



Massachusetts Institute of Technology

# Current Status of TMD Measurements at CLAS12

Timothy B. Hayward

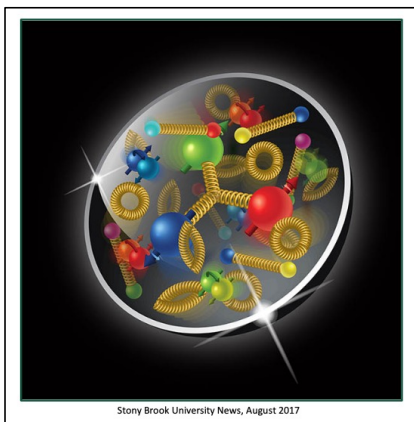


# Thomas Jefferson National Accelerator Facility

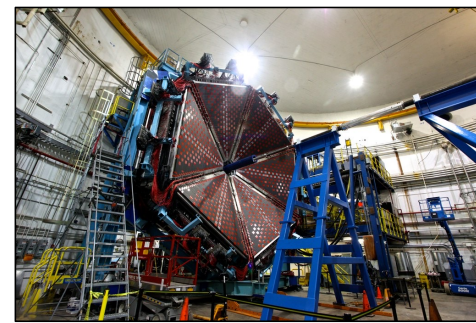
- Continuous Electron Beam Accelerator Facility (CEBAF) is located in Newport News, VA.
- Four experimental halls (A, B, C and D) receive a recently upgraded 12 GeV longitudinally polarized electron beam.
- Race track design with parallel north and south linear accelerators that pass the beam up to five times.
- CLAS12 located in Hall B.



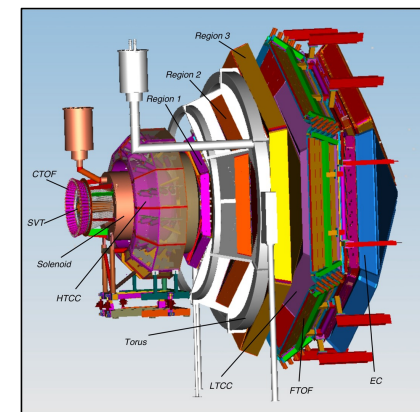
# CLAS12 (Hall B) Physics Program



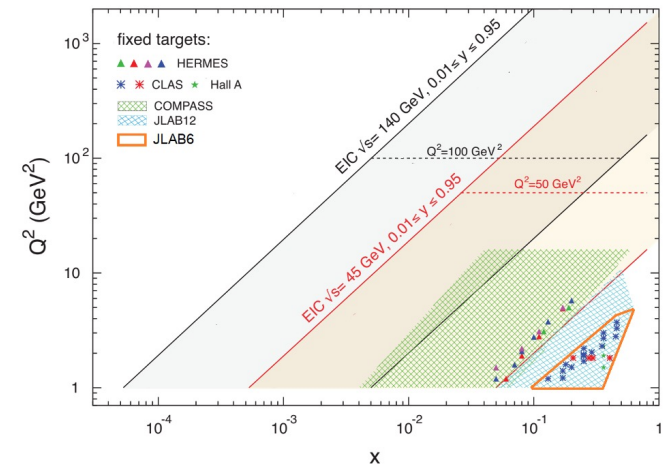
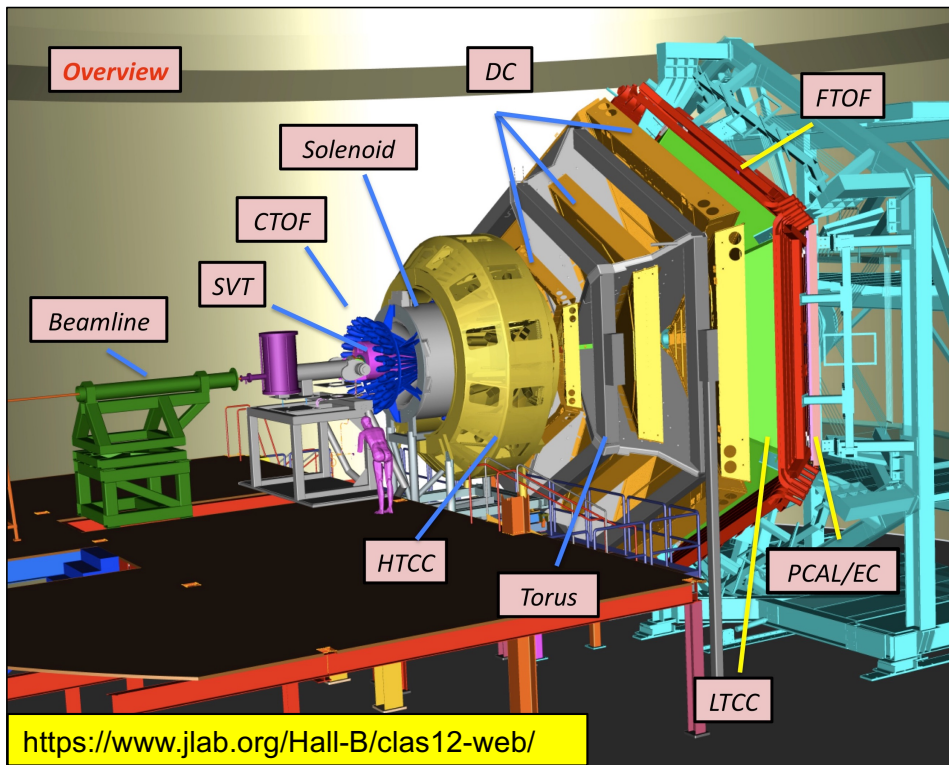
- International collaboration with more than 40 member institutions and 200 full members.
- CLAS(12) is the world's only large acceptance and high luminosity spectrometer for fixed target lepton scattering experiments.



1. Study of the nucleon resonance structure at photon virtualities from 2.0 to 12 GeV<sup>2</sup>
2. Study of Generalized Parton Distributions (GPDs), (2 +1) D imaging of the proton and the study of its gravitational and mechanical structure ([see talk this afternoon by Silvia Niccolai](#))
3. Study of the Transverse Momentum Dependence (TMDs) and the of 3D structure in momentum space.
4. Study of J/ψ Photoproduction, LHCb Pentaquarks and Timelike Compton Scattering.
5. Study of meson spectroscopy in search of hybrid mesons
6. Much more!



# CLAS12 Spectrometer



JLab: Valence quark distribution  
 Compass: Sea quark distribution  
 EIC: Gluon distribution

- CLAS12: very high luminosity ( $10^{34}$ ), wide acceptance, low  $Q^2$  (higher twist measurements)
- Began data taking in Spring 2018 – many “run periods” now available: liquid  $H_2$ ,  $D_2$ , polarized  $NH_3$  and  $ND_3$  etc.
- ~10.5 GeV electron beam, longitudinally polarized beam.



# SIDIS Observables at CLAS12

## Run Group A (Unpolarized LH<sub>2</sub> target)

- ★ unpolarized SIDIS cross section off proton
- ★  $A_{LU}$  in Beam Spin Asymmetries

## Run Group B (Unpolarized LD<sub>2</sub> target)

- ★ Complementary to RG-A  
→ allow for  $u/d$  quark flavor separation

## Run Group C (longitudinally polarized NH<sub>3</sub> and ND<sub>3</sub>)

- ★  $F_{UL}$  and  $F_{LL}$

## Run Group K (Unpolarized LH<sub>2</sub> target)

- ★ 6.5, 7.5, 8.4 GeV e- beam
- ★  $F_{UU,L}$ ,  $F_{UU,T}$  Separation

## Run Group H (transversely polarized NH<sub>3</sub>)

- ★  $F_{UT}$  structure function

→ scheduled for FY 2029

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} =$$

$$\frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} \right.$$

$$\left. + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right.$$

$$\left. + S_{\parallel} \left[ \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] \right.$$

$$\left. + S_{\parallel} \lambda_e \left[ \sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right] \right.$$

$$\left. + |S_{\perp}| \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) \right. \right.$$

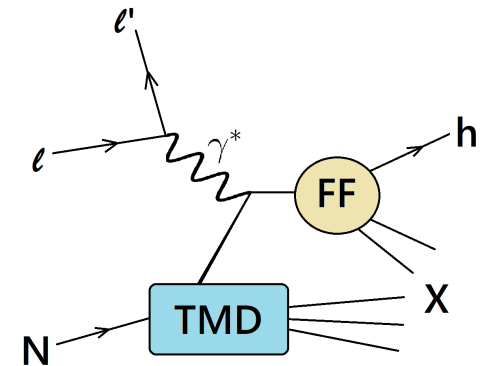
$$\left. + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \right.$$

$$\left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right]$$

$$\left. + |S_{\perp}| \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} \right. \right.$$

$$\left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right\}$$

The CLAS12 physics program will have access to the full SIDIS cross section including all observables in a variety of flavors. ([For nuclear TMDs see Lamia El Fassi's RGD talk this afternoon](#))

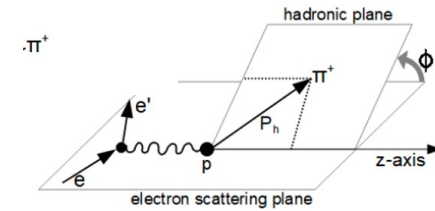


# TMDs from Single Hadron Production

$$F_{LU}^{\sin\phi_h} = \frac{2M}{Q} \mathcal{C} \left[ -\frac{\hat{h} \cdot k_T}{M_h} \left( x e \boxed{H_1^\perp} + \frac{M_h}{M} \boxed{f_1} \tilde{G}^\perp \right) + \frac{\hat{h} \cdot p_T}{M} \left( x g^\perp \boxed{D_1} + \frac{M_h}{M} \boxed{h_1^\perp} \tilde{E} \right) \right]$$

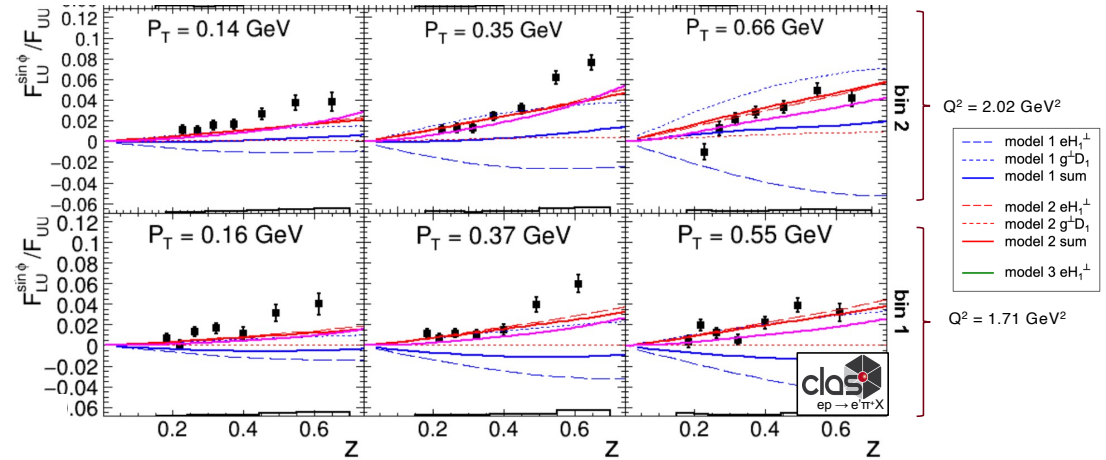
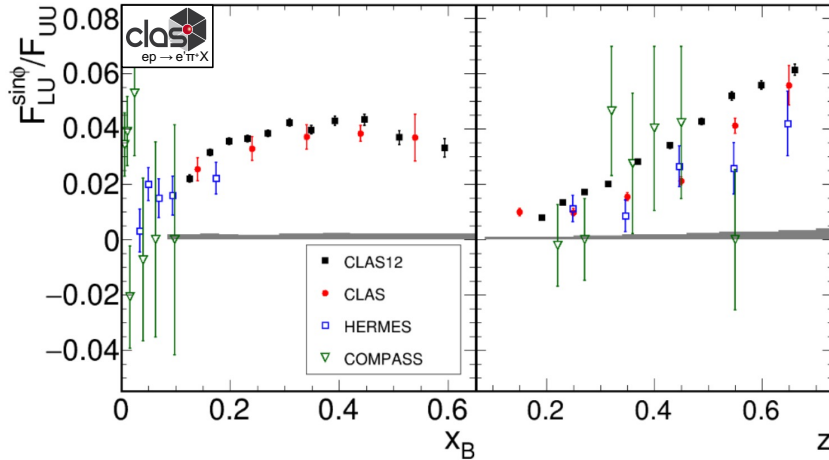
twist-3 pdf    unpolarized PDF    twist-3 t-odd PDF    Boer-Mulders  
Collins FF    twist-3 FF    unpolarized FF    twist-3 FF

A. Bacchetta et al., *JHEP* 0702, 093 (2007).



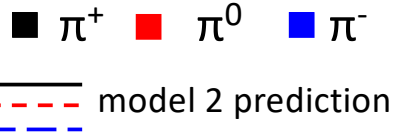
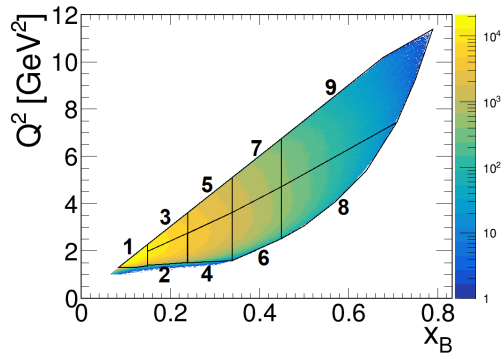
- model 1 (Mao et al., EPJ C 73) → Proton = active quark plus spectator scalar and axial-vector diquarks
- model 2 (Mao et al., EPJ C 74)
- - -  $eH_1^\perp$     - - -  $g^\perp D_1$
- model 3  $eH_1^\perp$  (Schweitzer et al.) →  $e(x)$  based on the chiral quark soliton model

First high-precision multidimensional study: important for constraints of PDFs.



