



Optimal anti-ferromagnets for light dark matter detection

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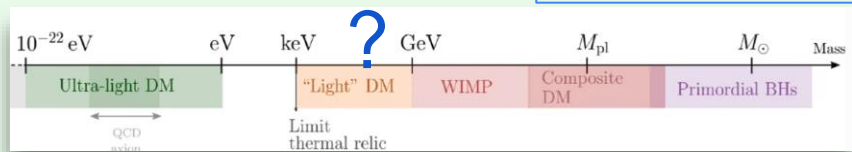
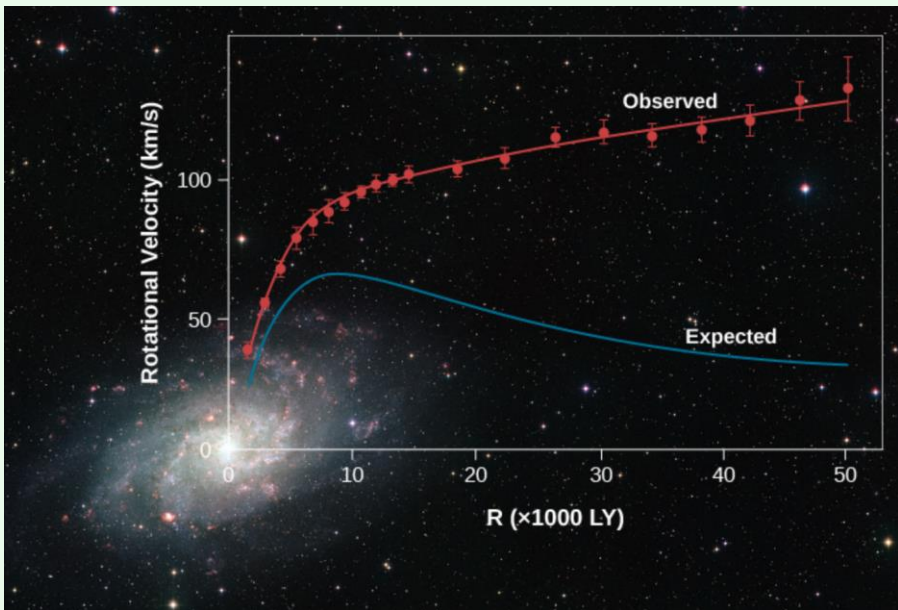
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Based on the work with Angelo Esposito ([arXiv: 2210.13516](https://arxiv.org/abs/2210.13516))

Dark Matter

Accounts for almost 85 % of mass

Spans over wide range of masses \longrightarrow Need variety of detection techniques



- * Primordial black hole mergers
- * Gamma rays from annihilation
- * CMB polarization rotation

- * Conversion in magnetic field
- * Light shining through walls
- * Nuclear spin precession
- * Mechanical sensors

- * Multi-tonne liquid noble elements
- * Bubble chambers
- * Cryogenic calorimeters
- * CCDs

Sub-GeV Dark matter

$$M \sim \text{keV} - \text{GeV} \implies E \sim \text{meV} - \text{keV}$$

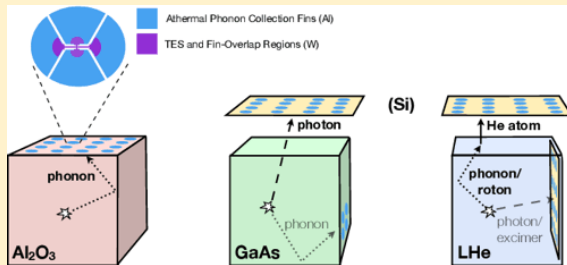
Condensed matter systems provide an ideal platform \implies

- * Semiconductors
- * Narrow-gap materials
- * Organic crystals
- * Superconductors

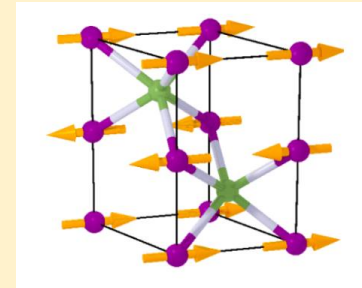
Collective excitations in condensed matter systems $\sim O(\text{meV})$. Ideal for the $O(\text{keV})$ dark matter.

E.g. Phonons in solids, superfluid helium.

Magnons in anti-ferromagnets (This work)



TESSERACT Dark Matter Project



Effective field theory

But many-body physics is hard Multiple scales in the problem !!

EFT ??

