

# Majorons Echoes of Leptogenesis

## DPF- PHENO 2024

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## ① Elevator Pitch

## ② Motivation

## ③ Model

## ④ Phenomenology

## ⑤ Results

## ⑥ Conclusion

## ⑦ References

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- If Baryon asymmetry generated from Leptogenesis, Lepton number violation required
- Assuming Lepton number violation generated by SSB of  $U(1)_L$  global  $\implies$  Irreducible Majoron Production
- If Majorons long lived, decay signatures observable today

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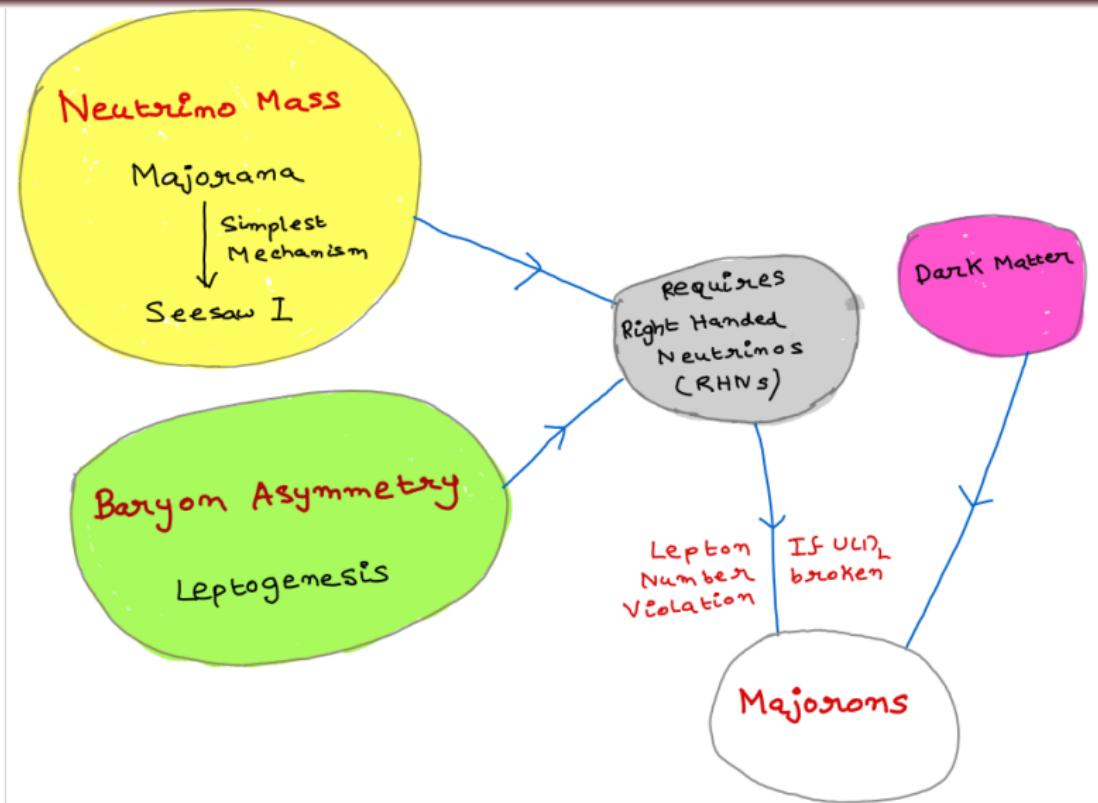
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Killing three birds with one stone?

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## Welcome to the singlet Majoron Model!

- $\mathcal{L}_{\text{int}} \supset \lambda \Phi NN + y_D LHN + h.c. + V(\Phi)$
- Scalar  $\Phi$  (carries Lepton number), 3 SM singlet Majorana Neutrinos  $N_{1,2,3}$
- $V(\Phi) = \kappa (\Phi^2 - f^2)^2$
- Has  $U(1)_L$  global symmetry
- $U(1)_L$  spontaneously broken
- $\Phi$  gets a VEV



Cosmological Irreducible Majoron Production  $\rightarrow$  Signatures of Leptogenesis ??