S. Diehl et al., *Phys. Rev. Lett.*, 128, 062005, (2022), [hep:ex] 2101.03544

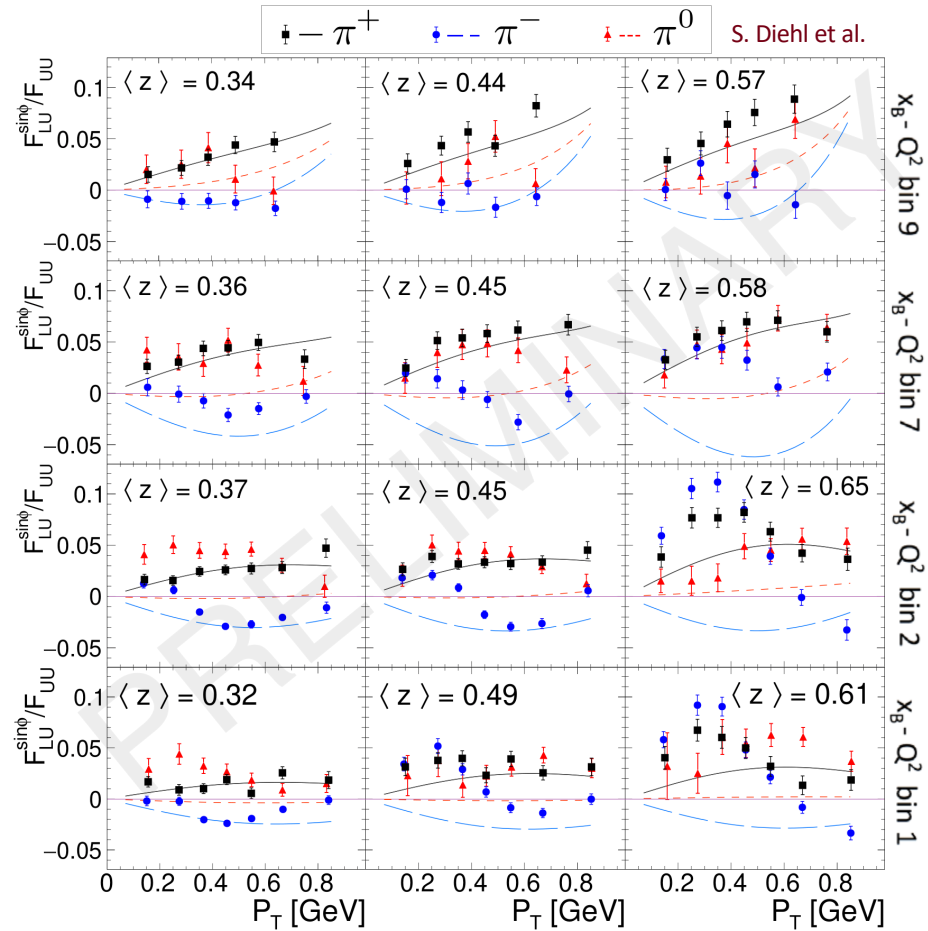
# Flavor Effects in Single Pion SIDIS



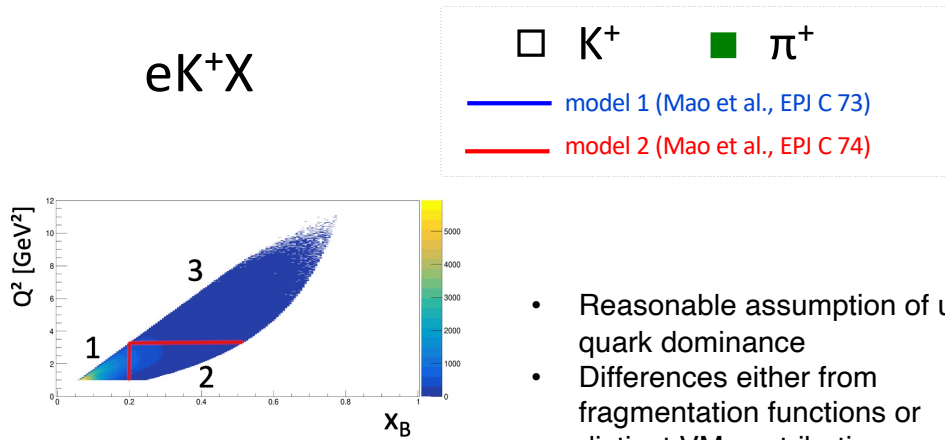
★ If Collins term only ( $H_1^\perp$ )  
 → hierarchy of the  $A_{LU}$ 's  
 $A_{LU}(\pi^-) < A_{LU}(\pi^0) = 0 < A_{LU}(\pi^+)$

★ Observed is more **Sivers-like** ( $g^\perp$ )  
 $A_{LU}(\pi^-) < A_{LU}(\pi^0) = A_{LU}(\pi^+)$

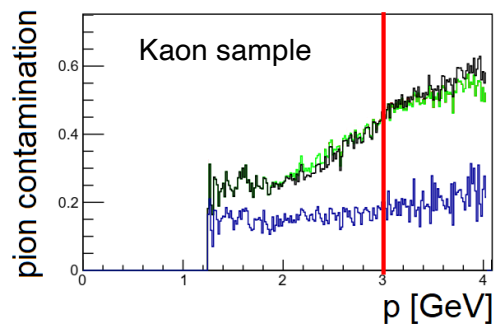
→ Asymmetry from struck u-quark



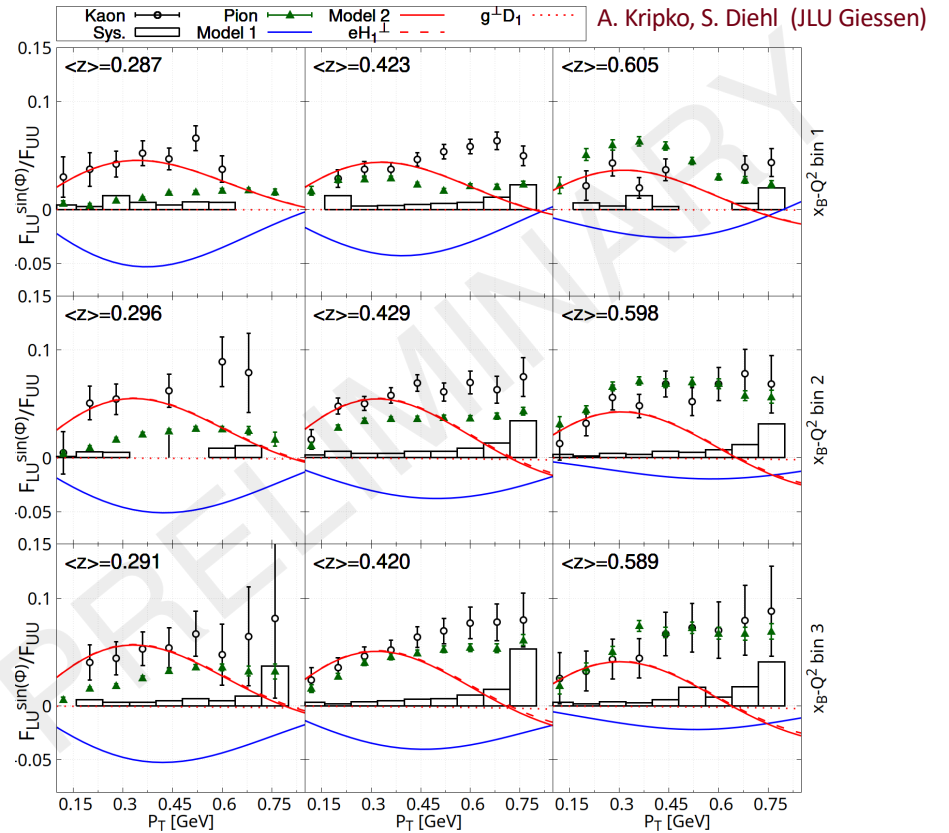
# Kaon SIDIS



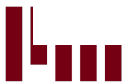
For Kaon SIDIS: Kaon PID based on a deep neural network



— TOF only  
— Deep neural network



For dihadron channels involving kaons see [C. Pecar's talk Friday](#)





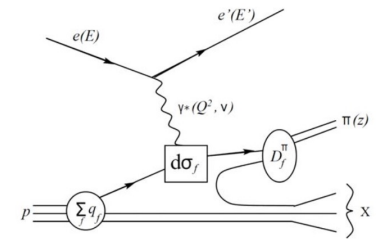
# Unpolarized Multiplicities of $ep \rightarrow e\pi X$

$$\frac{d\sigma}{dx dQ^2 dz dP_{h\perp}^2 d\phi_h} \sim F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos\phi_h \underline{F_{UU}^{\cos\phi_h}} + \epsilon \cos 2\phi_h \underline{F_{UU}^{\cos 2\phi_h}}$$

$$F_{UU}^{\cos\phi_h} = \frac{2M}{Q} \zeta \left( -\frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M_h} \left( x h H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{D}^\perp}{z} \right) + \frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M} \left( x f^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{H}}{z} \right) \right)$$

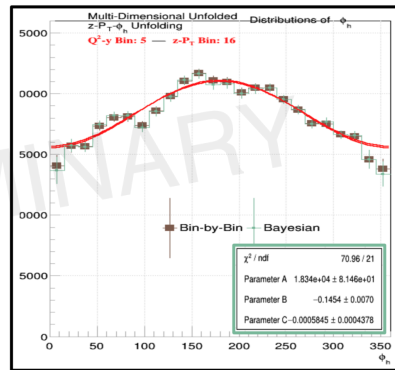
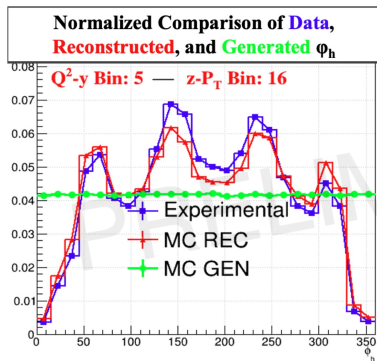
$$F_{UU}^{\cos 2\phi_h} = \zeta \left[ -\frac{2(\hat{\mathbf{h}} \cdot \mathbf{k}_T)(\hat{\mathbf{h}} \cdot \mathbf{p}_T) - \mathbf{k}_T \cdot \mathbf{p}_T}{M M_h} h_1^\perp H_1^\perp \right] \rightarrow \text{Leading twist}$$

- Next to leading twist: Sensitive to the Cahn Effect
- 4-D measurements  $[Q^2, y, z, P_T]$  for pion SIDIS
- 5-D bayesian unfolding (acceptance corrections)



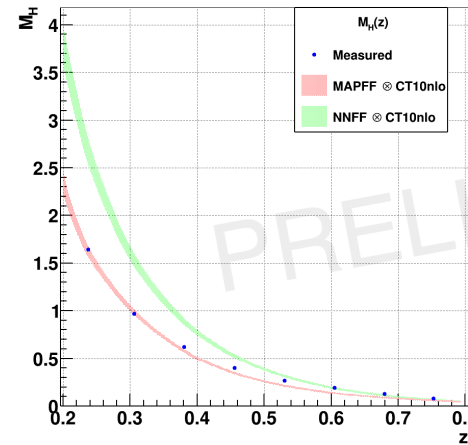
The  $\pi^0$   $p_T^2$  integrated multiplicities have been extracted and shown to be inline with the MAPFF  $\otimes$  CT10nlo leading order predictions.

$\pi^0$  Analysis by Marshall Scott

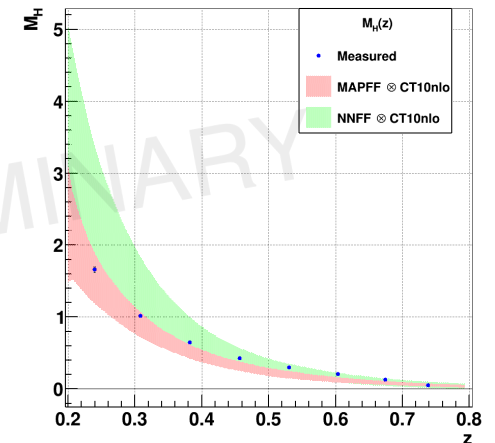


$\pi^+$  Analysis by Richard Capobianco

$x_B$ - $Q^2$  Bin 1 :  $M_H(z)$

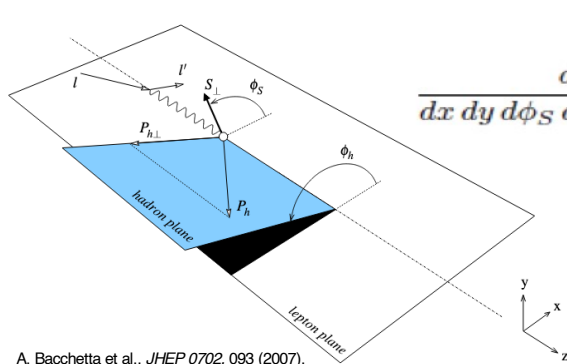


$x_B$ - $Q^2$  Bin 7 :  $M_H(z)$



# Understanding QCD, from observables to dynamics

- Goal: study the non-perturbative QCD dynamics in 3D space in details.
- Accurate physics interpretation requires separating multiple structure functions within a multidimensional space, with controlled systematics and careful evaluation of theoretical assumptions on non-perturbative quantities.

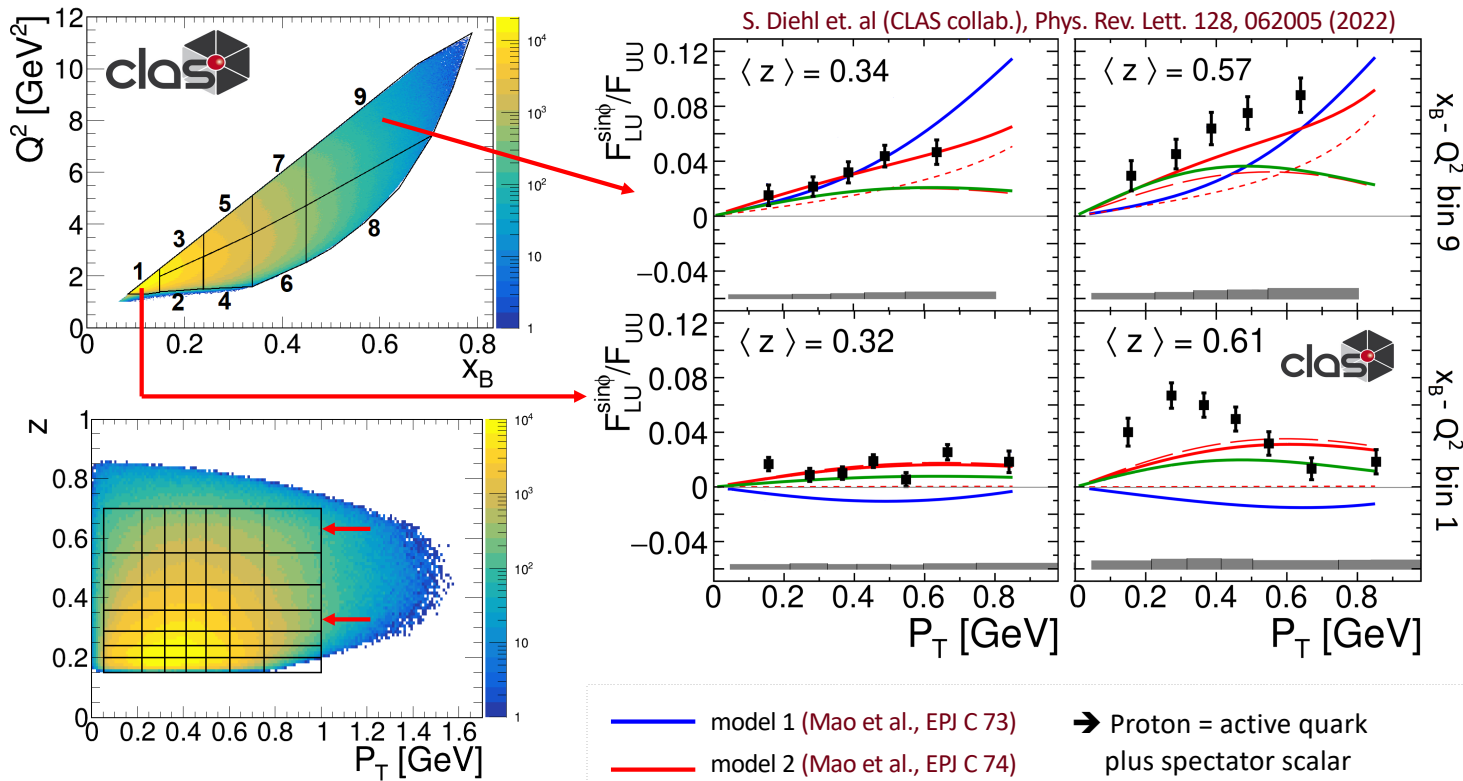


$$\begin{aligned}
 & F_{UU,T}(x, z, \mathbf{P}_{hT}^2, Q^2) \quad \text{TMD Parton Distribution Functions} \quad \text{TMD Parton Fragmentation Functions} \\
 \frac{d\sigma}{dx dy d\phi_S dz d\phi_h dP_{h\perp}^2} &= x \sum_q \left[ \mathcal{H}_{UU,T}^q(Q^2, \mu^2) \int d^2\mathbf{k}_\perp d^2\mathbf{P}_\perp f_1^a(x, \mathbf{k}_\perp^2; \mu^2) D_1^{a \rightarrow h}(z, \mathbf{P}_\perp^2; \mu^2) \delta(z\mathbf{k}_\perp - \mathbf{P}_{hT} + \mathbf{P}_\perp) \right. \\
 & \quad \left. + Y_{UU,T}(Q^2, \mathbf{P}_{hT}^2) + \mathcal{O}(M^2/Q^2) \right] \quad Q^2 \gg 1, k_\perp/Q \ll 1
 \end{aligned}$$

hard part

- Factorization allows the description using TMD-PDFs and TMD FFs.
- When there is disagreement:
  - Factorization is broken...? 😞
  - Unaccounted terms may contribute... 🤔
    - Theory should account for them... or
    - Experiment should measure and exclude them!

