
Flavor violating Higgs and Z decays at FCC-ee

— DPF-Pheno 2024 —
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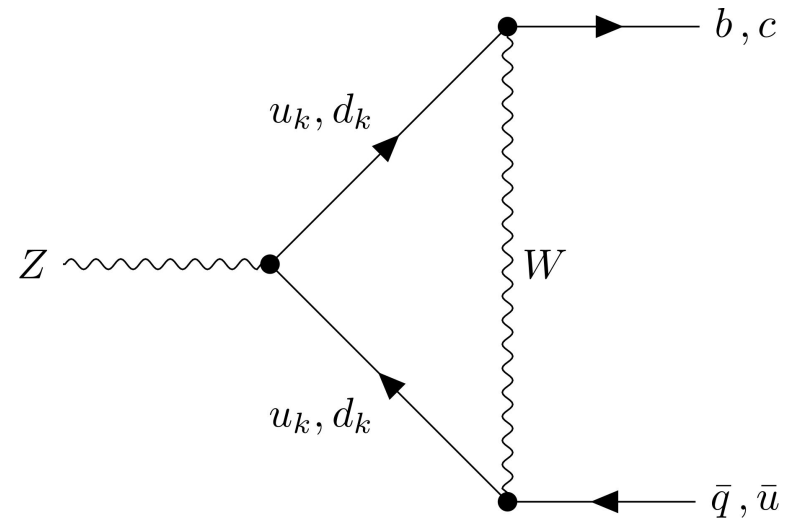
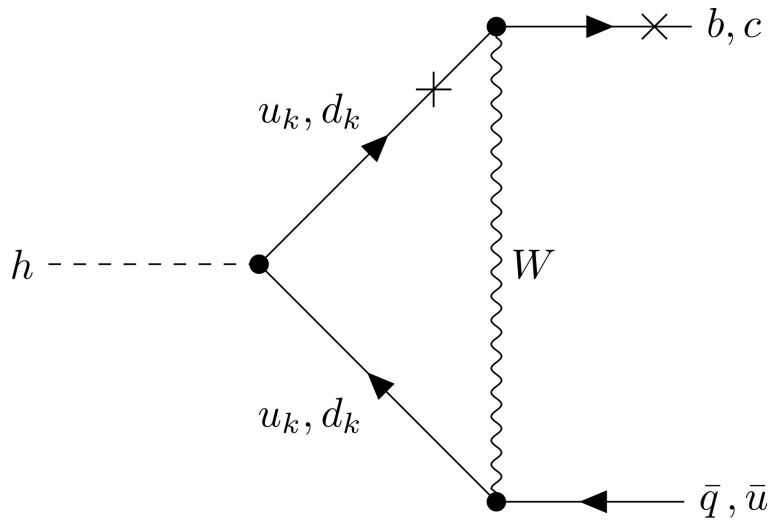
This talk

Based on [recent work](#) by J.F. Kamenik, A. Korajac, M.S., M. Tammaro and J. Zupan

We translate **advances in flavor tagging** with **novel statistical analysis techniques** to bounds on **Z/h \rightarrow bs, cu couplings** in future high energy **high statistics** ee-colliders

We compare to **updated SM predictions** and **BSM benchmarks** and find that FCC-ee can place bounds on **h \rightarrow bs,cu** that are **phenomenologically relevant**

Flavor Changing Neutral Currents



SM Prediction

We update the **SM predictions** for **B(h/Z→bs,bd,cu)** obtaining

$$\Gamma(h \rightarrow b\bar{s}) = (1.8 \pm 0.3) \times 10^{-10} \text{GeV} \quad \Gamma(h \rightarrow b\bar{d}) = (7.9 \pm 1.3) \times 10^{-12} \text{GeV}$$

$$\Gamma(Z \rightarrow b\bar{s}) = (5.2 \pm 0.9) \times 10^{-8} \text{GeV} \quad \Gamma(Z \rightarrow b\bar{d}) = (2.3 \pm 0.4) \times 10^{-9} \text{GeV}$$

with h/Z→cu being $O(10^6)$ smaller than h/Z→bs.

The main uncertainties are **CKM matrix elements** uncertainties (**~2%**) + **higher order QCD corrections**, which we estimate via partial two-loop mixed QCD-EW corrections (**~17%**)

Constraints

Indirect constraints much better than direct and $Z \rightarrow qq'$ much more constrained than $h \rightarrow qq'$

Decay	SM prediction	exp. bound	indir. constr.
$\mathcal{B}(h \rightarrow bs)$	$(8.9 \pm 1.5) \cdot 10^{-8}$	0.16	2×10^{-3}
$\mathcal{B}(h \rightarrow bd)$	$(3.8 \pm 0.6) \cdot 10^{-9}$	0.16	10^{-3}
$\mathcal{B}(h \rightarrow cu)$	$(2.7 \pm 0.5) \cdot 10^{-20}$	0.16	2×10^{-2}
$\mathcal{B}(Z \rightarrow bs)$	$(4.2 \pm 0.7) \cdot 10^{-8}$	2.9×10^{-3}	6×10^{-8}
$\mathcal{B}(Z \rightarrow bd)$	$(1.8 \pm 0.3) \cdot 10^{-9}$	2.9×10^{-3}	6×10^{-8}
$\mathcal{B}(Z \rightarrow cu)$	$(1.4 \pm 0.2) \cdot 10^{-18}$	2.9×10^{-3}	4×10^{-7}

FCC-ee

Very **clean environment** with **high statistics** + **controlled backgrounds** → **Precision machine.**

For $h \rightarrow qq'$, we can consider **Zh production with dileptonic Z** ($Z \rightarrow \text{MET}$ can be used as well but backgrounds differ) → $N_h = 6.7 \times 10^5$ before Z decay

For $Z \rightarrow qq'$, we simply look at the **Z pole** → $N_Z = 5 \times 10^{12}$



Analysis strategy

Our proposal is very simple. Let's take as an example $Z/h \rightarrow bs$.

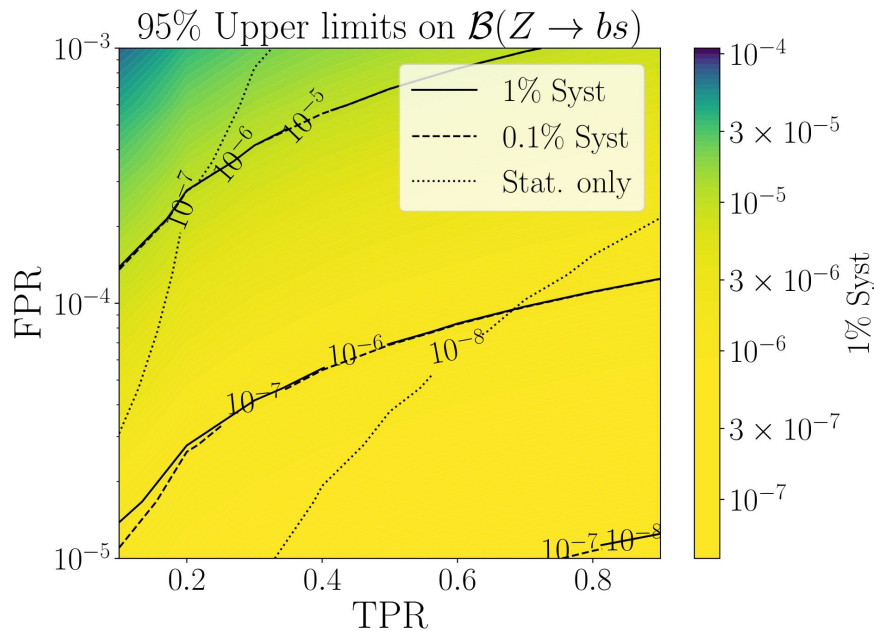
- We **select events** based on the appropriate di-jet channel, $Z(\rightarrow \ell\ell)h(\rightarrow jj)$ or $Z \rightarrow jj$. We obtain the total number of events \mathbf{N} .
- We **tag each jet** in each event using **two orthogonal b- and s-taggers**.
- We obtain the **measured events in each (n_b, n_s) bin, $\mathbf{N}_{b,s}$** . $(n_b, n_s) = \{(0,0), (0,1), (1,0), (1,1), (0,2), (2,0)\}$.
- We describe the relationship between $\mathbf{N}_{b,s}$ and \mathbf{N} with a **probabilistic model depending on $\mathbf{B}(Z/h \rightarrow bs)$** .
- We use this model to **perform statistical tests on $\mathbf{B}(Z/h \rightarrow bs)$** .

