

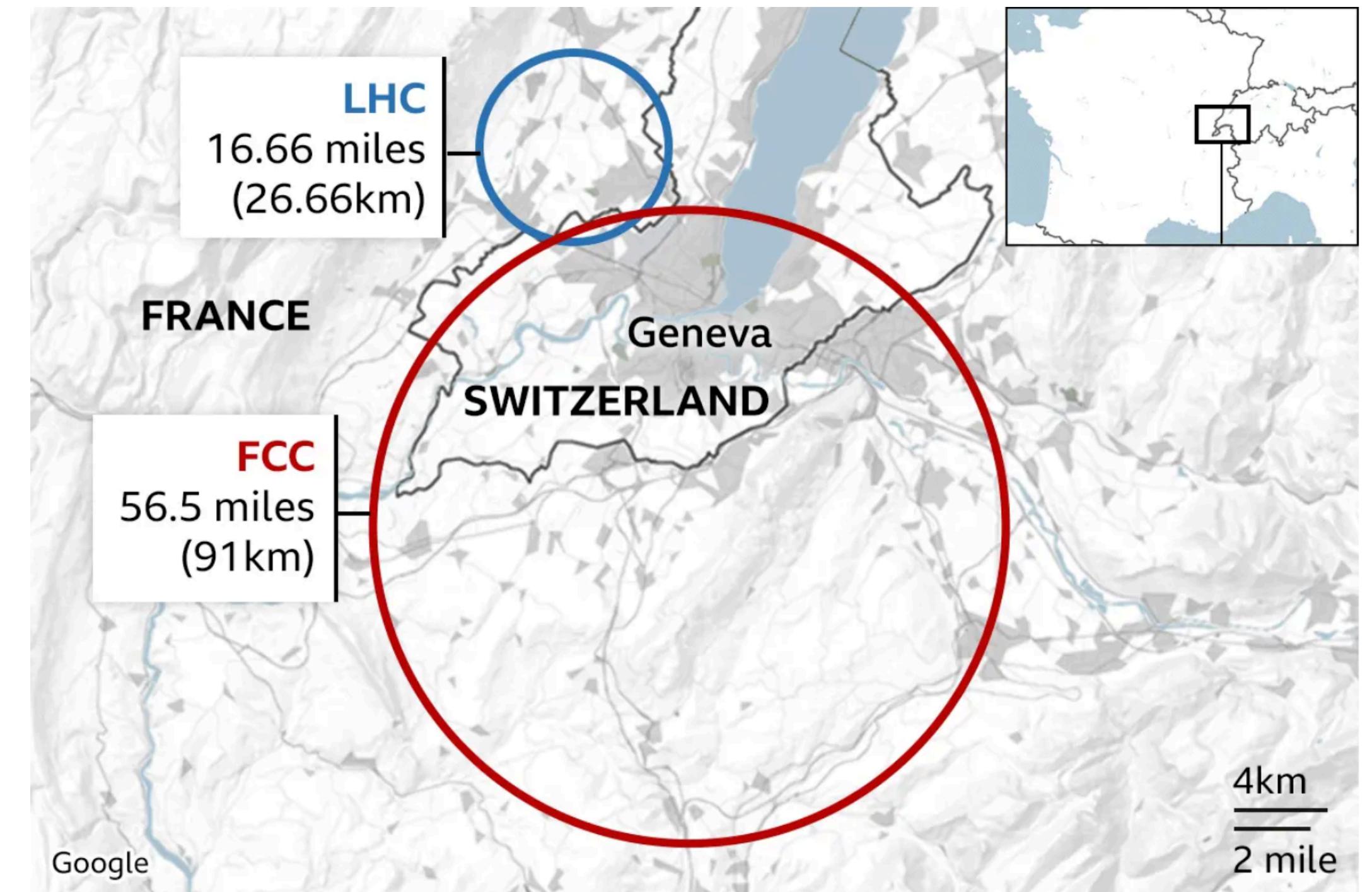
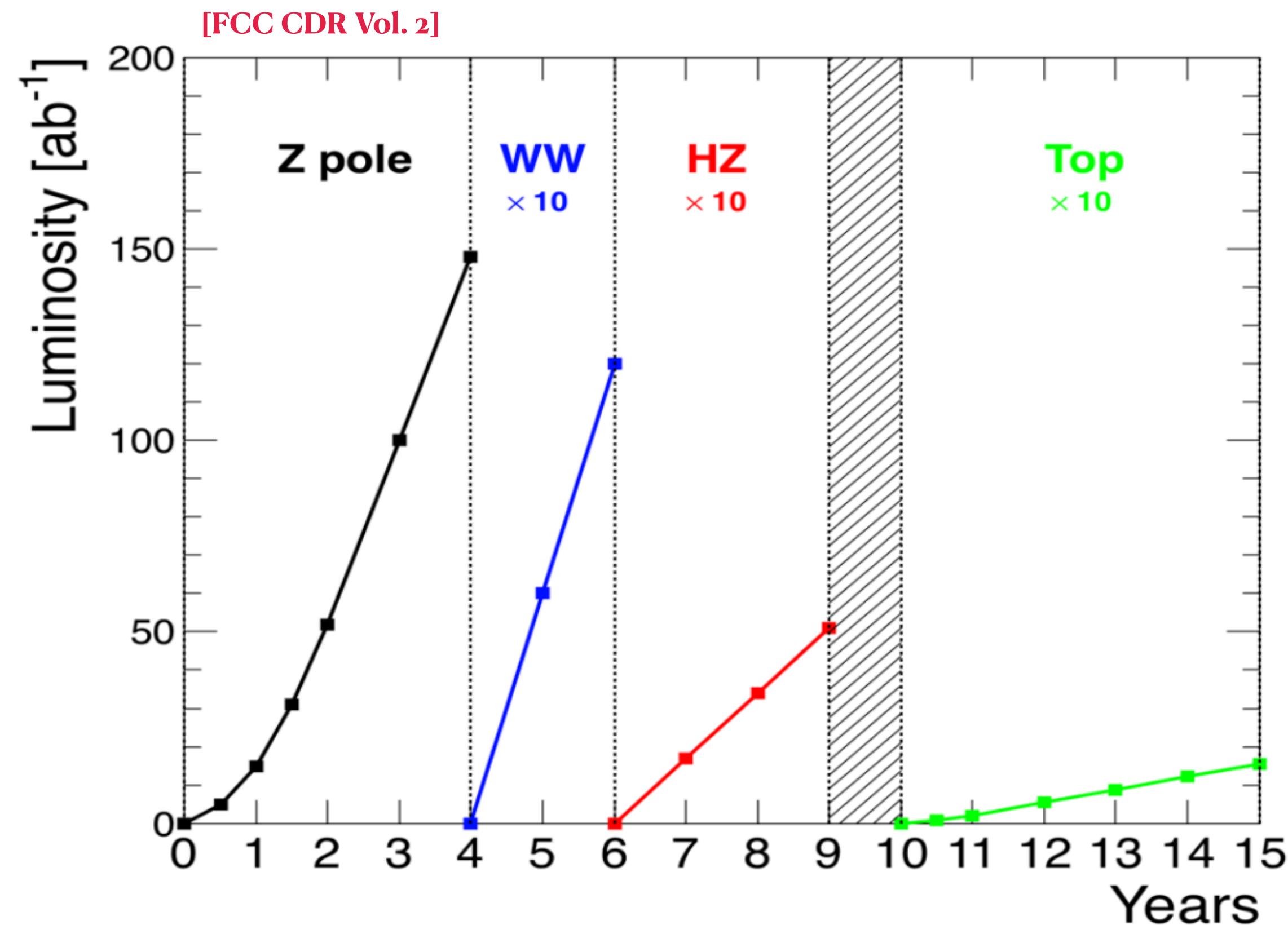
SUSY and Electroweak Precision Tests at Tera-Z Colliders

Kevin Langhoff

(Work in progress with Simon Knapen and Zoltan Ligeti)

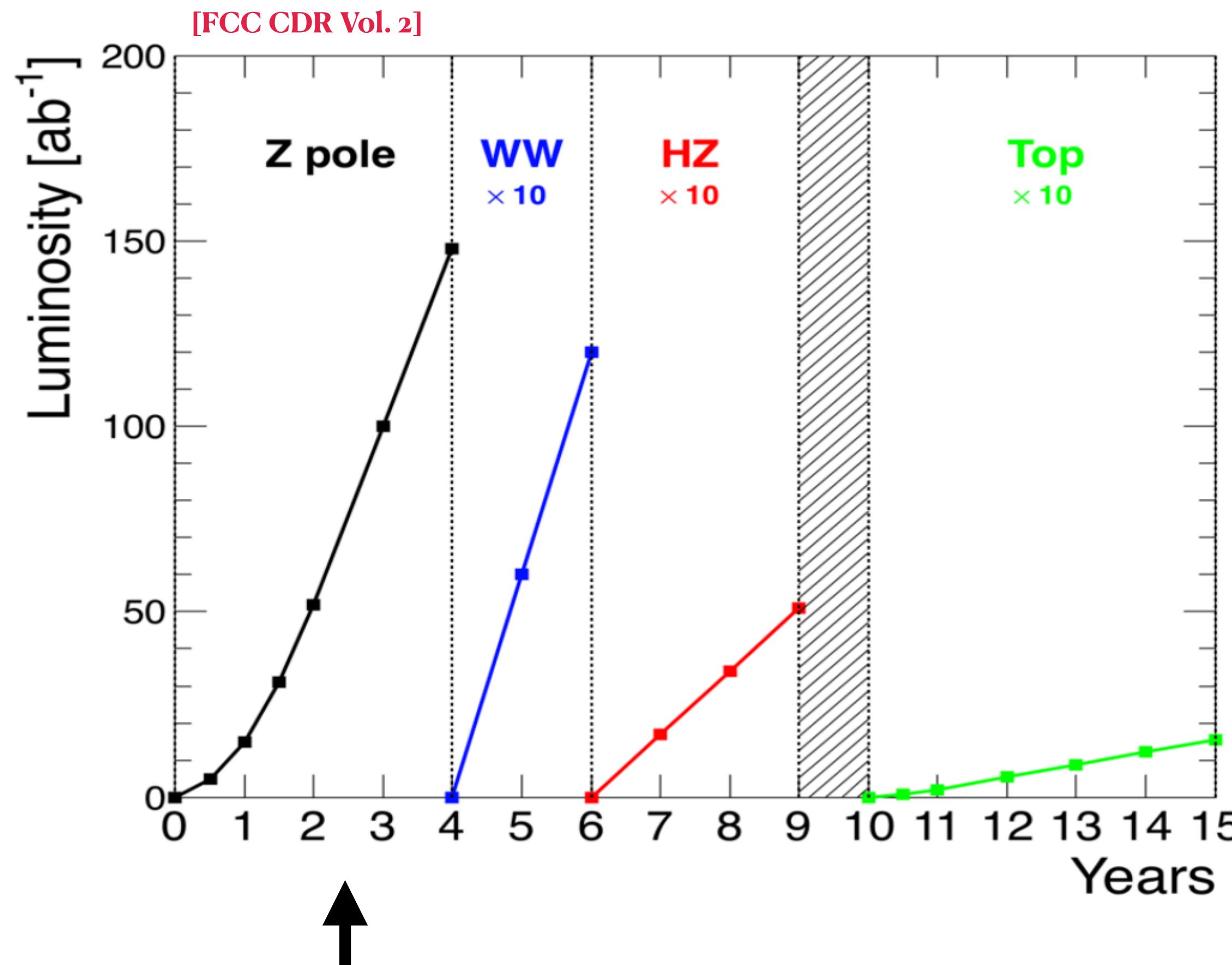
DPF Pheno (May 17th, 2024)

Looking to the Future

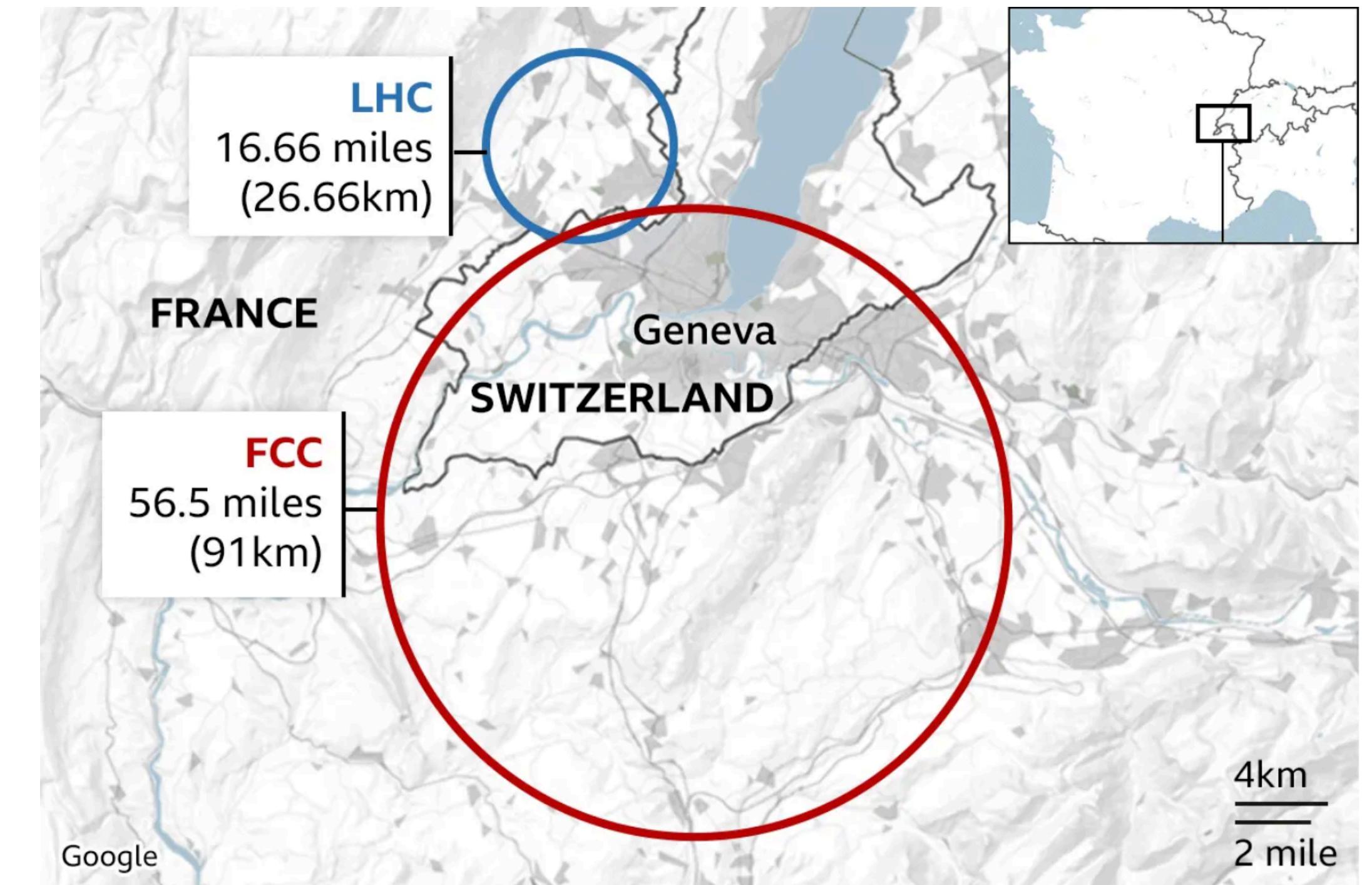


[Figure from BBC]

Looking to the Future



Will produce roughly 5×10^{12} Z-bosons!
(Roughly 10^5 times that produced at LEP)



[Figure from BBC]

Why do we want high statistics?

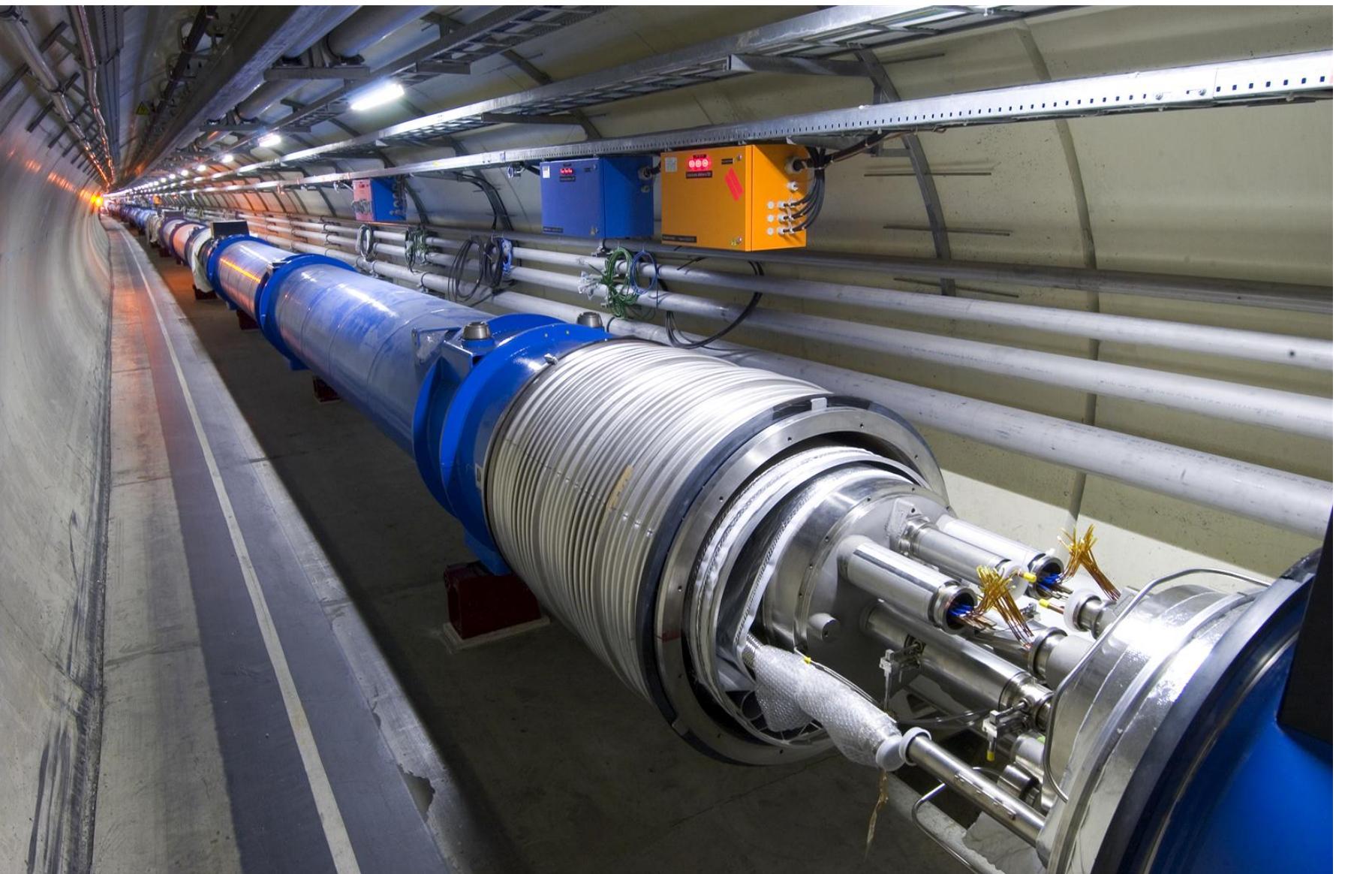
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What experiment explores the highest energy scales?

