
Non-linear top-Higgs CP violation

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The logo for DPF-PHENO 2024 features the text "DPF-PHENO 2024" in a bold, blue, sans-serif font. The text is centered within a light blue rectangular background that has a subtle, wispy cloud-like texture. The logo is flanked by two short, horizontal gold bars on either side.

DPF-PHENO 2024



Introduction

- ❑ Lack of experimental evidence of new physics may indicate a mass gap between SM and BSM scales
- ❑ BSM physics influencing the Higgs sector, two common EFTs: SMEFT and HEFT
- ❑ SMEFT Lagrangian

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_{i>4} \sum_k \frac{C_k^{(i)}}{\Lambda^{i-4}} \mathcal{O}_k^{(i)}$$

- ❑ HEFT merges chiral perturbation theory (χ PT) within the scalar sector with SMEFT across fermion and gauge sectors.
- ❑ we ask the question of *“how sensitive the LHC can be to sources of non-linear CP violation?”*

CP violation in top-Higgs sector (SMEFT)

The SMEFT approach

$$\mathcal{O}_{t\Phi} = |\Phi|^2 \bar{Q}_L \Phi^c t_R$$

This operator in the broken phase generates P-violating interactions for complex Wilson coefficients.

A phenomenologically identical parametrization of

$$\mathcal{L}_{\alpha,1}^{\text{SMEFT}} = -\frac{m_t}{v} \kappa_t \bar{t} (\cos \alpha + i\gamma^5 \sin \alpha) t h.$$

$\alpha \rightarrow$ CP phase $\kappa_t \rightarrow$ strength of the interaction

For SM, $\kappa_t = 1, \alpha = 0$

CP violation in top-Higgs sector (SMEFT)

renormalization of the SM Yukawa couplings, leads to

$$\mathcal{L}_{\alpha,2}^{\text{SMEFT}} \supset -\frac{3m_t}{2v^2} \bar{t}(\{\kappa_t \cos \alpha - 1\} + i\kappa_t \gamma^5 \sin \alpha) t h^2,$$

The $t\bar{t}hh$ interactions vanish for the SM point, $(\kappa_t, \alpha)_{\text{SM}} = (1, 0)$

$$\left. \frac{\Gamma_{\bar{t}th}}{\Gamma_{\bar{t}th^2}} \right|_{\gamma^5, \text{SMEFT}} = \frac{v}{3}$$

The relative strength of CP-violating tree-level three and four-point irreducible vertex functions

CP-violation in the top Higgs sector under the assumptions of SMEFT should manifest themselves predominantly in single Higgs physics → **significant statistical pull in a global analysis.**

CP violation in top-Higgs sector (HEFT)

The HEFT approach

- In HEFT which highlights the Higgs boson as a custodial singlet.
- In the non-linear sigma model of $SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$, GBs can be parametrized as

$$U(\pi^a) = \exp(i\pi^a \tau^a / v)$$

[Buchalla et al.1307.5017](#)
[Brivio et al.1604.06801](#)
[Dawson et al. 2311.16897](#)

- This transforms as $U \rightarrow LUR^\dagger$
- the top quark mass arises from

$$\mathcal{O}_{\bar{t}t} = -m_t \bar{Q}_L U t_R \quad \text{this operator can be dressed with a "flare" function}$$

$$Y_t(h) = 1 + c^{(1)} \frac{h}{v} + c^{(2)} \frac{h^2}{2v^2} + \dots,$$

CP violation in top-Higgs sector (HEFT)

The HEFT approach

This leads to CP-violating effects

$$\mathcal{L}_{\text{HEFT}} \supset Y_t(h) \mathcal{O}_{\bar{t}t} + \text{h.c.} \supset i \text{Im } c^{(1)} \frac{1}{\sqrt{2}} \bar{t} \gamma^5 t h + i \text{Im } c^{(2)} \frac{1}{2v\sqrt{2}} \bar{t} \gamma^5 t h^2 + \dots,$$

The parametrization of the HEFT interactions analogous to \mathcal{L}_α

$$\mathcal{L}_{\text{HEFT}} \supset -\frac{m_t}{v} \kappa_t \bar{t} (\cos \alpha + i \gamma^5 \sin \alpha) t h - \frac{m_t}{2v^2} \kappa_{tt} \bar{t} (\cos \beta + i \gamma^5 \sin \beta) t h^2.$$

The Higgs multiplicities remain uncorrelated.

