



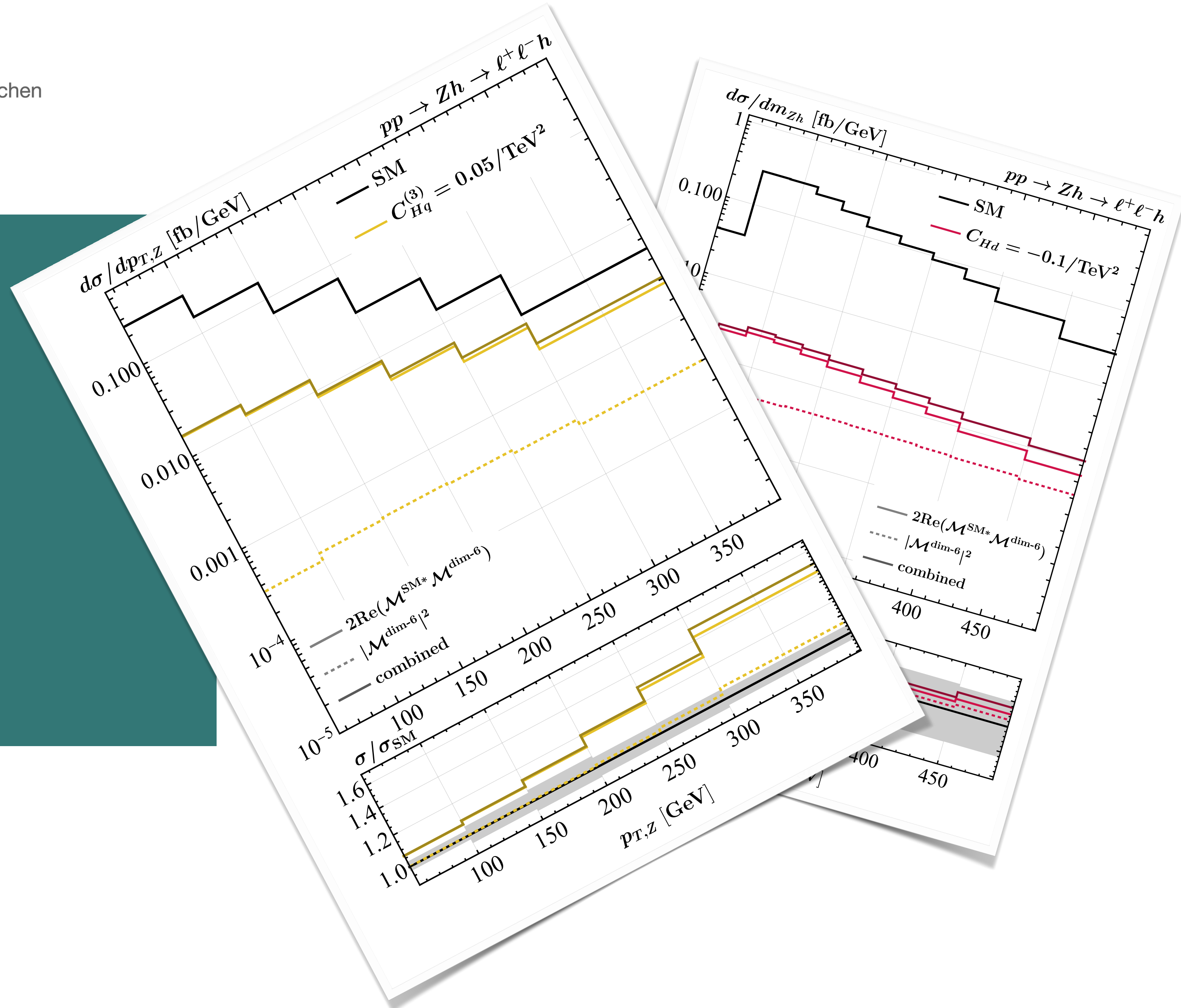
SFB 1258 | Neutrinos
Dark Matter
Messengers



TUM
Technische Universität München

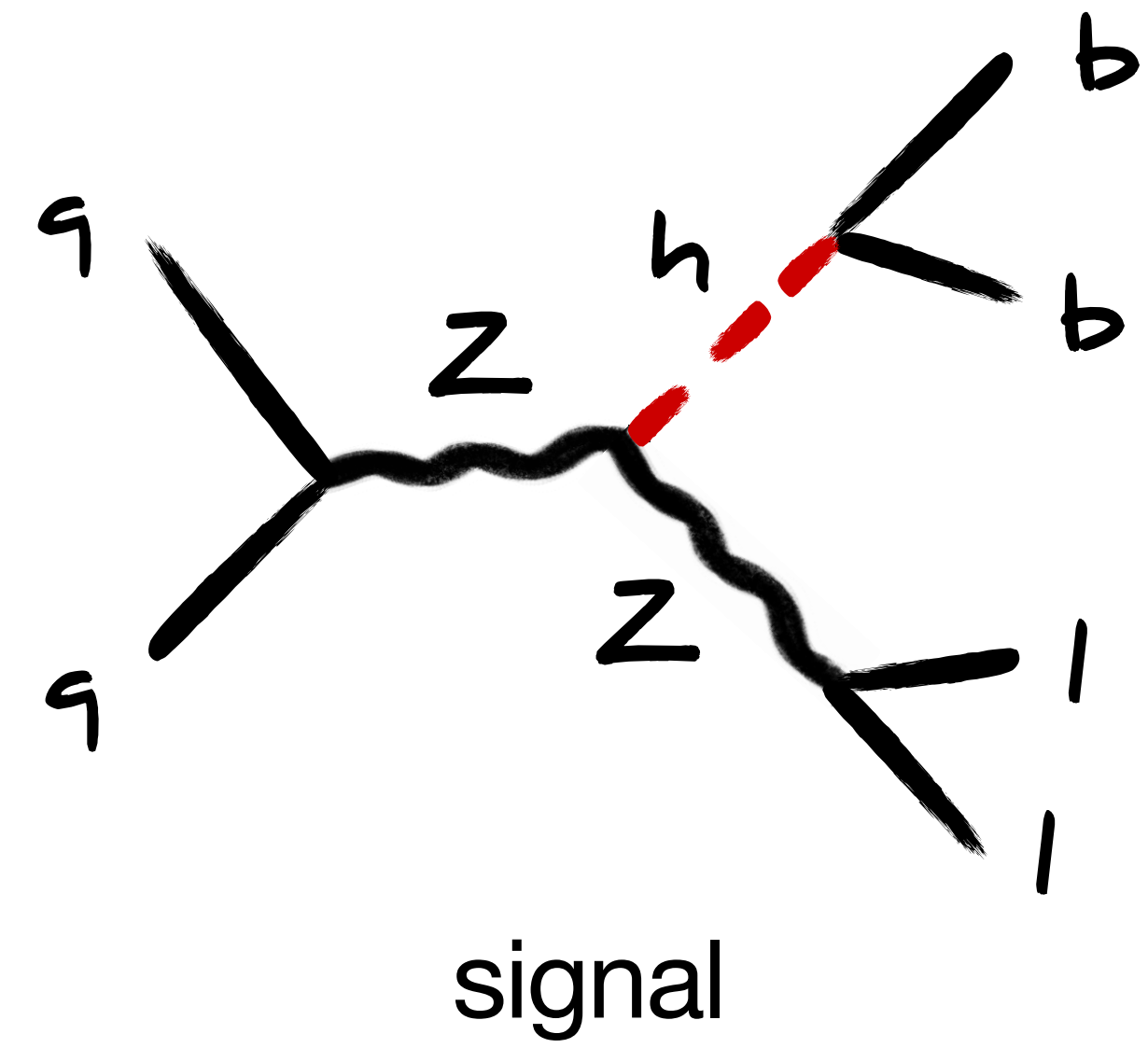
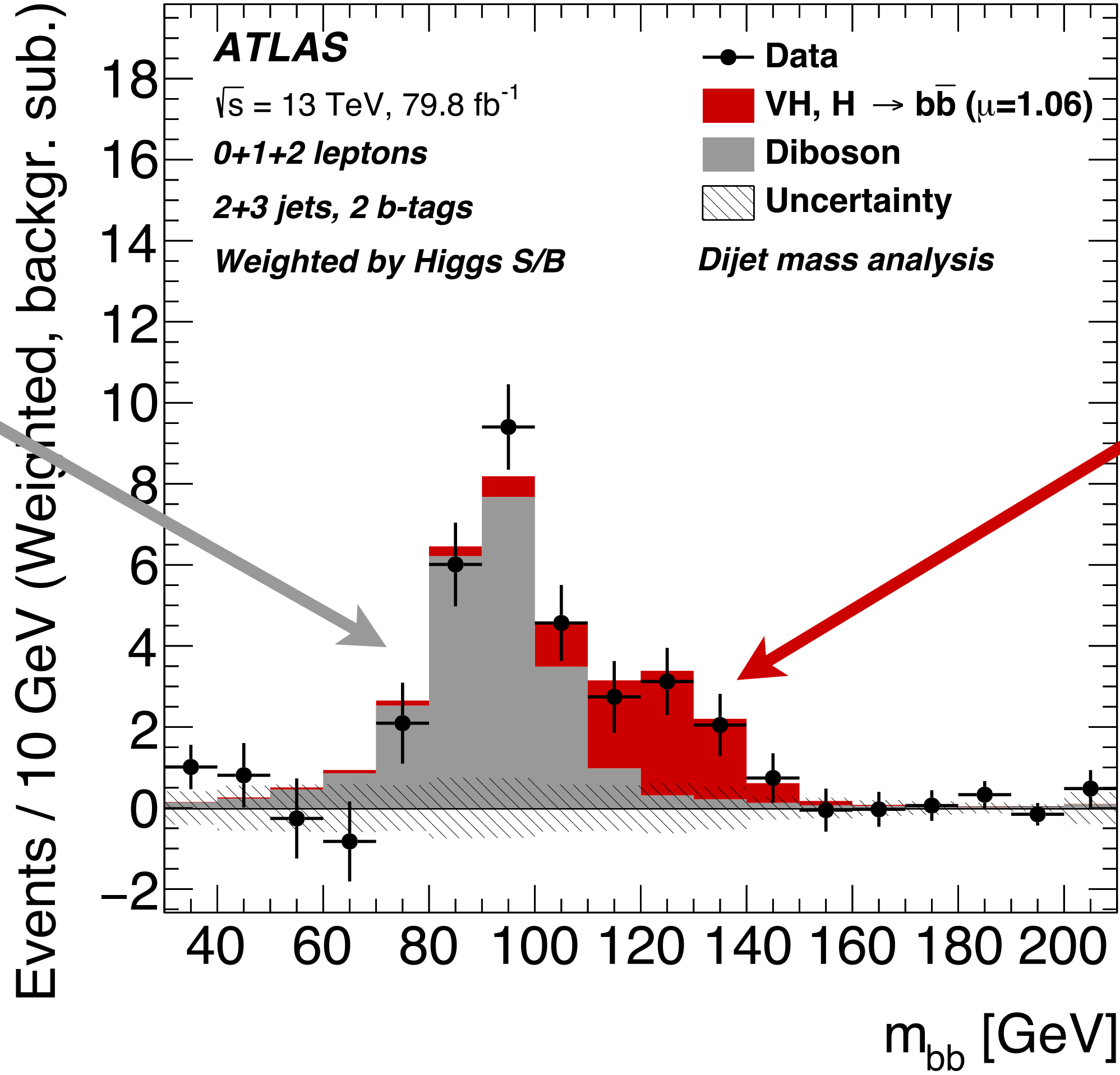
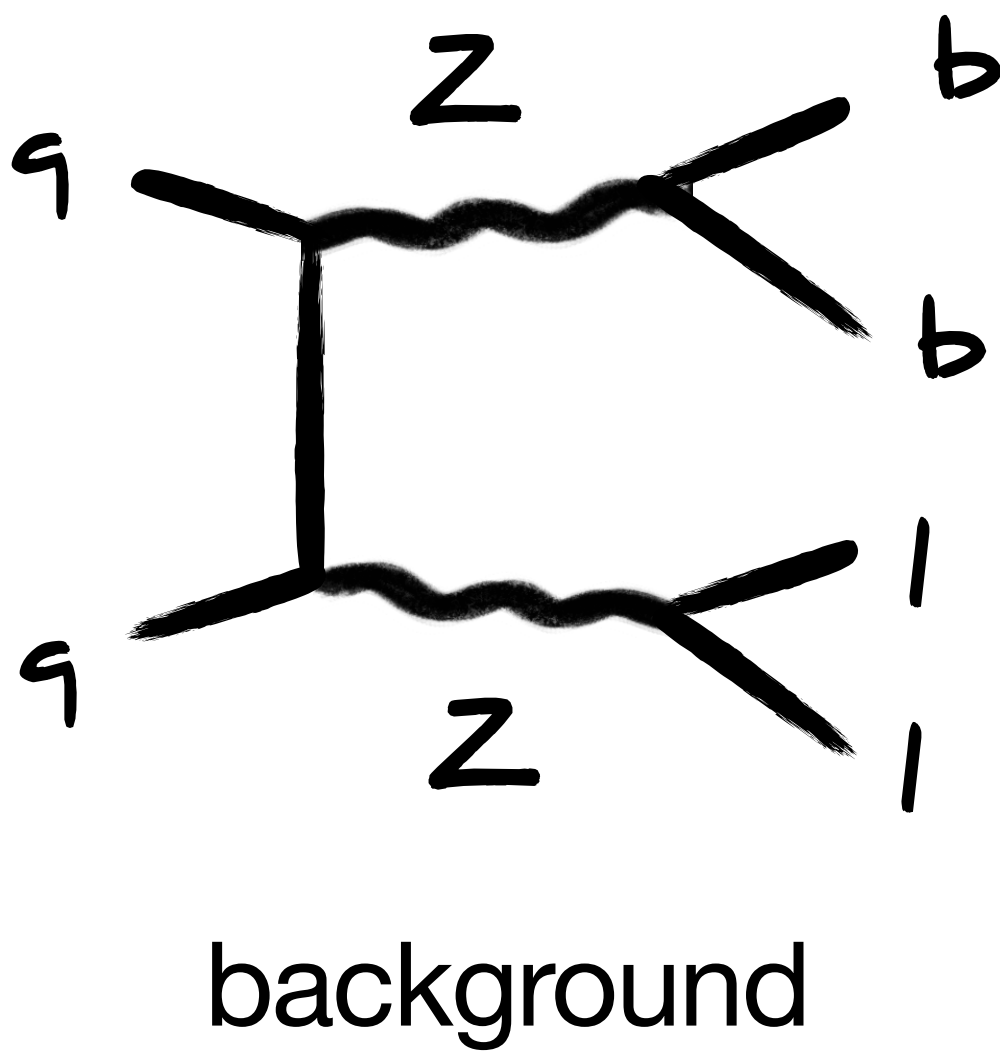
SMEFT at NNLO+PS: *Vh* production

Luc Schnell
EFT in Multiboson Production
June 10, 2024



Observation of $h \rightarrow b\bar{b}$ @ LHC Run II

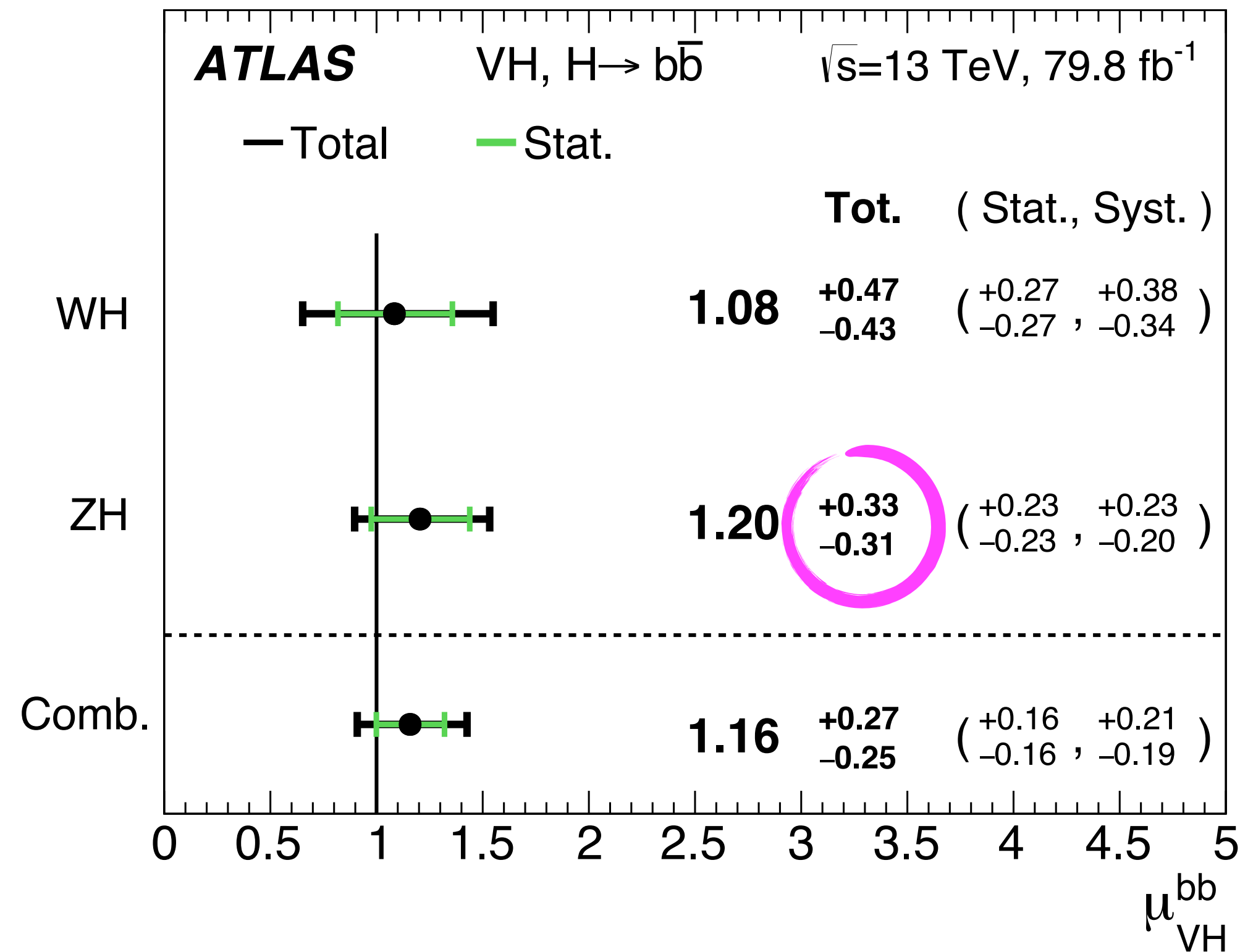
[ATLAS, 1808.08238]



[see also CMS, 1808.08242]

From 5σ to precision measurements

[ATLAS, 1808.08238]

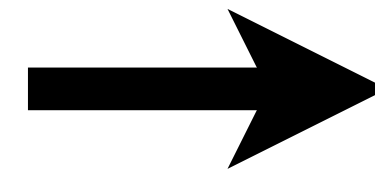
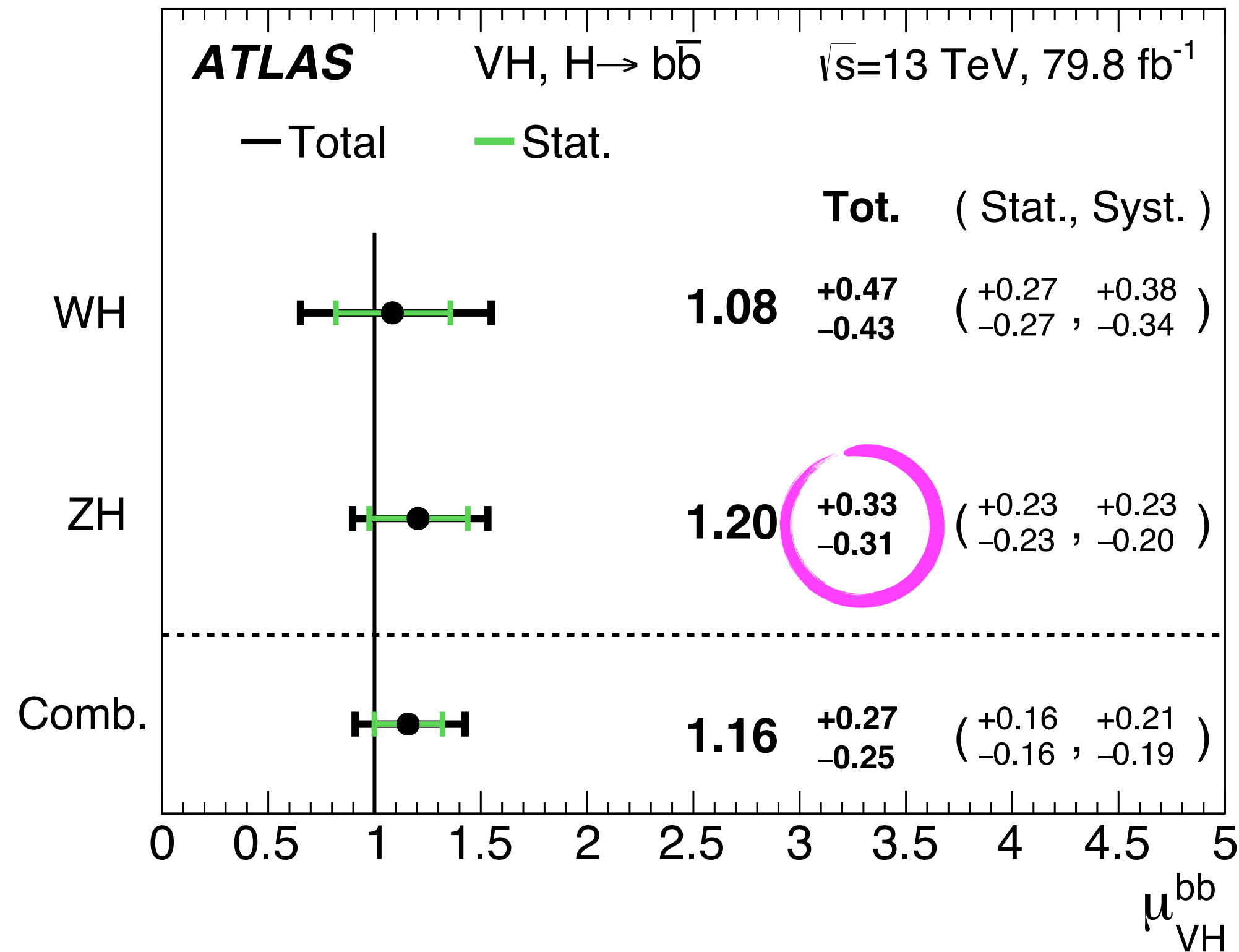


In LHC Run II, signal strength in Vh production found to be SM-like within 25%

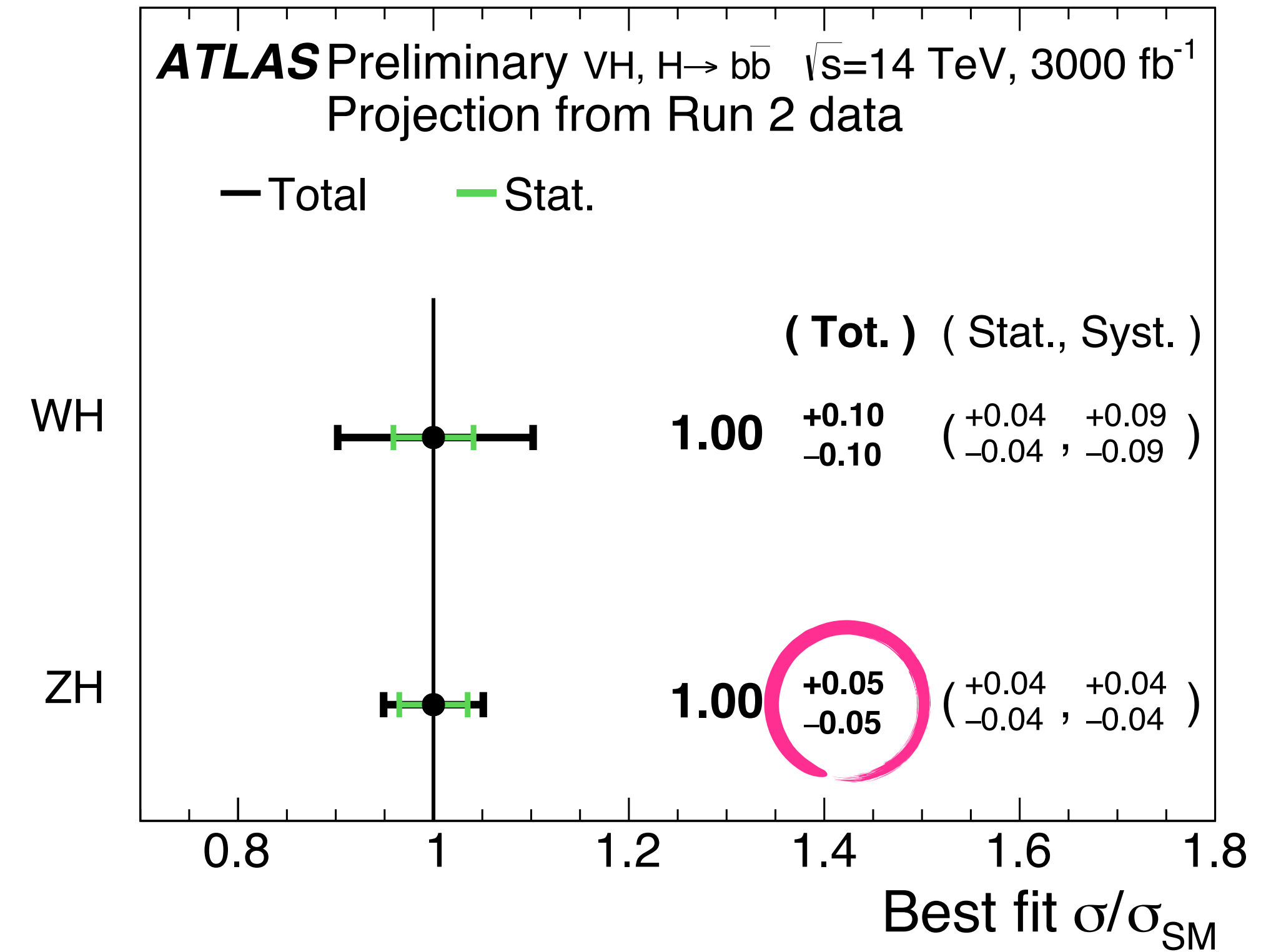
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[ATLAS, 1808.08238]



[ATL-PHYS-PUB-2018-054]

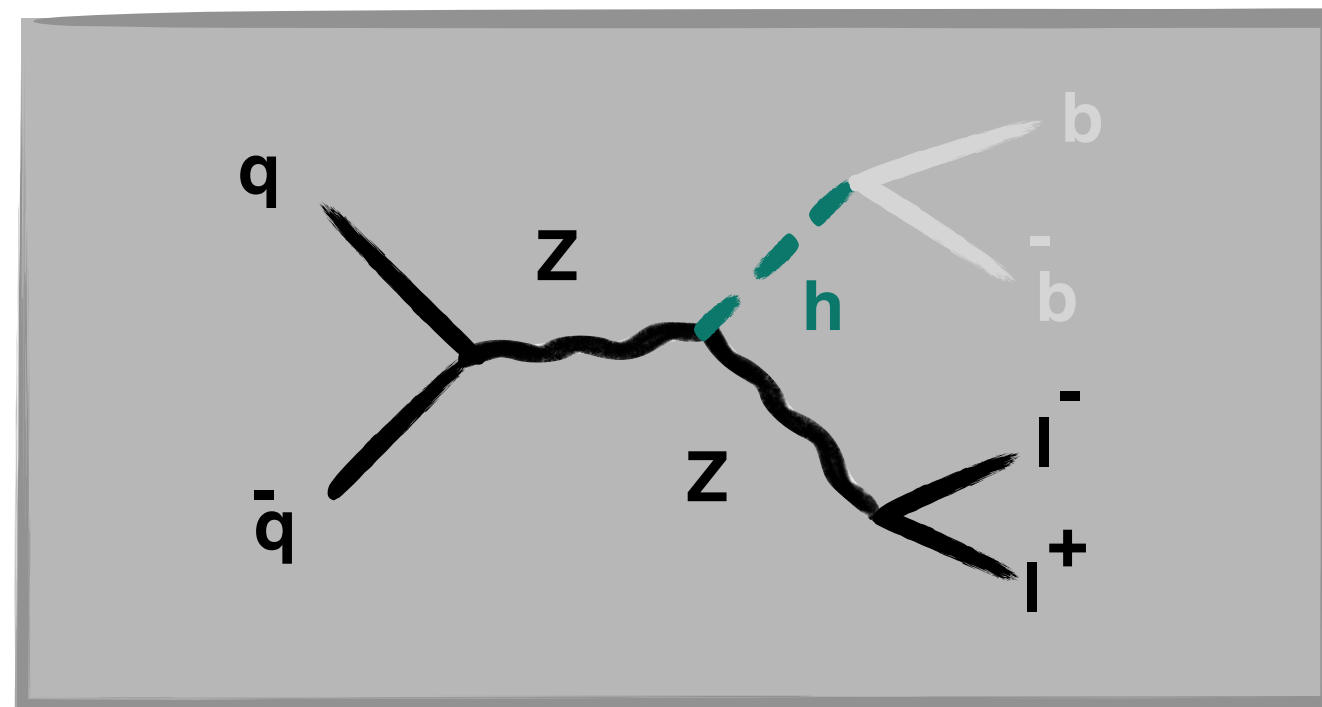


Ultimate accuracy projected to be 10% to 5% in Wh & Zh channel @ HL-LHC

[see also CMS, 1808.08242; CMS-PAS-FTR-18-011]

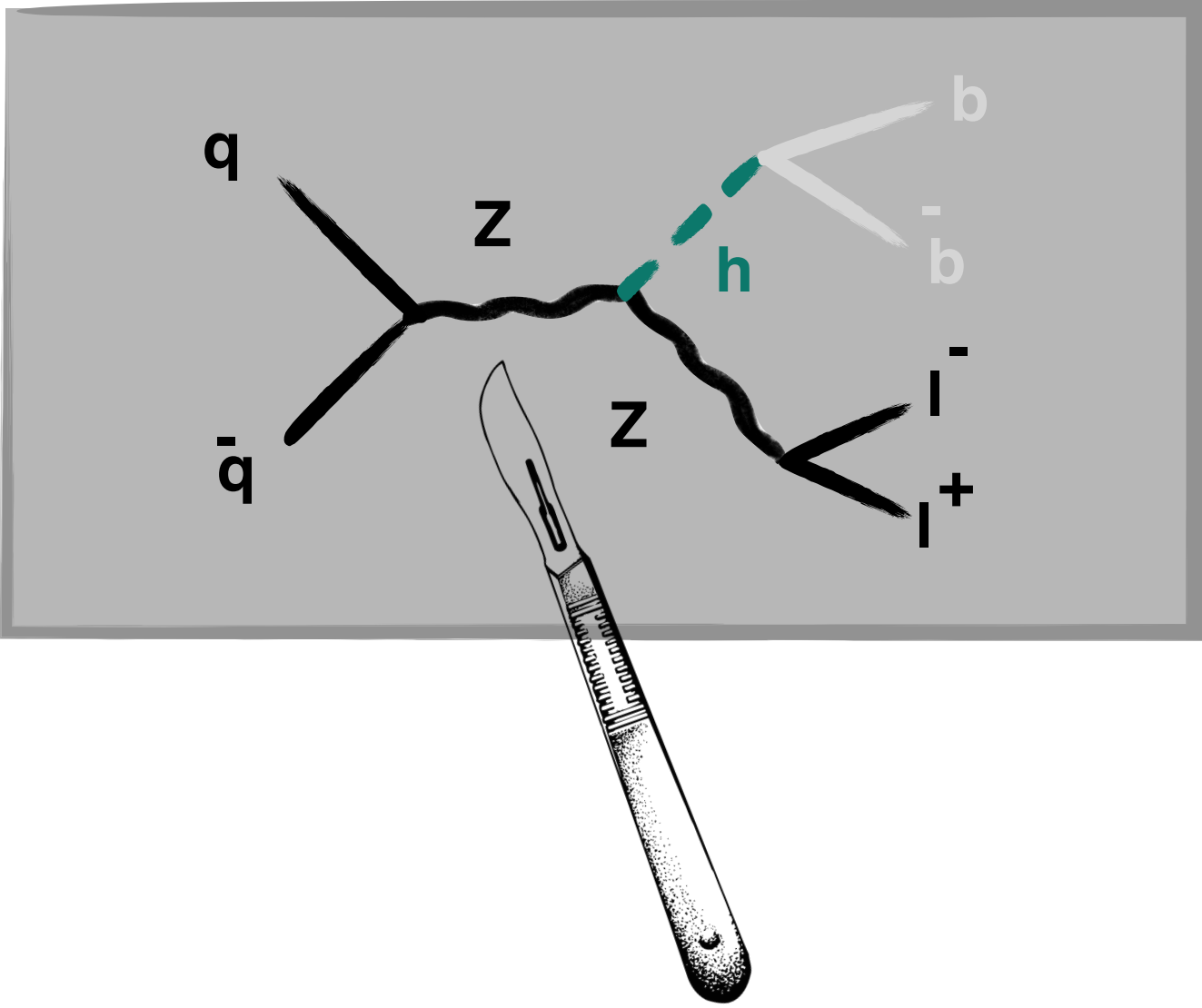
2. Anatomy of SMEFT Effects

2.1 Deviations from the SM



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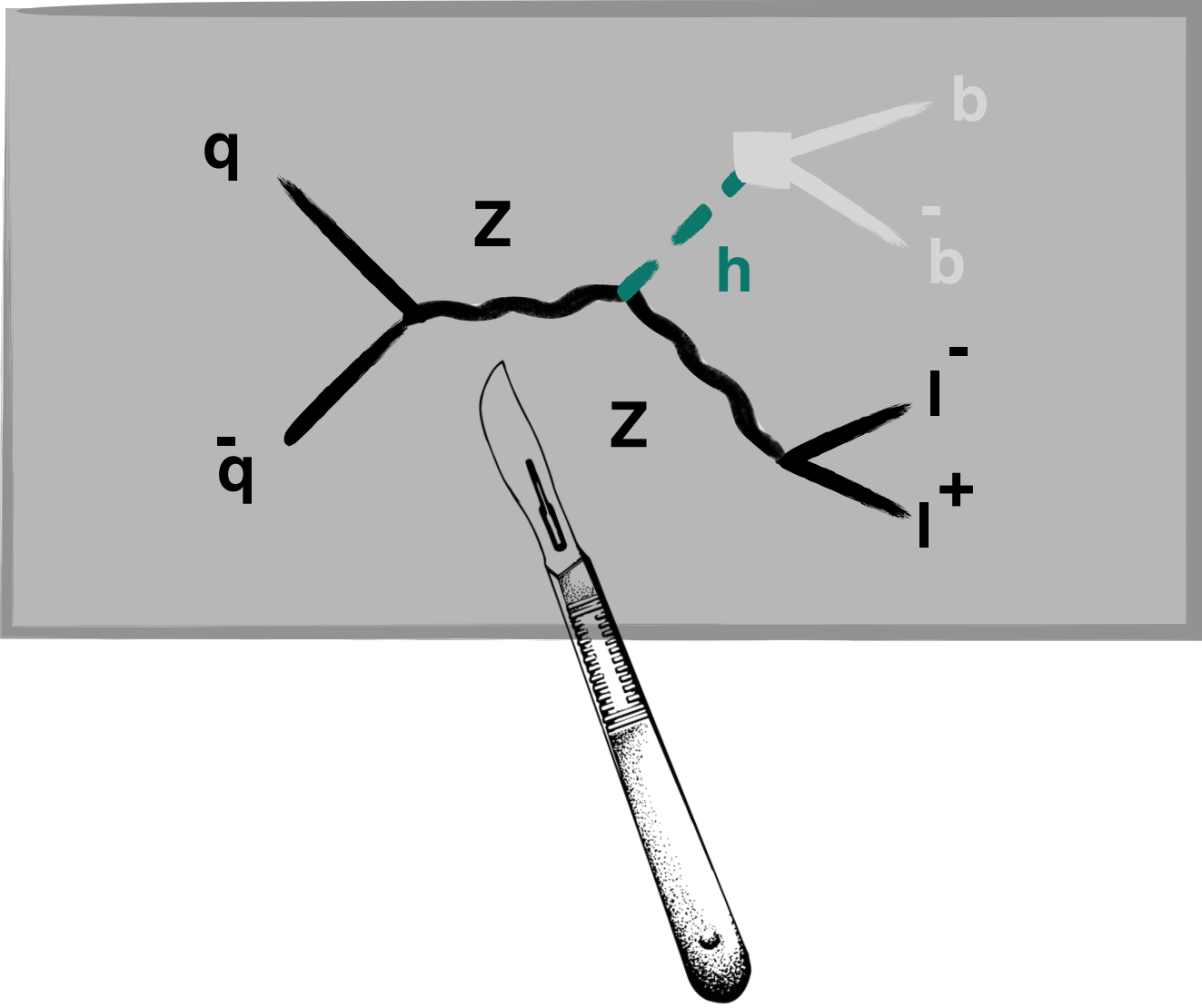
2.1 Deviations from the SM

QCD, Higgs operators: [\[2204.00663\]](#) (U. Haisch, D.J. Scott, M. Wiesemann, *et al.*)

$$Q_{bH} = y_b (H^\dagger H) \bar{q}_L b_R H,$$

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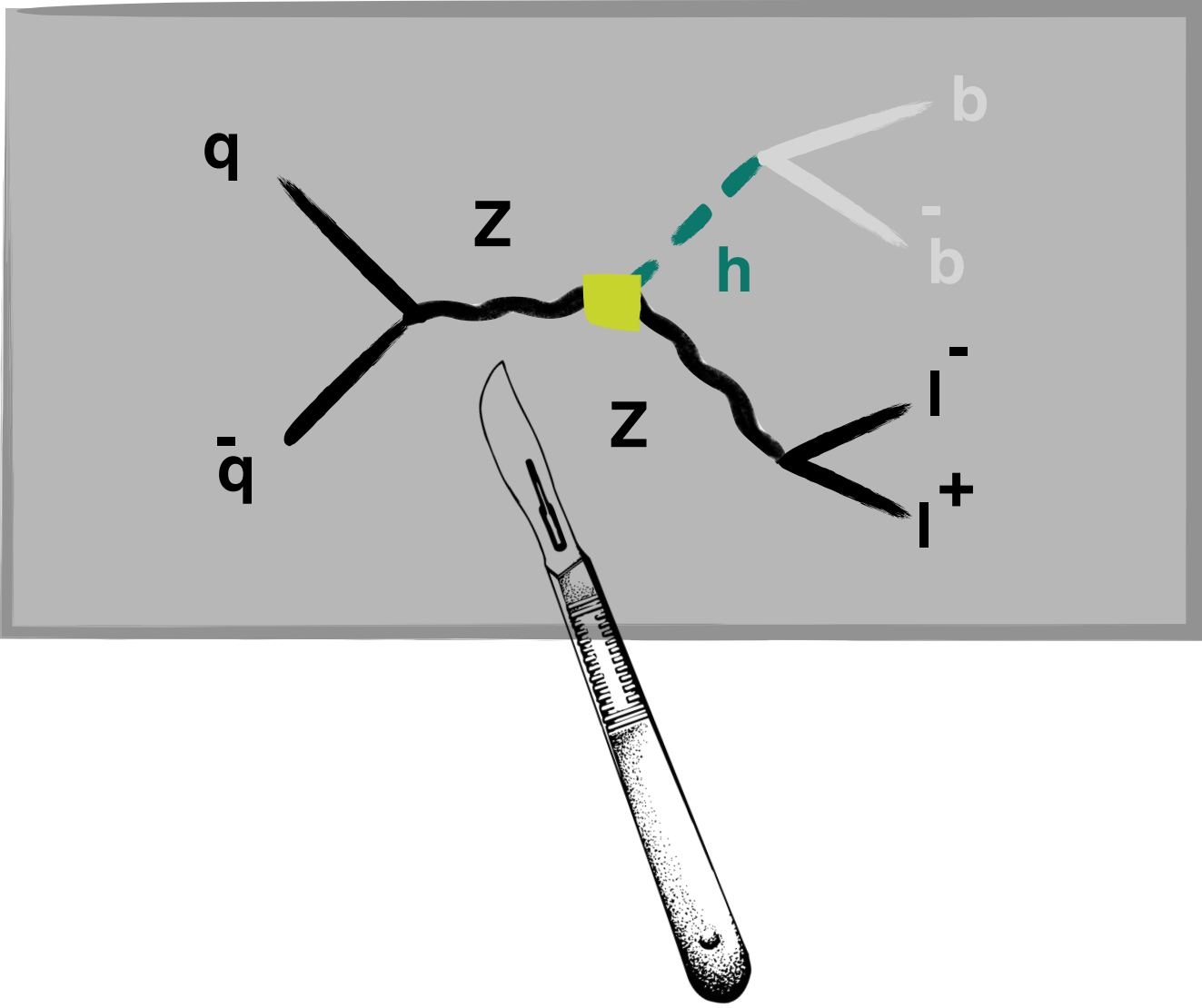
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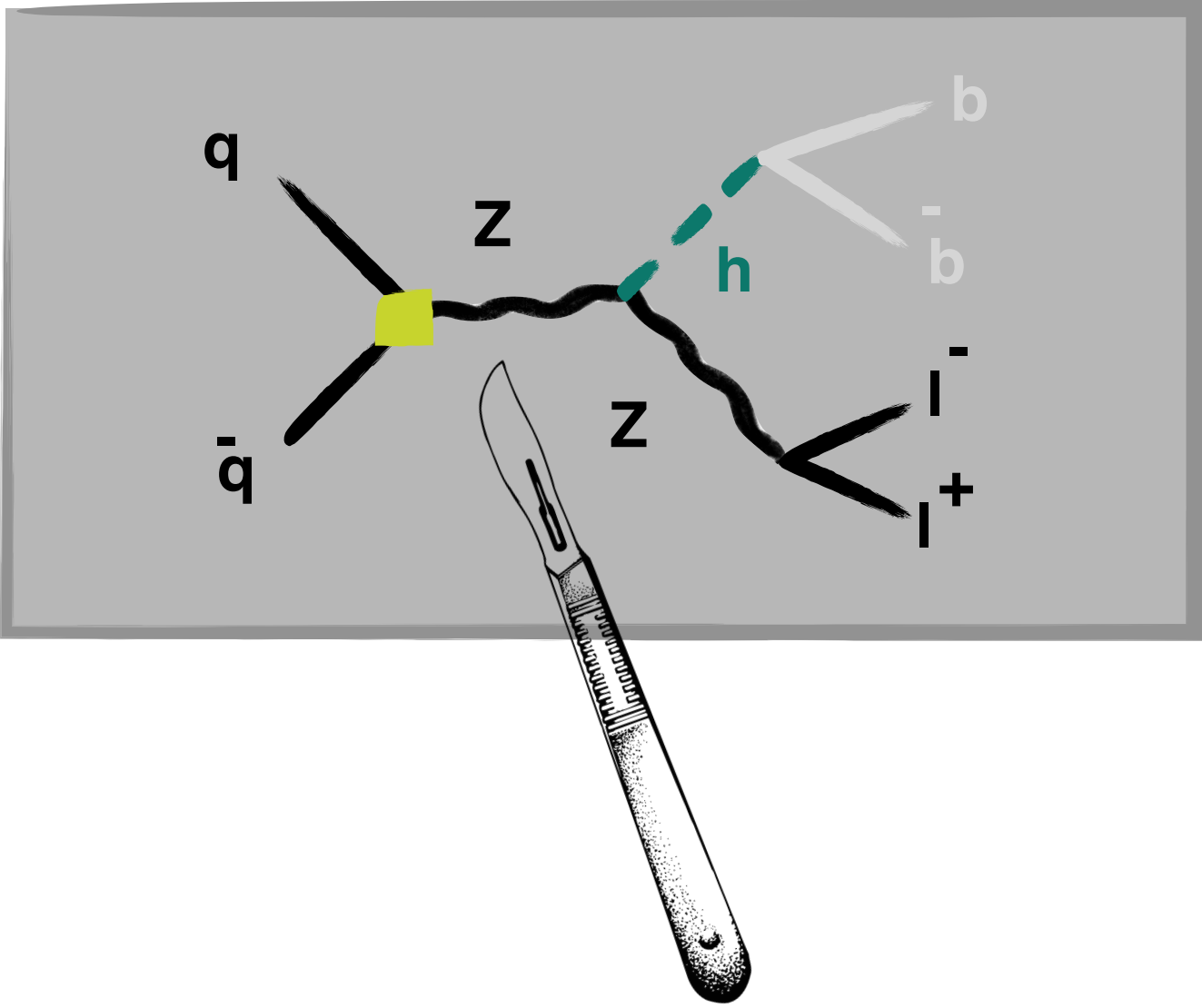
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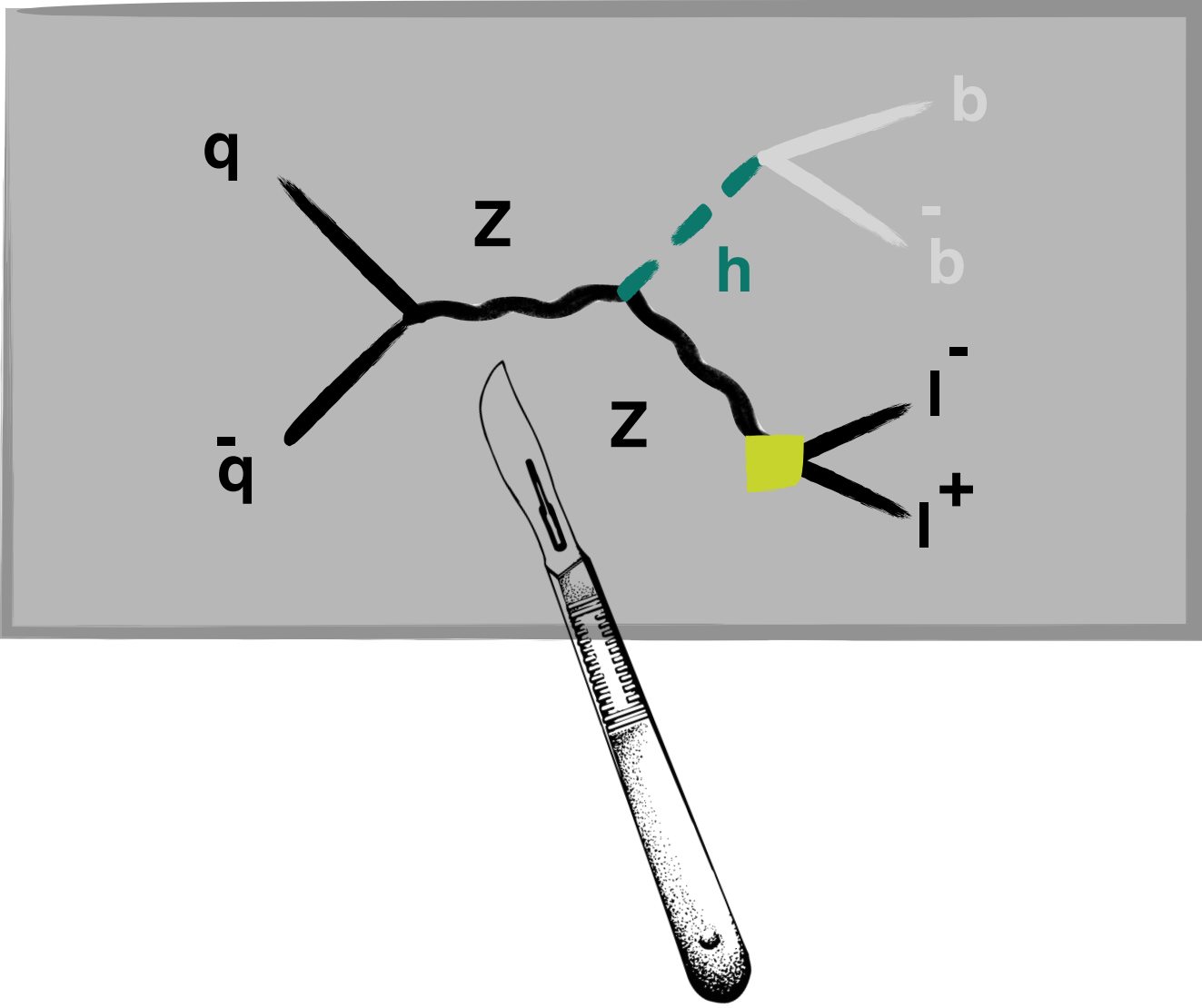
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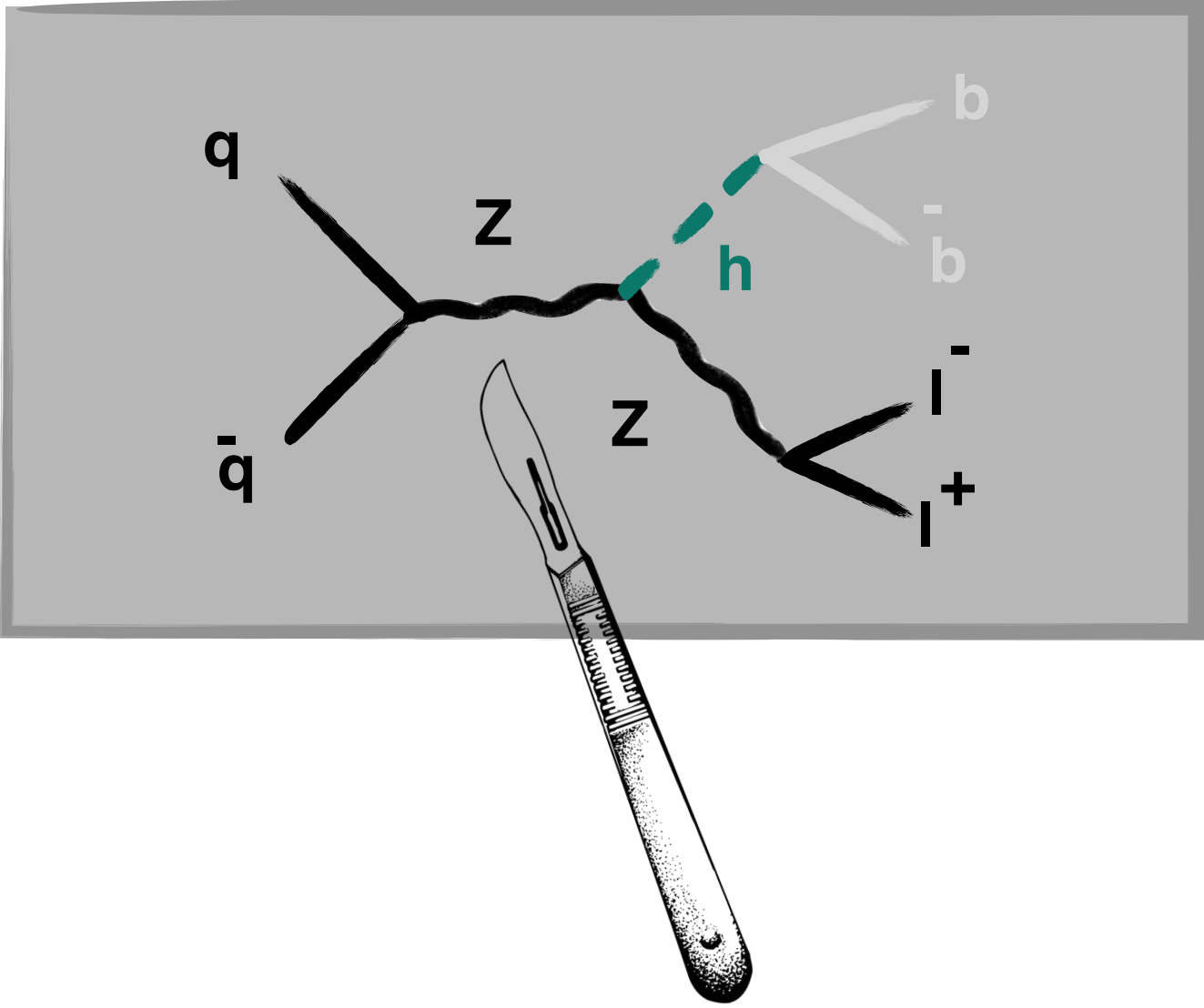
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Input scheme corrections: [\[2311.06107\]](#) (R. Gauld, U. Haisch, LS)

$$Q_{H\Box} = (H^\dagger H) \Box (H^\dagger H), \quad Q_{HD}, \quad Q_{ll}$$



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[ATLAS-CONF-2021-053](#) (ATLAS)
[CMS-PAS-HIG-19-005](#) (CMS)

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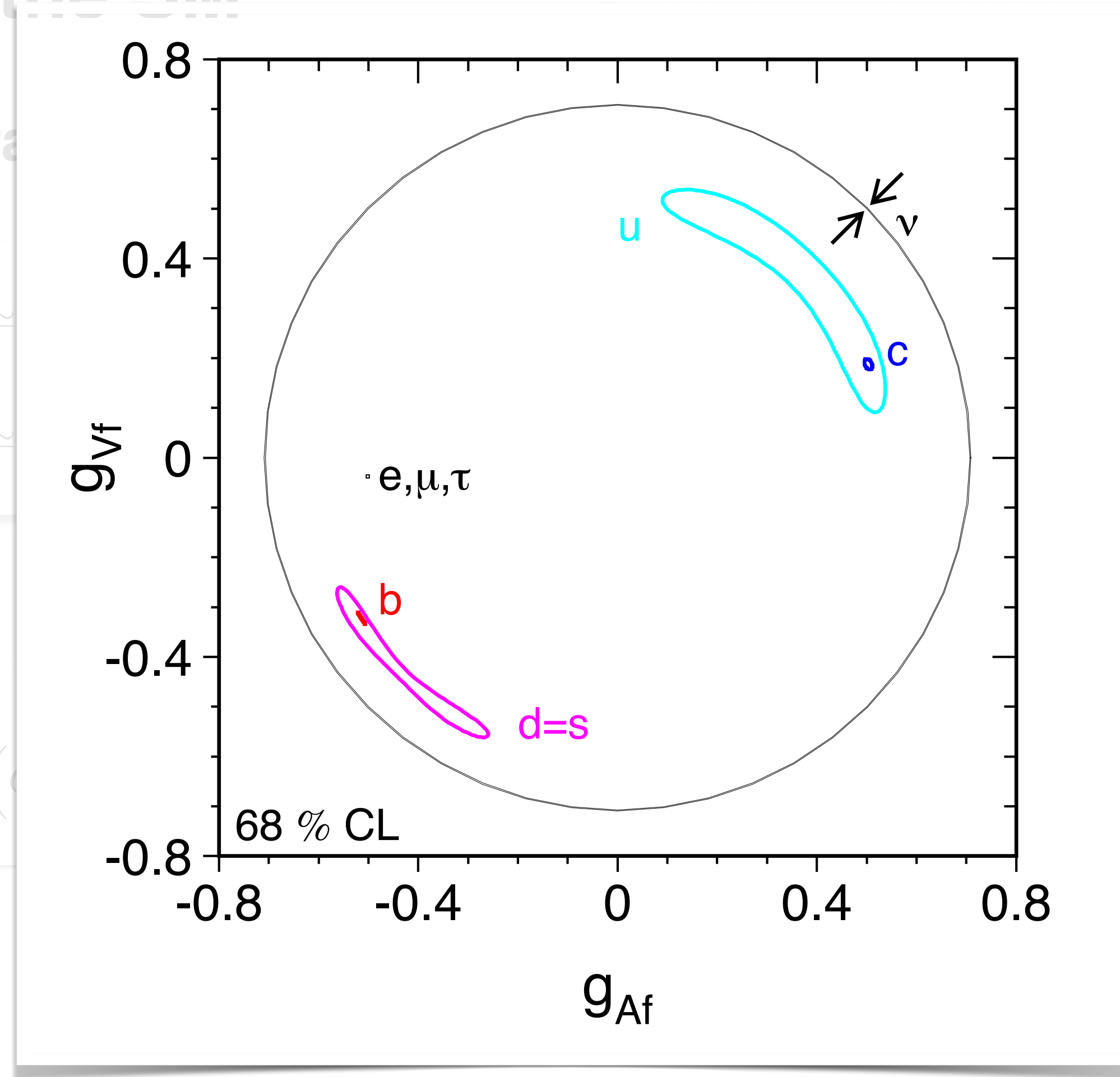
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S-HIG-19-005 (CMS)

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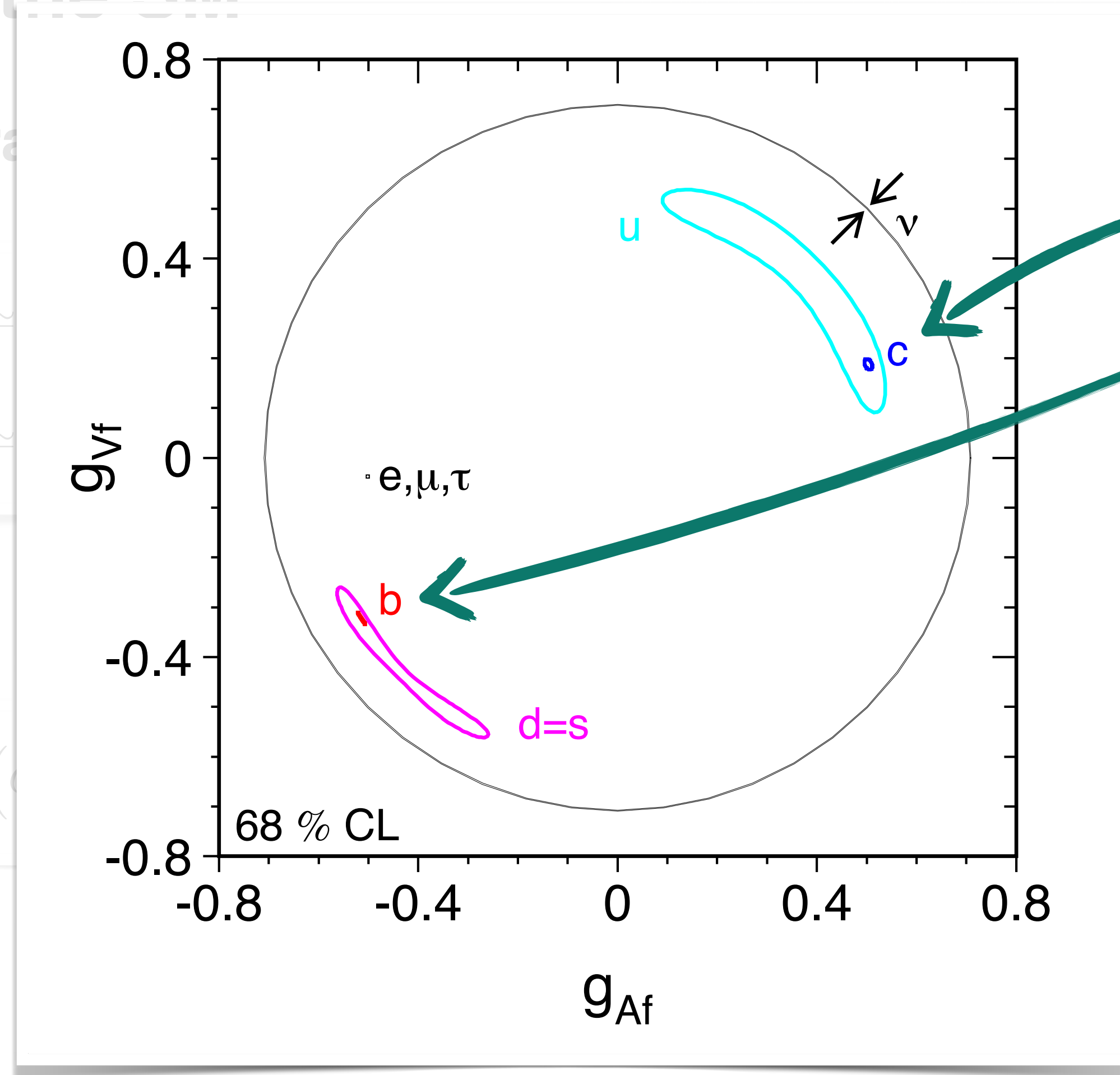
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Better constraints from **forward-backward** asymmetry measurements.

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CONF-2021-053 (ATLAS)
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$$\delta g_L^\psi = \frac{g_2}{c_w} \frac{v^2}{\Lambda^2} \left[g_{T_\psi^3} T_\psi^3 - g_{Q_\psi} Q_\psi - \frac{1}{2} \left(C_{H\psi_L}^{(1)} - 2T_\psi^3 C_{H\psi_L}^{(3)} \right) \right],$$

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$$\delta g_L^u \in [0.2, 6.8] \cdot 10^{-2},$$

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[hep-ex/0509008](#) (SLD et al.)

V(h)ll:

$$C_{Hl}^{(1)}, C_{Hl}^{(3)}, C_{He}$$

2. Anatomy of SMEFT Effects

2.1 Deviations from the SM

What are the **current constraints**?

