

# Prospects for constraining light-quark electroweak couplings at Higgs factories

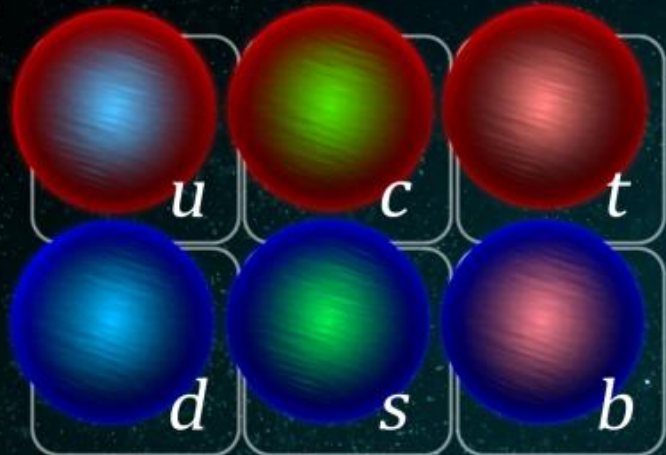
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based on work in collaboration with D. Jeans, J. Reuter, J. Tian, A.F. Żarnecki

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Quarks



Leptons



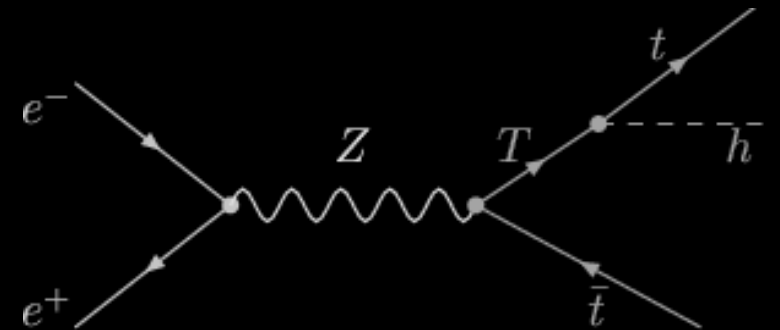
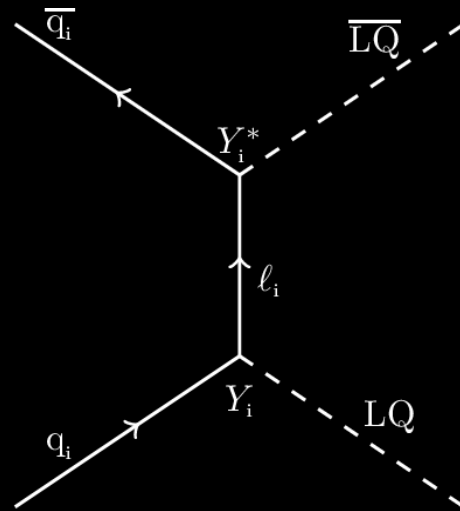
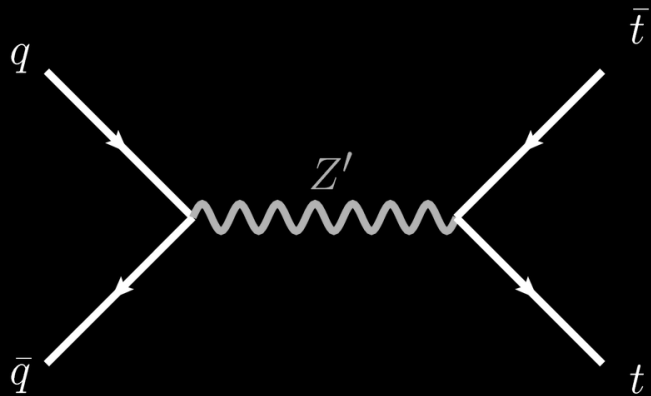
Higgs boson



Forces

A nice picture but it is not "self-explanatory":  
it contains many free parameters.

Measuring precision observables allows  
to constrain the SM parameters  
and to search for New Physics.