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What experiment explores the highest energy scales?

LHC?

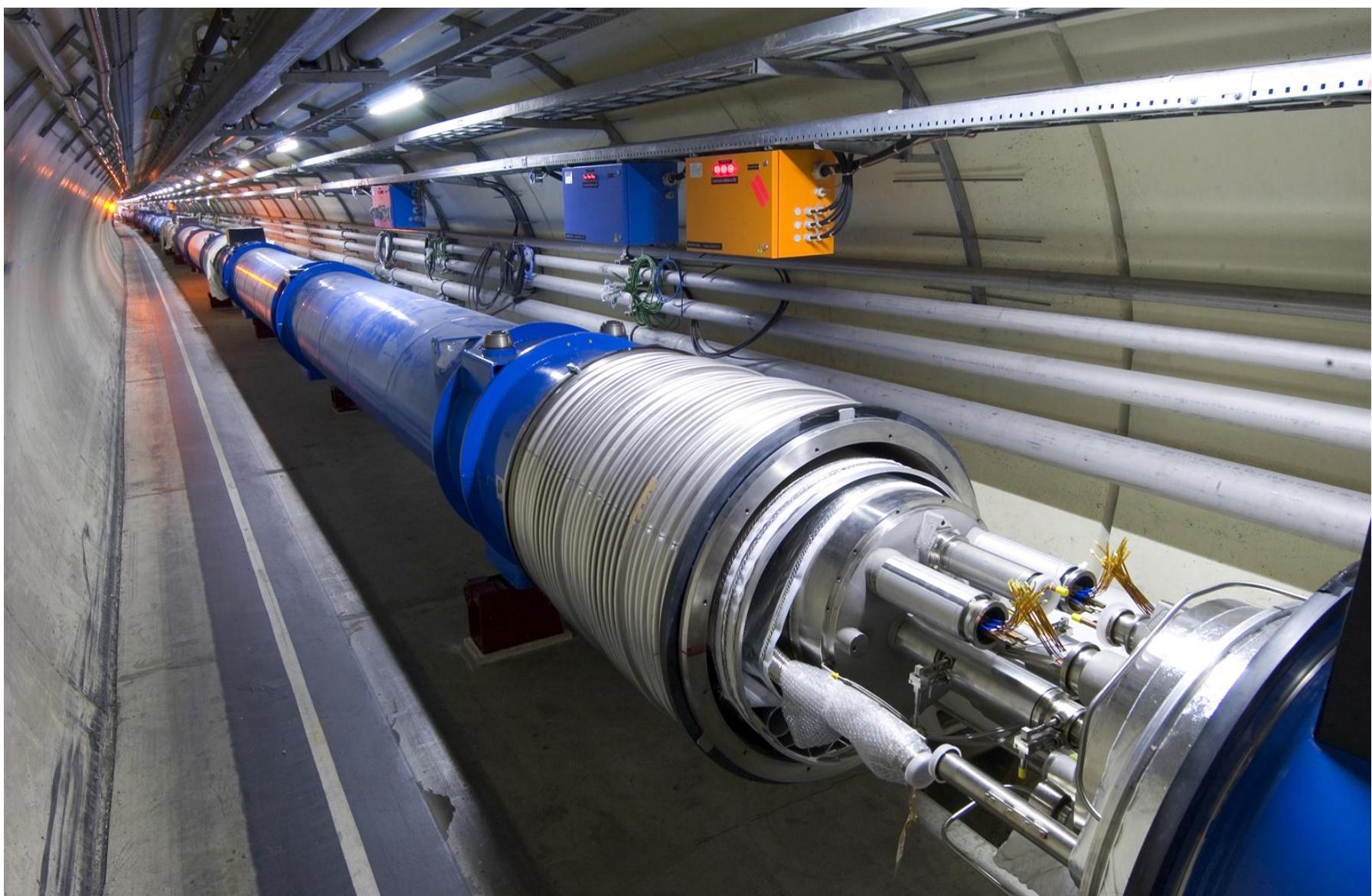


Directly explores energy scales $\Lambda \sim 10^3$ GeV.

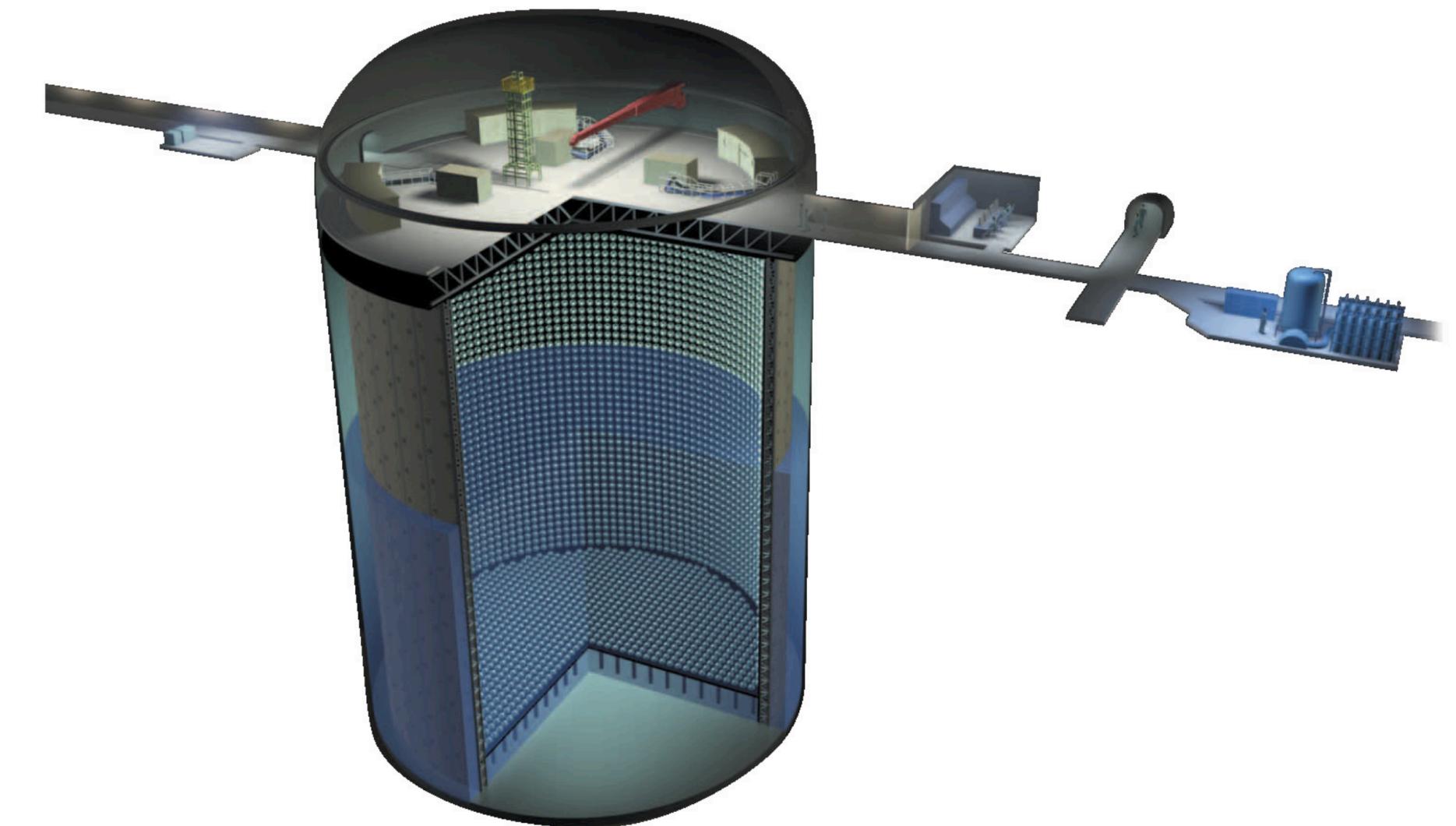
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LHC?



Super-Kamiokande



Directly explores energy scales $\Lambda \sim 10^3$ GeV.

Using 10^{34} protons, indirectly explores baryon violating Dim-6 operators at scales $\Lambda \sim 10^{16}$ GeV.

How can we use the FCC-ee to search for heavy new physics?

Electroweak Precision Tests (EWPTs)

- SM has many more observables than parameters \Rightarrow Predictions!

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$$\mathcal{L} = -\frac{1}{4g'^2}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4g^2}W_{\mu\nu}^AW^{A\mu\nu} + |D_\mu H|^2 - \frac{\lambda}{4}|H|^2 \left(|H|^2 - \frac{v^2}{2} \right)$$

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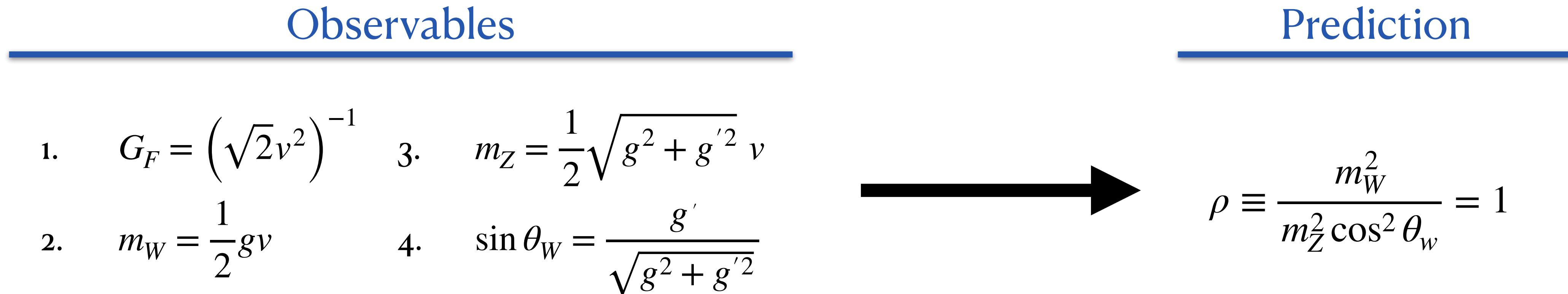
Observables

1. $G_F = \left(\sqrt{2}v^2\right)^{-1}$
2. $m_W = \frac{1}{2}gv$
3. $m_Z = \frac{1}{2}\sqrt{g^2 + g'^2} v$
4. $\sin \theta_W = \frac{g'}{\sqrt{g^2 + g'^2}}$

Electroweak Precision Tests (EWPTs)

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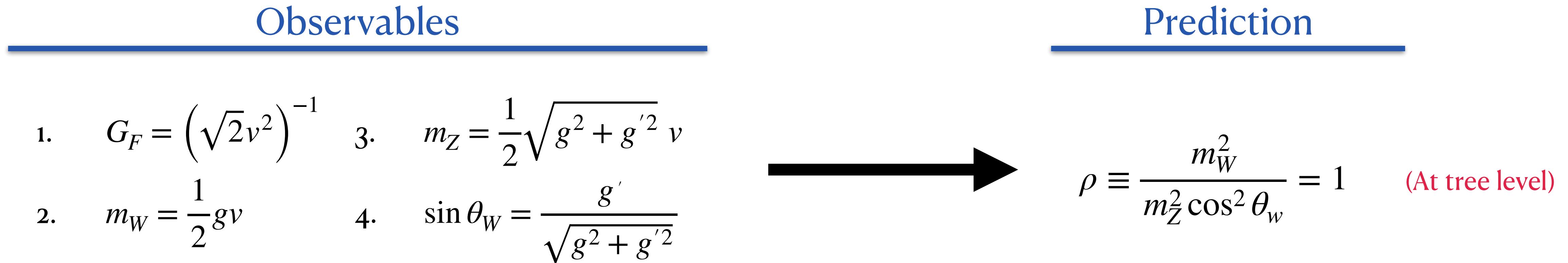
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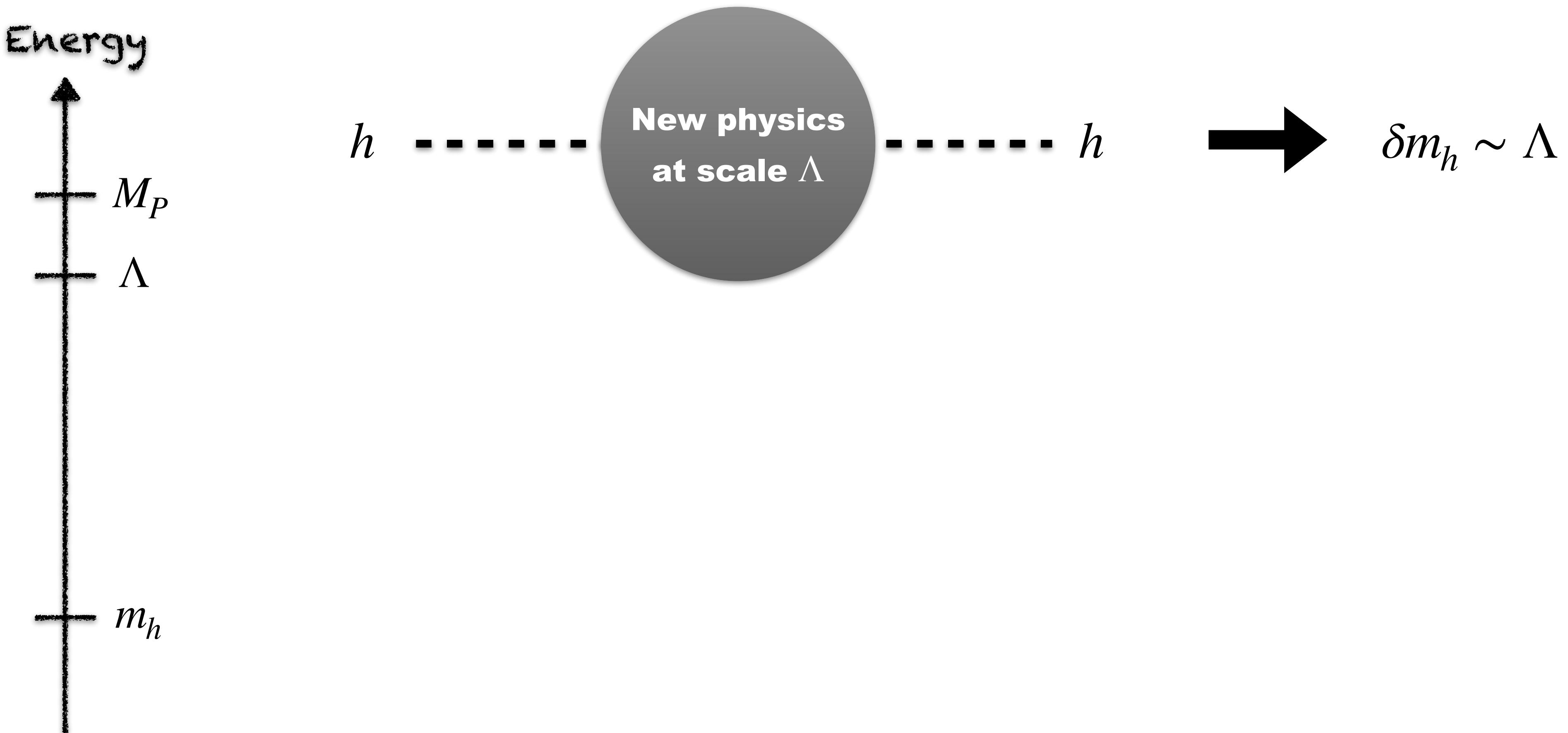
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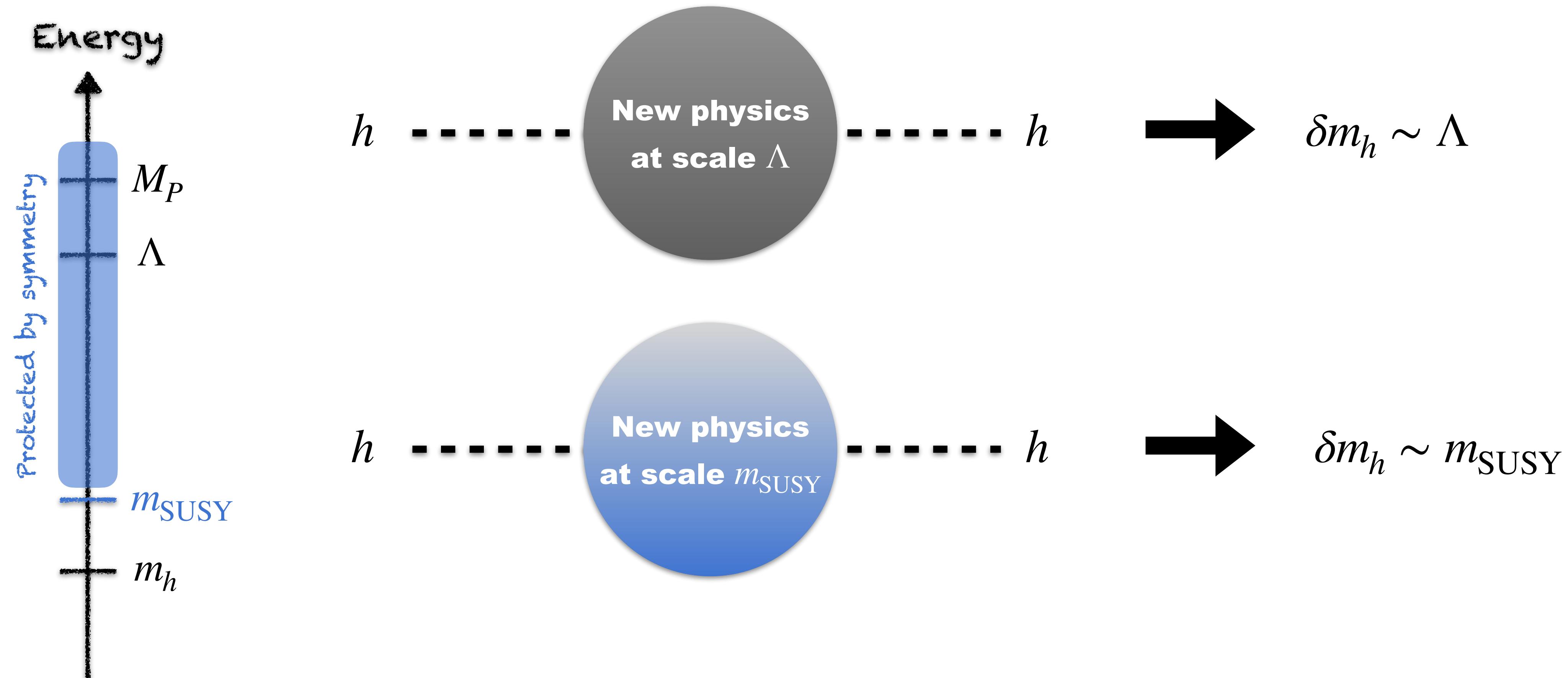
- Checks like this give us a method of indirectly discovering new physics!

