

# Collider Probes of Neutrino Magnetic Moment

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In collaboration with

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# Neutrino magnetic moment: theory

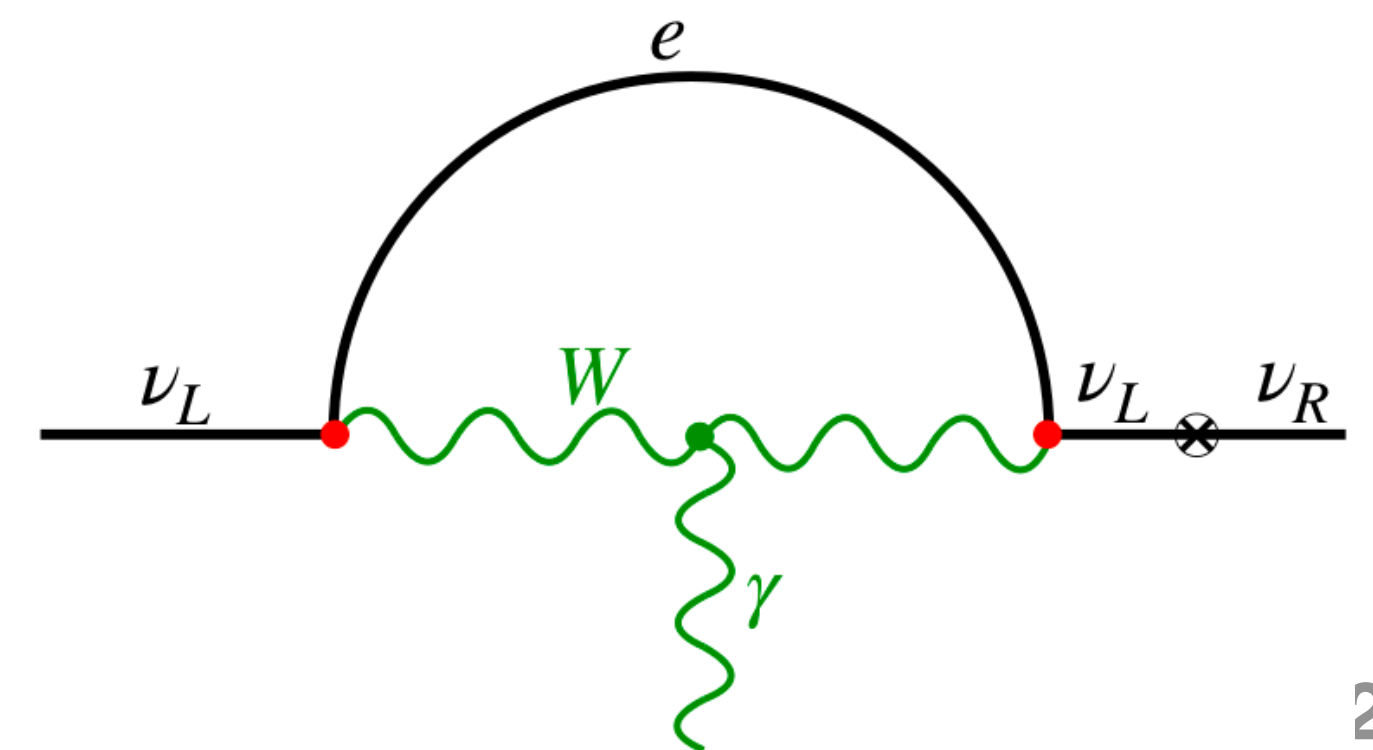
- Neutrino oscillation indicates that neutrinos have mass
- Addition of right-handed neutrino  $\nu_R$  ensures a nonzero magnetic moment

neutrino magnetic moment interaction,

$$\mathcal{L}_\nu^{mag} \supset \frac{1}{2} \mu_\nu^{\alpha\beta} \bar{\nu}_L^\alpha \sigma^{\mu\nu} \nu_R^\beta F_{\mu\nu}$$

- Adding  $\nu_R$  to SM can generate tiny magnetic moment,

$$\mu_\nu \sim 10^{-20} \mu_B \left( \frac{m_\nu}{0.1 \text{ eV}} \right) \sim 10^{-17} \left( \frac{m_\nu}{0.1 \text{ eV}} \right) \text{ GeV}^{-1}$$

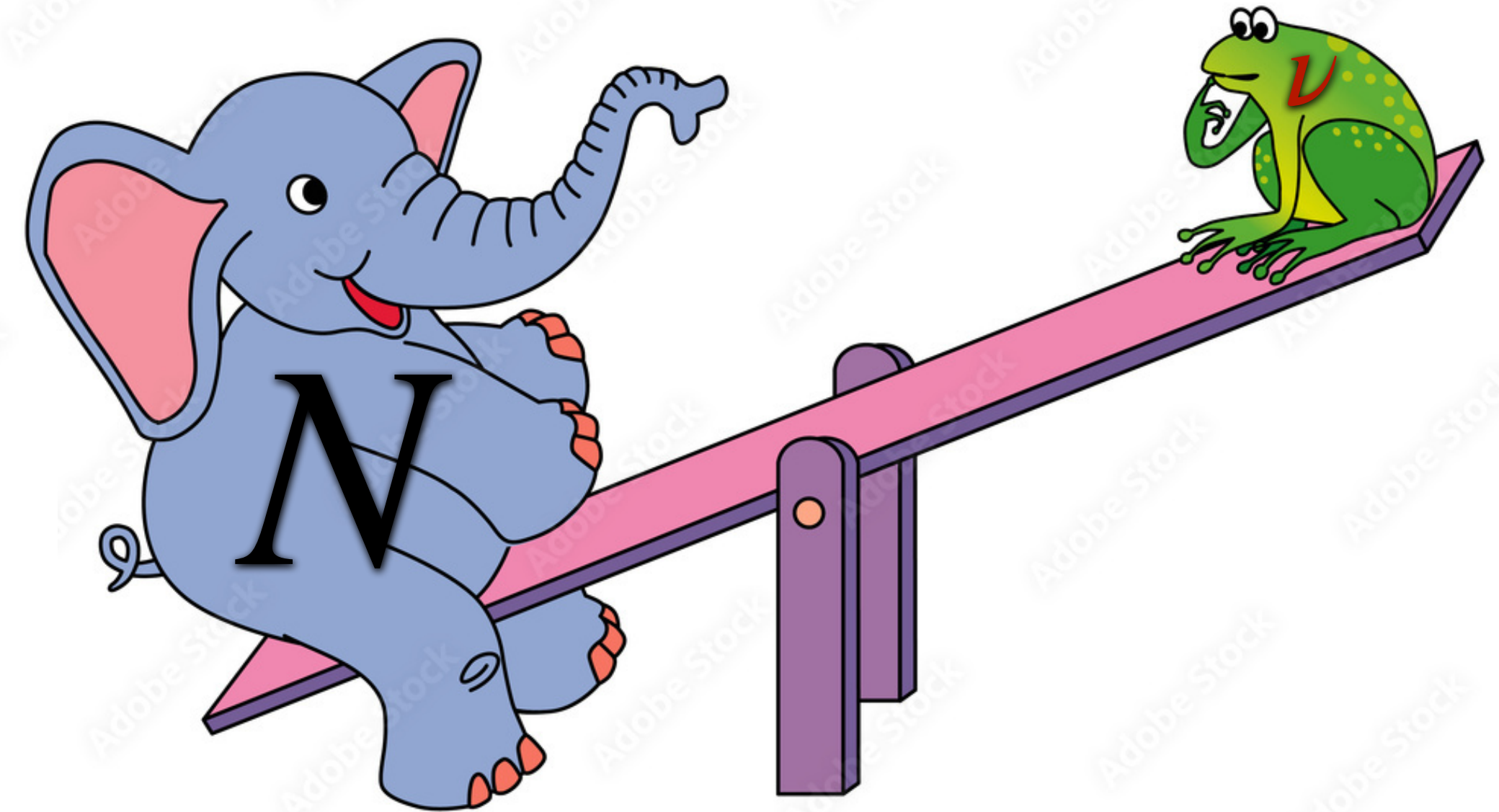


# Neutrino magnetic moment: theory

- In the framework of well-motivated Seesaw mechanism, mass generation involves heavy  $N_R$ ,  
i.e., heavy neutral lepton (HNL)

$$\mathcal{L}_\nu^{\text{mag}} \supset \frac{1}{2} \mu_\nu^{\alpha\beta} \bar{\nu}_L^\alpha \sigma^{\mu\nu} N_R^\beta F_{\mu\nu}$$

- $\mu_\nu$  can be **enhanced** in BSM theories considering the **dipole portal** between active  $\nu_L$  and sterile  $N_R$ , leading to “transition magnetic moment”



# Active-sterile neutrino transition magnetic moment

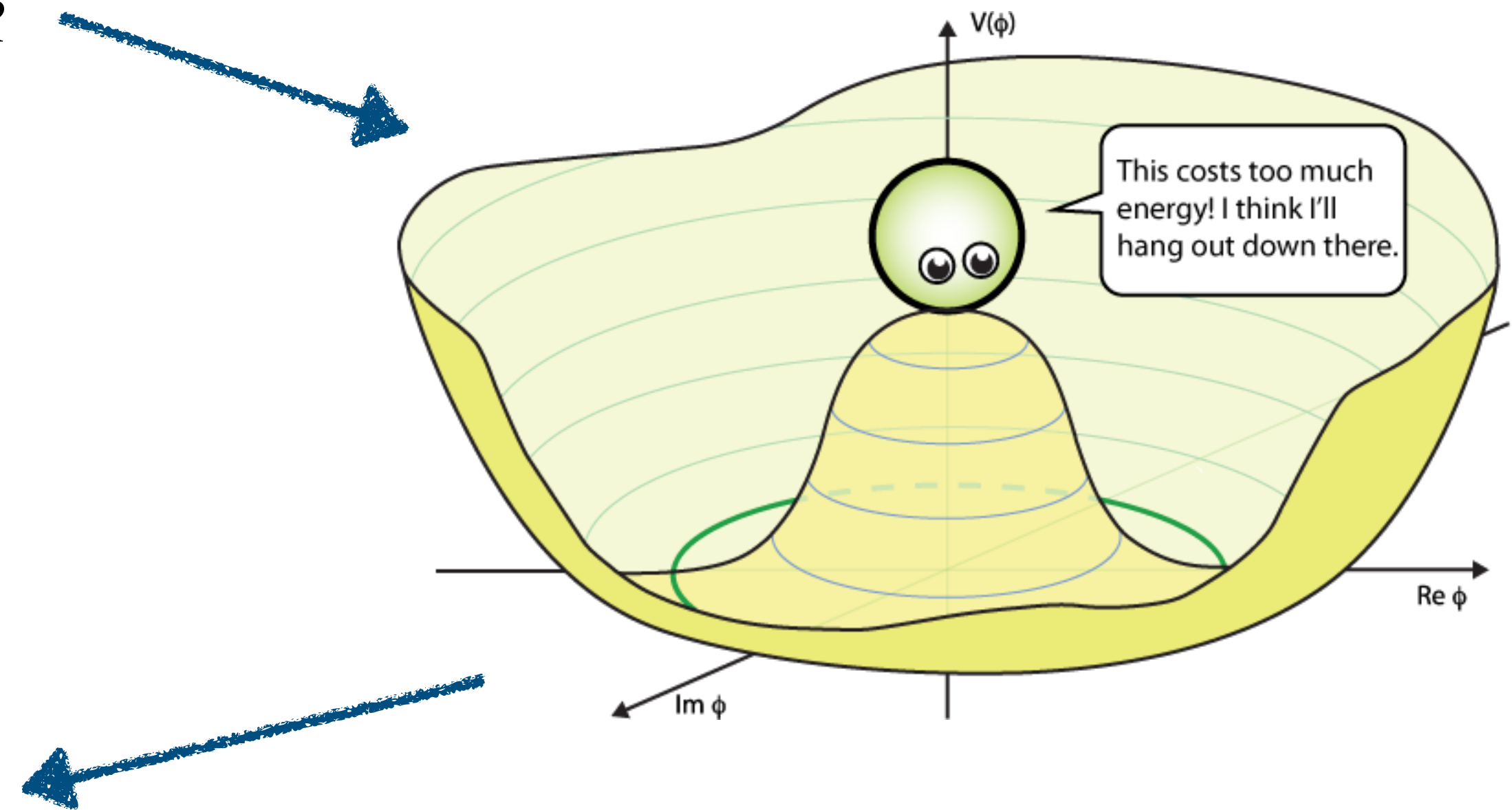
We consider 6-dim EFT Lagrangian with electroweak symmetry,

$$\mathcal{L} \supset \frac{c_B}{\Lambda^2} g' B_{\mu\nu} \bar{L}_L \tilde{H} \sigma^{\mu\nu} N_R + \frac{c_W}{\Lambda^2} g W_{\mu\nu}^a \sigma^a \bar{L}_L \tilde{H} \sigma^{\mu\nu} N_R$$

$$\mathcal{L} \supset \frac{c_W}{\Lambda^2} g W_{\mu\nu}^- \frac{v}{\sqrt{2}} \bar{l}_L \sigma^{\mu\nu} N_R$$

$$+ \left( \frac{c_B}{\Lambda^2} g' \cos \theta_w + \frac{c_W}{\Lambda^2} g \sin \theta_w \right) F_{\mu\nu} \frac{v}{\sqrt{2}} \bar{\nu}_L \sigma^{\mu\nu} N_R$$

$$+ \left( -\frac{c_B}{\Lambda^2} g' \sin \theta_w + \frac{c_W}{\Lambda^2} g \cos \theta_w \right) Z_{\mu\nu} \frac{v}{\sqrt{2}} \sigma^{\mu\nu} N_R$$