Results: $Z \rightarrow bs$

We scan over possible orthogonal b- and s-taggers with systematics. **TPR and FPR assume common efficiencies for both taggers.**

If no systematic uncertainties, the SM value could be reached. $Z \rightarrow qq'$ we are **systematics dominated**.

When the systematics are **very small but non-zero**, the upper limits are generally **above the SM values and the indirect constraints**.

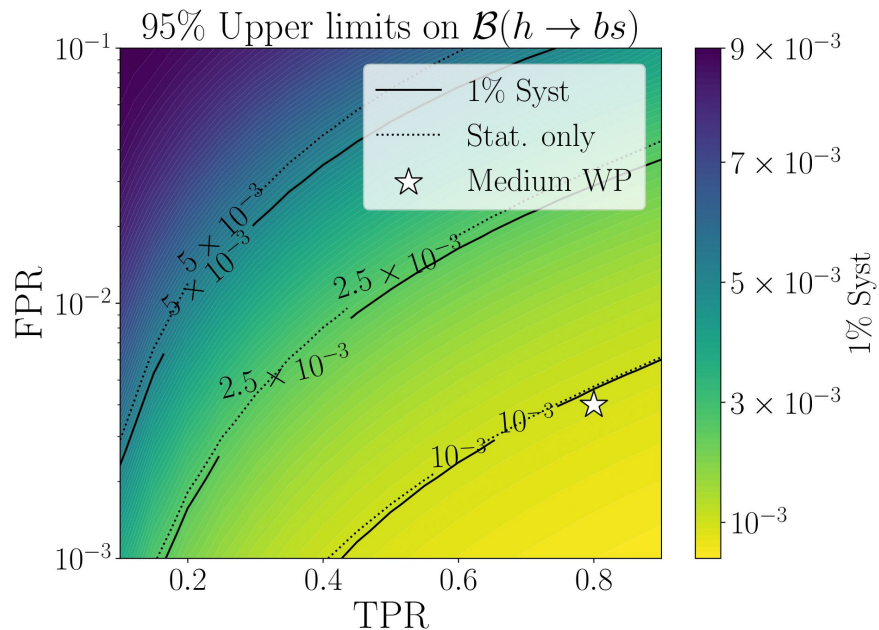


Results: $h \rightarrow bs$

We scan over possible orthogonal b- and s-taggers with systematics. **TPR and FPR assume common efficiencies for both taggers.**

The systematic uncertainties (**small**, but **achievable** with future dedicated calibrations) are **not too impactful here**. The analysis is **statistics dominated**.

The addition of the s-tagger **greatly increases the performance** of the analysis and yields an **upper limit on $\mathcal{B}(h \rightarrow bs)$ that could be better than indirect constraints**.



Constraints on BSM effects

We use an **effective lagrangian** to capture any BSM effects in $B(h/Z \rightarrow bs)$ (we can do something similar for bd, cu)

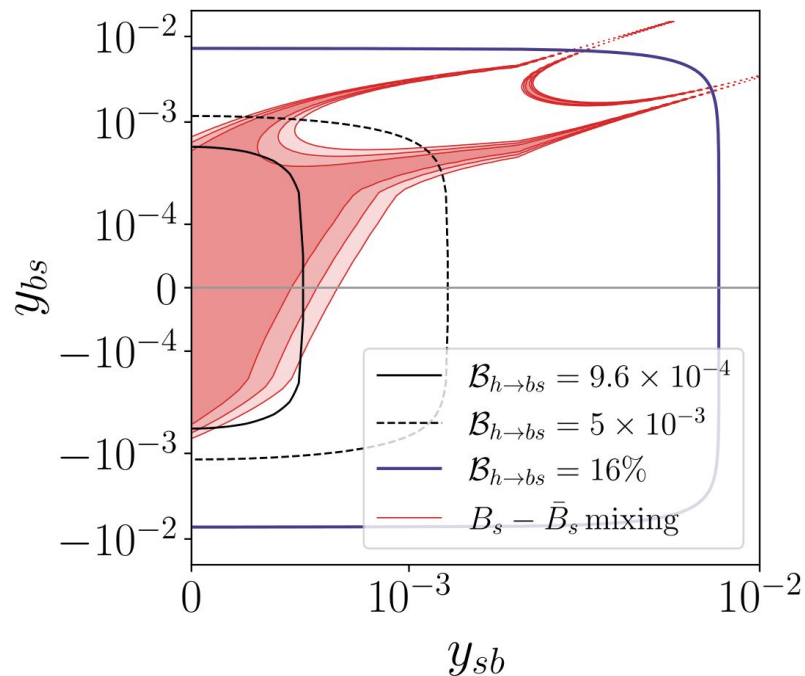
$$\mathcal{L} \supset y_{sb}(\bar{s}_L b_R)h + y_{bs}(\bar{b}_L s_R)h + \text{h.c.}$$

$$\mathcal{L} \supset g_{sb}^L(\bar{s}_L \gamma_\mu b_L)Z^\mu + g_{sb}^R(\bar{s}_R \gamma_\mu b_R)Z^\mu + \text{h.c.}$$

Results: $h \rightarrow bs$

When comparing explicitly with low-energy constraints, we observe how **the FCC-ee can probe regions indirect searches cannot.**

Black lines are **upper limits** from **FCC-ee**, **magenta** lines are **upper limits** from **LHC** and **red** regions correspond to the **allowed parameter space** at 1-, 2- and 3- σ level from **low-energy constraints**



Outlook

The FCC-ee has the potential to **explore flavor changing decays of the Higgs and Z bosons**, with similar expectations for the CEPC.

We **updated the SM predictions** for the $h/Z \rightarrow bs, bd, cu$ branching ratios. These are **orders of magnitude smaller than the FCC-ee reach**, so any signal in these channels would unambiguously imply existence of New Physics

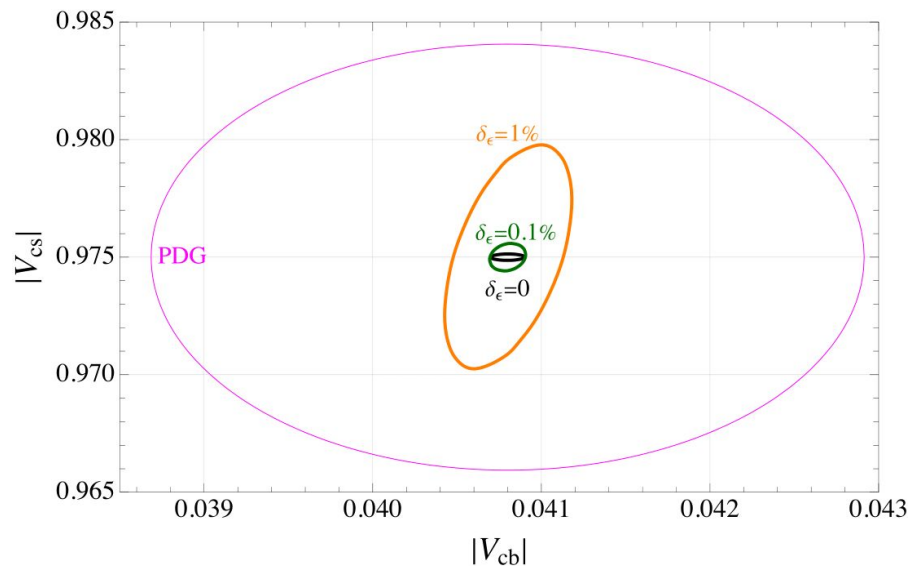
For $B(Z \rightarrow bs, bd, cu)$, indirect constraints already push towards the SM value which is **unreachable** without **almost perfectly calibrated perfect taggers**.

The projected sensitivities to $B(h \rightarrow bs, cu)$ go **well beyond the current constraints** from indirect probes. Even with only the b-tagger, the projected reach could probe significant portions of unconstrained NP parameter space.

