

# Cosmological Parameter Forecasts for a CMB-HD Survey

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University

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**Cosmological Parameter Forecasts for a CMB-HD Survey**

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# Outline

1. Introduction
2. Forecasting Methods and Data
3. Results
4. Summary

The background of the slide is a Cosmic Microwave Background (CMB) fluctuation map. It shows a complex, grainy pattern of colors representing temperature variations in the early universe. The colors range from dark blue (cooler regions) to bright yellow and orange (warmer regions). The pattern is highly irregular and non-uniform, with many small-scale fluctuations and larger-scale structures.

# Introduction

# Timeline of CMB Observations

## Past surveys



## Stage 2

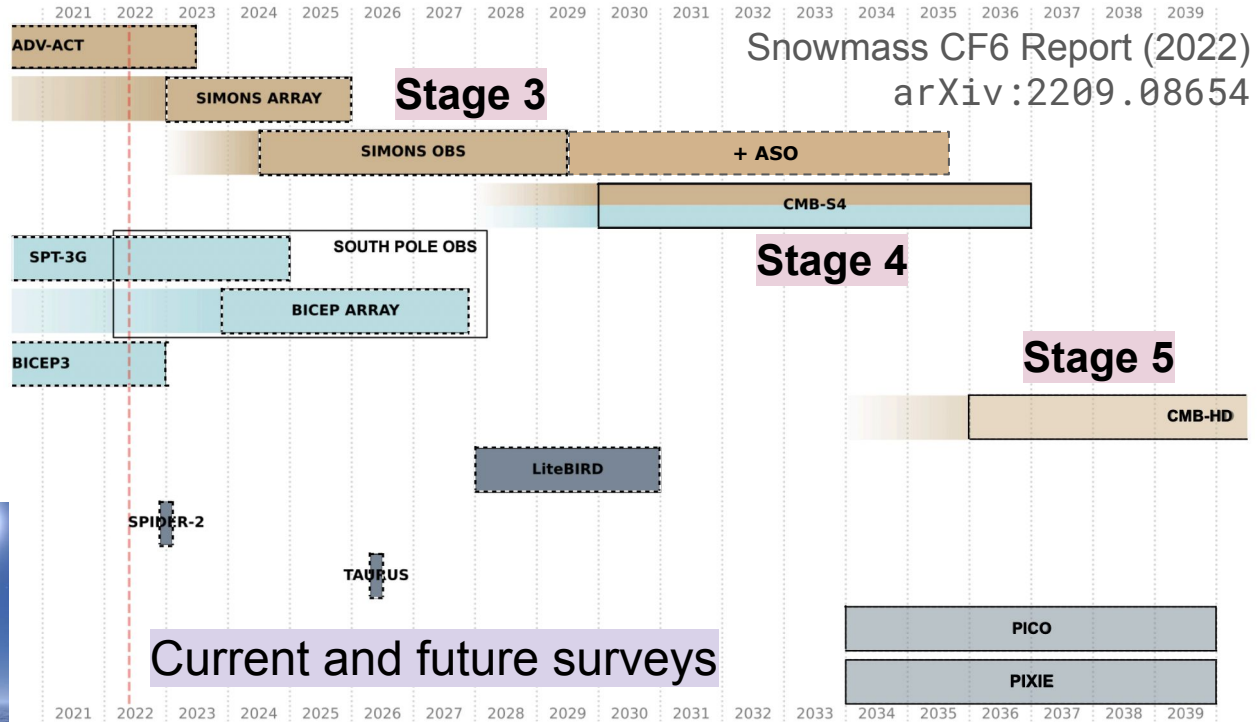
**ACTPol**

**SPTPol**



Mark Devlin

Daniel Luong-Van



**Figure 6-5.** Timeline of current and future ground-based CMB experiments. For context, the timeline also includes a few sub-orbital and satellite experiments in grey. Dashed boxes indicate fully-funded facilities. The fade-in regions indicate commissioning periods, while the boxes indicate full survey observations.

# Stage-5 CMB: CMB-HD

CMB-HD is a proposed low-noise, high-resolution millimeter-wave survey over half the sky.

- 6 times higher resolution & 3 times lower noise than CMB-S4
- Will measure angular scales  $30 < \ell < 20,000$
- 7 frequencies from 30 to 350 GHz
- Will be located in the Atacama desert in Chile

Forecasts will assume 90 & 150 GHz data over 60% of the sky, plus delensing, baryonic feedback, and DESI BAO.

Frequency (GHz)	30	40	90	150	220	280	350
Resolution (arcmin)	1.25	0.94	0.42	0.25	0.17	0.13	0.11
White noise level ( $\mu\text{K}\cdot\text{arcmin}$ ) <sup>a</sup>	6.5	3.4	0.7	0.8	2.0	2.7	100.0

<sup>a</sup> Sensitivity is for temperature maps. For polarization maps, the noise is  $\sqrt{2}$  higher.

(Snowmass 2021 CMB-HD White Paper; [arXiv:2203.05728](https://arxiv.org/abs/2203.05728))



# CMB Anisotropies

Maps

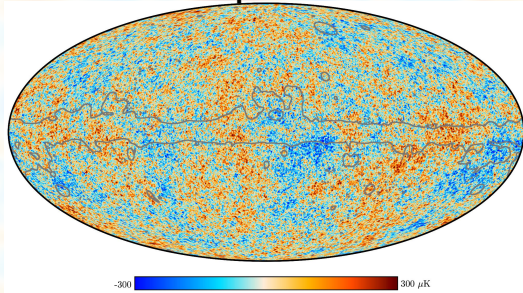


Power spectra

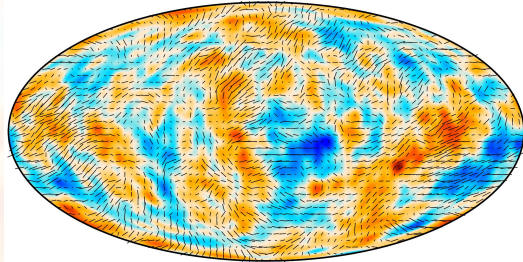


Parameters

Temperature



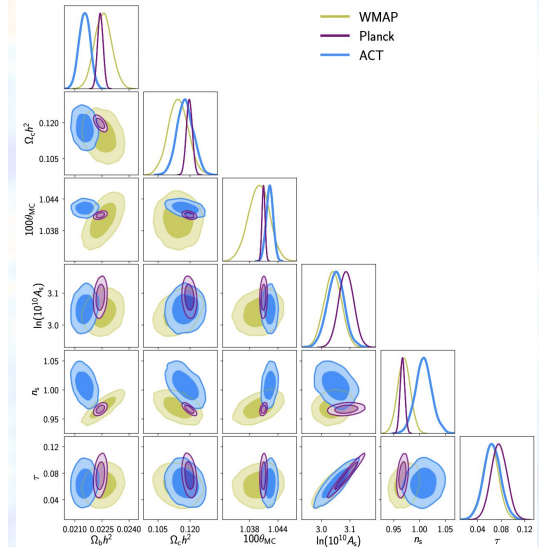
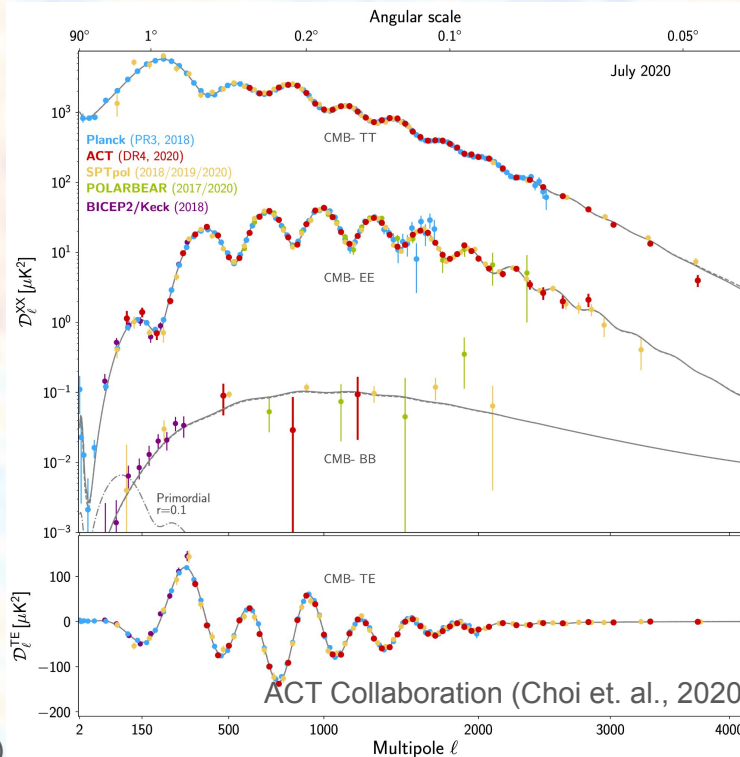
-300 300  $\mu\text{K}$



1 0.41  $\mu\text{K}$  -160 160  $\mu\text{K}$

Polarization

ESA and the Planck Collaboration (2018)

