muchas gracias!

Backup

$$\mathcal{O}_{HG} = H^\dagger H G_{\mu\nu}^A G^{A\mu\nu}$$

$$\mathcal{O}_{HB} = H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

$$\mathcal{O}_{HD} = (H^\dagger D_\mu H)^2$$

$$\mathcal{O}_{ll} = (\bar{l}_p \gamma_\mu l_q)$$

$$\mathcal{O}_{lq}^{(1)} = (\bar{l}_p \gamma_\mu l_q) (F_{\mu\nu}^A q^\nu)$$

$$\mathcal{O}_{lq}^{(3)} = (\bar{l}_p \gamma_\mu l_q) (F_{\mu\nu}^A q^\nu)^2$$

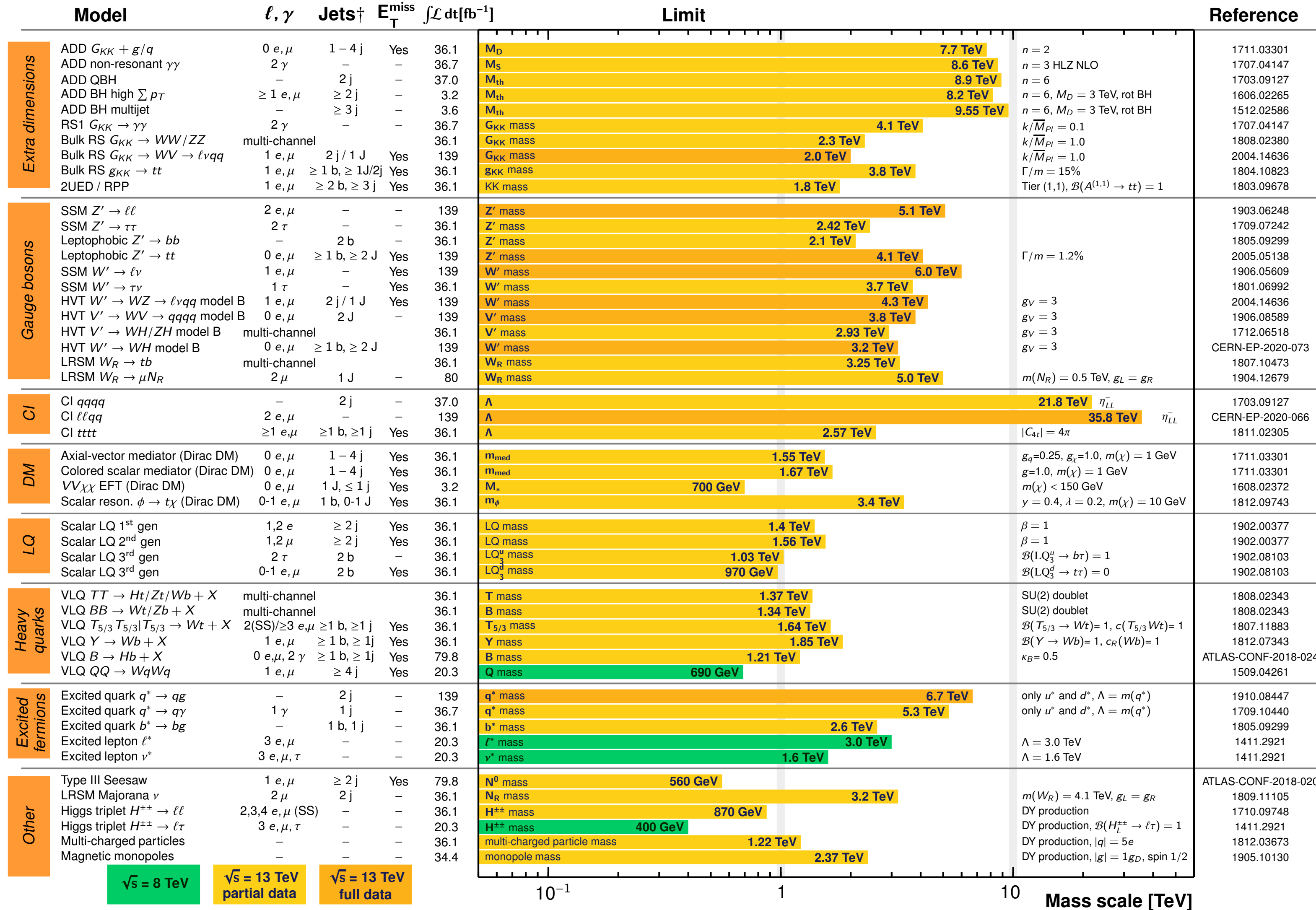
ATLAS Exotics Searches* - 95% CL Upper Exclusion Limits

Status: May 2020

ATLAS Preliminary

$$\int \mathcal{L} dt = (3.2 - 139) \text{ fb}^{-1}$$

$$\sqrt{s} = 8, 13 \text{ TeV}$$



*Only a selection of the available mass limits on new states or phenomena is shown.