The relative strength of CP-violation for the three and four-point interactions in HEFT

$$\left. \frac{\Gamma_{\bar{t}th}}{\Gamma_{\bar{t}th^2}} \right|_{\gamma^5, \text{HEFT}} = \frac{\kappa_t}{\kappa_{tt}} \frac{\sin \alpha}{\sin \beta} v$$

SMEFT vs HEFT

The SMEFT trajectory can be recovered by the HEFT choices

$$\kappa_{tt}^2 = 9(1 - 2\kappa_t \cos \alpha + \kappa_t^2)$$

$$\tan \beta = \frac{\kappa_t \sin \alpha}{\kappa_t \cos \alpha - 1}$$

$$\frac{d\sigma}{d\text{LIPS}} \sim |\mathcal{M}_{\text{SM}}|^2 + \boxed{2\text{Re}(\mathcal{M}_{\text{SM}}\mathcal{M}_{\mathcal{O}}^*)} + \boxed{|\mathcal{M}_{\mathcal{O}}|^2}.$$

Squared CP-odd contributions manifest in CP-even distributions, cross sections, transverse momentum distributions, etc.

Interference effects between SM and new physics are resolved through purpose-built CP odd observables.

Sensitive Processes for tth and tthh interactions

☐ Sensitive through rate:

- > gg \rightarrow h production CMS-PAS-FTR-16-002
- > Z boson-associated Higgs production PRD 89 013013 (2014), PRD 92 073006 (2015)
- > tthh & other di-Higgs production PLB 743, 93 (2015), ATL-PHYS-PUB-2022-053

☐ Sensitive through signed asymmetric variables

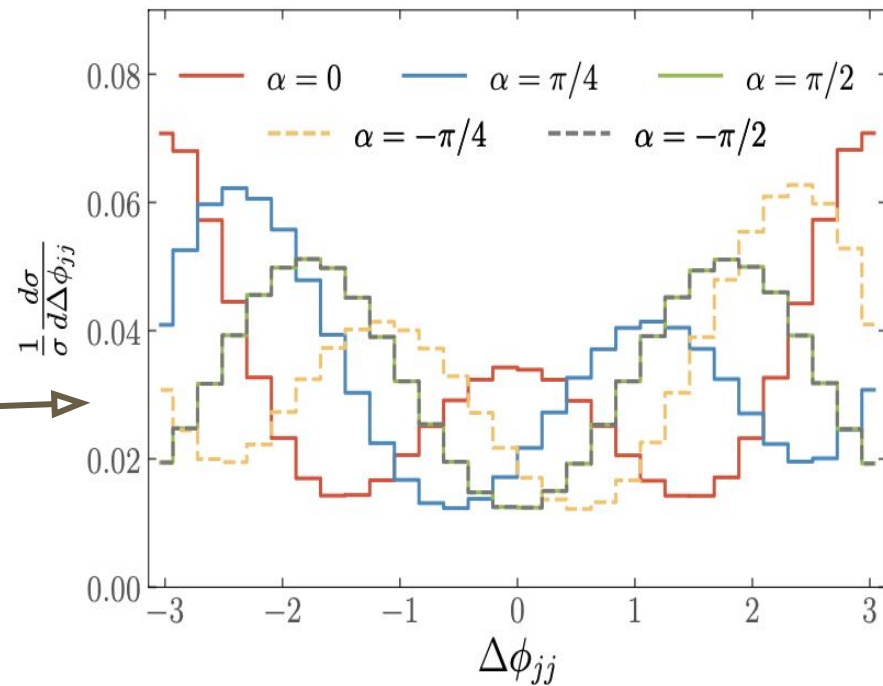
- > Gluon fusion h + 2j PRL 88 051801 (2002), PRD 90, 013010 (2014)
- > Top-associated Higgs production (tth) JHEP 06 079 (2018), JHEP 01 158 (2022)

