

# A Global Fit of Non-Relativistic Effective Dark Matter Operators Including Solar Neutrinos

Neal Avis Kozar

Aaron Vincent

Work with Aaron Vincent, Pat Scott, and help from the GAMBIT collaboration

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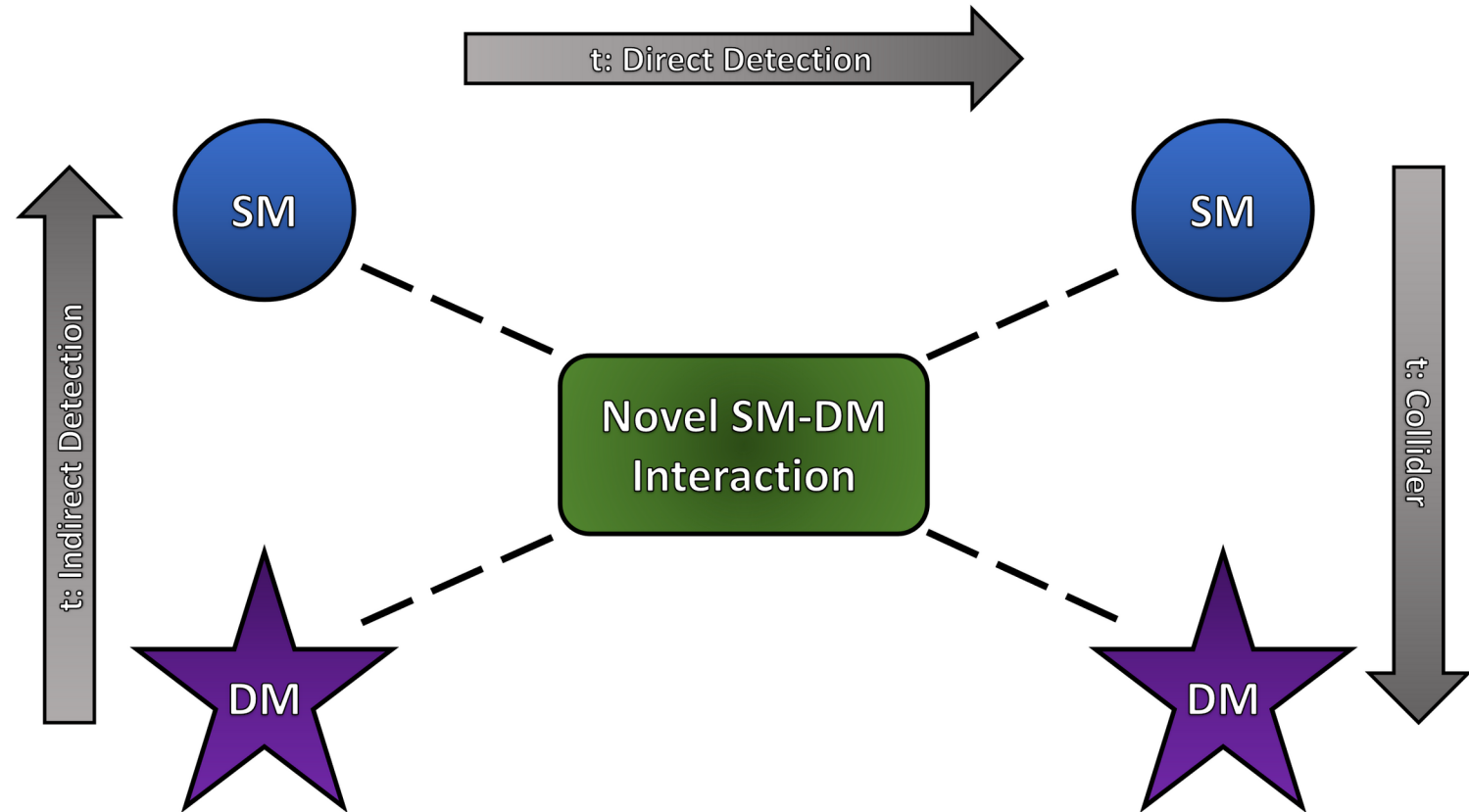
PHENO

# Introduction to Non-Relativistic Effective Operators

(NREOs)

# Search Types

- Indirect detection, direct detection, collider searches
- Each are independent detection methods
- Solar neutrinos act as a compliment to direct detection

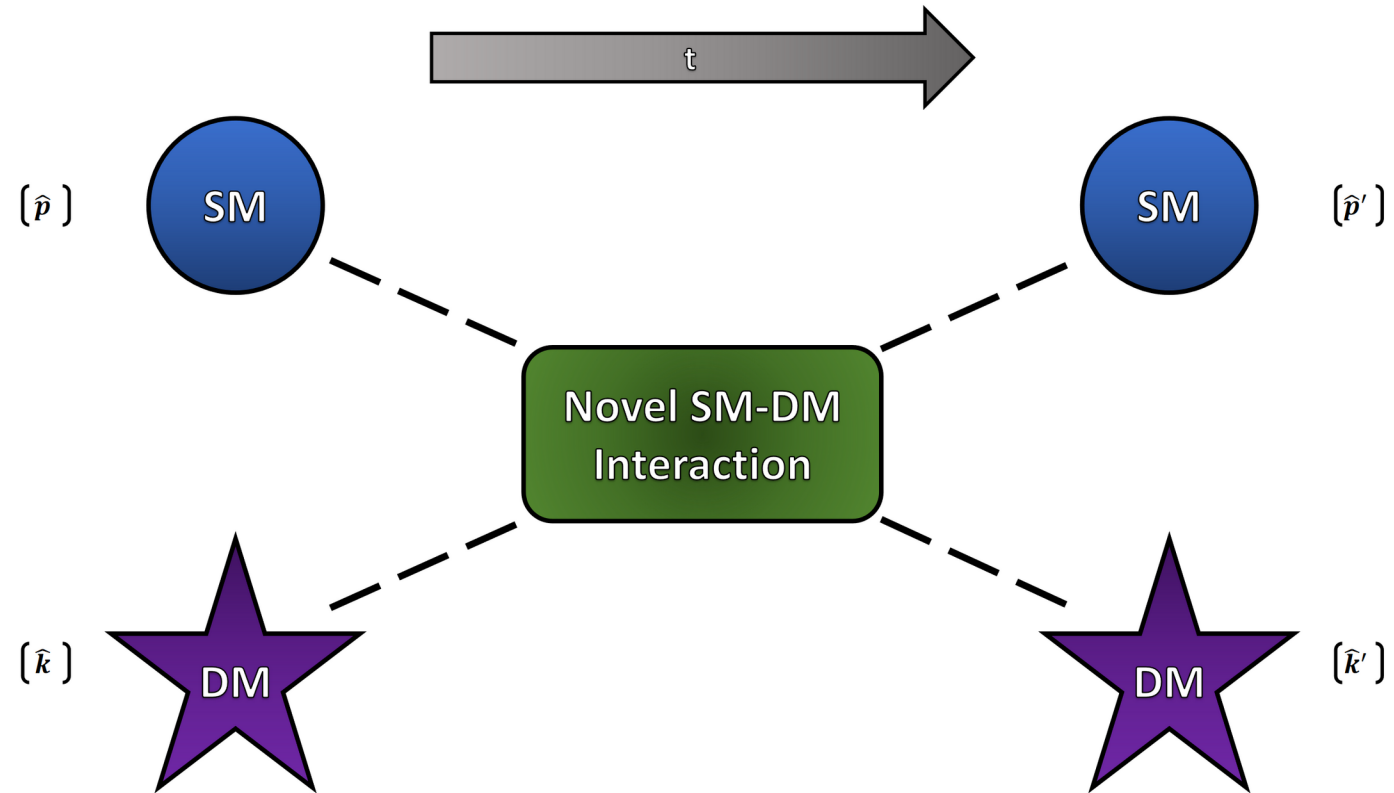


# Hermitian Operators

- The general case of a dark matter scattering interaction is considered
- The Hermitian operators that govern the interaction are

$$\mathbb{1}_{\chi N} , i\hat{\mathbf{q}} , \hat{\mathbf{v}}^\perp , \hat{\mathbf{S}}_\chi , \hat{\mathbf{S}}_N$$

$$\hat{\mathbf{v}}^\perp = \hat{\mathbf{v}} + \hat{\mathbf{q}}/(2\mu_N)$$



# Non-Relativistic Effective Operators

- Spin-independent:  $\hat{O}_1 = \mathbb{1}_{\chi N}$
- Spin-dependent:  $\hat{O}_4 = \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{S}}_N$
- Novel interactions, such as

$$\hat{O}_{10} = i\hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N}$$

- Acts as leading contributor to higher-energy theories [3]:

$$\mathcal{L} \supset \lambda_1 \phi \bar{\chi} \chi - ih_2 \phi \bar{q} \gamma^5 q \rightarrow \hat{\mathcal{H}} \supset (c_{10}^0 t^0 + c_{10}^1 t^1) \hat{O}_{10}$$

$$\hat{O}_1 = \mathbb{1}_{\chi N}$$

$$\hat{O}_2 = \hat{\mathbf{v}}^\perp \cdot \hat{\mathbf{v}}^\perp$$

$$\hat{O}_3 = i\hat{\mathbf{S}}_N \cdot \left( \frac{\hat{\mathbf{q}}}{m_N} \times \hat{\mathbf{v}}^\perp \right)$$

$$\hat{O}_4 = \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{S}}_N$$

$$\hat{O}_5 = i\hat{\mathbf{S}}_\chi \cdot \left( \frac{\hat{\mathbf{q}}}{m_N} \times \hat{\mathbf{v}}^\perp \right)$$

$$\hat{O}_6 = \left( \hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N} \right) \left( \hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N} \right)$$

$$\hat{O}_7 = \hat{\mathbf{S}}_N \cdot \hat{\mathbf{v}}^\perp$$

$$\hat{O}_8 = \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{v}}^\perp$$

$$\hat{O}_9 = i\hat{\mathbf{S}}_\chi \cdot \left( \hat{\mathbf{S}}_N \times \frac{\hat{\mathbf{q}}}{m_N} \right)$$

$$\hat{O}_{10} = i\hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N}$$

$$\hat{O}_{11} = i\hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N}$$

$$\hat{O}_{12} = \hat{\mathbf{S}}_\chi \cdot \left( \hat{\mathbf{S}}_N \times \hat{\mathbf{v}}^\perp \right)$$

$$\hat{O}_{13} = i \left( \hat{\mathbf{S}}_\chi \cdot \hat{\mathbf{v}}^\perp \right) \left( \hat{\mathbf{S}}_N \cdot \frac{\hat{\mathbf{q}}}{m_N} \right)$$

$$\hat{O}_{14} = i \left( \hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N} \right) \left( \hat{\mathbf{S}}_N \cdot \hat{\mathbf{v}}^\perp \right)$$

$$\hat{O}_{15} = - \left( \hat{\mathbf{S}}_\chi \cdot \frac{\hat{\mathbf{q}}}{m_N} \right) \left[ \left( \hat{\mathbf{S}}_N \times \hat{\mathbf{v}}^\perp \right) \cdot \frac{\hat{\mathbf{q}}}{m_N} \right]$$

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# Cross Section

- Cross section becomes a large sum over response functions

$$\frac{d\sigma_i}{dE}(w^2, q^2) = \frac{m_T}{2\pi w^2} P_{\text{tot}}(w^2, q^2)$$

$$P_{\text{tot}}(w^2, q^2) = \frac{4\pi}{2J+1} \sum_{\tau=0,1} \sum_{\tau'=0,1} \left\{ \left[ R_M^{\tau\tau'} \left( v_T^{\perp 2}, \frac{q^2}{m_N^2} \right) W_M^{\tau\tau'}(y) \right. \right. \\ \left. \left. + R_{\Sigma''}^{\tau\tau'} \left( v_T^{\perp 2}, \frac{q^2}{m_N^2} \right) W_{\Sigma''}^{\tau\tau'}(y) + R_{\Sigma'}^{\tau\tau'} \left( v_T^{\perp 2}, \frac{q^2}{m_N^2} \right) W_{\Sigma'}^{\tau\tau'}(y) \right] \right. \\ \left. + \frac{q^2}{m_N^2} \left[ R_{\Phi''}^{\tau\tau'} \left( v_T^{\perp 2}, \frac{q^2}{m_N^2} \right) W_{\Phi''}^{\tau\tau'}(y) + R_{\Phi''M}^{\tau\tau'} \left( v_T^{\perp 2}, \frac{q^2}{m_N^2} \right) W_{\Phi''M}^{\tau\tau'}(y) \right. \right. \\ \left. \left. + R_{\tilde{\Phi}'}^{\tau\tau'} \left( v_T^{\perp 2}, \frac{q^2}{m_N^2} \right) W_{\tilde{\Phi}'}^{\tau\tau'}(y) + R_{\Delta}^{\tau\tau'} \left( v_T^{\perp 2}, \frac{q^2}{m_N^2} \right) W_{\Delta}^{\tau\tau'}(y) \right. \right. \\ \left. \left. + R_{\Delta\Sigma'}^{\tau\tau'} \left( v_T^{\perp 2}, \frac{q^2}{m_N^2} \right) W_{\Delta\Sigma'}^{\tau\tau'}(y) \right] \right\}$$

- Effective Cross section

$$\sigma_p = \frac{(c_i^\tau \mu_n)^2}{\pi}$$

# Solar Capture

Capt'n General

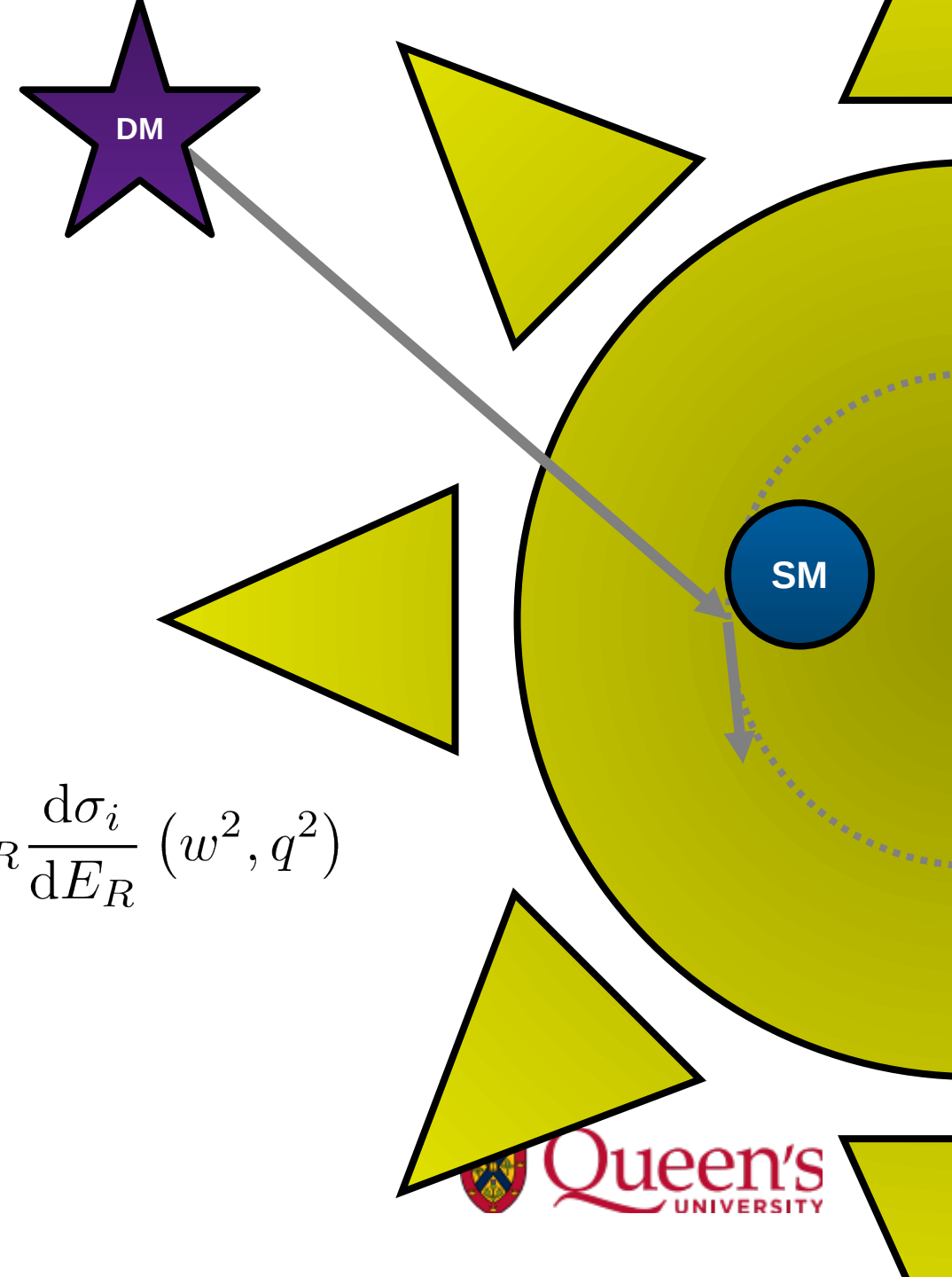


# Capture Process

- Dark matter is captured when it scatters to below the local escape velocity in the Sun

$$C = 4\pi \int_0^{R_\odot} dR R^2 \int_0^\infty du \frac{f(u)}{u} w \Omega_v^-(w)$$

$$\Omega_v^-(w) = \sum_i n_i w \Theta \left( \frac{\mu_i}{\mu_{+,i}^2} - \frac{u^2}{w^2} \right) \int_{E_k u^2 / w^2}^{E_k \mu_i / \mu_{+,i}^2} dE_R \frac{d\sigma_i}{dE_R} (w^2, q^2)$$