†Small-radius (large-radius) jets are denoted by the letter j (J).

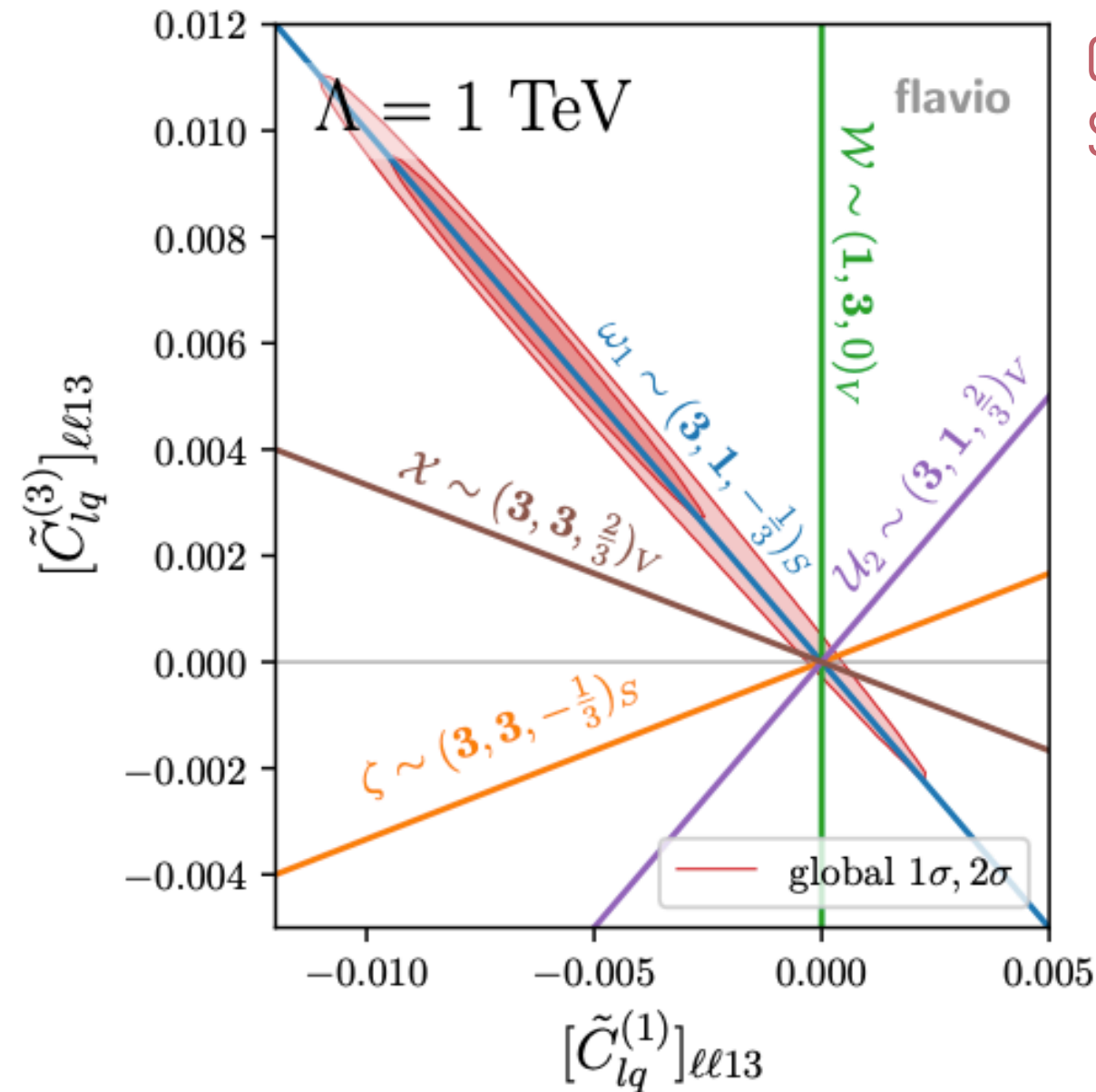
See talk by Patricia Conde Muño

Linear SM extensions are useful

- Linear SM extensions are a physically motivated subset of toy models

Herrero-Garcia, Schmidt arXiv:1903.10552

- Can be used to organise complex UV models
- Can motivate directions in the space of WCs



