Light-front distributions of the polarized deuteron

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in collaboration with Ch. Weiss 1906.11119,2006.03033, in preparation JLab LDRD project on EIC spectator tagging 1409.5768,1601.06665 Builds on Frankfurt, Kondratyuk, Strikman,...80s+





Deuteron

- Simplest non-trivial nucleus: bound *pn* system → loosely bound, 2.2 MeV binding energy
- Spin 1
 - \rightarrow 5 additional tensor polarizations
- Ab initio wave functions available → radial S and D wave
- Physics interest
 - ► Neutron structure, flavor decomposition → free neutron?
 - ► Short-range *NN* interaction
 - ► Influence of nuclear interactions on partonic properties → which nuclear configurations
 - Tomography of bound nuclear states, bound nucleon \rightarrow coherent, incoherent exclusive reactions
 - Non-nucleonic configurations
 - $\rightarrow \Delta\Delta$ components



Deuteron Spectator tagging



- Detection of nucleon in target fragmentation region: "spectator"
- Interaction w photon can be elastic, DIS, hard exclusive, SIDIS, etc.
 - Control over your initial nuclear state → Active nucleon identified, create effective targets
- Spectator can reinteract with other final-state hadrons
 - \rightarrow "Simple" for deuteron
- Spectator kinematics gives handle on initial state → On-shell extrapolation for free nucleon
 - \rightarrow Larger momenta for medium modifications

 Measurements with fixed target [BONuS, Deeps, LAD, BAND, Alert,..] and collider [EIC] with large acceptance far forward detectors

Tagged DIS: Theoretical Formalism

- General expression of SIDIS for a polarized spin 1 target
 - ► Tagged spectator DIS is SIDIS in the target fragmentation region

$$\vec{e} + \vec{T}
ightarrow e' + X + h$$

- 41 (18 + 23) structure functions
- Light-front structure of the deuteron
 - Natural for high-energy reactions as off-shellness of nucleons in LF quantization remains finite
- Dynamical model to express structure functions of the reaction
 - First step: impulse approximation (IA) model
 - ▶ Results for all SF: deuteron LF distributions × nucleon collinear pdfs
 - FSI corrections

High-energy scattering with nuclei [Frankfurt, Strikman 80s+]





- Virtual photon probes nucleus at fixed lightcone time $x^+ = x^0 + x^3$
- Scales can be separated using methods of light-front quantization and QCD factorization
- Tools for high-energy scattering known from ep
- Nuclear input: light-front momentum densities, spectral functions, overlaps with specific final states in breakup/tagging reactions
 - framework known for deuteron, can be extended to ³He but challenges
 - ► still **low-energy** nuclear physics, just formulated differently

Deuteron light-front wave function

Up to momenta of a few 100 MeV: dominated by *NN*

Can be evaluated in LFQM [Berestetsky, Frankfurt, Strikman, Terentev]

Overlap with on-shell free two-nucleon state

Schrödinger (non-rel) like eq. for the wf components, rotational invariance recovered

$$\Psi_{\lambda}(\boldsymbol{k},\lambda_{\boldsymbol{p}},\lambda_{\boldsymbol{n}}) = \sqrt{E_{\boldsymbol{k}}} \sum_{\lambda_{\boldsymbol{p}}^{\prime} \lambda_{\boldsymbol{n}}^{\prime}} \mathcal{D}_{\lambda_{\boldsymbol{p}} \lambda_{\boldsymbol{p}}^{\prime}}^{\frac{1}{2}} [R_{fc}(k_{1}^{\mu}/m)] \mathcal{D}_{\lambda_{\boldsymbol{n}} \lambda_{\boldsymbol{n}}^{\prime}}^{\frac{1}{2}} [R_{fc}(k_{2}^{\mu}/m)] \Phi_{\lambda}(\boldsymbol{k},\lambda_{\boldsymbol{p}}^{\prime},\lambda_{\boldsymbol{n}}^{\prime})$$

Differences with non-rel wave function:

- Melosh rotations to account for light-front spin
- k is the rel. 3-momentum in the rest frame of the on-shell NN state



Allows for the definition of nucleon LF momentum distributions \sim nucleon TMDs in deuteron

Helicity independent Helicity dependent Transversity

$$\begin{array}{ll} P_{[U]}(\alpha_{P}, \boldsymbol{p}_{P}\tau|_{U,S_{d},T_{d}}) & \gamma^{+} \\ P_{[S_{L}]}(\alpha_{P}, \boldsymbol{p}_{P}\tau|_{(U,S_{d},T_{d}}) & \gamma^{+}\gamma_{S} \\ P_{[S_{T}]}(\alpha_{P}, \boldsymbol{p}_{P}\tau|_{U,S_{d},T_{d}}) & i\sigma^{i+}\gamma_{S} \end{array}$$

deut: unpol, tensor deut: vector deut: vector

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J = 1

S + D-wave

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Nucleon LF momentum distributions

Unpolarized, helicity independent

$$P_{[U,U]} = f_{\mathbf{0}}^{\mathbf{2}}(k) + f_{\mathbf{2}}^{\mathbf{2}}(k)$$

Tensor polarized, helicity independent: needs D-wave, ~ Y_{2m}(θ, 0)

$$\begin{split} P_{[T_{LL},U]}(\alpha_{\rho},\boldsymbol{p}_{\rho T}) &= -\left(2f_{0} + \frac{f_{2}}{\sqrt{2}}\right) \frac{f_{2}}{\sqrt{2}} \frac{3}{2}(3\cos^{2}\theta_{k} - 1),\\ P_{[T_{LT},U]}(\alpha_{\rho},\boldsymbol{p}_{\rho T}) &= -\left(2f_{0} + \frac{f_{2}}{\sqrt{2}}\right) \frac{f_{2}}{\sqrt{2}} 6\cos\theta_{k}\sin\theta_{k},\\ P_{[T_{TT},U]}(\alpha_{\rho},\boldsymbol{p}_{\rho T}) &= -\left(2f_{0} + \frac{f_{2}}{\sqrt{2}}\right) \frac{f_{2}}{\sqrt{2}} 3\sin^{2}\theta_{k}, \end{split}$$

Vector polarized, helicity and transversity

$$\begin{split} P_{[S_L,S_L]}(a_{\rho},\boldsymbol{p}_{\rho T}) &= \left(f_{0} - \frac{f_{2}}{\sqrt{2}}\right) \left[F_{1}(k)\left(f_{0} - \frac{f_{2}}{\sqrt{2}}\right) + F_{2}(k)\left(f_{0} + \sqrt{2}f_{2}\right)\right] \\ P_{[S_T,S_L]}(a_{\rho},\boldsymbol{p}_{\rho T}) &= \left(f_{0} - \frac{f_{2}}{\sqrt{2}}\right) \left[U_{1}(k)\left(f_{0} - \frac{f_{2}}{\sqrt{2}}\right) - U_{2}(k)\left(f_{0} + \sqrt{2}f_{2}\right)\right] \\ P_{[S_L,S_T]}(a_{\rho},\boldsymbol{p}_{\rho T}) &= \left(f_{0} - \frac{f_{2}}{\sqrt{2}}\right) \left[-U_{1}(k)\left(f_{0} - \frac{f_{2}}{\sqrt{2}}\right) + U_{2}(k)\left(f_{0} + \sqrt{2}f_{2}\right)\right] \\ P_{[S_T,S_T]}^{[1]}(a_{\rho},\boldsymbol{p}_{\rho T}) &= \left(f_{0} - \frac{f_{2}}{\sqrt{2}}\right) \left[F_{1}(k)\left(f_{0} - \frac{f_{2}}{\sqrt{2}}\right) + F_{2}(k)\left(f_{0} + \sqrt{2}f_{2}\right)\right] \end{split}$$