What mysteries can we explore using these methods?

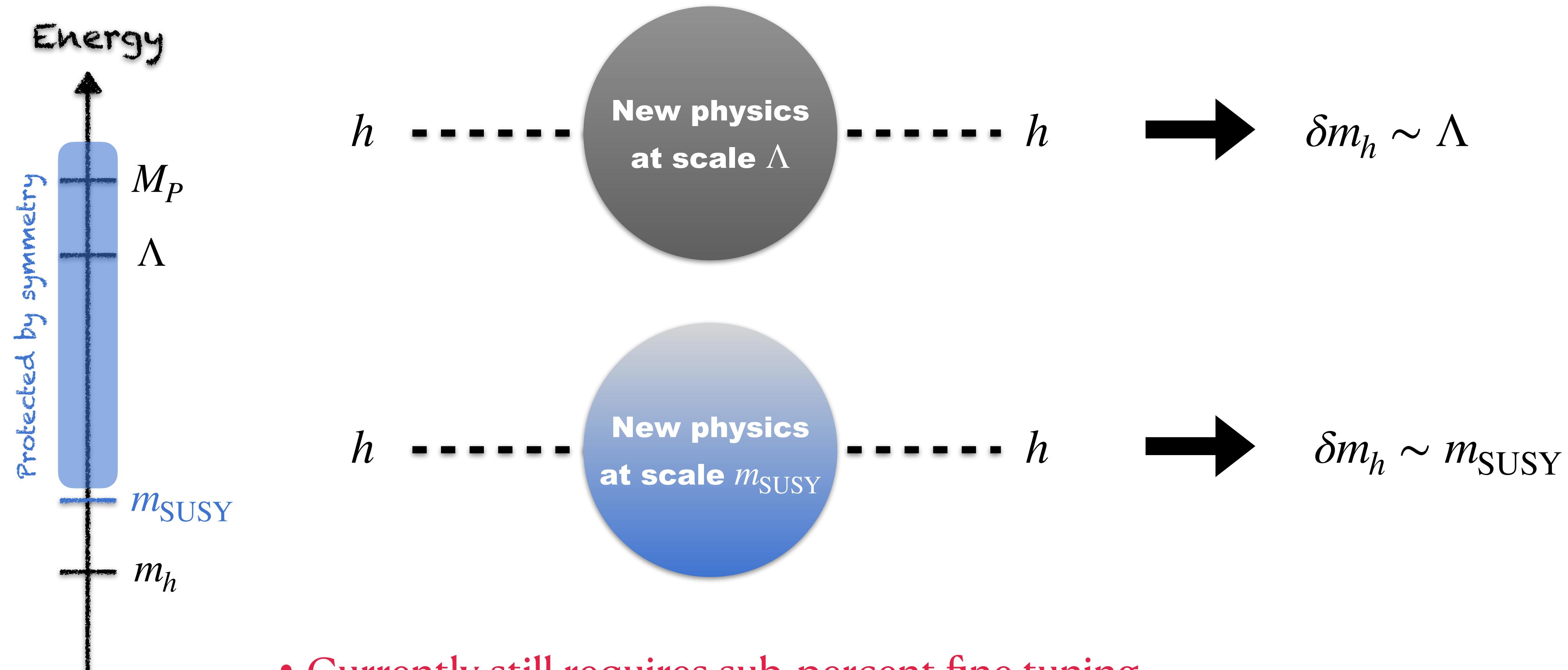
The Higgs Hierarchy Problem



The Higgs Hierarchy Problem

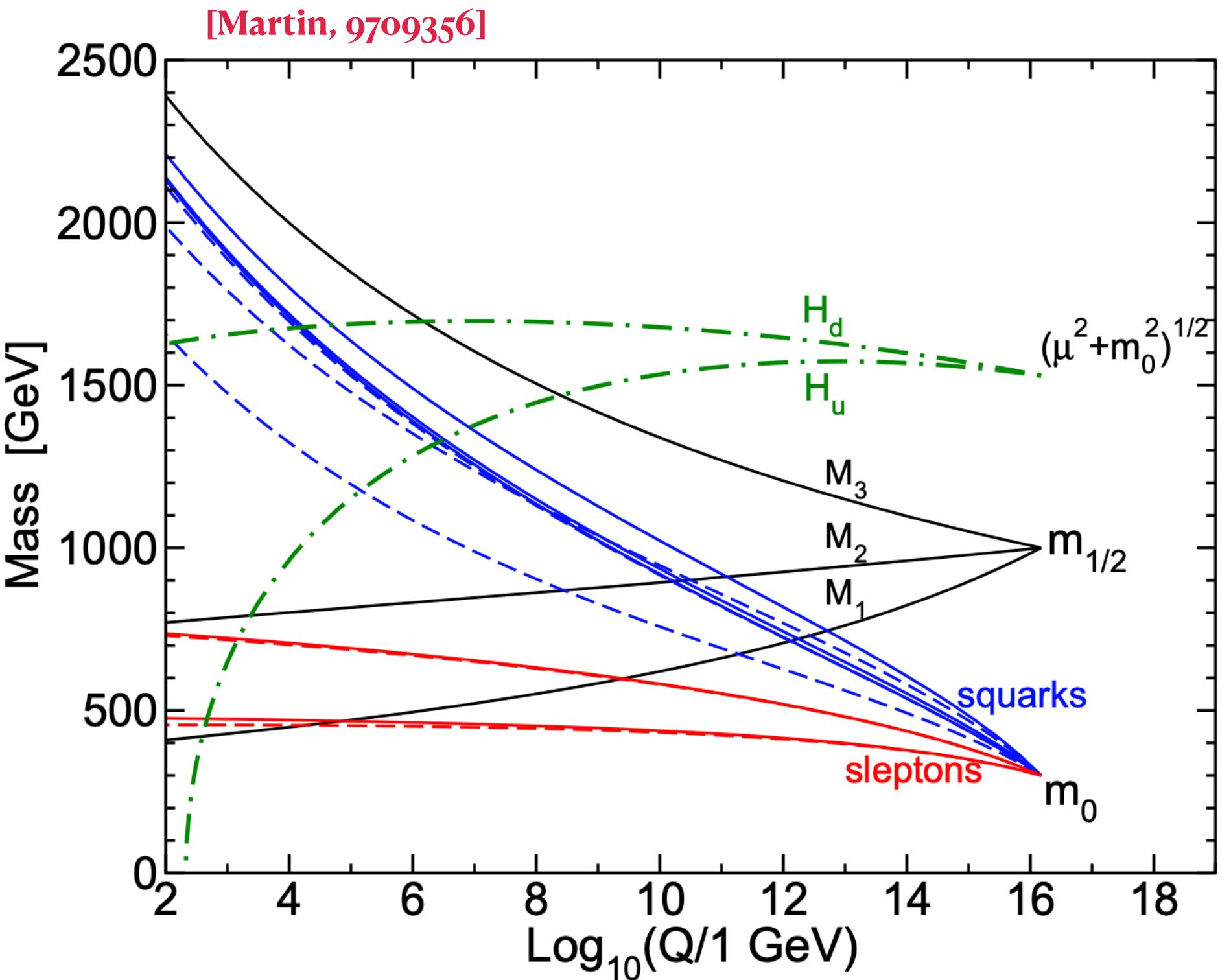


The Higgs Hierarchy Problem



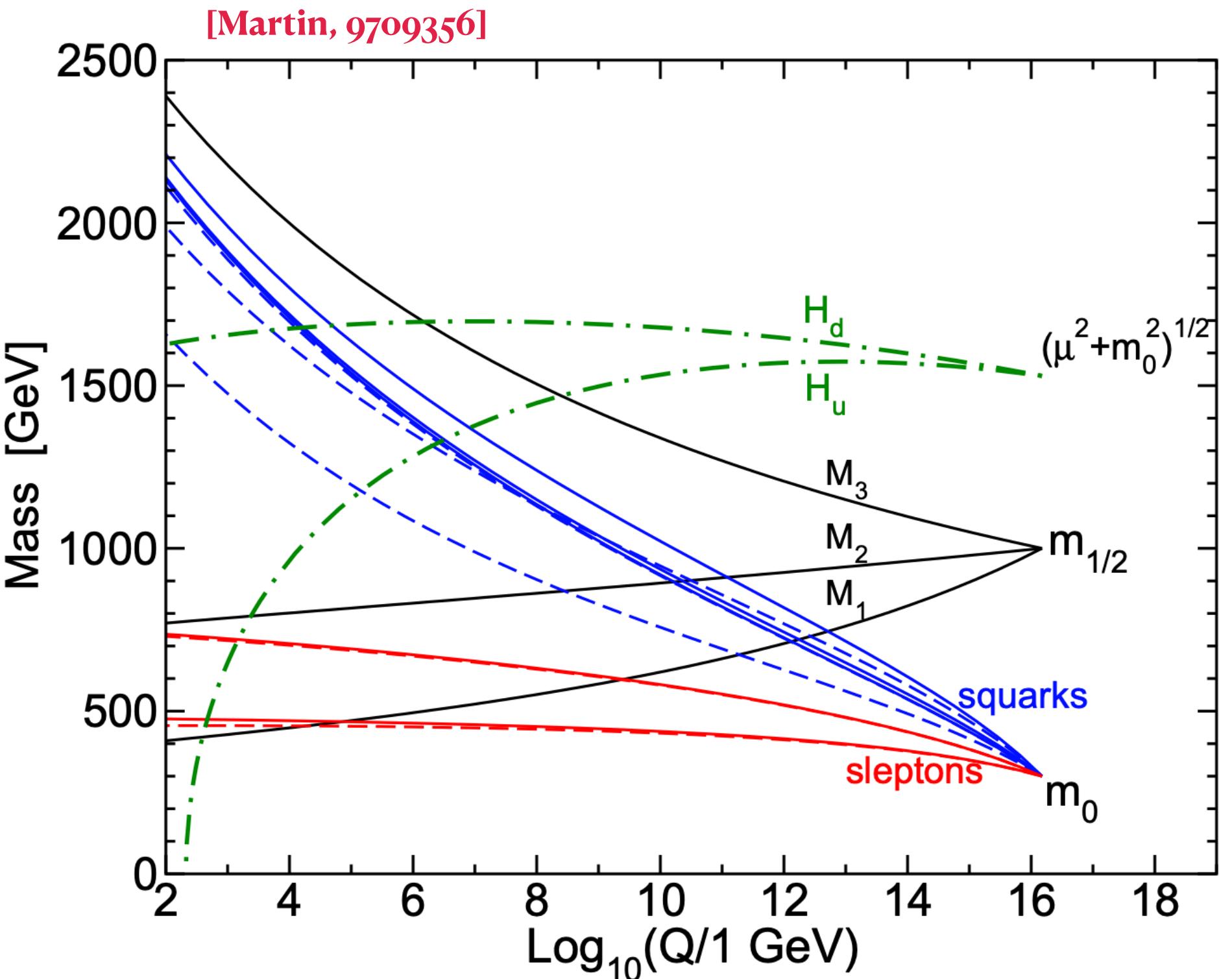
- Currently still requires sub-percent fine tuning.
- Strongest constraints are on colored sparticles (e.g. gluinos and squarks).

Can the FCC-ee See What The LHC Can't?



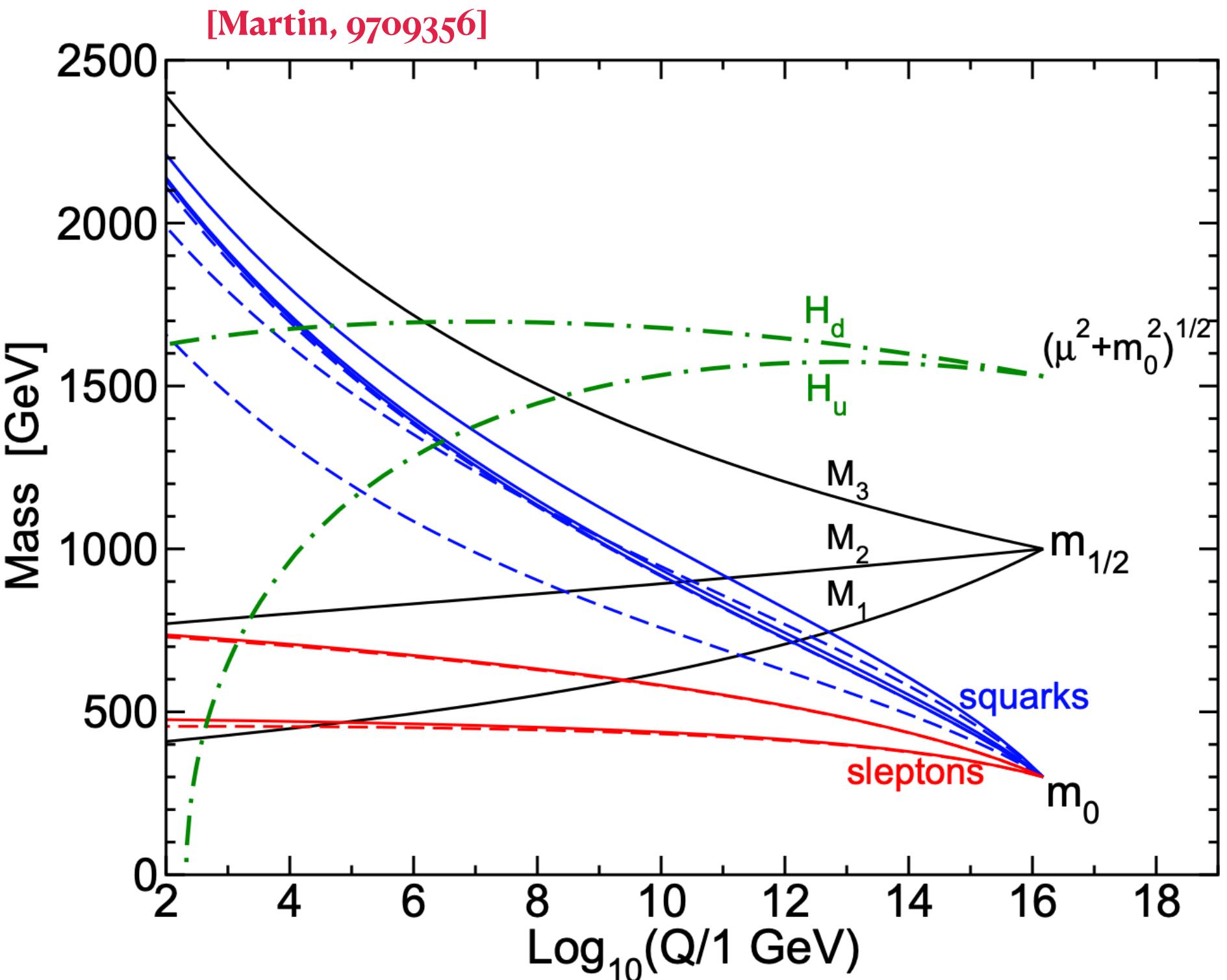
- Running motivates $m_{\text{colored}} > m_{\text{uncolored}}$.