# Constraints on neutrino magnetic moment and prospects of collider exp.

## Collider Probes of Neutrino Magnetic Moment...

Higher energy  $\sqrt{s}$  can

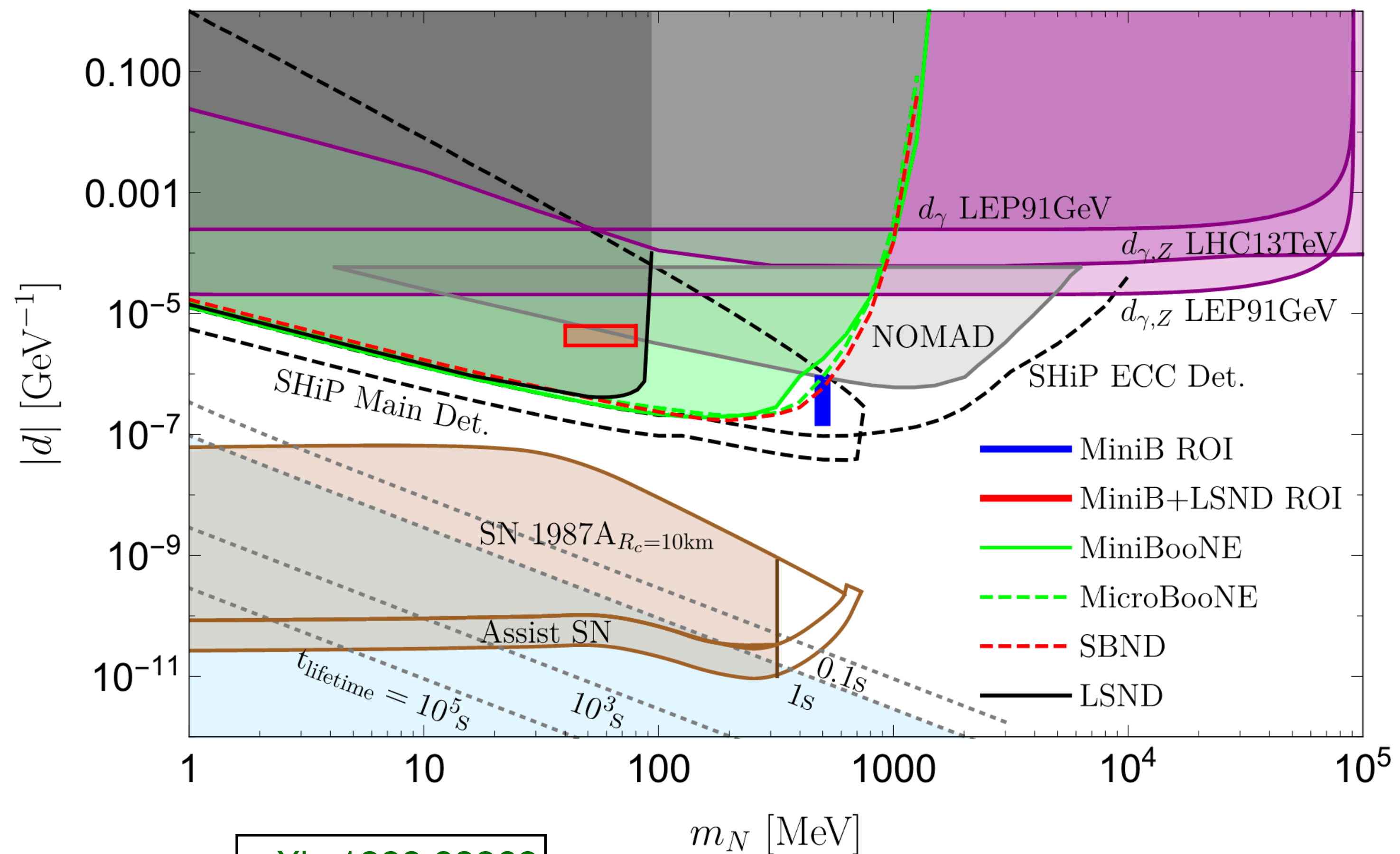
- produce and thus probe larger HNL mass  $m_N$

While...

Higher luminosity  $\mathcal{L}$  allows to

- test the sensitivity on  $d_\gamma$  more precisely since sensitivity reach,

$$d_\gamma \propto \mathcal{L}^{-1/4}$$



arXiv:1803.03262

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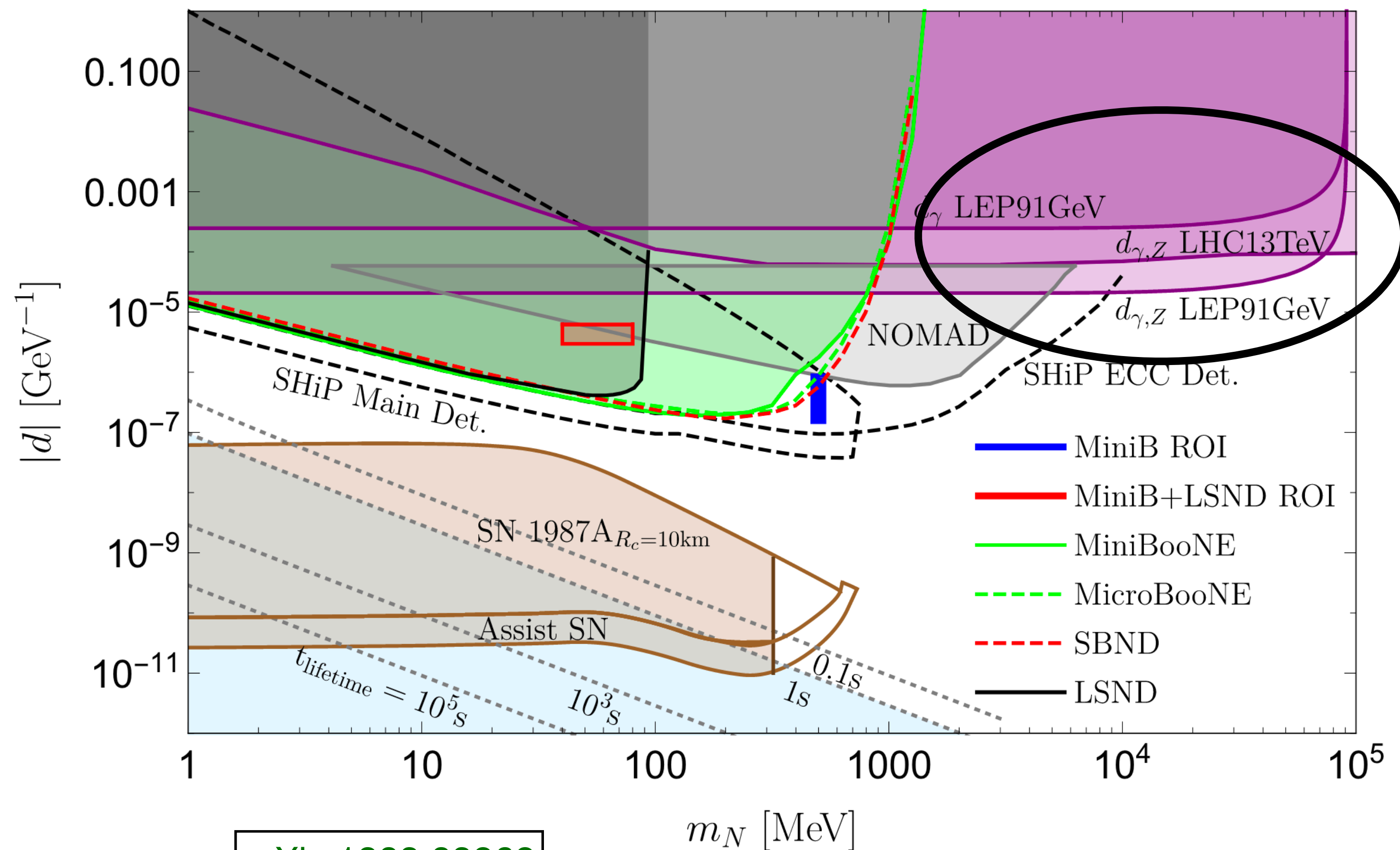
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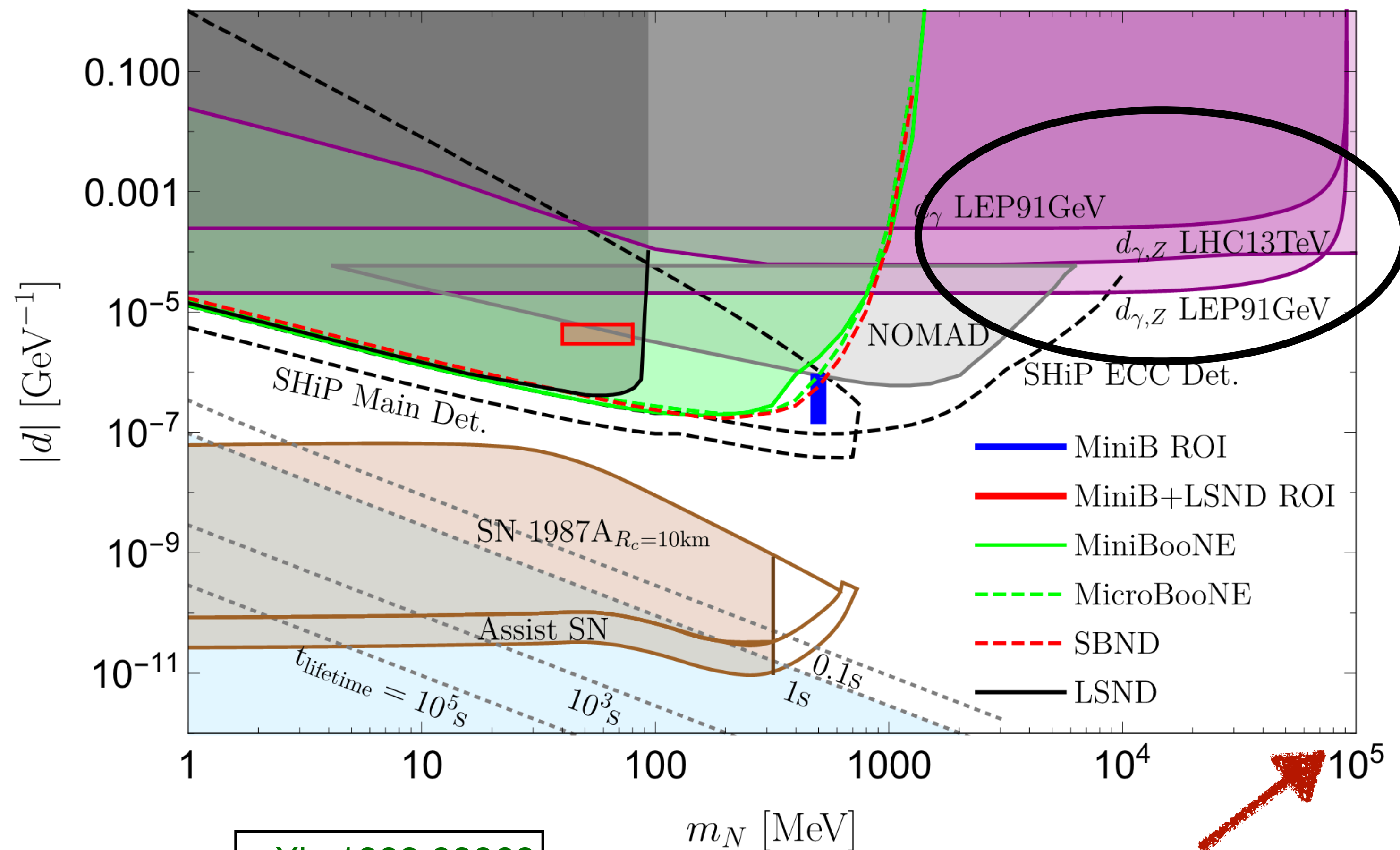
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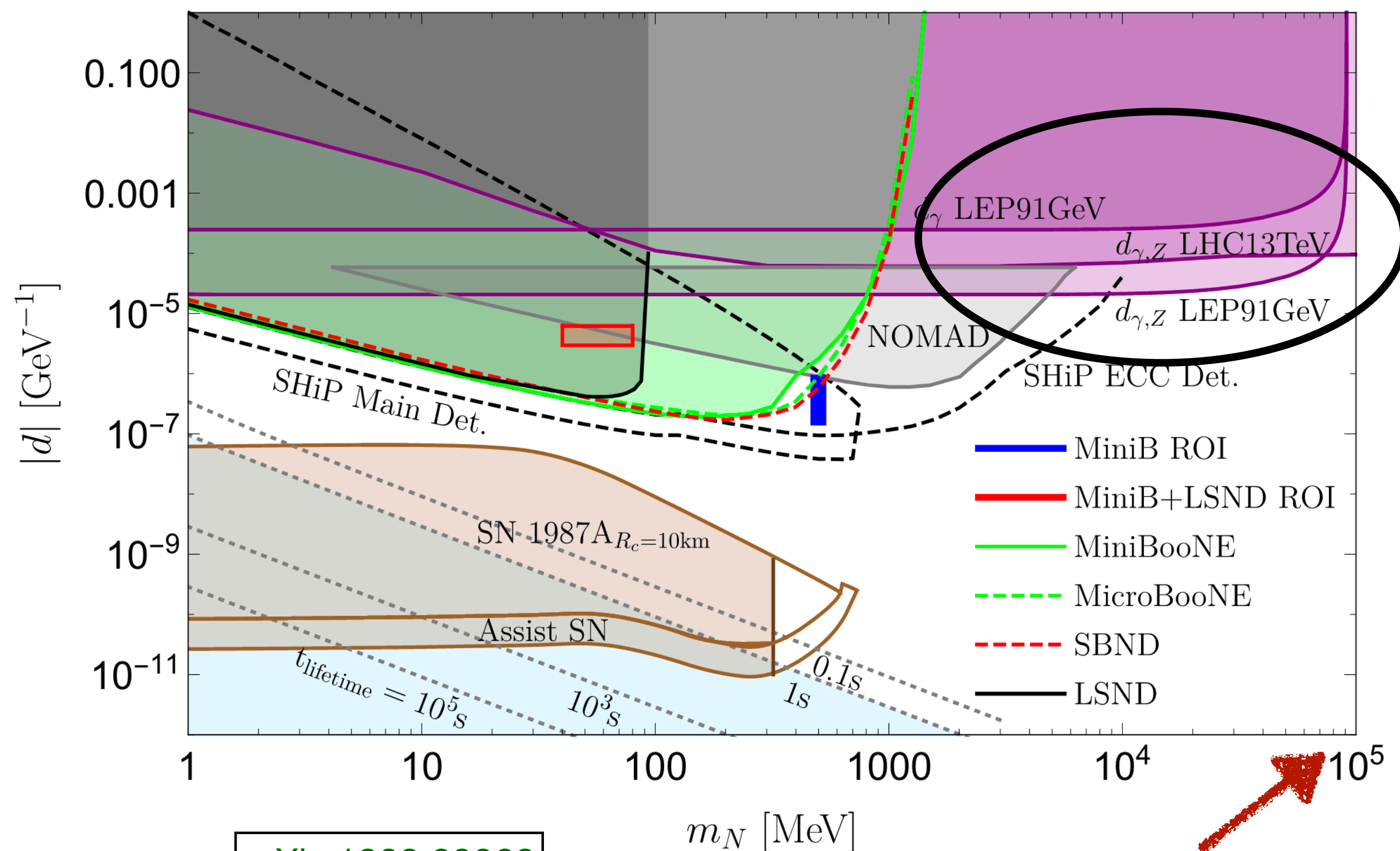
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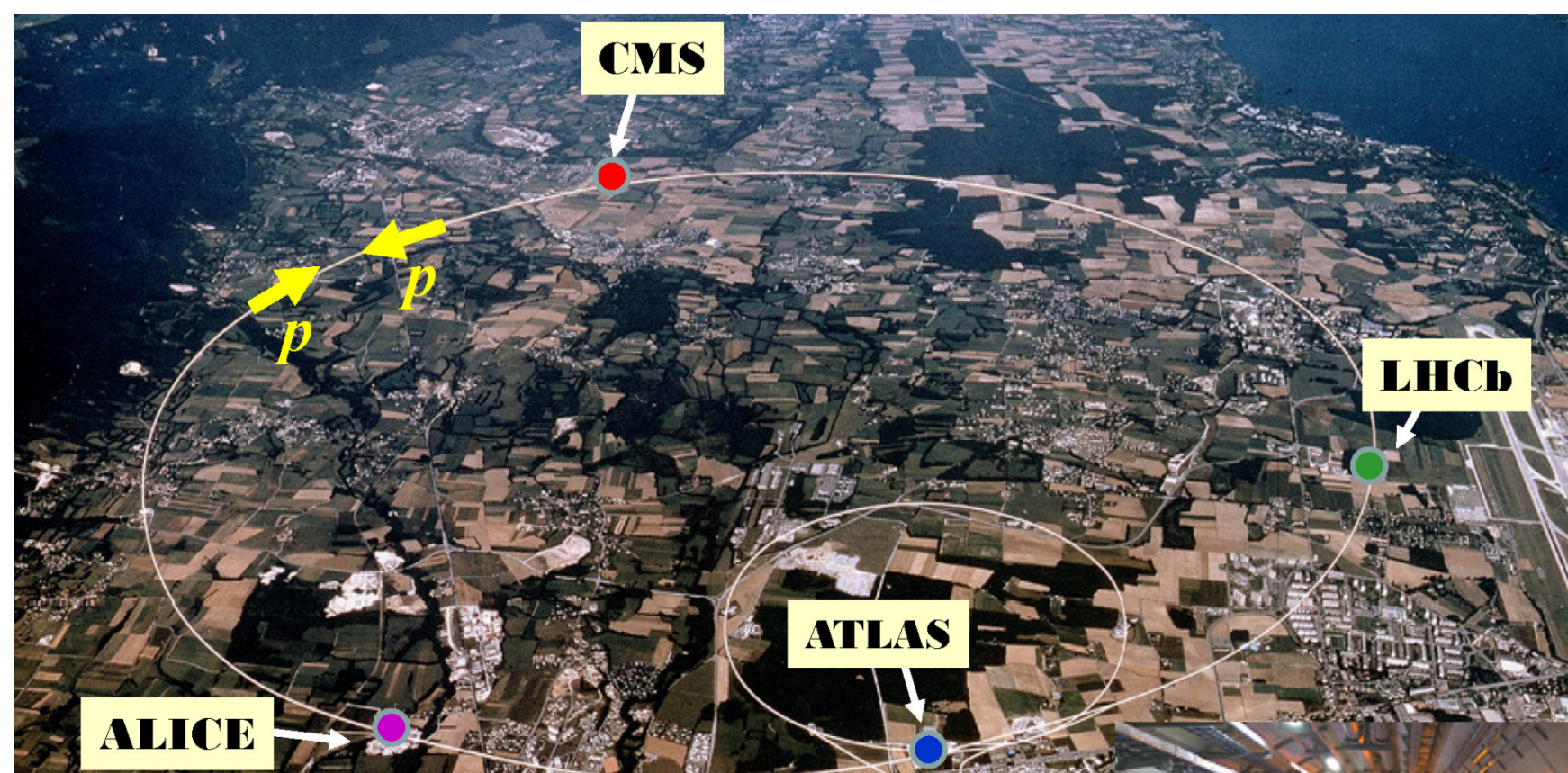
arXiv:1803.03262

