

# Lund Jet Plane studies at FCC-ee



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L. Panwar, B. Malaescu, L. Poggioli

contact email: [lata.panwar@cern.ch](mailto:lata.panwar@cern.ch)

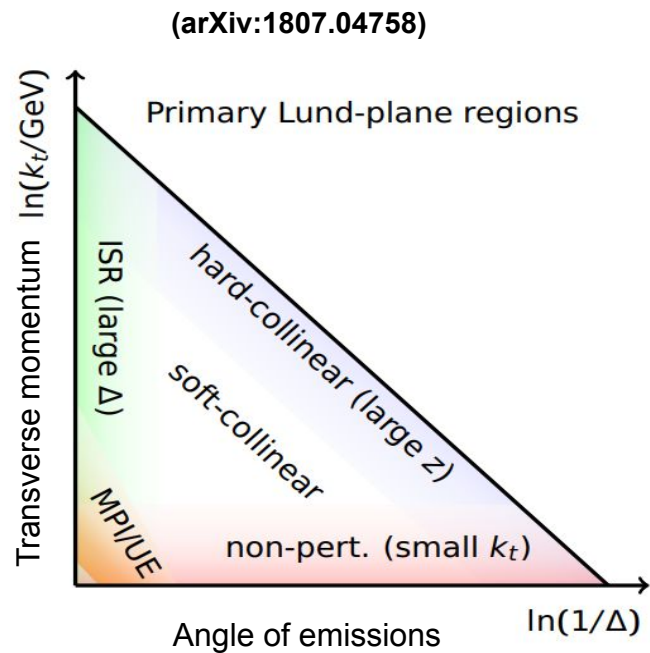
# Introduction and motivation

- **Analysis:** Prospects of QCD studies related to jet formation at FCC-ee using Lund Jet Plane (LJP) representation
  - motivated by the study of the sensitivity to  $\alpha_s$  at FCC-ee, probing of  $\alpha_s$  for different energies and tests of the renormalization group equation (RGE) in QCD
  - complementary to the 3/2 Jet cross-section ratio study for  $\alpha_s$
  - First study which looks at jet substructure at FCC-ee
- **Why at FCC-ee?**
  - provides a clean collision environment with high statistics for precise measurements
  - potential impact on detector parameters
- Use Delphes samples from [Winter2023](#) campaign simulated for IDEA detector at  $\sqrt{s} = 91$  GeV
  - Use light jets from process:  $ee \rightarrow Z \rightarrow \text{light jets}$  (**p8\_ee\_Zud\_ecm91**)

# Introduction and motivation

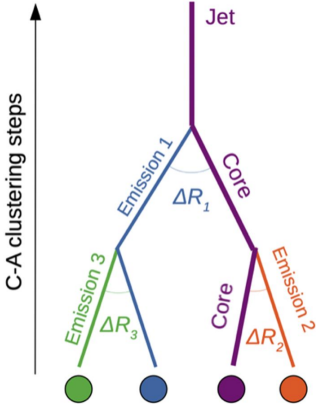
## Advantage of Lund Jet Plane method (LJP):

- QCD jet formation involves perturbative and non-perturbative effects; presence of these effects impact the precision of any measurement based on jets
- LJP works as a handle to separate these effects in a 2D representation using angle ( $\Delta$ ) and transverse momentum ( $k_t$ ) of emissions within the jets and further opens a possibility to understand QCD behaviour separately for these perturbative and non-perturbative effects
- **First let's understand LJP formation with more details**



# Introduction and motivation

- **Lund Jet plane (LJP)**



- Start with a jet and cluster it again with Cambridge/Aachen (C/A) to have angular order information of emissions
- Decluster them in reverse (start with wide angle emission first)
- Within the iterative declustering, harder branch is always taken as core branch
- fill a triangle plane of two Lund variables from core and emission

For “a” core and “b” emission branch

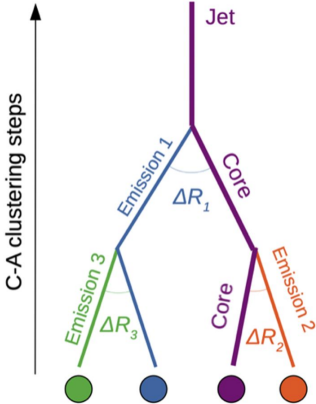
$$\Delta R = \Delta R_{ab} , \quad k_t \equiv p_{tb} \Delta R_{ab}$$

$$z \equiv p_{tb} / (p_{ta} + p_{tb})$$

$\Delta R_{ab}$  = angle of emission **b** wrt to core **a**  
 $k_t$  = transverse momentum of **b** wrt **a**  
 (for  $p_{tb} \ll p_{ta}$  and  $\Delta \ll 1$ )  
 $z$  = momentum fraction taken by **b**

# Introduction and motivation

- **Lund Jet plane (LJP)**



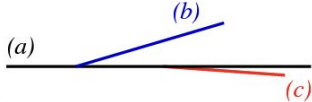
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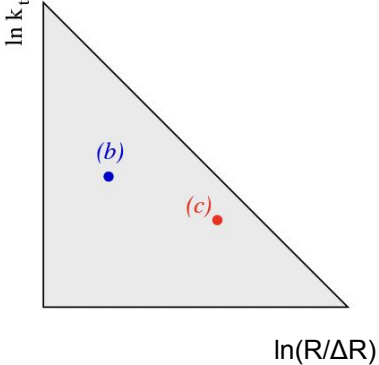
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JET



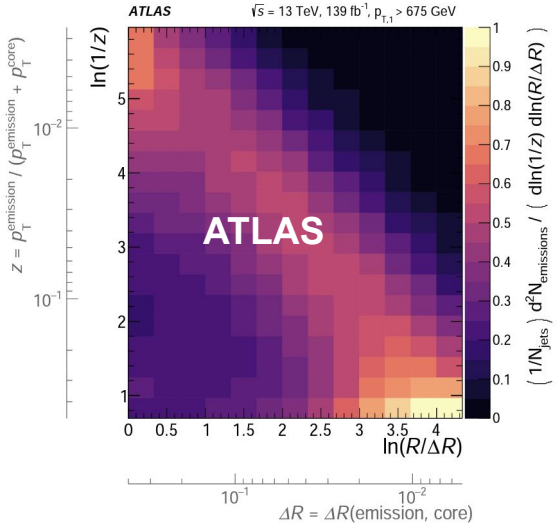
PRIMARY LUND PLANE



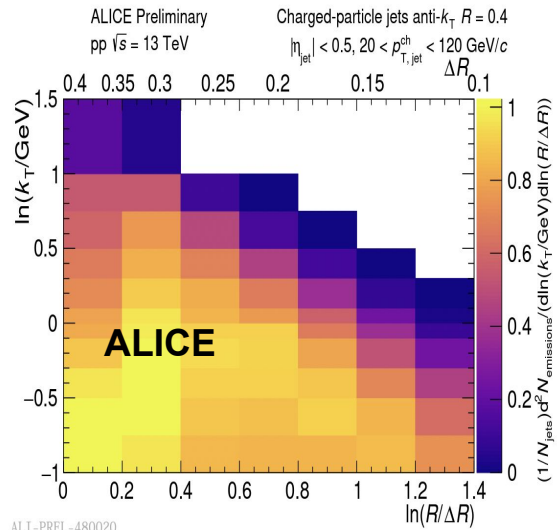
# Recent Lund Jet Plane based measurements