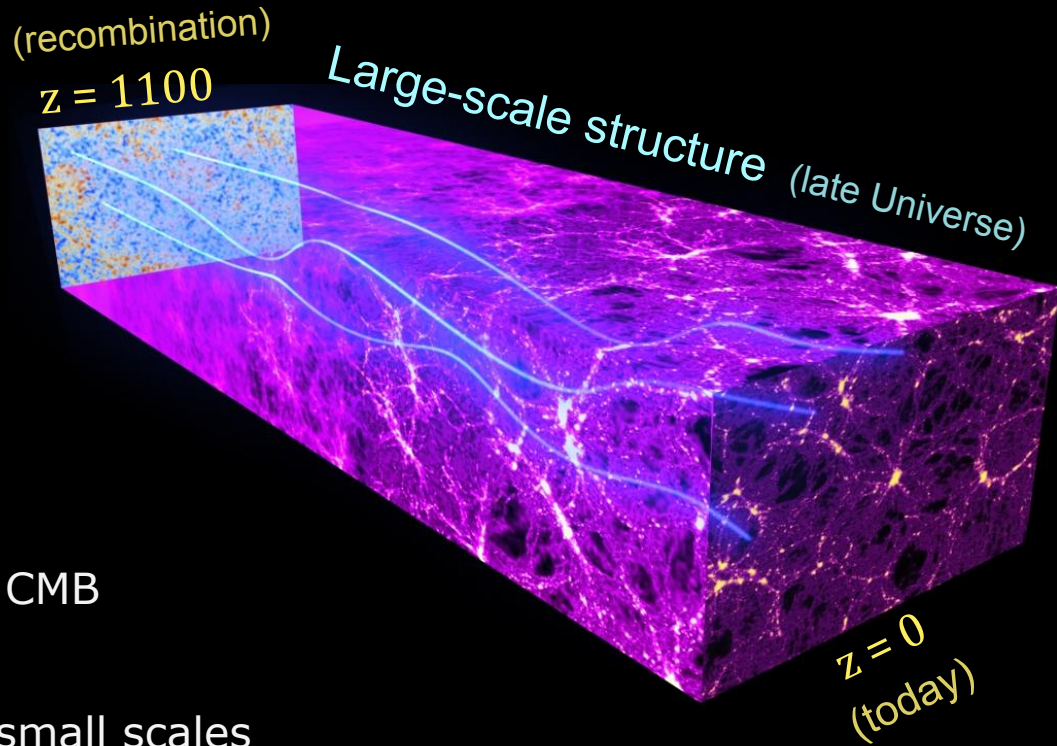


ACT Collaboration (Aiola et. al., 2020)

# CMB Lensing

Probes the matter distribution using the primary CMB as the backlight, without relying on baryonic tracers.

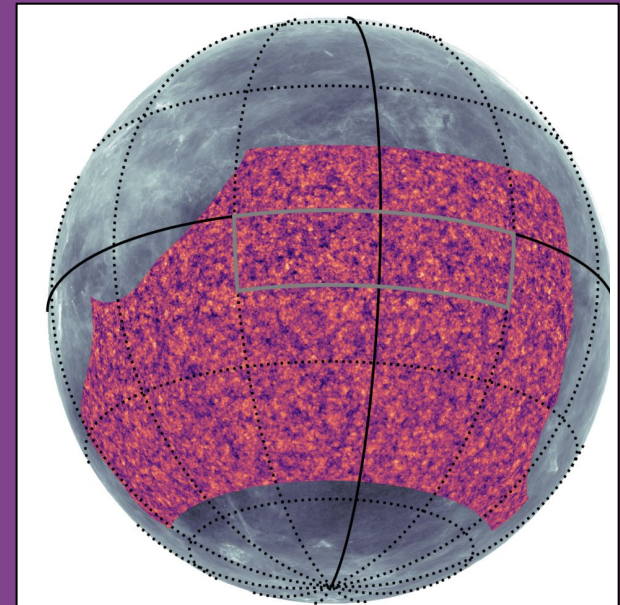
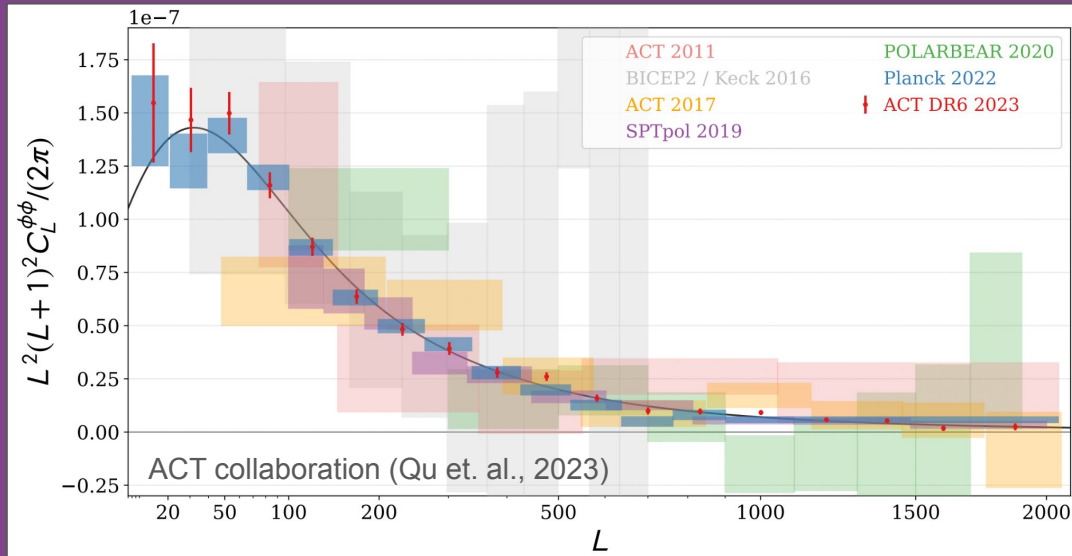
- Couples modes of the primary CMB
- Smooths the acoustic peaks
- Transfers power from large to small scales
- Converts E-mode polarization into B-modes



# CMB Lensing Reconstruction

Use the lensed CMB to reconstruct a map of the gravitational lensing potential

- Measure CMB lensing power spectrum
- Delens the CMB



ACT DR6 CMB lensing mass map

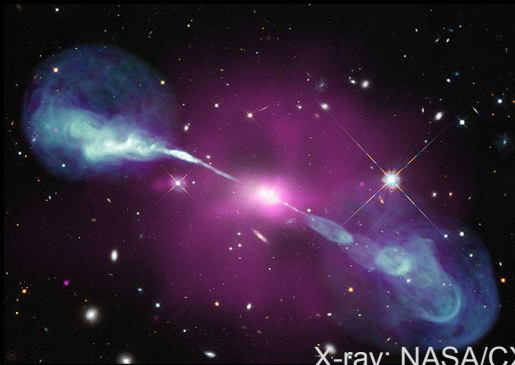
ACT collaboration (Madhavacheril et. al., 2023)



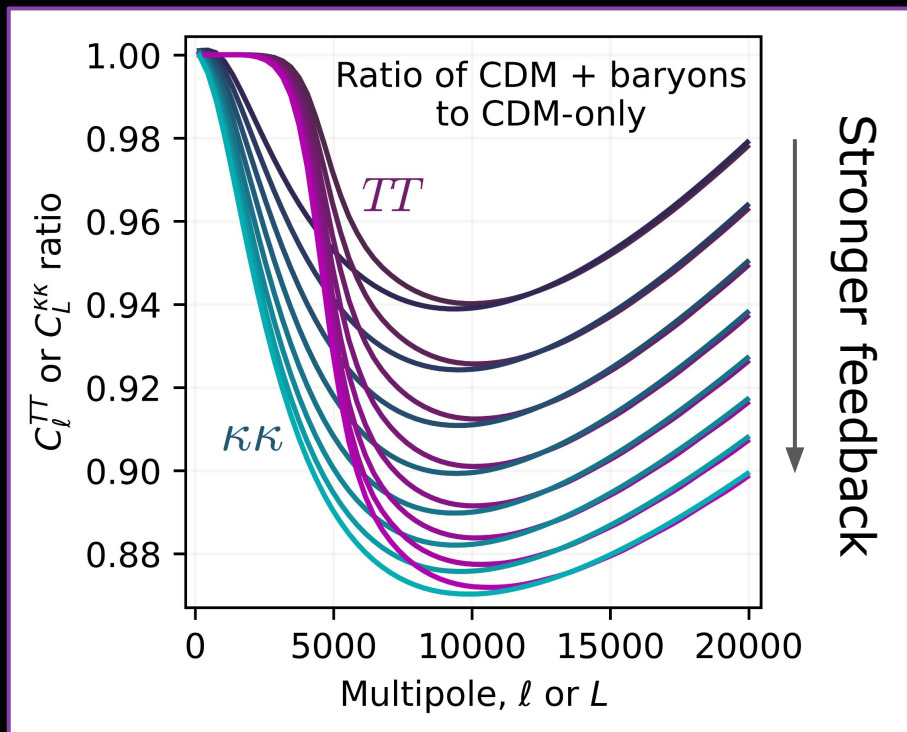
# Baryonic Feedback

Baryonic feedback processes change the matter distribution on small scales

- Can be probed by small-scale CMB lensing



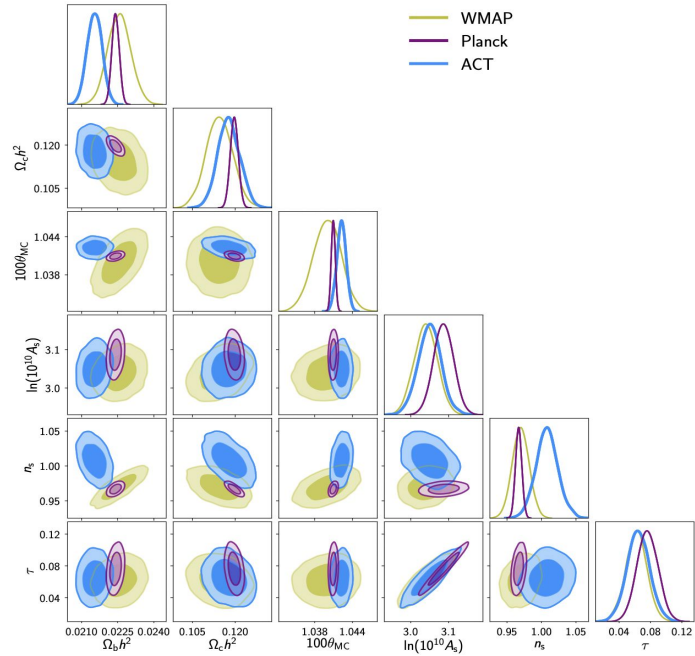
X-ray: NASA/CXC/SAO  
visual: NASA/STScI  
radio: NSF/NRAO/VLA