Only up to  
100 GeV

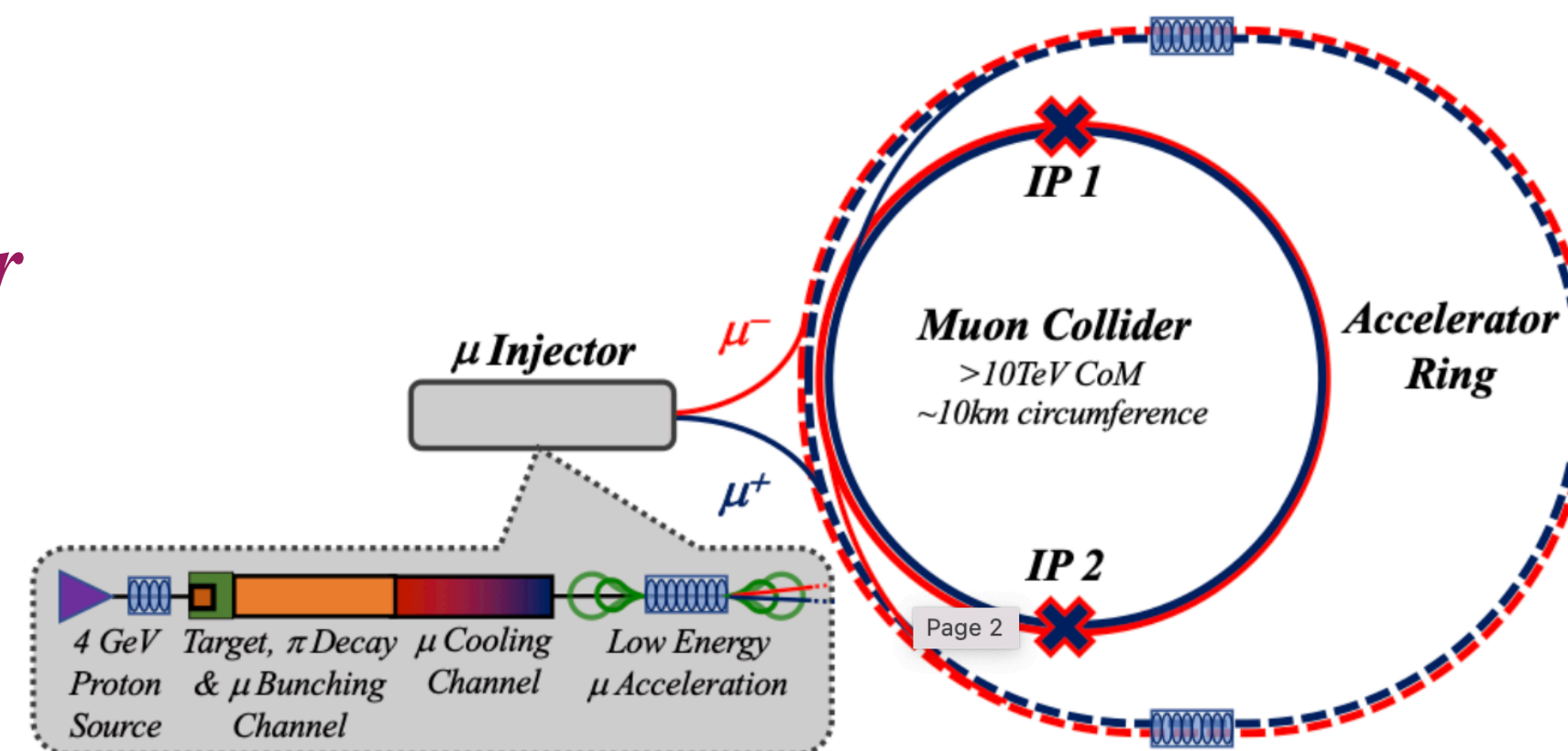


# Prospects of future experiments

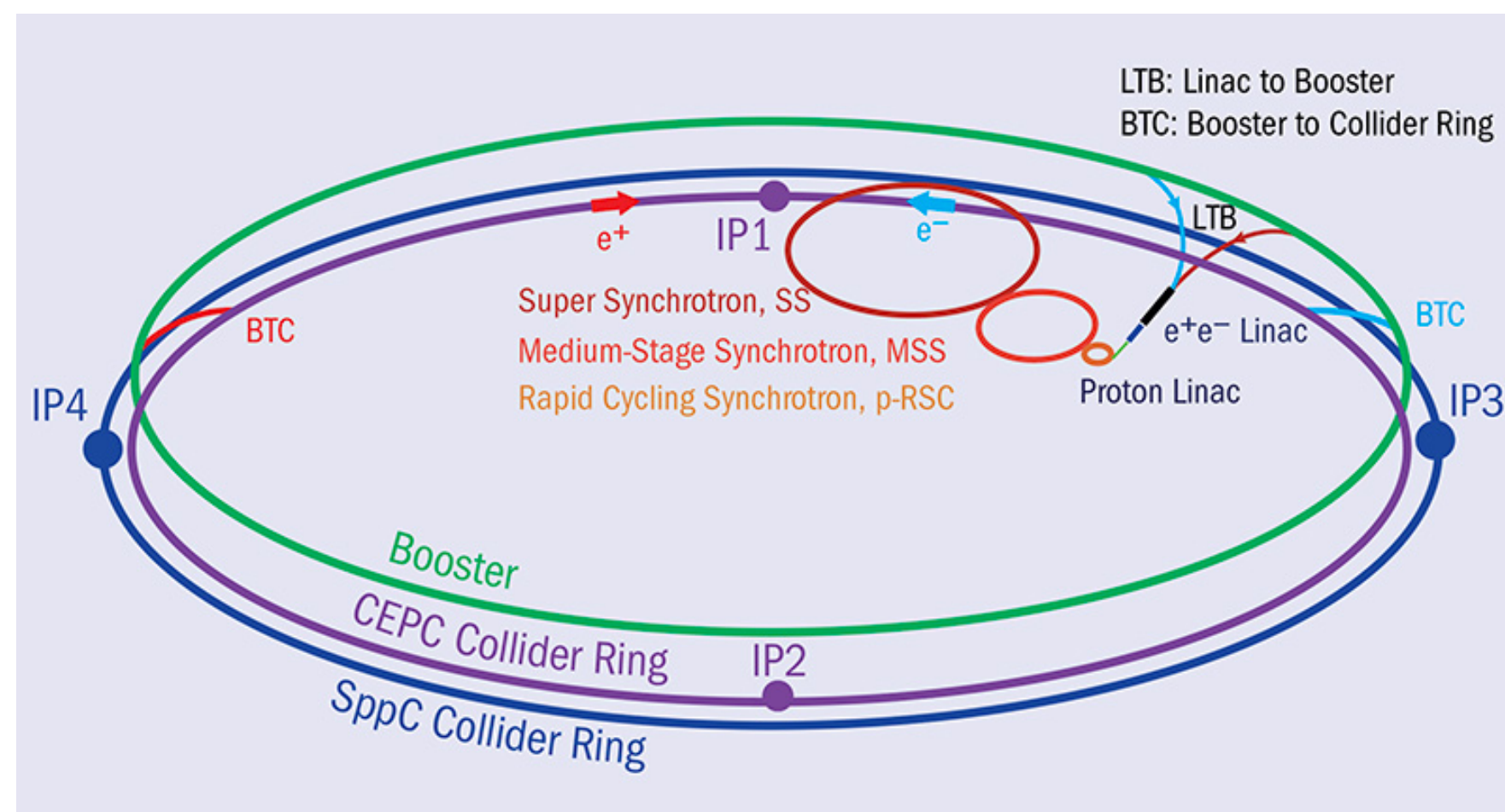
**High Lumi LHC**  
 $\sqrt{s} = 14 \text{ TeV}$ ,  
 $\mathcal{L} = 3 \text{ ab}^{-1}$   
**Operational by 2029**



