



Sensitivity of 1 TeV ILC to measure CP-odd Higgs interactions in ZZ-fusion

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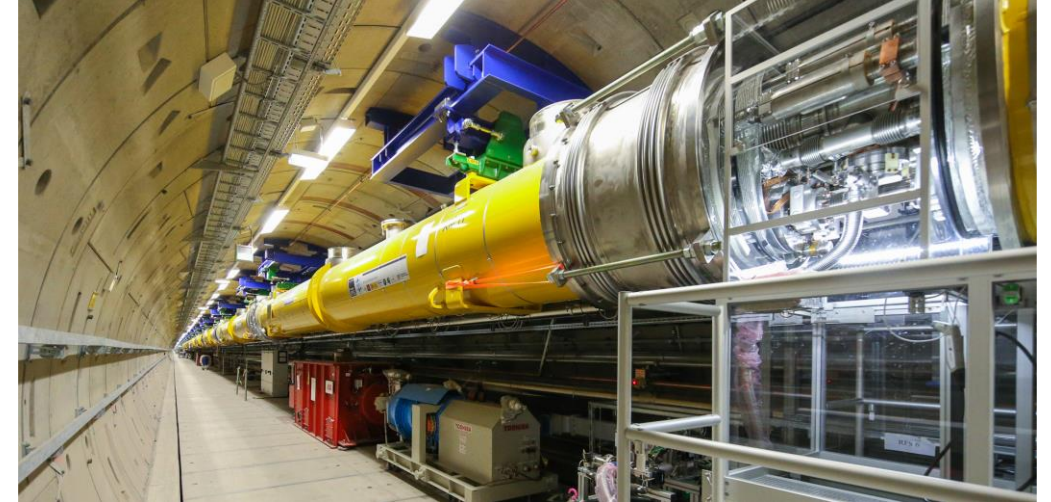
[ECFA meeting on ee to ZH angular measurements](#)

OPENING QUESTIONS/OUTLINE

1. Could 125 GeV Higgs mass eigenstate be a mixture of CP-odd and CP-even states via mixing angle Ψ_{CP} ?
2. If so, with what precision Ψ_{CP} can be measured at 1 TeV ILC ?
3. What is the interpretation of the measurement sensitivity (in the context of Snowmass CPV White paper [\[arXiv:2205.07715v3\]](https://arxiv.org/abs/2205.07715v3))?

A WORD ON ILC

	\sqrt{s}	beam polarisation	$\int L dt$ (baseline)
ILC	0.1 - 1 TeV	e-: 80% e+: 30% (20%)	2 ab ⁻¹ @ 250 GeV 0.2 ab ⁻¹ @ 350 GeV 4 ab ⁻¹ @ 500 GeV 8 ab ⁻¹ @ 1 TeV



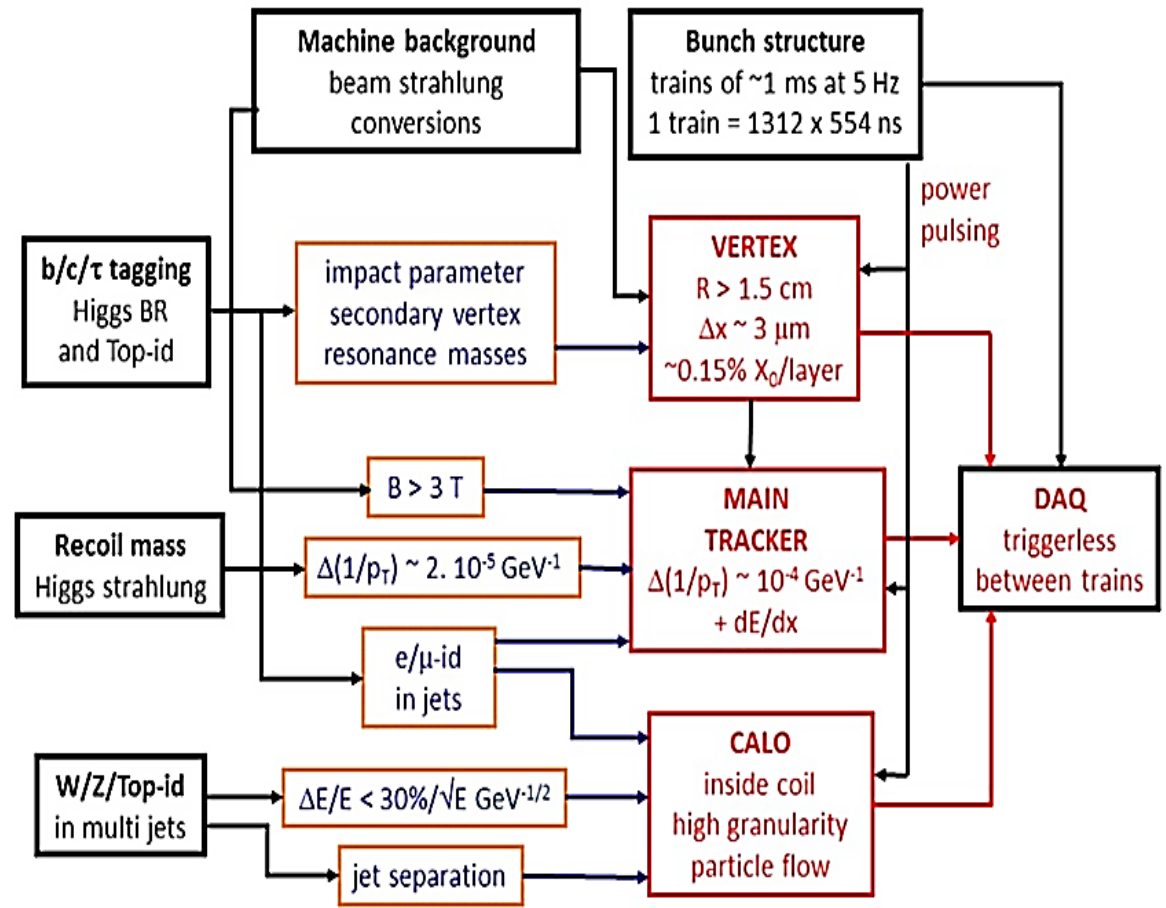
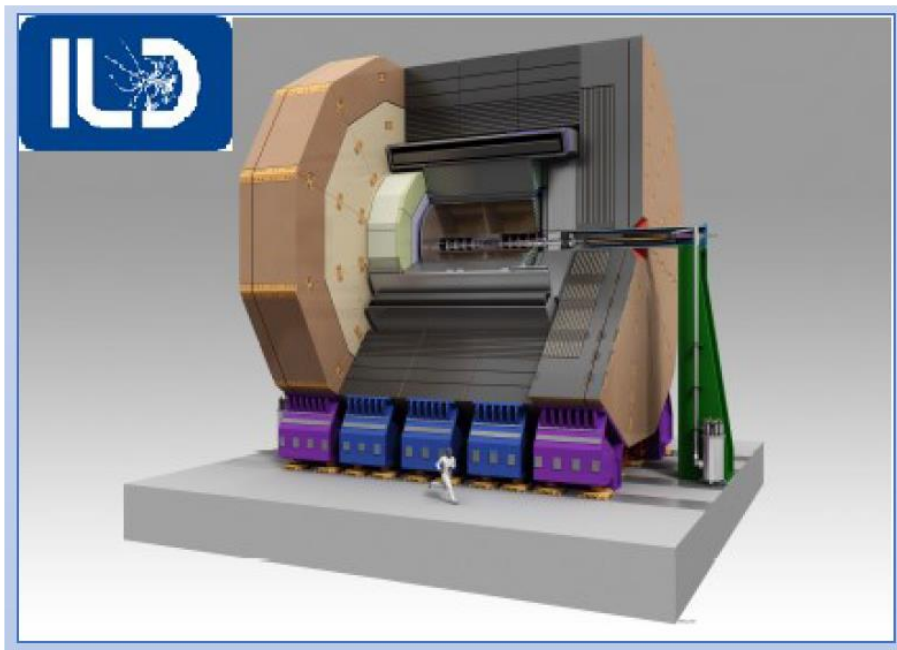
An off-shore Higgs factory, realized in collaboration with international partners, in order to reveal the secrets of the Higgs boson. The current designs of FCC-ee and ILC meet our scientific requirements. The US should actively engage in feasibility and design studies.