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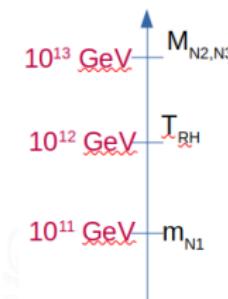
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# Leptogenesis I

- Assumption-

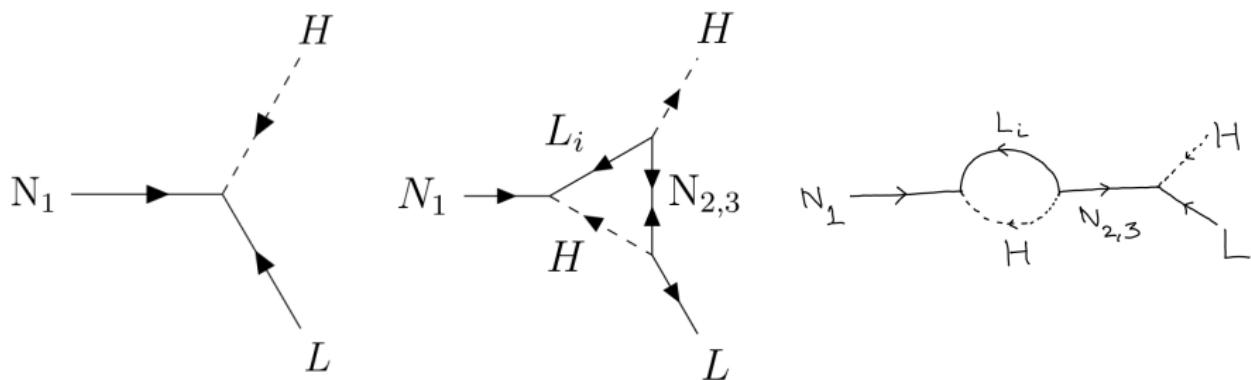
$$m_{N_2} = m_{N_3} \geq 100m_{N_1}$$



- Lepton asymmetry generated through  $N_1$  decay out of equilibrium, converted to Baryon asymmetry through sphalerons [**M. Fukugita, T. Yanagida, 1986**]
- Decay quantified by parameter  $K \equiv \frac{\Gamma_D}{H(T=m_{N_1})}$  [**Buchmüller et al. 2005**]

# Leptogenesis II

- CP violation

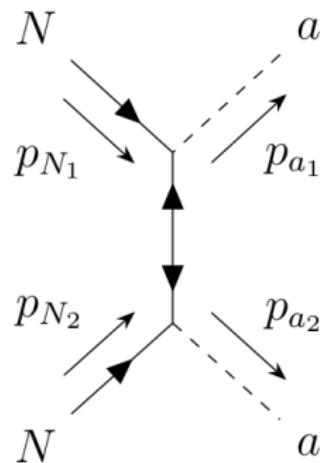
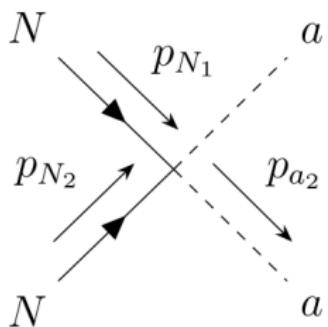


- Baryon asymmetry  $\eta_B \equiv \frac{n_B}{n_\gamma} = \frac{3}{4} \frac{a_{sph}}{f} \varepsilon_1 \kappa_f \simeq 0.96 \times 10^{-2} \varepsilon_1 \kappa_f$
- $\varepsilon_1, \kappa_f$  - Quantitative dependence on  $K \equiv \frac{\Gamma_D}{H(T=m_{N_1})}$

# Majoron Production I

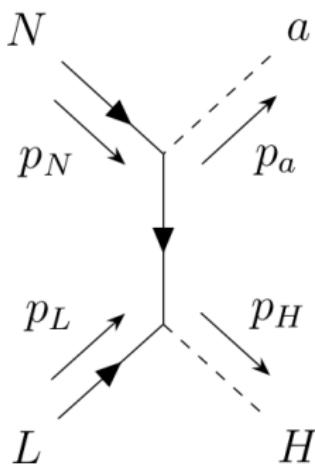
- Two dominant channels of Majoron production
  - $NN \rightarrow aa$
  - $NL \rightarrow Ha$

