

FASE $R\nu$: a non-unitary of the leptonic mixing matrix

Jesús Miguel Celestino Ramírez

Physics department, Cinvestav

Based on: 2309.00116



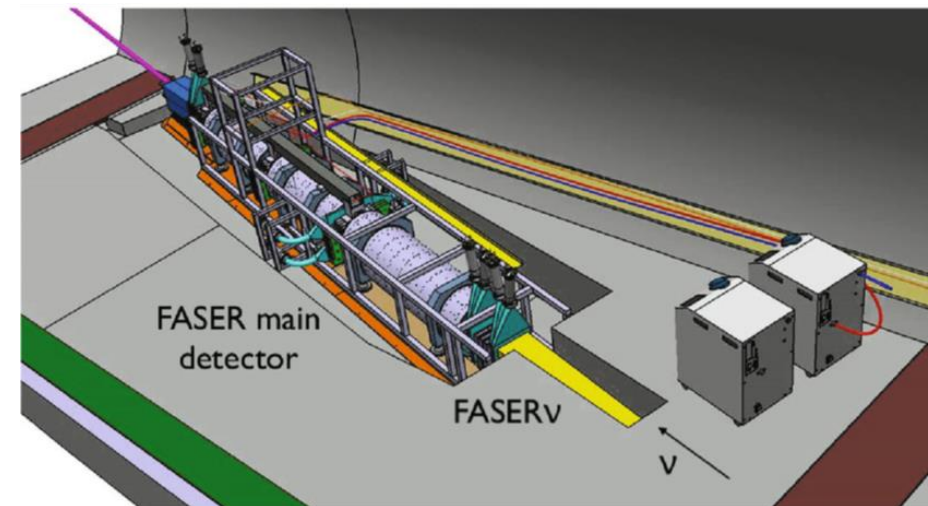
FASER experiment and FASER ν (FASER ν 2) detector

FASER ν features¹:

- has a total Tungsten target mass of 1.2 tons.
- A baseline of 480 m.
- Works from 100 GeV to 1 TeV.
- Expects, approximately, 1000 ν_e , 3000 ν_μ and 20 ν_τ



FASER:
ForwArd Search ExpeRiment at the LHC



¹Henso Abreu et al. Eur. Phys. J. C,80(1):61, 2020.

Henso Abreu et al. First Direct Observation of Collider Neutrinos with FASER at the LHC. 3 2023.

The PDG parametrization

$$U = R_{23}(\theta_{23}; 0)R_{13}(\theta_{13}; \delta)R_{12}(\theta_{12}; 0)P$$

$$R_{13}(\theta_{13}; \delta) = \begin{pmatrix} \cos \theta_{13} & 0 & \sin \theta_{13} e^{-i\delta} \\ 0 & 1 & 0 \\ -\sin \theta_{13} e^{i\delta} & 0 & \cos \theta_{13} \end{pmatrix}$$

Dirac phase

Majorana phase

$$P = \text{diag}(1, e^{i\alpha}, e^{i\beta})$$

Neutrino oscillation probability

$$P(\nu_\alpha \rightarrow \nu_\beta) = \left| \sum_j U_{\alpha j}^* U_{\beta j} e^{-\frac{i m_j^2 L}{2E}} \right|^2 = \delta_{\alpha\beta} - 4 \sum_{i>j} \Re\{U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*\} \sin^2\left(\frac{\Delta m_{ij}^2}{4E} L\right) - 2 \sum_{i>j} \Im\{U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*\} \sin\left(\frac{\Delta m_{ij}^2}{2E} L\right)$$

The symmetric Parametrization and the non-unitary effects

$$K = \omega_{23}(\theta_{23}; \phi_{23}) \omega_{13}(\theta_{13}; \phi_{13}) \omega_{12}(\theta_{12}; \phi_{12})^{2,3} \quad \omega_{23}(\theta_{23}; \phi_{23}) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & e^{-i\phi_{23}} s_{23} \\ 0 & -e^{i\phi_{23}} s_{23} & c_{23} \end{pmatrix}$$

We can extend this formalism to an arbitrary number of neutral heavy leptons :

$$U_{n \times n} = \omega_{n-1,n} \times \omega_{n-2,n} \times \cdots \times \omega_{1,n} \times \omega_{n-2,n-1} \times \cdots \times \omega_{23} \times \omega_{13} \times \omega_{12}$$

$$U_{n \times n} = \begin{pmatrix} N_{3 \times 3} & S_{3 \times m} \\ T_{m \times 3} & V_{m \times m} \end{pmatrix}, \quad n = m + 3 \quad \text{The light neutrino sector is no longer unitary.} \quad N = \begin{pmatrix} \alpha_{11} & 0 & 0 \\ \alpha_{21} & \alpha_{22} & 0 \\ \alpha_{31} & \alpha_{32} & \alpha_{33} \end{pmatrix} U^{SM}$$