And more...

In [arxiv:2405.08880](https://arxiv.org/abs/2405.08880) (by D. Marzocca, M.S. and M. Tammaro), similar techniques for $|V_{cs}|$ and $|V_{cb}|$ determination via $WW \rightarrow$ all hadronic @ FCC-ee

- Lattice free determination
- Possible solution to tension between inclusive vs exclusive $|V_{cb}|$ from meson decays.





Backup slides

Flavor Changing Neutral Currents

We update the **SM predictions** for **$\mathbf{B}(h \rightarrow bs, bd, cu)$** (see arXiv:1506.02718 and arXiv:2009.07166) and **$\mathbf{B}(Z \rightarrow bs, bd)$** (see Phys. Rev. D 22, 214 (1980)., Phys. Rev. D 27, 570 (1983) and Phys. Rev. D 27, 579 (1983))

We compute the **one-loop decay amplitude**

$$\Gamma(h/Z \rightarrow b\bar{q}) = N_C \frac{|\bar{\mathcal{M}}(h/Z \rightarrow q\bar{q}')|^2}{16\pi m_{h/Z}}$$

We perform the computation numerically with FeynArts+FeynCalc+LoopTools. We cross-checked results with Package-X and also checked that all the m_q -independent terms in the amplitude vanish due to the CKM unitarity;

Flavor Changing Neutral Currents

The experimental inputs are (when necessary we run to the appropriate scale through 3-loop RGE)

param.	value	param.	value	param	value
$ V_{tb} $	$0.999142^{+0.000018}_{-0.000023}$	$ V_{ts} $	$0.04065^{+0.00040}_{-0.00055}$	$ V_{td} $	$0.008519^{+0.000075}_{-0.000146}$
$m_t(m_Z)$	$171.512 \pm 0.329 \text{ GeV}$	$m_t(m_h)$	$167.036 \pm 0.315 \text{ GeV}$		
$m_b(m_Z)$	$2.871 \pm 0.024 \text{ GeV}$	$m_b(m_h)$	$2.796 \pm 0.024 \text{ GeV}$		
m_Z	$91.1876 \pm 0.0021 \text{ GeV}$	m_W	$80.377 \pm 0.012 \text{ GeV}$	m_h	$125.25 \pm 0.17 \text{ GeV}$
$\alpha^{-1}(m_Z)$	127.955 ± 0.009	$\alpha^{-1}(m_h)$	127.506 ± 0.009	$s_W^2(m_Z)$	0.23122 ± 0.00004
$\alpha_s(m_Z)$	0.1179 ± 0.0009	$\alpha_s(m_h)$	0.1126 ± 0.0008	$\alpha_s(m_t)$	0.1076 ± 0.0007

Flavor Changing Neutral Currents

The **direct constraints** are from LHC searches for $h \rightarrow$ others and from LEP measurements of the Z hadronic width.

The **main (or only) indirect constraints** are B_s mixing for $h \rightarrow bs$, B_d mixing for $h \rightarrow bd$, D mixing for $h \rightarrow cu$, $b \rightarrow s\ell^+\ell^-$ transitions for $Z \rightarrow bs$, B_d mixing for $Z \rightarrow bd$ and $B(D^0 \rightarrow \mu^+\mu^-)$ for $Z \rightarrow cu$

Putting it all together: **indirect constraints much better than direct** and **$Z \rightarrow qq'$ much more constrained than $h \rightarrow qq'$**

Analysis strategy

As a first approximation, we can **disregard all backgrounds that aren't $Zh, h \rightarrow bb, cc, ss, gg$ or $Z \rightarrow qq$** , mainly the $\tau^+\tau^-$ for $Z \rightarrow bs$ and the Drell-Yan, $W W$, ZZ for $h \rightarrow bs$.

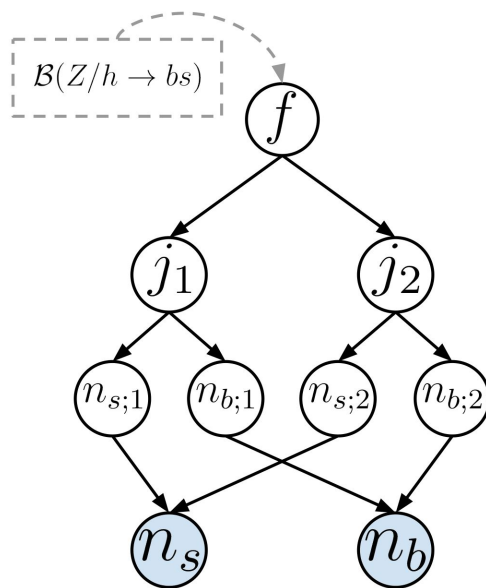
These other processes correspond to **subleading effects** and could be **reduced through optimized selection** or **incorporated into the analysis** as a re-scaling of the flavor-conserving contributions.

Because we are doing a proof-of-concept, we **avoid the use of dedicated MC simulations** and consider our model to be enough of a **faithful representation of the real physics** that it can be used to generate pseudo-data.

Analysis strategy

We follow arXiv:2209.01222 (see also arXiv:2201.11428,, arXiv:2004.12181) to **leverage orthogonal taggers** to extract information regarding small FCNC.

For example, for $h/Z \rightarrow bs$, we **categorize di-jet events** in terms of the number of **s-tagged** n_s and **b-tagged** n_b jets. The expected populations will depend on **BR($h/Z \rightarrow bs$)**



Analysis strategy

We write the **probabilistic model** in terms of efficiencies and of the relevant Branching ratios.

$$\bar{N}_{(n_b, n_s)} = \sum_f p(n_b, n_s | f, \nu) \bar{N}_f(\nu) \quad \bar{N}_f = \mathcal{B}(Z/h \rightarrow f) N_{Z/h} \mathcal{A}$$

We define a **parameter of interest** $\mu = \frac{\mathcal{B}(Z/h \rightarrow bs)}{\mathcal{B}(Z/h \rightarrow bs)_{\text{SM}}}$

and an **appropriate likelihood**

$$\mathcal{L}(\mu, \nu) = \mathcal{P}(N_{(n_b, n_s)} | \bar{N}_{(n_b, n_s)}(\mu, \nu)) p(\nu)$$

Analysis strategy

We **profile the likelihood** over a set of nuisance parameters and construct the **profile likelihood ratio**

$$\lambda(\mu) = \frac{\mathcal{L}(\mu, \hat{\nu}(\mu))}{\mathcal{L}(\hat{\mu}, \hat{\nu})}$$

which is used to compute the **test statistic**

$$t_{\mu} = -2 \text{Ln } \lambda(\mu)$$

With this we compute **95% CL upper limits** assuming $\mu_{\text{true}} = 0$ and solving for $t_{\mu} = (\Phi^{-1}(0.95))^2$. Due to the high statistics and simplicity of the strategy, we can use an **Asimov dataset** instead of using ensembles of pseudo-data.

