

Freeze-in Cogenesis of Asymmetric Dark Matter

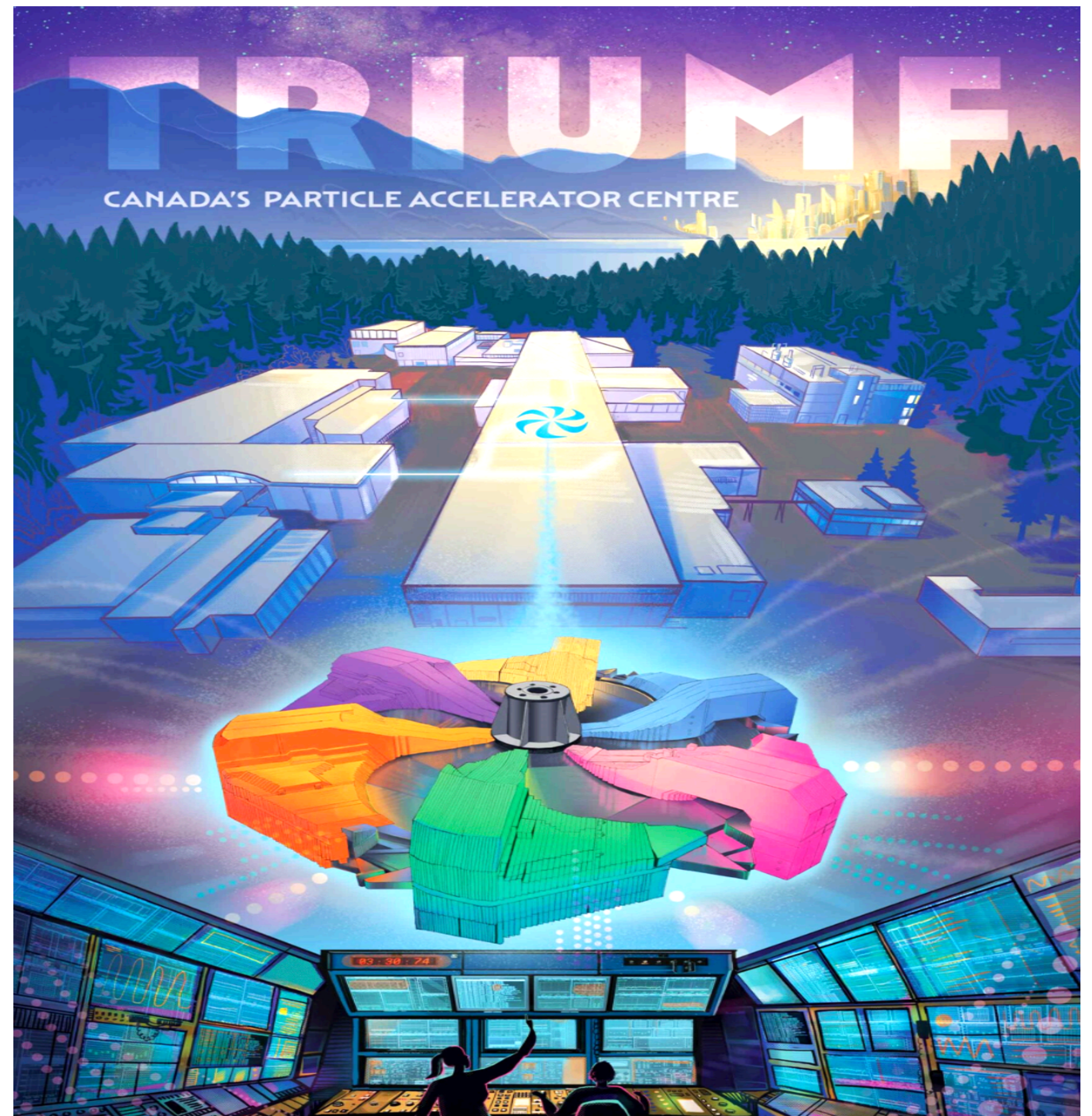
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Asymmetric Dark Matter

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Zurek, Phys. Rep. 2013; Petraki & Volkas Int. J. Mod.

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Sharing

vs.

Cogenesis



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Asymmetry is produced in dark or visible sector then transferred to other sector

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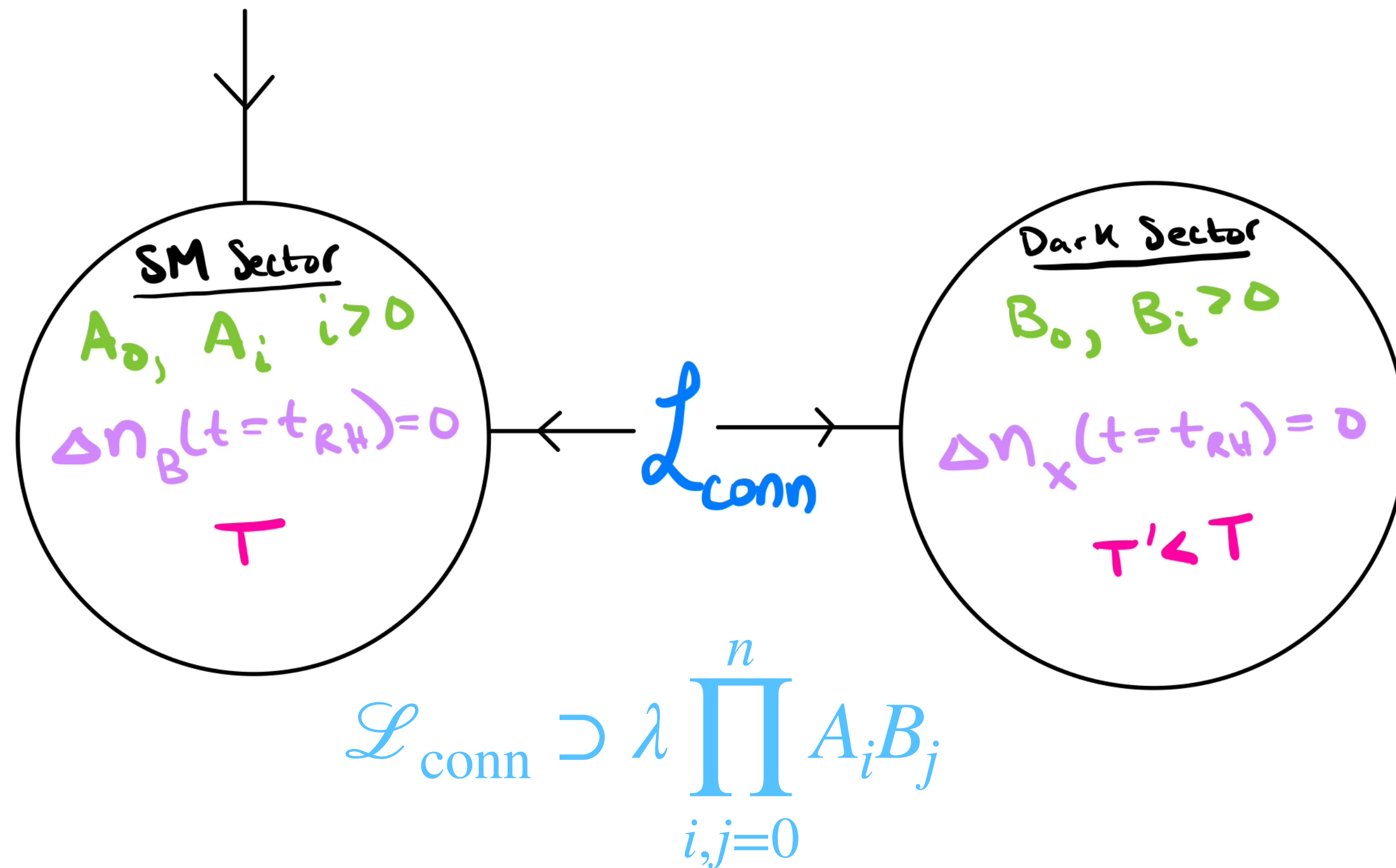
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ADM = Baryogenesis+Dark Matter

Asymmetric Freeze-in?