Greljo, Salko, Smolkovic, Stangl arXiv:2306.09401

Study of tension in exclusive V_{ub} extraction

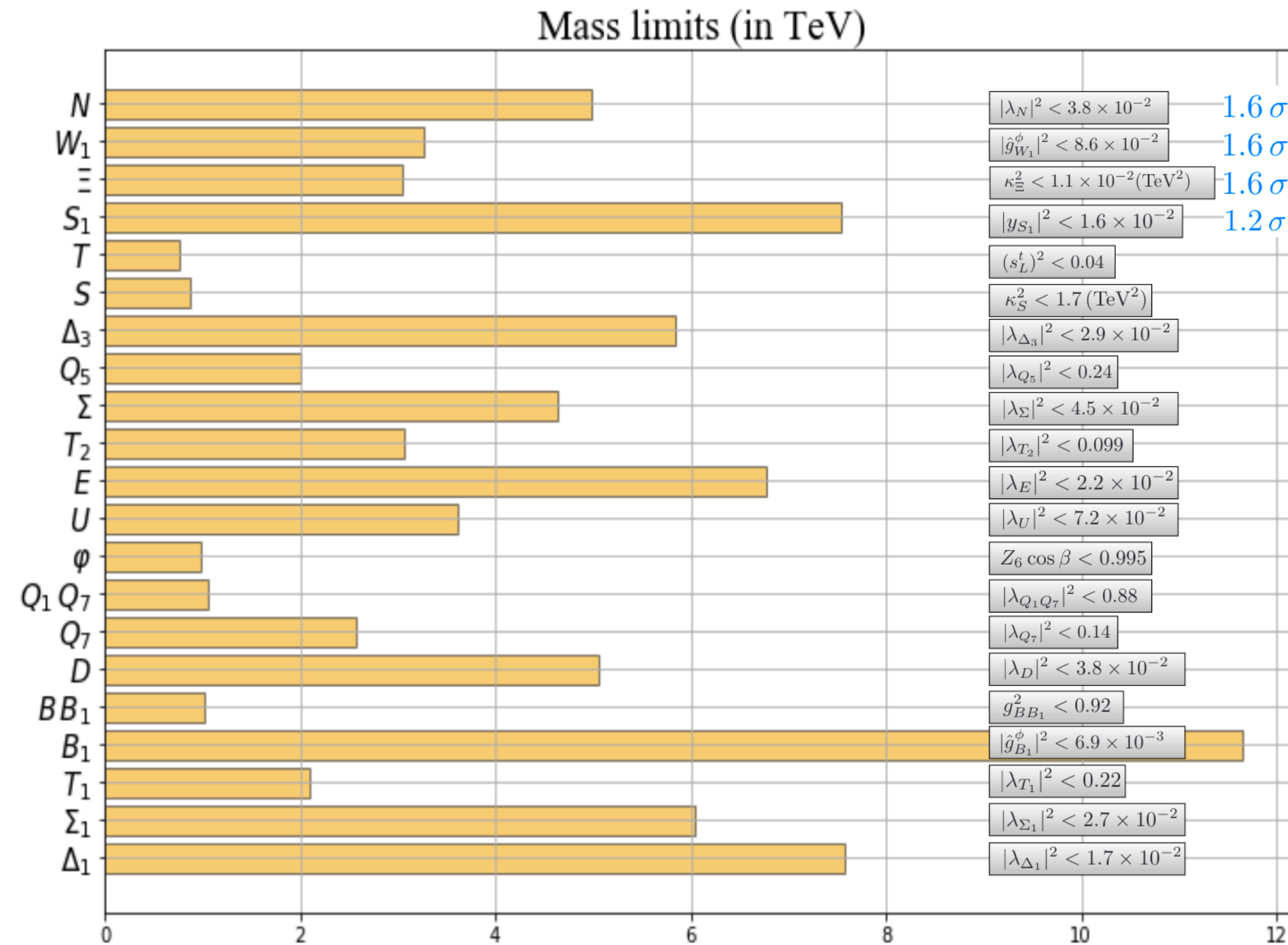
| Model | C_{HD} | C_{ll} | C_{Hl}^3 | C_{Hl}^1 | C_{He} | $C_{H\Box}$ | $C_{\tau H}$ | C_{tH} | C_{bH} |
|----------------|----------------|----------|-----------------|-----------------|----------------|----------------|---------------------|------------------|------------------|
| S | | | | | | $-\frac{1}{2}$ | | | |
| S_1 | | 1 | | | | | | | |
| Σ | | | $\frac{1}{16}$ | $\frac{3}{16}$ | | | $\frac{y_\tau}{4}$ | | |
| Σ_1 | | | $-\frac{1}{16}$ | $-\frac{3}{16}$ | | | $\frac{y_\tau}{8}$ | | |
| N | | | $-\frac{1}{4}$ | $\frac{1}{4}$ | | | | | |
| E | | | $-\frac{1}{4}$ | $-\frac{1}{4}$ | | | $\frac{y_\tau}{2}$ | | |
| Δ_1 | | | | | $\frac{1}{2}$ | | $\frac{y_\tau}{2}$ | | |
| Δ_3 | | | | | $-\frac{1}{2}$ | | $\frac{y_\tau}{2}$ | | |
| B_1 | 1 | | | | | $-\frac{1}{2}$ | $-\frac{y_\tau}{2}$ | $-\frac{y_t}{2}$ | $-\frac{y_b}{2}$ |
| Ξ | -2 | | | | | $\frac{1}{2}$ | y_τ | y_t | y_b |
| W_1 | $-\frac{1}{4}$ | | | | | $-\frac{1}{8}$ | $-\frac{y_\tau}{8}$ | $-\frac{y_t}{8}$ | $-\frac{y_b}{8}$ |
| φ | | | | | | | $-y_\tau$ | $-y_t$ | $-y_b$ |
| $\{B, B_1\}$ | | | | | | $-\frac{3}{2}$ | $-y_\tau$ | $-y_t$ | $-y_b$ |
| $\{Q_1, Q_7\}$ | | | | | | | | y_t | |