Anti-ferromagnets spontaneously break a host of spacetime and internal symmetries → gapless degrees of freedom (magnons).

$$L_{\chi} = \frac{c_6}{2} (\partial_t \chi^a)^2 - \frac{c_7}{2} (\partial_i \chi^a)^2 + \dots$$

Straightforward to include higher dim. Operators, explicit symmetry breaking terms within a well defined power counting scheme.

Why anti-ferromagnets ?

Better reach for spin-dependent interactions.

$$L \supset f(q) \mathbf{S}_{DM} \cdot \delta \boldsymbol{\rho}_s \text{ (magnons) , } f(q) \mathbf{S}_{DM} \cdot \nabla \delta \rho \text{ (phonons)}$$

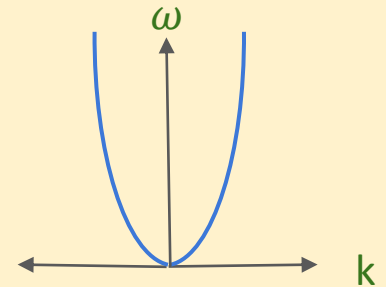
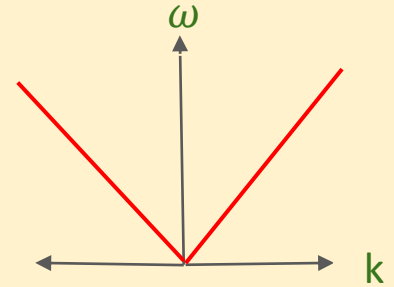
Two Type-I goldstone in anti-ferromagnets : $\omega \sim c k$

$$\text{Max. } \omega \sim 4 E y (1 - y) ; \quad y = \frac{c}{v} \quad \text{optimal } c \sim 0.5 v$$

Single Type-II goldstone in ferromagnets : $\omega \sim \frac{k^2}{2m}$

$$\text{Max. } \omega \sim 4 E \frac{x}{(1+x)^2} ; \quad x = \frac{m}{M} , m \sim O(\text{MeV})$$

Allows multi-magnon emission in anti-ferromagnets.

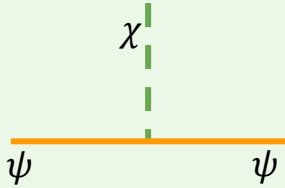


Put everything together...

$$\mathcal{L}_\psi^{\text{m.d.}} = -\frac{4g_\psi g_e}{\Lambda_\psi m_e} \left(\psi_{\text{nr}}^\dagger \frac{\sigma^i}{2} \psi_{\text{nr}} \right) \left(\delta^{ij} - \frac{\nabla^i \nabla^j}{\nabla^2} \right) \left(e_{\text{nr}}^\dagger \frac{\sigma^j}{2} e_{\text{nr}} \right)$$

S^j $\xrightarrow{\text{IR}}$

$$\rho_s^i = c_6 \delta^{ia} \chi^a + c_6 \delta^{i3} \epsilon^{ab} \dot{\chi}^a \chi^b$$

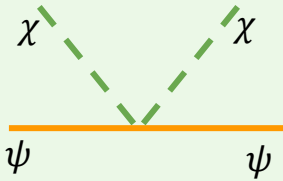


Compute decay rates
 $\Gamma(v_\psi)$



of events per kilogram of year
exposure.

DM velocity distribution



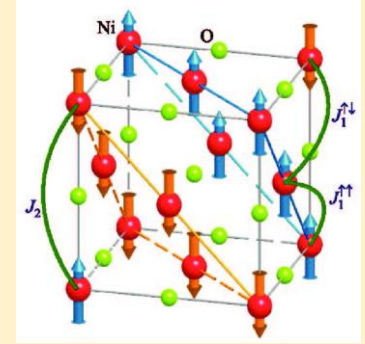
$$R = \frac{\rho_\chi}{\rho_\Gamma m_\chi} \int d^3 v_\chi f(v_\chi) \Gamma(v_\chi)$$

Matching

But c_6 needs to be determined \longrightarrow Use a matching procedure

“UV” theory = Heisenberg model

$$\mathcal{H} = \sum_{ij} J_{ij} \vec{S}_i \cdot \vec{S}_j$$



Neutron scattering cross-section

EFT

$$\frac{d^2\sigma}{d\Omega dE'} = V(\gamma r_0)^2 \frac{k'}{k} c_6 \frac{1 + \hat{q}_z^2}{4} \omega(q) \delta(E' - E - \omega(q))$$

Heisenberg model

$$\left(\frac{d^2\sigma}{d\Omega dE'} \right)^{(\pm)} = r_0^2 \frac{k'}{k} \left\{ \frac{1}{2} g F(\mathbf{\kappa}) \right\}^2 \frac{1}{4} (1 + \tilde{\kappa}_z^2) \exp\{-2W(\mathbf{\kappa})\} \frac{(2\pi)^3}{Nv_0}$$