☐ Sensitive through Z polarization

- > Z boson-associated Higgs production PRD 89 013013 (2014), PRD 92 073006 (2015)

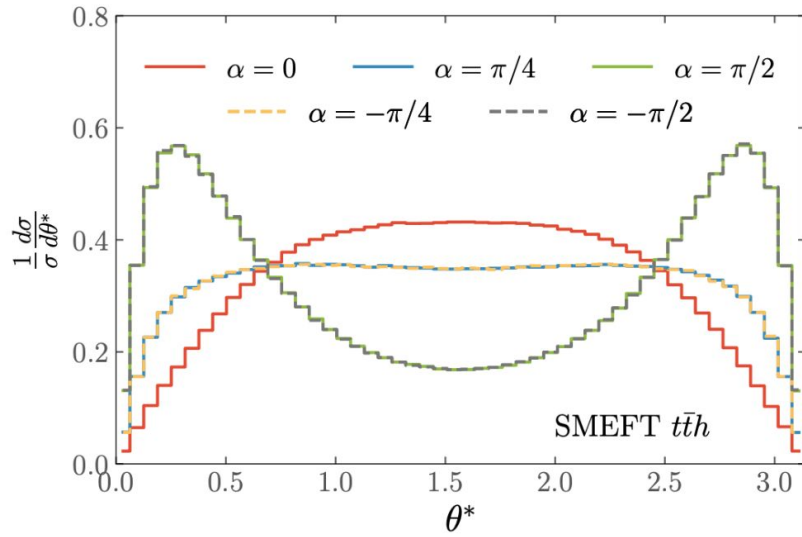
Sensitive Processes for tth and tthh interactions

- Sensitive through rate:
 - > gg \rightarrow h production
 - > Z boson-associated Higgs production
 - > tthh & other di-Higgs production
- Sensitive through signed asymmetric variables
 - > Gluon fusion h + 2j \rightarrow $\Delta\phi_{jj}$
 - > Top-associated Higgs production (tth)
- Sensitive through Z polarization
 - > Z boson-associated Higgs production



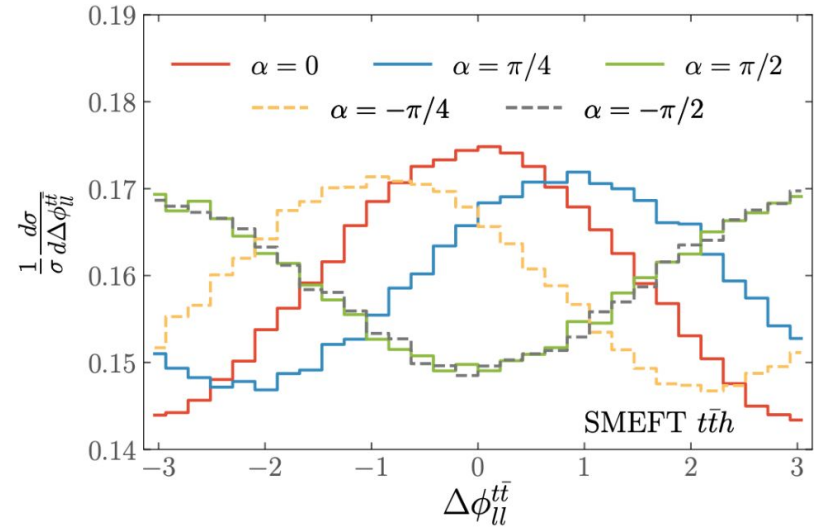
Distribution for the $\Delta\phi_{jj}$ ($= \phi_{j_1} - \phi_{j_2}$)
between the two tagging jets in h+2j

CP-odd observables for $t\bar{t}h$



Collins-Soper Angle

The angle between the top quark and the beam direction in the $t\bar{t}$ CM frame.