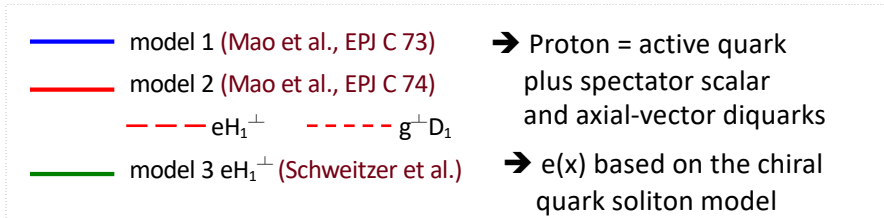
# Differences between multidimensional analysis and theory



S. Diehl et. al (CLAS collab.), Phys. Rev. Lett. 128, 062005 (2022)



- Certain regions of multidimensional analysis agree well with predictions while others clearly diverge (typically low  $P_T$  and high  $z$ ).



in total: 344 bins x 12 bins in  $\phi$   
 ~ 4130 BSA bins



# SIDIS cross section: separating $F_{UU,L}$

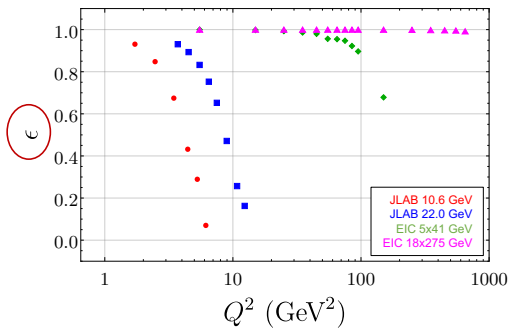
Semi-Inclusive:

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \epsilon F_{UU,L} + \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right.$$

ratio of longitudinal and transverse photon flux

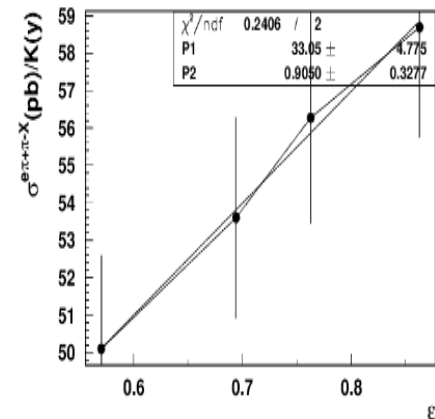
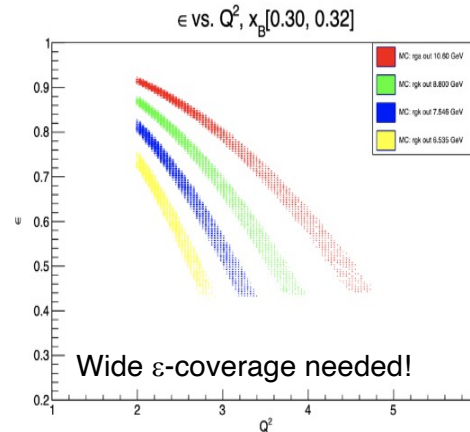
Hall-C E12-06-104  
 E12-23-014  
 Hall-B E12-16-010C

$$\left. + S_{\parallel} \left[ \sqrt{2\epsilon(1+\epsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \epsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] + S_{\parallel} \lambda_e \sqrt{1-\epsilon^2} F_{LL} \right.$$



- At higher energies longitudinal photon contributions are kinematically enhanced (at EIC 5 times bigger at  $Q^2 \sim 10$ )
- JLab studies critical for EIC data interpretation

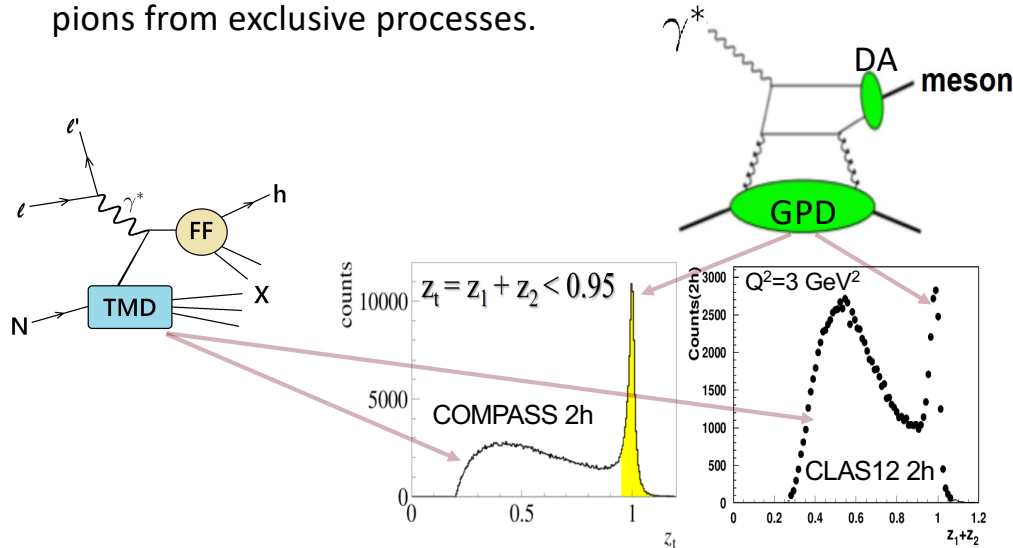
Separation of contributions from longitudinal and transverse photons critical for interpretation  
 $R = F_{UU,L}/F_{UU,T}$  depend on the process



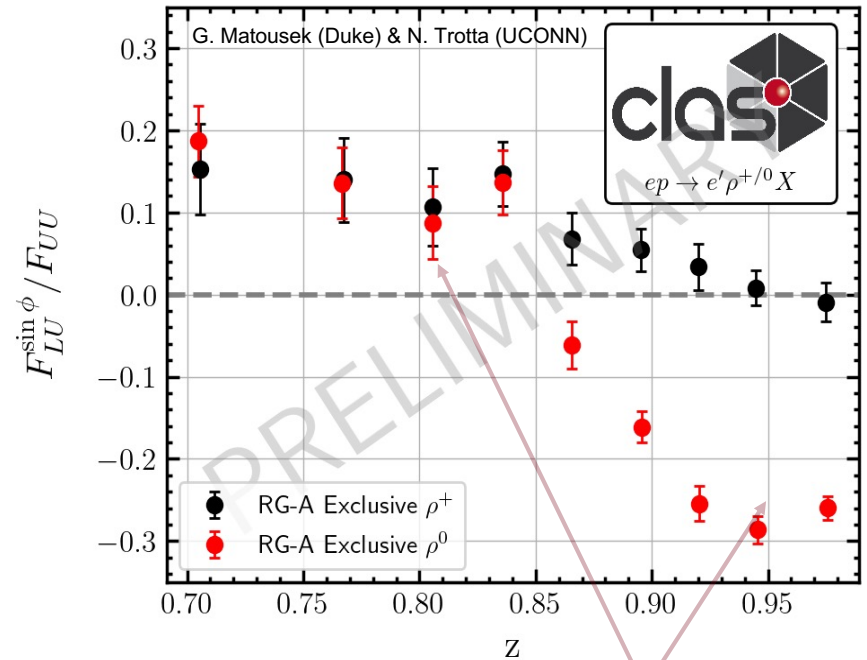


# Quark-gluon correlations; Impact of VMs

- A TMD based description is valid *only* for pions from current fragmentation **BUT** the  $e\pi X$  sample also contains pions from exclusive processes.



- Understanding of the SSAs of VMs is critical for interpretation of pion SIDIS.
- The fraction of diffractive mesons increases with energy.
- At large  $x$  the diffractive processes are suppressed by the minimum  $t$ .
- Fully evaluating the effect diffractive mesons have on the extraction of TMDs will be critical for EIC studies.

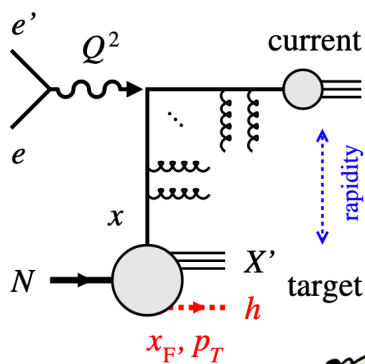


Comparison to  $\rho^0$  indicates where the “diffractive” events are appearing. There are separate dynamical contributions with wildly different azimuthal moments that complicate the picture. Which kinematic regions are contributing to the measurements in single pion observables?

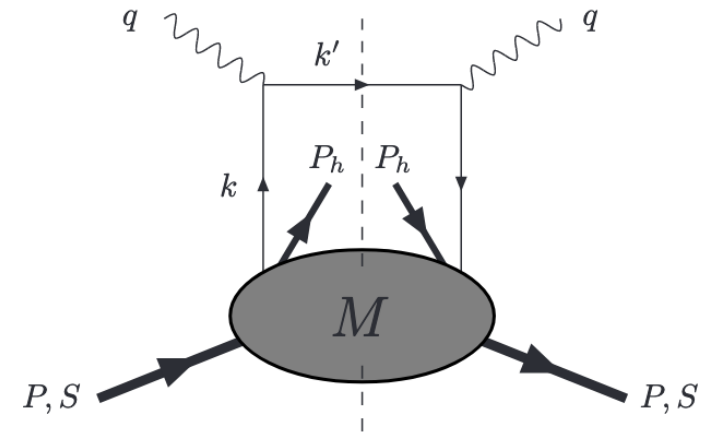
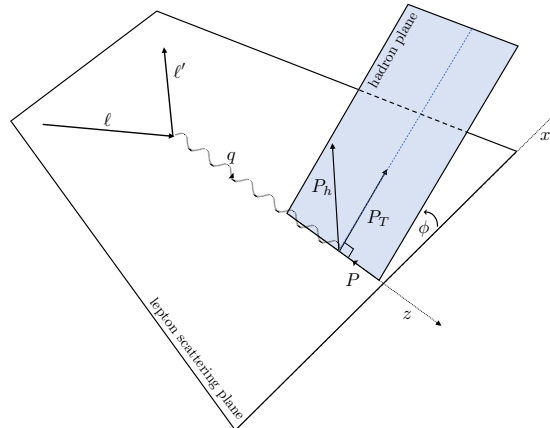
# The Neglected Other Hemisphere – Target Fragmentation

- Final state hadrons also form from the left-over target remnant (TFR) whose partonic structure is defined by “fracture functions”<sup>1,2</sup>: the probability for the target remnant to form a certain hadron given a particular ejected quark.
- In the TFR, factorization into  $x_B$  and  $z$  does not hold because it is not possible to separate quark emission from hadron production. Many ramifications!

$$\frac{d\sigma^{\text{TFR}}}{dx_B dy dz} = \sum_a e_a^2 (1 - x_B) \boxed{M_a(x_B, (1 - x_B)z)} \frac{d\hat{\sigma}}{dy}$$



The spectator partons are interesting too!



M. Anselmino et al., Phys. Lett. B. 706 (2011), 46-52, [hep-ph] 1109.1132

- L. Trentadue and G. Veneziano, Phys. Lett. B323 (1994) 201,
- M. Anselmino et al., Phys. Lett. B. 699 (2011), 108-118, [hep-ph] 1102.4214
- TFR/CFR Fig. from EIC Yellow Report, (2021) [physics.ins-det] 2103.05419

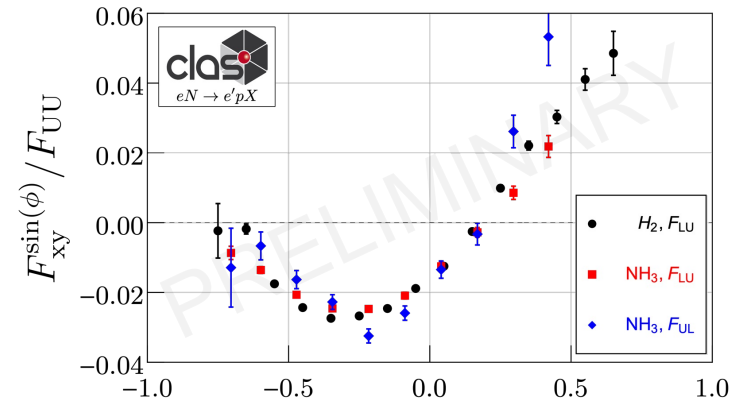
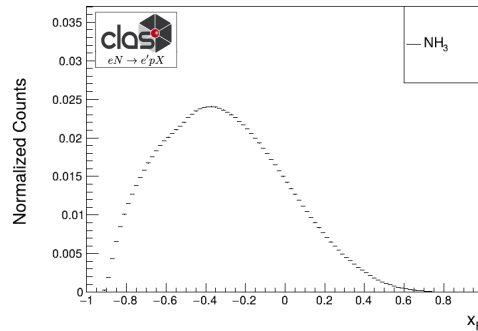
# Separating the Target and Current Regimes

## Feynman variable

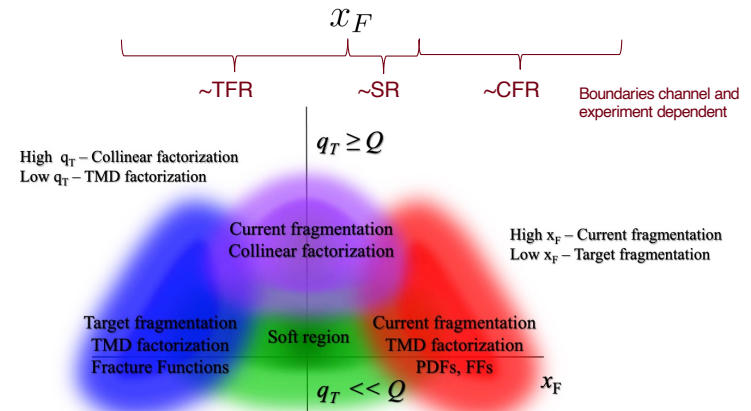
$$x_F = \frac{p_h^z}{p_h^z(\text{max})} \text{ in CM frame } \mathbf{p} = -\mathbf{q},$$

## Rapidity

$$y = \frac{1}{2} \log \frac{p_h^+}{p_h^-} = \frac{1}{2} \log \frac{E_h + p_h^z}{E_h - p_h^z}$$



- No clear *experimental* definition of what constitutes current production versus target production.
- Fixed target SIDIS experiments lack a clear rapidity gap.
- Structure functions, with different production mechanisms in both regions, give a possible clue.
- Odd-function (sine) modulations exhibit a sign flip around the transition from target to current fragmentation.
- The positive(negative) sign of twist-3 SSAs defines the CFR(TFR) dominance.