# Z decays to hadrons are constrained from LEP and SLC...

$$R_b = \Gamma(b\bar{b})/\Gamma(\text{hadrons})$$

$$\Gamma_{12}/\Gamma_8$$

OUR FIT is obtained by a simultaneous fit to several  $c$ - and  $b$ -quark measurements as explained in the note “The Z boson” and ref. LEP-SLC 06.

The Standard Model predicts  $R_b=0.21581$  for  $m_t=174.3$  GeV and  $M_H=150$  GeV.

VALUE	DOCUMENT ID	TECN	COMMENT
<b>0.21629 ± 0.00066</b> OUR FIT			
0.21594 ± 0.00094 ± 0.00075	1 ABE	05F SLD	$E_{\text{cm}}^{ee} = 91.28$ GeV
0.2174 ± 0.0015 ± 0.0028	2 ACCIARRI	00 L3	$E_{\text{cm}}^{ee} = 89-93$ GeV
0.2178 ± 0.0011 ± 0.0013	3 ABBIENDI	99B OPAL	$E_{\text{cm}}^{ee} = 88-94$ GeV
0.21634 ± 0.00067 ± 0.00060	4 ABREU	99B DLPH	$E_{\text{cm}}^{ee} = 88-94$ GeV
0.2159 ± 0.0009 ± 0.0011	5 BARATE	97F ALEP	$E_{\text{cm}}^{ee} = 88-94$ GeV

*Review of Particle Physics,  
PDG, 2022*

$$R_c = \Gamma(c\bar{c})/\Gamma(\text{hadrons})$$

$$\Gamma_{11}/\Gamma_8$$

OUR FIT is obtained by a simultaneous fit to several  $c$ - and  $b$ -quark measurements as explained in the note “The Z boson” and ref. LEP-SLC 06.

The Standard Model predicts  $R_c = 0.1723$  for  $m_t = 174.3$  GeV and  $M_H = 150$  GeV.

VALUE	DOCUMENT ID	TECN	COMMENT
<b>0.1721 ± 0.0030</b> OUR FIT			
0.1744 ± 0.0031 ± 0.0021	1 ABE	05F SLD	$E_{\text{cm}}^{ee} = 91.28$ GeV
0.1665 ± 0.0051 ± 0.0081	2 ABREU	00 DLPH	$E_{\text{cm}}^{ee} = 88-94$ GeV
0.1698 ± 0.0069	3 BARATE	00B ALEP	$E_{\text{cm}}^{ee} = 88-94$ GeV
0.180 ± 0.011 ± 0.013	4 ACKERSTAFF	98E OPAL	$E_{\text{cm}}^{ee} = 88-94$ GeV
0.167 ± 0.011 ± 0.012	5 ALEXANDER	96R OPAL	$E_{\text{cm}}^{ee} = 88-94$ GeV

$$\Gamma((u\bar{u} + c\bar{c})/2)/\Gamma(\text{hadrons})$$

$$\Gamma_9/\Gamma_8$$

This quantity is the branching ratio of  $Z \rightarrow$  “up-type” quarks to  $Z \rightarrow$  hadrons. Except ACKERSTAFF 97T the values of  $Z \rightarrow$  “up-type” and  $Z \rightarrow$  “down-type” branchings are extracted from measurements of  $\Gamma(\text{hadrons})$ , and  $\Gamma(Z \rightarrow \gamma + \text{jets})$  where  $\gamma$  is a high-energy ( $>5$  or  $7$  GeV) isolated photon. As the experiments use different procedures and slightly different values of  $M_Z$ ,  $\Gamma(\text{hadrons})$  and  $\alpha_S$  in their extraction procedures, our average has to be taken with caution.