- LJP studies at LHC  $\sqrt{s} = 13$  TeV, following recent theoretical proposal ([JHEP 12 \(2018\) 064](#))
- These studies measure the lund plane density for charged particles jets
- We are interested in following the same for FCC-ee environment

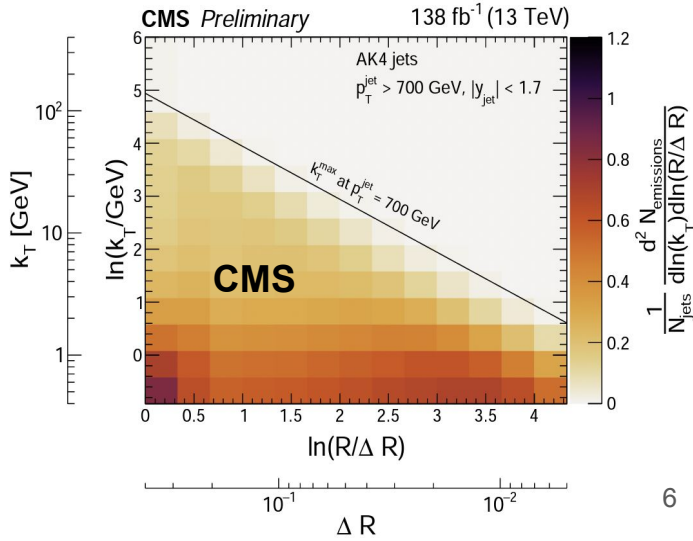
[arXiv 2004.03540](#)



[arXiv 2111.00020](#)



[CMS-PAS-SMP-22-007](#)



# Methodology

1. Framework: [HEP-FCC/FCCAnalyses](#)
2. Jet Clustering:
  - a. Input collection **ReconstructedParticles**  
(smeared reco particles)
  - b. Definitions:

Valencia jets  $R = 1.5$ ,  $\beta = 1.0$  inclusive clustering

Anti  $k_T$  jets  $R = 1.5$ , inclusive clustering

## Valencia jet clustering

$$d_{ij} = \min(E_i^{2\beta}, E_j^{2\beta})(1 - \cos \theta_{ij})/R^2$$

$$d_{iB} = p_T^{2\beta}$$

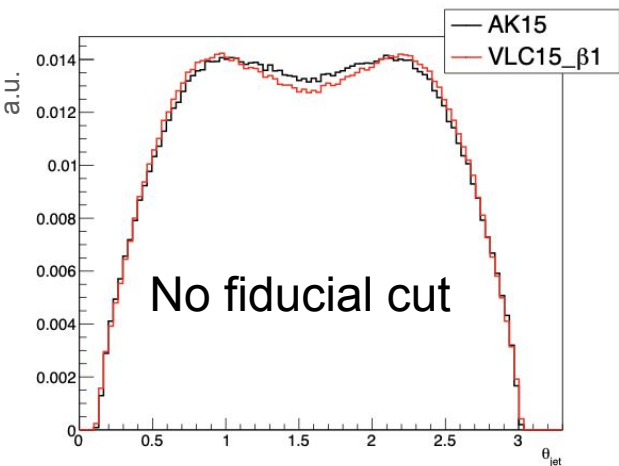
## Anti- $k_T$ and C/A jet clustering

$$d_{ij} = \min(p_{ti}^{2p}, p_{tj}^{2p}) \frac{\Delta R_{ij}^2}{R^2}, \quad \Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2,$$

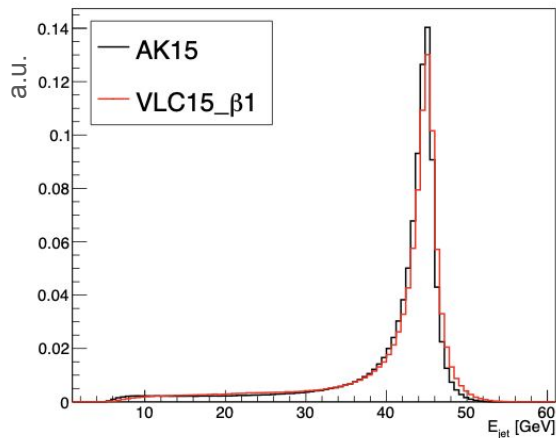
$$d_{iB} = p_{ti}^{2p}, \quad \text{for anti-}k_T \text{ } p = -1 \text{ and C/A } p=0$$

# Kinematic comparison for QCD jets: Valencia vs anti- $k_T$

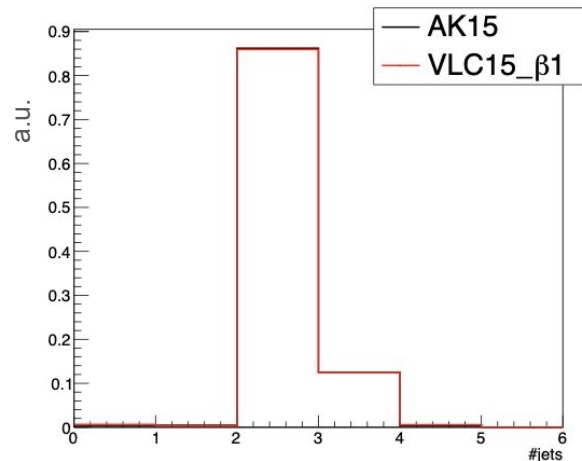
Process: ee\_Zud\_ecm91



$\theta_{jet}$



$E_{jet} \geq 10$  GeV



$N_{jets} \geq 2$

Selections	Selection Efficiency
Jet energy $\geq 10$ GeV	99.5%
$N_{jets} \geq 2$	99.1%

**NOTE:**

we use anti- $k_T$  algorithm for preliminary studies



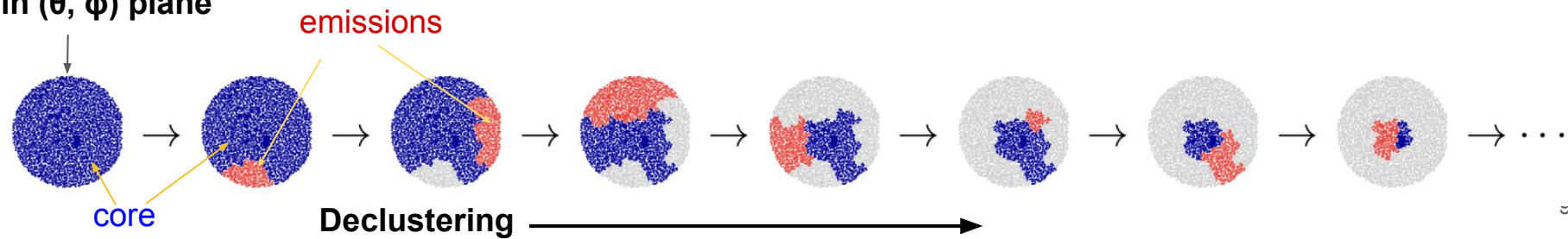
# Methodology

3. Once we have jet clustered, we save corresponding reco particle (smeared particles) constituents using "JetClusteringUtils::get\_constituents"