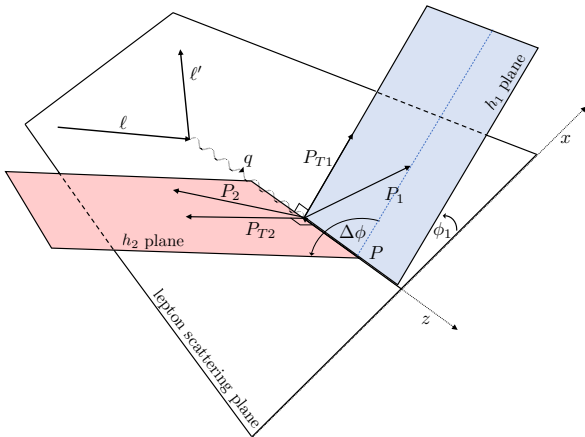


# Back-to-back (dSIDIS) Formalism

- When two hadrons are produced “back-to-back”<sup>1,2</sup> with one in the CFR and one in the TFR the structure function contains a convolution of a **fracture function** and a **fragmentation function**.
- Leading twist beam(target)-spin asymmetry.

		Quark polarization		
		U	L	T
Nucleon polarization	TFR	U	$\hat{u}_1$	$\hat{t}_1^h, \hat{t}_1^\perp$
		L	$\hat{u}_{1L}^\perp$	$\hat{t}_{1L}^h, \hat{t}_{1L}^\perp$
		T	$\hat{u}_{1T}^h, \hat{u}_{1T}^\perp$	$\hat{t}_{1T}^h, \hat{t}_{1T}^\perp$

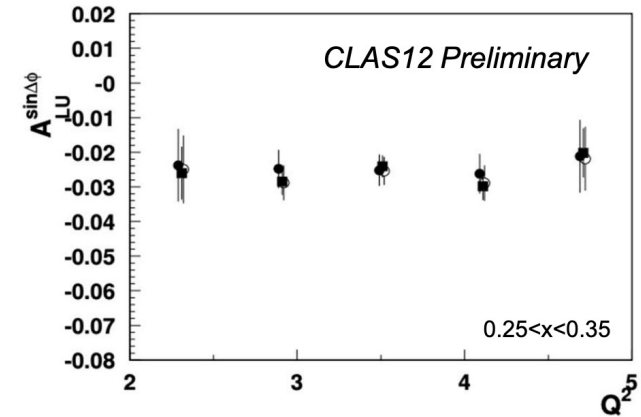
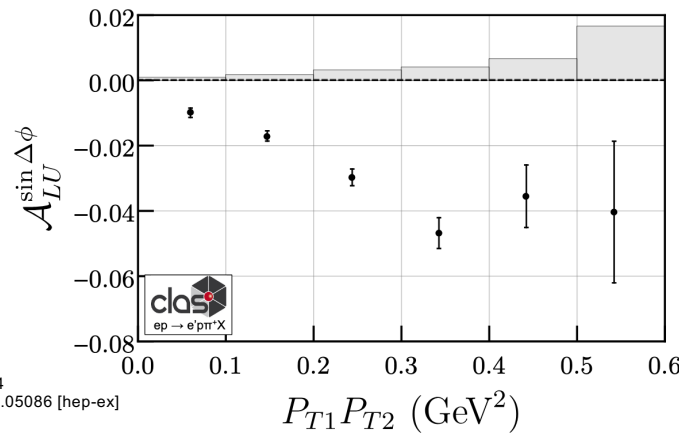
M. Anselmino et al., Phys. Lett. B. 706 (2011), 46-52, [hep-ph] 1109.1132



$$A_{LU} = -k(\epsilon) \frac{P_{T1} P_{T2}}{m_1 m_2} \frac{\mathcal{C} \left[ w_5 \hat{t}_1^{\perp h}(x, \zeta_2, P_{T2}) D_1(z_1, P_{T1}) \right]}{\mathcal{C} \left[ \hat{u}_1(x, \zeta_2, P_{T2}) D_1(z_1, P_{T1}) \right]} \sin(\Delta\phi)$$

Unique access to longitudinally polarized quarks in unpolarized nucleons... no corresponding PDF!  
Reverse situation in target-spin asymmetry (which uniquely has no depolarization, similar to Sivers)

H. Avakian and T.B. Hayward, Phys. Rev. Lett. 130 (2023) 2, 022501, 2208.05086 [hep-ex]

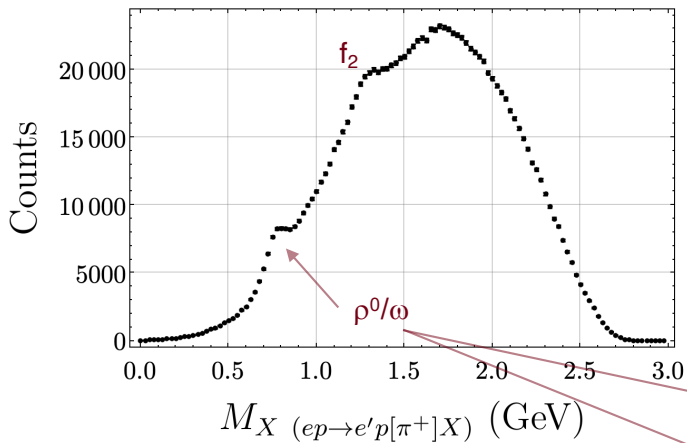


1. M. Anselmino et al., Phys. Lett. B. 706 (2011), 46-52, [hep-ph] 1109.1132  
 2. M. Anselmino et al., Phys. Lett. B. 713 (2012), 317-320, [hep-ph] 1112.2604  
 3. H. Avakian and T.B. Hayward, Phys. Rev. Lett. 130 (2023) 2, 022501, 2208.05086 [hep-ex]



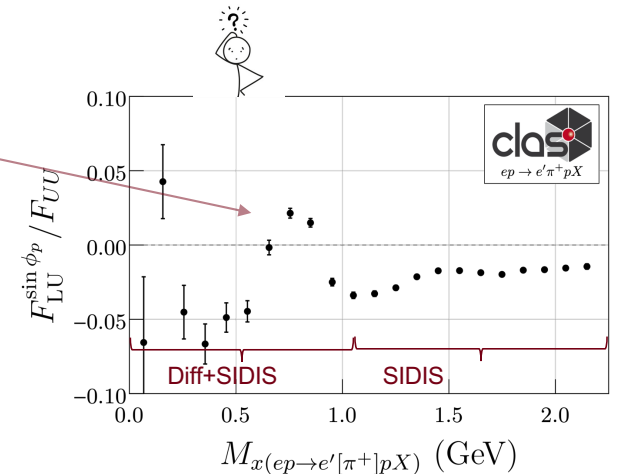
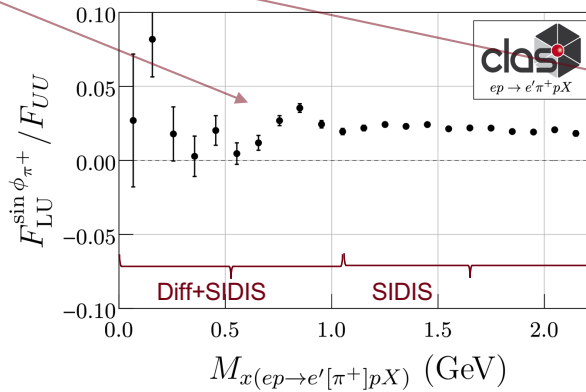
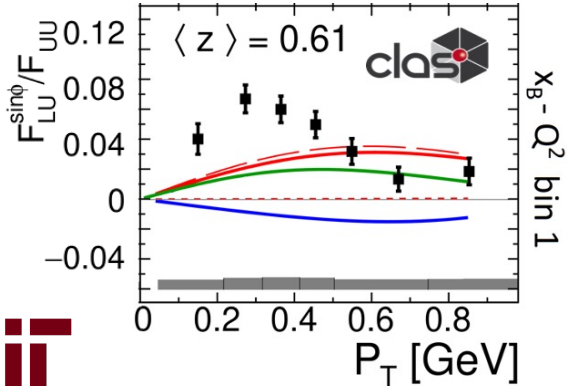


# Semi-exclusive measurements



- The dSIDIS/semi-exclusive measurements with target fragment detected not only allow access to new physics observables but also enables the *explicit* removal of vector meson contributions to the single hadron channels
  - (possible alternative method; *implicit* subtraction via MC c.f. [COMPASS: NPB 956 \(2020\)115039 \[hep:ex\] 1912.10322](#)).
- Earlier observed tendency for  $\pi^+$  results in certain kinematics can easily be explained by contributions of  $\pi^+$  coming from the decay of  $\rho^0$  with higher asymmetries that are not removable in single hadron SIDIS.

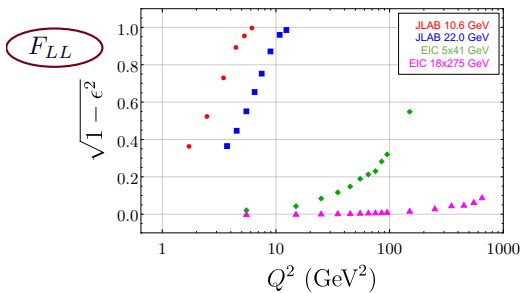
S. Diehl et al., *Phys. Rev. Lett.*, 128, 062005, (2022), [hep:ex] 2101.03544



# Helicity TMD (and the effect from $\rho^0$ )

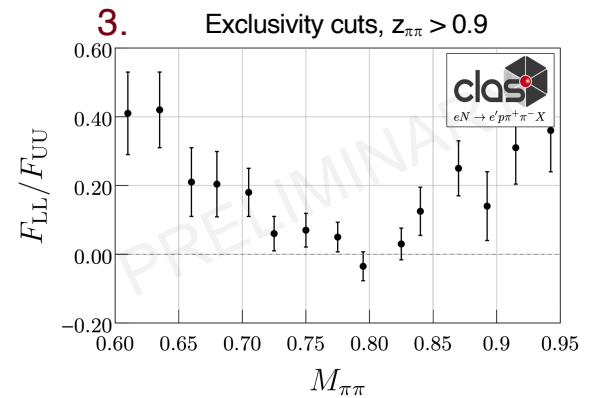
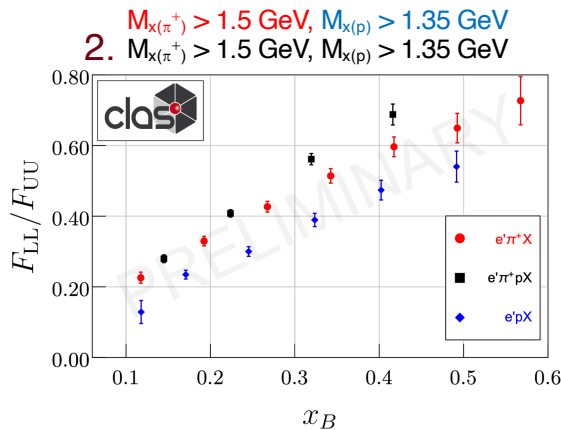
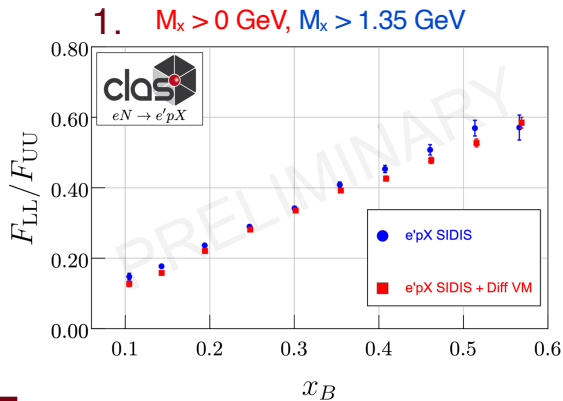
- $g_1(x, k_T)$  will be heavily kinematically suppressed at EIC.
- JLab22, with extension to higher  $P_T$ , would be critical for studies of  $g_1$  in the valance quark region.

$$F_{LL} \propto g_1(x, k_T) \otimes D_1(z, p_T)$$



1. Measurements of epX  $A_{LL}$  systematically higher after  $M_x$  cut to remove VMs
2. Semi-exclusive  $e'\pi^+pX$  with  $\rho$  removed larger than  $e'\pi^+X$  double-spin asymmetries
3. Measurements of  $A_{LL}$  for “diffractive”  $\rho^0$  indicate very small values (probably negative)

Contributions from VM may have caused underestimations of  $g_1$ !