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LHC:

$$\mu_{\text{ggF}}^{\gamma\gamma} = 1.05 \pm 0.09,$$

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[ATLAS-CONF-2021-053](#) (ATLAS)
[CMS-PAS-HIG-19-005](#) (CMS)

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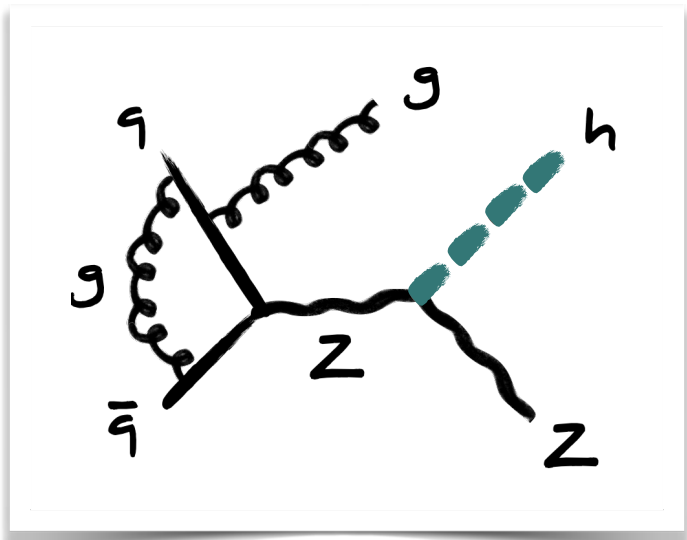
3. Higher-Order Corrections

3.1 Amplitudes

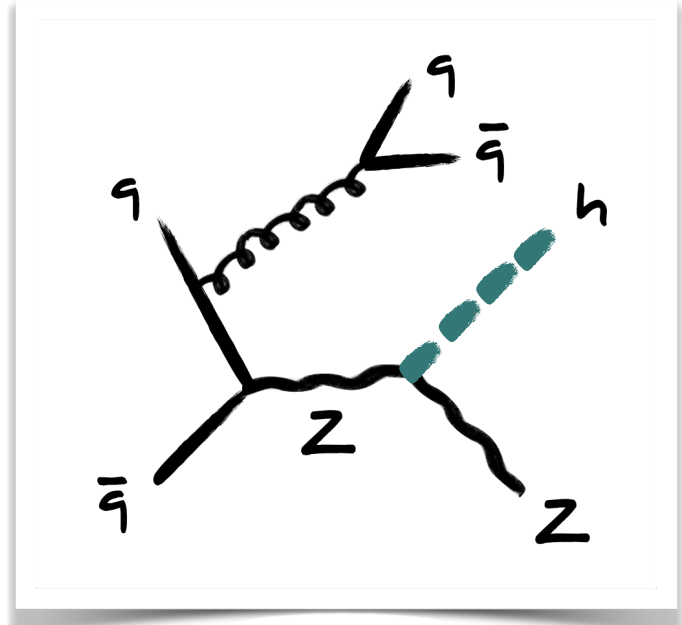
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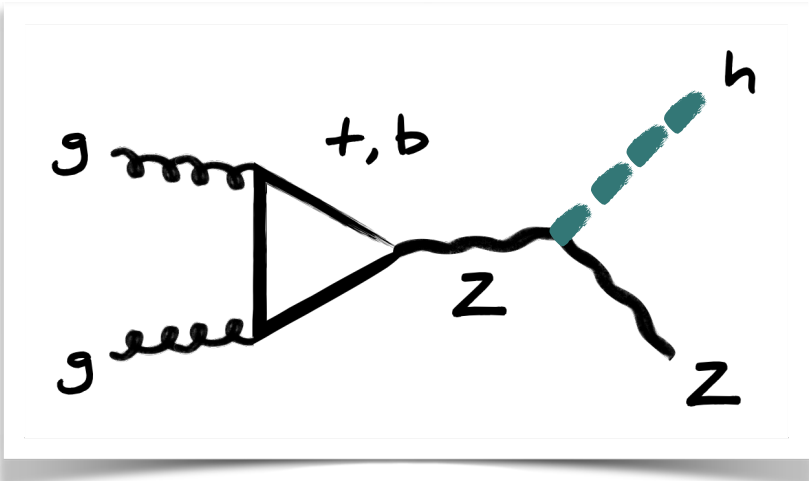
In the SM, the higher-order QCD corrections to Vh at **NNLO+PS** are well-known.



(B-type)



(C,D-type)



(A-type)

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[1601.00658] (J.M. Campbell, R.K. Ellis, C. Williams)

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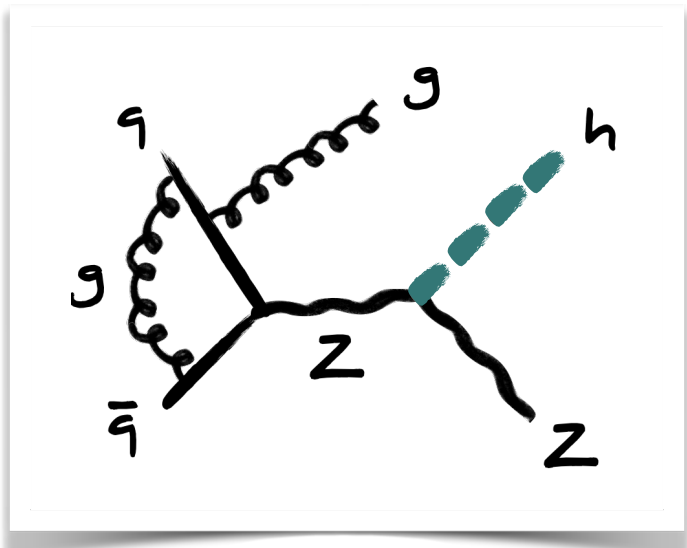
[1907.05836] (R. Gauld, A. Gehrmann-De Ridder, E.W.N. Glover, *et al.*)

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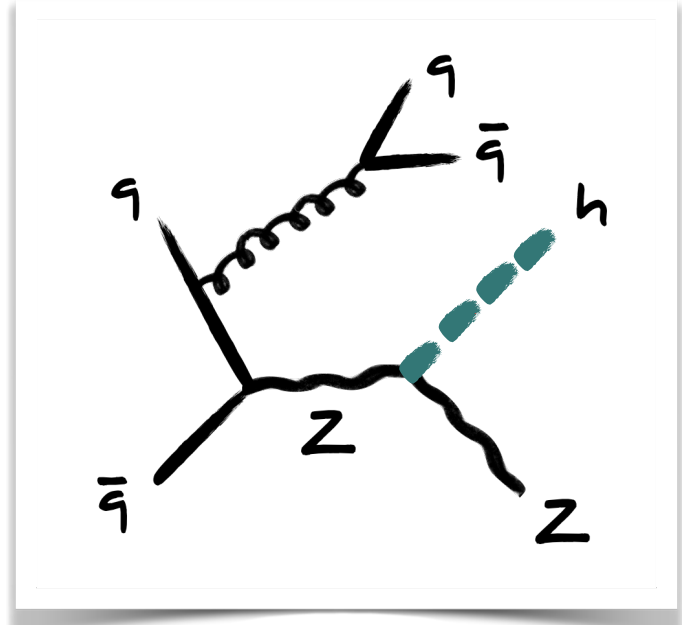
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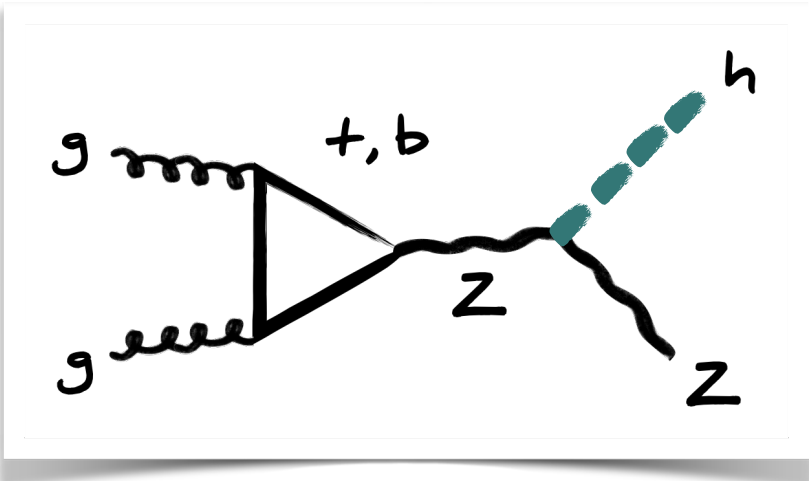
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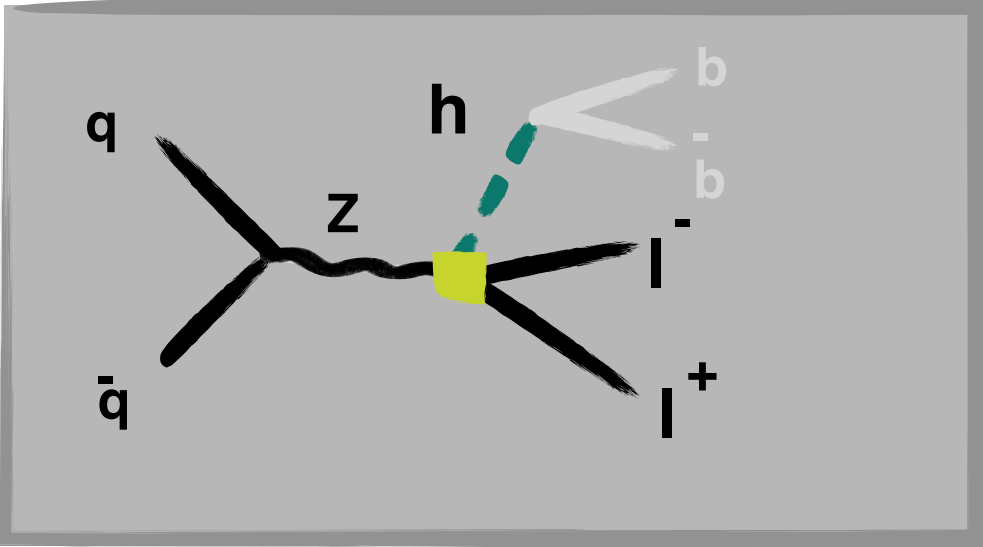
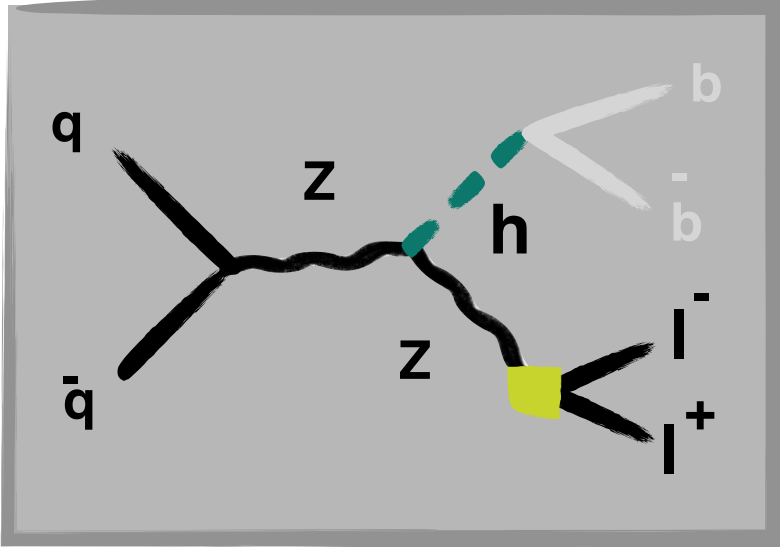
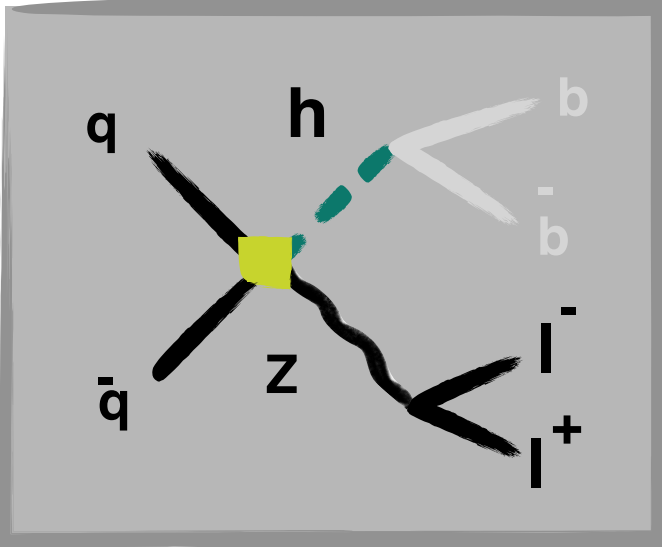
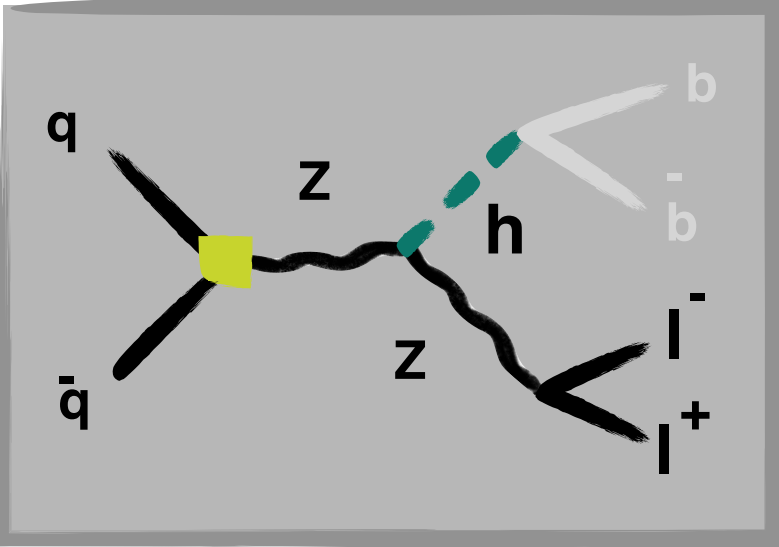
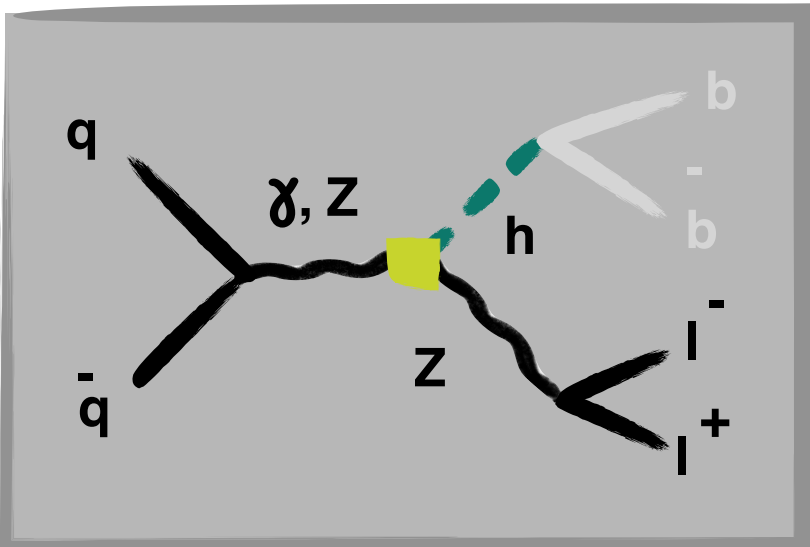
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Our goal is to calculate the **NNLO+PS** corrections to these **SMEFT** contributions:



[1512.02572] (K. Mimasu, V. Sanz, C. Williams)

[1609.04833] (C. Degrande, B. Fuks, K. Mawatari, *et al.*)

[1710.04143] (A. Greljo, G. Isidori, J.M. Lindert, *et al.*)

[1804.07407] (S. Alioli, W. Denkens, M. Girard, E. Mereghetti)

NLO:

NNLO: [2204.00663] (U. Haisch, D.J. Scott, M. Wiesemann, *et al.*)

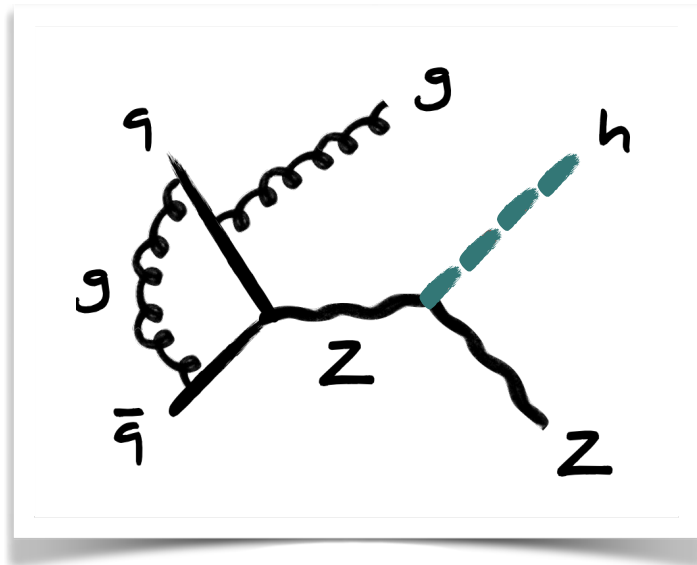
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3.2 $q\bar{q}$ -initiated contributions

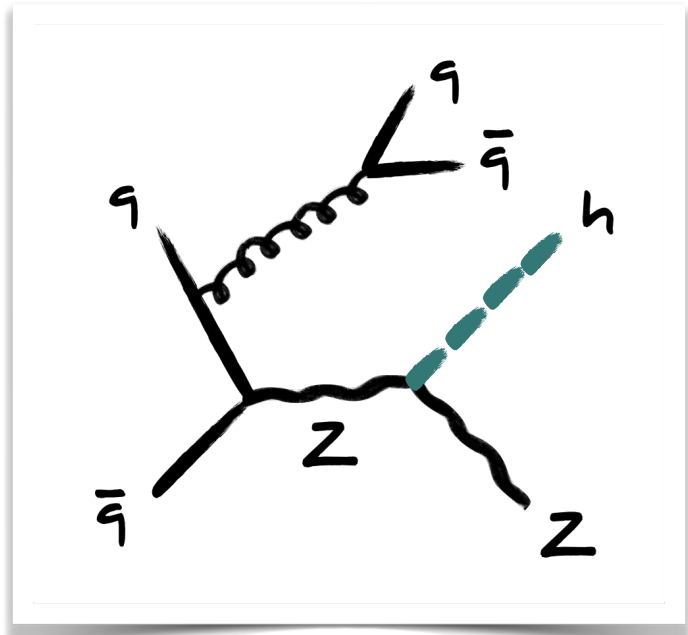
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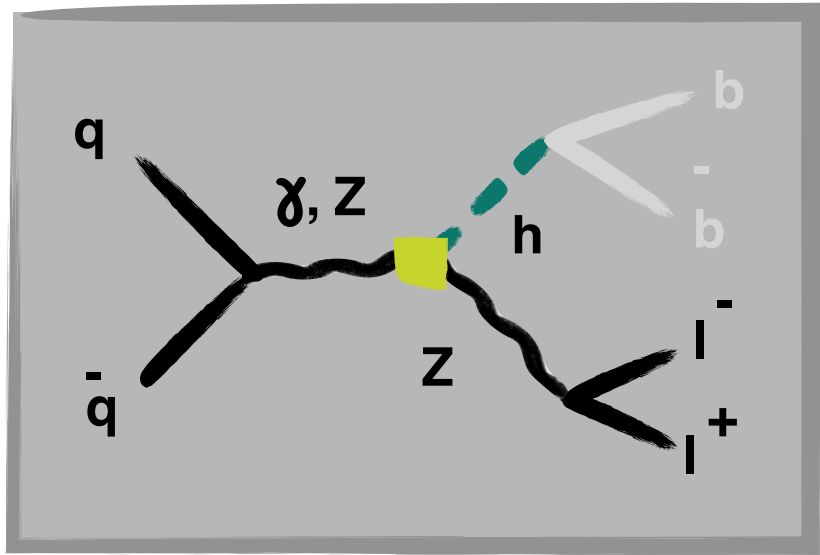


(B-type)



(C,D-type)

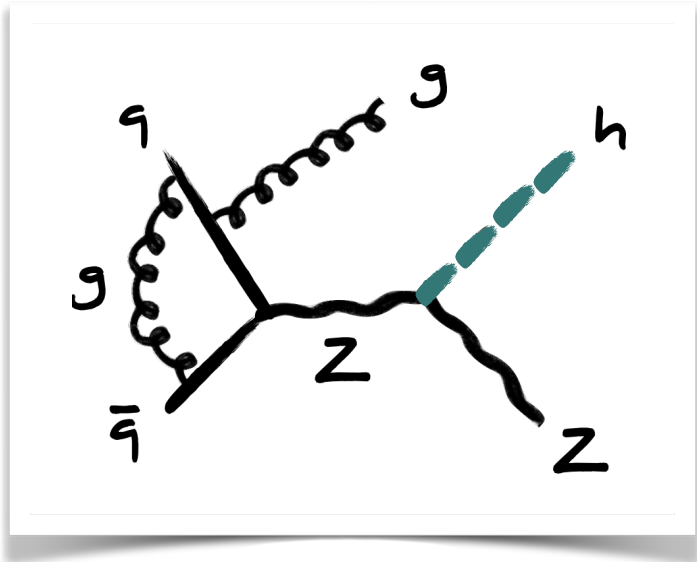
Diagram:



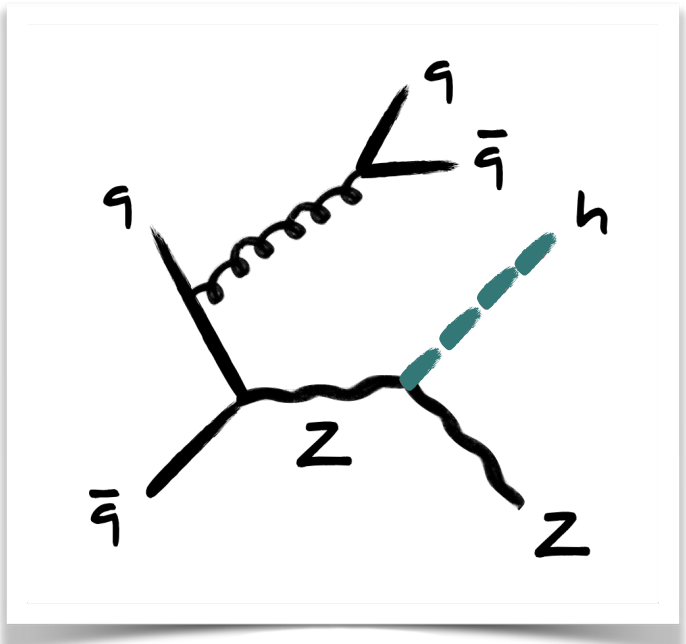
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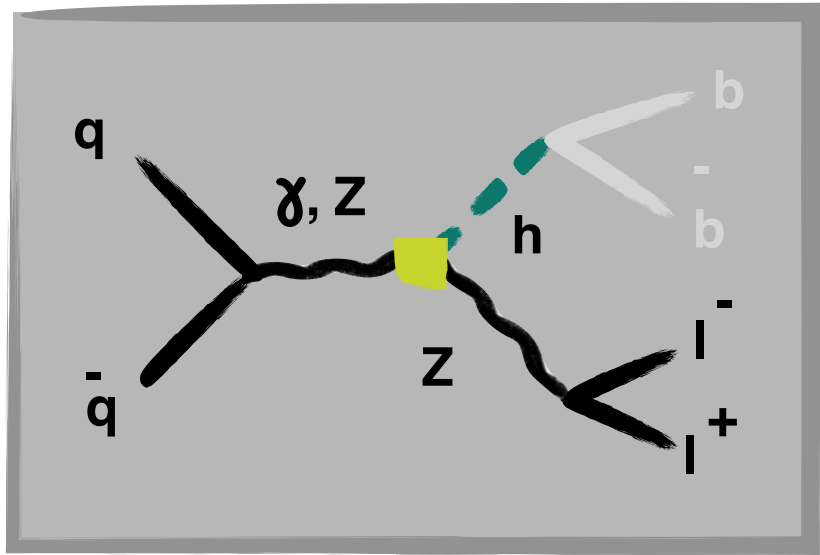


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We start with the **SM spinor-helicity amplitudes...**

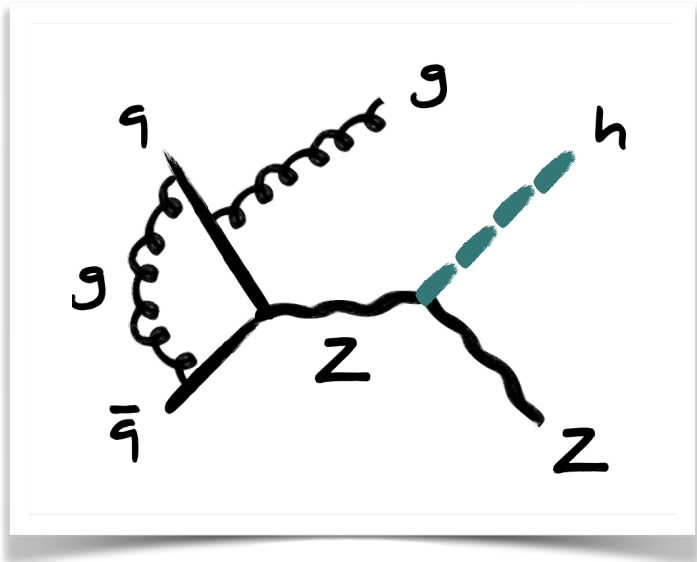
[10.3929/ethz-b-000448848] (Thesis of I. Majer)

[1112.1531] (T. Gehrmann, L. Tancredi)

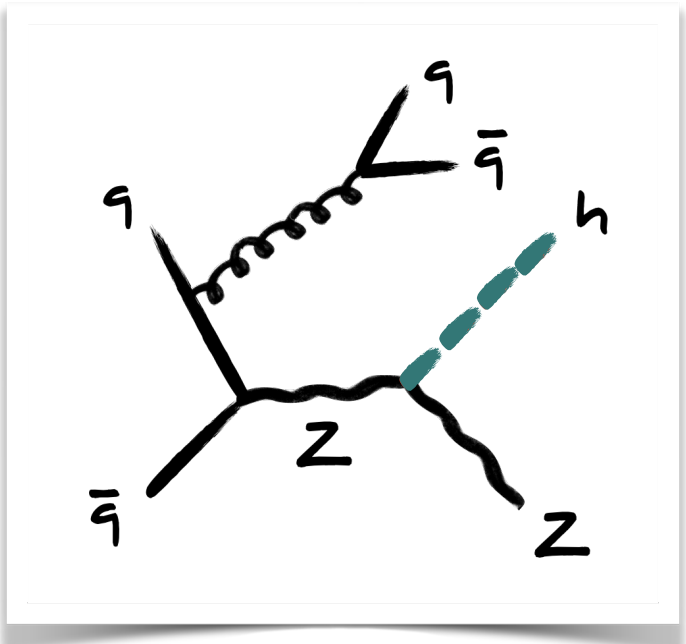
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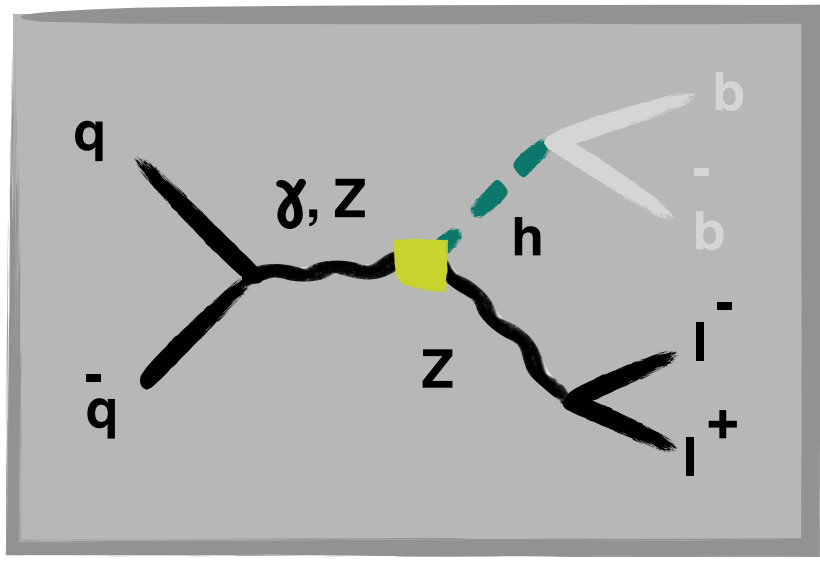


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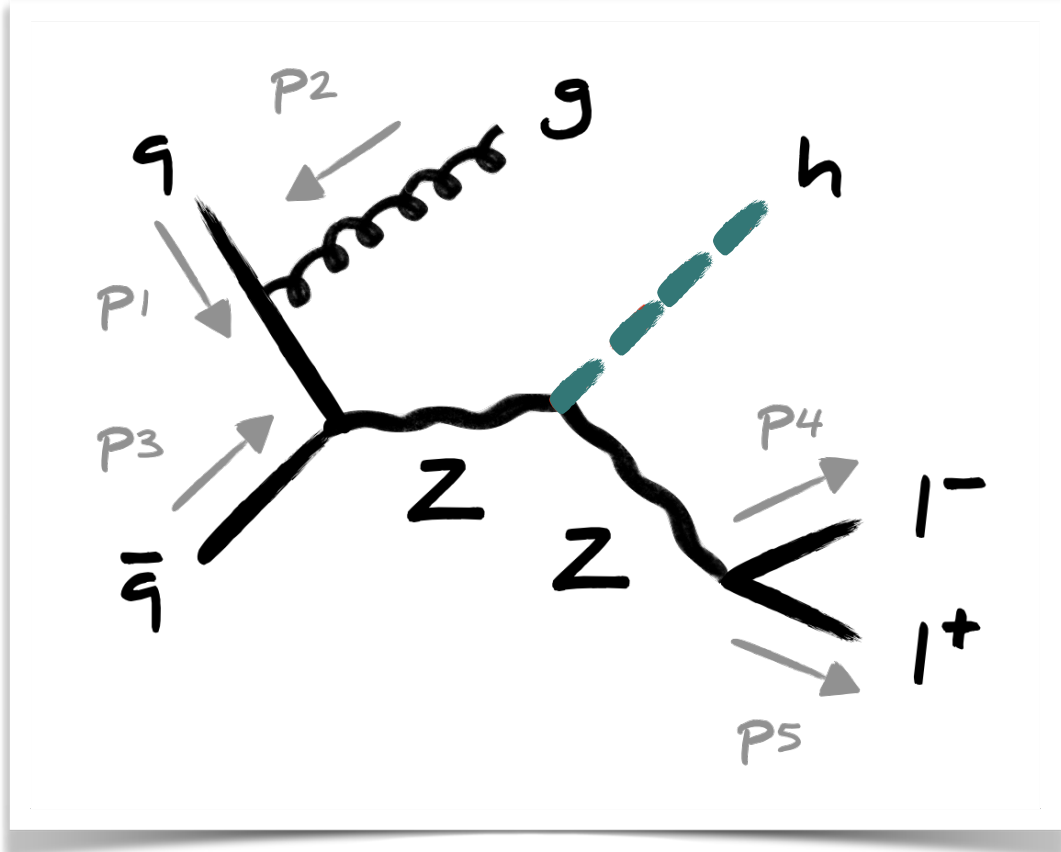
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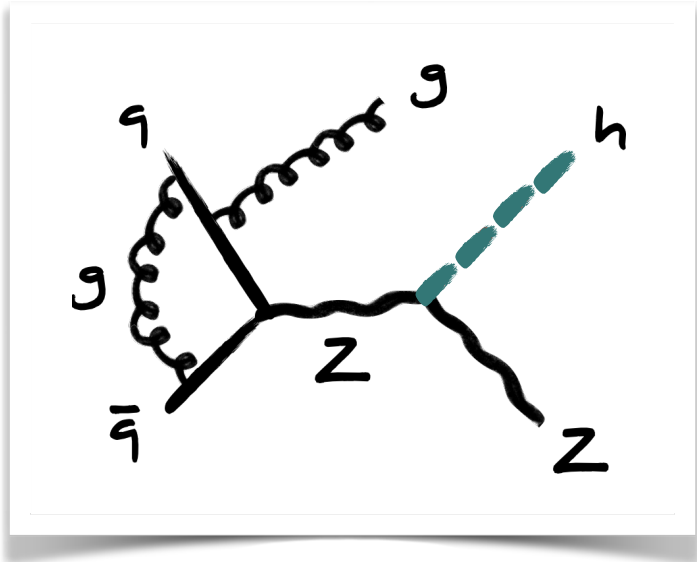


(B1g0Z)

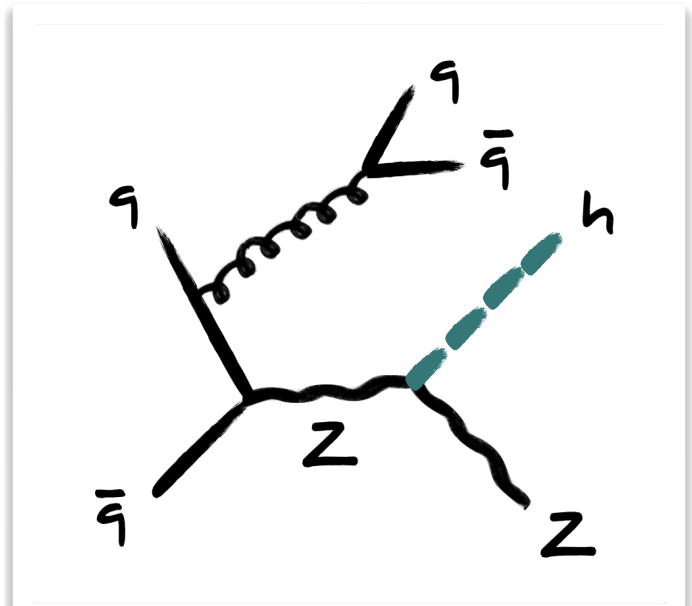
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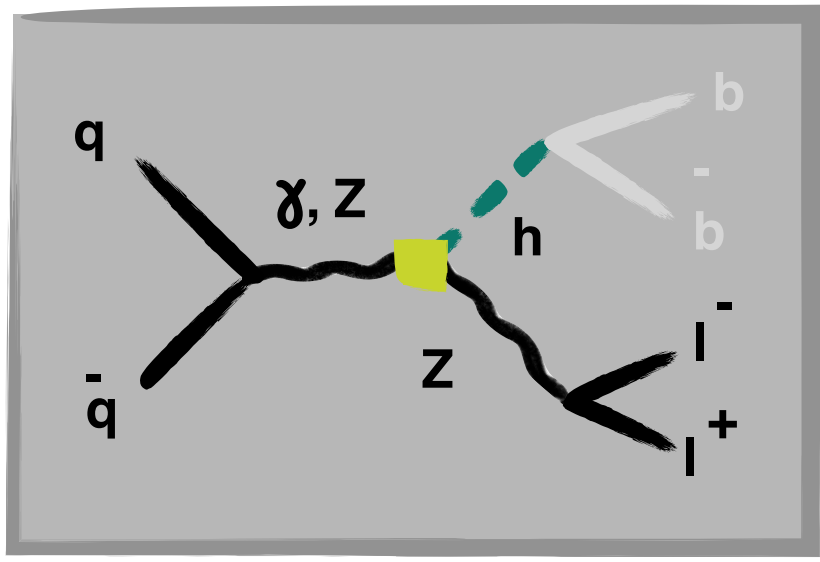


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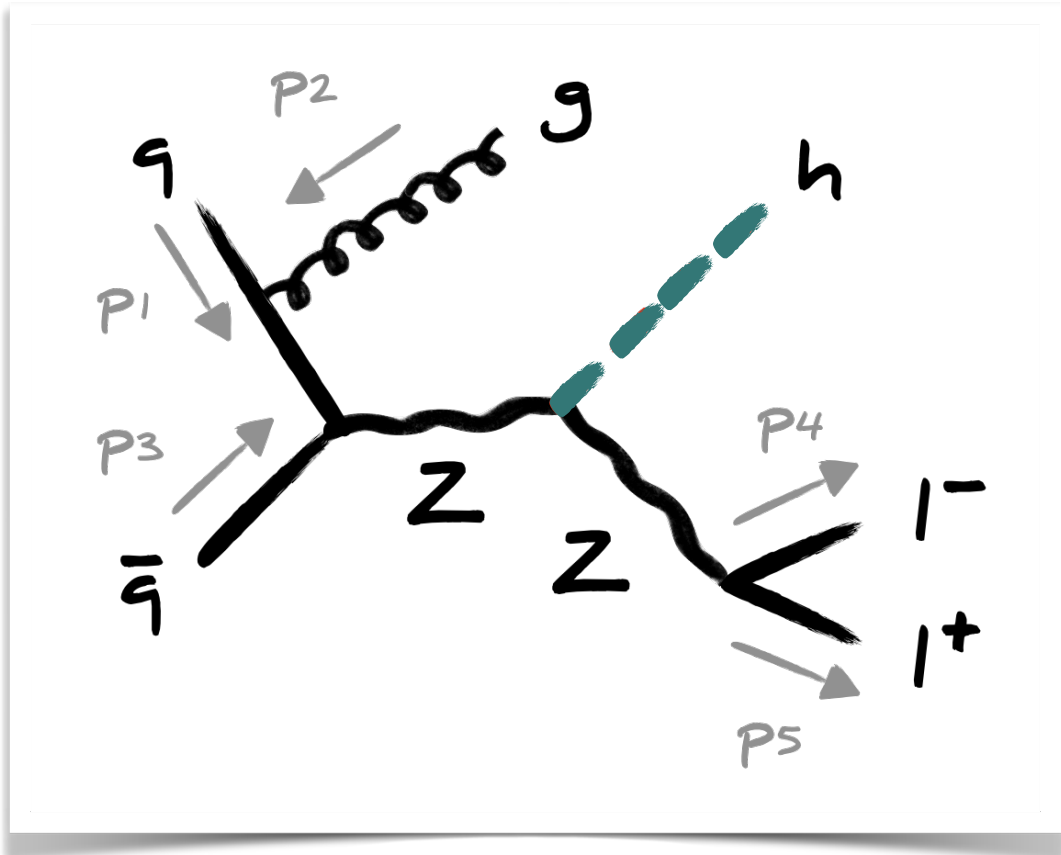
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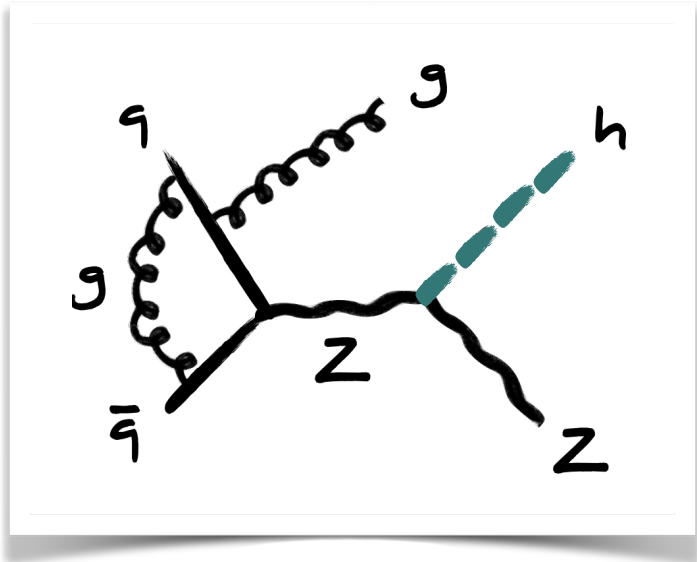
(B1g0Z)

$$B1g0Z = \frac{8\pi\alpha_s C_F}{C_A} \sum_{h_q, h_g, h_\ell = \pm} \left| \frac{g_{Zq}^{h_q} g_{Z\ell}^{h_\ell} g_{hZZ}}{D_Z(s_{123}) D_Z(s_{45})} \mathcal{A}_{B1g0Z} \left(1_q^{h_q}, 2_g^{h_g}, 3_{\bar{q}}^{-h_q}, 4_\ell^{h_\ell}, 5_{\bar{\ell}}^{-h_\ell} \right) \right|^2,$$

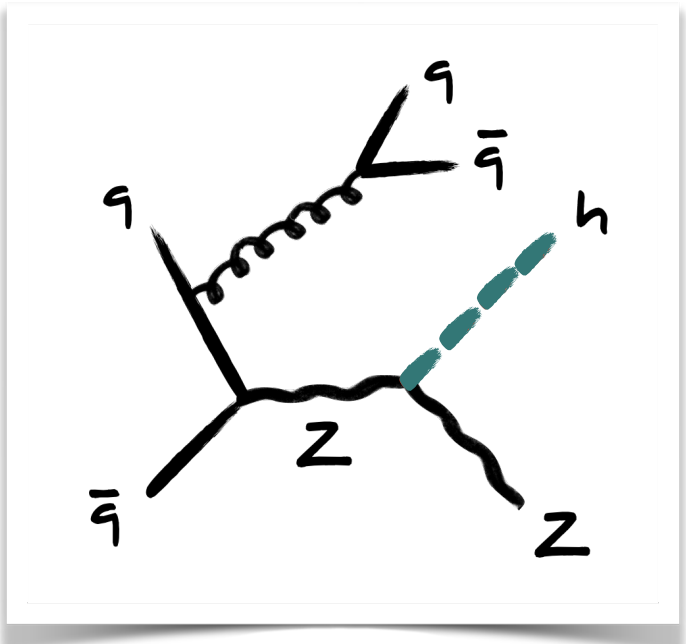
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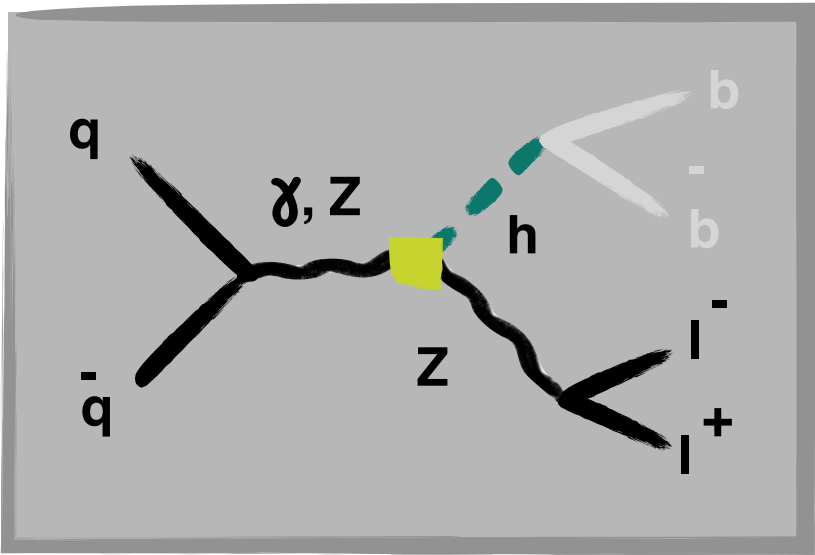


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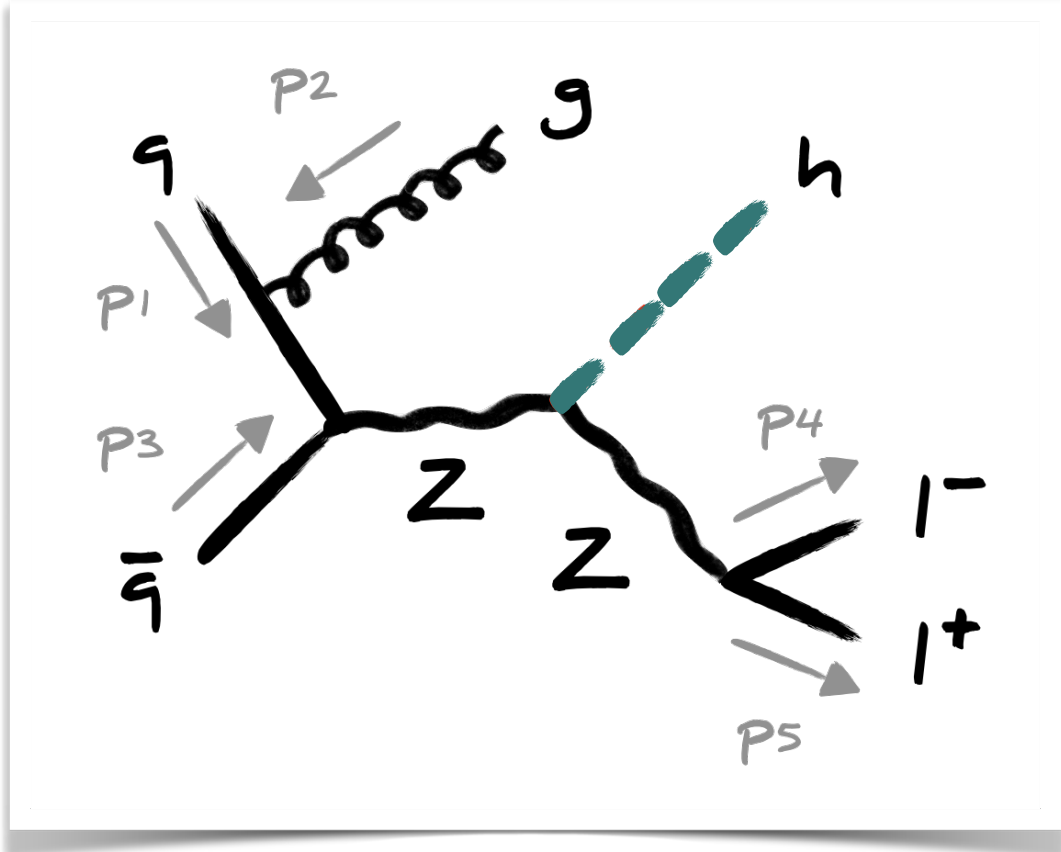
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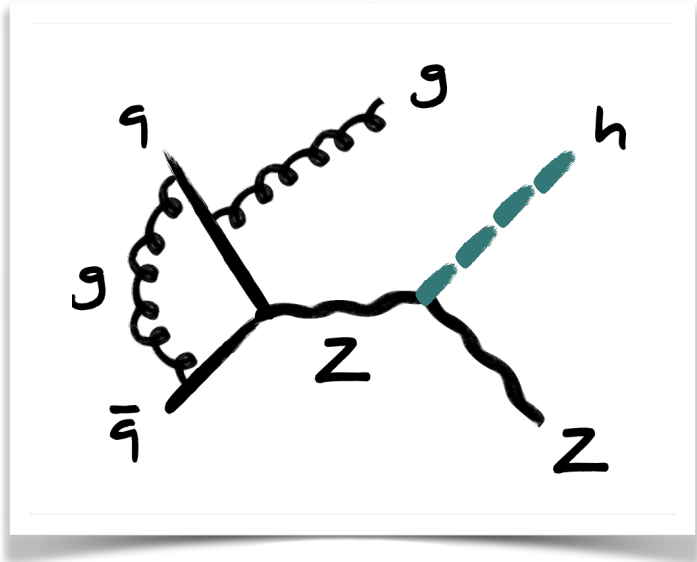
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$$\mathcal{A}_{B_{1g0Z}}(1_q^-, 2_g^-, 3_{\bar{q}}^+; 4_\ell^-, 5_{\bar{\ell}}^+) = \frac{\langle 34 \rangle}{\langle 12 \rangle \langle 23 \rangle} \left(\langle 13 \rangle [51] + \langle 23 \rangle [52] \right),$$

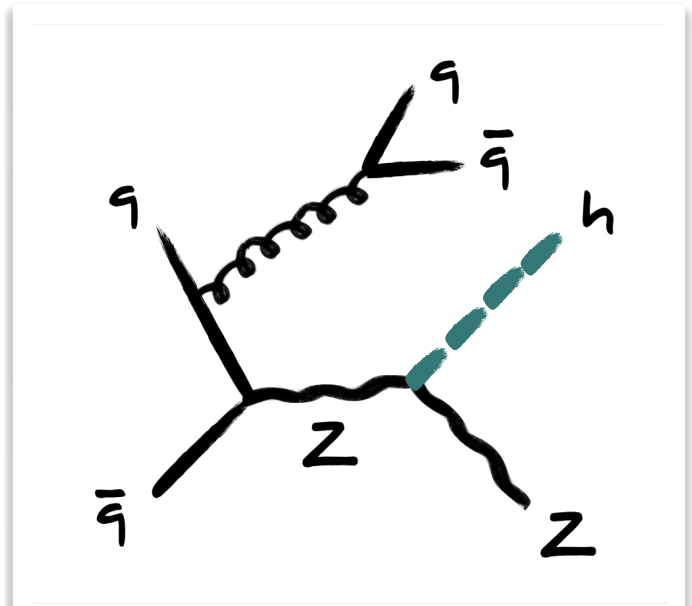
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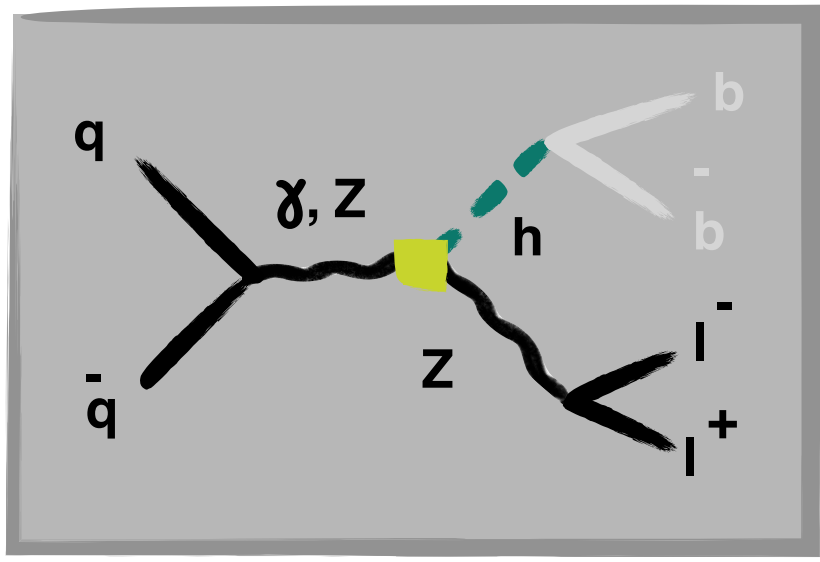


(B-type)



(C,D-type)

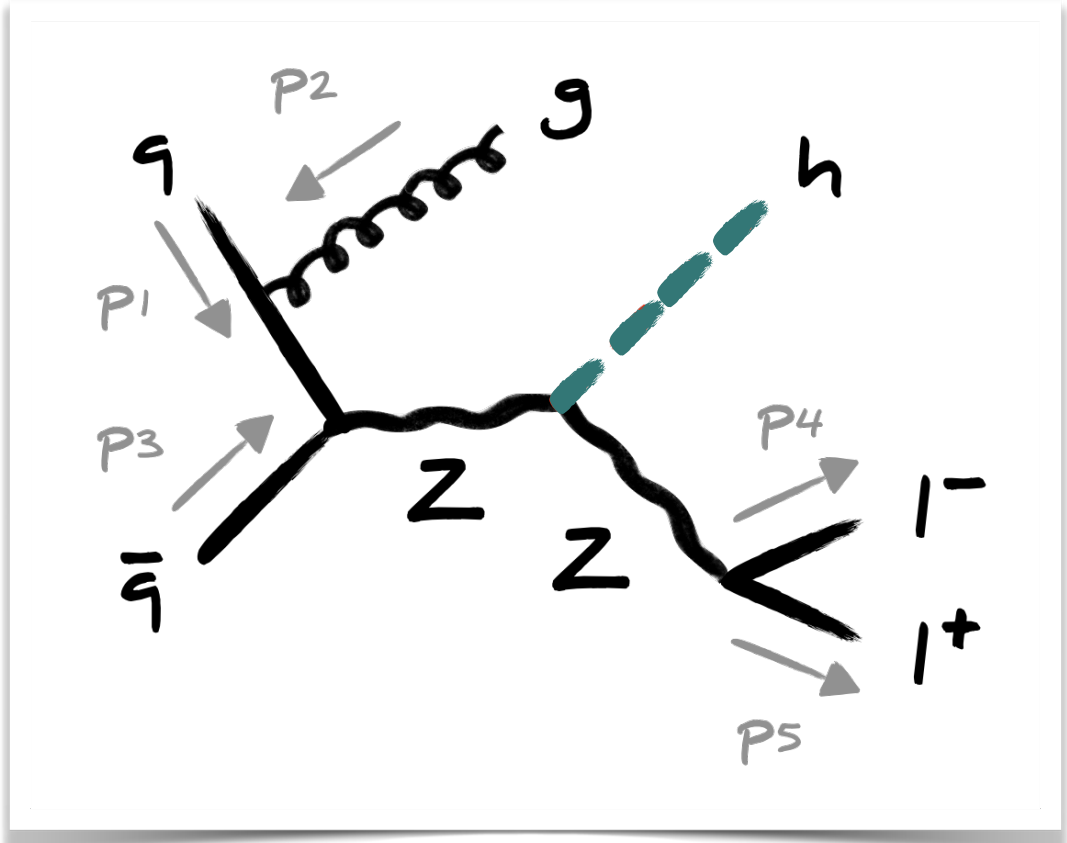
Diagram:



We start with the **SM spinor-helicity amplitudes...**

[10.3929/ethz-b-000448848] (Thesis of I. Majer)

[1112.1531] (T. Gehrmann, L. Tancredi)



(B1g0Z)

$$B_{1g0Z} = \frac{8\pi\alpha_s C_F}{C_A} \sum_{h_q, h_g, h_\ell = \pm} \left| \frac{g_{Zq}^{h_q} g_{Z\ell}^{h_\ell} g_{hZZ}}{D_Z(s_{123}) D_Z(s_{45})} \mathcal{A}_{B_{1g0Z}}(1_q^{h_q}, 2_g^{h_g}, 3_{\bar{q}}^{-h_q}, 4_\ell^{h_\ell}, 5_{\bar{\ell}}^{-h_\ell}) \right|^2,$$

$$\mathcal{A}_{B_{1g0Z}}(1_q^-, 2_g^-, 3_{\bar{q}}^+; 4_\ell^-, 5_{\bar{\ell}}^+) = \frac{\langle 34 \rangle}{\langle 12 \rangle \langle 23 \rangle} \left(\langle 13 \rangle [51] + \langle 23 \rangle [52] \right),$$



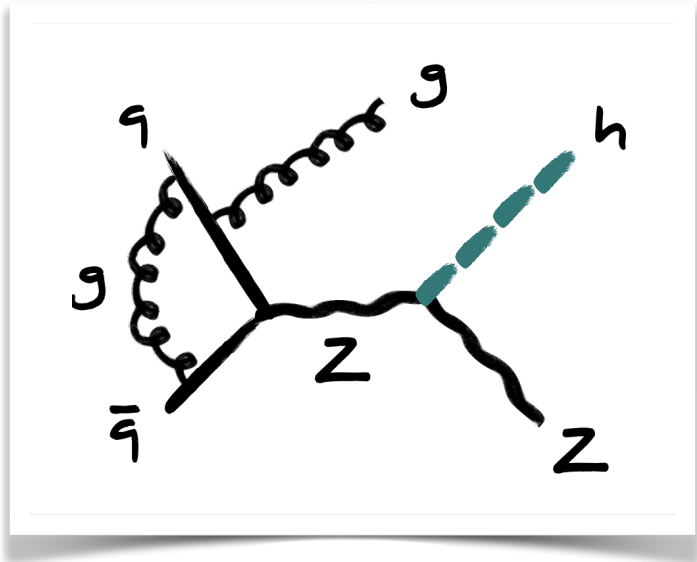
$$\langle 4 | \gamma_\mu | 5 \rangle \mathcal{A}_{qqg}^\mu(1_q^-, 2_g^-, 3_{\bar{q}}^+).$$

SM full amplitude

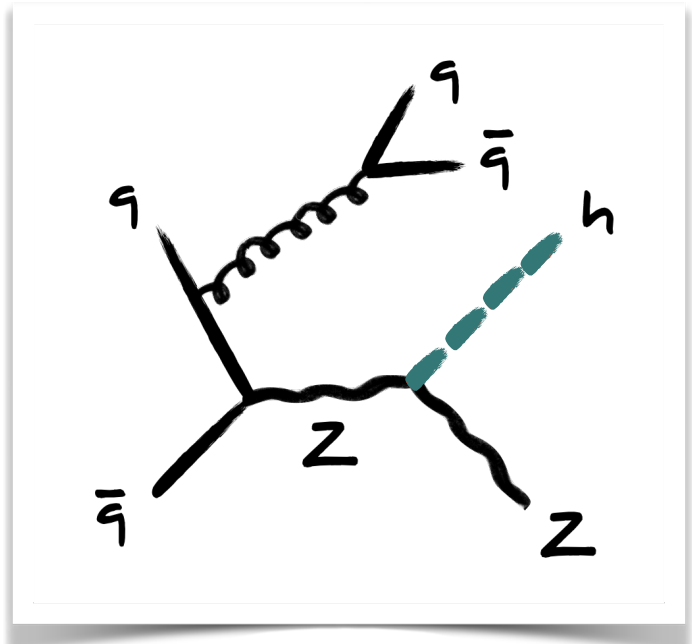
3. Higher-Order Corrections

3.2 $q\bar{q}$ -initiated contributions

Corrections:

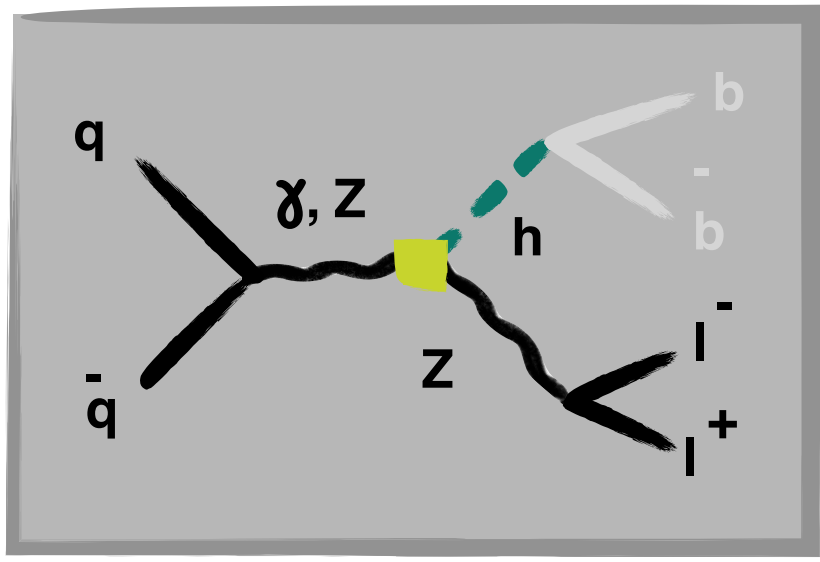


(B-type)



(C,D-type)

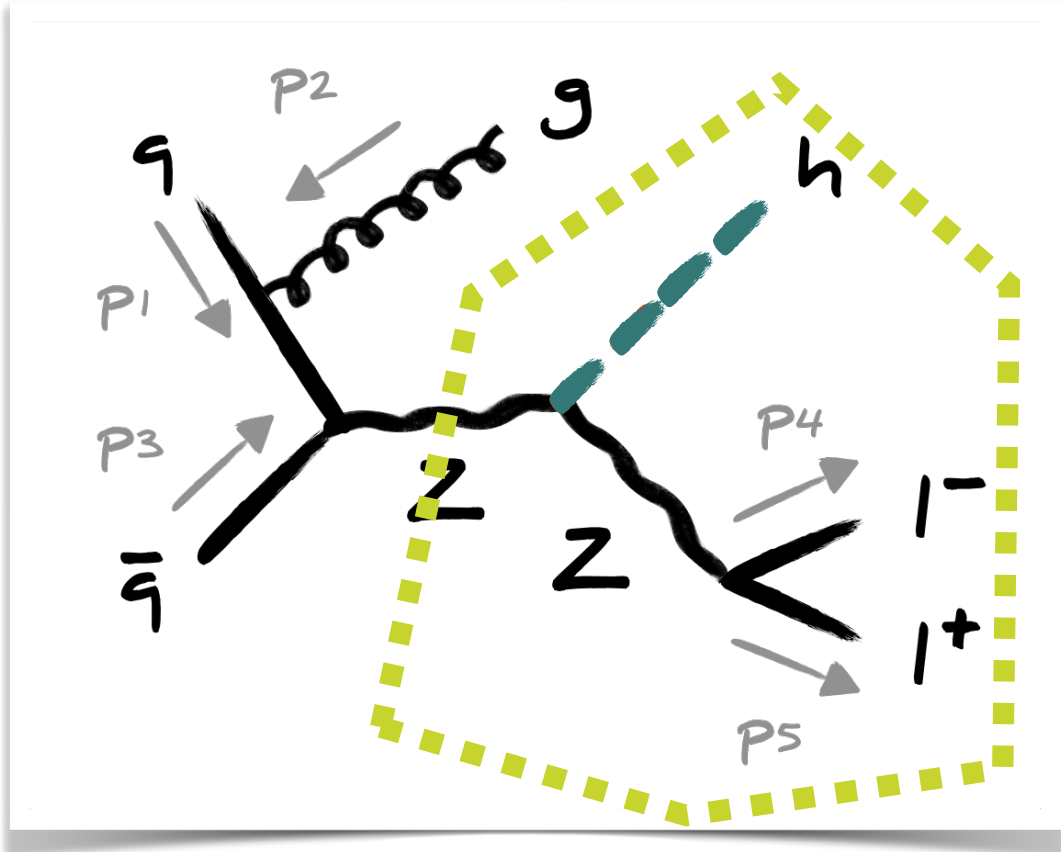
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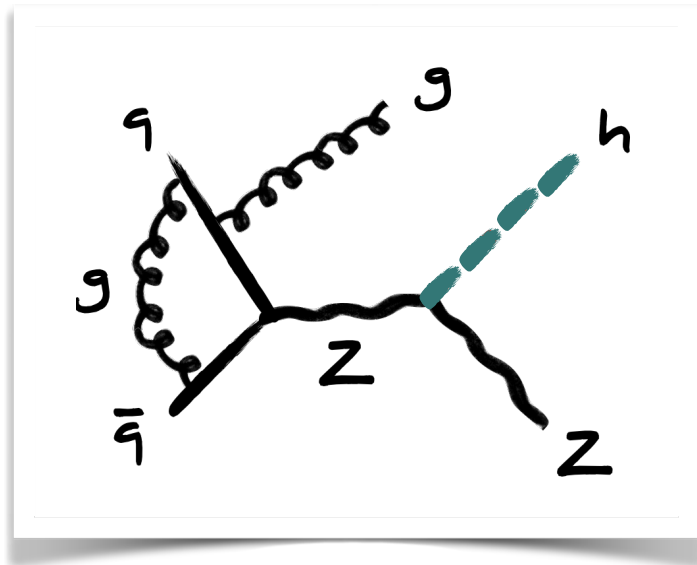
$$\langle 4 | \gamma_\mu | 5 \rangle \mathcal{A}_{qqq}^\mu \left(1_q^-, 2_g^-, 3_{\bar{q}}^+ \right).$$