Can the FCC-ee See What The LHC Can't?



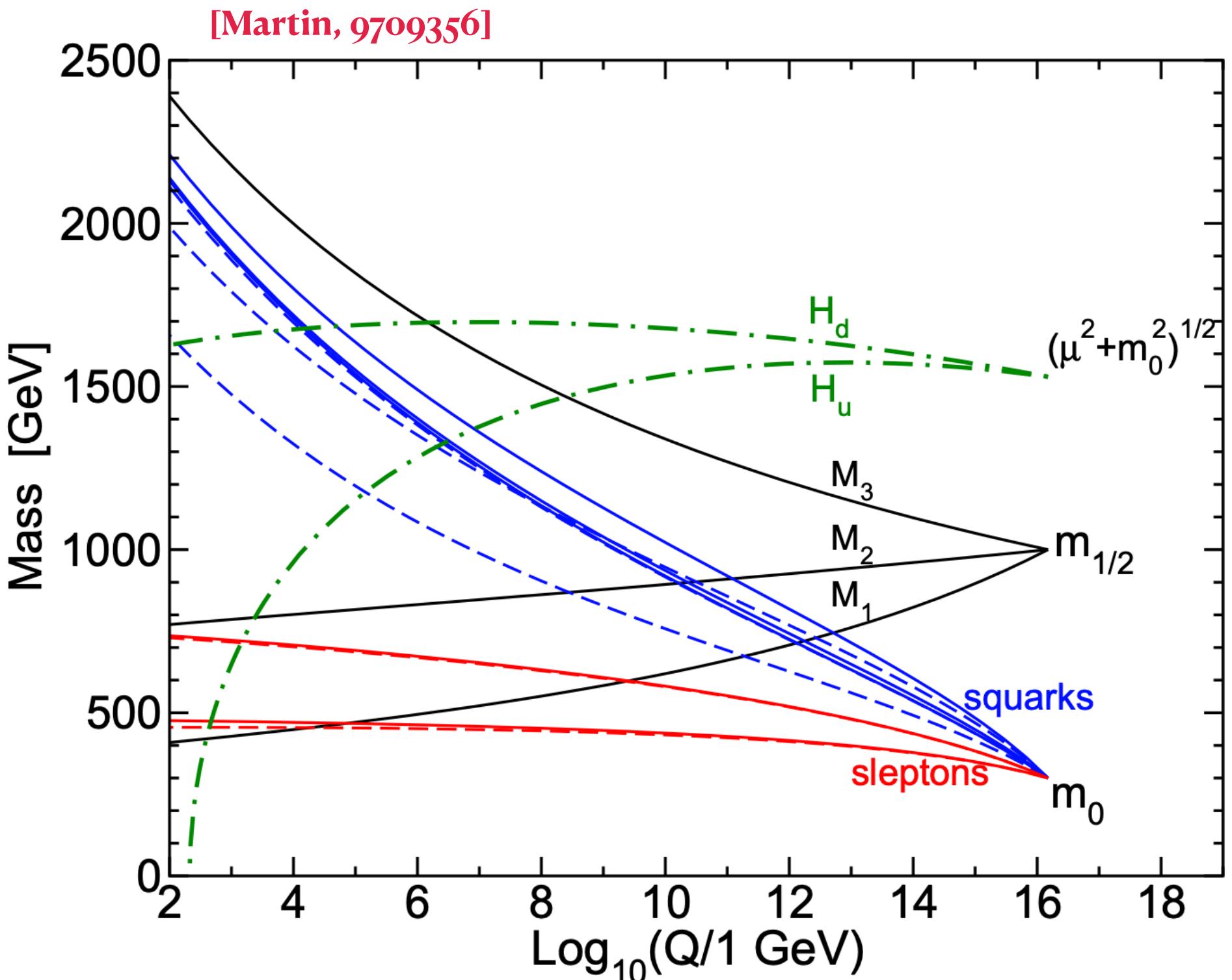
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- Dominant effect on EWPTs may come from color neutral sparticles.

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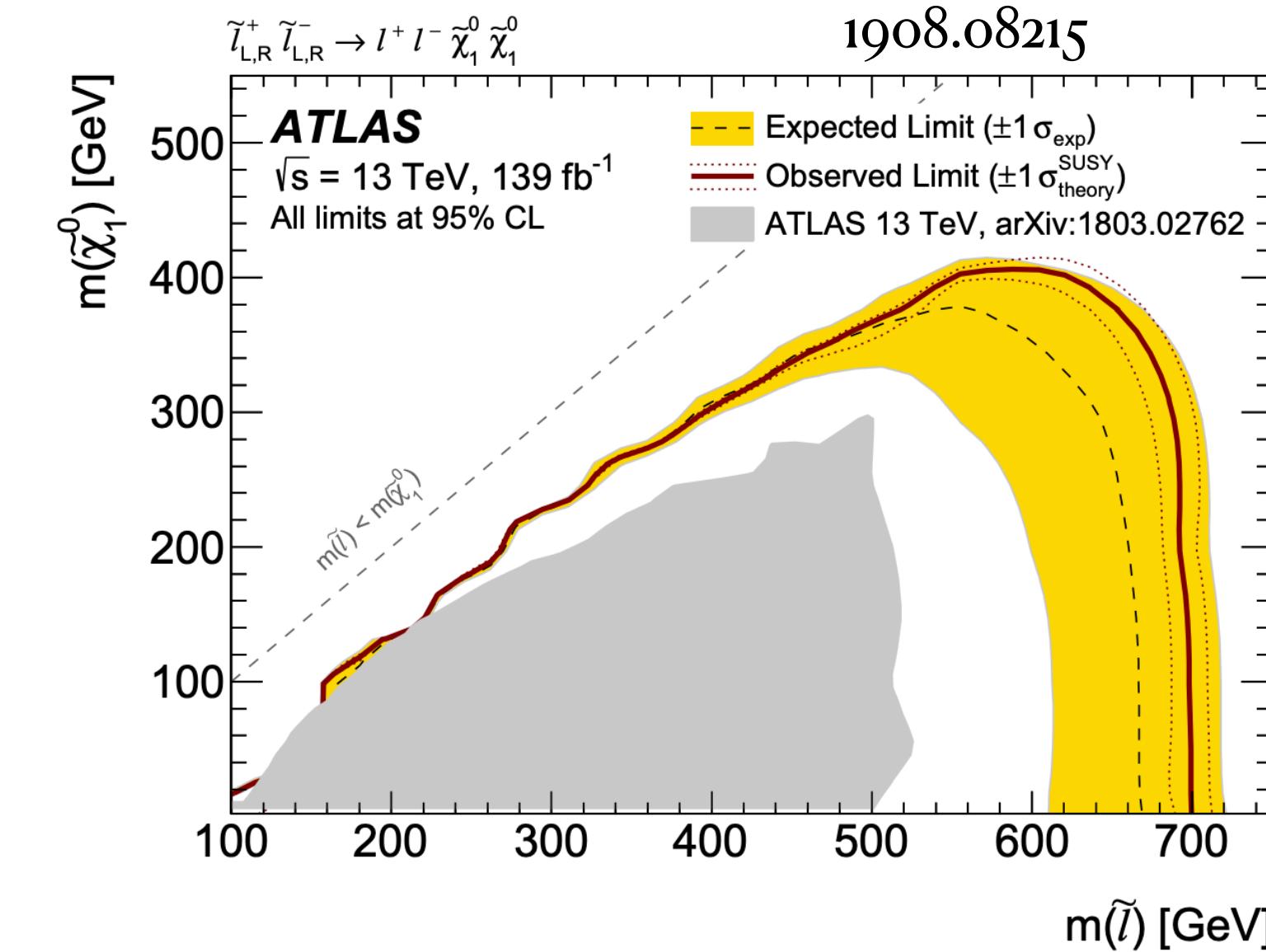
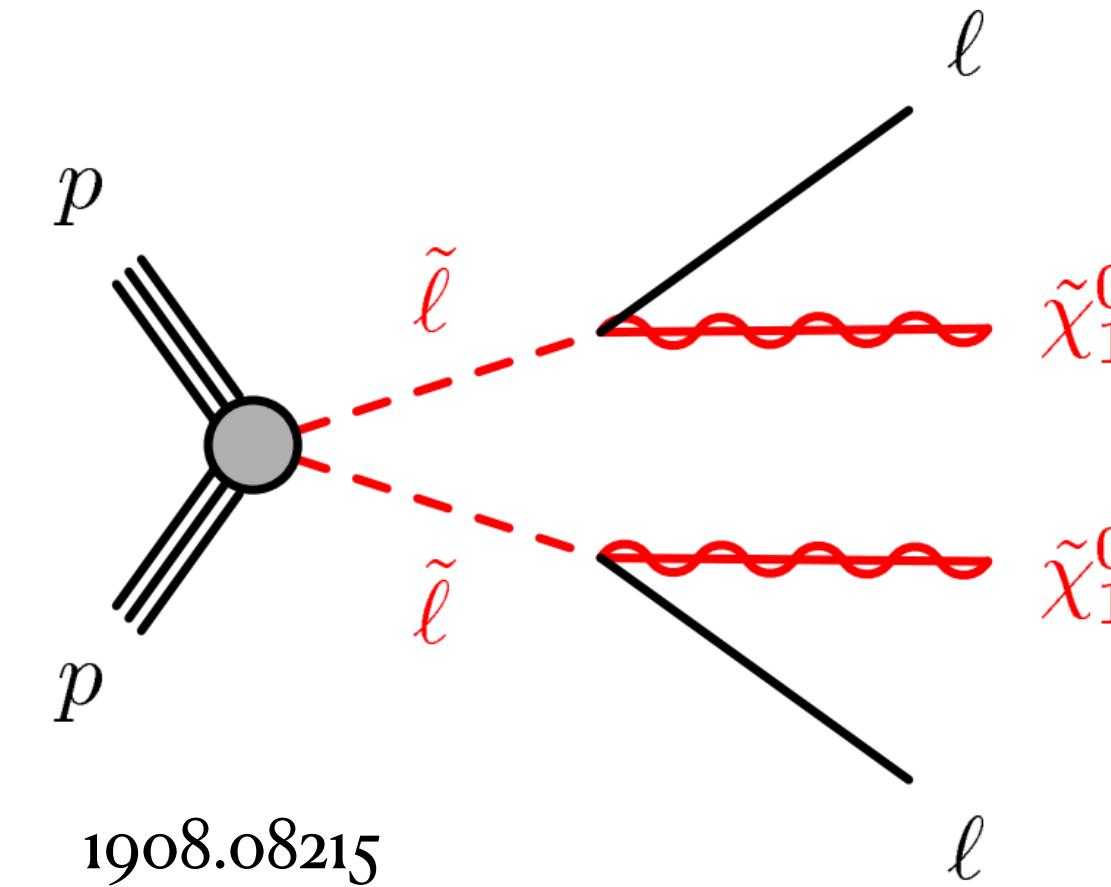


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⇒ FCC-ee may indirectly see SUSY using EWPTs even if the LHC sees nothing.

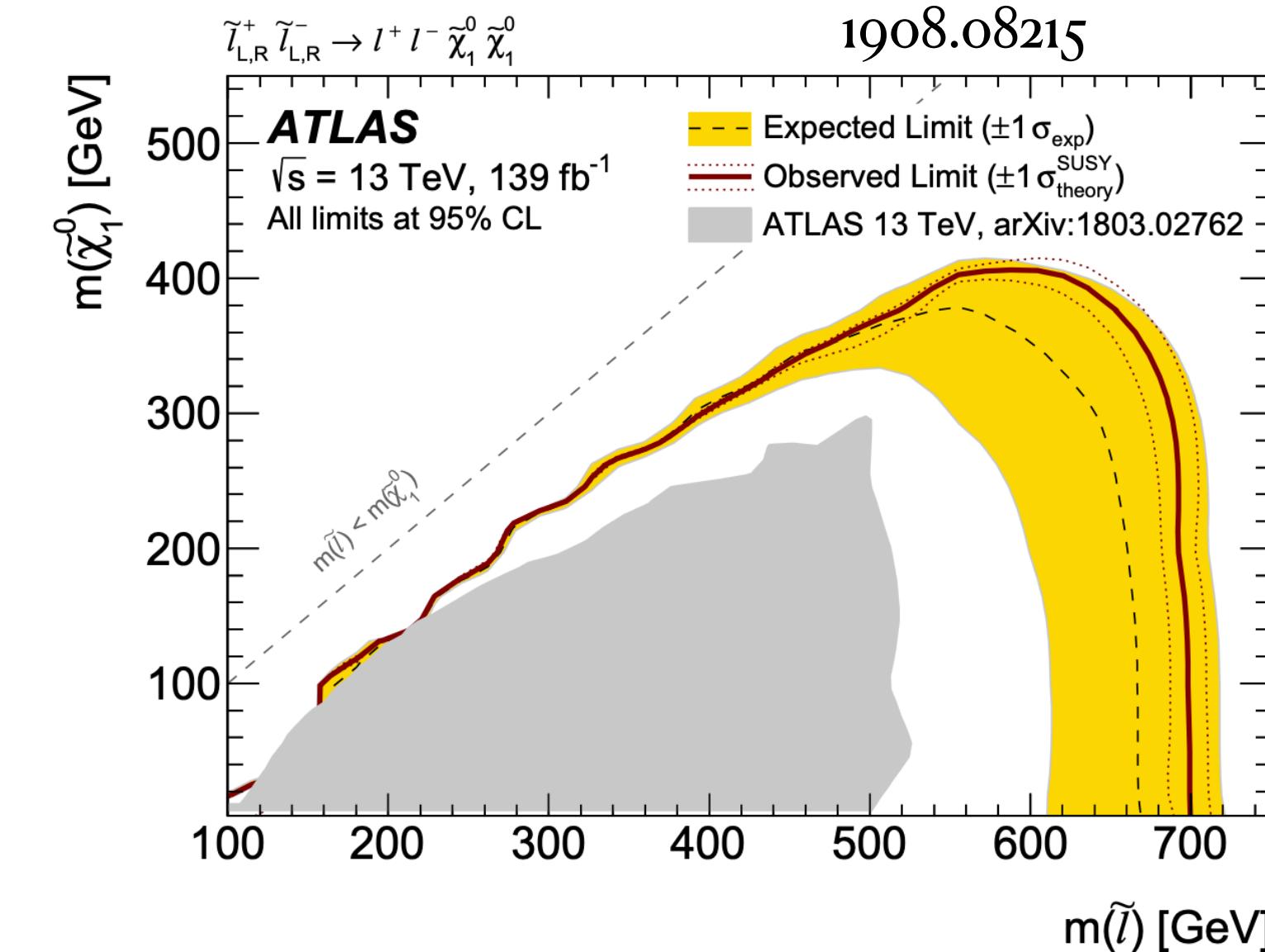
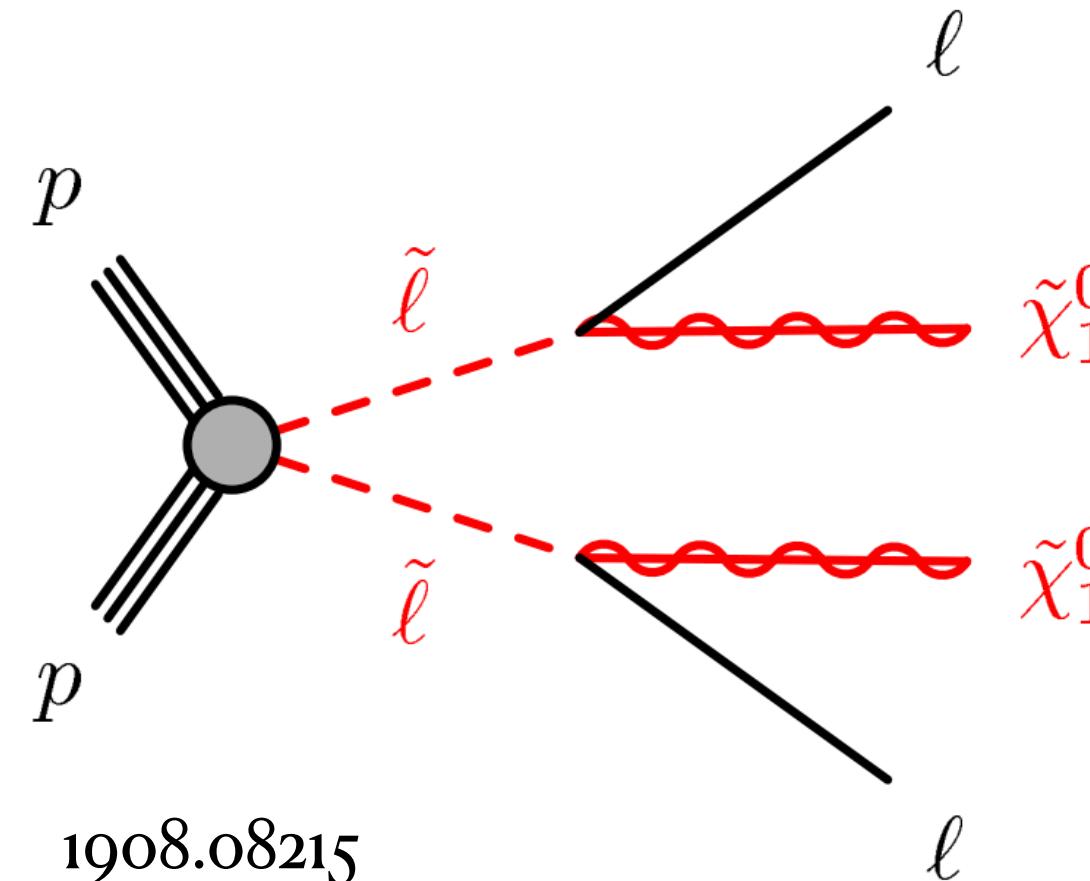
Simplified SUSY Models

LHC SUSY searches often consider representative simplified models.