# TFR Single Spin Asymmetries with Polarized NH<sub>3</sub>

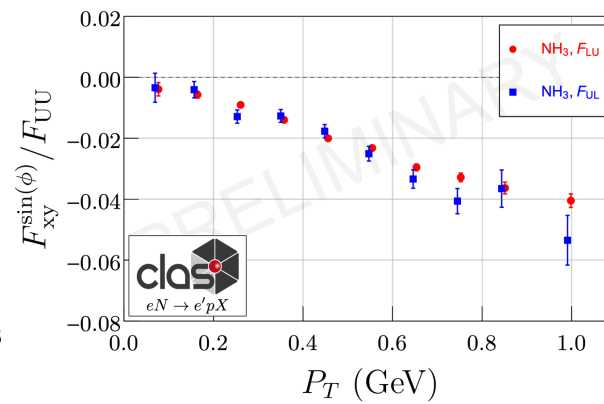
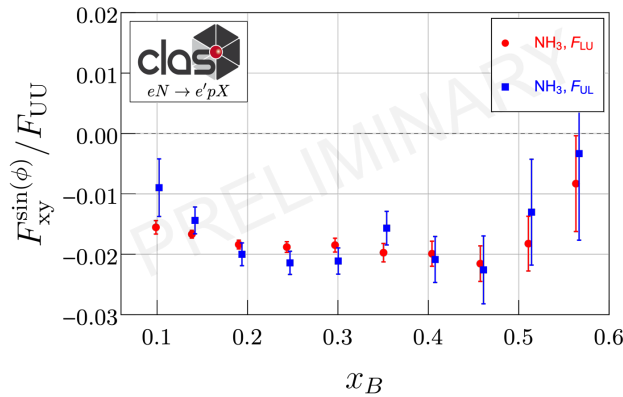
1. epX sample,  $M_X > 1.35$  GeV (“VM free”)
2. Near identical magnitude for  $F_{LU}$  and  $F_{UL}$ .
3. Twist-3 observables; simpler tensor structure in TFR.

$$F_{UL}^{\sin \phi_h} = -\frac{2|\vec{P}_{h\perp}|}{Q} x_B^2 \overset{u_L^h}{\text{unpolarized quarks in a longitudinally polarized proton}}$$

$$F_{LU}^{\sin \phi_h} = \frac{2|\vec{P}_{h\perp}|}{Q} x_B^2 \overset{l^h}{\text{longitudinally polarized quarks in an unpolarized proton}}$$

		Quark polarization	
		U	L
Nucleon polarization	U	$u^h$	$l^h$
	L	$u_L^h$	$l_L^h$

Twist-3 Collinear terms;  
Chen, K. B., Ma, J. P. and Tong, X. B., [hep-ph] 2308.11251



For more theory details on higher-twist FrFs see [talk Tuesday by X. B. Tong](#)

Situation in CFR more complicated

$$F_{LU}^{\sin \phi_h} = \frac{2M}{Q} c \left[ -\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} \left( x e H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{G}^\perp}{z} \right) + \frac{\hat{h} \cdot \mathbf{p}_T}{M} \left( x g^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{E}}{z} \right) \right],$$

$$F_{UL}^{\sin \phi_h} = \frac{2M}{Q} c \left[ -\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} \left( x h_L H_1^\perp + \frac{M_h}{M} g_{1L} \frac{\tilde{G}^\perp}{z} \right) + \frac{\hat{h} \cdot \mathbf{p}_T}{M} \left( x f_L^\perp D_1 - \frac{M_h}{M} h_{1L}^\perp \frac{\tilde{H}}{z} \right) \right]$$

A. Bacchetta et al., JHEP 0702, 093 (2007).

# Summary

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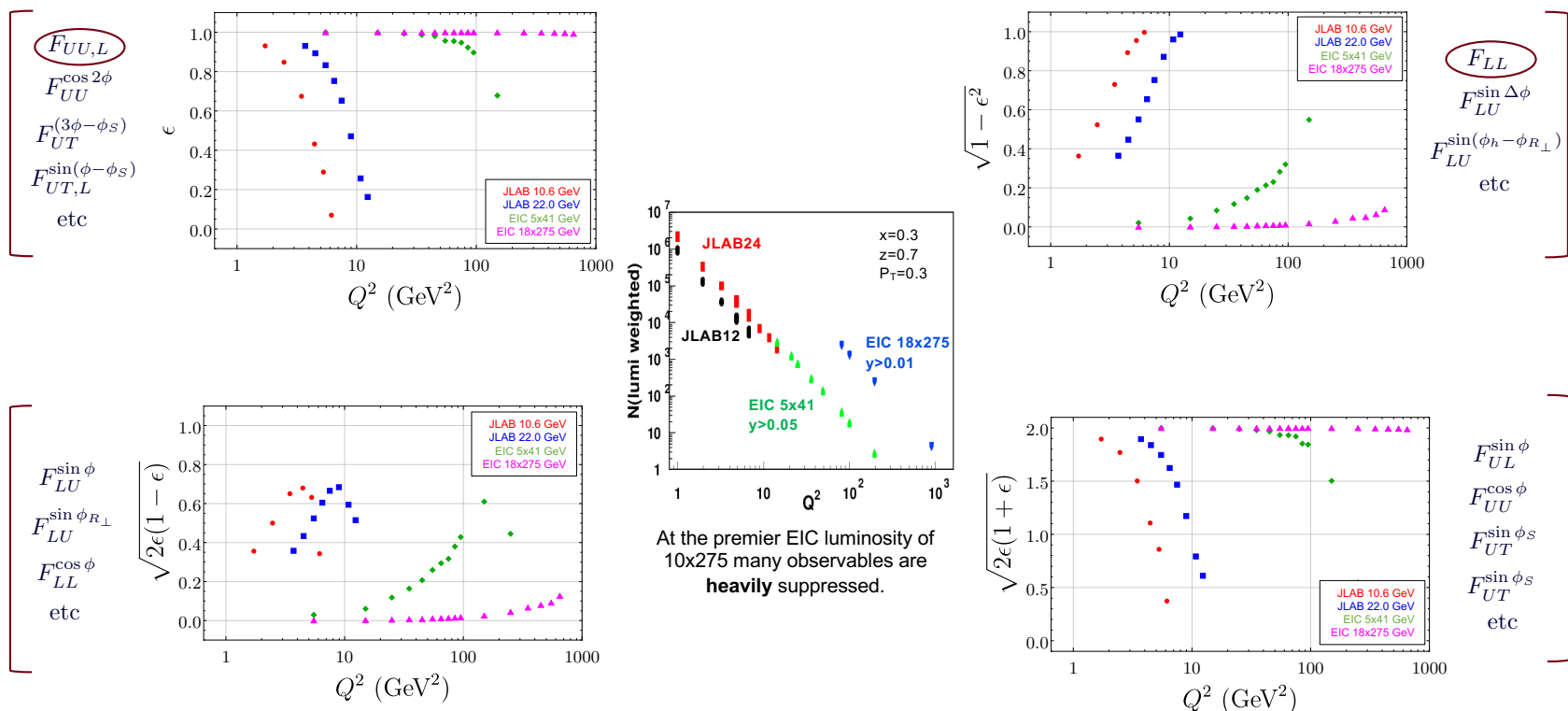
- CLAS12 can provide measurements with many orders of magnitude higher luminosity than previous experiments while also reliably measuring multiparticle final states.
- For interpreting the SIDIS data, it is critical to separate contributions from different structure functions in multidimensional space and also to distinguish between various production mechanisms within a given structure (including VMs).
- Contributions from diffractive VM challenge the factorized picture of SIDIS. Moving towards a “p-free SIDIS” might help address these challenges in phenomenology.
- The detection of target fragment baryons opens new avenues for studying the partonic structure of nucleons both by introducing new observables and by aiding in the separation of VM contributions.
- Many analyses not discussed: dihadrons (collinear and TMD), etc.



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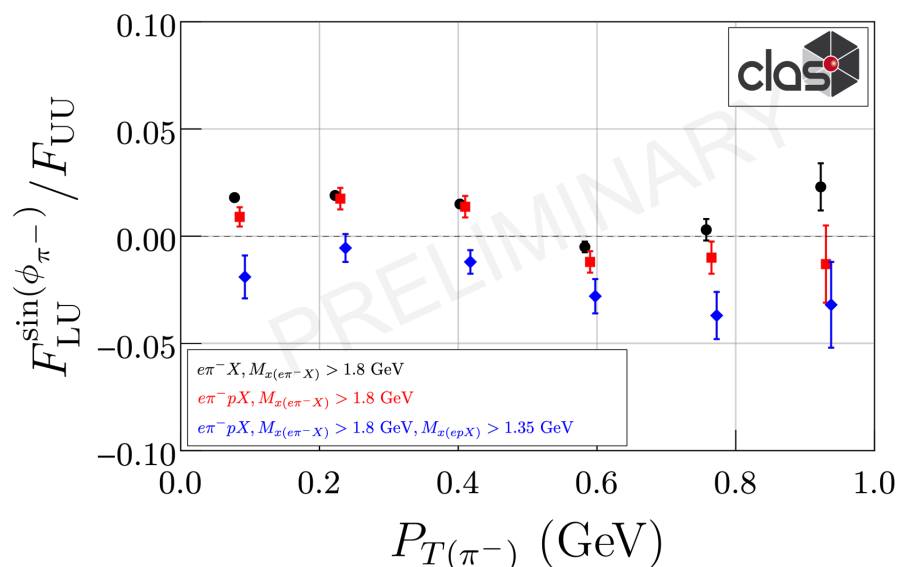
# Back up

# Effects of the Kinematic Factor JLab vs EIC



Access to several key SIDIS/TMD objects will be **extremely** difficult to measure at higher energy experiments, while others will have similar magnitudes across different energies, strengthening their interpretation.

Use sample of  $ep \rightarrow e'p \pi^- X$  and make plots with and without  $M_X$  cut ( $epX$ ) 1.35 GeV



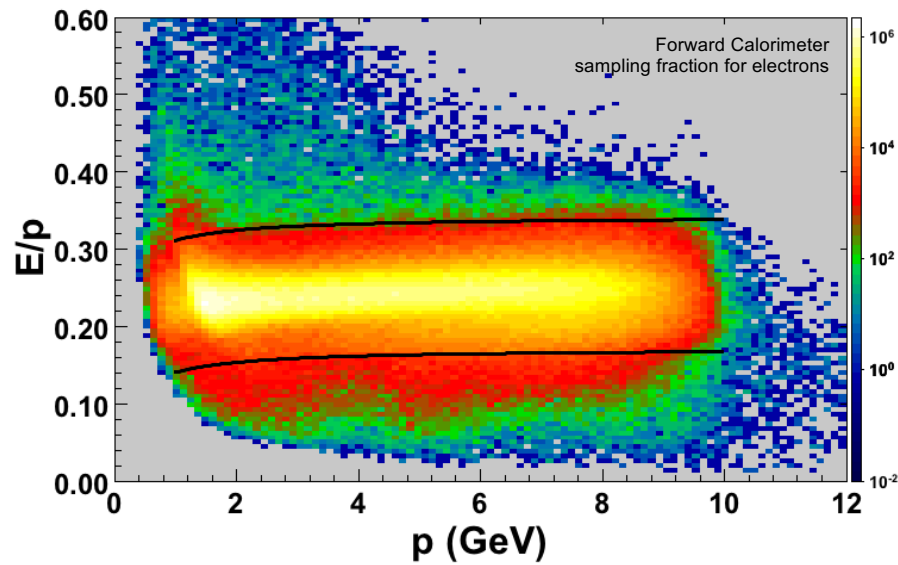
All points include  
 $M_X(e'\pi^- X) > 1.8 \text{ GeV}$   
 $\rightarrow$  out of resonance region

Filled circles with  
 $M_X(epX) > 1.35 \text{ GeV}$  ( $\rho$ -free),  
 significantly different and will  
 impose much less challenge for  
 phenomenology

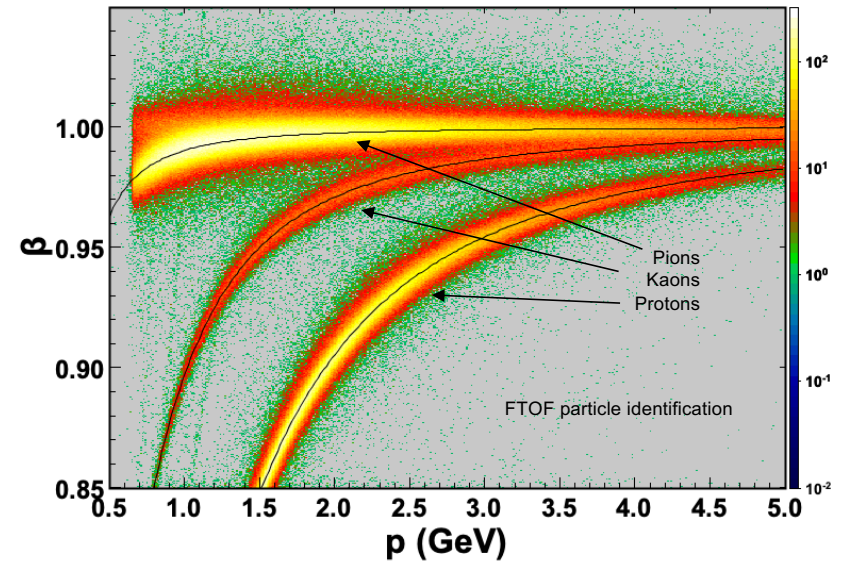
- Exclusive rho-0s have very significant impact on kinematic dependences of SIDIS SSAs, **in particular at low  $P_T$**
- Detection of the target proton introduces much smaller bias on the inclusive SSA, than the exclusive  $\rho$
- The procedure can be validated using direct subtraction of  $\rho$  (like DVCS/ $\pi^0$ )

# Particle Identification

- Electron
  - Electromagnetic calorimeter.
  - Cherenkov detector.



- Hadron
  - $\beta$  vs  $p$  comparison between vertex timing and event start time using forward and central time of flight systems ( $\sim 100$  ps resolution)



# Where is there disagreement?

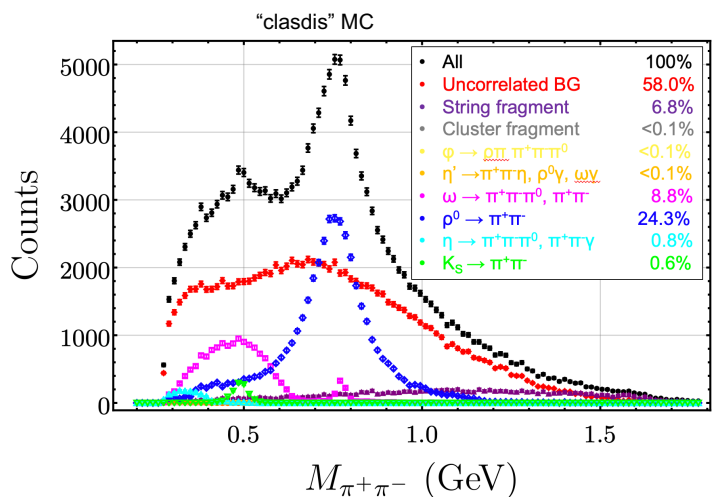
J12-24-RunGroupA

*J12-24-RunGroupA: “11 GeV Polarized Electrons on Liquid Hydrogen Target to Study Proton Structure, 3D Imaging, and Gluonic Excitations”*

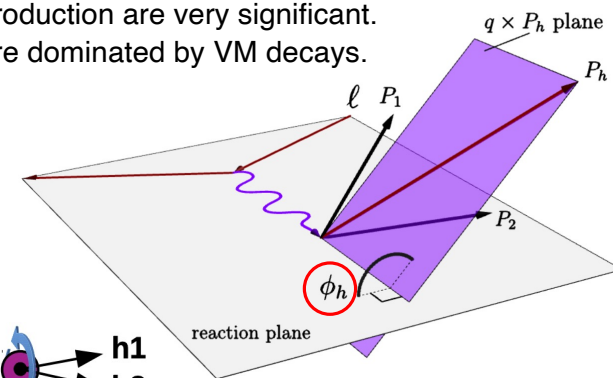
*C. Weiss, N. Sato*

*Semi-inclusive DIS and TMDs:* Phenomenological analysis of JLab 12 GeV SIDIS data has shown that there are basic open questions concerning the semi-inclusive pion/kaon production mechanism at few-GeV energies, regarding e.g. the role of vector meson decays (hadronic interactions),  $L/T$  photon cross sections, and current vs. target fragmentation dynamics. These questions are very interesting and reveal various aspects of nonperturbative dynamics in hadron production. They need to be addressed for a controlled use of the JLab SIDIS data in QCD factorization-based TMD analysis. Measurements of the basic semi-inclusive pion/kaon cross sections and multiplicity distributions will be essential for answering these questions. The analysis of the Run Group data should focus on providing these basic quantities. (Spin asymmetries or other ratio observables are often not sufficient for answering basic questions about the production mechanism, as deviations from theoretical expectations in such observables can result from various effects that cannot be disentangled.) With this focus, the SIDIS results from the Run Group could have a major impact on our understanding of the SIDIS mechanism and transform this field of research.