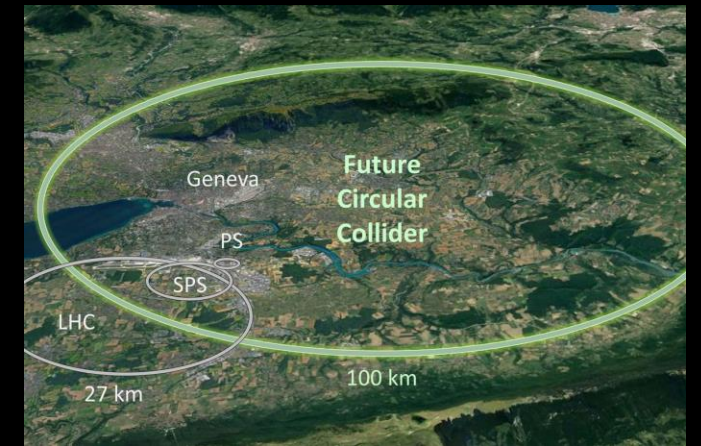
VALUE	DOCUMENT ID	TECN	COMMENT
<b>0.166 ± 0.009</b> OUR AVERAGE			
0.172 <sup>+0.011</sup> <sub>-0.010</sub>	1 ABBIENDI	04E OPAL	$E_{\text{cm}}^{ee} = 91.2$ GeV
0.160 ± 0.019 ± 0.019	2 ACKERSTAFF	97T OPAL	$E_{\text{cm}}^{ee} = 88-94$ GeV
0.137 <sup>+0.038</sup> <sub>-0.054</sub>	3 ABREU	95X DLPH	$E_{\text{cm}}^{ee} = 88-94$ GeV
0.137 ± 0.033	4 ADRIANI	93 L3	$E_{\text{cm}}^{ee} = 91.2$ GeV

...but not all of them!

Quantity	Value	Value (universal)	Standard Model
$\Gamma_{e^+e^-}$	$83.87 \pm 0.12$	$83.942 \pm 0.085$	$83.960 \pm 0.009$
$\Gamma_{\mu^+\mu^-}$	$83.95 \pm 0.18$	$83.941 \pm 0.085$	$83.959 \pm 0.009$
$\Gamma_{\tau^+\tau^-}$	$84.03 \pm 0.21$	$83.759 \pm 0.085$	$83.777 \pm 0.009$
$\Gamma_{\text{inv}}$	$498.9 \pm 2.5$	$500.5 \pm 1.5$	$501.445 \pm 0.047$
$\Gamma_{u\bar{u}}$	—	—	$299.89 \pm 0.20$
$\Gamma_{c\bar{c}}$	$300.3 \pm 5.3$	$300.0 \pm 5.2$	$299.81 \pm 0.20$
$\Gamma_{d\bar{d}}, \Gamma_{s\bar{s}}$	—	—	$382.77 \pm 0.14$
$\Gamma_{b\bar{b}}$	$377.4 \pm 1.3$	$377.0 \pm 1.2$	$375.73 \mp 0.18$
$\Gamma_{\text{had}}$	$1744.8 \pm 2.6$	$1743.2 \pm 1.9$	$1740.97 \pm 0.85$
$\Gamma_Z$	$2495.5 \pm 2.3$	$2495.5 \pm 2.3$	$2494.11 \pm 0.86$

*Review of Particle Physics,  
PDG, 2022*

Future  $e^+e^-$  colliders operating at the Z-pole would be a perfect place to study the couplings.