SM full amplitude

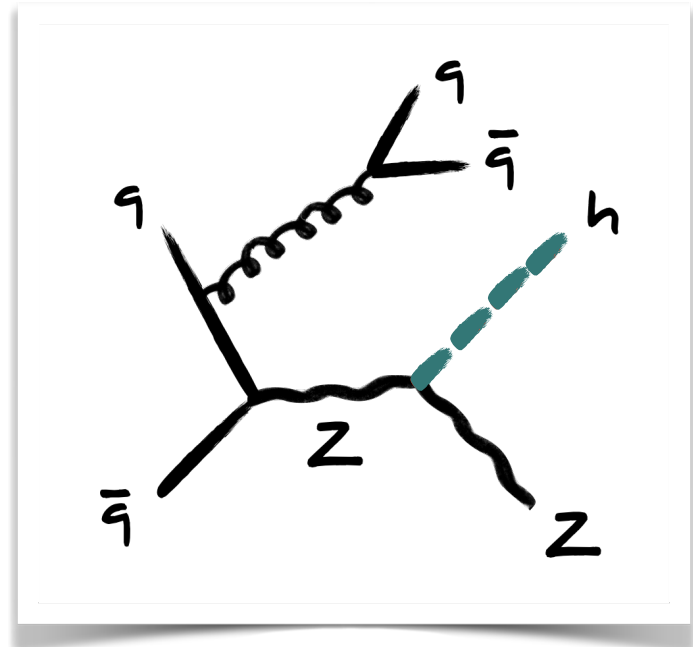
3. Higher-Order Corrections

3.2 $q\bar{q}$ -initiated contributions

Corrections:

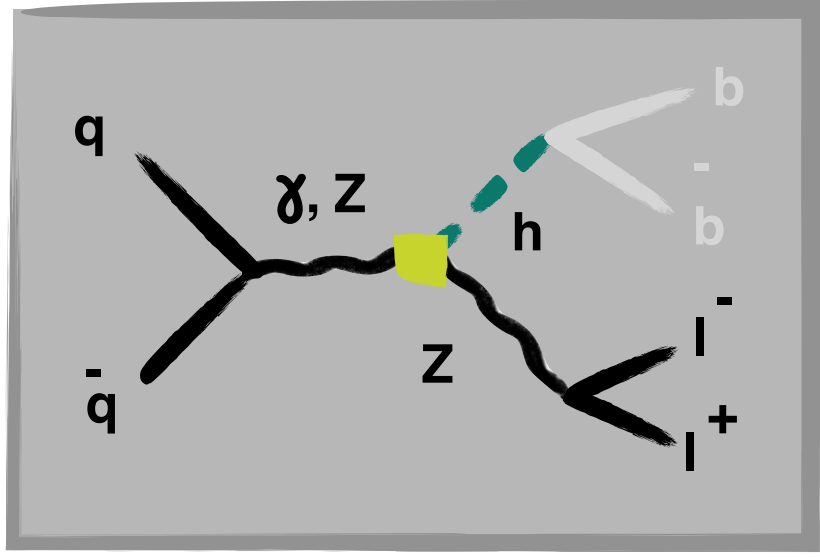


(B-type)



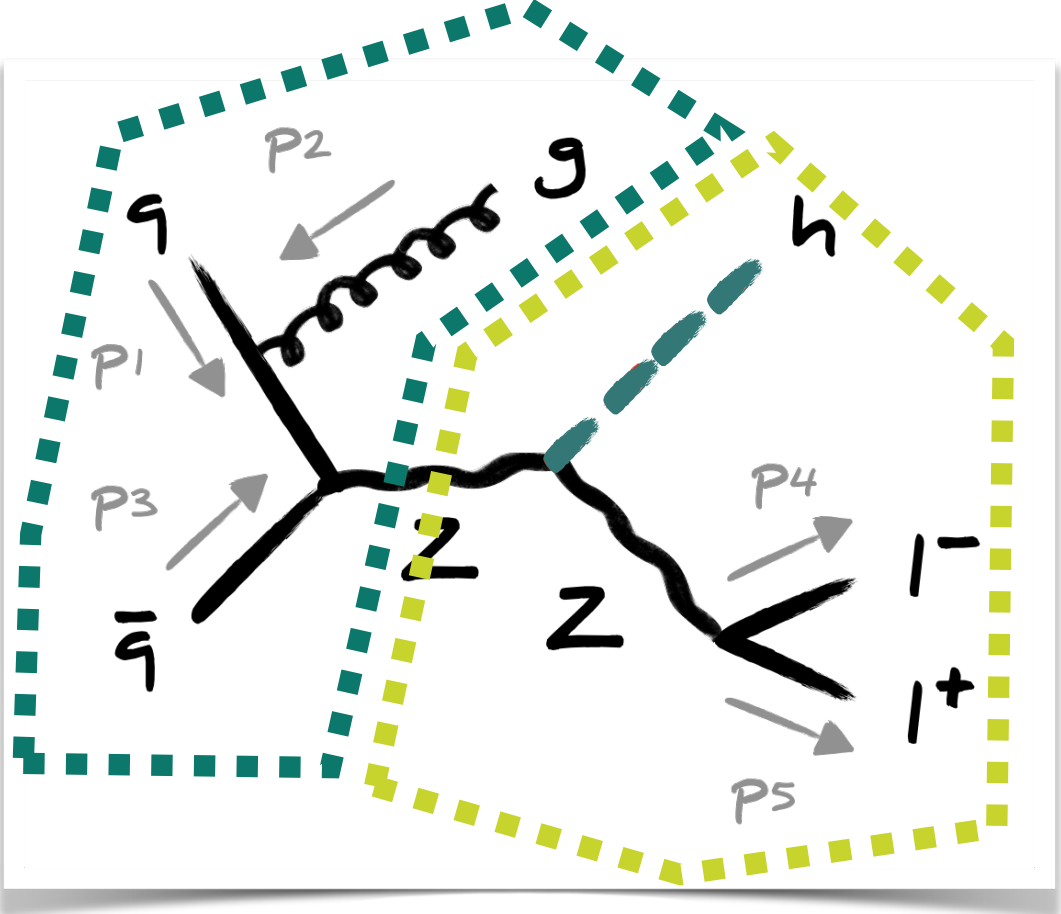
(C,D-type)

Diagram:



We start with the **SM spinor-helicity amplitudes...**

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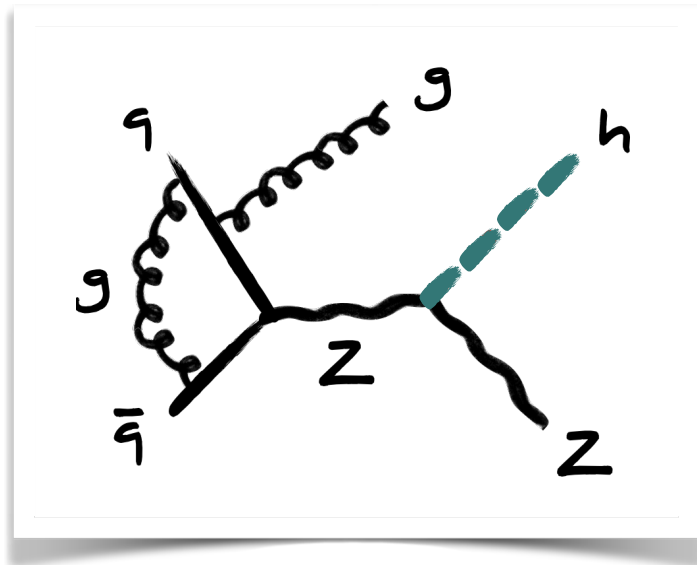
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SM full amplitude

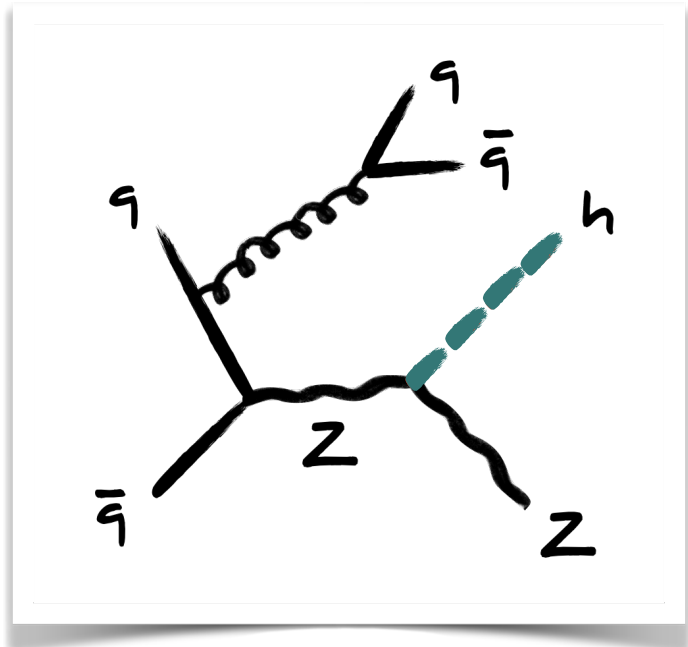
3. Higher-Order Corrections

3.2 $q\bar{q}$ -initiated contributions

Corrections:

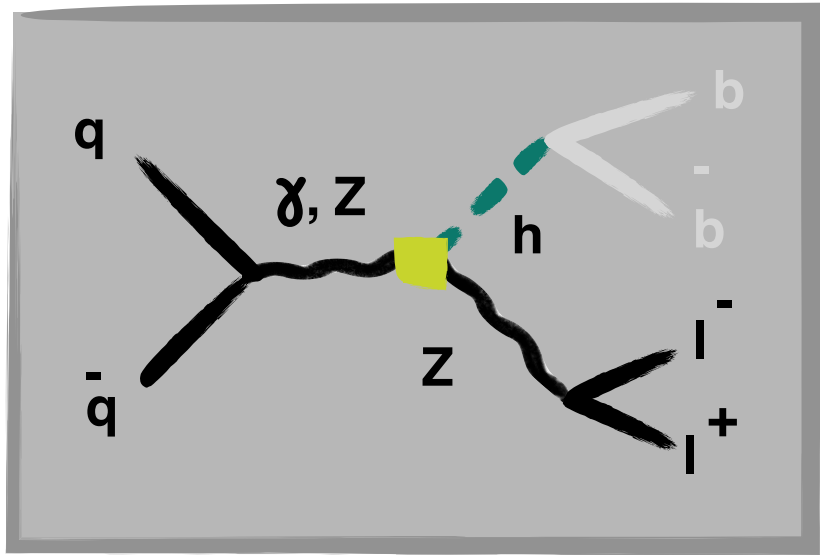


(B-type)



(C,D-type)

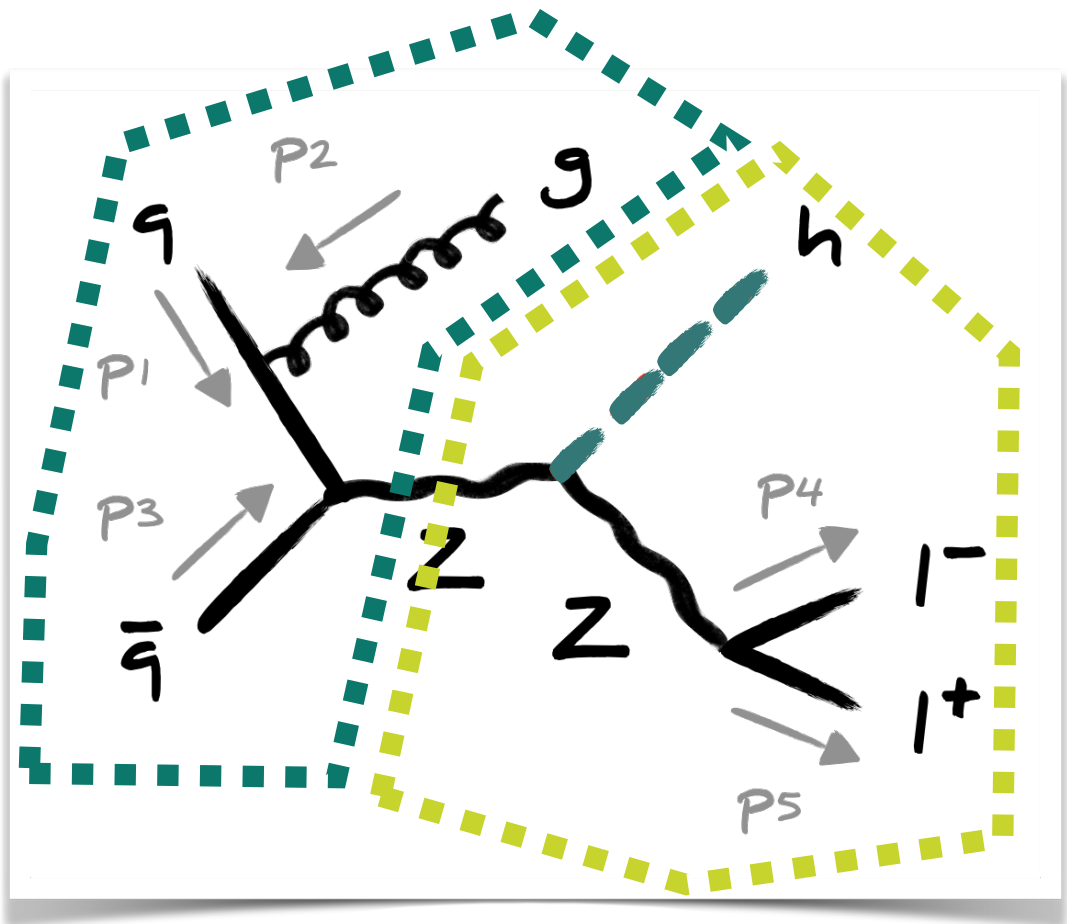
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$$\langle 4 | \gamma_\mu | 5 \rangle \mathcal{A}_{qqq}^\mu(1_q^-, 2_g^-, 3_{\bar{q}}^+).$$

SM full amplitude



$$\mathcal{A}_{qqq}^\mu(1_q^-, 2_g^-, 3_{\bar{q}}^+) = \frac{\langle 13 \rangle \langle 3 | \gamma^\mu | 1 \rangle + \langle 23 \rangle \langle 3 | \gamma^\mu | 2 \rangle}{2 \langle 12 \rangle \langle 23 \rangle}.$$

SM initial state

3. Higher-Order Corrections

3.2 $q\bar{q}$ -initiated contributions

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3.2 $q\bar{q}$ -initiated contributions

... and contract the **new helicity structures**.

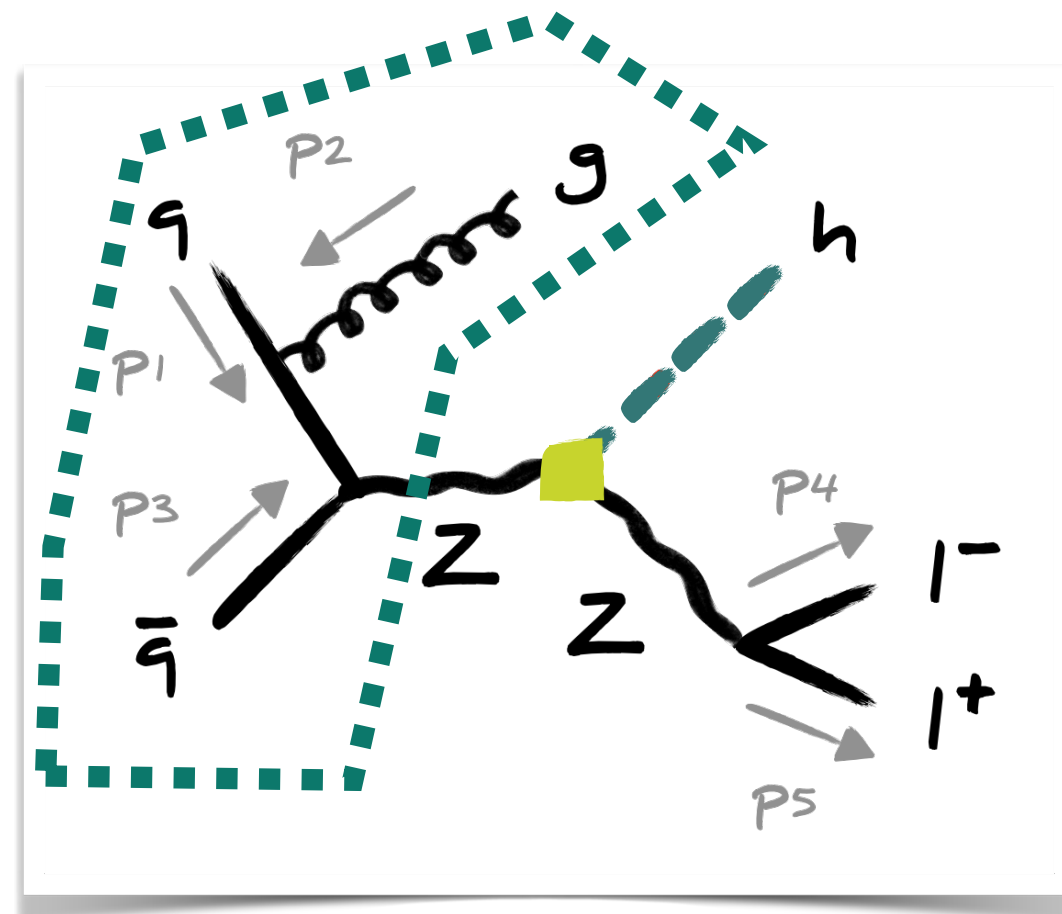
3. Higher-Order Corrections

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$$\mathcal{A}_{qgq}^\mu(1_q^-, 2_g^-, 3_{\bar{q}}^+) = \frac{\langle 13 \rangle \langle 3 | \gamma^\mu | 1 \rangle + \langle 23 \rangle \langle 3 | \gamma^\mu | 2 \rangle}{2 \langle 12 \rangle \langle 23 \rangle}.$$

SM initial state



(B1g0Z)

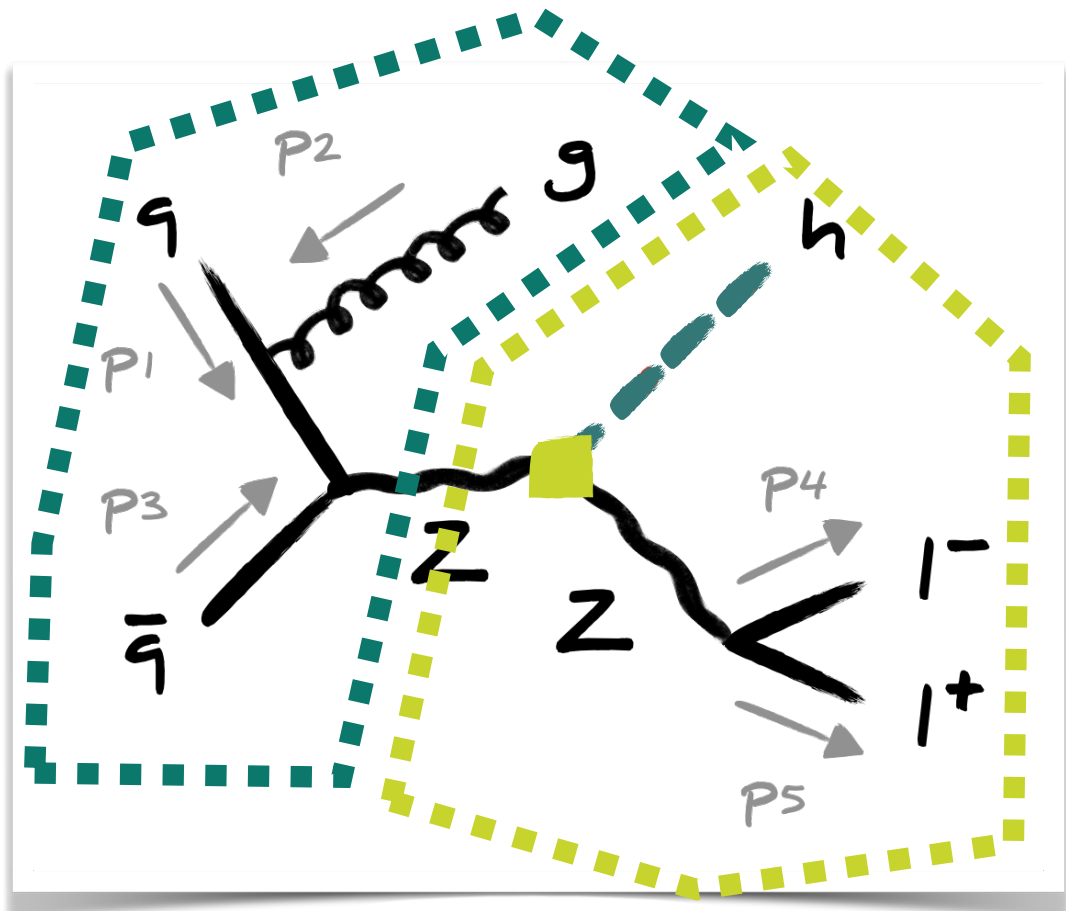
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SM initial state



(B1g0Z)

$$\mathcal{A}_{hZZ}^\mu(p_{123}, 4_\ell^-, 5_{\bar{\ell}}^+) = \frac{g_{Zq}^- g_{Z\ell}^-}{D_Z(s_{123}) D_Z(s_{45})} \left\{ \langle 4 | \gamma^\mu | 5 \rangle \left(g_{hZZ} + \delta g_{hZZ}^{(2)} (s_{123} + s_{34}) + \delta g_{hZZ}^{(3)} \right) - \delta g_{hZZ}^{(2)} p_{123}^\mu \langle 4 | \not{p}_{123} | 5 \rangle - \frac{\delta g_{hZZ}^{(1)}}{2} \left(\langle 4 | \gamma^\mu \not{p}_{123} | 4 \rangle [45] + \langle 45 \rangle [5 | \not{p}_{123} \gamma^\mu | 5] \right) \right\},$$

$$\mathcal{A}_{h\gamma Z}^\mu(p_{123}, 4_\ell^-, 5_{\bar{\ell}}^+) = \frac{g_{\gamma q}^- g_{Z\ell}^-}{s_{123} D(s_{45})} \left\{ - \frac{\delta g_{h\gamma Z}^{(1)}}{2} \left(\langle 4 | \gamma^\mu | 5 \rangle \left(\langle 4 | \not{p}_{123} | 4 \rangle + \langle 5 | \not{p}_{123} | 5 \rangle \right) - 2 (p_4^\mu + p_5^\mu) \langle 4 | \not{p}_{123} | 5 \rangle \right) + \delta g_{h\gamma Z}^{(2)} \left(\langle 4 | \gamma^\mu | 5 \rangle s_{123} - p_{123}^\mu \langle 4 | \not{p}_{123} | 5 \rangle \right) \right\},$$

New helicity structures

[1512.02572] (K. Mimasu, *et al.*)

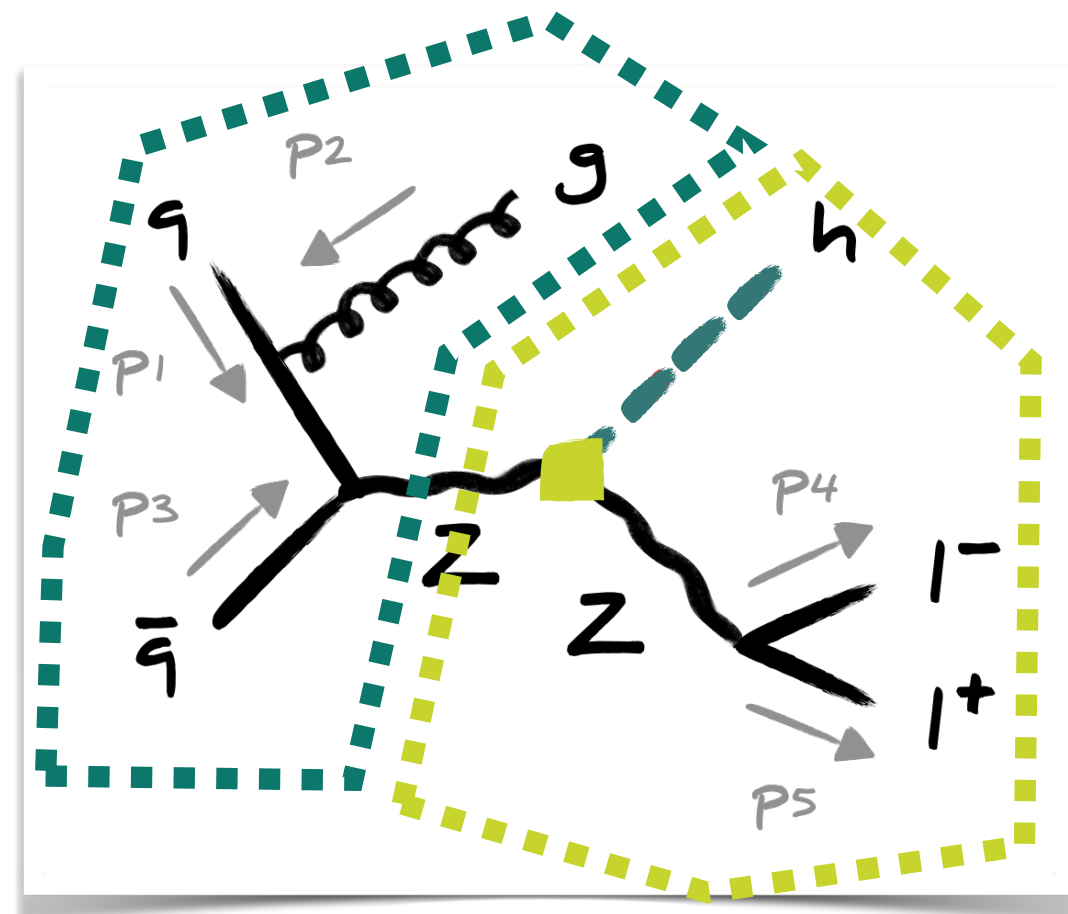
3. Higher-Order Corrections

3.2 $q\bar{q}$ -initiated contributions

... and contract the **new helicity structures**.

$$\mathcal{A}_{qqq}^\mu(1_q^-, 2_g^-, 3_{\bar{q}}^+) = \frac{\langle 13 \rangle \langle 3 | \gamma^\mu | 1 \rangle + \langle 23 \rangle \langle 3 | \gamma^\mu | 2 \rangle}{2 \langle 12 \rangle \langle 23 \rangle}.$$

SM initial state



(B1g0Z)

$$\mathcal{A}_{hZZ}^\mu(p_{123}, 4_\ell^-, 5_{\bar{\ell}}^+) = \frac{g_{Zq}^- g_{Z\ell}^-}{D_Z(s_{123}) D_Z(s_{45})} \left\{ \langle 4 | \gamma^\mu | 5 \rangle \left(g_{hZZ} + \delta g_{hZZ}^{(2)} (s_{123} + s_{34}) + \delta g_{hZZ}^{(3)} \right) - \delta g_{hZZ}^{(2)} p_{123}^\mu \langle 4 | \not{p}_{123} | 5 \rangle - \frac{\delta g_{hZZ}^{(1)}}{2} \left(\langle 4 | \gamma^\mu \not{p}_{123} | 4 \rangle [45] + \langle 45 | [5 | \not{p}_{123} \gamma^\mu | 5] \right) \right\},$$

$$\mathcal{A}_{h\gamma Z}^\mu(p_{123}, 4_\ell^-, 5_{\bar{\ell}}^+) = \frac{g_{\gamma q}^- g_{Z\ell}^-}{s_{123} D(s_{45})} \left\{ - \frac{\delta g_{h\gamma Z}^{(1)}}{2} \left(\langle 4 | \gamma^\mu | 5 \rangle \left(\langle 4 | \not{p}_{123} | 4 \rangle + \langle 5 | \not{p}_{123} | 5 \rangle \right) - 2 (p_4^\mu + p_5^\mu) \langle 4 | \not{p}_{123} | 5 \rangle \right) + \delta g_{h\gamma Z}^{(2)} \left(\langle 4 | \gamma^\mu | 5 \rangle s_{123} - p_{123}^\mu \langle 4 | \not{p}_{123} | 5 \rangle \right) \right\},$$

New helicity structures

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$$\mathcal{A}_{qqq,\mu} \left(1_q^{h_q}, 2_g^{h_g}, 3_{\bar{q}}^{-h_q} \right) \left[\mathcal{A}_{hZZ}^\mu(p_{123}, 4_\ell^{h_\ell}, 5_{\bar{\ell}}^{-h_\ell}) + \mathcal{A}_{h\gamma Z}^\mu(p_{123}, 4_\ell^{h_\ell}, 5_{\bar{\ell}}^{-h_\ell}) \right].$$

SMEFT full amplitude

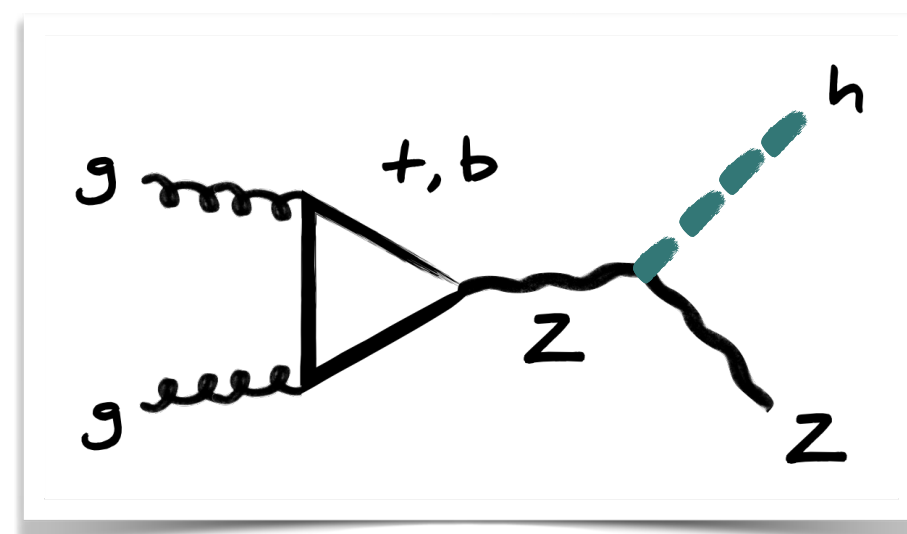
3. Higher-Order Corrections

3.3 gg -initiated contributions

3. Higher-Order Corrections

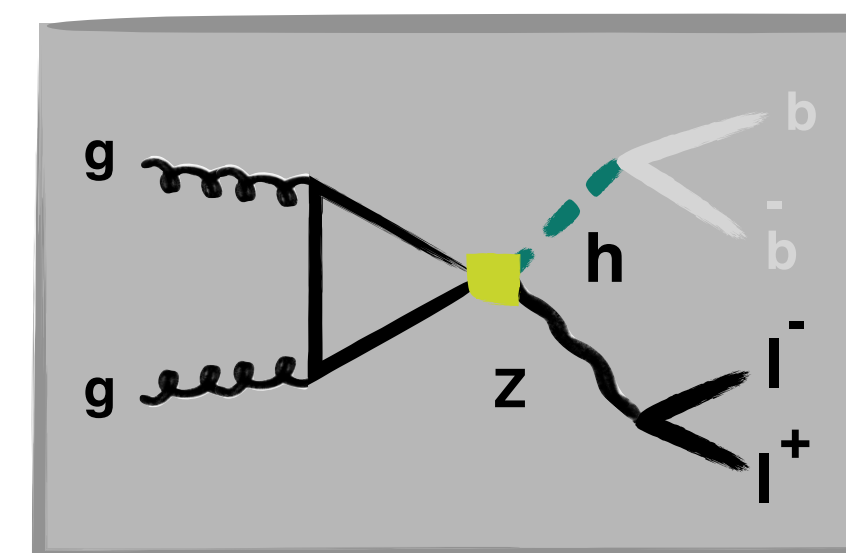
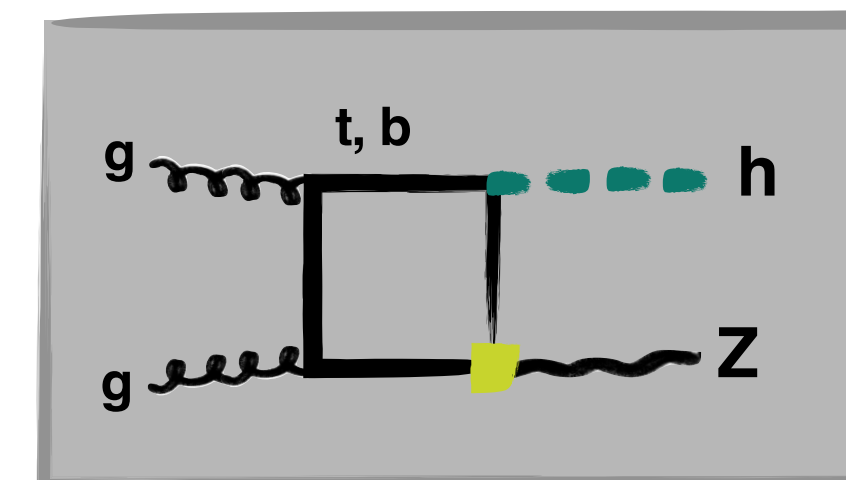
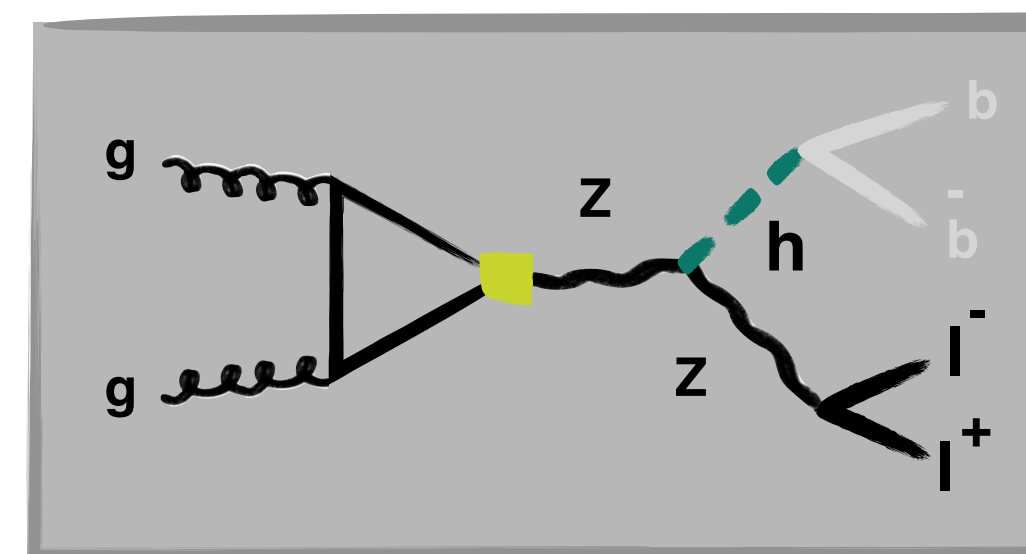
3.3 gg -initiated contributions

Corrections:



(A-type)

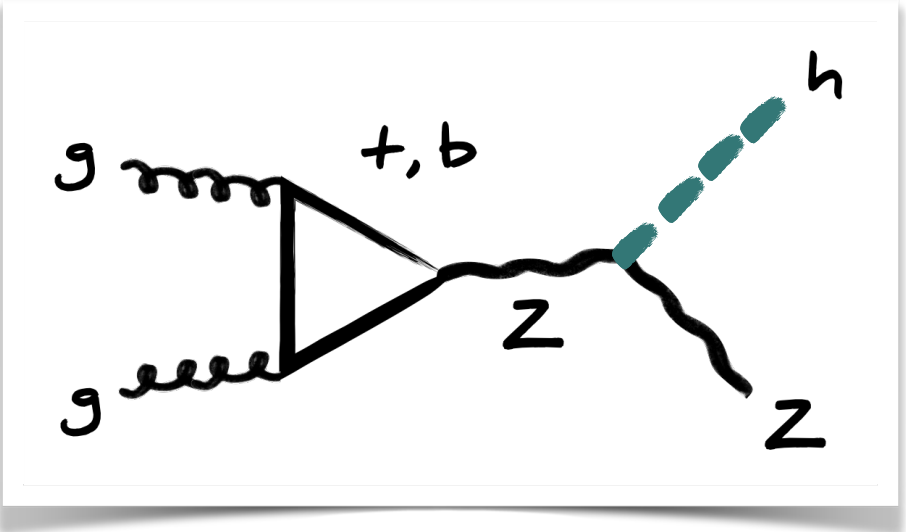
Diagrams:



3. Higher-Order Corrections

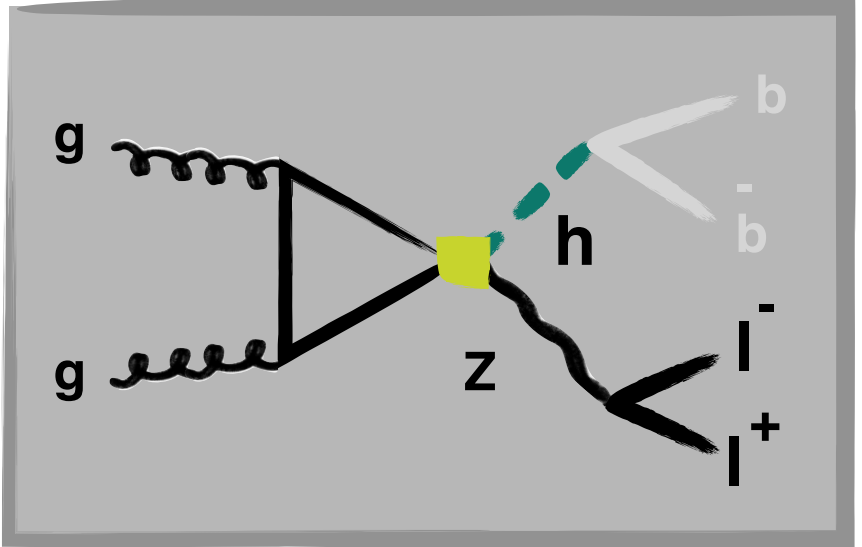
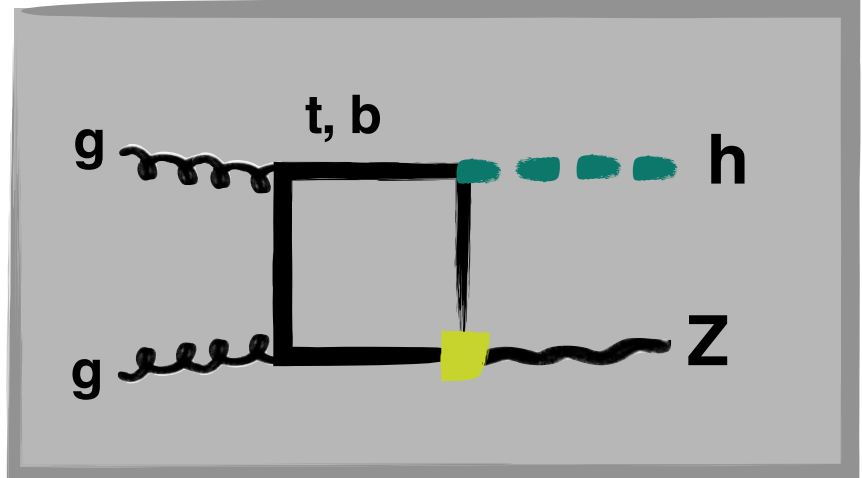
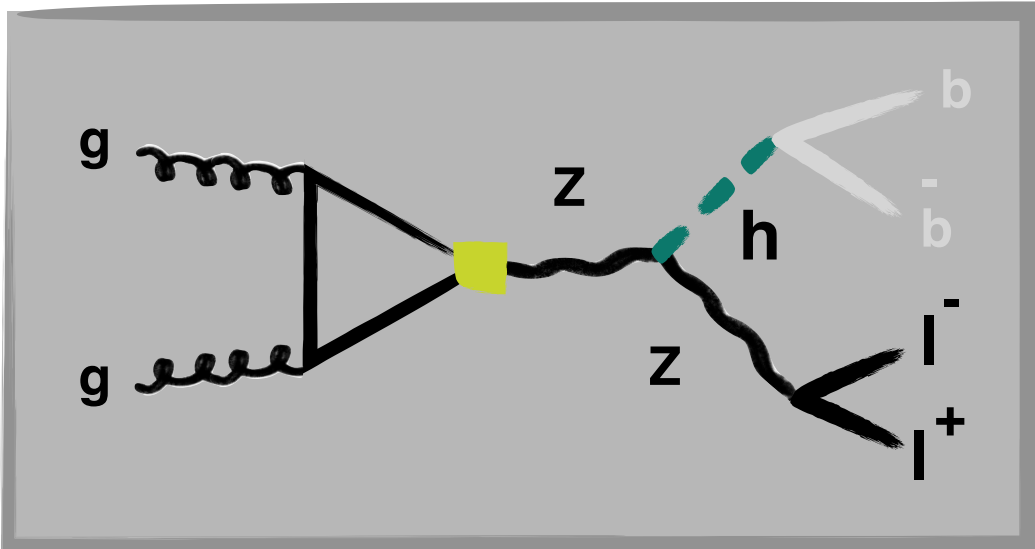
3.3 gg -initiated contributions

Corrections:



(A-type)

Diagrams:

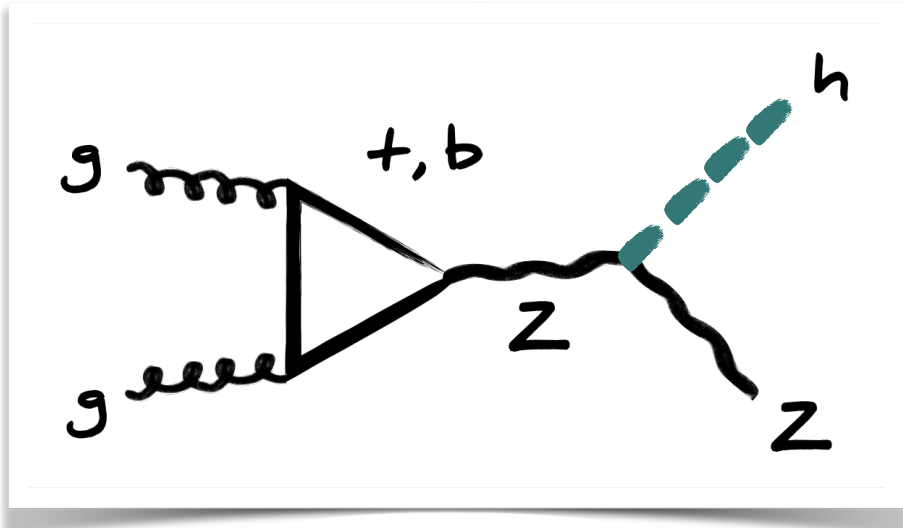


We start with the **SM spinor-helicity amplitudes...**

3. Higher-Order Corrections

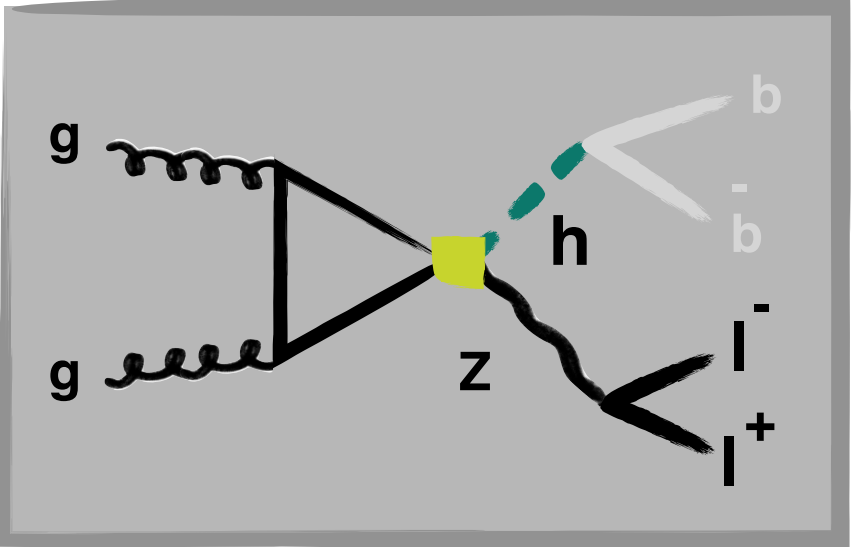
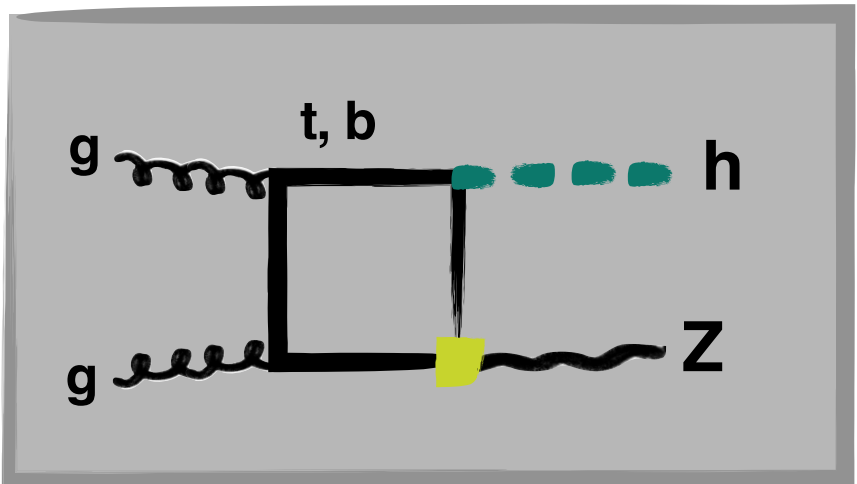
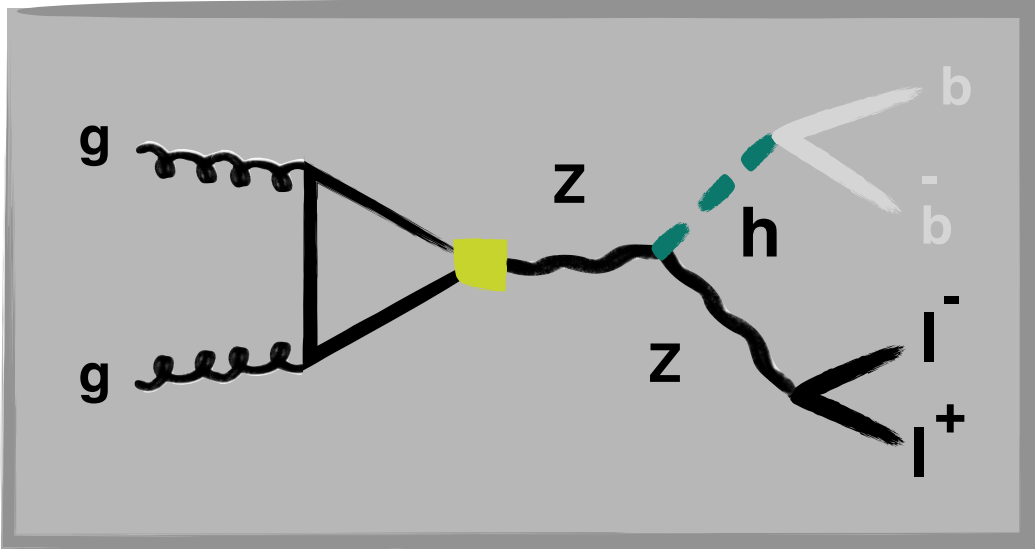
3.3 gg -initiated contributions

Corrections:



(A-type)

Diagrams:



We start with the **SM spinor-helicity amplitudes...**

$$A_{0g2Z} = \frac{\alpha_s^2}{8\pi^2 (C_A^2 - 1)^2} \sum_{h_g, h_\ell = \pm} \left| \sum_{q=t,b} \left(\mathcal{A}_\Delta^q + \sum_{s=\pm} \frac{m_q^2}{m_Z^2} \mathcal{A}_\square^{q,s} \right) \right|^2,$$

with

$$\mathcal{A}_\Delta^q = \frac{(g_{Zq}^- - g_{Zq}^+) g_{Z\ell}^{h_\ell} g_{hZZ}}{D_Z(s_{12}) D_Z(s_{34})} \mathcal{A}_{A_{0g2Z\Delta}}^q \left(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_\ell^{-h_\ell} \right),$$

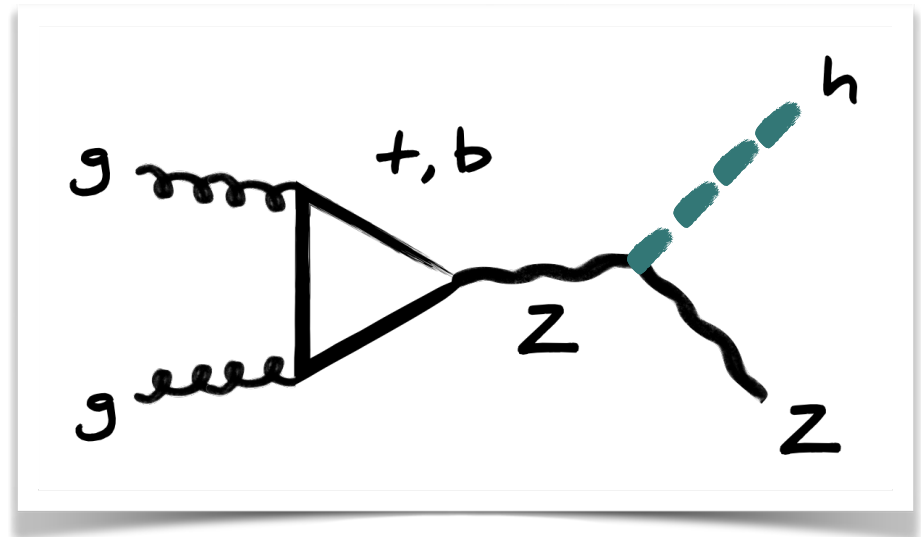
$$\mathcal{A}_{A_{0g2Z\Delta}}^q \left(1_g^+, 2_g^+, 3_\ell^-, 4_\ell^+ \right) = -\frac{2 [21] ([41] \langle 13 \rangle + [42] \langle 23 \rangle)}{\langle 12 \rangle} \left(1 - \frac{s_{12}}{m_Z^2} \right) \times m_q^2 C_0(s_{12}, 0, 0, m_q, m_q, m_q).$$

[1601.00658] (J.M. Campbell, R.K. Ellis, C. Williams)

3. Higher-Order Corrections

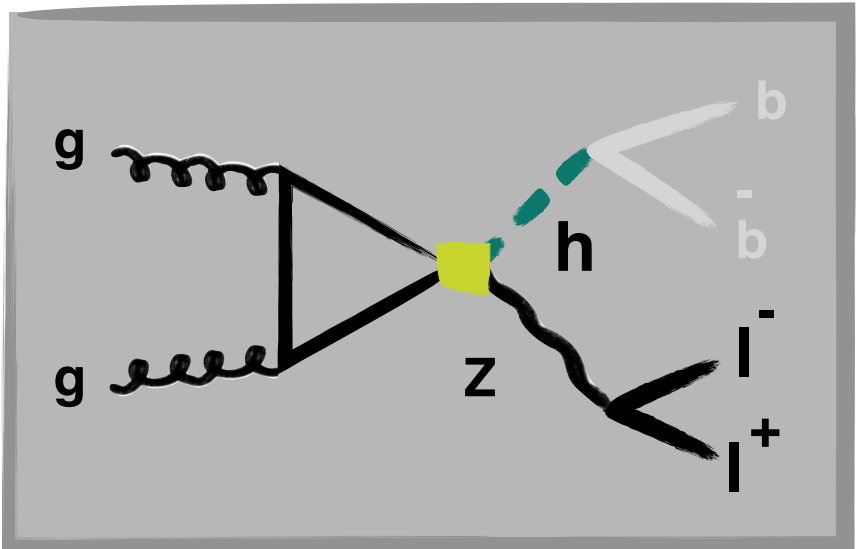
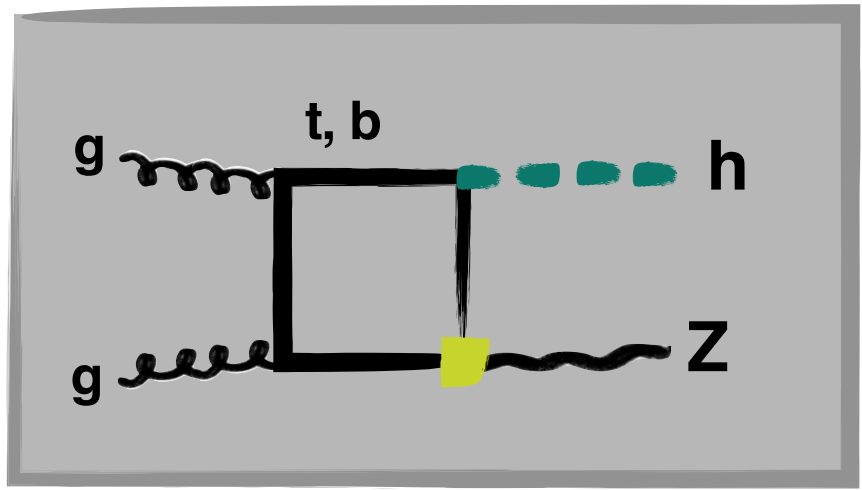
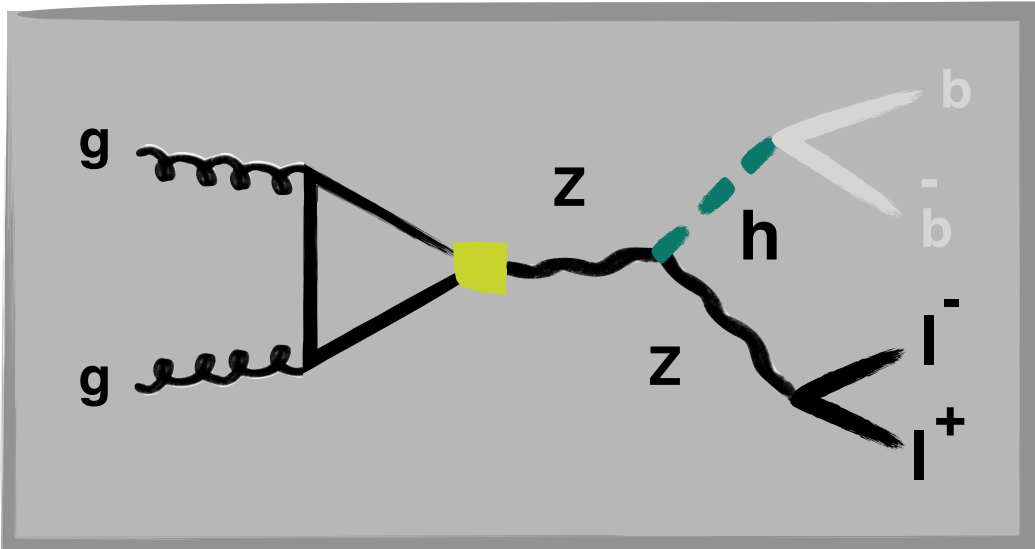
3.3 gg -initiated contributions

Corrections:



(A-type)

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Longitudinal contribution

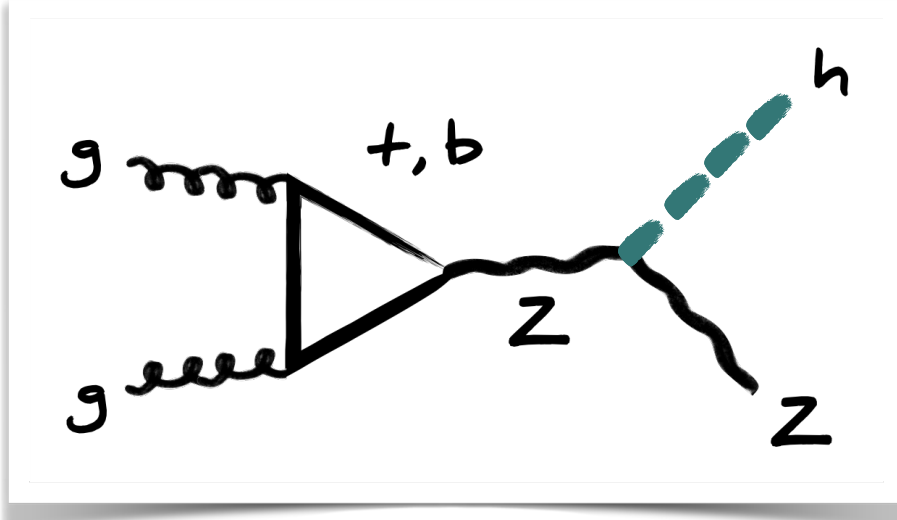
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3. Higher-Order Corrections