Azimuthal angle distribution

$$\Delta\phi_{ik}^{t\bar{t}} = \text{sgn} [\vec{p}_t \cdot (\vec{p}_i \times \vec{p}_k)] \arccos \left(\frac{\vec{p}_t \times \vec{p}_i}{|\vec{p}_t \times \vec{p}_i|} \cdot \frac{\vec{p}_t \times \vec{p}_k}{|\vec{p}_t \times \vec{p}_k|} \right)$$

Non-linear CPV in Top-Higgs sector: χ^2 Fit

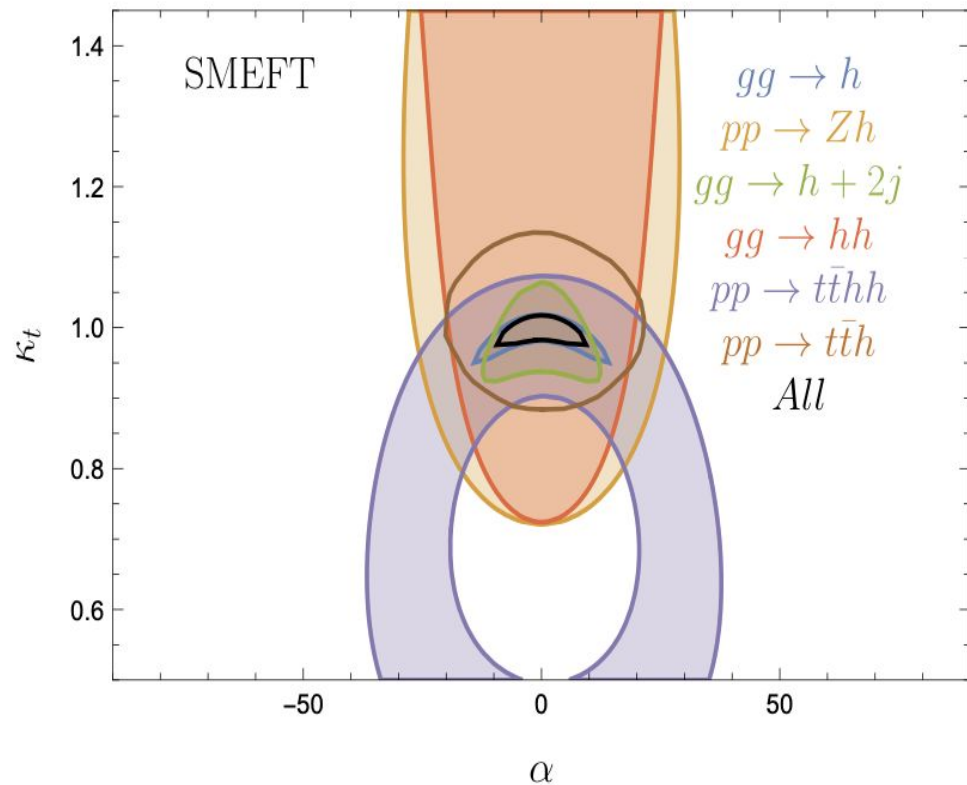
The asymmetries and total rates are used to set CL limits on the parameter space

$$(\kappa_t, \alpha, \kappa_{tt}, \beta)$$

$$\chi^2 = \sum_i \frac{(N_i - N_i^{\text{SM}})^2}{\sigma_i^2}$$

Directly probing the top Yukawa coupling through the $t\bar{t}h$ channel also leads to relevant complementary constraints.