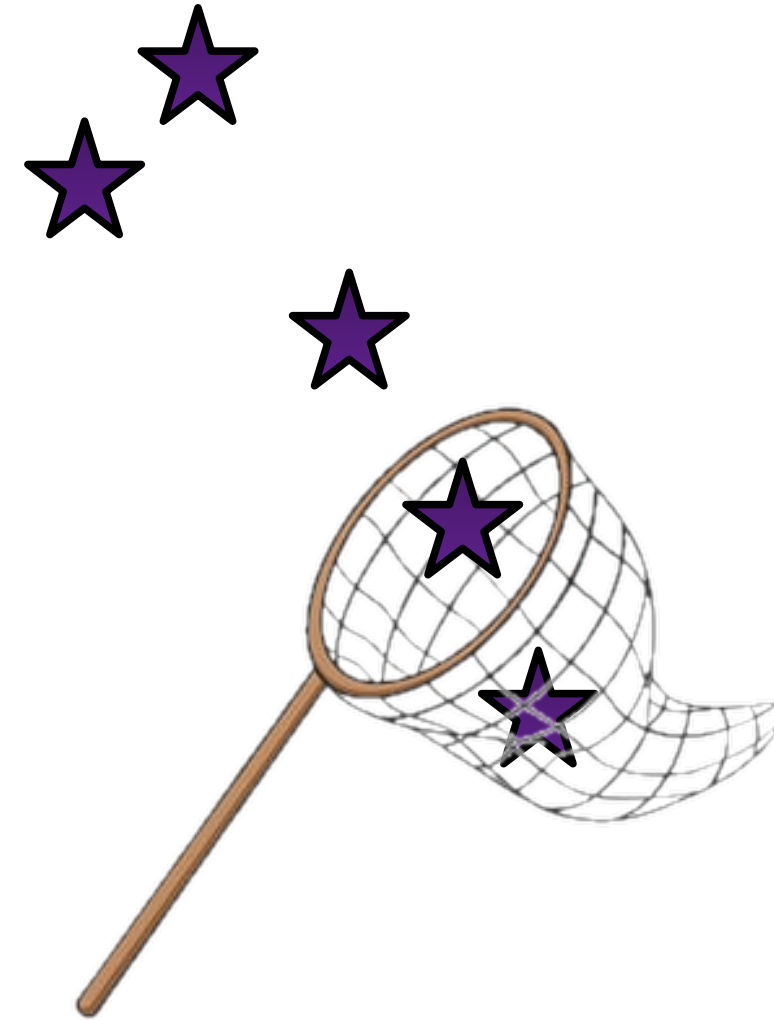
# Geometric Limit

- The Sun has a hard limit of dark matter capture

$$C_{\max}(t) = \pi R_{\odot}^2(t) \int_0^{\infty} \frac{f_{\odot}(u)}{u} w^2(u, R_{\odot}) du$$

$$C_{\max}(t) = \frac{1}{3} \pi \frac{\rho_{\chi}}{m_{\chi}} R_{\odot}^2(t) \left( e^{-\frac{3}{2} \frac{u_{\odot}^2}{u_0^2}} \sqrt{\frac{6}{\pi}} u_0 + \frac{6G_{\text{N}}M_{\odot} + R_{\odot}(u_0^2 + 3u_{\odot}^2)}{R_{\odot}u_{\odot}} \text{Erf} \left[ \sqrt{\frac{3}{2}} \frac{u_{\odot}}{u_0} \right] \right)$$

- We take minimum of the limit and capture rate



# Annihilation in the Sun

- The number density of dark matter is given by

$$\frac{dN_\chi(t)}{dt} = C(t) - A(t) - E(t) = 0$$

- At steady state, the annihilation rate only depends on the capture:

$$\Gamma_A = (C/2) \tanh^2(t/\tau)$$

- The final neutrino flux is found from branching ratios

$$\frac{d\Phi_\nu}{dE_\nu} = \frac{\Gamma_A}{4\pi D^2} \sum_f B_\chi^f \frac{dN_\nu^f}{dE_\nu}$$

# Other Applications

- The same calculation in other stars can be performed
  - Working on integration with GARSTEC to facilitate stellar evolution
- Can look at other phenomena like
  - Energy transport [4,5]
  - Modified main sequence lifetimes [6]
  - Triggering thermonuclear explosions in stellar remnants [7-9]

# Capt'n General

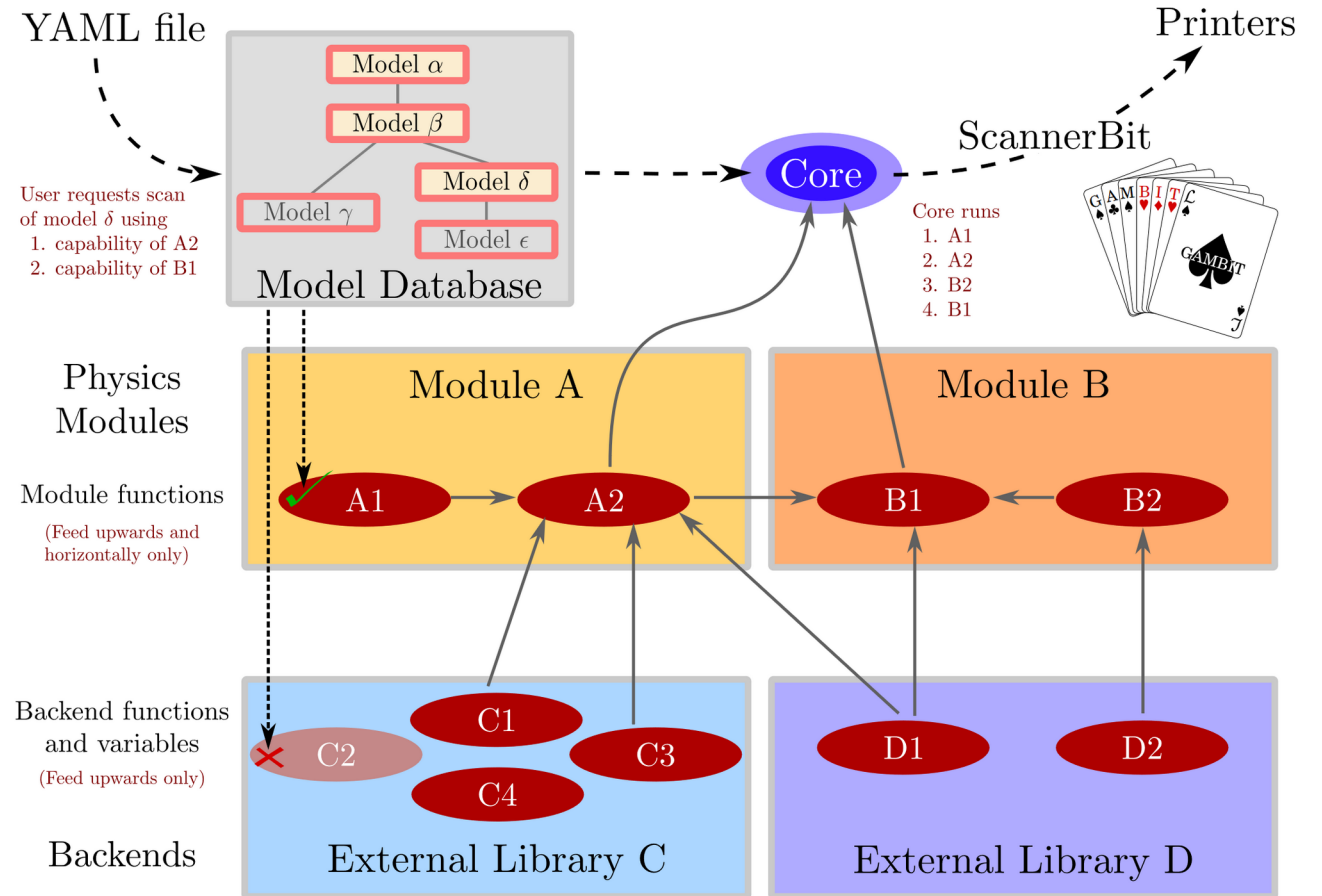
- Capt'n [10] was designed for capture rate calculations
  - As standalone
  - GAMBIT backend
  - DarkMESA companion
  - GARSTEC integration
- Capt'n uses several parameters to calculate the DM capture rate in  $\text{s}^{-1}$ 
  - Solar model including isotopic abundances
  - Dark matter halo parameters
  - Interaction model

# Global and Modular BSM Inference Tool

(GAMBIT)

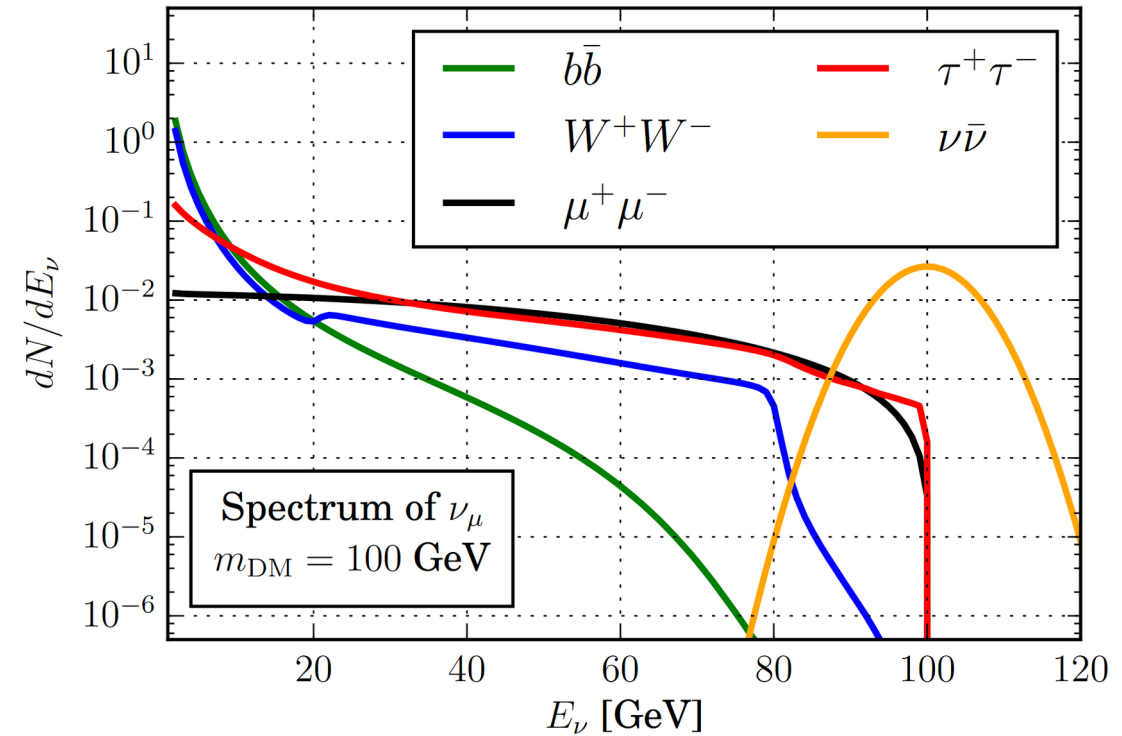
# GAMBIT

- GAMBIT [11] combines many separate branches of physics to perform global scans of novel physics using existing experimental data
- Modular design to promote contributions
- Global scans can pick out signals of new physics before single experiments



# IceCube Neutrino Observatory

- For the 79-string run, IceCube's [12] digital optical modules were arranged as:
  - 73 strings with 125 m horizontal spacing and 17 m vertical spacing
  - 6 strings with less than 75 m horizontal spacing and 7 m vertical spacing in the DeepCore [13]
- The data is broken into three independent streams, of two varieties:
  - Low energy: exterior strings act as muon veto for the central array (Summer Low and Winter Low)
  - Higher energy: no restrictions (Winter High)
- IceCube performs better at higher-energy neutrino detection



[14]

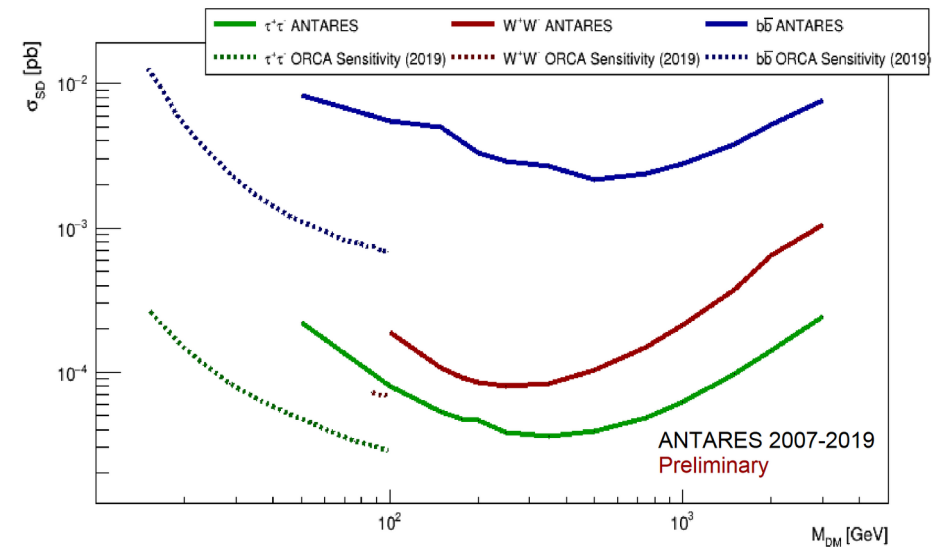
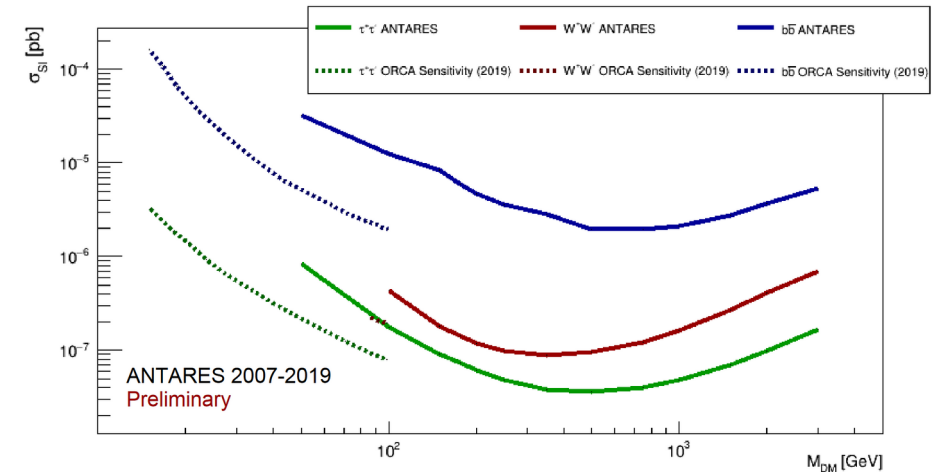
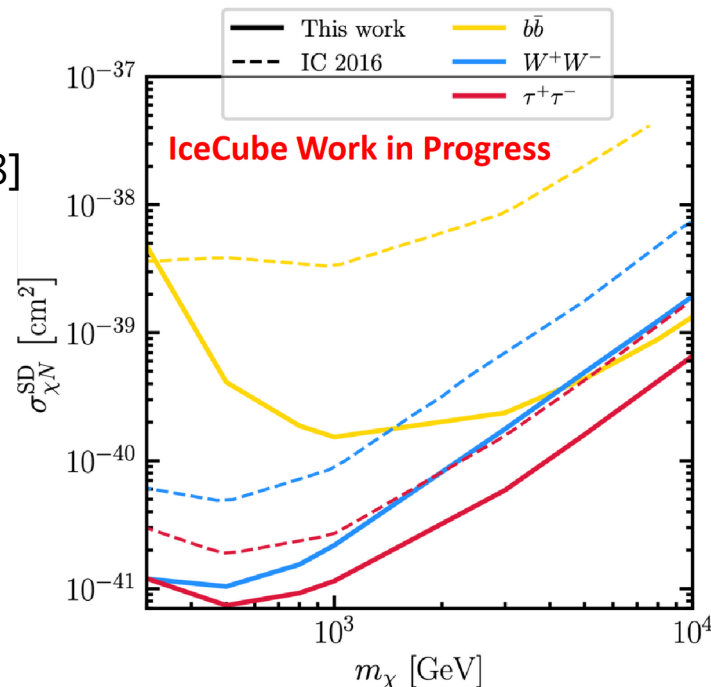