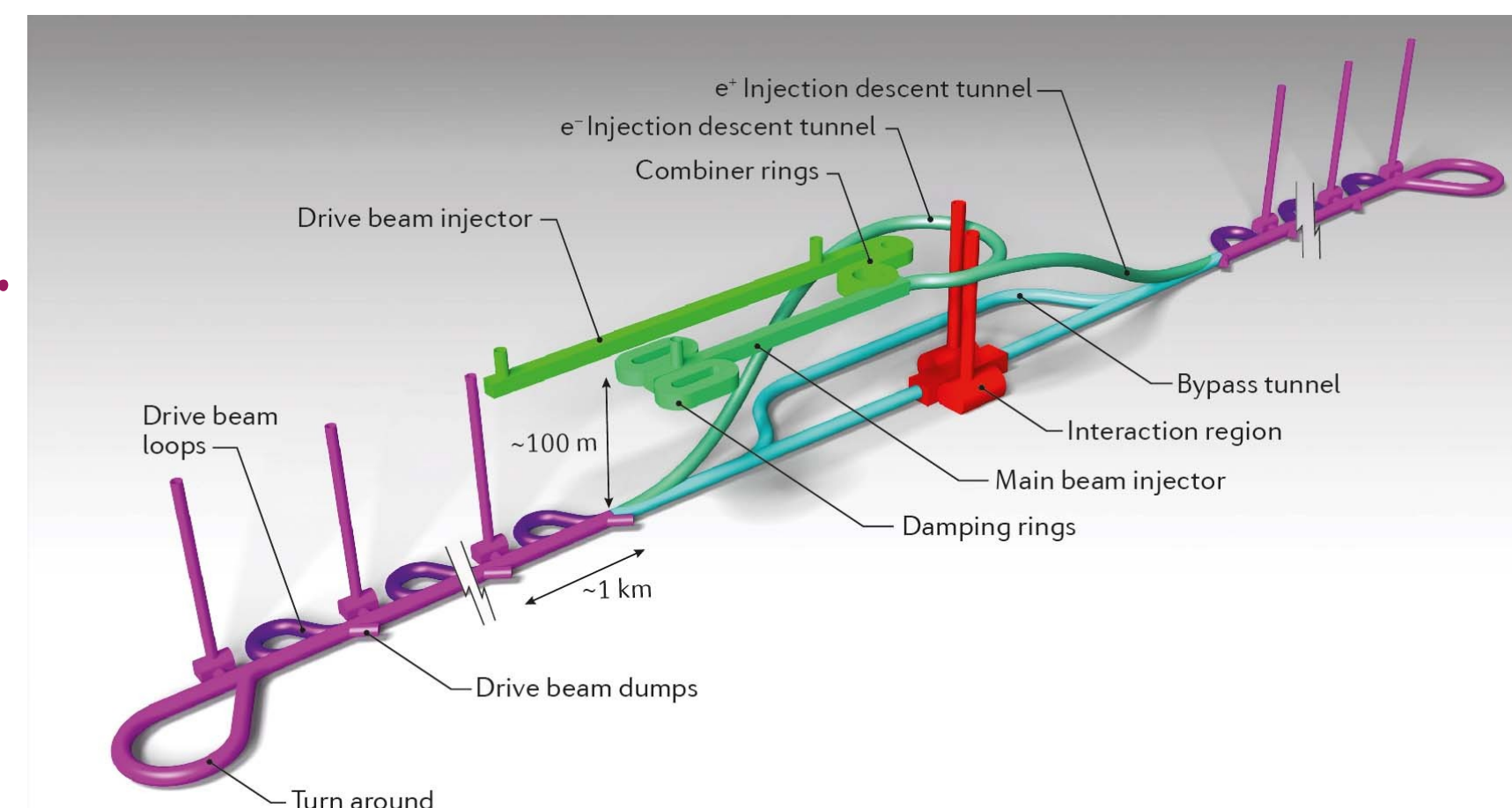
**Muon Collider**  
 $\sqrt{s} = 10 \text{ TeV}$ ,  
 $\mathcal{L} = 10 \text{ ab}^{-1}$



**Circular  $e^-e^+$  Collider (CEPC)**  
 $\sqrt{s} = 240 \text{ GeV}$ ,  
 $\mathcal{L} = 20 \text{ ab}^{-1}$



**Compact Linear Collider (CLIC)**  
 $\sqrt{s} = 3 \text{ TeV}$ ,  
 $\mathcal{L} = 3 \text{ ab}^{-1}$



# Previously on $\nu$ -dipole portal at colliders

Dipole portal to heavy neutral leptons

Gabriel Magill,<sup>1,2,\*</sup> Ryan Plestid,<sup>1,2,†</sup> Maxim Pospelov,<sup>1,3,4,‡</sup> and Yu-Dai Tsai

Heavy Neutral Leptons at Muon Colliders

Peiran Li, Zhen Liu, Kun-Feng Lyu

Collider imprints of right handed neutrino magnetic moment operator

Eung Jin Chun,<sup>1,\*</sup> Sanjoy Mandal,<sup>1,†</sup> and Rojalin Padhan<sup>2,3,‡</sup>

Daniele Barducci and Alessandro Dondarini<sup>a,b</sup>

Neutrino dipole portal at electron colliders

Yu Zhang,<sup>1</sup> Mao Song,<sup>2</sup> Ran Ding,<sup>2</sup> and Liangwen Chen<sup>3,4,\*</sup>

Probing active-sterile neutrino transition magnetic moments at  
LEP and CEPC

Yu Zhang<sup>1</sup> and Wei

Neutrino dipole portal at a high energy  $\mu$ -collider

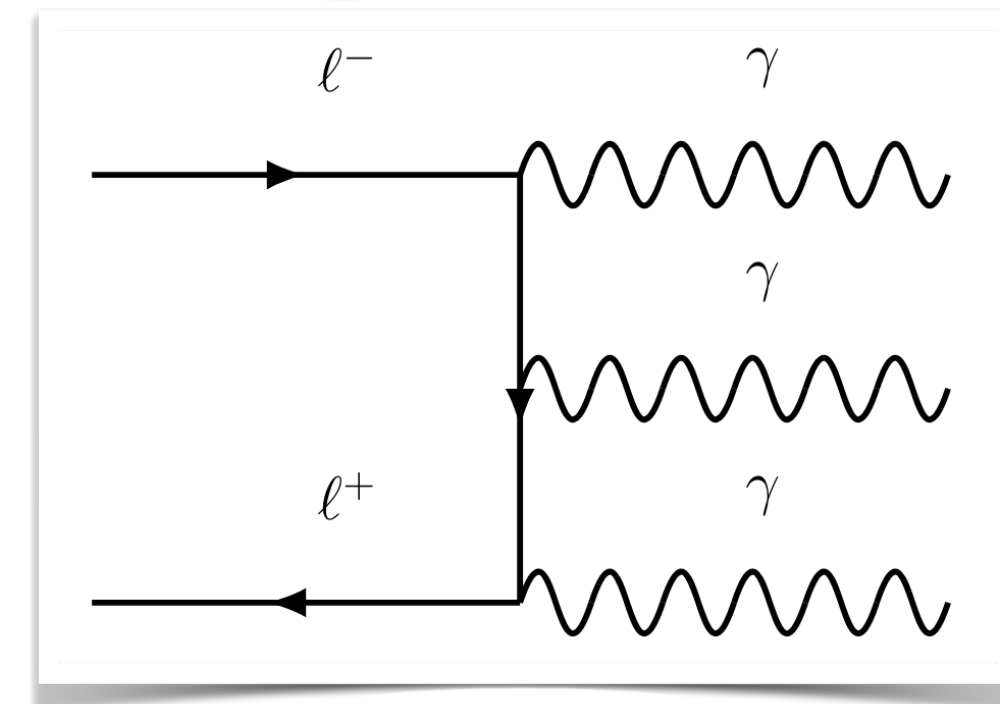
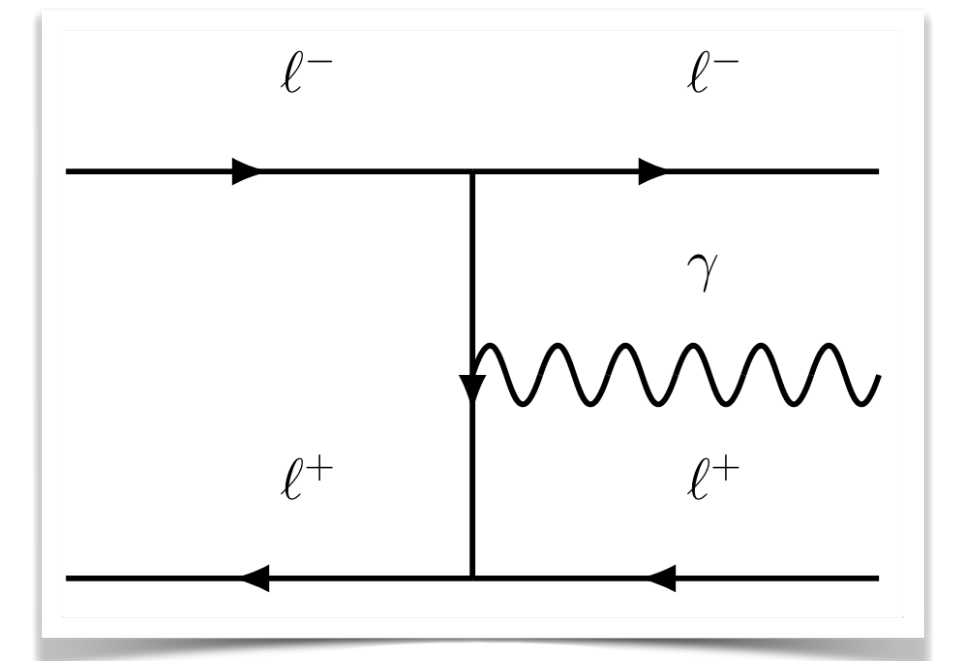
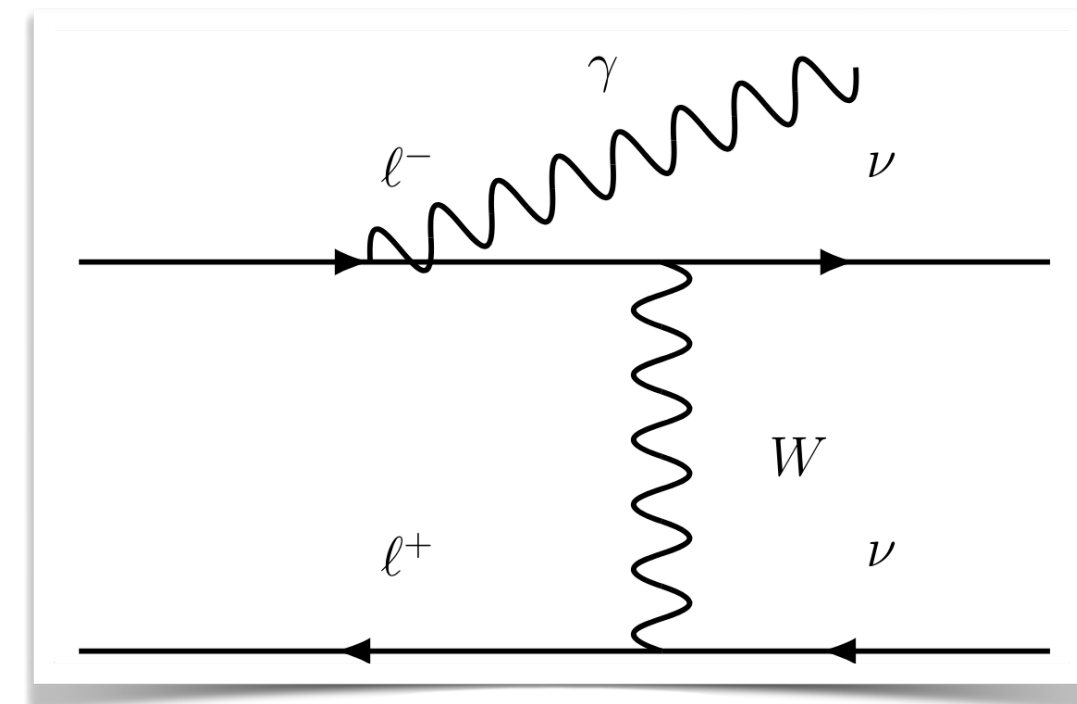
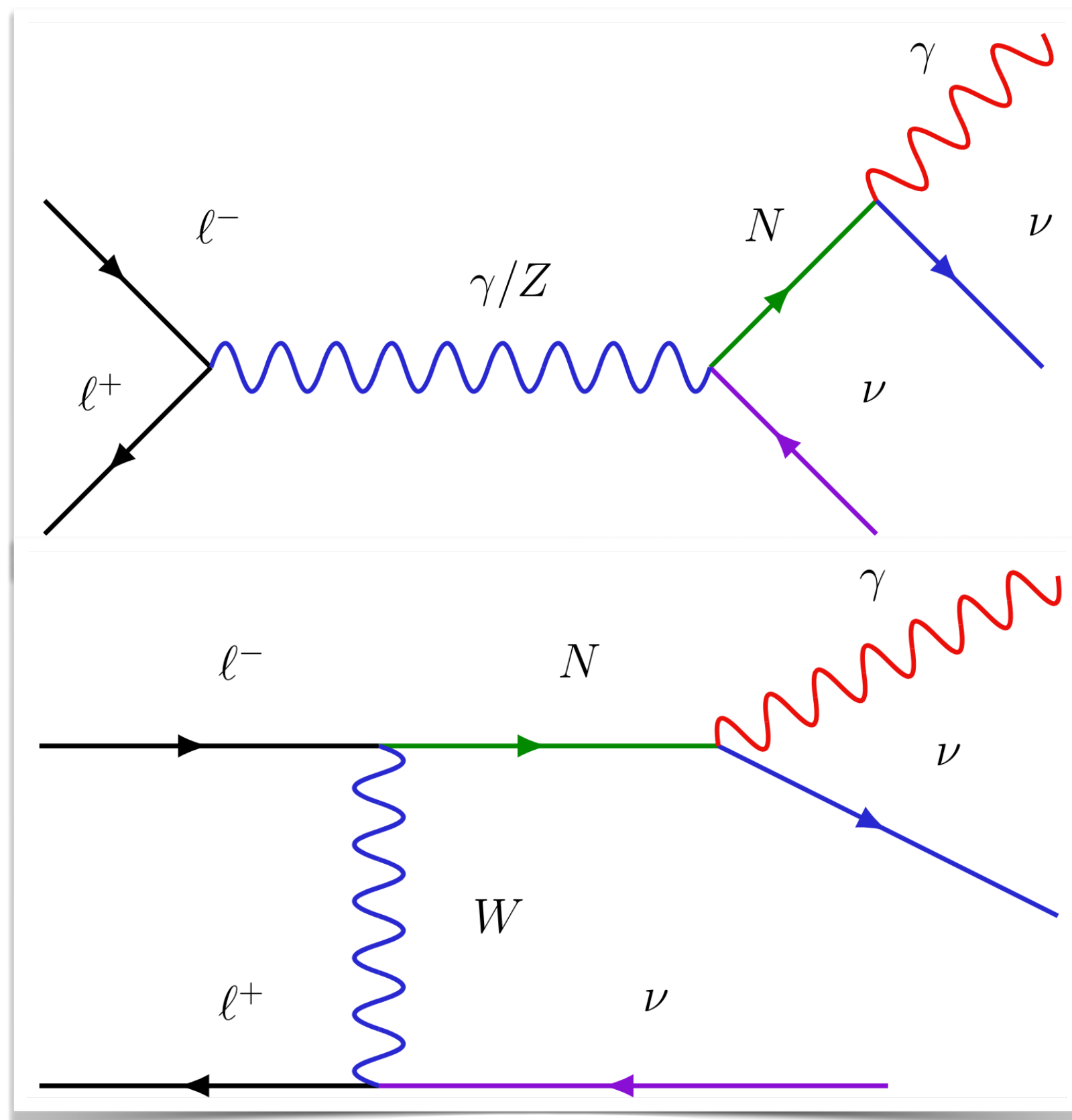
# Mono-photon signal and its background