Nuisance Parameters

Nuisance Param.	Nominal Value	Rel. uncert. (%)
$\mathcal{B}(h \rightarrow gg)$	1.4%	1.2
$\mathcal{B}(h \rightarrow ss)$	0.024%	160
$\mathcal{B}(h \rightarrow cc)$	2.9%	2.8
$\mathcal{B}(h \rightarrow bb)$	56%	0.4
$\epsilon_{\beta}^{\alpha}$	See text	1.0
N_h	6.7×10^5	0.5
\mathcal{A}	0.70	0.1

Nuisance param.	Nominal value	Rel. uncert. (in %)
$\mathcal{B}(Z \rightarrow uu + dd)$	27.01%	5.0
$\mathcal{B}(Z \rightarrow ss)$	15.84%	3.8
$\mathcal{B}(Z \rightarrow cc)$	12.03%	1.7
$\mathcal{B}(Z \rightarrow bb)$	15.12%	0.33
$\epsilon_{\beta}^{\alpha}$	See text	1.0
N_Z	5×10^{12}	10^{-3}
\mathcal{A}	0.994	10^{-3}

Possible BSM benchmarks

The $h \rightarrow bs$ effects can be generated in a **Two Higgs Doublet Model (2HDM)**. If we **decouple the heavy scalar H and pseudoscalar A** and assuming **no diagonal couplings of the second doublet**, we obtain

$$\mathcal{L}_{\text{Yukawa}} \supset - \left(\frac{m_i}{v} \delta_{ij} c_\alpha - Y_{ij}^d s_\alpha \right) \bar{d}_{Li} d_{Rj} h + \text{h.c.} + \dots$$

All SM predictions are re-scaled by c_α^2 and the couplings we are interested in will be $\mathbf{y}_{qq'} = \mathbf{Y}_{qq'} \mathbf{s}_\alpha$

Possible BSM benchmarks

The $Z \rightarrow bs$ and $h \rightarrow bs$ effects can be generated at the same time with **Vector-Like Quarks**. e.g. vector-like singlet down-type quarks, (D_L, D_R) , singlets under $SU(2)_L$ and with hypercharge $-1/3$. We obtain the FCNC from the mixture with the SM down-type quarks after EWSB

$$\mathcal{L}_{\text{VLQ}}^D \supset \frac{g}{2c_W} X_{ij}^d (\bar{d}^i \gamma^\mu P_L d^j) Z_\mu + X_{ij}^d \frac{m_j}{v} (\bar{d}^i P_R d^j) h + \text{h.c.}$$

we can read $\mathbf{g}_{qq'}$ and $\mathbf{y}_{qq'}$ as different combinations of $\mathbf{X}_{qq'}$. We can do the same with a vector-like doublet with hypercharge $1/6$ to get different chiralities.

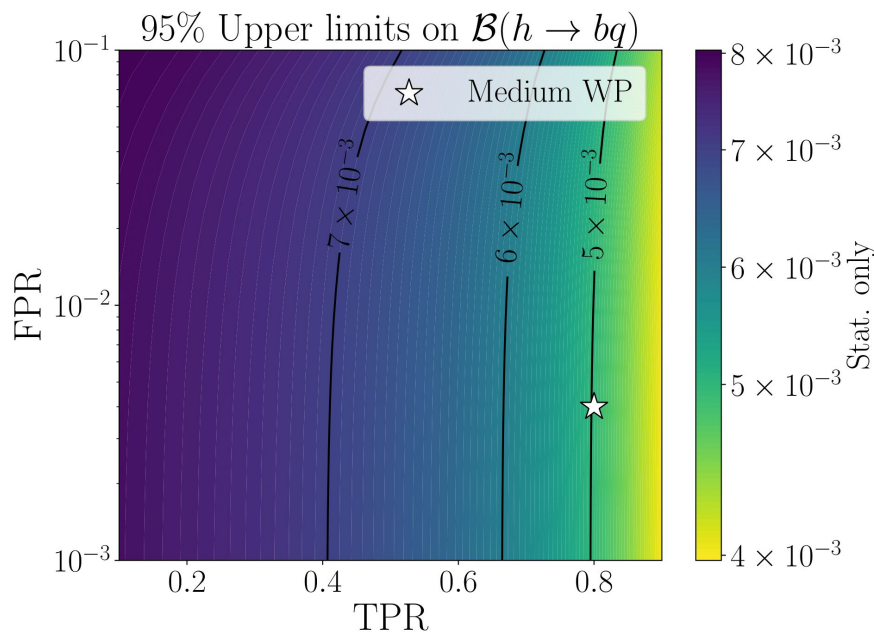
Results: Higgs

We obtain limits on $\mathbf{B}(h \rightarrow bs) + \mathbf{B}(h \rightarrow bd)$ by using **only a b-tagger**.

We scan over possible taggers by assuming **identical True Positive Rates (TPRs)** and **False Positive Rates (FPRs)** for **all taggers**.

With no systematics, we observe that for $\text{FPR} < 10^{-2}$ (after the FPR saturates) and TPR in $[0.4, 0.8]$ we are **already in an interesting region for BSM limits**.

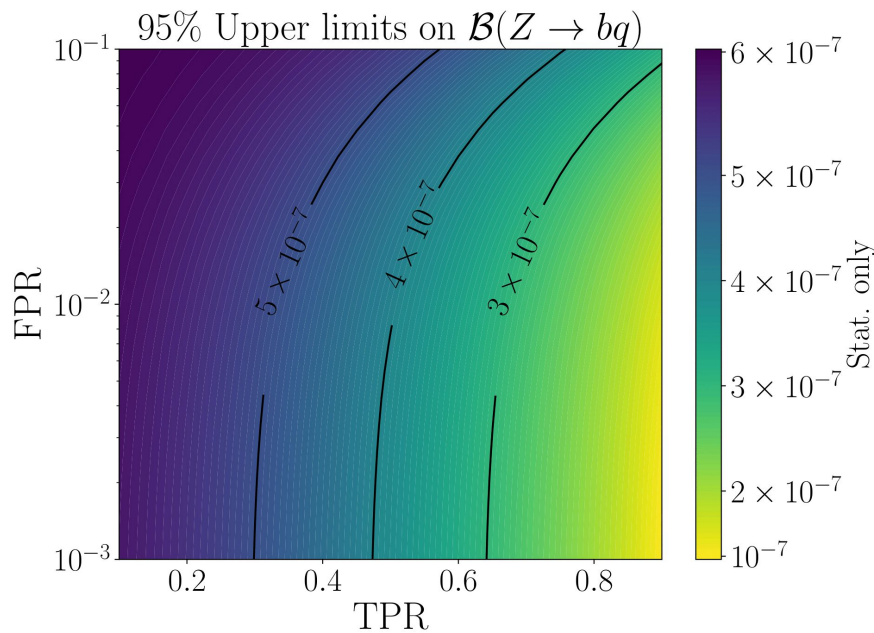
We show with a star a tagger based on reported taggers in the literature.



Results: Z boson

For $\text{BR}(Z \rightarrow bs) + \text{BR}(Z \rightarrow bd)$ with a **b-tagger**, the limits are **lower than for $h \rightarrow qq'$** due to the **higher statistics** even if there is **no asymmetry between $Z \rightarrow bb$ and $Z \rightarrow ss$** to enhance the analysis.

However, the **indirect limits are much better** and this **analysis is not competitive**.



Results: $h \rightarrow bs$

We also use **explicit Tight and Medium WPs** derived from **reported taggers**

$$\text{Loose :} \quad \epsilon_{\beta;\text{Loose}}^b = \{0.02, 0.001, 0.02, 0.90\}, \quad \epsilon_{\beta;\text{Loose}}^s = \{0.20, 0.90, 0.10, 0.01\},$$

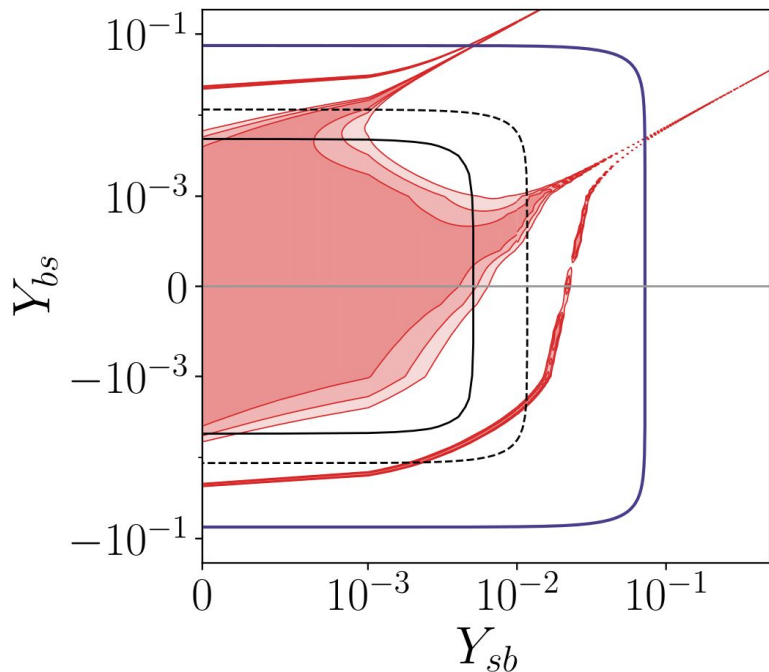
$$\text{Medium :} \quad \epsilon_{\beta;\text{Med}}^b = \{0.007, 0.0001, 0.003, 0.80\}, \quad \epsilon_{\beta;\text{Med}}^s = \{0.09, 0.80, 0.06, 0.004\},$$

All WPs are **similar** and provide **competitive limits**. Additionally, they are consistent with the approximate scan shown before.