Source	$e^-e^+ \rightarrow c\bar{c}$				$e^-e^+ \rightarrow b\bar{b}$			
	$P_{e^-e^+}(-0.8, +0.3)$ $R_c$	$A_{FB}^{c\bar{c}}$	$P_{e^-e^+}(+0.8, -0.3)$ $R_c$	$A_{FB}^{c\bar{c}}$	$P_{e^-e^+}(-0.8, +0.3)$ $R_b$	$A_{FB}^{b\bar{b}}$	$P_{e^-e^+}(+0.8, -0.3)$ $R_b$	$A_{FB}^{b\bar{b}}$
<b>Statistics</b>	<b>0.18%</b>	<b>0.38%</b>	<b>0.27%</b>	<b>0.52%</b>	<b>0.12%</b>	<b>0.24%</b>	<b>0.23%</b>	<b>0.70%</b>
Preselection eff.	<0.01%	0.12%	0.02%	0.16%	<0.01%	0.08%	0.06%	0.12%
Background	0.01%	0.01%	0.02%	0.02%	0.01%	0.01%	0.06%	<0.01%
heavy quark mistag	0.11%	<0.01%	0.06%	<0.01%	0.12%	<0.01%	0.22%	<0.01%
<i>uds</i> mistag	0.03%	<0.01%	0.02%	<0.01%	0.08%	<0.01%	0.14%	<0.01%
Angular correlations	0.10%	0.10%	0.10%	0.10%	0.10%	0.10%	0.10%	0.10%
Beam Polarisation	<0.01%	<0.01%	0.02%	0.01%	<0.01%	0.01%	0.03%	0.15%
<b>Systematics</b>	<b>0.15%</b>	<b>0.16%</b>	<b>0.12%</b>	<b>0.19%</b>	<b>0.18%</b>	<b>0.13%</b>	<b>0.29%</b>	<b>0.22%</b>
<b>Total</b>	<b>0.24%</b>	<b>0.41%</b>	<b>0.30%</b>	<b>0.55%</b>	<b>0.21%</b>	<b>0.27%</b>	<b>0.37%</b>	<b>0.73%</b>

A. Irles *et al.*, [2306.11413]

The branching ratios to heavy quarks could be well constrained e.g. at ILC thanks to excellent flavour-tagging.

But how to take the measurement if...

- tagging is imperfect ( $s$  quark)?
- tagging is unavailable ( $u, d$  quarks)?



How to measure Z couplings  
to light quarks?

# General idea

We want to measure quark couplings:

$$c_f = v_f^2 + a_f^2$$

They are given in the SM by:

$$v_f = 2I_{3,f} - 4Q_f \sin^2 \theta_W \quad a_f = 2I_{3,f}$$

$\Gamma_{had}$  reads (exact at fixed order):

$$\Gamma_{had} = N_c \frac{G_\mu M_Z^3}{24\pi\sqrt{2}} \left( 1 + \frac{\alpha_s}{\pi} + \dots \right) (3c_d + 2c_u)$$

and  $\Gamma_{had+\gamma}$ :

$$\Gamma_{had+\gamma} = N_c \frac{G_\mu M_Z^3}{24\pi\sqrt{2}} f(y_{cut}) \frac{\alpha}{2\pi} (3q_d^2 c_d + 2q_u^2 c_u)$$

The correction factor  $f(y_{cut})$  to be determined for a given value of the resolution parameter  $y_{cut}$ .

# Measurement at the Z-pole

We can measure radiative and non-radiative cross sections separately and disentangle the couplings  $c_d$  and  $c_u$ :

$$\sigma_{Z \rightarrow had} = \mathcal{C}_1 \cdot (3c_d + 2c_u)$$

$$\sigma_{Z \rightarrow had+\gamma} = \mathcal{C}_2 \cdot (3c_d + 8c_u)$$

Note: in this picture, the couplings are universal among quarks of the same type. This assumption can be lifted by employing heavy-flavour tagging.

How to generate Monte Carlo  
events?

# Analysis setup

We want to consider:

$$e^+ e^- \rightarrow q\bar{q}(\gamma)$$

Experimentally measured photons can originate not only from the Final State Radiation but also from the Initial State Radiation, hadronisation and decays...