# Forecasting Methods and Data

# Forecasting Methods



ACT Collaboration (Aiola et. al., 2020)

8-parameter model:  $\Lambda$ CDM +  $N_{\text{eff}} + \sum m_\nu$

+ prior  $\sigma(\tau) = 0.007$  from *Planck* (2018)

Data from CMB-HD + DESI BAO

(A. Aghamousa et. al., 2016)

**Fisher matrix**: baseline method

- Quick, but assumes Gaussian parameter posteriors

**Markov chain Monte Carlo (MCMC)**:

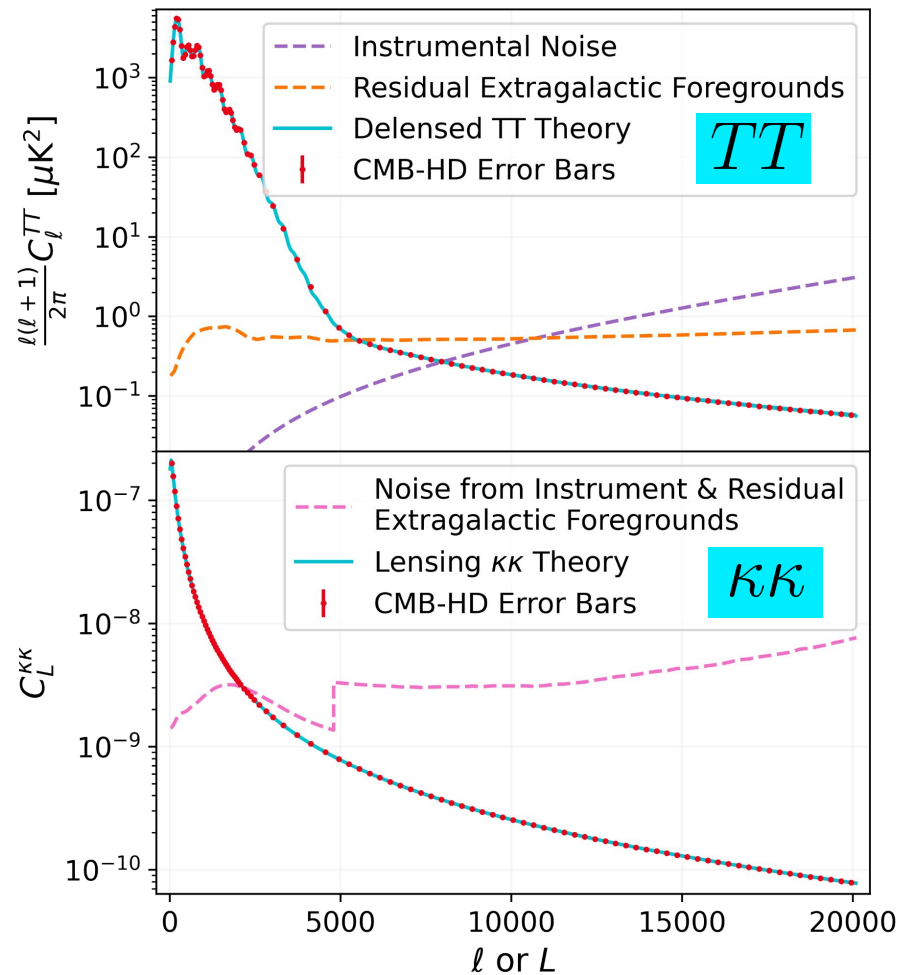
used to check Fisher

- Slower, but can recover non-Gaussian parameter posteriors

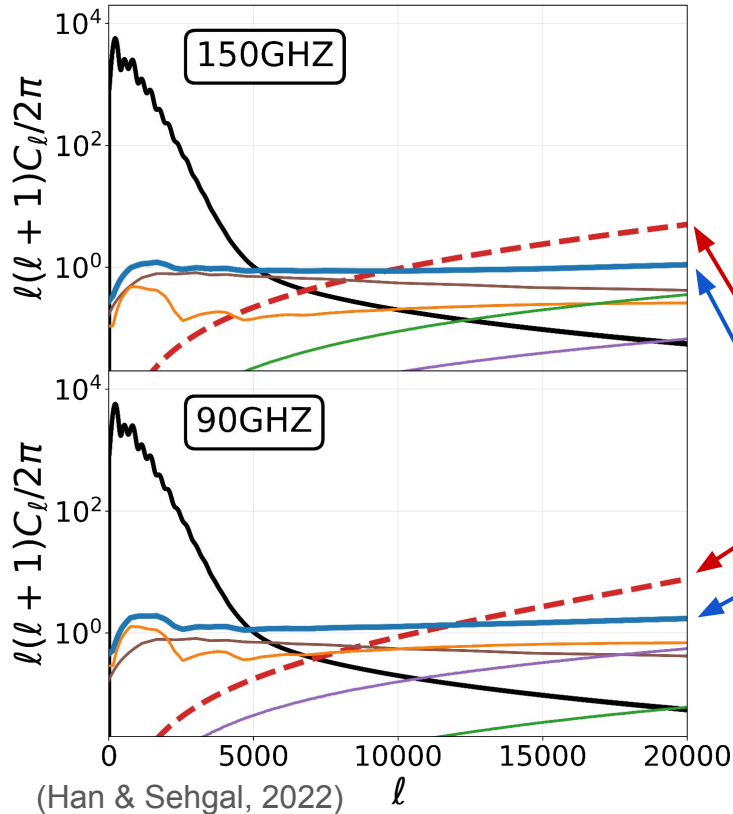
# CMB-HD Data: Power Spectra

Lensed or delensed CMB  $TT$ ,  $TE$ ,  $EE$ ,  $BB$  power spectra + CMB lensing  $\kappa\kappa$  power spectrum

- Multipoles  $\ell \in [1000, 20000]$ 
  - (Multipoles  $\ell \in [30, 1000]$  from ASO)
- Combined noise + foregrounds from 90 and 150 GHz channels



# Instrumental Noise and Residual Extragalactic Foregrounds



On small scales, the CMB and lensing signals are contaminated by extragalactic foreground emission.

CMB noise at 90 and 150 GHz includes:

- $TT, TE, EE, BB$ : instrumental noise
- $TT$ : residual extragalactic foregrounds

A Cosmic Microwave Background (CMB) fluctuation map showing temperature variations across the sky. The map is a complex, irregular pattern of colors ranging from deep blue (cooler) to bright yellow and orange (warmer). The fluctuations are distributed across the entire field of view, with some larger-scale structures and many smaller-scale variations.