**P5 Panel
Recommendation 2**

- Comes as a 'ready to take' project (mature design, proven technologies)
- Largest ever accelerator prototype (operating now as E-XFEL), full industrialization of ILC-type SCRF cavity production
- Tunable, upgradeable (from Z-pole, via Higgs factory mode, 500 GeV up to 1 TeV, or by replacing accelerating structures with advanced technologies)
- Numerous benefits from the high energy phases (≥ 500 GeV) and beam polarization

A WORD ON ILD

- Two validated detector concepts: ILD and SiD
- Physics driven requirements
- Decades of extensive detector R&D \Rightarrow mature design (& available technologies)
- Multiple R&D collaborations involved (CALICE, FCAL, LCTPC,..)



SENSITIVE OBSERVABLE

- Generic model of CPV mixing: $h_{125} = H \cdot \cos \Psi_{CP} + A \cdot \sin \Psi_{CP}$
- CP-sensitive observable: angle between production planes $\Delta\phi$
- As shown in [\[arXiv:2203.11707v3\]](https://arxiv.org/abs/2203.11707v3) $\Delta\Phi$ carries the most information on the Higgs CP state

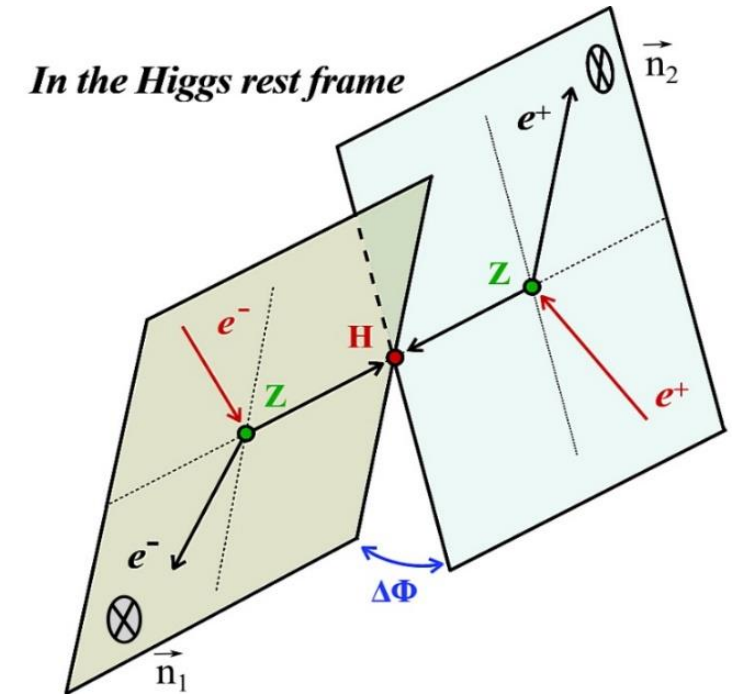
$$\Delta\Phi = \begin{cases} \arccos(\cos \Delta\Phi), & \text{sgn}(\sin \Phi) \geq 0 \\ 2\pi - \arccos(\cos \Delta\Phi), & \text{sgn}(\sin \Phi) < 0 \end{cases}$$

$$\cos \Phi = (\hat{n}_1 \cdot \hat{n}_2)$$

$$\text{sgn}(\sin \Phi) = \frac{\mathbf{q}_1 \cdot (\hat{n}_1 \times \hat{n}_2)}{|\mathbf{q}_1 \cdot (\hat{n}_1 \times \hat{n}_2)|}$$