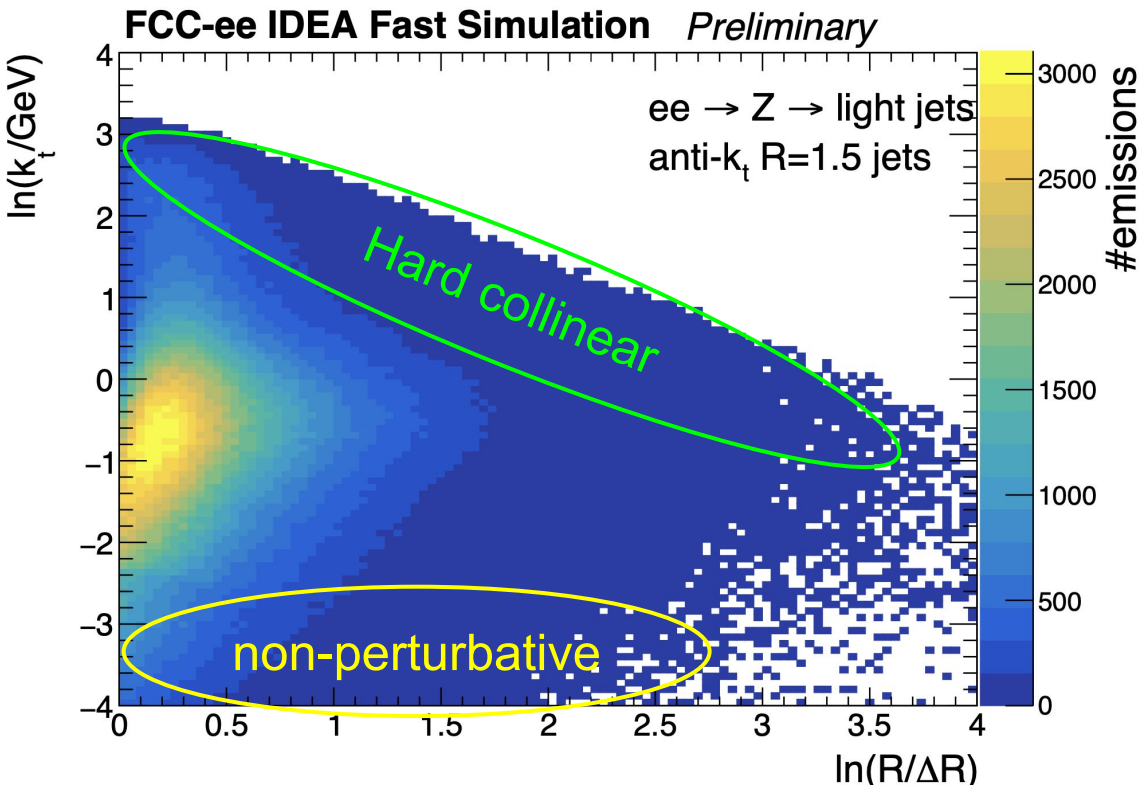
4. Pick constituents of a jet

- The clustering information is not saved during jet reconstruction so first we recluster jet again with AK15 algorithm by saving the clustering subjet information using fastjet dedicated functions
- Afterwards, picking the same subjets, jet is clustered using C/A algorithm to follow angular-ordered clustering
- Now we go back and do declustering in angular order; start from wide angle first
- Calculate LJP variables using core and emission subjets iteratively and fill the LJP plane

**C/A re-clustered anti- $k_t$  jet in  $(\theta, \phi)$  plane**

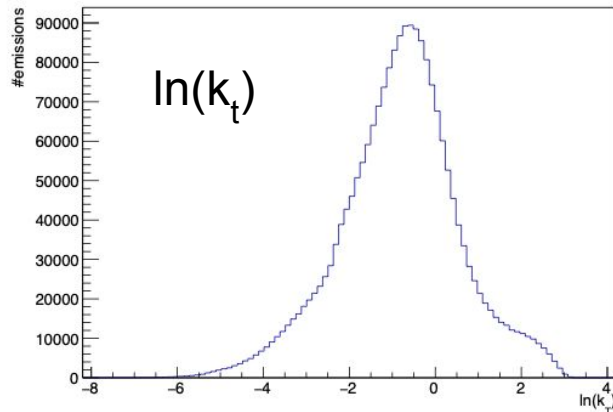


# First look LJP representation (after event selection)

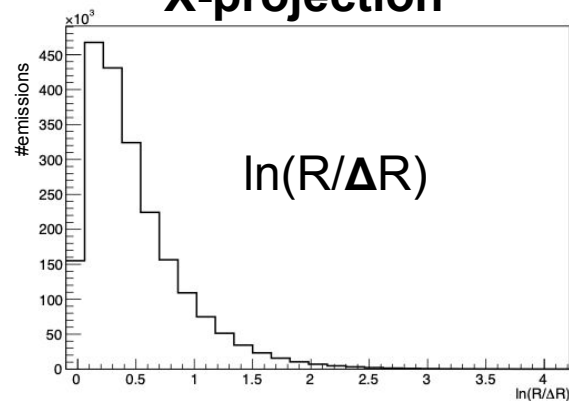


(LJP representation of jets using smeared particle constituents from fast simulation)

## Y-projection



## X-projection



# Summary and other possibilities

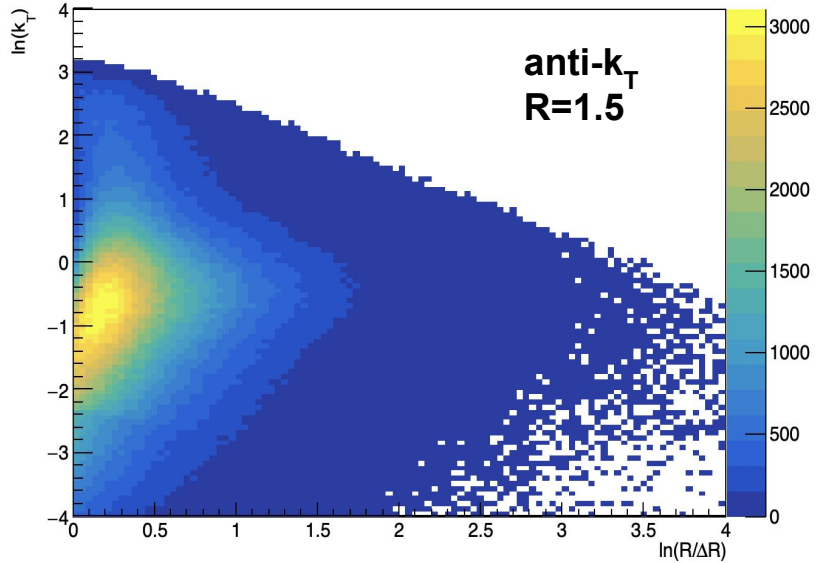
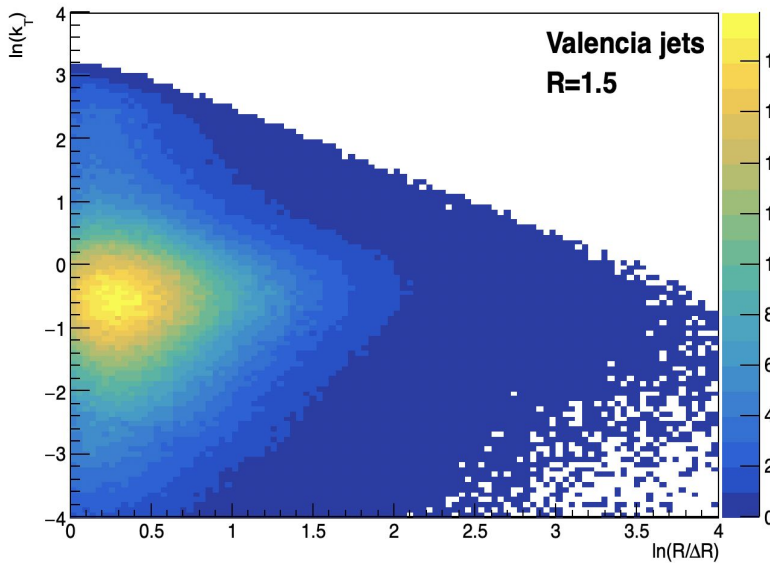
- First study which looks at jet substructure at FCC-ee
  - Motivated by the study of the sensitivity to  $\alpha_s$  and test of RGE at FCC-ee
  - Present preliminary LJP representation for QCD jets (for AK15 inclusive jets) using delphes samples
  - explore sensitivity to detector parameters
- We need fullsim for a given  $\alpha_s$  value to study the reconstruction of the LJP for different options of detector technologies.
- An  $\alpha_s$  scan will be necessary to study the sensitivity of the reconstructed LJP to  $\alpha_s$
- **Other prospects:**
  - LJP tool can be used to develop tagging methods, e.g. heavy flavour jet tagging, EM objects tagging etc.