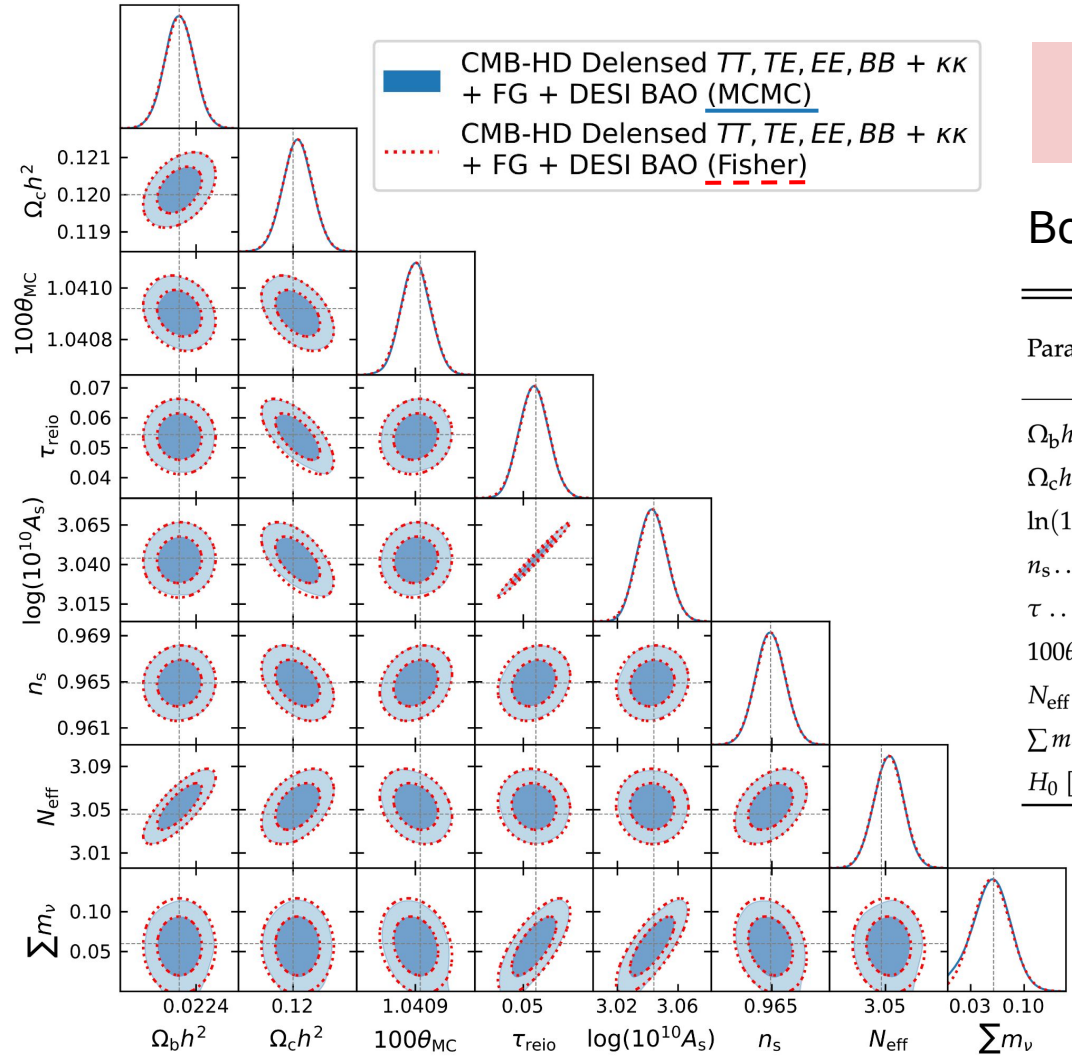
# Results

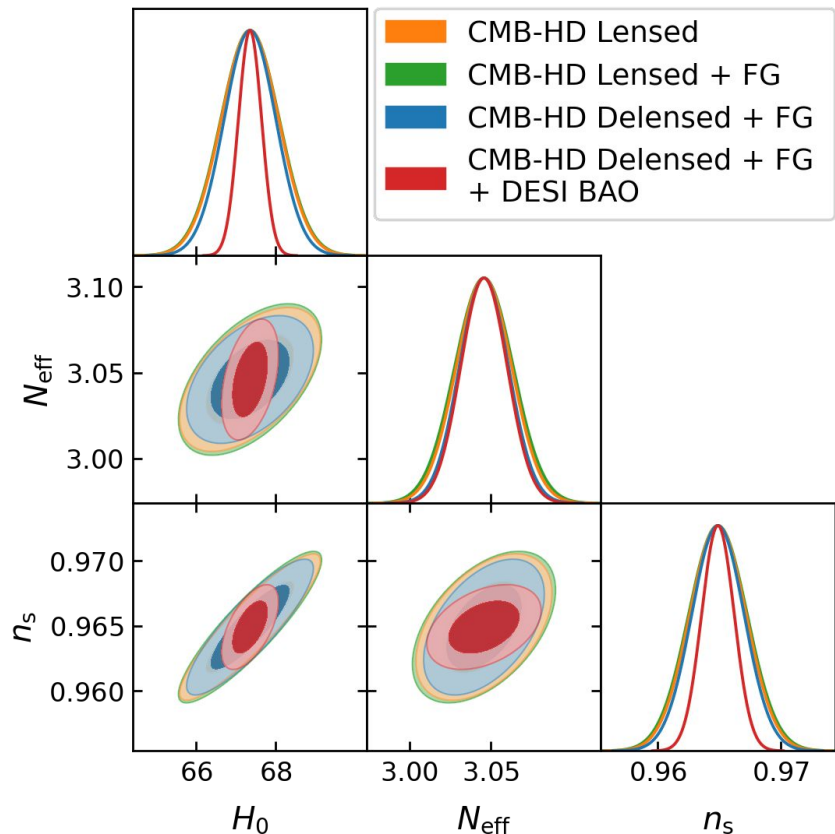
# Fisher vs. MCMC

Both methods give consistent results:

Parameter	Fiducial	MCMC 1 $\sigma$ error	Fisher 1 $\sigma$ error	Fisher / MCMC
$\Omega_b h^2$ .....	0.022370	0.0000258	0.0000263	1.02
$\Omega_c h^2$ .....	0.12000	0.000410	0.000414	1.01
$\ln(10^{10} A_s)$ .....	3.044	0.00953	0.00974	1.02
$n_s$ .....	0.9649	0.00133	0.00134	1.01
$\tau$ .....	0.0544	0.00505	0.00515	1.02
$100\theta_{MC}$ .....	1.040920	0.0000583	0.0000598	1.03
$N_{eff}$ .....	3.046	0.0139	0.0143	1.03
$\sum m_\nu$ [eV] .....	0.060	0.0243	0.0244	1.00
$H_0$ [km s $^{-1}$ Mpc $^{-1}$ ]	67.36	0.284	0.293	1.03

Ratio of parameter error bars from Fisher vs. MCMC





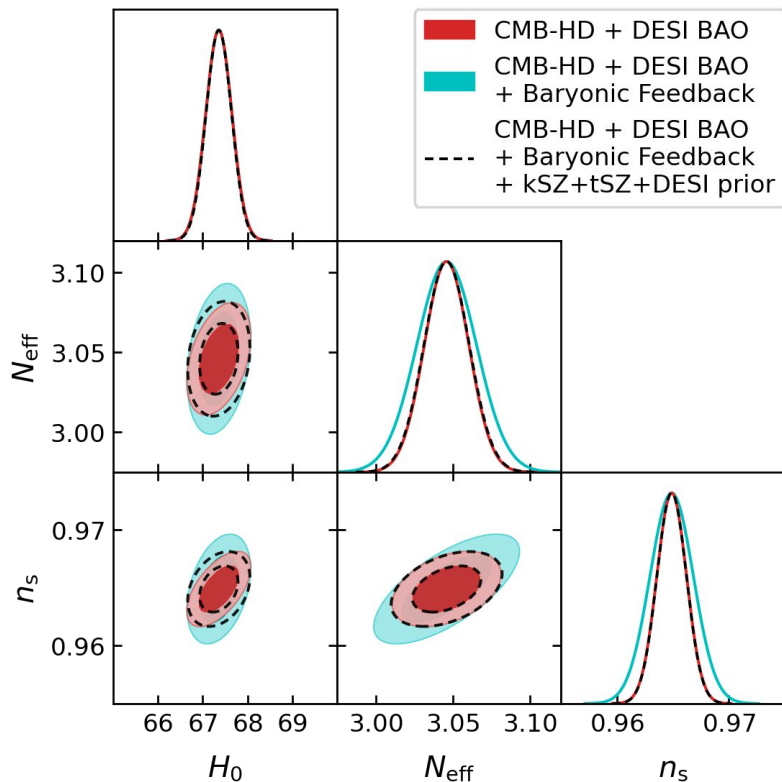
## Fisher Forecasts

- **Residual extragalactic foregrounds**: slight increase in parameter errors
- **Delensing**: reduces parameter errors
- **BAO**: reduces parameter degeneracies



Baryonic feedback strength characterized by parameter

$\log_{10}(T_{\text{AGN}}/\text{K})$  (Mead et. al., 2020)



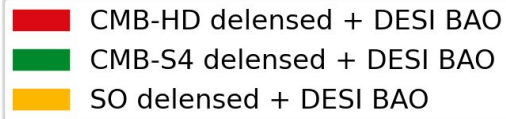
# Baryonic feedback

Assume CMB-HD SZ x CMB lensing can constrain  $\log_{10}(T_{\text{AGN}}/\text{K})$  to 0.06% (extrapolation from points below)

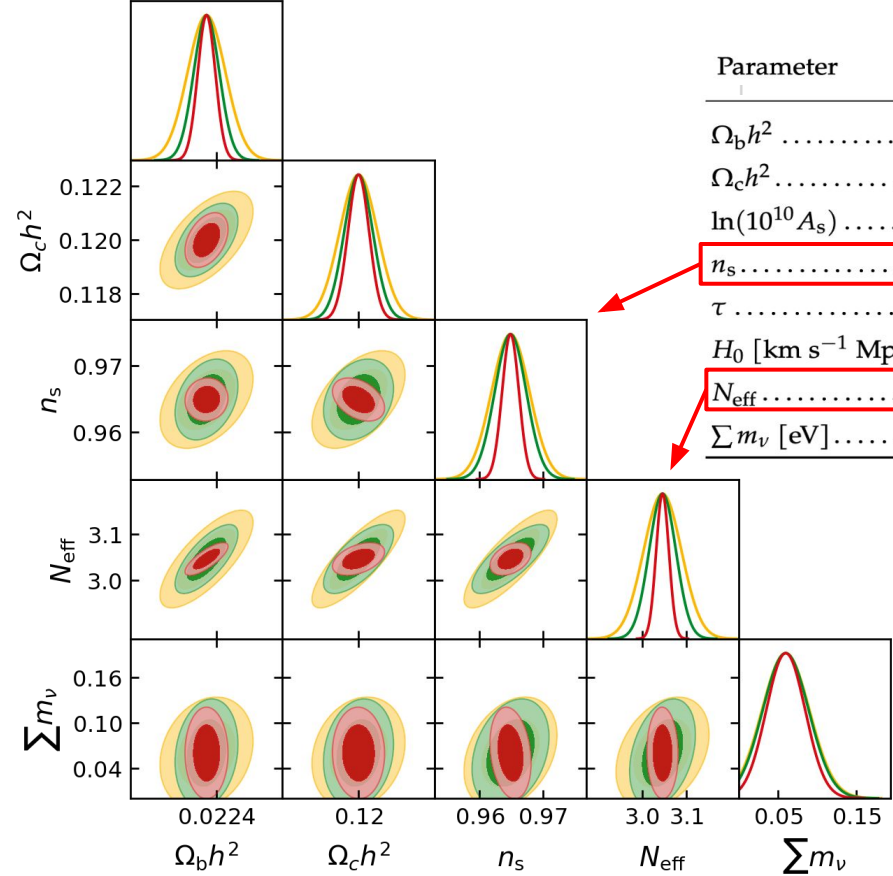
- 6% constraint from KiDS lensing x ACT+Planck tSZ (Tröster et. al., 2022)
- CMB-HD will have 25 times sky area of KiDS, at least an order of magnitude better lensing S/N, and 20 times deeper sensitivity than ACT+Planck