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sum_{ij}^3 N_{\alpha i}^* N_{\alpha j} N_{\beta i} N_{\beta j}^* - 4 \sum_{i>j} \Re\{N_{\alpha i}^* N_{\alpha j} N_{\beta i} N_{\beta j}^*\} \sin^2\left(\frac{\Delta m_{ij}^2}{4E_\nu} L\right) - 2 \sum_{i>j} \Im\{N_{\alpha i}^* N_{\alpha j} N_{\beta i} N_{\beta j}^*\} \sin\left(\frac{\Delta m_{ij}^2}{2E_\nu} L\right)$$

²J. Schechter and J. W. F. Valle. Phys. Rev. D, 25:2951, 1982.

³W. Rodejohann, J.W.F. Valle. Phys.Rev.D 84 (2011), 073011

The features and approximations of symmetric parametrization

$$P(\nu_\alpha \rightarrow \nu_\beta) \approx \sum_{ij}^3 N_{\alpha i}^* N_{\alpha j} N_{\beta i} N_{\beta j}^*$$

$$P_{ee} = \alpha_{11}^4$$

$$P_{\mu e} = \alpha_{11}^2 |\alpha_{21}|^2$$

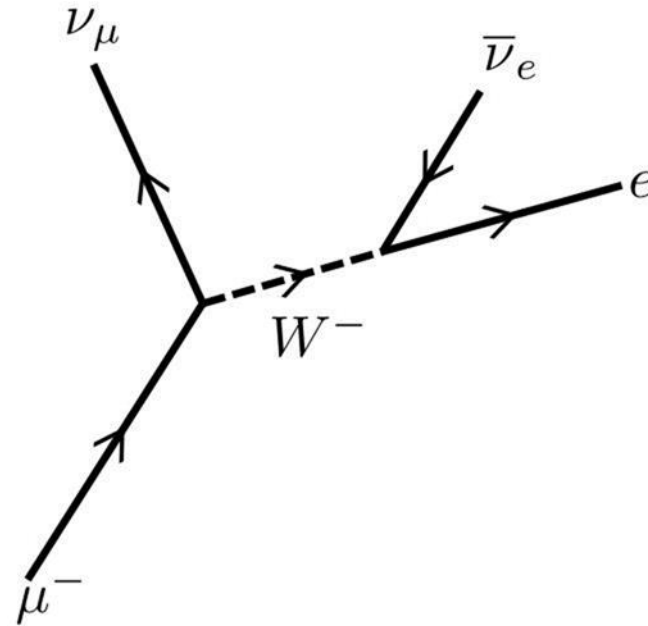
$$P_{\mu\mu} = (|\alpha_{21}|^2 + \alpha_{22}^2)^2$$