ϵ_{β}^b	ϵ_{β}^s	$\mathcal{B}(h \rightarrow bs)$ (95% CL)
$\epsilon_{\beta;\text{Loose}}^b$	$\epsilon_{\beta;\text{Loose}}^s$	1.3×10^{-3}
$\epsilon_{\beta;\text{Loose}}^b$	$\epsilon_{\beta;\text{Med}}^s$	9.6×10^{-4}
$\epsilon_{\beta;\text{Med}}^b$	$\epsilon_{\beta;\text{Loose}}^s$	1.4×10^{-3}
$\epsilon_{\beta;\text{Med}}^b$	$\epsilon_{\beta;\text{Med}}^s$	1.0×10^{-3}

Results: $h \rightarrow bs + 2\text{HDM}$

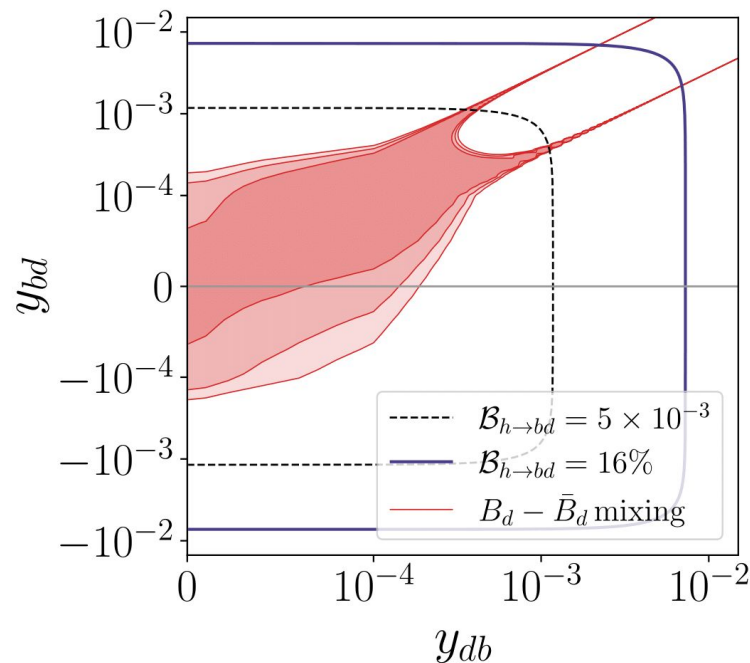
We consider $m_H = m_A = 1 \text{ TeV}$ and different values of s_α . Although the details change, the conclusions hold: **the FCC-ee can probe regions indirect searches cannot.**



Results: $h \rightarrow bd$

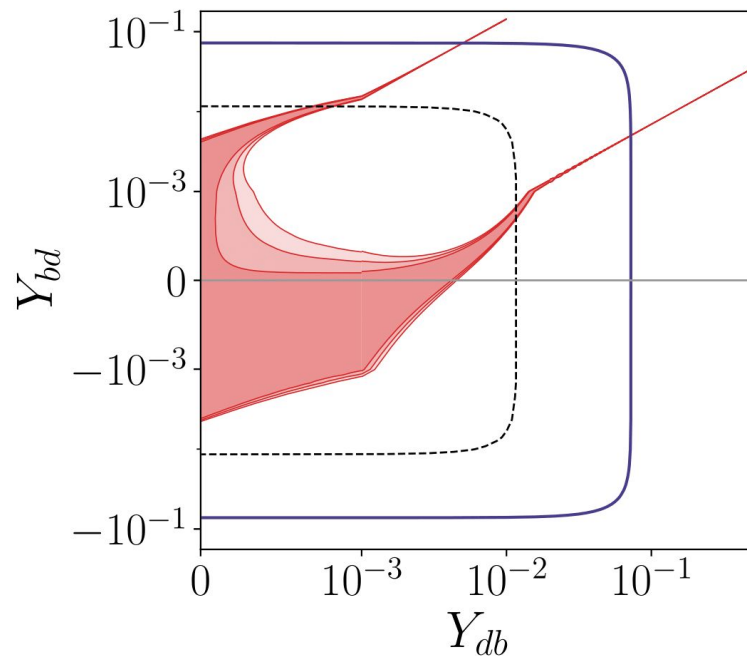
When comparing explicitly with low-energy constraints, we observe how **the FCC-ee can probe regions indirect searches cannot.**

The right plot assumes **no effects from H and A.**



Results: $h \rightarrow bd + 2\text{HDM}$

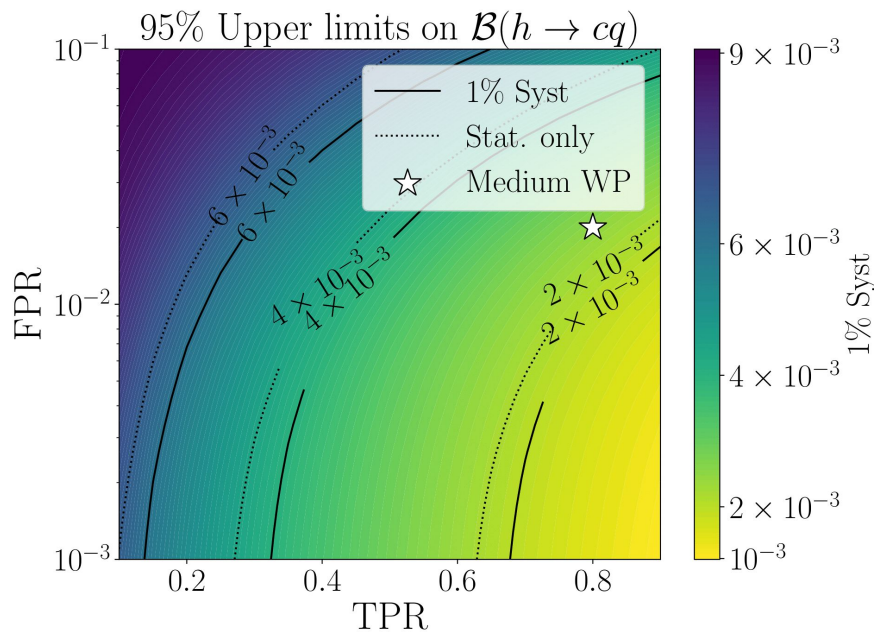
If we consider $m_H = m_A = 1 \text{ TeV}$ and different values of s_α although the details change, the conclusions hold: **the FCC-ee can probe regions indirect searches cannot.**



Results: $h \rightarrow cu$

We consider only a **c-tagger** as there is no state-of-the-art u-tagger.

With only a c-tagger, whose systematics are mildly impactful, **the upper limits are competitive for BSM benchmarks.**



Results: $h \rightarrow cu$

Again, we can use the reported efficiencies for the c-tagger

Loose : $\epsilon_{\beta; \text{Loose}}^c = \{0.07, 0.07, 0.90, 0.04\},$

Medium : $\epsilon_{\beta; \text{Med}}^c = \{0.02, 0.008, 0.80, 0.02\},$

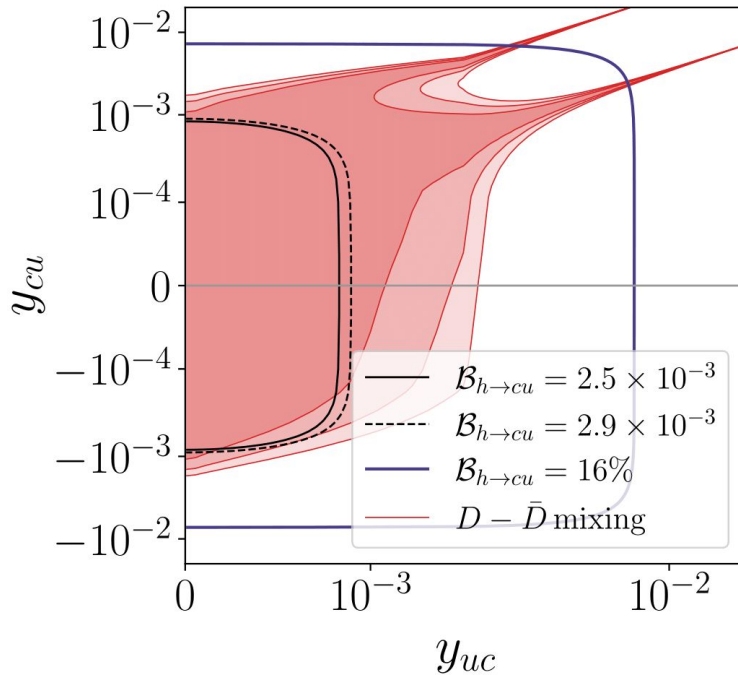
Both WPs are pretty similar and consistent with the scan.

