

# *Discovering Minimal Dark Matter at Future Muon Colliders*

DPF-PHENO

University of Pittsburgh / Carnegie Mellon University

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*Rodolfo Capdevilla*

Fermilab



Federico  
Meloni, DESY



Rosa Simoniello,  
CERN



Jose Zurita,  
U. Valencia

*RC, Federico Meloni, Jose Zurita, ArXiv: 2405.xxxxx*

*RC, Federico Meloni, Rosa Simoniello, Jose Zurita, JHEP 06 (2021) 133*

# Outline

## 1. Introduction

## 2. Minimal Dark Matter

- Properties
- Projections

## 3. Soft Tracks

- Signal Regions
- Backgrounds

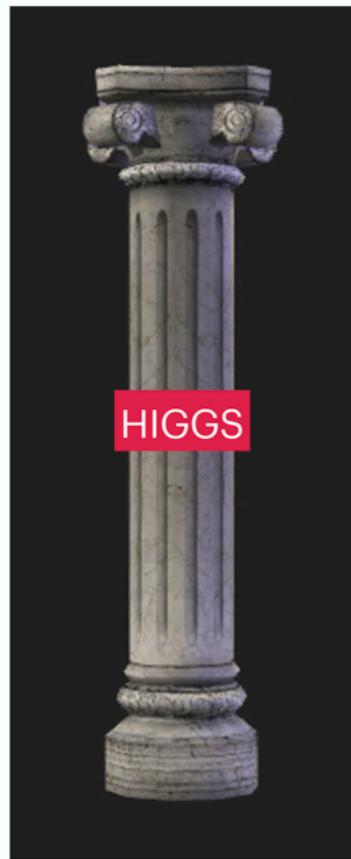
## 4. Results

- The Importance of the 3TeV MuC!

# 1. Introduction

- Pillars for the Energy Frontier:

## Foundational Physics Cases



Precision

Energy

*Patrick Meade*

### **Higgs:**

*Is there a more fundamental description of EWSB?  
What mechanism sets the scale and stabilizes the  
Higgs mass?*

...

### **BSM:**

*What is the nature of Dark Matter?  
What is the mechanism for Baryogenesis?  
What is the mechanism for neutrino masses?  
The unknown! How can nature surprise us?*

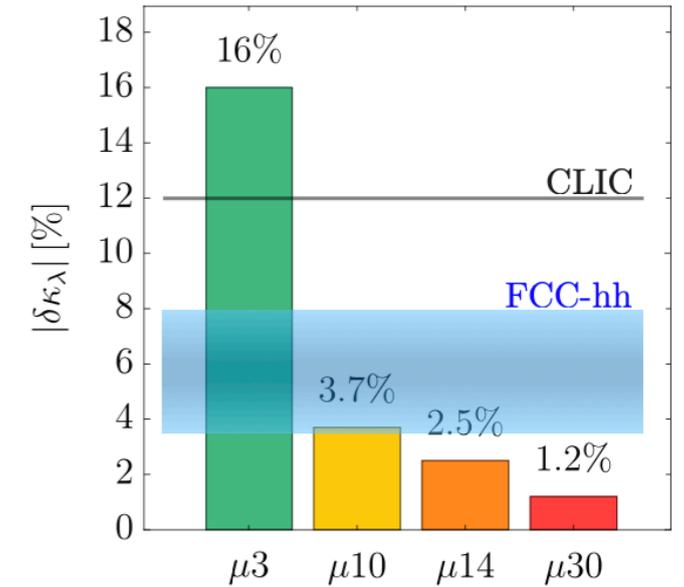
...

# 1. Introduction

- MuC strong candidate for both:

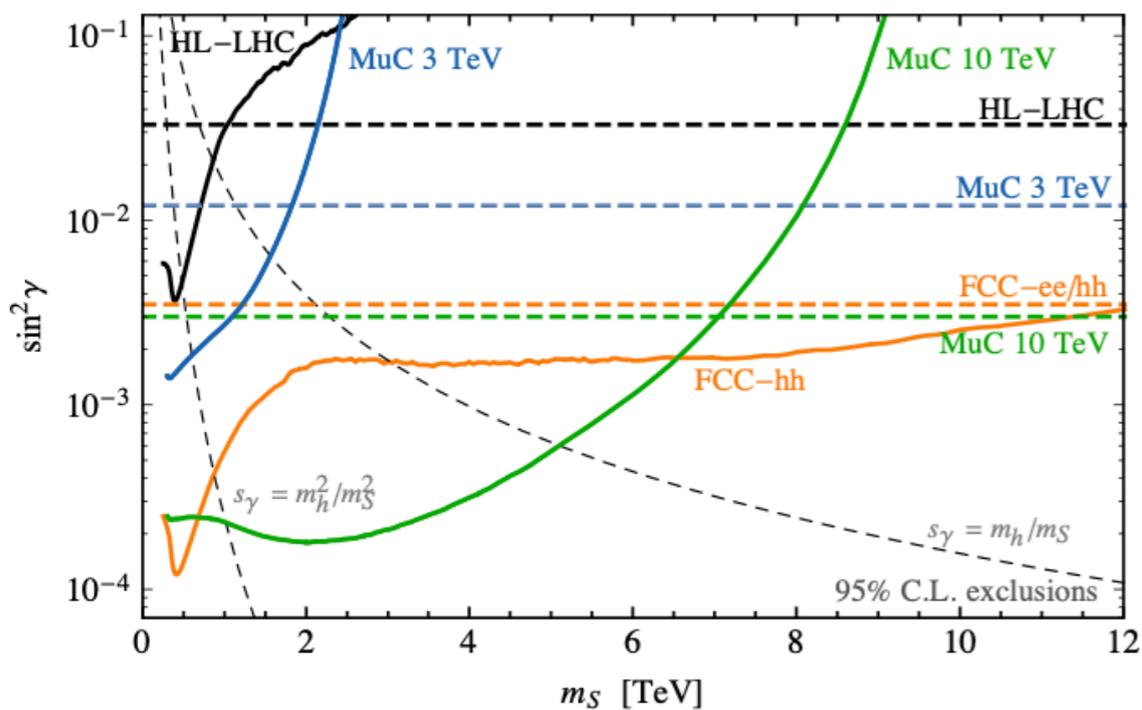
## Higgs/Precision

$\kappa$ -0 fit	HL-LHC	LHeC	HE-LHC	ILC	CLIC	CEPC	FCC-ee	FCC-ee/ $\mu^+\mu^-$
			S2 S2'	250 500 1000	380 1500 3000		240 365	eh/hh 10000
$\kappa_W$ [%]	1.7	0.75	1.4 0.98	1.8 0.29 0.24	0.86 0.16 0.11	1.3	1.3 0.43	0.14
$\kappa_Z$ [%]	1.5	1.2	1.3 0.9	0.29 0.23 0.22	0.5 0.26 0.23	0.14	0.20 0.17	0.12
$\kappa_g$ [%]	2.3	3.6	1.9 1.2	2.3 0.97 0.66	2.5 1.3 0.9	1.5	1.7 1.0	0.49
$\kappa_\gamma$ [%]	1.9	7.6	1.6 1.2	6.7 3.4 1.9	98* 5.0 2.2	3.7	4.7 3.9	0.29
$\kappa_{Z\gamma}$ [%]	10.	—	5.7 3.8	99* 86* 85*	120* 15 6.9	8.2	81* 75*	0.69
$\kappa_c$ [%]	—	4.1	— —	2.5 1.3 0.9	4.3 1.8 1.4	2.2	1.8 1.3	0.95
$\kappa_t$ [%]	3.3	—	2.8 1.7	— 6.9 1.6	— — 2.7	—	— —	1.0
$\kappa_b$ [%]	3.6	2.1	3.2 2.3	1.8 0.58 0.48	1.9 0.46 0.37	1.2	1.3 0.67	0.43
$\kappa_\mu$ [%]	4.6	—	2.5 1.7	15 9.4 6.2	320* 13 5.8	8.9	10 8.9	0.41
$\kappa_\tau$ [%]	1.9	3.3	1.5 1.1	1.9 0.70 0.57	3.0 1.3 0.88	1.3	1.4 0.73	0.44

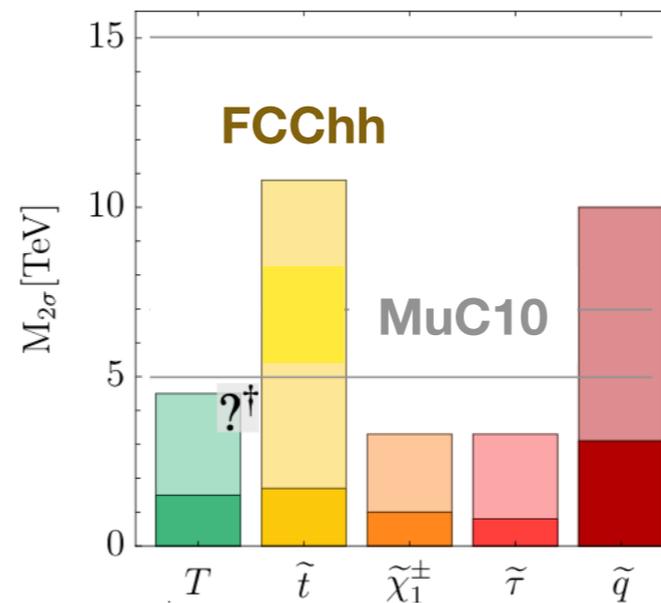


H. Al Ali et al., Muon Smasher's guide + Delphes

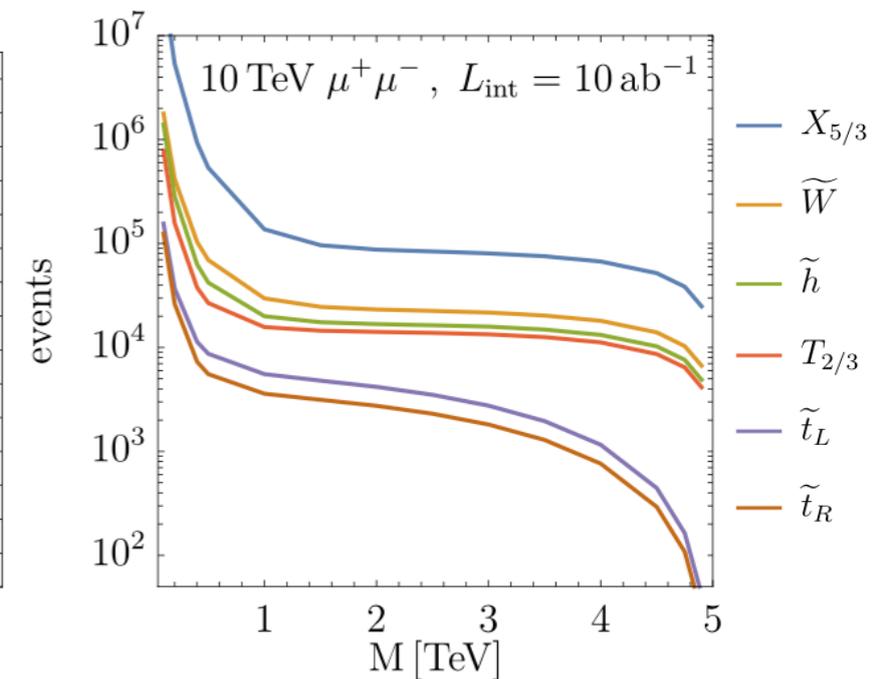
## BSM/Unknown



H. Al Ali et al., Muon Smasher's guide



D. Buttazzo,  
R. Franceschini,  
A. Wulzer,  
JHEP 05 (2021) 219



R. K. Ellis et al.,  
arXiv:1910.11775

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1. Introduction

## 2. Minimal Dark Matter

- **Properties**
- Projections

3. Soft Tracks

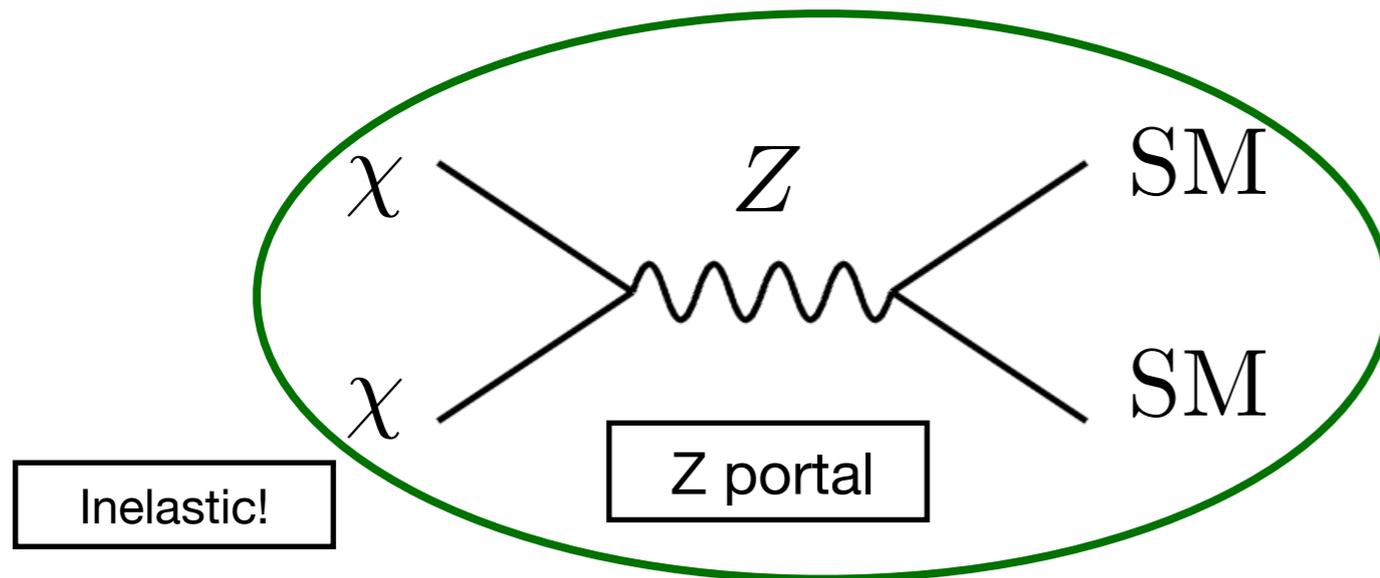
- Signal Regions
- Backgrounds

4. Results

- The Importance of the 3TeV MuC!

# 2. Minimal Dark Matter

- The Model:



Cirelli, Fornengo, Strumia, Nucl. Phys. B 753 (2006) 178-194  
 Cirelli, Strumia, New J. Phys. 11 (2009) 105005  
 Hisano, Ishiwata, Nagata, Takesako, JHEP 07 (2011) 005  
 Low, Wang, JHEP 08 (2014) 161  
 DelNobile, Nardecchia, Panci, JCAP 04 (2016) 048  
 Baumgart et al., JHEP 01 (2019) 036

EW multiplets

$$SU(3)_c \times SU(2)_L \times U(1)_Y$$

$$\chi_{\tilde{H}} = \begin{pmatrix} \chi_{\tilde{H}}^+ \\ \chi_{\tilde{H}}^0 \\ \chi_{\tilde{H}}^- \end{pmatrix}$$

**(1, 2, 1/2)**  
Higgsino-like

$$\chi_{\tilde{W}} = \begin{pmatrix} \chi_{\tilde{W}}^+ \\ \chi_{\tilde{W}}^0 \\ \chi_{\tilde{W}}^- \end{pmatrix}$$

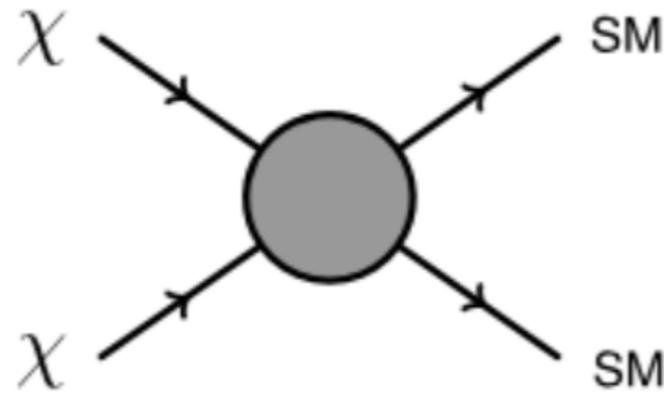
**(1, 3, 0)**  
Wino-like

Neutral component = DM

# 2. Minimal Dark Matter: Properties

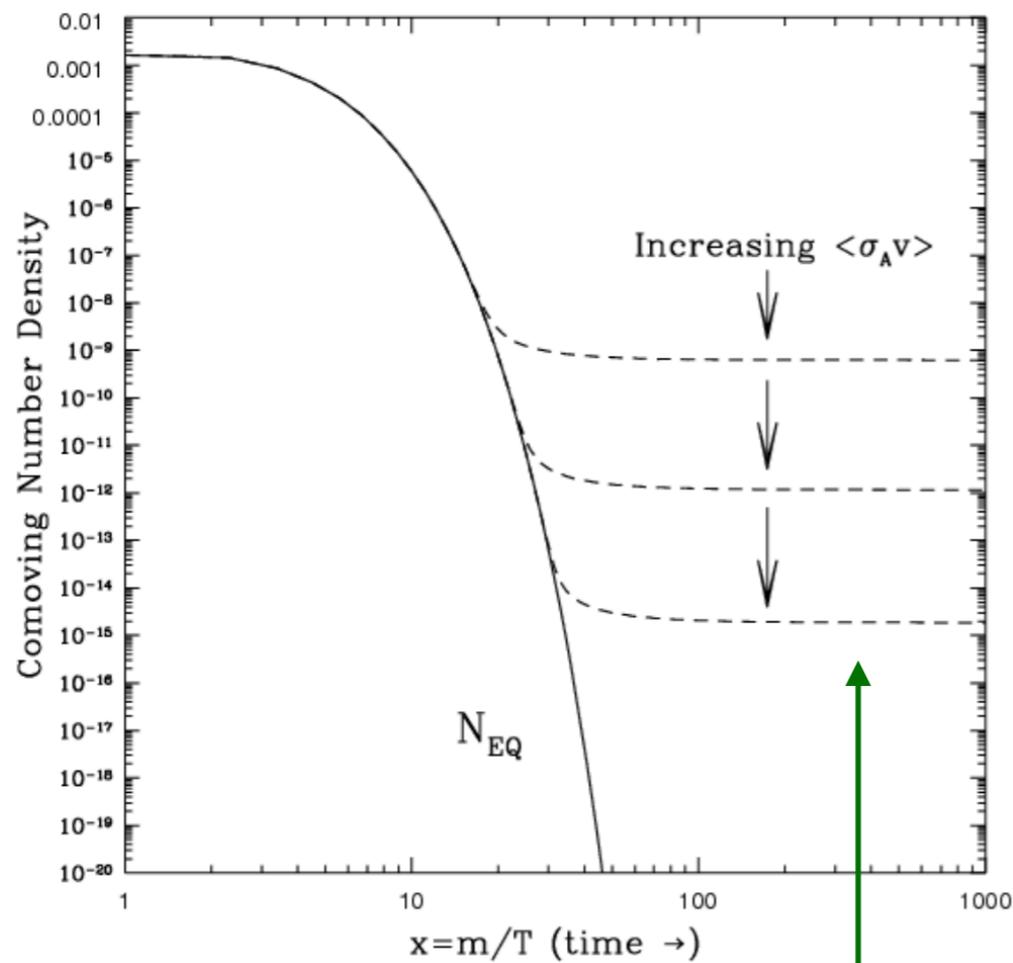
- DM Freeze Out:

*Annihilation in the early Universe*

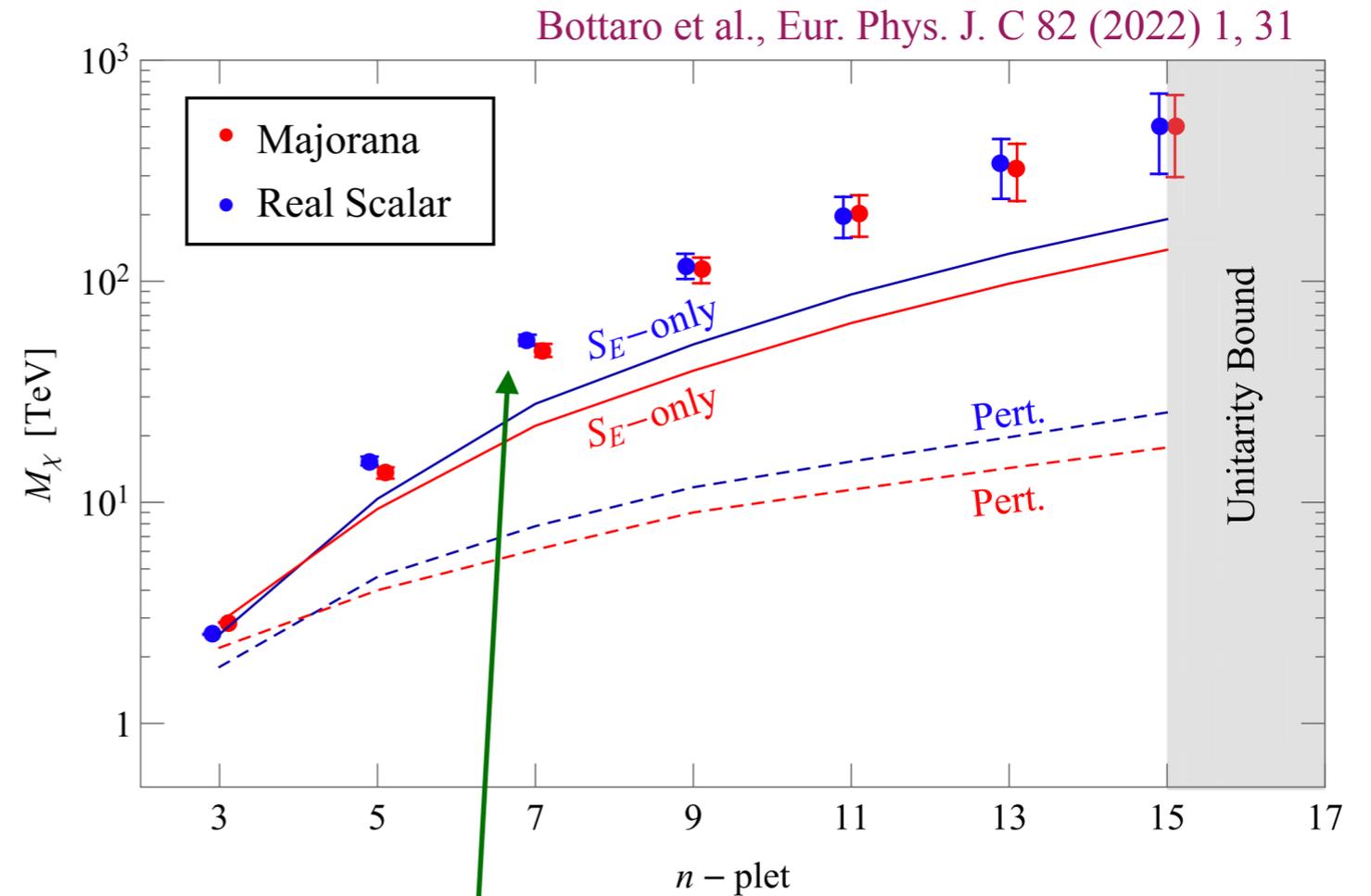


Cirelli, Fornengo, Strumia, Nucl. Phys. B 753 (2006) 178-194

$$\langle \sigma v \rangle \sim \frac{g_2^4 n^4 + 8g_2^2 g_Y^2 Y^2 n^2}{64\pi M^2 g_\chi} \quad \begin{matrix} \text{(Scalar)} \\ \text{(Large } n) \end{matrix}$$



*More annihilation requires heavier DM*



*Mass for which  $n$ -plet represents 100% of DM*

# 2. Minimal Dark Matter: Properties

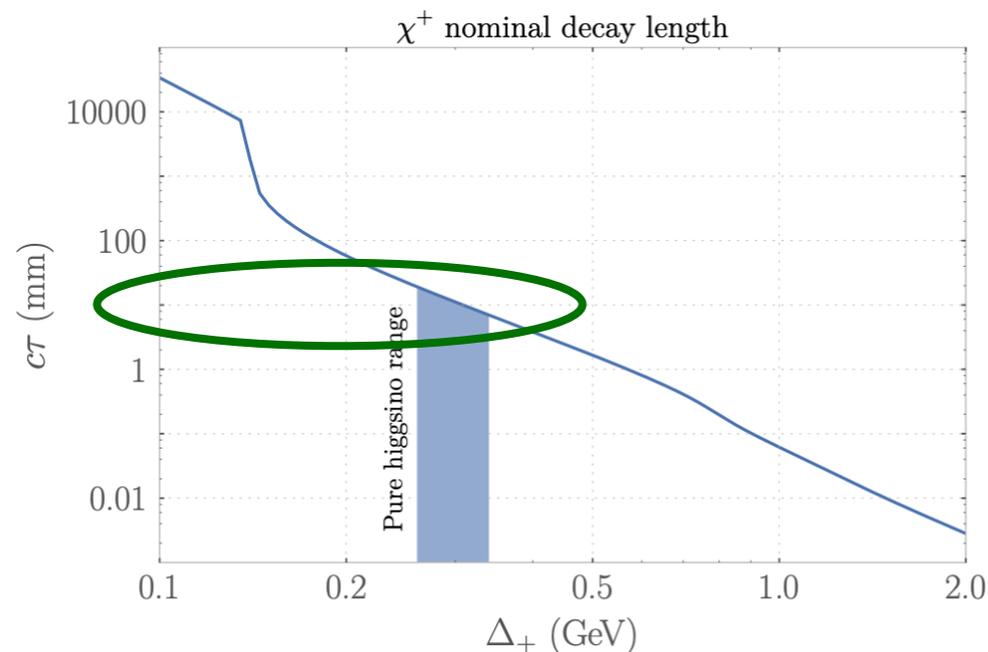
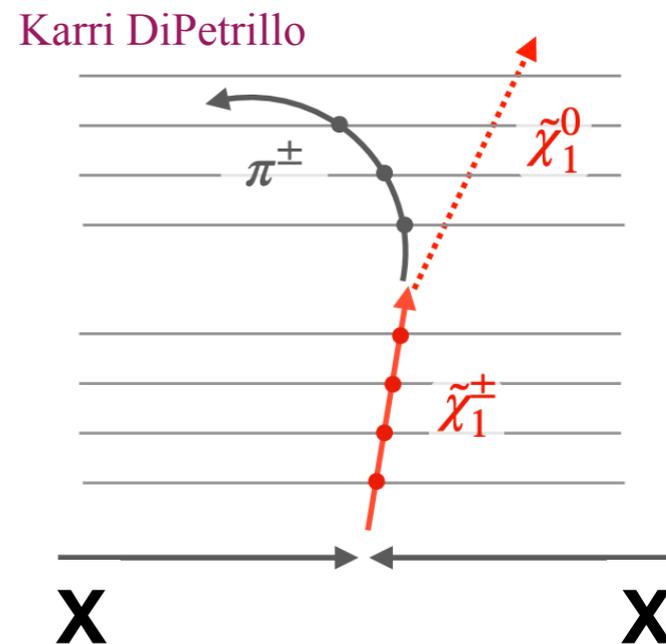
- Lifetime:

$$\Delta m = m_{\tilde{\chi}^+} - m_{\tilde{\chi}^0} > 0$$

Small mass splitting  
(from loops)

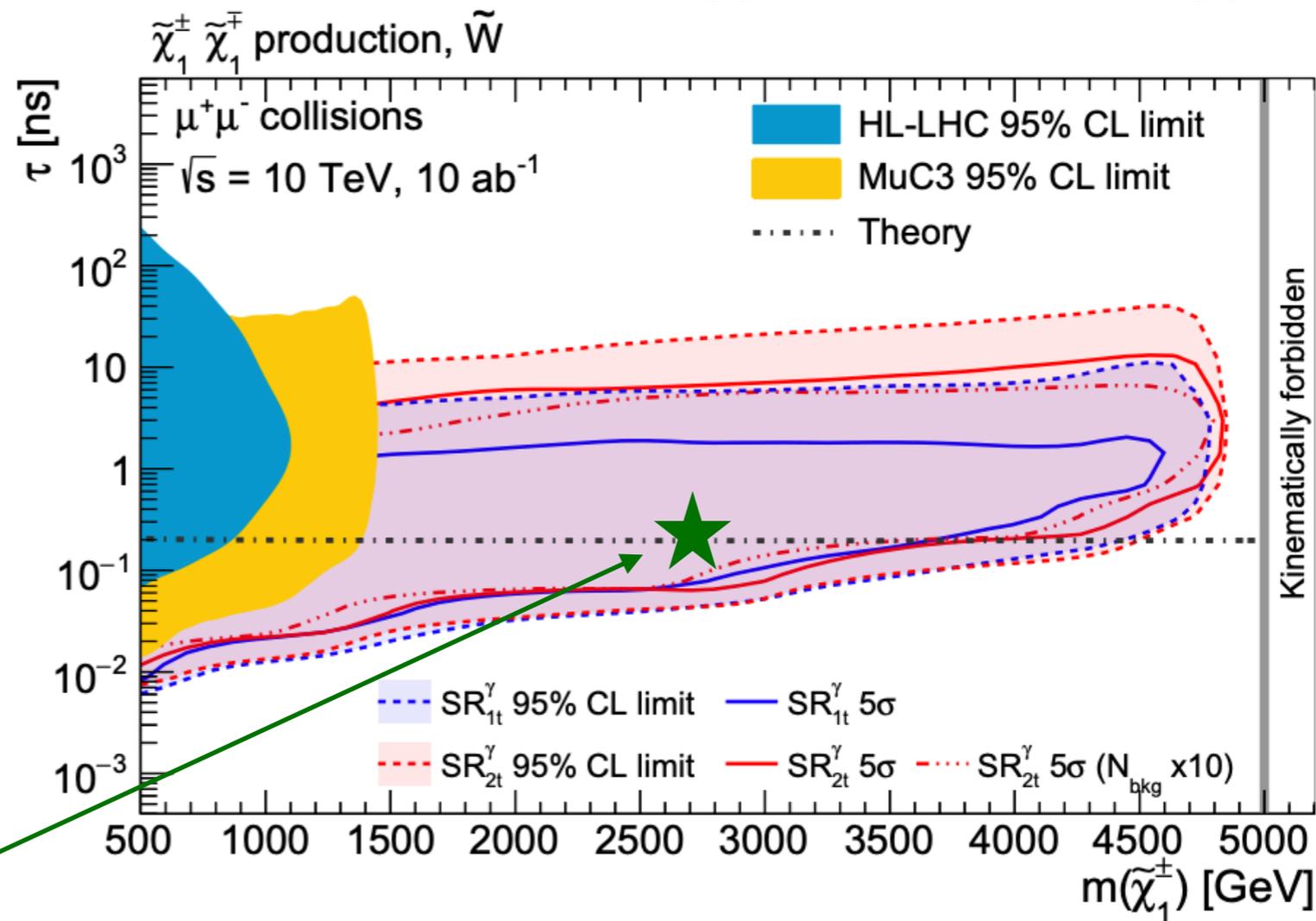


Long lifetime  
Disappearing Tracks  
(DT)



R. Mahbubani, P. Schwaller, J. Zurita, JHEP 06 (2017) 119

Thermal target mass  
2.7 TeV



Capdevilla, Meloni, Simoniello, Zurita, JHEP 06 (2021) 133

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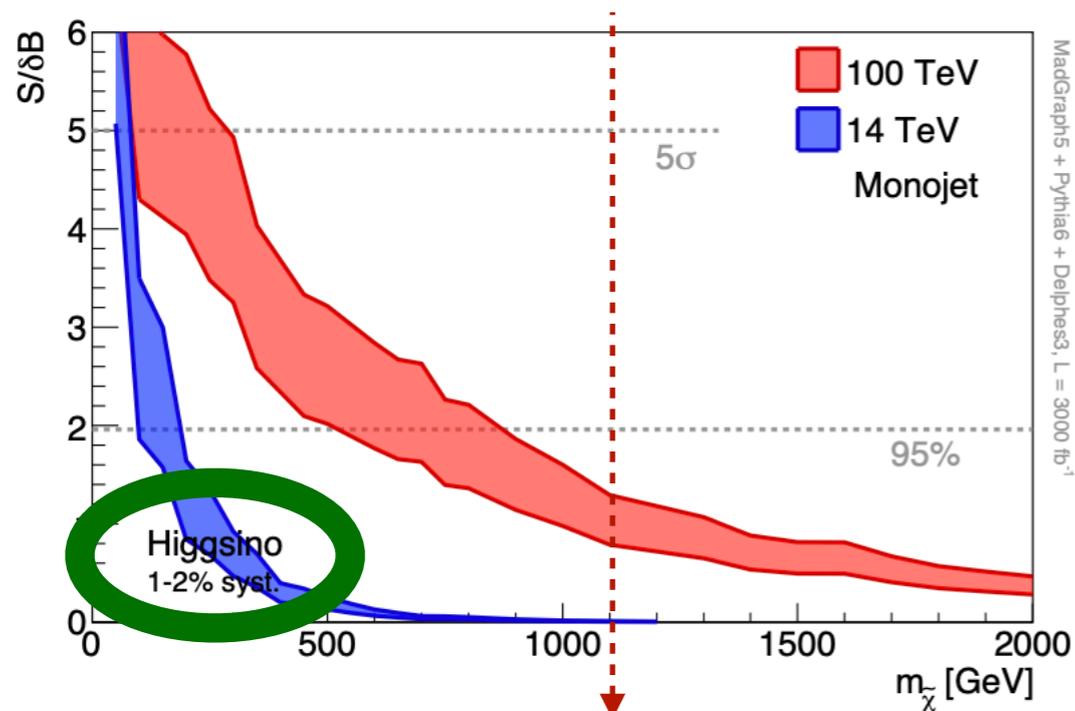
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4. Results

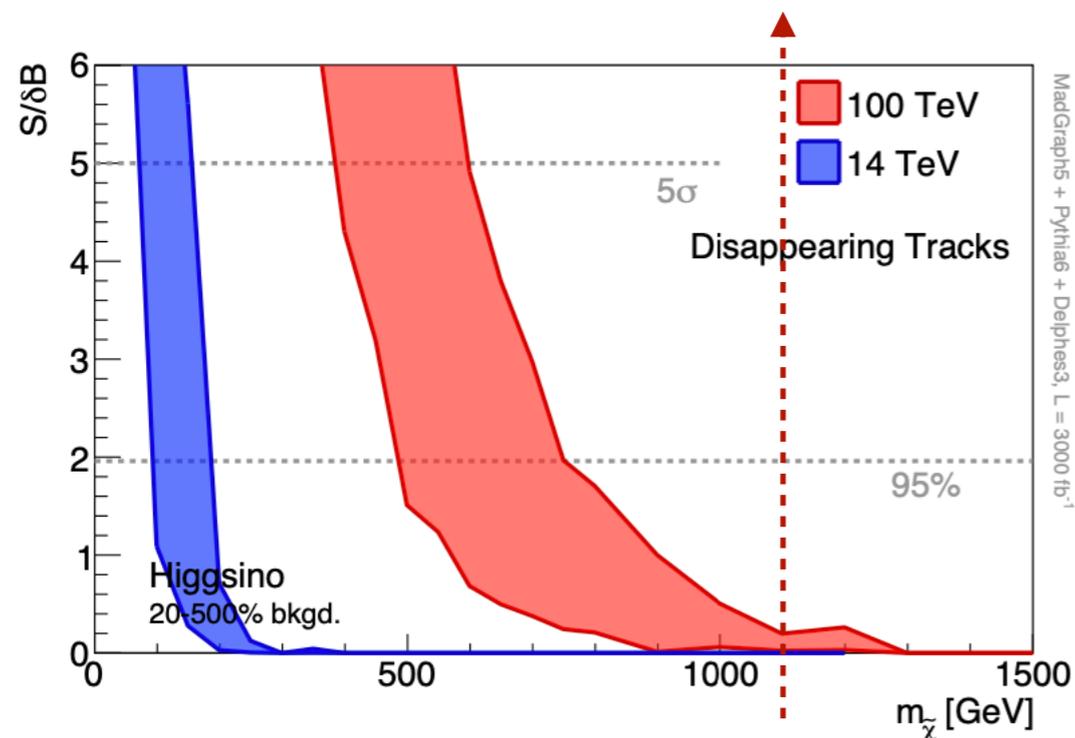
- The Importance of the 3TeV MuC!