highest statistical abundance \rightarrow most sensitive



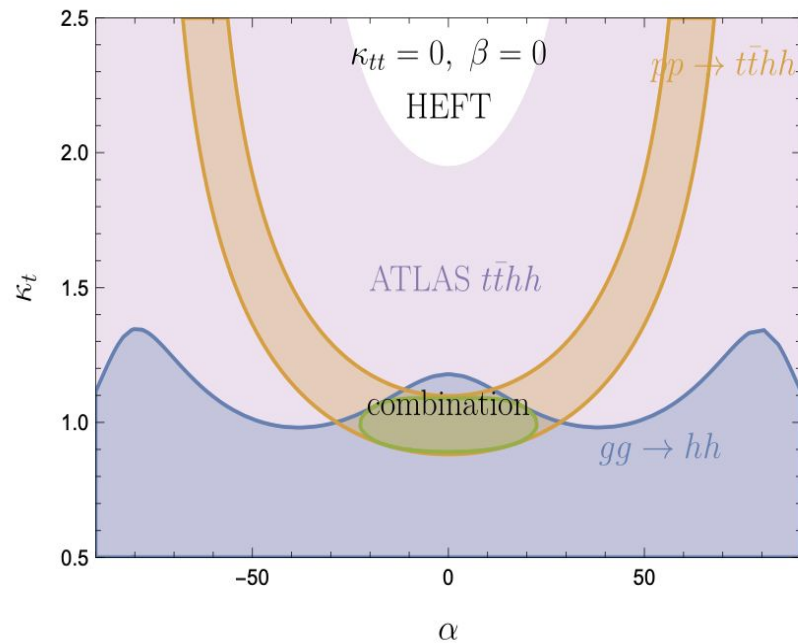
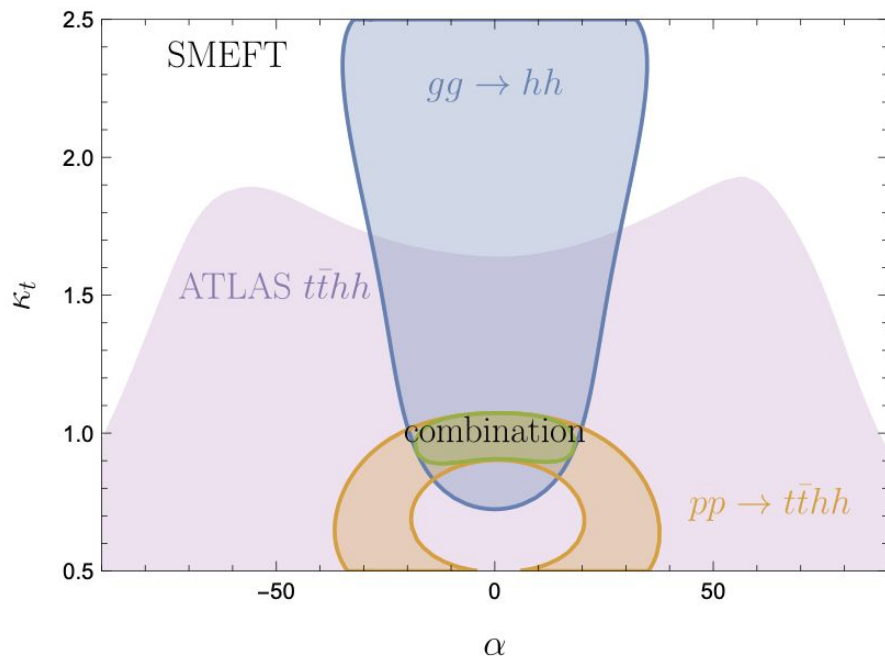
95% CL limits for the 13 TeV HL-LHC with 3 ab^{-1} [SMEFT]

SMEFT

VS

HEFT

Multi-Higgs production serves as means to distinguish non-linearity



95% CL limits at the 13 TeV HL-LHC with 3 ab^{-1} of data for hh and tthh channels