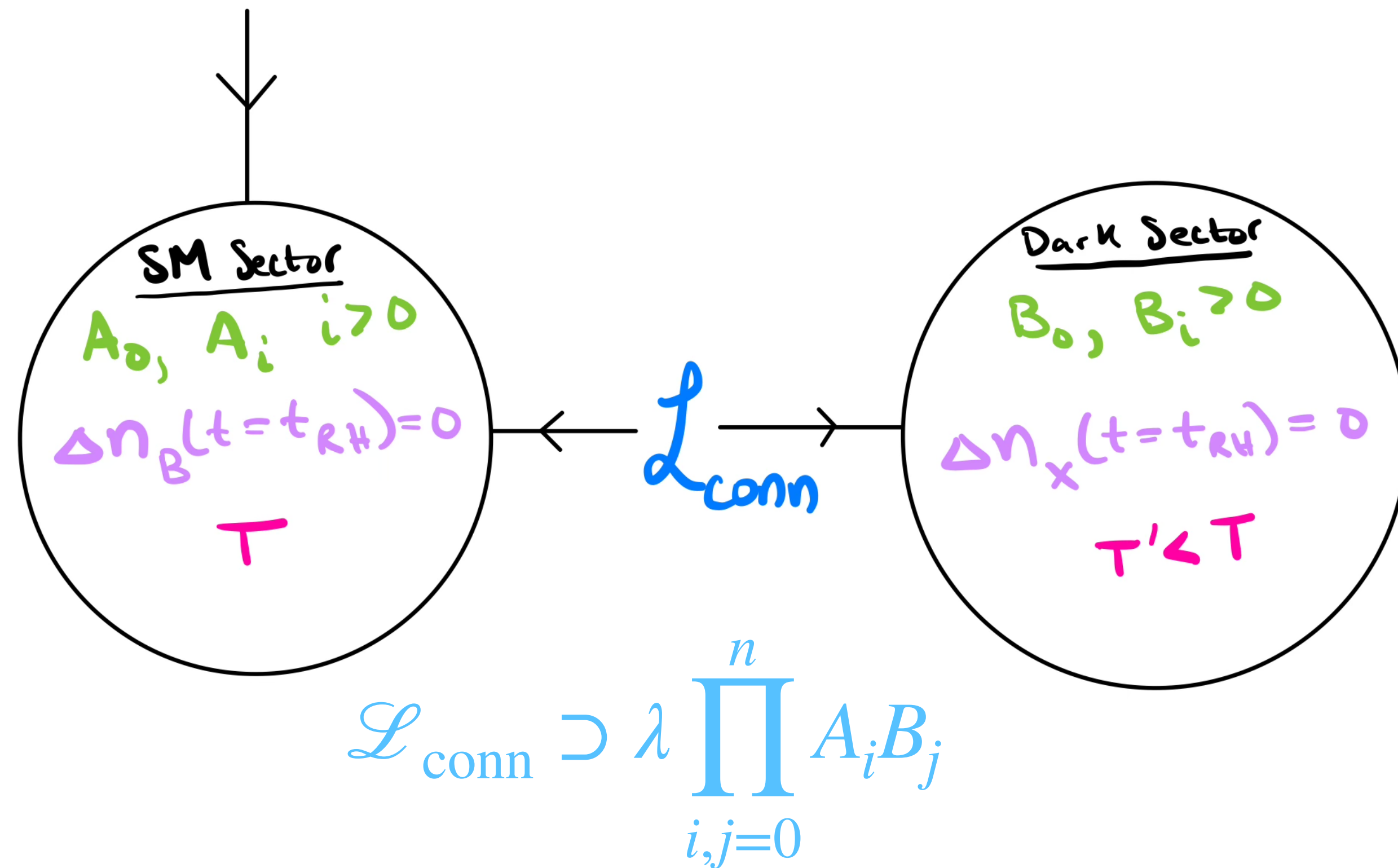
Asymmetric Freeze-in?

Reheating



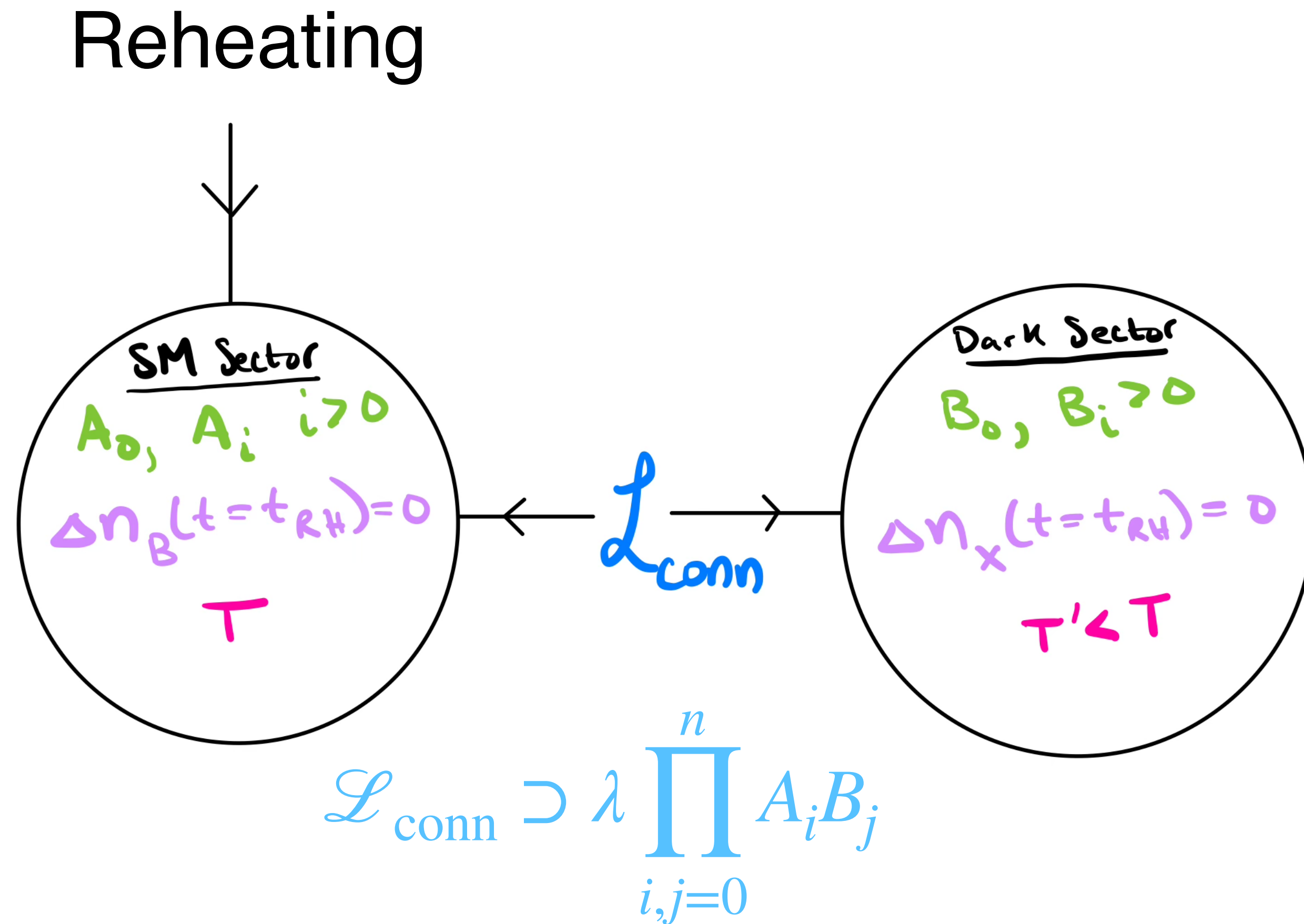
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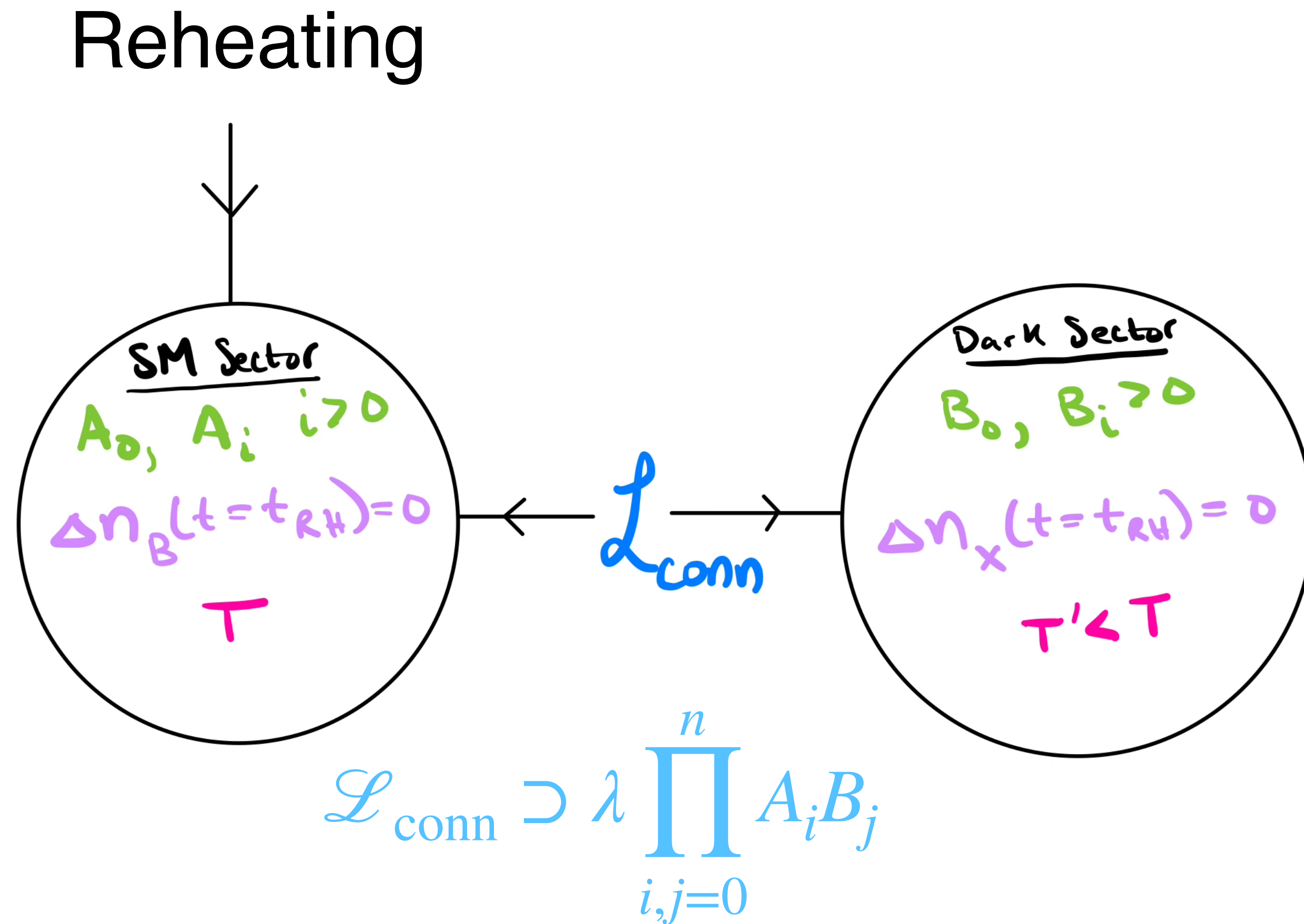


