

# MULTI-HIGGS PRODUCTION TO DISTINGUISH HEFT FROM SMEFT

Collaborators: J. Sanz-Cillero, R. Gómez-Ambrosio, R. Delgado-López, J. Martínez-Martín and F. J. Llanes-Estrada.

EFTs in Multiboson production, Padova, Tuesday 11<sup>th</sup> June, 2024



Alexandre Salas-Bernárdez

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- 1 Introduction and motivation.

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See also: 2204.01763 (Phys. Rev. D) and 2207.09848 (Comm. Th. Phys.)

# Introduction

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One of the most uncharted and promising sectors in SM

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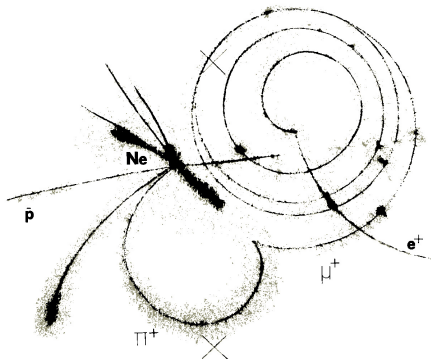
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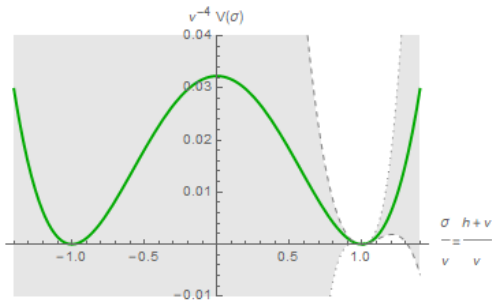
- Could EW Goldstone bosons ( $\omega_i$ s) resemble a  $\pi$  (pion)?
- SUSY? 2HDM?, etc.



# The Electroweak SB Sector

## One of the most uncharted and promising sectors in SM

- Nature of Higgs boson and EW gauge bosons? Composite or not?
- Measurable: Higgs self interaction and its coupling to electroweak gauge bosons.



*SMEFT*  $\subset$  *HEFT*

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- Higgs Effective Field Theory (HEFT):  
Chiral Lagrangian

$$\mathcal{L}_{\text{HEFT}} = \frac{1}{2} \partial_\mu h \partial^\mu h - V(h) + \frac{1}{2} \mathcal{F}(h) \partial_\mu \omega^i \partial^\mu \omega^j \left( \delta_{ij} + \frac{\omega^i \omega^j}{v^2 - \omega^2} \right) .$$

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What is their relation?

**“Flare Function”**

## In a few words...

Basically, SMEFT assumes the SM EWSB structure, where the Higgs boson is part of an  $SU(2)_L$  doublet.

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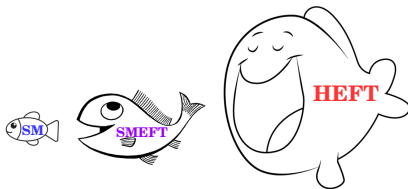
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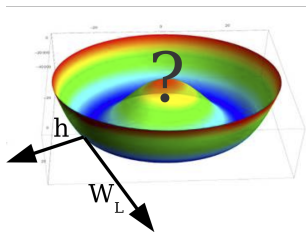
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On the other hand, HEFT casts the Higgs boson  $h$  as an  $SU(2)_L$  singlet.



# Geometric distinction HEFT/SMEFT

- Several works have provided field-redefinition invariant criteria to distinguish SMEFT from HEFT:
  - R. Alonso, E. E. Jenkins, and A. V. Manohar, "A Geometric Formulation of Higgs Effective Field Theory: Measuring the Curvature of Scalar Field Space," Phys. Lett. B754 (2016) 335–342, arXiv:1511.00724 [hep-ph]. "Sigma Models with Negative Curvature," Phys.Lett.B756,358(2016),arXiv:1602.00706 [hep-ph]. "Geometry of the Scalar Sector," JHEP 08 (2016) 101, arXiv:1605.03602 [hep-ph]." (Cohen et al., 2021, p. 95)
  - T. Cohen, N. Craig, X. Lu, and D. Sutherland: "Is SMEFT Enough?", JHEP 03, 237, arXiv:2008.08597 [hep-ph]. "Unitarity Violation and the Geometry of Higgs EFTs", (2021), arXiv:2108.03240 [hep-ph].