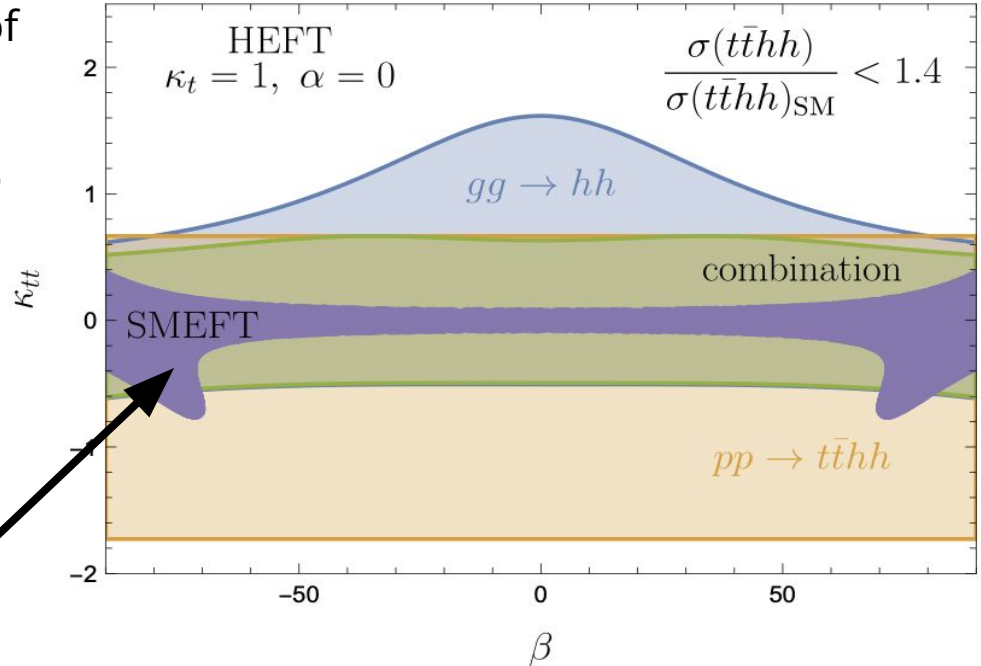
Non-linear CP violation

- ❑ Sets constraints on the magnitude of the contact interaction (κ_{tt})
- ❑ $gg \rightarrow hh$ production is very sensitive to κ_{tt} and associated CPV in HEFT
- ❑ The role of $t\bar{t}hh$ production remains critical, even when only the κ_{tt} effects are considered

SMEFT region selected from a fit to single Higgs data

$$\kappa_{tt}^2 = 9(1 - 2\kappa_t \cos \alpha + \kappa_t^2)$$

$$\tan \beta = \frac{\kappa_t \sin \alpha}{\kappa_t \cos \alpha - 1}$$



95% CL limits on (κ_{tt}, β) at the 13 TeV with 3 ab^{-1} of data for hh and $t\bar{t}hh$ channels in HEFT

Conclusion

- ❑ We explored CPV in top-Higgs sector at the LHC by combining the sensitivity of a range of single and double Higgs production processes.
- ❑ In SMEFT, multi-Higgs production does not lead to any significant sensitivity gain as single Higgs processes encompass all the relevant correlations in dim-6.
- ❑ But, the paradigm shifts when considering non-linear sources of CP violation.
- ❑ LHC shows sensitivity when discriminating between SMEFTy and HEFTy CP violation in the top-Higgs sector.
- ❑ Due to statistical limitations of multi-H study at the LHC, future hadron colliders are necessary