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Small λ ensures the sectors do not equilibrate with one another

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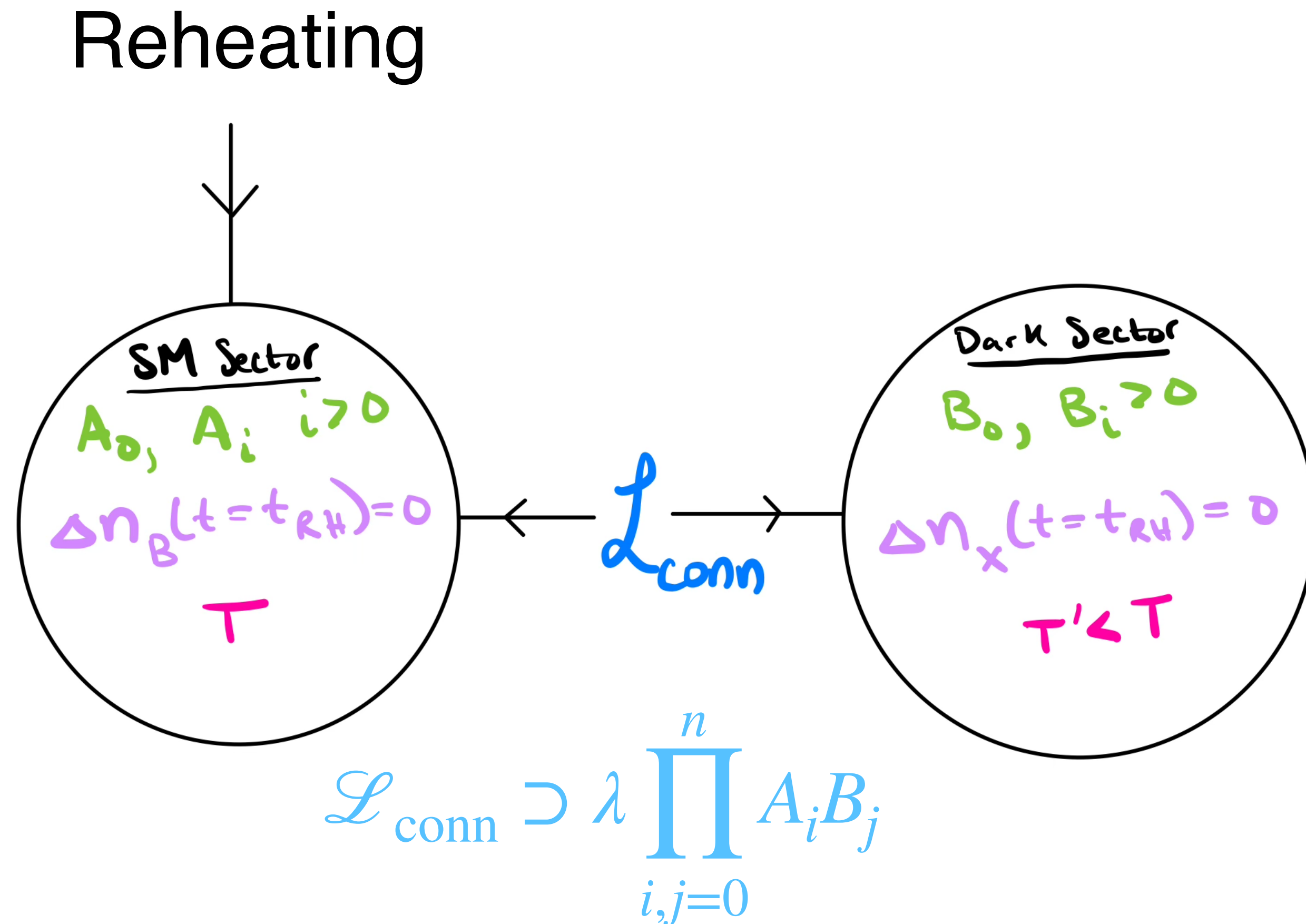
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[Hall, March-Russell, West \[1010.0245\]](#)

$\lambda \ll 1 \implies$ depleting the symmetric component difficult

$\mathcal{L}_{\text{conn}}$ transforms under $B - L$ and X but if total is conserved, CPT and Unitarity require asymmetries vanish at leading

order in λ [Hook \[1105.3728\]](#); [Unwin \[1406.3027\]](#); [Baltes, et. al. \[1407.4566\]](#);

Unitarity and CPT

Unitarity \implies

$$\sum_f |\mathcal{M}(i \rightarrow f)|^2 = \sum_f |\mathcal{M}(f \rightarrow i)|^2$$

[Hook \[1105.3728\]](#); [Unwin \[1406.3027\]](#); [Baltes, et. al. \[1407.4566\]](#);

Equilibrium $\implies f_{i_1} \cdots f_{i_n} = f_{f_1} \cdots f_{f_m}$

Example: LHN (single flavor)

Unitarity $\implies |\mathcal{M}(LH \rightarrow \bar{L}H^\dagger)|^2 - |\mathcal{M}(\bar{L}H^\dagger \rightarrow LH)|^2 = 0$

Equilibrium $\implies f_L f_H = f_{\bar{L}} f_{H^\dagger}$

To violate CP and produce asymmetry, need: more on-shell states+departure from equilibrium

Additional States and Interactions

NLO in λ : CP can be violated if there are additional processes with differing particle number!