# Conditions on $\mathcal{F} = F^2$ for SMEFT's validity

In [2204.01763](#) we found an easier analytical criterion for SMEFT to be valid:

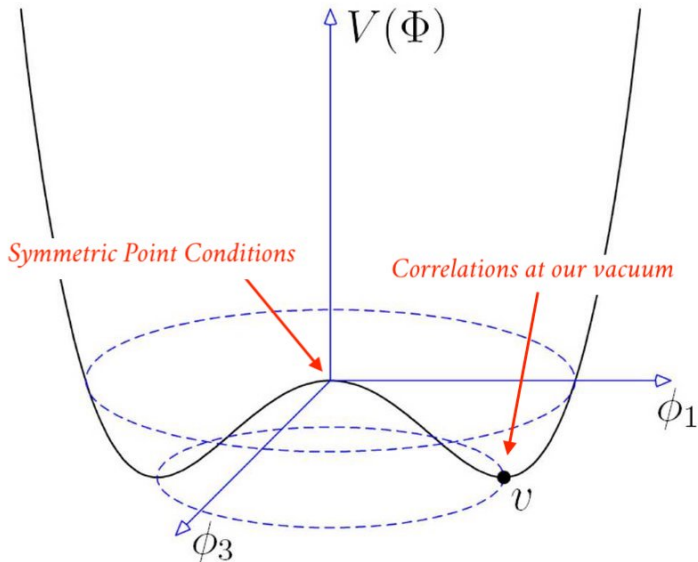
1  $\mathcal{F}(h_1^*) = 0$  must have a double zero.

2 At that point  $h_1^*$ ,

$$\mathcal{F}'(h_1^*) = 0, \quad \mathcal{F}''(h_1^*) = \frac{2}{v^2}.$$

3 Analyticity of the SMEFT Lagrangian: all even derivatives to vanish at the symmetric point,  $F^{(\ell)}(h_1^*) = 0$  for even  $\ell$ . From the point of view of  $\mathcal{F}$  this implies the vanishing of all odd derivatives,  $\mathcal{F}^{(2\ell+1)}(h_1^*) = 0$ .

# Origin of SMEFT correlations: just match two Taylor exp.





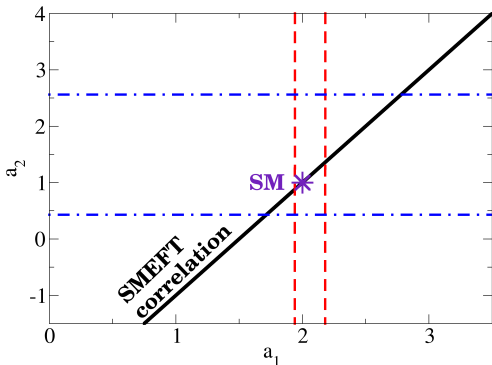
SMEFT assumption  $\Rightarrow$  HEFT parameters correlation

Correlations among HEFT parameters due to SMEFT structure:

(Bands from single Higgs production at ATLAS (ATLAS-CONF-2020-027) and Higgs Pair production at

CMS <https://arxiv.org/abs/2202.09617>)  $\mathcal{F}(h) = 1 + a_1 h/v + a_2 h^2/v^2 + \dots$ ,

$$k_{2V} = 4k_V - 3$$

Same game with the potential  $V(h)$  and the Yukawas... (see [2207.09848](https://arxiv.org/abs/2207.09848))

# Amplitudes and Cross sections

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## High energy measurements

In the TeV region the potential is subleading. The flare function  $\mathcal{F}$  encodes relevant physics (it accompanies the GB kinetic term)

$$\mathcal{F}(h_{\text{HEFT}}) = 1 + \sum_{n=1}^{\infty} a_n \left( \frac{h_{\text{HEFT}}}{v} \right)^n.$$

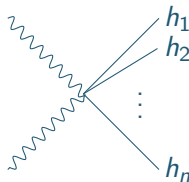
At high energies (Equivalence Theorem)  $\omega \simeq W_L$

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At high energies (Equivalence Theorem)  $\omega \simeq W_L$   
 $\Rightarrow \omega\omega \rightarrow n \times h$  can test SMEFT framework.



$$= -\frac{n! a_n}{2v^n} s$$

Measure  $\mathcal{F}$  expansion in multi-Higgs final states

$$T_{\omega\omega\rightarrow h} = -\frac{a_1 s}{2v}$$

$$T_{\omega\omega\rightarrow hh} = -\frac{s}{v^2} \left( a_2 - \frac{a_1^2}{4} \right),$$

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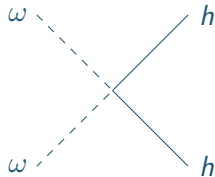
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$$T_{\omega\omega\rightarrow 4h} = -\frac{4s}{v^4} \left( 3\hat{a}_4 + \hat{a}_2^2 (B - 1) \right),$$

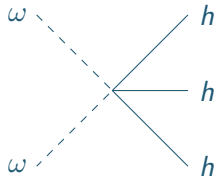
where  $\hat{a}_2 = a_2 - a_1^2/4$  and  $\hat{a}_4 = a_4 - \frac{3}{4}a_1a_3 + \frac{5}{12}a_1^2(a_2 - a_1^2/4)$ .