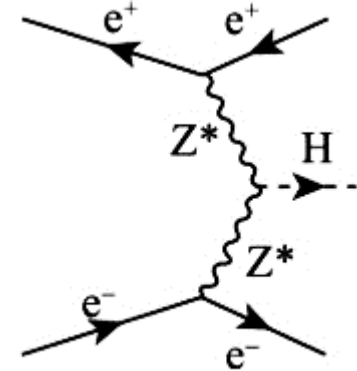
$$\hat{n}_1 = \frac{q_{e_i^-} \times q_{e_f^-}}{|q_{e_i^-} \times q_{e_f^-}|}$$

$$\hat{n}_2 = \frac{q_{e_i^+} \times q_{e_f^+}}{|q_{e_i^+} \times q_{e_f^+}|}$$



SIGNAL AND BACKGROUND

1 TeV	σ (fb)	Expected in 8 ab^{-1} full range	Reconstructed with ILD
Signal:			$2 \cdot 10^5$ DELPHES $\sim 36.6 \text{ ab}^{-1}$
$e^+e^- \rightarrow H e e, H \rightarrow b\bar{b}$	13	104000	3495 full sim. $\sim 0.22 \text{ ab}^{-1}$
$e^+e^- \rightarrow q\bar{q}l^+l^-$	255	$2 \cdot 10^6$	$1 \cdot 10^6$ DELPHES
			5886 full sim.
$e^+e^- \rightarrow q\bar{q}$	9375	$75 \cdot 10^6$	120343 full sim.
$e^+e^- \rightarrow q\bar{q}lv$	4116	$32.9 \cdot 10^6$	955058 full sim.

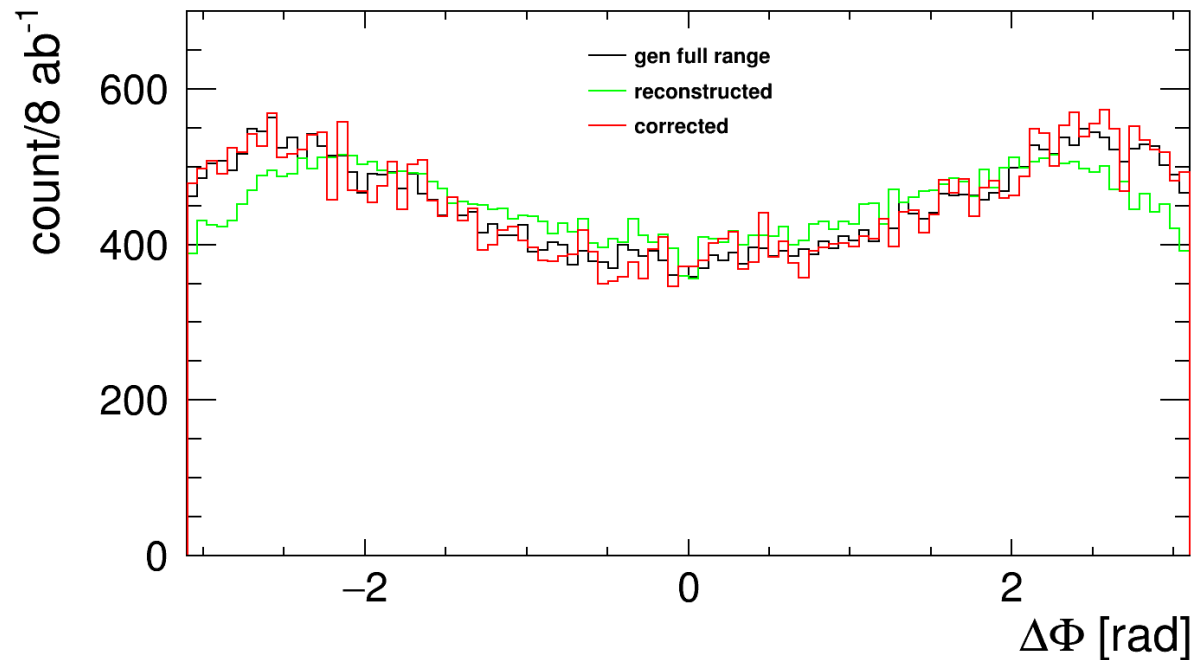


- Generator level WHIZARD
V2.8.3/UFO/Higgs characterization
model signal and WHIZARD 1.95/SM
background
- Unpolarized beams
- $H \rightarrow b\bar{b}$ (to suppress $e e \gamma$ background)
- b-tagging efficiency is idealized to 100%

500 GeV, 1 TeV energies are optimal due to interplay of x-section and centrality

GENERATED AND RECONSTRUCTED SIGNAL

Corrected reconstructed signal for pure scalar $\Psi_{CP}=0$, **generated** information (WHIZARD) and **uncorrected** reconstructed signal



- Acceptance correction needed to retrieve full physical information
- Generated information is reasonably well reproduced with corrected reconstructed data