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For simplicity we will do the same:

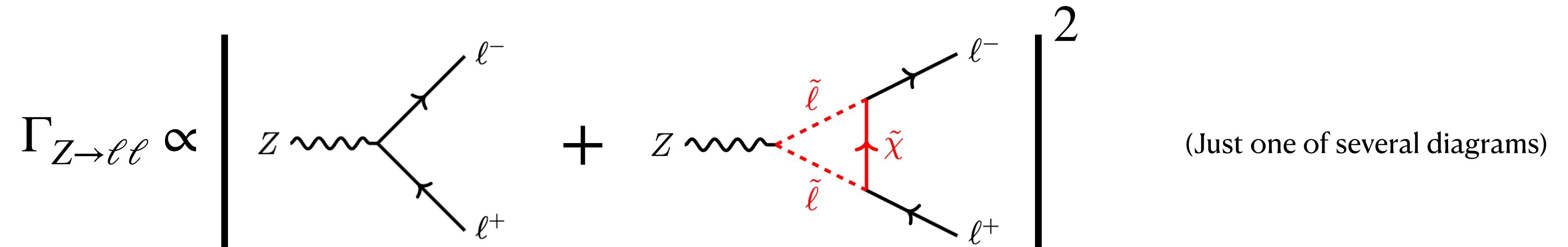
1. Pure Bino + RH Slepton model $\supset (\tilde{B}, \tilde{e})$
2. Pure Wino + LH Slepton model $\supset (\tilde{W}, \tilde{L})$.

How might SUSY show up in EWPTs?

Let $\tilde{\chi} = (\tilde{W}, \tilde{B})$ and $\tilde{\ell} = (\tilde{L}, \tilde{e})$.

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$$\Gamma_{Z \rightarrow \ell\ell} \propto \left| Z \text{ wavy line} \begin{array}{c} \ell^- \\ + \\ \ell^+ \end{array} \right. + \left| Z \text{ wavy line} \begin{array}{c} \tilde{\ell} \\ \tilde{\chi} \\ \tilde{\ell} \\ \tilde{\chi} \end{array} \begin{array}{c} \ell^- \\ \times \\ \ell^+ \end{array} \right|^2 \quad (\text{Just one of several diagrams})$$
$$\Gamma_{Z \rightarrow \ell\ell} - \Gamma_{Z \rightarrow \ell\ell}^{(SM)} \propto \text{Re} \left(Z \text{ wavy line} \begin{array}{c} \ell^- \\ \times \\ \ell^+ \end{array} \times \left| Z \text{ wavy line} \begin{array}{c} \tilde{\ell} \\ \tilde{\chi} \\ \tilde{\ell} \\ \tilde{\chi} \end{array} \begin{array}{c} \ell^- \\ \times \\ \ell^+ \end{array} \right|^2 \right)$$

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$$\Gamma_{Z \rightarrow \ell\ell} - \Gamma_{Z \rightarrow \ell\ell}^{(SM)} \propto \text{Re} \left(Z \text{ wavy line} \begin{array}{c} \ell^- \\ + \\ \ell^+ \end{array} \times Z \text{ wavy line} \begin{array}{c} \tilde{\ell} \\ \tilde{\chi} \\ \tilde{\ell} \\ \tilde{\chi} \end{array} \begin{array}{c} \ell^- \\ + \\ \ell^+ \end{array} \right)$$
$$\frac{\Gamma_{Z \rightarrow \ell\ell} - \Gamma_{Z \rightarrow \ell\ell}^{(SM)}}{\Gamma_{Z \rightarrow \ell\ell}^{(SM)}} \propto \frac{g^2}{16\pi^2} \left(\frac{m_Z}{M_{\text{SUSY}}} \right)^2 \longrightarrow M_{\text{SUSY}}^{\text{probed}} \sim 1 \text{ TeV} \times \left(\frac{\delta\Gamma/\Gamma}{10^{-5}} \right)$$

Some details

$\Gamma(Z \rightarrow \ell\bar{\ell})$ is not the best observable. Instead we use

$$R_\ell \equiv \frac{\Gamma(Z \rightarrow \text{hadrons})}{\Gamma(Z \rightarrow \ell\bar{\ell})}$$

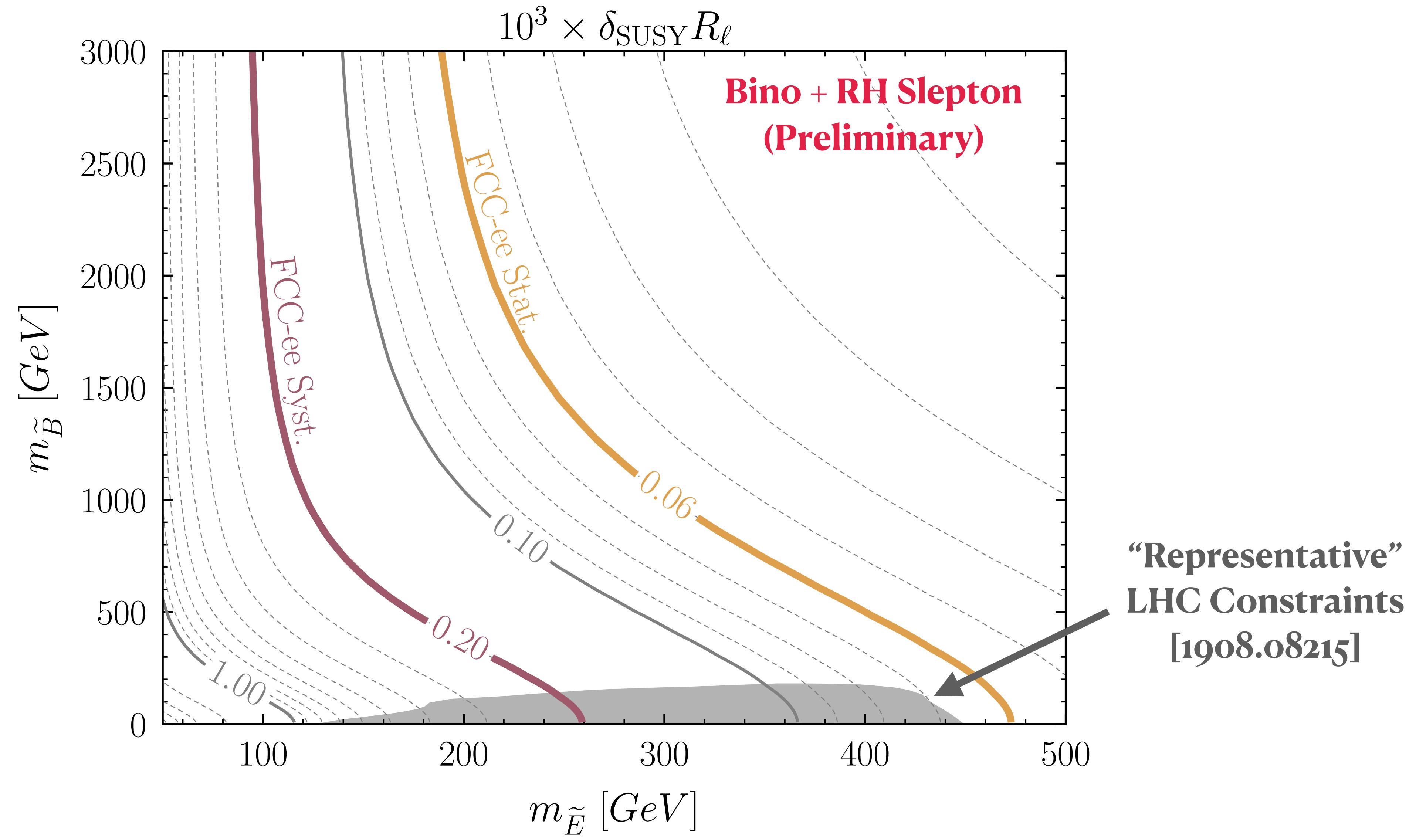
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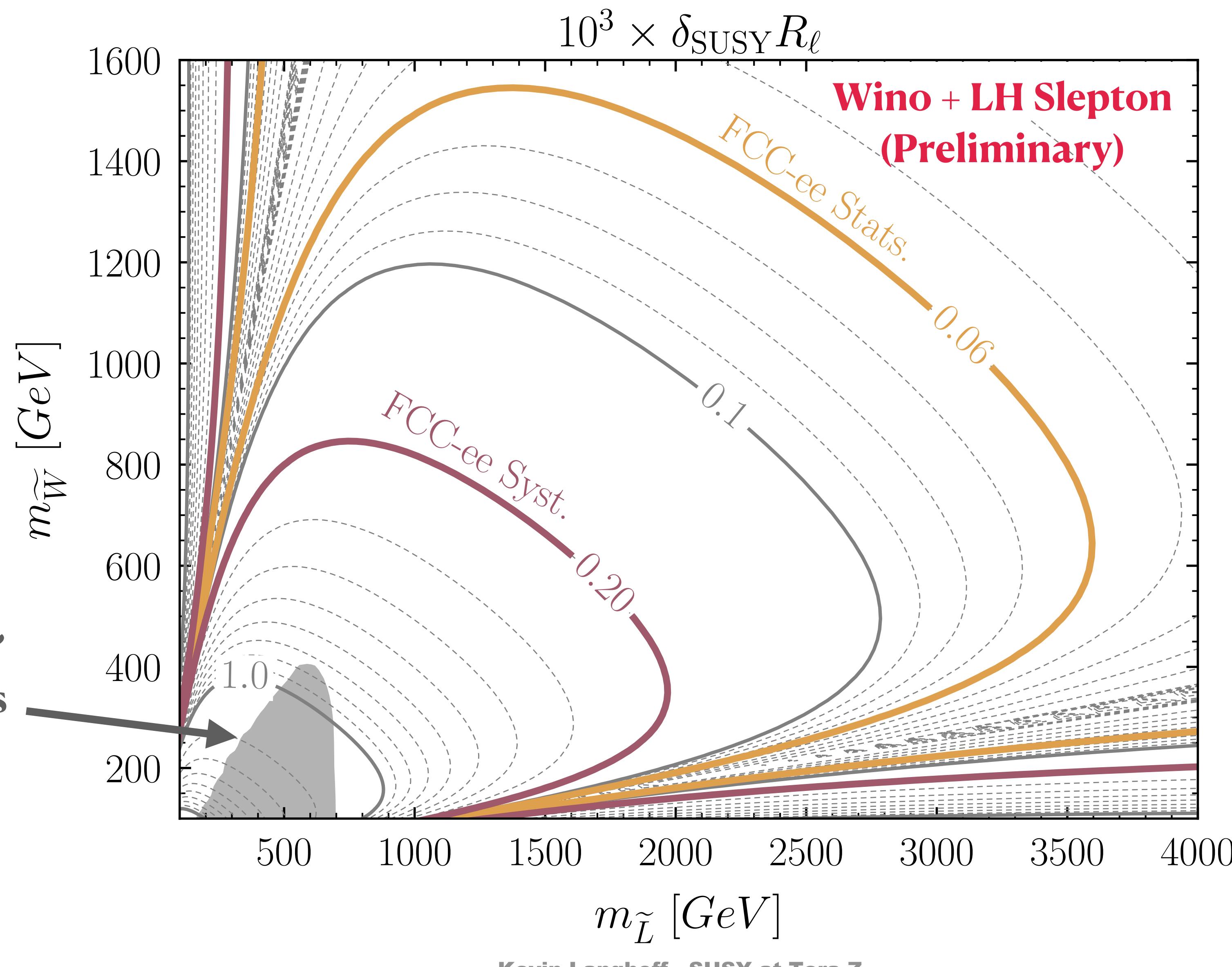
Still depends on θ_W and $\alpha_s(M_Z)$. These must be determined by other measurements.

Results



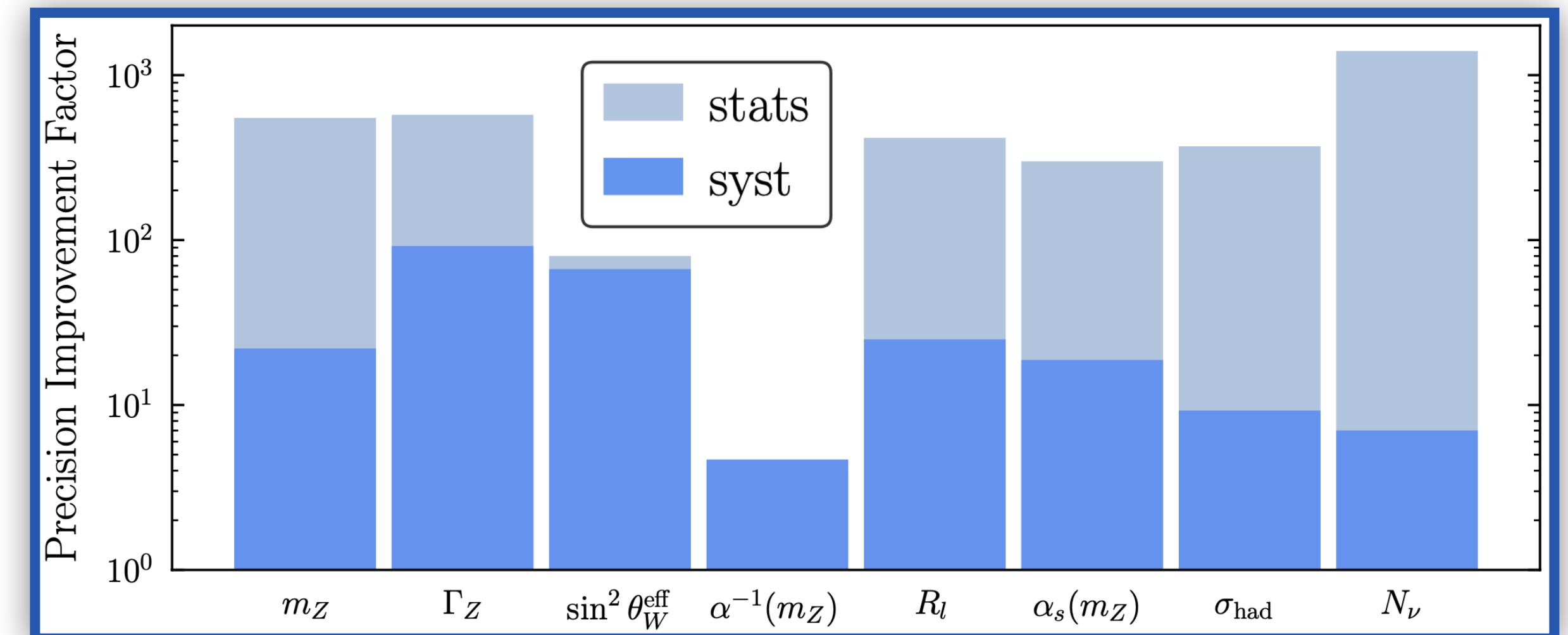
Results

“Representative”
LHC Constraints
[1908.08215]



Conclusion

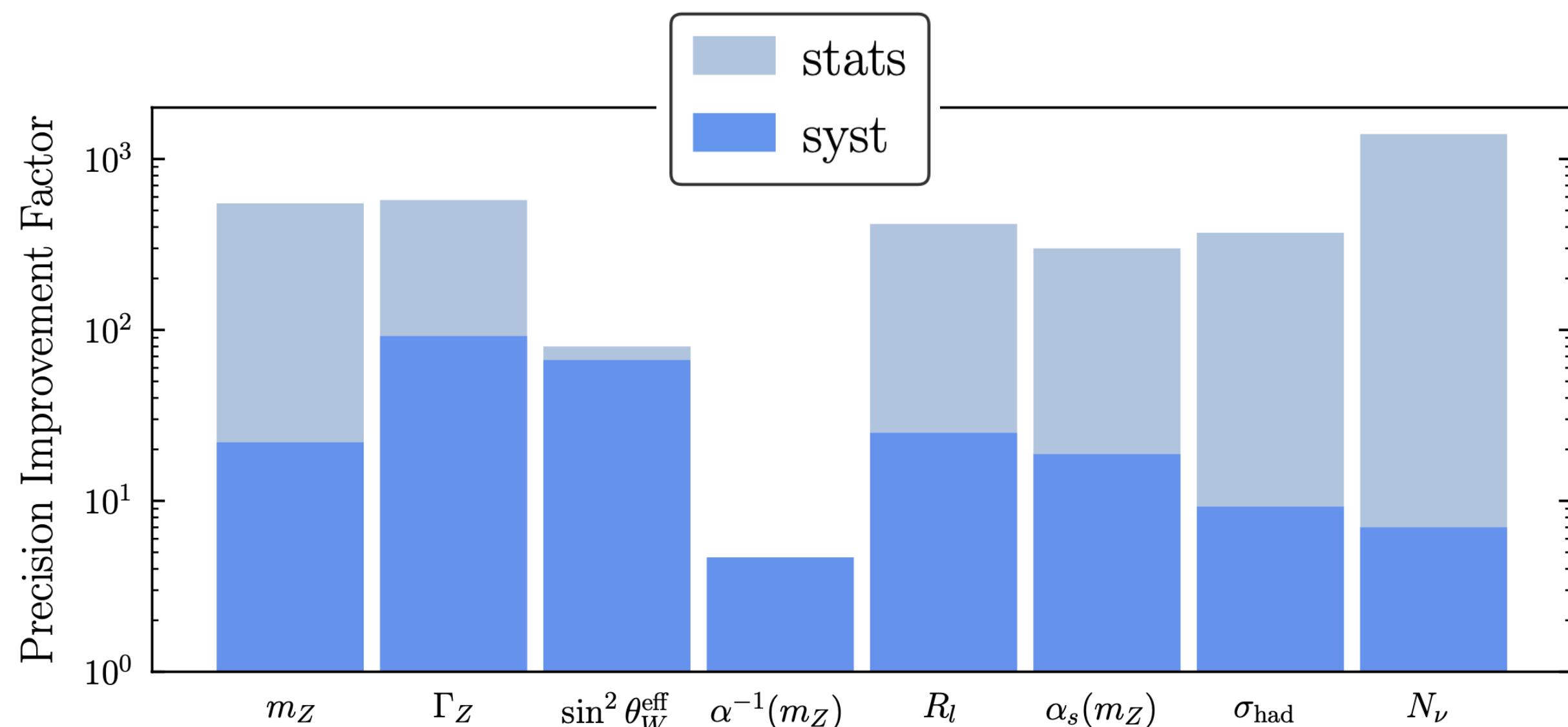
- EWPTs at the FCC-ee are interesting ways to search for new physics.
- These searches can be complimentary to direct searches at the LHC.
- There exists some SUSY parameter space which may be explored at the FCC-ee.
- A more thorough investigation into which observables/signatures are motivated by various models may motivate further dedication to the reduction of certain systematics.