Effective  $h^n \omega \omega$  vertices (see [2401.18002](#))

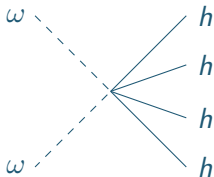
In [2401.18002](#) we found a very nice field redefinition that eliminated the  $h\omega\omega$  vertex. Leaving only the contributing diagrams:



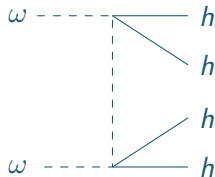
(a)



(b)



(c)



(d)



## SMEFT vs HEFT phenomenology

Dimension 6 (8) SMEFT operators contributing to  $\mathcal{F}(h)$  are  
 $|H|^{2(4)} \square |H|^2 / \Lambda^{2(4)}$

$$a_{1/2} = a = 1 + \frac{d}{2} + \frac{d^2}{2} \left( \frac{3}{4} + \rho \right) + \mathcal{O}(d^3),$$

$$a_2 = b = 1 + 2d + 3d^2(1 + \rho) + \mathcal{O}(d^3),$$

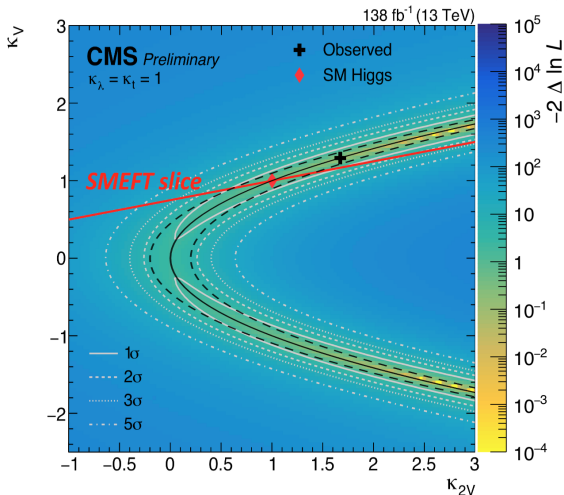
$$a_3 = \frac{4}{3}d + d^2 \left( \frac{14}{3} + 4\rho \right) + \mathcal{O}(d^3),$$

$$a_4 = \frac{1}{3}d + d^2 \left( \frac{11}{3} + 3\rho \right) + \mathcal{O}(d^3), ,$$

with,

$$d = \frac{2v^2 c_{H\square}^{(6)}}{\Lambda^2}, \quad \rho = \frac{c_{H\square}^{(8)}}{2(c_{H\square}^{(6)})^2}.$$

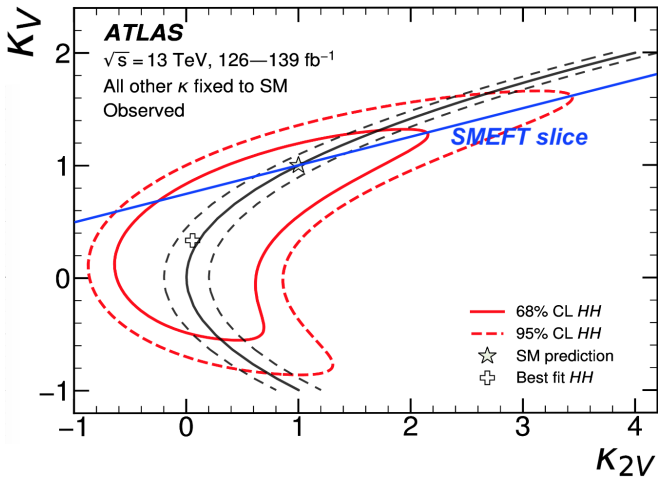
# Detour: how well does the Eq. Th. perform?



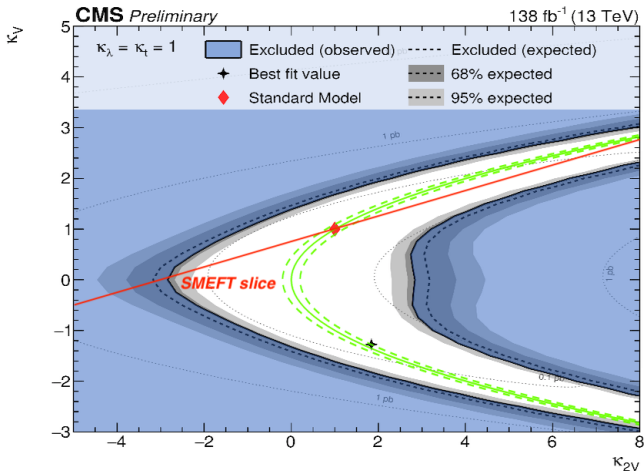
Remember  $T_{\omega\omega \rightarrow hh} = -\frac{s}{v^2} (k_2 - k_1^2)$