# Direct Detection Experiments

- Fourteen direct detection experiments were included:
  - LUX 2016 [15]
  - XENON1T 2018 [16]
  - PandaX-II 2016 [17] and 2017 [18]
  - PICO-60 2017 [19]
  - CRESST-II [20]
  - CDMSlite [21]
  - DarkSide-50 [22]
  - CRESST-III [29]
  - LZ [30]
  - PandaX-4T [31]
  - SIMPLE [32]
  - SuperCDMS [33]
  - XENON100 [34]
- Additionally, projections are included from:
  - DARWIN [35]
  - PICO-500 [36]

# Added Experiments

- Four extra experiments were included in a post processing run:
  - ANTARES from Dark Ghosts 2022 presented by Chiara Poirè [23]
  - IceCube Update from Dark Ghosts 2022 presented by Stephan Meighen-Berger [24]
  - SuperK analysis from 2015 [27]
  - DeepCore analysis from 2022 [28]



# Results and Scans

# GAMBIT Scan Parameters

- The common parameters are shared between all GAMBIT scans

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## Common model parameters

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$\log_{10}(m_{\text{dm}})$ (GeV)	(0, 4)
$\rho_0$ (GeV cm <sup>-3</sup> )	0.5
$v_0$ (km sec <sup>-1</sup> )	(216, 264)
$v_{\text{rot}}$ (km sec <sup>-1</sup> )	(216, 264)
$v_{\text{esc}}$ (km sec <sup>-1</sup> )	(453, 603)

- These scans are presented as profiled likelihoods with 90% C.L.
- All scans have 3 decay channel versions: bottom quark, W boson, and tau

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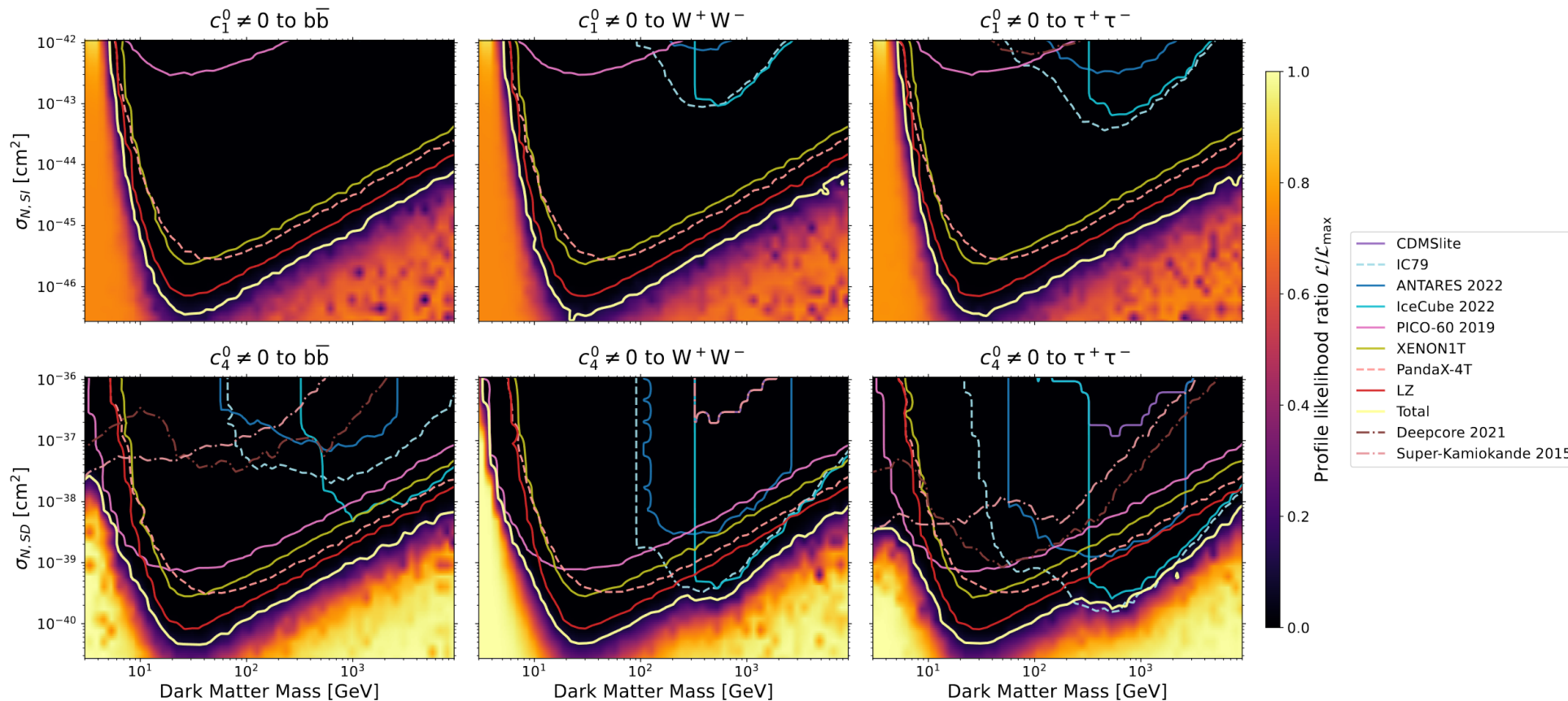
## Coupling parameters (GeV<sup>-2</sup>)

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$\log_{10}(c_1^0)$	(-10, -6)
$\log_{10}(c_3^0)$	(-6, -3)
$\log_{10}(c_4^0)$	(-8, -3)
$\log_{10}(c_5^0)$	(-5, -2)
$\log_{10}(c_6^0)$	(-5, -1)
$\log_{10}(c_7^0)$	(-4, -1)
$\log_{10}(c_8^0)$	(-6, -4)
$\log_{10}(c_9^0)$	(-6, -1)
$\log_{10}(c_{10}^0)$	(-6, -2)
$\log_{10}(c_{11}^0)$	(-9, -5)
$\log_{10}(c_{12}^0)$	(-8, -4)
$\log_{10}(c_{13}^0)$	(-5, -1)
$\log_{10}(c_{14}^0)$	(-3, 1)
$\log_{10}(c_{15}^0)$	(-5, -2)

# Spin-Independent and Spin-Dependent Channel

- The three annihilation channels for  $c_1$  (top) and  $c_4$  (bottom)

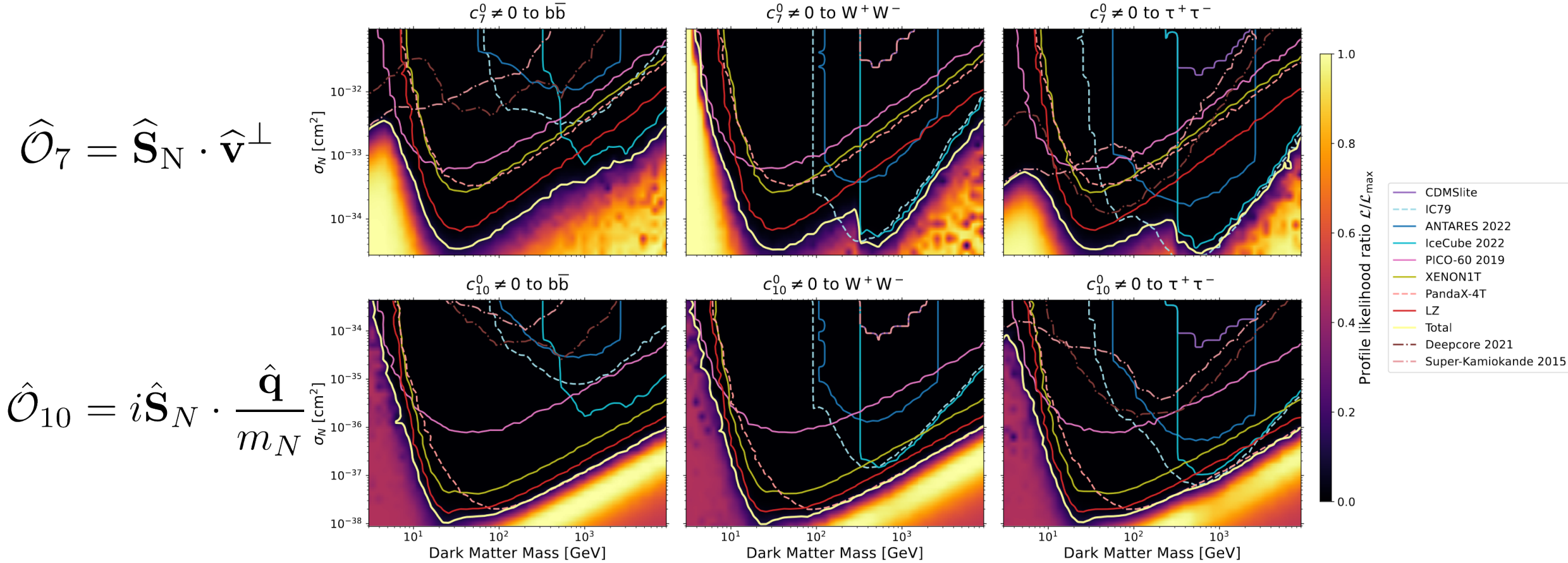


$$\hat{\mathcal{O}}_1 = \mathbb{1}_{\chi N}$$

$$\hat{\mathcal{O}}_4 = \hat{\mathbf{S}}_{\chi} \cdot \hat{\mathbf{S}}_N$$

# C<sub>7</sub> and C<sub>10</sub> Coupling Experiment Breakdown

- The three annihilation channels for c<sub>7</sub> (top) and c<sub>10</sub> (bottom)



$$\mathcal{L} \supset -\lambda_3 \bar{\chi} \gamma^\mu \chi G_\mu - h_4 \bar{q} \gamma_\mu \gamma^5 q G^\mu \rightarrow \hat{\mathcal{H}} \supset (c_7^0 t^0 + c_7^1 t^1) \hat{O}_7$$

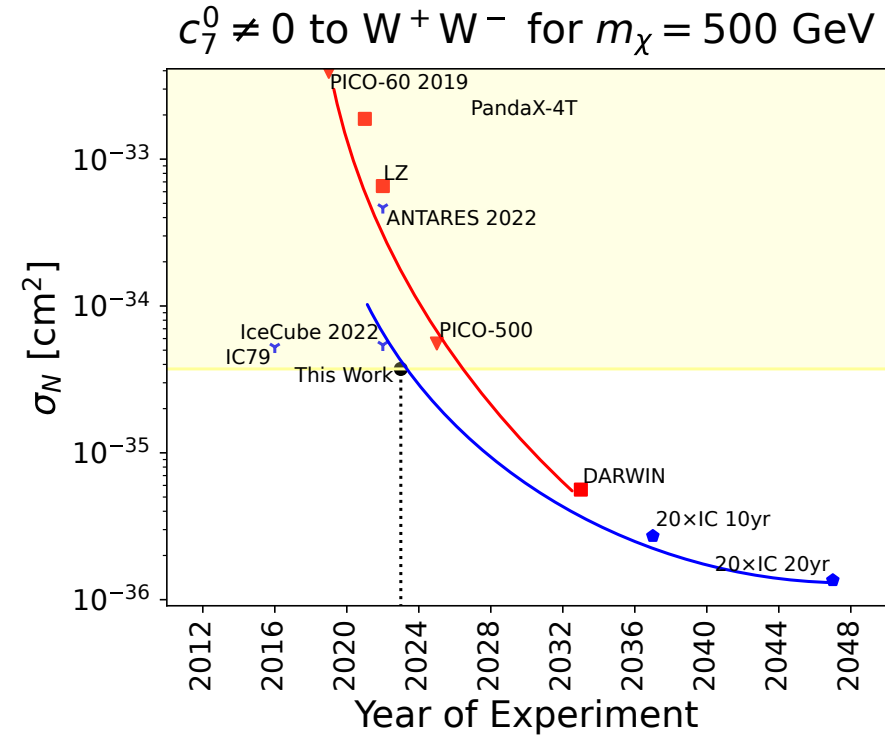
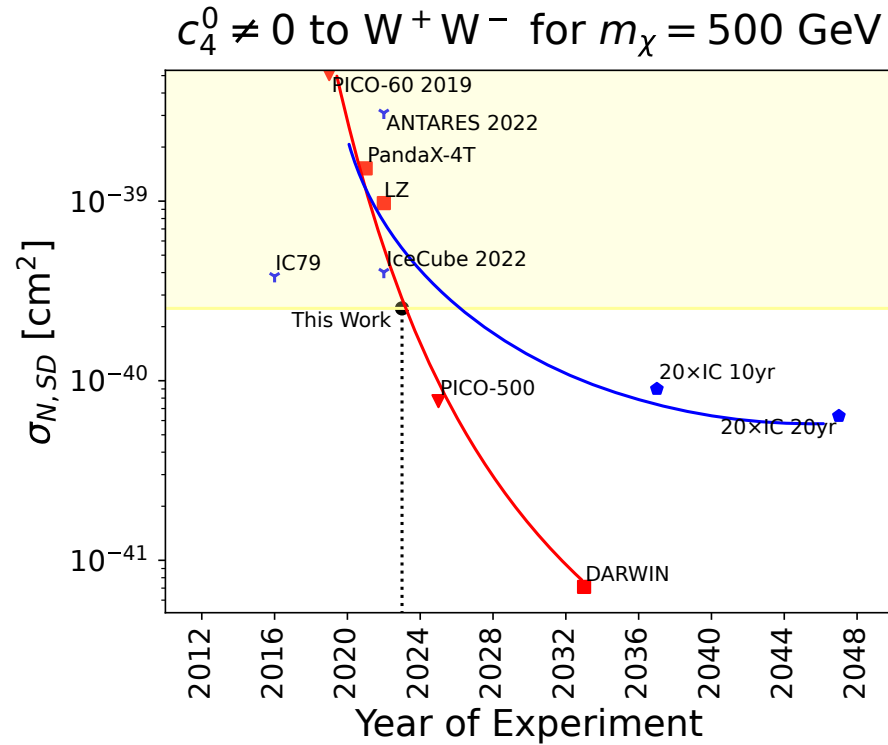
$$\mathcal{L} \supset -\lambda_1 \phi \bar{\chi} \chi - i h_2 \phi \bar{q} \gamma^5 q \rightarrow \hat{\mathcal{H}} \supset (c_{10}^0 t^0 + c_{10}^1 t^1) \hat{O}_{10}$$



# Future Outlook

- Future prospects for neutrino telescopes in comparison with direct detection

$$\text{Projection} = \text{IC2022} \times \left( \frac{V}{V_{\text{IC2022}}} \frac{T}{T_{\text{IC2022}}} \right)^{-\frac{1}{2}}$$



# Conclusions



# Conclusions

- [Capt'n](#) open to public and has already seen use by [GAMBIT](#) community ([2106.02056](#))
- This is some of the first set of global constraints on non-relativistic effective operator dark matter from direct detection experiments in addition to solar neutrinos
- IceCube solar neutrinos can assist with spin-dependent direct detection searches
- Whenever new data is added to GAMBIT this work can be re-run with trivial modifications to improve constraints
- This work has been modified for use in a Supernova scattering search lead by Christopher Cappiello
- Current work to use this in stellar evolution and solar calibration