# BACKUP

## Technical questions

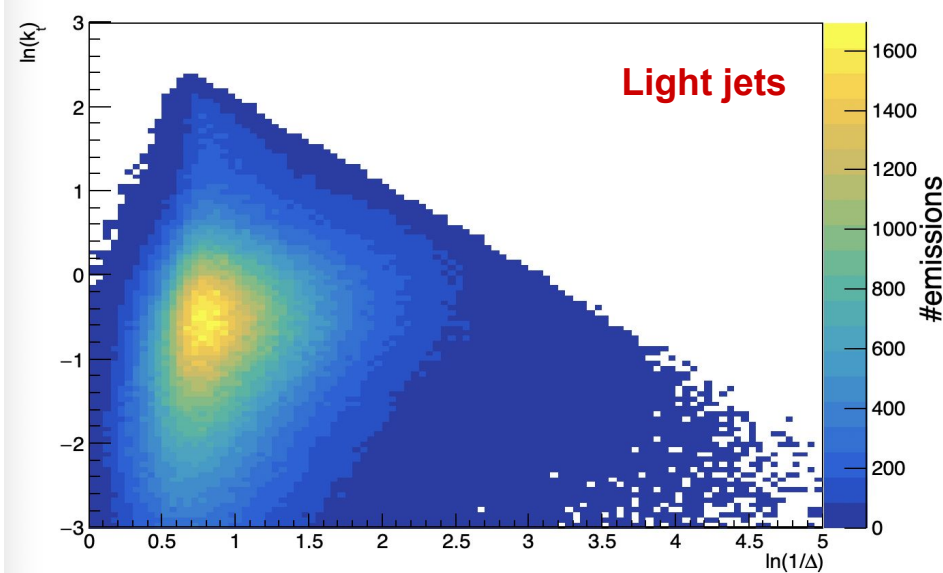
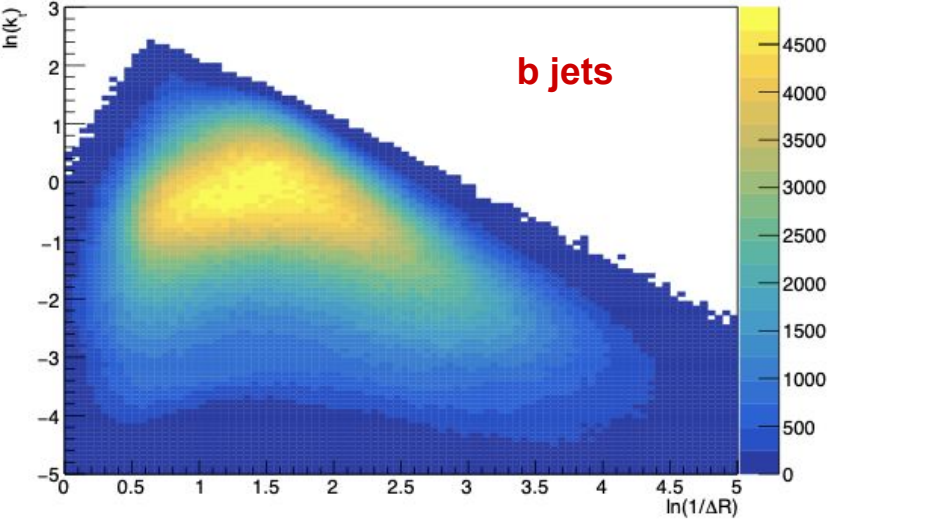
- In order to make progress further, we need recipe to reconstruct truth jets, currently I do not understand how to extract it from current samples

# First look LJP representation for QCD light jets (after event selection)



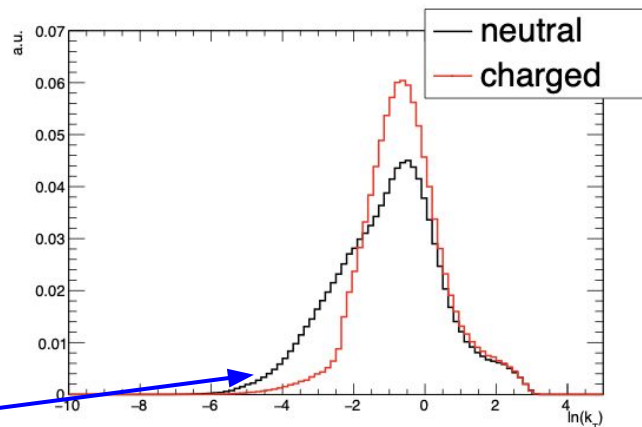
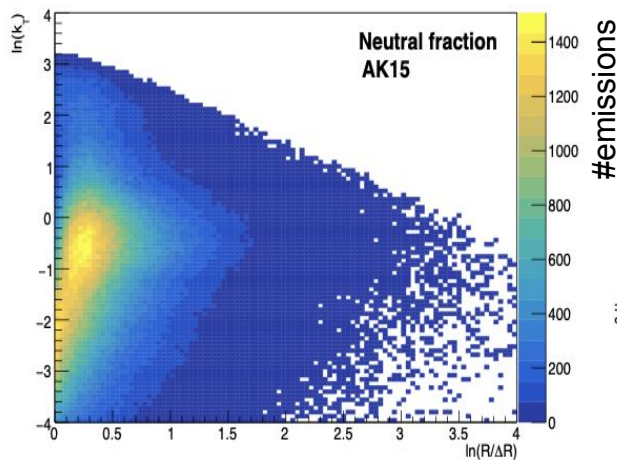
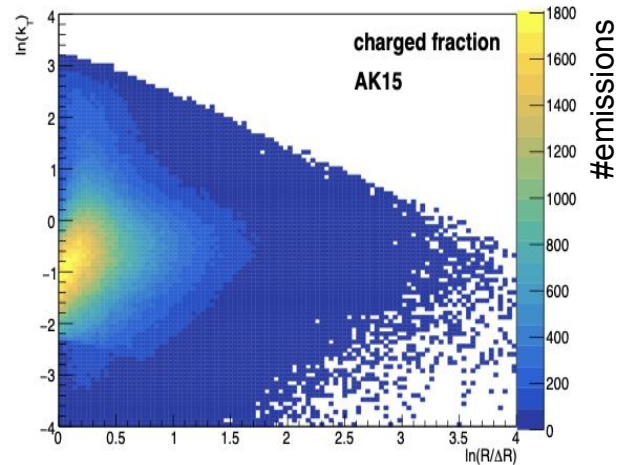
# First look of LJP representation of valencia jets (R=0.5) at FCC-ee