CMS-B2G-22-003

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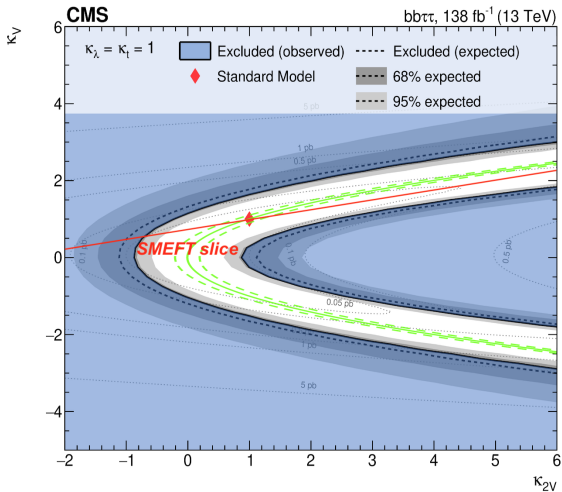


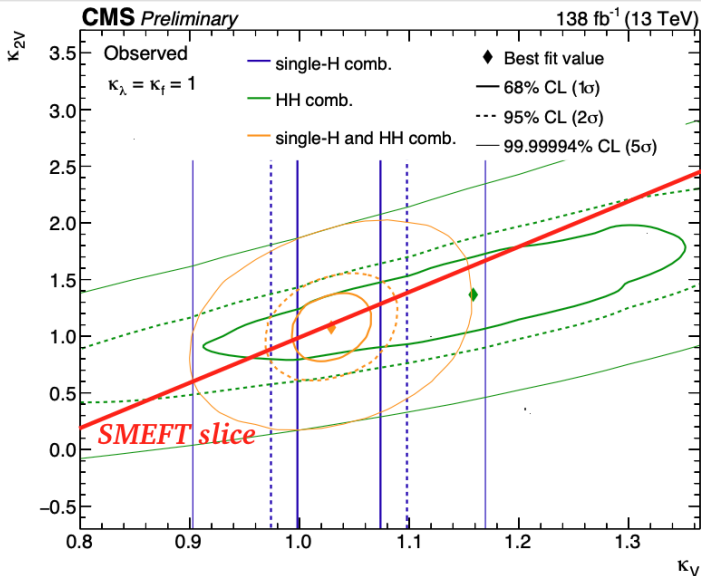
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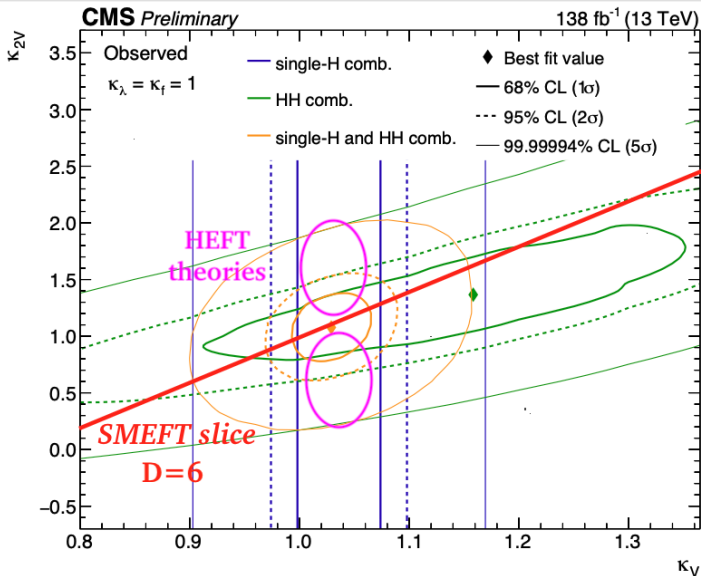
CMS-PAS-HIG-21-005 (with one Higgs boson decaying to  $\bar{b}b$  and the other one to  $W^+W^-$ )