Backup Slides

Electroweak Precision Tests at the Z-pole

There are many measurements which can be performed at the Z-pole.



Many measurements are systematics limited!

Which systematics should we prioritize reducing?

Observable	Present value ± error	FCC-ee Stat.	FCC-ee Syst.
m_Z (keV)	$91,186,700 \pm 2200$	5	100
Γ_Z (keV)	$2,495,200 \pm 2300$	8	100
$R_\ell^Z (\times 10^3)$	$20,767 \pm 25$	0.06	0.2–1.0
$\alpha_s(m_Z) (\times 10^4)$	1196 ± 30	0.1	0.4–1.6
$R_b (\times 10^6)$	$216,290 \pm 660$	0.3	< 60
$\sigma_{\text{had}}^0 (\times 10^3)$ (nb)	$41,541 \pm 37$	0.1	4
$N_\nu (\times 10^3)$	2991 ± 7	0.005	1
$\sin^2 \theta_W^{\text{eff}} (\times 10^6)$	$231,480 \pm 160$	3	2–5
$1/\alpha_{\text{QED}}(m_Z) (\times 10^3)$	$128,952 \pm 14$	4	Small
$A_{\text{FB}}^{b,0} (\times 10^4)$	992 ± 16	0.02	1–3
$A_{\text{FB}}^{\text{pol},\tau} (\times 10^4)$	1498 ± 49	0.15	< 2
m_W (MeV)	$80,350 \pm 15$	0.5	0.3
Γ_W (MeV)	2085 ± 42	1.2	0.3
$\alpha_s(m_W) (\times 10^4)$	1170 ± 420	3	Small
$N_\nu (\times 10^3)$	2920 ± 50	0.8	Small
m_{top} (MeV)	$172,740 \pm 500$	17	Small
Γ_{top} (MeV)	1410 ± 190	45	Small
$\lambda_{\text{top}}/\lambda_{\text{top}}^{\text{SM}}$	1.2 ± 0.3	0.1	Small
ttZ couplings	$\pm 30\%$	0.5–1.5%	Small

[FCC CDR]

Oblique Corrections

- Assuming heavy new physics dominantly modifies SM gauge boson propagators, corrections from heavy new physics can be quantified by a set of oblique parameters.



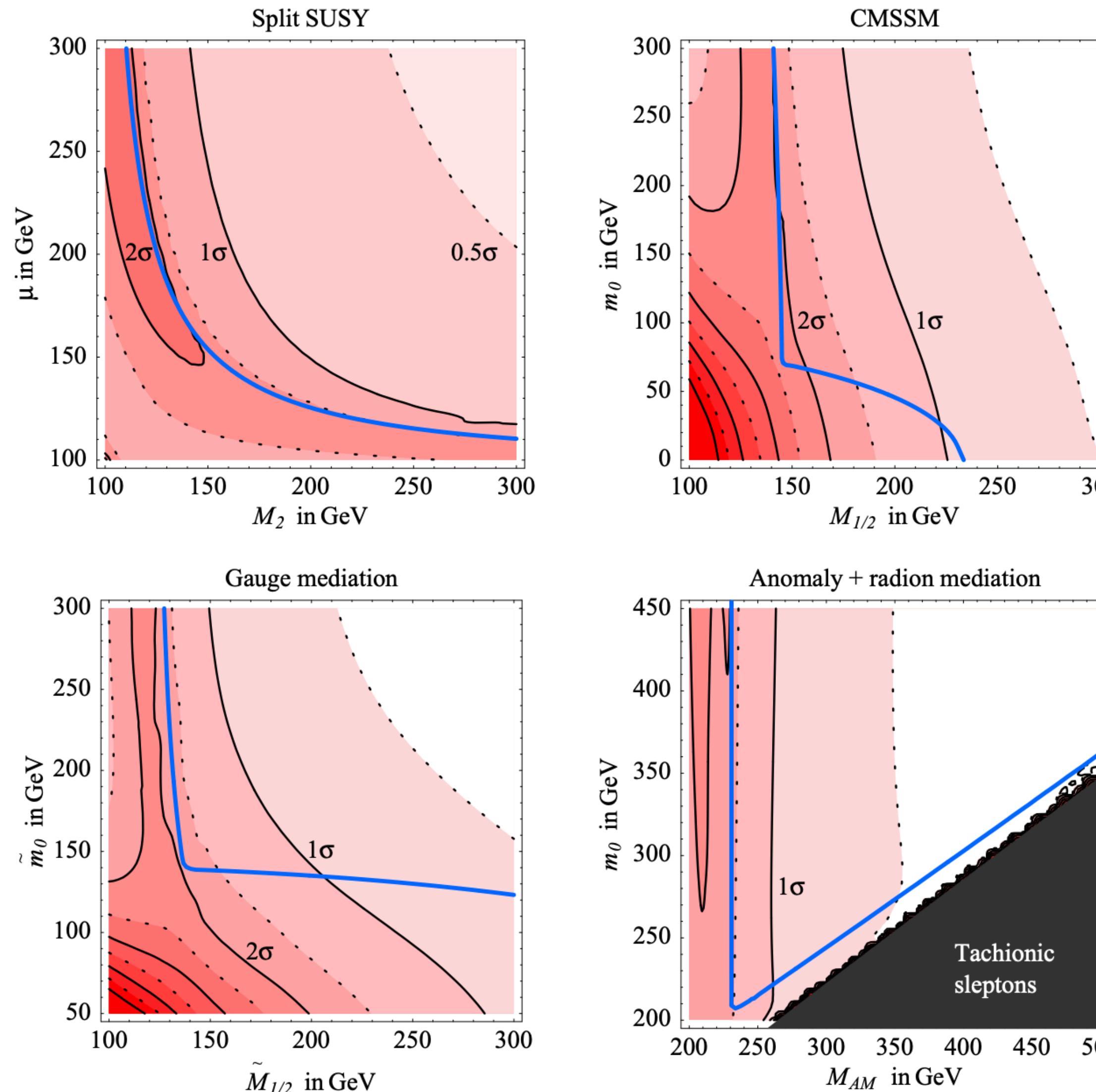
Oblique parameter	Corresponding dim-6 operator
$\hat{S} = \frac{g}{g'} \Pi'_{W^3 B}(0)$	$\mathcal{O}_S = H^\dagger \tau^a H W_{\mu\nu}^a B^{\mu\nu}$
$\hat{T} = m_W^{-2} [\Pi_{W^3 W^3}(0) - \Pi_{W^+ W^-}(0)]$	$\mathcal{O}_T = H^\dagger D_\mu H ^2$
$W = \frac{1}{2} m_W^2 \Pi''_{W^3 W^3}(0)$	$\mathcal{O}_W = \frac{1}{2} (D_\rho W_{\mu\nu}^a)^2$
$Y = \frac{1}{2} m_W^2 \Pi''_{BB}(0)$	$\mathcal{O}_Y = \frac{1}{2} (\partial_\rho B_{\mu\nu})^2$

- Simple, but not completely general.

X	$\hat{S} \times \left(\frac{m_X^2}{m_W^2} \right)$	$\hat{T} \times \left(\frac{m_X^2}{m_W^2} \right)$	$W \times \left(\frac{m_X^2}{m_W^2} \right)$	$Y \times \left(\frac{m_X^2}{m_W^2} \right)$
\tilde{E}	0	0	0	$\frac{\alpha_Y}{40\pi}$
\tilde{L}	$-\frac{\alpha_W c_{2\beta}}{16\pi}$	$\frac{\alpha_W c_{2\beta}^2}{16\pi}$	$\frac{\alpha_W}{80\pi}$	$\frac{\alpha_Y}{80\pi}$
\tilde{B}	0	0	0	0
\tilde{W}	0	0	$\frac{\alpha_W}{15\pi}$	0

Supersymmetry and precision data after LEP2 [0502095]

Guido Marandella^a, Christian Schappacher^b, Alessandro Strumia^c



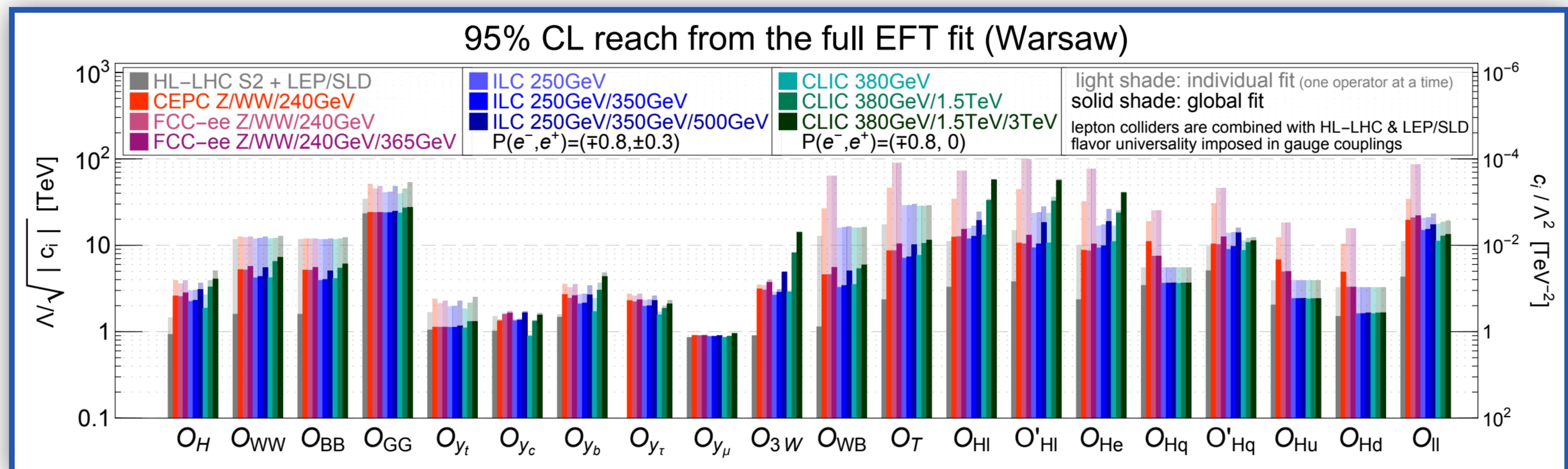
Focuses on
oblique corrections

Electroweak Precision Tests

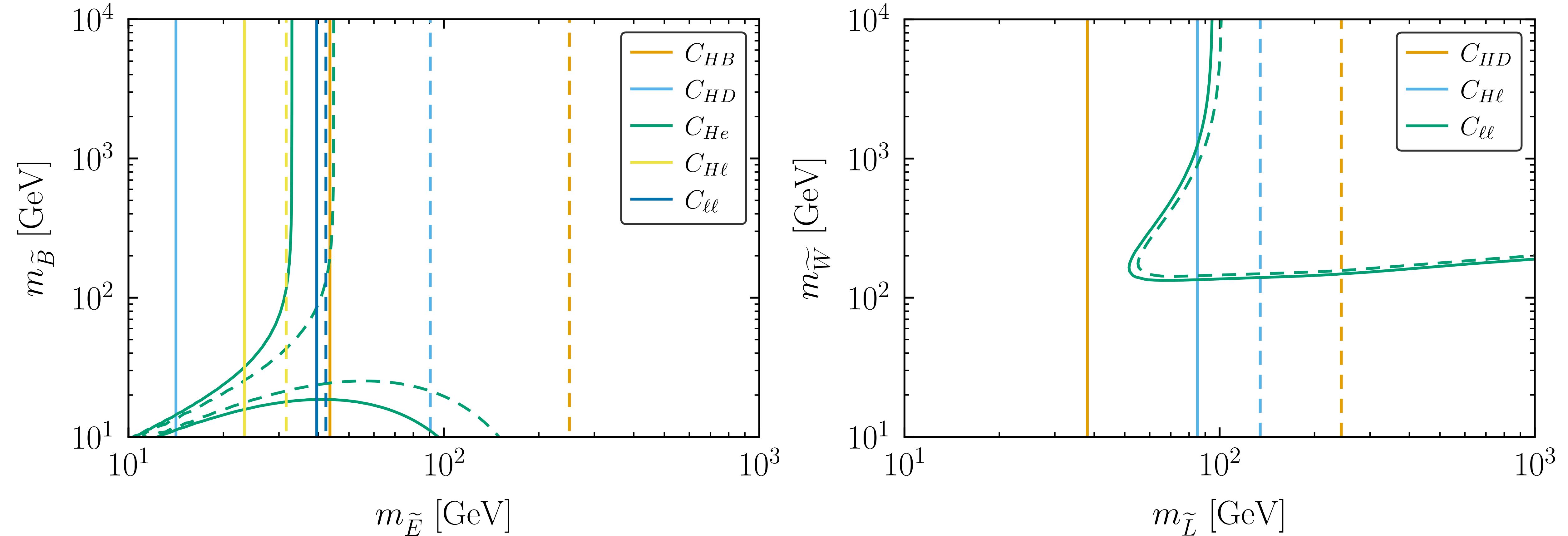
- The most general method of indirectly searching for heavy new physics is SMEFT.

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_{n=5}^{\infty} \sum_i \frac{c_i^{(n)}}{\Lambda^{n-4}} \mathcal{O}_i^{(n)}$$

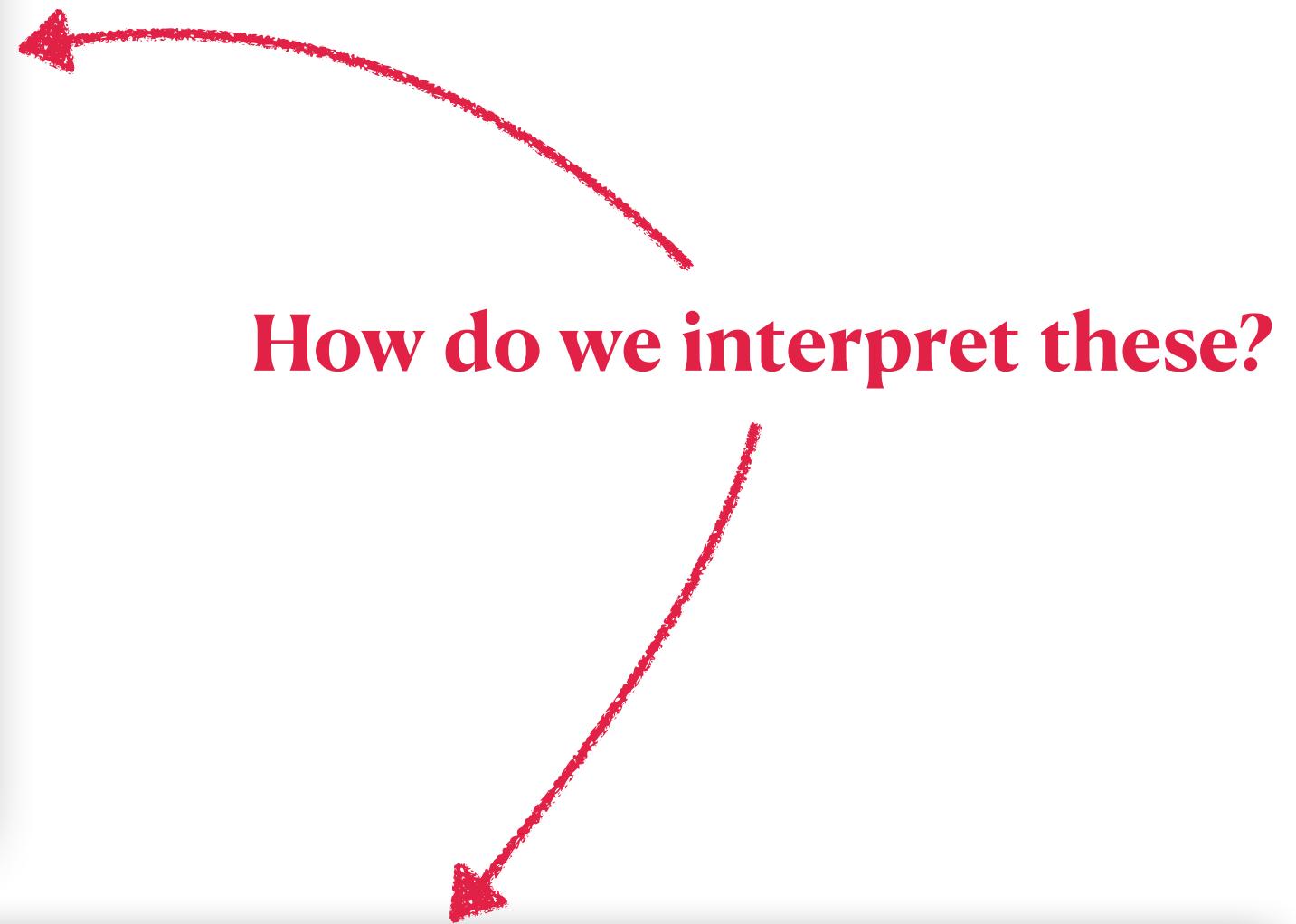
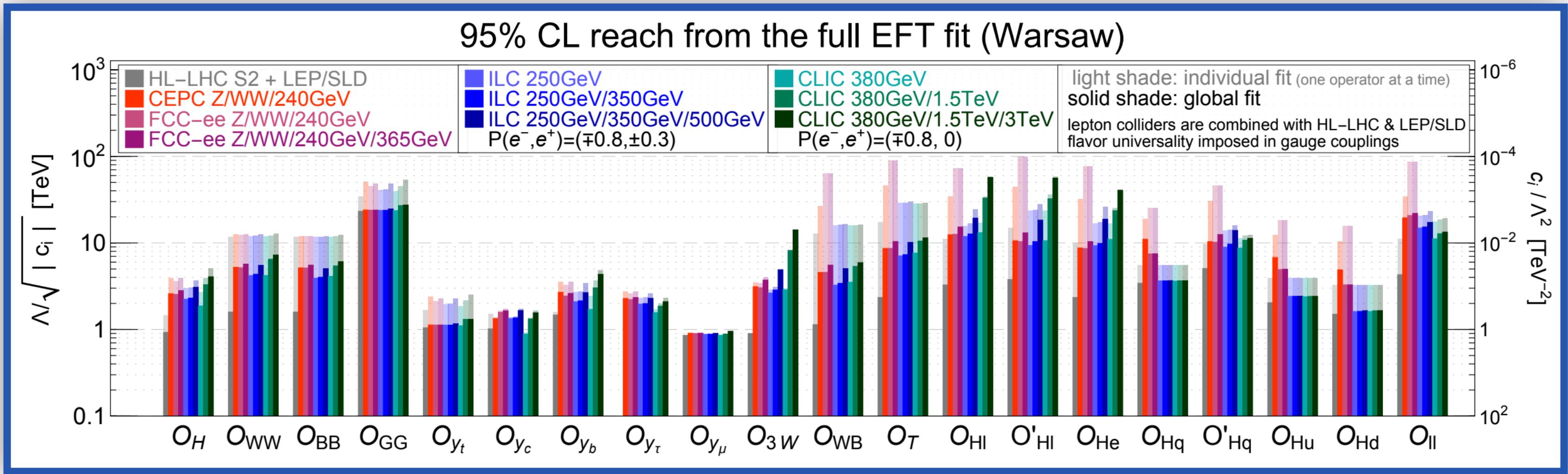
- Assuming CP conservation and MFV, about 20 operators are relevant for EWPTs.