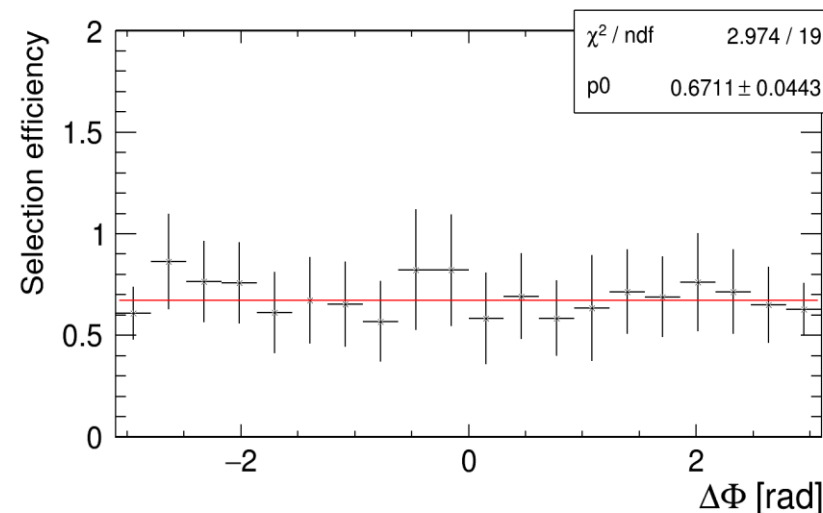
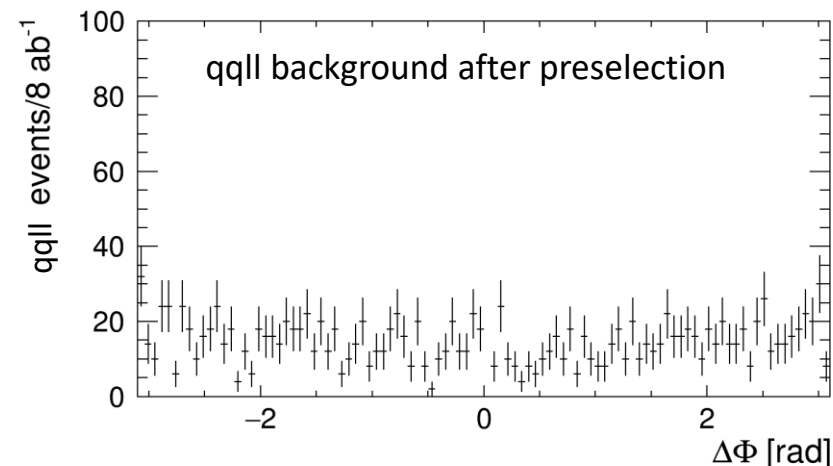
EVENT SELECTION

○ Preselection – electron isolation:

- $m_{e^+e^-} > 200$ GeV (veto HZ)
- $E_{e^\pm} > 60$ GeV
- DELPHES electron isolation
 - $\Delta R_{max} = 0.5$
 - $p_{Tmin} = 0.5$ GeV
 - $I = \frac{\sum_{i \neq P}^{p_T(i) > p_T^{min}} p_T(i)}{p_T(P)} < 0.12$
- Signal preselection efficiency: **~71%**

○ Selection cuts:

- 80 GeV $< m_{q\bar{q}} < 160$ GeV
- $m_{Z_1, Z_2} > 30$ GeV
- $p_{Tee} > 15$ GeV,
- $p_{Tmiss} > 150$ GeV
- Selection efficiency: **96%**
- **Total signal efficiency: ~ 68%**

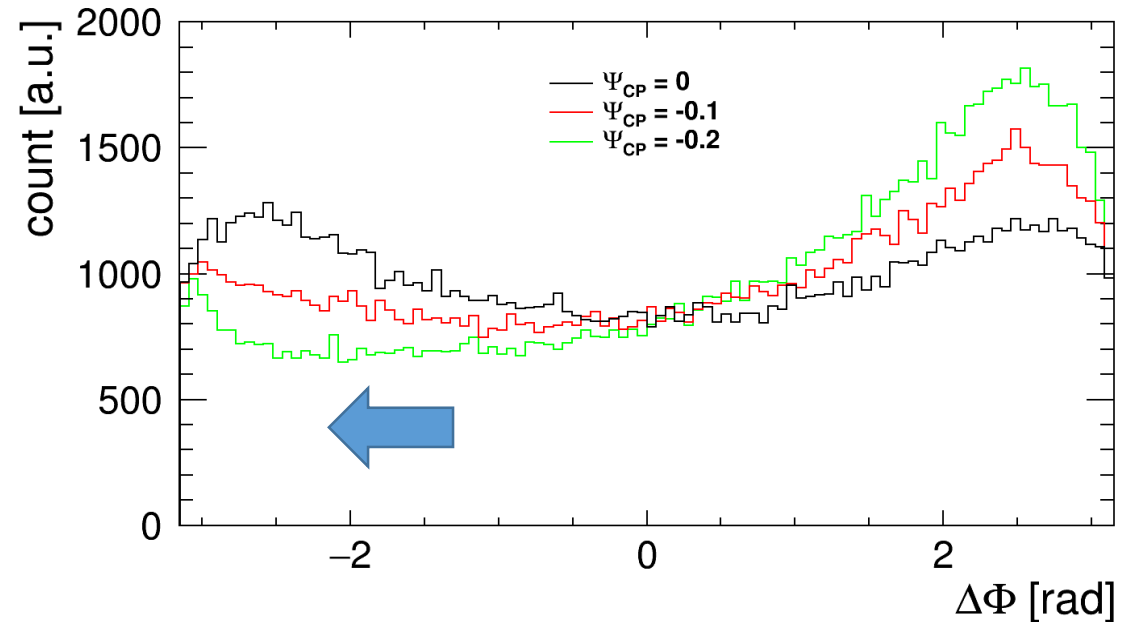
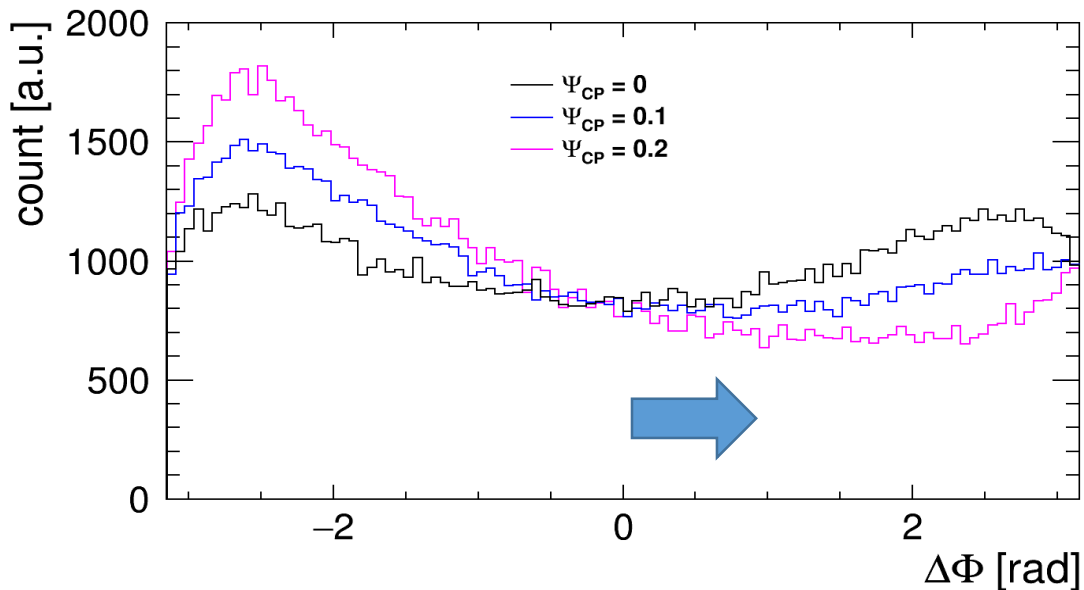