# 2. Minimal Dark Matter: Projections

- Hadron colliders

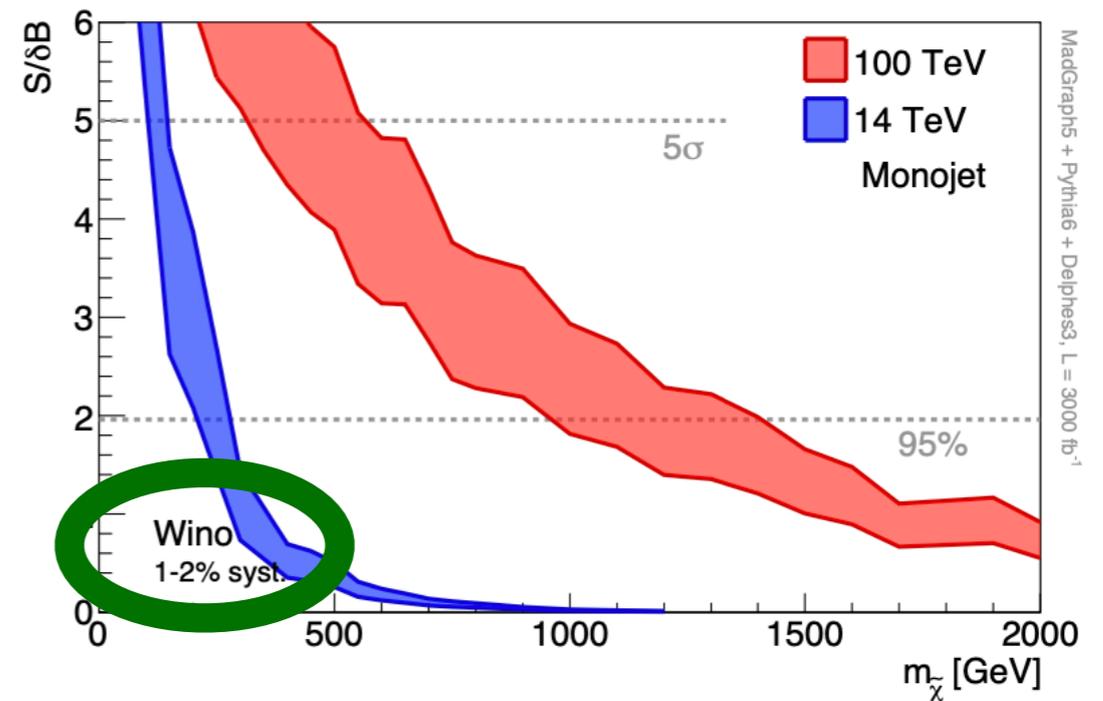


Thermal Target! ~ 1.1 TeV

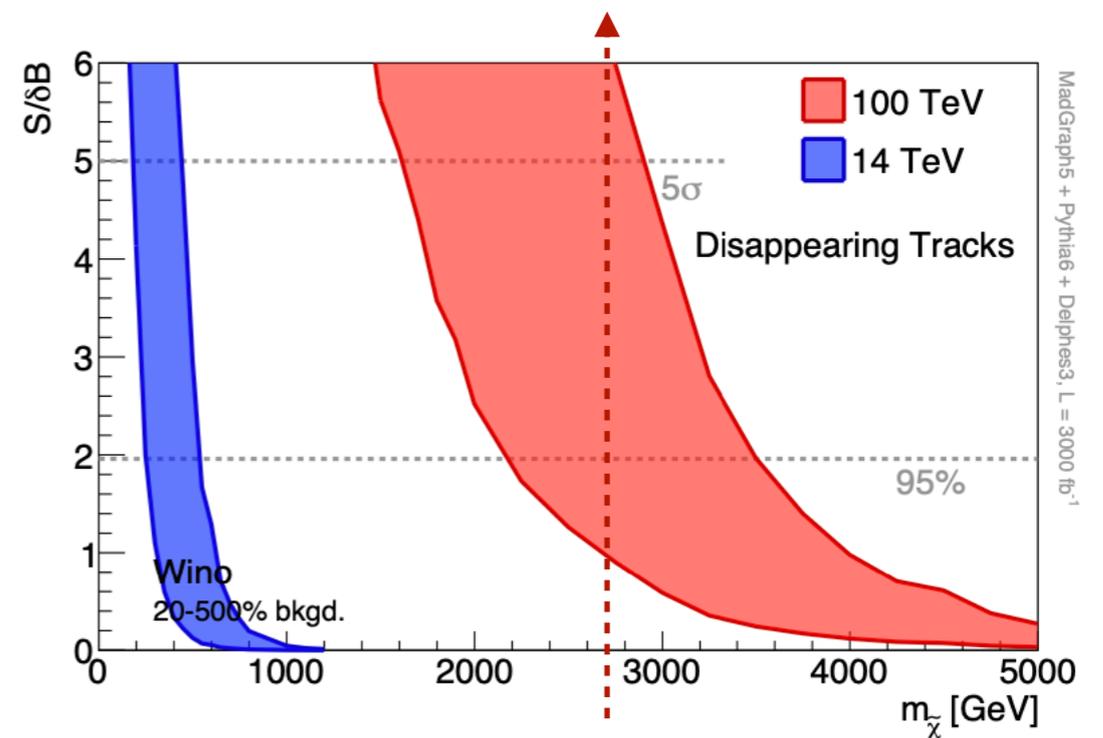


In more recent studies FCChh can reach the thermal target!

M. Low, L. Wang, JHEP 08 (2014) 161



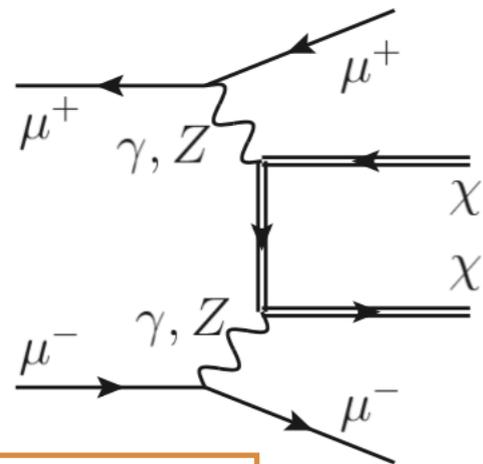
~ 2.7 TeV



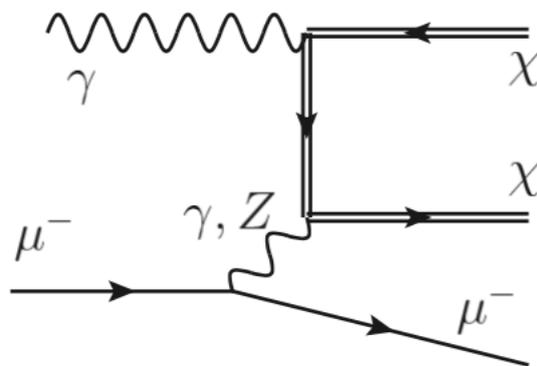
# 2. Minimal Dark Matter: Projections

T. Han, Z. Liu, L. Wang, X. Wang,  
Phys. Rev. D 103 (2021) 7, 075004

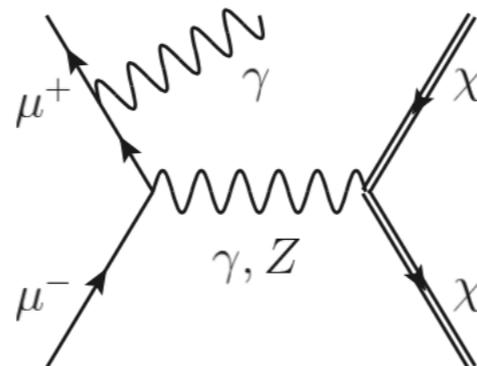
- Muon colliders



di-muon + MET

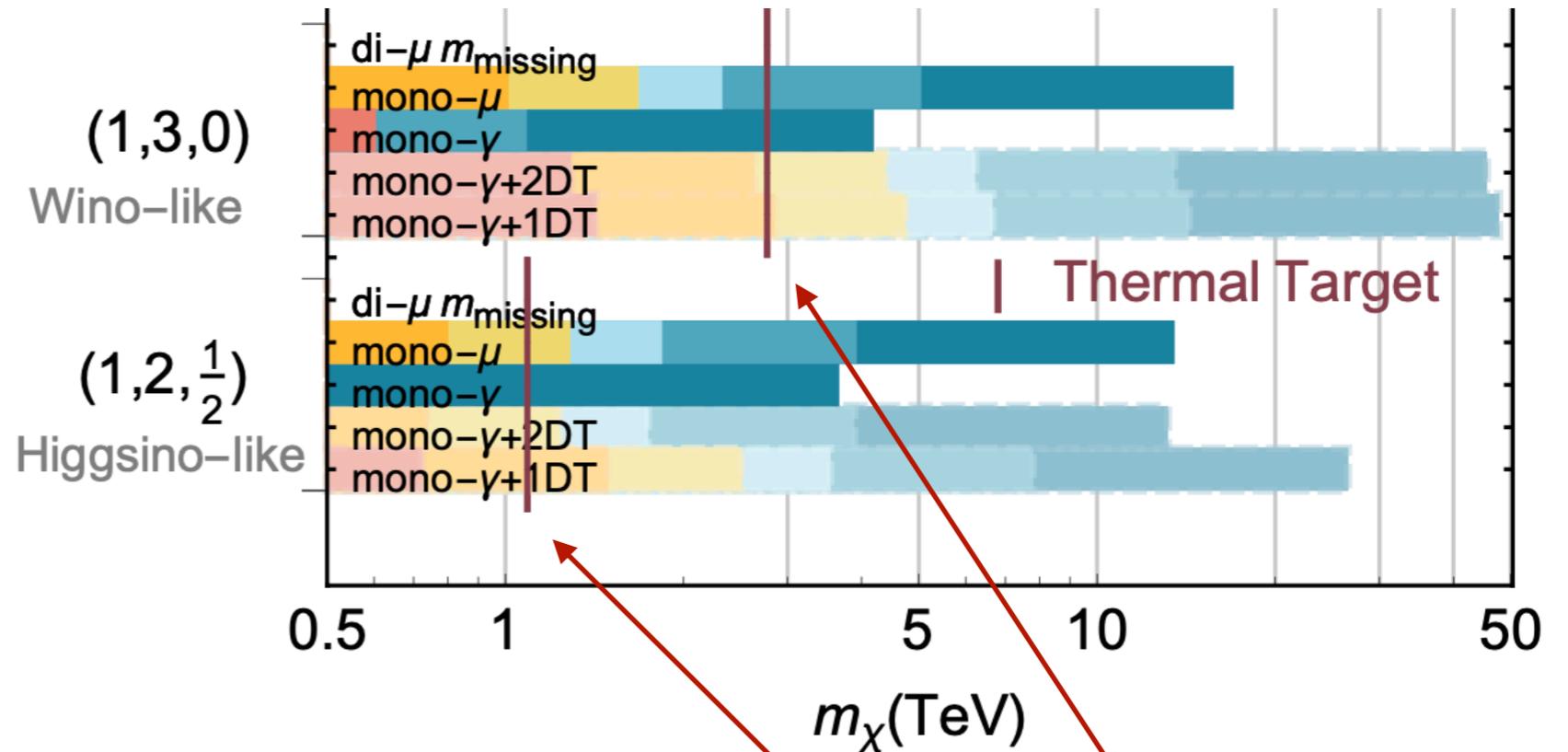


mono-muon



Mono-photon

Muon Collider  $2\sigma$  Reach  
( $\sqrt{s} = 3, 6, 10, 14, 30, 100$  TeV)



The 10 TeV MuC  
can reach the  
thermal target (?)

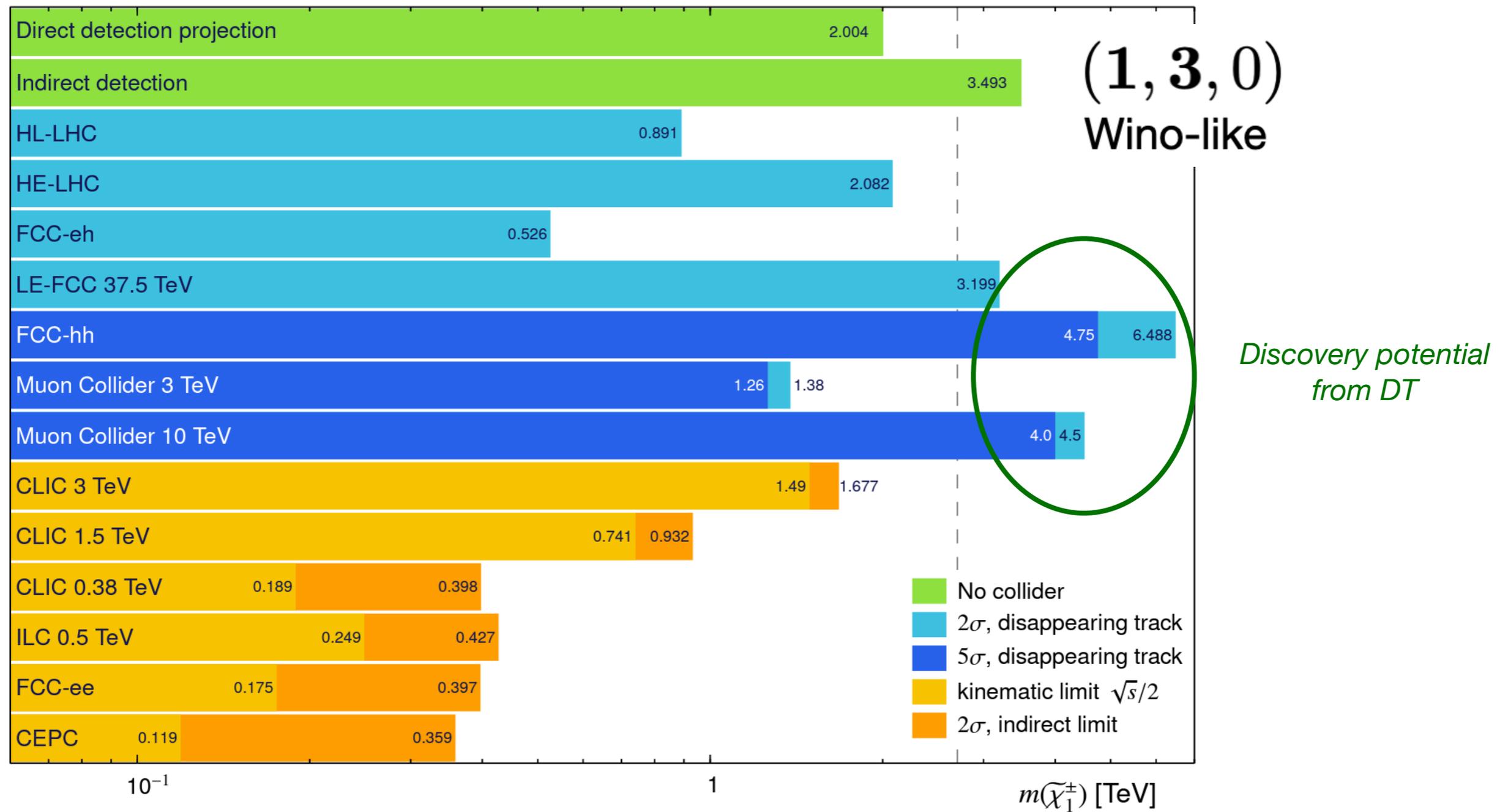
Need DT

BIB impact?

## 2. Minimal Dark Matter: Projections

- Triplet MDM:

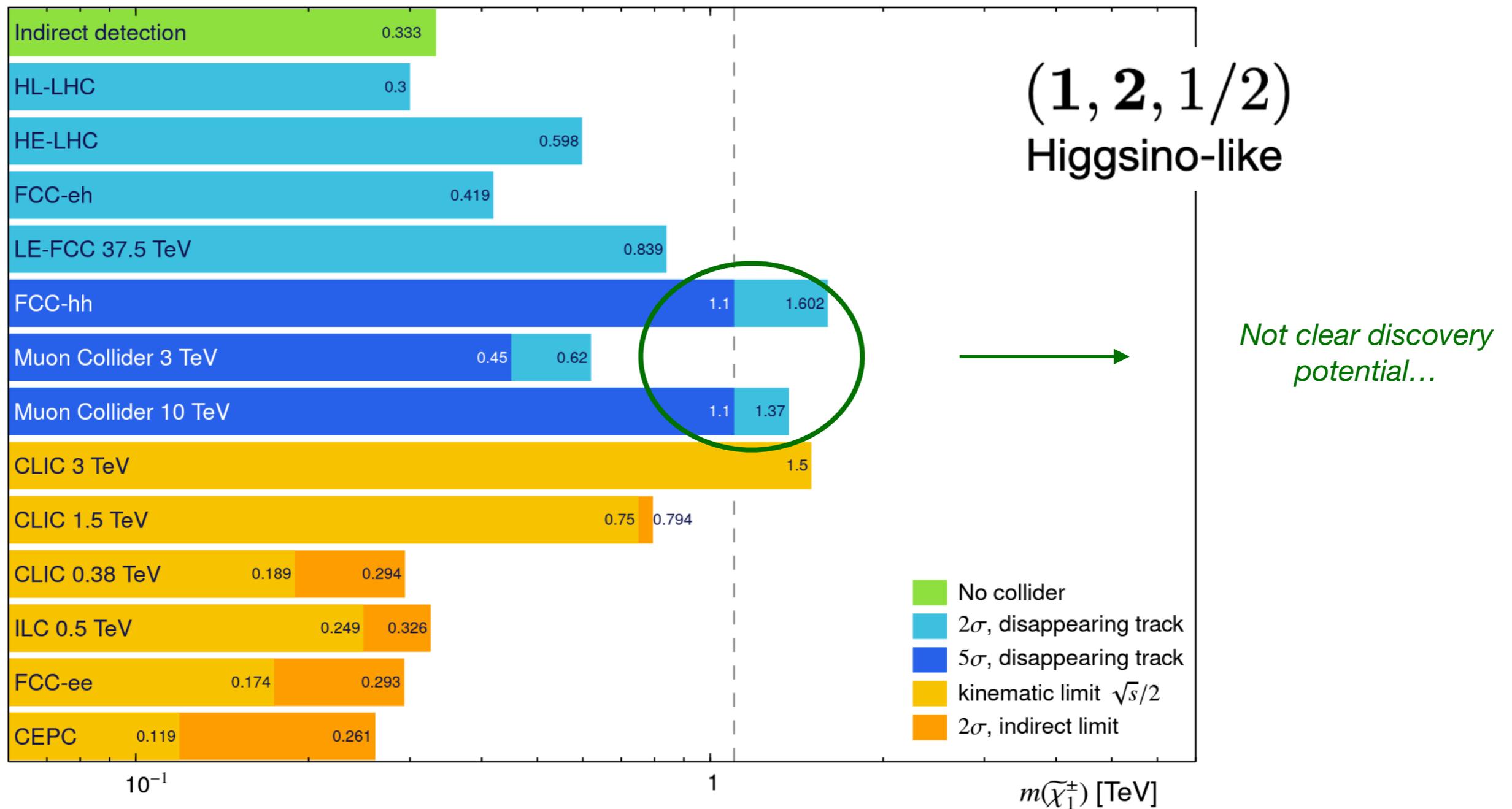
Capdevilla, Meloni, Simoniello, Zurita, JHEP 06 (2021) 133