$\ln(k_t)$  vs  $\ln(1/\Delta)$



# LJP for charged and neutral jet fraction (after event selection)

$\ln(k_{\perp})$  vs  $\ln(R/\Delta R)$

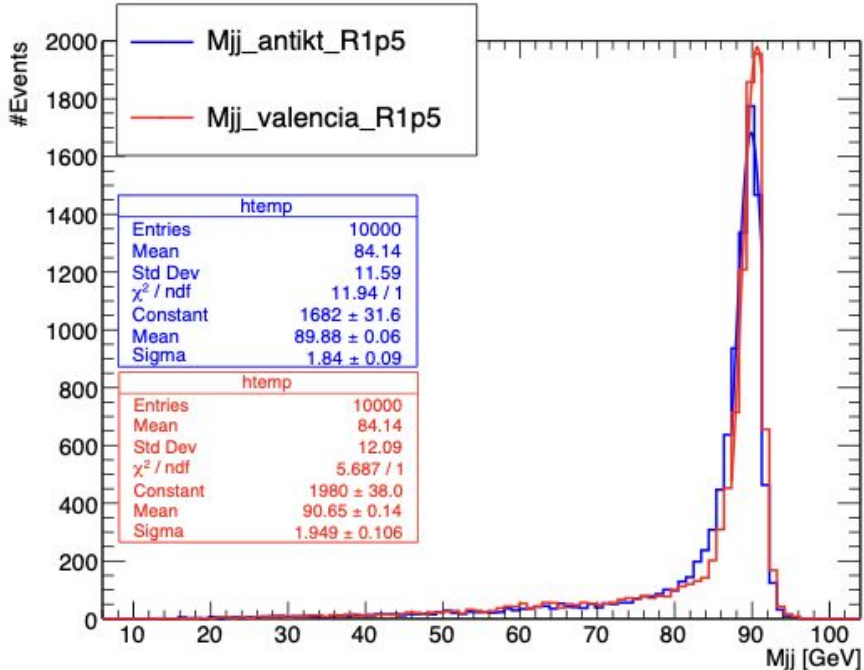


- tail distribution mostly contains neutral fraction
- Hard collinear region doesn't have much difference in both representation



# Valencia vs anti-kt $m_{jj}$ distribution for R=1.5

- Valencia jets has slight better mass resolution for reconstructed  $m_Z$ ; but mass scale is same



# Jet Clustering

Framework: [HEP-FCC/FCCAnalyses](#)

Jet Clustering: (according to examples given [here](#))

- Input collection **ReconstructedParticles**

```
.Define("pseudo_jets", "JetClusteringUtils::set_pseudoJets_xyzm(RP_px, RP_py, RP_pz, RP_m)")
```

- Definitions: clustering\_kt, clustering\_cambridge, clustering\_valencia (with  $\beta=1$ ) ([link](#))

- Configuration settings: (**R=0.5**)

- **exclusive jet clustering:** upto exactly 4 jets

```
.Define("FCCAnalysesJets_valencia", "JetClustering::clustering_valencia(0.5, 2, 4, 0, 10, 1., 1.)(pseudo_jets)")
```

```
.Define("FCCAnalysesJets_kt", "JetClustering::clustering_kt(0.5, 2, 4, 0, 10)(pseudo_jets)")
```

```
.Define("FCCAnalysesJets_cambridge", "JetClustering::clustering_cambridge(0.5, 2, 4, 0, 10)(pseudo_jets)")
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- Configuration settings: (**R=0.5**)

- **exclusive jet clustering:** upto exactly 4 jets

- **inclusive jet clustering:** with 5 GeV pT cut on jets

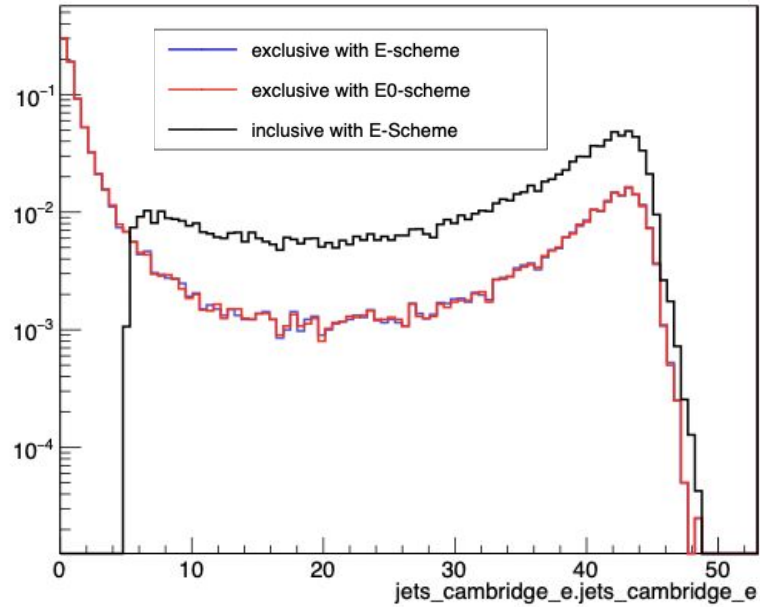
```
.Define("FCCAnalysesJets_valencia", "JetClustering::clustering_valencia(0.5, 0, 5, 0, 0, 1., 1.)(pseudo_jets)")
```