Model:

$$\mathcal{L} = -y_i \bar{L} \tilde{H} P_R N_i - \lambda_i \bar{\chi} \phi P_R N_i - \frac{1}{2} m_i \bar{N}_i^c N_i + \text{h.c.}, \quad i = 1, 2$$

Field Content:

SM Fields: LH lepton L , Higgs doublet H

SM singlets: Majorana N_i , Dirac χ , complex scalar ϕ

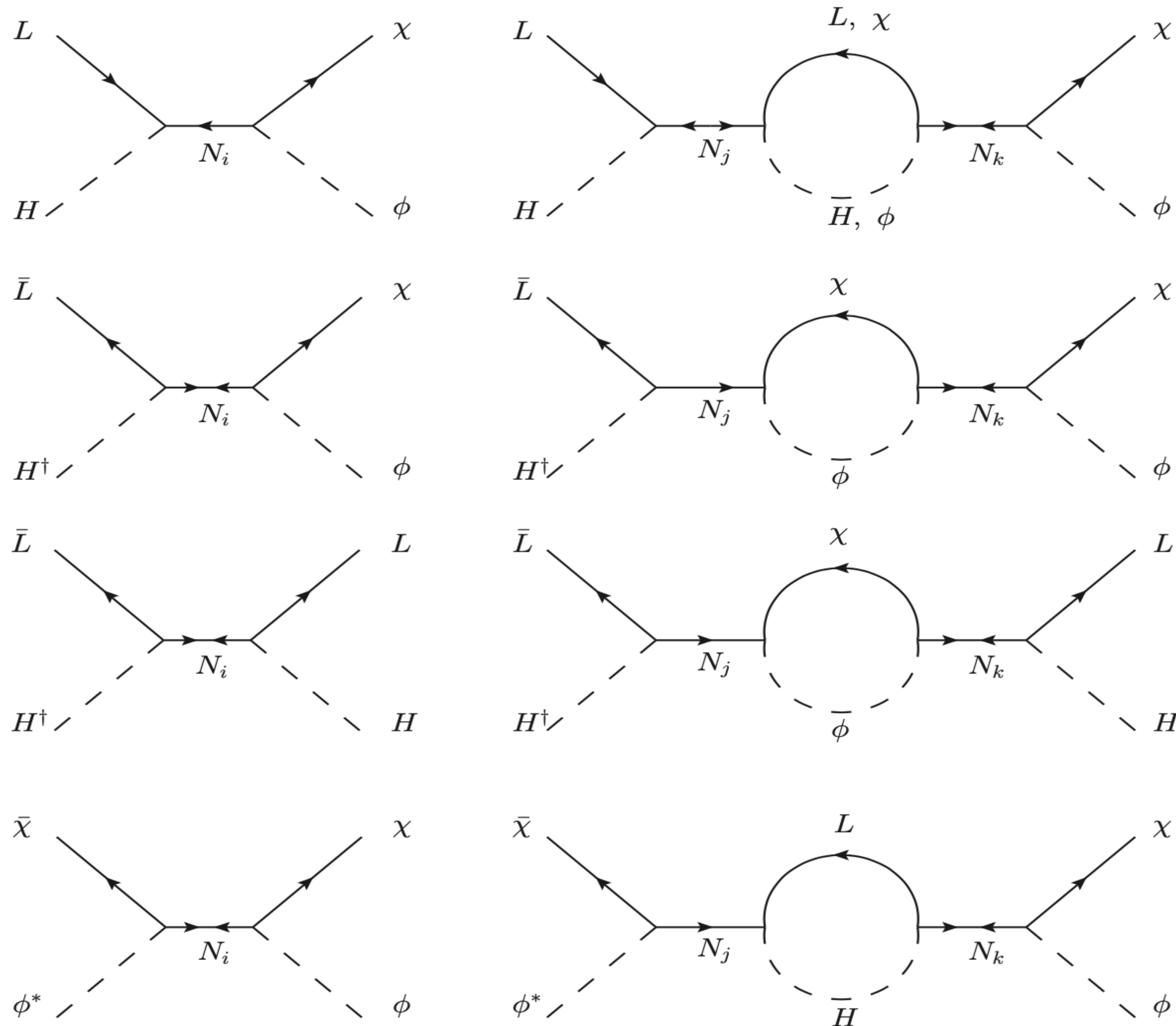
Lepton Number: $L_\phi = -(1 - L_\chi)$

Cosmology:

Assume the universe reheats to SM only and $m_{N_i} \gg T_{\text{RH}} > m_\chi, m_\phi \dots$ N_i never produced on-shell (Dirac ν version see [Blažek, et. al. \[2404.16934\]](#))

With $m_\phi > m_\chi$, dark hypercharge ensures χ is stable... DM?

Freeze-in Asymmetries



UV Freeze-in: Dark sector frozen in and establishes (minimum) dark temperature

$$\xi_\chi \equiv T_\chi/T \neq 1$$

CP Violation: CP Asymmetries ensured through the introduction of χ , ϕ and m_N

χ, ϕ sector out of equilibrium \implies
 $f_L f_H \neq f_\chi f_\phi$

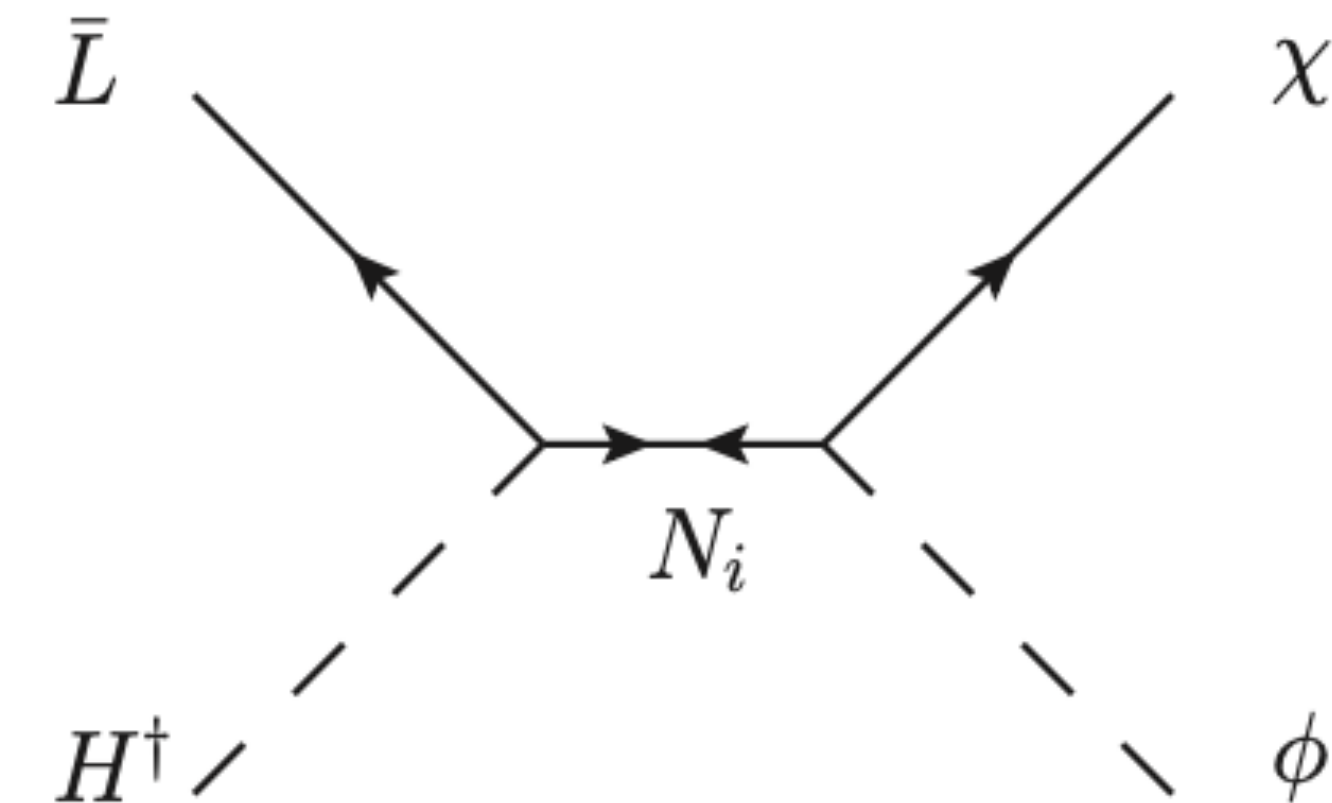
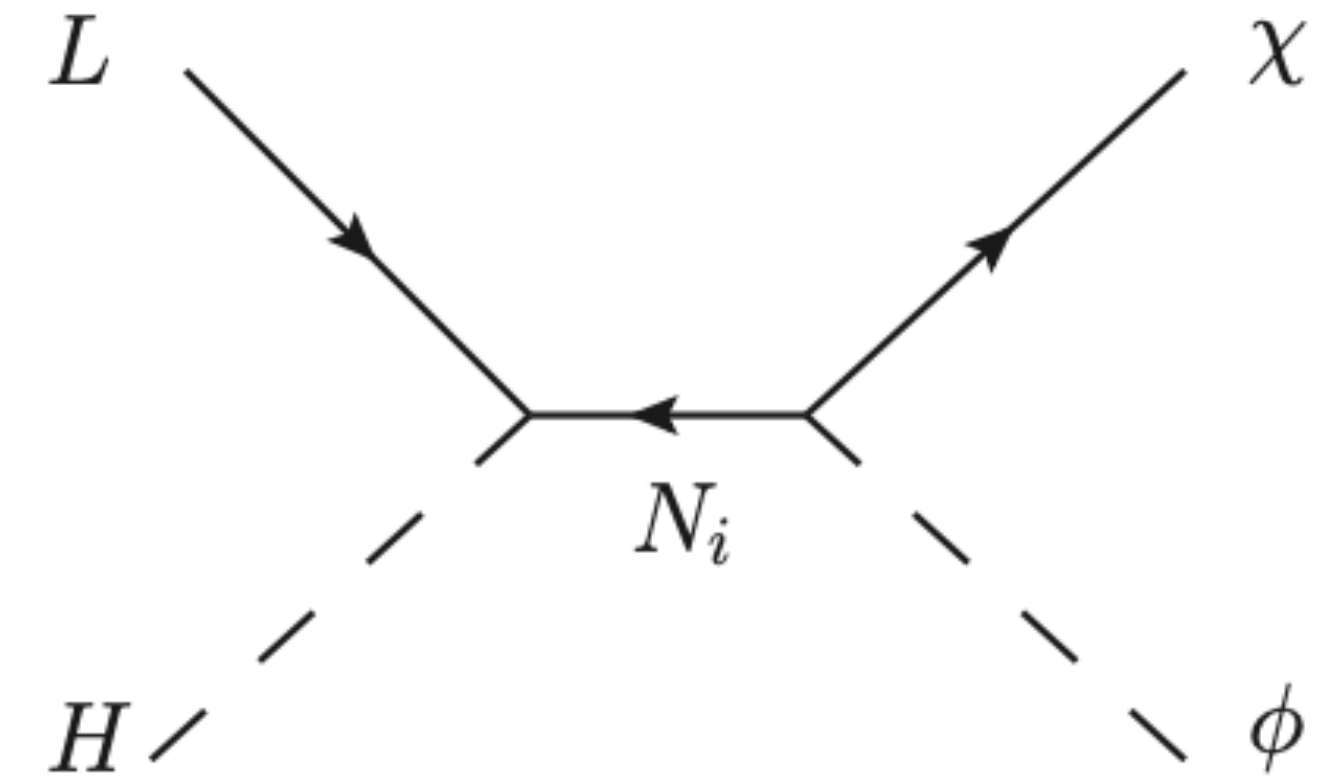
Net asymmetry can be produced!