## 2. Minimal Dark Matter: Projections

- Doublet MDM:

Capdevilla, Meloni, Simoniello, Zurita, JHEP 06 (2021) 133



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# 3. Soft Tracks

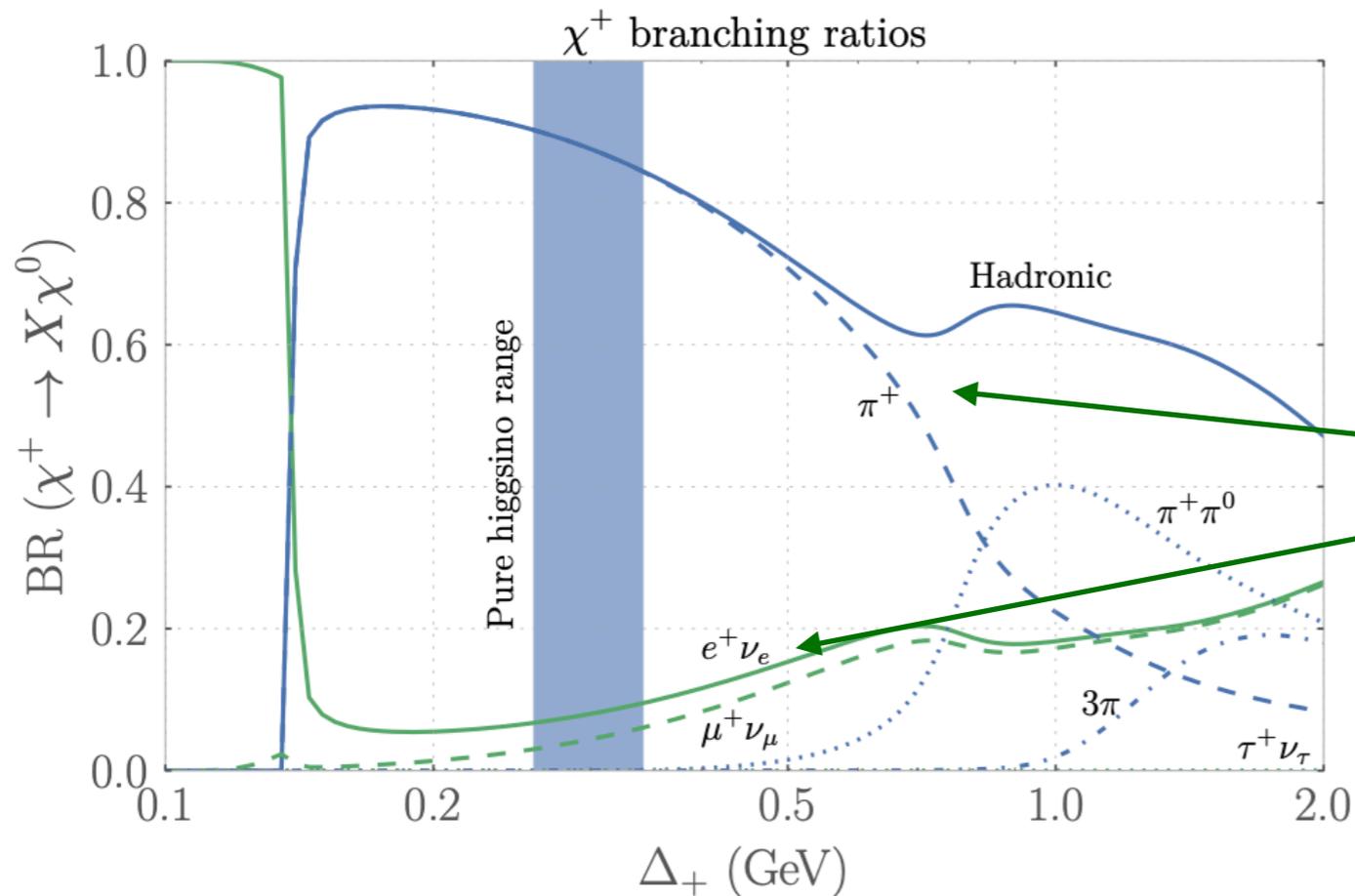
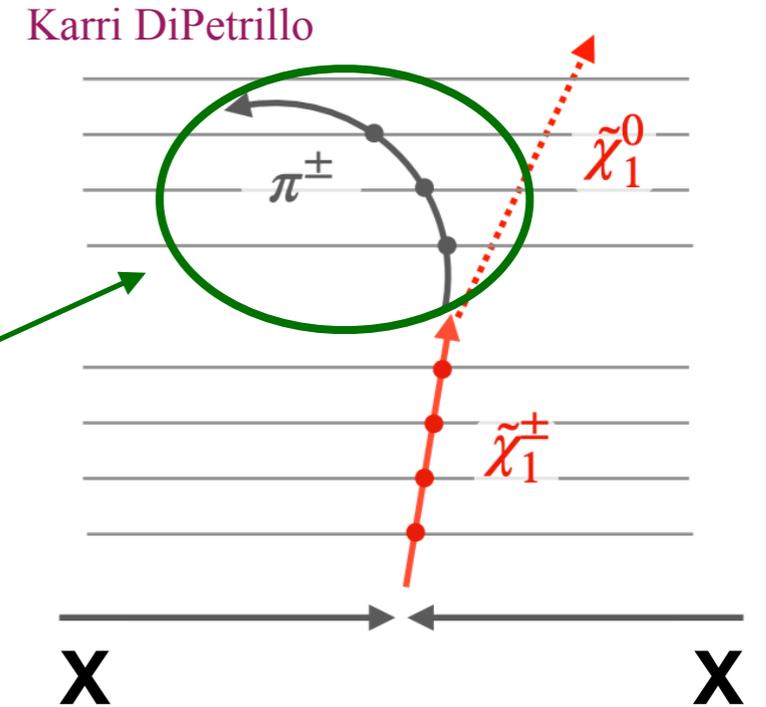
- Definition:

$$\Delta m = m_{\chi^+} - m_{\chi^0} > 0$$

Small mass splitting  
(from loops)



Long lifetime  
Disappearing Tracks  
Soft Tracks (ST)



Soft pions  
Soft muons  
Soft electrons = ST

R. Mahbubani, P. Schwaller, J. Zurita, JHEP 06 (2017) 119

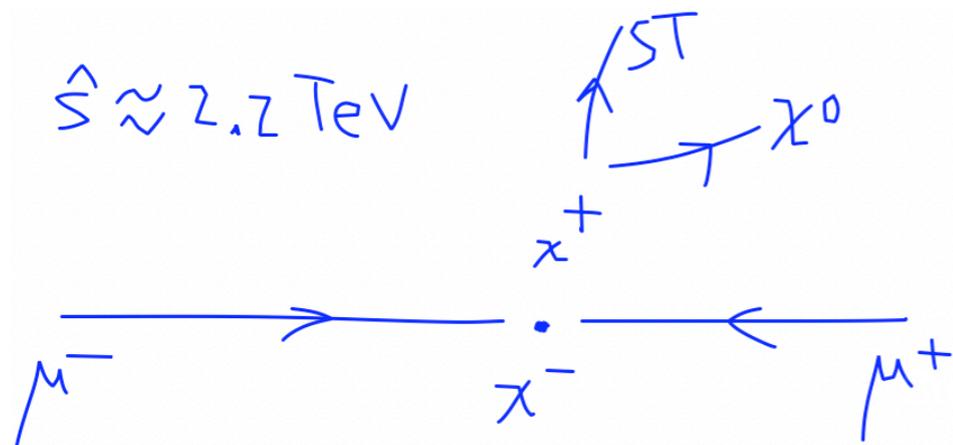
### 3. Soft Tracks: Signal Region

Thermal Higgsino  
(doublet MDM)

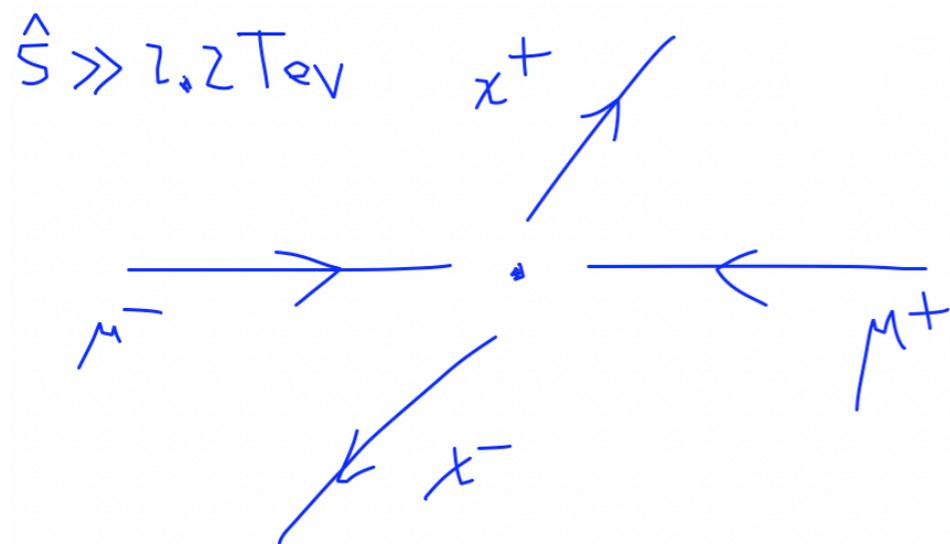
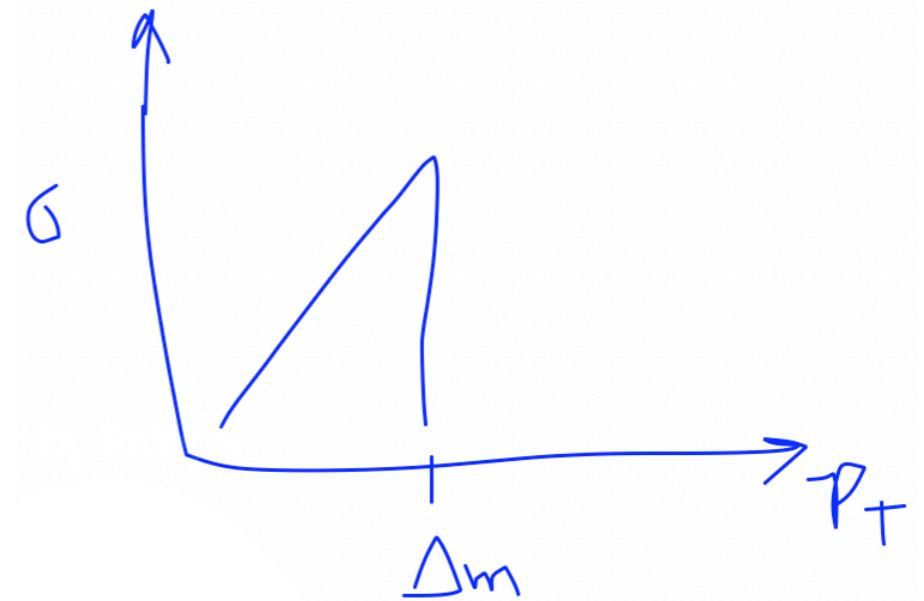
Very small gap!