| Model | C_{Hq}^3 | C_{Hq}^1 | $(C_{Hq}^3)_{33}$ | $(C_{Hq}^1)_{33}$ | C_{Hu} | C_{Hd} | C_{tH} | C_{bH} |
|-------|-----------------|-----------------|----------------------------------|---------------------------------|---------------|----------------|-------------------------|-----------------|
| U | $-\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $\frac{1}{4}$ | | | $\frac{y_t}{2}$ | |
| D | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | | | | $\frac{y_b}{2}$ |
| Q_5 | | | | | | $-\frac{1}{2}$ | | $\frac{y_b}{2}$ |
| Q_7 | | | | | $\frac{1}{2}$ | | $\frac{y_t}{2}$ | |
| T_1 | $-\frac{1}{16}$ | $-\frac{3}{16}$ | $-\frac{1}{16}$ | $-\frac{3}{16}$ | | | $\frac{y_t}{4}$ | $\frac{y_b}{8}$ |
| T_2 | $-\frac{1}{16}$ | $\frac{3}{16}$ | $-\frac{1}{16}$ | $\frac{3}{16}$ | | | $\frac{y_t}{8}$ | $\frac{y_b}{4}$ |
| T | | | $-\frac{1}{2} \frac{M_T^2}{v^2}$ | $\frac{1}{2} \frac{M_T^2}{v^2}$ | | | $y_t \frac{M_T^2}{v^2}$ | |

Ellis, Madigan, Mimasu, Sanz, You arXiv:2012.02779

FitMaker group: Fit to top, Higgs, diboson and EW data

Linear SM extensions are useful



| Model | C_{HD} | C_{ll} | C_{Hl}^3 | C_{Hl}^1 | C_{He} | $C_{H\Box}$ | $C_{\tau H}$ | C_{tH} | C_{bH} |
|----------------|----------------|----------|-----------------|-----------------|----------------|----------------|---------------------|------------------|------------------|
| S | | | | | | $-\frac{1}{2}$ | | | |
| S_1 | | 1 | | | | | | | |
| Σ | | | $\frac{1}{16}$ | $\frac{3}{16}$ | | | $\frac{y_\tau}{4}$ | | |
| Σ_1 | | | $-\frac{1}{16}$ | $-\frac{3}{16}$ | | | $\frac{y_\tau}{8}$ | | |
| N | | | $-\frac{1}{4}$ | $\frac{1}{4}$ | | | | | |
| E | | | $-\frac{1}{4}$ | $-\frac{1}{4}$ | | | $\frac{y_\tau}{2}$ | | |
| Δ_1 | | | | | $\frac{1}{2}$ | | $\frac{y_\tau}{2}$ | | |
| Δ_3 | | | | | $-\frac{1}{2}$ | | $\frac{y_\tau}{2}$ | | |
| B_1 | 1 | | | | | $-\frac{1}{2}$ | $-\frac{y_\tau}{2}$ | $-\frac{y_t}{2}$ | $-\frac{y_b}{2}$ |
| Ξ | -2 | | | | | $\frac{1}{2}$ | y_τ | y_t | y_b |
| W_1 | $-\frac{1}{4}$ | | | | | $-\frac{1}{8}$ | $-\frac{y_\tau}{8}$ | $-\frac{y_t}{8}$ | $-\frac{y_b}{8}$ |
| φ | | | | | | | $-y_\tau$ | $-y_t$ | $-y_b$ |
| $\{B, B_1\}$ | | | | | | $-\frac{3}{2}$ | $-y_\tau$ | $-y_t$ | $-y_b$ |
| $\{Q_1, Q_7\}$ | | | | | | | | y_t | |