$$P_{e\tau} = \alpha_{11}^2 |\alpha_{31}|^2$$

$$P_{\mu\tau} \approx \alpha_{22}^2 |\alpha_{32}|^2$$

$$P_{\tau\tau} = (|\alpha_{32}|^2 + |\alpha_{31}|^2 + \alpha_{33}^2)^2$$

$$|\alpha_{ij}| \leq \sqrt{(1 - \alpha_{ii}^2)(1 - \alpha_{jj}^2)}$$

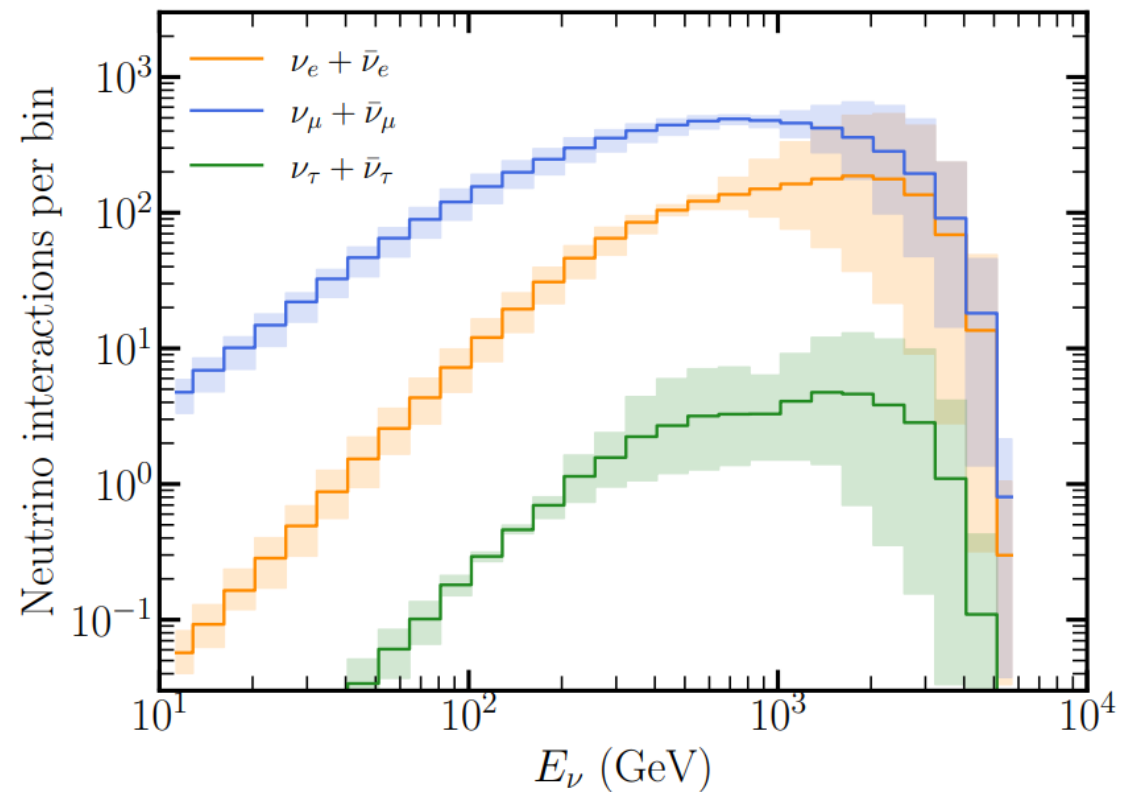


$${}^6G_\mu = G_F \sqrt{(NN^\dagger)_{11}(NN^\dagger)_{22}} = G_F \sqrt{\alpha_{11}^2 (\alpha_{22}^2 + |\alpha_{21}|^2)}$$

Neutrinos events computation

$$N_{\alpha}^{SM} = \epsilon_{\alpha} N_T \int f(E_{reco}) R(E_{reco}, E_{\nu}) \sigma_{\alpha}(E_{\nu}) \phi_{\alpha} dE_{\nu} dE_{reco}$$

Lepton flavor	FASER ν		FASER ν 2	
	10 ² -10 ⁴ GeV	100-600 GeV	10 ² -10 ⁴ GeV	100-600 GeV
e	1095 \pm 937	307 \pm 101	44230	20775
μ	2807 \pm 909	1163 \pm 190	193630	85044
τ	19 \pm 19	6 \pm 4	767	314



χ^2 analysis

We take into account each disappearance and appearance channel for each flavor.