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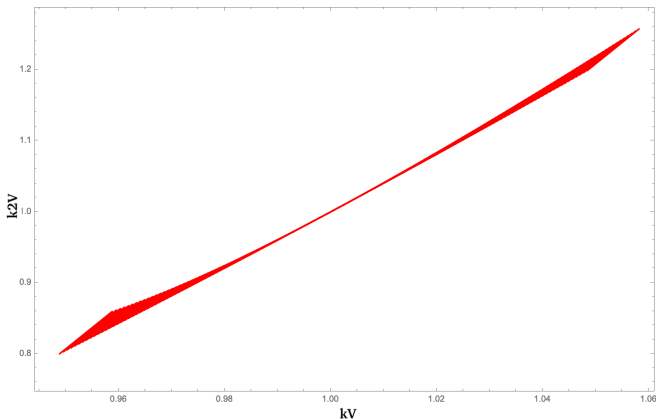
CMS 2206.09401 (with Higgs bosons  $b\bar{b}\tau^+\tau^-$  final states)

Recent combination of analyses: CMS-HIG-23-006

## Recent combination of analyses: HEFT regions



In case you are wondering...  $D = 8$



for  $|d| \leq 0.1$  (within allowed CMS bounds) and  $\rho = \left| \frac{c_{H\Box}^{(8)}}{2(c_{H\Box}^{(6)})^2} \right| \leq 1$



# Benchmark Points for the comparison: SMEFT BP

SMEFT BP (the choice of  $\rho$  is not really relevant):

$$d = \frac{2v^2 c_{H\Box}^{(6)}}{\Lambda^2} = 0.1, \quad \rho = \frac{c_{H\Box}^{(8)}}{2(c_{H\Box}^{(6)})^2} = 1.$$

within the most precise experimental determinations up to date from **ATLAS 2207.00092**,  $a = \kappa_V = 1.035 \pm 0.031$ , and **CMS 2207.00043**,  $a = \kappa_V = 1.014 \pm 0.029$ .

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$$\Rightarrow \boxed{\frac{a_1}{2} = 1.05} \text{ and } \boxed{a_2 = 1.20}.$$

## Benchmark Points for the comparison: First HEFT BP

**BP1**<sup>(a<sub>1</sub>)</sup>: Simplest exponential flare function that matches the  $D = 6$  SMEFT prediction for  $a_1$ :

$$\mathcal{F}(h) = \exp \left\{ a_1 \frac{h}{v} \right\} \quad \implies$$
$$a_2 = \frac{a_1^2}{2!} = 2.205, \quad a_3 = \frac{a_1^3}{3!} \approx 1.54, \quad a_4 = \frac{a_1^4}{4!} \approx 0.81.$$

**BP1**<sup>(a<sub>1</sub>, a<sub>2</sub>)</sup>: Simplest exponential flare function that matches the  $D = 6$  SMEFT prediction for  $a_1$  and  $a_2$ :

$$\mathcal{F}(h) = \exp \left\{ a_1 \frac{h}{v} + \left( a_2 - \frac{a_1^2}{2} \right) \frac{h^2}{v^2} \right\} \quad \implies$$
$$a_3 = \left( a_1 a_2 - \frac{a_1^3}{3} \right) \approx -0.57, \quad a_4 = \left( \frac{a_2^2}{2} - \frac{a_1^4}{12} \right) \approx -0.90.$$

## Benchmark Points for the comparison: Second HEFT BP

**BP2<sup>(a<sub>1</sub>)</sup>**: Simplest rational flare function that matches the  $D = 6$  SMEFT prediction for  $a_1$ :

$$\mathcal{F}(h) = \left(1 - \frac{a_1 h}{2 v}\right)^{-2} \implies$$

$$b = \frac{3}{4} a_1^2 \approx 3.31, \quad a_3 = \frac{1}{2} a_1^3 \approx 4.63, \quad a_4 = \frac{5}{16} a_1^4 \approx 6.08,$$

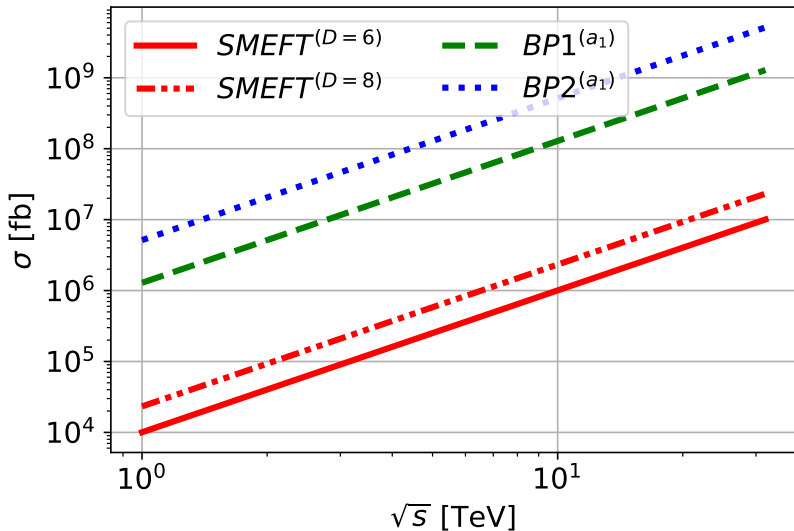
**BP2<sup>(a<sub>1</sub>, a<sub>2</sub>)</sup>**: Simplest rational flare function that matches the  $D = 6$  SMEFT prediction for  $a_1$  and  $a_2$ :

$$\mathcal{F}(h) = \left(1 - \frac{a_1 h}{2 v} - \left(\frac{a_2}{2} - \frac{3a_1^2}{8}\right) \frac{h^2}{v^2}\right)^{-2} \implies$$