| Model | C_{Hq}^3 | C_{Hq}^1 | $(C_{Hq}^3)_{33}$ | $(C_{Hq}^1)_{33}$ | C_{Hu} | C_{Hd} | C_{tH} | C_{bH} |
|-------|-----------------|-----------------|----------------------------------|---------------------------------|---------------|----------------|-------------------------|-----------------|
| U | $-\frac{1}{4}$ | $\frac{1}{4}$ | $-\frac{1}{4}$ | $\frac{1}{4}$ | | | $\frac{y_t}{2}$ | |
| D | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | $-\frac{1}{4}$ | | | | $\frac{y_b}{2}$ |
| Q_5 | | | | | | $-\frac{1}{2}$ | | $\frac{y_b}{2}$ |
| Q_7 | | | | | $\frac{1}{2}$ | | $\frac{y_t}{2}$ | |
| T_1 | $-\frac{1}{16}$ | $-\frac{3}{16}$ | $-\frac{1}{16}$ | $-\frac{3}{16}$ | | | $\frac{y_t}{4}$ | $\frac{y_b}{8}$ |
| T_2 | $-\frac{1}{16}$ | $\frac{3}{16}$ | $-\frac{1}{16}$ | $\frac{3}{16}$ | | | $\frac{y_t}{8}$ | $\frac{y_b}{4}$ |
| T | | | $-\frac{1}{2} \frac{M_T^2}{v^2}$ | $\frac{1}{2} \frac{M_T^2}{v^2}$ | | | $y_t \frac{M_T^2}{v^2}$ | |

Ellis, Madigan, Mimasu, Sanz, You arXiv:2012.02779

FitMaker group: Fit to top, Higgs, diboson and EW data

Linear SM extensions are complicated

de Blas, Criado, Pérez-Victoria, Santiago arXiv:1711.10391
MatchingTools: Criado arXiv:1710.06445

$$\begin{aligned}
 -\mathcal{L}_{\text{leptons}}^{(4)} = & (\lambda_N)_{ri} \bar{N}_{Rr} \tilde{\phi}^\dagger l_{Li} + (\lambda_E)_{ri} \bar{E}_{Rr} \phi^\dagger l_{Li} && \text{Exotic fermion interactions} \\
 & + (\lambda_{\Delta_1})_{ri} \bar{\Delta}_{1Lr} \phi e_{Ri} + (\lambda_{\Delta_3})_{ri} \bar{\Delta}_{3Lr} \tilde{\phi} e_{Ri} \\
 & + \frac{1}{2} (\lambda_\Sigma)_{ri} \bar{\Sigma}_{Rr}^a \tilde{\phi}^\dagger \sigma^a l_{Li} + \frac{1}{2} (\lambda_{\Sigma_1})_{ri} \bar{\Sigma}_{1Rr}^a \phi^\dagger \sigma^a l_{Li} \\
 & + (\lambda_{N\Delta_1})_{rs} \bar{N}_{Rr}^c \phi^\dagger \Delta_{1Rs} + (\lambda_{E\Delta_1})_{rs} \bar{E}_{Lr} \phi^\dagger \Delta_{1Rs} \\
 & + (\lambda_{E\Delta_3})_{rs} \bar{E}_{Lr} \tilde{\phi}^\dagger \Delta_{3Rs} + \frac{1}{2} (\lambda_{\Sigma\Delta_1})_{rs} \bar{\Sigma}_{Rr}^{ca} \tilde{\phi}^\dagger \sigma^a \Delta_{1Rs}
 \end{aligned}$$