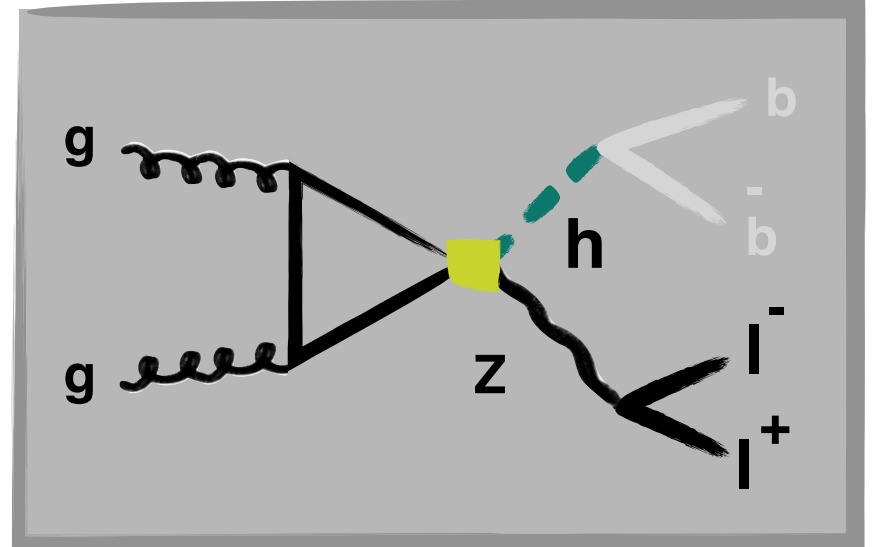
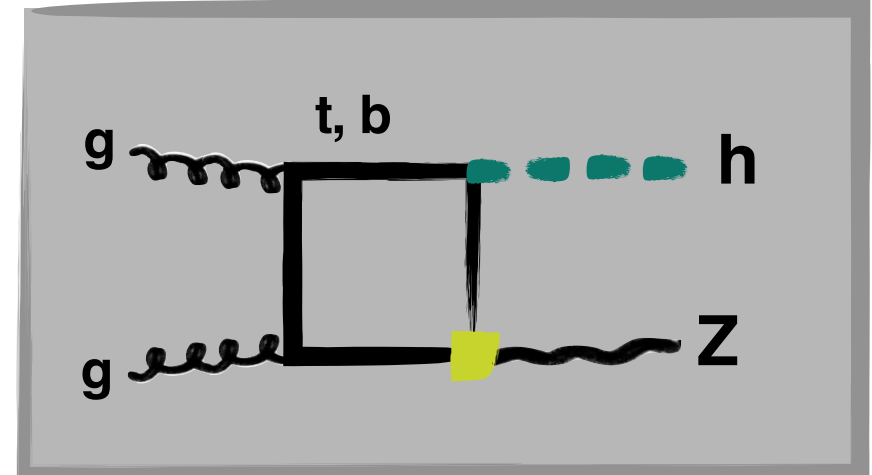
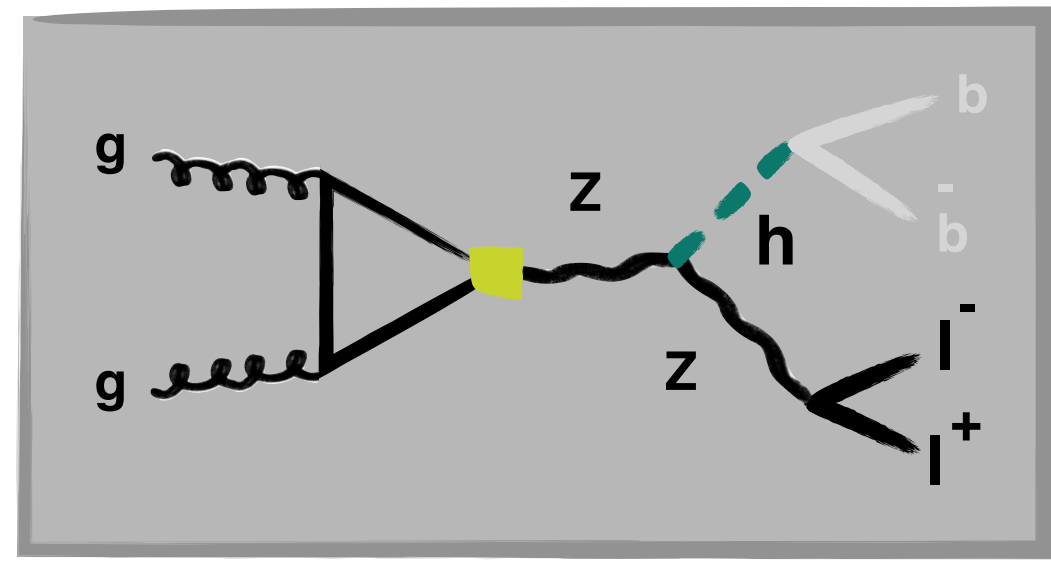
3.3 gg -initiated contributions

Corrections:



(A-type)

Diagrams:



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Only axial part contributes

Longitudinal contribution

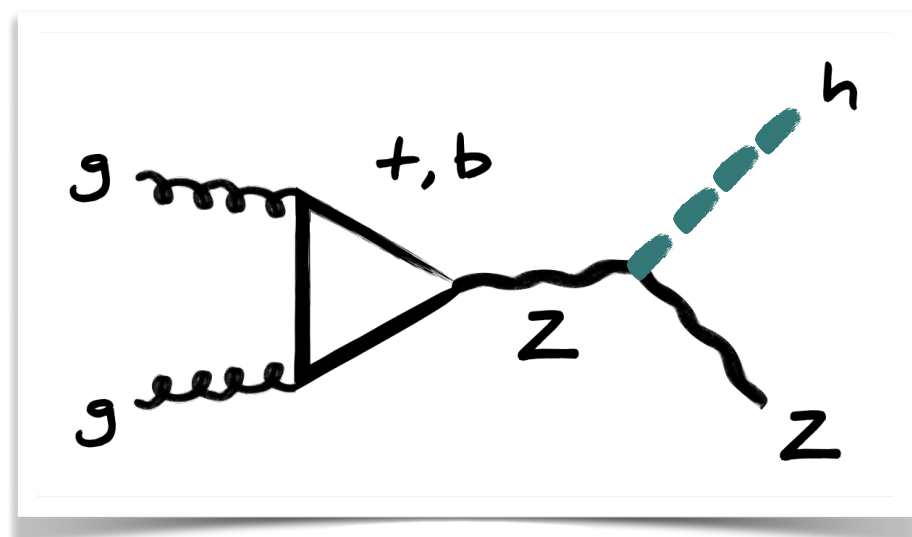
$$\mathcal{A}_{A0g2Z\Delta}^q (1_g^+, 2_g^+, 3_\ell^-, 4_\ell^+) = -\frac{2 [21] ([41] \langle 13 \rangle + [42] \langle 23 \rangle)}{\langle 12 \rangle} \left(1 - \frac{s_{12}}{m_Z^2} \right) \times m_q^2 C_0(s_{12}, 0, 0, m_q, m_q, m_q).$$

[1601.00658] (J.M. Campbell, R.K. Ellis, C. Williams)

3. Higher-Order Corrections

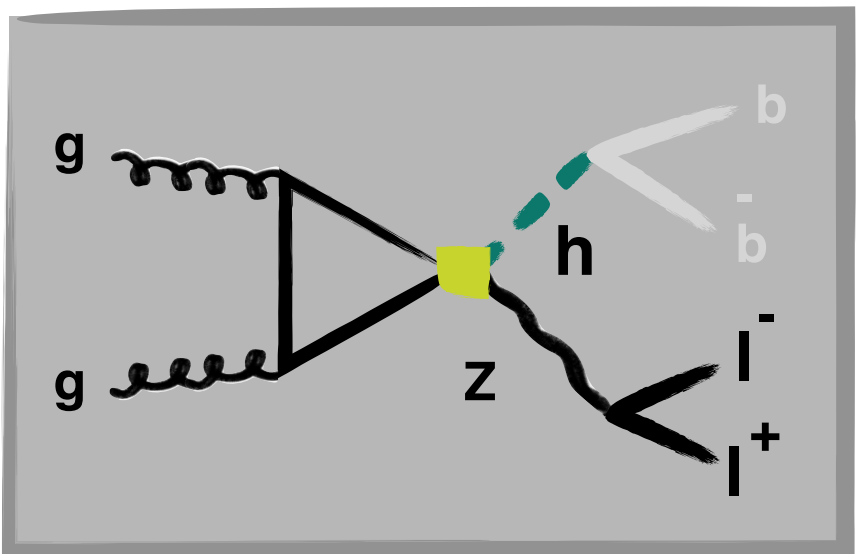
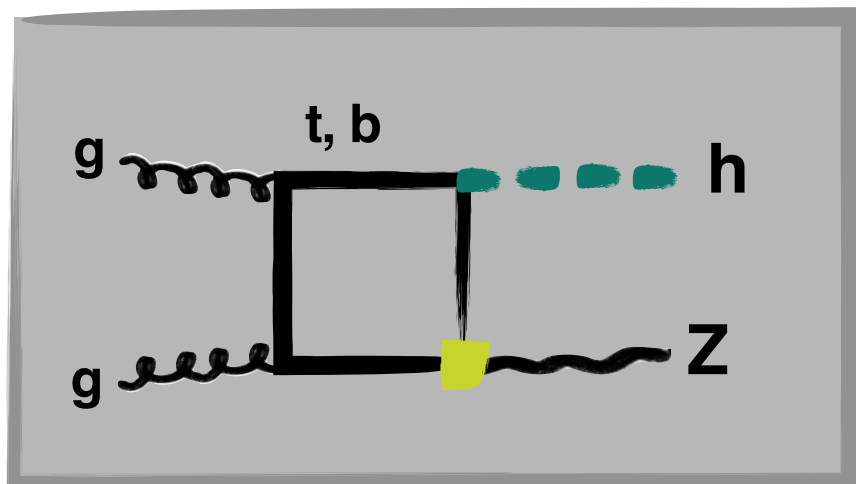
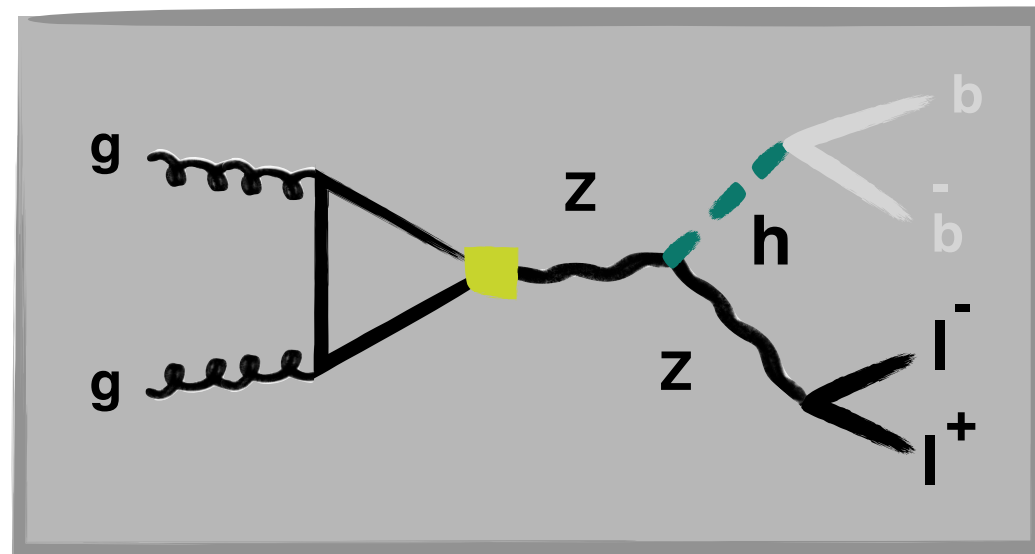
3.3 gg -initiated contributions

Corrections:



(A-type)

Diagrams:



We start with the **SM spinor-helicity amplitudes...**

$$A_{0g2Z} = \frac{\alpha_s^2}{8\pi^2 (C_A^2 - 1)^2} \sum_{h_g, h_\ell = \pm} \left| \sum_{q=t,b} \left(\mathcal{A}_\Delta^q + \sum_{s=\pm} \frac{m_q^2}{m_Z^2} \mathcal{A}_\square^{q,s} \right) \right|^2,$$

with

$$\mathcal{A}_\Delta^q = \frac{(g_{Zq}^- - g_{Zq}^+) g_{Z\ell}^{h_\ell} g_{hZZ}}{D_Z(s_{12}) D_Z(s_{34})} \mathcal{A}_{A0g2Z\Delta}^q (1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_\ell^{-h_\ell}),$$

Only axial part contributes

Longitudinal contribution

Anomaly cancellation in the **SM**:

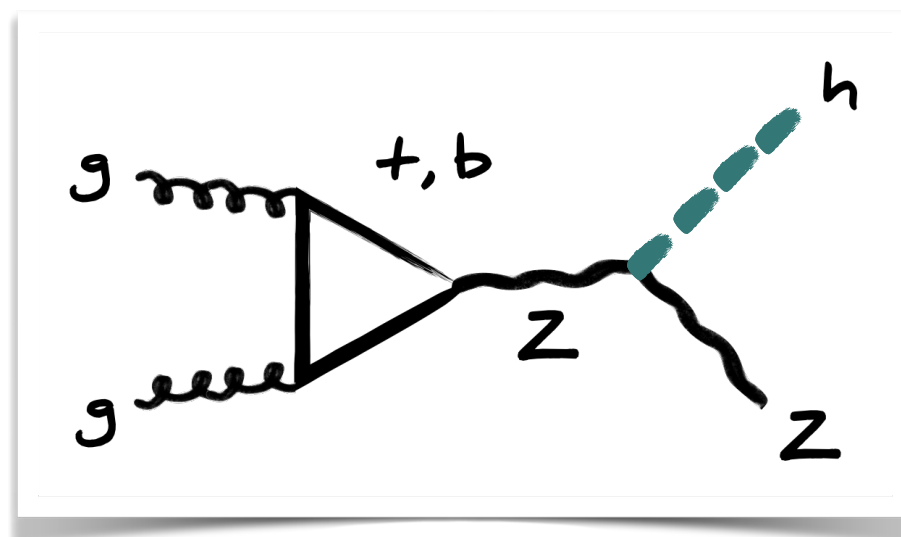
$$(g_{Zt}^- - g_{Zt}^+) = -(g_{Zb}^- - g_{Zb}^+),$$

$$\mathcal{A}_{A0g2Z\Delta}^q (1_g^+, 2_g^+, 3_\ell^-, 4_\ell^+) = -\frac{2 [21] ([41] \langle 13 \rangle + [42] \langle 23 \rangle)}{\langle 12 \rangle} \left(1 - \frac{s_{12}}{m_Z^2} \right) \times m_q^2 C_0(s_{12}, 0, 0, m_q, m_q, m_q).$$

3. Higher-Order Corrections

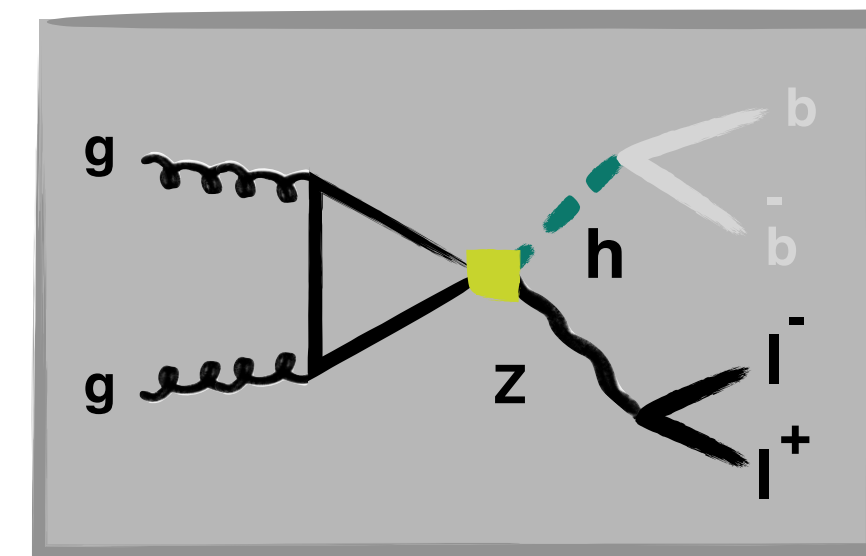
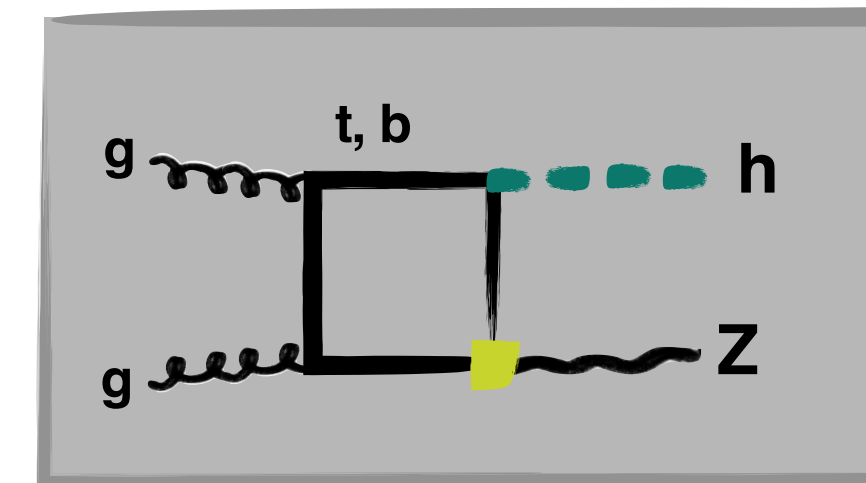
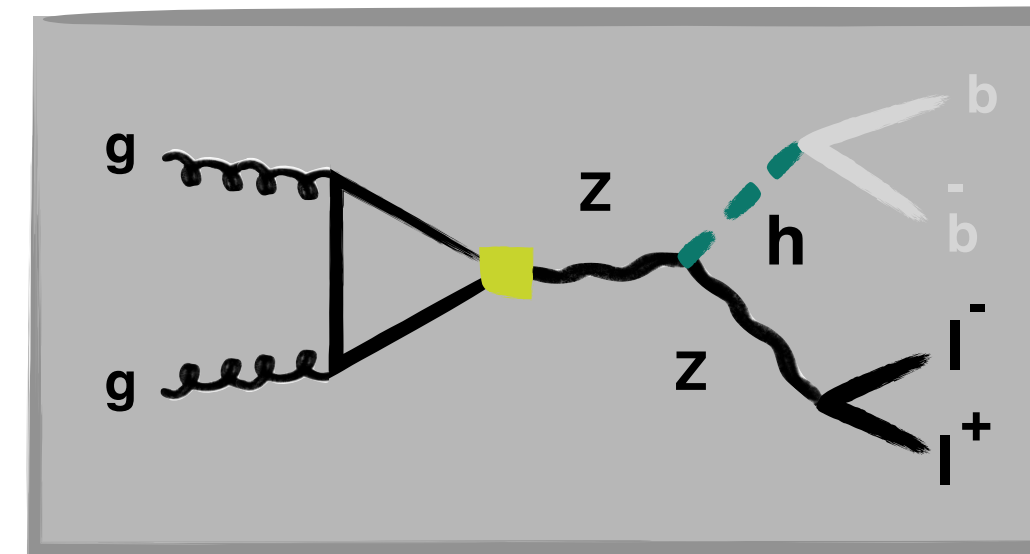
3.3 gg -initiated contributions

Corrections:



(A-type)

Diagrams:



We start with the **SM spinor-helicity amplitudes...**

$$A_{0g2Z} = \frac{\alpha_s^2}{8\pi^2 (C_A^2 - 1)^2} \sum_{h_g, h_\ell = \pm} \left| \sum_{q=t,b} \left(\mathcal{A}_\Delta^q + \sum_{s=\pm} \frac{m_q^2}{m_Z^2} \mathcal{A}_{\square}^{q,s} \right) \right|^2,$$

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Only axial part contributes

Longitudinal contribution

$$\mathcal{A}_{A0g2Z\Delta}^q \left(1_g^+, 2_g^+, 3_\ell^-, 4_\ell^+ \right) = -\frac{2 [21] ([41] \langle 13 \rangle + [42] \langle 23 \rangle)}{\langle 12 \rangle} \left(1 - \frac{s_{12}}{m_Z^2} \right) \times m_q^2 C_0(s_{12}, 0, 0, m_q, m_q, m_q).$$

Anomaly cancellation in the **SM**:

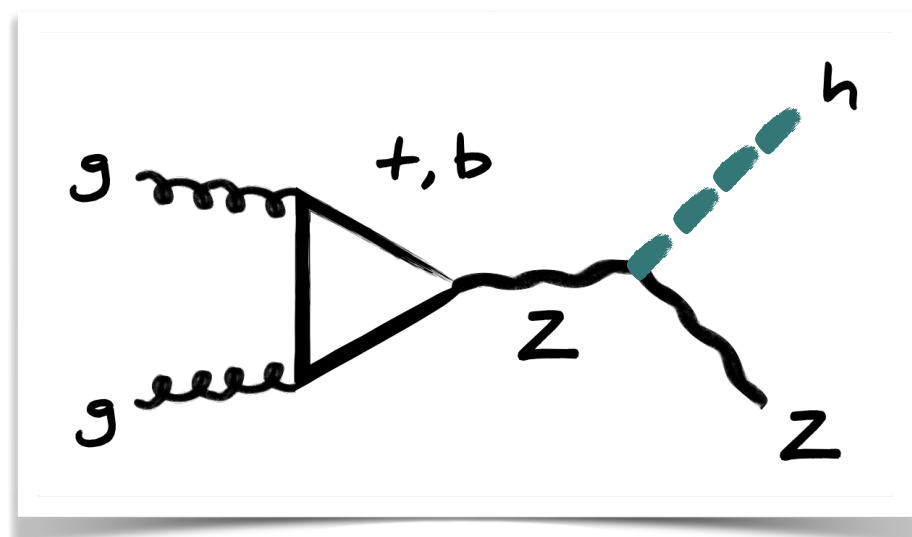
$$(g_{Zt}^- - g_{Zt}^+) = -(g_{Zb}^- - g_{Zb}^+),$$

$$\sum_{q=t,b} (g_{Zq}^- - g_{Zq}^+) \mathcal{A}_{A0g2Z\Delta}^q = (g_{Zt}^- - g_{Zt}^+) \left(\mathcal{A}_{A0g2Z\Delta}^t - \mathcal{A}_{A0g2Z\Delta}^b \right),$$

3. Higher-Order Corrections

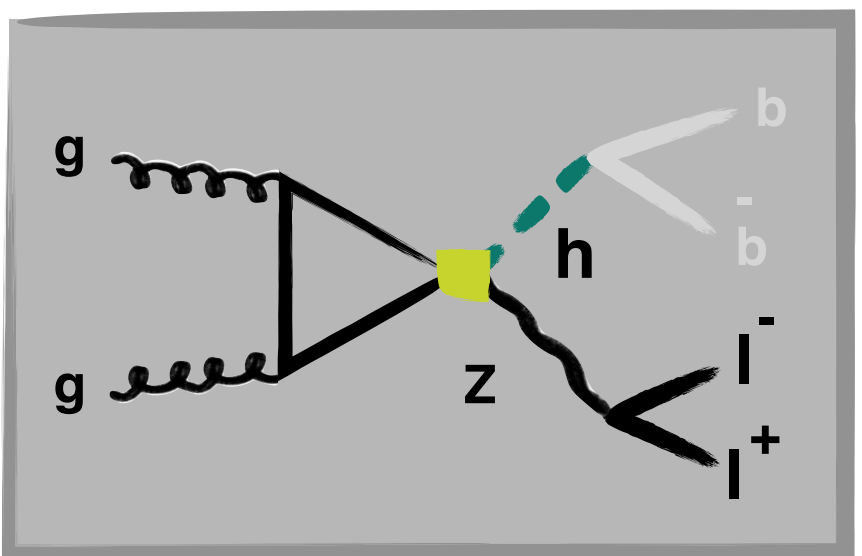
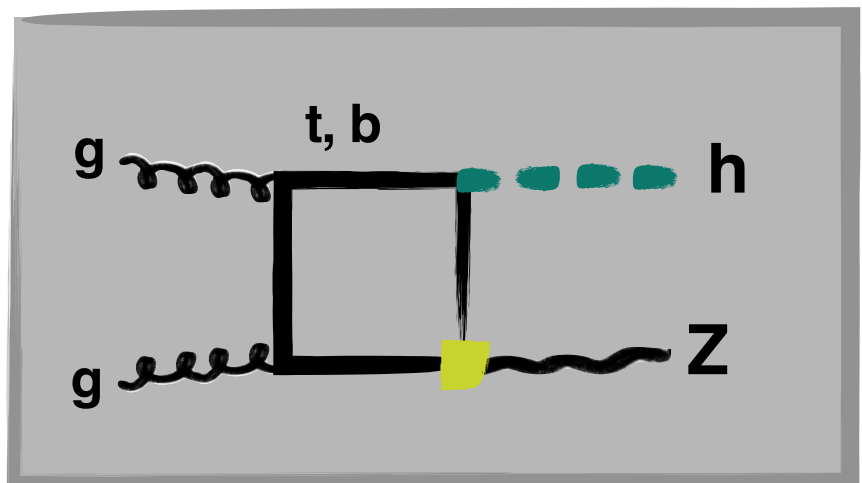
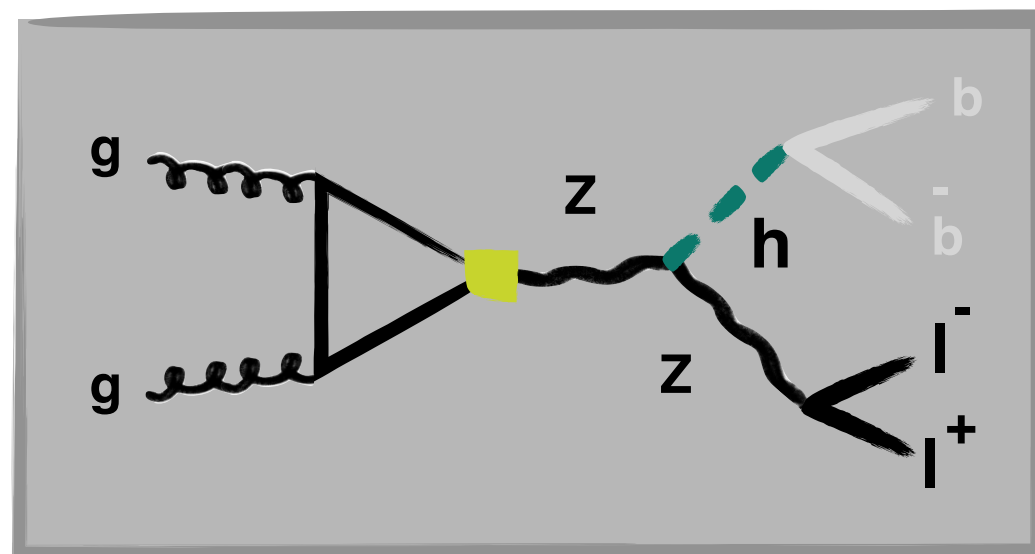
3.3 gg -initiated contributions

Corrections:



(A-type)

Diagrams:



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$$A_{0g2Z} = \frac{\alpha_s^2}{8\pi^2 (C_A^2 - 1)^2} \sum_{h_g, h_\ell = \pm} \left| \sum_{q=t,b} \left(\mathcal{A}_\Delta^q + \sum_{s=\pm} \frac{m_q^2}{m_Z^2} \mathcal{A}_\square^{q,s} \right) \right|^2,$$

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Only axial part contributes

Longitudinal contribution

$$\mathcal{A}_{A0g2Z\Delta}^q \left(1_g^+, 2_g^+, 3_\ell^-, 4_\ell^+ \right) = -\frac{2 [21] ([41] \langle 13 \rangle + [42] \langle 23 \rangle)}{\langle 12 \rangle} \left(1 - \frac{s_{12}}{m_Z^2} \right) \times m_q^2 C_0(s_{12}, 0, 0, m_q, m_q, m_q).$$

Anomaly cancellation in the **SM**:

$$(g_{Zt}^- - g_{Zt}^+) = -(g_{Zb}^- - g_{Zb}^+),$$

$$\sum_{q=t,b} (g_{Zq}^- - g_{Zq}^+) \mathcal{A}_{A0g2Z\Delta}^q = (g_{Zt}^- - g_{Zt}^+) \left(\mathcal{A}_{A0g2Z\Delta}^t - \mathcal{A}_{A0g2Z\Delta}^b \right),$$

→ how does this work in the **SMEFT**?

3. Higher-Order Corrections

3.3 gg -initiated contributions

3. Higher-Order Corrections

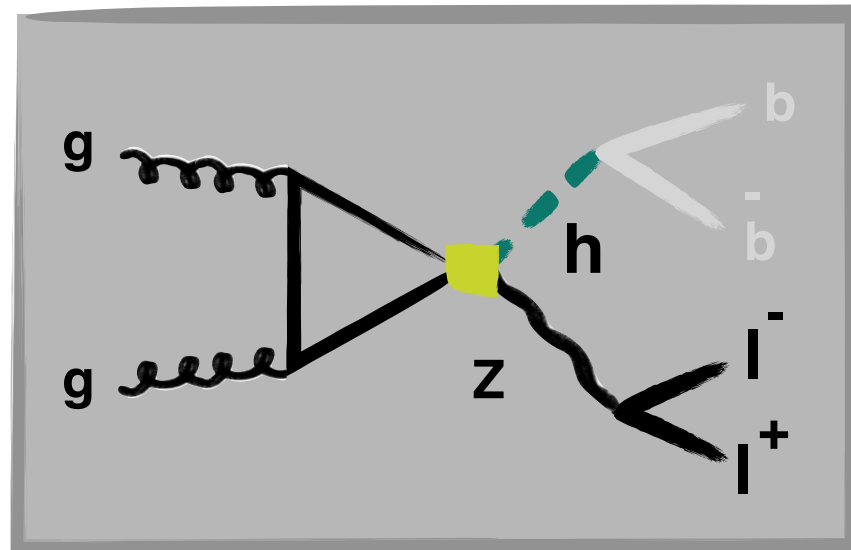
3.3 gg -initiated contributions

Anomaly cancellation in the **SMEFT**:

3. Higher-Order Corrections

3.3 gg -initiated contributions

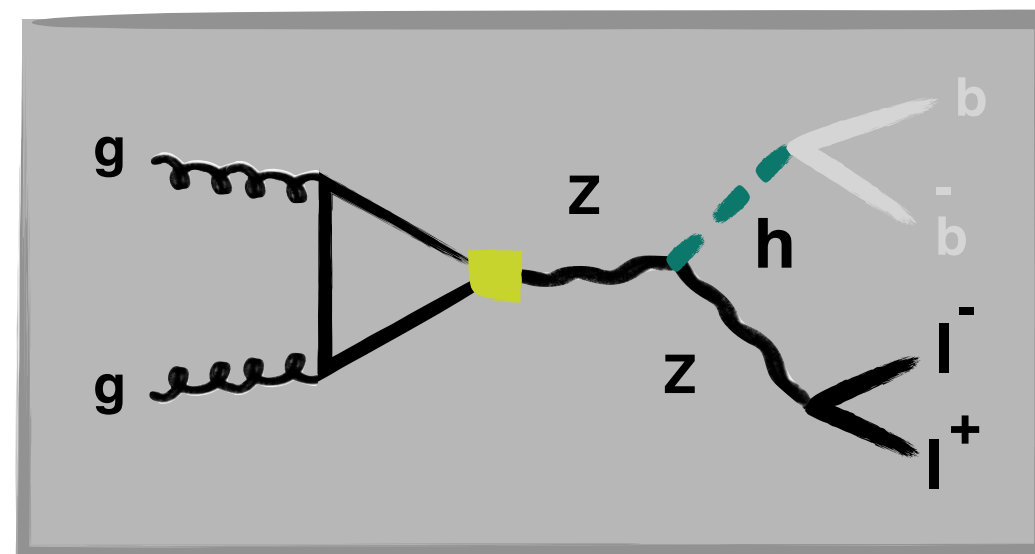
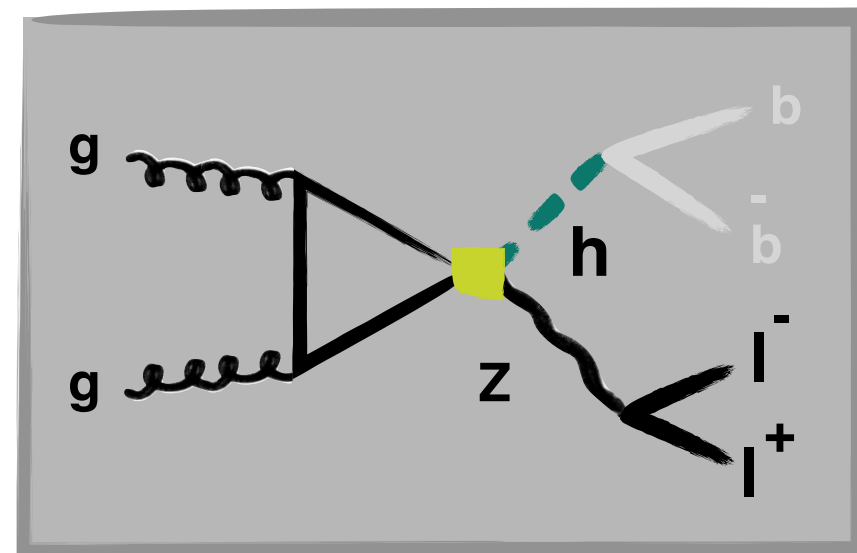
Anomaly cancellation in the **SMEFT**:



3. Higher-Order Corrections

3.3 gg -initiated contributions

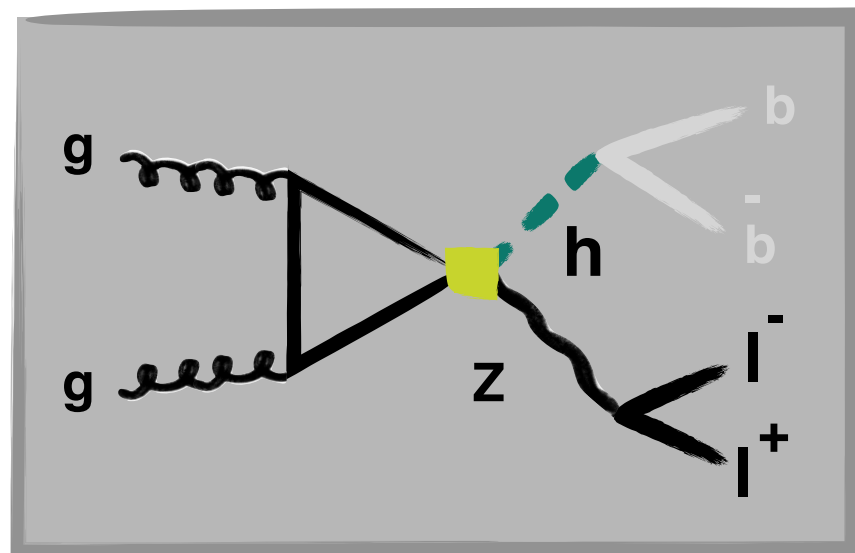
Anomaly cancellation in the **SMEFT**:



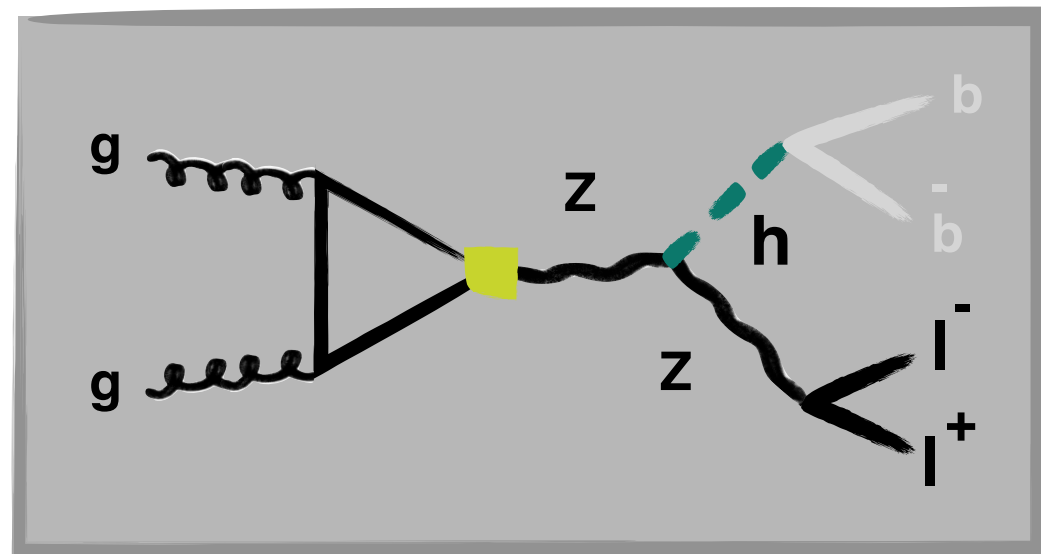
3. Higher-Order Corrections

3.3 gg -initiated contributions

Anomaly cancellation in the **SMEFT**:



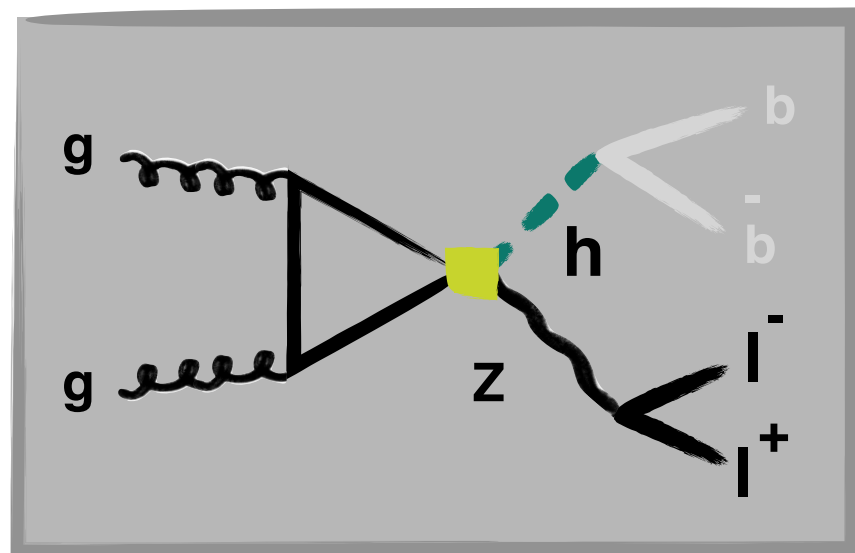
$$\frac{(\delta g_{hZq}^{(1)-} - \delta g_{hZq}^{(1+)}) g_{Z\ell}^{h\ell}}{D_Z(s_{34})} \cdot \frac{\mathcal{A}_{A0g2Z\Delta}^q(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell})}{1 - \frac{s_{12}}{m_Z^2}},$$



3. Higher-Order Corrections

3.3 gg -initiated contributions

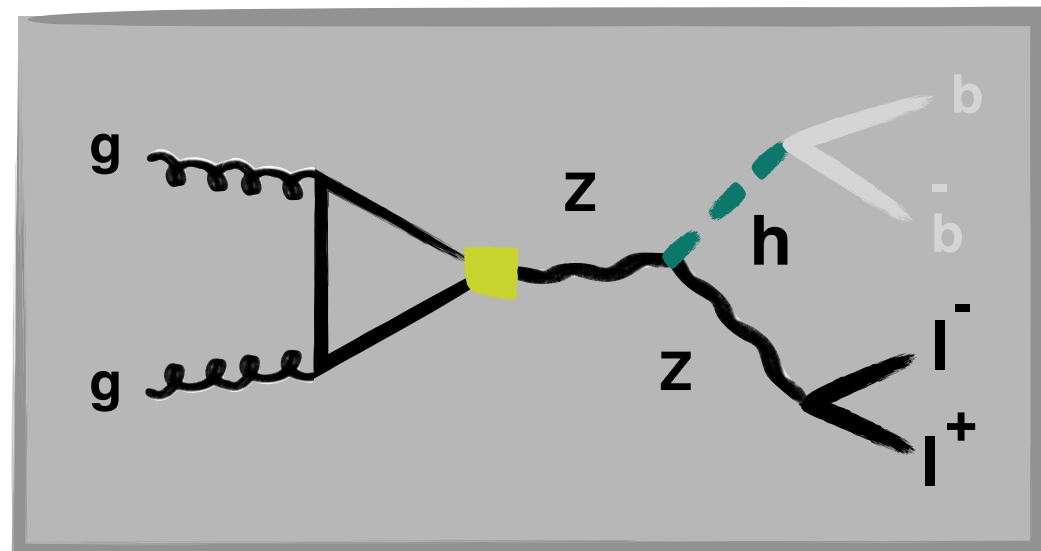
Anomaly cancellation in the **SMEFT**:



$$\frac{(\delta g_{hZq}^{(1)-} - \delta g_{hZq}^{(1)+}) g_{Z\ell}^{h\ell}}{D_Z(s_{34})}$$

$$\frac{\mathcal{A}_{A0g2Z\Delta}^q (1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell})}{1 - \frac{s_{12}}{m_Z^2}},$$

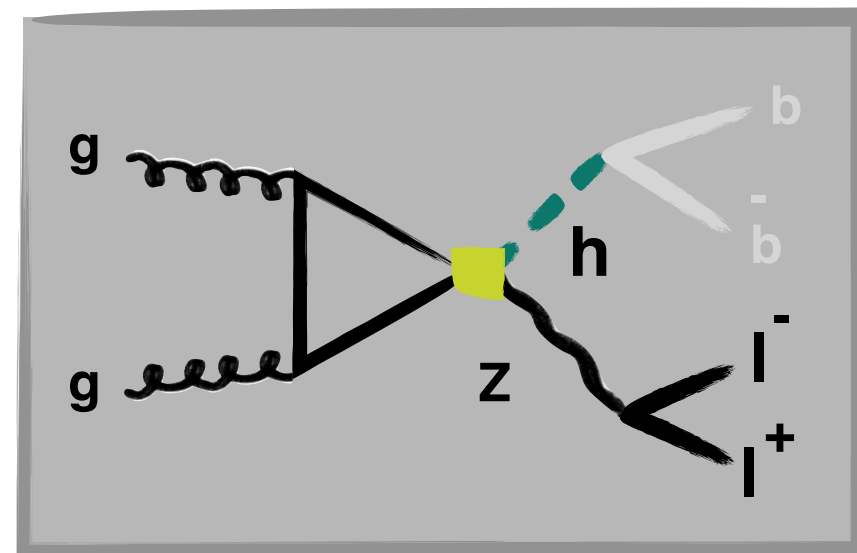
No longitudinal contribution
 (massless leptons)



3. Higher-Order Corrections

3.3 gg -initiated contributions

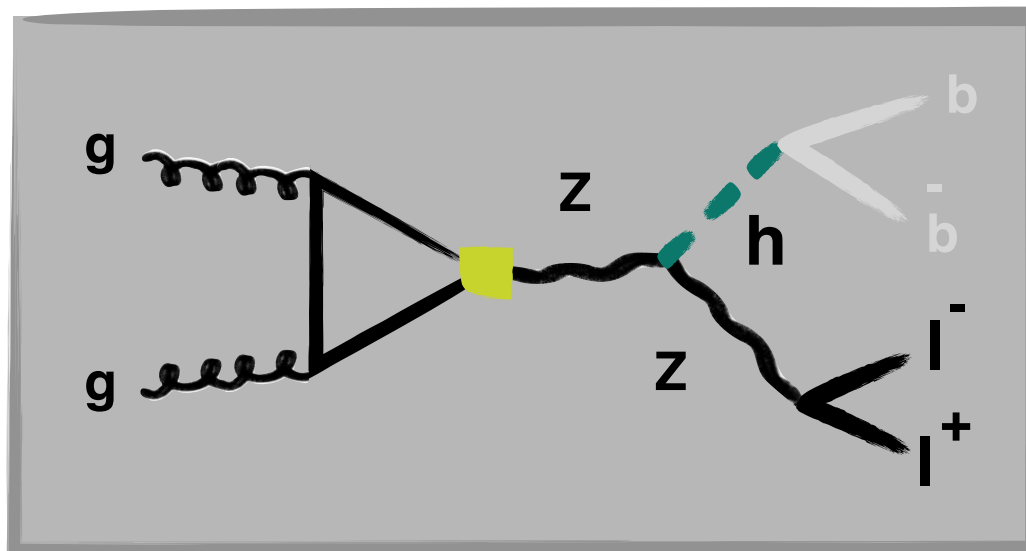
Anomaly cancellation in the **SMEFT**:



$$\frac{(\delta g_{hZq}^{(1)-} - \delta g_{hZq}^{(1)+}) g_{Z\ell}^{h\ell}}{D_Z(s_{34})}$$

$$\frac{\mathcal{A}_{A0g2Z\Delta}^q(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell})}{1 - \frac{s_{12}}{m_Z^2}},$$

No longitudinal contribution
(massless leptons)



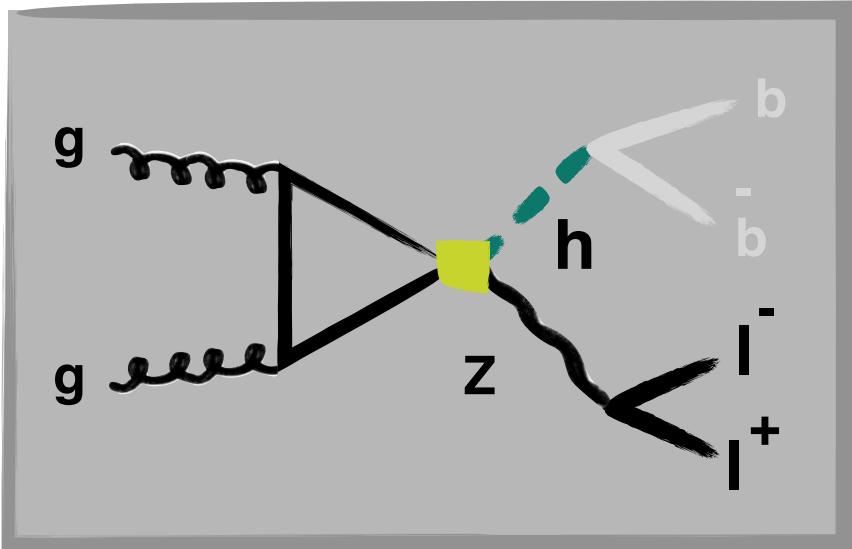
$$\frac{(\delta g_{Zq}^{(1)-} - \delta g_{Zq}^{(1)+}) g_{Z\ell}^{h\ell} g_{hZZ}}{D_Z(s_{12})D_Z(s_{34})}$$

$$\mathcal{A}_{A0g2Z\Delta}^q(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell})$$

3. Higher-Order Corrections

3.3 gg -initiated contributions

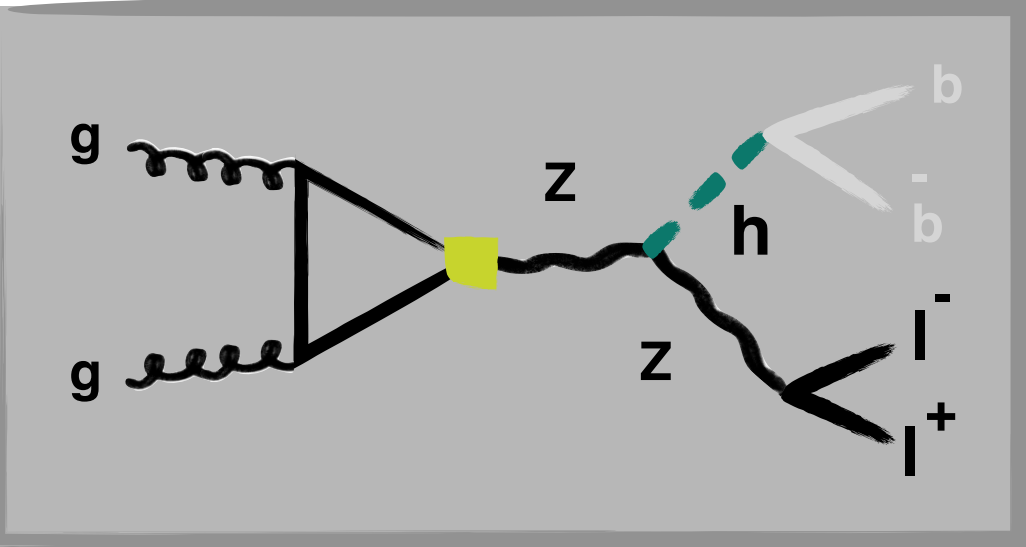
Anomaly cancellation in the **SMEFT**:



$$\frac{(\delta g_{hZq}^{(1)-} - \delta g_{hZq}^{(1)+}) g_{Z\ell}^{h\ell}}{D_Z(s_{34})}$$

$$\frac{\mathcal{A}_{A0g2Z\Delta}^q(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell})}{1 - \frac{s_{12}}{m_Z^2}}$$

No longitudinal contribution
(massless leptons)



$$\frac{(\delta g_{Zq}^{(1)-} - \delta g_{Zq}^{(1)+}) g_{Z\ell}^{h\ell} g_{hZZ}}{D_Z(s_{12})D_Z(s_{34})}$$

$$\mathcal{A}_{A0g2Z\Delta}^q(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell}) =$$

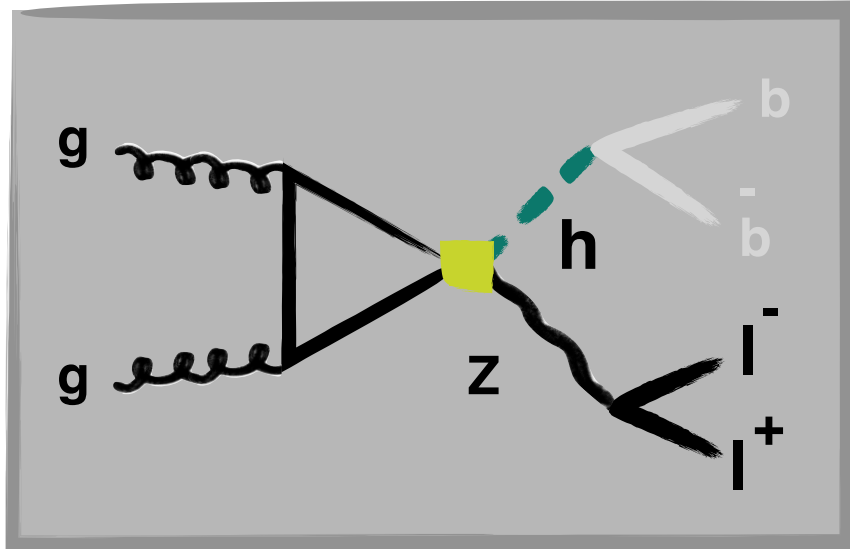
$$-\frac{(\delta g_{hZq}^{(1)-} - \delta g_{hZq}^{(1)+}) g_{Z\ell}^{h\ell}}{D_Z(s_{34})} \frac{1}{1 - \frac{s_{12}}{m_Z^2}}$$

$$\mathcal{A}_{A0g2Z\Delta}^q(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell})$$

3. Higher-Order Corrections

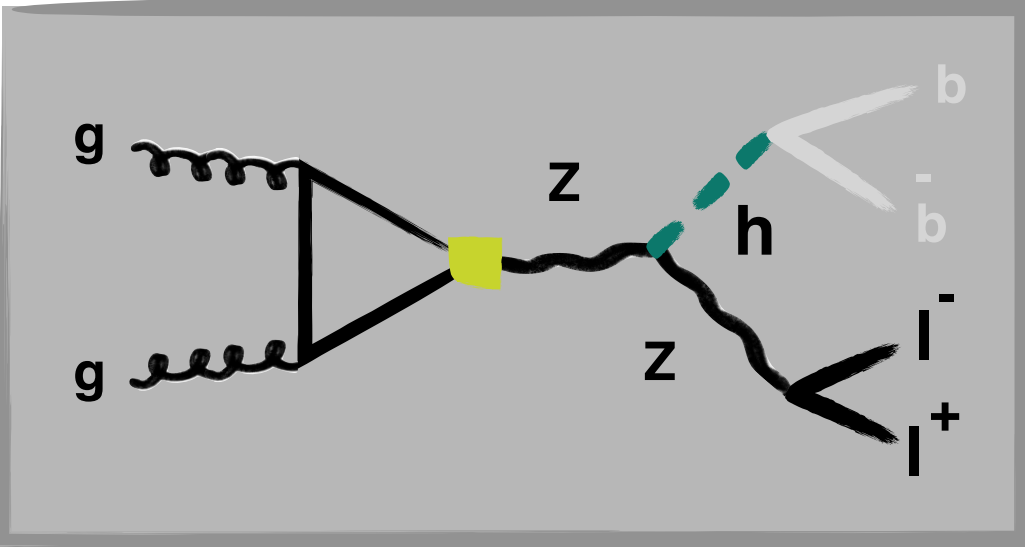
3.3 gg -initiated contributions

Anomaly cancellation in the **SMEFT**:



$$\frac{(\delta g_{hZq}^{(1)-} - \delta g_{hZq}^{(1)+}) g_{Z\ell}^{h\ell}}{D_Z(s_{34})} \mathcal{A}_{A0g2Z\Delta}^q \left(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell} \right) \frac{1}{1 - \frac{s_{12}}{m_Z^2}}$$

No longitudinal contribution
(massless leptons)

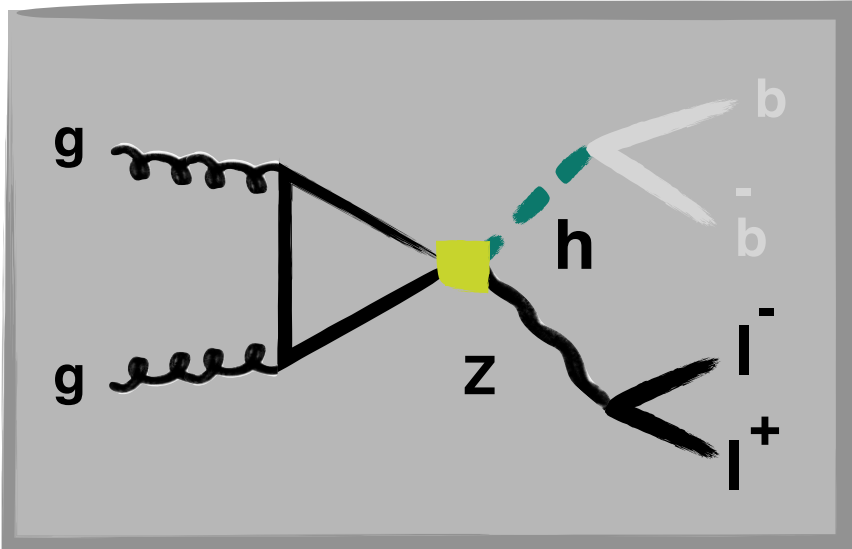


$$\frac{(\delta g_{Zq}^{(1)-} - \delta g_{Zq}^{(1)+}) g_{Z\ell}^{h\ell} g_{hZZ}}{D_Z(s_{12})D_Z(s_{34})} \mathcal{A}_{A0g2Z\Delta}^q \left(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell} \right) = \frac{(\delta g_{hZq}^{(1)-} - \delta g_{hZq}^{(1)+}) g_{Z\ell}^{h\ell}}{D_Z(s_{34})} \frac{1}{1 - \frac{s_{12}}{m_Z^2}} \mathcal{A}_{A0g2Z\Delta}^q \left(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell} \right)$$

3. Higher-Order Corrections

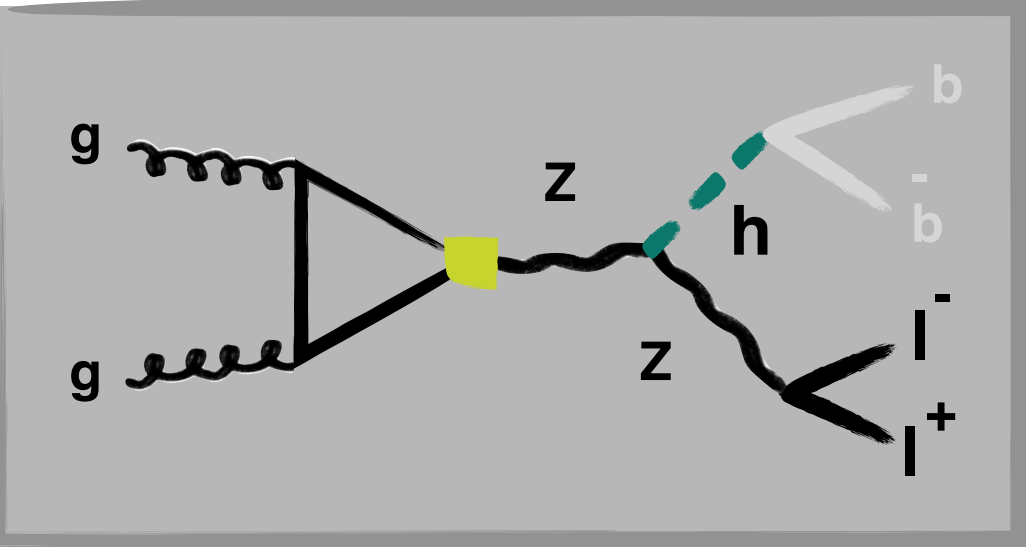
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Anomaly cancellation in the **SMEFT**:



$$\frac{(\delta g_{hZq}^{(1)-} - \delta g_{hZq}^{(1+)}) g_{Z\ell}^{h\ell}}{D_Z(s_{34})} \mathcal{A}_{A0g2Z\Delta}^q \left(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell} \right) \frac{1 - \frac{s_{12}}{m_Z^2}}{1 - \frac{s_{12}}{m_Z^2}}$$

No longitudinal contribution (massless leptons)



$$\frac{(\delta g_{Zq}^{(1)-} - \delta g_{Zq}^{(1+)}) g_{Z\ell}^{h\ell} g_{hZZ}}{D_Z(s_{12})D_Z(s_{34})} \mathcal{A}_{A0g2Z\Delta}^q \left(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell} \right) = \frac{(\delta g_{hZq}^{(1)-} - \delta g_{hZq}^{(1+)}) g_{Z\ell}^{h\ell}}{D_Z(s_{34})} \frac{1}{1 - \frac{s_{12}}{m_Z^2}} \mathcal{A}_{A0g2Z\Delta}^q \left(1_g^{h_g}, 2_g^{h_g}, 3_\ell^{h_\ell}, 4_{\bar{\ell}}^{-h_\ell} \right)$$

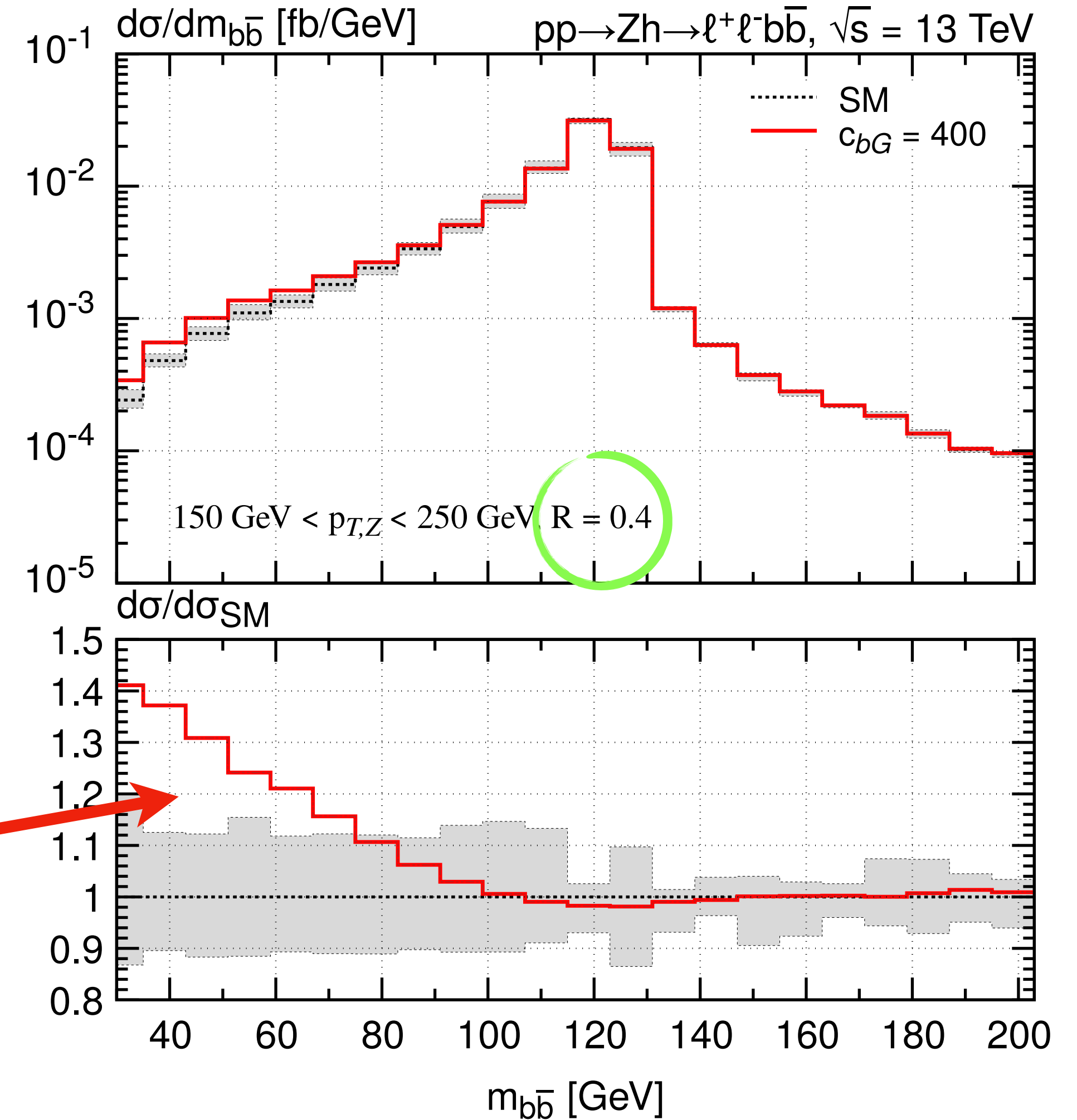
The SMEFT is **anomaly-free** (up to spurious “irrelevant” anomalies that can be subtracted).

→ Great advantage e.g. with respect to the κ framework.