Energy Transfer

Energy Transfer: Processes such as $LH \rightarrow \chi\phi$ transfer energy into dark sector, establish $T_\chi \dots$

$$\xi_\chi^3 \frac{d\xi_\chi}{dT} = - \frac{150 m_{\text{Pl}} \sigma_0}{1.66 g_*^{1/2} (2\pi)^5} \left[(1 - \xi_\chi^7) F_1(m_i, y_i, \lambda_i) + \frac{35 T^2}{4 m_1^2} (1 - \xi_\chi^9) F_2(m_i, y_i, \lambda_i) \right]$$

Sakharov conditions require $T_\chi \neq T$ for non-vanishing asymmetries to arise

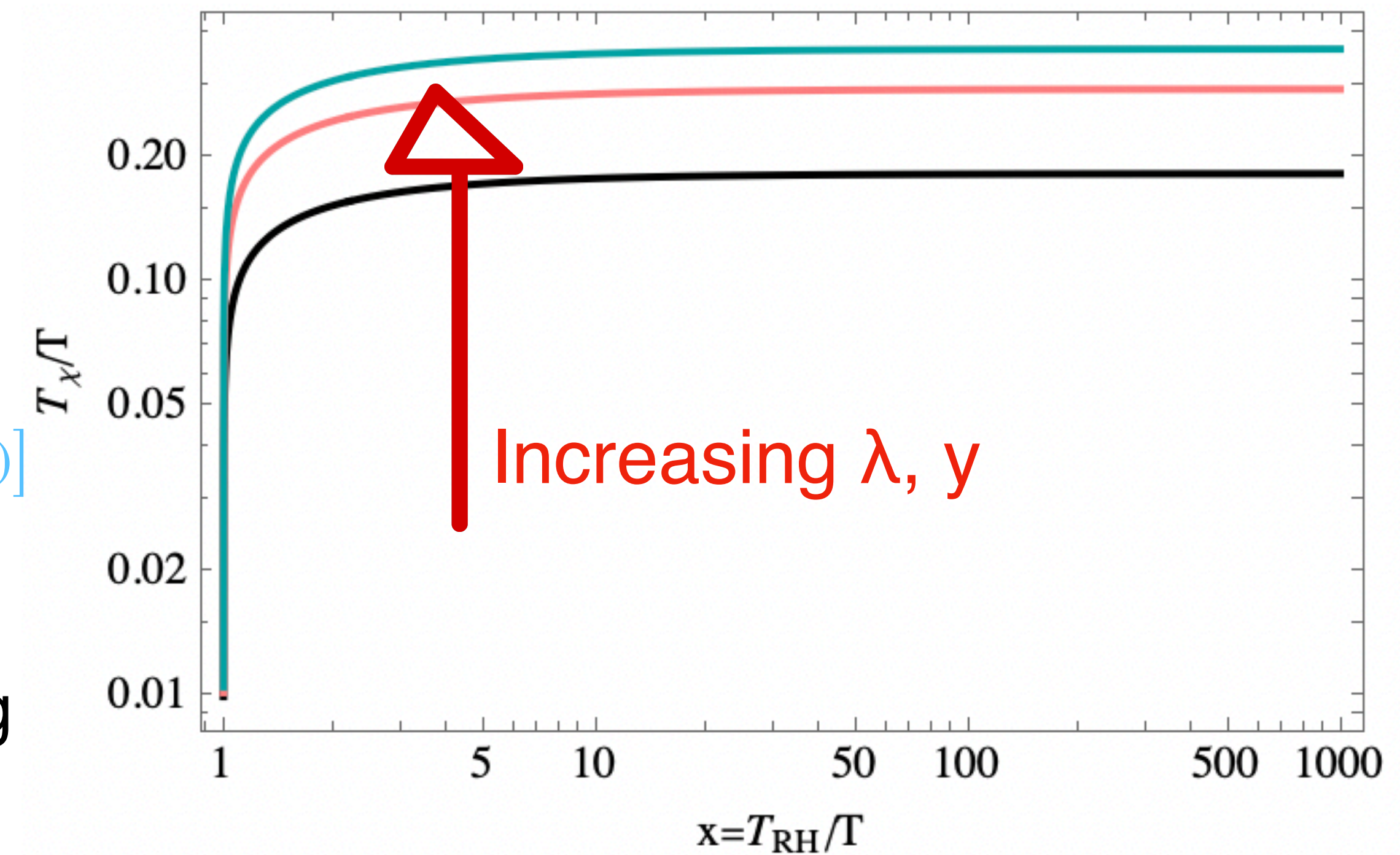


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Freeze-in Cogenesis of Heavy ADM

Asymmetry Generation: Determined by asymmetries $\epsilon_{L,\chi}$ in scattering processes, mediated by $N_{1,2}$

$$\frac{d\Delta Y_L}{dx} \propto (1 - \xi_\chi^8) \epsilon_L x^{-4}, \quad \frac{d\Delta Y_\chi}{dx} \propto (1 - \xi_\chi^8) \epsilon_\chi x^{-4}$$