$$-\mathcal{L}_S^{(5)} = \frac{1}{f} \left[(\tilde{k}_S^\phi)_r \mathcal{S}_r D_\mu \phi^\dagger D^\mu \phi + (\tilde{\lambda}_S)_r \mathcal{S}_r |\phi|^4 \right] \quad \text{Dimension-5 scalar interactions}$$

$$\begin{aligned}
 -\mathcal{L}_q^{(5)} = & (\tilde{k}_S^B)_r \mathcal{S}_r B_{\mu\nu} B^{\mu\nu} + (\tilde{k}_S^W)_r \mathcal{S}_r W_{\mu\nu}^a W^{a\mu\nu} + (\tilde{k}_S^G)_r \mathcal{S}_r G_{\mu\nu}^A G^{\mu\nu A} \\
 & + (\tilde{k}_S^{\tilde{B}})_r \mathcal{S}_r B_{\mu\nu} \tilde{B}^{\mu\nu} + (\tilde{k}_S^{\tilde{W}})_r \mathcal{S}_r W_{\mu\nu}^a \tilde{W}^{a\mu\nu} + (\tilde{k}_S^{\tilde{G}})_r \mathcal{S}_r G_{\mu\nu}^A \tilde{G}^{\mu\nu A} \\
 & + \left\{ (\tilde{y}_S^e)_{rij} \mathcal{S}_r \bar{e}_{Ri} \phi^\dagger l_{Lj} + (\tilde{y}_S^d)_{rij} \mathcal{S}_r \bar{d}_{Ri} \phi^\dagger q_{Lj} + (\tilde{y}_S^u)_{rij} \mathcal{S}_r \bar{u}_{Ri} \phi^\dagger q_{Lj} \right\} \\
 & + (\tilde{k}_\Xi^\phi)_r \Xi_r^a D_\mu \phi^\dagger \sigma^a D^\mu \phi + (\tilde{\lambda}_\Xi)_r \Xi_r^a |\phi|^2 \phi^\dagger \sigma^a \phi \\
 & + (\tilde{k}_\Xi^{WB})_r \Xi_r^a W_{\mu\nu}^a B^{\mu\nu} + (\tilde{k}_\Xi^{W\tilde{B}})_r \Xi_r^a W_{\mu\nu}^a \tilde{B}^{\mu\nu} \\
 & + \left\{ (\tilde{y}_\Xi^e)_{rij} \Xi_r^a \bar{e}_{Ri} \phi^\dagger \sigma^a l_{Lj} + (\tilde{y}_\Xi^d)_{rij} \Xi_r^a \bar{d}_{Ri} \phi^\dagger \sigma^a q_{Lj} + (\tilde{y}_\Xi^u)_{rij} \Xi_r^a \bar{u}_{Ri} \phi^\dagger \sigma^a q_{Lj} \right\} \\
 & + \left\{ (\tilde{k}_{\Xi_1})_r \Xi_{1r}^{a\dagger} D_\mu \tilde{\phi}^\dagger \sigma^a D^\mu \phi + (\tilde{\lambda}_{\Xi_1})_r \Xi_{1r}^{a\dagger} |\phi|^2 \tilde{\phi}^\dagger \sigma^a \phi + (\tilde{y}_{\Xi_1}^e)_{rij} \Xi_{1r}^{a\dagger} \bar{e}_{Ri} \tilde{\phi}^\dagger \sigma^a l_{Lj} \right. \\
 & \left. + (\tilde{y}_{\Xi_1}^d)_{rij} \Xi_{1r}^{a\dagger} \bar{d}_{Ri} \tilde{\phi}^\dagger \sigma^a q_{Lj} + (\tilde{y}_{\Xi_1}^u)_{rij} \Xi_{1r}^{a\dagger} \bar{q}_{Li} \tilde{\phi}^\dagger \sigma^a \phi u_{Rj} + \text{h.c.} \right\}
 \end{aligned}$$