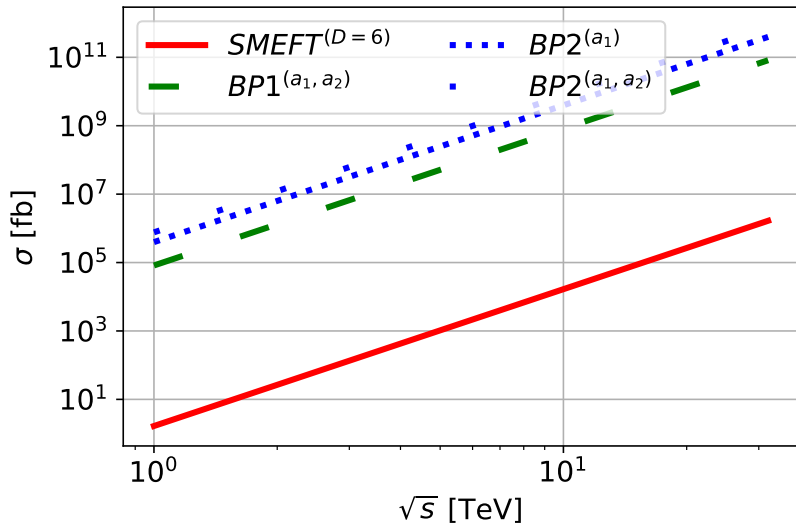
$$a_3 = \frac{1}{8} (-5a_1^3 + 12a_1 a_2) \approx -2.01,$$

$$a_4 = \frac{1}{64} (-25a_1^4 + 24a_1^2 a_2 + 48a_2^2) \approx -4.53,$$

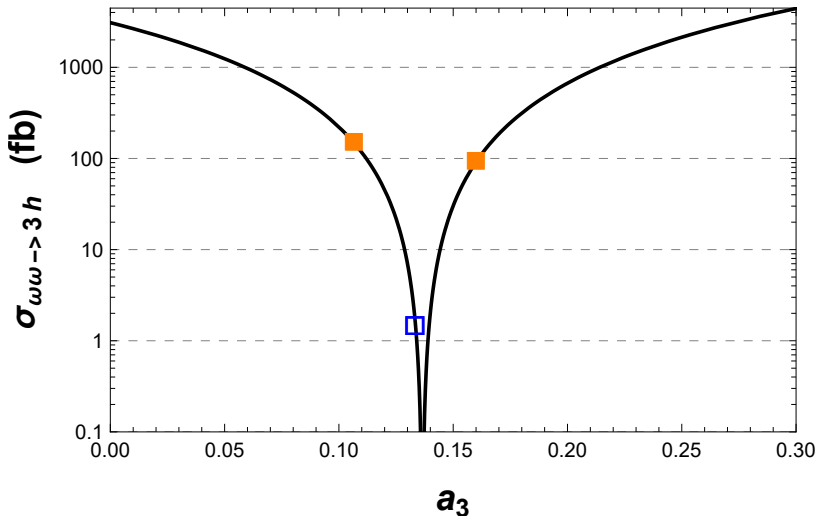
## Cross section comparison: two Higgses



## Cross section comparison: three Higgses

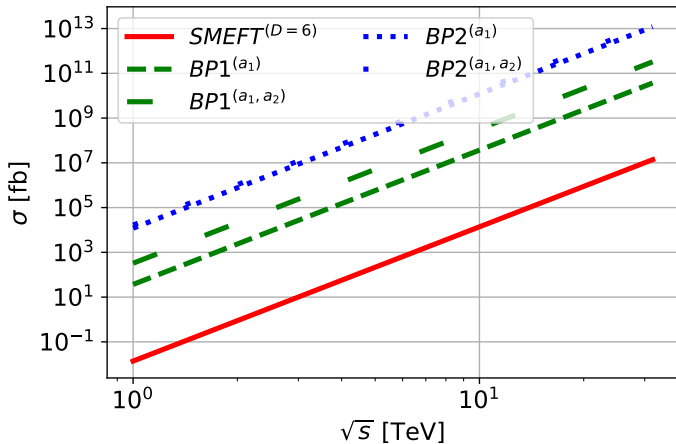


## Cross section comparison: three Higgses



Deviating  $a_3$  only 10% of SMEFT value drastically changes XS.