Signal:  $\ell^+ \ell^- \rightarrow \bar{\nu} N$  (on-shell)

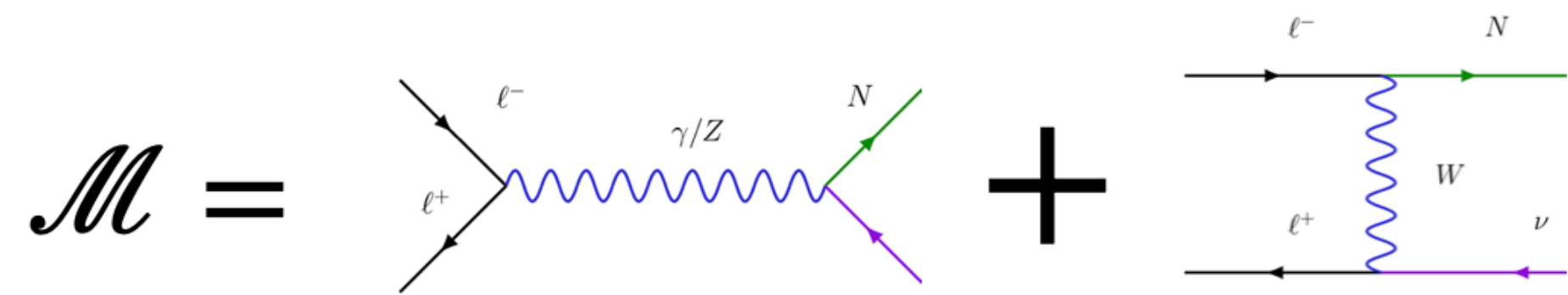
and  $N$  decays to a photon:  $N \rightarrow \nu \gamma$

Background

$\ell^+ \ell^- \rightarrow \nu \bar{\nu} \gamma$ ,  $\ell^+ \ell^- \rightarrow \ell^+ \ell^- \gamma$ ,  $\ell^+ \ell^- \rightarrow \gamma \gamma \gamma$



# Cross-section $\sigma(\ell^+ \ell^- \rightarrow \nu N)$

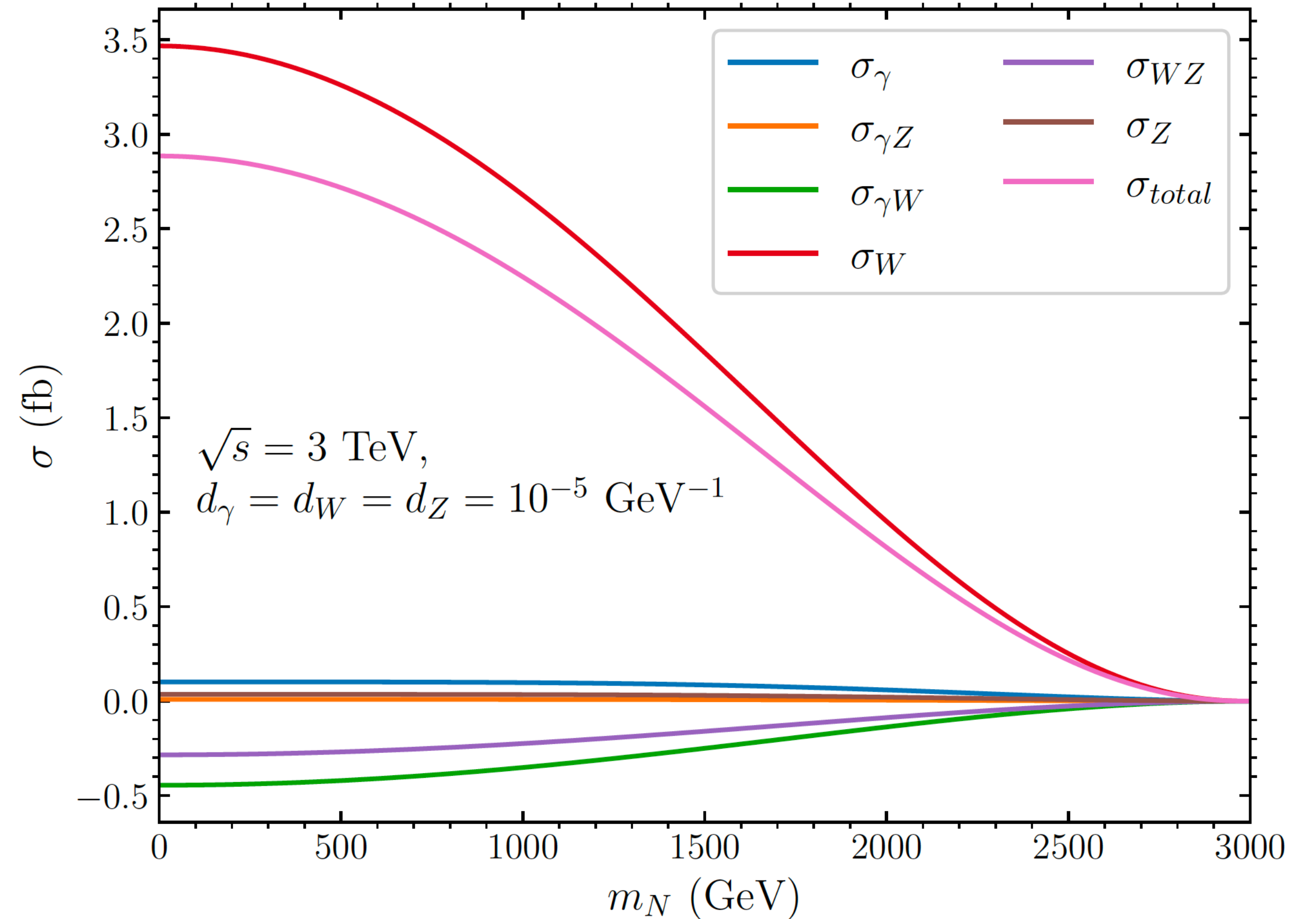


$$\mathcal{M} = \mathcal{M}_\gamma + \mathcal{M}_Z + \mathcal{M}_W$$

squared terms

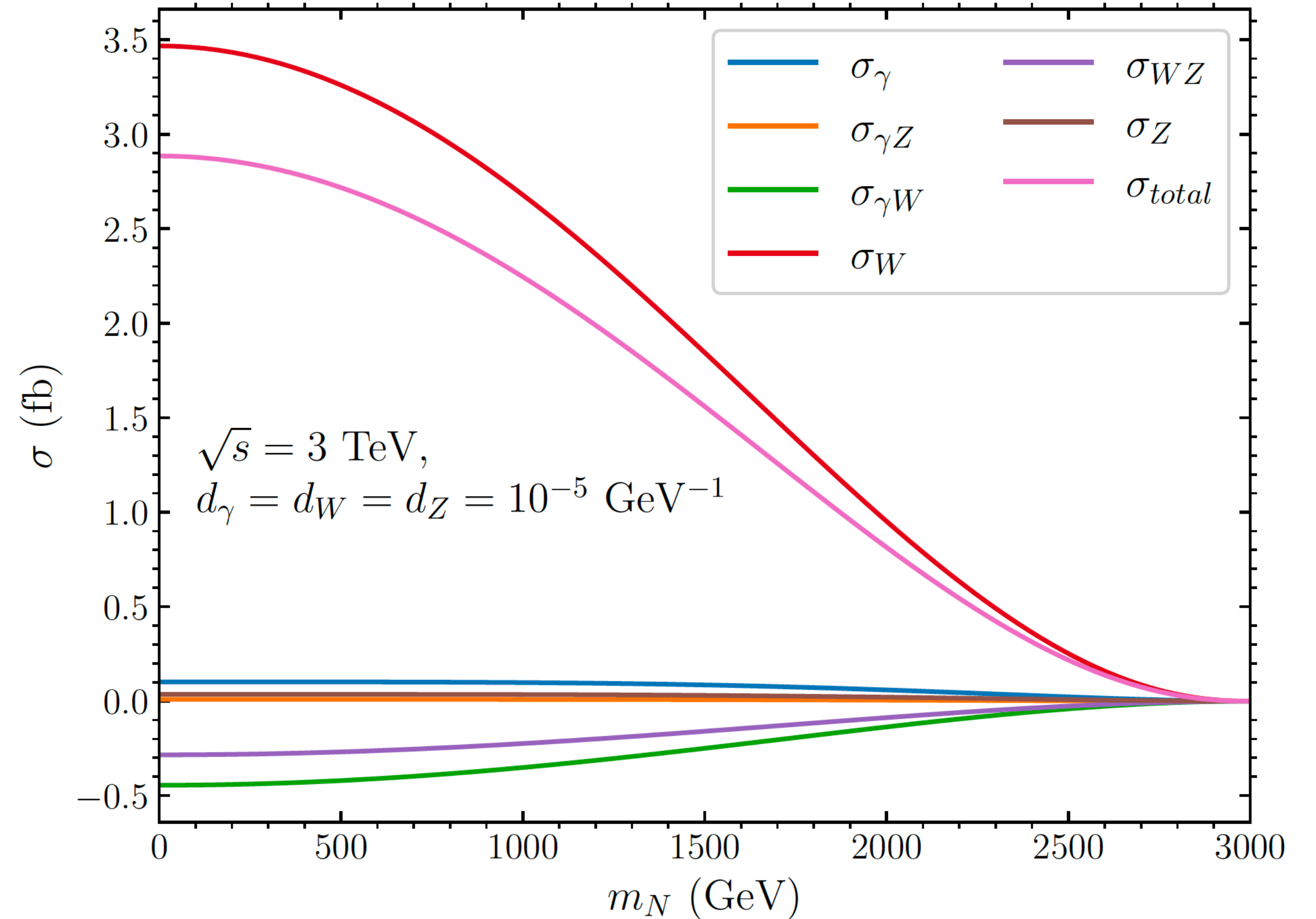
$$\sigma_{tot} = \underbrace{\sigma_\gamma + \sigma_Z + \sigma_W}_{\text{squared terms}} + \underbrace{\sigma_{\gamma Z} + \sigma_{\gamma W} + \sigma_{WZ}}_{\text{interference terms}}$$