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# Thank You

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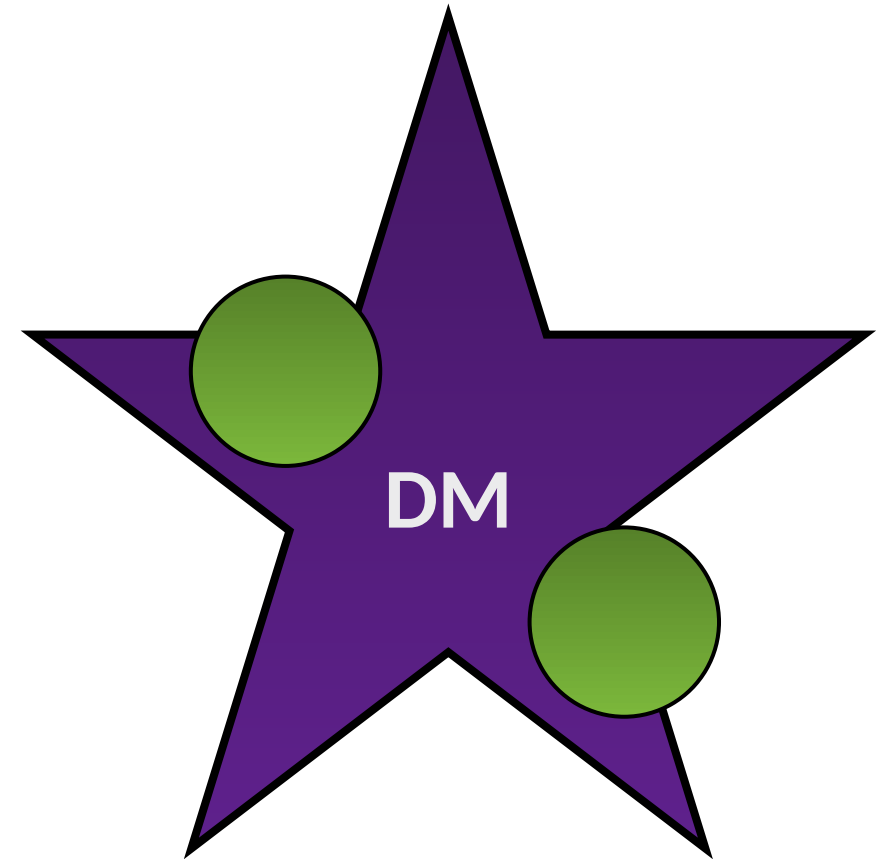
# Backup Slides



# Advantages of an Effective Field Theory

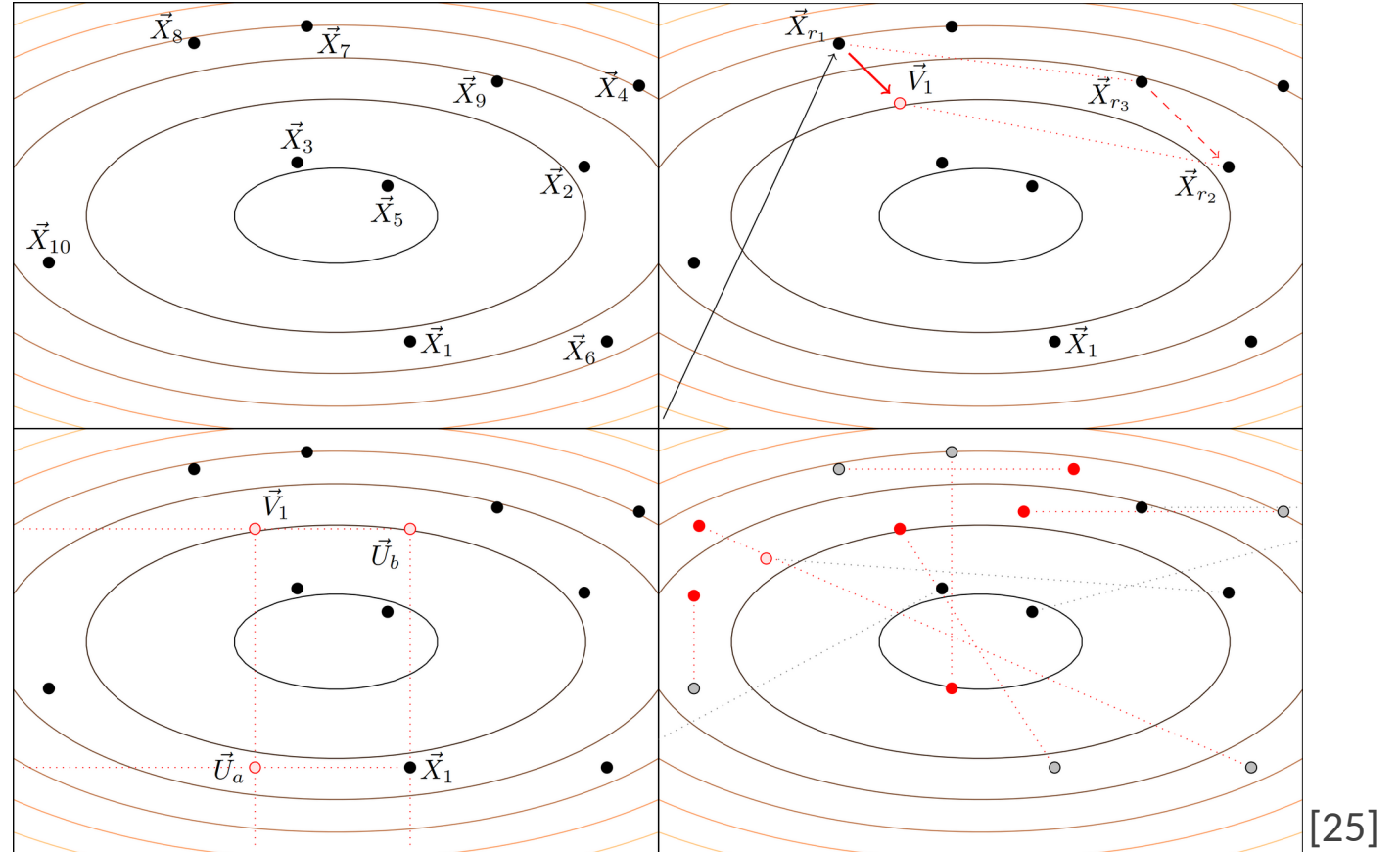
- High-energy theory parameterization
- Fitzpatrick et. al. [2] describe a toy model dark matter effective field theory
- Dark matter substructure can be ignored at galactic halo velocities

$$\hat{q}_{\max} = 200 \text{ MeV}$$



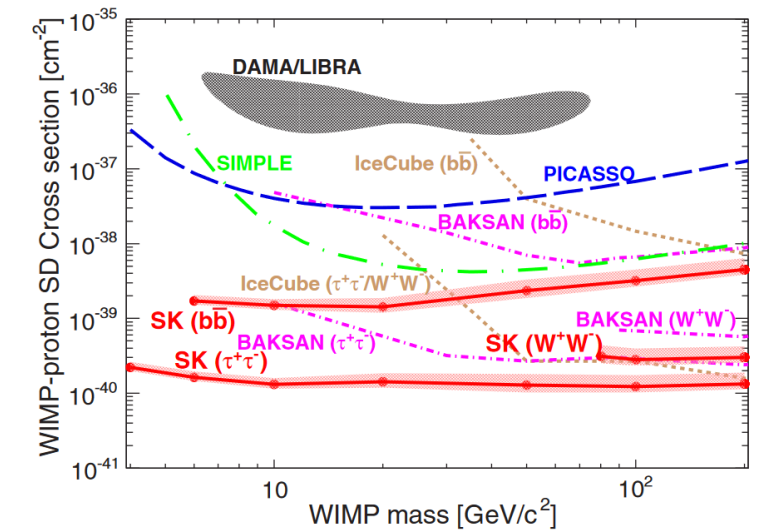
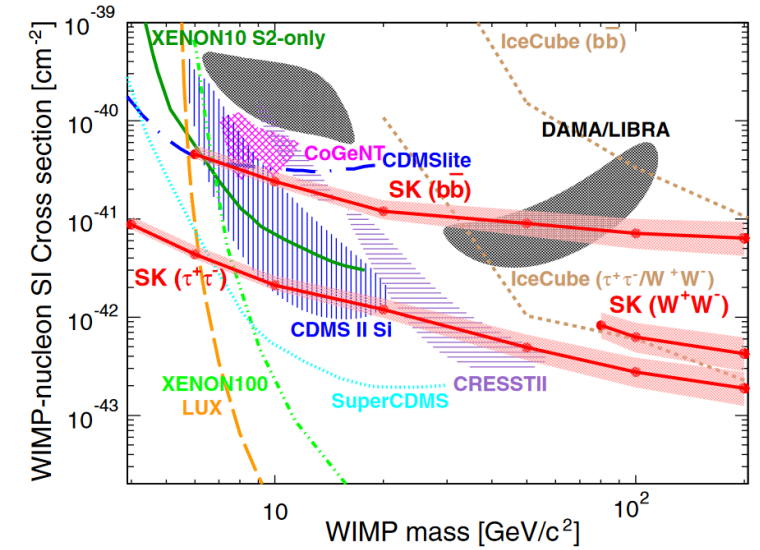
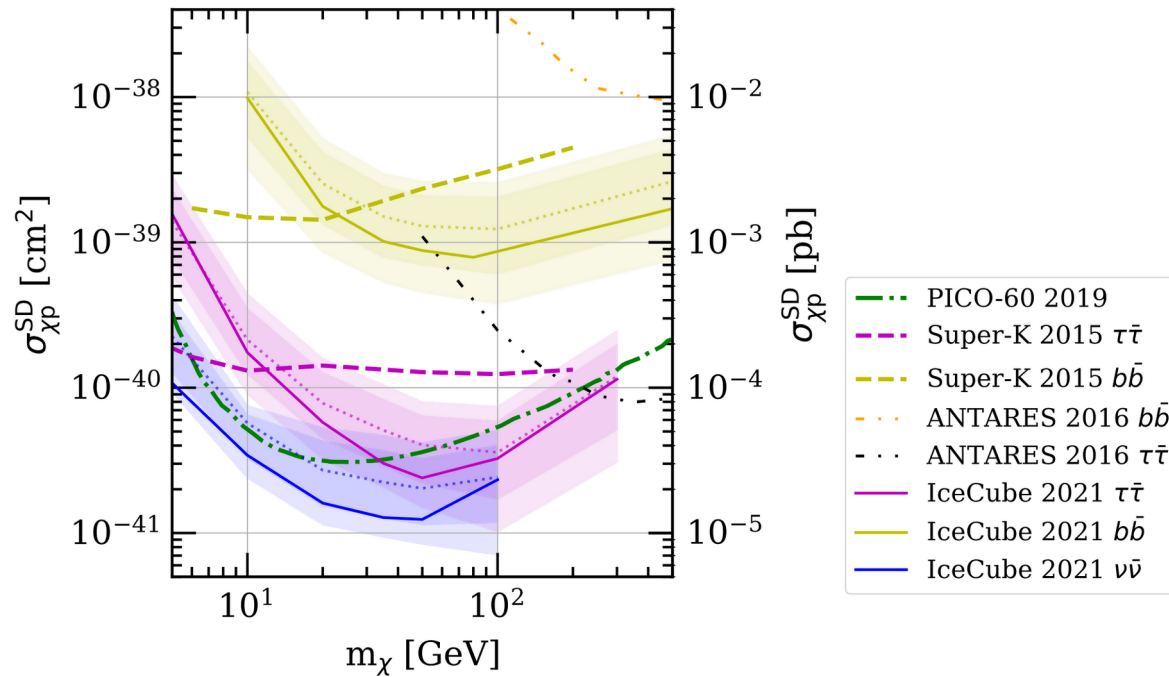
# Scanning with Diver

- Diver is a differential evolution scanner in GAMBIT
- It can rapidly map likelihood contours
- But cannot give posteriors
- Differential evolution occurs in three steps
  - Mutation
  - Crossover
  - Selection



# SuperK and DeepCore

- SuperK analysis from 2015 [27]
- DeepCore analysis from 2022 [28]



# Dent et. al. [3] Tables

- Spin-0 Wimp

TABLE VII. Non-relativistic reduction of operators for a spin-0 WIMP

Scalar Mediator	
$(S^\dagger S)(\bar{q}q)$	$\longrightarrow \left( \frac{h_1^N g_1}{m_\phi^2} \right) \mathcal{O}_1$
$(S^\dagger S)(\bar{q}\gamma^5 q)$	$\longrightarrow \left( \frac{h_2^N g_1}{m_\phi^2} \right) \mathcal{O}_{10}$
Vector Mediator	
$i(S^\dagger \partial_\mu S - \partial_\mu S^\dagger S)(\bar{q}\gamma^\mu q)$	$\longrightarrow 0$
$i(S^\dagger \partial_\mu S - \partial_\mu S^\dagger S)(\bar{q}\gamma^\mu \gamma^5 q)$	$\longrightarrow \left( \frac{2ig_4 h_4^N}{m_G^2} \frac{m_N}{m_S} \right) \mathcal{O}_{10}$
Charged Spinor Mediator	
$(S^\dagger S)(\bar{q}q)$	$\longrightarrow \frac{y_1^\dagger y_1 - y_2^\dagger y_2}{m_Q m_S} f_T^N \mathcal{O}_1$
$(S^\dagger S)(\bar{q}\gamma^5 q)$	$\longrightarrow i \frac{y_2^\dagger y_1 - y_1^\dagger y_2}{m_Q m_S} \tilde{\Delta}^N \mathcal{O}_{10}$

(after using Fierz identities)

## Dent et. al. [3] Tables

- Spin-1/2 WIMP

TABLE VIII. Operators for a spin- $\frac{1}{2}$  WIMP via a neutral mediator

Scalar Mediator	
$\bar{\chi}\chi\bar{q}q$	$\rightarrow \left(\frac{h_1^N \lambda_1}{m_\phi^2}\right) \mathcal{O}_1$
$\bar{\chi}\chi\bar{q}\gamma^5 q$	$\rightarrow \left(\frac{h_2^N \lambda_1}{m_\phi^2}\right) \mathcal{O}_{10}$
$\bar{\chi}\gamma^5 \chi\bar{q}q$	$\rightarrow \left(-\frac{h_1^N \lambda_2 m_N}{m_\phi^2 m_\chi}\right) \mathcal{O}_{11}$
$\bar{\chi}\gamma^5 \chi\bar{q}\gamma^5 q$	$\rightarrow \left(\frac{h_2^N \lambda_2 m_N}{m_\phi^2 m_\chi}\right) \mathcal{O}_6$
Vector Mediator	
$\bar{\chi}\gamma^\mu \chi\bar{q}\gamma_\mu q$	$\rightarrow \left(-\frac{h_3^N \lambda_3}{m_G^2}\right) \mathcal{O}_1$
$\bar{\chi}\gamma^\mu \chi\bar{q}\gamma_\mu \gamma^5 q$	$\rightarrow \left(-\frac{2h_4^N \lambda_3}{m_G^2}\right) \left(-\mathcal{O}_7 + \frac{m_N}{m_\chi} \mathcal{O}_9\right)$
$\bar{\chi}\gamma^\mu \gamma^5 \chi\bar{q}\gamma_\mu q$	$\rightarrow \left(-\frac{2h_3^N \lambda_4}{m_G^2}\right) (\mathcal{O}_8 + \mathcal{O}_9)$
$\bar{\chi}\gamma^\mu \gamma^5 \chi\bar{q}\gamma_\mu \gamma^5 q$	$\rightarrow \left(\frac{4h_4^N \lambda_4}{m_G^2}\right) \mathcal{O}_4$

