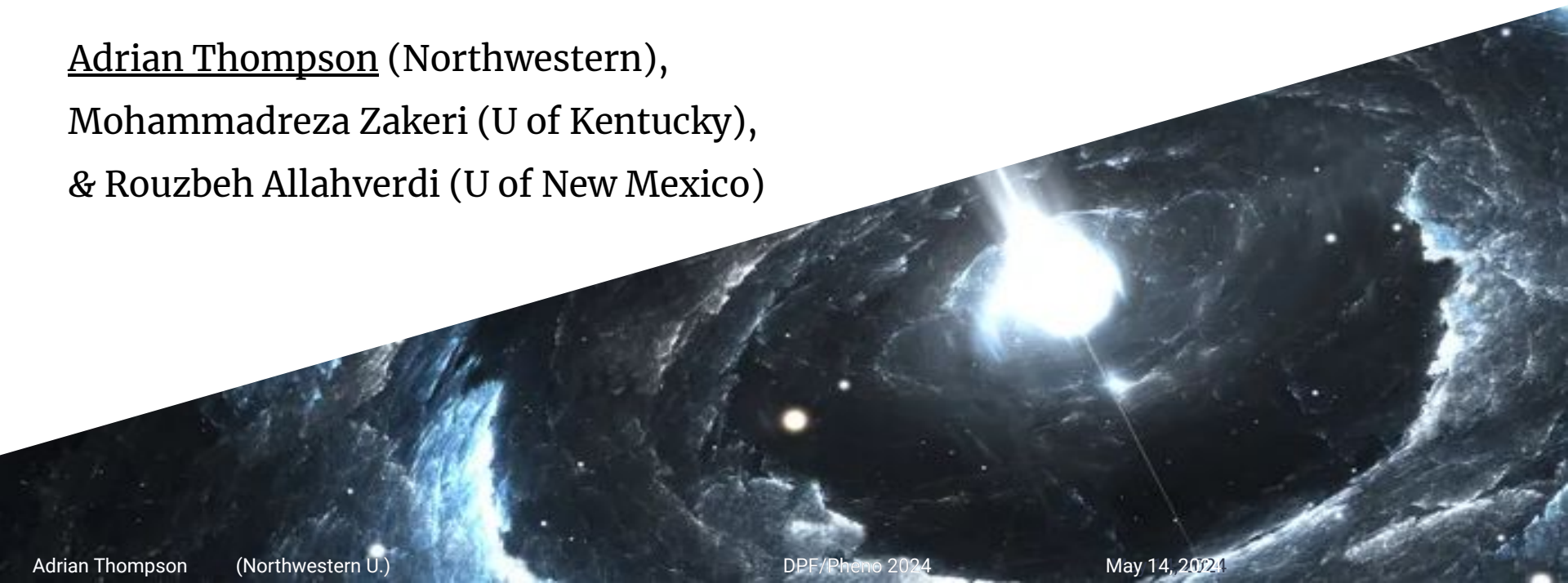


# Baryon Number Violation in Neutron Stars and the Lab

Adrian Thompson (Northwestern),  
Mohammadreza Zakeri (U of Kentucky),  
& Rouzbeh Allahverdi (U of New Mexico)



# Baryon Number Violation: Theoretical Motivation

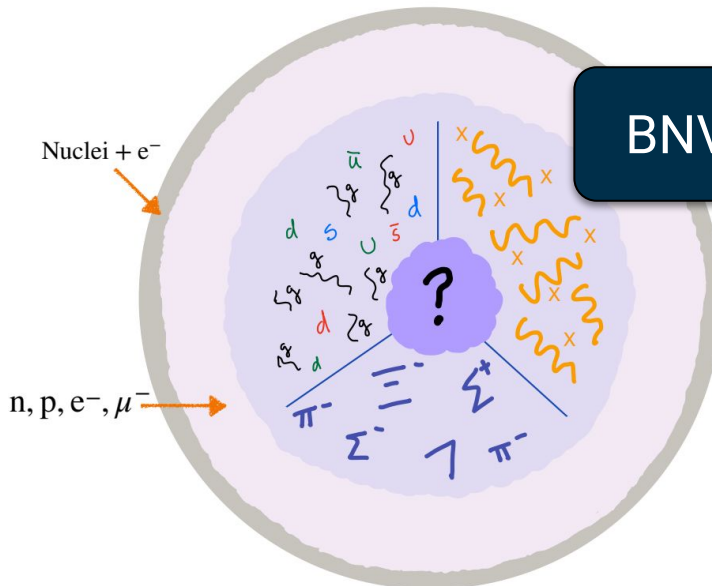
- Baryogenesis
  - Sakharov conditions
    - i. CP violation
    - ii.  $B$  violation
    - iii. Out-of-thermal-equilibrium
- Dark Matter and the Baryon-DM abundance coincidence puzzle
  - $\Omega_{\text{DM}} : \Omega_{\text{Baryon}} \approx 5 : 1$
- Neutron lifetime anomaly and neutron-anti-neutron oscillations

# Baryon number violating phenomenology below $\Lambda_{\text{QCD}}$

- Inspired by:
  - B-Mesogenesis scenarios
  - Hyperon decays to dark sector particles
  - neutron anomaly
- Typical setup: Heavy scalar(s) mediator & GeV-scale fermion(s)
- B-violation with chiral perturbation theory

Baryon  $\rightarrow \psi \gamma$  and other Rare Decays

Alonso-Álvarez, Elor, Escudero, Fornal, Grinstein, Camalich [[2111.12712](#)]  
also: Davoudiasl, Morrissey, Sigurdson, Tulin [[1106.4320](#)]



BNV in Neutron Stars

Berryman, Gardner, Zakeri [[2305.13377](#)]  
[[2311.13649](#)] [[2201.02637](#)]

# Specific Model: A Majorana fermion + color-triplet scalar

	SU(3) <sub>c</sub>	SU(2) <sub>L</sub>	U(1) <sub>Y</sub>
$X^{1,2}$	<b>3</b>	<b>1</b>	+4/3
$\psi$	<b>1</b>	<b>1</b>	0

(suppressing color indices)

$$\mathcal{L} \supset \lambda_i \left( X \bar{u}_i P_L \psi + X^* \bar{\psi} P_R u_i \right) + \lambda'_{ij} \left( X^* \bar{d}_i P_L d_j^c + X \bar{d}_j^c P_R d_i \right)$$

- If  $X^{1,2}$  have CP-violating phases, baryon asymmetry can be explained
- If  $(m_p - m_e) < m_\psi < (m_p + m_e)$   $\psi$  can be the DM
- $\lambda' = 0$  for  $i=j$
- $m_\psi \sim 1$  GeV
- $m_X \gtrsim 1$  TeV

See e.g.:

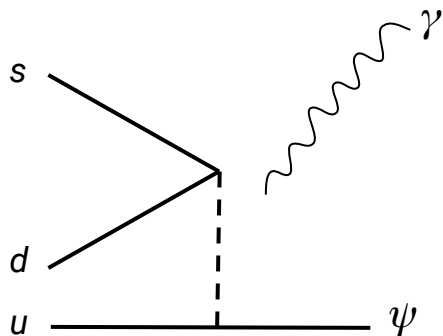
Allahverdi, Dev, Dutta [[1712.02713](#)]