interference terms



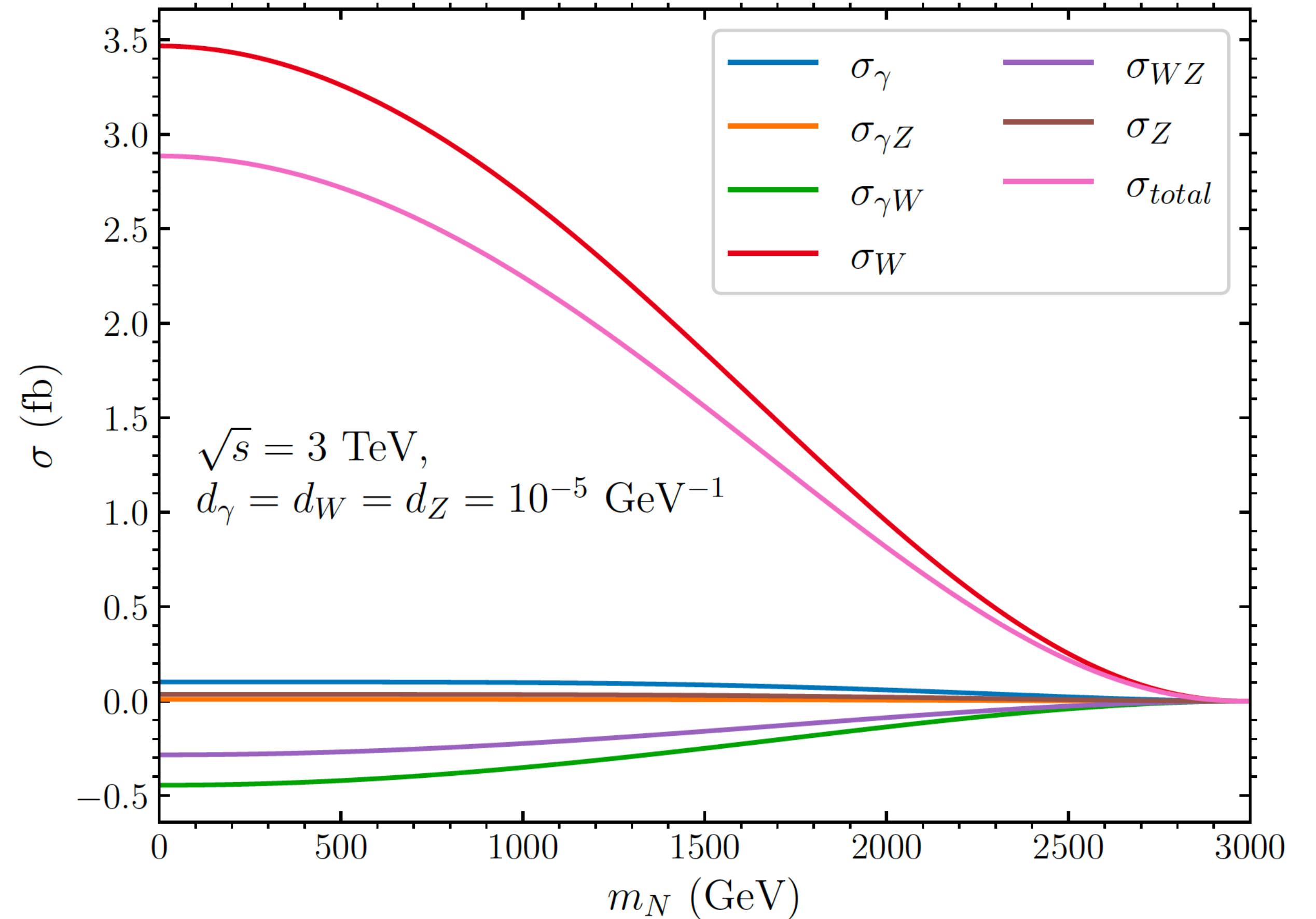
# Cross-section $\sigma(\ell^+ \ell^- \rightarrow \nu N)$

$$\begin{aligned}
 \mathcal{M} &= \text{[Feynman Diagram 1]} + \text{[Feynman Diagram 2]} \\
 &= \mathcal{M}_\gamma + \mathcal{M}_Z + \mathcal{M}_W \\
 &\quad \text{squared terms} \\
 \sigma_{tot} &= \underbrace{\sigma_\gamma + \sigma_Z + \sigma_W}_{\text{squared terms}} \\
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 \end{aligned}$$



# Cross-section $\sigma(\ell^+ \ell^- \rightarrow \nu N)$

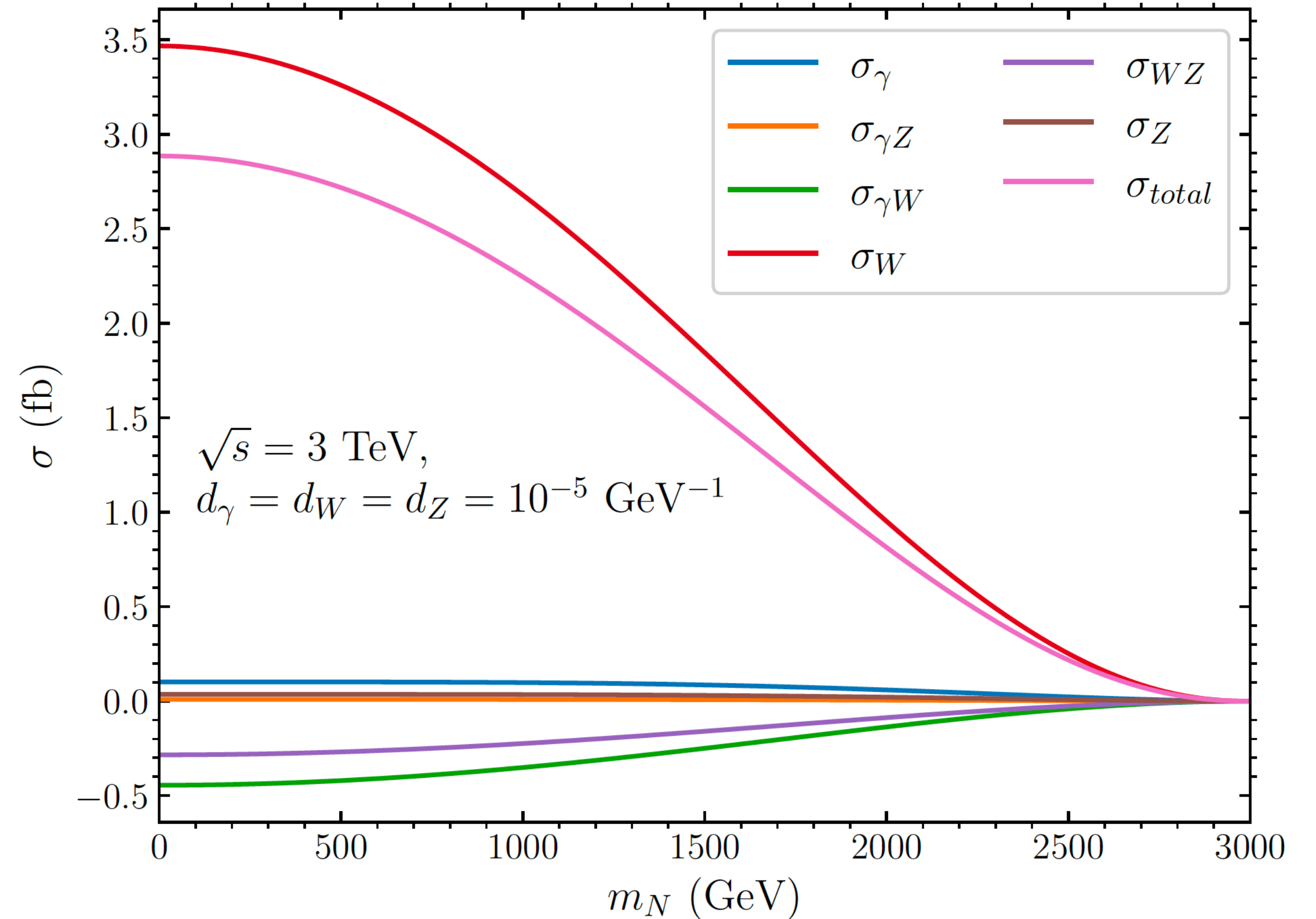
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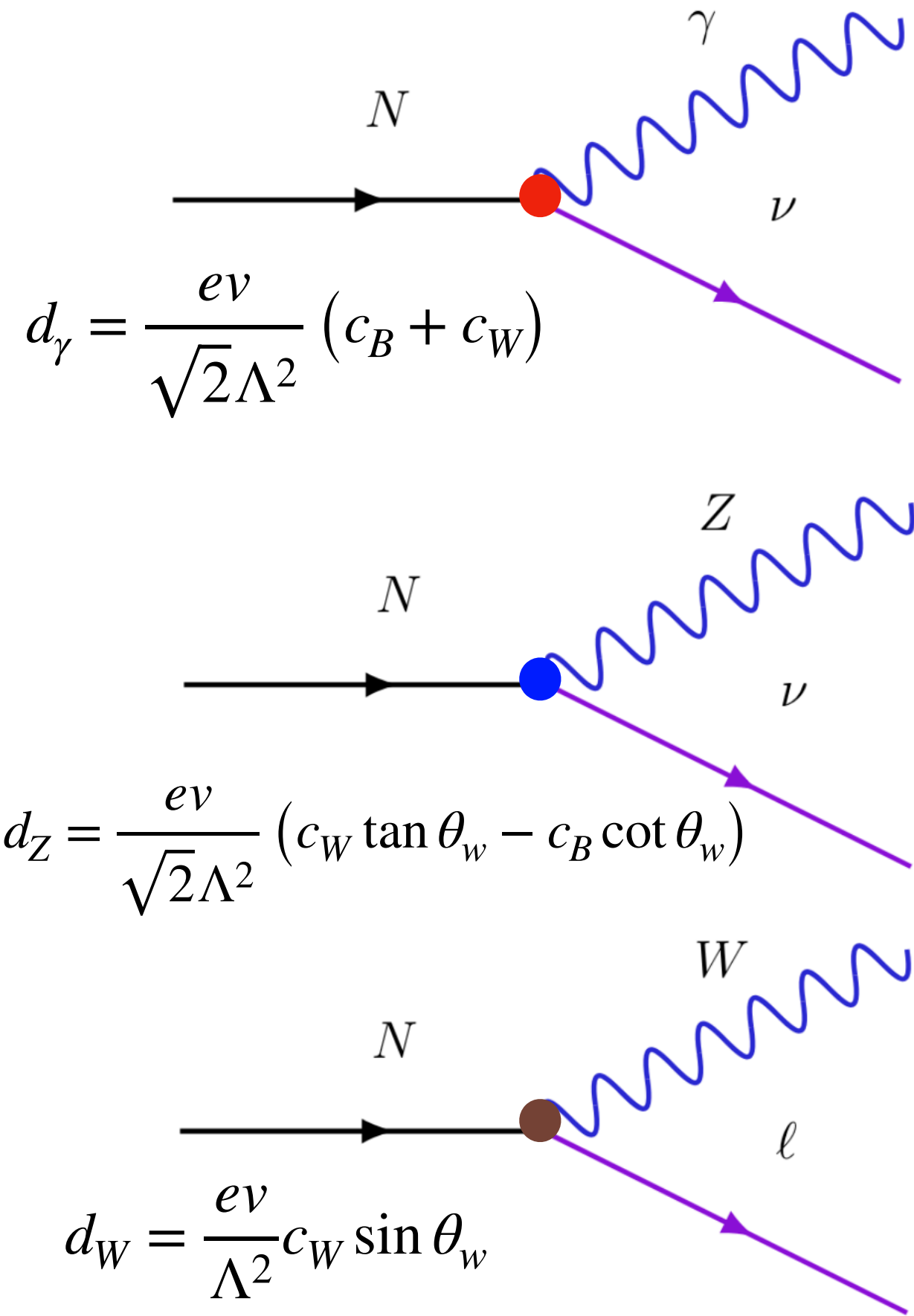
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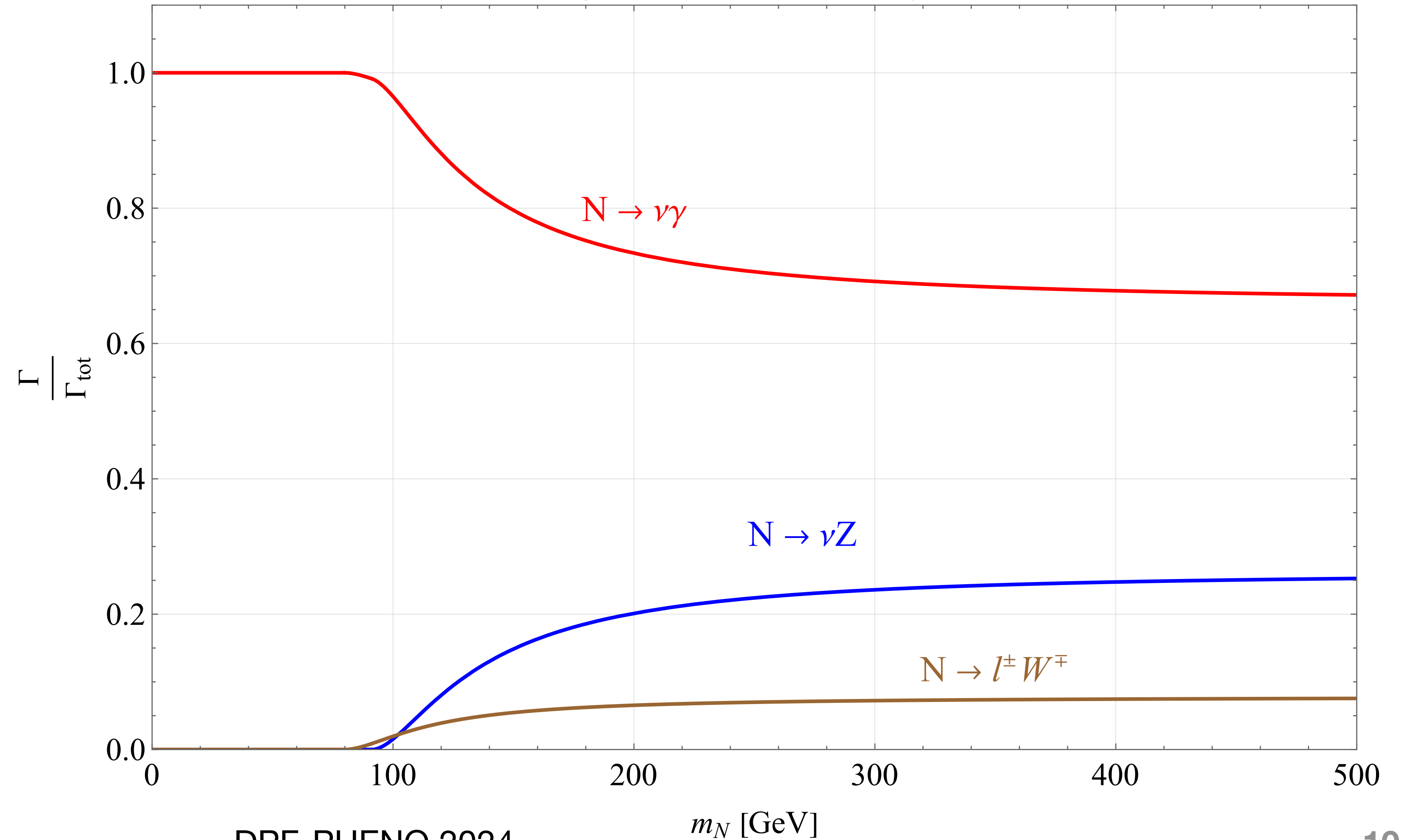
We found them to be non-vanishing in contrast to a previous study (arXiv:2301.06050)