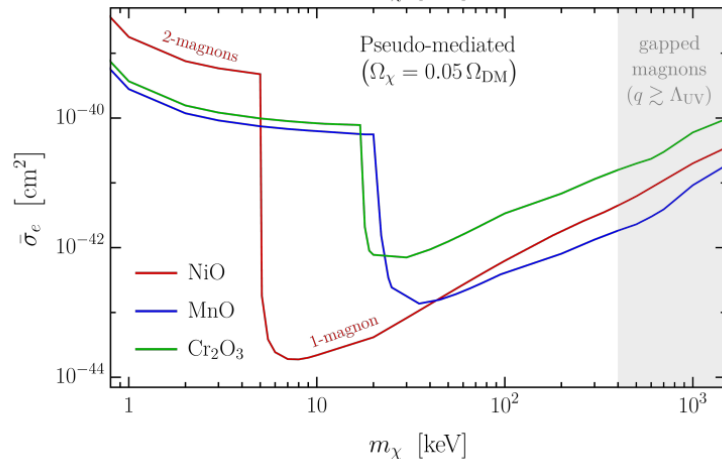
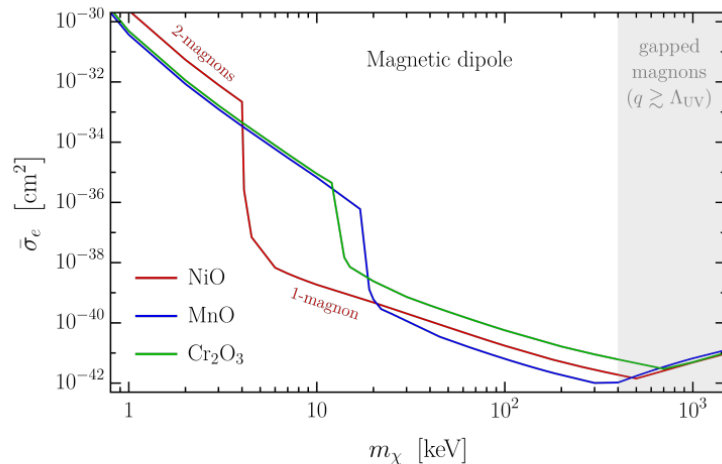
$$\times \sum_{a \sim 0,1} \sum_{\mathbf{q}, \boldsymbol{\tau}} (n_{\mathbf{q},a} + \frac{1}{2} \pm \frac{1}{2}) \delta(\hbar\omega_{\mathbf{q},a} \mp \hbar\omega) \delta(\mathbf{\kappa} \mp \mathbf{q} - \boldsymbol{\tau}) \{u_{\mathbf{q}}^2 + v_{\mathbf{q}}^2 + 2u_{\mathbf{q}}v_{\mathbf{q}} \cos \boldsymbol{\rho} \cdot \boldsymbol{\tau}\}.$$

Cross-Section

Compute the DM-electron cross section σ_e .

For NiO, $c \sim v$ and therefore has the best mass reach ($O(\text{keV})$) for single magnon.

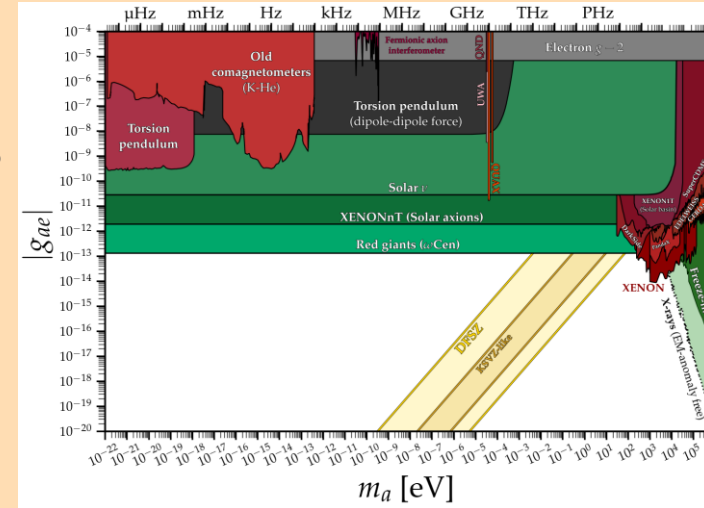
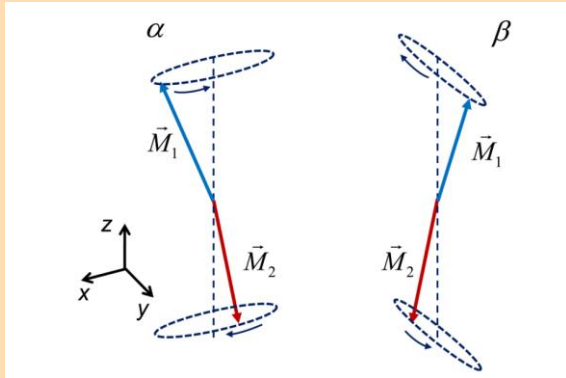
Two magnon rates have $O(\text{keV})$ reach for all cases.