One may encounter the following issues:

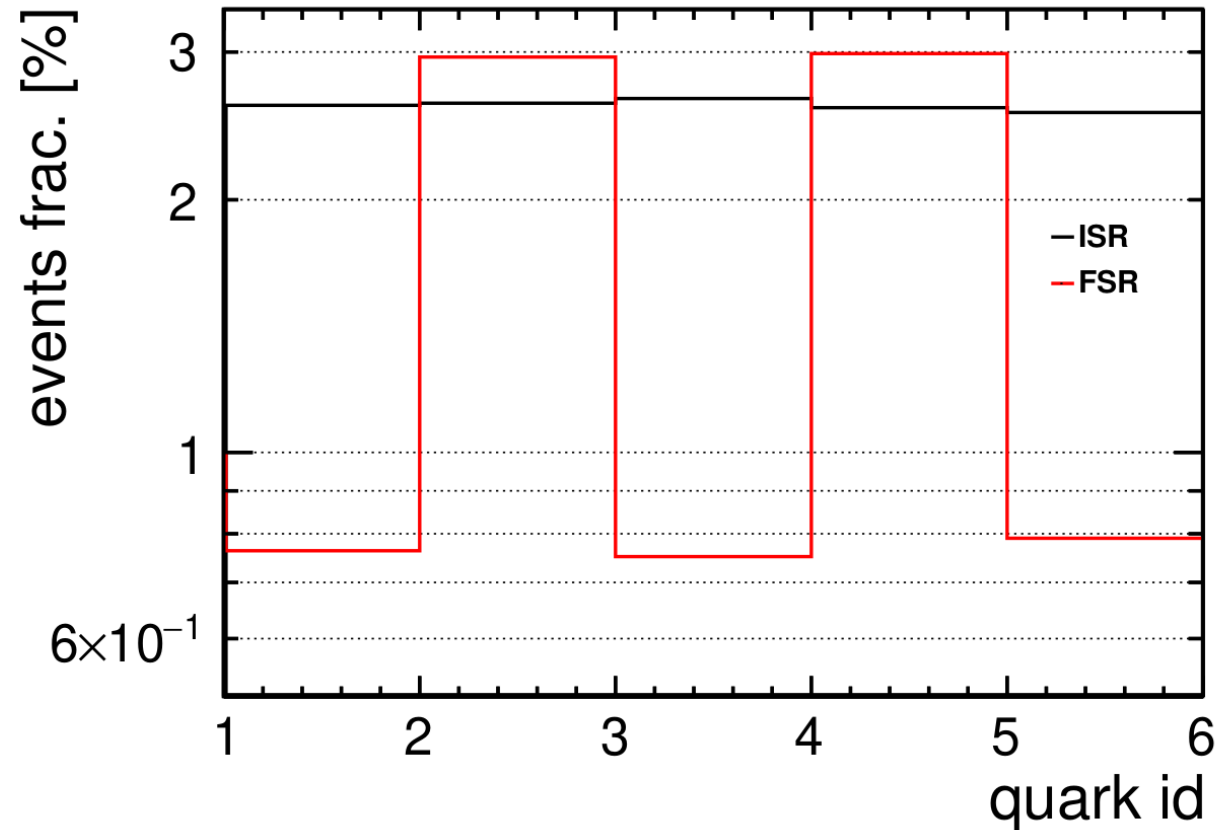
- **Matrix Element** calculations may be either divergent or very slow for small photon-emission angles,
- **ISR structure functions** can be used for small angles but a proper matching procedure is needed,
- **FSR showers** are important to account for QCD emissions but they may cause double-counting,
- photons coming from **hadronisation** and **hadron decays** have to be included properly.

# Matching procedure – *Whizard* perspective

- matching: *soft* physics invisible in the detector, hard physics properly reconstructed
- soft ISR photons simulated using built-in structure functions
- soft FSR photons simulated using parton showers
- hard photons simulated using full ME calculations
  - momentum transfer and energy to define *soft* and *hard* regimes

# Efficiency of the matching procedure

- About 4% of *Whizard* events are rejected to avoid double-counting.