Marginalizing over the feedback model, including the SZ prior, does not change parameter errors

# Parameter Results



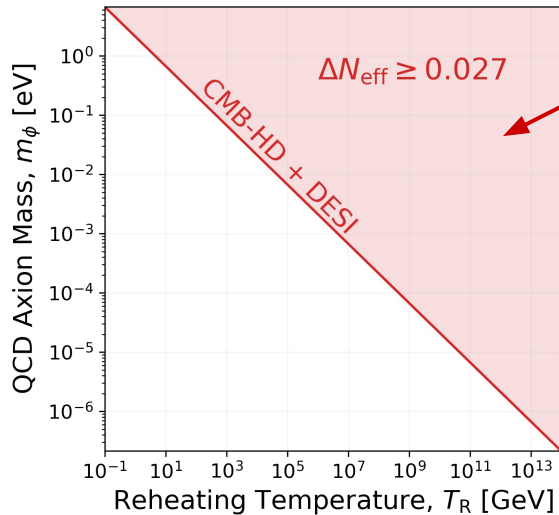
Parameter	Fiducial	1 $\sigma$ Error		Ratio of 1 $\sigma$ Errors	
		CMB-HD	CMB-HD / SO	CMB-HD / CMB-S4	
$\Omega_b h^2$ .....	0.022370	0.000026	0.46	0.67	
$\Omega_c h^2$ .....	0.12000	0.00041	0.55	0.73	
$\ln(10^{10} A_s)$ .....	3.044	0.0098	0.84	0.86	
$n_s$ .....	0.9649	0.0013	0.43	0.52	
$\tau$ .....	0.0544	0.0052	0.85	0.87	
$H_0$ [km s $^{-1}$ Mpc $^{-1}$ ]	67.36	0.29	0.81	0.91	
$N_{\text{eff}}$ .....	3.046	0.014	0.33	0.47	
$\Sigma m_\nu$ [eV] .....	0.06	0.025	0.83	0.86	



Factor of two improvement on  $\sigma(N_{\text{eff}})$  and  $\sigma(n_s)$

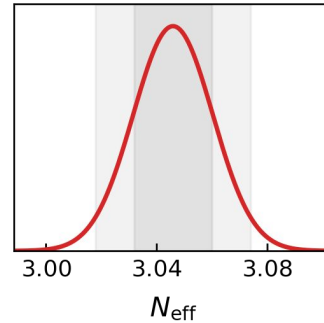
# Effective Number of Relativistic Species

Can detect or rule out any new light particle that was in thermal equilibrium after inflation at  $2\sigma$ .

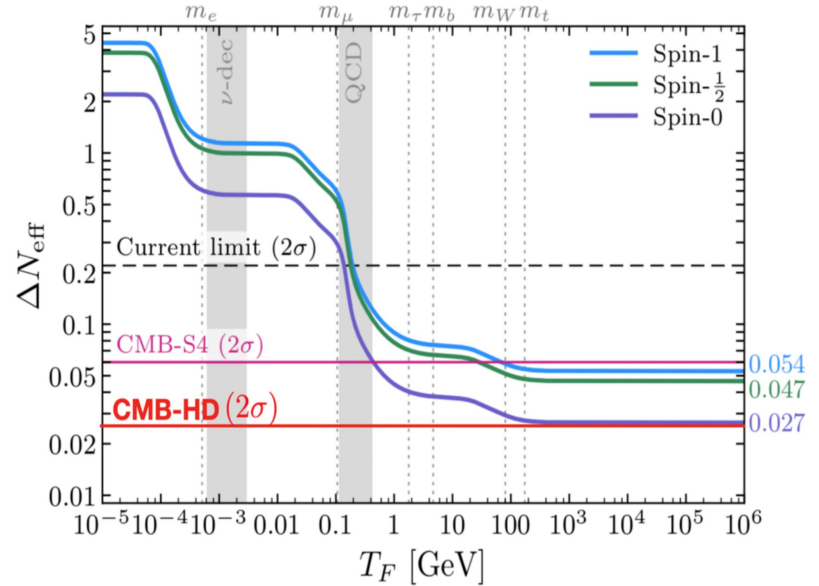


Requires  
 $\Delta N_{\text{eff}} \geq 0.027$

Can be ruled out  
 by CMB-HD +  
 DESI at  $2\sigma$

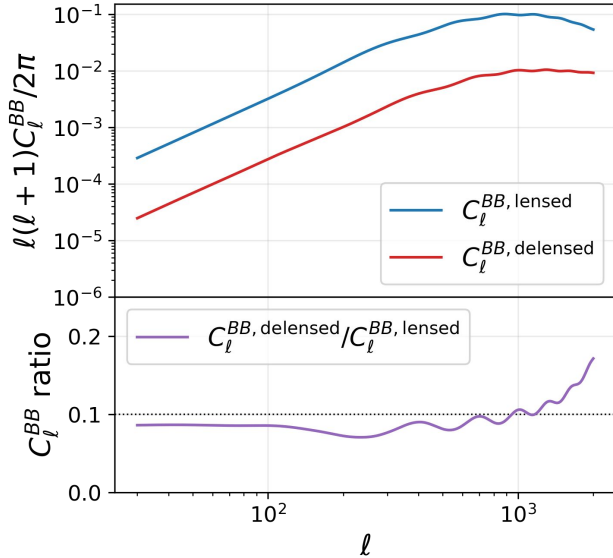


**CMB-HD + DESI**  
 $\sigma(N_{\text{eff}}) = 0.014$



# Inflation

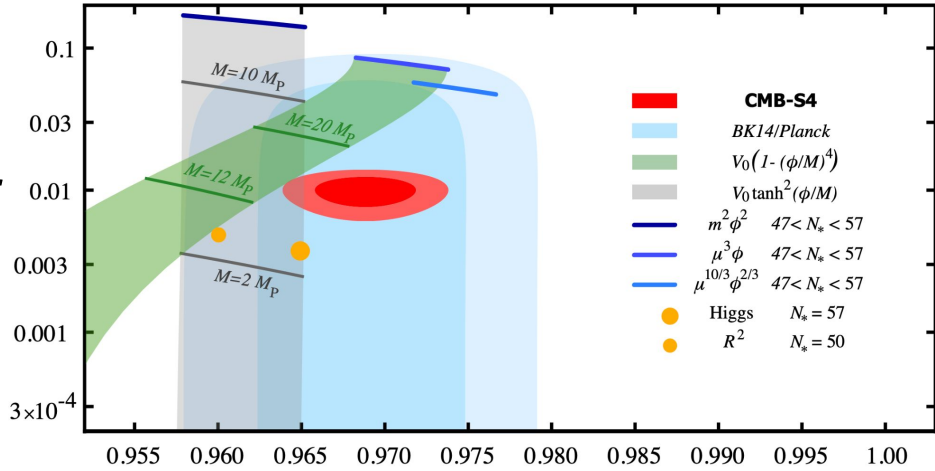
## CMB-HD Delensing



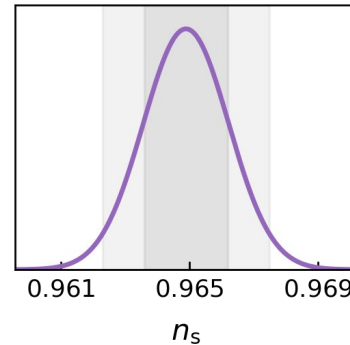
+Large-scale B-modes

Remove 90% of B-mode lensing over 60% of the sky

$r$



$n_s$



CMB-HD + DESI

$\sigma(n_s) = 0.0013$

(2 x smaller than precursors)

# CMB-HD Forecasting Codes

[github.com/CMB-HD](https://github.com/CMB-HD)



## CMB-HD Collaboration

CMB-HD software

👤 2 followers 🔗 <https://cmb-hd.org>

### Popular repositories

**hdlike**

Public

CMB-HD Likelihood

● Jupyter Notebook

**hdfisher**

Public

CMB-HD Fisher Forecast Code

● Jupyter Notebook

Both have options to include delensing, DESI BAO, and baryonic feedback.

## hdlike :

- Compatible with CAMB and Cobaya
- Examples to easily reproduce HD forecasts and run new ones

## hdfisher :

- Compatible with CAMB
  - Can vary any parameter that can be passed to `camb.set_params()`
- Example notebook to reproduce Fisher forecasts and plots
- Example notebook + python script to calculate a new Fisher matrix

# Summary

- The low noise and high resolution of CMB-HD will lead to tight constraints on a  $\Lambda\text{CDM} + N_{\text{eff}} + \sum m_\nu$  model
  - We find  $\sigma(N_{\text{eff}}) = 0.014$  and  $\sigma(n_s) = 0.0013$  after including residual extragalactic foregrounds, delensing, and DESI BAO
- CMB-HD is sensitive to the effects of baryonic feedback on the small-scale matter distribution
- The CMB-HD likelihood and Fisher forecasting codes are publicly available at [github.com/CMB-HD](https://github.com/CMB-HD)

The background of the slide is a Cosmic Microwave Background (CMB) fluctuation map, showing a complex pattern of blue and orange/yellow spots representing temperature variations in the early universe. The text is overlaid on a semi-transparent white rectangular area.