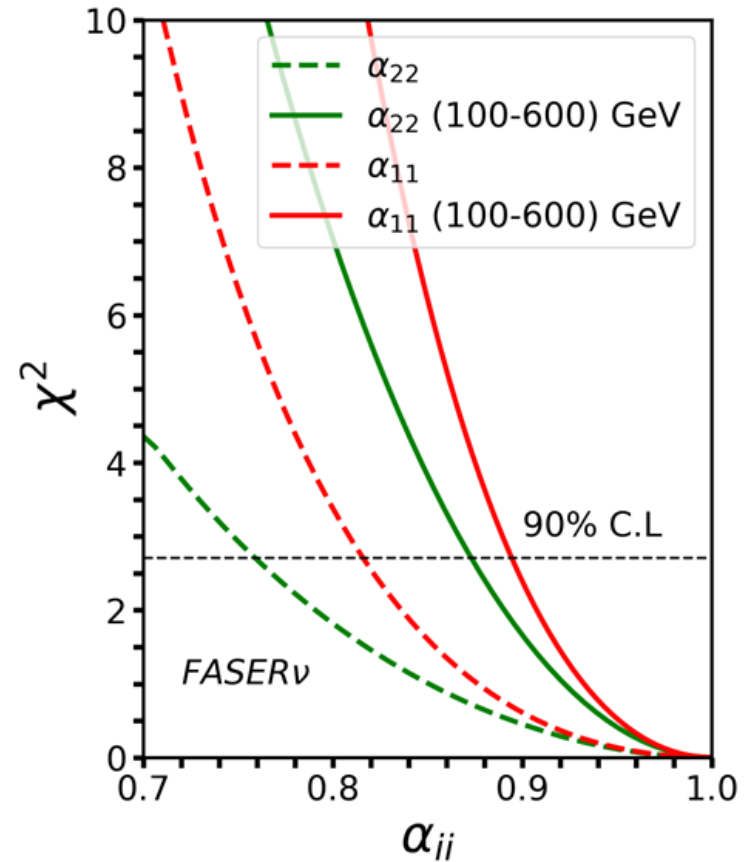
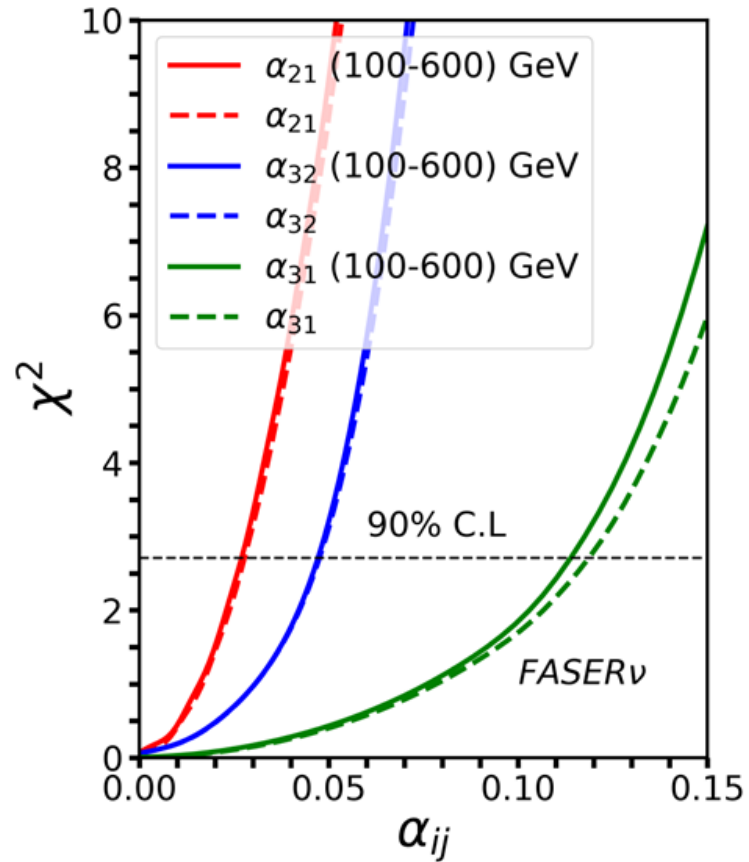
$$\chi^2 = \sum_{\alpha=1}^3 \frac{(N_{\alpha}^{NU} - N_{\alpha}^{exp})^2}{\sigma^2} + \sum_{ij} \frac{(\alpha_{ij} - \delta_{ij})^2}{\sigma_{ij}^2}$$

We have included priors to the values of α_{ij} that will be marginalized in our fit, using as errors, σ_{ij} , the current constraints⁶.