Dev, Mohapatra [[1504.07196](#)]

Allahverdi, Dutta, Sinha [[1005.2804](#)]

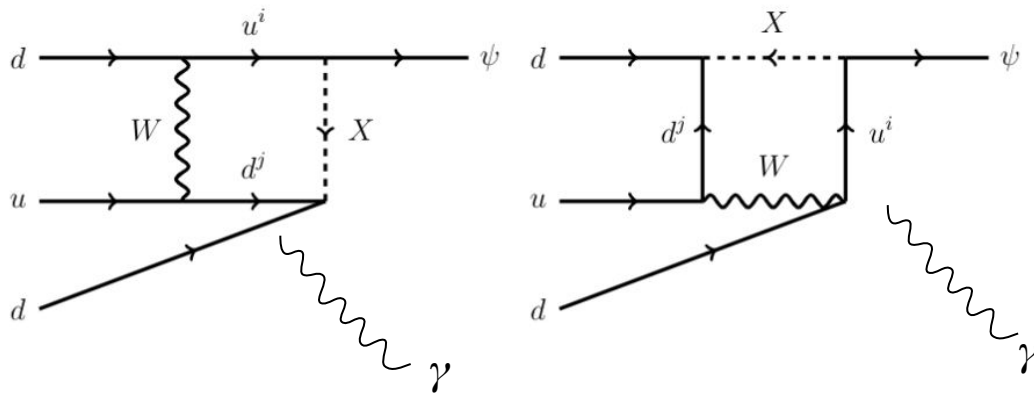
# Decays of the Baryons to $\psi$ and a Photon ( $\Delta B=1$ )

$\Lambda \rightarrow \psi \gamma$  decay at tree level



ds-u coupling or  $\lambda_1 \lambda'_{12}$

$n \rightarrow \psi \gamma$  decay at loop level



All higher-generational couplings:  $\lambda_k \lambda'_{ij}$

# Operator Matching to the ChiPT Lagrangian (*d-s-u* coupling)

New physics “spurion”

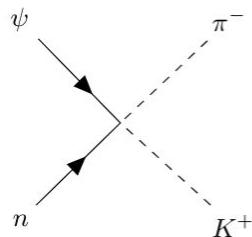
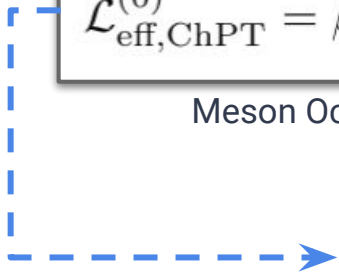
$$O_{ij} \equiv \frac{1}{2} \epsilon_{jkl} (q_k q_l) (q_i \psi) \iff \mathcal{L}_6 = \text{Tr}[\hat{C}^R O]$$



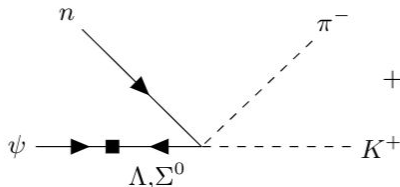
$$\mathcal{L}_{\text{eff,ChPT}}^{(0)} = \beta \text{Tr}[\hat{C}^R u^\dagger B_R \psi u]$$