$$NN \rightarrow aa$$



# Majoron Production II

$$NL \rightarrow Ha$$



- $N$  in thermal bath  $\rightarrow$  Freezes in irreducible Majoron density

# Irreducible Majoron production I

- $m_\nu = \frac{m_D^2}{m_N}$
- $m_D = iU\sqrt{d_I}R^T\sqrt{d_h}$  [J. Casas, A. Ibarra, 2001]
- U- PMNS matrix,  $d_I = \text{diag}(m_{\nu_1}, m_{\nu_2}, m_{\nu_3})$ ,  
 $d_h = \text{diag}(m_{N_1}, m_{N_2}, m_{N_3})$ , R- orthogonal matrix
- Majoron relic density at late times  $Y_a$ 
  - Depends on mass of lightest active neutrino  $m_\nu$ , Neutrino mass hierarchy, K, R matrix from Cassas-Ibarra Parameterization[1],  $m_{N_1}$  ( $m_{N_2} = m_{N_3} = 100m_{N_1}$ )
  - Majoron yield minimized for Normal Hierarchy,  $m_\nu = 0$ ,

$$R = \begin{pmatrix} \cos(\theta) & \sin(\theta) & 0 \\ -\sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad (1)$$

Thus, these parameters fixed from now on

# Irreducible Majoron production II

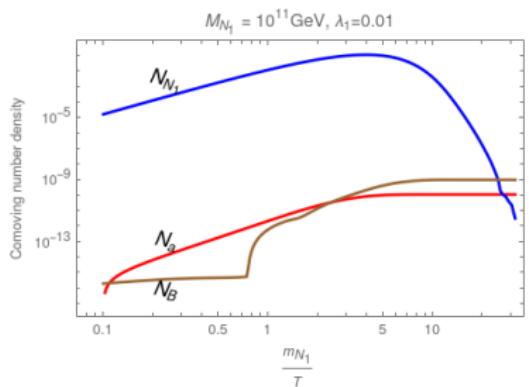
- Irreducible minimal Majoron relic density at late times

$$Y_a = 10^{-11} \left( \frac{10}{z_{eq}(K)} \right) \left( \frac{10^{11}}{M_{N_1}} \right) \times \quad (2)$$

$$\left( \frac{\lambda_1}{10^{-2}} \right)^2 \left( 1 + 33.3 \left( \frac{\lambda_1}{10^{-2}} \right)^2 \left( \frac{10^{11}}{M_{N_1}} \right) \right) \quad (3)$$

- $\lambda_1 = \frac{m_{N_1}}{\sqrt{2}f}$  ,  $f$ -  $U(1)_L$  SSB scale

**AMRITA**  
VISHWA VIDYAPEETHAM



# Majoron Decay

Decay channels at tree level

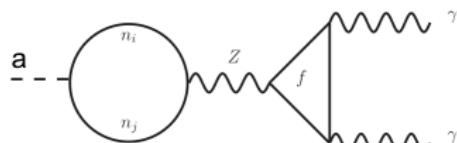
$$a \rightarrow \nu\nu$$

$$\Gamma(a \rightarrow \nu\nu) \simeq \frac{m_a}{16\pi f^2} \sum_{i=1}^3 m_{\nu_i}^2$$

[C. Garcia-Cely, J. Heeck,  
2017]

Decay channel at two loops

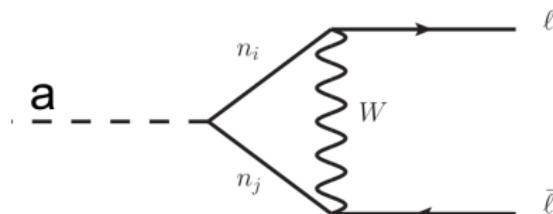
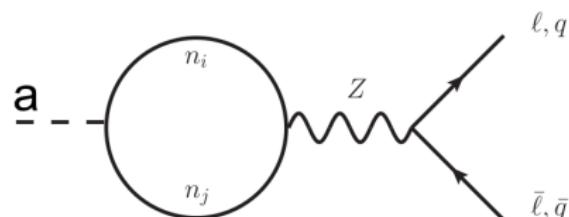
$$a \rightarrow \gamma\gamma$$



**Figure 1:** [C. Garcia-Cely, J. Heeck, 2017],[J. Heeck, H. Patel, 2019]

Decay channels at one loop

$$a \rightarrow \bar{f}f$$



**Figure 2:** [C. Garcia-Cely, J. Heeck, 2017]

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# Irreducible majoron relic as fraction of Dark Matter