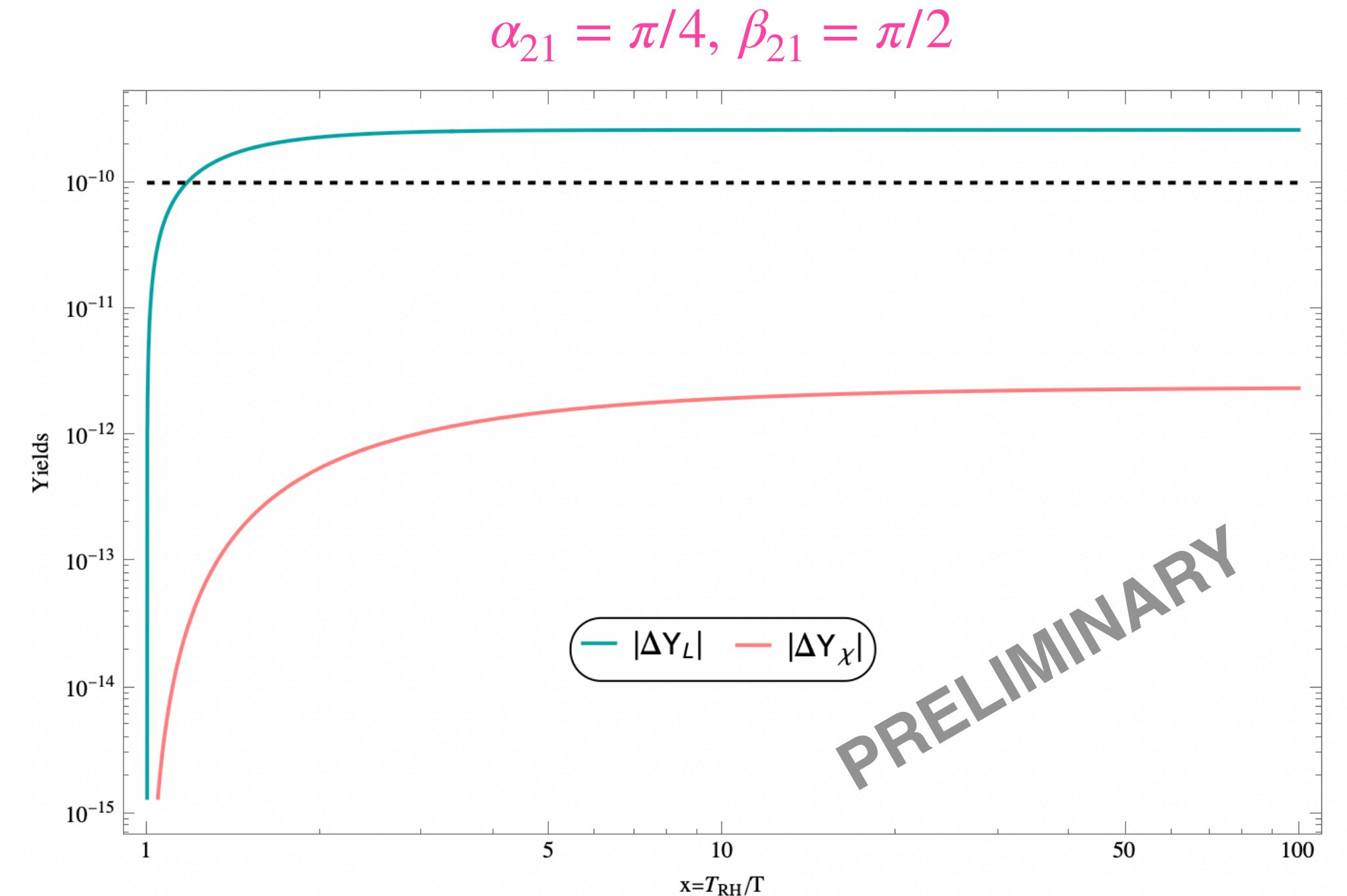
+ **Wash-out** and **Wash-in** Terms

ADM mass: fixed by the asymmetries

Sphalerons convert lepton asymmetry to baryon asymmetry

$$\Delta Y_B = c_s \Delta Y_L \implies \Omega_{ADM} / \Omega_B = c_s^{-1} (Y_{ADM} / \Delta Y_L) (m_\chi / m_p) \implies$$

$$m_\chi \approx 5 c_s (\Delta Y_L / \Delta Y_\chi) m_p \approx 200 \text{ GeV}$$



$$m_1 = 4 \times 10^3 \text{ TeV}, m_2 = 15 \times 10^3 \text{ TeV}, T_{RH} = 50 \text{ TeV}$$

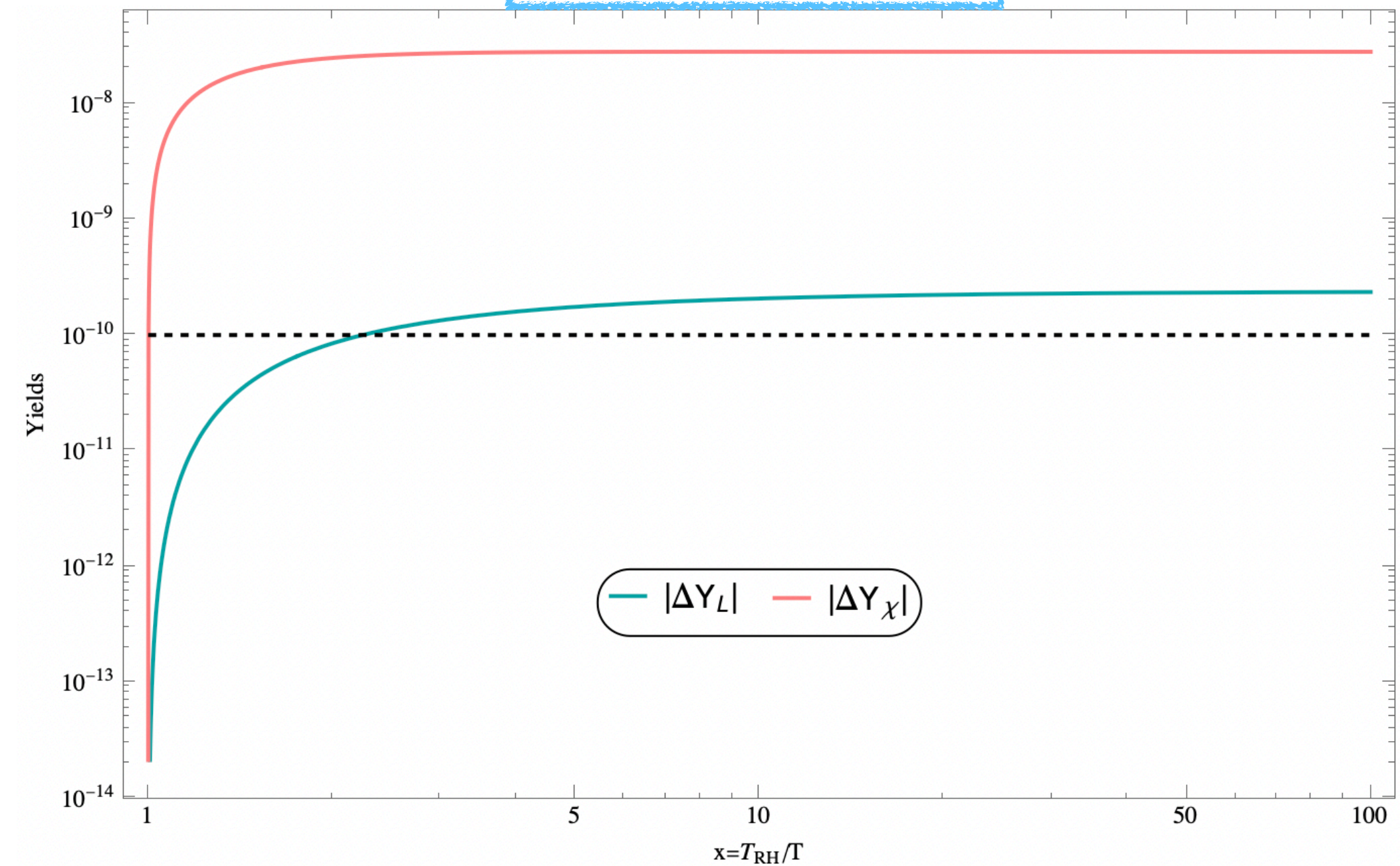
Freeze-in Cogenesis of ~~Heavy~~ ADM

Asymmetry Generation: Completely determined by asymmetries $\epsilon_{L,\chi}$ in scattering processes, mediated by $N_{1,2}$

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Stronger phase in **visible** or **dark** sector!

$$\alpha_{21} = \pi/2, \beta_{21} = \pi/4$$



$$m_1 = 4 \times 10^3 \text{ TeV}, m_2 = 15 \times 10^3 \text{ TeV}, T_{\text{RH}} = 50 \text{ TeV}$$

ADM mass: Leads to larger asymmetry in respective sector

$$m_\chi \approx 5c_s(\Delta Y_L/\Delta Y_\chi)m_p \approx 15 \text{ MeV}$$

Symmetric Component?