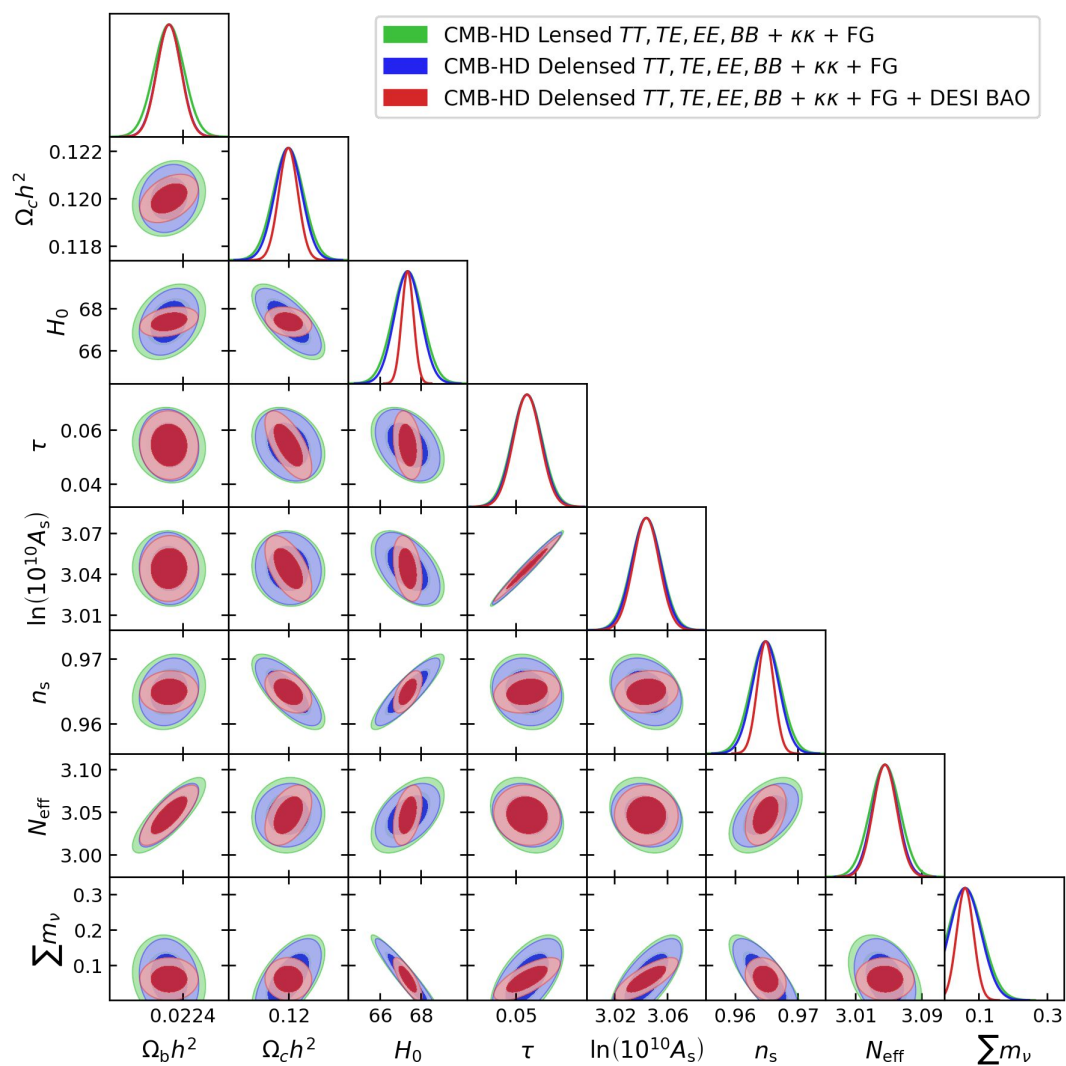
# Thank you!

Questions?

A Cosmic Microwave Background (CMB) fluctuation map showing temperature variations across the sky. The map uses a color scale where blue represents cooler regions and orange/red represents warmer regions. The fluctuations are distributed in a complex, non-uniform pattern.

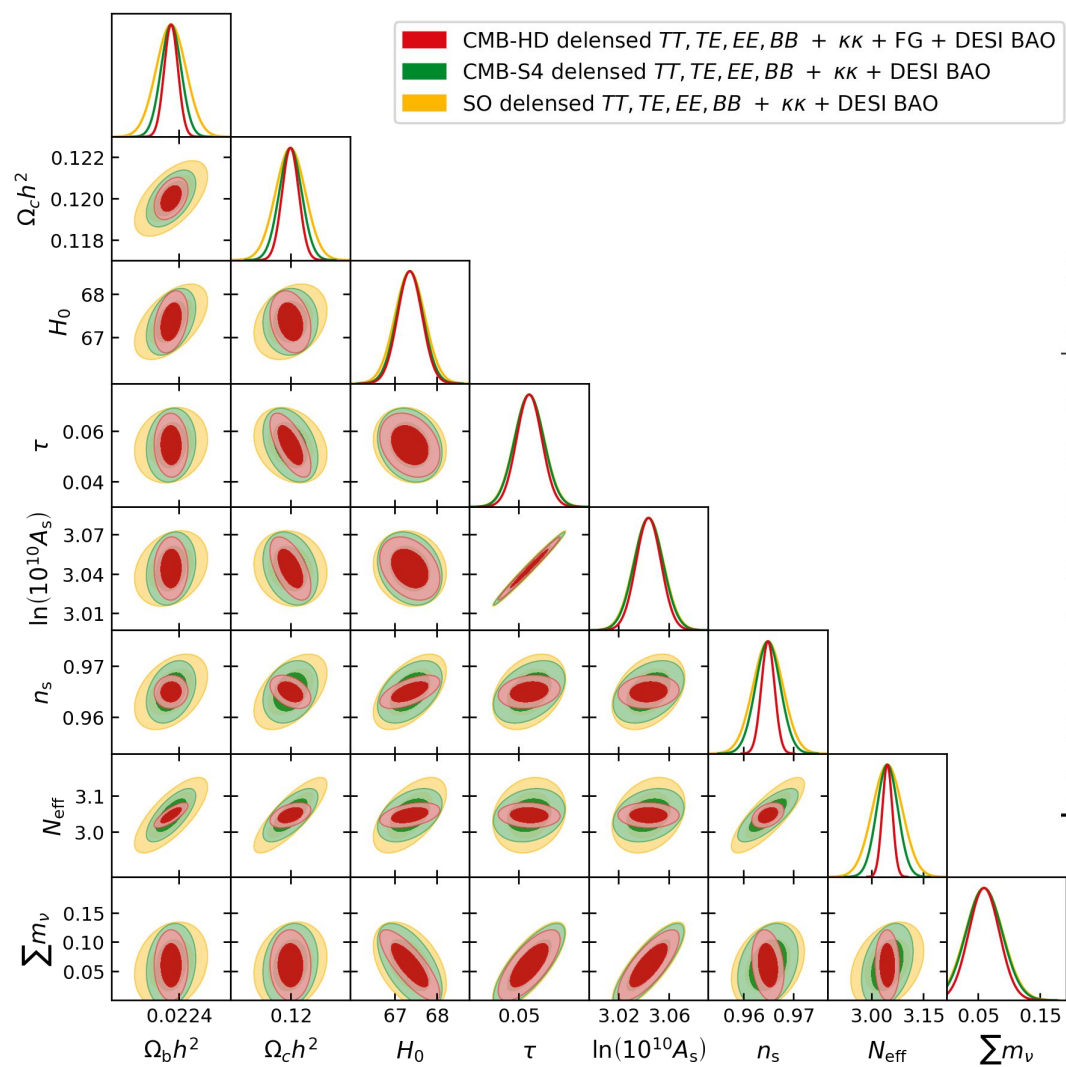
# Extra slides





Parameter	Fiducial	$\ell_{\max}, L_{\max} = 20,000$				$\ell_{\max}, L_{\max} = 10,000$
		HD Lensed	HD Lensed + FG	HD Delensed + FG	<b>HD Delensed + FG + DESI BAO</b>	HD Delensed + FG + DESI BAO
$\Lambda\text{CDM} + N_{\text{eff}} + \Sigma m_\nu$						
$\Omega_b h^2$ .....	0.022370	0.000032	0.000033	0.000027	0.000026	0.000026
$\Omega_c h^2$ .....	0.12000	0.00064	0.00065	0.00058	0.00041	0.00041
$\ln(10^{10} A_s)$ .....	3.044	0.011	0.011	0.011	0.0098	0.010
$n_s$ .....	0.9649	0.0023	0.0024	0.0021	0.0013	0.0014
$\tau$ .....	0.0544	0.0056	0.0057	0.0054	0.0052	0.0054
$H_0$ [km s <sup>-1</sup> Mpc <sup>-1</sup> ]	67.36	0.72	0.74	0.65	0.29	0.29
$N_{\text{eff}}$ .....	3.046	0.017	0.018	0.015	0.014	0.015
$\Sigma m_\nu$ [eV] .....	0.06	0.050	0.051	0.047	0.025	0.026

Table IV. Forecasted cosmological parameter constraints from CMB-HD  $TT$ ,  $TE$ ,  $EE$ ,  $BB$  and  $\kappa\kappa$  power spectra for a  $\Lambda\text{CDM} + N_{\text{eff}} + \Sigma m_\nu$  model. All forecasts include a  $\tau$  prior of  $\tau = 0.054 \pm 0.007$  from *Planck* [1]. The first two columns list the parameters and their fiducial values. The following two columns list their forecasted marginalized  $1\sigma$  uncertainties when using lensed spectra with or without foregrounds in the temperature maps. The fifth column shows the forecast when delensing the CMB spectra, and the sixth column shows the change when including DESI BAO data [16]. In each of these cases we use CMB and CMB lensing multipoles out to  $\ell_{\max}, L_{\max} = 20,000$  for CMB-HD. The last column lists the same information as the sixth column, but instead using a maximum multipole of  $\ell_{\max}, L_{\max} = 10,000$  for both CMB and CMB lensing power spectra. We see in particular that  $n_s$  and  $N_{\text{eff}}$  constraints are tightened when including multipoles beyond 10,000 for a CMB-HD type survey. We show corresponding forecasts for  $\Lambda\text{CDM}$  and  $\Lambda\text{CDM} + N_{\text{eff}}$  models in Appendix C.