Meson Octet

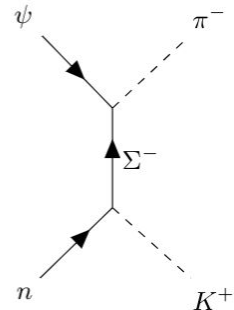
Baryon Octet



+

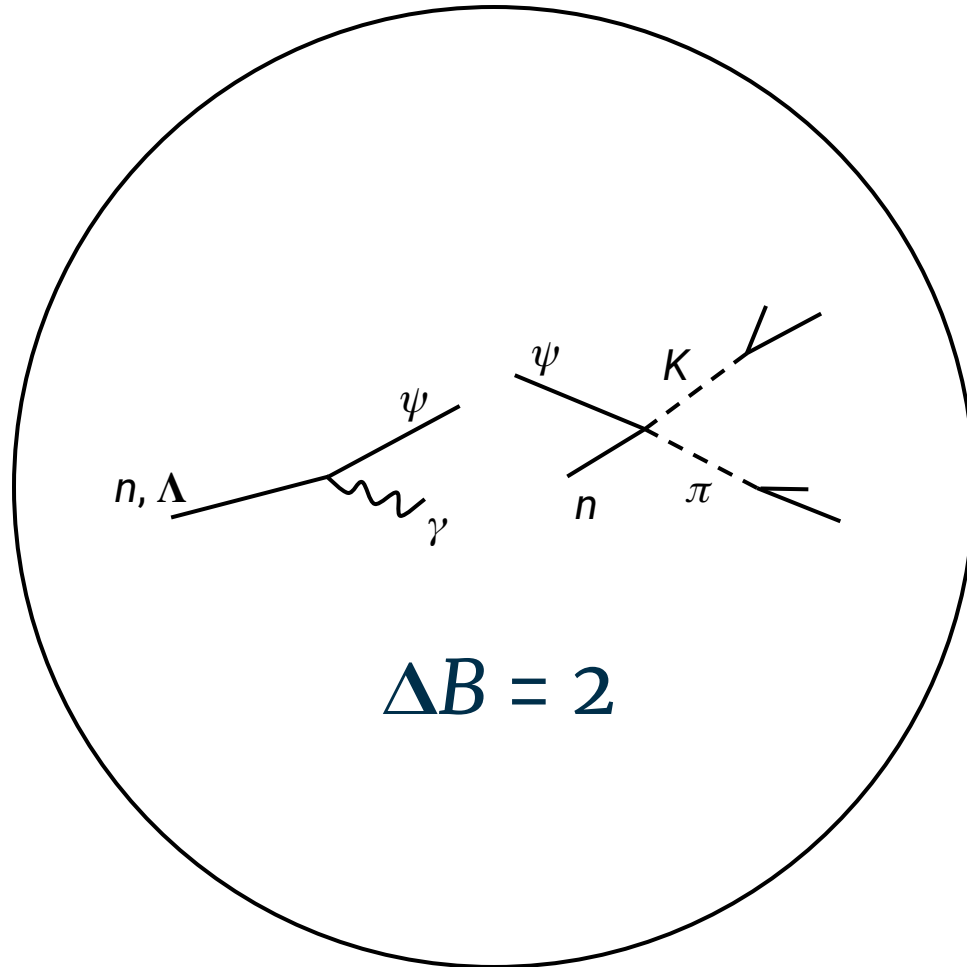


+



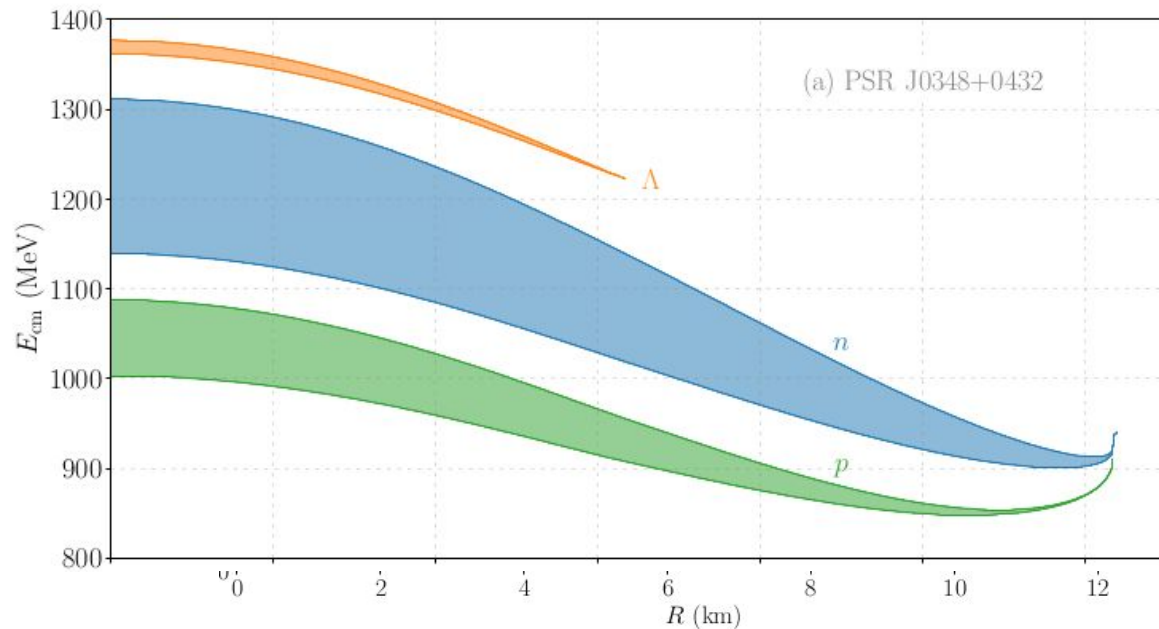
1. Match the quark-level operator to the SU(3) representation after integrating out the heavy  $X$
2. Write down the SU(3)-invariant interactions between the new physics spurion  $C^R$  and the meson octet  $u \sim e^{\phi/f}$  and baryon octet  $B$

Neutron Star



# Enhancement of the Baryon CM Energy in Dense Matter

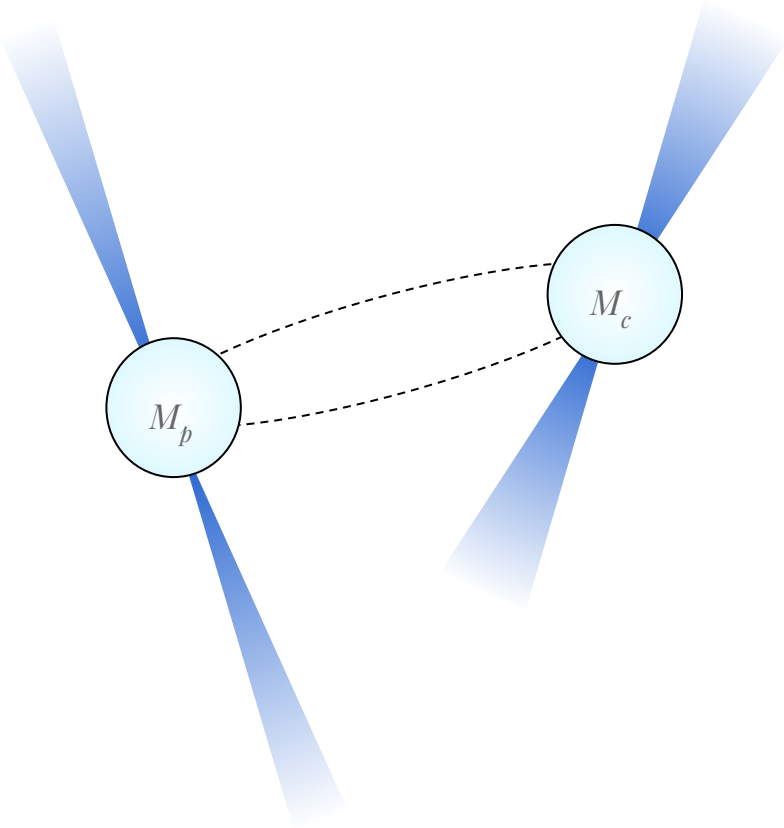
- Dense nuclear matter: baryons get a kinetic mass  $\rightarrow$  lifts the CM frame energy
- Allows us to probe decays that would otherwise be kinematically forbidden in vacuum!
  - $\rightarrow$  We can decay to  $\psi$  with masses up to  $\sim 1.5$  GeV





# Impact of $\Delta B$ processes on Binary Pulsars

Berryman, Gardner, Zakeri [\[2305.13377\]](#)  
[\[2311.13649\]](#) [\[2201.02637\]](#)



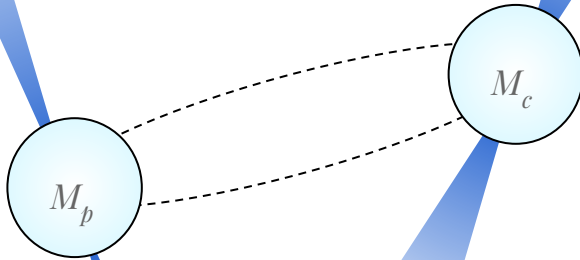
$$\frac{\dot{B}}{4\pi} = - \int e^{\nu(r)} \left[ 1 - \frac{2M(r)}{r} \right]^{-\frac{1}{2}} \Gamma_{\text{nm}}(r) n(r) r^2 dr.$$

# Impact of $\Delta B$ processes on Binary Pulsars

Berryman, Gardner, Zakeri [\[2305.13377\]](#)  
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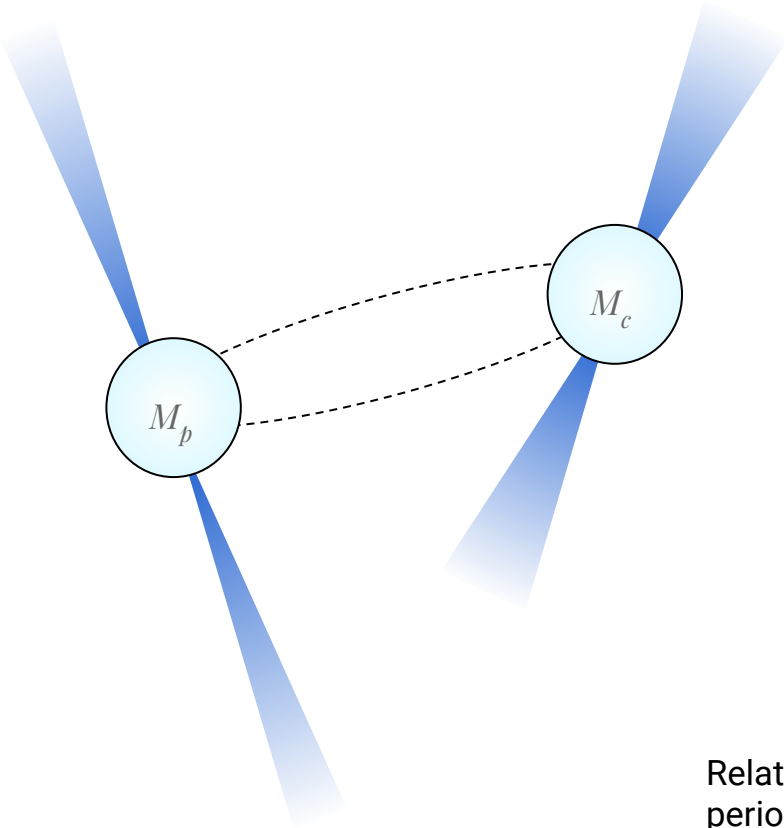
$$\frac{\dot{B}}{4\pi} = - \int e^{\nu(r)} \left[ 1 - \frac{2M(r)}{r} \right]^{-\frac{1}{2}} \Gamma_{\text{nm}}(r) n(r) r^2 dr.$$