# Dipole couplings and decay widths



Branching ratio of the  $N_R$  decay channels

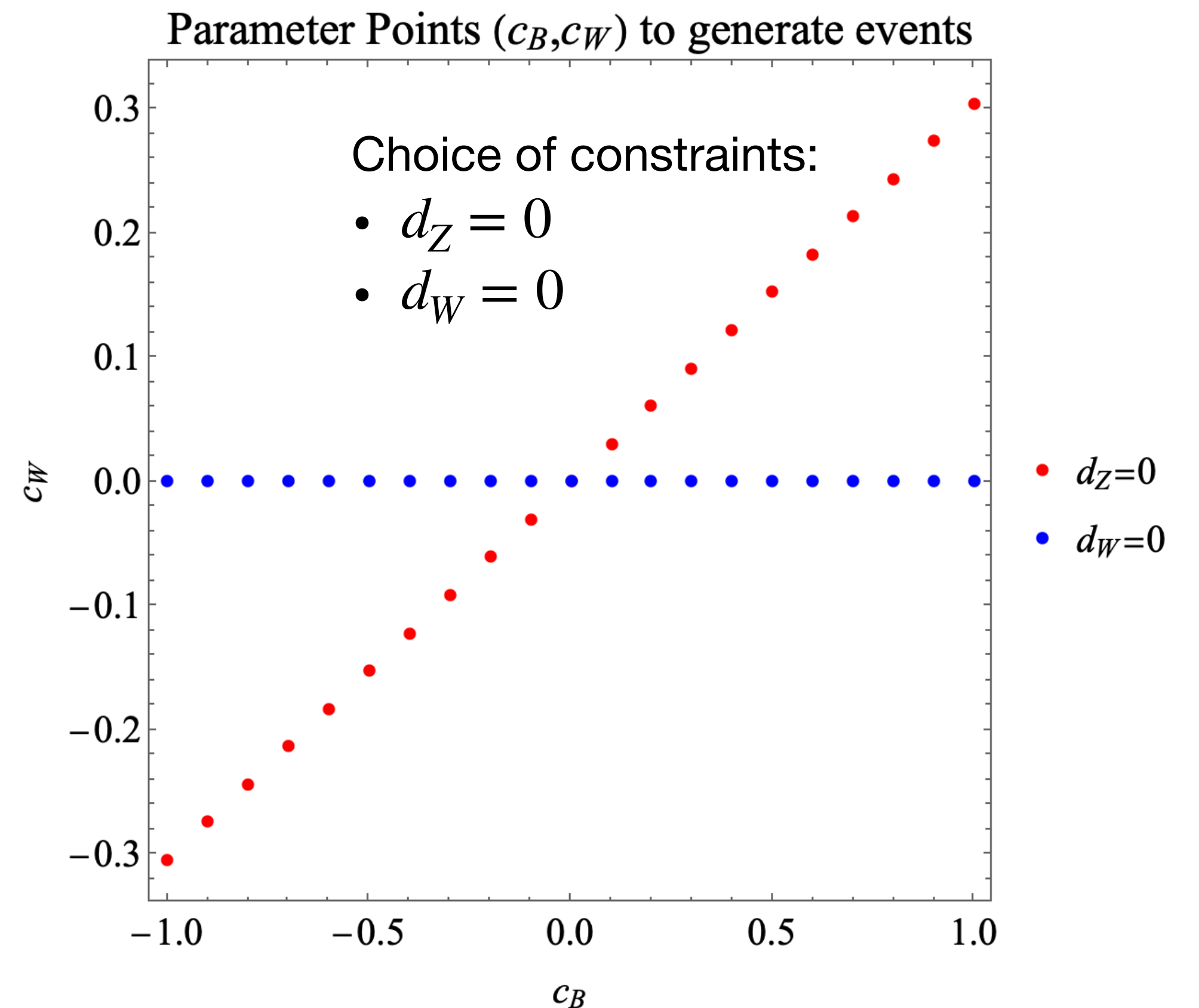




# Analysis

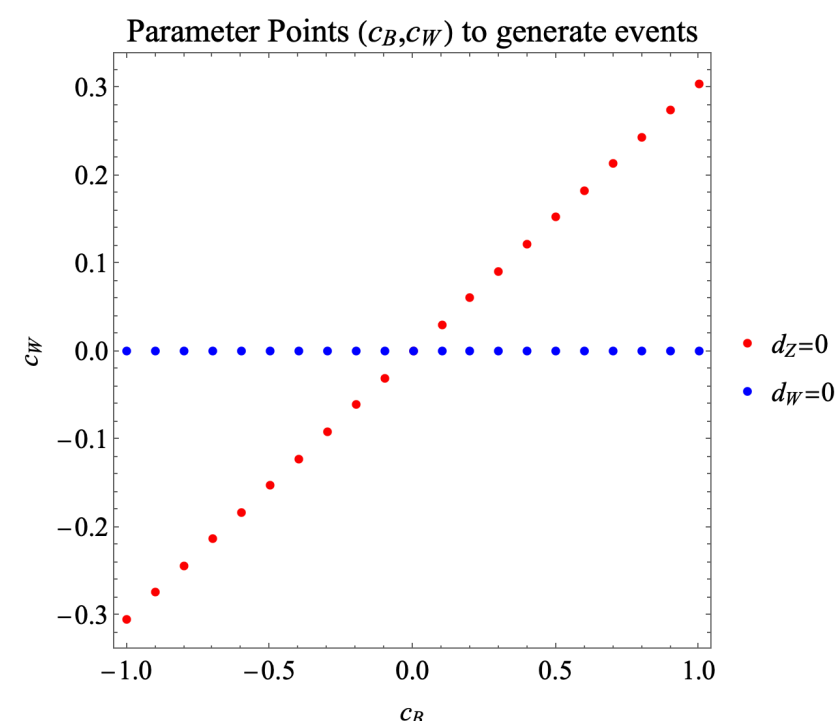
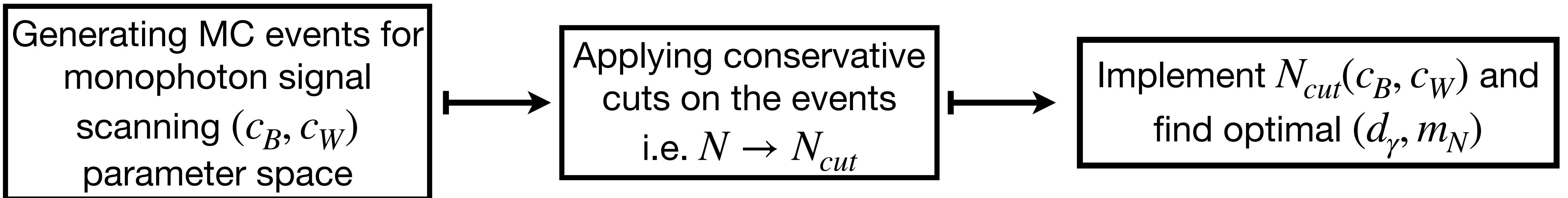
$$2 \rightarrow 3$$
$$(c_B, c_W) \rightarrow (d_\gamma, d_Z, d_W)$$

- Goal is to probe  $d_\gamma \propto (c_B + c_W)$
- Note that  $(d_\gamma, d_Z, d_W)$  are correlated, we can impose constraints on them to evaluate exclusion limit on  $d_\gamma$
- We generate Monte Carlo events scanning  $(c_B, c_W)$  parameter space



# Analysis

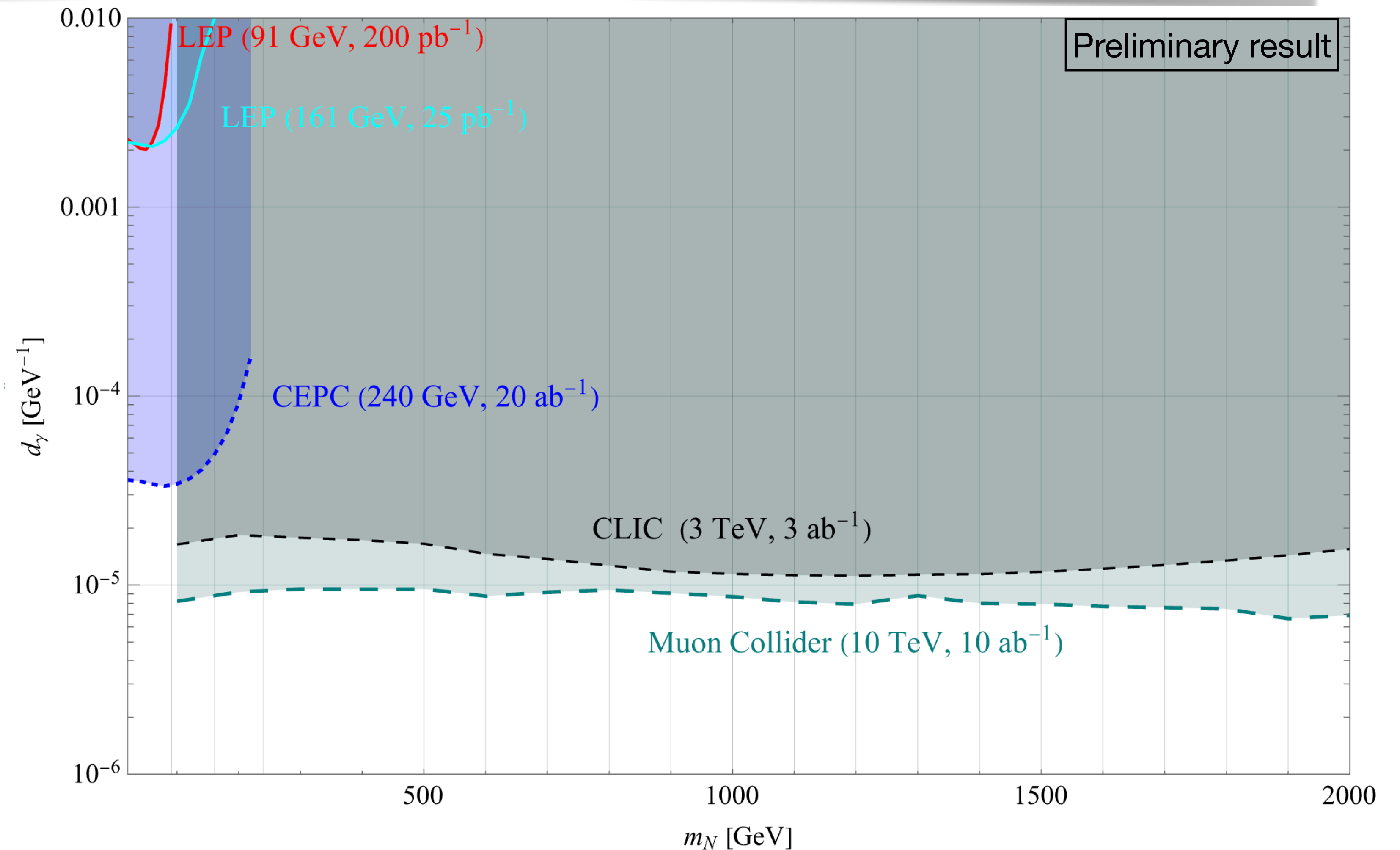
With choices of constraints (e.g.  $d_W = 0, d_Z = 0$ )...