$$\begin{aligned}
 -\mathcal{L}_{SV} = & (\delta_{BS})_{rs} \mathcal{B}_{r\mu} D^\mu \mathcal{S}_s + (\delta_{W\Xi})_{rs} \mathcal{W}_{r,\mu} D^\mu \Xi_s && \text{Scalar-vector mixed} \\
 & + \left\{ (\delta_{\mathcal{L}^1\varphi})_{rs} \mathcal{L}_{1r\mu}^{1\dagger} D^\mu \varphi_s + (\delta_{\mathcal{W}^1\Xi_1})_{rs} \mathcal{W}_{1r\mu}^{1\dagger} D^\mu \Xi_{1s} + \text{h.c.} \right\} && \text{interactions} \\
 & + (\varepsilon_{S\mathcal{L}_1})_{rst} \mathcal{S}_r \mathcal{L}_{1s\mu}^\dagger \mathcal{L}_{1t}^\mu + (\varepsilon_{\Xi\mathcal{L}_1})_{rst} \Xi_r^a \mathcal{L}_{1s\mu}^\dagger \sigma^a \mathcal{L}_{1t}^\mu \\
 & + \left\{ (\varepsilon_{\Xi_1\mathcal{L}_1})_{rst} \Xi_{1i}^a \mathcal{L}_{1s\mu}^\dagger \sigma^a \tilde{\mathcal{L}}_{1t}^\mu + \text{h.c.} \right\} \\
 & + \left\{ (g_{S\mathcal{L}_1})_{rs} \phi^\dagger (D_\mu \mathcal{S}_r) \mathcal{L}_{1s}^\mu + (g'_{S\mathcal{L}_1})_{rs} (D_\mu \phi)^\dagger \mathcal{S}_r \mathcal{L}_{1s}^\mu \right. \\
 & \quad + (g_{\Xi\mathcal{L}_1})_{rs} \phi^\dagger \sigma^a (D_\mu \Xi_r^a) \mathcal{L}_{1s}^\mu + (g'_{\Xi\mathcal{L}_1})_{rs} (D_\mu \phi)^\dagger \sigma^a \Xi_r^a \mathcal{L}_{1s}^\mu \\
 & \left. + (g_{\Xi_1\mathcal{L}_1})_{rs} \tilde{\phi}^\dagger \sigma^a (D_\mu \Xi_{1r}^a)^\dagger \mathcal{L}_{1s}^\mu + (g'_{\Xi_1\mathcal{L}_1})_{rs} (D_\mu \tilde{\phi})^\dagger \sigma^a \Xi_{1r}^{a\dagger} \mathcal{L}_{1s}^\mu + \text{h.c.} \right\},
 \end{aligned}$$

- Lagrangian contains terms up to dimension 5 **sufficient to generate dimension-6 operators at tree level**
- Also includes “mixed” terms with multiple exotic multiplets

7 pages...

Going past dimension 6



- Tree-level completions of operators of odd mass dimension written down up to dimension 11
 - Database of 500,000 Lagrangians \Rightarrow Requires computational tools!
 - Matching onto any specific basis still needs to be done by hand

12772 16179461 8614953467442367 63d 11 37.9148278684193 $\text{loop}^{**2} \text{loopv}2 * v^{**2} yd * ye / \Lambda$ 2s6f_4 4 3 1

There are many search results. Let's make a more specific query.

```
In [20]: # Extend the query to look at the models with fewer than 5 fields that need to be at less than 7000 TeV
df[
  (df["democratic_num"] % df.exotics["S,01,0,1/3,-1"] == 0) &
  (df["democratic_num"] % df.exotics["S,00,0,1,0"] == 0) &
  (df["scale"] < 7000) &
  (df["n_fields"] < 5)
]
```

Out[20]:

| | democratic_num | stringent_num | op | dim | scale | symbolic_scale | topology | n_fields | n_scalars | n_fermions | min_loops | max_loops |
|-------|----------------|------------------|-----|-----|------------------|---|----------|----------|-----------|------------|-----------|-----------|
| 8387 | 3379507 | 30579275025083 | 10 | 9 | 5967.42299748072 | $\text{loop}^{**2} v^{**2} yd * ye / \Lambda$ | 0s6f_1 | 3 | 3 | 0 | 2 | |
| 12771 | 12372529 | 1378968263787181 | 63d | 11 | 37.9148278684193 | $\text{loop}^{**2} \text{loopv}2 * v^{**2} yd * ye / \Lambda$ | 2s6f_4 | 4 | 3 | 1 | 2 | |
| 12772 | 16179461 | 8614953467442367 | 63d | 11 | 37.9148278684193 | $\text{loop}^{**2} \text{loopv}2 * v^{**2} yd * ye / \Lambda$ | 2s6f_4 | 4 | 3 | 1 | 2 | |

Symbolic matching estimates

Investigation of *magic zeros*

Arkani-Hamed, Harigaya arXiv:2106.01373
 Craig, Garcia Garcia, Vainshtein, Zhang arXiv:2112.05770