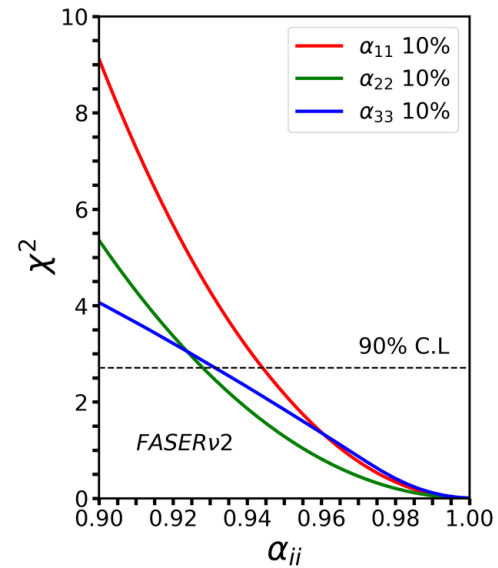
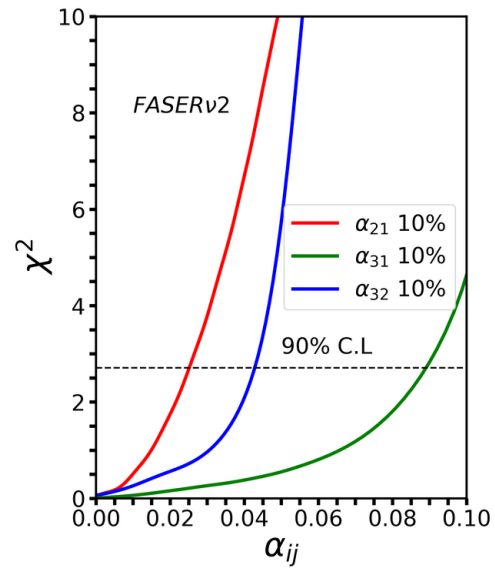
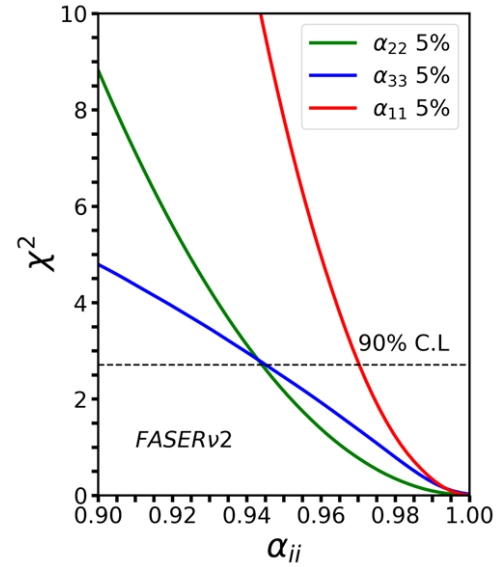
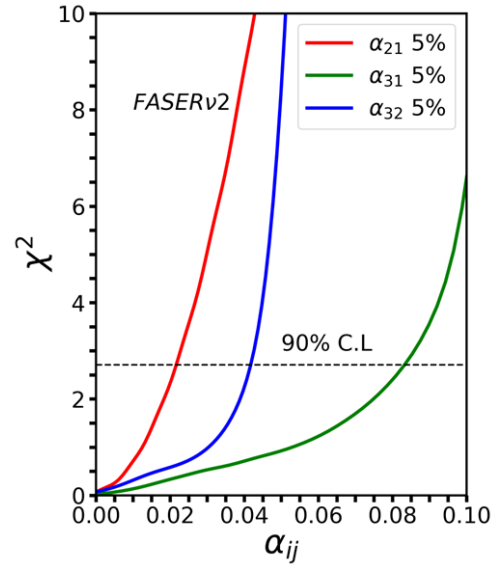
$$N_{\alpha}^{NU} = \frac{1}{\alpha_{11}^2 (\alpha_{22}^2 + |\alpha_{21}|^2)} (N_{\alpha} P_{\alpha\alpha} + \sum_{\beta \neq \alpha} P_{\alpha\beta} N_{\beta})$$

⁶D. V. Forero, C. Giunti, C. A. Ternes, and M. Tortola. Phys.Rev.D, 104(7):075030, 2021.

FASER ν Results



FASER ν 2 Results



Parameters	FASER ν		FASER ν 2		Current limit
	10^2 - 10^4 GeV	100-600 GeV	100-600 GeV (5%)	100-600 GeV (10%)	
$\alpha_{11} \geq$	0.818	0.894	0.97	0.944	0.969
$\alpha_{22} \geq$	0.760	0.873	0.944	0.928	0.995
$\alpha_{33} \geq$	-	-	0.945	0.932	0.890
$\alpha_{21} \leq$	0.028	0.027	0.022	0.025	0.013
$\alpha_{31} \leq$	0.118	0.114	0.083	0.089	0.033
$\alpha_{32} \leq$	0.048	0.048	0.042	0.043	0.009

Conclusions

- We find that the expected FASERv sensitivity to non-unitarity parameters might give complementary information, useful perhaps in a global analysis.
- On the other hand, for the FASERv2 case, the perspectives are much better and the sensitivity to the α_{11} (related with the electron neutrino disappearance channel) and α_{33} (related with the tau neutrino disappearance channel) parameters could be quite competitive with current restrictions.

*Thank
you!*

Back up

The charged current (CC) lagrangian

$$L = \frac{-g}{\sqrt{2}} W_{\mu}^{-} \sum_{i=1}^3 \sum_{j=1}^n K_{ij} \bar{l} \gamma^{\mu} P_L \nu_j$$

The CC interaction does not concern the Neutral heavy leptons because they are singlets under the electro-weak symmetry. Just the new massive state is taking account in the CC interaction.

$$U_{n \times n} = \begin{pmatrix} N_{3 \times 3} & S_{3 \times m} \\ T_{m \times 3} & V_{m \times m} \end{pmatrix}$$

$$K = (N_{3 \times 3} \quad S_{3 \times m})$$

The process of marginalizing the α parameters

As we said, all the Alpha parameters are involved in the analysis. We did a scan of all the Alpha parameters and the marginalized part is to find the combination of the other 5 Alpha parameters (that you are not interested in) that minimize the chi-squared value for each value of the Alpha parameter that we are interested in analysis.