```
.Define("FCCAnalysesJets_kt", "JetClustering::clustering_kt(0.5, 0, 5, 0, 0)(pseudo_jets)")
```

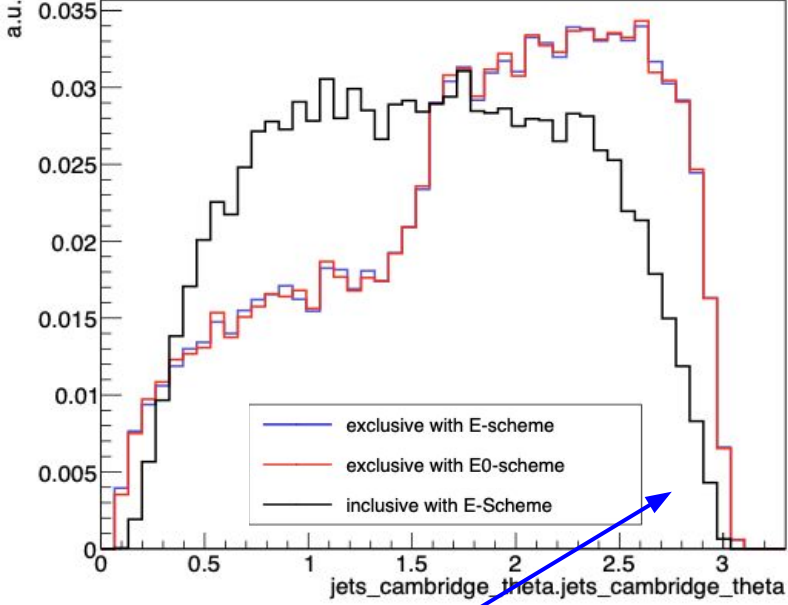
```
.Define("FCCAnalysesJets_cambridge", "JetClustering::clustering_cambridge(0.5, 0, 5, 0, 0)(pseudo_jets)")
```

# Cambridge Jet Kinematic distributions

Jet E

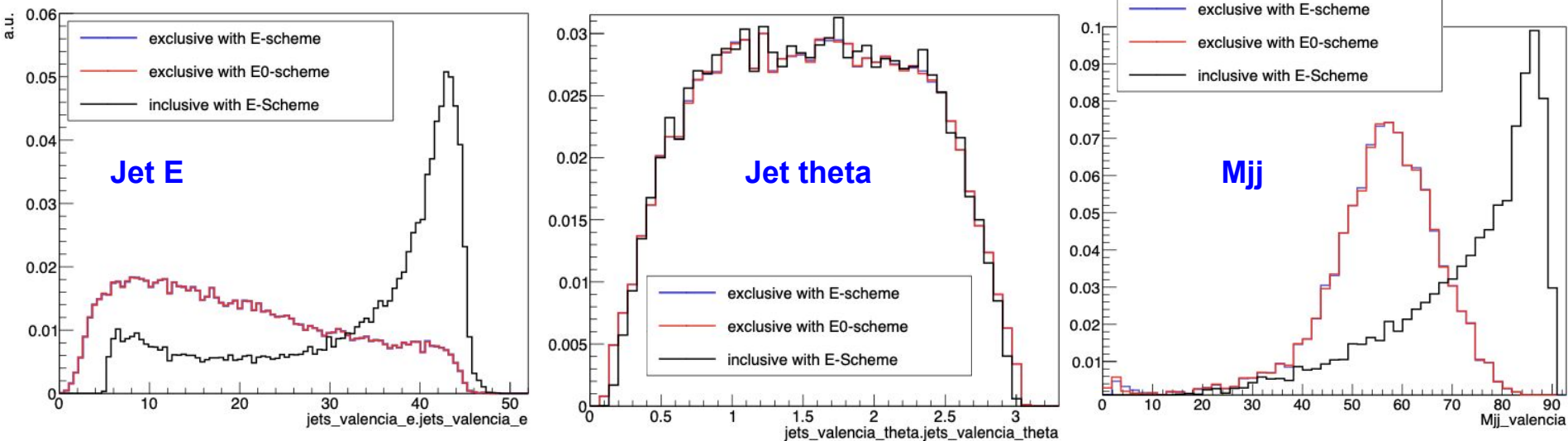


Jet theta



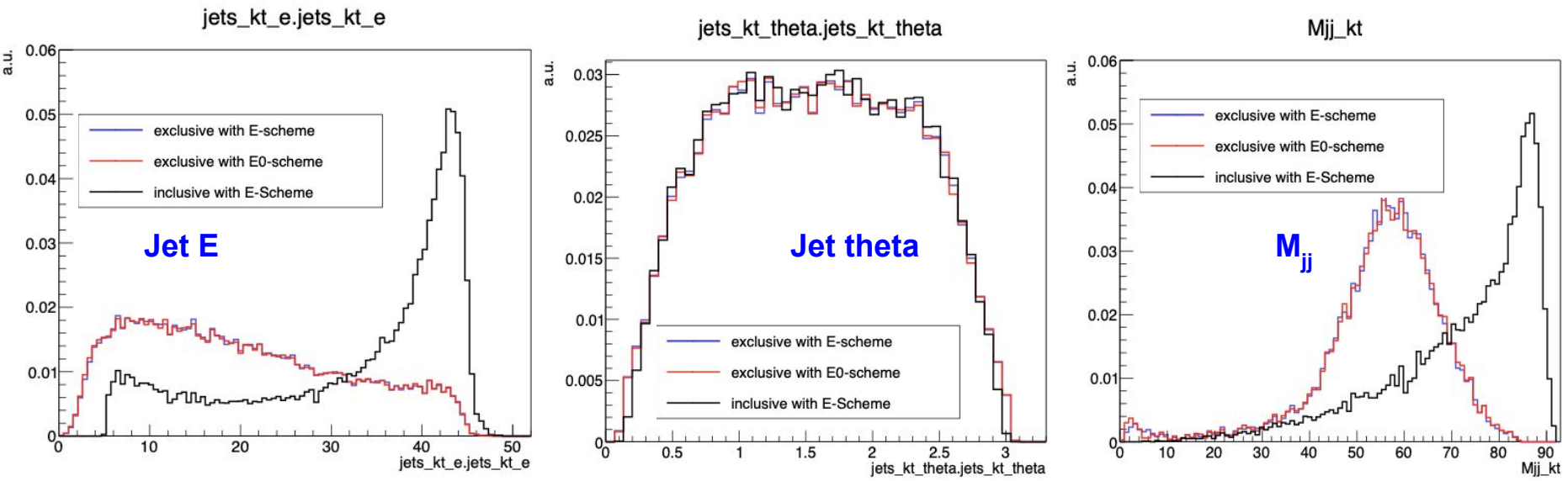
- With 5 GeV p<sub>T</sub> cut in inclusive clustering, jet theta distribution give symmetric distribution. But, in exclusive clustering, theta distribution becomes asymmetric ⇒ clustering uses Δθ so the difference of p<sub>T</sub> cut used in inclusive clustering does not explain this ⇒ points to some bug?
  - Inclusive clustering looks more reasonable. Checks with valencia algorithm is on next slide.

# Valencia Jet Kinematic distributions



- Exclusive and inclusive clustering completely changes the valencia jet kinematics