Parameter	Fiducial	HD Delensed + FG + DESI BAO
$\Lambda\text{CDM} + N_{\text{eff}} + \sum m_\nu$		
$\Omega_b h^2$ .....	0.022370	0.000026
$\Omega_c h^2$ .....	0.12000	0.00041
$\ln(10^{10} A_s)$ .....	3.044	0.0098
$n_s$ .....	0.9649	0.0013
$\tau$ .....	0.0544	0.0052
$H_0$ [km s <sup>-1</sup> Mpc <sup>-1</sup> ]	67.36	0.29
$N_{\text{eff}}$ .....	3.046	0.014
$\sum m_\nu$ [eV] .....	0.06	0.025

Parameter	Fiducial	1 $\sigma$ Error			Ratio of 1 $\sigma$ Errors	
		SO + DESI BAO	CMB-S4 + DESI BAO	CMB-HD + DESI BAO	CMB-HD / SO	CMB-HD / CMB-S4
$\Lambda$ CDM+ $N_{\text{eff}}+\Sigma m_\nu$						
$\Omega_b h^2$ .....	0.022370	0.000057	0.000039	0.000026	0.46	0.67
$\Omega_c h^2$ .....	0.12000	0.00074	0.00056	0.00041	0.55	0.73
$\ln(10^{10} A_s)$ .....	3.044	0.012	0.011	0.0098	0.84	0.86
$n_s$ .....	0.9649	0.0030	0.0025	0.0013	0.43	0.52
$\tau$ .....	0.0544	0.0061	0.0060	0.0052	0.85	0.87
$H_0$ [km s $^{-1}$ Mpc $^{-1}$ ]	67.36	0.36	0.32	0.29	0.81	0.91
$N_{\text{eff}}$ .....	3.046	0.043	0.030	0.014	0.33	0.47
$\Sigma m_\nu$ [eV] .....	0.06	0.030	0.029	0.025	0.83	0.86

Table III. Forecasted cosmological parameter constraints for a  $\Lambda$ CDM +  $N_{\text{eff}}$  +  $\Sigma m_\nu$  model from SO-like, CMB-S4-like, and CMB-HD-like delensed  $TT$ ,  $TE$ ,  $EE$ ,  $BB$  and  $\kappa\kappa$  power spectra when combined with DESI BAO. The first two columns list the parameters and their fiducial values. The following three columns list the forecasted marginalized 1 $\sigma$  uncertainties on each parameter for the three experiments, and the last two columns list the ratios of these values. The forecasts for CMB-HD include expected residual extragalactic foregrounds in the temperature power spectrum. All forecasts include a  $\tau$  prior of  $\tau = 0.054 \pm 0.007$  from *Planck* [1]. We find improvement in all parameters considered for a CMB-HD-like experiment compared to precursor surveys; we also find the most significant improvement for  $n_s$  and  $N_{\text{eff}}$ , of about a factor of two or more. These forecasts are also depicted in Fig. 7.

Parameter	CDM	+ feedback	+ SZ prior
$\Omega_b h^2$ .....	0.000026	0.000028	0.000027
$\Omega_c h^2$ .....	0.00041	0.00046	0.00041
$\ln(10^{10} A_s)$ .....	0.0095	0.010	0.010
$n_s$ .....	0.0013	0.0021	0.0013
$\tau$ .....	0.0051	0.0056	0.0056
$100\theta_{MC}$	0.000058	0.000064	0.000060
$N_{\text{eff}}$ .....	0.014	0.020	0.014
$\sum m_\nu$ [eV] .....	0.024	0.026	0.027
$\log_{10}(T_{\text{AGN}}/\text{K})$ ...	—	0.040	0.0047
$H_0$ [km s <sup>-1</sup> Mpc <sup>-1</sup> ]	0.28	0.29	0.27
$\sigma_8$ .....	0.0033	0.0033	0.0033

Table V. Shown are the cosmological constraints from the combination of CMB-HD delensed  $TT$ ,  $TE$ ,  $EE$ ,  $BB$ , and  $\kappa\kappa$  power spectra with DESI BAO for the baseline  $\Lambda\text{CDM} + N_{\text{eff}} + \sum m_\nu$  model, a  $\Lambda\text{CDM} + N_{\text{eff}} + \sum m_\nu + \text{baryonic feedback}$  model from `HMCode-2020` [60], and a  $\Lambda\text{CDM} + N_{\text{eff}} + \sum m_\nu + \text{baryonic feedback}$  model including a 0.06% prior on the feedback parameter  $\log_{10}(T_{\text{AGN}}/\text{K})$  expected from from a joint analysis of CMB-HD kSZ, tSZ, and lensing data (see Section VD for details). All results shown here are from the likelihood and MCMC chains as opposed to Fisher forecasts. We also include  $100\theta_{MC}$ , and separate the two derived parameters,  $H_0$  and  $\sigma_8$ , which is the linear root-mean-square matter fluctuations today.

Parameter	Fiducial	HD Lensed	HD Delensed
$\Lambda$ CDM+ $N_{\text{eff}}+\sum m_\nu$		+ FG + DESI BAO	+ FG + DESI BAO
$\Omega_b h^2$ .....	0.022370	0.000032	0.000026
$\Omega_c h^2$ .....	0.12000	0.00045	0.00041
$\ln(10^{10} A_s)$ .....	3.044	0.010	0.0098
$n_s$ .....	0.9649	0.0014	0.0013
$\tau$ .....	0.0544	0.0055	0.0052
$H_0$ [km s $^{-1}$ Mpc $^{-1}$ ]	67.36	0.30	0.29
$N_{\text{eff}}$ .....	3.046	0.017	0.014
$\sum m_\nu$ [eV] .....	0.06	0.025	0.025

Table IX. Here we compare the forecasted  $1\sigma$  parameter constraints from lensed (third column) and delensed (fourth column) CMB-HD  $TT$ ,  $TE$ ,  $EE$ ,  $BB$  and  $\kappa\kappa$  power spectra when including DESI BAO in order to see how much improvement is gained from delensing alone. The parameter names and fiducial values are listed in the first and second columns, respectively. We find that delensing improves parameter constraints even after including DESI BAO, with the most improvement seen for  $N_{\text{eff}}$ .

Parameter	Fiducial	$\ell_{\max}, L_{\max}$ for HD Delensed + FG + DESI BAO				
		1000	3000	5000	10,000	20,000
$\Lambda\text{CDM}+N_{\text{eff}}+\sum m_\nu$						
$\Omega_b h^2$ .....	0.022370	0.00016	0.000039	0.000027	0.000026	0.000026
$\Omega_c h^2$ .....	0.12000	0.0024	0.00054	0.00042	0.00041	0.00041
$\ln(10^{10} A_s)$ .....	3.044	0.014	0.011	0.011	0.010	0.0098
$n_s$ .....	0.9649	0.0048	0.0023	0.0018	0.0014	0.0013
$\tau$ .....	0.0544	0.0065	0.0060	0.0057	0.0054	0.0052
$H_0$ [km s <sup>-1</sup> Mpc <sup>-1</sup> ]	67.36	0.80	0.32	0.29	0.29	0.29
$N_{\text{eff}}$ .....	3.046	0.15	0.030	0.018	0.015	0.014
$\sum m_\nu$ [eV] .....	0.06	0.037	0.029	0.028	0.026	0.025

Table X. Shown are the forecasted  $1\sigma$  uncertainties from delensed CMB-HD  $TT$ ,  $TE$ ,  $EE$ ,  $BB$  and  $\kappa\kappa$  spectra plus DESI BAO, when varying the maximum multipole  $\ell_{\max}$  or  $L_{\max}$  for the CMB spectra. The parameter names and fiducial values are listed in the first and second columns, respectively, while the remaining columns list the  $1\sigma$  parameter errors for the given maximum multipole. We see that to obtain  $\sigma(n_s) = 0.0013$  and  $\sigma(N_{\text{eff}}) = 0.014$ , for example, requires the full range of multipoles out to 20,000.

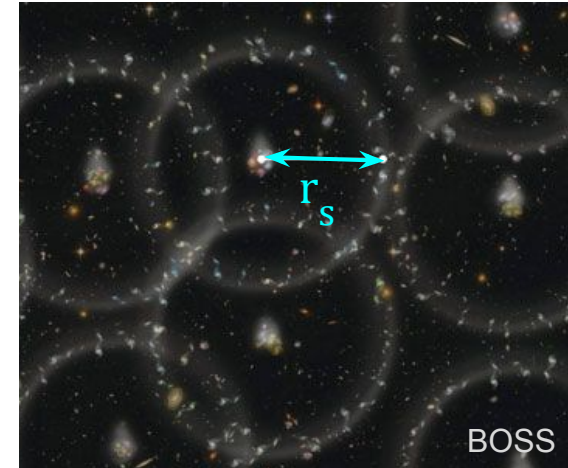
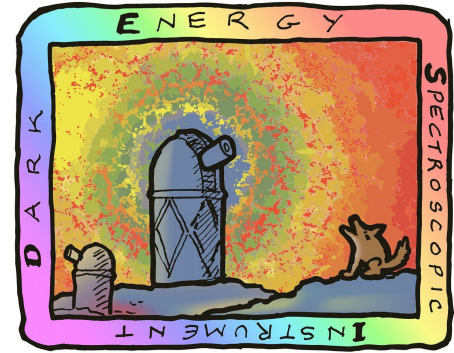
# DESI BAO Data

Forecast combination of CMB-HD and DESI BAO data:

- Mock DESI measurements of  $r_s / d_V(z)$ , where

$$d_V(z) \equiv \left[ (1+z)^2 d_A^2(z) \frac{cz}{H(z)} \right]^{1/3} \quad (\text{Eisenstein et al., 2005})$$

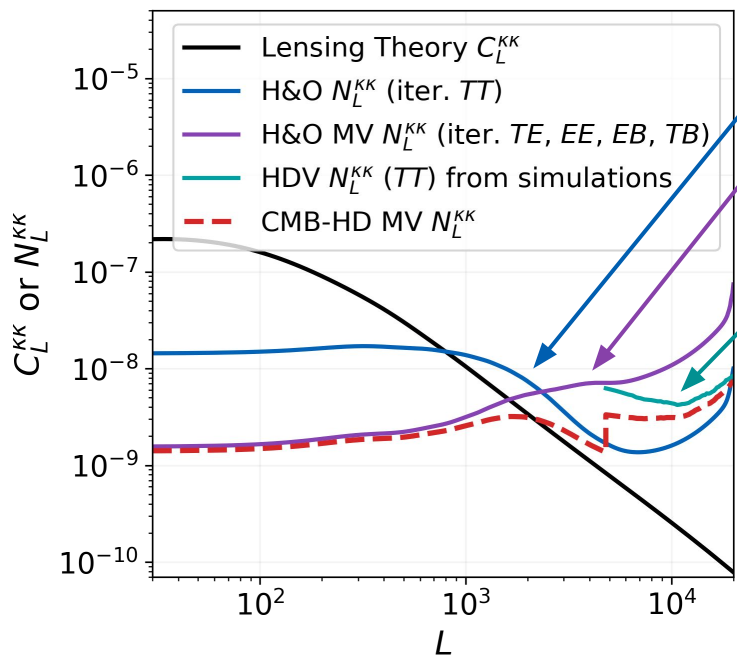
- Derived from DESI forecasts for their baseline ( $0.65 < z < 1.85$ ) and bright ( $0.05 < z < 0.45$ ) galaxy surveys over 14,000 square degrees (Aghamousa et al., 2016)





# Lensing Noise

Minimum-variance combination of  $TT$ ,  $TE$ ,  $EE$ ,  $EB$ ,  $TB$  quadratic estimators



$TT$  for  $L < 5000$  and

$TE, EE, EB, TB$  on all scales:

- H&O estimator (Hu & Okamoto, 2002)
- Iterative delensing lowers noise (Hotinli et. al., 2021)

$TT$  for  $L > 5000$ :

- HDV estimator (Hu, DeDeo, & Vale, 2007)
- From simulations (Han & Sehgal, 2022)

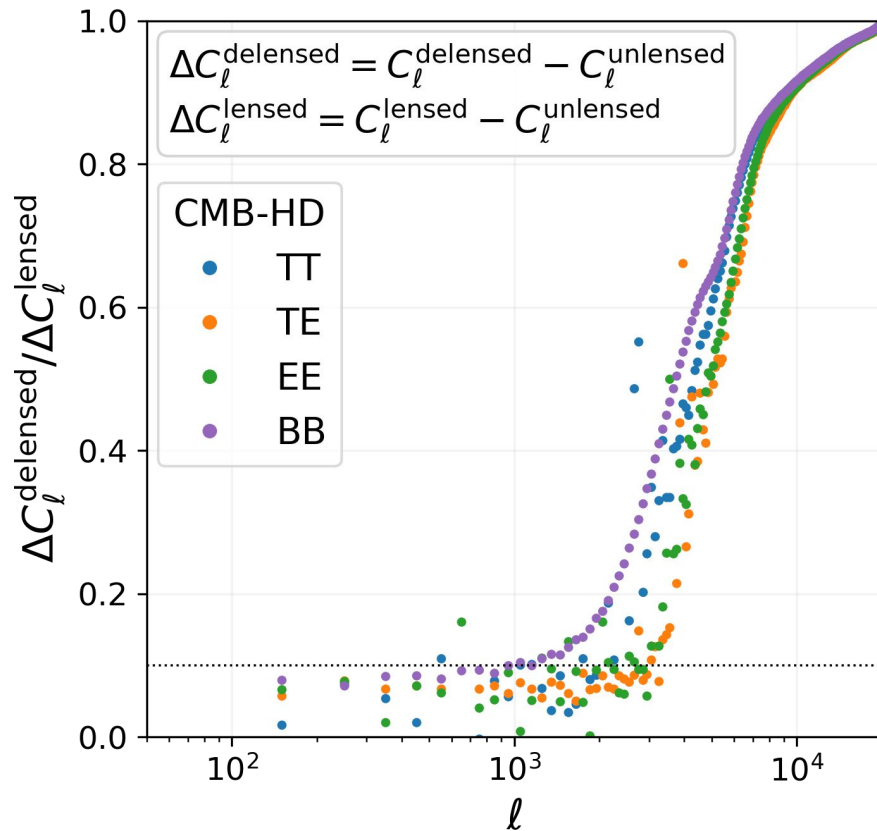
# Delensing

Use reconstructed lensing map to delens the observed CMB.

- Gain sharpened picture of the universe at  $z = 1100$ .

Combine delensed CMB  $TT$ ,  $TE$ ,  $EE$ ,  $BB$  power spectra with CMB lensing  $\kappa\kappa$  power spectrum to replace the lost lensing information.

## Fraction of lensing removed from the CMB power spectra:

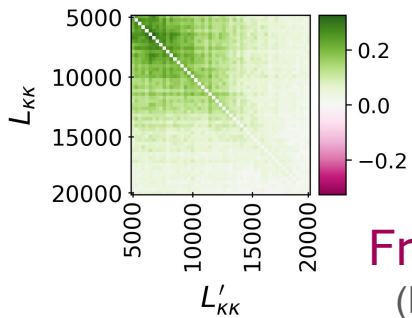


# CMB-HD Data: Covariance Matrix

Off-diagonal elements are from  
lensing-induced correlations

(Diagonal elements are not shown)

## Lensing x Lensing

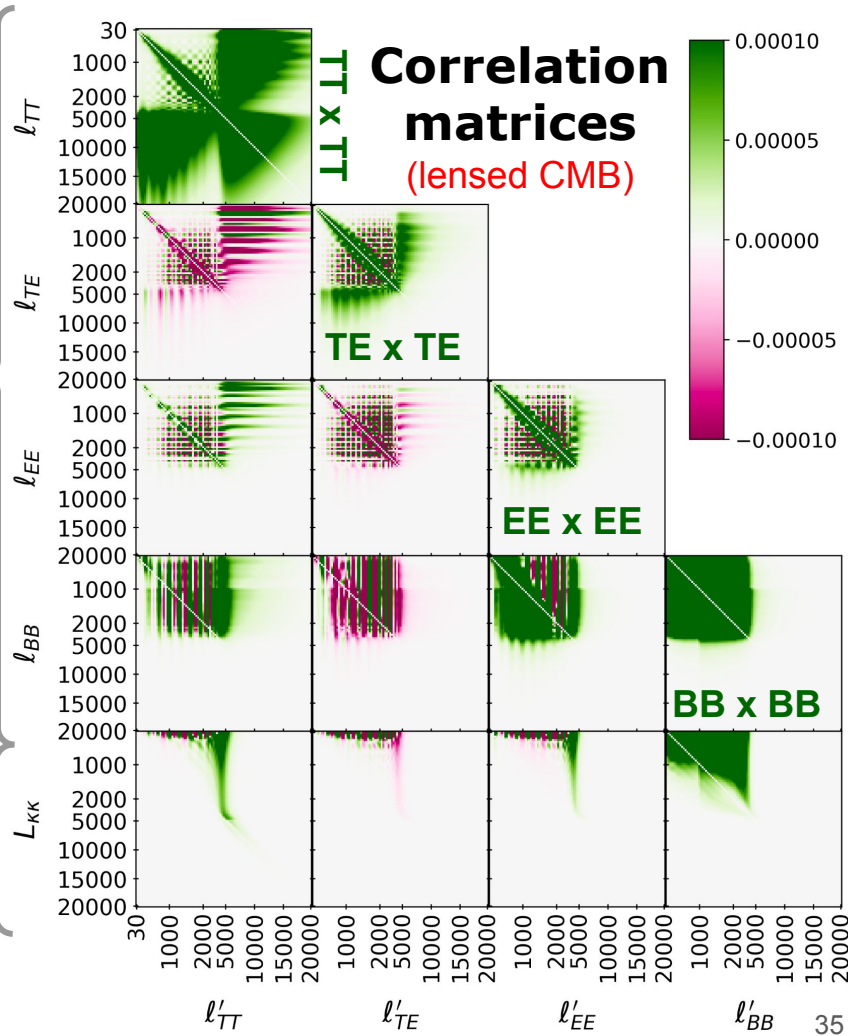


From simulations  
(Han & Sehgal, 2022)

Analytic  
(Hotinli et. al., 2021)

CMB x  
Lensing

CMB x CMB



Correlation  
matrices  
(lensed CMB)

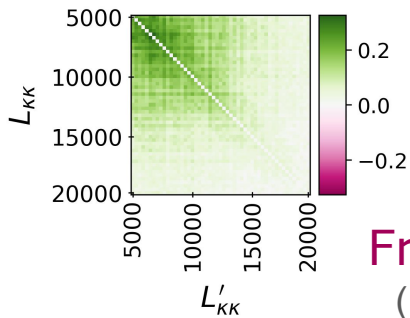


# CMB-HD Data: Covariance Matrix

Off-diagonal elements are from  
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## Lensing x Lensing



From simulations  
(Han & Sehgal, 2022)

Analytic  
(Hotinli et. al., 2021)

CMB x  
Lensing

CMB x CMB