[2012.13989] (F. Feruglio)

[2012.07740] (Q. Bonnefoy, L. Di Luzio, Ch. Grojean, A. Paul, A.N. Rossia)

Phenomenology analysis

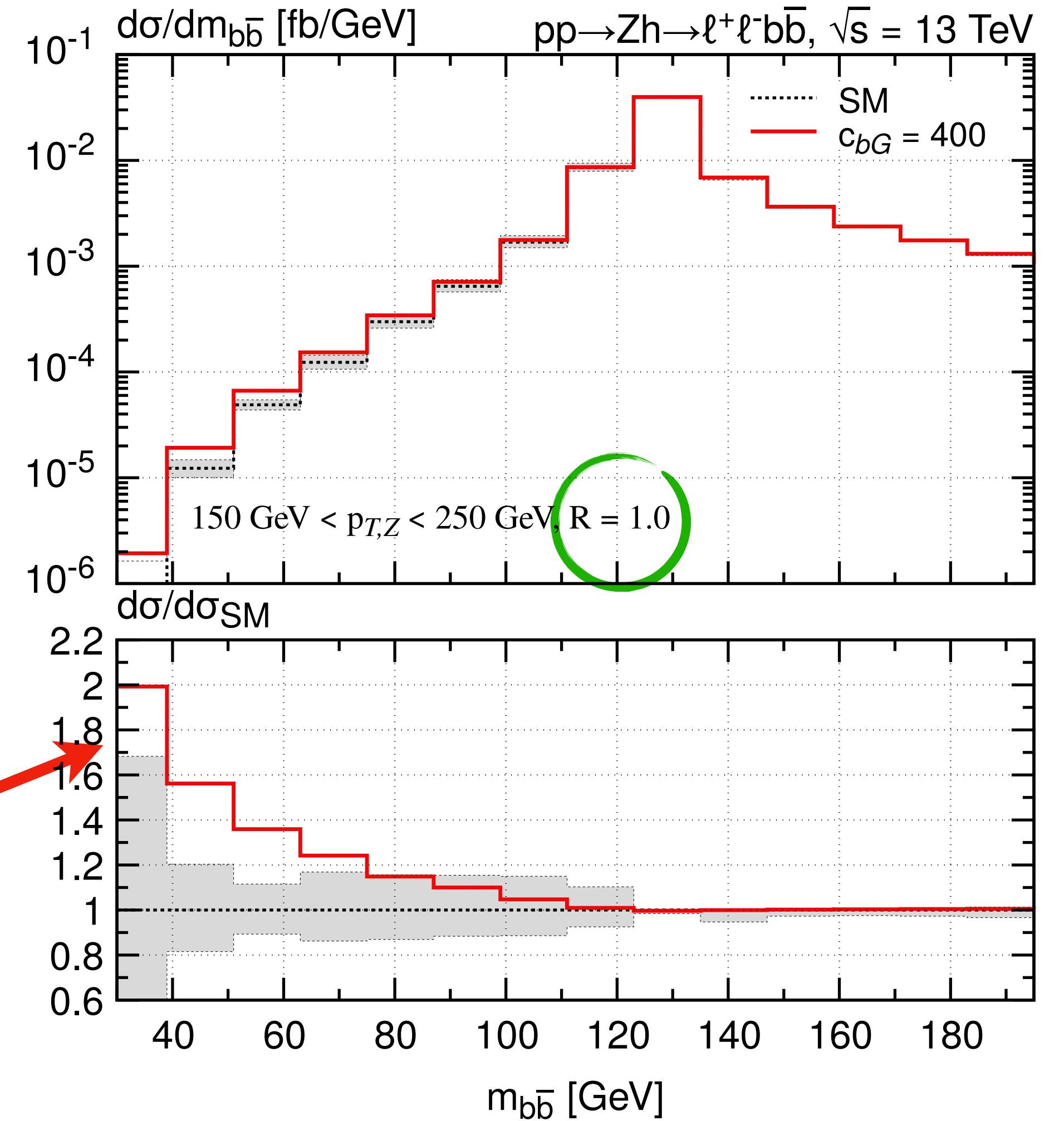


extra gluon emission in leading-order Q_{bG} contribution tends to reduce dibottom invariant mass relative to SM

Phenomenology analysis



size of effect depends on radius parameter R used to reconstruct anti- k_t jets



4. Phenomenology

4.1 Matrix element library

4. Phenomenology

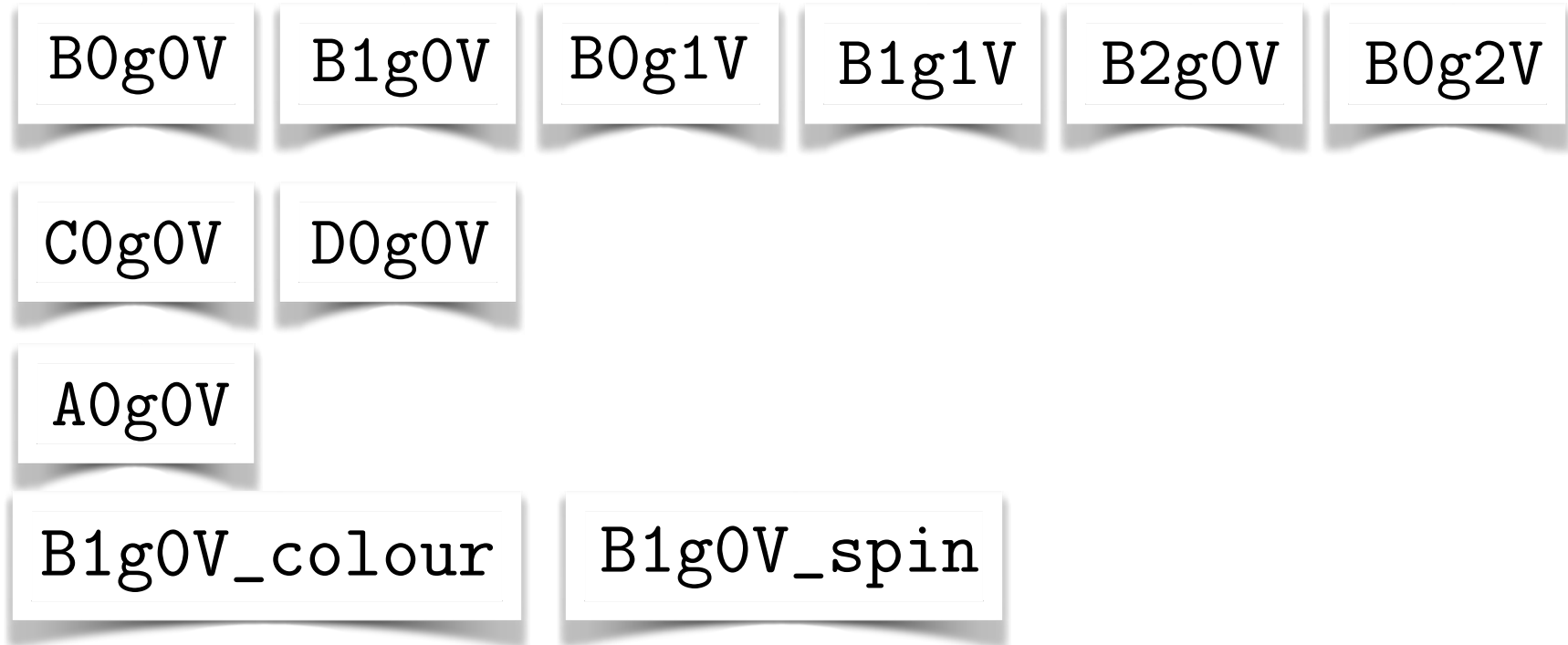
4.1 Matrix element library

We implemented all squared matrix elements in a **Fortran library** using spinor helicity amplitudes...

4. Phenomenology

4.1 Matrix element library

We implemented all squared matrix elements in a **Fortran library** using spinor helicity amplitudes...



$$2s_b \mathcal{B}_{ij} = -N \sum_{\substack{\text{spins} \\ \text{colours}}} \mathcal{M}_{\{c_k\}} \left(\mathcal{M}_{\{c_k\}}^\dagger \right)_{\substack{c_i \rightarrow c'_i \\ c_j \rightarrow c'_j}} T_{c_i, c'_i}^a T_{c_j, c'_j}^a.$$

$$\mathcal{B}_j^{\mu\nu} = N \sum_{\{i, s_j, s'_j\}} \mathcal{M}(\{i\}, s_j) \mathcal{M}^\dagger(\{i\}, s'_j) (\epsilon_{s_j}^\mu)^* \epsilon_{s'_j}^\nu,$$

4. Phenomenology

4.1 Matrix element library

We implemented all squared matrix elements in a **Fortran library** using spinor helicity amplitudes...

B0g0V	B1g0V	B0g1V	B1g1V	B2g0V	B0g2V
C0g0V	D0g0V				
A0g0V					
B1g0V_colour	B1g0V_spin				

$$2s_b \mathcal{B}_{ij} = -N \sum_{\substack{\text{spins} \\ \text{colours}}} \mathcal{M}_{\{c_k\}} \left(\mathcal{M}_{\{c_k\}}^\dagger \right)_{\substack{c_i \rightarrow c'_i \\ c_j \rightarrow c'_j}} T_{c_i, c'_i}^a T_{c_j, c'_j}^a$$

$$\mathcal{B}_j^{\mu\nu} = N \sum_{\{i, s_j, s'_j\}} \mathcal{M}(\{i\}, s_j) \mathcal{M}^\dagger(\{i\}, s'_j) (\epsilon_{s_j}^\mu)^* \epsilon_{s'_j}^\nu$$

```
! =====
! Standard Model
! =====
! ( 1q-, 2g-, 3qb+; 4l-, 5lb+ )
! Particles before the ";" are incoming, after outgoing.
! This corresponds to the LL case.
complex(8) function B1g0V_Hel_SM_LL_minus(i1,i2,i3,i4,i5,K)
  integer, intent(in) :: i1,i2,i3,i4,i5
  type(Event_t), intent(in) :: K
  type(Constants_t) :: C

  ! Get Constants from K
  C = K%C

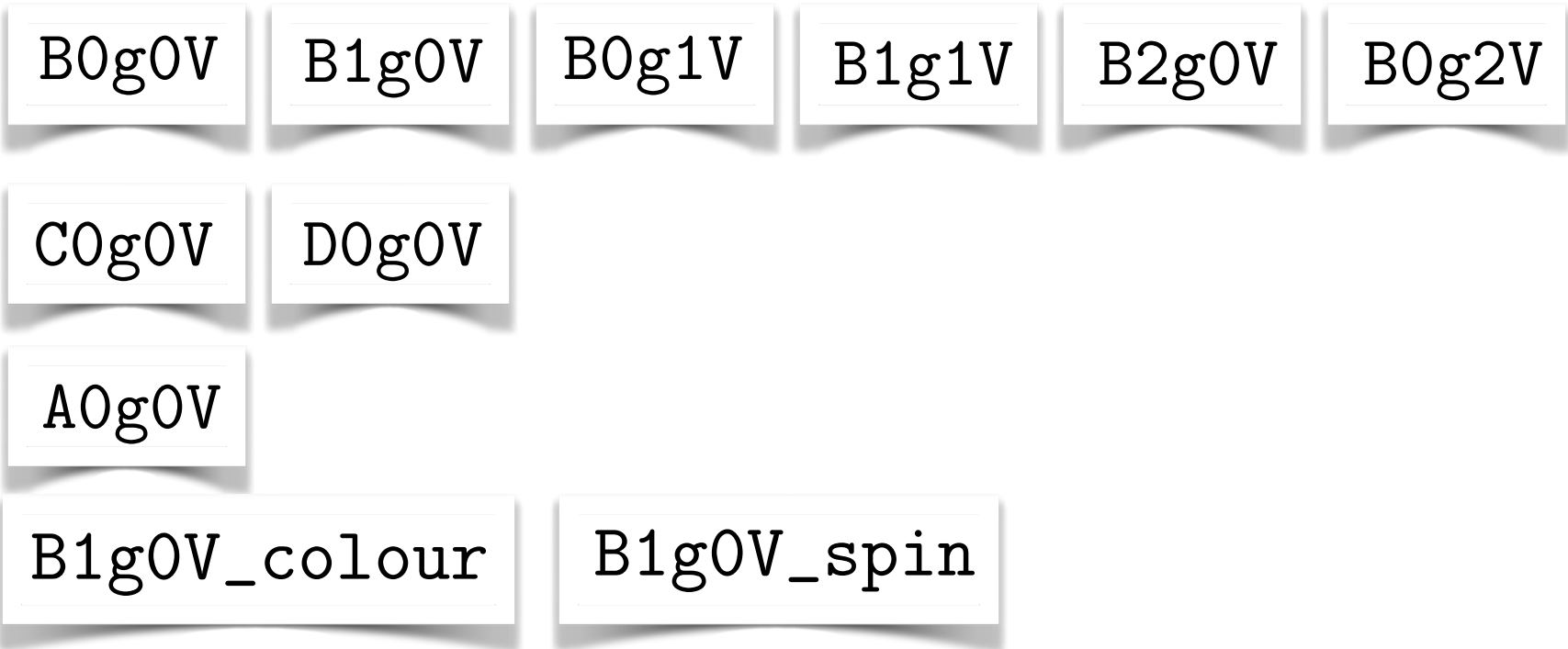
  ! The helicity amplitude
  B1g0V_Hel_SM_LL_minus = K%Za(i3,i4)/K%Za(i1,i2)/K%Za(i2,i3) &
    * (K%Za(i1,i3)*K%Zb(i5,i1)+K%Za(i2,i3)*K%Zb(i5,i2))

end function B1g0V_Hel_SM_LL_minus
! =====
```

4. Phenomenology

4.1 Matrix element library

We implemented all squared matrix elements in a **Fortran library** using spinor helicity amplitudes...



$$2s_b \mathcal{B}_{ij} = -N \sum_{\substack{\text{spins} \\ \text{colours}}} \mathcal{M}_{\{c_k\}} \left(\mathcal{M}_{\{c_k\}}^\dagger \right)_{\substack{c_i \rightarrow c'_i \\ c_j \rightarrow c'_j}} T_{c_i, c'_i}^a T_{c_j, c'_j}^a$$

$$\mathcal{B}_j^{\mu\nu} = N \sum_{\{i, s_j, s'_j\}} \mathcal{M}(\{i\}, s_j) \mathcal{M}^\dagger(\{i\}, s'_j) (\epsilon_{s_j}^\mu)^* \epsilon_{s'_j}^\nu$$

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  C = K%C

  ! The helicity amplitude
  B1g0V_Hel_SM_LL_minus = K%Za(i3,i4)/K%Za(i1,i2)/K%Za(i2,i3) &
    * (K%Za(i1,i3)*K%Zb(i5,i1)+K%Za(i2,i3)*K%Zb(i5,i2))