Axions

Can also hunt for axion and axion like particles via the electron coupling $L \supset \frac{g_{aee}}{f_a} \vec{\nabla} a \cdot \vec{S}_e$

$\omega \sim m_a, k \sim m_a v_a \ll m_a \implies$ couples to the zero modes of the antiferromagnet \sim THz resonance



Reproduced from <https://cajohare.github.io/AxionLimits/docs/ae.html>

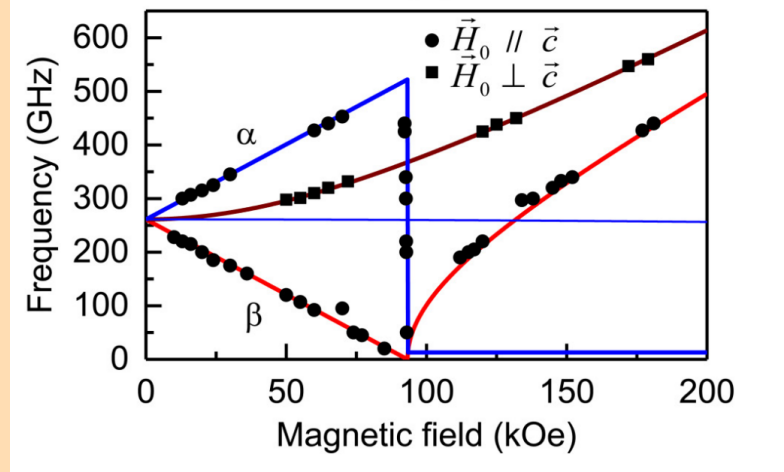
Include effects of anisotropy \longrightarrow gapped magnons. Can be tuned using a B field.

$$\mathcal{L}_{AFM}^{(2)} = \frac{c_6}{2} \dot{\chi}^a \dot{\chi}^a - \frac{c_2}{2} \partial_i \chi^a \partial^i \chi^a - \frac{c_3}{2} \chi^a \chi^a + c_6 \mu B_3 \epsilon_{ab} \chi^a \dot{\chi}^b$$

Two gapped modes with linear B dependence.

$$\omega_{\pm} = \frac{c_3}{c_6} \pm \mu B$$

Compute rates for exciting a single mode. Can be used to constrain g_{aee} beyond astrophysical limits for long lived magnons.

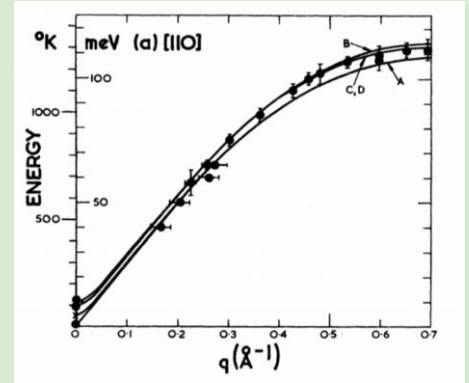


Conclusions

- Anti-ferromagnets can probe spin-dependent interactions down to $O(\text{keV})$ masses.
- Allow for multi-magnon emission which can be utilized as background discrimination.
- Can also be utilized to look axions and axion like particles.
- EFT's provide an effective and simple computational tool in a complicated many body setting.

“Light” Dark Matter

- Typical magnon energies ~ 1-100 meV



Start with some well-motivated UV models ; Interactions mediated by a scalar or vector ;

Magnetic dipole DM

$$\longrightarrow \mathcal{L}_\psi^{\text{m.d.}} = \frac{g_\psi}{\Lambda_\psi} V_{\mu\nu} \bar{\psi} \sigma^{\mu\nu} \psi + g_e V_\mu \bar{e} \gamma^\mu e$$

Pseudo-mediated DM

$$\longrightarrow \mathcal{L}_\chi^{\text{p.m.}} = g_\psi \phi \bar{\psi} \psi + g_e \phi i \bar{e} \gamma^5 e$$