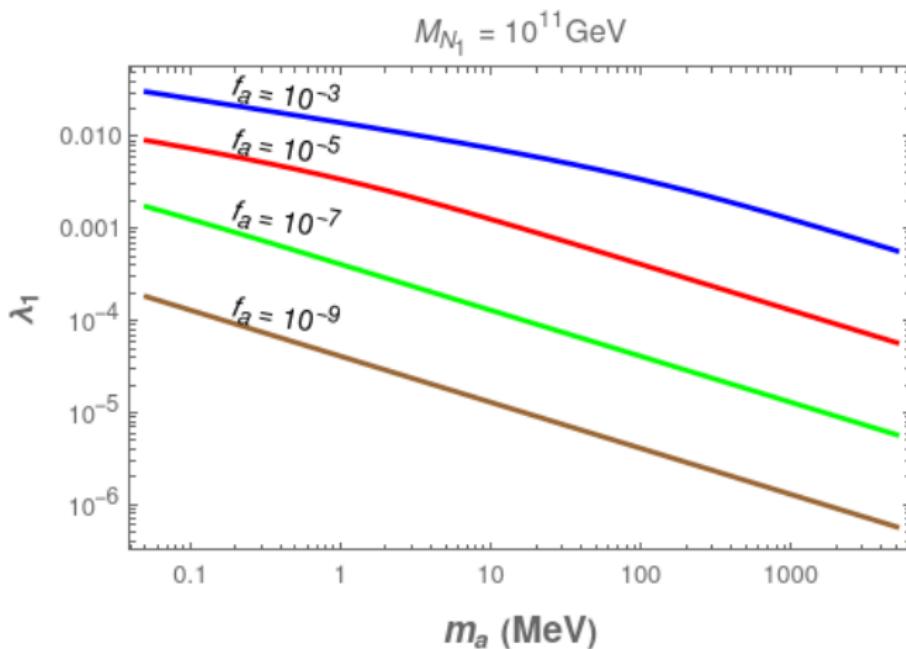


Figure 3:  $f_a = \frac{\rho_a}{\rho_{\text{DM}}}$ ,  $\lambda_1 = \frac{m_{N_1}}{\sqrt{2}f}$ ,  $f - U(1)_L$  SSB scale

# Constraints from decay to photons: INTEGRAL

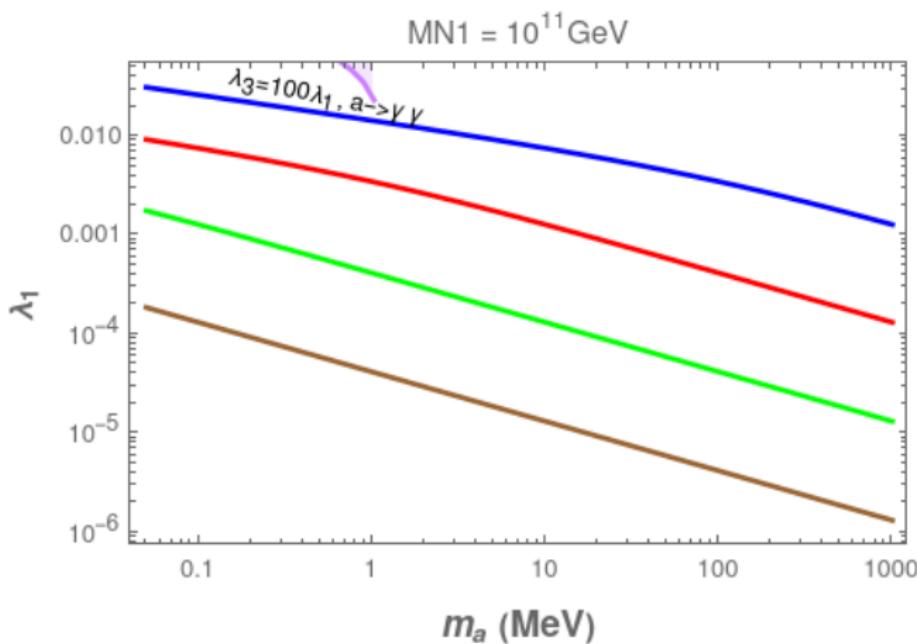


Figure 4: [K. Zurek et al., 2013]