end function B1g0V_Hel_SM_LL_minus
! =====
```

B1g0Z amplitude
we saw earlier

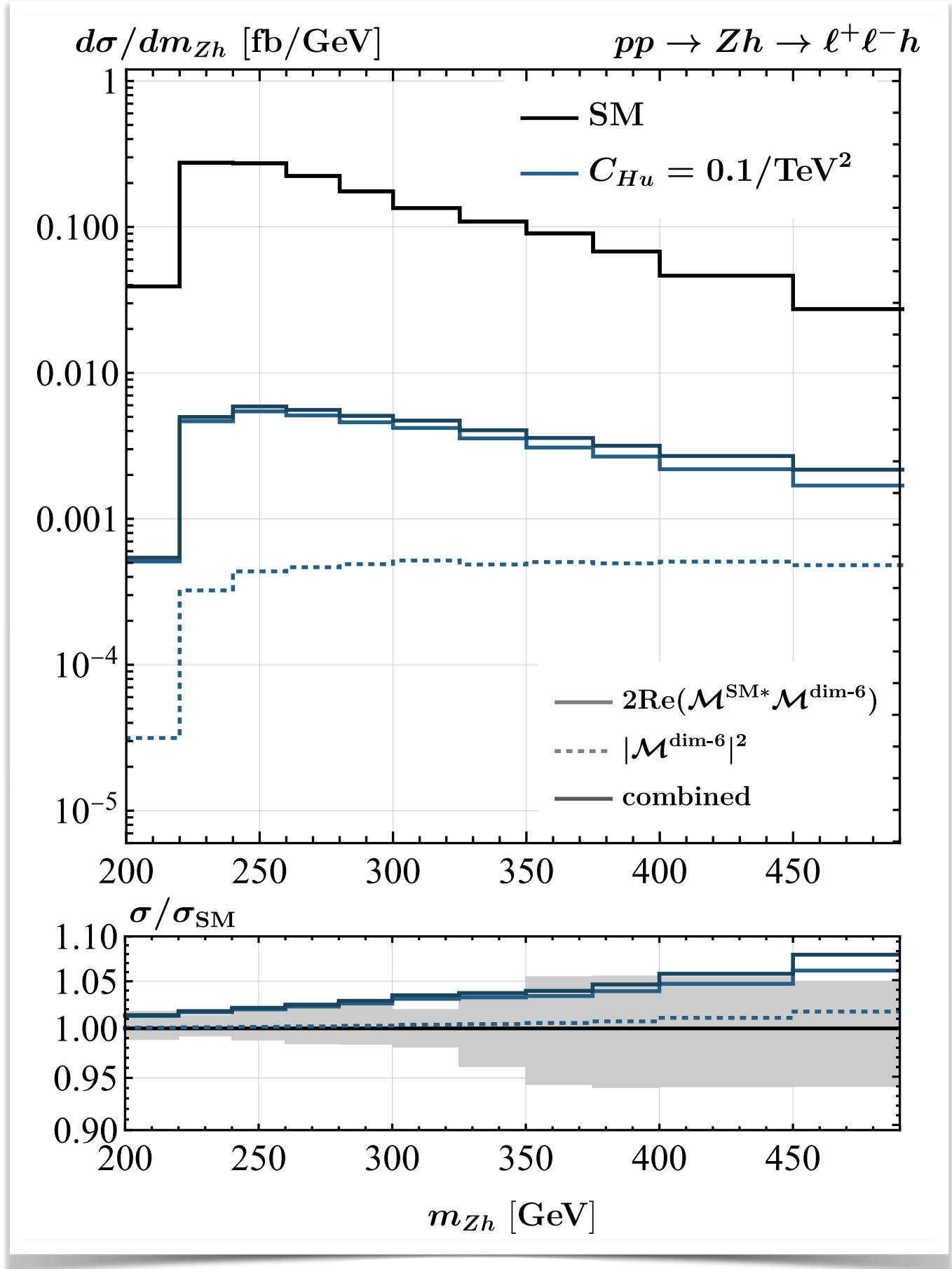
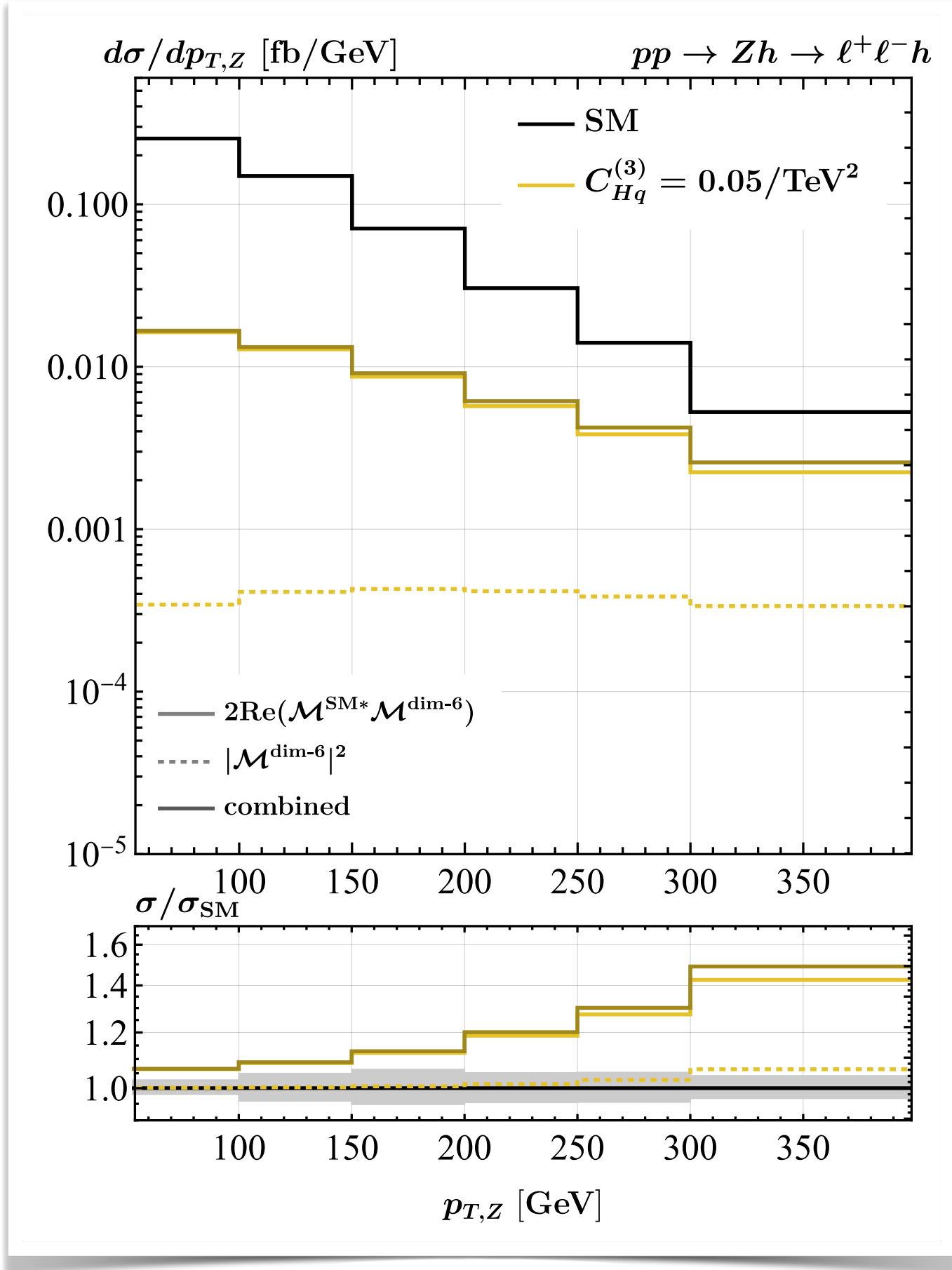
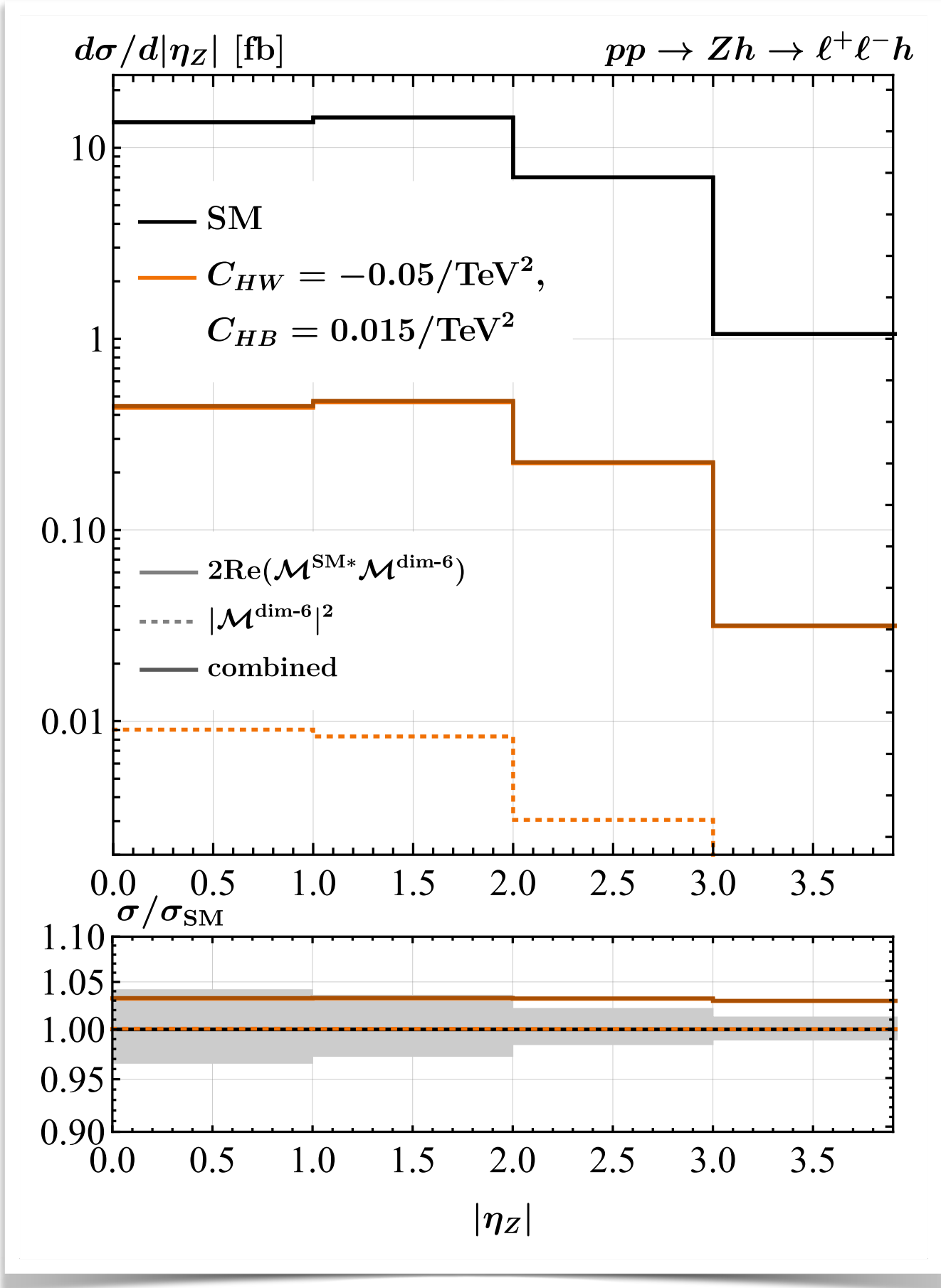
<13>

4. Phenomenology

4.3 Spectra

4. Phenomenology

4.3 Spectra

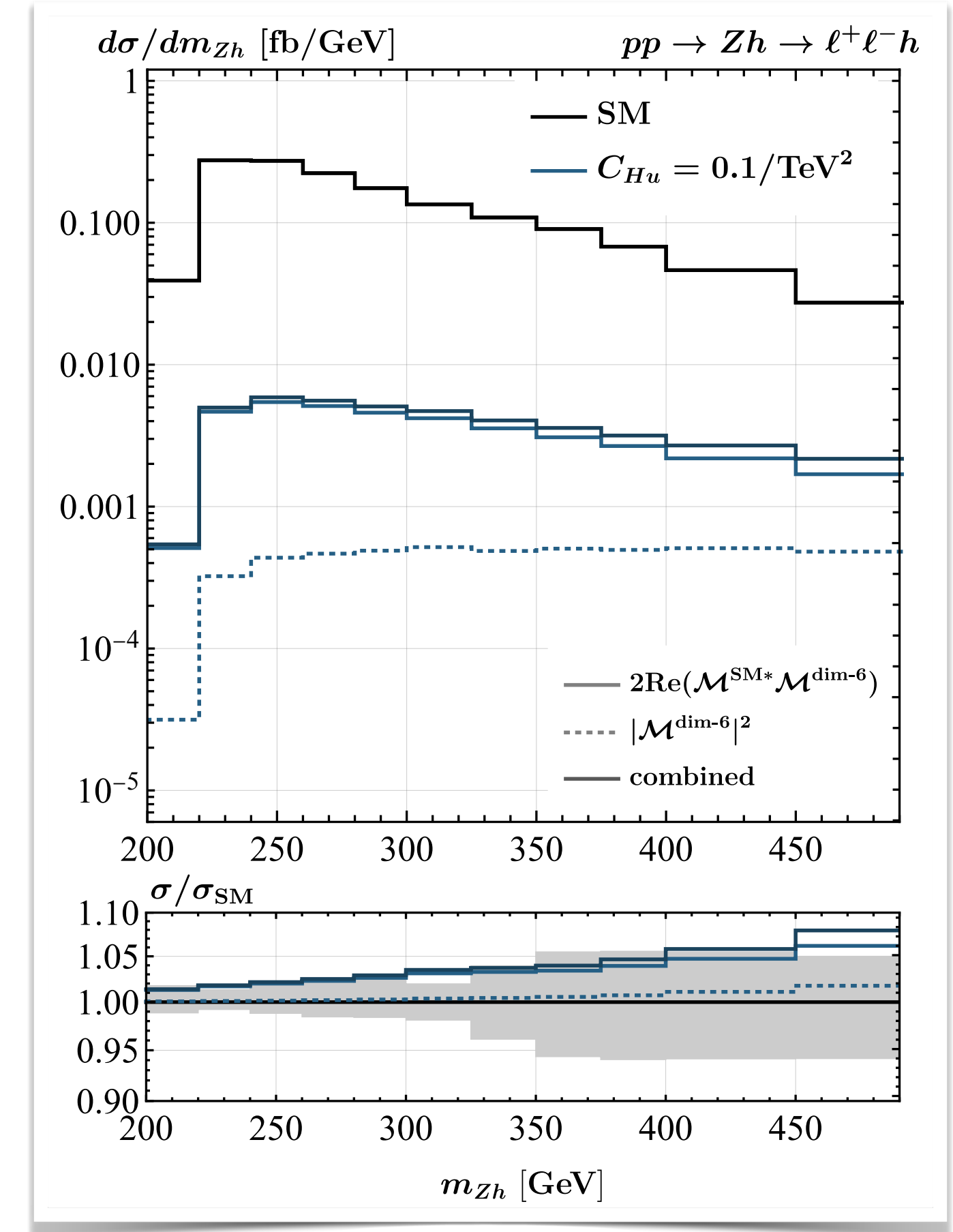
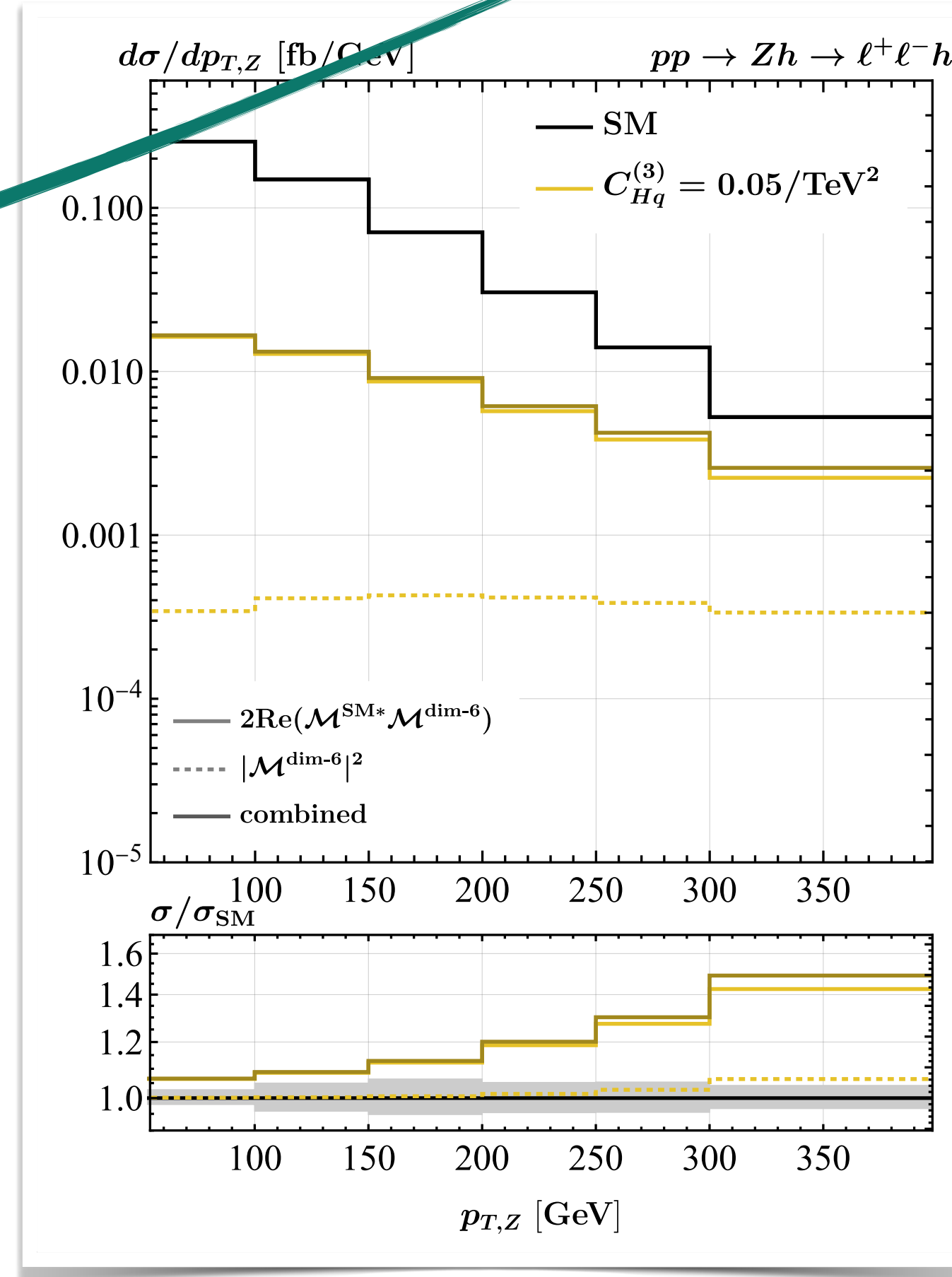
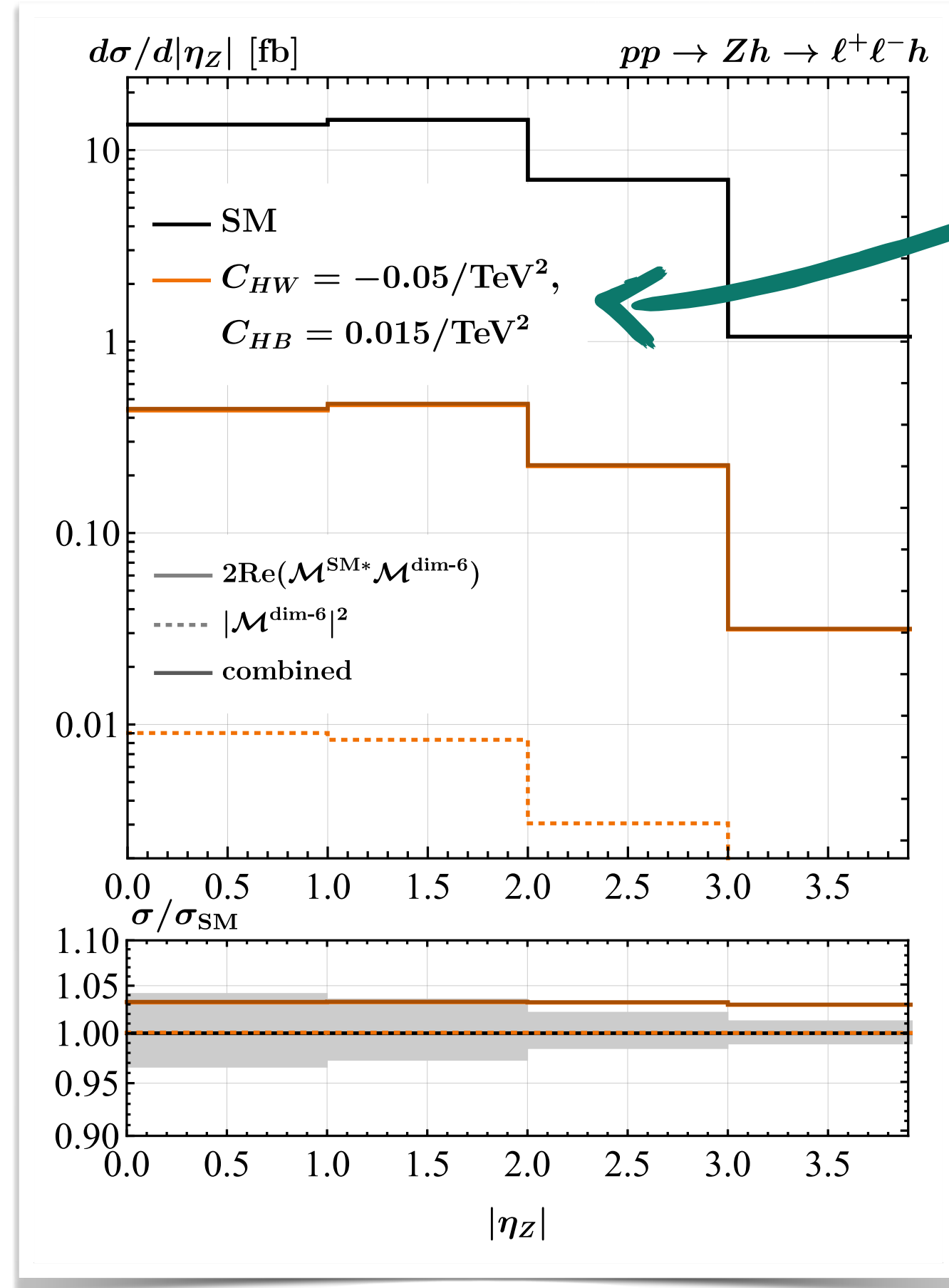


4. Phenomenology

4.3 Spectra

[2311.06107] (R. Gauld, U. Haisch, LS)

Parameter benchmarks discussed in our paper.

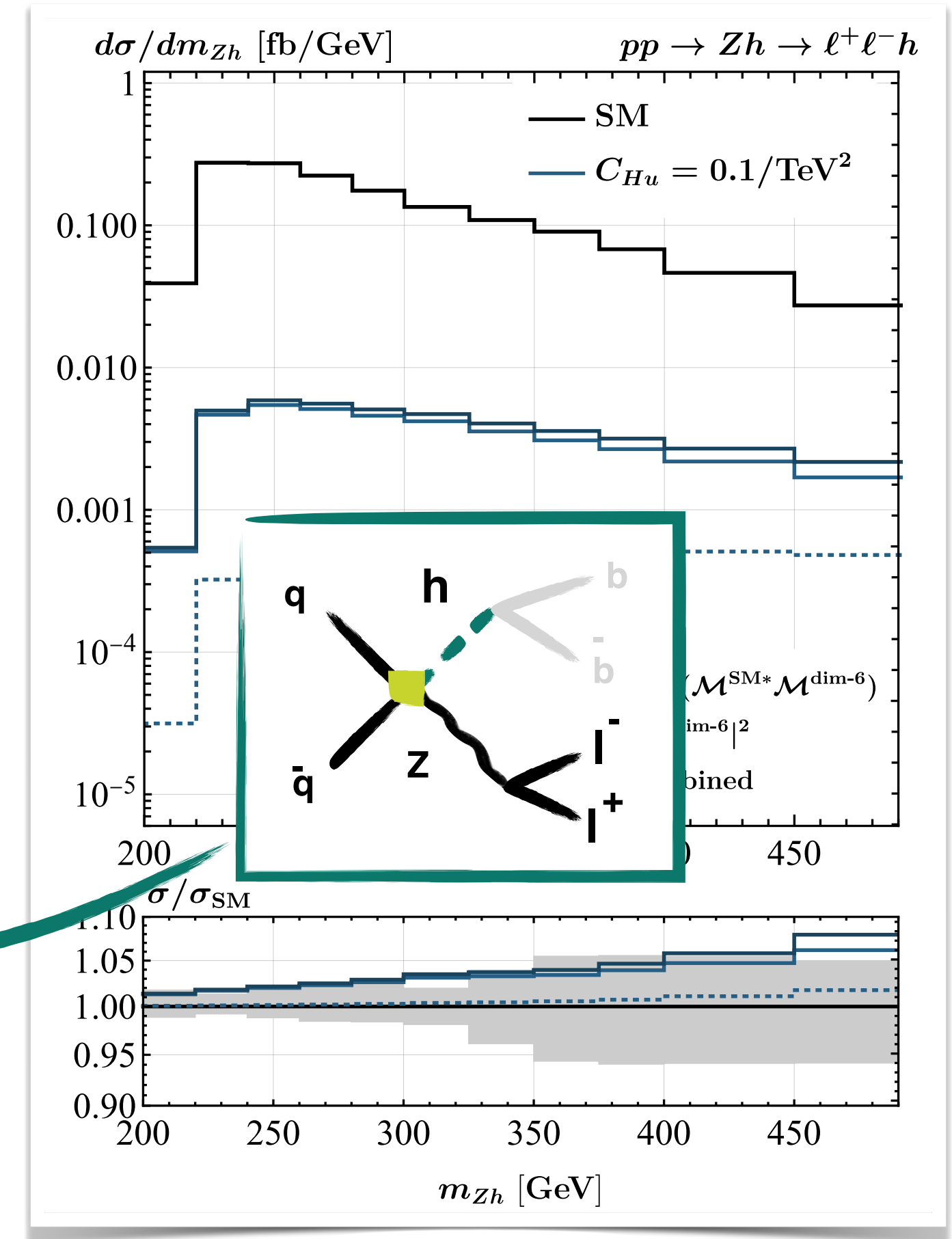
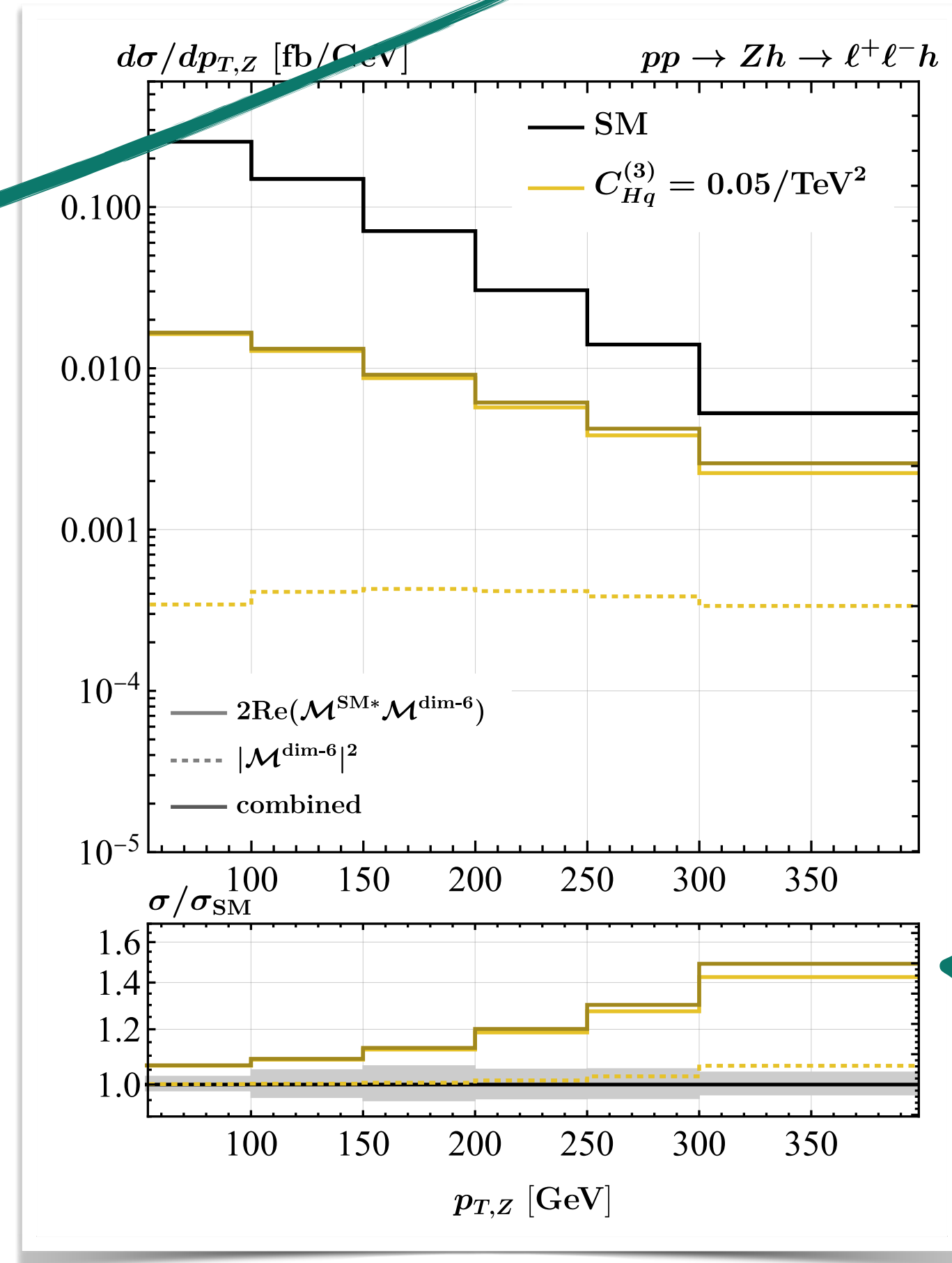
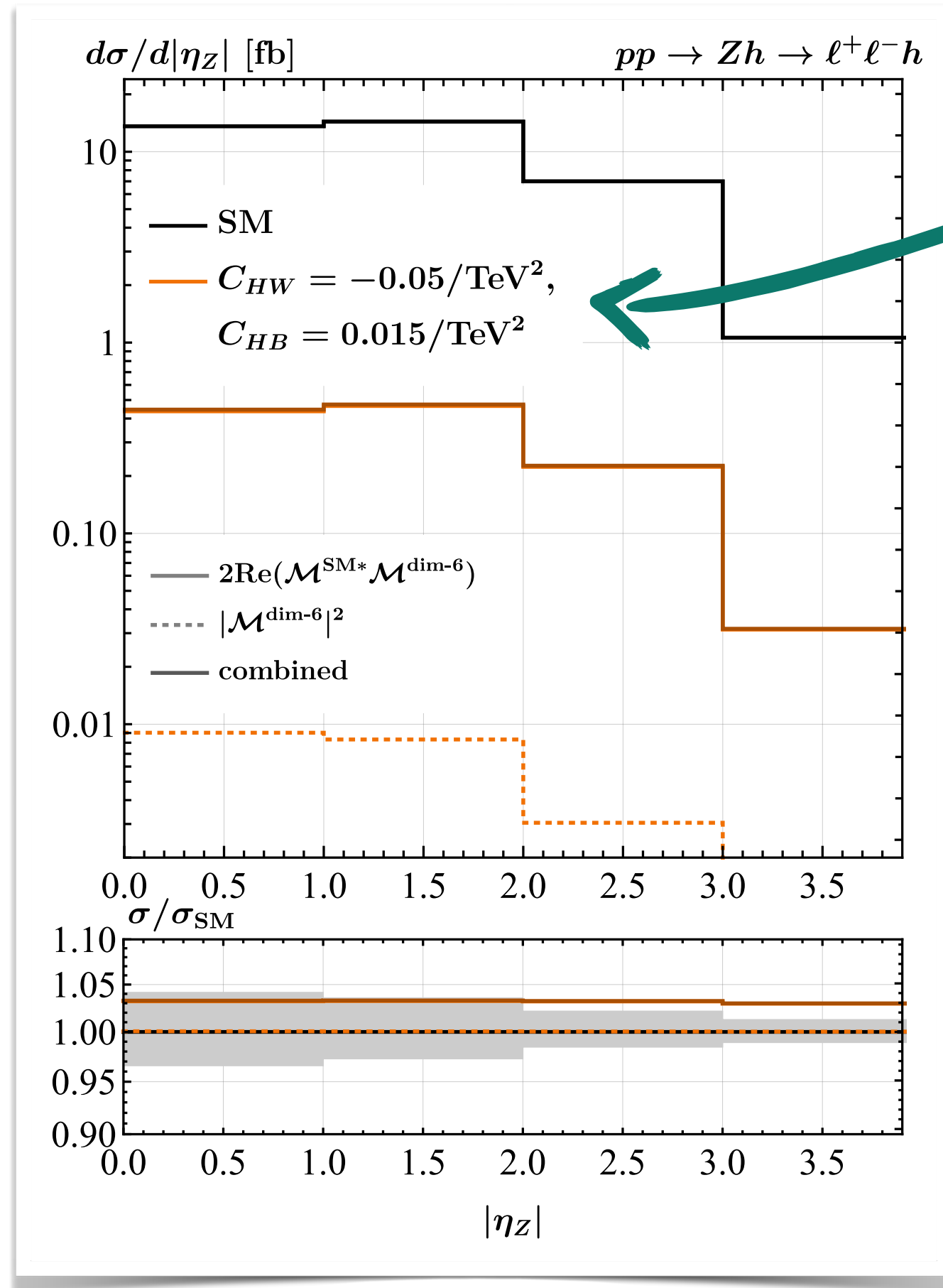


4. Phenomenology

4.3 Spectra

[2311.06107] (R. Gauld, U. Haisch, LS)

Parameter benchmarks discussed in our paper.

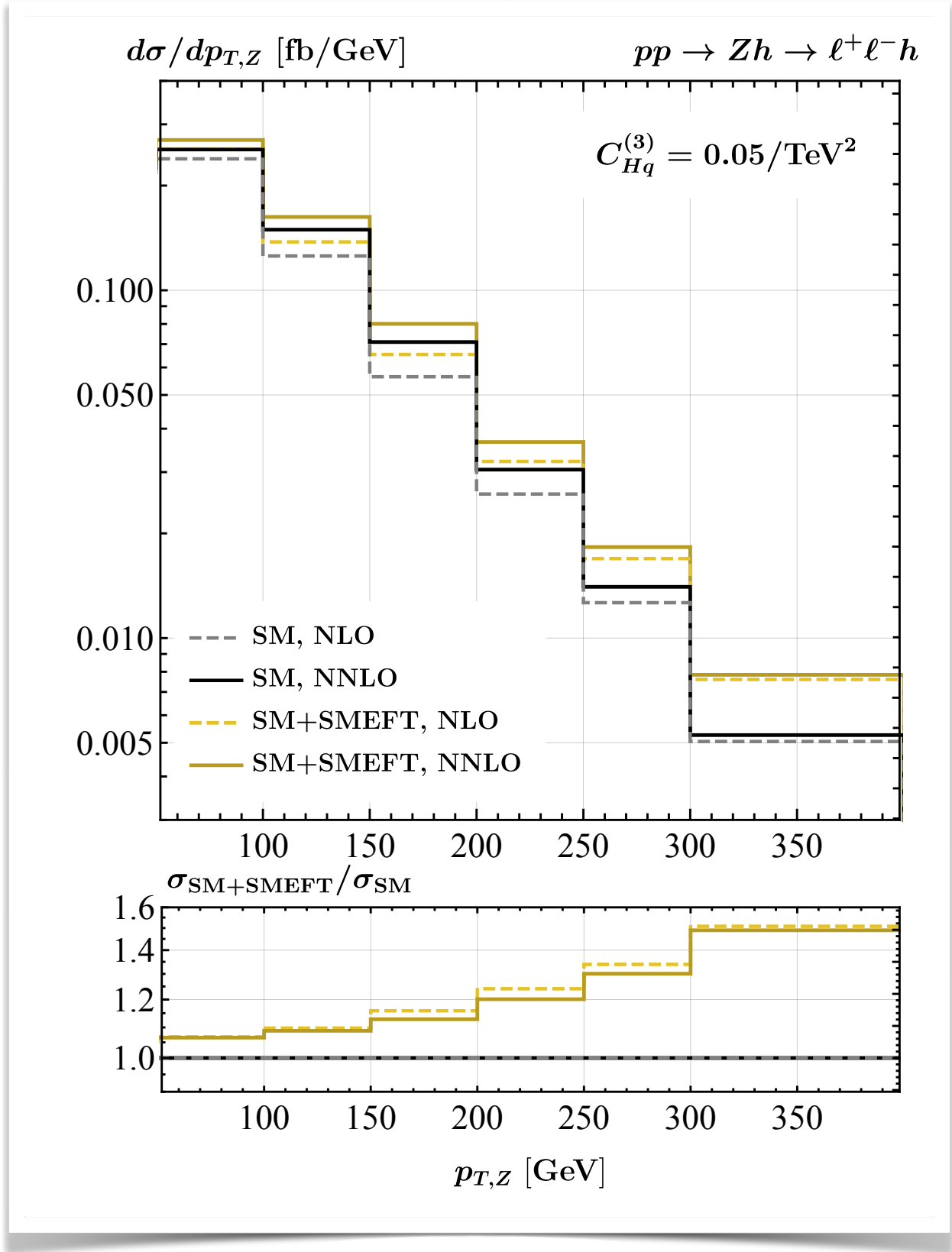
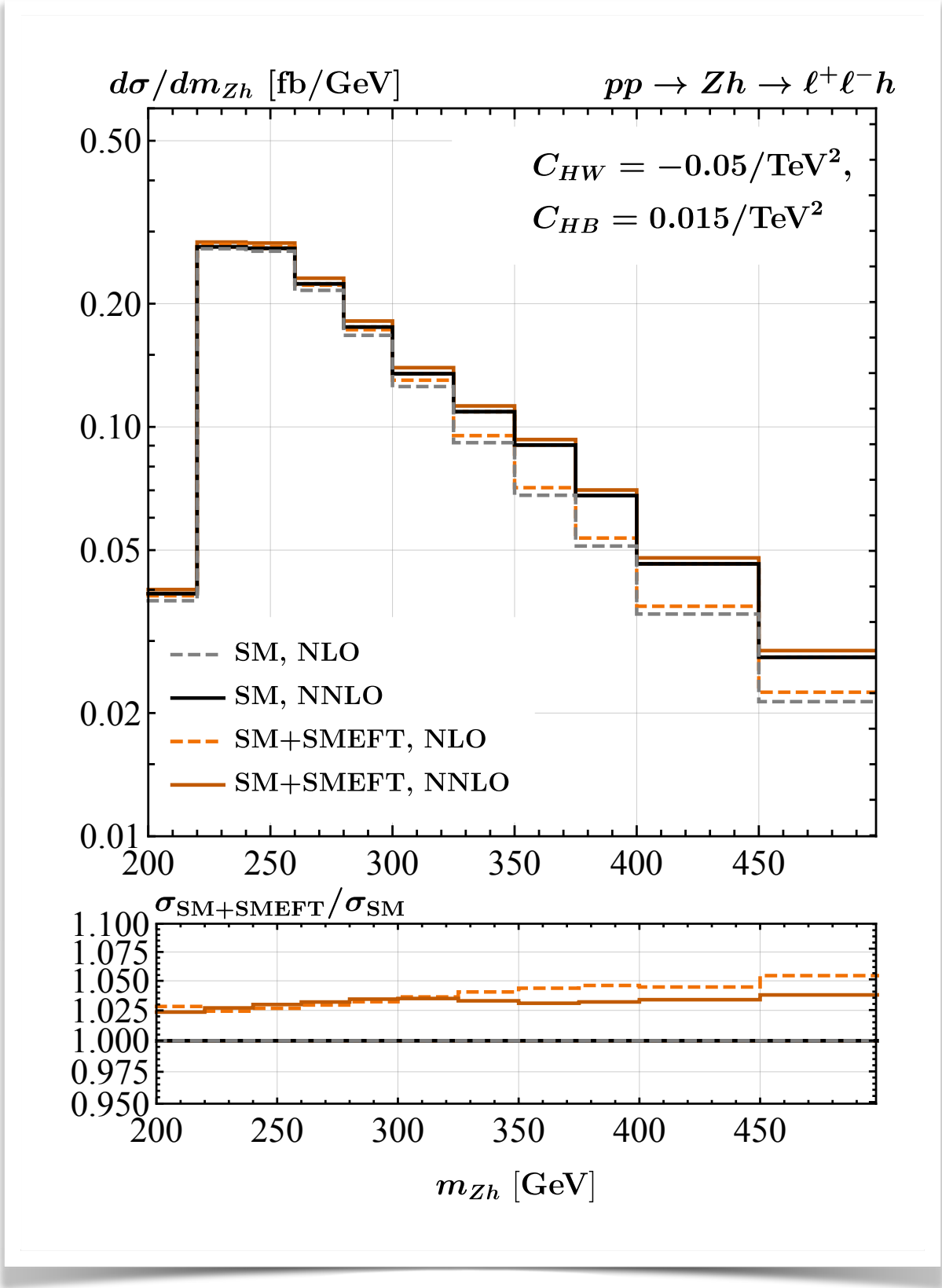
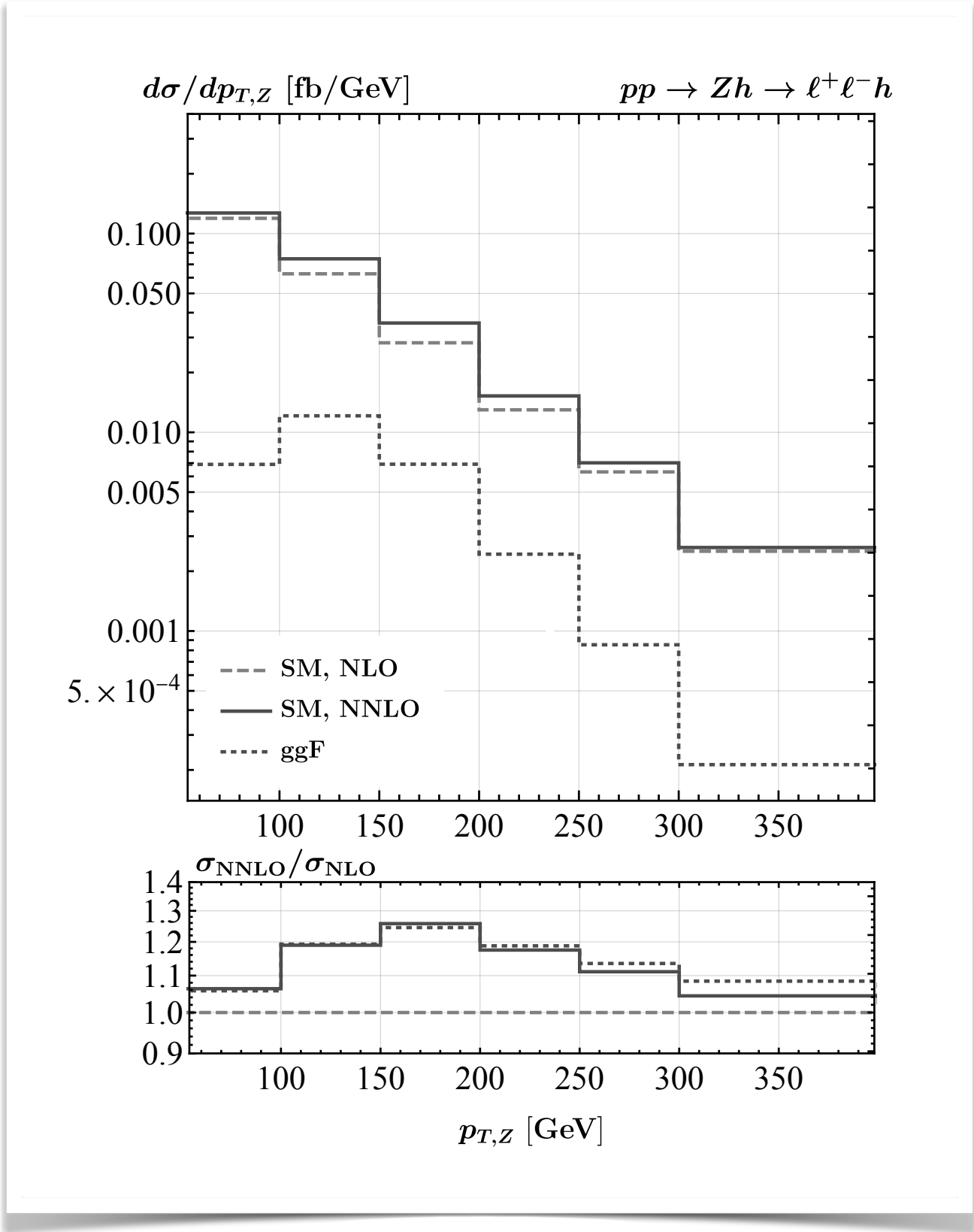


4. Phenomenology

4.4 NNLO vs NLO

4. Phenomenology

4.4 NNLO vs NLO

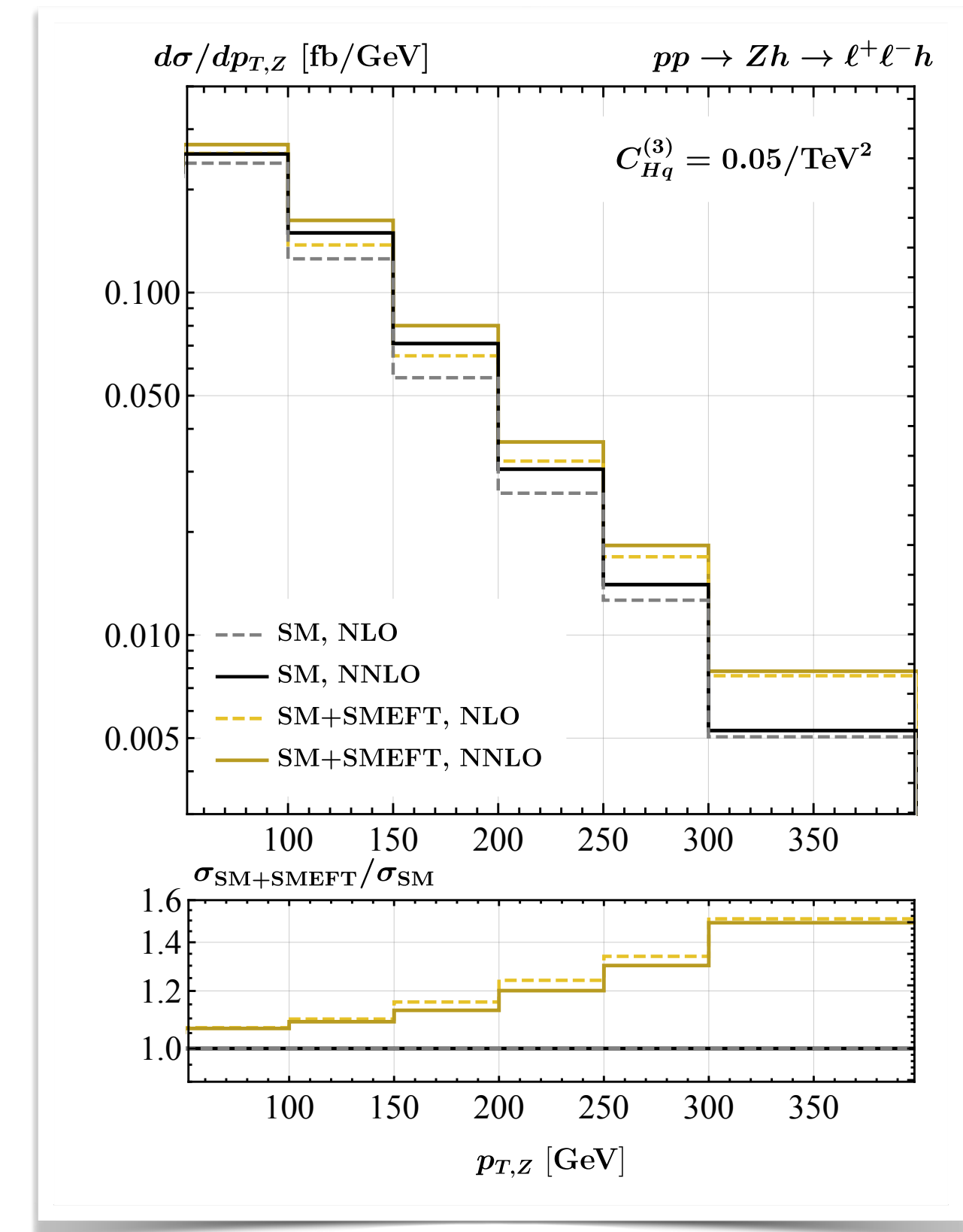
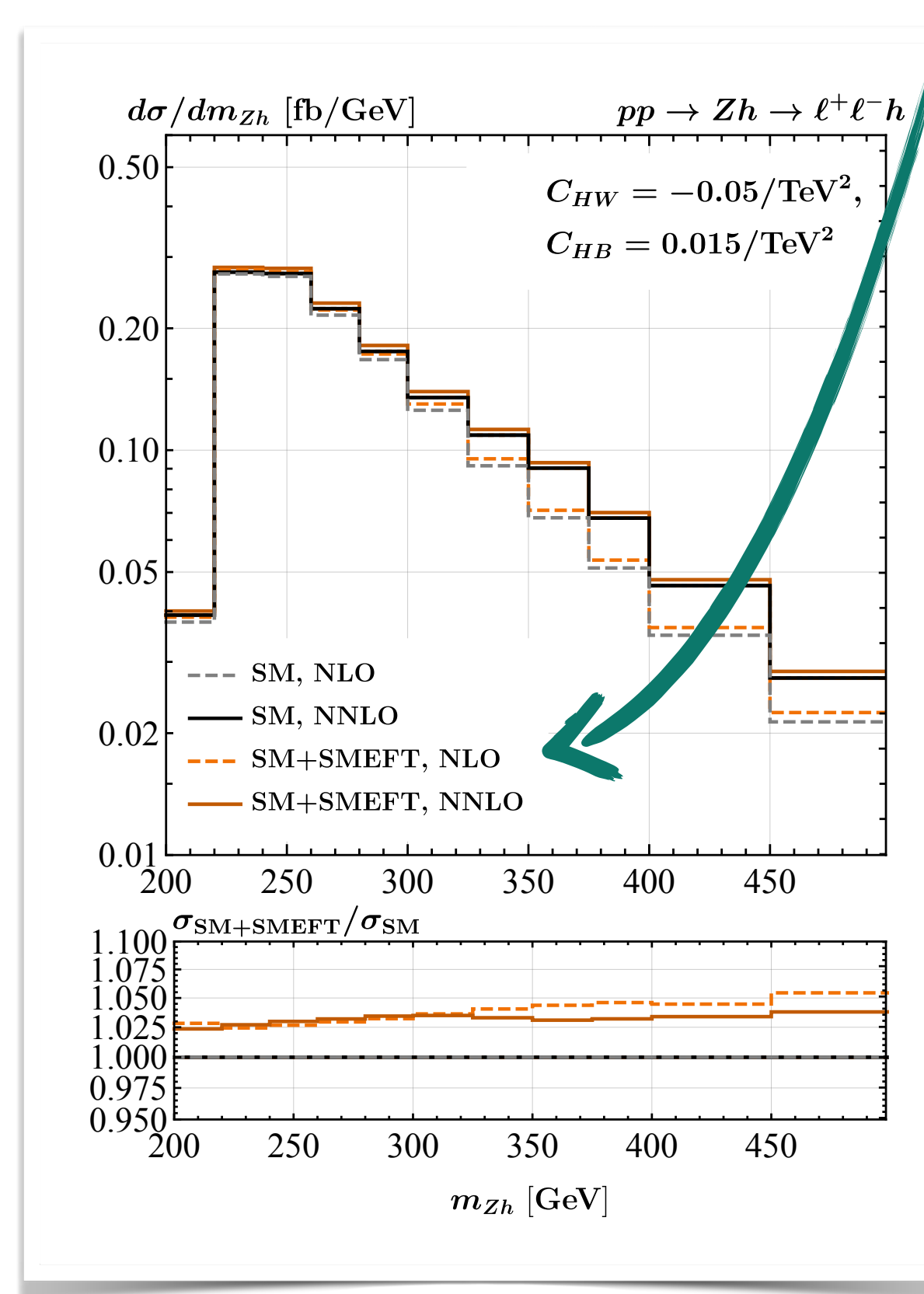
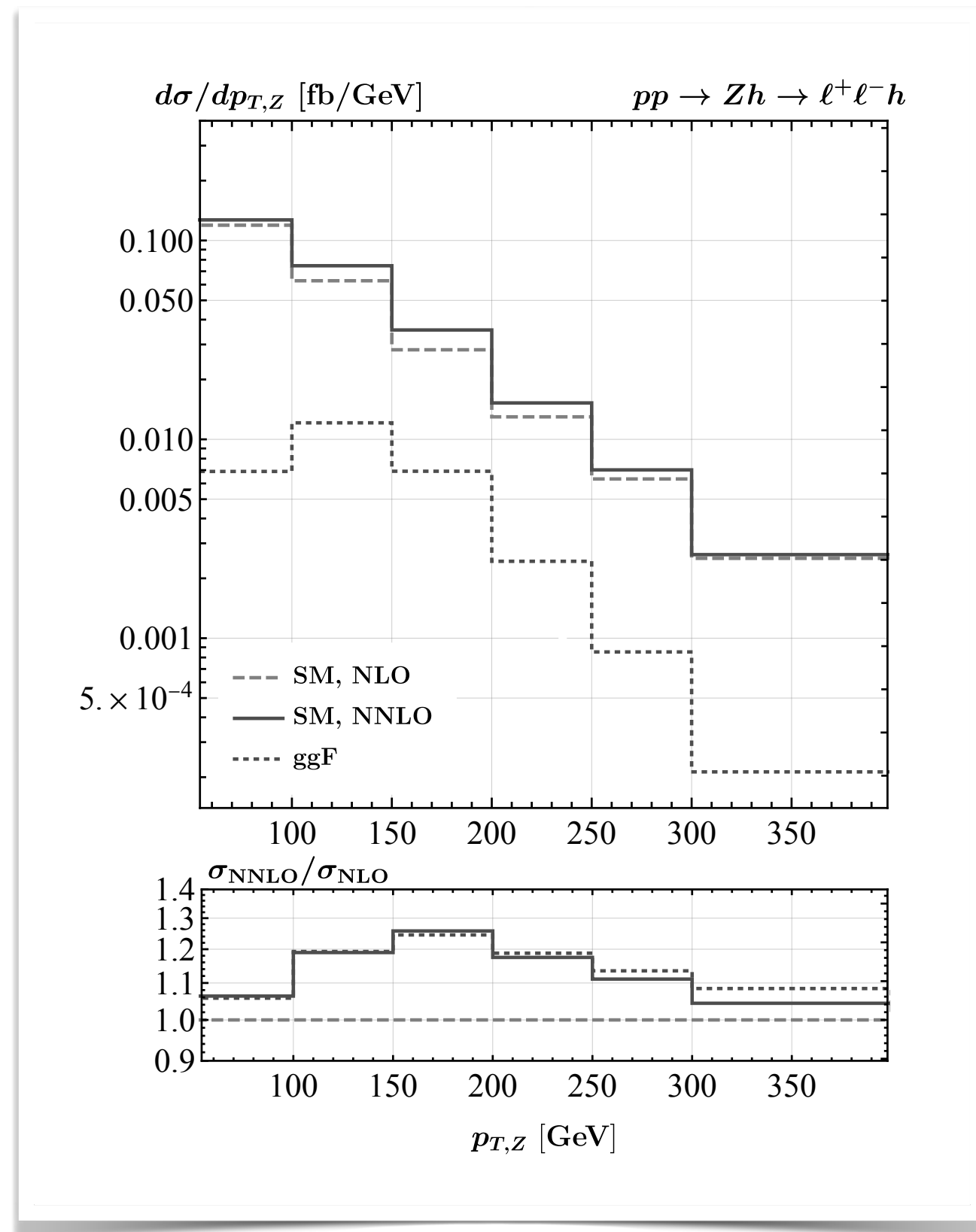


4. Phenomenology

4.4 NNLO vs NLO

[1804.07407] (S. Alioli, W. Dekens, M. Girard, E. Mereghetti)

NLO+PS, $|M_{\text{dim-4}} + M_{\text{dim-6}}|^2$ only

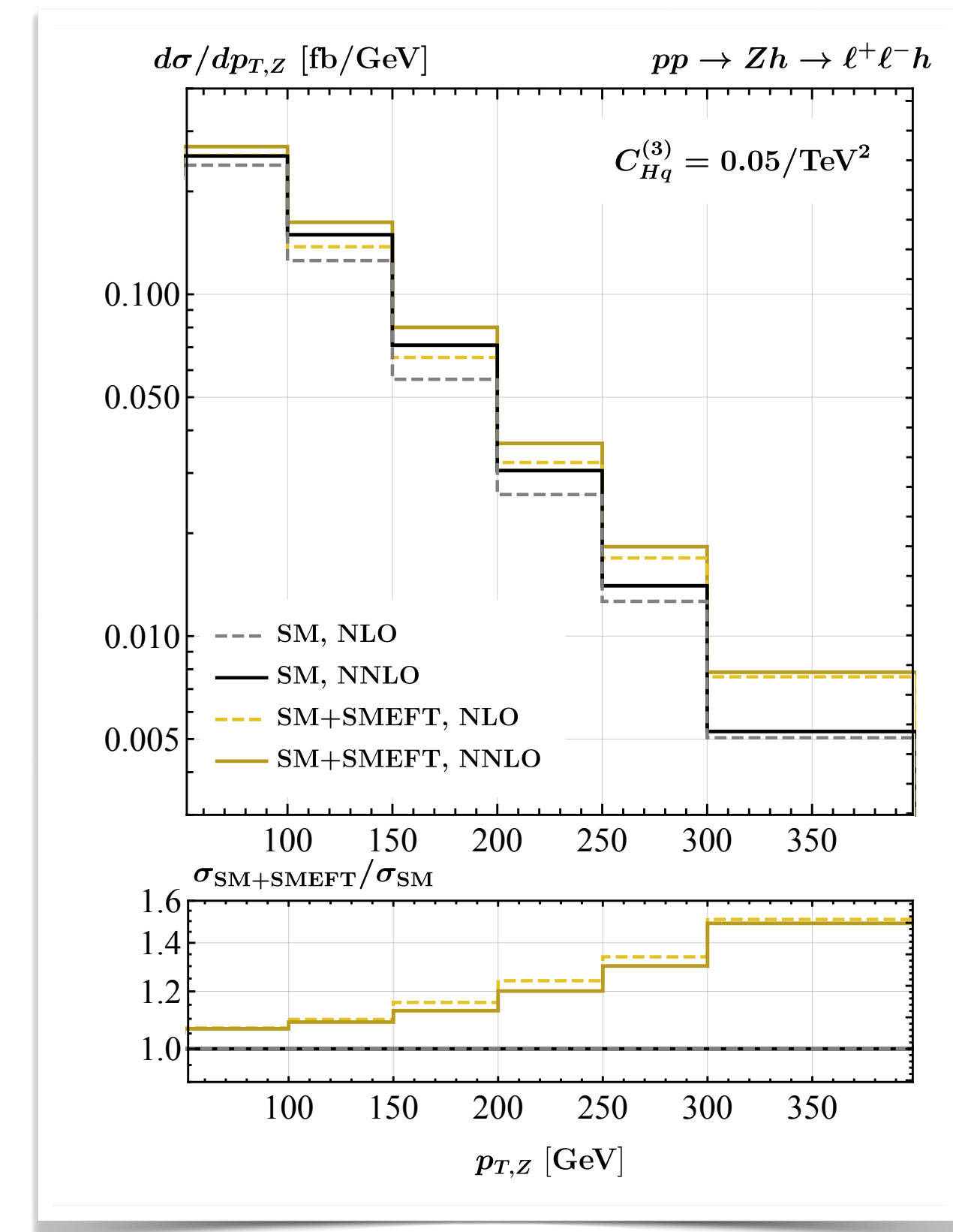
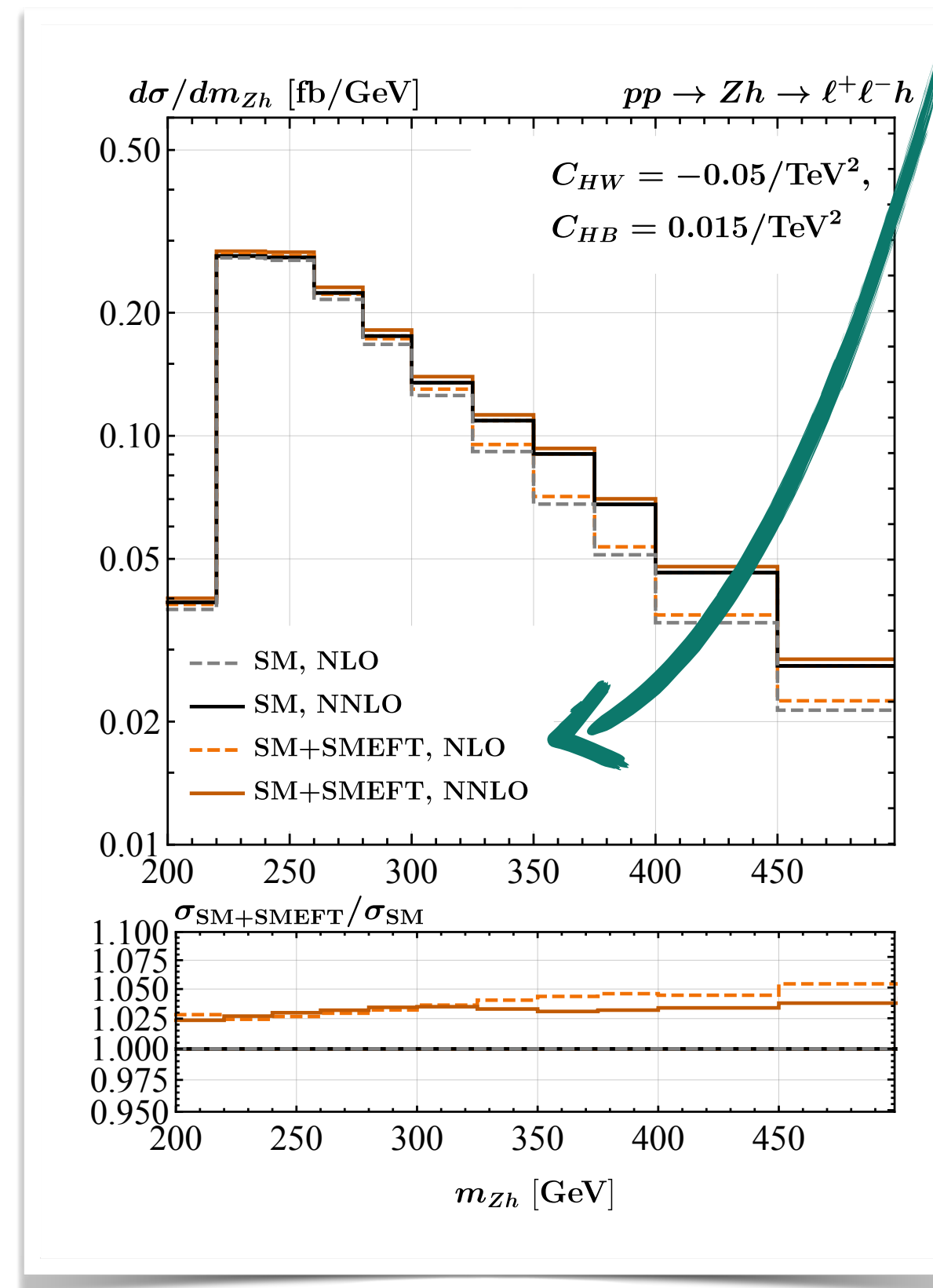
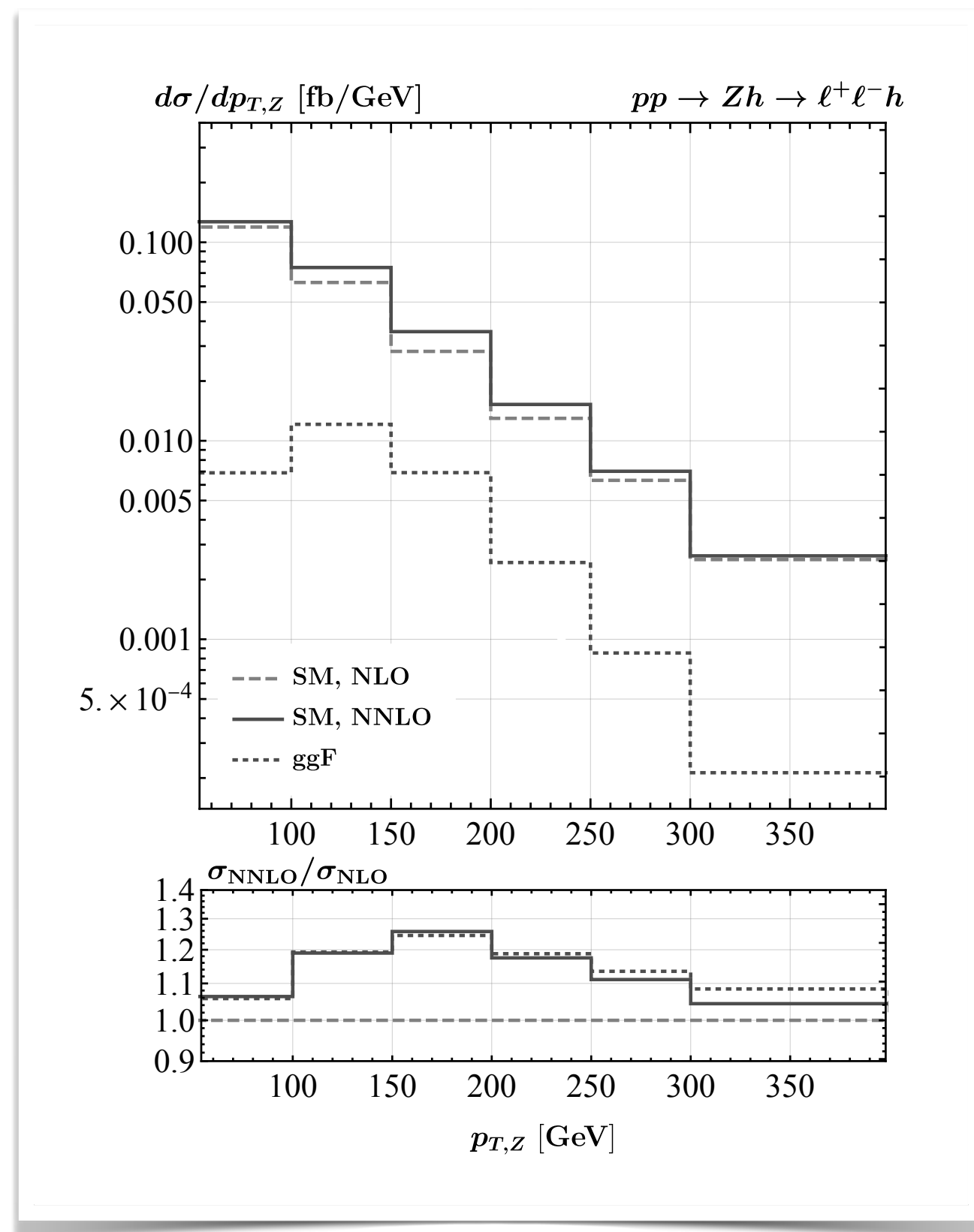


4. Phenomenology

4.4 NNLO vs NLO

[1804.07407] (S. Alioli, W. Dekens, M. Girard, E. Mereghetti)

NLO+PS, $|M_{\text{dim-4}} + M_{\text{dim-6}}|^2$ only



Our NNLO+PS code can do SM, linear SMEFT, quadratic SMEFT individually (+ input scheme corrections).

5. Conclusions

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→ **useful tool for future Higgs characterisation studies at the LHC**
- ▶ In our calculation we encountered **interesting theoretical aspects**, including the un- and recontraction of spinor-helicity amplitudes and the cancellation of gauge anomalies in the SMEFT.

Backup



4. Phenomenology

4.2 POWHEG MiNNLO_{PS} event generator

4. Phenomenology

4.2 POWHEG MiNNLO_{PS} event generator [\[1908.06987\]](#) (P. Monni, E. Re. M. Wieseemann, G. Zanderighi)

[\[2006.04133\]](#) (P. Monni, E. Re. M. Wieseemann)

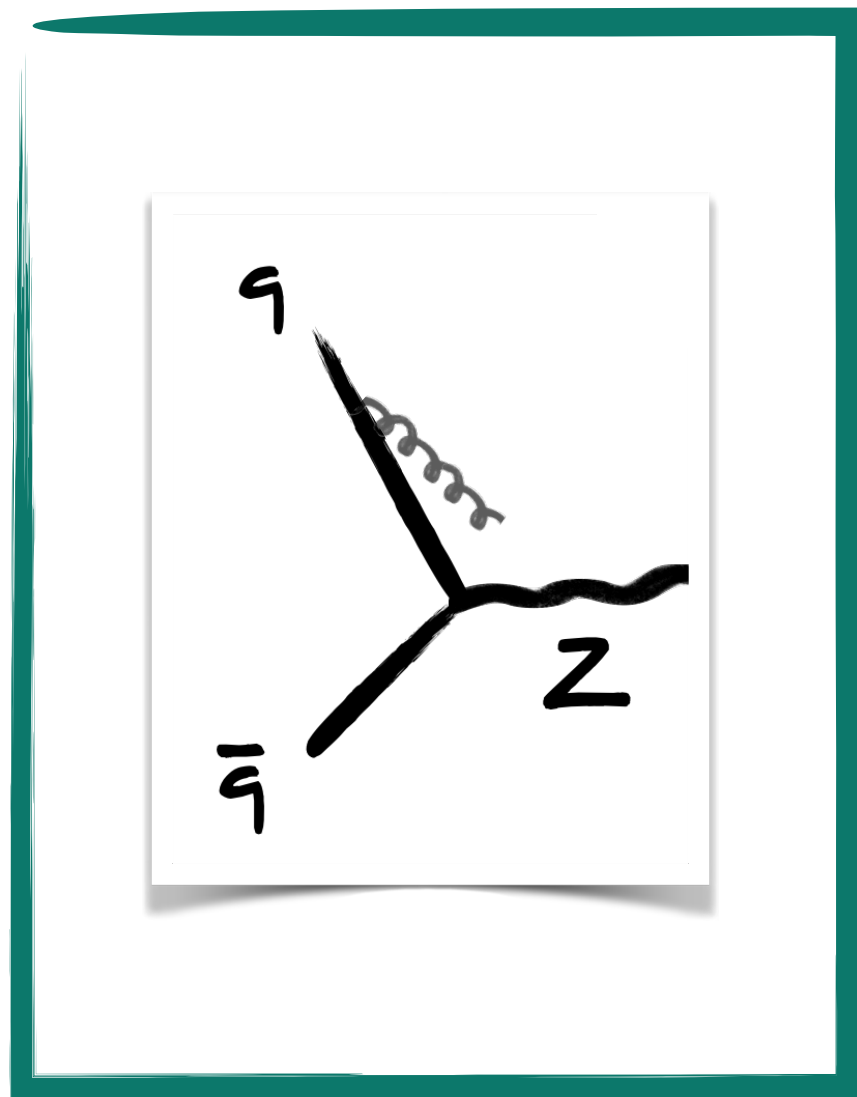
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4. Phenomenology

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IR singularities

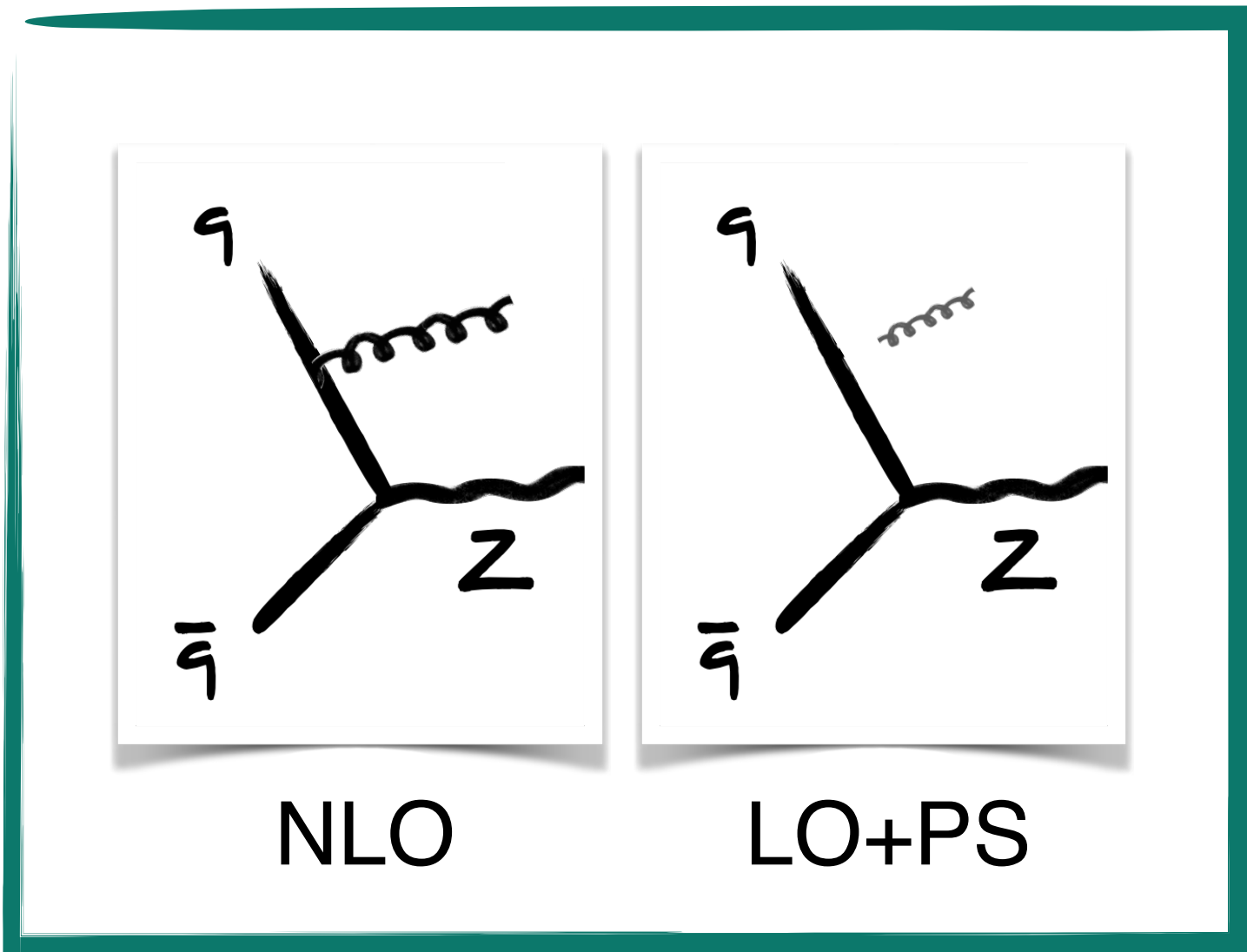
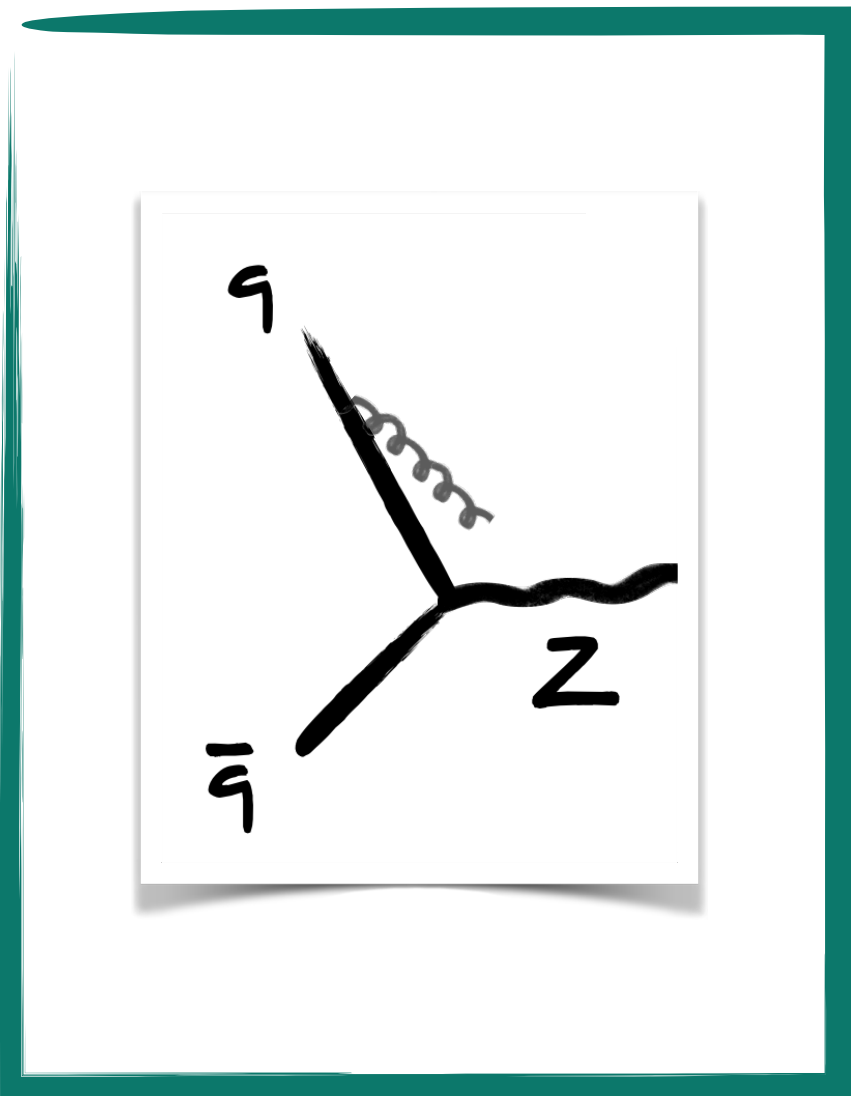
Deal with cases
where emitted parton
is soft or coll.

4. Phenomenology

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IR singularities

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Matching

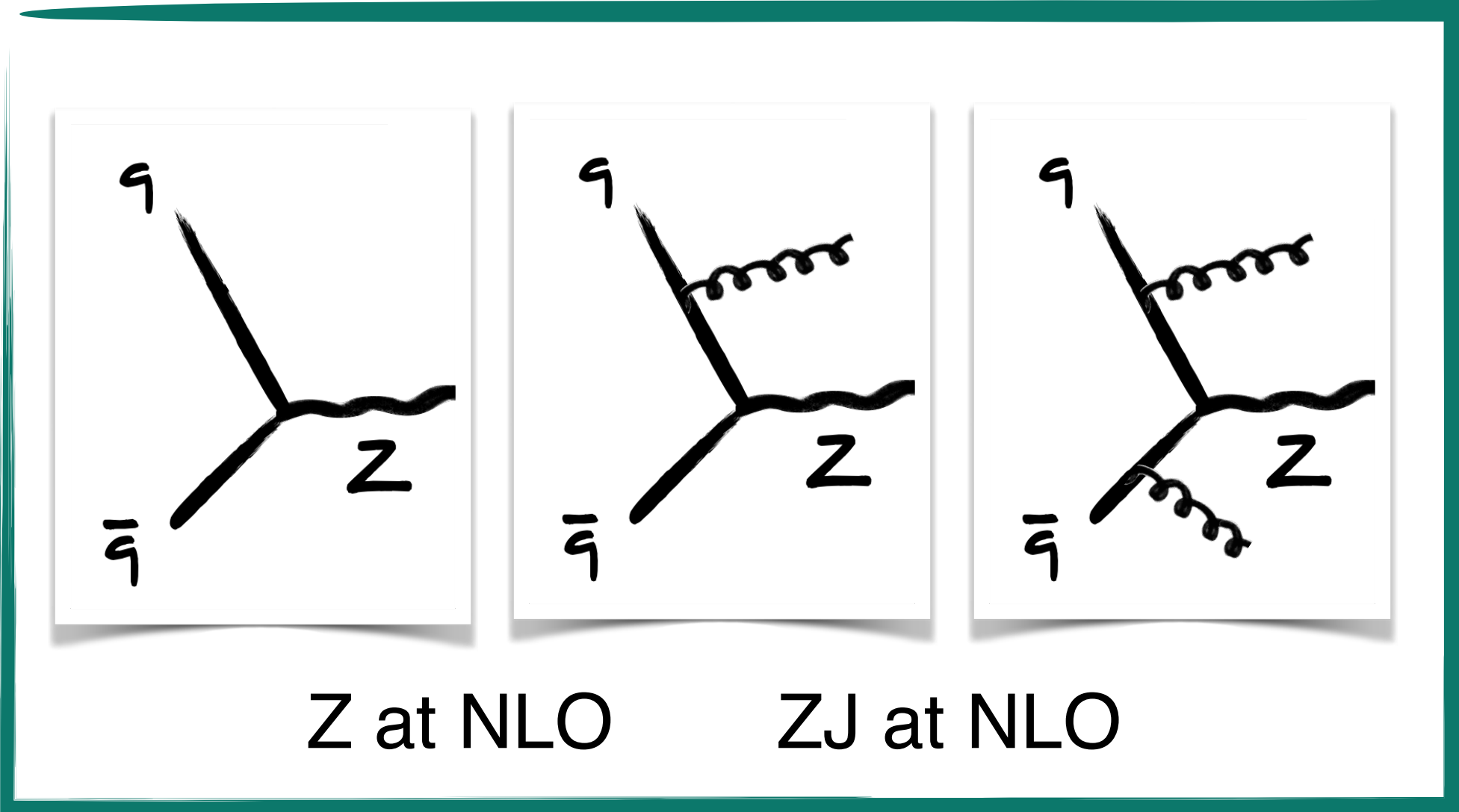
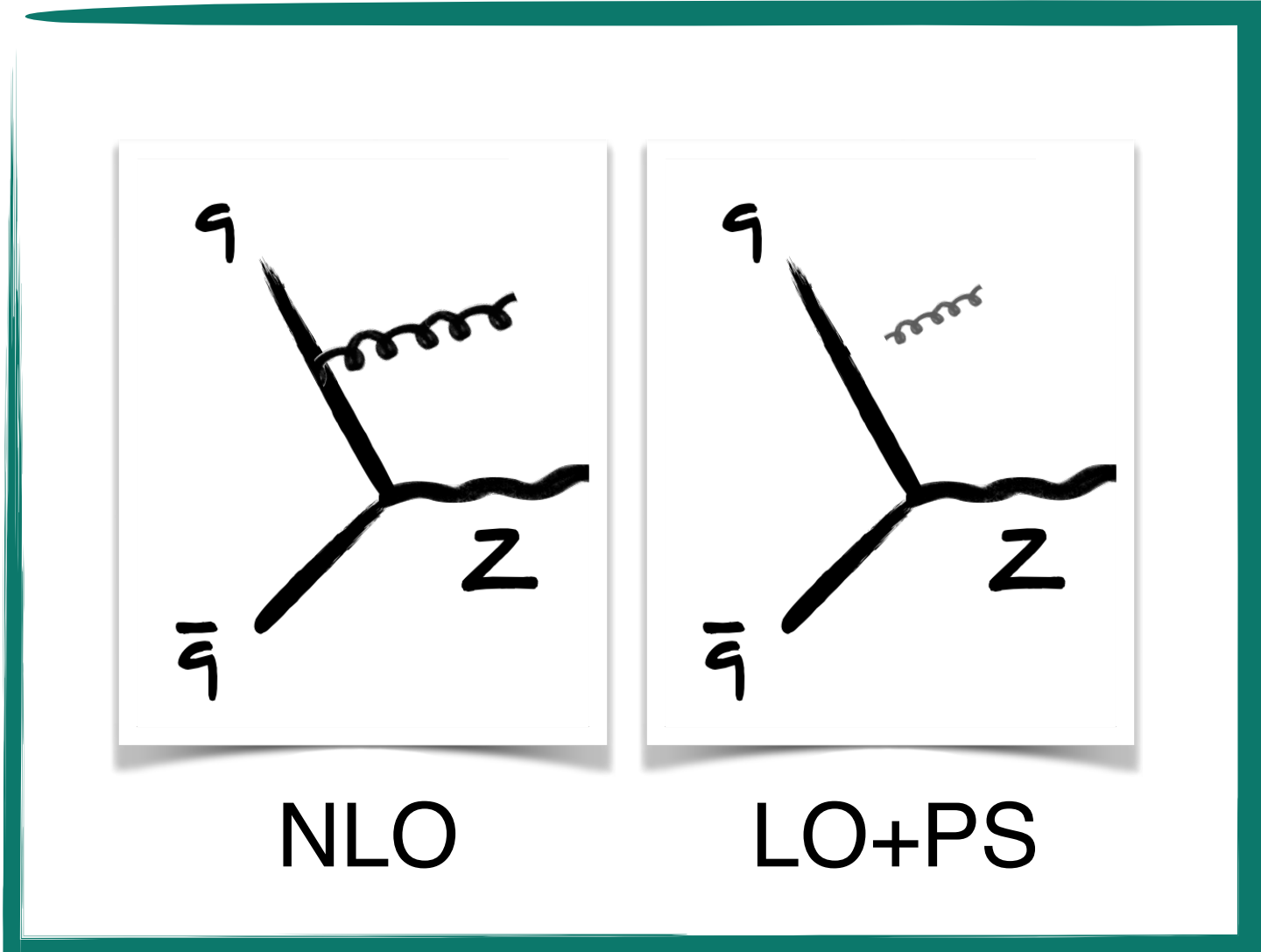
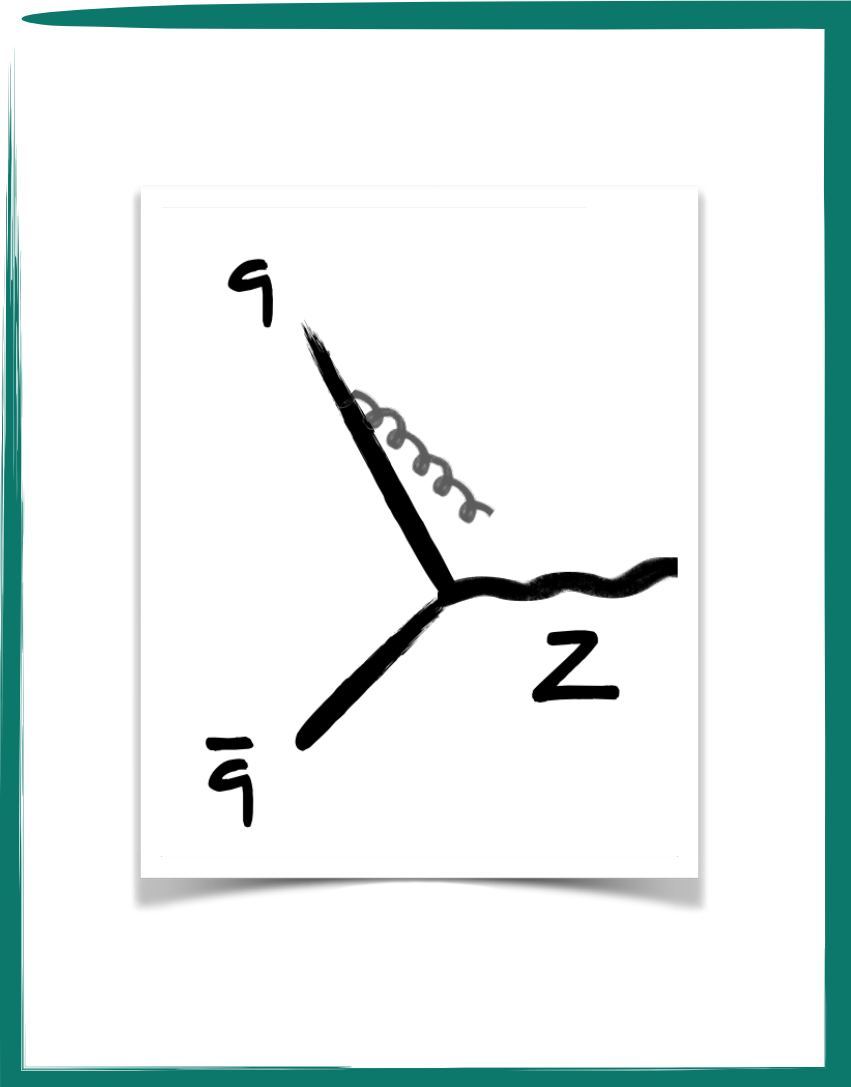
Avoid double counting between the full real and the approx. real from the PS.

4. Phenomenology

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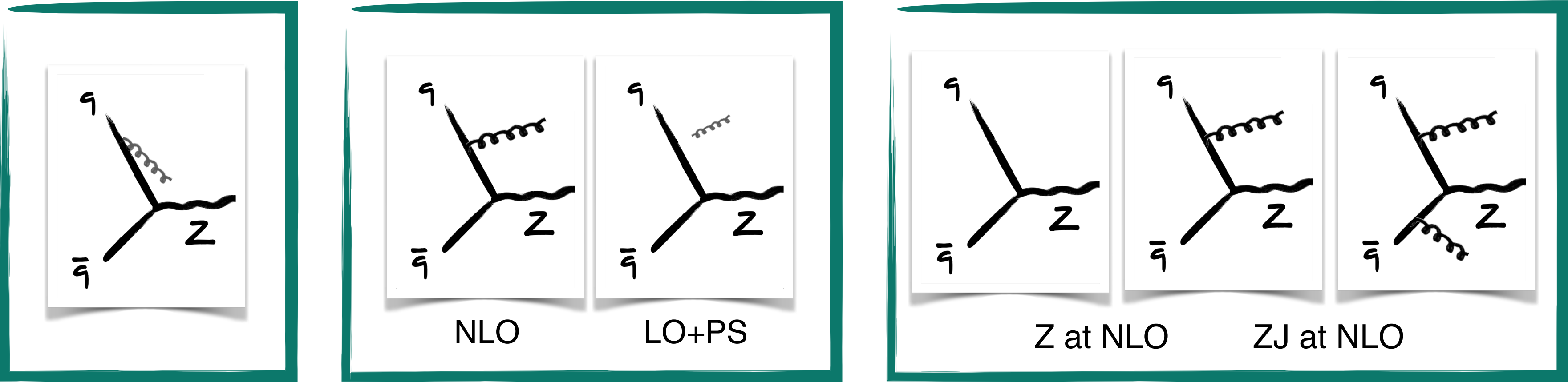
Merging

Combine Z at NLO with ZJ at NLO.

4. Phenomenology

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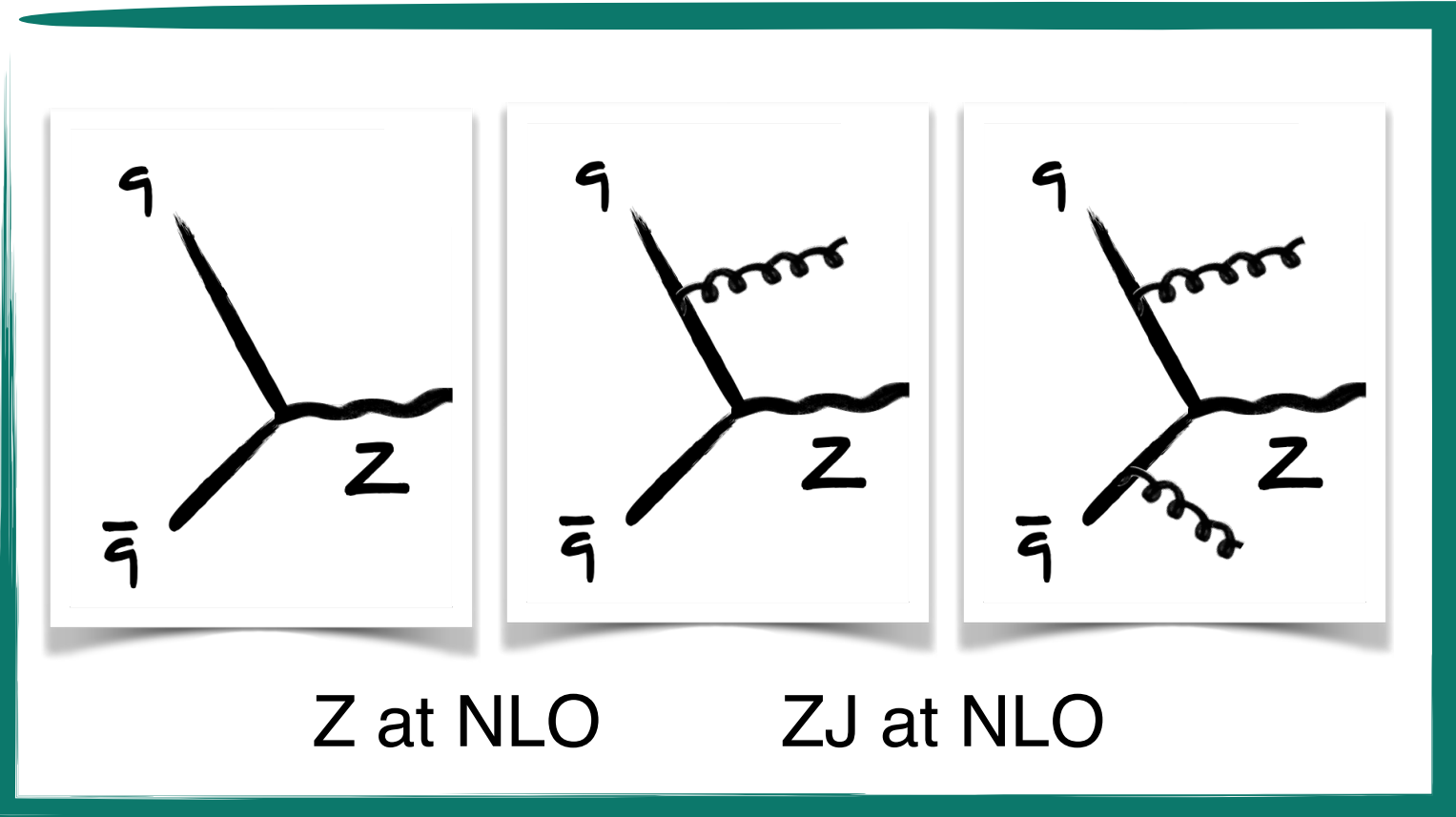
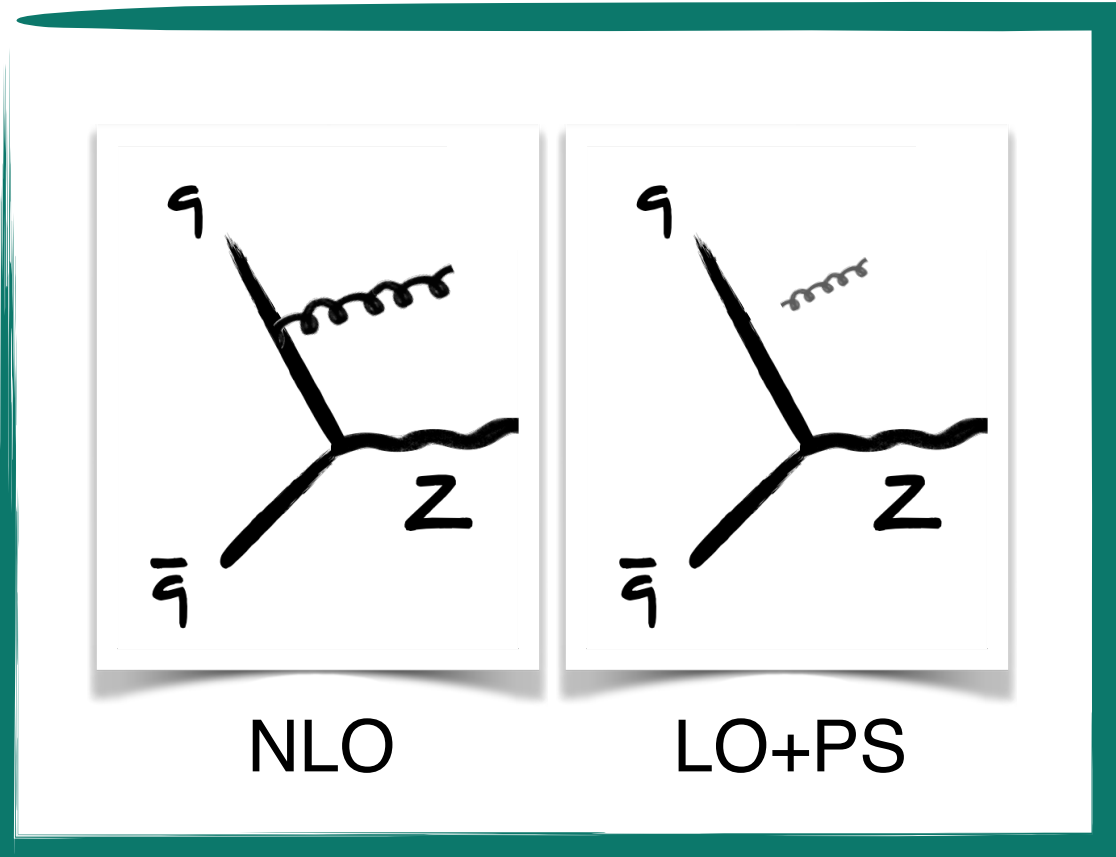
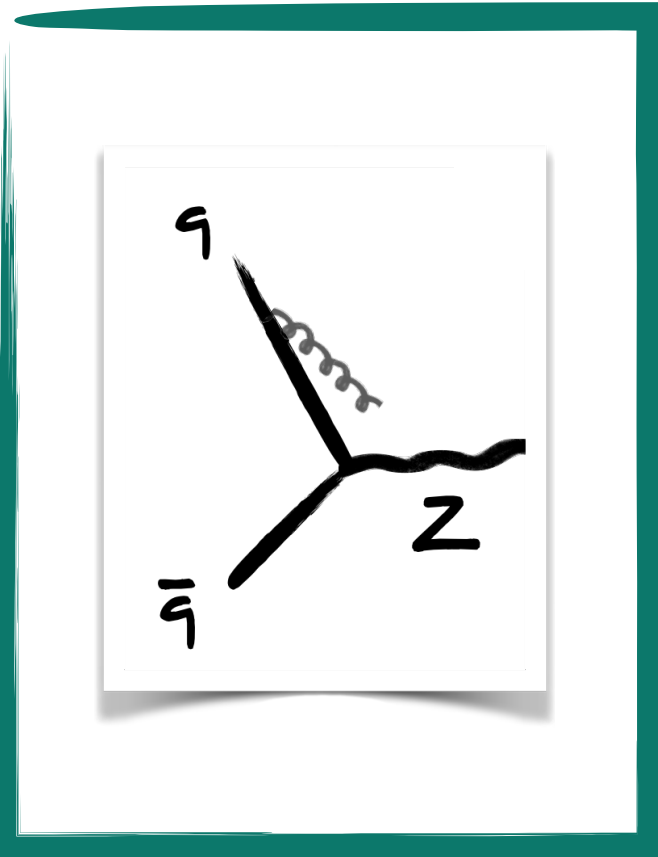
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Master formula



4. Phenomenology

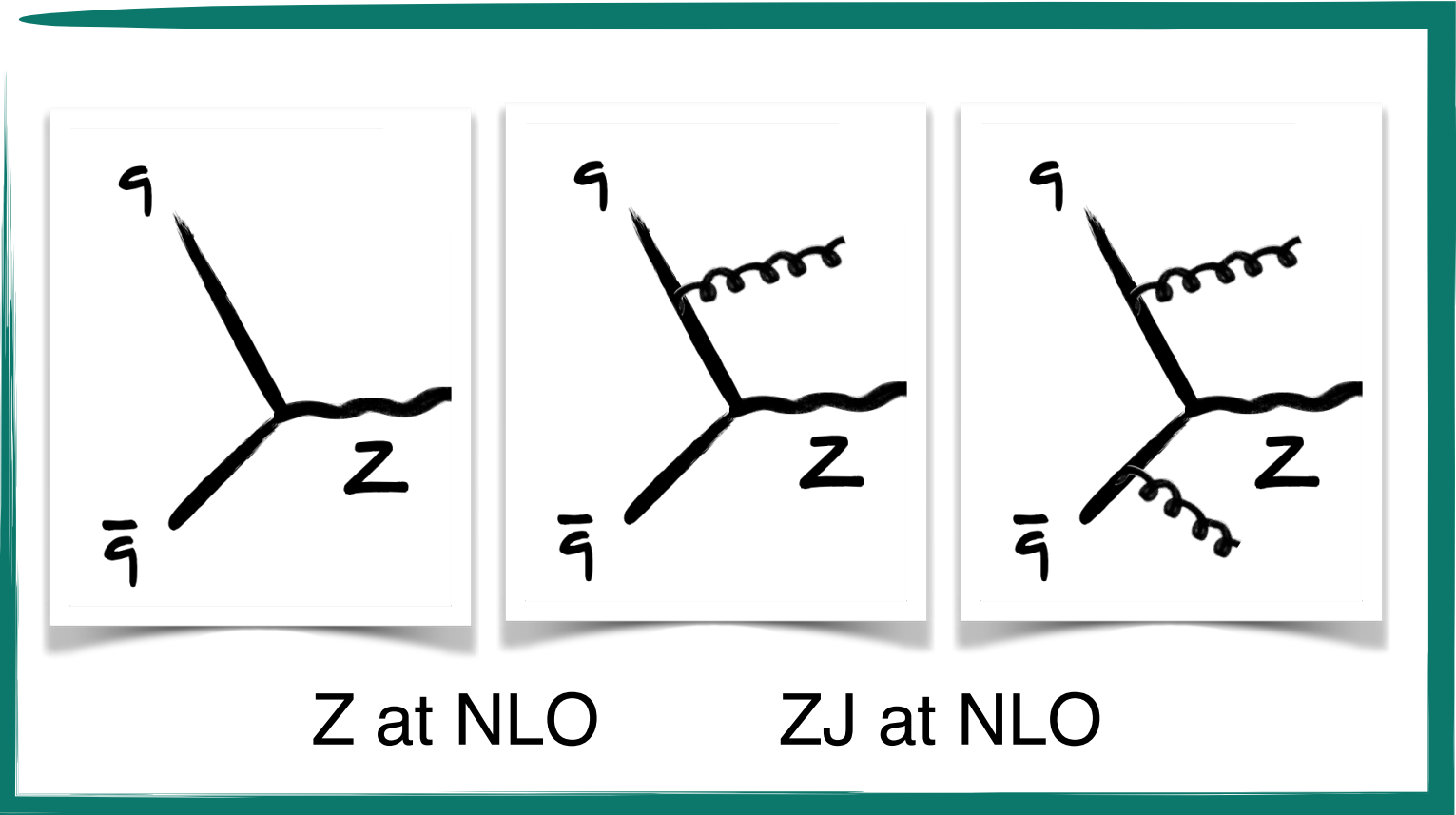
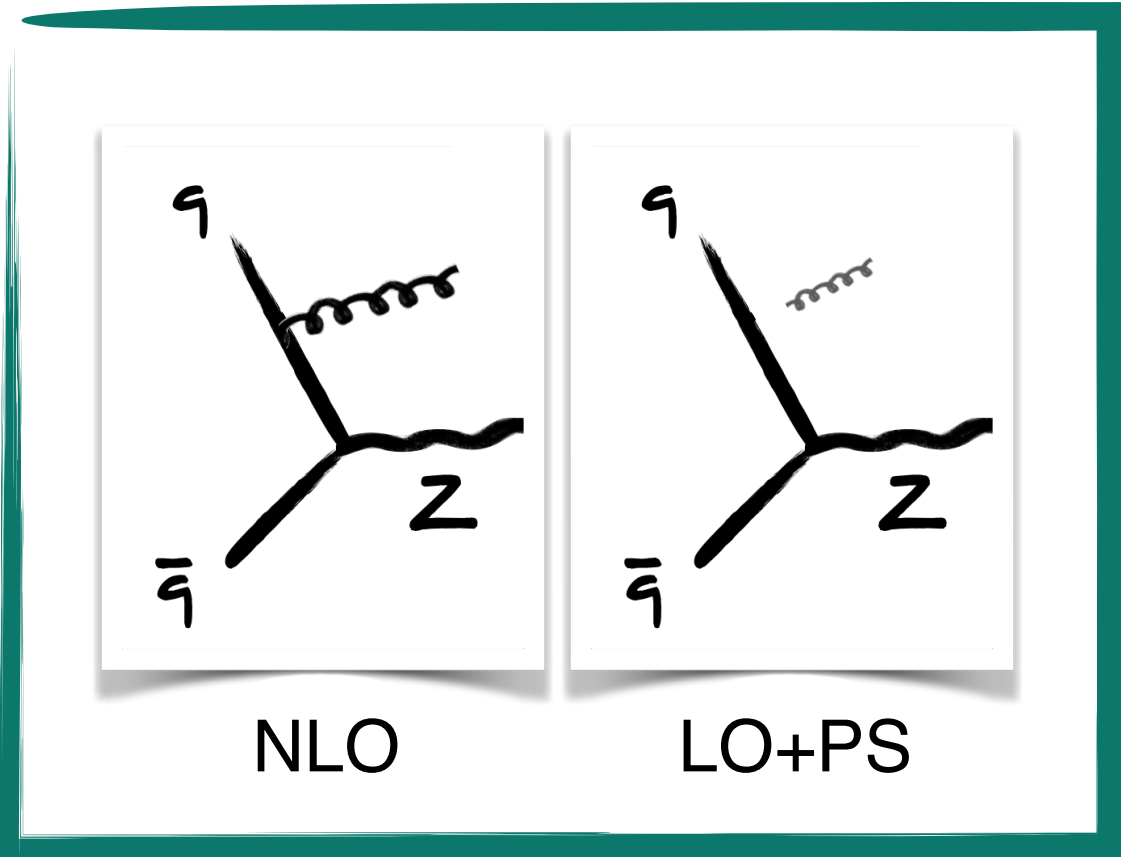
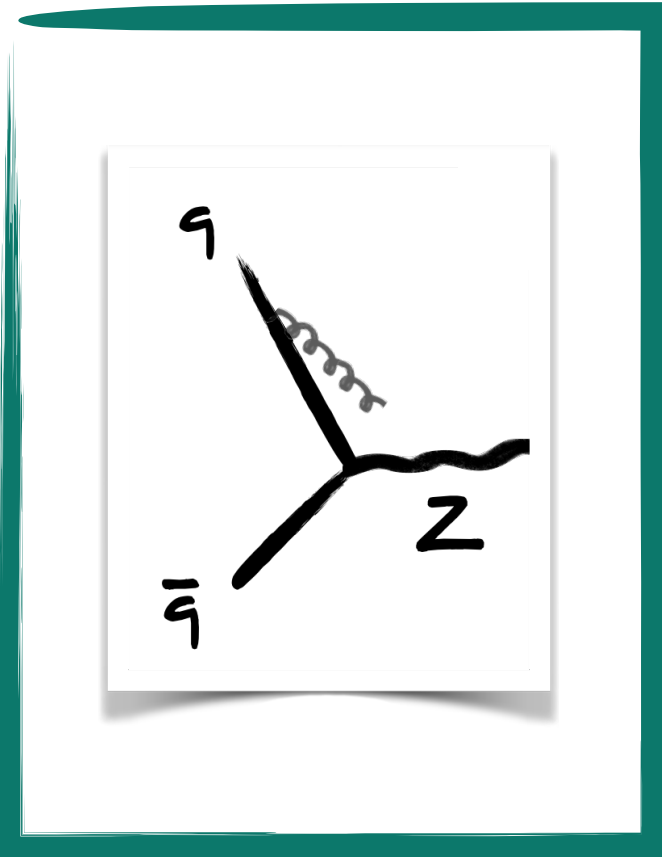
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4. Phenomenology

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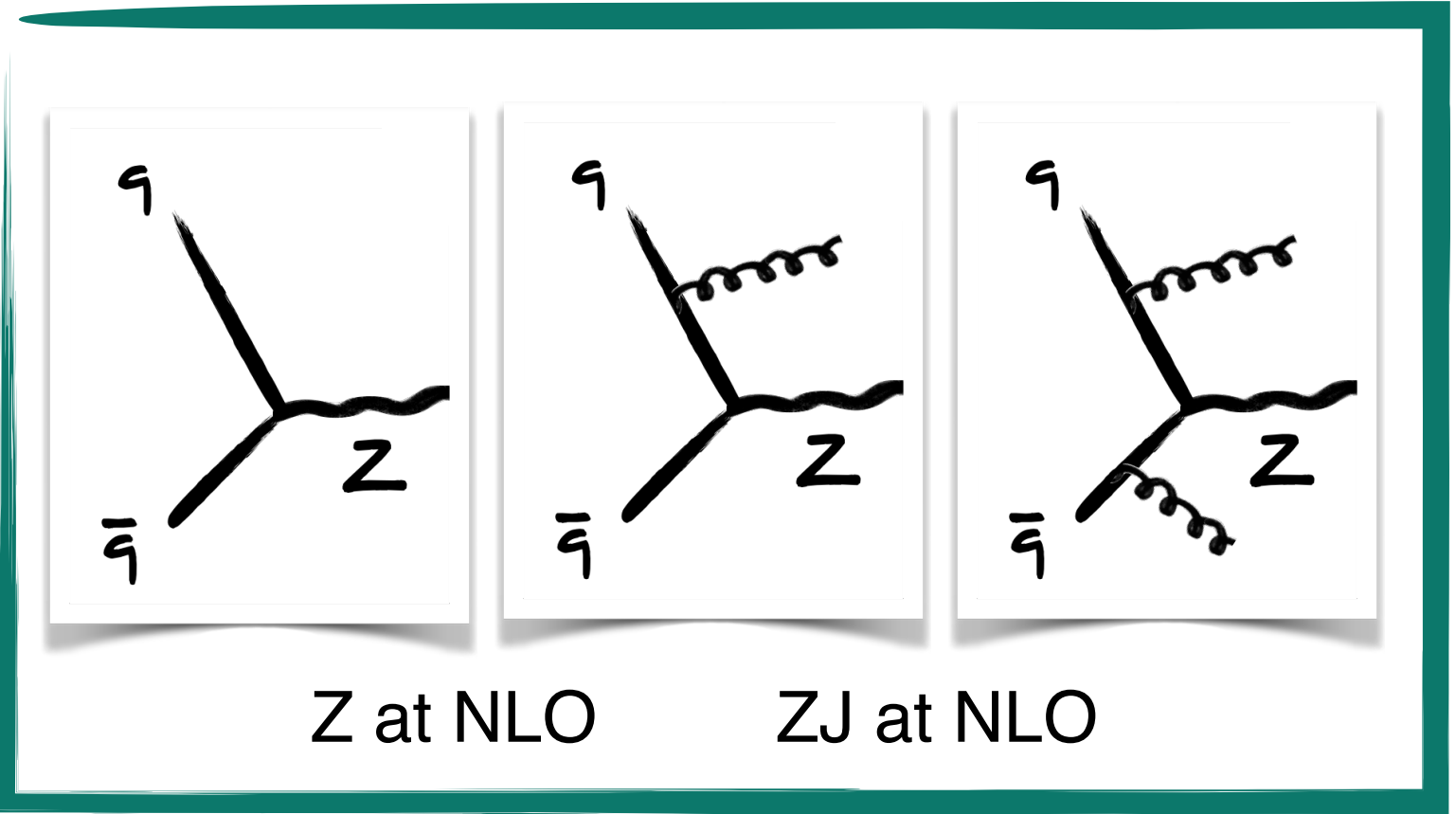
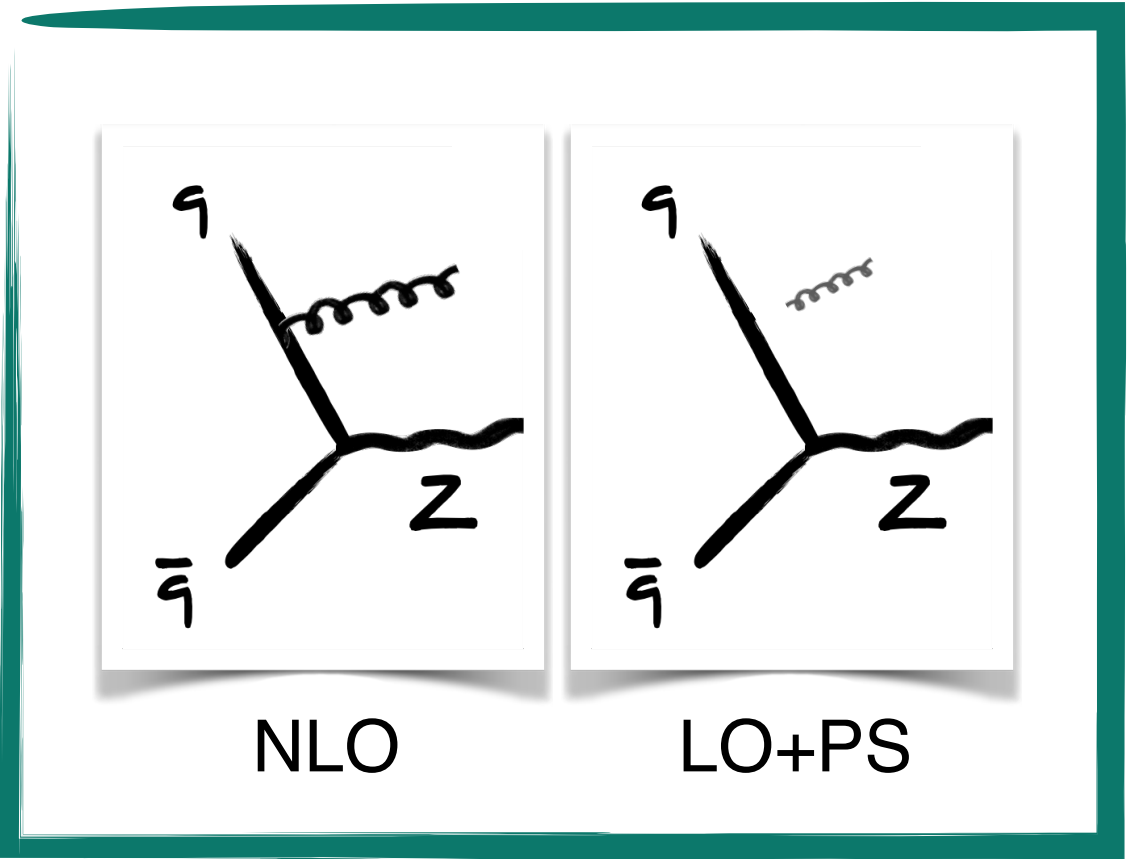
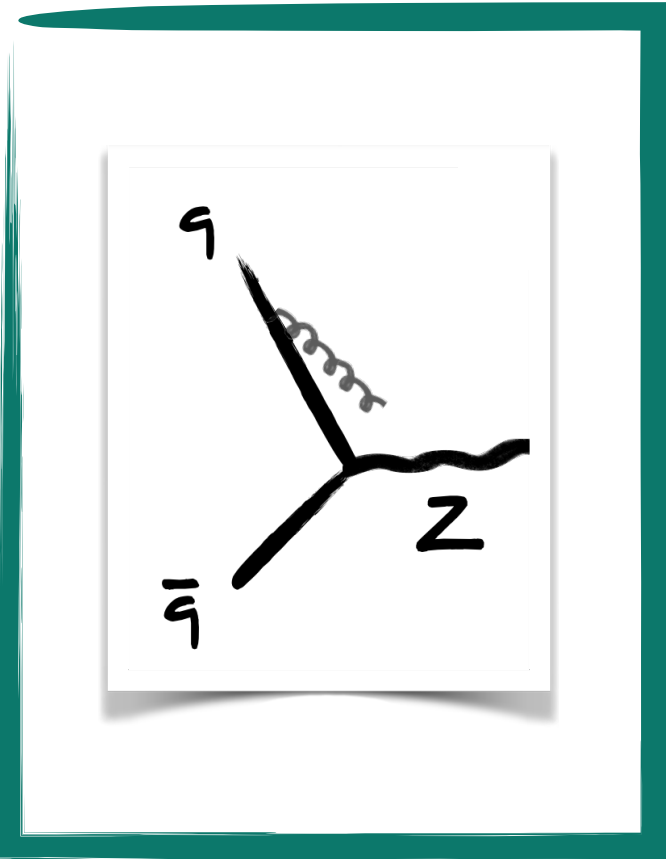
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Subtraction counterterms.

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4. Phenomenology

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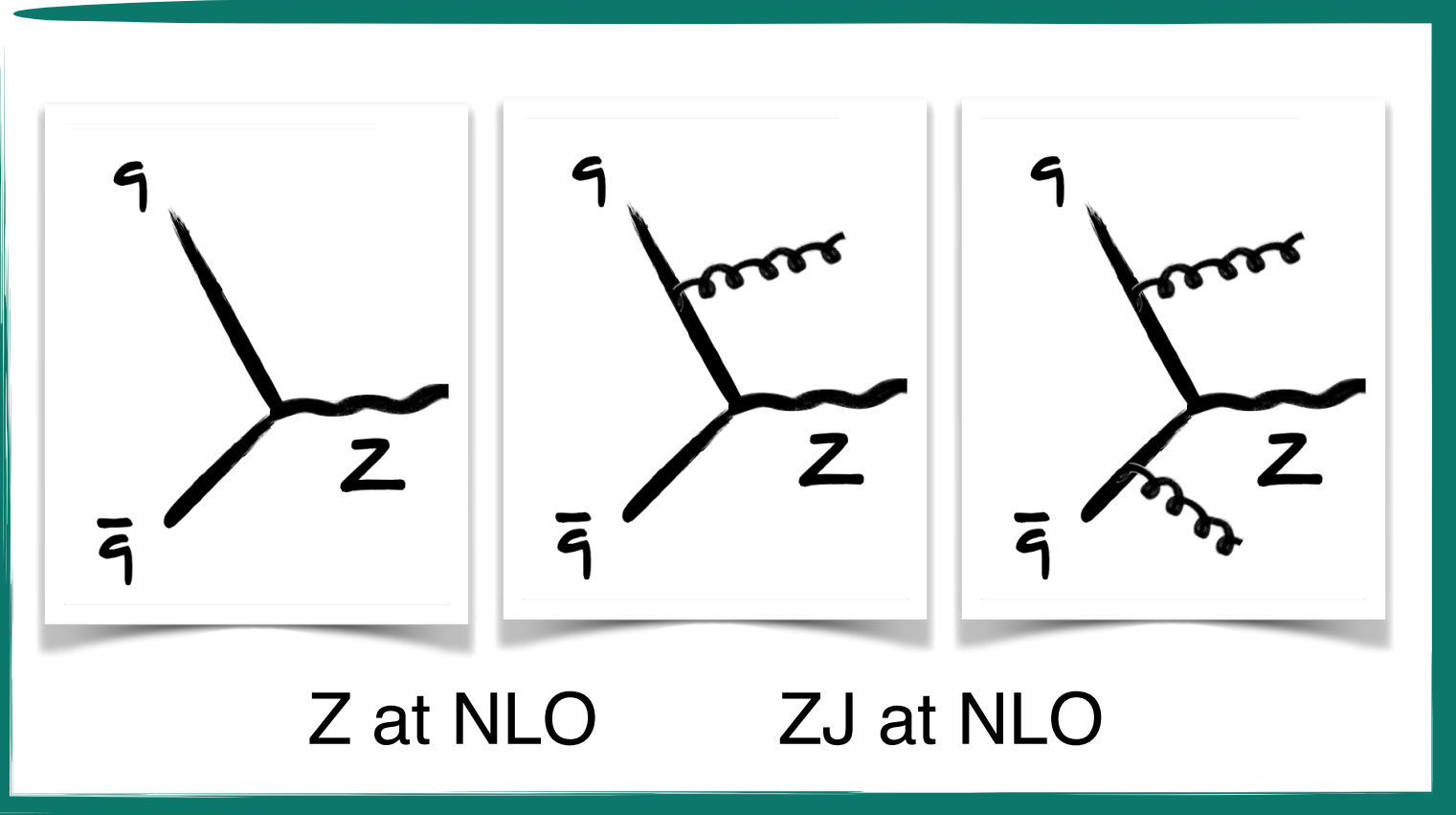
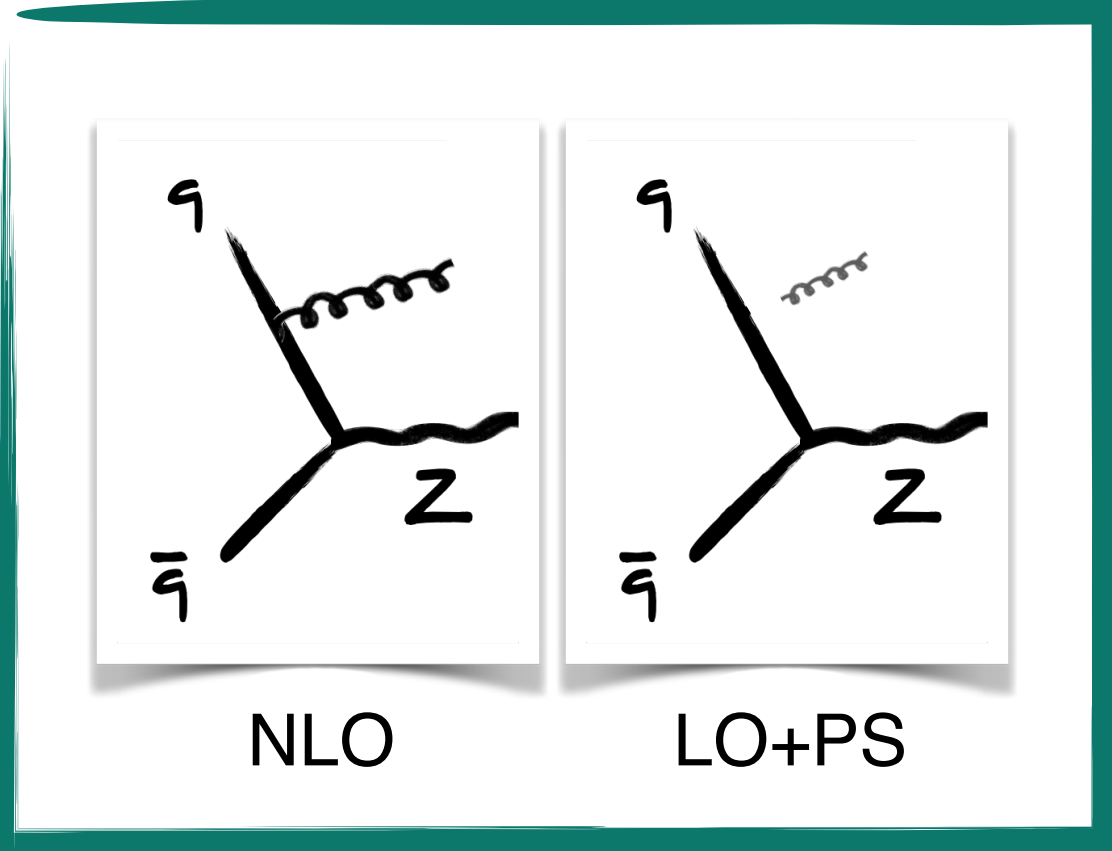
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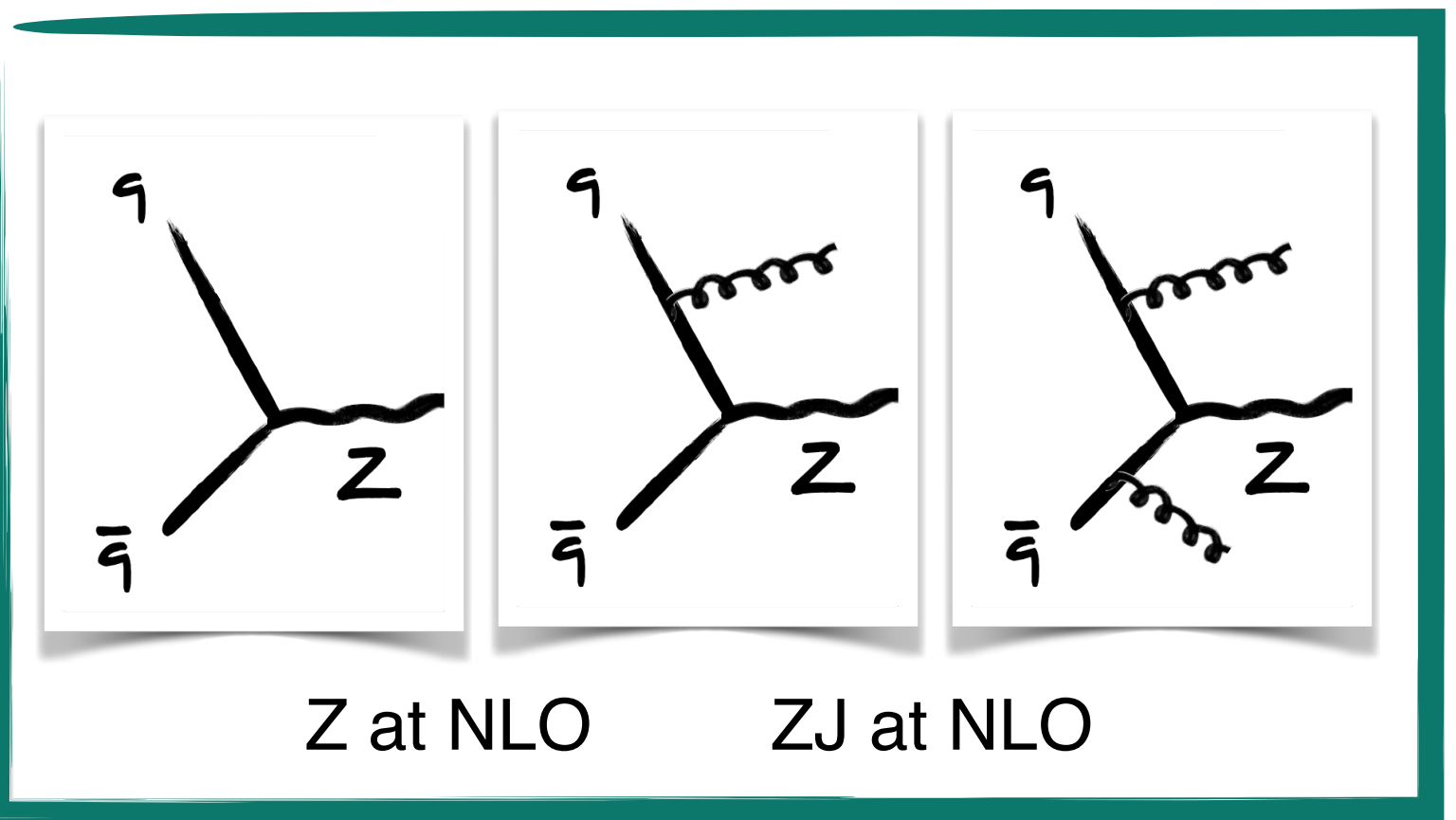
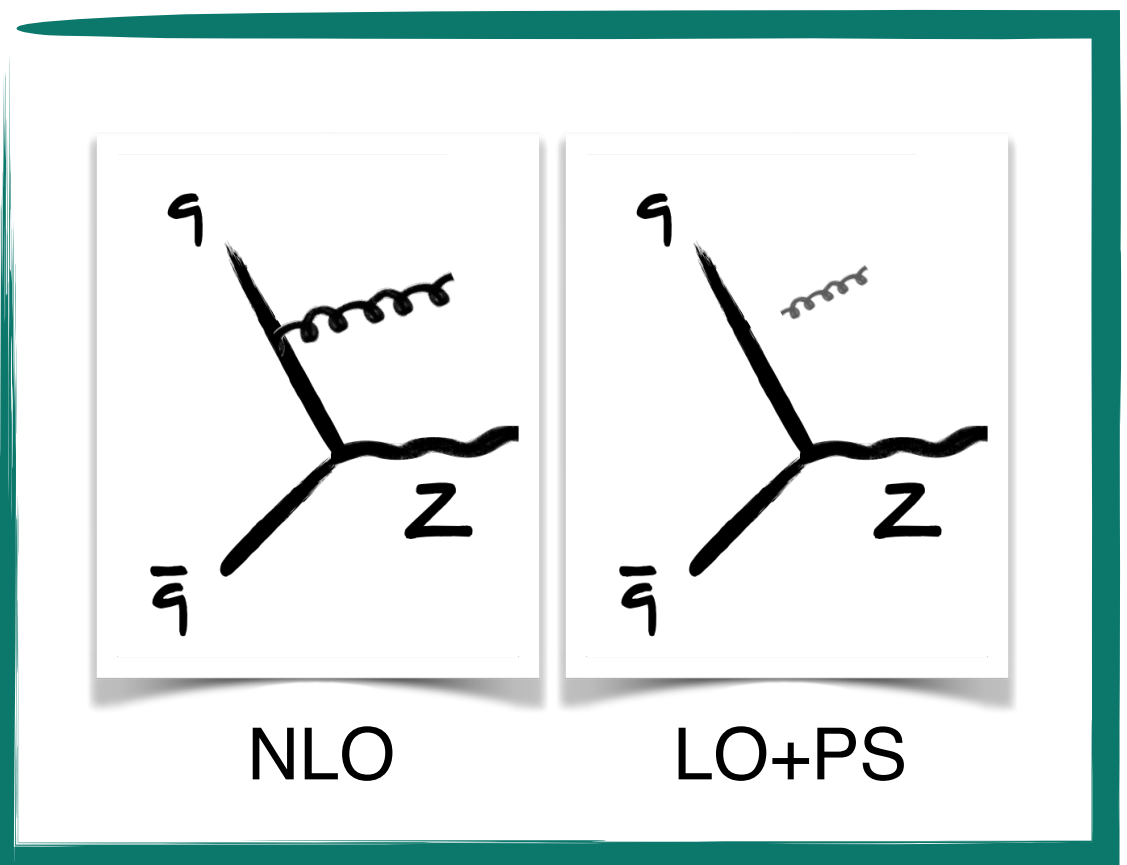
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Master formula



Sudakov form factor includes hardest emission at full NLO accuracy.
→ only use PS below p_T^{min}

4. Phenomenology

4.2 POWHEG MiNNLO_{PS} event generator

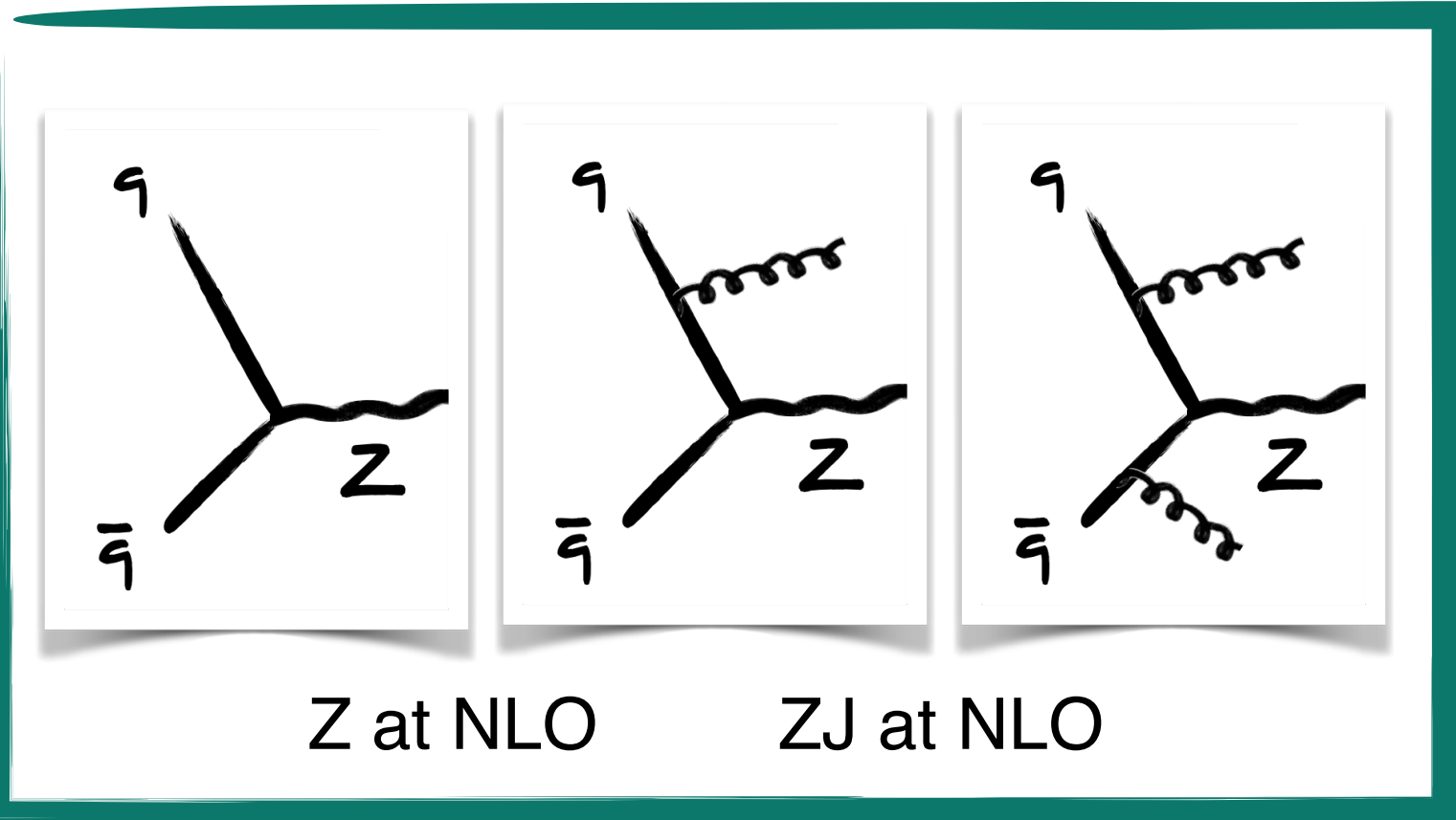
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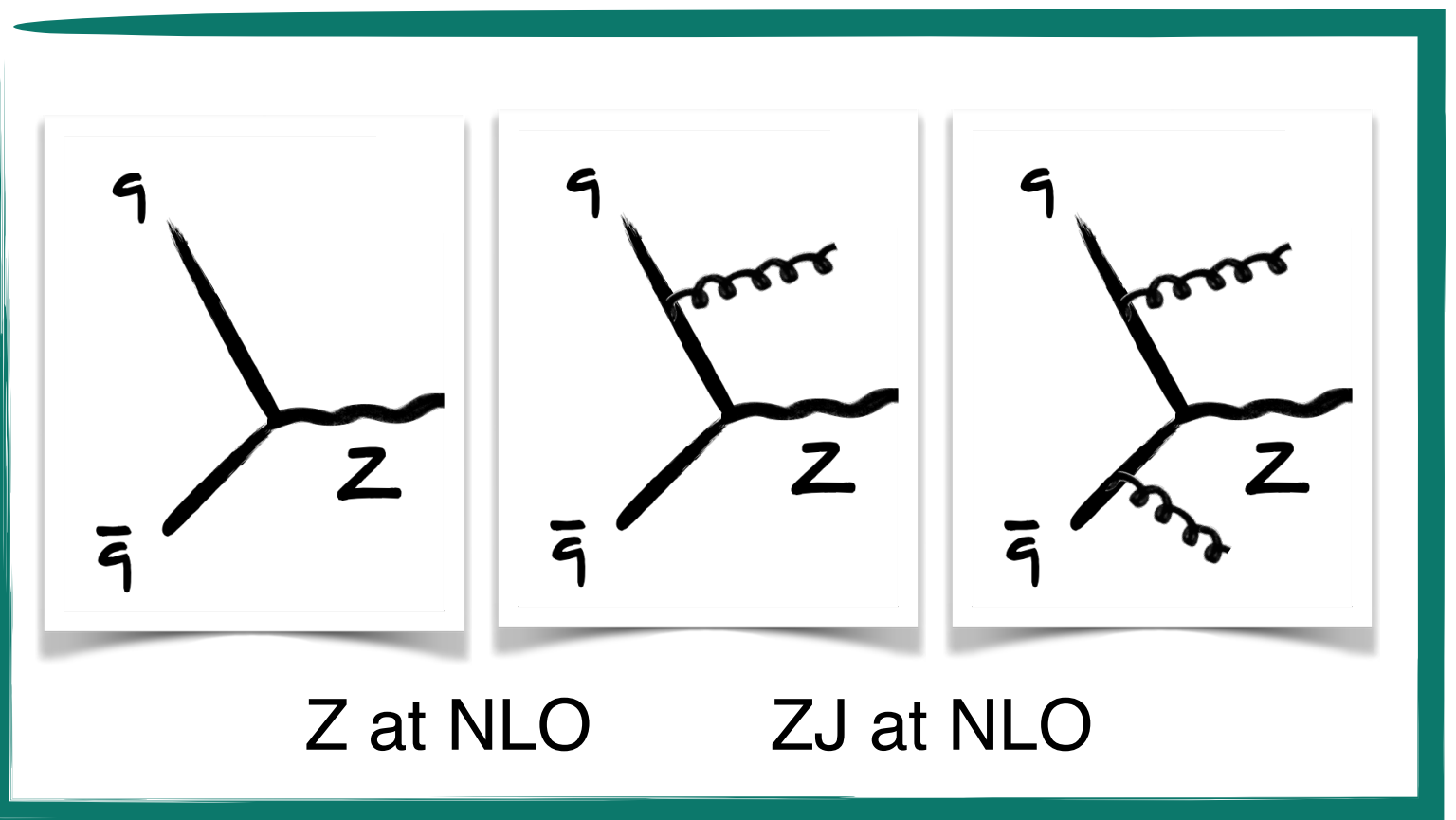
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Subtraction counterterms.

Add (N)NLO terms to retain (N)NLO accuracy when emitted parton has small p_T .

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Master formula for Vh_j



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Master formula for Vh_j

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```
! Switches
SM          0
Linear      1
Quadratic   0
```

```
! Input scheme
InputScheme 2
```

```
! SMEFT
SMEFTScale 1000d0 ! Scale of SMEFT operators

Warsaw      1      ! Switch (on/off)
ChE         0d0    ! SMEFT coefficient
CHl1        0d0    ! SMEFT coefficient
CHl3        0d0    ! SMEFT coefficient
CHq1        0.05d0 ! SMEFT coefficient
```