$$m_\chi = 1.1 \text{ TeV}$$

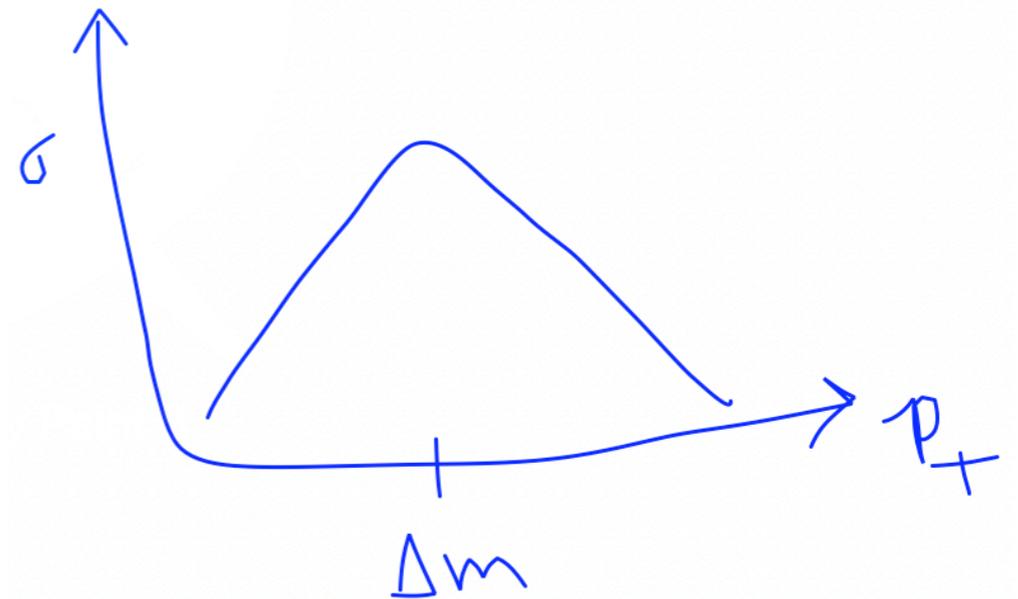
$$\Delta m \sim 0.3 \text{ GeV}$$



Threshold  
production



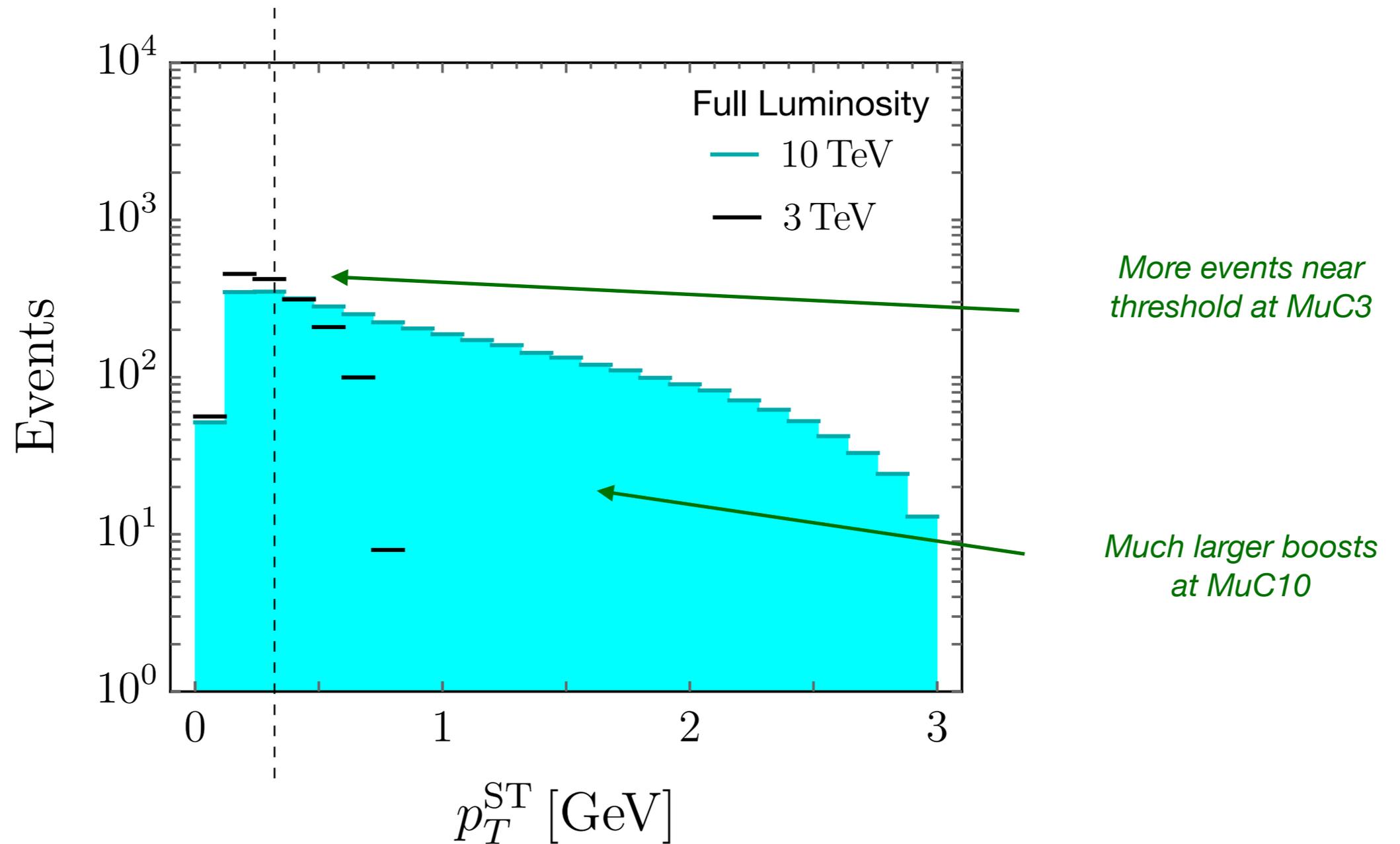
Boosted  
production



### 3. Soft Tracks: Signal Region

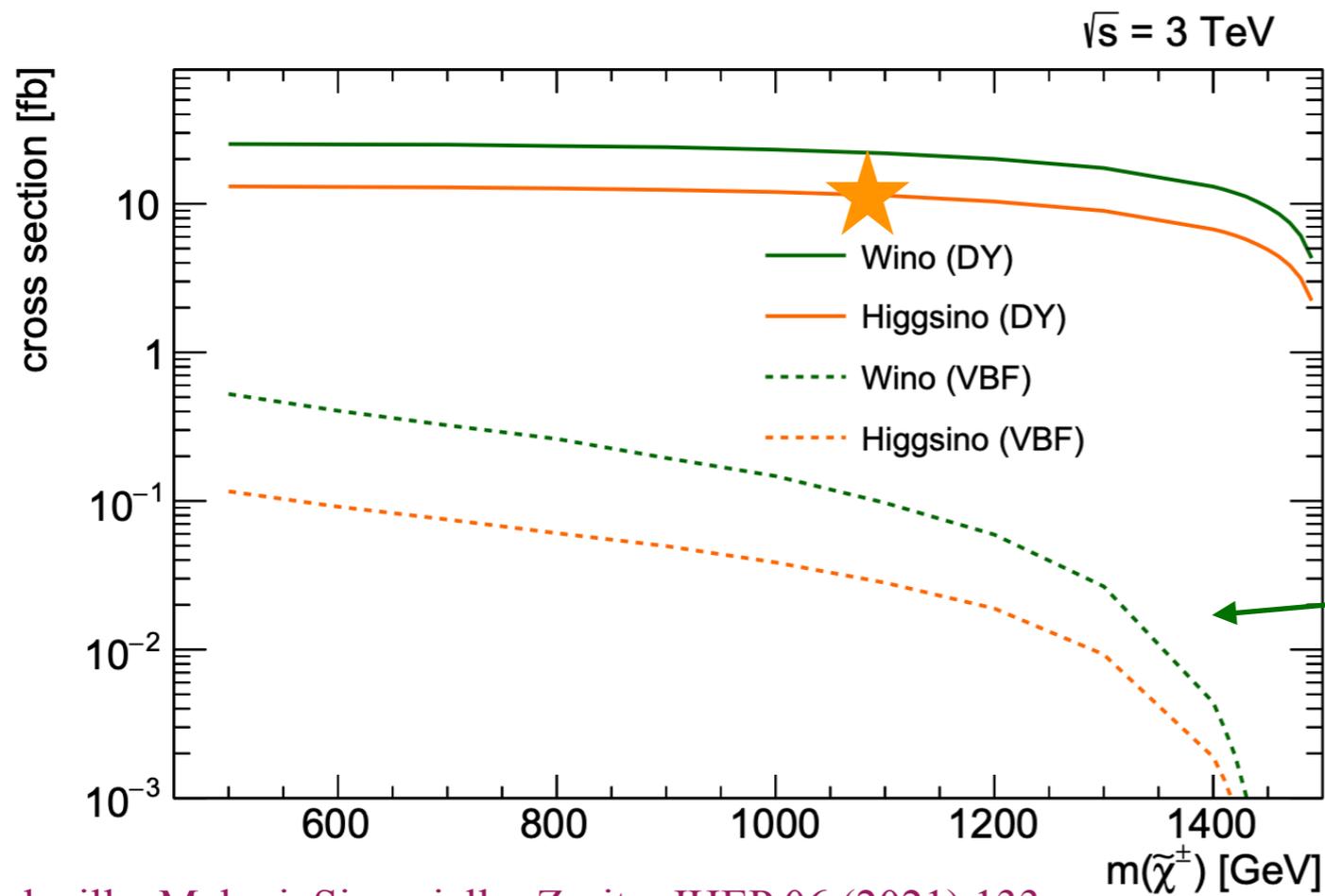
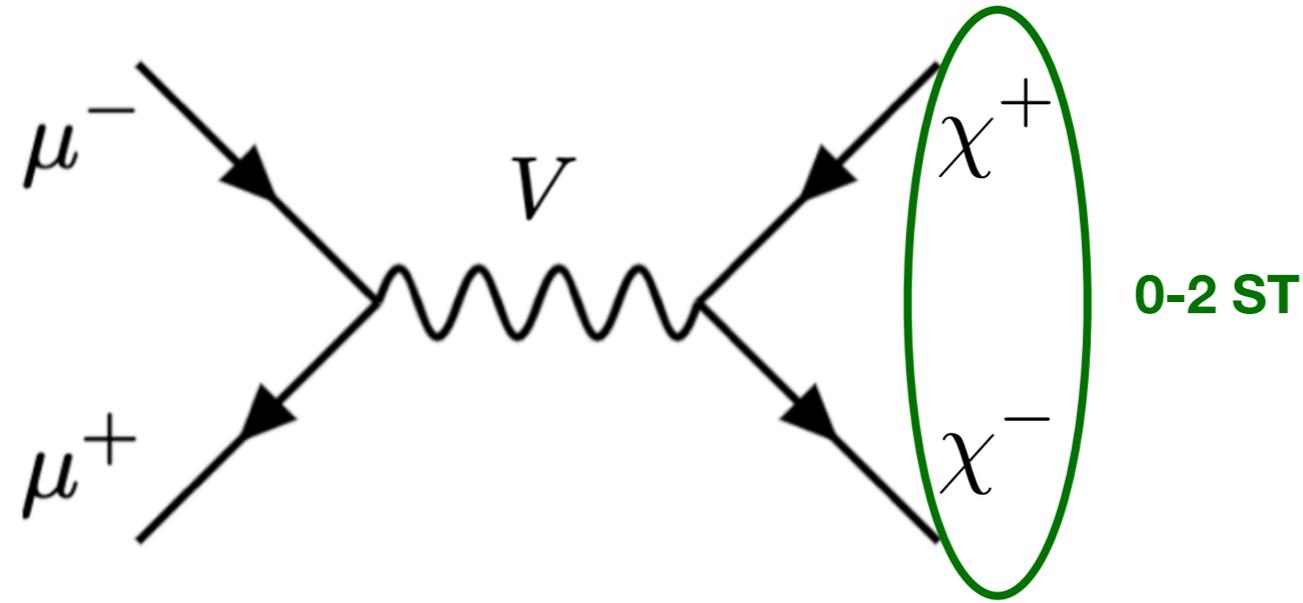
*Thermal Higgsino  
(doublet MDM)*

$$m_\chi = 1.1 \text{ TeV}$$
$$\Delta m \sim 0.3 \text{ GeV}$$



### 3. Soft Tracks: Signal Region

- Drell-Yan:



*Drell-Yan-like process dominates ST production*

*VBF processes are subdominant (For signal)*

Capdevilla, Meloni, Simoniello, Zurita, JHEP 06 (2021) 133

### 3. Soft Tracks: Signal Region

- Signal Regions:

*Thermal Higgsino  
(doublet MDM)*

#### MuC 3 TeV

1ST 0 $\gamma$ 14%	1ST 1 $\gamma$ 2%
2ST 0 $\gamma$ 75%	2ST 1 $\gamma$ 9%

$\sigma_T = 12.53(3)$  fb

↑  
*About 1k signal events  
in this signal region*

#### MuC 10 TeV

1ST 0 $\gamma$ 7%	1ST 1 $\gamma$ 2%
2ST 0 $\gamma$ 65%	2ST 1 $\gamma$ 20%

$\sigma_T = 1.7996(36)$  fb

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- **Backgrounds**

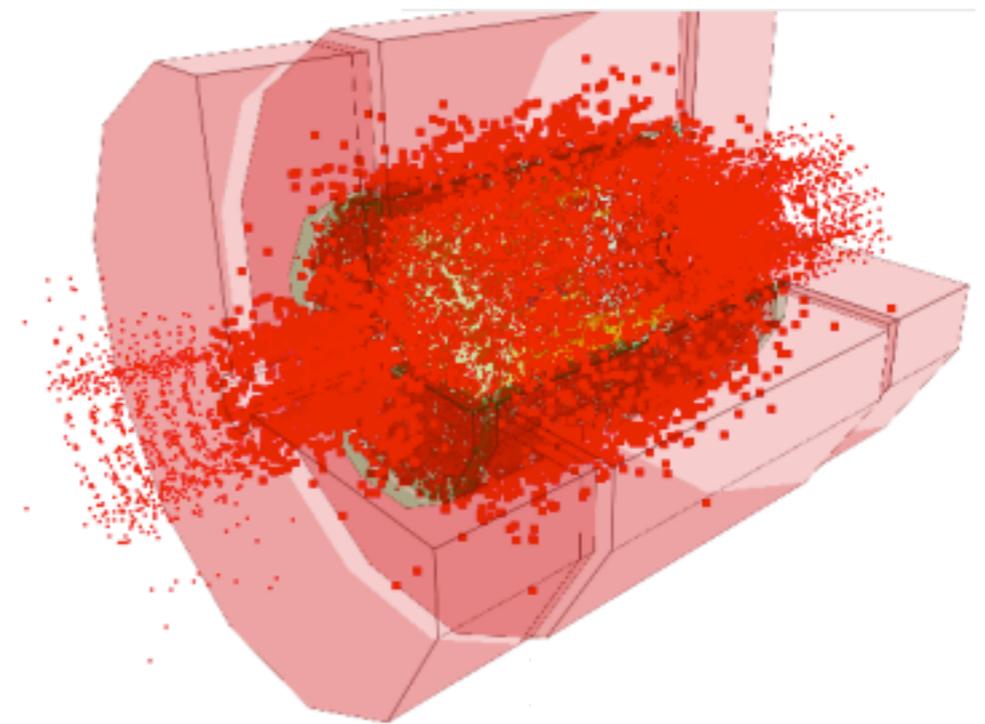
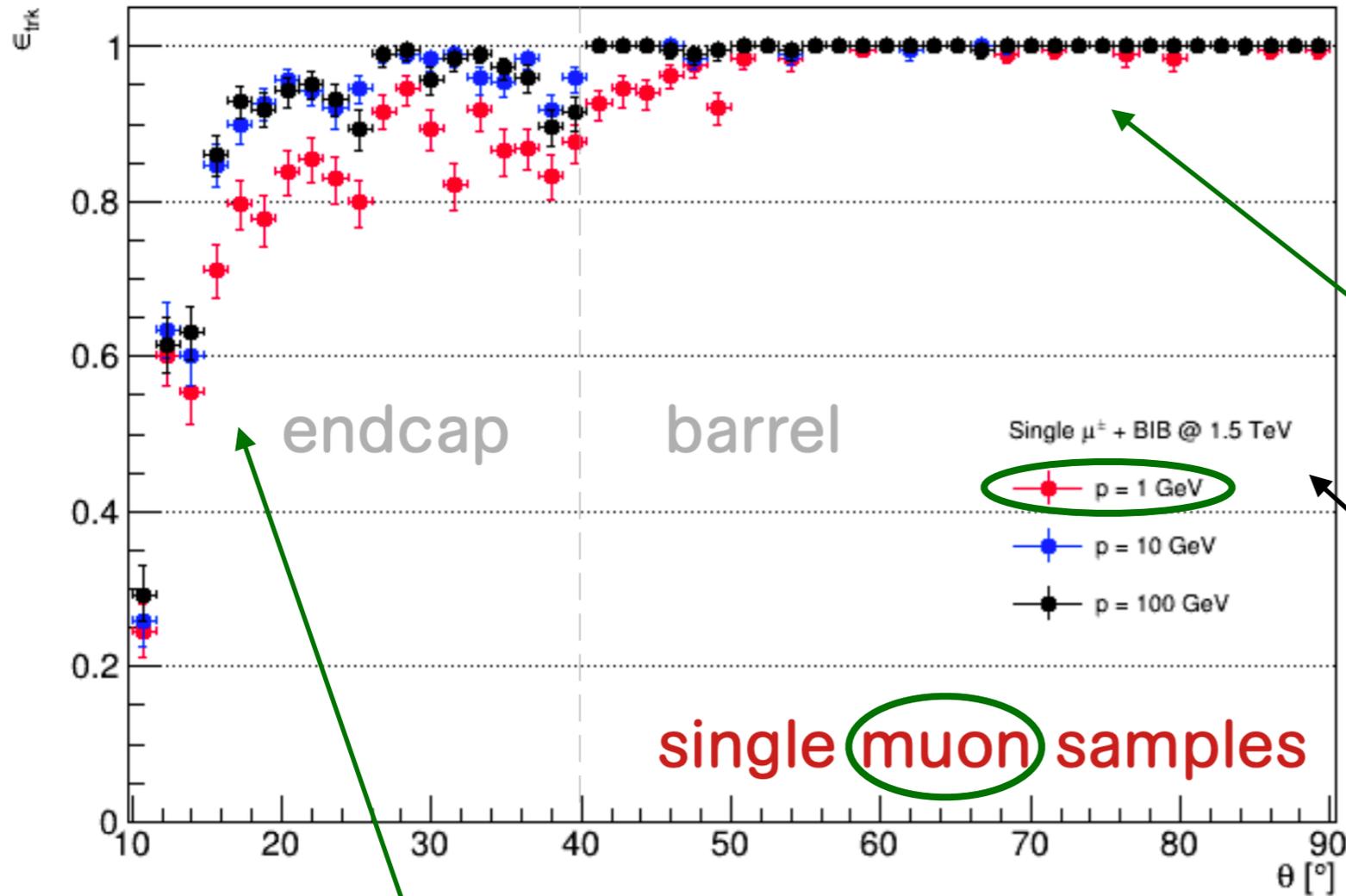
## 4. Results

- The Importance of the 3TeV MuC!

# 3. Soft Tracks: Backgrounds

- BIB: Track Reconstruction

C. Accettura et al., Eur. Phys. J. C **83** (2023) 9, 864



Central angular region:

Small probability of missing a track immersed in the BIB

Forward/backward angular regions:

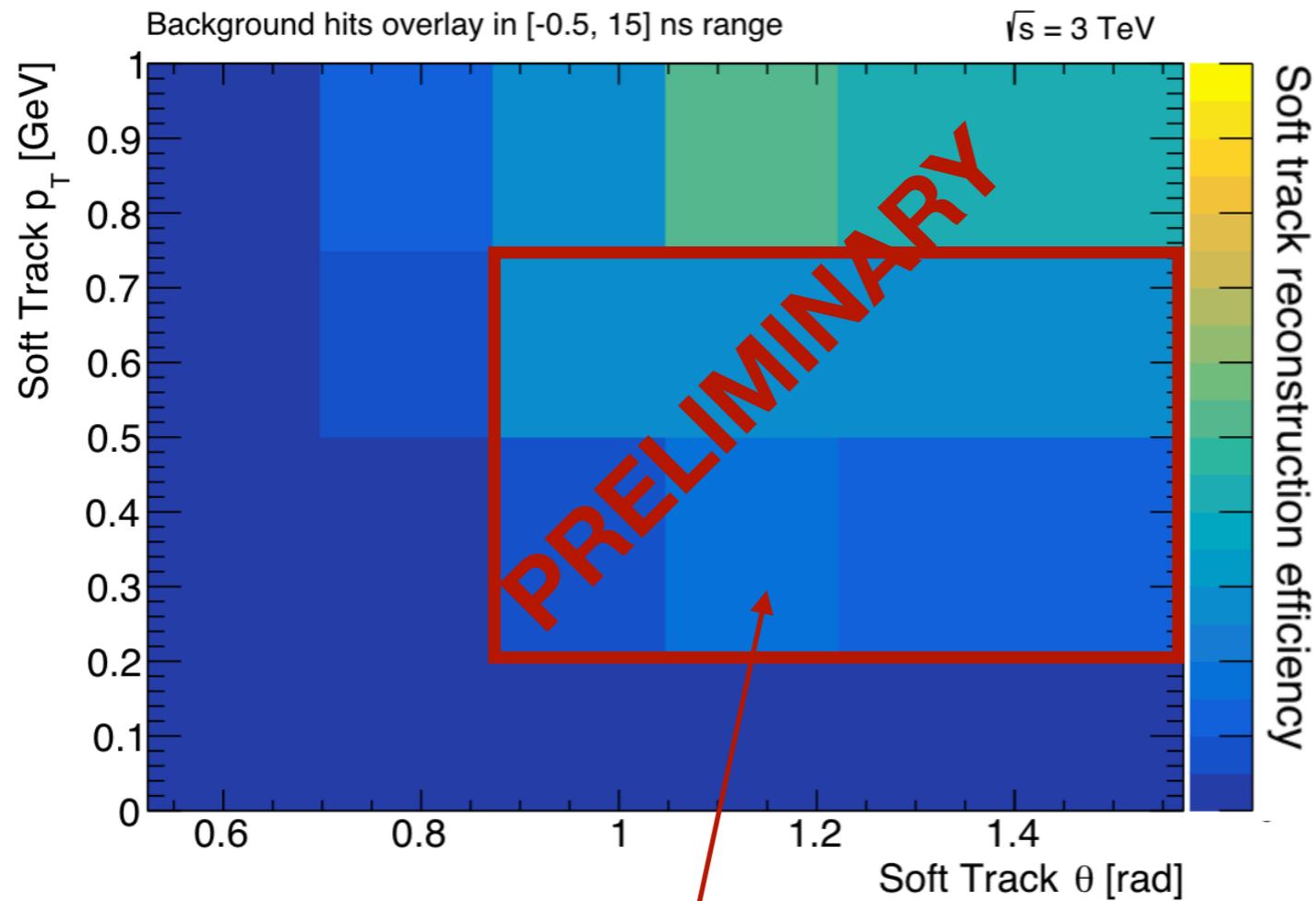
Large probability of missing a track immersed in the BIB

BIB Data from the MAP collaboration

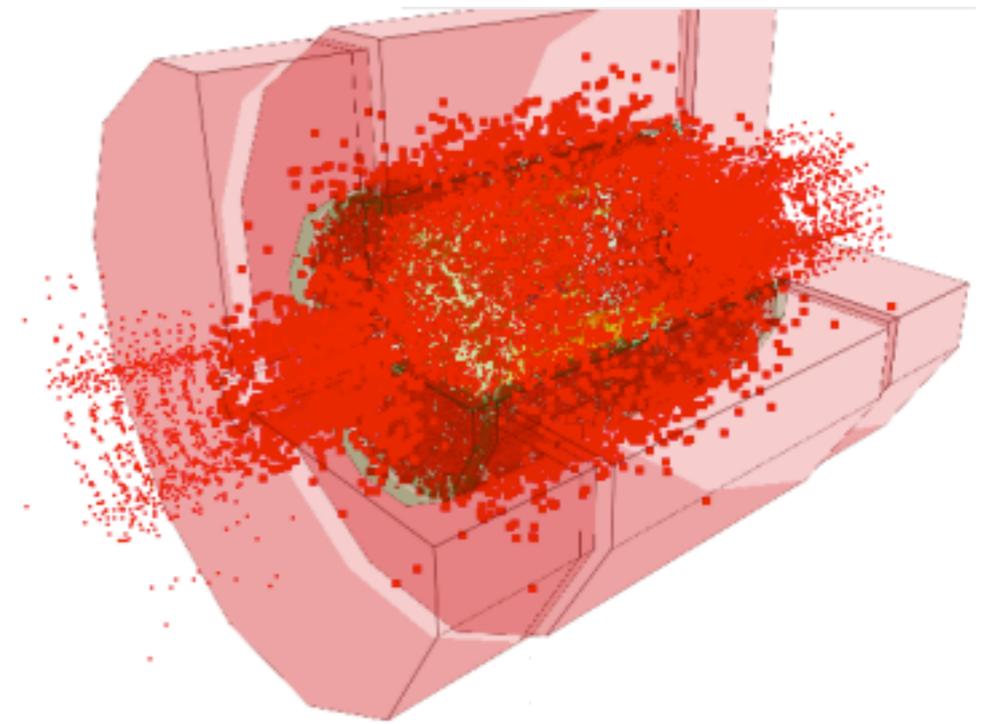
N.V. Mokhov, S.I. Striganov, Phys. Procedia 37 (2012)