# TMD Dihadron Fragmentation Functions



- Spin-azimuthal correlations in hadron pair production are very significant.
- Hadron pairs in SIDIS (from JLab to LHC) are dominated by VM decays.

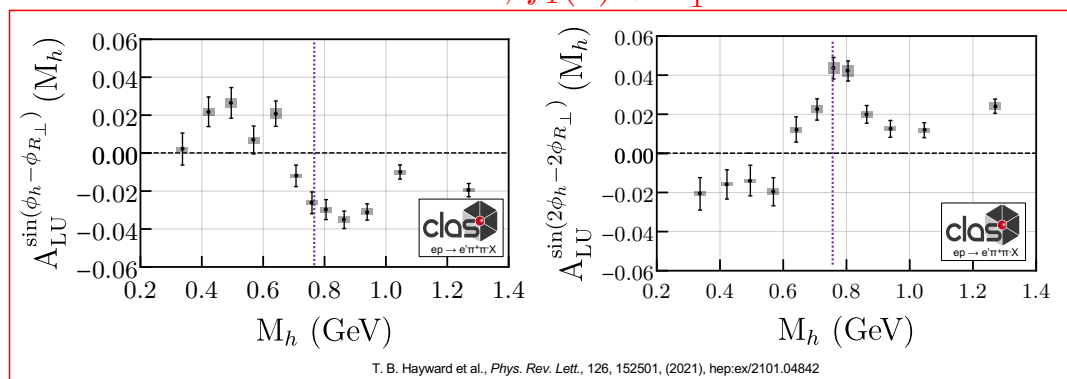


$$G_1 = \text{Diagram 1} - \text{Diagram 2}$$

The diagram shows two circular diagrams representing the fragmentation function  $G_1$ . The first diagram shows a lepton (blue) interacting with a quark (purple) which then fragments into two hadrons,  $h_1$  and  $h_2$ . The second diagram is similar but with different spin orientations for the quark and hadrons.

Twist 2,  $f_1(x) \otimes G_1^{\perp|\ell,m\rangle}$

- Dihadron studies allow for the existence of FFs with no single hadron analog.
- $G_1^\perp$  describes the azimuthal dependence of an unpolarized hadron pair on the helicity of the struck quark.
- **First ever observation.**

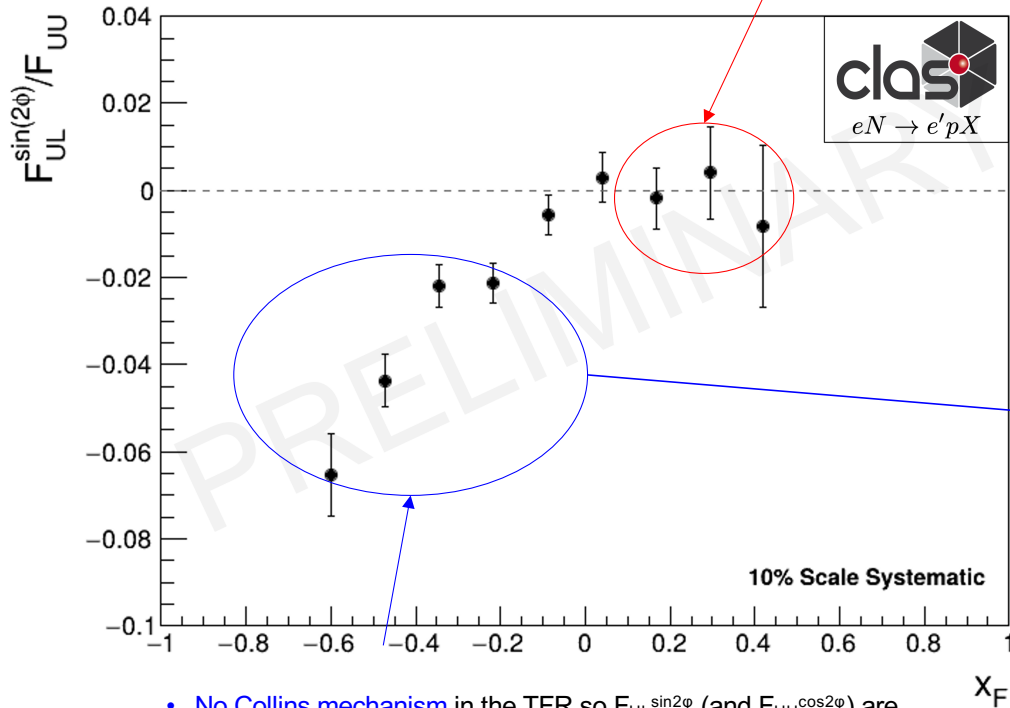


T. B. Hayward et al., Phys. Rev. Lett., 126, 152501, (2021), hep:ex/2101.04842

# Kotzinian-Mulders (Worm-gear L)

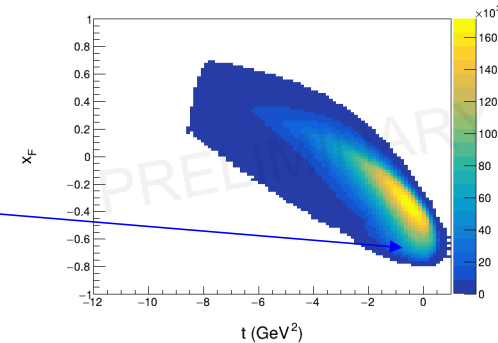
$$F_{UL}^{\sin 2\phi_h} = C \left[ -\frac{2(\hat{h} \cdot \mathbf{k}_T)(\hat{h} \cdot \mathbf{p}_T) - \mathbf{k}_T \cdot \mathbf{p}_T}{MM_h} h_{1L}^\perp H_1^\perp \right]$$

A. Bacchetta et al., JHEP 02 (2007) 093 [hep-ph] 0611265



- No Collins mechanism in the TFR so  $F_{UL}^{\sin 2\phi}$  (and  $F_{UU}^{\cos 2\phi}$ ) are  $\geq$  twist-4. We would expect small magnitude at  $-x_F$ .... and yet.

- The  $F_{UL}^{\sin 2\phi}$  asymmetry is theoretically purely generated by the **Collins mechanism** (also  $\cos 2\phi$ )
- Hadronization in the TFR is more isotropic – there is no additional chiral-odd quantity like the **Collins function** to pair with the **Kotzinian-Mulders TMD** because factorization into separate soft and hard scale processes does not hold.



- Are effects at large negative  $x_F$  that disagree with predictions the result of low  $t$  events where theory may break down (**even** with  $M_x$  cut above  $\rho$ )?
- CFR consistent with zero (in agreement with COMPASS and HERMES)

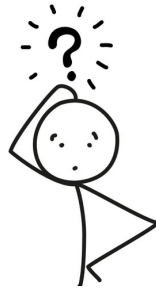


# Potential Ambiguities

$$\frac{d\sigma^{\text{TFR}}}{dx_B dy d\zeta d^2\mathbf{P}_{h\perp} d\phi_S} = \frac{2\alpha_{\text{em}}^2}{Q^2 y} \left\{ \left(1 - y + \frac{y^2}{2}\right) \times \sum_a e_a^2 \left[ M(x_B, \zeta, \mathbf{P}_{h\perp}^2) - |\mathbf{S}_\perp| \frac{|\mathbf{P}_{h\perp}|}{m_h} M_T^h(x_B, \zeta, \mathbf{P}_{h\perp}^2) \sin(\phi_h - \phi_S) \right] + \lambda_l y \left(1 - \frac{y}{2}\right) \sum_a e_a^2 \left[ S_{\parallel} \Delta M_L(x_B, \zeta, \mathbf{P}_{h\perp}^2) \hat{u}_{1T}^\perp + |\mathbf{S}_\perp| \frac{|\mathbf{P}_{h\perp}|}{m_h} \Delta M_T^h(x_B, \zeta, \mathbf{P}_{h\perp}^2) \cos(\phi_h - \phi_S) \right] \right\}.$$

M. Anselmino et al., Phys. Lett. B. 699 (2011), 108-118, [hep-ph] 1102.4214

The same azimuthal asymmetries can appear in both the CFR and TFR complicating their interpretation...



Sivers-like modulation!

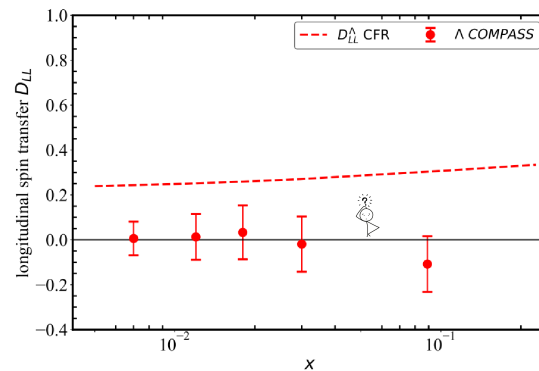
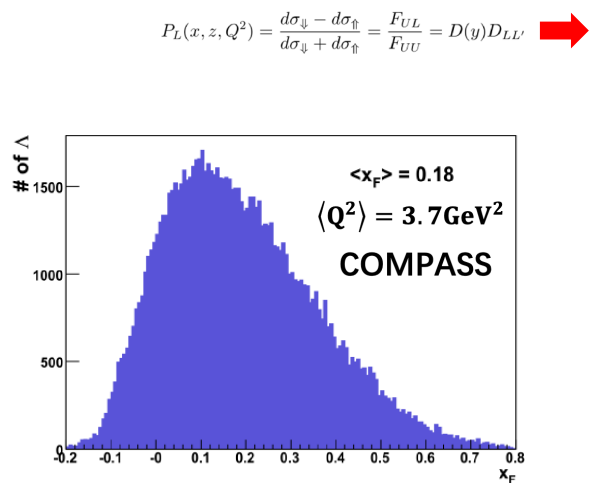
$$\begin{aligned} [F_{UT,T}^{\sin(\phi_h - \phi_S)}]_{\text{TFR}} &= - \sum_a e_a^2 x_B \frac{|\mathbf{P}_{h\perp}|}{m_h} M_T^h(x_B, \zeta, \mathbf{P}_{h\perp}^2) \\ [F_{UT,T}^{\sin(\phi_h - \phi_S)}]_{\text{CFR}} &= \mathcal{C} \left[ - \frac{\hat{\mathbf{h}} \cdot \mathbf{k}_\perp}{m_N} f_{1T}^\perp D_1 \right] \end{aligned}$$

$$\begin{aligned} [F_{LT}^{\cos(\phi_h - \phi_S)}]_{\text{TFR}} &= \sum_a e_a^2 x_B \frac{|\mathbf{P}_{h\perp}|}{m_h} \Delta M_T^h(x_B, \zeta, \mathbf{P}_{h\perp}^2) \\ [F_{LT}^{\cos(\phi_h - \phi_S)}]_{\text{CFR}} &= \mathcal{C} \left[ \frac{\hat{\mathbf{h}} \cdot \mathbf{k}_\perp}{m_N} g_{1T} D_1 \right] \end{aligned}$$

... while some asymmetries uniquely appear in a single kinematic region, strengthening their interpretation.

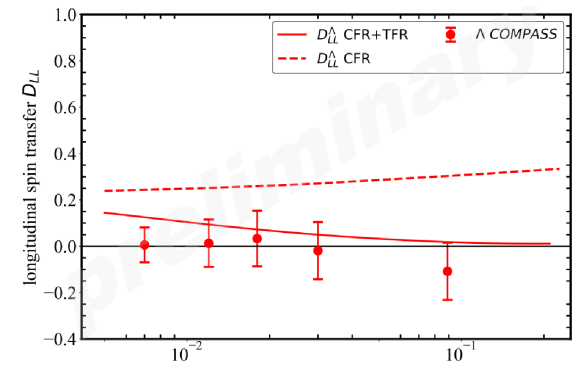
# Potential Ambiguities; An Example

- The self analyzing  $\Lambda$ -baryon decay allows for the targeted extraction of information on polarization transfer from struck quark to produced hadrons.
- The spin-transfer coefficient,  $D_{LL}$ , serves as a stringent test for QCD (Quantum Chromodynamics) predictions, especially those involving polarized parton distributions and fragmentation functions.



$$D_{LL'} = \frac{\sum_a e_a^2 f_a(x, Q^2) G_a(z, Q^2)}{\sum_a e_a^2 f_a(x, Q^2) D_a(z, Q^2)} \omega_q(z_\Lambda, P_{h\perp})$$

COMPASS data from Eur. Phys. J. C64, 171-179 (2009)  
 CFR+TFR analysis by X. Zhao, T. Liu, Y. Zhou, [SPIN-2023](#)