Thank you

Back up

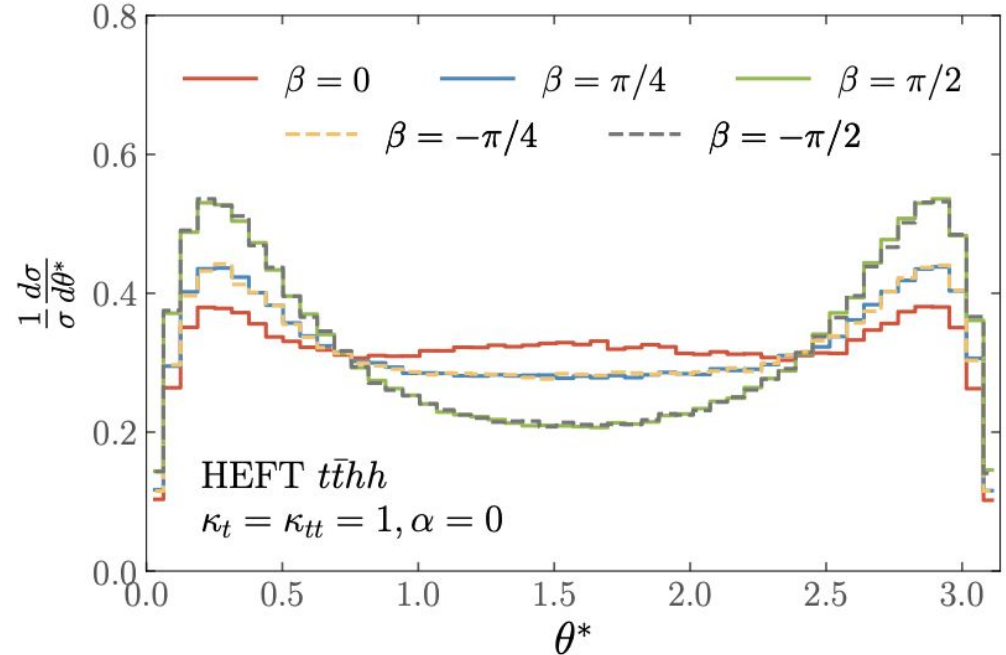
$$\begin{aligned}\mathcal{L}_{\text{SMEFT}} &\supset \frac{C_{t\Phi}}{\Lambda^2} \mathcal{O}_{t\Phi} + \text{h.c.} \\ &\supset i \text{Im}(C_{t\Phi}) \frac{v^2}{\sqrt{2}\Lambda^2} \bar{t}\gamma^5 t h + i \text{Im}(C_{t\Phi}) \frac{3v}{2\sqrt{2}\Lambda^2} \bar{t}\gamma^5 t h^2 + \dots\end{aligned}$$

After renormalisation of the SM Yukawa couplings and assuming a purely CP-even SM coupling of the top quark

$$\frac{1}{\Lambda^2} \begin{pmatrix} \text{Re } C_{t\Phi} \\ \text{Im } C_{t\Phi} \end{pmatrix} = -\frac{\sqrt{2} m_t}{v^3} \begin{pmatrix} \kappa_t \cos \alpha - 1 \\ \kappa_t \sin \alpha \end{pmatrix}.$$

Beyond linearity: tthh inclusive hh production

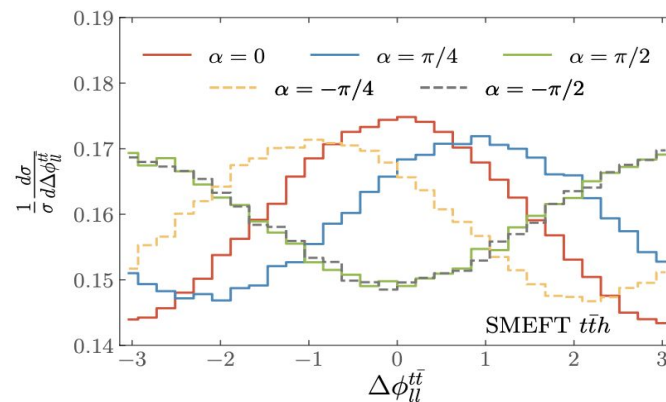
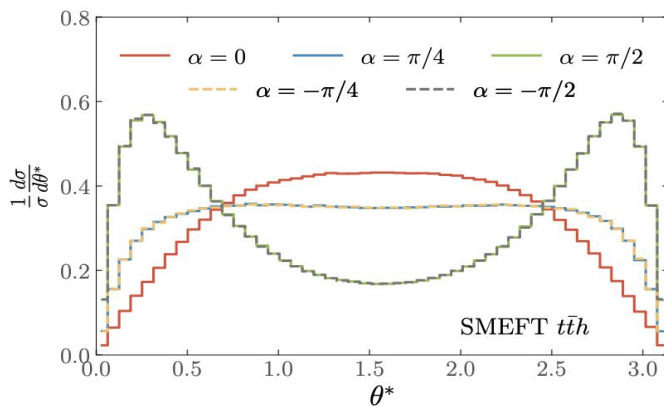
The angle between the top quark and the beam direction in the tt CM frame