- **Unbiased selection w.r.t. $\Delta\Phi$**
- Background is CP insensitive, fully suppressed (preselection efficiency $\leq 10^{-4}$)

ANGULAR OBSERVABLE $\Delta\Phi$ AND MIXING ANGLE Ψ_{CP}

○ Minimum of $\Delta\Phi$ shifts for non-zero Ψ_{CP}

- Differently from the $H \rightarrow \tau\tau$ angular observable whose dependence on Ψ_{CP} can be derived from the differential x-section, here Ψ_{CP} has to be extracted **empirically**



HOW TO EXTRACT Ψ_{CP} ?

✓ Minimum of $\Delta\Phi$ is sensitive to Ψ_{CP} ;

1. Determine position of the local minimum
(b/a) from experimental (pseudo) data:

$$f(\Delta\Phi, \Psi_{CP}) = A + B \cdot \cos(a \cdot \Delta\Phi - b)$$

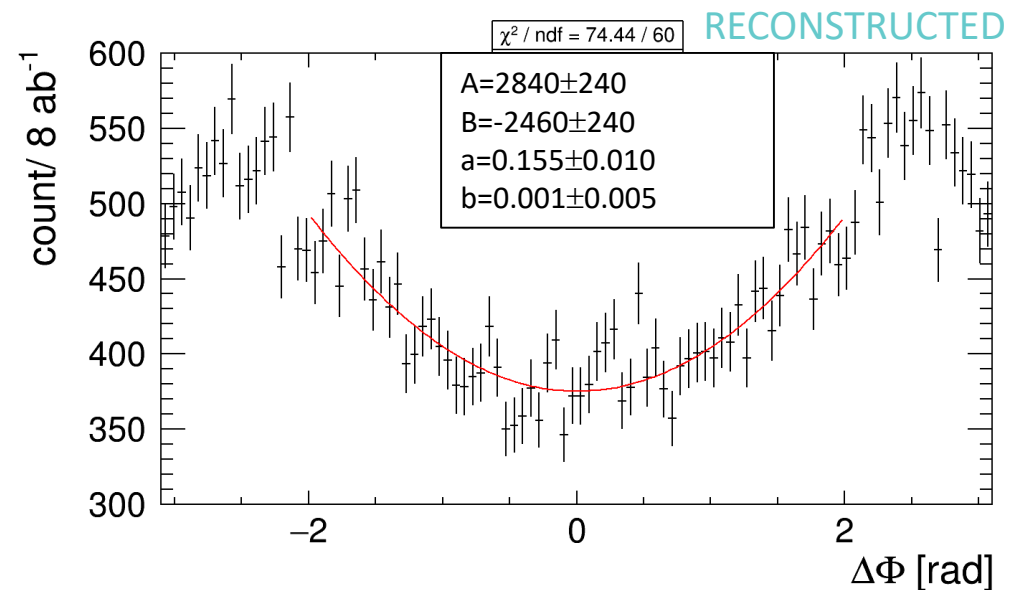
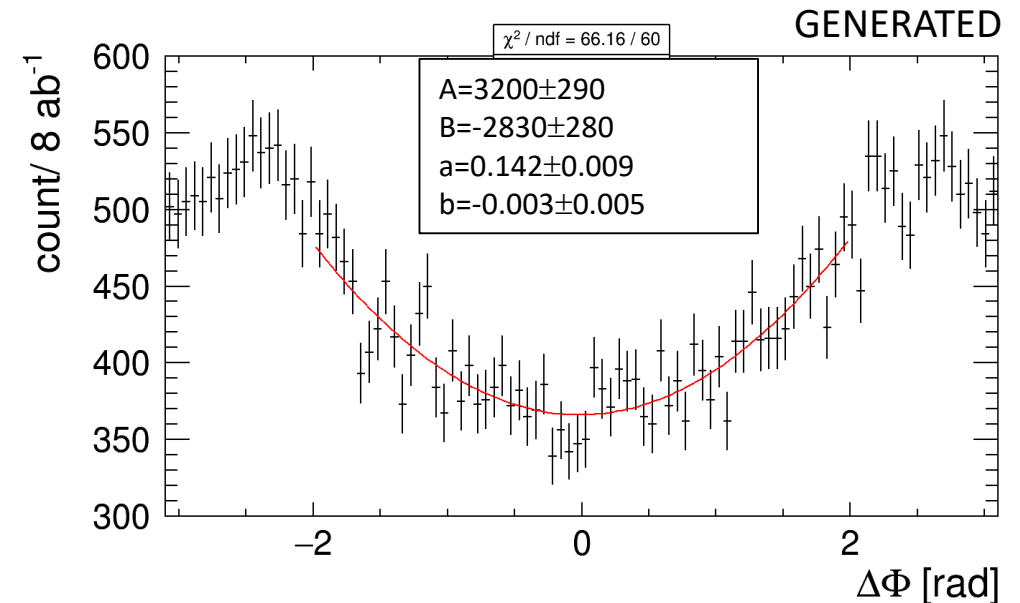
2. Position (b/a)/ Ψ_{CP} is a linear function of Ψ_{CP} :