  - **Jet energy:** peaks ~45 GeV for lights jets coming from Z-decay for inclusive; exclusive clustering loses the correlations with hard particles
  - **Jet theta:** looks more and less similar for inclusive and exclusive clusterings
  - **M<sub>jj</sub>:** for inclusive, it peaks close to Z-mass, but, for exclusive this is not a case

# $k_t$ -Jet Kinematic distributions

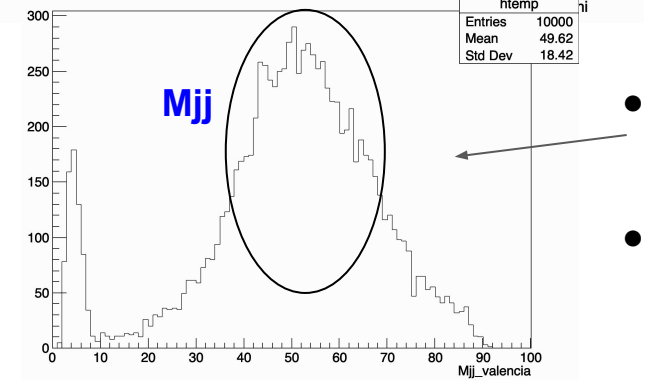
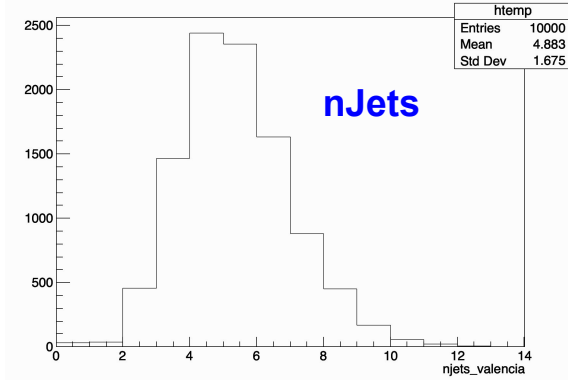
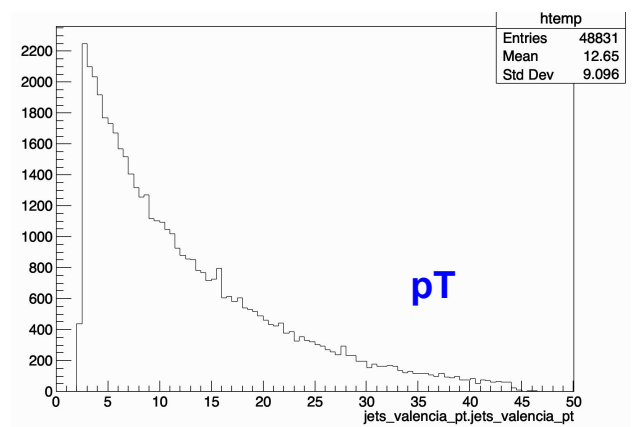
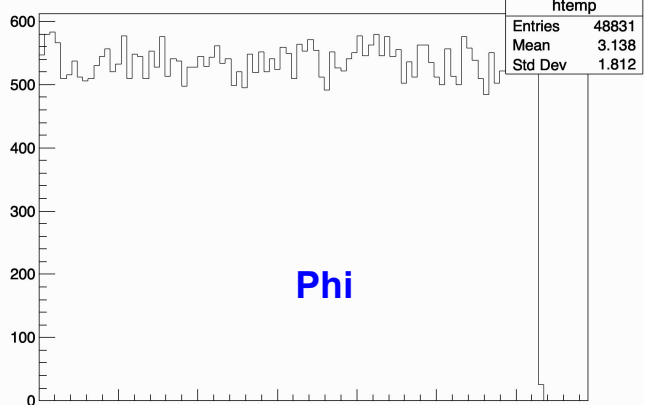
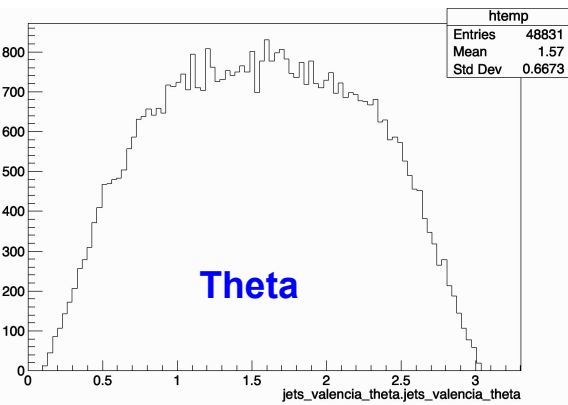


- $k_t$ -clustering also shows same behaviour with inclusive and exclusive clustering
- The kinematics is very similar to valencia jets

# Other checks for exclusive clustering

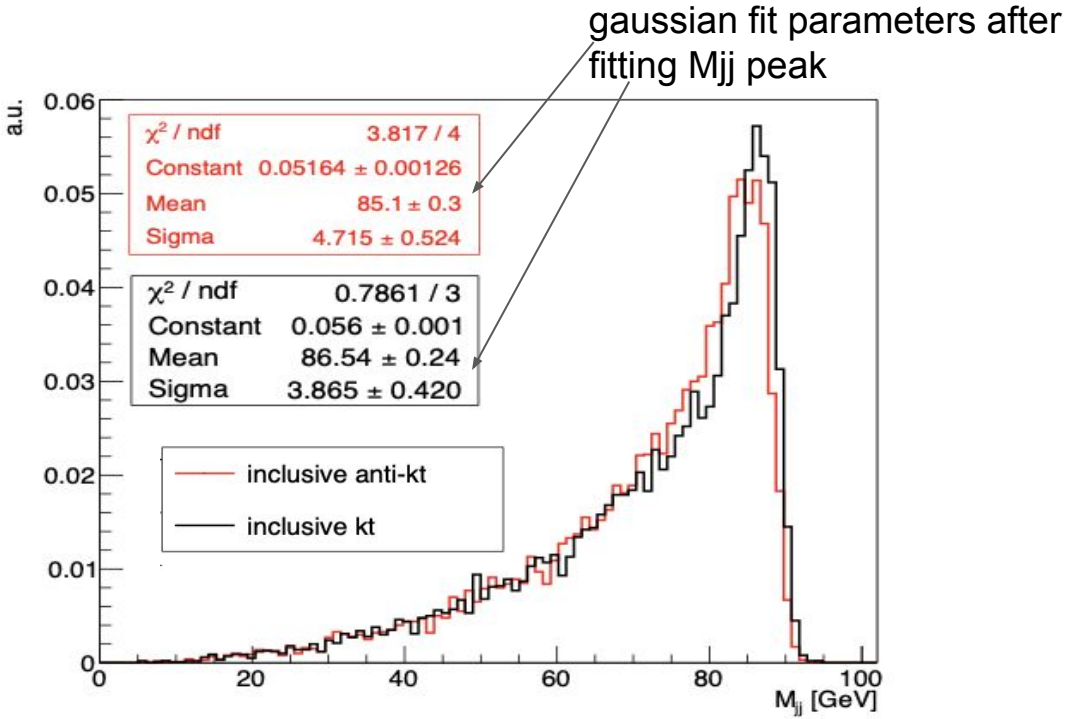
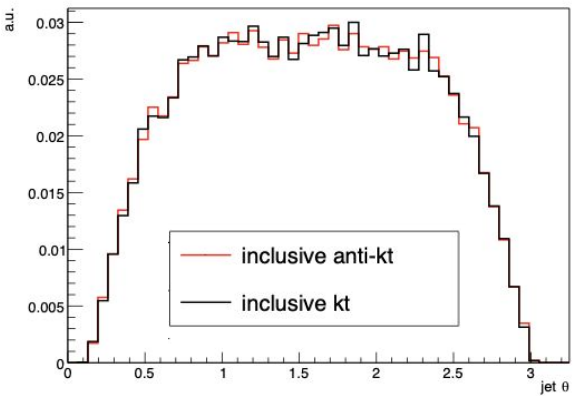
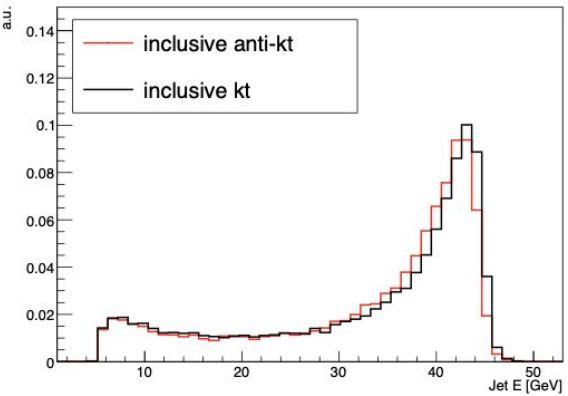
- Tried with one more exclusive configuration for valencia jets where there is selection on dcut (instead of njets)