- Important cuts:
- photon:  $p_{T,\gamma} > 20 \text{ GeV}, |\eta_\gamma| < 2.5$
  - Veto lepton
  - Veto Z-resonance

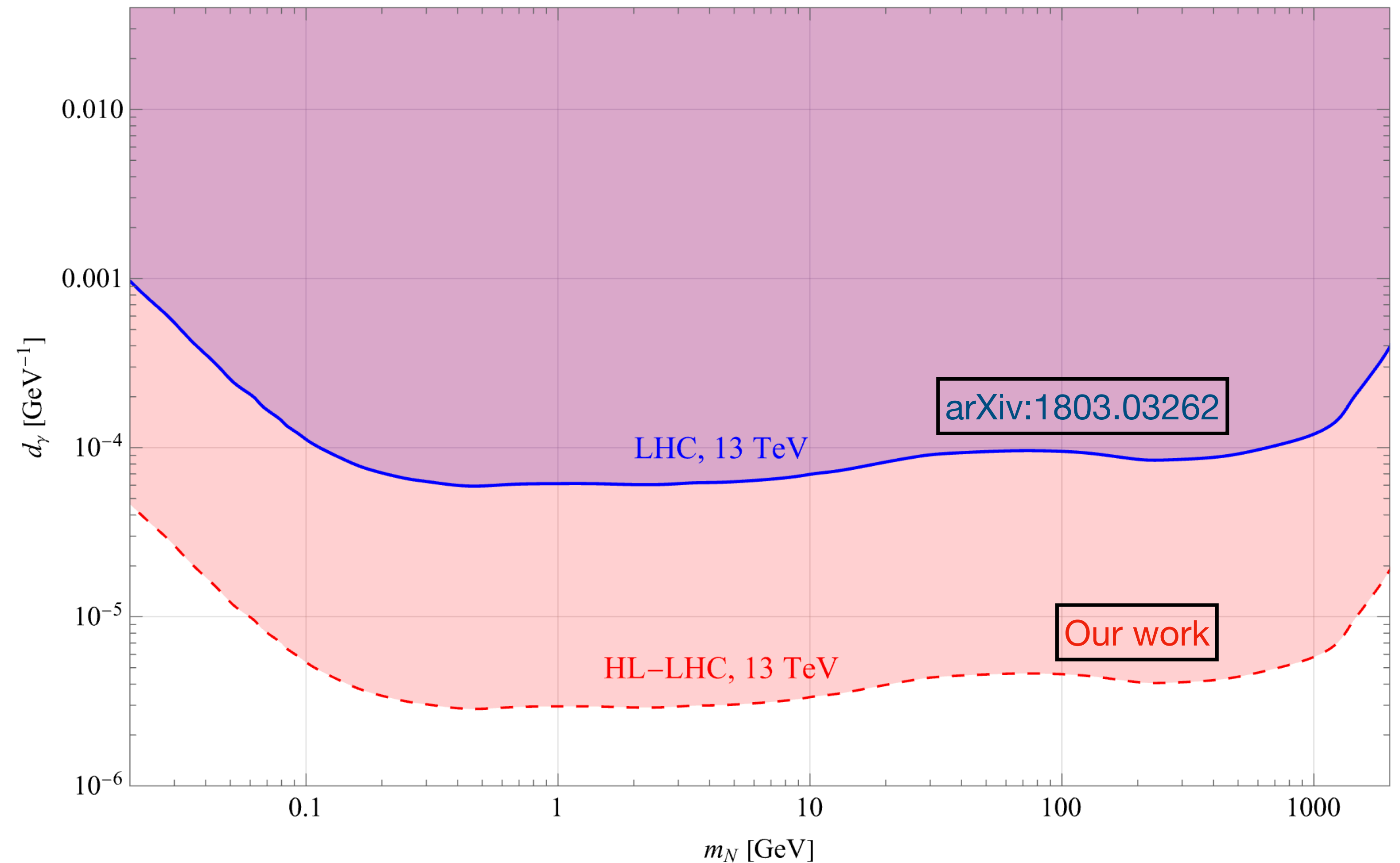
# Our results

With the constraint  $d_Z = 0$ ,  
high **energy** and **luminosity**  
increase the sensitivity  
to probe the  
parameters  $d_\gamma$  and  $m_N$



# Our results

- We can also explore the parameter space at the hadron collider
- With the constraint  $d_W = 0$ , high luminosity ( $36.1 \text{ fb}^{-1} \rightarrow 3000 \text{ fb}^{-1}$ ) improves the sensitivity by an order of magnitude



# Summary

- Calculated HNL production cross-section and decay widths analytically
- Evaluated sensitivity reach on  $d_\gamma$  (and  $m_N$ ) obtained from mono-photon signal events
- Plan to extend our investigation to other unique signals of HNL
- With the projected sensitivity on  $d_\gamma$  and  $m_N$ , unconstrained region in the parameter space  $(d_\gamma, m_N)$  can be tested at the proposed future colliders

**Backup...**

# Intensity and $d_\gamma$

## Derivation

$$S(B) = \sigma_{S(B)} \mathcal{L} \epsilon, \quad \sigma_S \propto d_\gamma^2$$

$$\frac{S}{\sqrt{B}} = \text{const} \times d_\gamma^2 \mathcal{L}^{1/2}$$

$$\frac{S}{\sqrt{B}} = 2.71 \quad (95 \% \text{ CL})$$

$$\therefore d_\gamma^2 \propto \mathcal{L}^{-1/2}$$

**High intensity** allows to

- access the “ $d_\gamma$ -well” deeper since limit for  $d_\gamma \propto \mathcal{L}^{-1/4}$

# Analysis

- Cuts applied on the future experiments:

- # of photons = 1

- # of leptons = 0

- $E_\gamma \notin [E_{z\gamma} \pm 5]$  (removes on-shell  $Z + \gamma$  background)  $\left( E_{z\gamma} = \frac{s - m_Z^2}{2\sqrt{s}} \right)$

- $E_\gamma > E_{\gamma,max}$  where  $E_{\gamma,max} = \frac{\sqrt{s}}{1 + \sin \theta_\gamma / \sin \theta_b}$  is the maximum photon

energy in individual event in SM

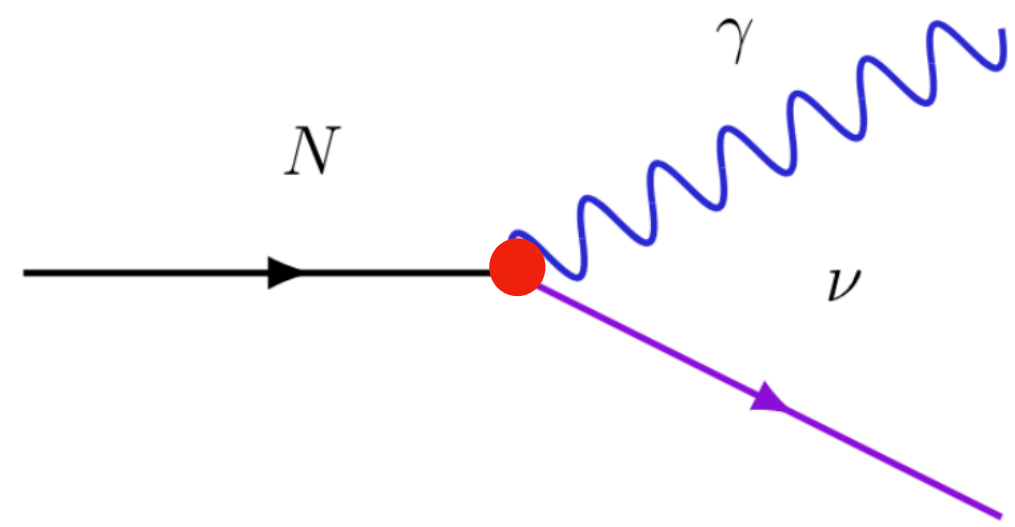
- Definition of visible particles:

- Visible photon:  $p_{T,\gamma} > 20 \text{ GeV}$ ,  $|\eta_\gamma| < 2.5$

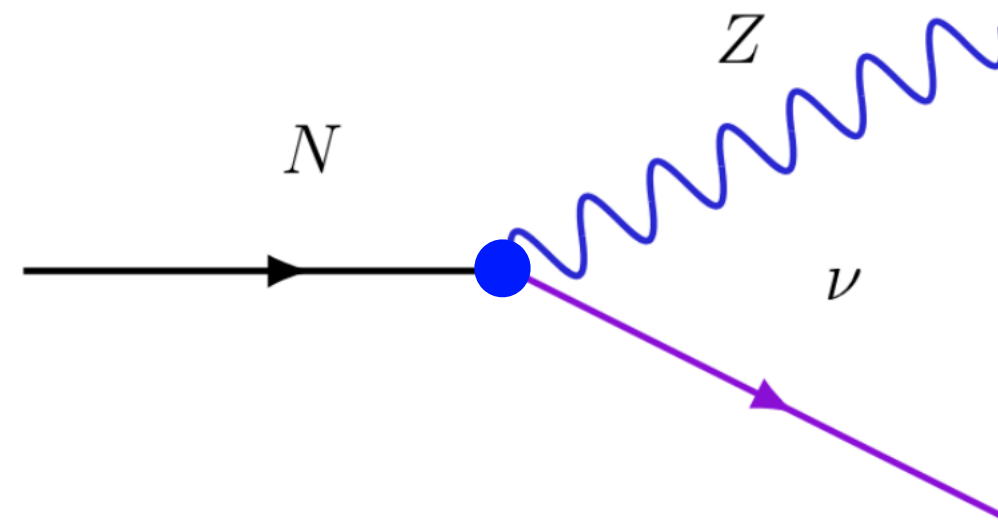
- Visible lepton:  $p_{T,\ell} > 20 \text{ GeV}$ ,  $|\eta_\ell| < 2.5$



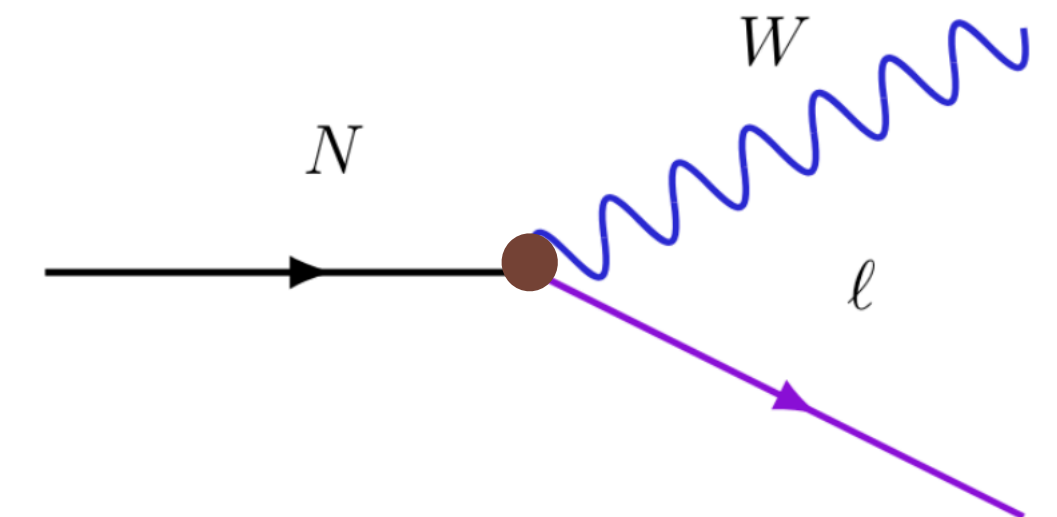
# Dipole couplings and decay widths



$$d_\gamma = \frac{ev}{\sqrt{2}\Lambda^2} (c_B + c_W)$$



$$d_Z = \frac{ev}{\sqrt{2}\Lambda^2} (c_W \tan \theta_w - c_B \cot \theta_w)$$



$$d_W = \frac{ev}{\Lambda^2} c_W \sin \theta_w$$

$$\Gamma_{N \rightarrow \nu \gamma} = \frac{d_\gamma^2 m_N^3}{2\pi}$$

$$\Gamma_{N \rightarrow \nu Z} = \frac{d_Z^2 (m_N^2 - M_Z^2) (2m_N^2 + M_Z^2)}{4\pi m_N^3}$$

$$\begin{aligned} \Gamma_{N \rightarrow W l} = & \frac{d_W^2}{4\pi m_N^3} \sqrt{((m_l - M_W)^2 - m_N^2)} \\ & \times \sqrt{((m_l + M_W)^2 - m_N^2)} \\ & \times \left[ 2(m_l^2 - m_N^2)^2 - M_W^2(m_l^2 + m_N^2) - M_W^4 \right] \end{aligned}$$

# Analytic results for the signal

Analytic expression for cross-section  $\sigma(\mu^+\mu^- \rightarrow \nu N)$

$$\sigma_\gamma = \frac{\alpha d_\gamma^2 (m^2 - s)^2 (2m^2 + s)}{3s^3}$$

$$\sigma_{\gamma Z} = \frac{\alpha d_\gamma d_Z (c_w^2 - 3s_w^2) (m^2 - s)^2 (2m_N^2 + s) (s - M_Z^2)}{6c_w s_w s^2 [(s - M_Z^2)^2 + \Gamma_Z^2 M_Z^2]}$$

$$\sigma_{\gamma W} = \frac{\alpha d_\gamma d_W}{\sqrt{2} s_w s^2} \left[ 2W^2 (-m^2 + s + W^2) \log \frac{-m_N^2 + s + M_W^2}{M_W^2} - (m_N^2 - s) (m_N^2 - s - 2M_W^2) \right]$$

$$\sigma_W = -\frac{\alpha d_W^2 (m_N^2 - s)}{2s_w^2 s^2} \left[ 2(m_N^2 - s) - (m_N^2 - s - 2M_W^2) \log \frac{-m_N^2 + s + M_W^2}{M_W^2} \right]$$

$$\sigma_{WZ} = -\frac{\alpha d_W d_Z (c_w^2 - s_w^2) (s - M_Z^2)}{2\sqrt{2} c_w s_w^2 s [(s - M_Z^2)^2 + \Gamma_Z^2 M_Z^2]} \left[ (m_N^2 - s) (m_N^2 - s - 2M_W^2) - 2M_W^2 (-m_N^2 + s + M_W^2) \log \frac{-m_N^2 + s + M_W^2}{M_W^2} \right]$$

$$\sigma_Z = \frac{\alpha d_Z^2 (c_w^4 - 2c_w^2 s_w^2 + 5s_w^4) (m_N^2 - s)^2 (2m_N^2 + s) (s - M_Z^2)}{24c_w^2 s_w^2 s [(s - M_Z^2)^2 + \Gamma_Z^2 M_Z^2]}$$