More importantly, **they provide competitive limits.**

ϵ_{β}^c	$\mathcal{B}(h \rightarrow cu)$ (95% CL)
$\epsilon_{\beta; \text{Loose}}^c$	2.9×10^{-3}
$\epsilon_{\beta; \text{Med}}^c$	2.5×10^{-3}

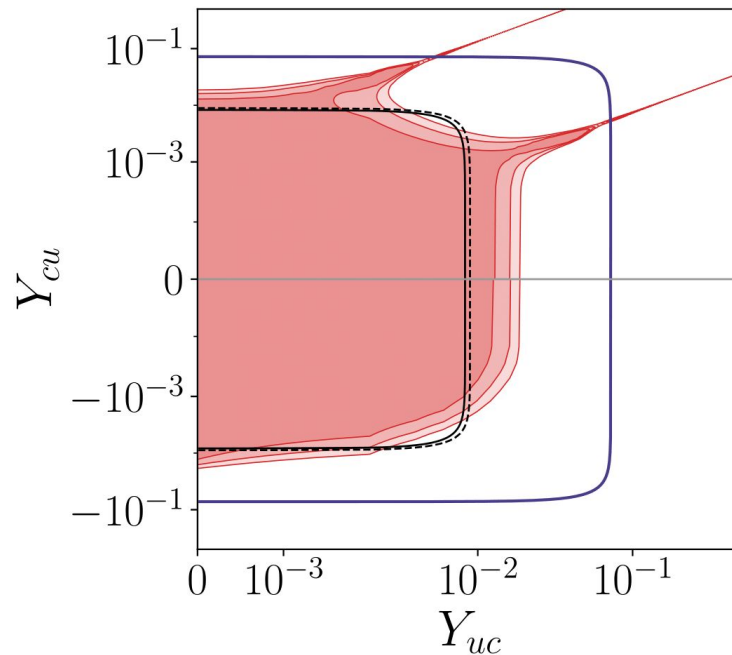
Results: $h \rightarrow cu$

We again see how the **FCC-ee probes regions beyond the reach of indirect searches.**



Results: $h \rightarrow cu + 2\text{HDM}$

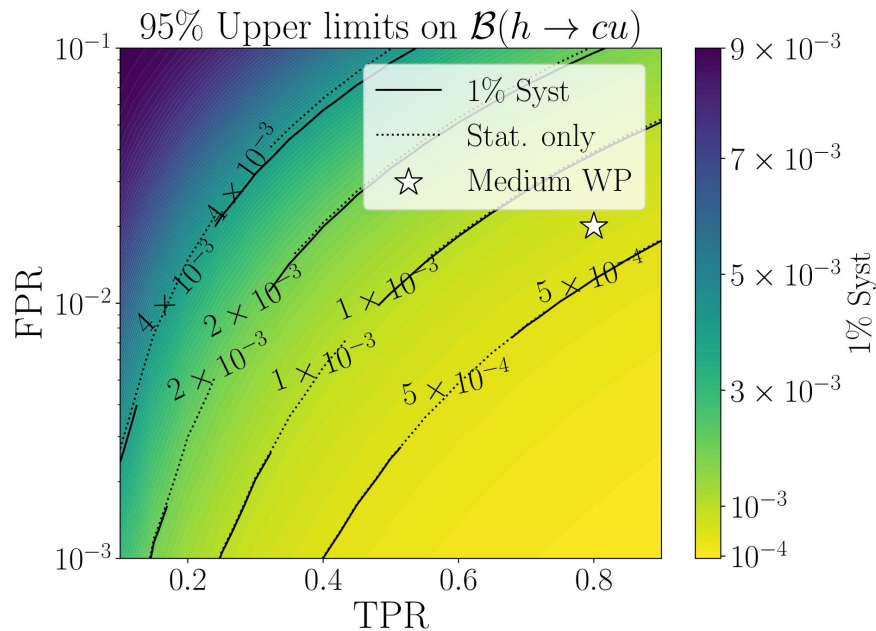
If we consider $m_H = m_A = 1 \text{ TeV}$ and different values of s_α although the details change, the conclusions hold: **the FCC-ee can probe regions indirect searches cannot.**



Results: $h \rightarrow cu$

If we add an idealized u-tagger, the performance **greatly increases** again.

Additionally, the Medium WP can go higher in FPR and still have less mistags in $(n_c, n_u)=(1,1)$ than for $(n_b, n_s)=(1,1)$ due to **the smallness of $h \rightarrow uu+dd$** compared to $h \rightarrow ss$.



Analysis strategy

From the likelihood + test statistic we obtain **confidence intervals, discovery significance** and/or **upper limits** on BR(h/Z→bs)

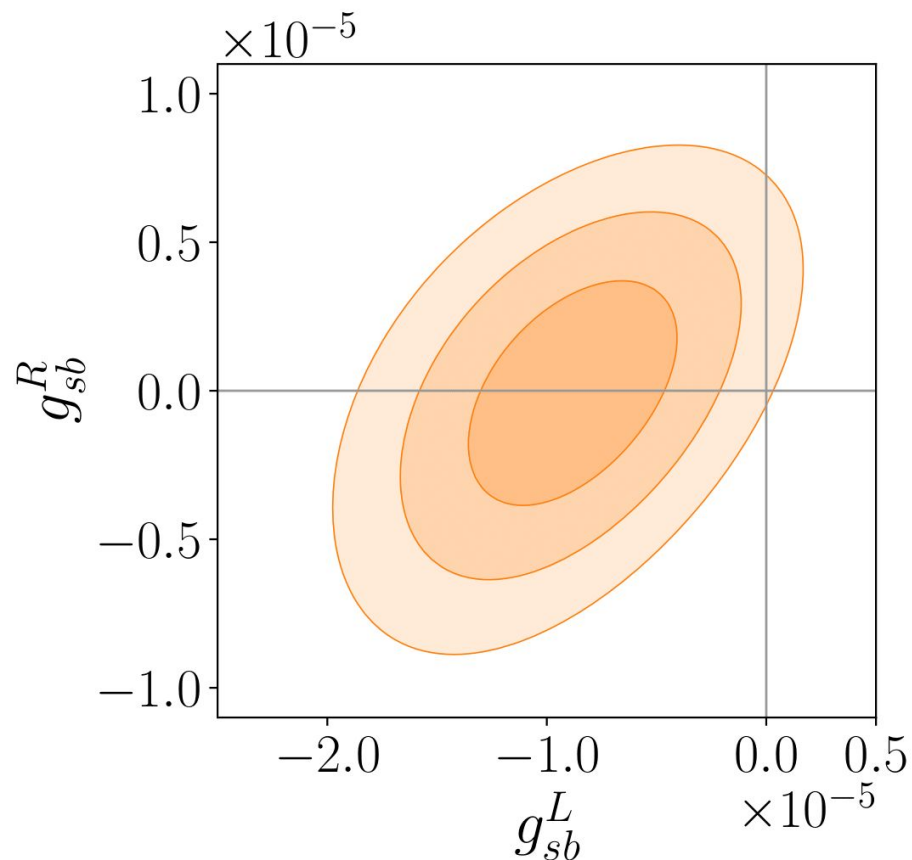
$$\lambda(\mu) = \frac{\mathcal{L}(\mu, \hat{\nu}(\mu))}{\mathcal{L}(\hat{\mu}, \hat{\nu})} \quad t_{\mu} = -2 \text{Ln } \lambda(\mu)$$

Besides the **95% CL upper limits**, we can also compute

- **68% confidence intervals** assuming $\mu_{\text{true}}=1$ and solving for $t_{\mu} = 1$
- **Discovery significance** assuming $\mu_{\text{true}}=1$ and computing for $Z = \sqrt{t_0}$.