The code will be released on the **POWHEG webpage!**

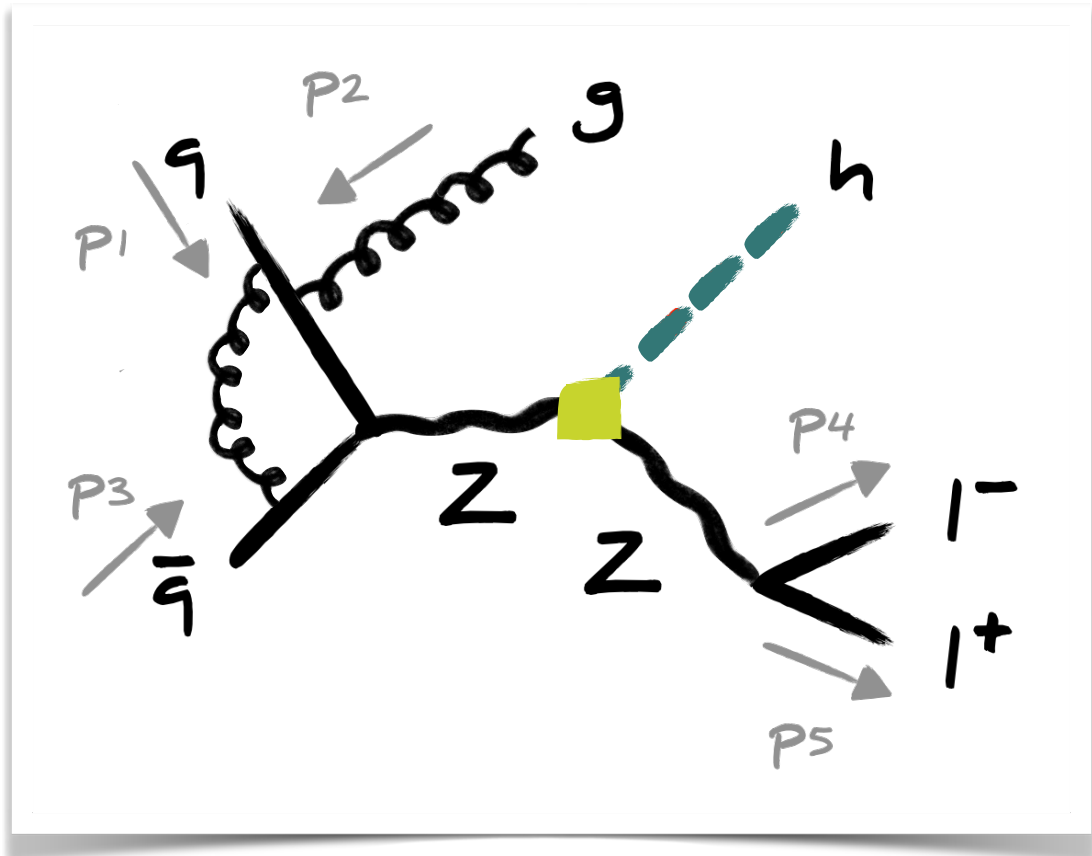
Higher-Order Corrections

$q\bar{q}$ -initiated contributions

... and repeat.

[1112.1531] (T. Gehrmann, L. Tancredi)

$$\mathcal{A}_{B1g1Z} = \alpha \mathcal{A}_\alpha + \beta \mathcal{A}_\beta + \gamma \mathcal{A}_\gamma$$



(B1g1Z)

Loop coefficients:

$$\Omega = I^{(1)}(\epsilon) \Omega^{(0)} + \Omega^{(1), \text{finite}},$$

with $\Omega = \alpha, \beta, \gamma$

$$\Omega^{(1), \text{finite}} = C_A \Omega_1^{(1), \text{finite}} + \frac{1}{C_A} \Omega_2^{(1), \text{finite}} + \beta_0 \Omega_3^{(1), \text{finite}},$$

(same as in the SM)

Helicity amplitudes:

$$\mathcal{A}_{\text{nc}} = \langle 13 \rangle [21] \frac{\langle 14 \rangle [51] + \langle 24 \rangle [52] + \langle 34 \rangle [53]}{2s_{123} \langle 12 \rangle}$$

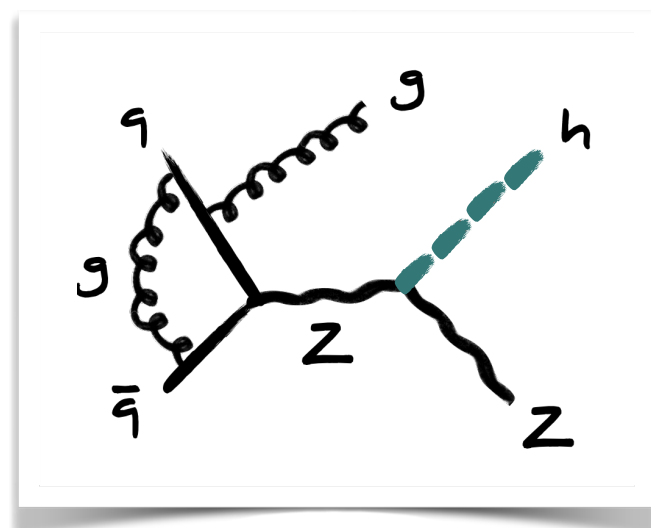
(add contribution, since momentum is carried away by the Higgs and therefore $p_1 + p_2 + p_3 \neq p_4 + p_5$)

Obtain **SMEFT spinor-helicity amplitudes** by un- and recontracting the SM initial-state amplitude.

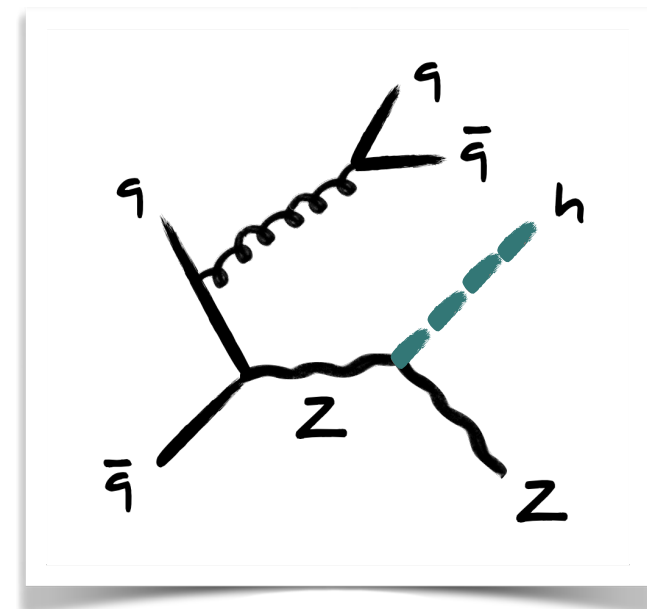
Interesting Aspects of the Calculation

$q\bar{q}$ -initiated contributions

Corrections:

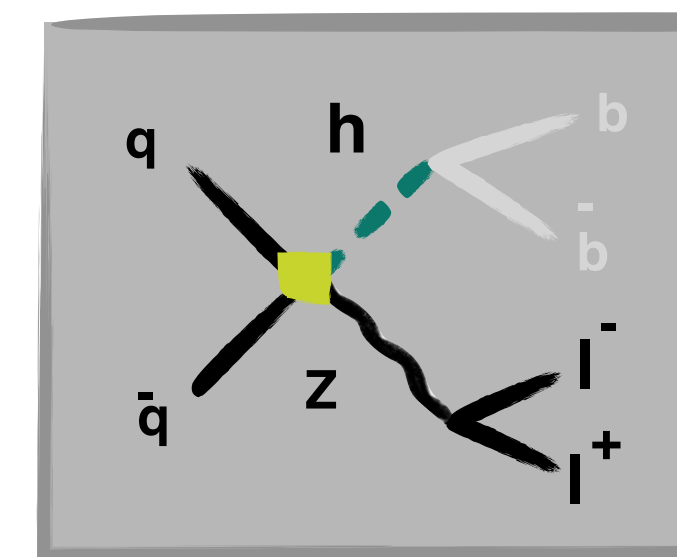
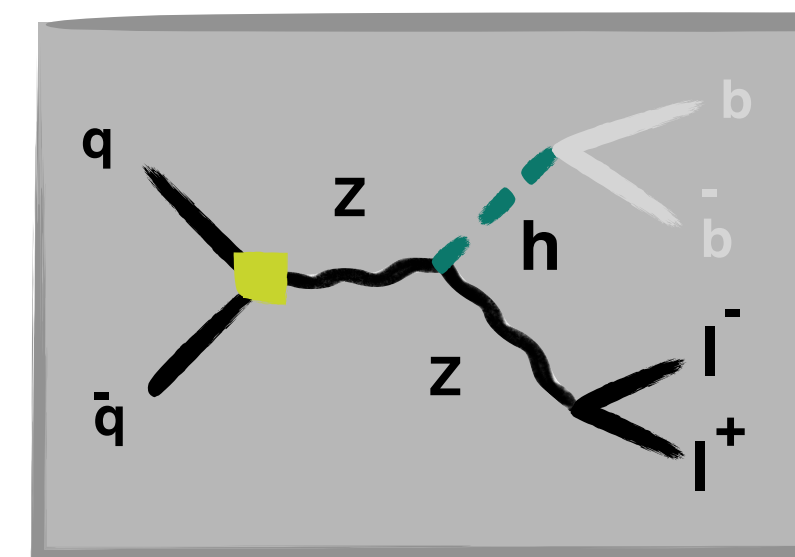


(B-type)



(C,D-type)

Diagrams:



These contributions give **overall factors** to the SM amplitude.

$$B1g0Z = \frac{8\pi\alpha_s C_F}{C_A} \sum_{h_q, h_g, h_\ell = \pm} \left| \frac{g_{Zq}^{h_q} g_{Z\ell}^{h_\ell} g_{hZZ}}{D_Z(s_{23}) D_Z(s_{45})} \mathcal{A}_{B1g0Z} \left(1_q^{h_q}, 2_g^{h_g}, 3_{\bar{q}}^{-h_q}; 4_\ell^{h_\ell}, 5_{\bar{\ell}}^{-h_\ell} \right) \right|^2,$$

$$\delta g_{Zd}^{(1)-} = \frac{v^2 g_+}{2} \left(C_{Hq}^{(1)} + C_{Hq}^{(3)} \right), \quad \delta g_{Zu}^{(1)-} = \frac{v^2 g_+}{2} \left(C_{Hq}^{(1)} - C_{Hq}^{(3)} \right),$$

Direct contributions

$$\left(\frac{\delta g_{hZq}^{(1)h_q} g_{Z\ell}^{h_\ell}}{D_Z(s_{45})} + \frac{g_{Zq}^{h_q} \delta g_{hZ\ell}^{(1)h_\ell}}{D_Z(s_{123})} \right) \mathcal{A}_{B1g0Z} \left(1_q^{h_q}, 2_g^{h_g}, 3_{\bar{q}}^{-h_q}; 4_\ell^{h_\ell}, 5_{\bar{\ell}}^{-h_\ell} \right),$$

„Quartic“ contributions

(+ input scheme corrections)

Details of the calculation

The POWHEG method

$$\sigma_{\text{NLO}} = \int d\Phi_n \mathcal{L} \left[\mathcal{B}(\Phi_n) + \mathcal{V}_b(\Phi_n) \right] + \int d\Phi_{n+1} \mathcal{L} \mathcal{R}(\Phi_{n+1}) \\ + \int d\Phi_{n,\oplus} \mathcal{L} \mathcal{G}_{\oplus,b}(\Phi_{n,\oplus}) + \int d\Phi_{n,\ominus} \mathcal{L} \mathcal{G}_{\ominus,b}(\Phi_{n,\ominus}),$$

→ how to deal with IR singularities?

Soft/collinear
divergences

Subtraction:

$$\bar{B}(\mathbf{P}_F) \equiv B(\mathbf{P}_F) + V(\mathbf{P}_F) \\ + \sum_{\alpha} \int d\Phi_{\text{rad}}^{(\alpha)} \left(R^{(\alpha)}(\vec{\mathbf{P}}_{FJ}^{(\alpha)}) - C^{(\alpha)}(\vec{\mathbf{P}}_{FJ}^{(\alpha)}) \right) \\ + \sum_{\alpha_{\oplus}} \int \frac{dz}{z} G_{\oplus}^{(\alpha_{\oplus})}(\{\mathbf{P}_F, z\}) + \sum_{\alpha_{\ominus}} \int \frac{dz}{z} G_{\ominus}^{(\alpha_{\ominus})}(\{\mathbf{P}_F, z\}).$$

→ **inclusive** (N)NLO

$$\langle \mathcal{O} \rangle_{\text{NLO}} = \int d\Phi_F \bar{B}(\mathbf{P}_F) \left[\Delta_{\text{pwg}}(\mathbf{P}_F, p_{T,\text{pwg}}) \mathcal{O}(\Phi_F) \right. \\ \left. + \sum_{\alpha} \int_{p_{T,\text{pwg}}} d\Phi_{\text{rad}}^{(\alpha)} \frac{R^{(\alpha)}(\vec{\mathbf{P}}_{FJ}^{(\alpha)})}{B(\mathbf{P}_F)} \Delta_{\text{pwg}}(\mathbf{P}_F, q_{T,\text{rad}}^{(\alpha)}) \mathcal{O}(\vec{\Phi}_{FJ}^{(\alpha)}) \right]$$

Master formula

Sudakov form factor:

$$\Delta_{\text{pwg}}(\mathbf{P}_F, p_{T,\text{pwg}}) \equiv \exp \left[- \sum_{\alpha} \int d\Phi_{\text{rad}}^{(\alpha)} \frac{R^{(\alpha)}(\vec{\mathbf{P}}_{FJ}^{(\alpha)}) \theta(q_{T,\text{rad}}^{(\alpha)} - p_{T,\text{pwg}})}{B(\mathbf{P}_F)} \right],$$

→ **exclusive** above p_T^{min}

→ **parton shower** for radiation below p_T^{min}

Operators considered in our work

$$Q_{H\Box} = (H^\dagger H) \Box (H^\dagger H)$$

$$Q_{HD} = (H^\dagger D_\mu H)^* (H^\dagger D^\mu H)$$

$$Q_{bH} = y_b (H^\dagger H) \bar{q}_L b_R H$$

$$Q_{bG} = \frac{g_s^3}{(4\pi)^2} y_b \bar{q}_L \sigma_{\mu\nu} T^a b_R H G^{a,\mu\nu}$$

$$Q_{HG} = \frac{g_s^2}{(4\pi)^2} (H^\dagger H) G_{\mu\nu}^a G^{a,\mu\nu}$$

$$Q_{3G} = \frac{g_s^3}{(4\pi)^2} f^{abc} G_\mu^{a,\nu} G_\nu^{b,\sigma} G_\sigma^{c,\mu}$$

Operators normalised such that Wilson coefficients are expected to be of $O(1)$ in UV-complete weakly-coupled BSM models

Factorisable contributions

Since operators $Q_{H\Box}$, Q_{HD} & Q_{bH} do not contain a gluon, associated SMEFT effects factorise to all orders in strong coupling constant. SMEFT results can be obtained from SM matrix elements by following simple replacement:

$$y_b^2 \rightarrow y_b^2 \left\{ 1 + \frac{2v^2}{\Lambda^2} \left[C_{H\Box} - \frac{C_{HD}}{4} - \text{Re}(C_{bH}) \right] \right\}$$



corrections due to
Higgs wave function



correction due to
Yukawa operator

Factorisable contributions

For example in case of partial $h \rightarrow b\bar{b}$ decay rate factorisable corrections are:

$$\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{\text{fac}} = \frac{3y_b^2 m_h}{16\pi} \left\{ 1 + \frac{2v^2}{\Lambda^2} \left[C_{H\Box} - \frac{C_{HD}}{4} - \text{Re}(C_{bH}) \right] \right\} \\ \times \left[1 + \frac{\alpha_s}{\pi} 5.67 + \left(\frac{\alpha_s}{\pi} \right)^2 29.15 \right]$$

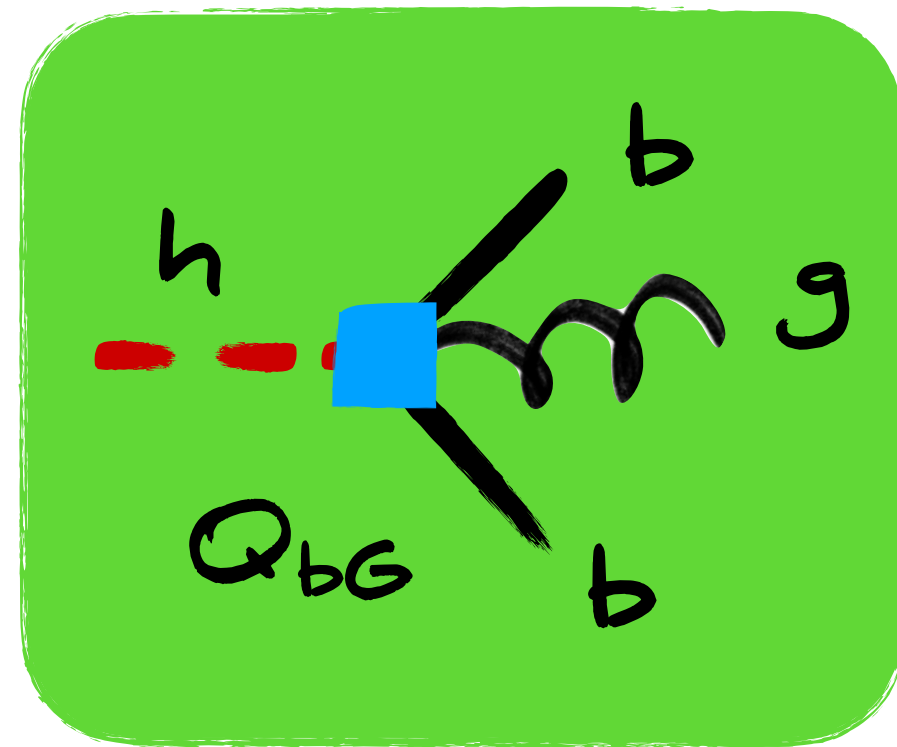


NLO & NNLO QCD
correction in SM

[in principle extension to N⁴LO possible using SM results given in Baikov et al., hep-ph/0511063; Herzog et al., 1707.01044]

Non-factorisable contributions

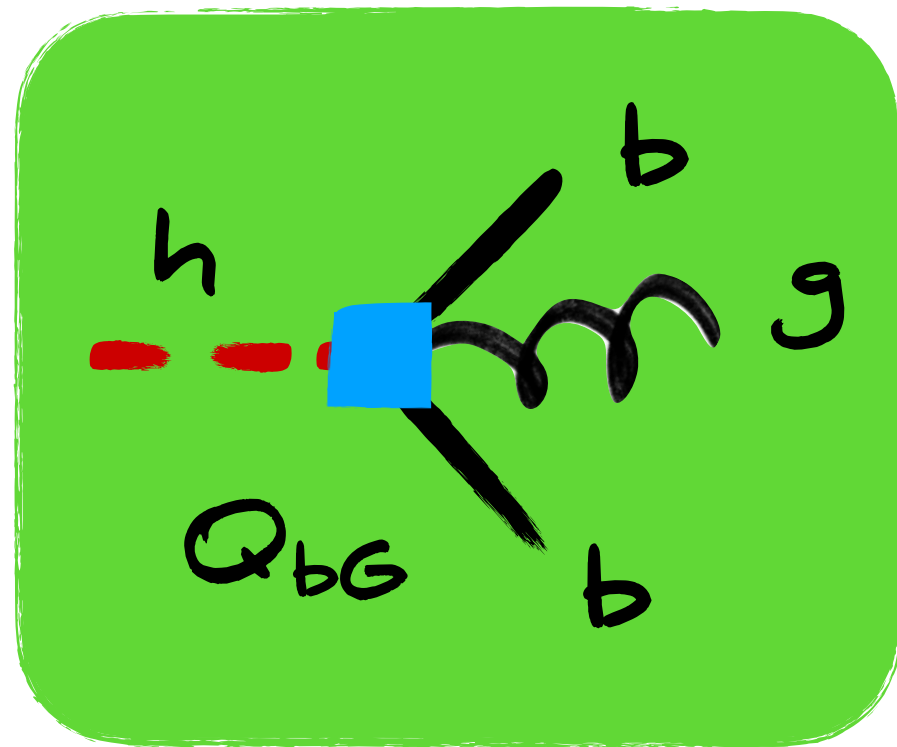
Dominant non-factorisable corrections arise from dipole operator Q_{bG} :



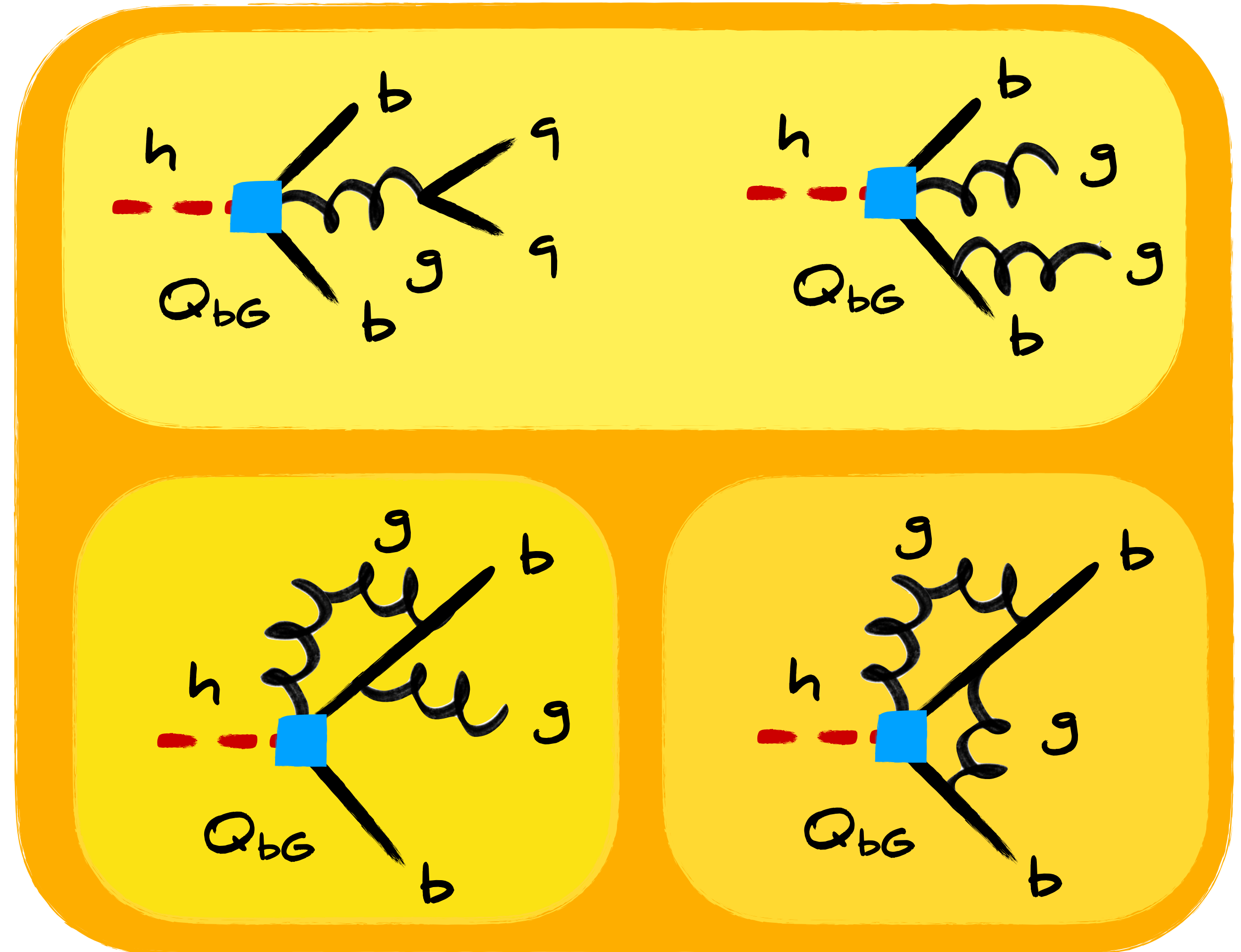
leading contribution from
interference of $h \rightarrow b\bar{b}g$
amplitude in SMEFT & SM

Non-factorisable contributions

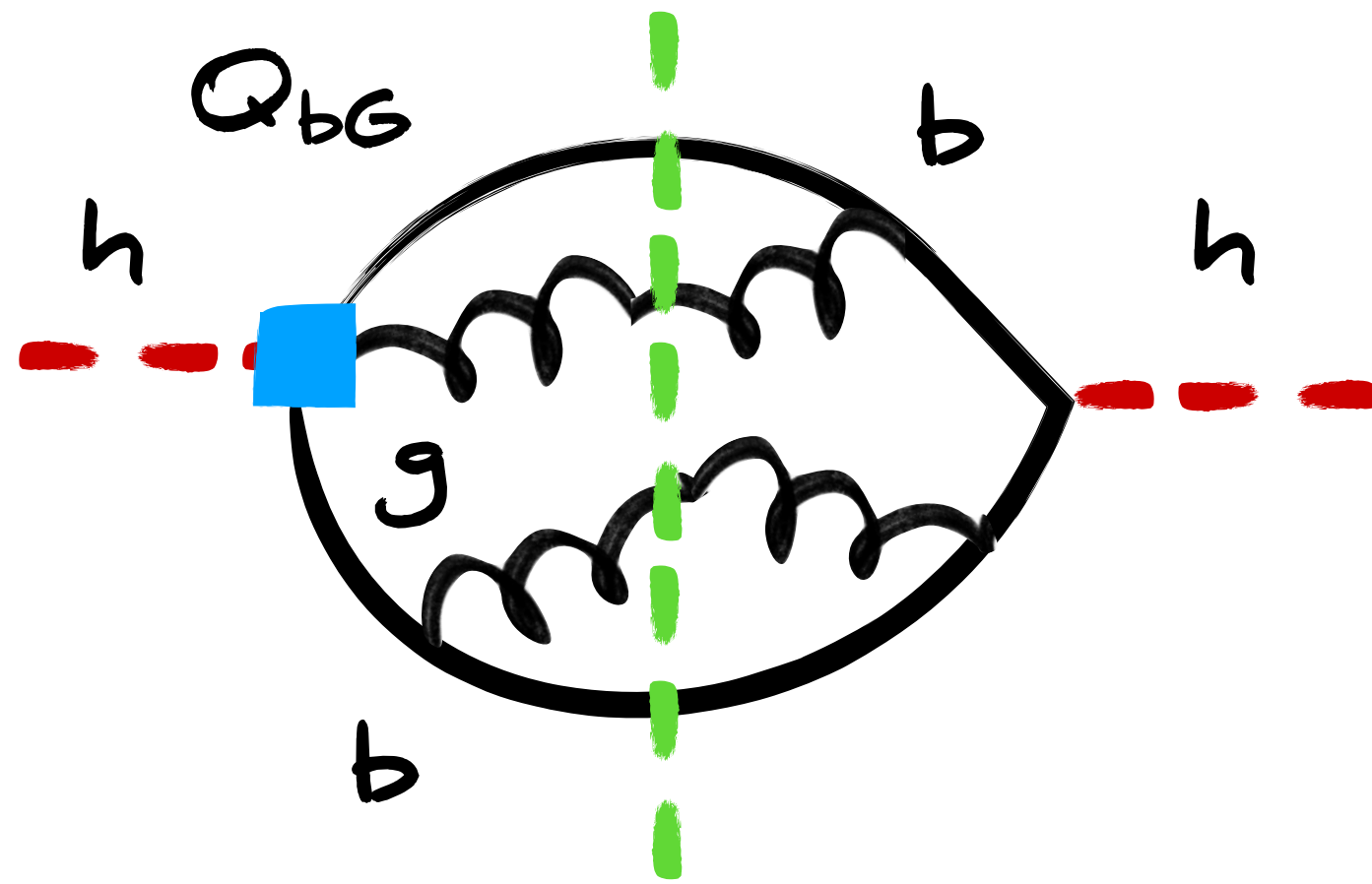
Dominant non-factorisable corrections arise from dipole operator Q_{bG} :



beyond leading order, double
real, 1-loop single real &
2-loop virtual contributions



Non-factorisable contributions



$$\begin{aligned}
 f_{bb\bar{b}gg}(p_1, p_2, p_3, p_4) = & \frac{4y_{24}^2}{y_{23}y_{34}y_{234}} + \frac{y_{13}^2 y_{24}^2}{2y_{14}y_{23}y_{34}y_{134}y_{234}} + \frac{(10}{ \\
 & + \frac{(4y_{24} + 19y_{34} - 4)y_{24}}{y_{23}y_{134}y_{234}} + \frac{(4y_{14}(y_{23} + 2) + y_{13}(12y_{24} + 7))}{2y_{34}y_{134}y_{234}} \\
 & - \frac{2y_{34}^2}{y_{13}y_{14}y_{134}} + \frac{y_{34}^2(y_{23} + y_{24} + y_{34} - 1)}{y_{13}y_{14}y_{23}y_{134}} + \frac{y_{34}^2(y_{23} + 3y_{24} +}{ \\
 & + \frac{18y_{34} + 2y_{24}(4y_{13} + 2y_{23} + 2y_{24} + 2y_{34} + 19) - 3}{2y_{134}y_{234}} + \frac{12y_{14}}{ \\
 & + \frac{2y_{14}y_{24}(2y_{24} + 3y_{34} - 1) + y_{34}(3y_{34}^2 + (9y_{24} - 2)y_{34} + 4}{y_{13}y_{23}y_{134}y_{234}}
 \end{aligned}$$