$$\dot{M}^{\text{eff}} = \left( \partial_{\varepsilon_c} M + \left( \frac{\Omega^2}{2} \right) \partial_{\varepsilon_c} I \right) \left( \frac{\dot{B}}{\partial_{\varepsilon_c} B} \right)$$



# Impact of $\Delta B$ processes on Binary Pulsars

Berryman, Gardner, Zakeri [\[2305.13377\]](#)  
[\[2311.13649\]](#) [\[2201.02637\]](#)



$$\frac{\dot{B}}{4\pi} = - \int e^{\nu(r)} \left[ 1 - \frac{2M(r)}{r} \right]^{-\frac{1}{2}} \Gamma_{\text{nm}}(r) n(r) r^2 dr.$$

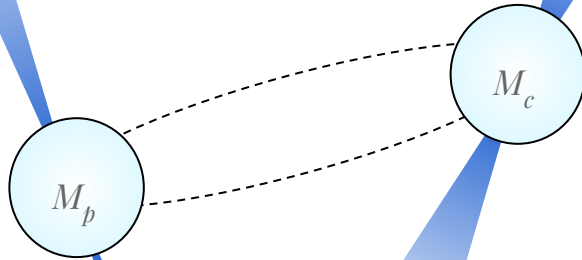
$$\dot{M}^{\text{eff}} \equiv \frac{d}{dt} \left( M + \frac{1}{2} I \Omega^2 \right) = \underbrace{b(M) \left( \frac{\dot{B}}{B} \right) M + b(I) \left( \frac{\dot{B}}{B} \right) \left( \frac{2\pi^2 I}{P_s^2} \right)}_{\text{RNV}} - \frac{4\pi^2 I \dot{P}_s}{P_s^3}$$

$$\left( \frac{\dot{P}_b}{P_b} \right)^{\text{obs}} = \underbrace{\left( \frac{\dot{P}_b}{P_b} \right)^{\text{GR}} + \left( \frac{\dot{P}_b}{P_b} \right)^{\dot{E}}}_{\text{intrinsic}} + \left( \frac{\dot{P}_b}{P_b} \right)^{\text{ext}}$$

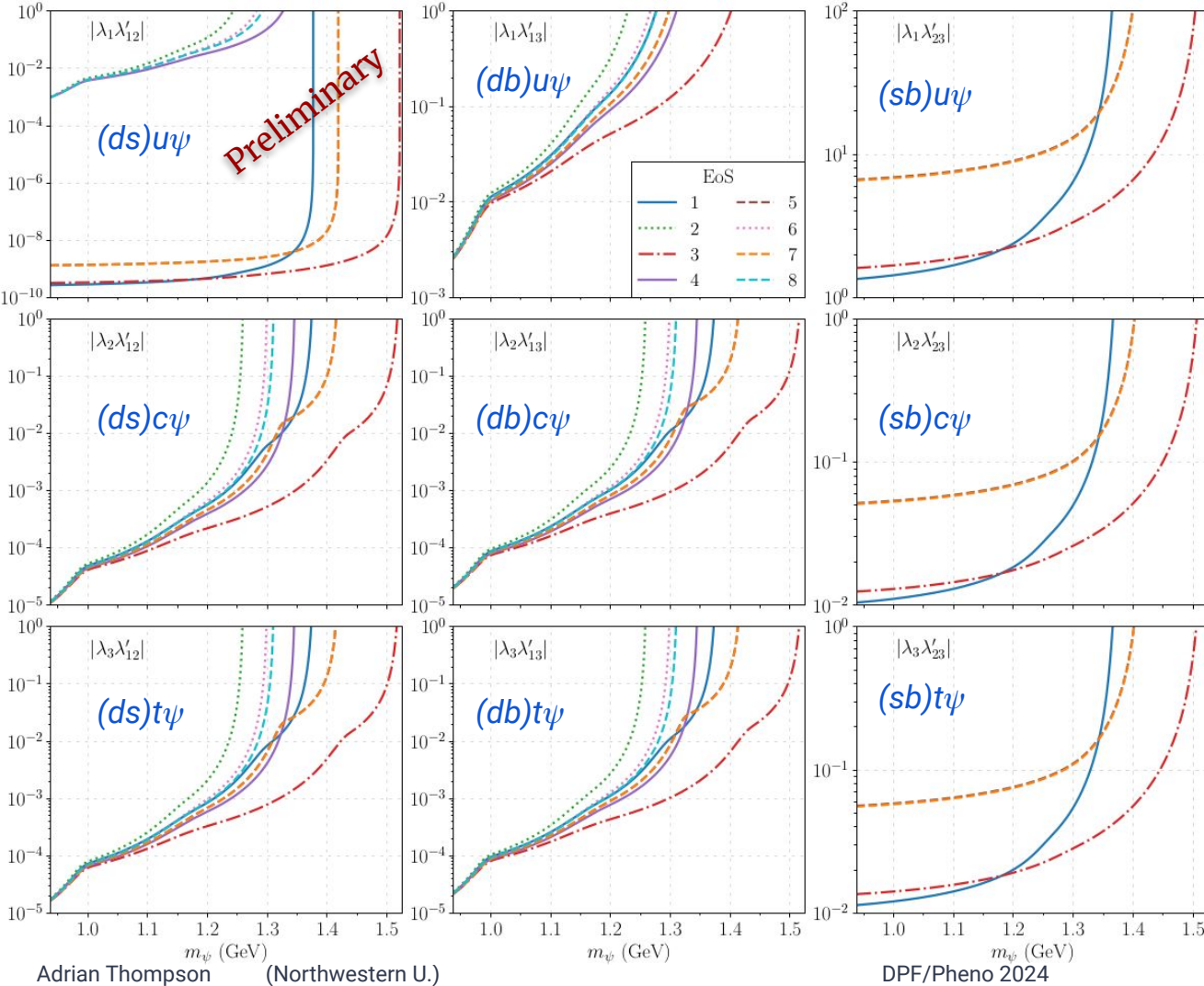
Relative rate of orbital  
period decay

BNV perturbs the energy loss

# Systems in this study



Name	J0348+0432	J1614-2230	J0737-3039A/B
$M_p (M_\odot)$	2.01(4)	1.908(16)	1.338 185(+12, -14) [A]
$M_c (M_\odot)$	0.172(3)	0.493(3)	1.248 868(+13, -11) [B]
$ \dot{B}/B _{2\sigma} (\text{yr}^{-1})$	$1.8 \times 10^{-10}$	$2.0 \times 10^{-11}$	$4.0 \times 10^{-13}$