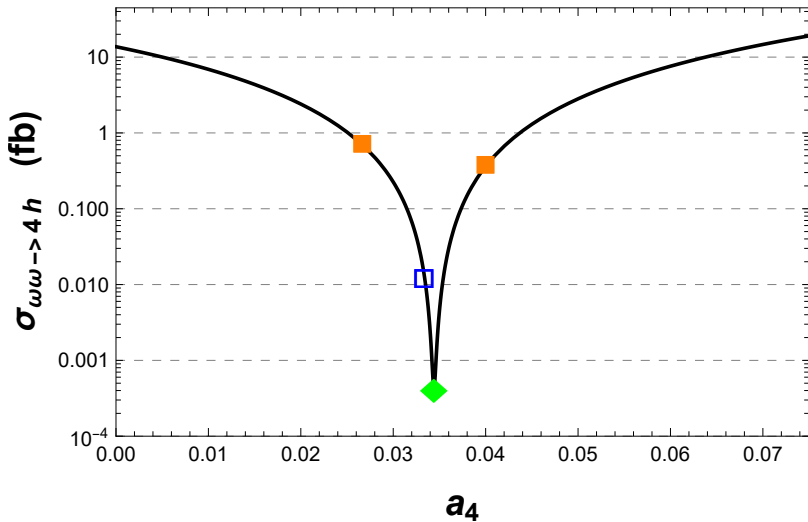
## Cross section comparison: four Higgses



Integration performed through new open-source code MaMuPaXS  
[github.com/mamupaxs](https://github.com/mamupaxs)



## Cross section comparison: four Higgses



Deviating  $a_4$  only 10% of SMEFT value drastically changes XS.

# Collider estimate and SMEFT limits

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## SMEFT exclusion bounds

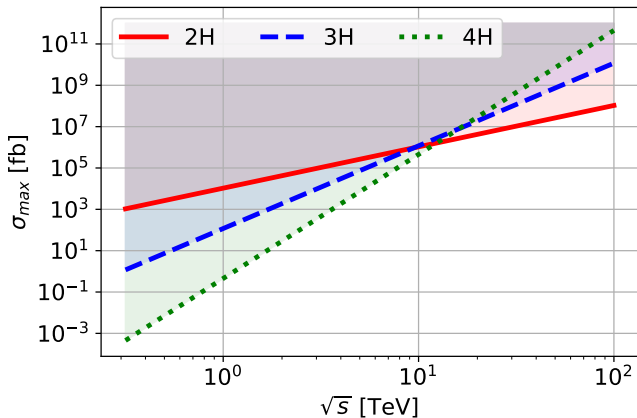


Figure 1: SMEFT exclusion plot for the cross sections for 2, 3 and 4 Higgs bosons with  $|d| \leq d_{\max} = 0.1$  and  $|\rho| \leq \rho_{\max} = 1$ .

## Exclusion plot: EFT perturbativity

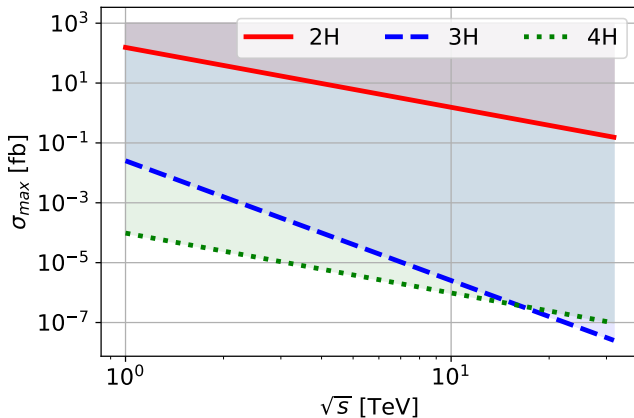


Figure 2: Exclusion plot for the maximum value of the cross sections for 2, 3 and 4 Higgs bosons with the constraint  $|\rho| \leq \rho_{\max} = 1$  and

$$\text{EFT-expansion tolerance } \epsilon = 0.1. \quad \left| \frac{c_{H\Box S}^{(6)}}{\Lambda^2} \right| = \left| \frac{dS}{2v^2} \right| \leq \epsilon \ll 1$$

# The Effective W approximation

In the Effective W approximation (EWA),  $W_L$  are radiated collinear to initial particles (expected to dominate XS).