# Constraints from decay to $e^+e^-$ : 511 KeV line INTEGRAL SPI

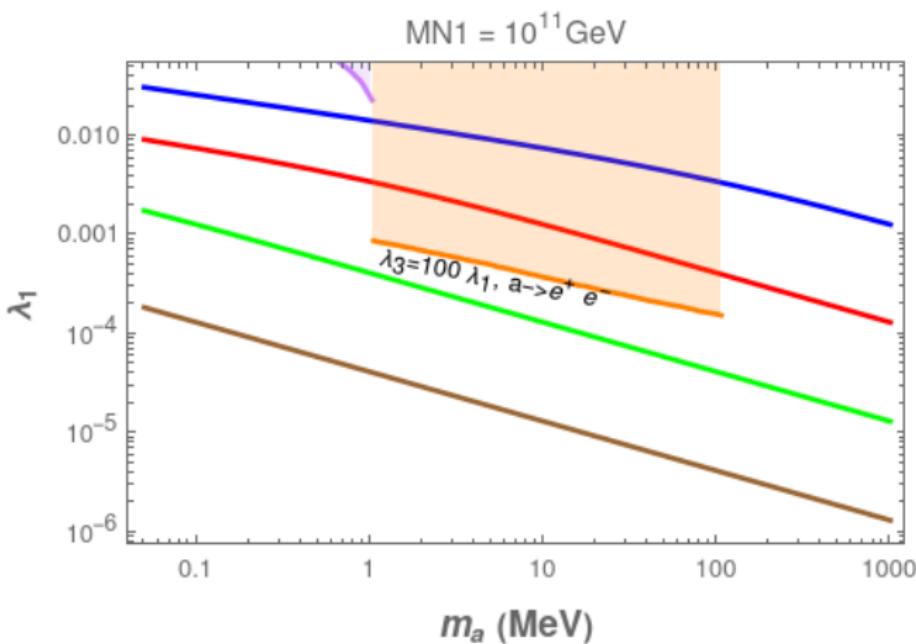


Figure 5: [P.D. la Torre Luque, S. Balaji, J. Silk, 2024]

# Constraints from decay to $e^+e^-$ : 511 KeV INTEGRAL SPI

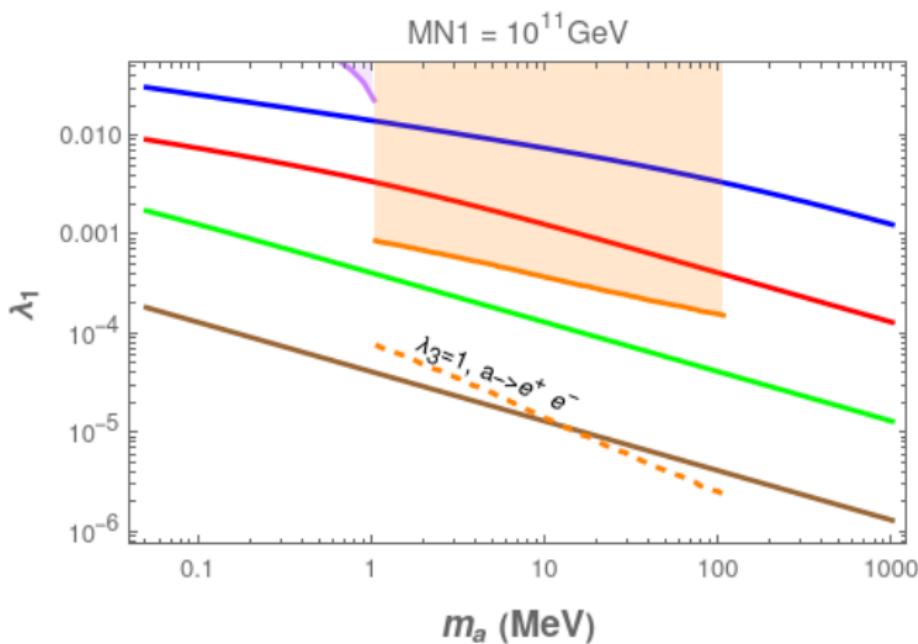


Figure 6: [P.D. la Torre Luque, S. Balaji, J. Silk, 2024]