- We looked at constraints on the coupling product

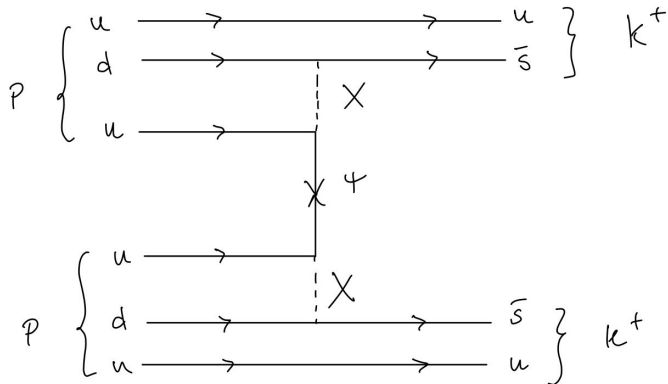
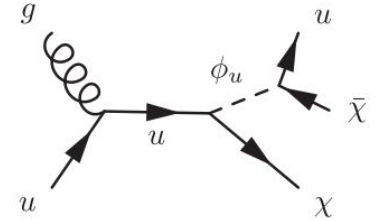
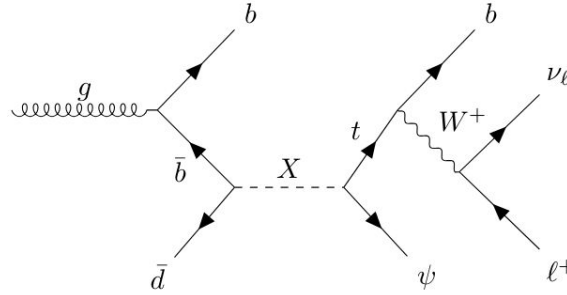
$$|\lambda_k \lambda'_{ij}|$$

- We find stringent constraints from binary pulsars down to the  $10^{-5}$  level (nucleonic Equation of State or EoS)
- Potentially as low as  $10^{-9}$  if we have hyperonic EoS!

# Laboratory Probes

- Collider searches:
  - Monotop, Monojet, and missing energy searches
- Di-nucleon decay searches:
  - Super-K: large volume detectors search for spontaneous di-proton decay

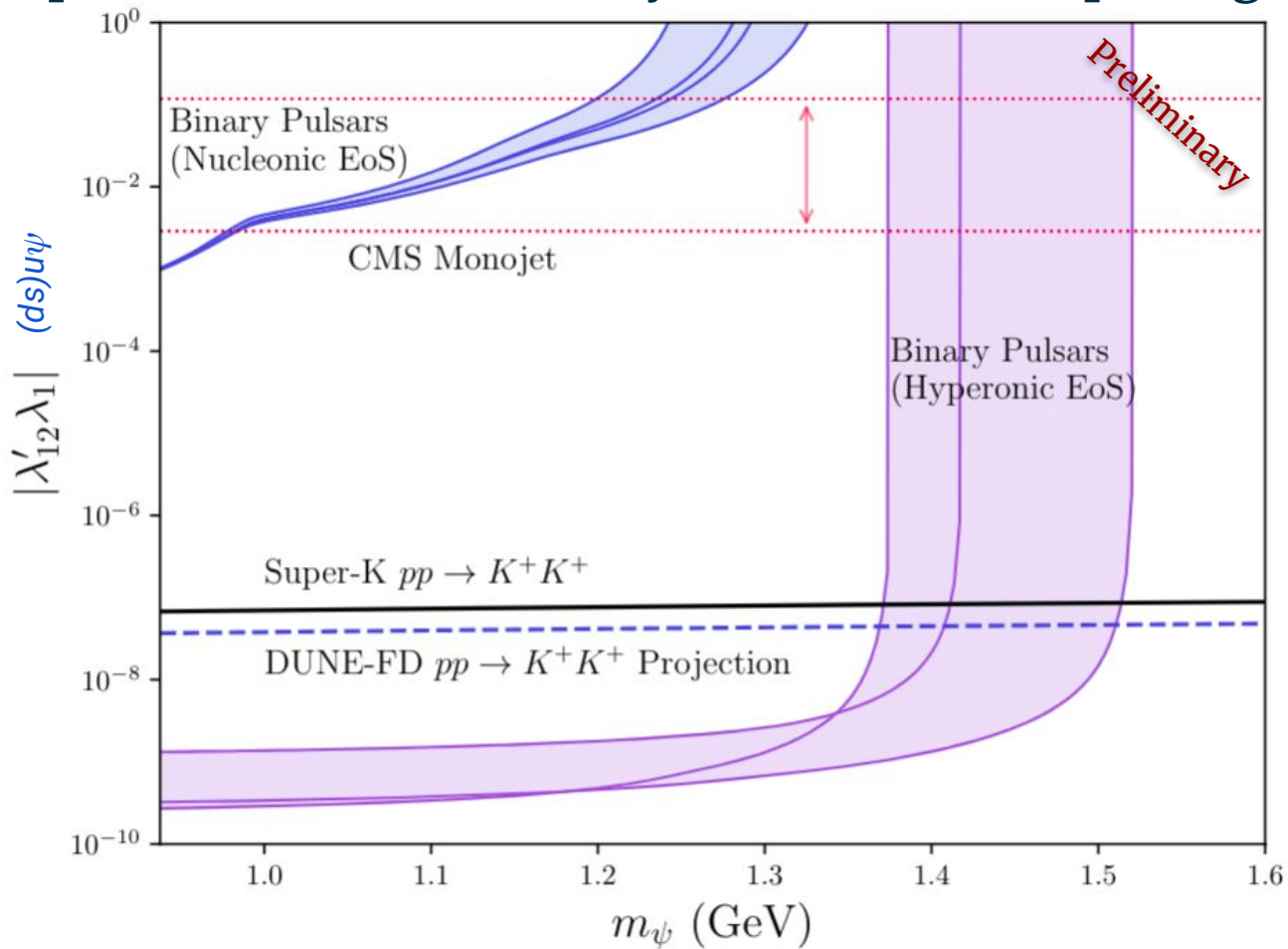
See e.g.: [\[2404.14844\]](#)