- Magic zero: a quantity suppressed without an *apparent* symmetry explanation
- E.g. Vanishing dipole coefficient $H^\dagger \ell \sigma^{\mu\nu} e^c F_{\mu\nu}$ in model with two vector-like Dirac fermions: $S \sim (1,1)_0$ and $L \sim (1,2)_{1/2}$

$$\mathcal{L} \supset -m_L L^0 L^{c0} - m_S S S^c - \boxed{Y'_V H^0 L^0 S^c} + Y_L H^+ e S^c - Y_R H^- L^0 e^c + \text{h.c.}$$

$$\sim \tau_L \equiv \frac{e}{32\pi^2} \cdot \frac{v}{\sqrt{2}} \cdot \frac{Y_L Y_R Y'_V{}^*}{|m_L|^2 - |m_S|^2} \xrightarrow{\mathcal{P}'} -\tau_L$$

- Generalised parity symmetry \mathcal{P}' : $L^0 \leftrightarrow S^{c\dagger}$, $L^{c0} \leftrightarrow S^\dagger$, $m_L \leftrightarrow m_S^*$, $Y'_V \leftrightarrow Y'_V{}^*$, $Y_L \leftrightarrow Y_R^*$
- But dipole operator even under parity!

Investigation of *magic zeros*

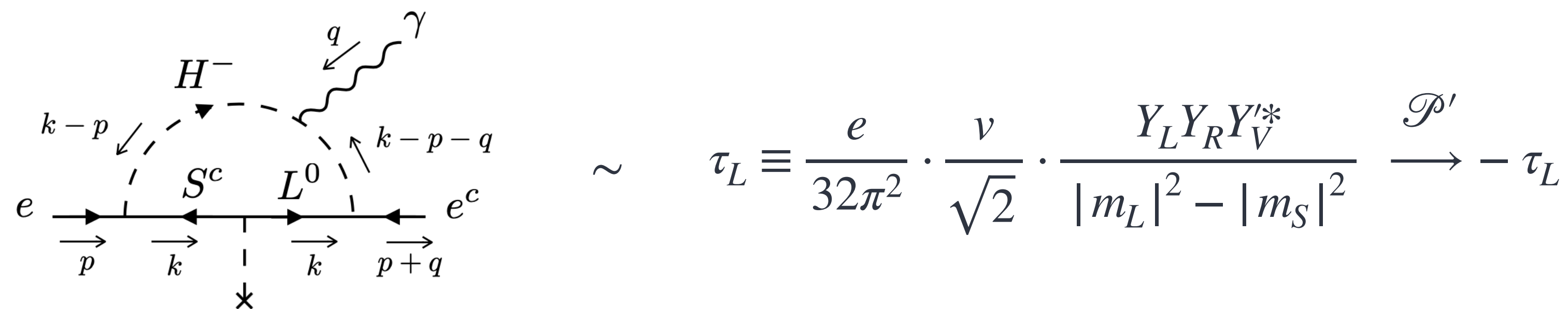
Arkani-Hamed, Harigaya arXiv:2106.01373
 Craig, Garcia Garcia, Vainshtein, Zhang arXiv:2112.05770

- Magic zero: a quantum
- E.g. Vanishing dipole moment
 $L \sim (1,2)_{1/2}$

```
In[3]:= alpha0eB [1, 1] /. MatchingResult
Out[3]= 
$$\frac{1}{384 M\Delta^2 M N^2 \pi^2} \text{g1 onelooporder} (4 M N^2 \lambda\Delta^1 [1] \times \lambda\Delta^1\text{bar} [\text{mif3}] \times \text{yl} [1, \text{mif3}] - 3 i\text{CPV}^2 M N^2 \lambda\Delta^1 [1] \times \lambda\Delta^1\text{bar} [\text{mif3}] \times \text{yl} [1, \text{mif3}] + M\Delta^2 \lambda\Delta^1 [\text{mif3}] \times \lambda\Delta^1\text{bar} [1] \times \text{yl} [\text{mif3}, 1])$$

In[4]:= alpha0eB [1, 1] /. MatchingResult /. yl [x_, y_] => 0
Out[4]= 0
```

$S \sim (1,1)_0$ and



- Generalised parity symmetry \mathcal{P}' : $L^0 \leftrightarrow S^{c\dagger}$, $L^{c0} \leftrightarrow S^\dagger$, $m_L \leftrightarrow m_S^*$, $Y'_V \leftrightarrow Y'^*_V$, $Y_L \leftrightarrow Y^*_R$
- But dipole operator even under parity!