# 3. Soft Tracks: Backgrounds

- BIB: Track Reconstruction



*Order 10-30% reconstruction efficiency in the signal region*



## Soft Track

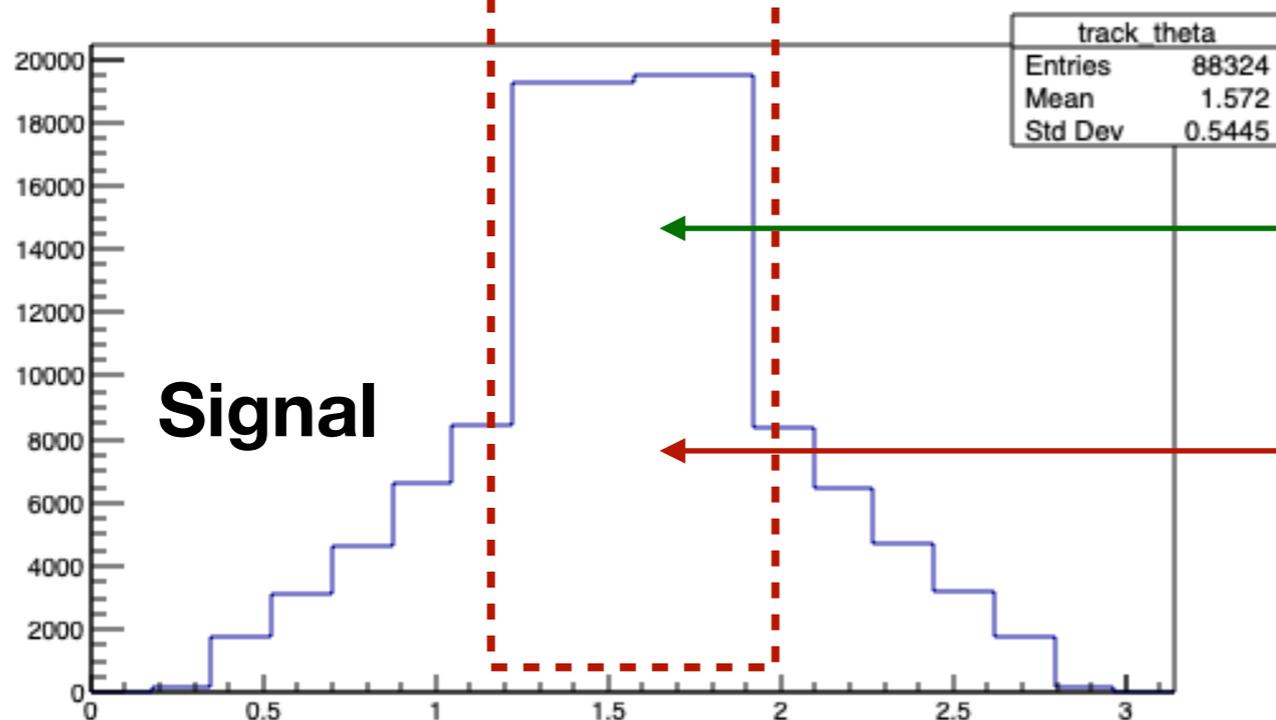
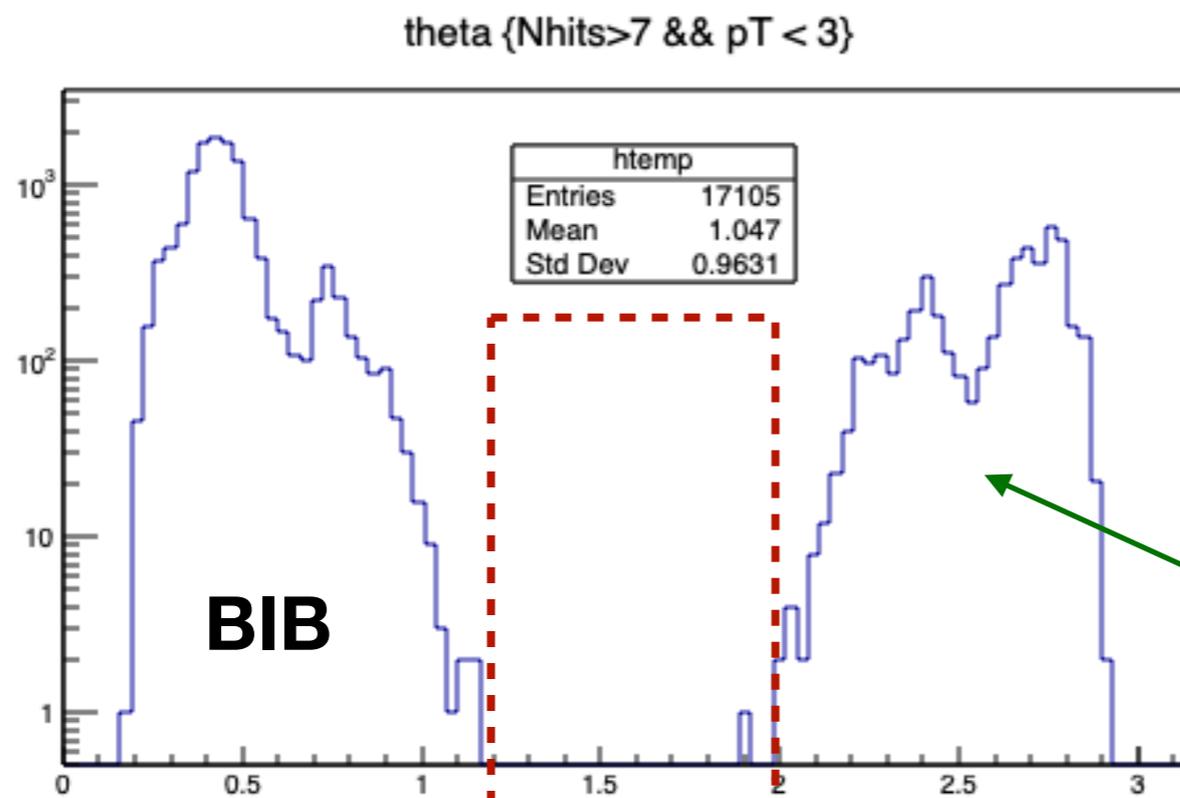
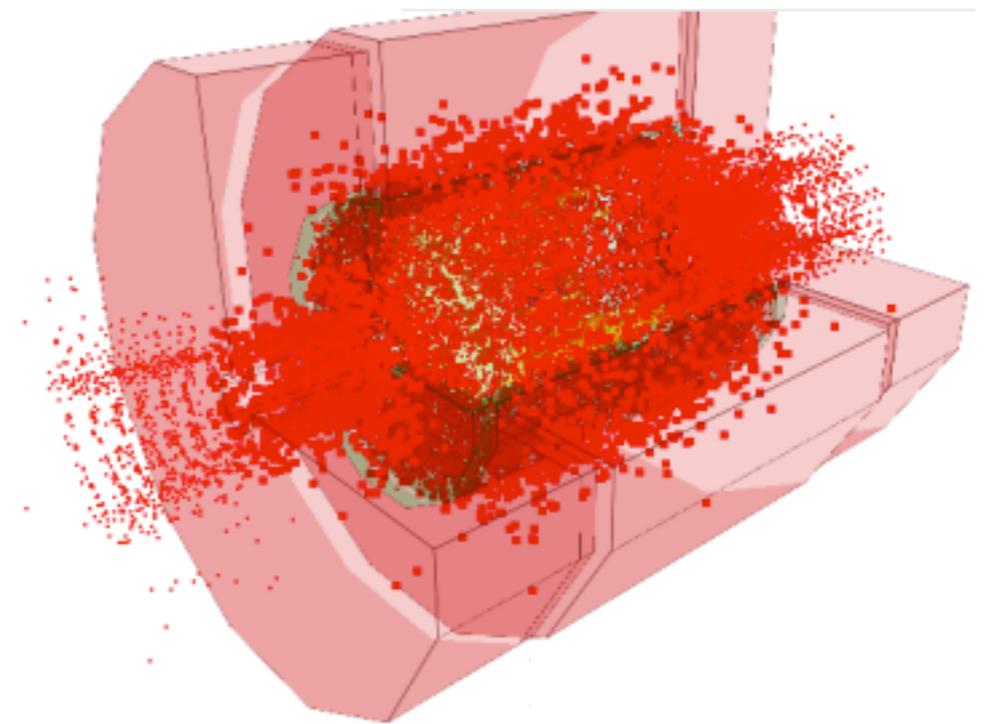
$$60^\circ \leq \theta_{ST} \leq 120^\circ$$
$$0.2 \leq p_T^{ST} \leq 0.75 \text{ GeV}$$

## Photons

$$10^\circ \leq \theta_\gamma \leq 170^\circ$$
$$p_T^\gamma \geq 40 \text{ GeV}$$

# 3. Soft Tracks: Backgrounds

- BIB: Fake Tracks



The BIB fake tracks want to be forward/backward

The signal wants to be central

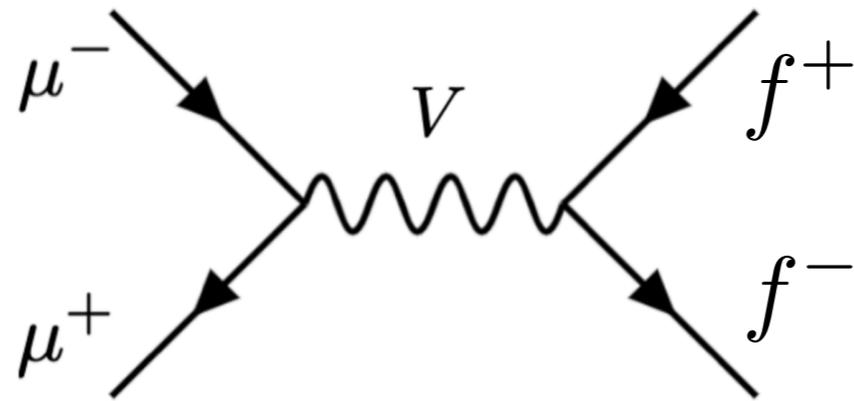
This is why:

$$60^\circ \leq \theta_{ST} \leq 120^\circ$$

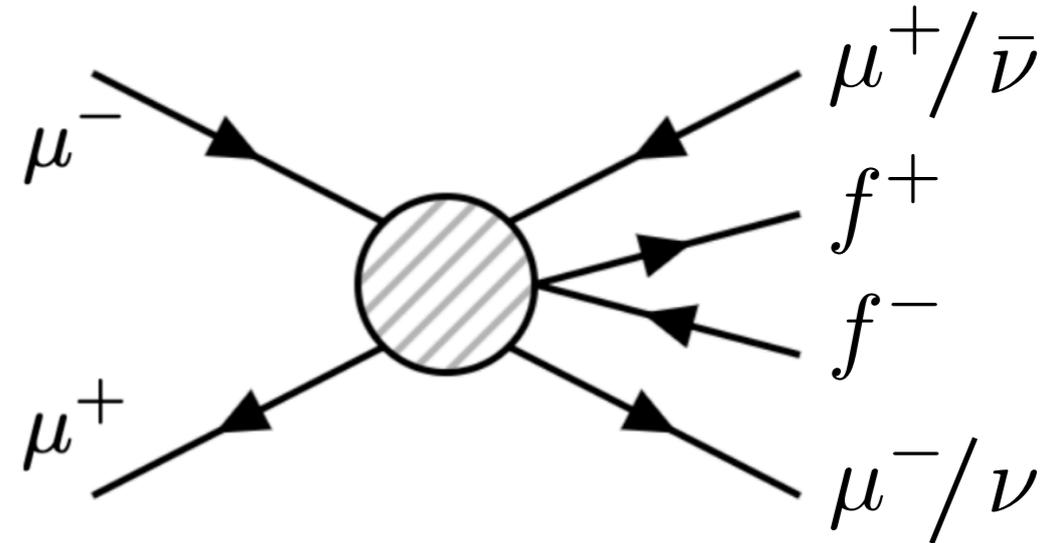
$\theta_{ST}$

### 3. Soft Tracks: Backgrounds

- ST from Leptons/Hadrons:  $f = \ell, \tau, j$



*DY-like process is subdominant*



*VBF and Bhabha-like processes dominate background production*

$\mu^+ \mu^- \rightarrow \gamma + X (+ Z \rightarrow \nu\nu)$		
X	$\sigma(\gamma X)$ [fb]	$\sigma(\gamma X Z)$ [fb]
$\ell^+ \ell^- \nu_e \bar{\nu}_e$	242.0	2.828
$\ell^+ \ell^- \mu^+ \mu^-$	60.45	0.012
$e^+ \nu_e \mu^- \bar{\nu}_\mu + \text{CP}$	226.6	2.710
$\tau^+ \tau^- \nu_e \bar{\nu}_e$	6.493	0.058
$\tau^+ \tau^- \mu^+ \mu^-$	30.86	0.006
$\tau^+ \nu_\tau \mu^- \bar{\nu}_\mu + \text{CP}$	226.2	2.722
$j j \nu_e \bar{\nu}_e$	104.5	0.904
$j j \mu^+ \mu^-$	30.63	0.019
$j j \mu^- \bar{\nu}_\mu + \text{CP}$	1215.	11.57

$$p_T^\gamma \geq 20 \text{ GeV}$$

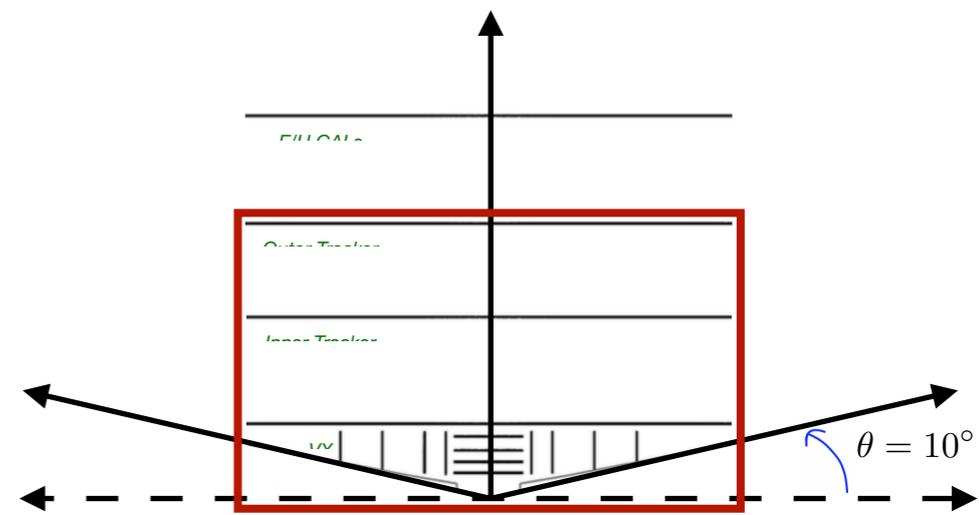
$$|\eta_\gamma| < 2.44$$

$$p_T^\ell \geq 0.1 \text{ GeV}$$

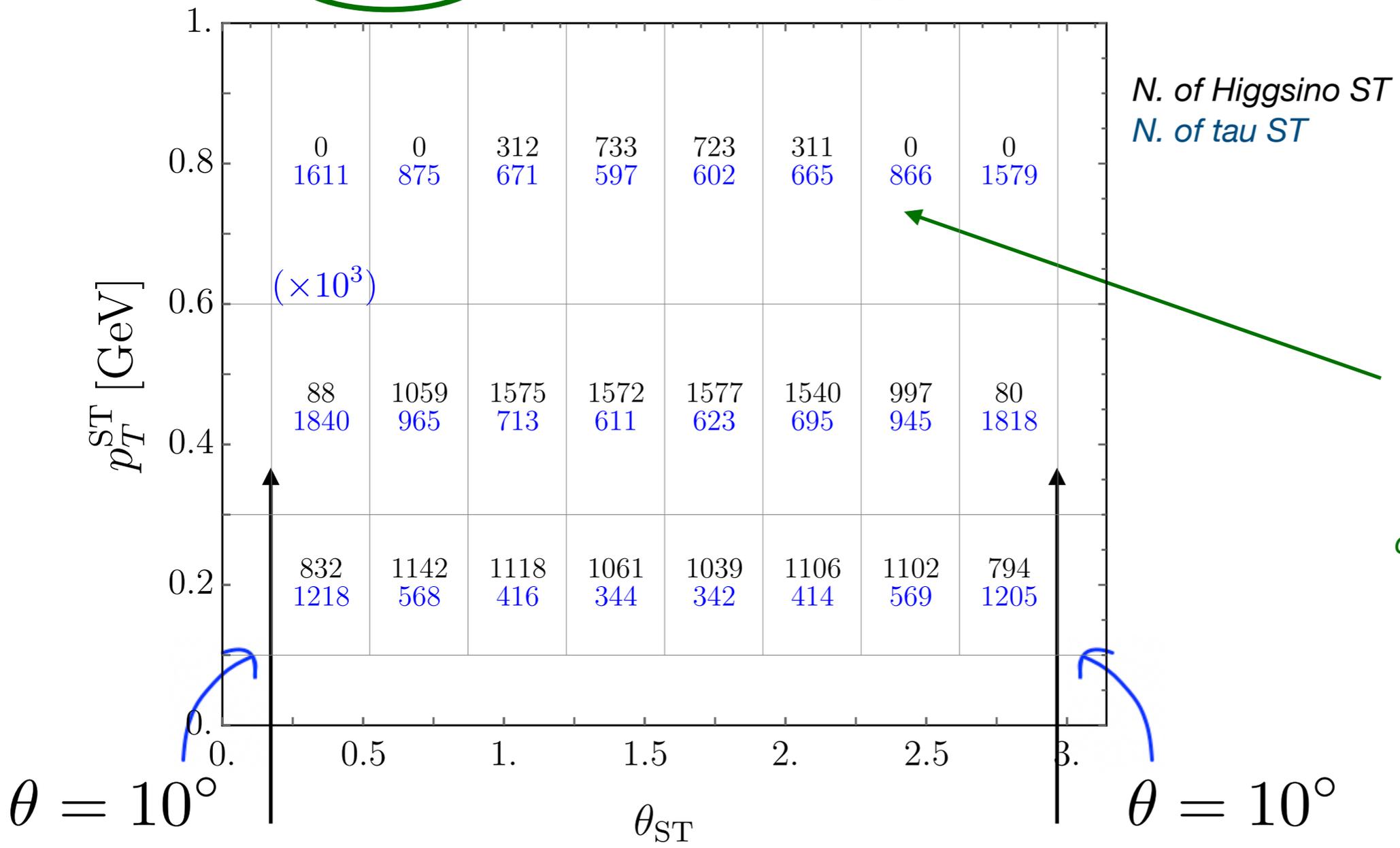
$$p_T^j \geq 0.1 \text{ GeV}$$

# 3. Soft Tracks: Backgrounds

- Backgrounds:



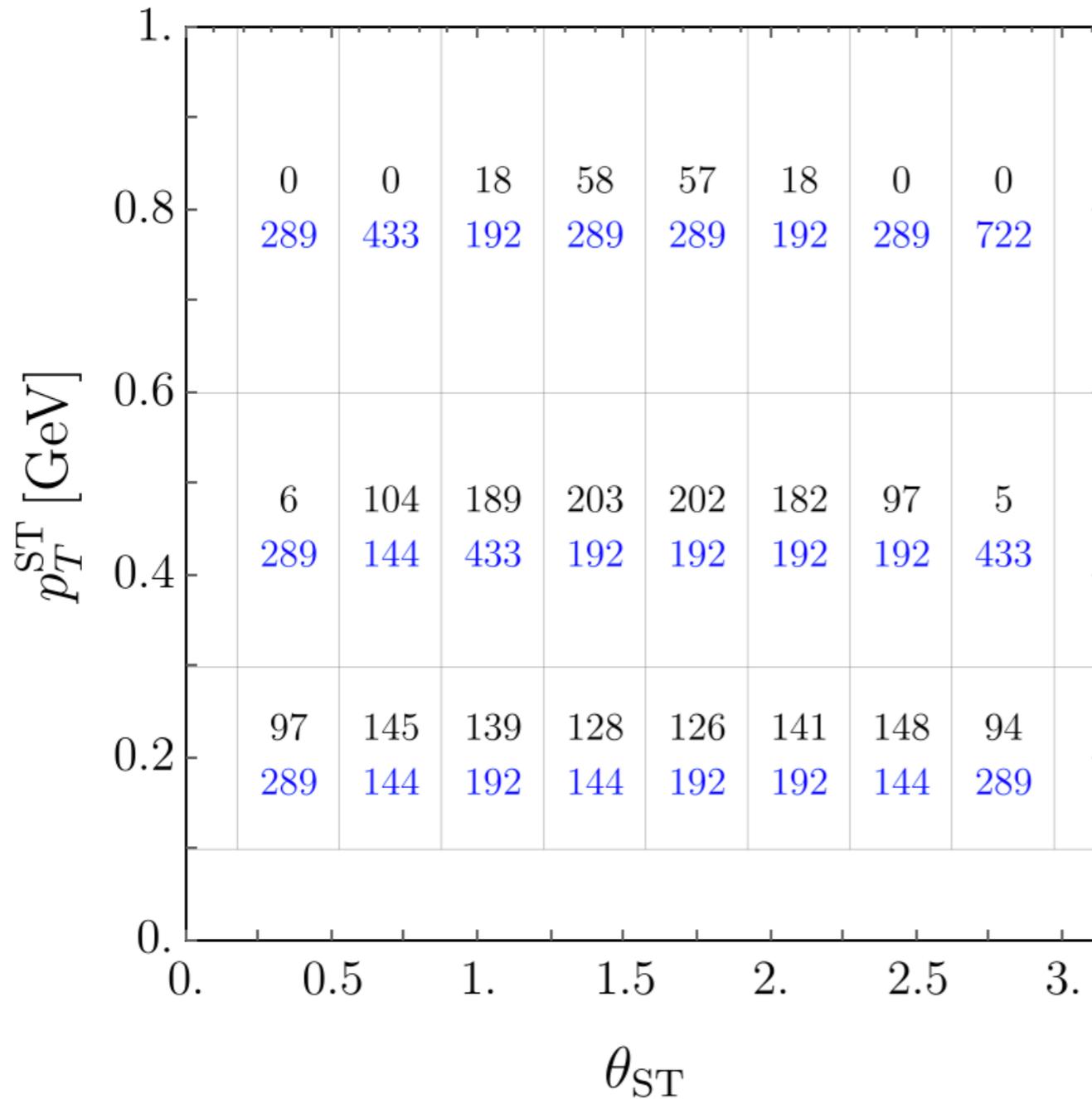
2ST0 $\gamma$ , MuC3, 1ab<sup>-1</sup>, Higgsinos



*Bad luck!*  
*The signal region with more events is overwhelmed by the background!*

# 3. Soft Tracks: Backgrounds

- Backgrounds:



*N. of Higgsino ST*  
*N. of tau ST*

MuC3,  $1\text{ab}^{-1}$

2ST1 $\gamma$ , Higgsinos

$p_T^\gamma \geq 10\text{ GeV}$

$N_{\text{tot}} = 2157$

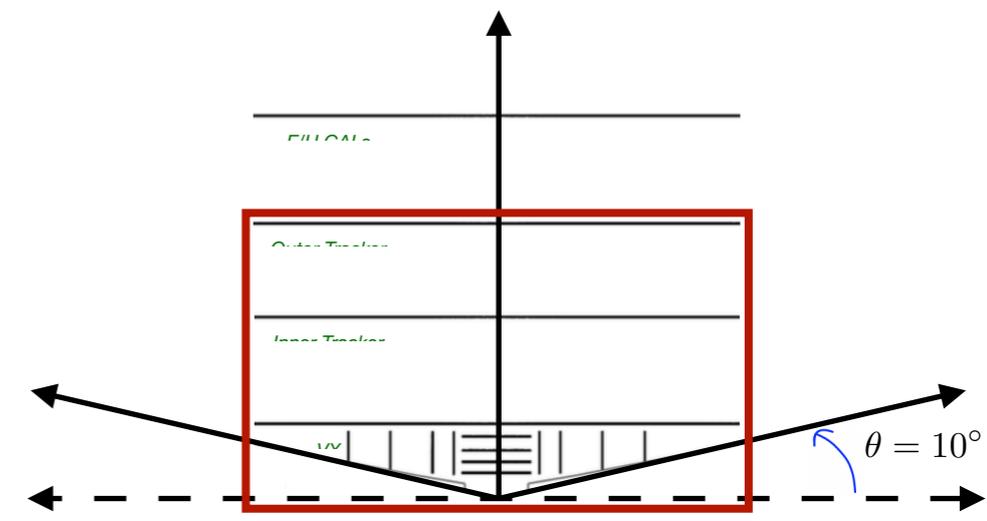
$N_{\text{tot}} = 6350$

*Good luck!*

*The photon in the event pushes the ST candidates out of the acceptance!!!*

*This is why:*

$p_T^\gamma \geq 40\text{ GeV}$



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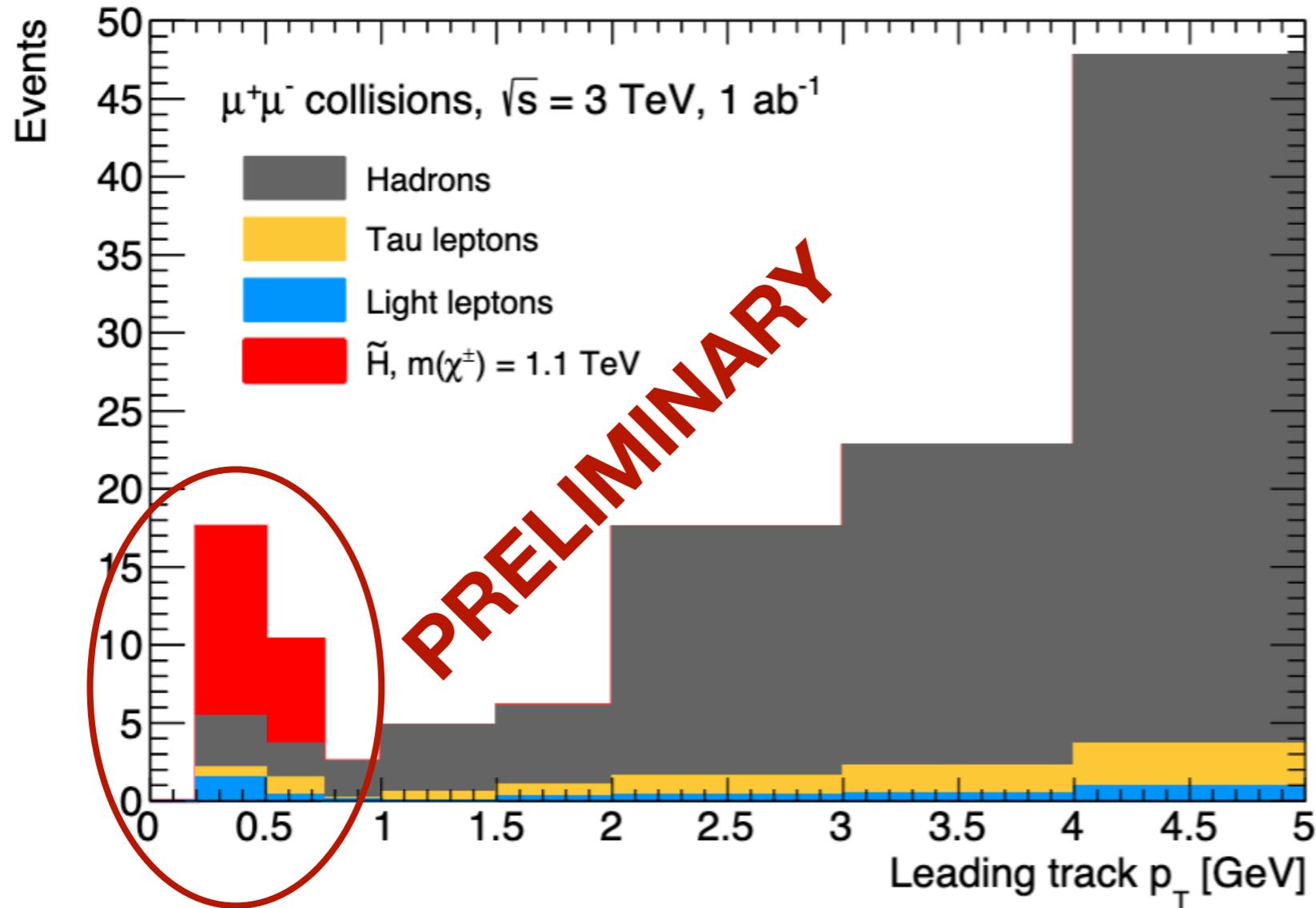
## 4. Results

- **The Importance of the 3TeV MuC!**

# 4. Results

- The Importance of the 3TeV Collider:

Signal region:  
 2 ST + 1 gamma  
 $0.2 < p_T < 0.75 \text{ GeV}$



Vetoos:  
 Hard tracks  
 Heavy neutrals

Photon  $p_T$  above  
 40 GeV

Fakes:  
 Random ECAL hits from  
 the BIB that can mimic a  
 photon

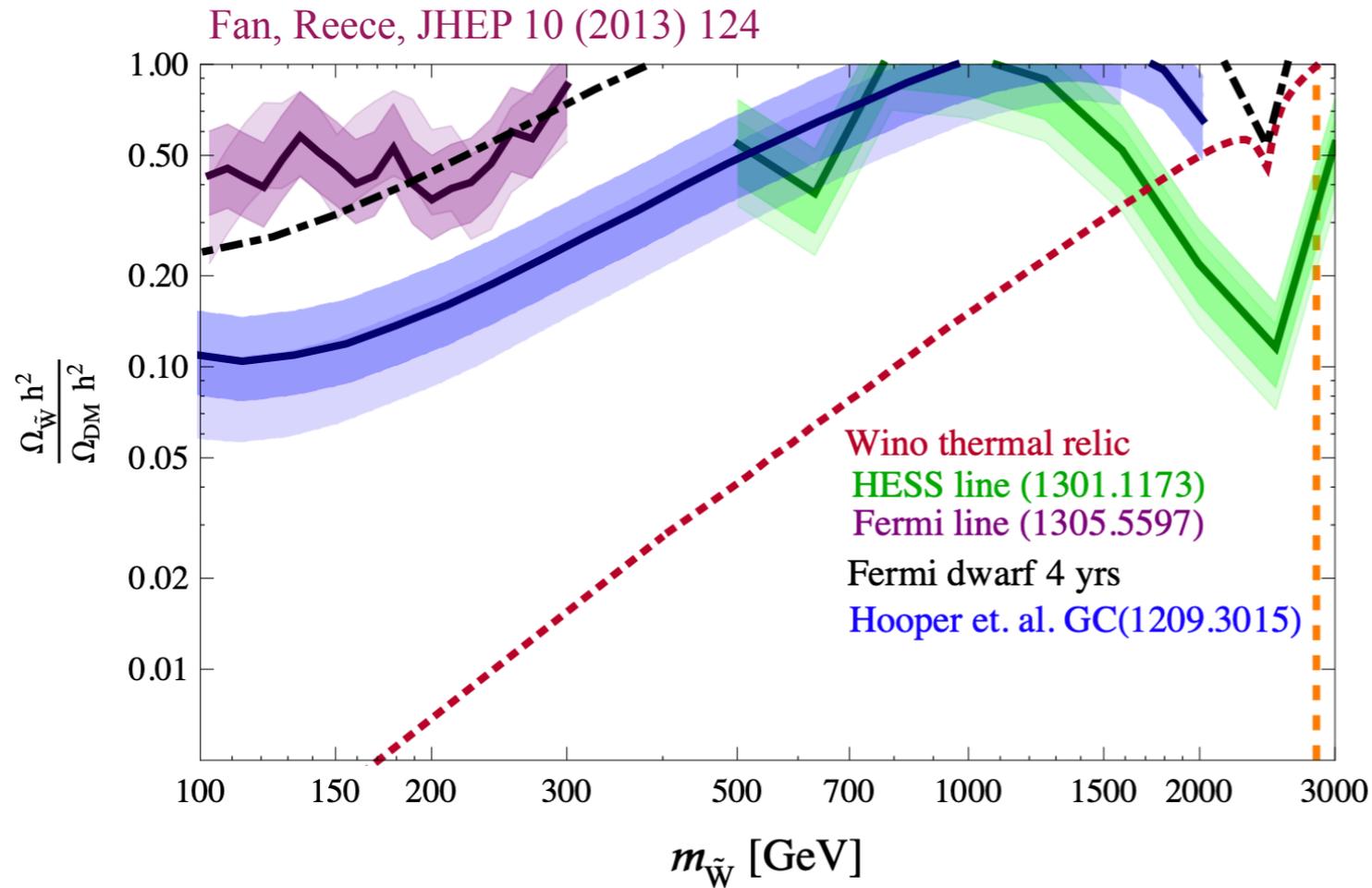
Incoherent pair  
 production via  
 synchrotron

Five sigma for the  
 Thermal Higgsino  
 (Doublet MDM)

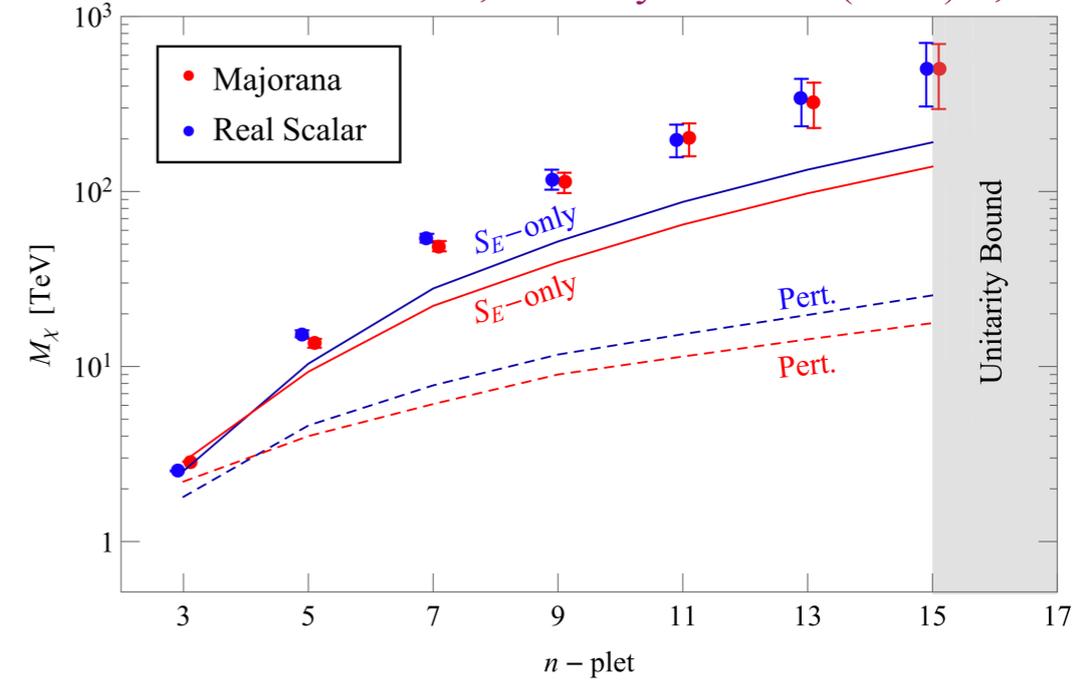
# 4. Results

- The Importance of the 3TeV Collider:

**Not just the Higgsino  
(doublet MDM)**



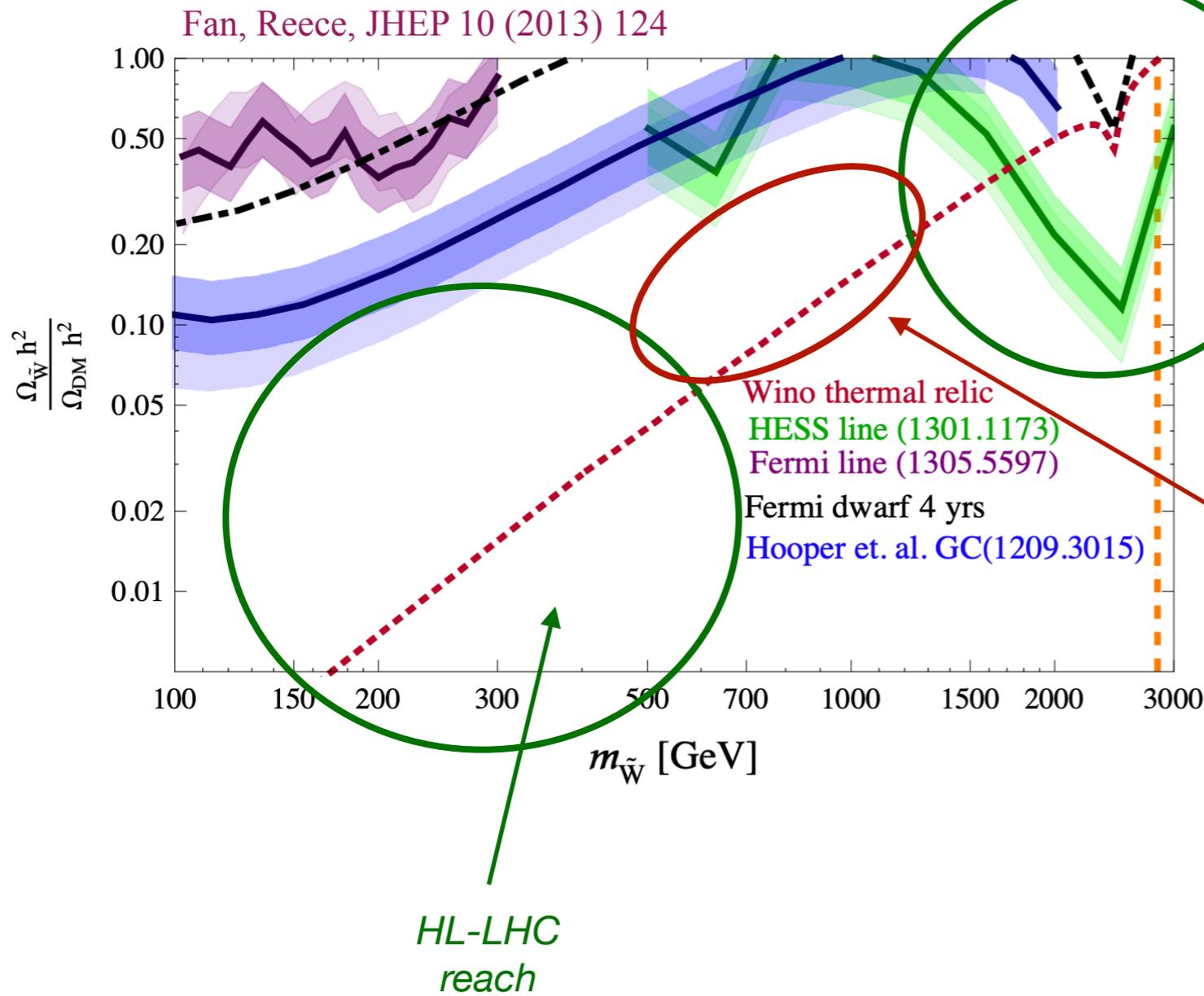
Bottaro et al., Eur. Phys. J. C 82 (2022) 1, 31



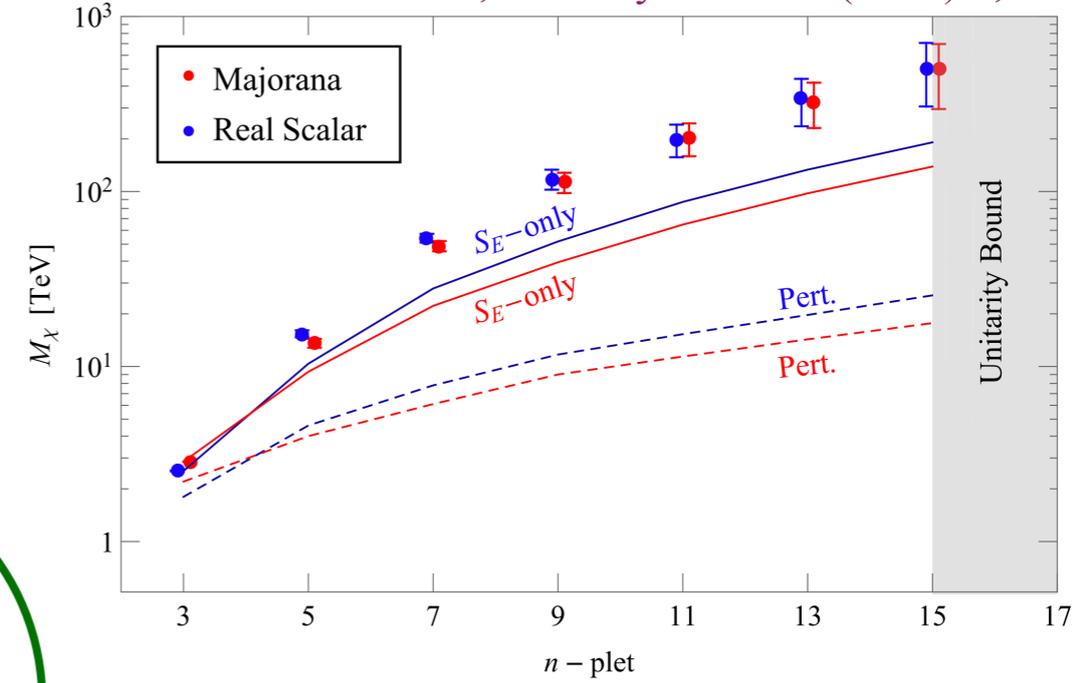
# 4. Results

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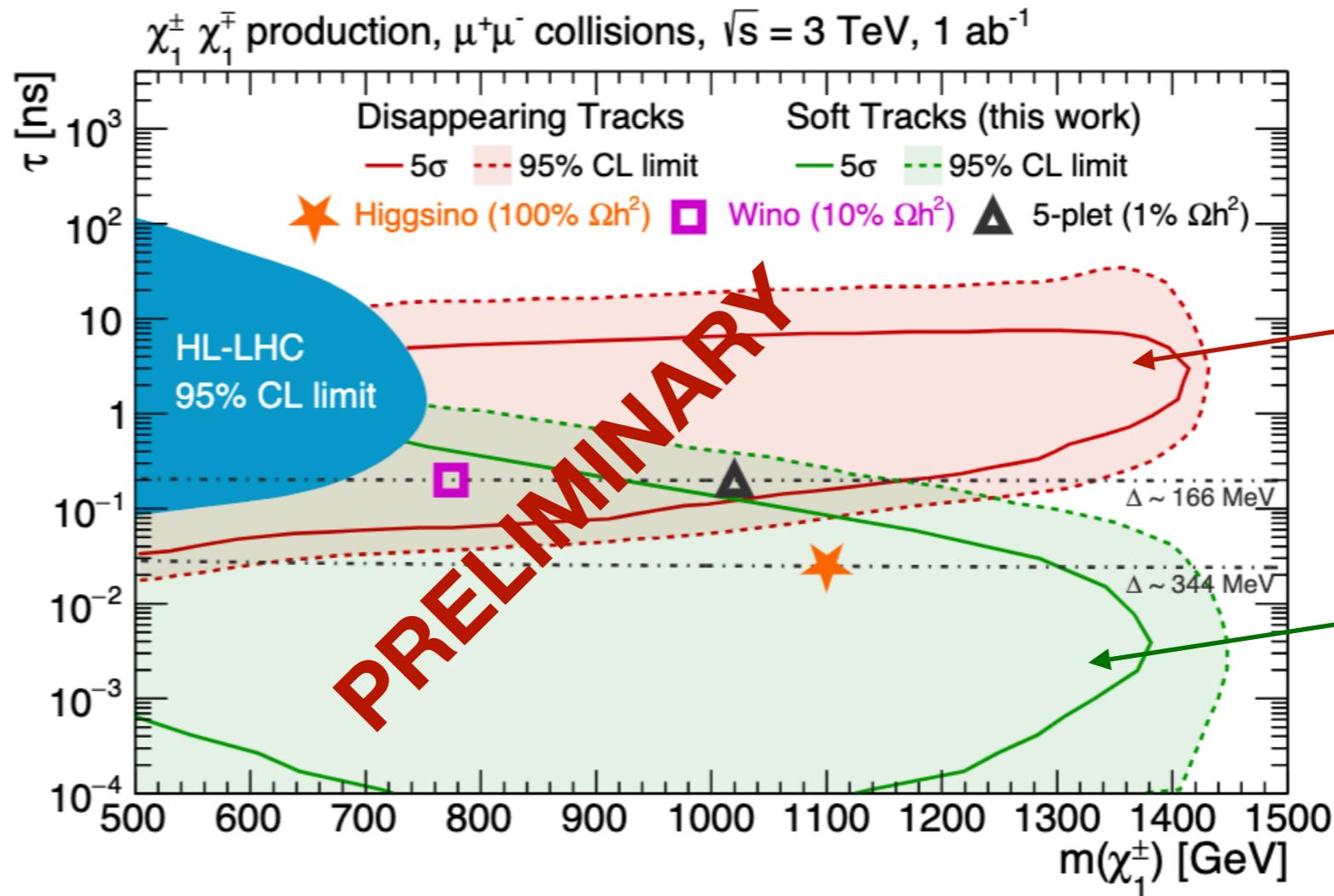
Indirect  
detection  
reach

**MuC?**

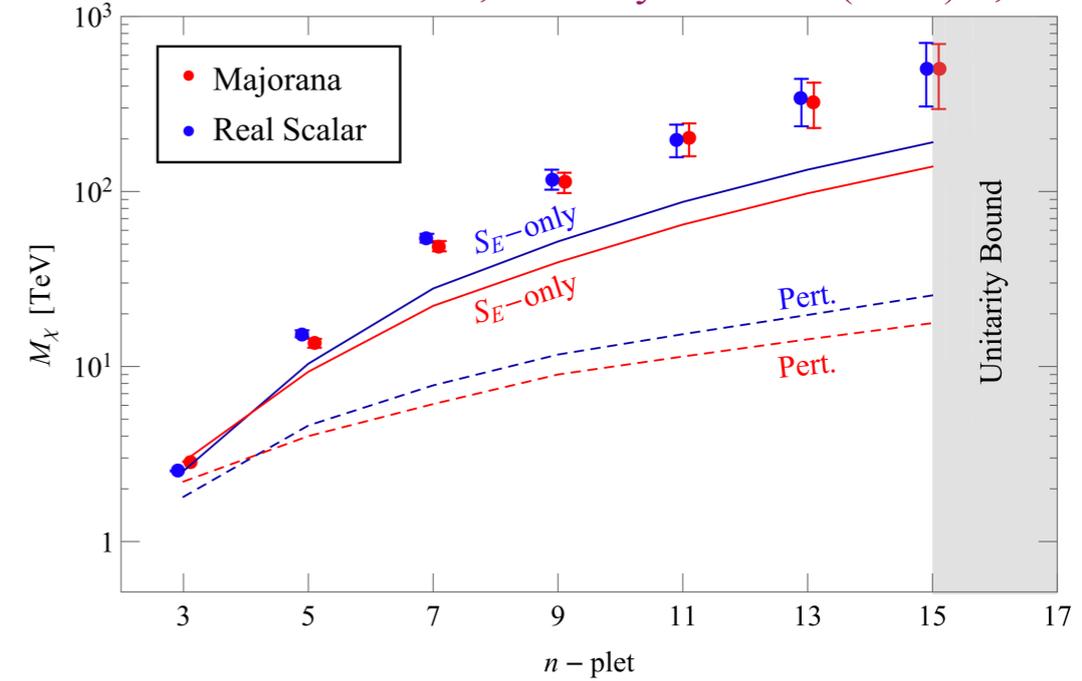
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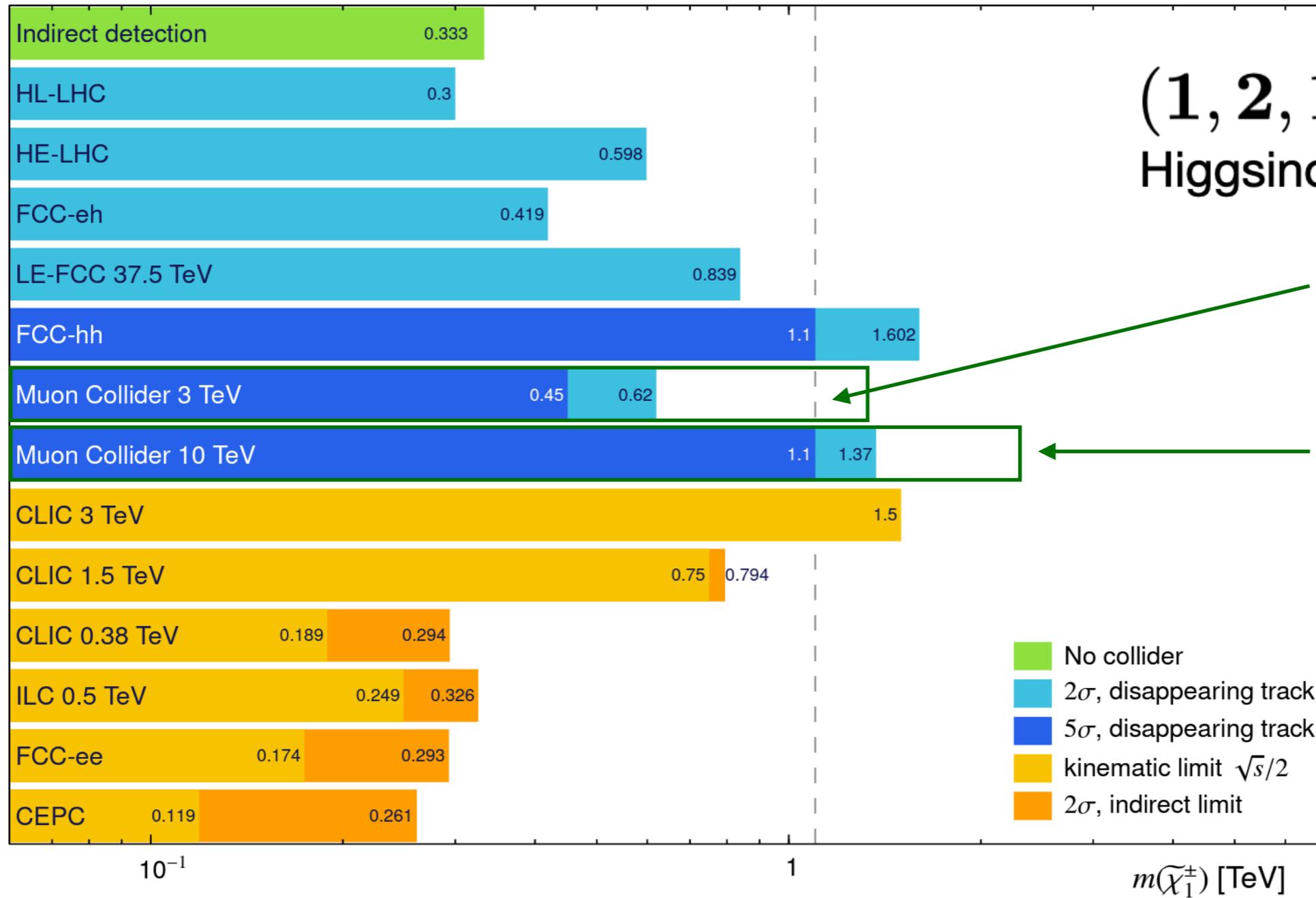


Previous  
result from  
DT

NEW  
result from  
ST

# 4. Results

- Projections:



**(1, 2, 1/2)**  
Higgsino-like

*The thermal target will be discovered!*

*Updated results from Federico Meloni et al. Disappearing Tracks*

# Outline

## 1. Introduction

## 2. Minimal Dark Matter

- Properties
- Projections

## 3. Soft Tracks

- Signal Regions
- Backgrounds

## 4. Results

- The Importance of the 3TeV MuC!

# Summary

1. Minimal Dark Matter models constitute high motivated targets for future colliders. Small multiplets (doublets/triplets) have thermal masses at the reach of foreseeable MuC. Larger multiplets (5-plet and above) that can explain 1-10% of the DM in the Universe also falls into the multi-TeV range that can be discovered at MuC.
2. Soft Track searches will be possible at the Muon Collider. Using this technique **the 3TeV Muon Collider has the potential of discovering the thermal Higgsino-like minimal Dark Matter candidate**. This result suggest that the 3TeV Muon collider is not only a stage to the 10TeV machine but it is also a powerful discovery machine.
3. The Muon Collider program (3 -> 10 TeV) will be able to discover and characterize minimal WIMPs. A combination of Disappearing Track and Soft Track searches will allow us to determine the mass of the thermal relic, as well as the mass gap between this particle and its companion charged state.

*Thank You!*

# Discovering Minimal Dark Matter at Muon Colliders

- Minimal Dark Matter models extend the Standard Model by incorporating a single electroweak multiplet, with its neutral component serving as a candidate for the thermal relic dark matter in the Universe. These models predict TeV-scale particles with sub-GeV mass splittings  $\Delta$ . Collider searches aim at producing the charged member of the electroweak multiplet which then decays into dark matter and a charged particle. Traditionally, these searches involve signatures of missing energy and disappearing tracks. Due to the small size of  $\Delta$ , the transverse momentum of this charged particle is too soft to be resolved at hadron colliders. In this talk, I show that a Muon Collider is capable of detecting these soft charged decay products, providing a means to discover TeV thermal relics with an almost degenerate charged companion. Our technique also facilitates the determination of  $\Delta$ , allowing for a comprehensive characterization of the dark sector. Our results indicate that a 3 TeV muon collider will have the capability to discover the highly motivated thermal Higgsino-like dark matter candidate as well as other scenarios of Minimal Dark Matter featuring larger multiplets whose neutral component corresponds to a fraction of the total dark matter in the Universe. This study highlights the potential of a muon collider to make significant discoveries even at its early stages of operation.