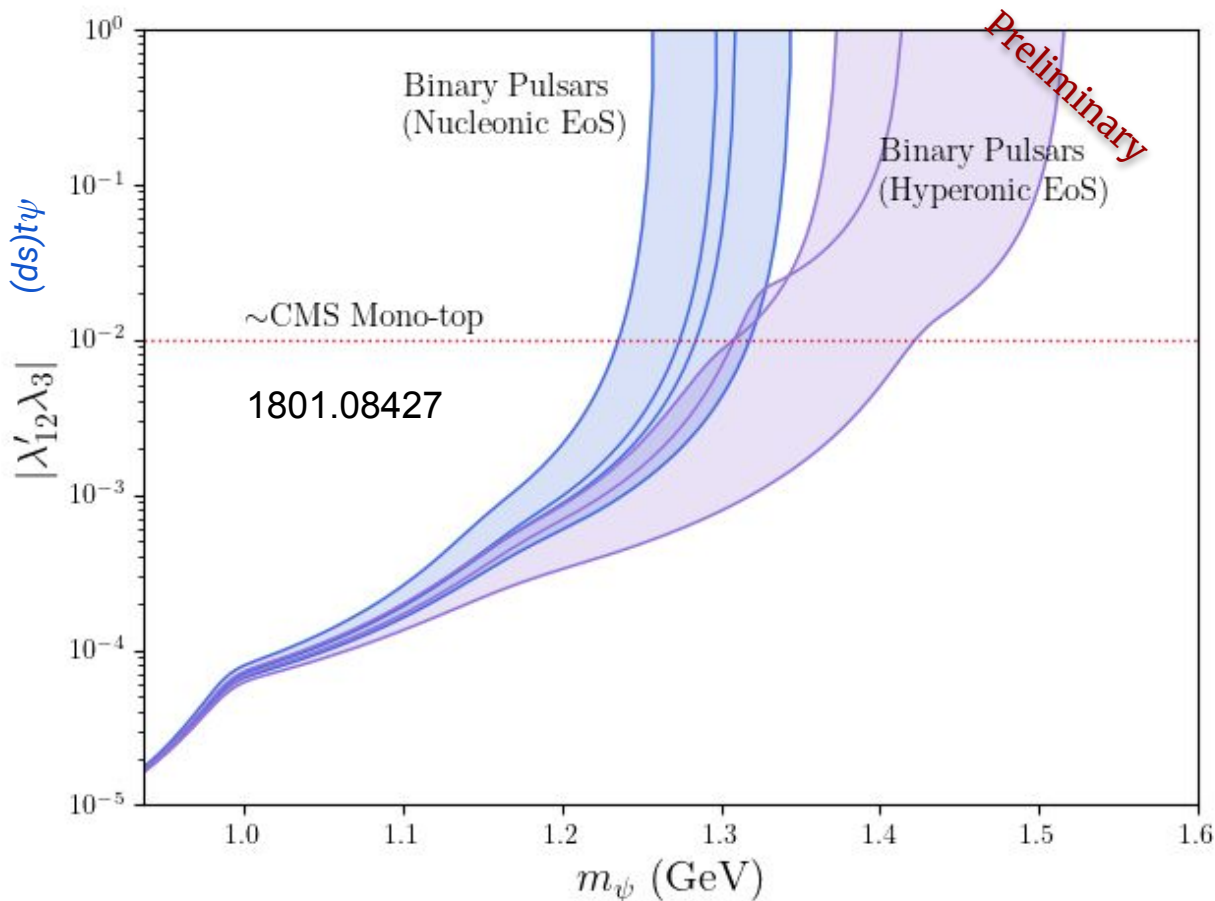
$$\tau(pp \rightarrow K^+ K^+) = \frac{8}{\pi} (\lambda_1 \lambda'_{12})^4 \frac{\Lambda_{\text{QCD}}^{10} \rho_N}{m_p^2 m_\psi^2 m_X^8}$$

Assuming this scales with atomic number as  $\sim Z$ , we can rescale the Super-K sensitivity using other nuclei such as  $^{40}\text{Ar}$

# Comparison with Laboratory Limits: lowest quark generation couplings



# Comparison with Laboratory Limits: Higher generational couplings



- Di-nucleon decays  $pp \rightarrow K^+K^+$  highly suppressed for higher generational couplings (CKM + loop suppressed)
- Binary pulsar constraints no longer benefit from pure tree-level couplings to  $\Lambda$ -baryons
- Binary pulsar set leading bounds below  $m_ψ < 1.3$  GeV  $\rightarrow$  collider searches probe higher masses



# What about dark matter laboratory searches?

$\psi$  can be the dark matter if:

$$m_p - m_e < m_\psi < m_p + m_e$$

Consider the Earth-captured ambient DM flux through a large detector:

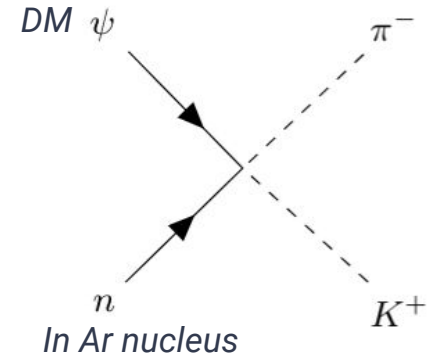
$$f_\psi(\vec{v}) = \frac{1}{N_{\text{esc}} \pi^{3/2} v_0^3} \exp\left(-\frac{(\vec{v} + \vec{v}_\oplus)^2}{v_0^2}\right) \Theta(v_{\text{esc}} - |\vec{v} + \vec{v}_\oplus|)$$

Then look for  $\psi n \rightarrow \pi^- K^+$  in the detector; a very unique final state!

E.g. DUNE Far Detector (FD):

$$|\lambda_1 \lambda'_{12}| > 2.69 \times 10^{-7} \left(\frac{m_X}{\text{TeV}}\right)^2$$

DUNE-FD sensitivity to DM, 90% CL



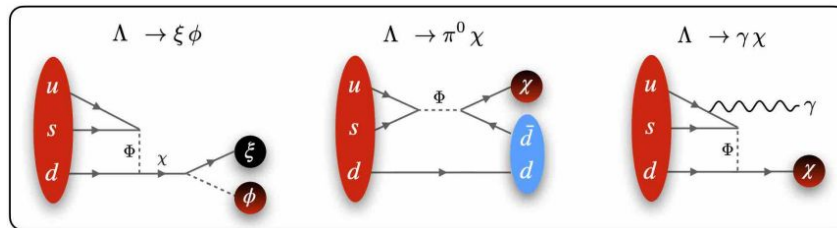
# Outlook

- Neutron stars are extremely sensitive probes of baryon number violation; sensitive to TeV scale mediators
- Whether or not NS have hyperonic EoS makes a huge difference – a good motivation to study nuclear matter and strange physics!
- Laboratory probes and colliders complimentary to these bounds for larger masses of the Majorana fermion  $> \text{GeV}$ , and for higher-generational couplings

# *Backup Deck*

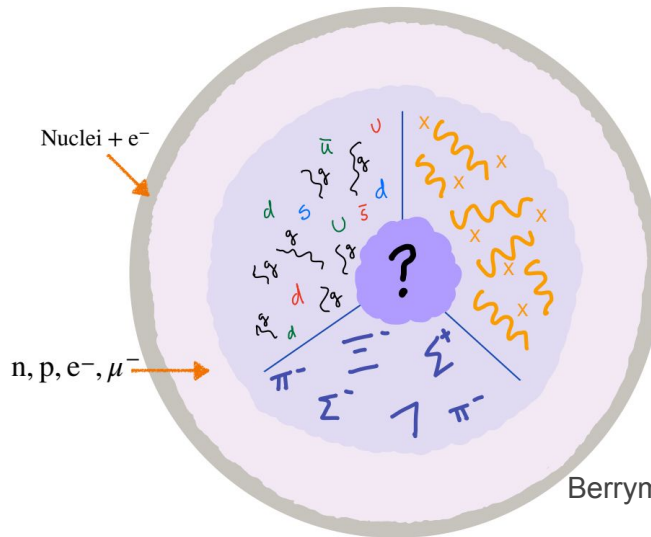
# Baryon number violating phenomenology below $\Lambda_{\text{QCD}}$