# CMB Constraints from decay to muons: From CMB anisotropy

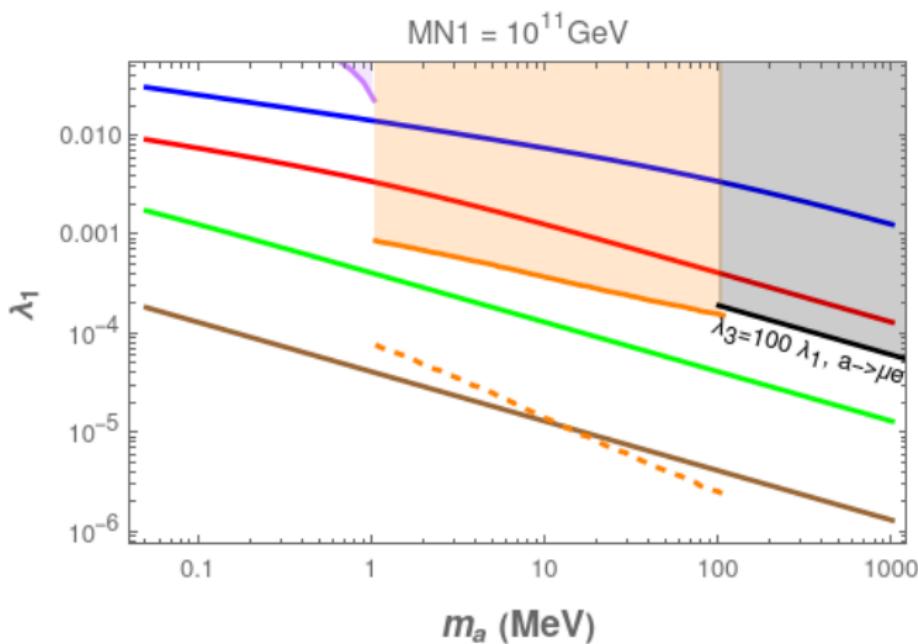


Figure 7: [T.R. Slatyer, C.-L. Wu, 2017]

# CMB Constraints from decay to muons: From CMB anisotropy

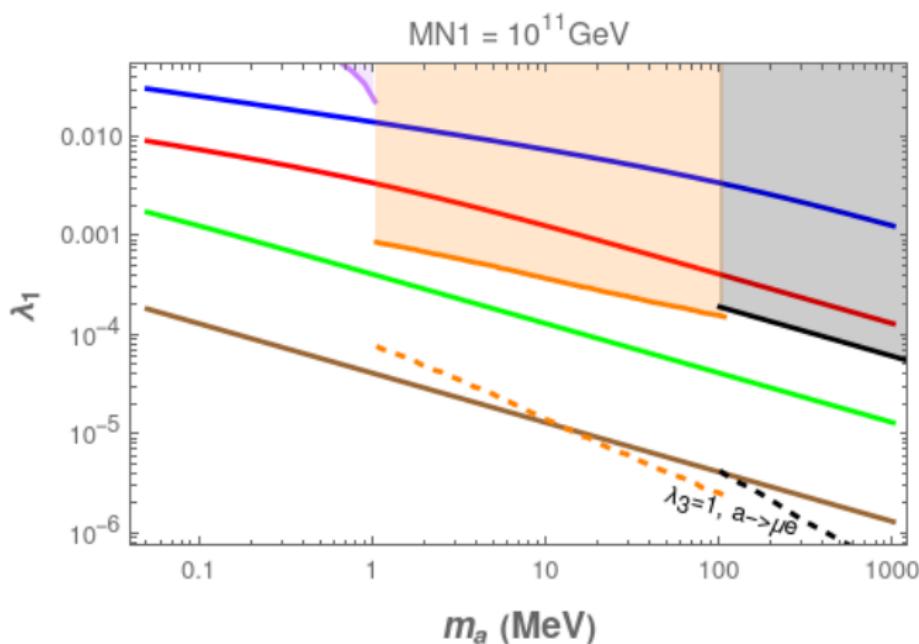


Figure 8: From CMB anisotropy induced by DM decay

- Plots are preliminary and we are working on decays into more channels which make the parameter space more constrained.
- Also, the above plots are being refined.



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# Conclusion

- Leptogenesis signatures obtained from irreducible Majoron density
- Signatures observable in current experiments
- Certain parts of parameter space ruled out from current experiments

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## References

- [1] J. Casas and A. Ibarra, "Oscillating neutrinos and e," *Nuclear Physics B*, vol. 618, no. 1–2, p. 171–204, Dec. 2001. [Online]. Available: [http://dx.doi.org/10.1016/S0550-3213\(01\)00475-8](http://dx.doi.org/10.1016/S0550-3213(01)00475-8)
- [2] M. Fukugita and T. Yanagida, "Baryogenesis Without Grand Unification," *Phys. Lett. B*, vol. 174, pp. 45–47, 1986.
- [3] W. Buchmüller, P. Di Bari, and M. Plümacher, "Leptogenesis for pedestrians," *Annals of Physics*, vol. 315, no. 2, p. 305–351, Feb. 2005. [Online]. Available: <http://dx.doi.org/10.1016/j.aop.2004.02.003>
- [4] C. Garcia-Cely and J. Heeck, "Neutrino lines from majoron dark matter," *Journal of High Energy Physics*, vol. 2017, no. 5, May 2017. [Online]. Available: [http://dx.doi.org/10.1007/JHEP05\(2017\)102](http://dx.doi.org/10.1007/JHEP05(2017)102)