## Charged Scalar Mediator

$\bar{\chi}\chi\bar{q}q$	$\rightarrow \frac{l_2^\dagger l_2 - l_1^\dagger l_1}{4m_\phi^2} f_{Tq}^N \mathcal{O}_1$
$\bar{\chi}\chi\bar{q}\gamma^5 q$	$\rightarrow i \frac{l_1^\dagger l_2 - l_2^\dagger l_1}{4m_\phi^2} \Delta \tilde{q}^N \mathcal{O}_{10}$
$\bar{\chi}\gamma^5 \chi\bar{q}q$	$\rightarrow i \frac{l_1^\dagger l_1 - l_2^\dagger l_2}{4m_\phi^2} \frac{m_N}{m_\chi} f_{Tq}^N \mathcal{O}_{11}$
$\bar{\chi}\gamma^5 \chi\bar{q}\gamma^5 q$	$\rightarrow \frac{l_1^\dagger l_1 - l_2^\dagger l_2}{4m_\phi^2} \frac{m_N}{m_\chi} \Delta \tilde{q}^N \mathcal{O}_6$
$\bar{\chi}\gamma^\mu \chi\bar{q}\gamma_\mu q$	$\rightarrow -\frac{l_1^\dagger l_1 + l_2^\dagger l_2}{4m_\phi^2} \mathcal{N}_q^N \mathcal{O}_1$
$\bar{\chi}\gamma^\mu \gamma^5 \chi\bar{q}\gamma_\mu q$	$\rightarrow \frac{l_1^\dagger l_2 + l_2^\dagger l_1}{2m_\phi^2} \mathcal{N}_q^N (\mathcal{O}_8 + \mathcal{O}_9)$
$\bar{\chi}\gamma^\mu \chi\bar{q}\gamma_\mu \gamma^5 q$	$\rightarrow \frac{l_1^\dagger l_2 + l_2^\dagger l_1}{2m_\phi^2} \Delta_q^N (\mathcal{O}_7 - \frac{m_N}{m_\chi} \mathcal{O}_9)$
$\bar{\chi}\gamma^\mu \gamma^5 \chi\bar{q}\gamma_\mu \gamma^5 q$	$\rightarrow -\frac{l_1^\dagger l_1 + l_2^\dagger l_2}{m_\phi^2} \Delta_q^N \mathcal{O}_4$
$\bar{\chi}\sigma^{\mu\nu} \chi\bar{q}\sigma_{\mu\nu} q$	$\rightarrow \frac{l_2^\dagger l_2 - l_1^\dagger l_1}{m_\phi^2} \delta_q^N \mathcal{O}_4$
$\epsilon_{\mu\nu\alpha\beta} \bar{\chi}\sigma^{\mu\nu} \chi\bar{q}\sigma^{\alpha\beta} q$	$\rightarrow \frac{l_2^\dagger l_1 - l_1^\dagger l_2}{m_\phi^2} \delta_q^N (i\mathcal{O}_{10} - i\frac{m_N}{m_\chi} \mathcal{O}_{11} + 4\mathcal{O}_{12})$

## Charged Vector Mediator

$\bar{\chi}\chi\bar{q}q$	$\rightarrow \frac{d_2^\dagger d_2 - d_1^\dagger d_1}{4m_V^2} f_{Tq}^N \mathcal{O}_1$
$\bar{\chi}\chi\bar{q}\gamma^5 q$	$\rightarrow i \frac{d_1^\dagger d_1 - d_2^\dagger d_2}{4m_V^2} \Delta \tilde{q}^N \mathcal{O}_{10}$
$\bar{\chi}\gamma^5 \chi\bar{q}q$	$\rightarrow i \frac{d_1^\dagger d_1 - d_2^\dagger d_2}{4m_V^2} \frac{m_N}{m_\chi} f_{Tq}^N \mathcal{O}_{11}$
$\bar{\chi}\gamma^5 \chi\bar{q}\gamma^5 q$	$\rightarrow \frac{d_2^\dagger d_2 - d_1^\dagger d_1}{4m_V^2} \frac{m_N}{m_\chi} \Delta \tilde{q}^N \mathcal{O}_6$
$\bar{\chi}\gamma^\mu \chi\bar{q}\gamma_\mu q$	$\rightarrow \frac{d_2^\dagger d_2 + d_1^\dagger d_1}{8m_V^2} \mathcal{N}_q^N \mathcal{O}_1$
$\bar{\chi}\gamma^\mu \gamma^5 \chi\bar{q}\gamma_\mu q$	$\rightarrow -\frac{d_2^\dagger d_1 + d_1^\dagger d_2}{4m_V^2} \mathcal{N}_q^N (\mathcal{O}_8 + \mathcal{O}_9)$
$\bar{\chi}\gamma^\mu \chi\bar{q}\gamma_\mu \gamma^5 q$	$\rightarrow \frac{d_2^\dagger d_1 + d_1^\dagger d_2}{4m_V^2} \Delta_q^N (\mathcal{O}_7 - \frac{m_N}{m_\chi} \mathcal{O}_9)$
$\bar{\chi}\gamma^\mu \gamma^5 \chi\bar{q}\gamma_\mu \gamma^5 q$	$\rightarrow -\frac{d_2^\dagger d_2 + d_1^\dagger d_1}{2m_V^2} \Delta_q^N \mathcal{O}_4$

TABLE X. Non-relativistic reduction of operators for a spin-1 WIMP

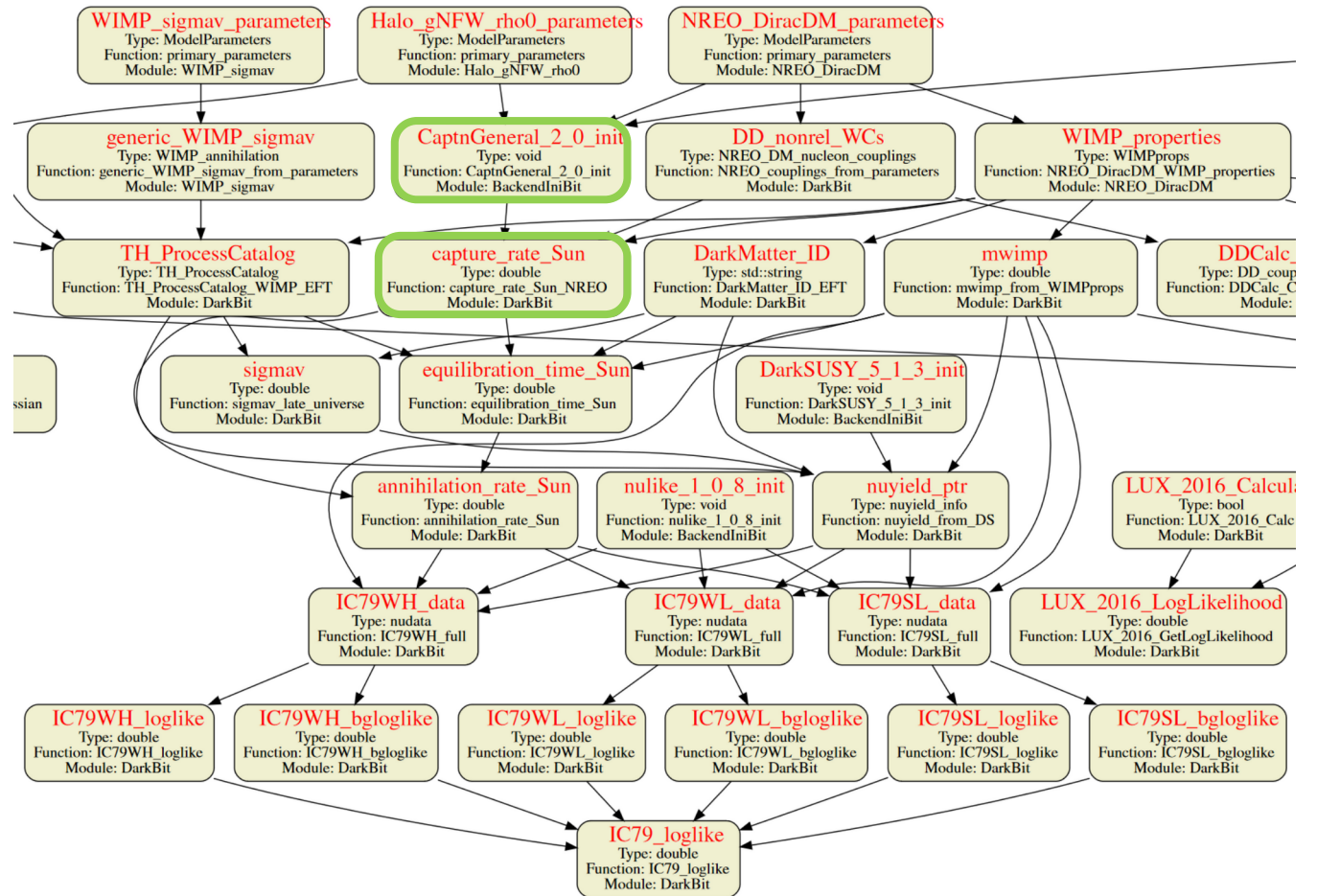
# Dent et. al. [3] Tables

- Spin-1 WIMP

Scalar Mediator	
$X_\mu^\dagger X^\mu \bar{q} q$	$\rightarrow \left( \frac{b_1 h_1^N}{m_\phi^2} \right) \mathcal{O}_1$
$X_\mu^\dagger X^\mu \bar{q} \gamma^5 q$	$\rightarrow \left( \frac{b_1 h_2^N}{m_\phi^2} \right) \mathcal{O}_{10}$
Vector Mediator	
$(X_\nu^\dagger \partial_\mu X^\nu - \partial_\mu X_\nu^\dagger X^\nu)(\bar{q} \gamma^\mu q)$	$\rightarrow 0$
$(X_\nu^\dagger \partial_\mu X^\nu - \partial_\mu X_\nu^\dagger X^\nu)(\bar{q} \gamma^\mu \gamma^5 q)$	$\rightarrow \left( \frac{-3b_5 h_4^N}{m_G^2} \frac{m_N}{m_X} \right) \mathcal{O}_{10}$
$\partial_\nu (X^{\nu\dagger} X_\mu + X_\mu^\dagger X^\nu)(\bar{q} \gamma^\mu q)$	$\rightarrow \left( \frac{\text{Re}(b_6) h_3^N}{m_G^2} \frac{m_N}{m_X} \right) (\mathcal{O}_5 + \mathcal{O}_6 - \frac{q^2}{m_N^2} \mathcal{O}_4)$
$\partial_\nu (X^{\nu\dagger} X_\mu + X_\mu^\dagger X^\nu)(\bar{q} \gamma^\mu \gamma^5 q)$	$\rightarrow \left( -\frac{2\text{Re}(b_6) h_4^N}{m_G^2} \frac{m_N}{m_X} \right) \mathcal{O}_9$
$\partial_\nu (X^{\nu\dagger} X_\mu - X_\mu^\dagger X^\nu)(\bar{q} \gamma^\mu q)$	$\rightarrow \left( -\frac{4\text{Im}(b_6) h_3^N}{m_G^2} \frac{m_N}{m_X} \right) \mathcal{O}_{17}$
$\partial_\nu (X^{\nu\dagger} X_\mu - X_\mu^\dagger X^\nu)(\bar{q} \gamma^\mu \gamma^5 q)$	$\rightarrow \left( \frac{4\text{Im}(b_6) h_4^N}{m_G^2} \frac{m_N}{m_X} \right) \mathcal{O}_{18}$
$\epsilon_{\mu\nu\rho\sigma} (X^{\nu\dagger} \partial^\rho X^\sigma + X^\nu \partial^\rho X^{\sigma\dagger})(\bar{q} \gamma^\mu q)$	$\rightarrow \left( \frac{\text{Re}(b_7) h_3^N}{m_G^2} \frac{m_N}{m_X} \right) \mathcal{O}_{11}$
$\epsilon_{\mu\nu\rho\sigma} (X^{\nu\dagger} \partial^\rho X^\sigma + X^\nu \partial^\rho X^{\sigma\dagger})(\bar{q} \gamma^\mu \gamma^5 q)$	$\rightarrow \left( \frac{\text{Re}(b_7) h_4^N}{m_G^2} \frac{m_N}{m_X} \right) (i \frac{q^2}{m_X m_N} \mathcal{O}_4 - i \frac{m_N}{m_X} \mathcal{O}_6 - 2\mathcal{O}_{14})$
$\epsilon_{\mu\nu\rho\sigma} (X^{\nu\dagger} \partial^\rho X^\sigma - X^\nu \partial^\rho X^{\sigma\dagger})(\bar{q} \gamma^\mu q)$	$\rightarrow \left( \frac{2\text{Im}(b_7) h_3^N}{m_G^2} \right) (\mathcal{O}_8 + \mathcal{O}_9)$
$\epsilon_{\mu\nu\rho\sigma} (X^{\nu\dagger} \partial^\rho X^\sigma - X^\nu \partial^\rho X^{\sigma\dagger})(\bar{q} \gamma^\mu \gamma^5 q)$	$\rightarrow \left( \frac{4\text{Im}(b_7) h_4^N}{m_G^2} \right) \mathcal{O}_4$
Charged Spinor Mediator	
$(X_\mu^\dagger X_\nu)(\bar{q} \gamma^\mu \gamma^\nu q)$	$\rightarrow \left( \frac{y_3^\dagger y_3 - y_4^\dagger y_4}{m_Q m_X} \right) (f_{Tq}^N \mathcal{O}_1 + 2\delta_q^N \mathcal{O}_4)$
$(X_\mu^\dagger X_\nu)(\bar{q} \gamma^\mu \gamma^\nu \gamma^5 q)$	$\rightarrow \left( \frac{y_4^\dagger y_3 - y_3^\dagger y_4}{m_Q m_X} \right) (i\Delta_q^N \mathcal{O}_{10} + i\delta_q^N \mathcal{O}_{11} - 2i\delta_q^N \mathcal{O}_{12} - 2i\delta_q^N \mathcal{O}_{18})$

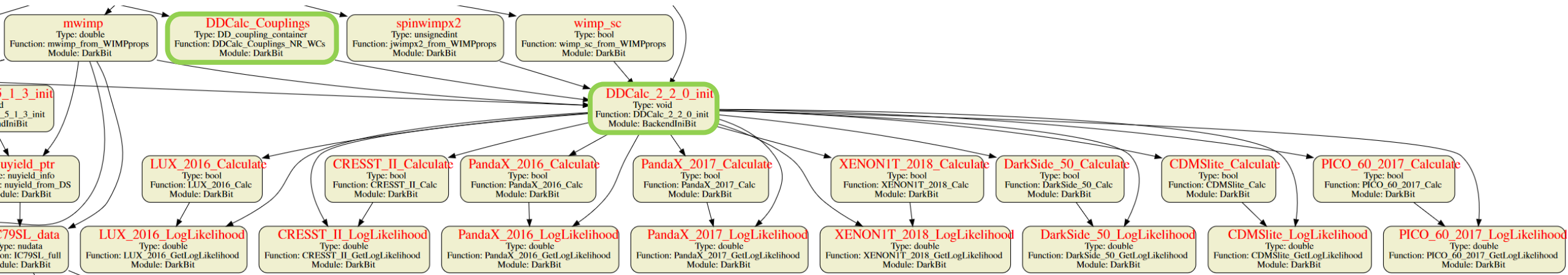
# GAMBIT-Capt'n Dependency

- Capt'n acts as a backend of DarkBit
- It is used to calculate the capture rate for GAMBIT