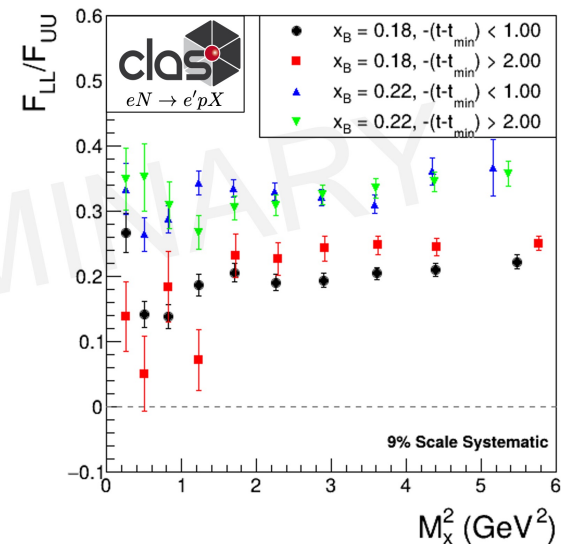
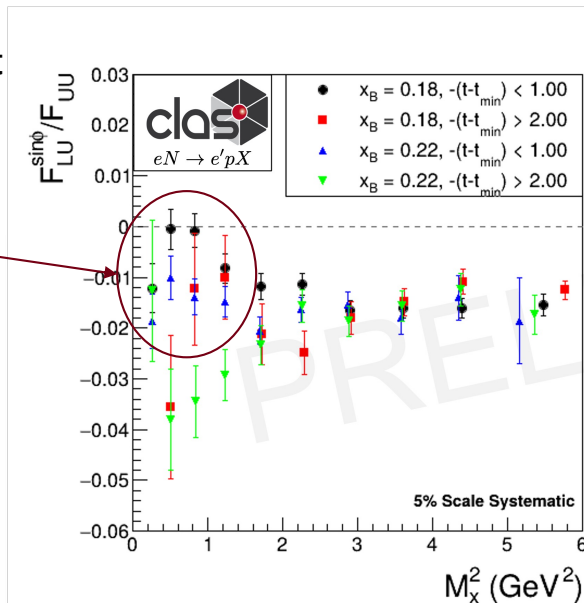
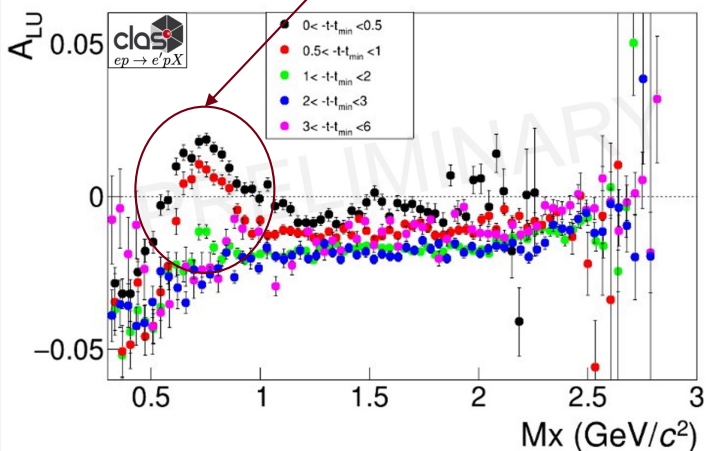


$$D_{LL}^\Lambda(x, z, Q^2) = \frac{\sum_q e_q^2 z^2 f_{1q}(x_B, Q^2) G_{1Lq}^\Lambda(z_\Lambda, Q^2)}{\sum_q e_q^2 [z^2 f_{1q}(x_B, Q^2) D_{1q}^\Lambda(z_\Lambda, Q^2) + \frac{\zeta}{z} M_q^\Lambda(x_B, \zeta, Q^2)]}$$

Target fragmentation contribution!

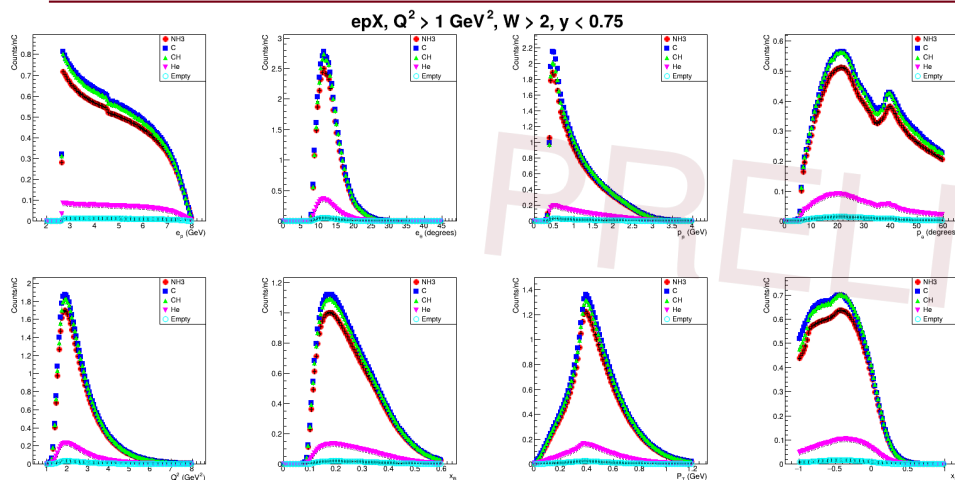
# Constructing $\rho^0$ free SIDIS

Clear indications of the contributions of  $\rho$  in epX SIDIS for SSAs with the largest contributions coming at low values of  $t$  where diffractive/GPD physics dominates.



- When appropriately binned in  $x_B$ , to account for  $F_{LL}(x_B)$  dependence, similar evidence exists of a drop off at low missing masses in the double spin asymmetry.
- Appropriate accounting of  $\rho$  contributions critical for extraction of the helicity dependence.

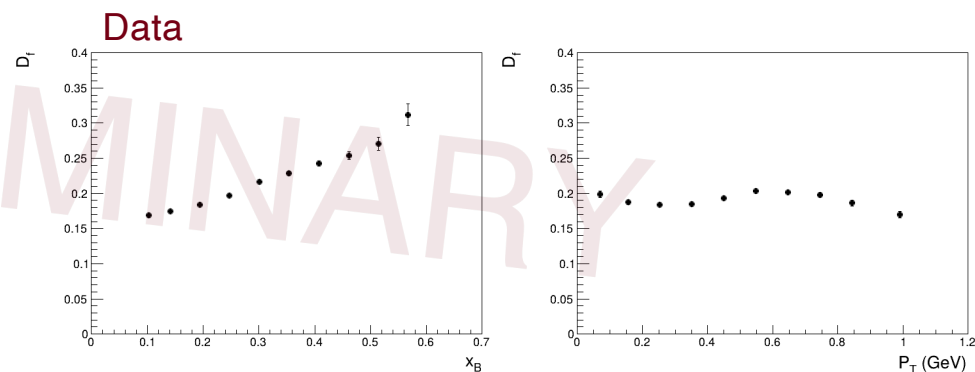
# Dilution Factor Results



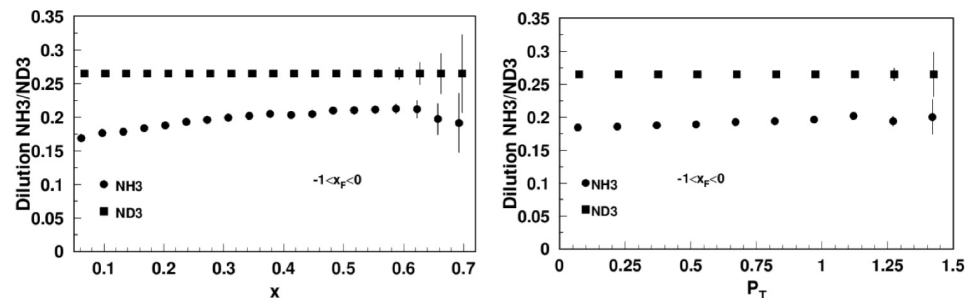
Contributions per nC for five target types

Target	Accumulated Charge (nC)	Fraction of Total Charge
NH <sub>3</sub>	3732256.069	0.720
C	424018.352	0.082
CH <sub>2</sub>	181775.304	0.035
Helium Bath	380446.688	0.073
Empty Target	462880.790	0.089

Integrated dilution factor:  $0.1815 \pm 0.0006$



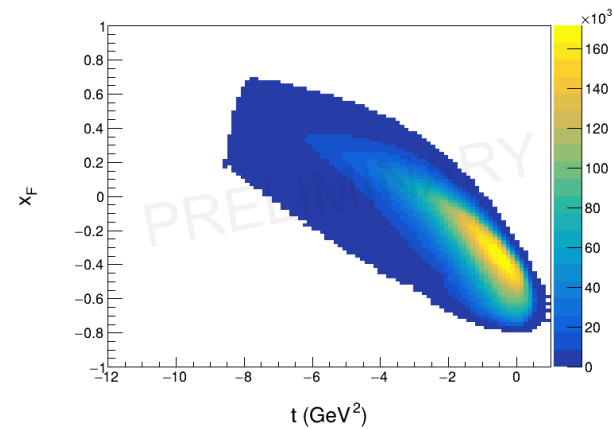
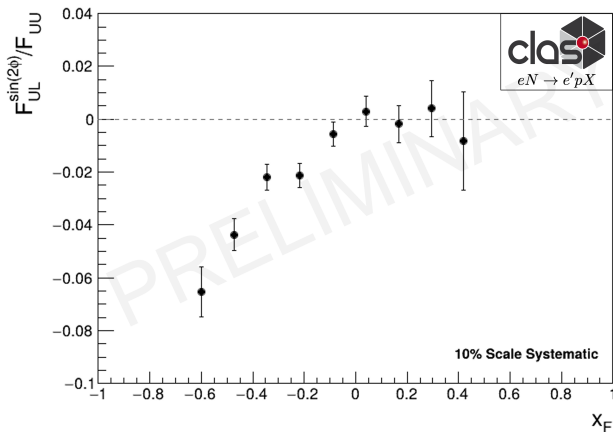
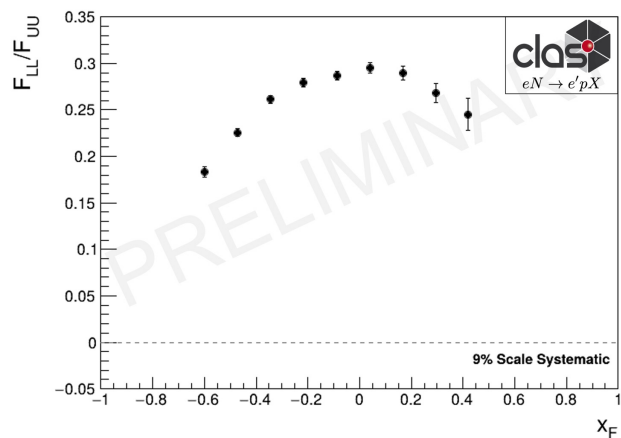
MC (10:7 P:N ratio constructed)



Results qualitatively in agreement with clasdis MC (no nuclear effects)



# Large negative $x_F$



# Categorizing Fracture Functions

- At leading twist fracture functions exist that can be organized into tables of quark and nucleon polarizations just like the more familiar PDFs.
- Access to *both*  $k_T$  and  $p_T$  effects gives  $2 \times 8 = 16$  FrFs.

		Quark polarization		
		U	L	T
Nucleon polarization	U	$f_1$		$h_1^\perp$
	L		$g_{1L}$	$h_{1L}^\perp$
	T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

$\xleftarrow{\text{CFR}} \quad \xrightarrow{\text{TFR}}$

		Quark polarization		
		U	L	T
Nucleon polarization	U	$\hat{u}_1$	$\hat{l}_1^{\perp h}$	$\hat{t}_1^h, \hat{t}_1^\perp$
	L	$\hat{u}_{1L}^{\perp h}$	$\hat{l}_{1L}$	$\hat{t}_{1L}^h, \hat{t}_{1L}^\perp$
	T	$\hat{u}_{1T}^h, \hat{u}_{1T}^\perp$	$\hat{l}_{1T}^h, \hat{l}_{1T}^\perp$	$\hat{t}_{1T}^h, \hat{t}_{1T}^{\perp h}$ $\hat{t}_{1T}^{\perp \perp}, \hat{t}_{1T}^{\perp h}$

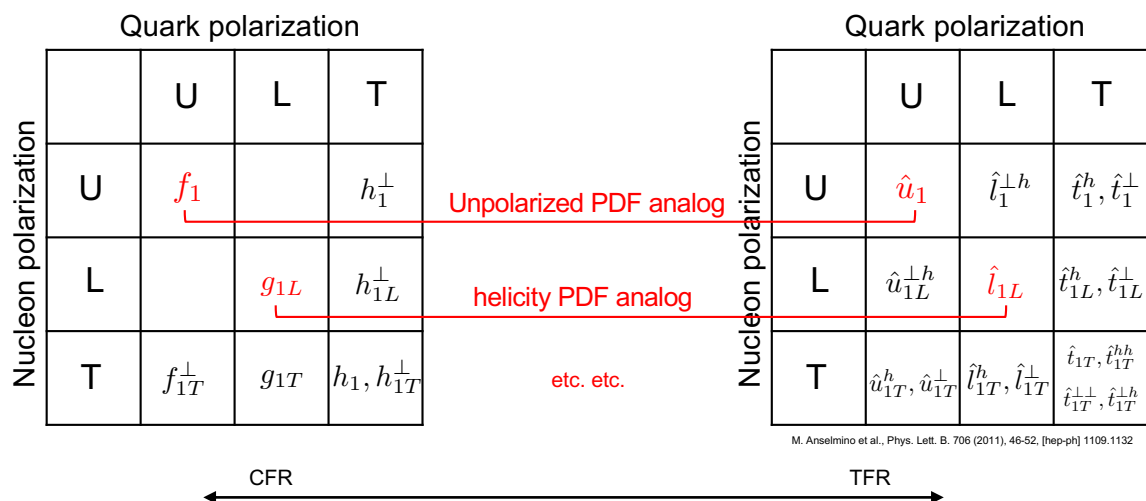
M. Anselmino et al., Phys. Lett. B. 706 (2011), 46-52, [hep-ph] 1109.1132

# Analog to PDFs; Momentum Sum Rules

- A direct relationship exists to the eight leading twist PDFs after the fracture functions are integrated over the fractional longitudinal nucleon momentum,  $\zeta$ .

$$\sum_h \int_0^{1-x} d\zeta \zeta M_a(x, \zeta) = (1-x) f_a(x)$$

M. Anselmino et al., Phys. Lett. B. 699 (2011), 108, [hep-ph] 1102.4214



M. Anselmino et al., Phys. Lett. B. 706 (2011), 46-52, [hep-ph] 1109.1132



# Single hadron limitations

- FrFs describing transversely polarized quarks are chiral odd and inaccessible in TFR single hadron production where there is no access to a chiral odd FF.
- Functions with double superscripts containing h and  $\perp$  have give the unique possibility of measuring longitudinal polarized quarks in unpolarized nucleons (and vice versa) but disappear after integration over either momentum.