$$(b/a) / \Psi_{CP} = k \cdot \Psi_{CP} + m$$

3. Determine from simulation coefficients k, m

4. Ψ_{CP} can be retrieved from quadratic equation:

$$k \cdot \Psi_{CP}^2 + m \cdot \Psi_{CP} - (b/a) = 0$$



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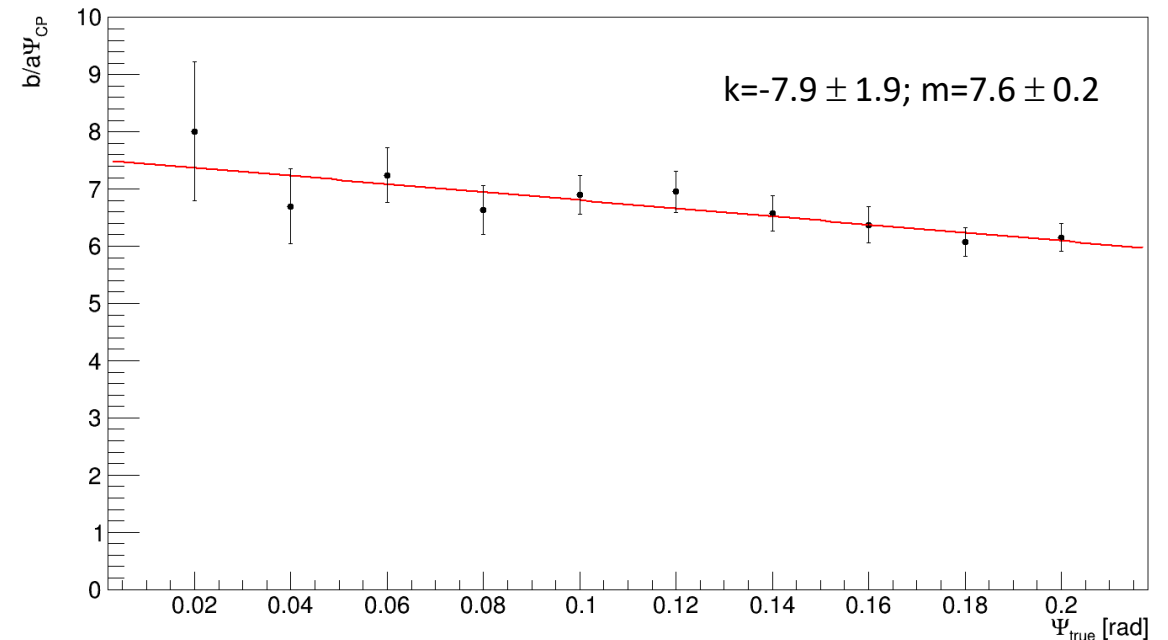
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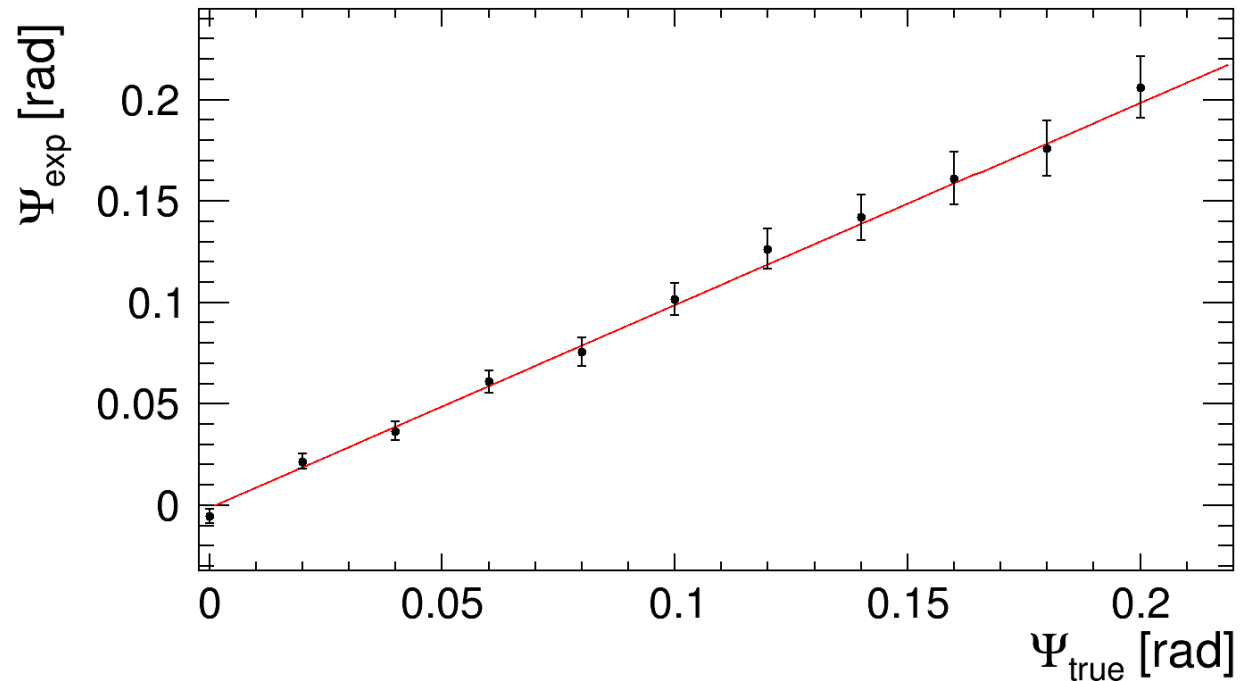