Results: $Z \rightarrow bs$

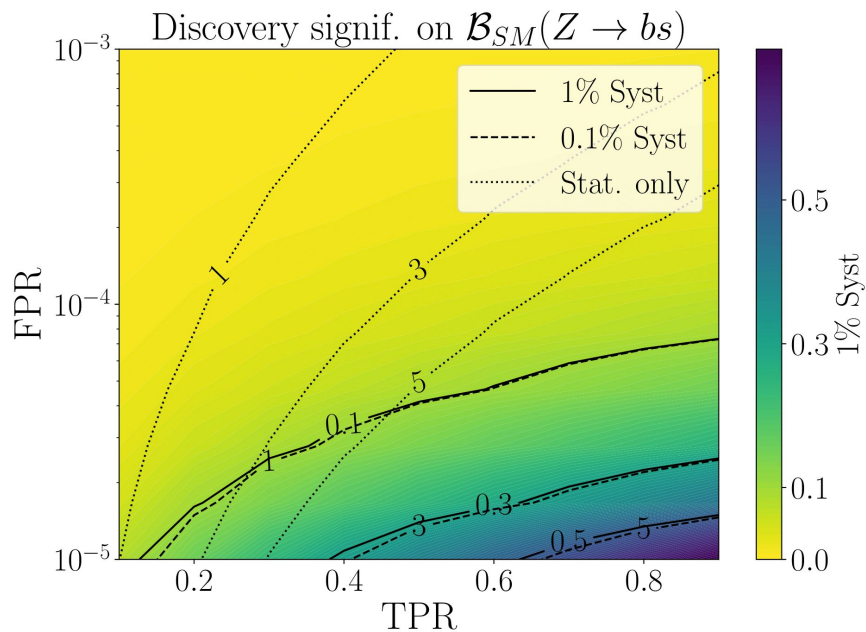
The indirect limits on the couplings are at the SM prediction level. It's hard to show them in the same scale as the FCC-ee limits!



Results: $Z \rightarrow bs$

We can reframe this in terms of the **discovery significance**.

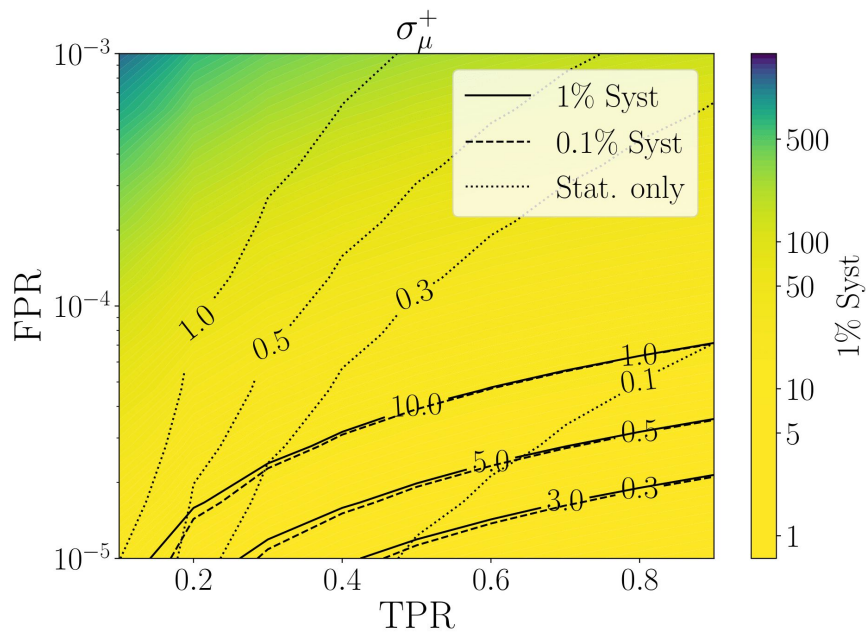
We see how the SM value **cannot be discovered** with this strategy except with almost no uncertainties and pushing the limits of the taggers.



Results: $Z \rightarrow b\bar{s}$

Another complementary viewpoint is the **upper limit of the 95% confidence interval** on the signal strength in units of its MLE estimate.

We observe how **systematic uncertainties degrade the performance**, with a 30% achievable with very small uncertainties only for almost perfect taggers.



Results: $Z \rightarrow bs$

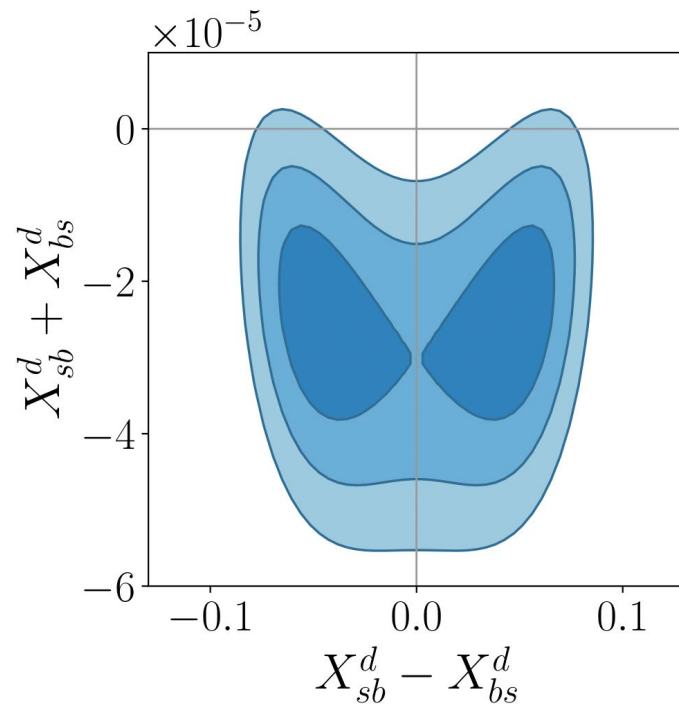
We see how we need the combination of **very small uncertainties** and **very small FPR** to be competitive with indirect constraints.

$(\text{TPR}, \text{FPR}, \Delta\epsilon_\beta^\alpha/\epsilon_\beta^\alpha)$	σ_μ^+ for $\mu_{\text{true}} = 1$	Discov. signif. (in σ)	$\mathcal{B}(Z \rightarrow bs)$ (95% CL)
$(0.4, 10^{-4}, 1\%)$	0.40(stat.)+32(syst.)	0.032	1.8×10^{-6}
$(0.4, 10^{-4}, 0.1\%)$	0.40(stat.)+3.2(syst.)	0.32	1.8×10^{-7}
$(0.2, 10^{-5}, 1\%)$	0.36(stat.)+6.3 (syst.)	0.16	4.2×10^{-7}
$(0.2, 10^{-5}, 0.1\%)$	0.36(stat.)+0.63 (syst.)	1.4	4.2×10^{-8}

VLQ from $h \rightarrow bs + Z \rightarrow bs$

$X_{bs} + X_{sb}$ is **strongly constrained**, mostly by $b \rightarrow s \ell^+ \ell^-$ transitions generated by $Z \rightarrow bs$ and reflects the preference for negative values of $g_{bs, sb}$.