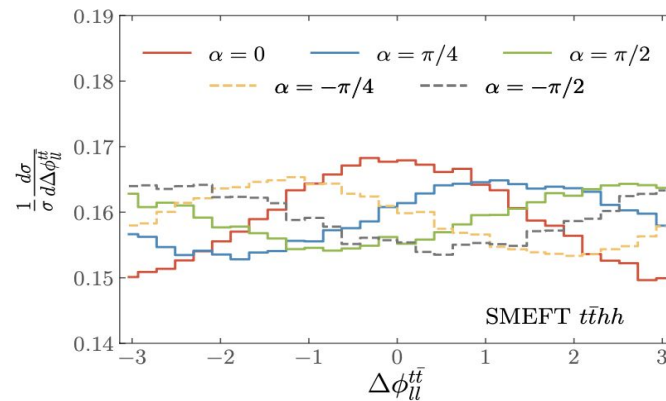
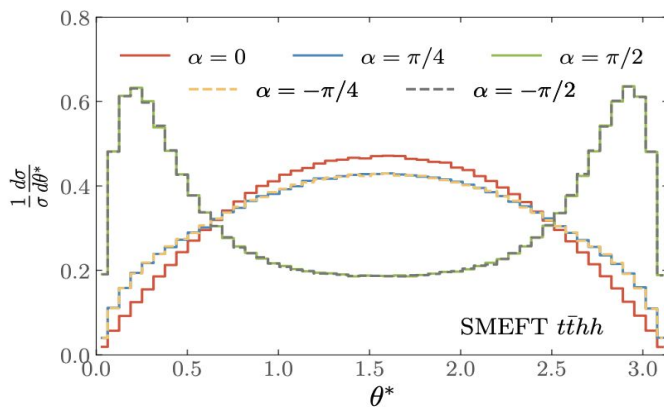
Collins-Soper angle θ^* for the tthh process in HEFT framework.

CP-odd observables

tth



tthh



Collins-Soper Angle

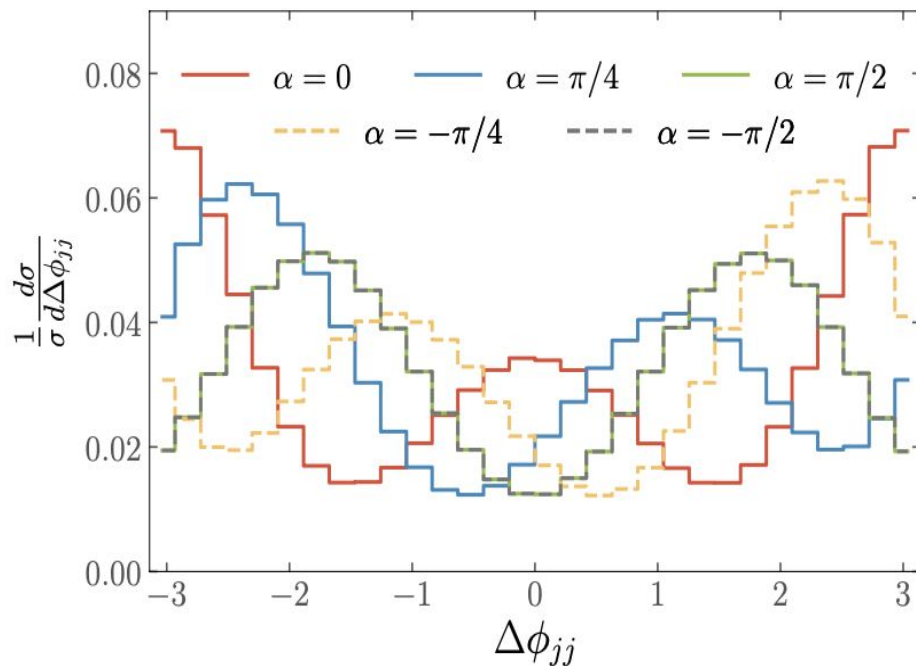
Azimuthal angle distribution

Gluon fusion $h + 2j$ production

□ Rapidity ordered jets : $\eta_{j1} > \eta_{j2}$

□ Azimuthal angular difference

$$\Delta\phi_{jj} = \phi_{j1} - \phi_{j2}$$



Distribution for the azimuthal angle difference between the two tagging jets in $h+2j$ production