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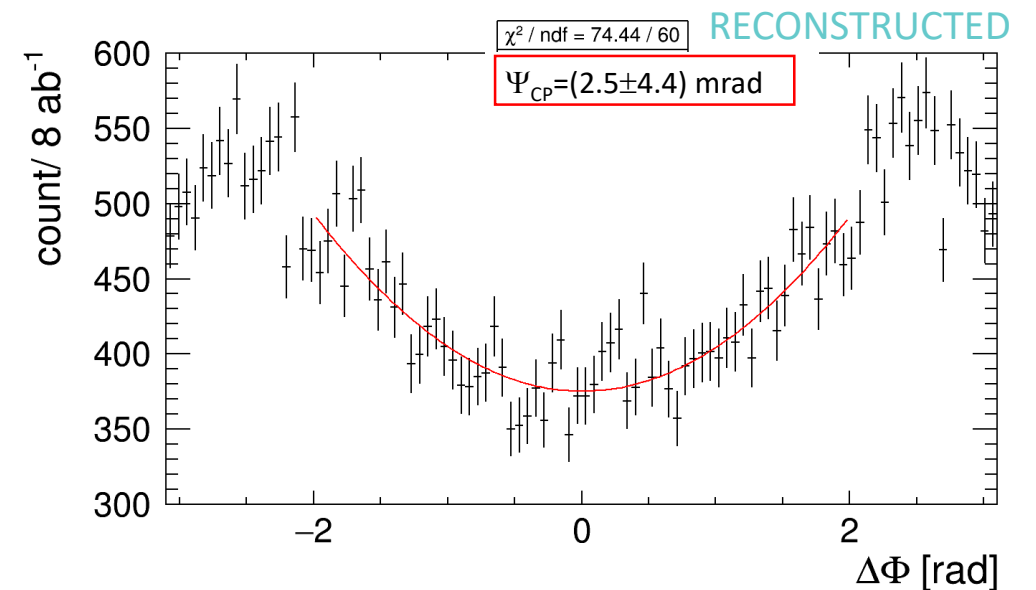
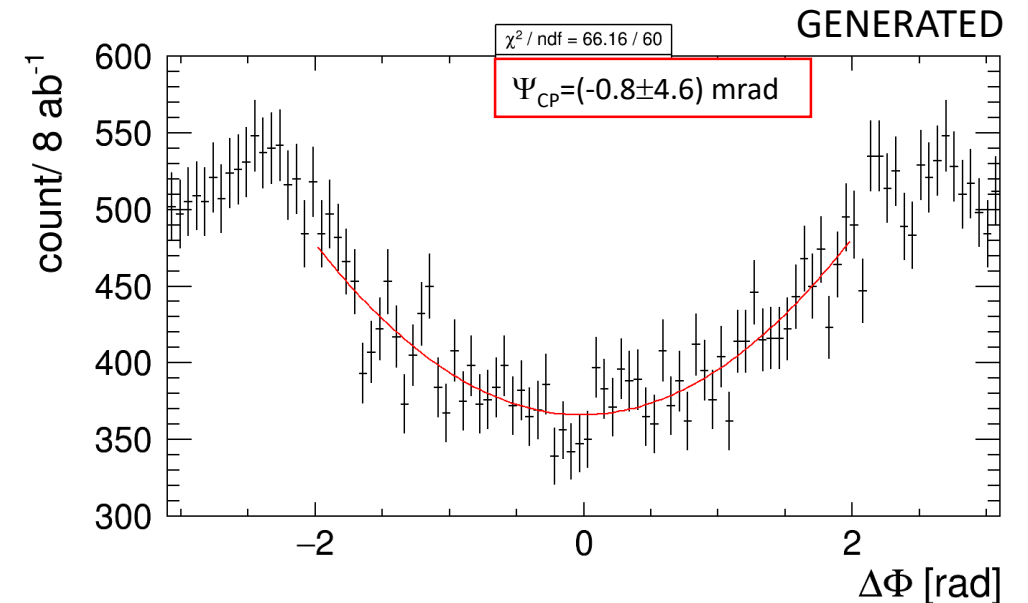
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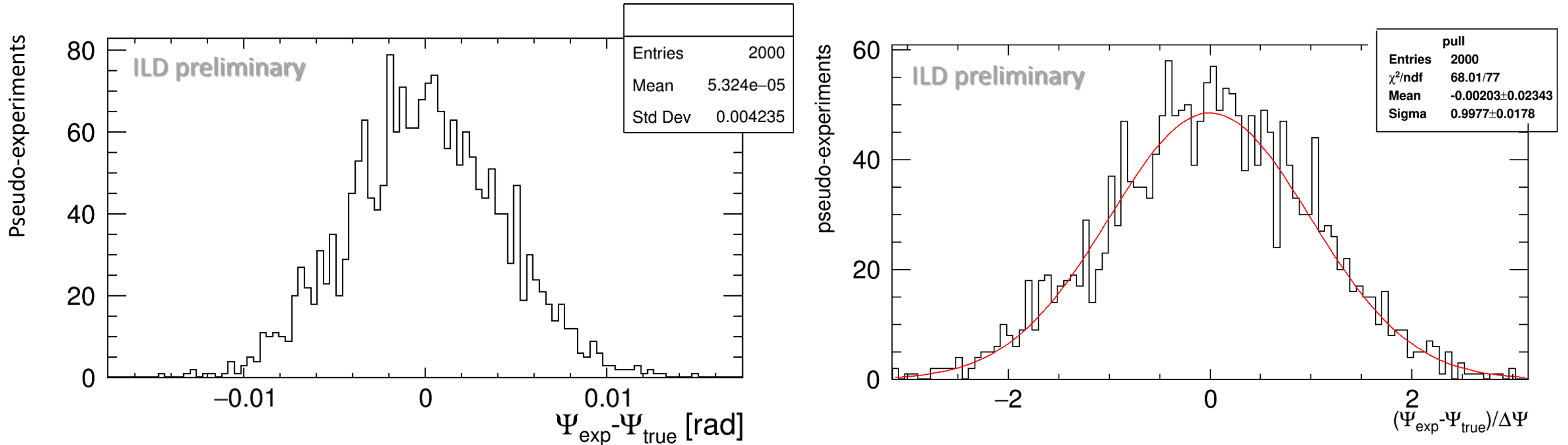
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PSEUDO-EXPERIMENTS