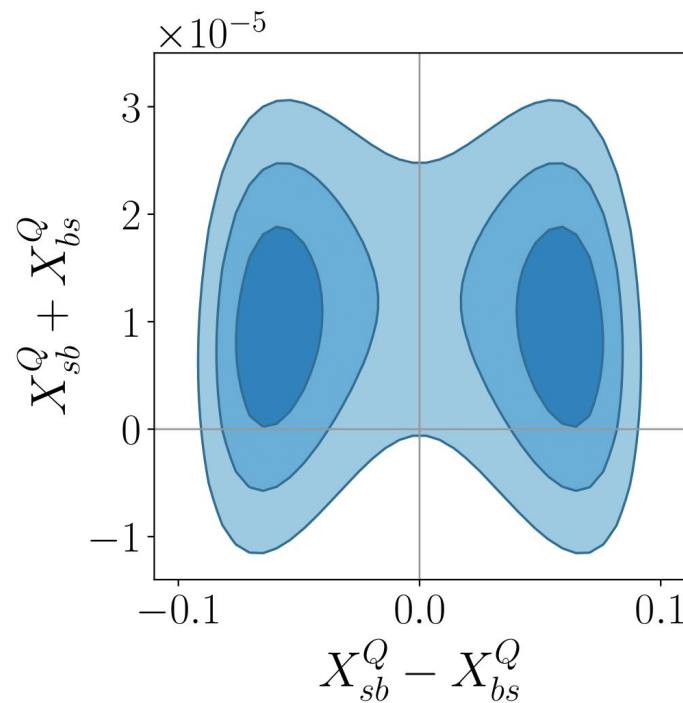
$X_{bs} - X_{sb}$ is **more weakly** constrained, reflecting mostly B_s mixing generated from both $h \rightarrow bs$ and $Z \rightarrow bs$ and reflecting the weaker constraints on both y_{sb} and g_{sb} (the bs couplings are suppressed by a m_b/m_s factor)



VLQ from $h \rightarrow bs + Z \rightarrow bs$

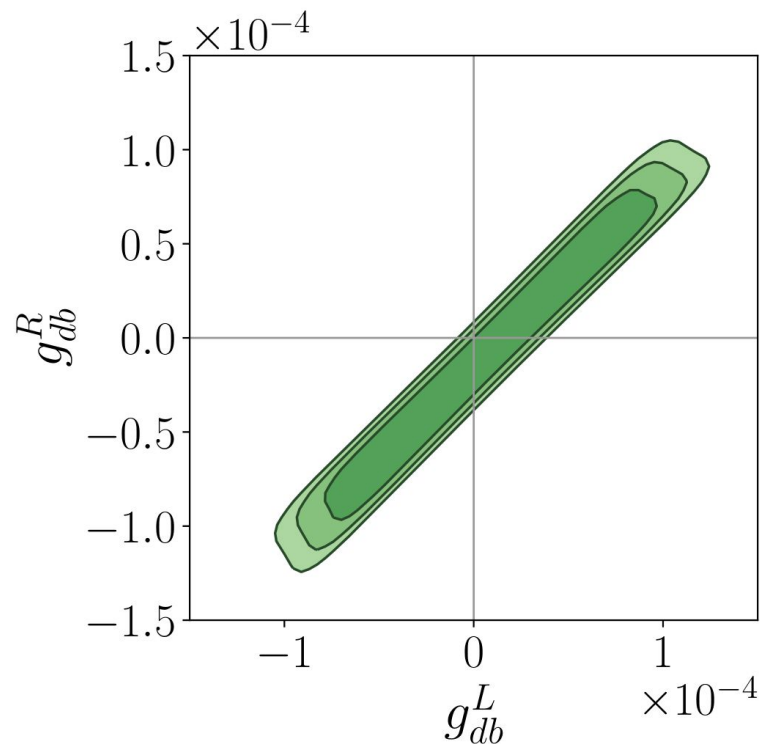
The results are mostly unchanged if we use an $SU(2)_L$ doublet instead of a singlet.

The differences arise due to the change in chiralities, with the right-handed currents now generated more constrained than the left-handed currents of the singlet case.



Results: $Z \rightarrow b\bar{d}$

The indirect limits on the couplings are close to the the SM prediction level. It's hard to show them in the same scale as the FCC-ee limits!

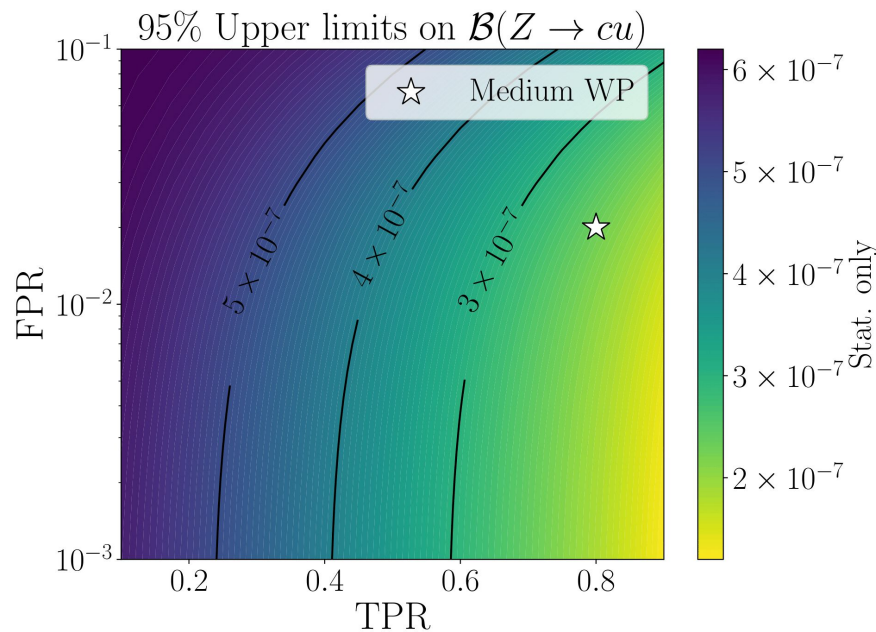


Results: $Z \rightarrow cu$

The situation is similar for $Z \rightarrow cu$.

With no u-tagger, the results are **almost identical to the $Z \rightarrow bq$ case.**

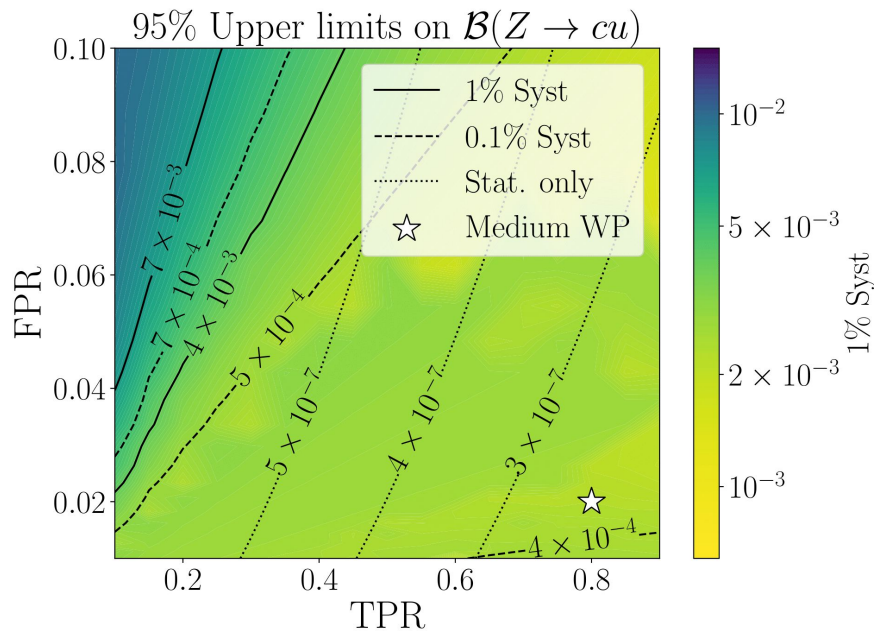
We again observe how the results are **not competitive with the indirect constraints.**



Results: $Z \rightarrow cu$

Systematics **hinder the already suboptimal** performance, as the analysis is **systematics dominated**.

We do not implement an idealized u-tagger because it cannot distinguish between u- and d-quarks. This causes the $Z \rightarrow uu+dd$ background to be \sim twice as large as $Z \rightarrow ss$ for equivalent TPR,FPR.



Results: $Z \rightarrow cu$

The indirect limits on the couplings are not at the SM prediction level, but still much lower than the FCC-ee reach.