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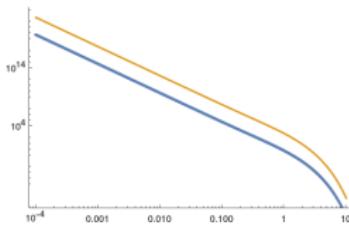
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Backup I



**Figure 9:** Dimensionless integral in  $\gamma_{NN \rightarrow aa}$  (blue) and 1000\* Interpolated function of  $\gamma_{NN \rightarrow aa}$  vs z

## Backup II

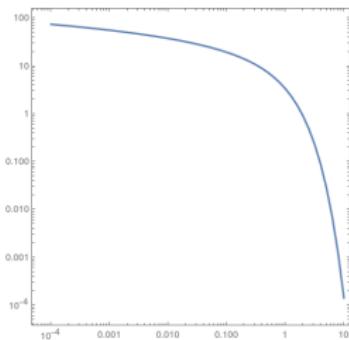


Figure 10: Dimensionless integral in  $\gamma_{NL \rightarrow Ha}$  vs  $z$

## Backup III

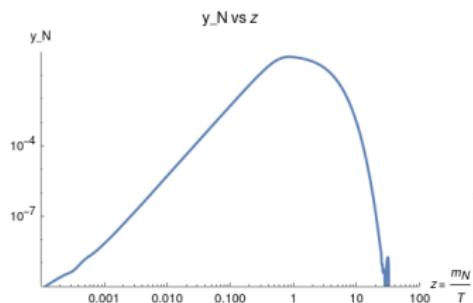


Figure 11: Evolution of  $N_1$  starting from zero initial abundance

# Singlet Majoron Model and Majoronic seesaw

- SM + 3 singlet Majorana neutrino + scalar  $\sigma = \frac{(f+\sigma_0)e^{i\theta}}{\sqrt{2}}$ ,  
 $\theta = \frac{a}{f}$
- $f$  = Lepton Number breaking scale,  $\sigma_0$  = Heavy scalar
- $U(1)_L$  broken spontaneously
- $L = -\bar{L}yHN - \frac{1}{2}\bar{N}^C\kappa\sigma N + \text{h.c.}$ ,  
SSB  $\rightarrow \kappa\sigma \rightarrow M_R = \frac{\kappa f}{\sqrt{2}}$ ,  $yH \rightarrow m_D = \frac{yv}{\sqrt{2}}$
- Mass term for active and sterile neutrinos

$$\begin{pmatrix} 0 & m_D \\ m_D^T & m_R \end{pmatrix}$$

- For  $M_R \gg m_D$ :  $M_\nu \simeq -m_D M_R^{-1} m_D^T$



$$NN \rightarrow aa$$

- At tree level

$$\sum_{\text{spin } N1, N2} |\mathcal{M}_{NN \rightarrow aa}|^2 = \frac{|\lambda|^4 s}{8m_N^2} - \frac{5}{2} |\lambda|^4 + |\lambda|^4 \left\{ \frac{u-m_N^2}{t-m_N^2} + \frac{t-m_N^2}{u-m_N^2} \right\}$$

- $\lambda$  is the  $\Phi NN$  coupling constant

- $\sigma \propto |\lambda|^4$

- Contribution to Boltzmann equation

$$\gamma_{NN \rightarrow aa} = \frac{T m_N^7}{2048 \pi^5 f^4} \gamma_{NN \rightarrow aa}^{\text{dimless}}(z = \frac{m_N}{T})$$

$$\Gamma_{NN \rightarrow aa} = 2 \left( \frac{N}{N_{eq}} \right)^2 \gamma_{NN \rightarrow aa} = \text{Fudge factor} \times \gamma_{NN \rightarrow aa}, \text{ Fudge factor} = 2 \left( \frac{N}{N_{eq}} \right)^2$$