- Inspired by B-Mesogenesis scenarios, dark sector particles from Hyperon decays, and neutron anomaly
- Typical setup: Heavy scalar(s) & GeV-scale fermion(s)
- We describe the B-violating models at the meson-baryon level: Chiral perturbation theory



Alonso-Álvarez, Elor, Escudero, Fornal, Grinstein, Camalich [[2111.12712](#)]

also: Davoudiasl, Morrissey, Sigurdson, Tulin [[1106.4320](#)]



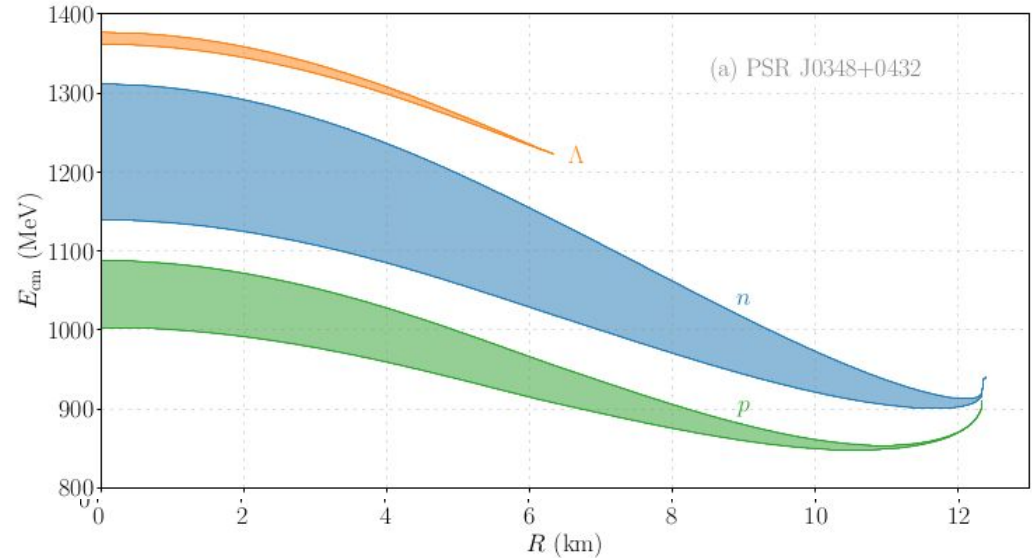
Berryman, Gardner, Zakeri [[2305.13377](#)] [[2311.13649](#)] [[2201.02637](#)]

# Enhancement of the Baryon CM Energy in Dense Matter

Vector meson self-energy  
↓

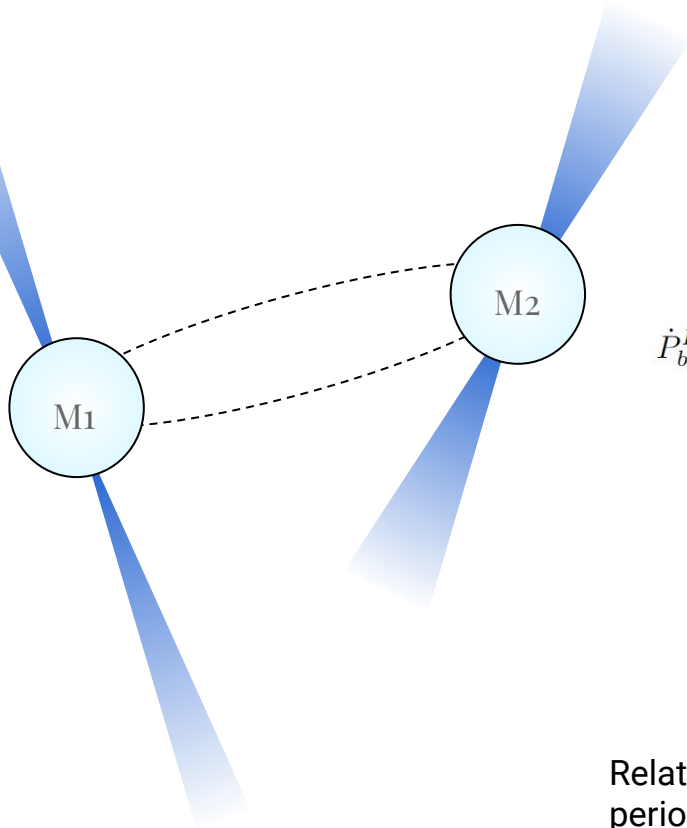
$$k^{*\mu} \equiv k^\mu - \Sigma^\mu = \left\{ E^*(k^*), \vec{k} - \vec{\Sigma} \right\}$$

- In the dense nuclear matter, baryons get a kinetic mass which lifts the available energy in the CM frame
- This allows us to probe decays that would otherwise be kinematically forbidden in vacuum!
  - → We can decay to  $\psi$  with masses up to  $\sim 1.5$  GeV



# Impact of $\Delta B$ processes on the Star's spin rate

Berryman, Gardner, Zakeri [\[2305.13377\]](#)  
[\[2311.13649\]](#) [\[2201.02637\]](#)



$$\frac{\dot{B}}{4\pi} = - \int e^{\nu(r)} \left[ 1 - \frac{2M(r)}{r} \right]^{-\frac{1}{2}} \Gamma_{\text{nm}}(r) n(r) r^2 dr.$$

$$\dot{P}_b^{\dot{E}} = -2 \left( \frac{\dot{M}_1^{\text{eff}} + \dot{M}_2^{\text{eff}}}{M_1 + M_2} \right) P_b, \quad \dot{M}^{\text{eff}} = \left( \partial_{\varepsilon_c} M + \left( \frac{\Omega^2}{2} \right) \partial_{\varepsilon_c} I \right) \left( \frac{\dot{B}}{\partial_{\varepsilon_c} B} \right)$$

$$\left( \frac{\dot{P}_b}{P_b} \right)^{\text{obs}} = \underbrace{\left( \frac{\dot{P}_b}{P_b} \right)^{\text{GR}} + \left( \frac{\dot{P}_b}{P_b} \right)^{\dot{E}}}_{\text{intrinsic}} + \left( \frac{\dot{P}_b}{P_b} \right)^{\text{ext}}$$

Relative rate of orbital  
period decay

BNV perturbs the energy loss term

# Operator Matching to the ChiPT Lagrangian ( $d$ - $s$ - $u$ coupling)

Match the quark-level operator to the SU(3) representation after integrating out the heavy  $X$ :

$$O_{ij} \equiv \frac{1}{2} \epsilon_{jkl} (q_k q_l) (q_i \psi) \iff \mathcal{L}_6 = \text{Tr}[\hat{C}^R O]$$

$$\hat{C}^R[(ds)u] = \frac{\lambda'_{12} \lambda_1}{m_X^2} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