Non-factorisable contributions

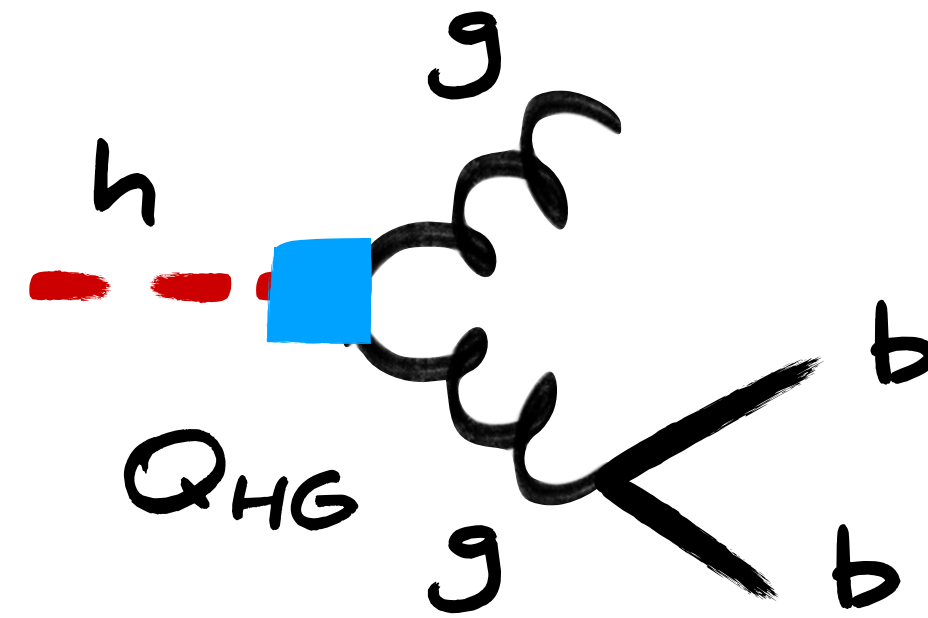
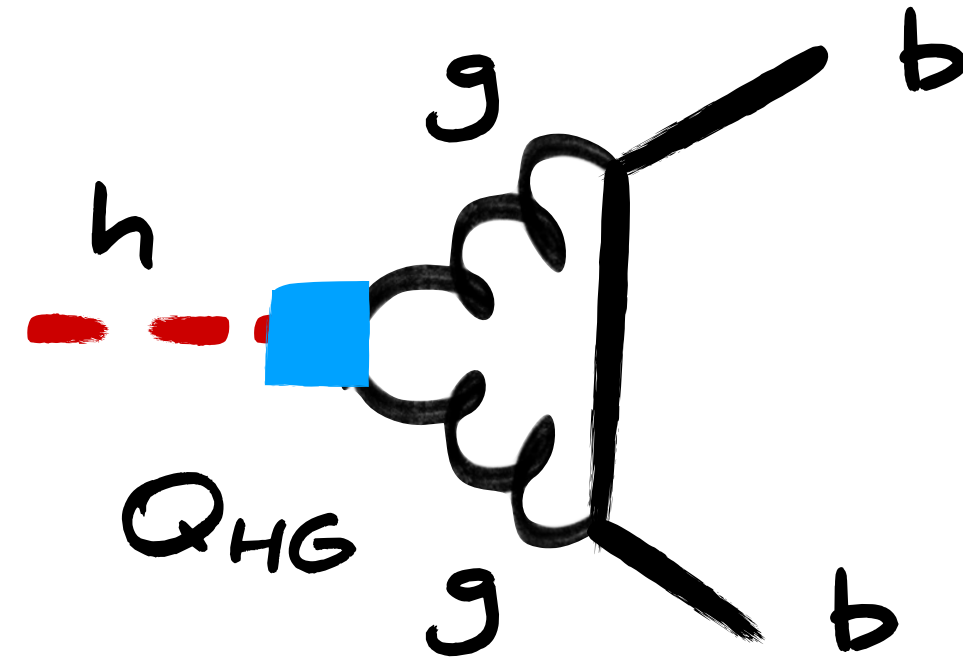
Q_{bG} corrections implemented into POWHEG-BOX. Possible to obtain realistic exclusive description of $pp \rightarrow Zh \rightarrow l^+l^-b\bar{b}$ production with NNLO accuracy using MiNLO' & MiNNLO_{PS} methods. Applying code to Higgs decay leads to:

$$\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{\text{non}} = \frac{3y_b^2 m_h}{16\pi} \left(\frac{\alpha_s}{\pi}\right)^2 \frac{m_h^2}{3v^2} \left[1 + \frac{\alpha_s}{\pi} 17.32\right] \frac{v^2}{\Lambda^2} \text{Re}(C_{bG})$$



new term represents
a 60% correction

Contributions from Q_{HG}

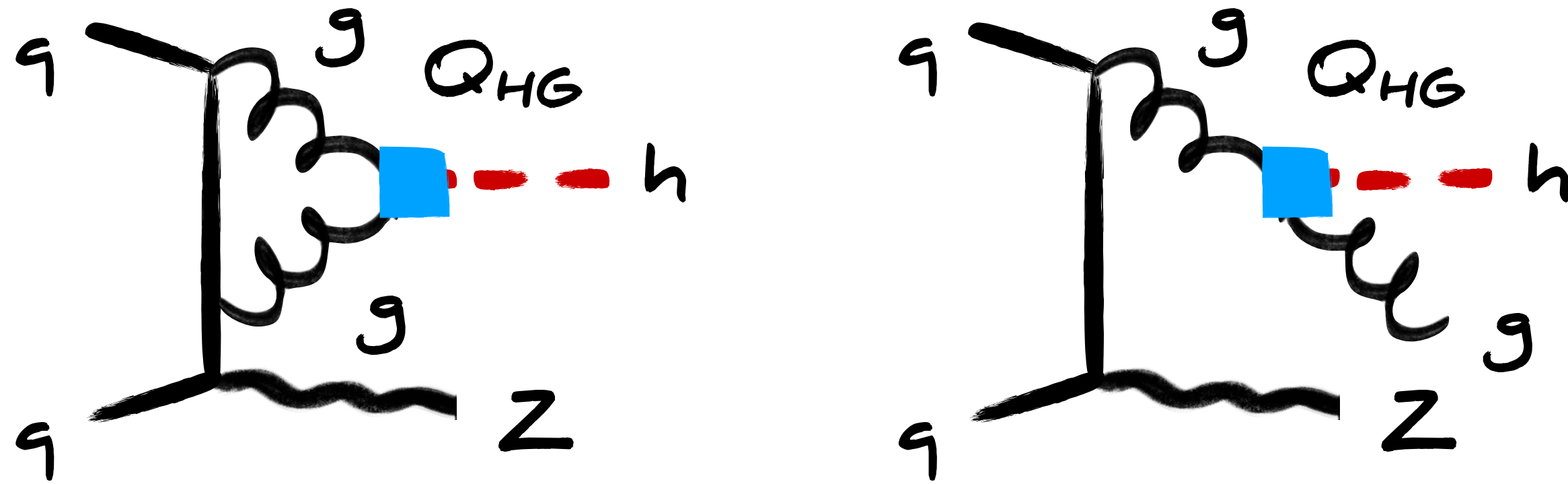


$$c_{HG} = \frac{v^2}{\Lambda^2} C_{HG} \in [-0.09, 0.06]$$

[Ellis et al., 2012.02779]

$$\frac{\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{HG}}{\Gamma(h \rightarrow b\bar{b})_{\text{SM}}^{\text{LO}}} = \left(\frac{\alpha_s}{\pi}\right)^2 \left[\frac{19}{3} - 2\zeta_2 + \frac{1}{3} \ln^2 \left(\frac{m_b^2}{m_h^2} \right) \right] c_{HG} \in [-2.7, 1.7] \cdot 10^{-3}$$

Contributions from Q_{HG}



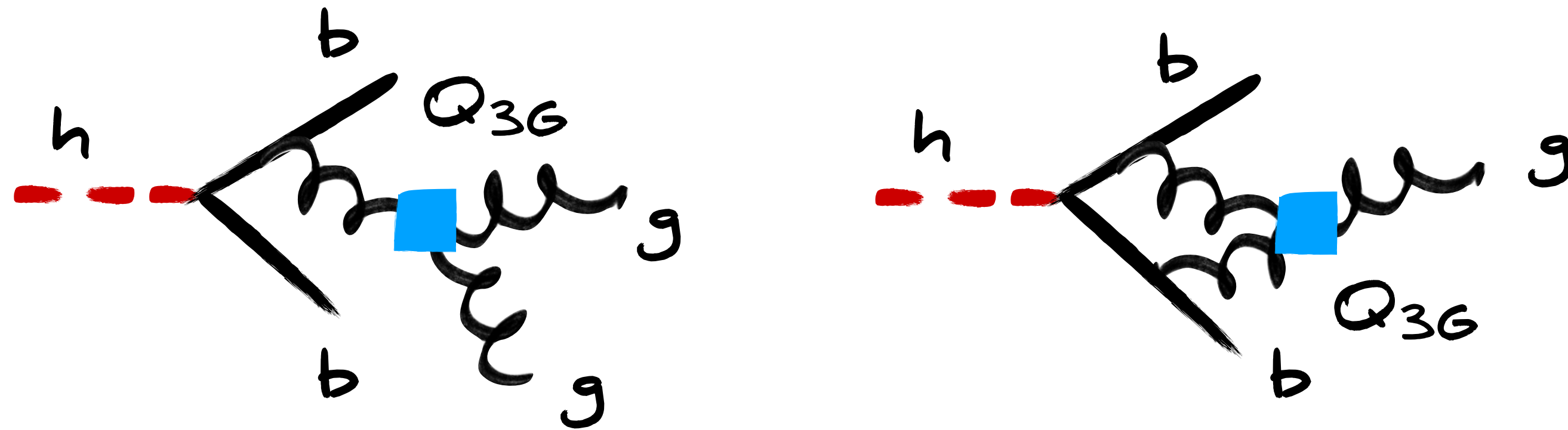
$$c_{HG} = \frac{v^2}{\Lambda^2} C_{HG} \in [-0.09, 0.06]$$

[Ellis et al., 2012.02779]

$$\frac{\sigma(pp \rightarrow hZ)_{\text{SMEFT}}^{HG}}{\sigma(pp \rightarrow hZ)_{\text{SM}}^{\text{LO}}} = 3 \left(\frac{\alpha_s}{\pi} \right)^2 \delta c_{HG} \in [-3.9, 2.4] \cdot 10^{-3}$$

numerically, one has $\delta = 10.7$

Contributions from Q_{3G}



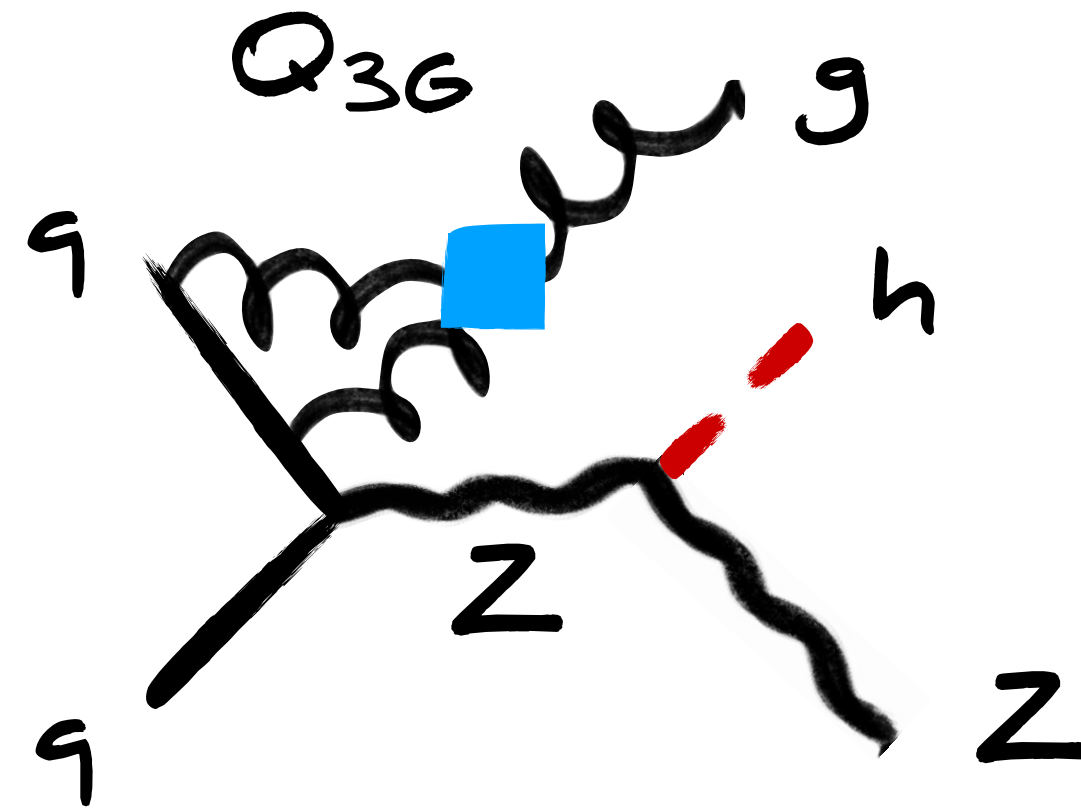
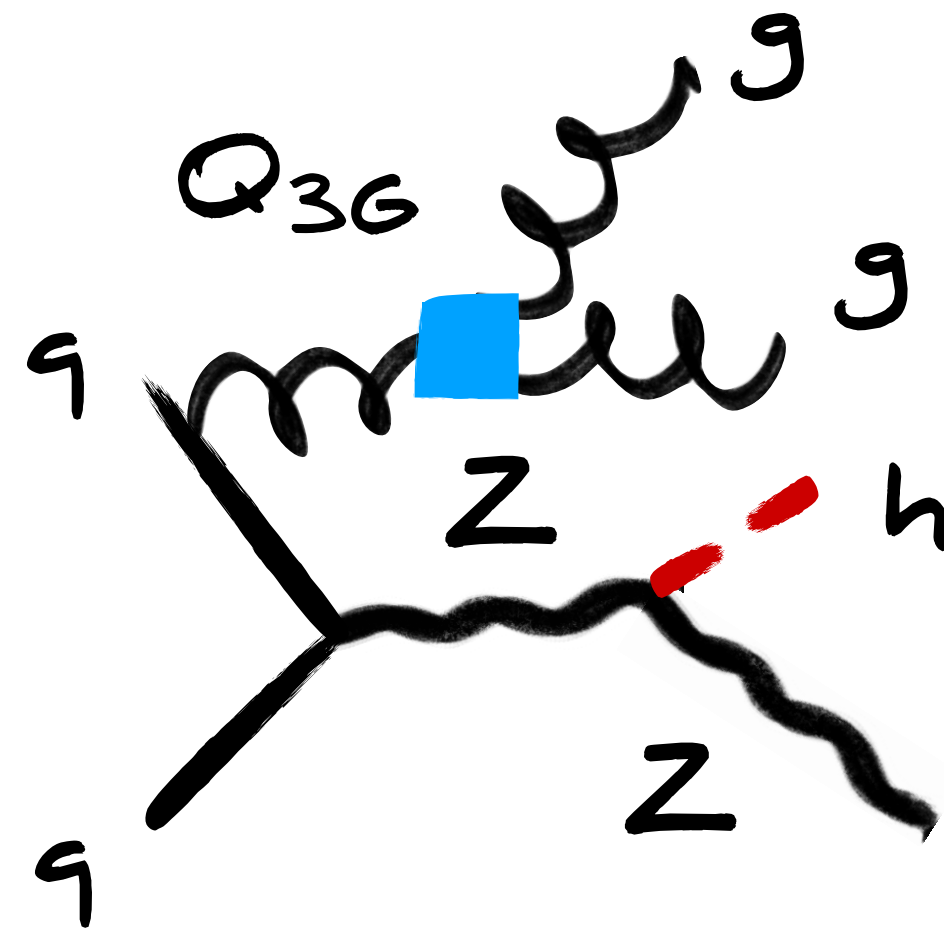
$$c_{3G} = \frac{v^2}{\Lambda^2} C_{3G} \in [-12.5, -4.1]$$

[Ellis et al., 2012.02779]

$$\frac{\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{3G}}{\Gamma(h \rightarrow b\bar{b})_{\text{SM}}^{\text{LO}}} = N_{3G}^{\text{dec}} \left(\frac{\alpha_s}{\pi}\right)^2 \frac{m_h^2}{v^2} c_{3G} \in [-0.3, -0.1] \cdot 10^{-3}$$

explicit calculation gives $N_{3G}^{\text{dec}} = 2.23$

Contributions from Q_{3G}



$$c_{3G} = \frac{v^2}{\Lambda^2} C_{3G} \in [-12.5, -4.1]$$

[Ellis et al., 2012.02779]

$$\frac{\sigma(pp \rightarrow hZ)_{\text{SMEFT}}^{3G}}{\sigma(pp \rightarrow hZ)_{\text{SM}}^{\text{LO}}} = N_{3G}^{\text{prod}} \left(\frac{\alpha_s}{\pi} \right)^3 c_{3G} \in [-5.8, -1.9] \cdot 10^{-3}$$

quoted number corresponds to $N_{3G}^{\text{prod}} = 10$

Phenomenology analysis

We have seen that QCD corrections associated to operators other than $Q_{H\Box}$, Q_{HD} , Q_{bH} & Q_{bG} do not exceed level of a few permille

Maximal size of factorisable corrections to partial $h \rightarrow b\bar{b}$ decay rate can be derived from global fits of SMEFT Wilson coefficients:

$$\frac{\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{\text{N}^3\text{LO}}}{\Gamma(h \rightarrow b\bar{b})_{\text{SM}}^{\text{N}^3\text{LO}}} - 1 \in [-39, 26]\% \quad \text{for} \quad c_{bH} = \frac{v^2}{\Lambda^2} \text{Re}(C_{bH}) \in [-0.13, 0.20]$$

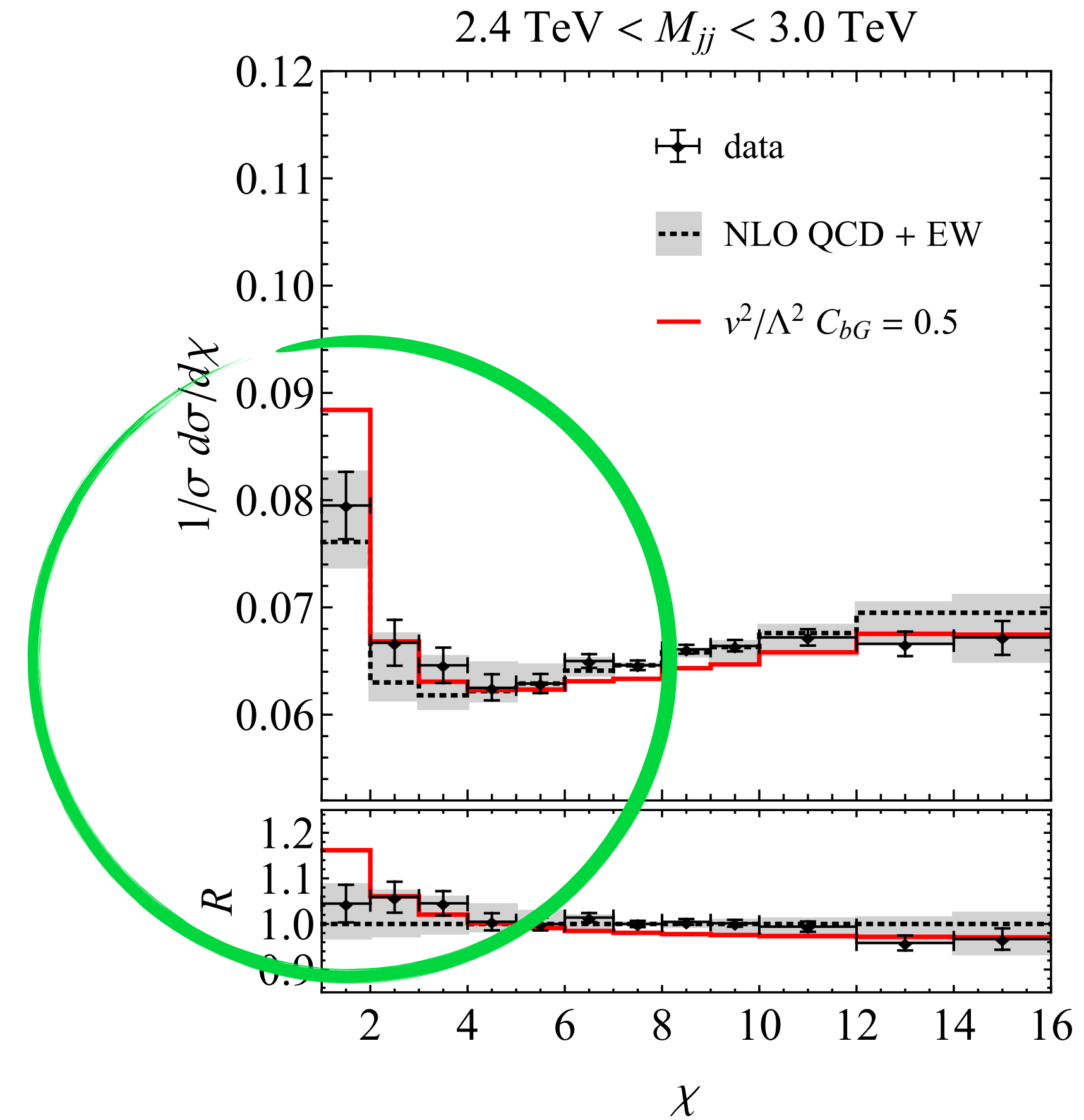
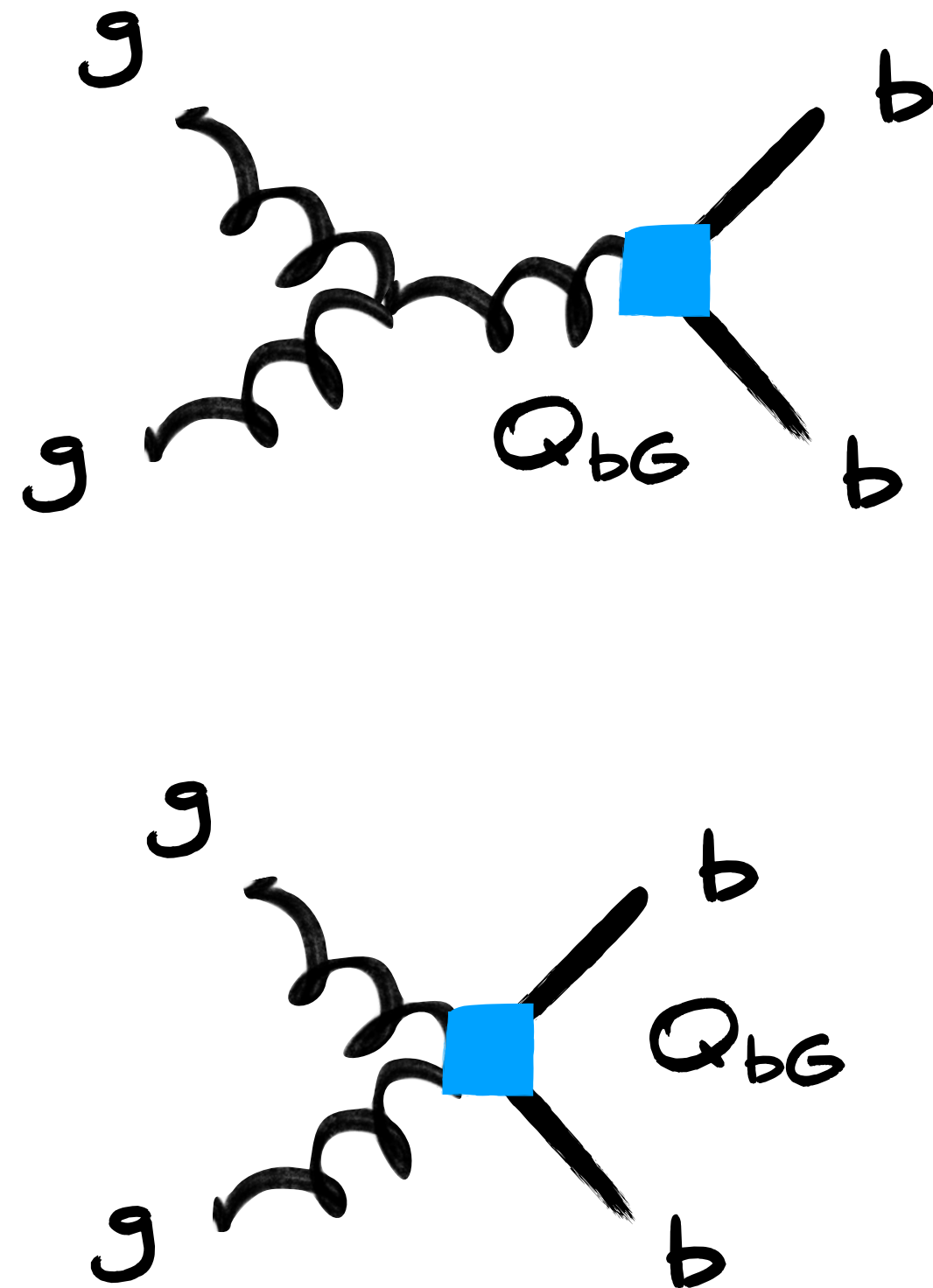
[Ellis et al., 2012.02779]

Interlude: bounds on dipole operator Q_{bG}

Observable	Wilson coefficient	95% CL bound
Dijet angular distributions	$ c_{bG} $	2864
Two b -tagged jets	$ c_{bG} $	152
Z -boson production with two b -jets	$ c_{bG} $	438
Searches for neutron electric dipole moment	$ \text{Im}(c_{bG}) $	0.05

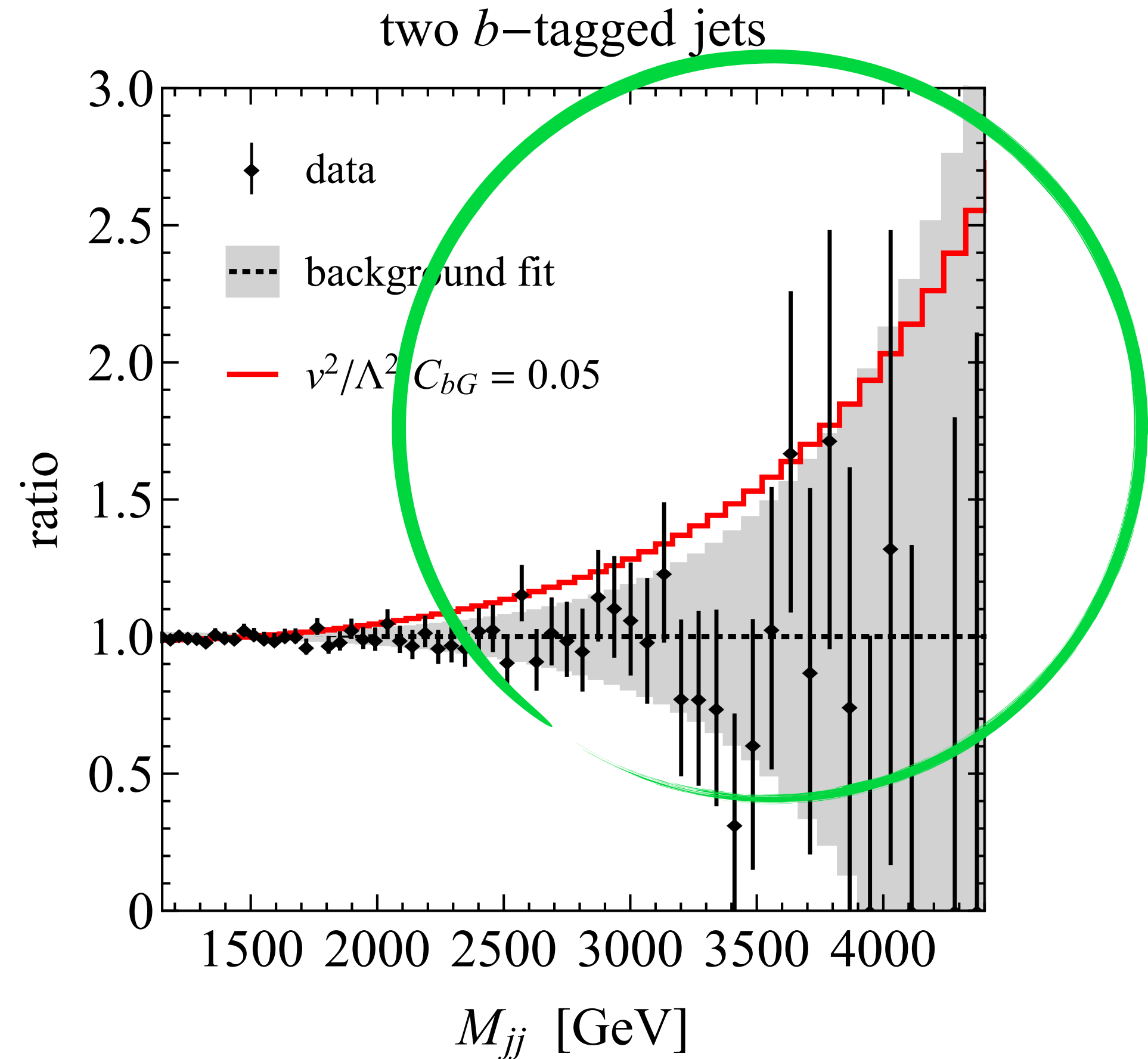
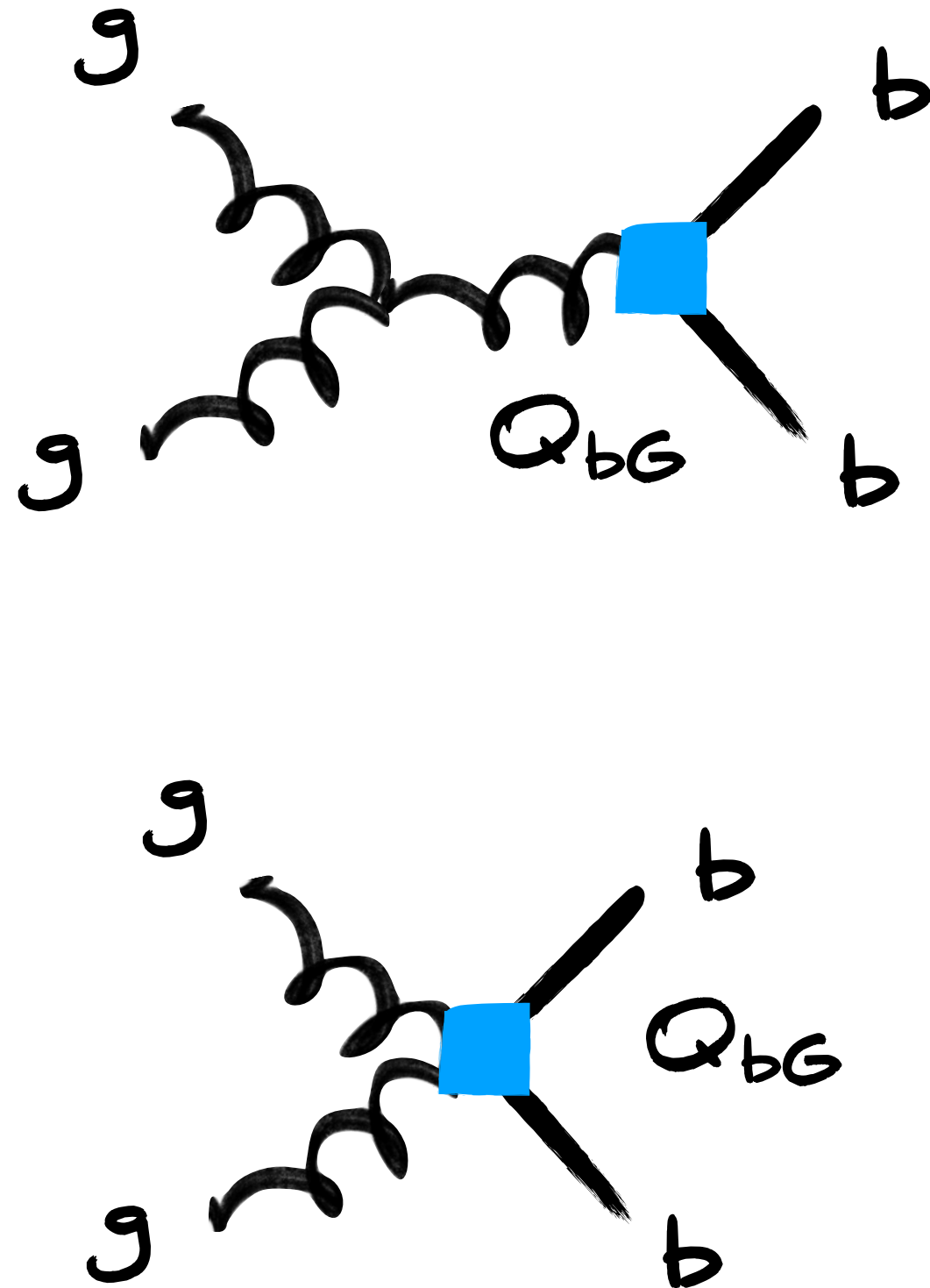
Due to chirality-flipping nature of Q_{bG} no interference between SMEFT & SM amplitudes for $m_b = 0$. Resulting LHC bounds on $|c_{bG}|$ thus very weak. $|\text{Im}(c_{bG})|$ instead severely constrained by neutron electric dipole moment

Bounds on dipole-type operator Q_{bG}



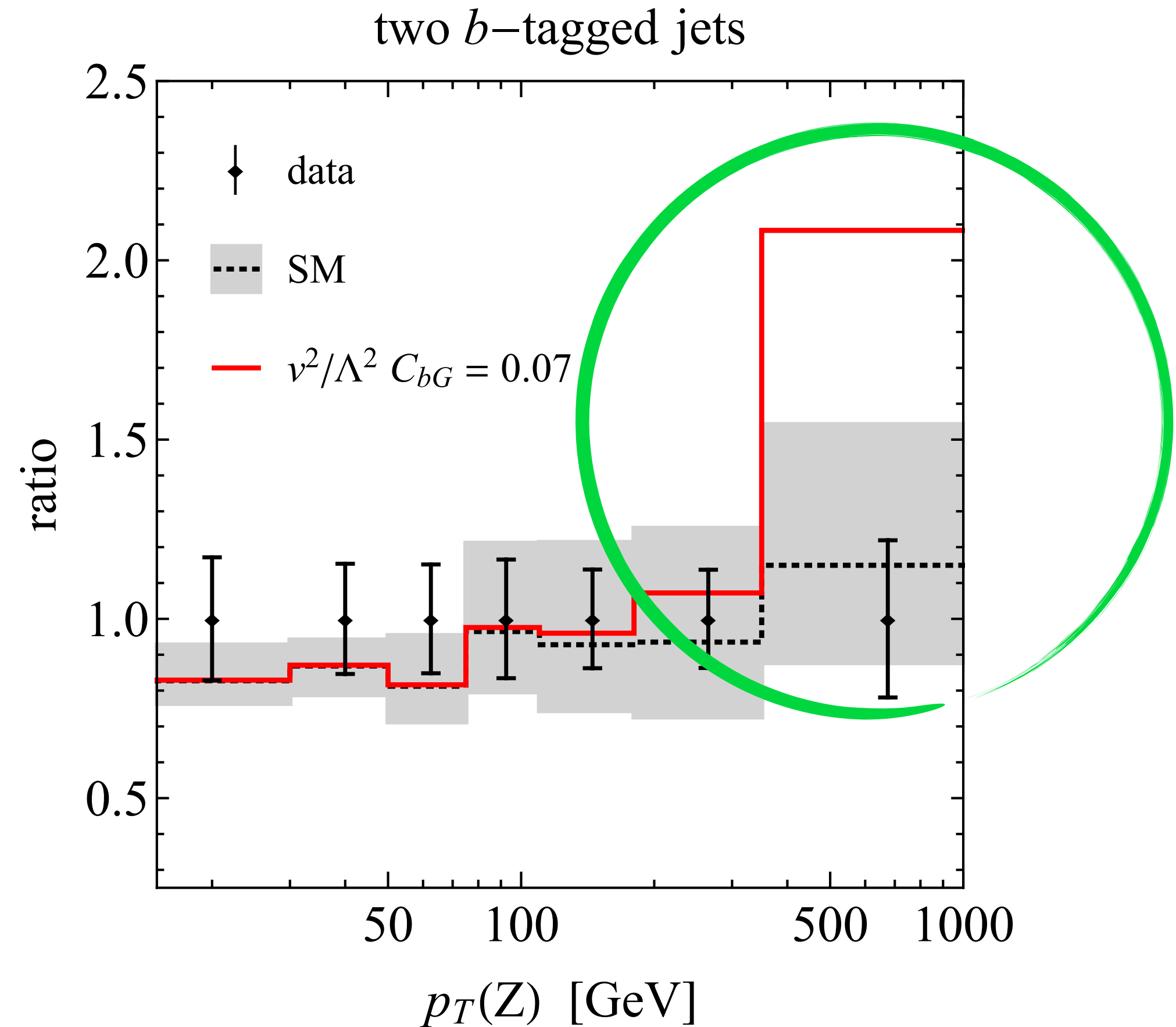
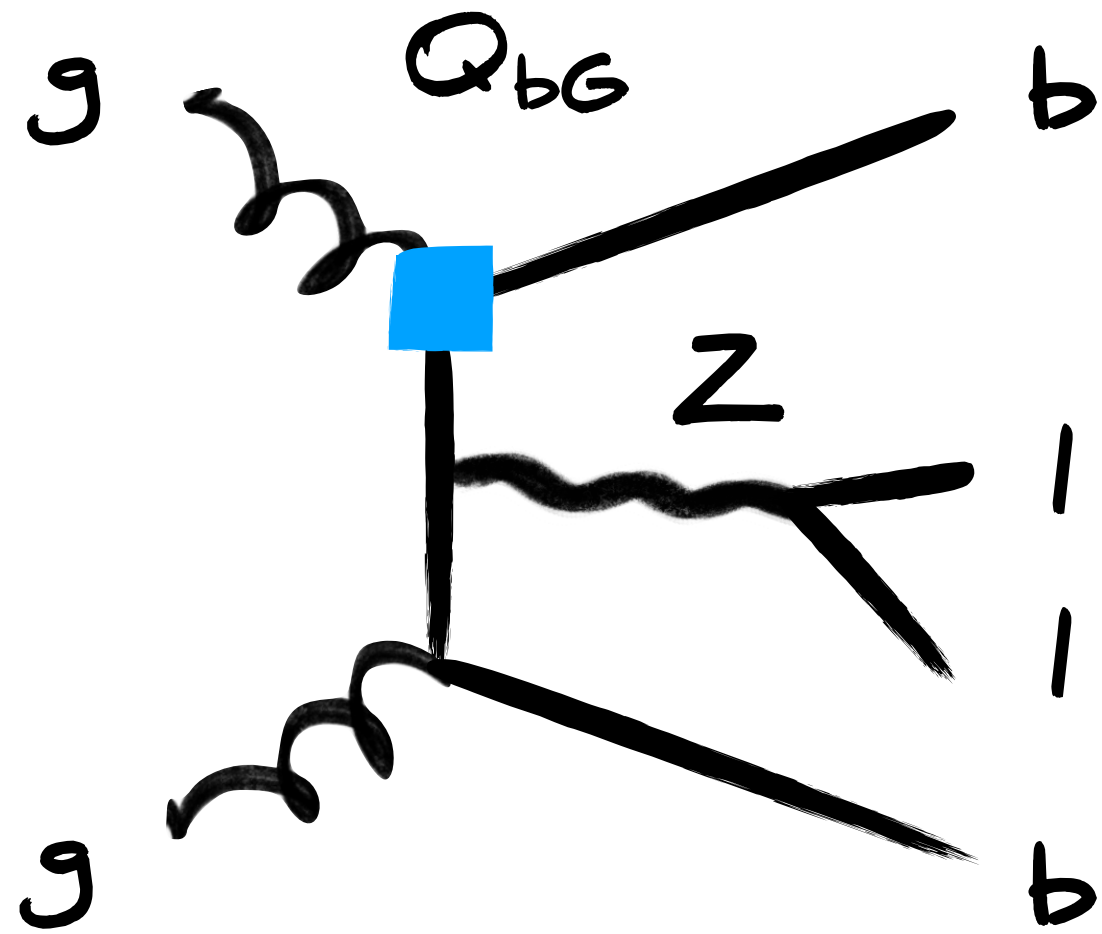
Q_{bG} contributions lead to an enhanced activity of high-energy jets in central region

Bounds on dipole-type operator Q_{bG}



Q_{bG} contributions lead to an enhancement of rate for high dijet invariant masses

Bounds on dipole-type operator Q_{bG}



Q_{bG} effects grow with transverse momentum & lead to more events at high $p_T(Z)$

Phenomenology analysis

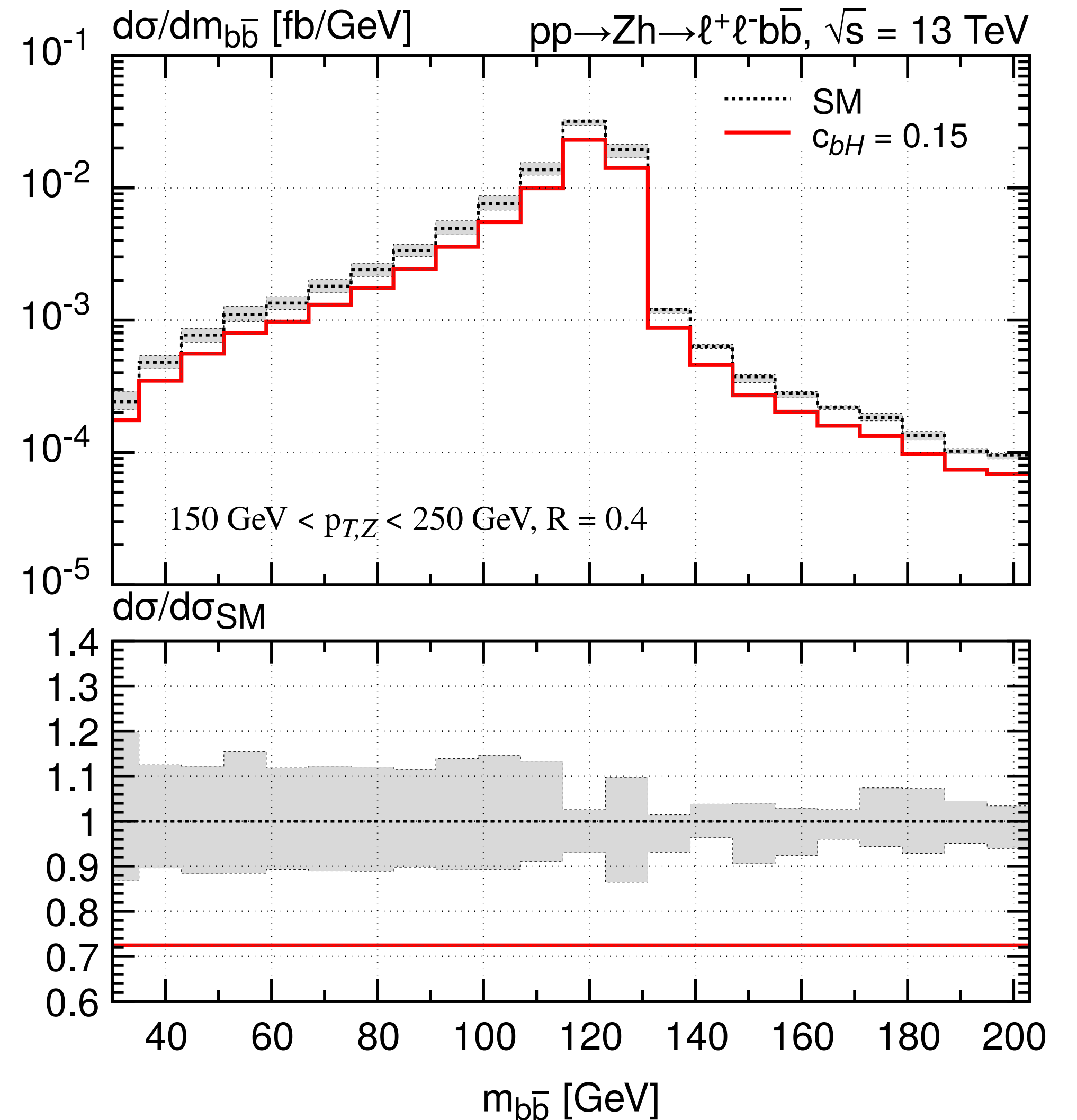
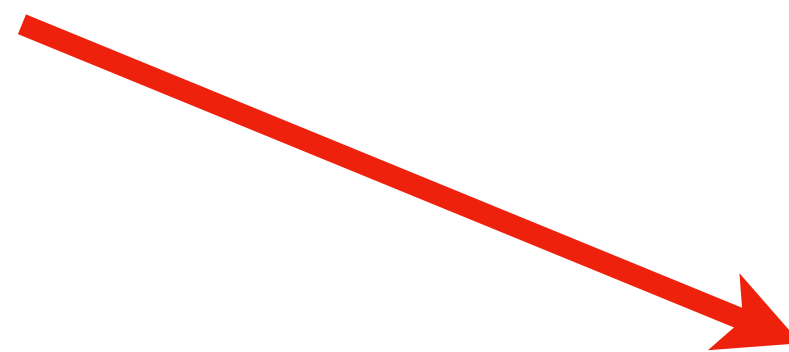
Despite large Wilson coefficient of Q_{bG} possible size of non-factorisable contributions to partial $h \rightarrow b\bar{b}$ decay rate smaller than that of factorisable ones by a factor of $O(5)$:

$$\frac{\Gamma(h \rightarrow b\bar{b})_{\text{SMEFT}}^{\text{N}^3\text{LO}}}{\Gamma(h \rightarrow b\bar{b})_{\text{SM}}^{\text{N}^3\text{LO}}} - 1 \in [-6.3, 6.3]\% \text{ for } c_{bG} = \frac{v^2}{\Lambda^2} \text{Re}(C_{bG}) \in [-438, 438]$$

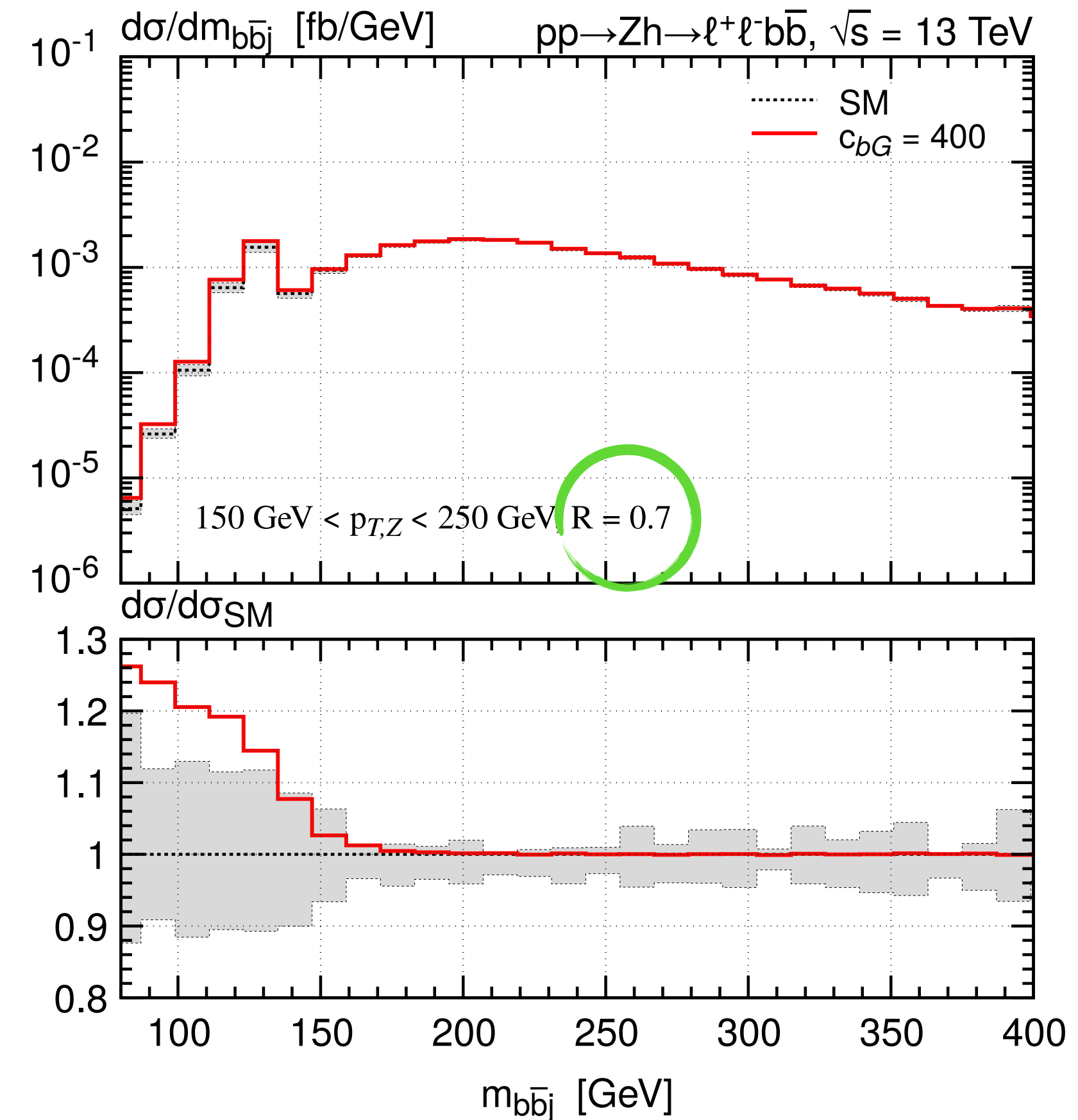
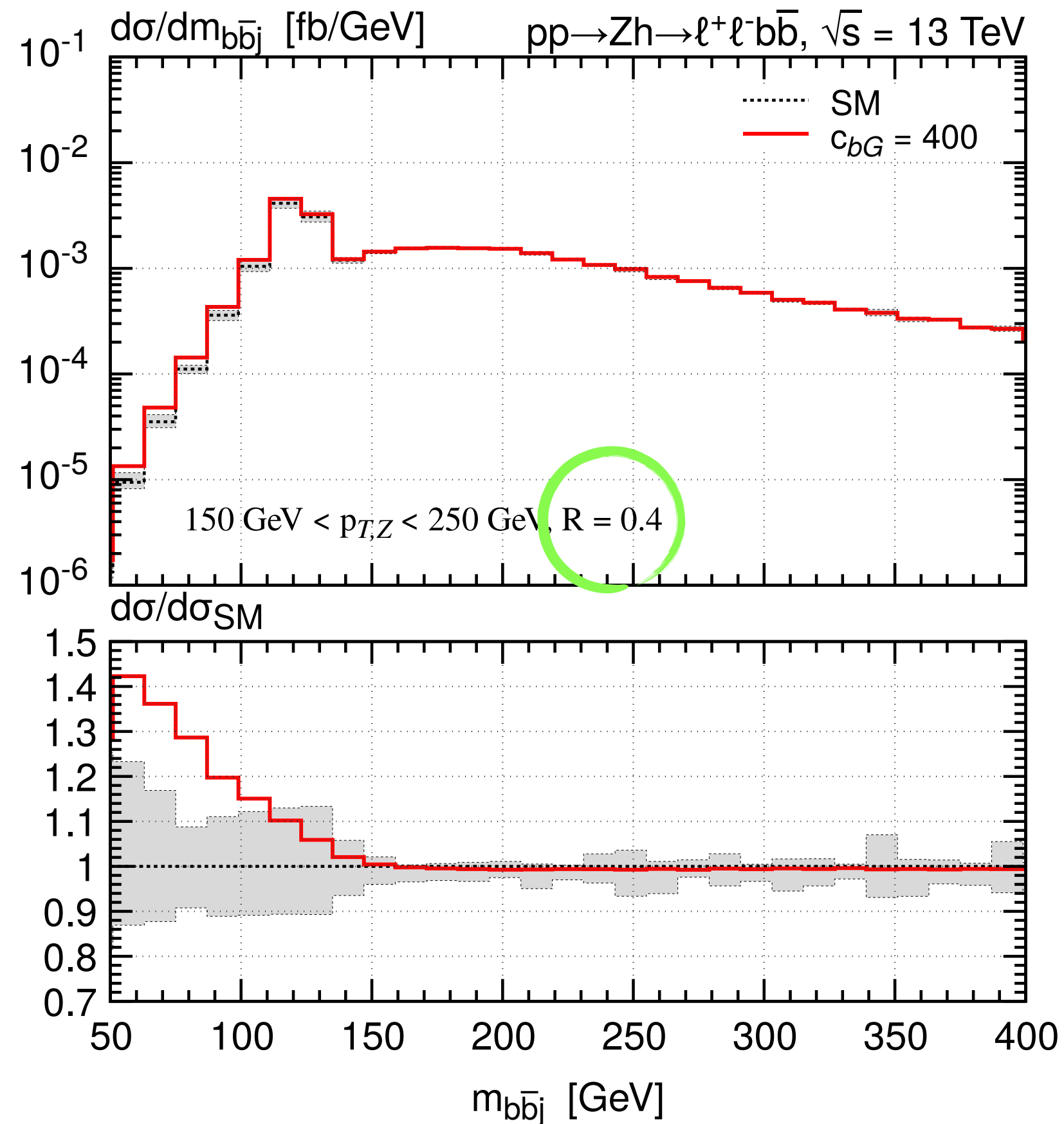
But non-factorisable contributions lead to non-trivial modifications of spectra in $pp \rightarrow Zh \rightarrow l^+l^-b\bar{b}$ production

Phenomenology analysis

factorisable contributions just lead to a constant shift, i.e. a K-factor, in all $pp \rightarrow Zh \rightarrow \ell^+ \ell^- b \bar{b}$ distributions



Phenomenology analysis

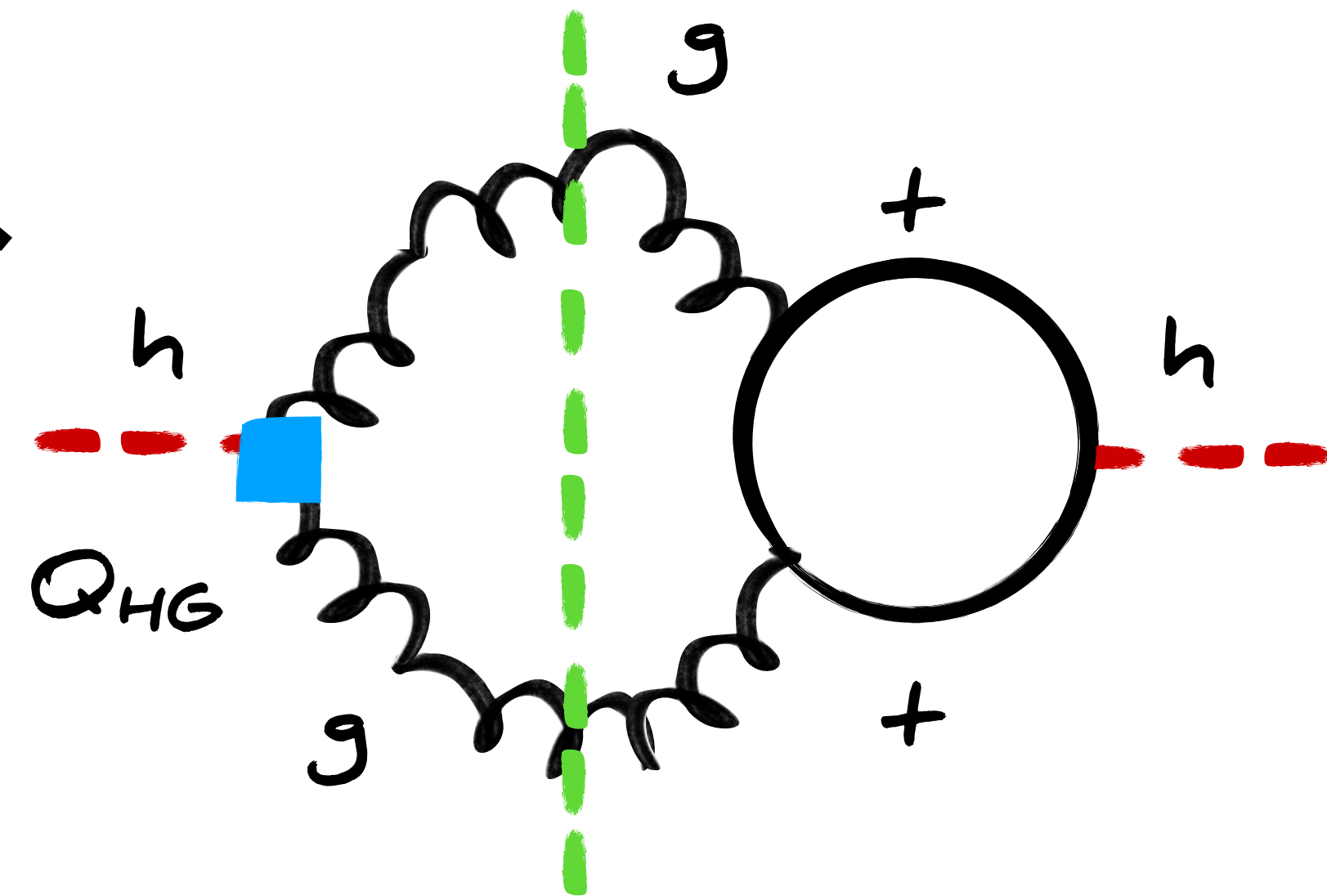


Also 3-jet invariant mass reduced on average. Effects again R-dependent

SMEFT corrections to total Higgs width

$$\Gamma_h^{\text{SMEFT}} = (1 + 2c_{\text{kin}}) \left[\Gamma_h^{\text{SM}} - (2\Delta c_{bH} - K_{bG} \Delta_{\text{non}} c_{bG}) \Gamma(h \rightarrow b\bar{b})_{\text{SM}}^{\text{LO}} + 6K_{HG} c_{HG} \Gamma(h \rightarrow gg)_{\text{SM}}^{\text{LO}} \right]$$

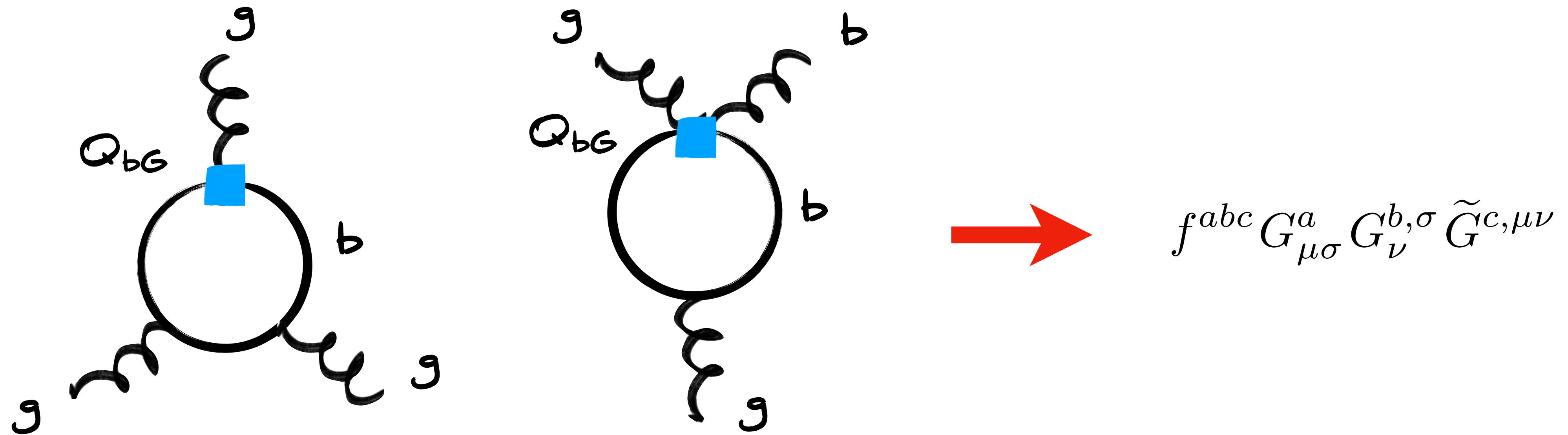
$$K_{HG} = 1.844$$



Event selections

In our differential analysis we select events with two charged leptons (electrons or muons) to explore the $Zh \rightarrow \ell^+ \ell^- b\bar{b}$ signature. The leptons are required to have a transverse momentum of $p_{T,\ell} > 15 \text{ GeV}$ and a pseudorapidity of $|\eta_\ell| < 2.5$. The invariant mass of the dilepton pair is restricted to $m_{\ell^+\ell^-} \in [75, 105] \text{ GeV}$. The events are furthermore required to have at least two b -jets, which are reconstructed using the anti- k_t algorithm [65] as implemented in FastJet [66]. We impose transverse momentum cuts of $p_{T,b} > 25 \text{ GeV}$ and a rapidity threshold of $|\eta_b| < 2.5$ on the b -jets. The definition of potential additional jets use the same thresholds as those of the b -jets. The dominant background processes are $Z + \text{jets}$, $t\bar{t}$, single-top and diboson production. The latter three types of backgrounds can be substantially reduced by requiring large values of $p_{T,Z}$ [67]. Hence, to improve the signal-to-background ratio we impose $p_{T,Z} \in [150, 250] \text{ GeV}$. Notice that this $p_{T,Z}$ requirement corresponds to the second resolved $p_{T,Z}$ bin as recommended in the stage 1.2 simplified template cross sections (STXS) framework [68–70] which is also implemented in the latest ATLAS LHC Run II measurements of the $pp \rightarrow Zh \rightarrow \ell^+ \ell^- b\bar{b}$ process [71, 72]. We will also comment on how our results are modified if the other two resolved regions, i.e. $p_{T,Z} \in [75, 150] \text{ GeV}$ and $p_{T,Z} > 250 \text{ GeV}$, are considered.

Bounds on dipole-type operator Q_{bG}



1-loop threshold corrections involving Q_{bG} generate CP-violating Weinberg operator. This operator leads to a non-zero neutron electric dipole moment at hadronic scale