Constraints from SMEFT

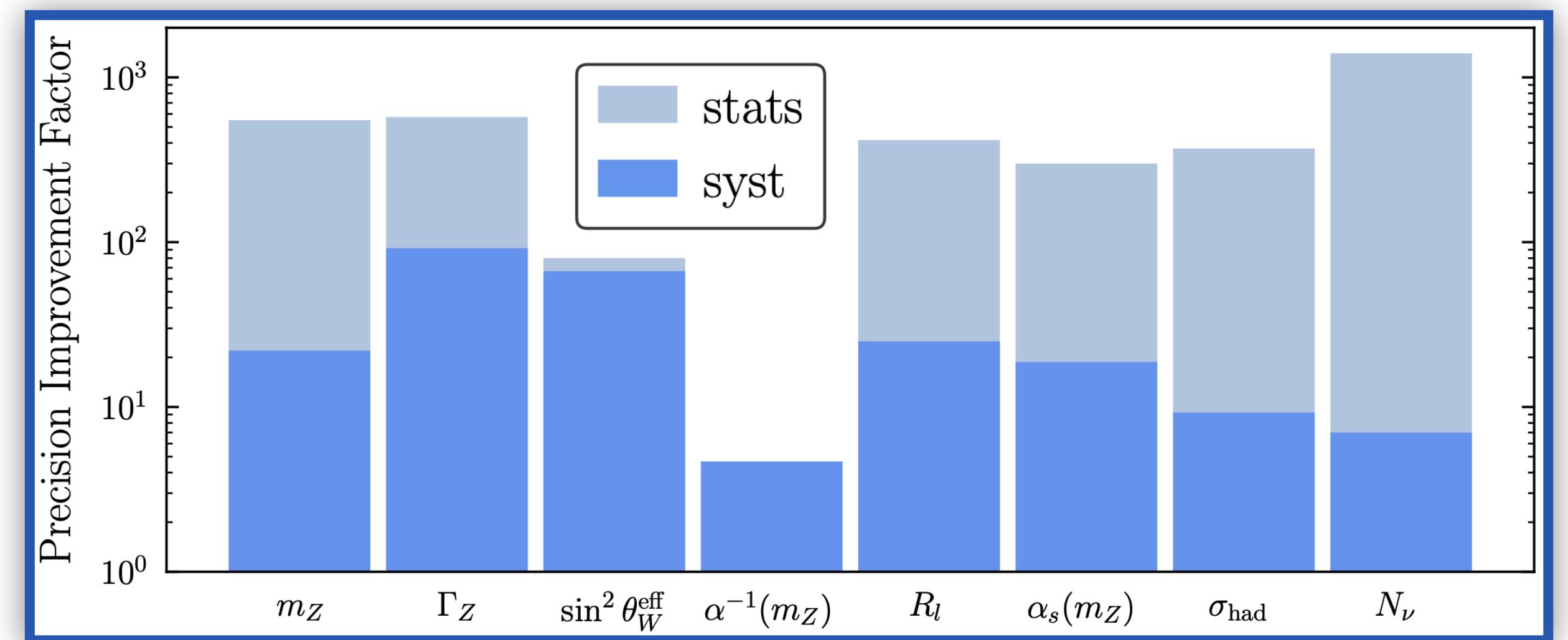


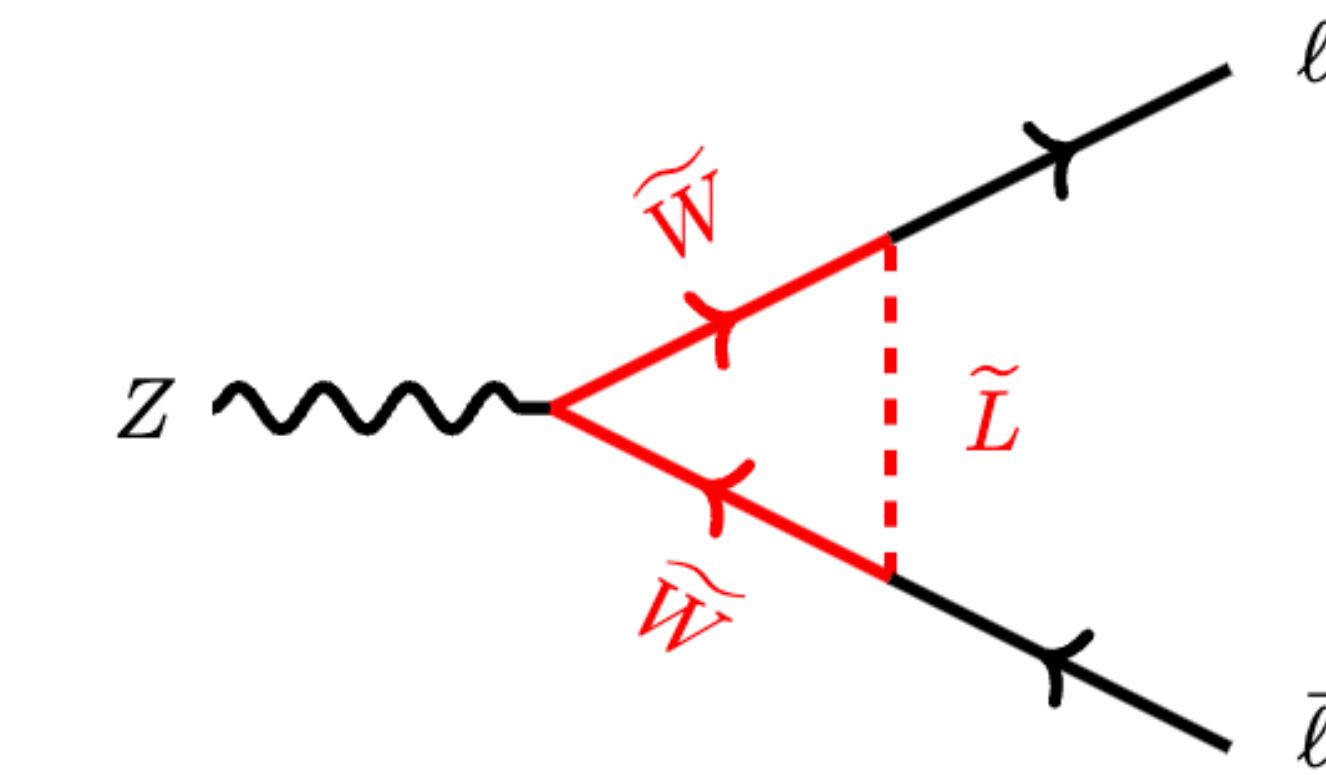
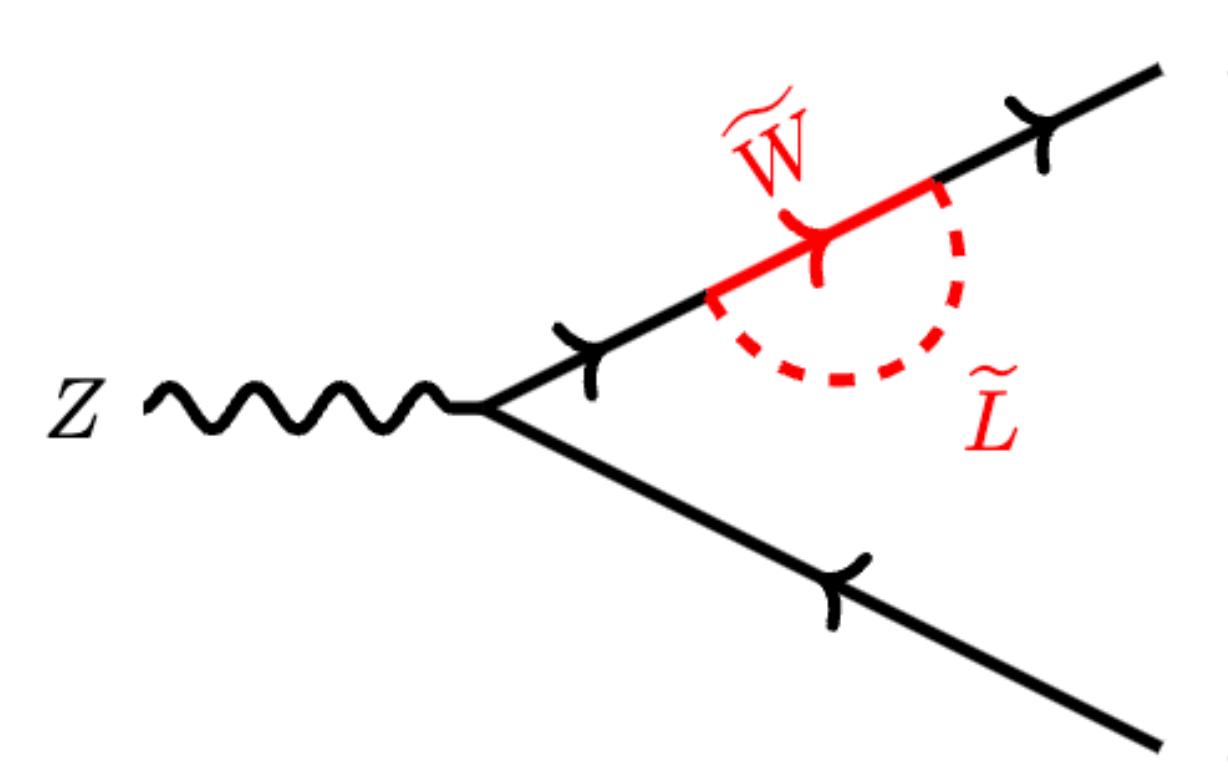
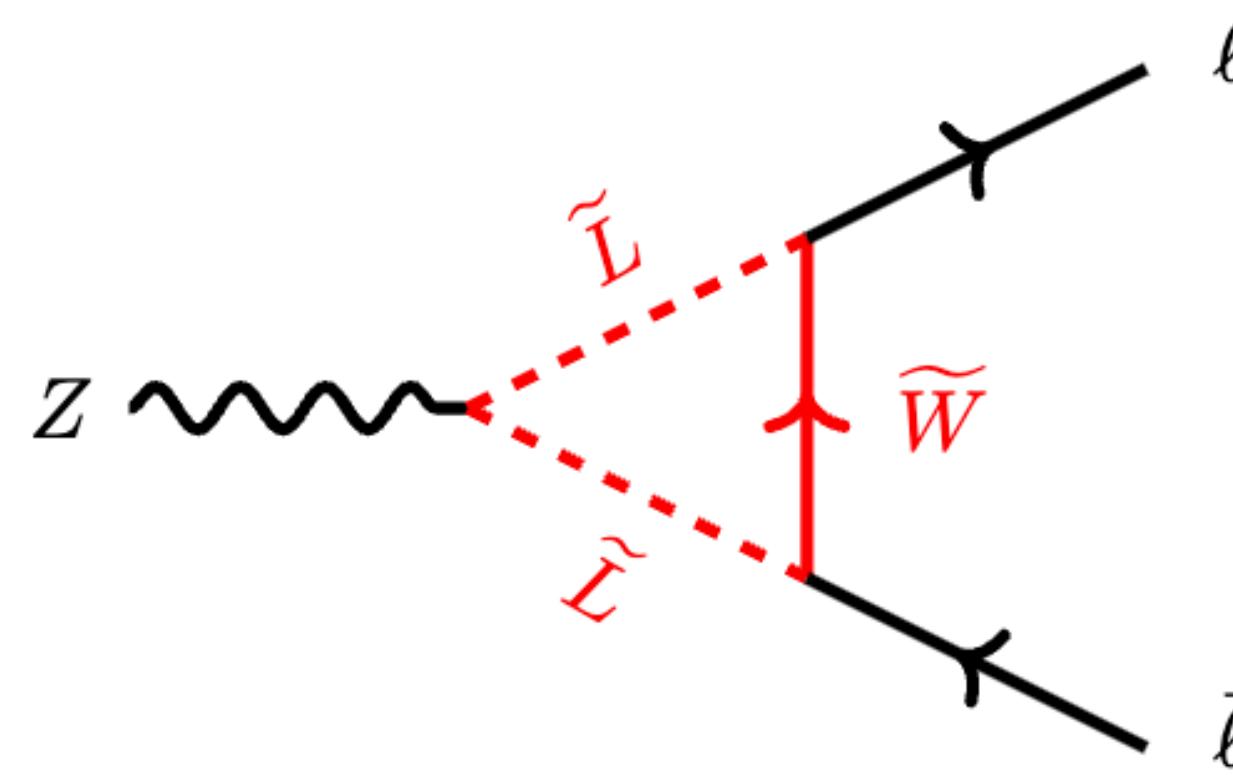
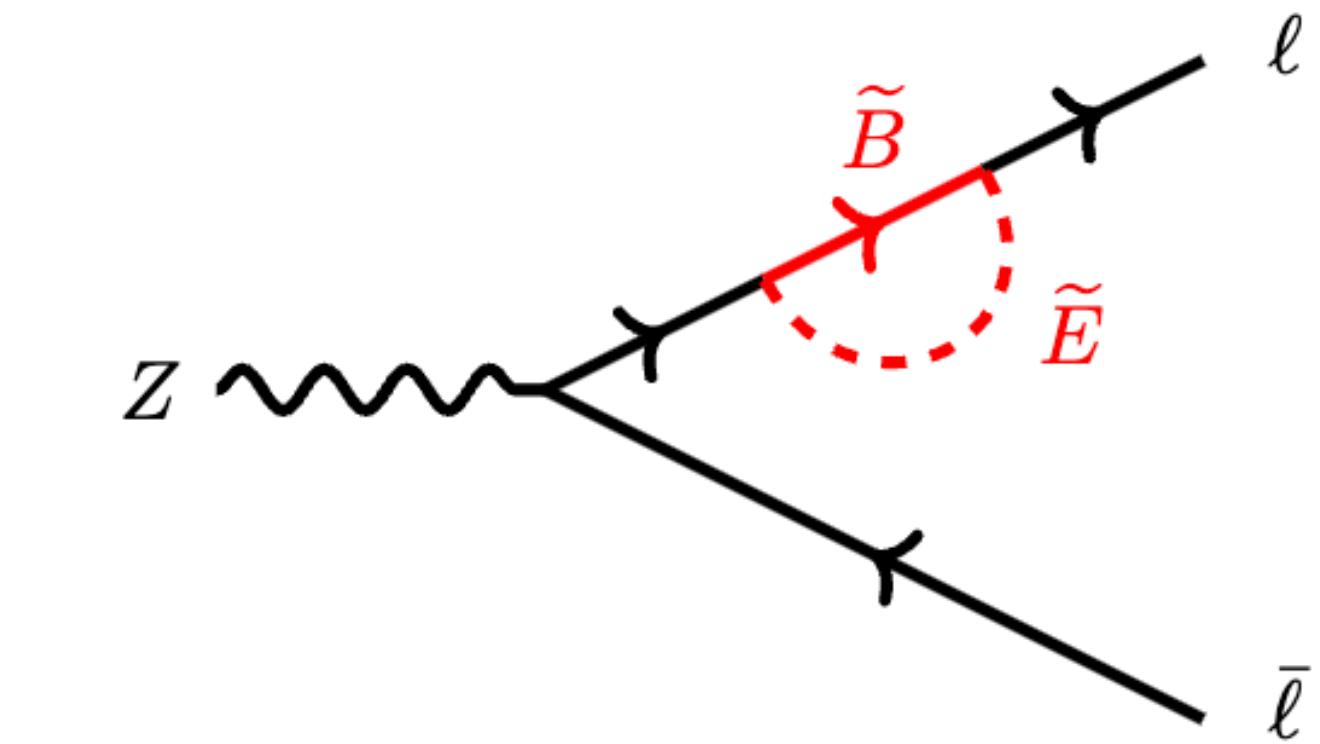
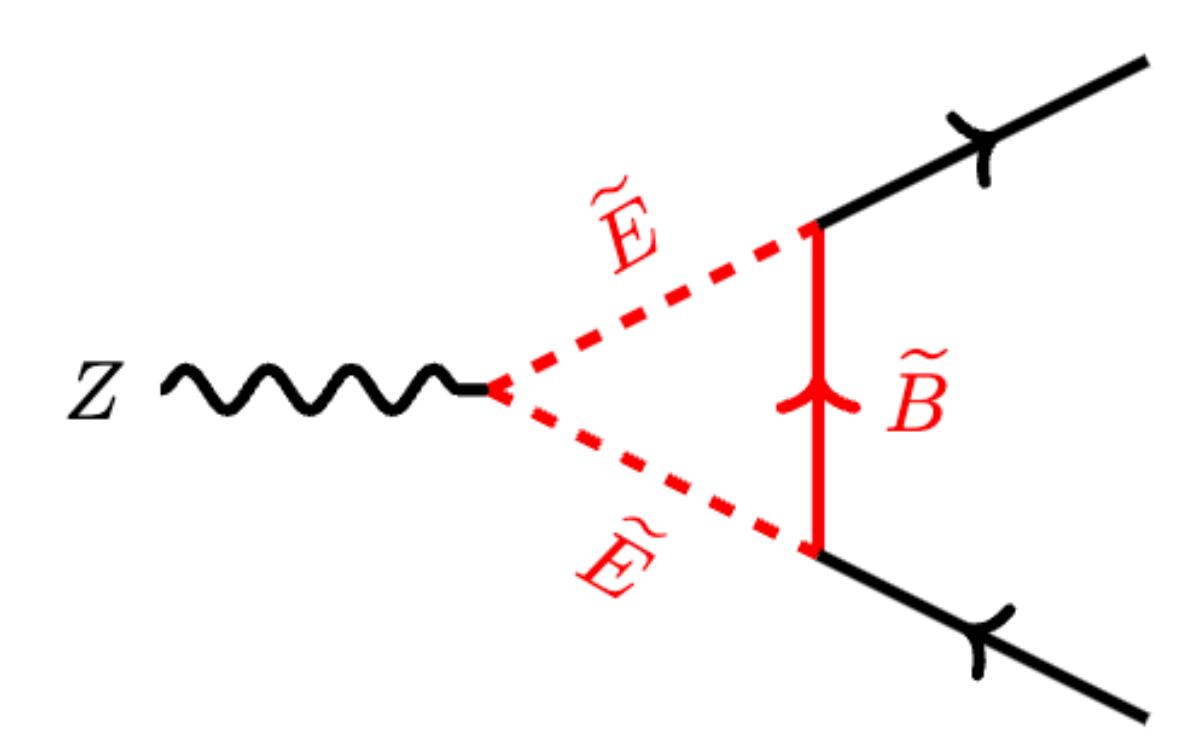
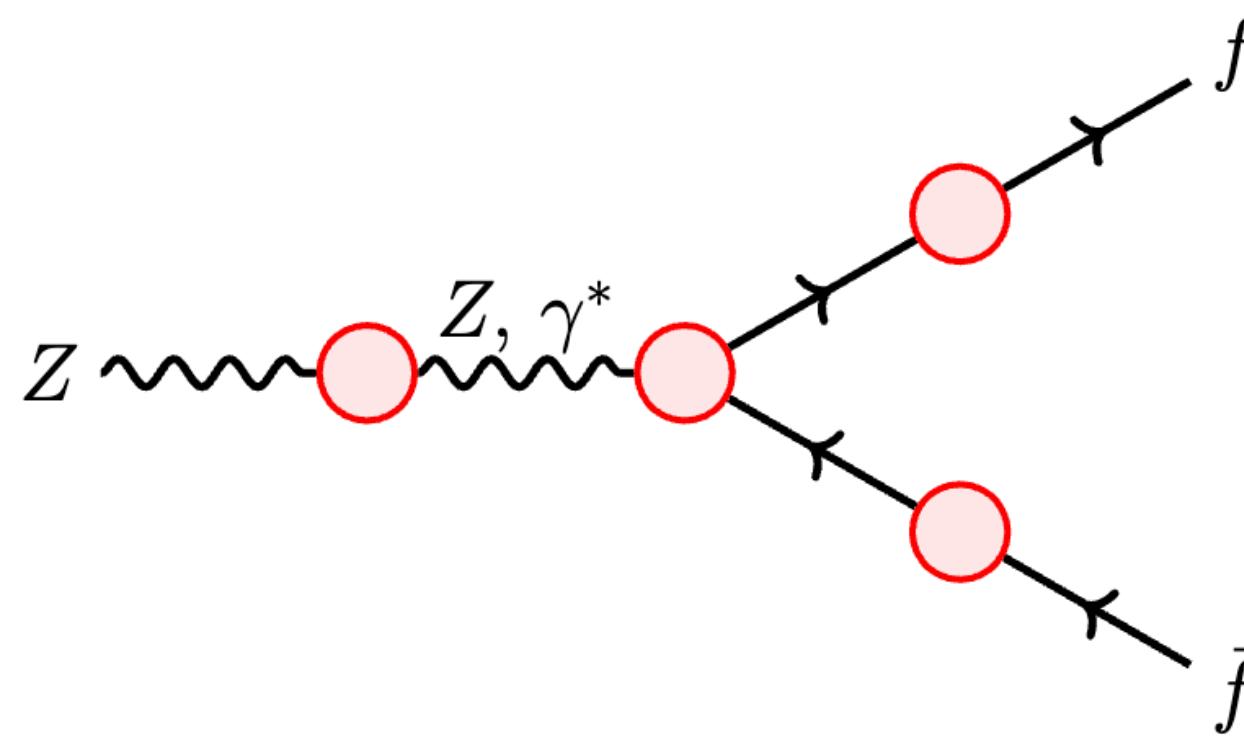
A Tale of Two Bar Plots