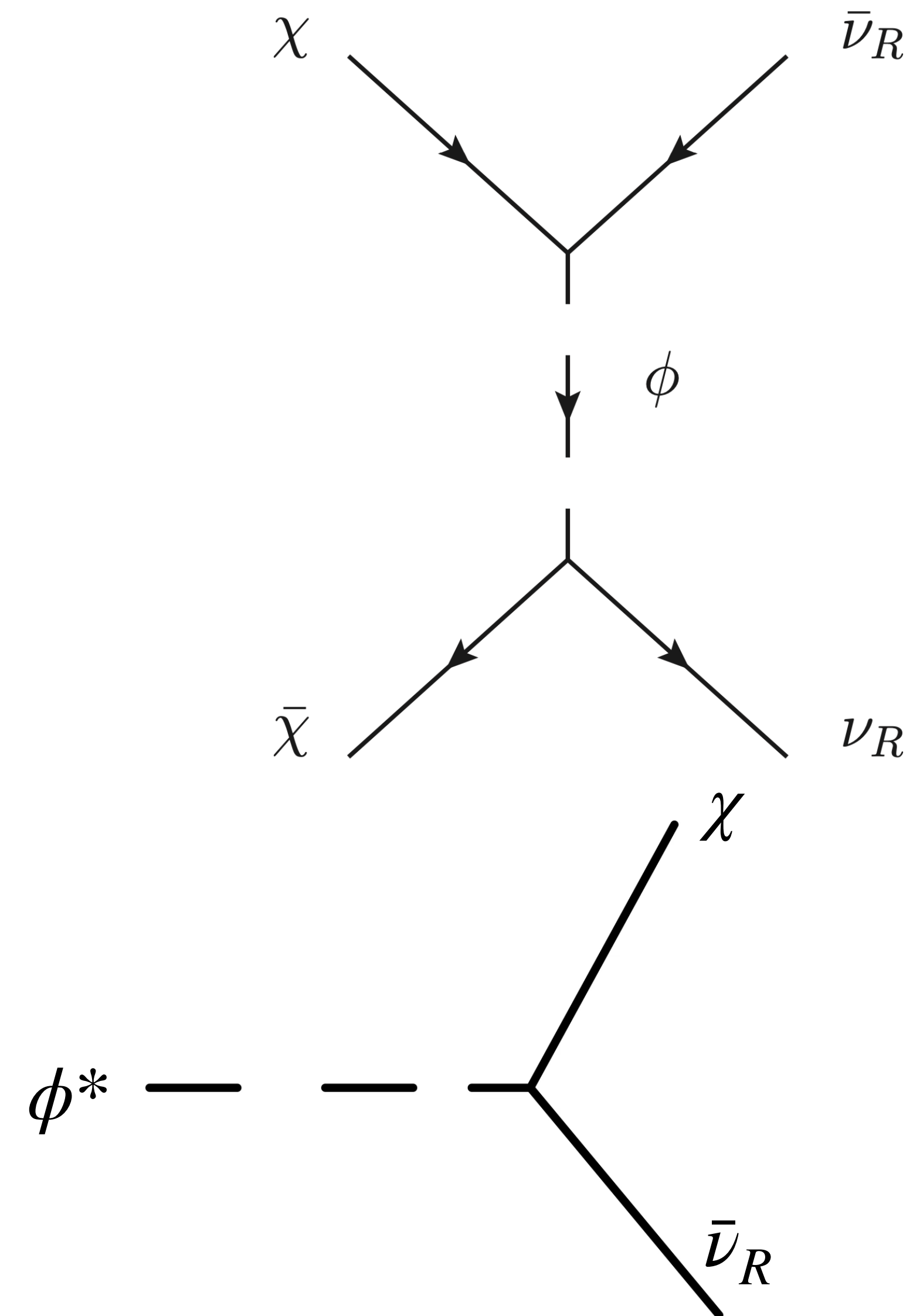
Symmetric Component: A large symmetric component is also frozen in at tree-level

$$\frac{d\Sigma Y_\chi}{dx} \propto (1 - \xi_\chi^8) \sigma(LH \rightarrow \chi\phi) x^{-4} + (1 - \xi_\chi^6) \sigma(\bar{L}H^\dagger \rightarrow \chi\phi) x^{-2}$$

Depletion: Transfer symmetric component into a dark sink
[Bhattiprolu et. al. \[2312.43152\]](#)

Introduce a single flavor of RH Dirac neutrinos

$$\mathcal{L} = -\kappa \bar{\chi} \phi \nu_R + \text{h.c.}$$



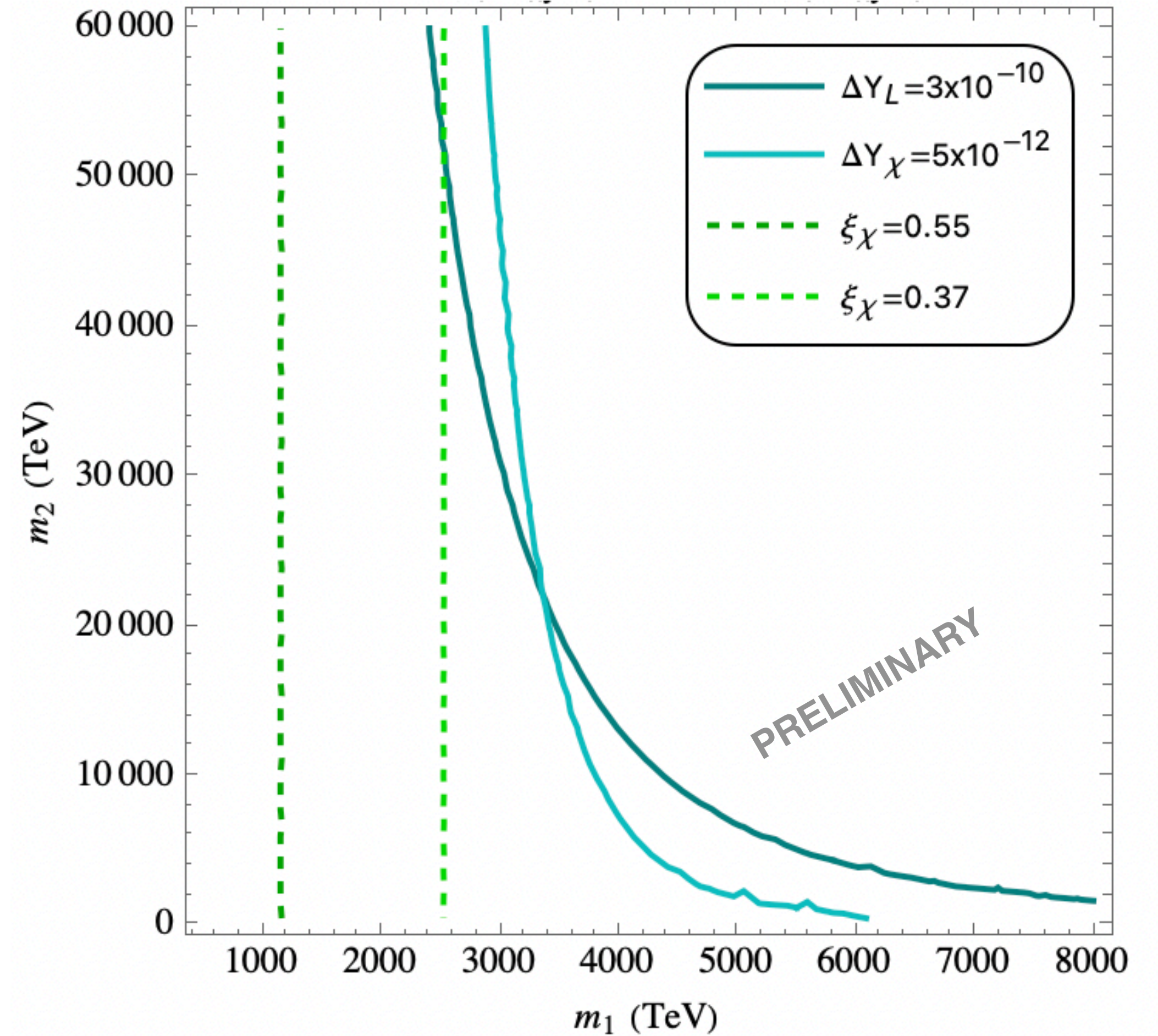
Thermalization and N_{eff}

Thermalization: Light ν_R provides thermal bath which ensures the dark sector remains in thermal equilibrium with T_χ

\implies Constraints on ξ_χ from $\Delta N_{\text{eff}} = \rho_{\nu_R}/\rho_\nu < 0.3$

$$\implies \xi_{\chi,i} \lesssim 0.67 \times \left[\frac{g_{*S}^\chi(T_i) g_{*S}(T_f)}{g_{*S}^\chi(T_f) g_{*S}(T_i)} \right]^{-1/3}$$

$$\Delta N_{\text{eff}} = \rho_{\nu_R}/\rho_\nu < 0.06 \implies \xi_{\chi,i} \lesssim 0.45 \times \left[\frac{g_{*S}^\chi(T_i) g_{*S}(T_f)}{g_{*S}^\chi(T_f) g_{*S}(T_i)} \right]^{-1/3}$$



Takeaways

Theoretical constraints with freezing-in asymmetric dark matter: **no CPV**

Caveat: particle number violation permits CP Violation even with (separately) equilibrated dark sector

Can freeze-in sufficient lepton and dark asymmetry via scattering when $T_{\text{RH}} < m_N$

Phase dependence allows both $\Delta Y_L \gg \Delta Y_\chi$, $\Delta Y_L \ll \Delta Y_\chi$ and $m_{\text{ADM}} \gg m_p$,

$m_{\text{ADM}} \ll m_p$

Future work: Neutrino masses? Generalize the model, direct baryogenesis?