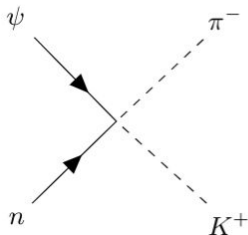
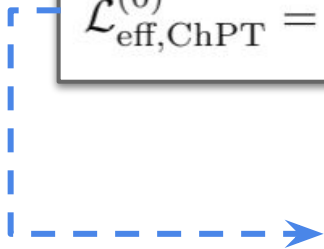
SU(3)-invariant interactions with meson/baryon octets:



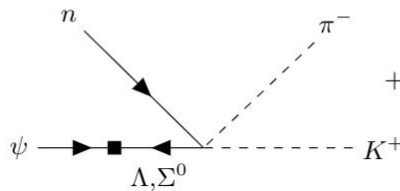
$$\Phi = \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -\frac{2\eta_8}{\sqrt{6}} \end{pmatrix}, \quad B = \begin{pmatrix} \frac{\Lambda^0}{\sqrt{6}} + \frac{\Sigma^0}{\sqrt{2}} & \Sigma^+ & p \\ \Sigma^- & \frac{\Lambda^0}{\sqrt{6}} - \frac{\Sigma^0}{\sqrt{2}} & n \\ \Xi^- & \Xi^0 & -\frac{2\Lambda^0}{\sqrt{6}} \end{pmatrix}$$

$$\mathcal{L}_{\text{eff,ChPT}}^{(0)} = \beta \text{Tr}[\hat{C}^R u^\dagger B_R \psi u]$$

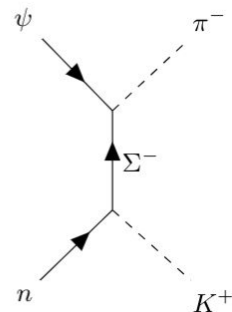
$$b_R^\dagger [-i\sigma^2] \psi_R^* = \bar{b} P_L \psi^c \quad \text{and} \quad u = e^{i\Phi/f_\pi}$$



+



+



# Expansion of the ChiPT New Physics Lagrangian: Zeroth order

$$\mathcal{L}_{\text{eff,ChPT}}^{(0)} = \beta \text{Tr}[\hat{C}^R u^\dagger B_R \psi u]$$

$$b_R^\dagger [-i\sigma^2] \psi_R^* = \bar{b} P_L \psi^c \text{ and } u = e^{i\Phi/f_\pi}$$

$$\Phi = \begin{pmatrix} \frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} & \pi^+ & K^+ \\ \pi^- & -\frac{\pi^0}{\sqrt{2}} + \frac{\eta_8}{\sqrt{6}} & K^0 \\ K^- & \bar{K}^0 & -\frac{2\eta_8}{\sqrt{6}} \end{pmatrix}, \quad B = \begin{pmatrix} \frac{\Lambda^0}{\sqrt{6}} + \frac{\Sigma^0}{\sqrt{2}} & \Sigma^+ & p \\ \Sigma^- & \frac{\Lambda^0}{\sqrt{6}} - \frac{\Sigma^0}{\sqrt{2}} & n \\ \Xi^- & \Xi^0 & -\frac{2\Lambda^0}{\sqrt{6}} \end{pmatrix}$$



$$u^\dagger \simeq 1 - i\frac{\phi}{2f_\pi} - \frac{\phi^\dagger \phi}{8f_\pi^2}$$

$$\mathcal{L}_{\text{eff,ChPT}}^{(0)} = \beta \frac{\lambda_1 \lambda'_{12}}{m_X^2} \left( \frac{1}{\sqrt{6}} \bar{\psi}^c P_R \Lambda + \frac{1}{\sqrt{2}} \bar{\psi}^c P_R \Sigma^0 + \text{h.c.} \right) + \mathcal{O}(1/f_\pi)$$



# Expansion of the ChiPT New Physics Lagrangian: First order in $1/f_\pi$

$$\mathcal{L}_{\text{eff,ChPT}}^{(0)} = \beta \text{Tr}[\hat{C}^R u^\dagger B_R \psi u]$$

$$u^\dagger \simeq 1 - i \frac{\phi}{2f_\pi} - \frac{\phi^\dagger \phi}{8f_\pi^2}$$

$$\mathcal{L}_{\text{eff,ChPT}}^{(0)} \supset \frac{\beta}{f_\pi} \frac{\lambda_1 \lambda'_{12}}{m_X^2} \left( \frac{iK^- \bar{\psi}^c P_R p}{\sqrt{2}} - \frac{iK^+ \bar{\psi}^c P_R \Xi^-}{\sqrt{2}} + \frac{i\pi^- \bar{\psi}^c P_R \Sigma^+}{\sqrt{2}} - \frac{i\pi^+ \bar{\psi}^c P_R \Sigma^-}{\sqrt{2}} + \text{h.c.} \right)$$

# Expansion of the ChiPT New Physics Lagrangian: Second order in $1/f_\pi^2$

$$\mathcal{L}_{\text{eff,ChPT}}^{(0)} = \beta \text{Tr}[\hat{C}^R u^\dagger B_R \psi u] \quad u^\dagger \simeq 1 - i \frac{\phi}{2f_\pi} - \frac{\phi^\dagger \phi}{8f_\pi^2}$$

$$\begin{aligned} \mathcal{L}_{\text{eff,ChPT}}^{(0)} \supset \frac{\beta}{f_\pi^2} \frac{\lambda_1 \lambda'_{12}}{m_X^2} & \left( -\sqrt{\frac{3}{8}} K^- K^+ \bar{\psi}^c P_R \Lambda - \frac{K^- K^+ \bar{\psi}^c P_R \Sigma^0}{2\sqrt{2}} + \frac{\pi^+ K^- \bar{\psi}^c P_R n}{2} + \sqrt{\frac{3}{2}} \frac{\eta^8 K^- \bar{\psi}^c P_R p}{4} + \frac{\pi^0 K^- \bar{\psi}^c P_R p}{4\sqrt{2}} \right. \\ & + \sqrt{\frac{3}{2}} \frac{\eta^8 K^+ \bar{\psi}^c P_R \Xi^-}{4} + \frac{\pi^- K^+ \bar{\psi}^c P_R \Xi^0}{2} + \frac{\pi^0 K^+ \bar{\psi}^c P_R \Xi^-}{4\sqrt{2}} - \frac{K^0 \pi^+ \bar{\psi}^c P_R \Xi^-}{4F^2} \\ & + \frac{\pi^0 \pi^- \bar{\psi}^c P_R \Sigma^+}{2\sqrt{2}} + \frac{\pi^0 \pi^+ \bar{\psi}^c P_R \Sigma^-}{2\sqrt{2}} - \frac{K^+ \bar{K}^0 \bar{\psi}^c P_R \Sigma^-}{4} - \frac{\pi^- \bar{K}^0 \bar{\psi}^c P_R p}{4} \\ & \left. - \frac{K^0 K^- \bar{\psi}^c P_R \Sigma^+}{4} - \frac{1}{\sqrt{2}} \pi^- \pi^+ \bar{\psi}^c P_R \Sigma^0 + \text{h.c.} \right) + \mathcal{O}(1/f_\pi^3) \end{aligned}$$

# Neutron Star Hyperonic EoS