# How to select events?

*work in progress*



# Event reconstruction

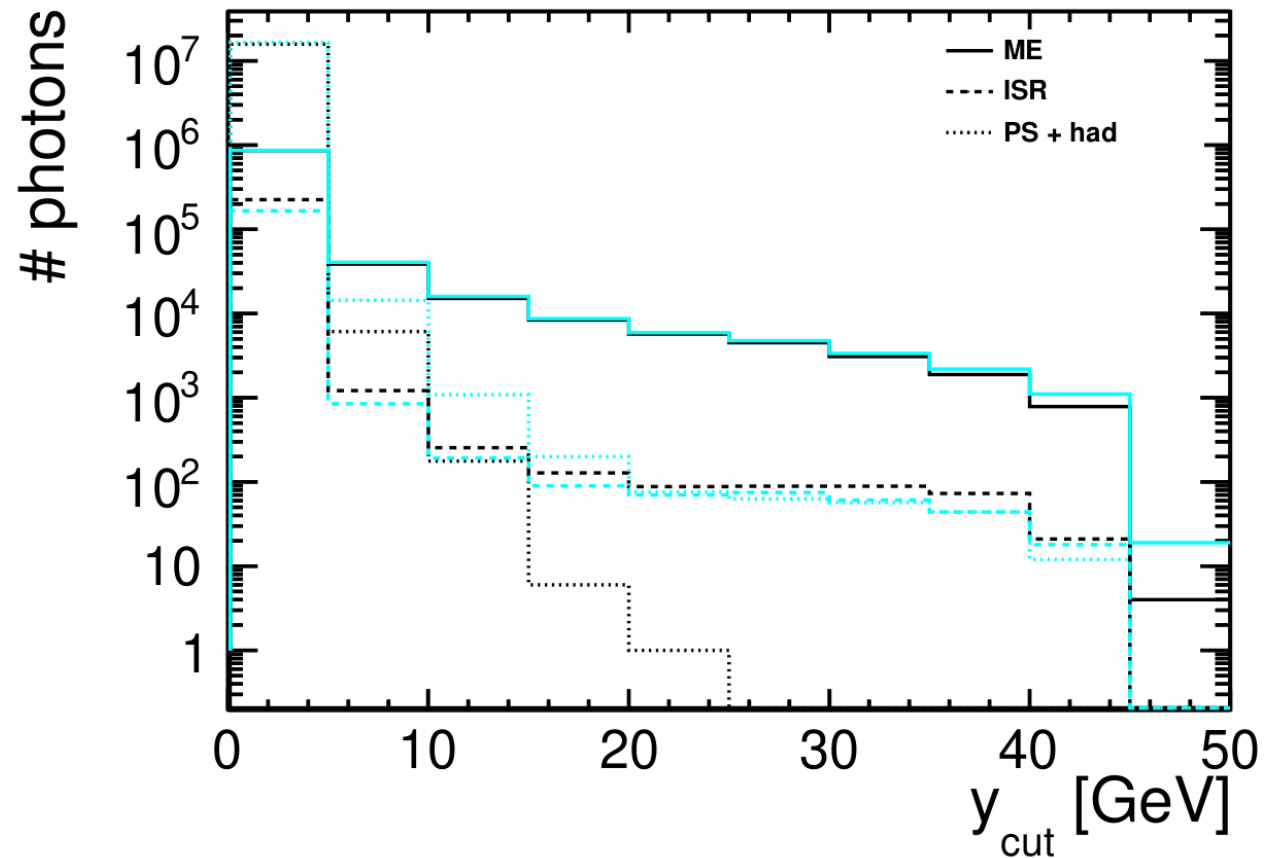
Measurable photons can originate from:

- Initial State Radiation,
- Final State Radiation,
- hadronisation and decays.

The interesting information comes only from FSR so reconstruction criteria should reduce other contributions.

# Isolation criterion $y_{\text{cut}}$

$$y_{\text{cut}} = E_{\gamma} \cdot \sin(\theta_{\gamma q_i}^{\text{min}})$$



preliminary

# Conclusions

- Couplings of the Z boson to light quarks are poorly constrained but an improvement could be achieved at future lepton colliders.
- Proper assessment of the uncertainties requires a deep understanding of theoretical calculations, event simulation and reconstruction.
- *Work in progress...*