$$\Delta\Psi_{\text{(stat.)}}^{\text{CP}} = 4 \text{ mrad}$$



- 2000 pseudo-experiments give 4 mrad for statistical dissipation of the mean
- Pull distribution indicates that uncertainties are correctly estimated
- Systematic error from the fit parameters uncertainties gives ~1 mrad

INTERPRETATION

- Common framework is defined in the Snowmass CPV White paper: benchmark parameter

$$f_{CP} \sim \sin^2(\Delta\Psi_{CP}) \text{ quantifying relative contribution from CP-odd amplitude } f_{CP}^{hX} \equiv \frac{\Gamma_{h \rightarrow X}^{CP \text{ odd}}}{\Gamma_{h \rightarrow X}^{CP \text{ odd}} + \Gamma_{h \rightarrow X}^{CP \text{ even}}}$$

- Interpretation for LHC/HL-LHC and future Higgs factories, for EFT and CP-sensitive observable based measurements

(68% CL, pure scalar)

[\[arXiv:2205.07715v3\]](https://arxiv.org/abs/2205.07715v3)

Collider	<i>pp</i>	<i>pp</i>	<i>pp</i>	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14.000	14.000	100.000	250	350	500	1.000	1.300	125	125	3.000	(theory)
\mathcal{L} (fb ⁻¹)	300	3.000	30.000	250	350	500	1.000	1.000	250	20	1.000	
<i>HZZ/HWW</i>	$4.0 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.9 \cdot 10^{-5}$	$2.9 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	$3.0 \cdot 10^{-6}$ (10 ab ⁻¹)	✓	✓	✓	✓	$< 10^{-5}$
<i>Hγγ</i>	–	0.50	✓	–	–	–	–	–	0.06	–	–	$< 10^{-2}$
<i>HZγ</i>	–	~1	✓	–	–	–	~1	–	–	–	–	$< 10^{-2}$
<i>Hgg</i>	0.12	0.011	✓	–	–	–	–	–	–	–	–	$< 10^{-2}$
<i>Ht\bar{t}</i>	0.24	0.05	✓	–	–	0.29	0.08	✓	–	–	✓	$< 10^{-2}$
<i>Hττ</i>	0.07	0.008	✓	0.01	0.01	0.02	0.06	–	✓	✓	✓	$< 10^{-2}$
<i>Hμμ</i>	–	–	–	–	–	–	–	–	–	✓	–	$< 10^{-2}$

1 TeV ILC

- ✓ First measurement in VBF
- ✓ First measurement in HZZ vertex based on angular observable
- ✓ Full background simulation of ILD detector and fast simulation of the signal
- ✓ Realistic ILC running scenario

INTERPRETATION

(68% CL, pure scalar)

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\mathcal{L} (fb ⁻¹)	300	3,000	30,000	250	350	500	8 ab⁻¹	1,000	250	20	1,000	
<i>HZZ/HWW</i>	$4.0 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.9 \cdot 10^{-5}$	$2.9 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	$1.6 \cdot 10^{-5}$	✓	✓	✓	✓	$< 10^{-5}$
<i>Hγγ</i>	-	0.50	✓	-	-	-	-	-	0.06	-	-	$< 10^{-2}$
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<i>Ht\bar{t}</i>	0.24	0.05	✓	-	-	0.29	0.08	✓	-	-	✓	$< 10^{-2}$
<i>Hττ</i>	0.07	0.008	✓	0.01	0.01	0.02	0.06	-	✓	✓	✓	$< 10^{-2}$
<i>Hμμ</i>	-	-	-	-	-	-	-	-	-	✓	-	$< 10^{-2}$

SUMMARY

- ✓ Complete simulation of CP Higgs mixing angle (Ψ_{CP}) measurement is performed at 1 TeV ILC with the ILD detector
- ✓ This is the first result in VBF fusion based on angular observable ($\Delta\Phi$);
- ✓ Knowing the dependence of $\Delta\Phi$ minimum to Ψ_{CP} from simulation, Ψ_{CP} can be determined from (experimental) data;
- ✓ From 8 ab^{-1} of 1 TeV ILC data, pure scalar state should be measured with 4 mrad statistical uncertainty of Ψ_{CP} at 68% CL; Systematic uncertainty from the fit is found to be smaller (< 1 mrad);
- ✓ The above uncertainty corresponds to $f_{\text{CP}} \approx 1.6 \cdot 10^{-5}$ approaching theoretical target;
- ✓ The precision can be improved in combination with other Higgs decay channels (i.e. $\text{H} \rightarrow \text{WW} \rightarrow 4\text{-jets}$).