```
.Define("FCCAnalysesJets_valencia", "JetClustering::clustering_valencia(0.5, 1, 6, 0, 0, 1., 1.)(pseudo_jets)")
```



- Here also Mjj peaks around 50 GeV for jets coming from Z-decay
- Exclusive clustering does not allow to reproduce Z-mass well

# $k_t$ vs anti- $k_t$ Jet Kinematic with inclusive clustering

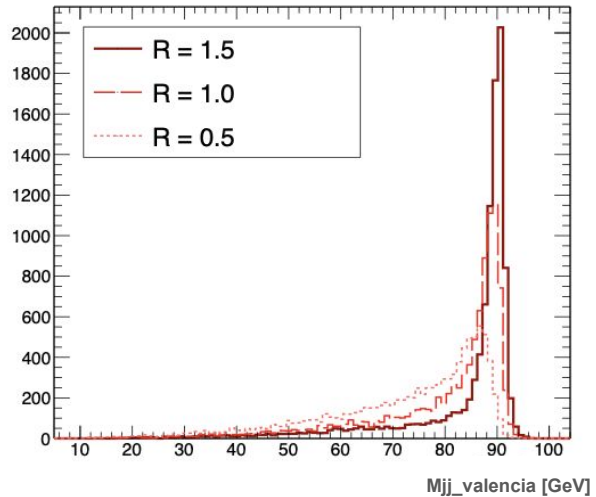
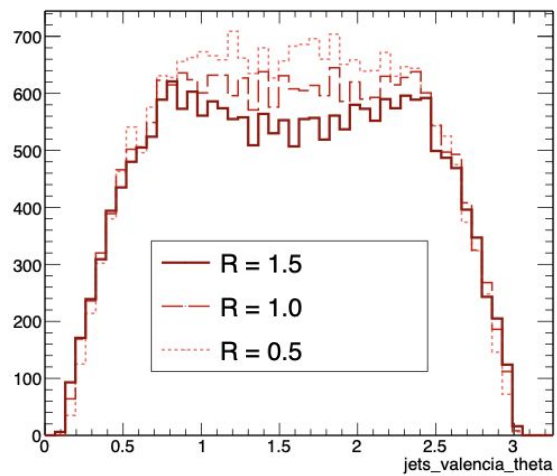
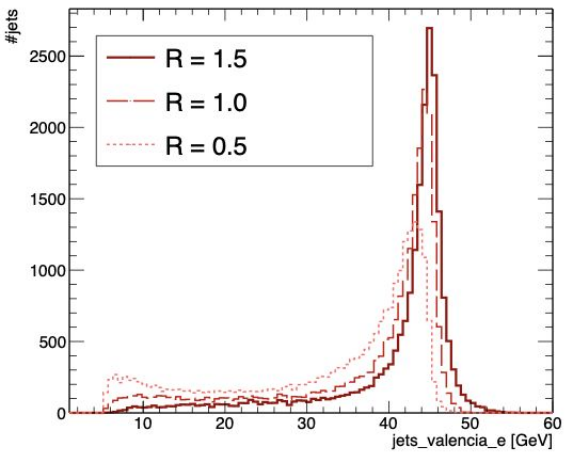


$k_t$  and anti- $k_t$  algorithms give a slight difference in jet kinematics which could be sensitive to choice of jet size. (this needs to be studied with jet sizes)

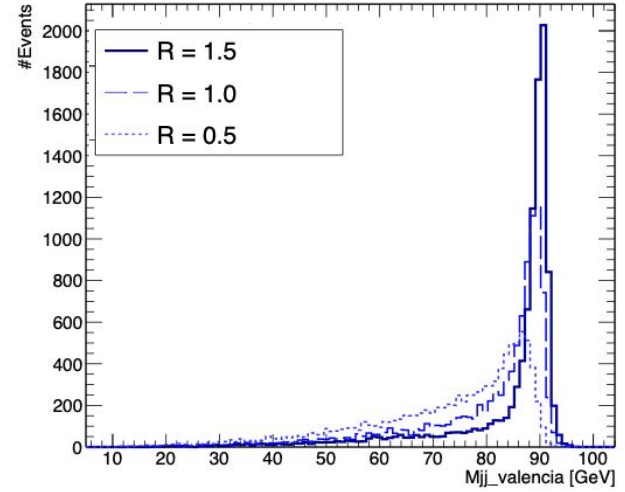
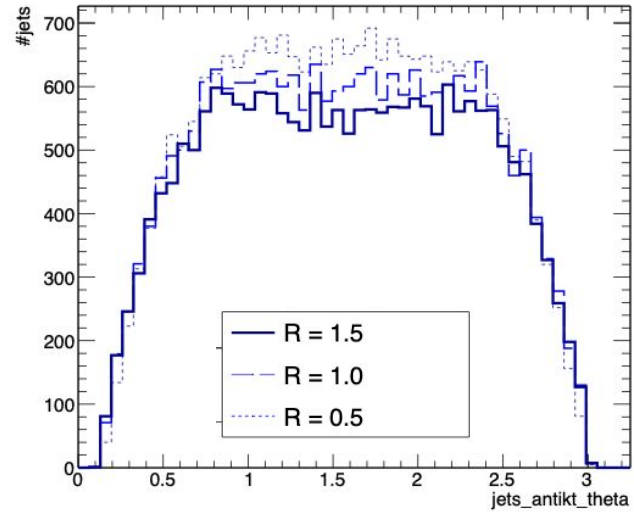
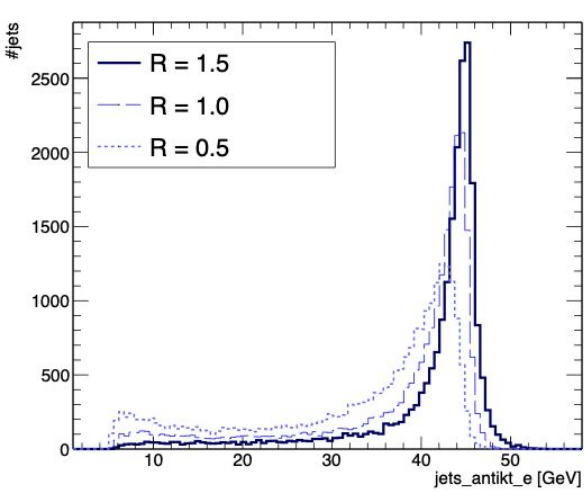
Note: Fastjet doesn't allow anti-kt algorithm with exclusive clustering



# Inclusive Valencia Jet Kinematic distributions for different R



# Inclusive anti- $k_T$ Jet Kinematic distributions for different R



# Ideas for next steps:

Binning of LJP variables ( $k_T$ ,  $\Delta R$ )

$$\ln(k_T) = [-3, -2, -1, 0, 1]$$

$$\ln(R/\Delta R) = [0, 1, 2, 3]$$

$$p_T \text{ binning} = [10, 25, 35, 40, 45]$$



Total 64 bins

⇒ LJP 2D distribution in every  $p_T$  bins at reco level

## Ideas for next steps:

- Try to create similar unfolding input as we have in ATLAS to run unfolding in one go, but.....

KEY: TH1D    h1\_incl\_unfolding\_tjet\_kt\_DeltaR\_pt\_nominal;1

KEY: TH2F    h2\_incl\_unfolding\_resp\_kt\_DeltaR\_pt\_nominal;1

KEY: TH1F    h1\_incl\_unfolding\_rjet\_kt\_DeltaR\_pt\_nominal;1

- I do not see any recipe for truth jets from Delphes, it is not available in delphes samples also
- I only have mapping between truth and reco level particles
  - Make 2D LJP distributions for reco in every pT bin
  - Map truth particle with reco particle and fill truth level 2D map in reco pT bin