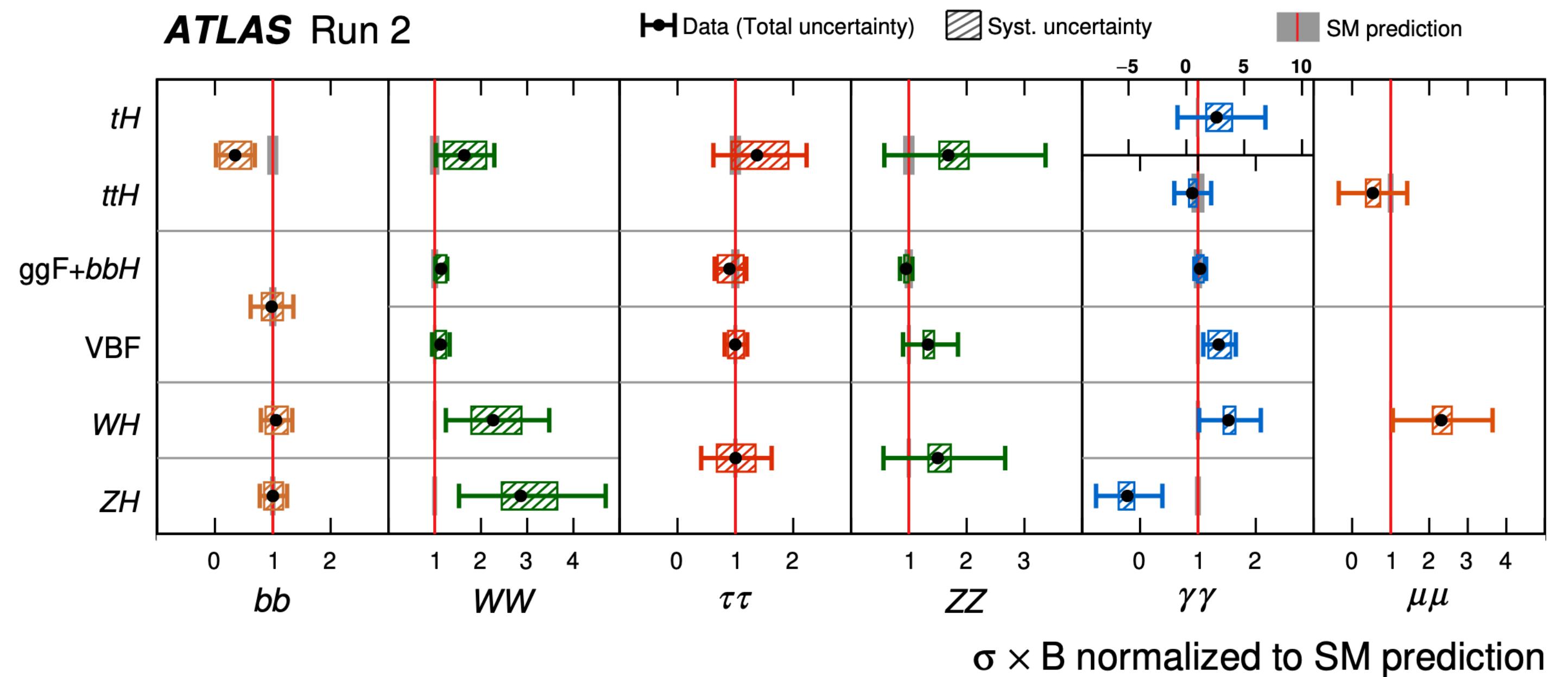
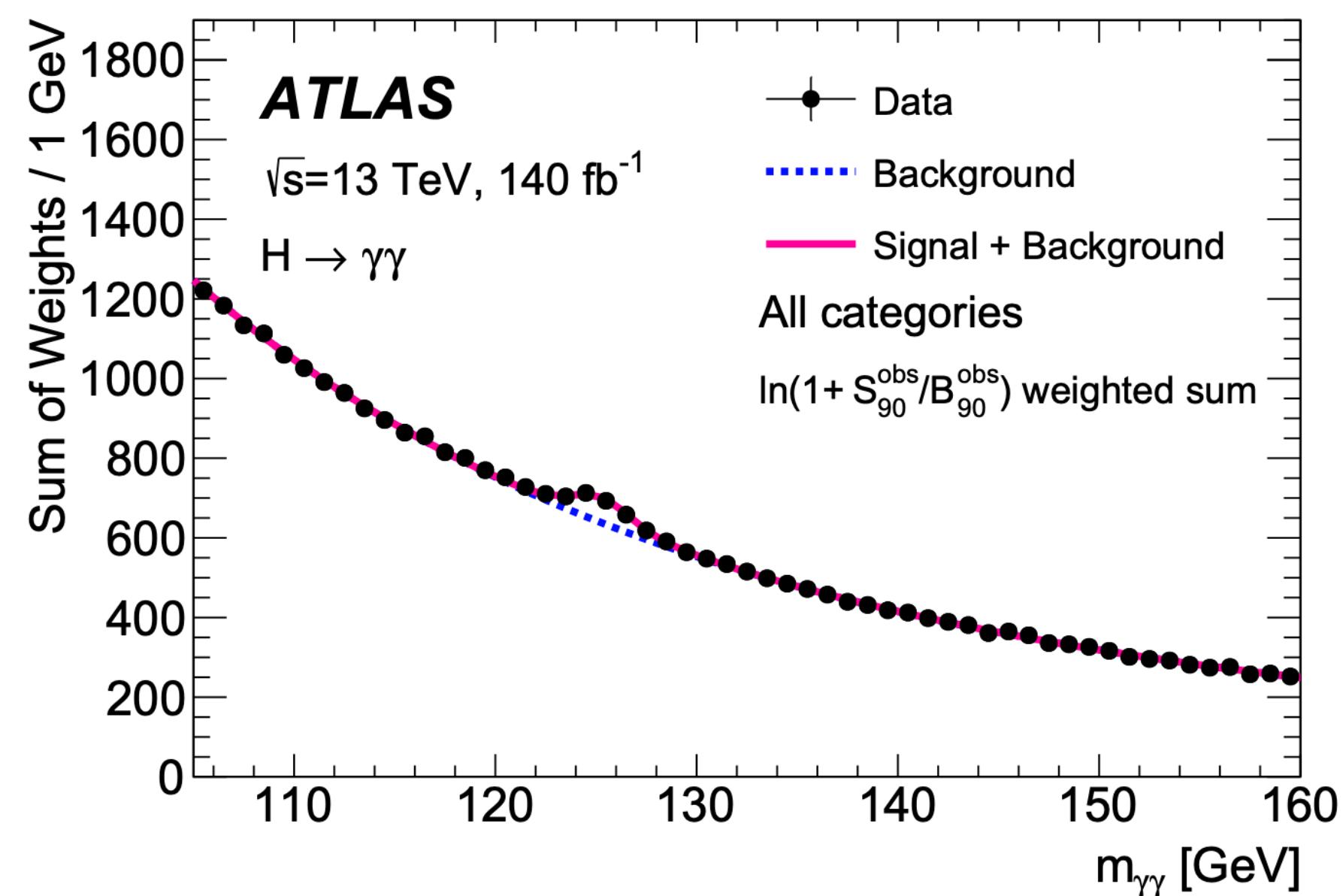
Questions

1. Which SMEFT operators are most interesting?
2. Which systematics should experimentalists be most motivated to decrease?

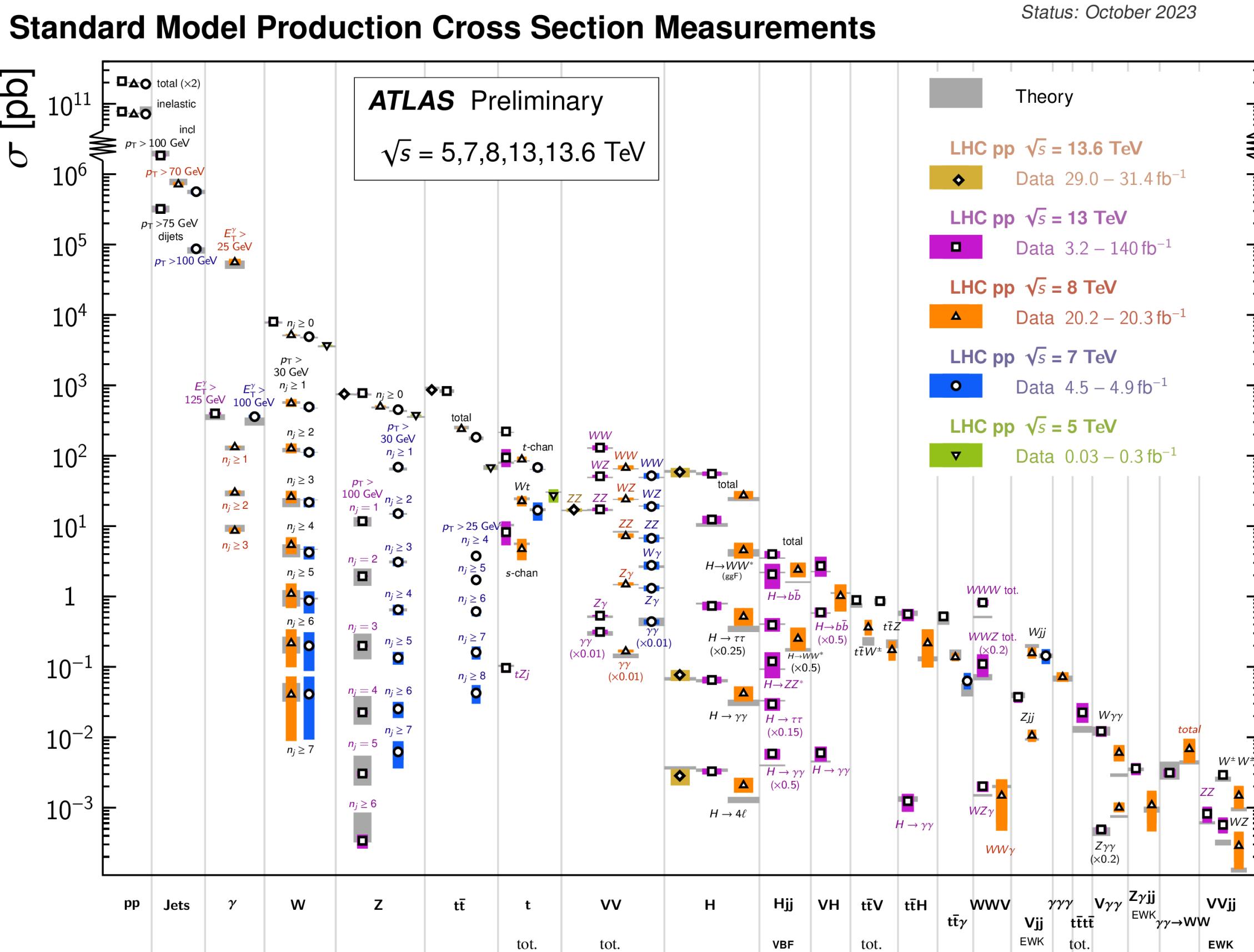




The LHC has been very successful!



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The Standard Model is extremely predictive!

Many mysteries remain!

Finding answers may require a different collider.