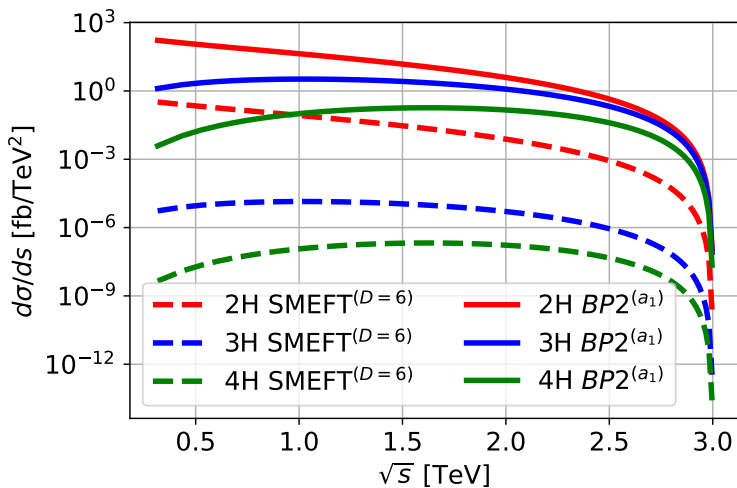
Collider estimate: 3 TeV CLIC  $e^+e^-$ 

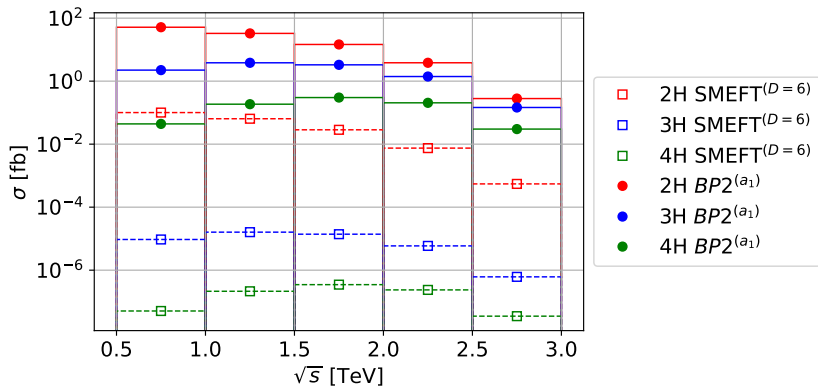
In the EWA factorization, the total cross section,  $\sigma_{tot}$ , is provided by the hard subprocess cross section times an appropriate  $W_L$ -luminosity function of the form,

$$\frac{d\sigma_{tot}}{ds} = \frac{\alpha^2}{8\pi^2 s s_{\theta_W}^2} \left[ 2 \left( \frac{s}{s_{tot}} - 1 \right) - \left( \frac{s}{s_{tot}} + 1 \right) \log \frac{s}{s_{tot}} \right] \times \sigma(s) \Big|_{W_L^+ W_L^- \rightarrow n \times h}$$

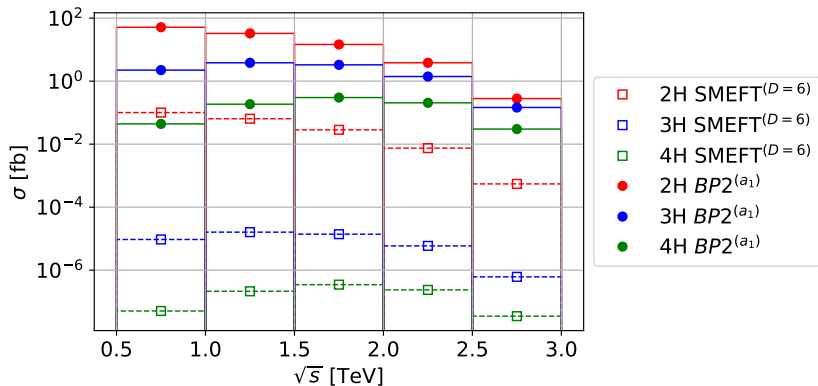
1508.03544

## Differential XS in the EWA



$e^+e^- \rightarrow e^+e^- + n \times h$  cross section in the EWA



$e^+e^- \rightarrow e^+e^- + n \times h$  cross section in the EWA

CLIC at 3 TeV expected to have  $5000 \text{ fb}^{-1}$  luminosity. [1812.02093](#)

# Conclusions

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- 2 Computed  $\omega\omega \rightarrow hhh$  and  $\omega\omega \rightarrow hhhh$  at LO HEFT amplitudes and cross sections.
- 3 HEFT cross sections can be both small and big. SMEFT ones are usually suppressed.
- 4 Observation of three and four  $hs$  final states at CLIC 3 TeV  $e^+e^-$  could signal SMEFT is not enough.

# Acknowledgments

Funded by research grant PID2022-137003NB-I00 from Spanish MCIN/AEI/10.13039/501100011033/ and EU FEDER.