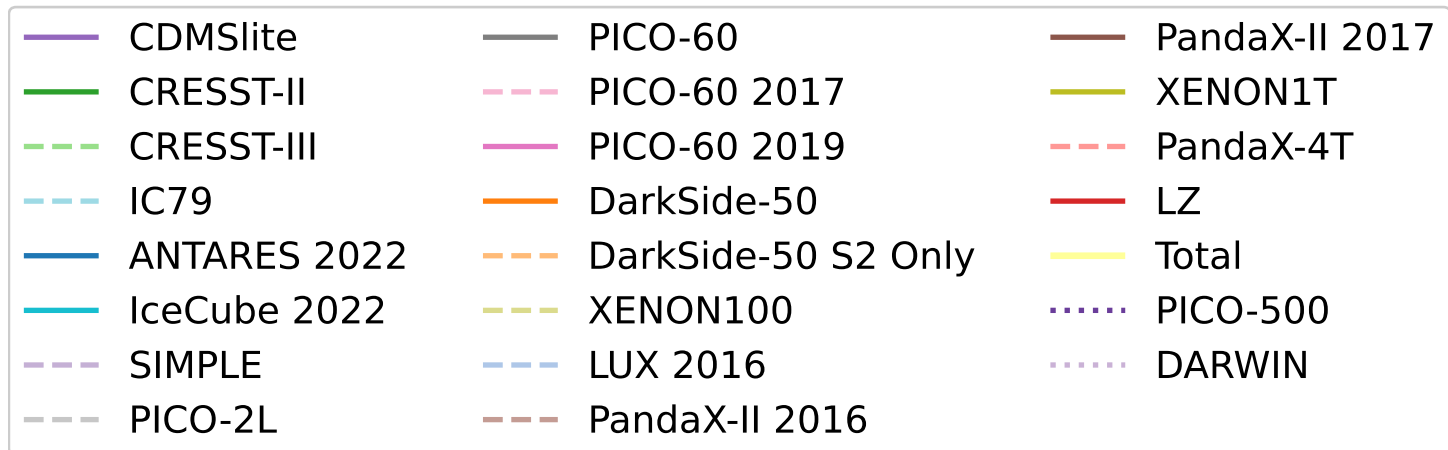
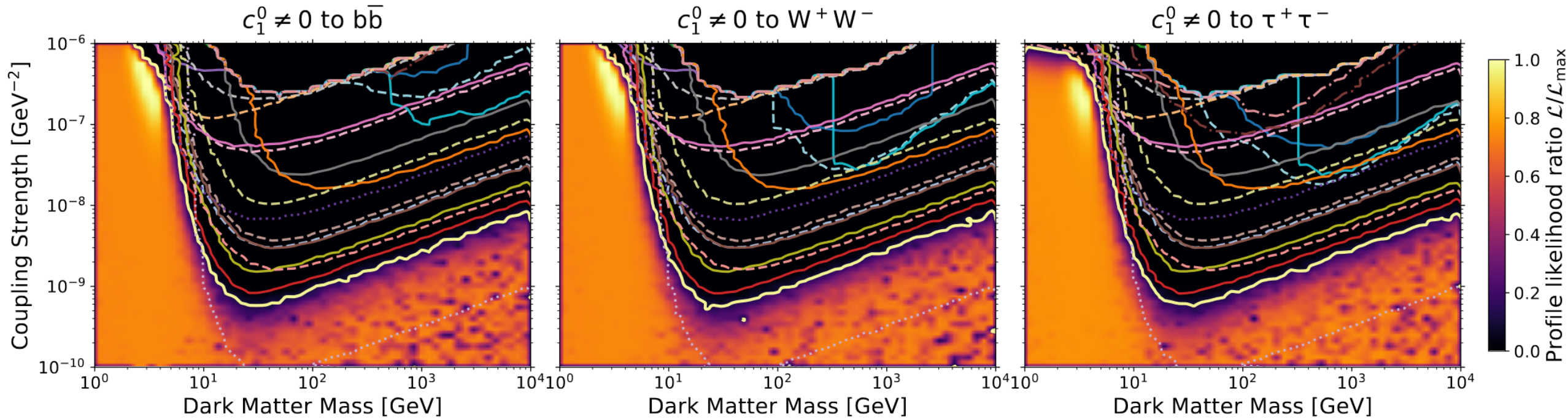
# GAMBIT Direct Detection

- DDCalc acts to translate the couplings to cross sections for the DD experiments

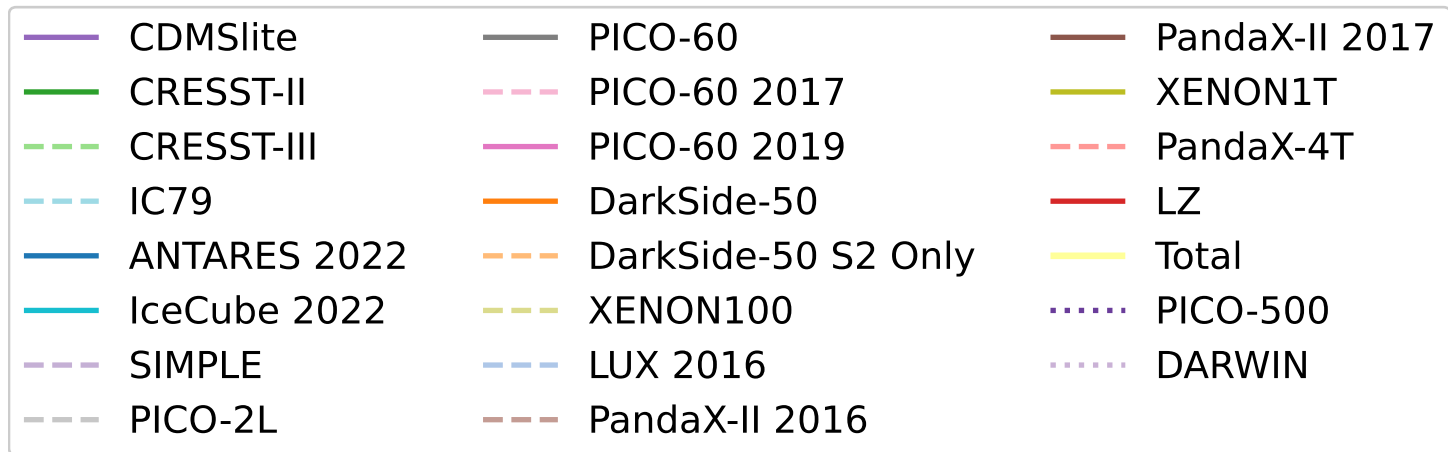
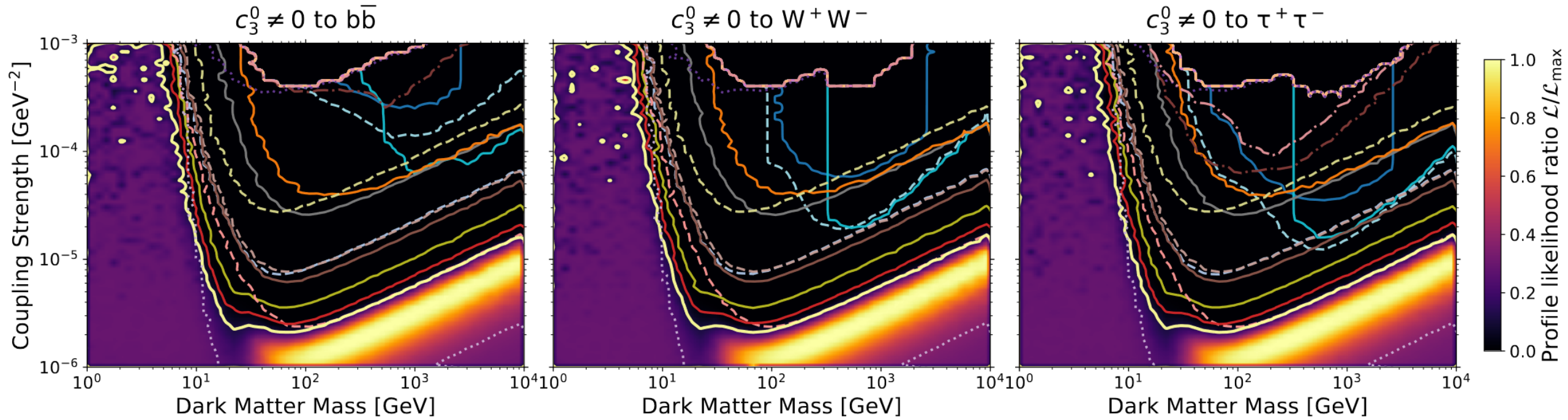




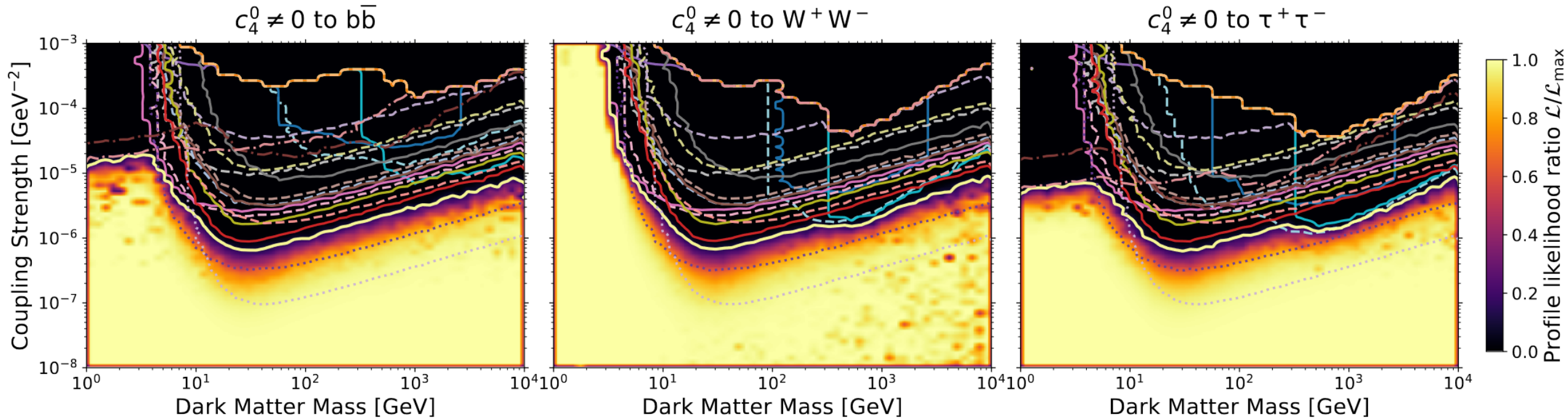
# $c_1$ Channels



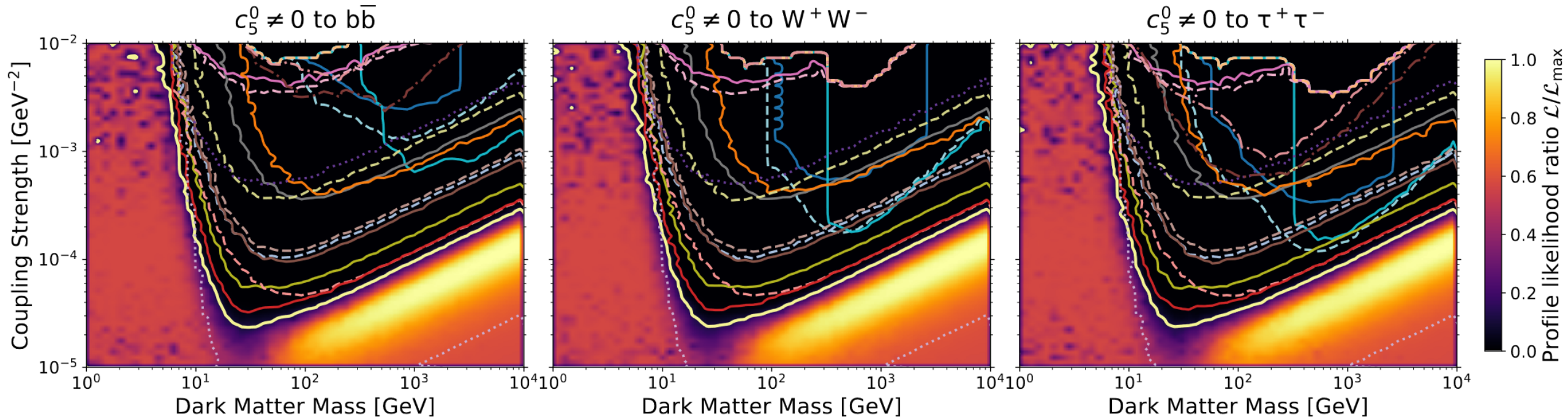
# $c_3$ Channels



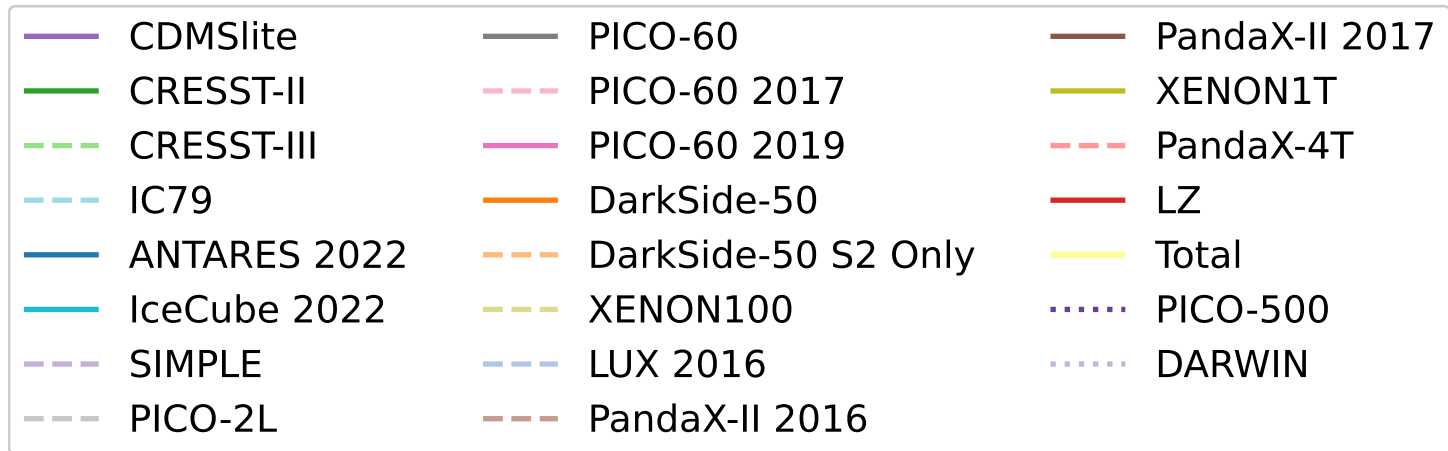
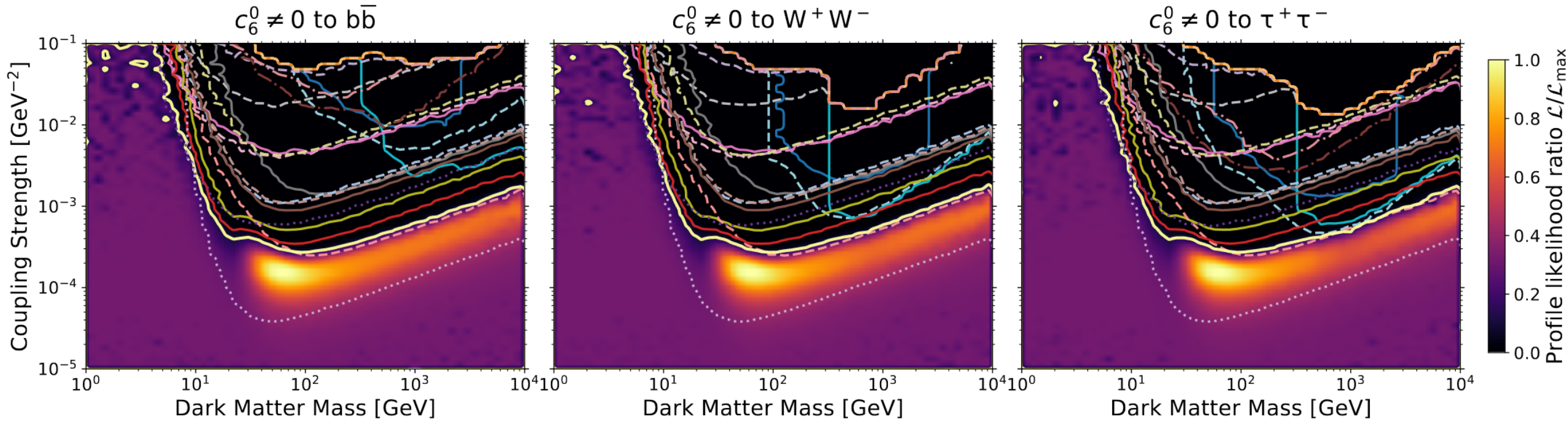
# $c_4$ Channels