Thank You!

Backup

Unitarity and CPT

Unitarity \implies

$$\sum_f |\mathcal{M}(i \rightarrow f)|^2 = \sum_f |\mathcal{M}(f \rightarrow i)|^2$$

Hook [1105.3728]; Unwin [1406.3027]; Baldes, et. al. [1407.4566];

Collision terms \implies

$$\mathcal{C} = \sum_f \int \dots \int d\Pi_{i_1} \dots d\Pi_{i_n} d\Pi_{f_1} \dots d\Pi_{f_m} \delta^4 \left(\sum_{i=1}^n p_i - \sum_{j=1}^m p_j \right) (2\pi)^4 \{ f_{i_1} \dots f_{i_n} |\mathcal{M}(i \rightarrow f)|^2 - f_{f_1} \dots f_{f_m} |\mathcal{M}(f \rightarrow i)|^2 \}$$

Equilibrium $\implies f_{i_1} \dots f_{i_n} = f_{f_1} \dots f_{f_m}$

Cancellation in equilibrium as required by the third Sakharov condition

Unitarity and CPT

Unitarity \implies

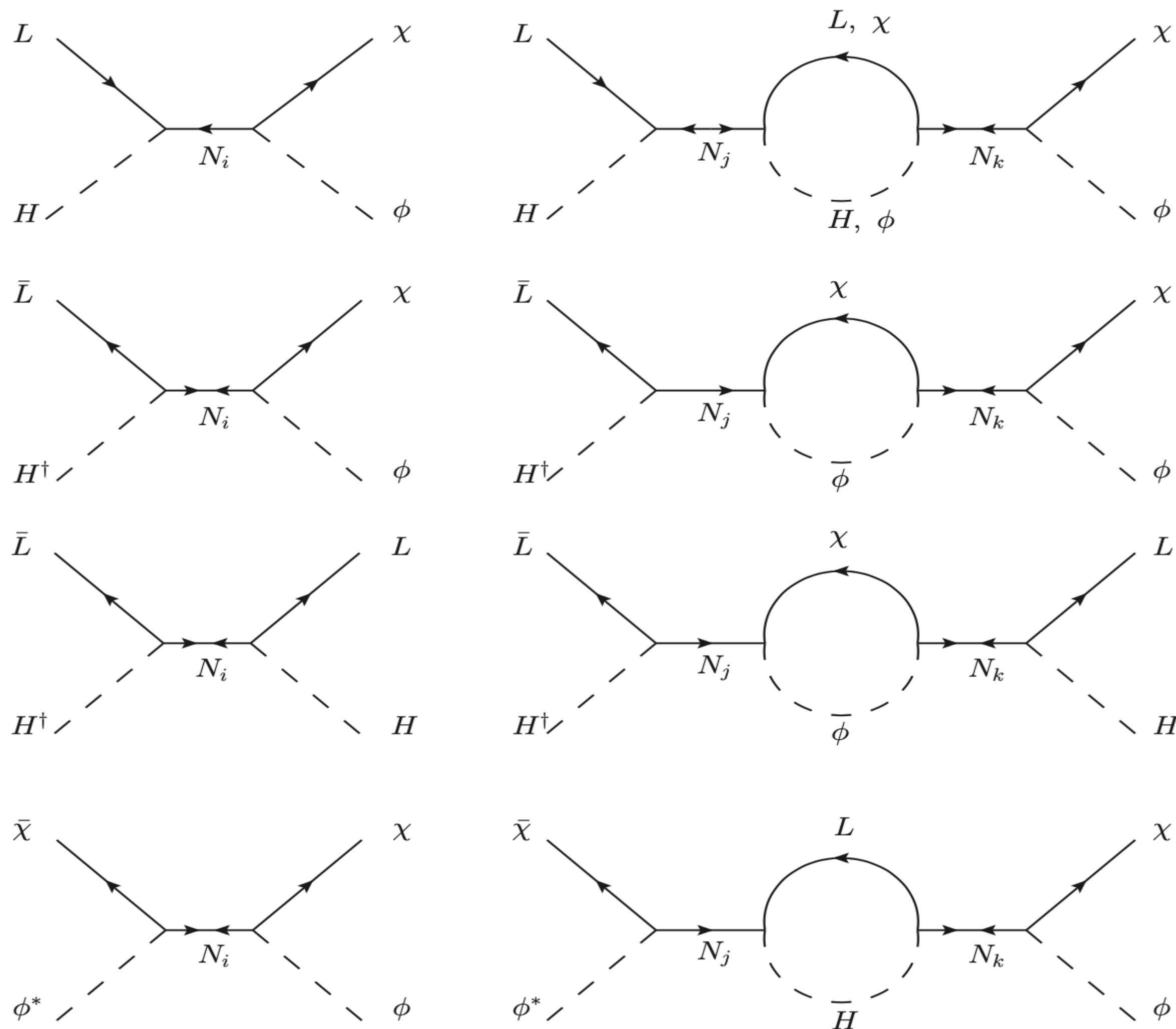
$$\begin{aligned} & |\mathcal{M}(\chi\phi \rightarrow \bar{\chi}\phi^*)|^2 - |\mathcal{M}(\bar{\chi}\phi^* \rightarrow \chi\phi)|^2 \\ & + |\mathcal{M}(\chi\phi \rightarrow LH)|^2 - |\mathcal{M}(\bar{\chi}\phi^* \rightarrow \bar{L}H^\dagger)|^2 \\ & + |\mathcal{M}(\chi\phi \rightarrow \bar{L}H^\dagger)|^2 - |\mathcal{M}(\bar{\chi}\phi^* \rightarrow LH)|^2 = 0 \end{aligned}$$

Collision terms \implies

$$\begin{aligned} \mathcal{C}_{\Delta\chi} \supset & \int d\Pi_L d\Pi_H d\Pi_\chi d\Pi_\phi \delta^4(p_L + p_H - p_\chi - p_\phi) (2\pi)^4 \\ & \times \left[(f_L^{\text{eq}} f_H^{\text{eq}} - f_\chi^{\text{eq}} f_\phi^{\text{eq}}) \left(|\mathcal{M}(LH \rightarrow \chi\phi)|^2 - |\mathcal{M}(\bar{L}H^\dagger \rightarrow \bar{\chi}\phi^*)|^2 + |\mathcal{M}(LH \rightarrow \bar{\chi}\phi^*)|^2 - |\mathcal{M}(\bar{L}H^\dagger \rightarrow \chi\phi)|^2 \right) \right] + \dots \end{aligned}$$

χ, ϕ sector out of equilibrium $\implies f_L f_H \neq f_\chi f_\phi$ **Net asymmetry can be produced!**

Freeze-in Cogeneration of ADM



Freeze-in: Dark sector frozen in and establishes (minimum) dark temperature

$$\xi_\chi \equiv T_\chi/T$$

CP Violation: CP Asymmetries ensured through the introduction of χ , ϕ and m_N

CPT+Unitarity:

$$\epsilon(\chi\phi^* \rightarrow \bar{\chi}\phi) \equiv \epsilon_\chi = - [\epsilon(LH^\dagger \rightarrow \chi\phi^*) + \epsilon(\bar{L}H \rightarrow \chi\phi^*)]$$

$$\epsilon(LH^\dagger \rightarrow \bar{L}H) \equiv \epsilon_L = [\epsilon(LH^\dagger \rightarrow \chi\phi^*) - \epsilon(\bar{L}H \rightarrow \chi\phi^*)]$$