- $NL \rightarrow Ha$

- At tree level
$$\sum_{spin} |\bar{M}|^2 = \frac{1}{4} \frac{(m_N^2 y_D^2)(u - m_L^2)}{f^2(t - m_N^2)}$$
- $\sigma \propto |\lambda|^2 y_D^2$
- Assumption- One generation of  $L$ , one Majorana neutrino  $N$
- Contribution to Boltzmann equation
$$\gamma_{NL \rightarrow Ha} = \frac{T^4 (m_N^2 y_D^2)}{(512\pi^5) f^2} \gamma_s(\frac{m_N}{T})$$
 $\gamma_s(\frac{m_N}{T})$  dimensionless integral
- $\Gamma_{NL \rightarrow Ha} = \left( \frac{N}{N_{eq}} \right) \gamma_{NL \rightarrow Ha}$  = Fudge factor  $\times \gamma_{NL \rightarrow Ha}$ , Fudge factor =  $\left( \frac{N}{N_{eq}} \right)$
- $L$  in thermal equilibrium



- $a \rightarrow \bar{f} f$

- $\Gamma(a \rightarrow \bar{q} q) \simeq \frac{3m_\theta}{8\pi} |g_{Jqq'}^P|^2$
- $\Gamma(a \rightarrow \bar{l} l') \simeq \frac{3m_\theta}{8\pi} \left( |g_{Jll'}^P|^2 + |g_{Jll'}^S|^2 \right)$
- $g_{Jll'}^P \simeq \frac{m_l + m_{l'}}{16\pi^2 \nu} \left( \delta_{ll'} T_3^I \text{tr} K + K_{ll'} \right)$
- $g_{Jll'}^S \simeq \frac{m_l - m_{l'}}{16\pi^2 \nu} K_{ll'}$
- $g_{Jqq'}^P \simeq \frac{m_q}{8\pi^2 \nu} \delta_{qq'} T_3^q \text{tr} K$
- $g_{Jqq'}^S = 0$
- $T_3^{d,I} = -\frac{1}{2} = -T_3^u$
- $K = \frac{m_D m_D^\dagger}{vf}$



# Casas-Ibarra Parameterization Incorporation I

- $y_D LH^\dagger N$  term generalized to 3 generation of Leptons and in principle, multiple generations of  $N$
- Assume 3 generations of  $N$
- Then,  $y_D LH^\dagger N \rightarrow (y_D)_{ij} L_i H^\dagger N_j$ ,  $i, j \in \{1, 2, 3\}$
- $(m_D)_{ij} = \frac{(y_D)_{ij} v}{\sqrt{2}}$
- $m_D = iU\sqrt{d_l}R^T\sqrt{d_h}$
- $d_l = \text{diag}(m_{\nu_1}, m_{\nu_2}, m_{\nu_3})$ ,  $d_h = \text{diag}(m_{N_1}, m_{N_2}, m_{N_3})$
- $R$ = complex Unitary matrix in general
- Our assumption- R= Identity,  $m_{N_1} = m_N$ ,  $m_{N_2} = m_{N_3} = f$

# Casas-Ibarra Parameterization Incorporation II

- For  $N_1 L \rightarrow Ha$ ,  $\sum_{spin} |\mathcal{M}|^2 = \frac{(m_N^2 (y_{D1i})^\dagger y_{D1i})(u - m_L^2)}{f^2(t - m_N^2)}$   
 $= m_N^2 (y_D^\dagger y_D)_{11} \frac{(u - m_L^2)}{f^2(t - m_N^2)}$
- For normal ordering
  - $\sum_{i=1,2,3} \gamma_{N_1 L_i \rightarrow Ha} = \frac{T^4 (m_N^3 m_\nu)}{(1024\pi^5)((f^2 \nu^2))} \gamma_s \left( \frac{m_N}{T} \right)$
  - $m_\nu$  mass of lightest active neutrino mass eigenstate (which is  $m_{\nu 1}$  for NO)
- For inverted ordering
  - $\sum_{i=1,2,3} \gamma_{N_1 L_i \rightarrow Ha} = \frac{T^4 (m_N^3 \sqrt{{\Delta_{m_{32}}}^2 - {\Delta_{m_{21}}}^2 + m_\nu^2})}{(1024\pi^5)((f^2 \nu^2))} \gamma_s \left( \frac{m_N}{T} \right)$
  - $m_\nu$  mass of lightest active neutrino mass eigenstate (which is  $m_{\nu 3}$  for IO)