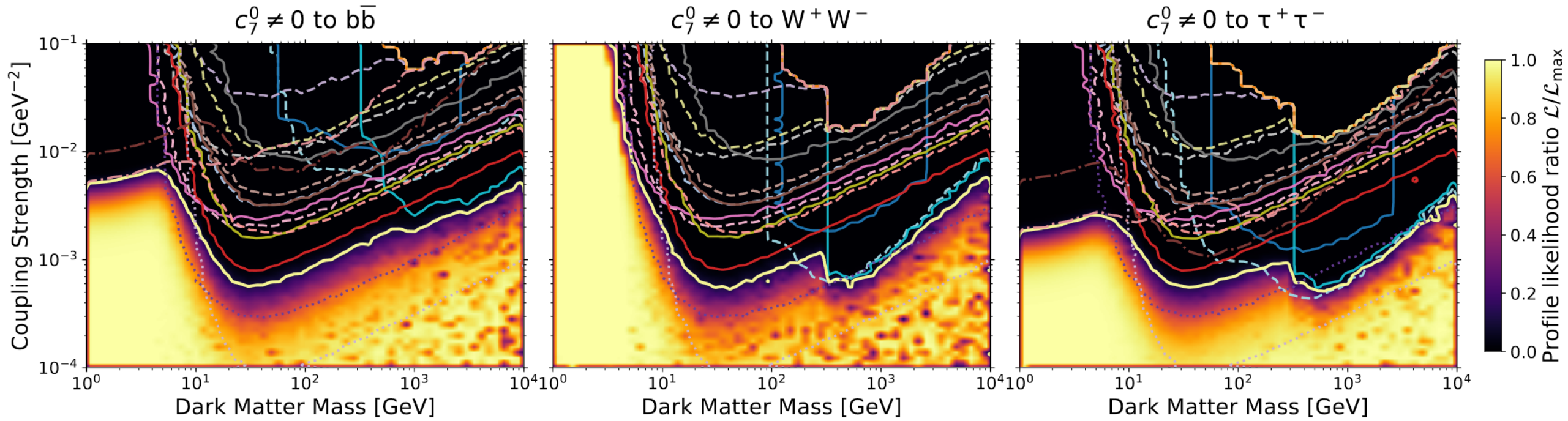
# $c_5$ Channels



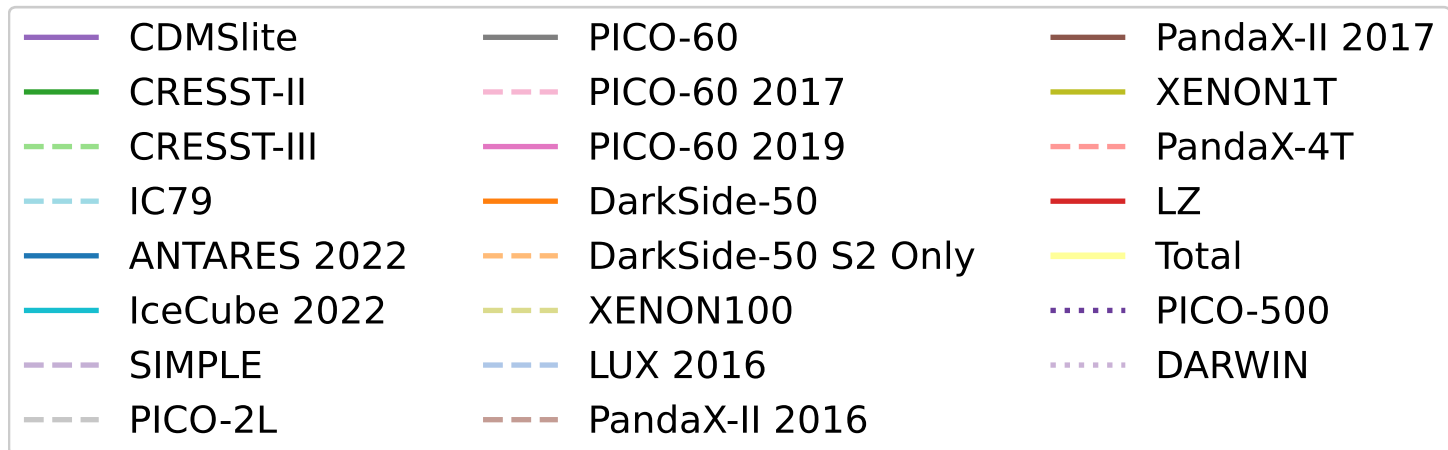
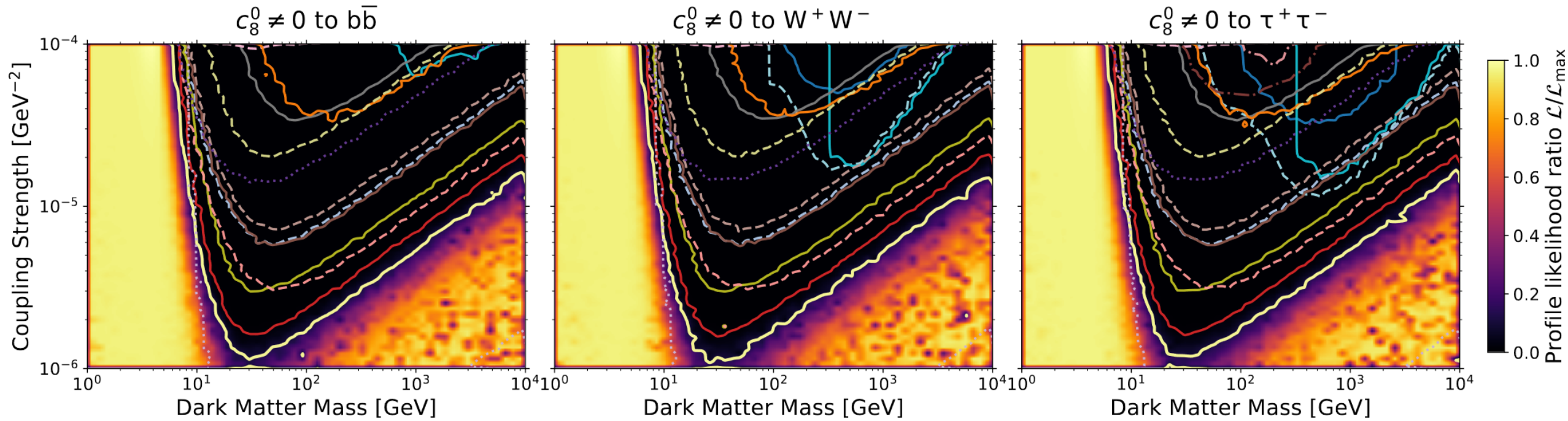
# $c_6$ Channels



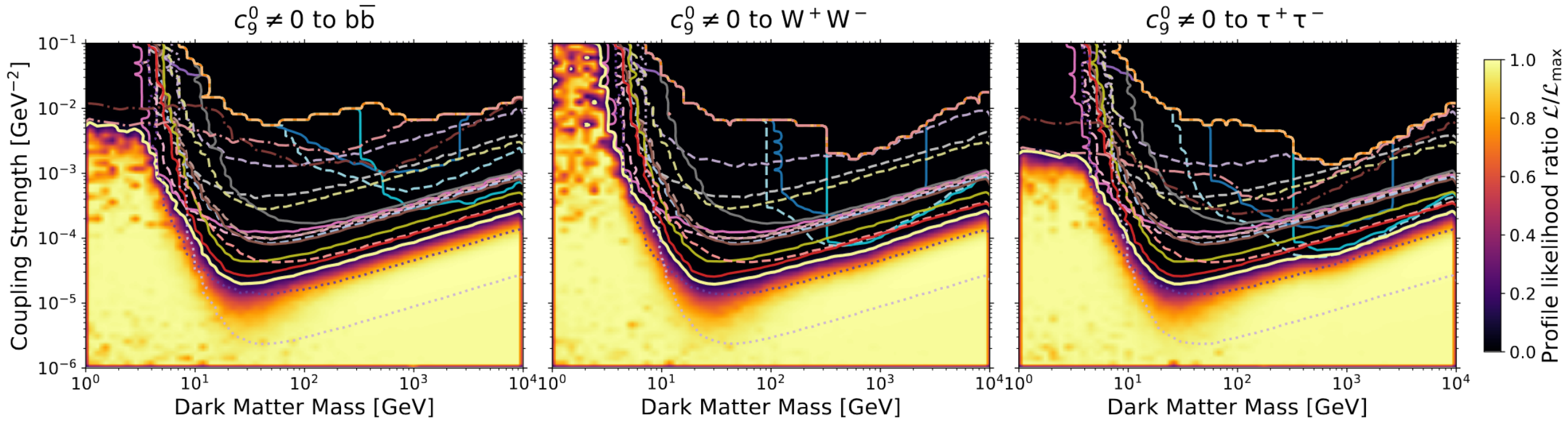
# $c_7$ Channels



# $c_8$ Channels

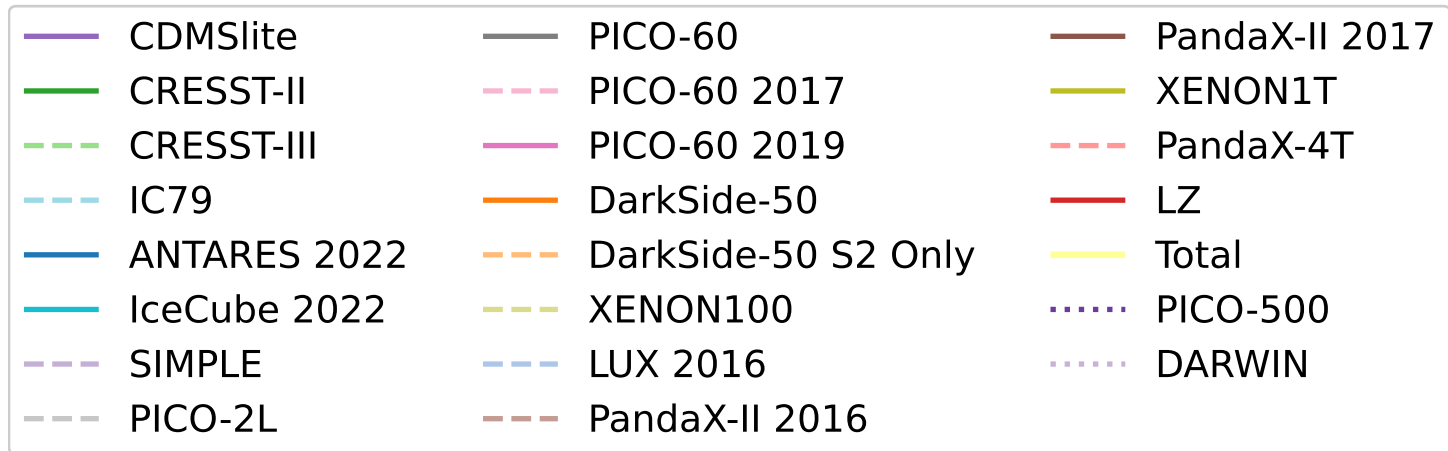
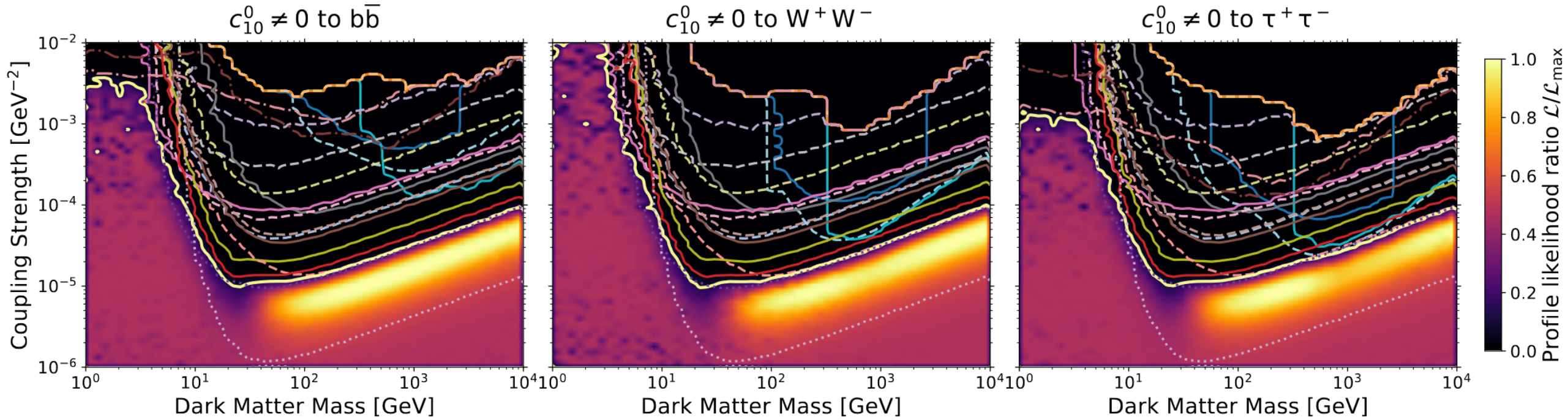