Remarkable symmetry between helicity and transversity

 \rightarrow Rotational invariance + relativistic spin effects

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Nucleon LF momentum distributions: Sum Rules

baryon

$$\begin{split} &\int \frac{d\,\alpha_p}{\alpha_p}\,d^2\boldsymbol{p}_{PT}\,\boldsymbol{P}_{[U,U]}(\alpha_p,\boldsymbol{p}_{PT}) = 1\,,\\ &\int \frac{d\,\alpha_p}{\alpha_p}\,d^2\boldsymbol{p}_{PT}\,\boldsymbol{P}_{[T,U]}(\alpha_p,\boldsymbol{p}_{PT}) = 0\,, \end{split}$$

momentum

$$\begin{split} &\int \frac{d\alpha_p}{\alpha_p} d^2 p_{pT} (2 - \alpha_p) P_{[U,U]}(\alpha_p, \boldsymbol{p}_{pT}) = 1 , \\ &\int \frac{d\alpha_p}{\alpha_p} d^2 p_{pT} (2 - \alpha_p) P_{[T,U]}(\alpha_p, \boldsymbol{p}_{pT}) = 0 \end{split}$$

axial

$$\int \frac{d\alpha_p}{\alpha_p} d^2 p_{pT} P_{[S_L, S_L]}(\alpha_p, \boldsymbol{p}_{pT}) = S_d^z \frac{g_{Ad}}{2g_A}, \qquad \int \frac{d\alpha_p}{\alpha_p} d^2 p_{pT} P_{[S_L, S_T]}(\alpha_p, \boldsymbol{p}_{pT}) = 0,$$

$$\int \frac{d\alpha_p}{\alpha_p} d^2 p_{pT} P_{[S_T, S_L]}^{||}(\alpha_p, \boldsymbol{p}_{pT}) = 0, \qquad \int \frac{d\alpha_p}{\alpha_p} d^2 p_{pT} P_{[S_T, S_T]}^{||}(\alpha_p, \boldsymbol{p}_{pT}) = S_d^T \frac{g_{Ad}}{2g_A},$$

$$1 - \frac{3}{2}\omega_2 = \frac{g_{Ad}}{2g_A}. \qquad \rightarrow \text{ cfr correction in inclusive polarized ed DIS}$$

Probabilistic Distributions for pure states



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Probabilistic Distributions for pure states

- At small momenta *S*-wave dominates
 - ightarrow polarization of nucleon is transferred from deuteron one
- Depolarization at larger momenta → D-wave
- Limits at p_{dT} = 0 → on-shell extrapolation
- Relativistic spin effects → sideways polarization
- Positivity remains for any mixed deuteron state

Tagged DIS with deuteron: model for the IA



 Hadronic tensor can be written as a product of nucleon hadronic tensor with deuteron light-front densities

 $\begin{array}{l} \text{All SF can be written as} \\ F_{ij}^k = \{ \text{kin. factors} \} \times \{ F_{1,2}(\tilde{x}, Q^2) \text{ or } g_{1,2}(\tilde{x}, Q^2) \} \times \{ P_{[U,U]}, P_{[T,U]} \text{ or } P_{[S,S]} \} \end{array}$

In the IA the following structure functions are $zero \rightarrow$ sensitive to FSI

- beam spin asymmetry $[F_{LU}^{\sin \phi_h}]$
- target vector polarized single-spin asymmetry [8 SFs]
- target tensor polarized double-spin asymmetry [7 SFs]
- Applied in studies of F₂ and tensor and vector polarized asymmetries [1906.11119,2006.03033,2108.08314, etc.]

■ Tagged reactions on deuteron have unique capabilities → control over nuclear effects

- Light-front is natural picture for high-energy nuclear scattering
- Deuteron structure can be quantified using polarized LF distributions
 → "our" TMDs (of nucleons in deuteron)
- Interesting relativistic spin effects
- Creates phi-dependent structures, spin-orbit effects etc.
- In proper reaction theory FSI need to be accounted for. → Distorted momentum distributions
- Lots of interesting physics opportunities ...

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