		Quark polarization		
		U	L	T
Nucleon polarization	U	$f_1$		$h_1^\perp$
	L		$g_{1L}$	$h_{1L}^\perp$
	T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

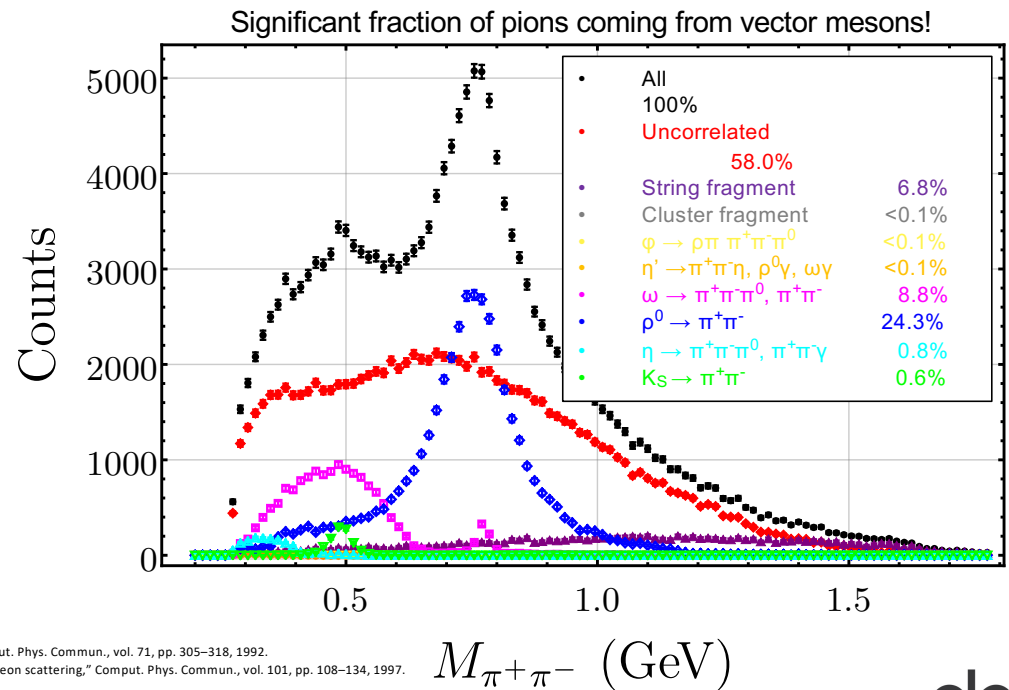
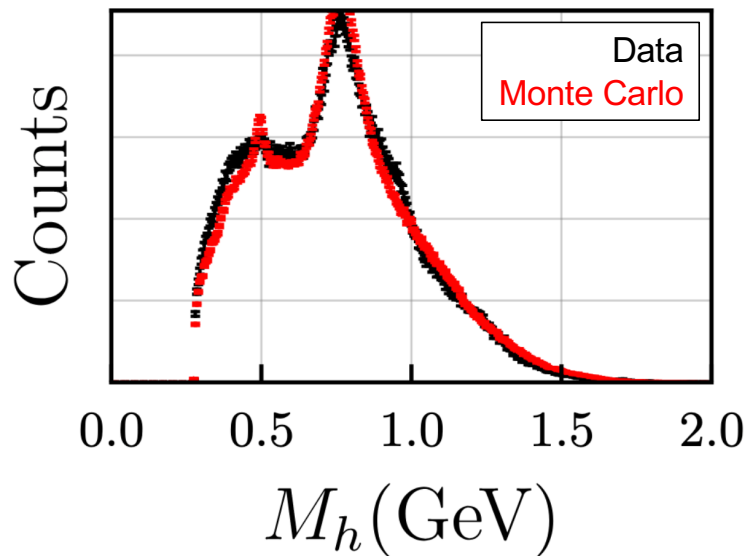
CFR  $\longleftrightarrow$  TFR

		Quark polarization		
		U	L	T
Nucleon polarization	U	$\hat{u}_1$	$\hat{l}_1^{\perp h}$	$\hat{t}_1^h, \hat{t}_1^\perp$
	L	$\hat{u}_{1L}^{\perp h}$	$\hat{l}_{1L}$	$\hat{t}_{1L}^h, \hat{t}_{1L}^\perp$
	T	$\hat{u}_{1T}^h, \hat{u}_{1T}^\perp$	$\hat{l}_{1T}^h, \hat{l}_{1T}^\perp$	$\hat{t}_{1T}^h, \hat{t}_{1T}^{\perp h}$ $\hat{t}_{1T}^{\perp\perp}, \hat{t}_{1T}^{\perp h}$

M. Anselmino et al., Phys. Lett. B. 706 (2011), 46-52, [hep-ph] 1109.1132

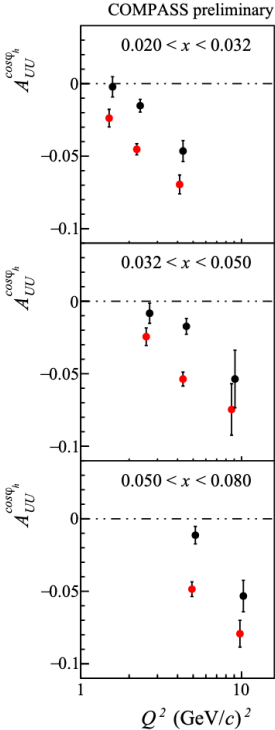
# Monte Carlo and Vector Mesons

- SIDIS MC “clasdis”<sup>1</sup> based on PEPSI<sup>2</sup> generator, the polarized version of the well-known LEPTO<sup>3</sup> generator.
- Parameters changed to reproduce observed distributions include average transverse momentum, fraction of spin-1 light mesons and fraction of spin-1 strange mesons.
- CLAS12 detector system described in “GEMC”<sup>4</sup>, a detailed GEANT4 simulation package.



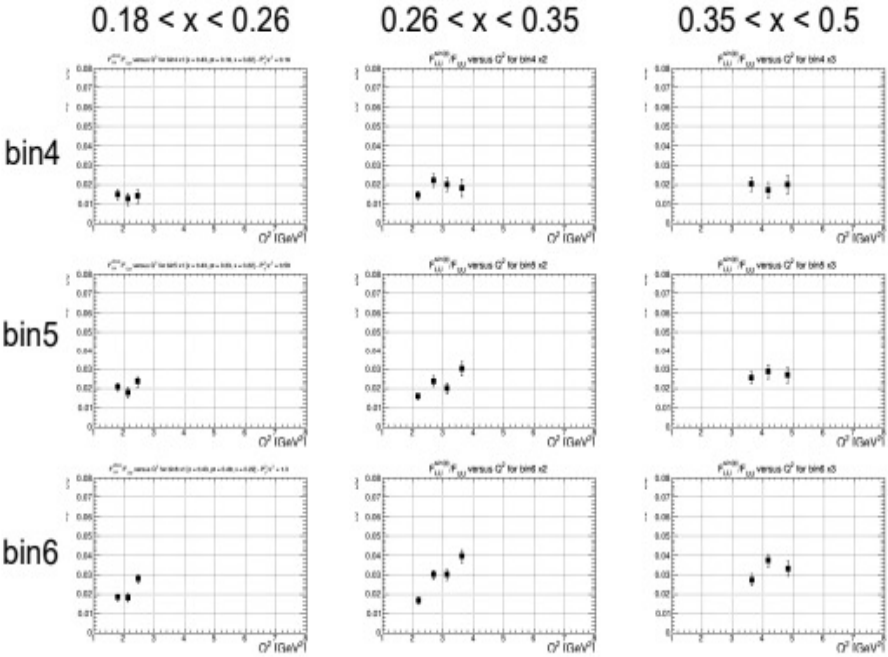
1. H. Avakian, “clasdis,” <https://github.com/JeffersonLab/clasdis>, 2020.
2. L. Mankiewicz, A. Schafer, and M. Veltri, “Pepsi: A monte carlo generator for polarized leptoproduction,” *Comput. Phys. Commun.*, vol. 71, pp. 305–318, 1992.
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# Q<sup>2</sup> measurements



[A. Moretti, Proc. of DIS 2021]

## CLAS12 $\pi^+$ $F_{LU}$





# $\pi^+$ double spin asymmetry

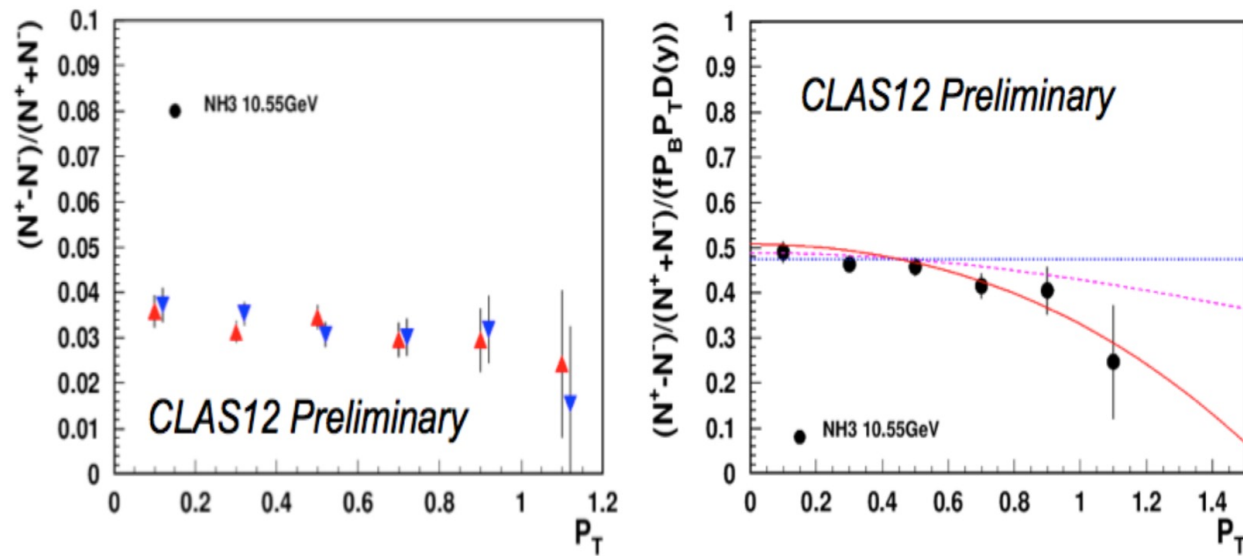
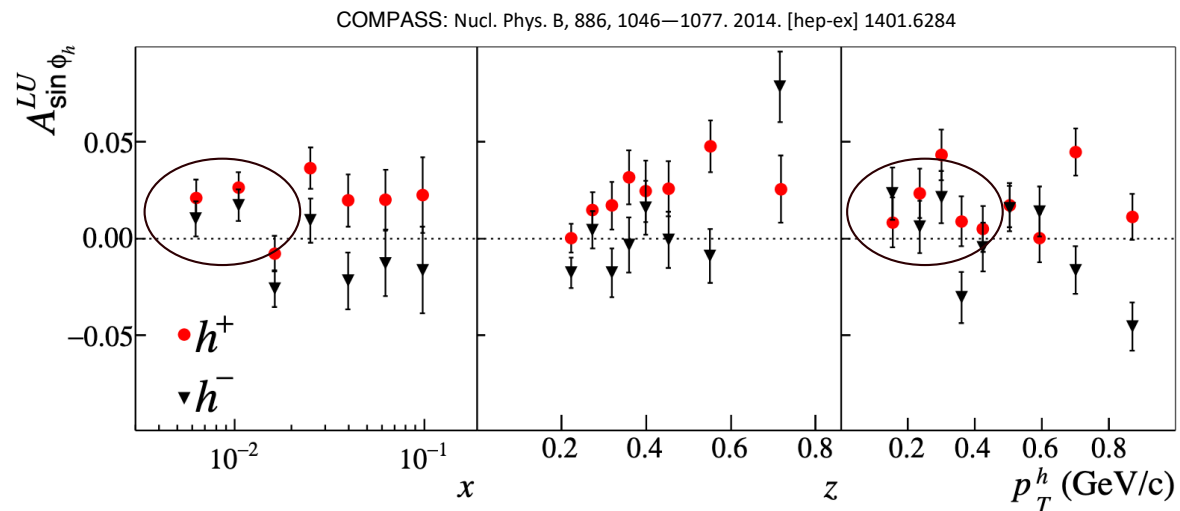


Figure 11: The  $P_T$ -dependence of the raw asymmetry in a bin in (left) and the double spin asymmetry corrected for polarization, dilution, and depolarization factors (right). Dotted line is for the equal widths of  $f_1(x, k_T)$ , dashed magenta line for 10% difference in Gaussian widths, and the red curve corresponds to widths predicted by lattice [Mus05] (see APPENDIX:A)

# COMPASS LiD BSAs



**Fig. 9:**  $A_{\sin \phi_h}^{LU}$  integrated asymmetries for positive (red points) and negative (black triangles) hadrons as functions of  $x$ ,  $z$  and  $p_T^h$ . The error bars show statistical uncertainties only.

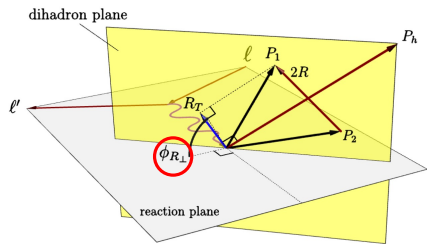
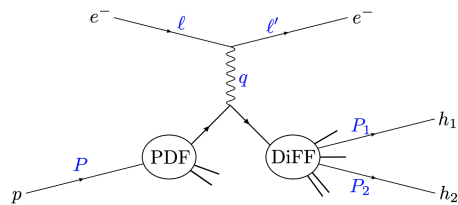
Low  $x$  (low  $Q^2$ ), high  $z$ , or low  $P_T$  show evidence of possible  $\rho^0$  contributions

# Collinear Dihadron Production

$$F_{LU}^{\sin \phi_{R\perp}} = -x \frac{\vec{R} \sin \theta}{Q} \left[ \frac{M}{M_h} x e^q(x) \underbrace{H_1^{\triangleleft q}(z, \cos \theta, M_h)}_{\text{twist-3 pdf}} + \frac{1}{z} \underbrace{f_1^q(x)}_{\text{unpolarized pdf}} \underbrace{\tilde{G}(z, \cos \theta, M_h)}_{\text{twist-3 FF}} \right]$$

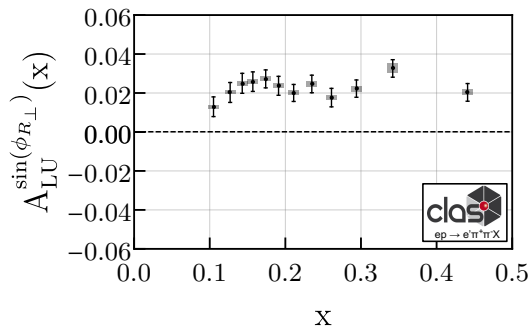
“Interference Fragmentation Function”

A. Bacchetta and M. Radici, *Phys. Rev. D.*, 67, 094002, (2003), hep.ex/021300

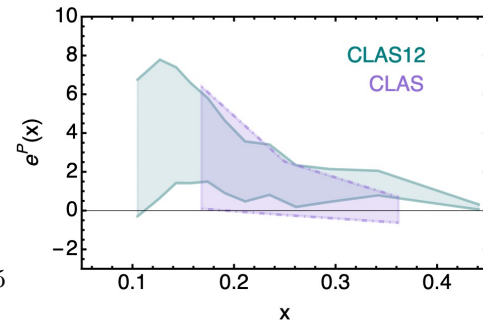


First measurement of dihadron  $A_{LU}$ , first extraction of  $e(x)$

- IFF measured at Belle combined with  $F_{LU}$  from CLAS12
- Twist-3 PDF (quark gluon correlations)
- Related to quark contributions to nucleon mass
- $\perp$  force on  $\perp$  polarized quarks in a unpolarized nucleon (similar to Boer-Mulders)



T. B. Hayward et al., *Phys. Rev. Lett.*, 126, 152501, (2021), [hep.ex] 2101.04842



A. Courtoy et al., *Phys. Rev. D.*, 106, 014027, (2022), [hep.ph] 2203.14975