# $c_9$ Channels

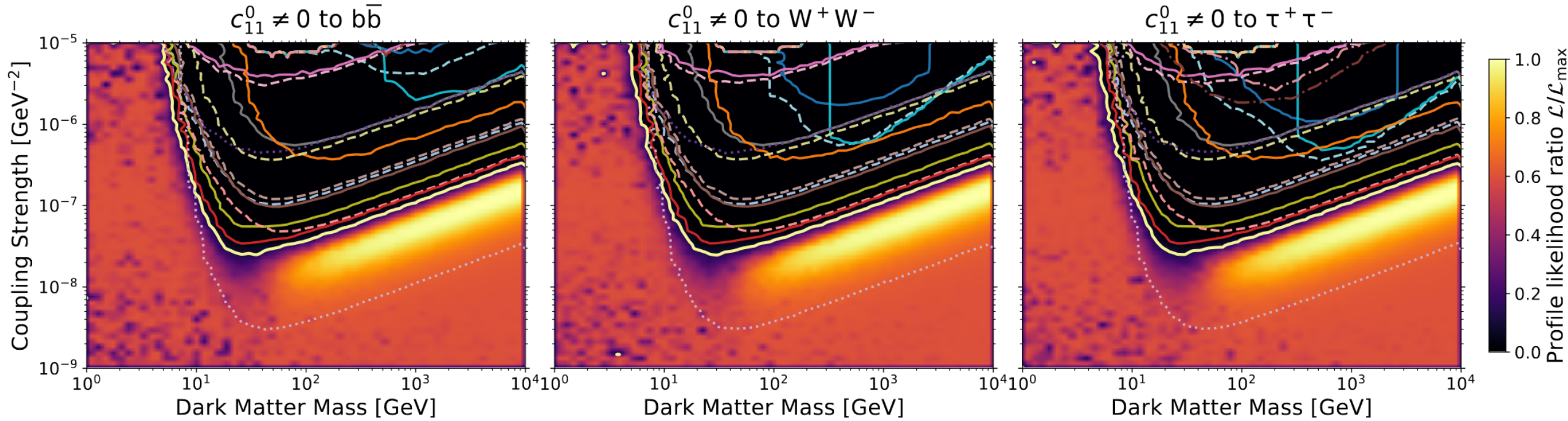




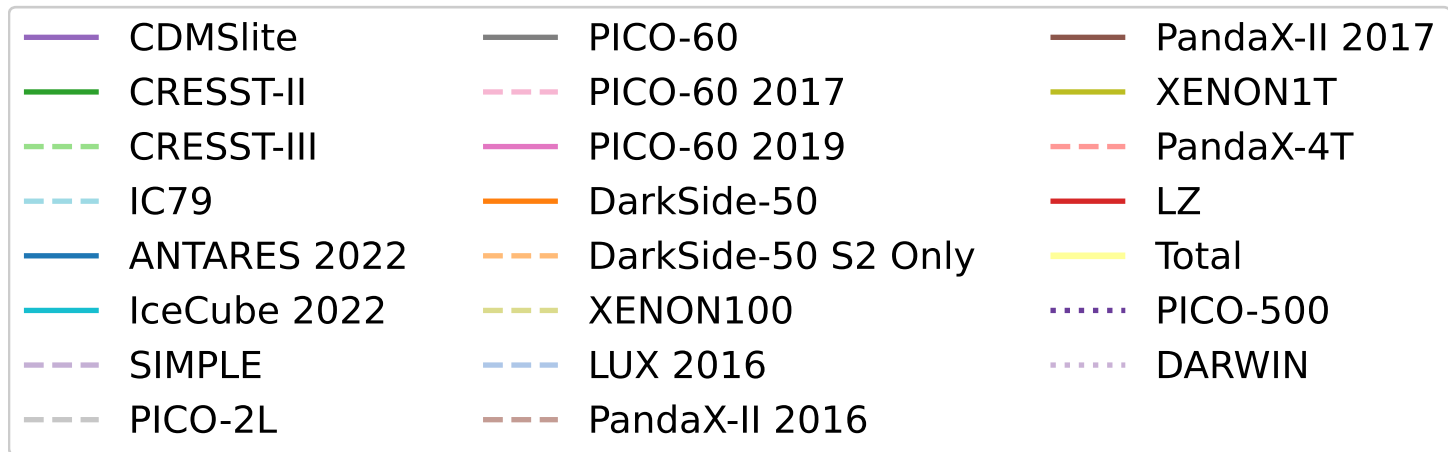
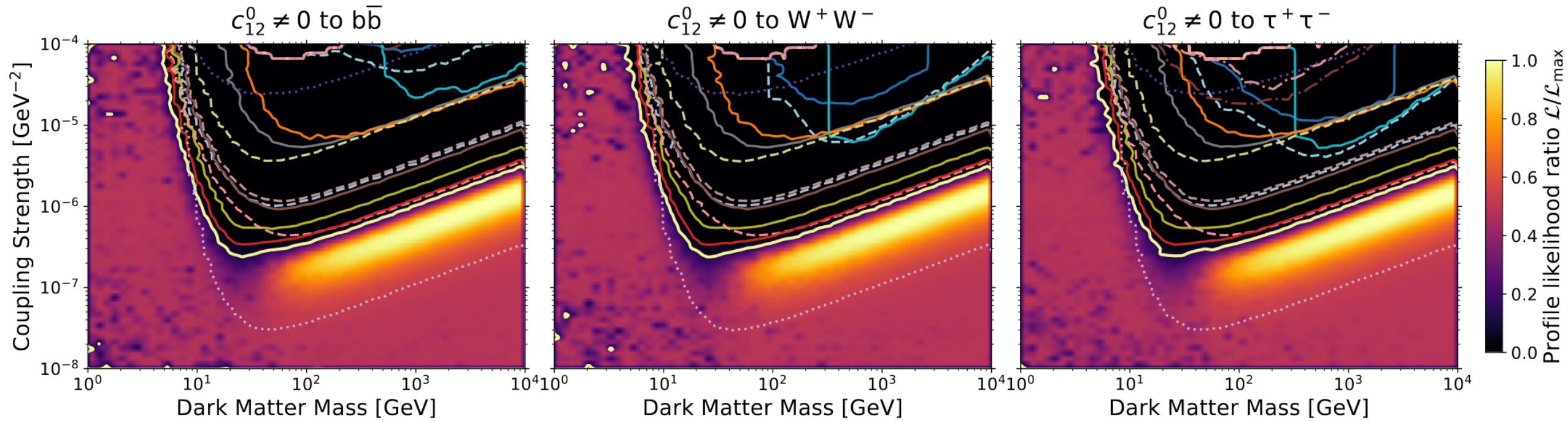
# $c_{10}$ Channels



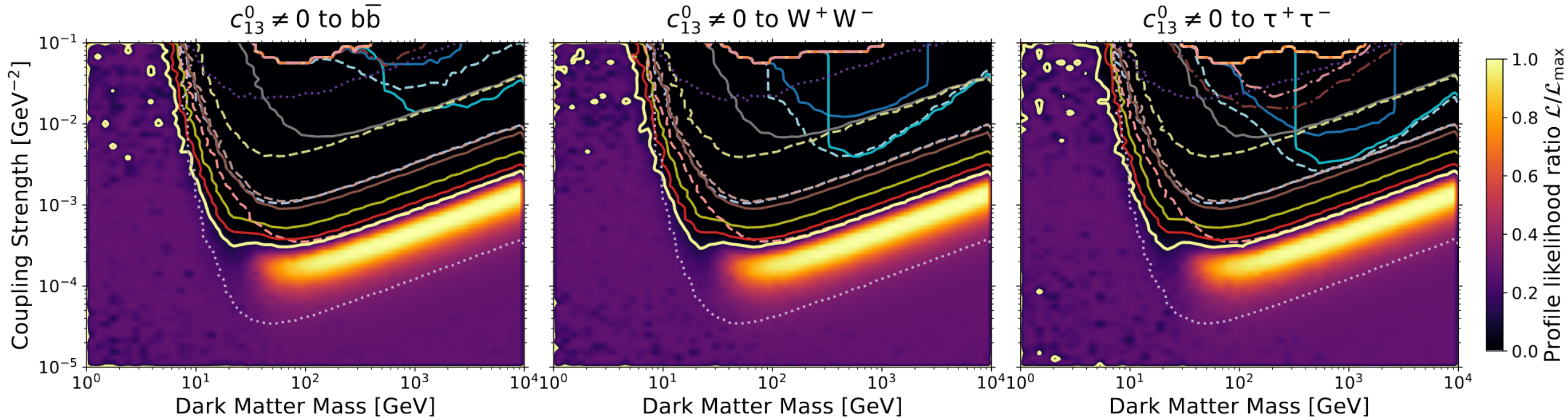
# $c_{11}$ Channels



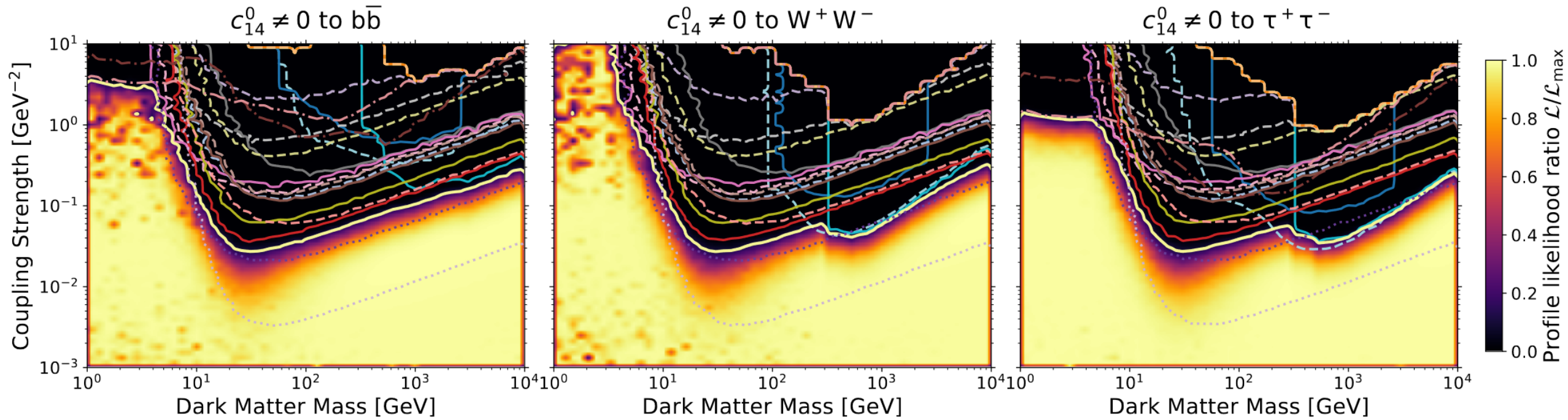
# $c_{12}$ Channels



# $c_{13}$ Channels



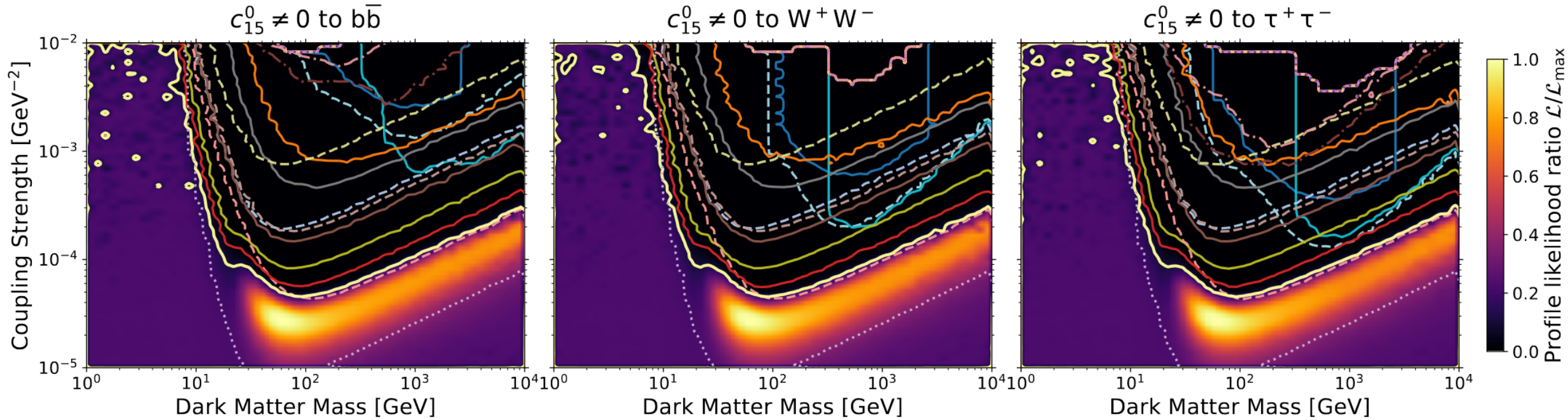
# $c_{14}$ Channels



- |                  |                           |                  |
|------------------|---------------------------|------------------|
| — CDMSlite       | — PICO-60                 | — PandaX-II 2017 |
| — CRESST-II      | - - - PICO-60 2017        | — XENON1T        |
| - - - CRESST-III | — PICO-60 2019            | - - - PandaX-4T  |
| - - - IC79       | — DarkSide-50             | — LZ             |
| — ANTARES 2022   | - - - DarkSide-50 S2 Only | — Total          |
| — IceCube 2022   | - - - XENON100            | - - - PICO-500   |
| - - - SIMPLE     | - - - LUX 2016            | - - - DARWIN     |
| - - - PICO-2L    | - - - PandaX-II 2016      |                  |



# $c_{15}$ Channels

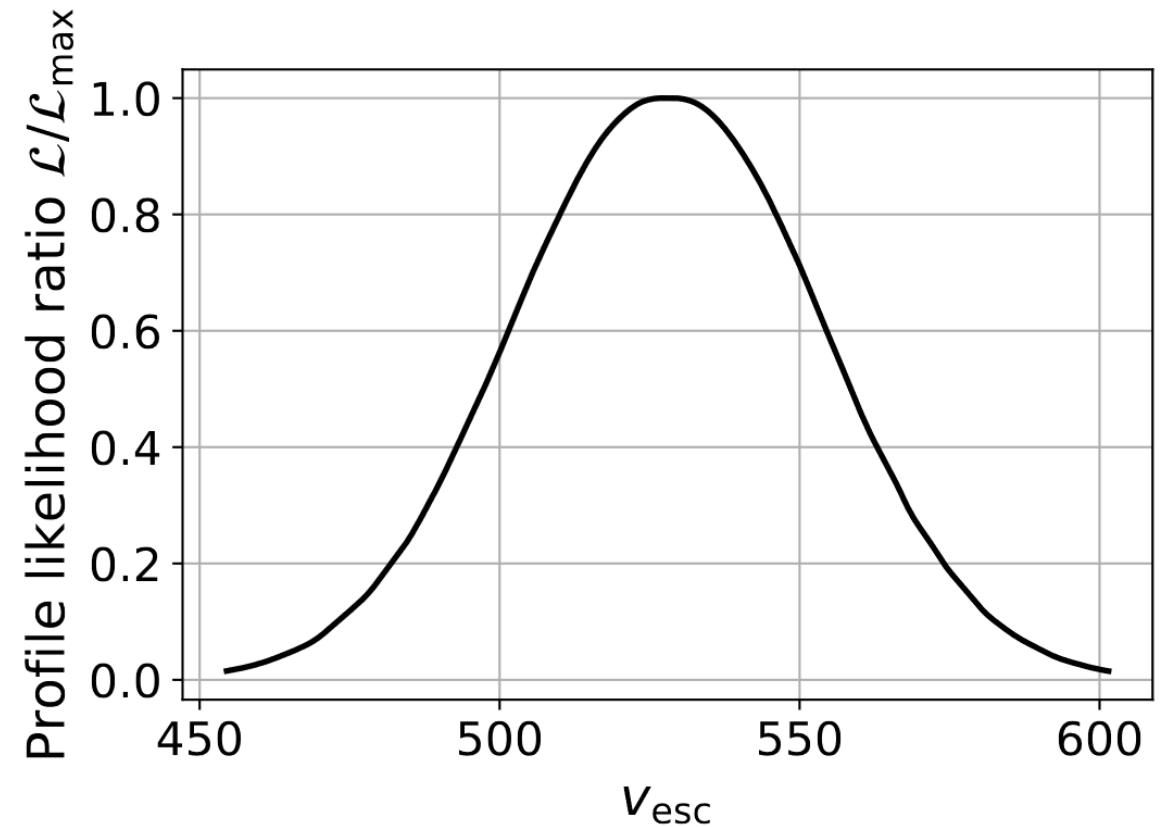
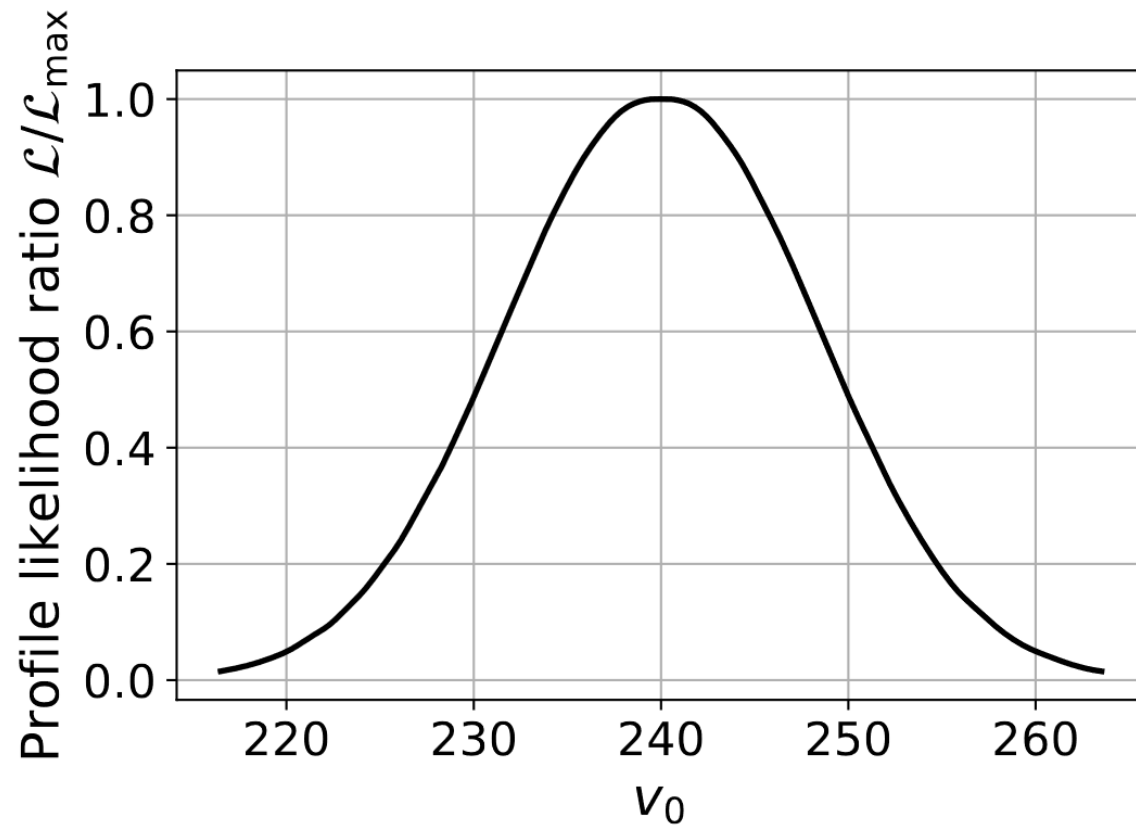


- |                  |                           |                  |
|------------------|---------------------------|------------------|
| — CDMSlite       | — PICO-60                 | — PandaX-II 2017 |
| — CRESST-II      | - - - PICO-60 2017        | — XENON1T        |
| - - - CRESST-III | — PICO-60 2019            | - - - PandaX-4T  |
| - - - IC79       | — DarkSide-50             | — LZ             |
| — ANTARES 2022   | - - - DarkSide-50 S2 Only | — Total          |
| — IceCube 2022   | — XENON100                | - - - PICO-500   |
| - - - SIMPLE     | - - - LUX 2016            | - - - DARWIN     |
| - - - PICO-2L    | - - - PandaX-II 2016      |                  |



# Nuisance Parameters

- The nuisance parameters showed no preference





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