Probing LFV, PV ALPs at the Forward Physics Facility and a Future Muon Collider

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B. Batell, H. Davoudiasl, E. Neil, S. Trojanowski arXiv:2403.????

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Image Credit: DALL·E 3 Prompt: LFV, PV ALPs at the Forward Physics Facility and a Future Muon Collider



• LFV: Lepton-Flavor Violating



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- PV: Parity-Violating
- ALP: Axion-like Particle
  - Pseudo-Nambu Goldstone modes of a spontaneously broken approximate global symmetry.
  - For our purposes: has derivative coupling to fermions
  - QCD Axion, Pion



$$\sim \left(\frac{eg^2}{32\pi^2}\frac{m_\nu}{m_W}\right)^2$$

• ALP Effective Lagrangian:

$$\mathcal{L} = \frac{1}{2} \left(\partial_{\mu} a\right)^2 - \frac{1}{2} m_a^2 a^2 + \frac{\partial_{\mu} a}{\Lambda} \sum_{f,f'} \bar{f} \gamma^{\mu} \left(V_{ff'} - A_{ff'} \gamma^5\right) f' + \cdots$$

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• Lepton sector:

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• Lepton sector (equations of motion):

$$\mathcal{L}_{\ell} = \frac{a}{\Lambda} \sum_{\ell,\ell'} \overline{\ell} \left( (m_{\ell} - m_{\ell'}) V_{\ell\ell'} - (m_{\ell} + m_{\ell'}) A_{\ell\ell'} \gamma^5 \right) \ell'$$

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- Two take-aways:
  - Vector current coupling vanishes for  $\ell = \ell' \ (\ell \to \ell e^{-iV_{\ell\ell}a/\Lambda})$
  - Mass hierarchy in coupling: focus on  $\tau$

• ALP- $\tau$  sector:

$$\mathcal{L}_{\tau\ell} \approx \frac{\partial_{\mu} a}{\Lambda} \left[ C_{\tau\tau} \, \bar{\tau} \gamma^{\mu} \gamma^5 \tau + \sum_{\ell=e,\mu} \, \bar{\ell} \gamma^{\mu} (V_{\ell\tau} - A_{\ell\tau} \gamma^5) \, \tau \right] + H.c.$$

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- Focus on  $C_{\tau\mu}$
- ALP- "dark-fermion" sector:

$$\mathcal{L}_{\chi} = \frac{\partial_{\mu}a}{\Lambda} C_{\chi\chi}\bar{\chi}\gamma^{\mu}\gamma^{5}\chi$$

- Under the right conditions,  $\chi$  can be a candidate for dark matter
- If  $m_a > m_\tau + m_\ell$ ,  $2m_\chi$ , can decay  $a \to \ell \tau$ ,  $a \to \chi \chi$

# Contribution to $(g - 2)_{\mu}$

- Currently: Outstanding anomaly between theory and experiment for  $(g-2)_{\mu}$ 
  - Fermilab + Brookhaven:

 $\Delta a_{\mu} = (249 \pm 48) \times 10^{-11} \, (5.1\sigma)$ 

• In limit  $m_{ au} \gg m_{\ell}$ 

$$\Delta a_{\ell} = -\frac{m_{\ell}^2 C_{\ell\tau}^2}{16\pi^2 \Lambda^2} \left[ f(m_a^2/m_{\tau}^2) + \frac{m_{\tau}}{m_{\ell}} g(m_a^2/m_{\tau}^2) \cos 2\theta \right]$$

• Positive for  $\theta \gtrsim \frac{\pi}{4} + \frac{m_{\ell}}{m_{\tau}}$ 



$$f(x) = \frac{2x^2 \log x}{(x-1)^3} + \frac{1-3x}{(x-1)^2}$$
$$g(x) = \frac{2x^2(2x-1)\log x}{(x-1)^4} - \frac{5-19x+20x^2}{3(x-1)^2}$$

• Flavor-violating decays



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  - Weak for  $m_a > m_{ au}$
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- Higgs decays (arXiv:2105.05866, H. Davoudiasl, **R.M.**, N. Miesch, E. Neil)
- Electromagnetic Lepton-Nucleus Collisions
  - Production dependent only on  $C_{\ell\tau}$
  - Limits depend on ALP decay
  - For O(few) GeV ALP, need O(TeV) energies in ion rest frame.





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- FLUKA predictions:
  - Muons from ATLAS during HL-LHC
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- FLUKA predictions:
  - Muons from ATLAS during HL-LHC
  - Energies from 10 GeV 5 TeV
- FASER 2
  - Transverse size  $1m \times 3m$  (~ few  $\times 10^{14}$  muons)
  - Thin lead plates
- FASER $\nu$  2
  - Transverse size of  $40 \text{ cm} \times 40 \text{ cm}$  (~ few  $\times 10^{12}$  muons)
  - 20 tons of Tungsten (W) interspersed w/ emulsion layers







- $\mu^-W \rightarrow \tau^-Wa$ ,  $(a \rightarrow \mu^+\tau^-)$ 
  - No charge ID for f.s. leptons
  - SM background ( $\mu^-W \rightarrow \mu^-W\tau^+\tau^-$ )
- $\mu^- W \rightarrow \tau^- Wa$ ,  $(a \rightarrow \chi \bar{\chi})$ 
  - Require  $\tau^- \rightarrow 3h$  or  $\tau^- \rightarrow \mu^- \nu \nu$ + 2mm  $\tau^-$  track in emulsion detector

5000



# Limits from FASER $\nu$ 2

- Assuming  $a \rightarrow \chi \overline{\chi}$  is dominant
- Disclaimer: To be competitive, requires  $C_{\tau\tau} < 10^{-2}$
- Probes explanation to muon
  g 2 anomaly in narrow range
  of angles
- Can be used as a pilot study for similar study at a Muon Collider



# Looking Forward to a 3 TeV Muon Collider

- Consider muon thin target experiment
  - 2 cm lead (Pb) plate on beam axis
  - Assume  $N_{\mu} = 10^{20}$  muons on target
- Signal
  - $\mu^- Pb \rightarrow \tau^- Pb a$ ,  $(a \rightarrow \mu^+ \tau^-)$ 
    - Almost no background with charge ID
  - $\mu^- Pb \rightarrow \tau^- Pb a$ ,  $(a \rightarrow \chi \chi)$ 
    - Almost no SM background
  - Require  $\tau^- \rightarrow 3h$
- Explores large parameter space of couplings including all explanations to  $\Delta a_{\mu}$  for  $m_{\tau} < m_a < 30$  GeV



# Takeaways/Concluding Remarks

- Forward-Physics Facility:
  - Flux of muons with up to 5 TeV of energy
  - Probes small region of LFV ALP parameter space
  - Potential improvements from more tau identification or higher-than-expected muon luminosity
  - Detector-environment similar to that of a Muon Collider fixed target experiment, can be used as a pilot study
  - More generically, could test viability of physics searches and inform experimental design for a future Muon Collider
- 3 TeV Muon Collider
  - Can fully probe model's explanation to muon g-2
  - Offers competitive constraints even in presence of on-diagonal couplings
  - Massive undertaking... hopefully we will see it in our lifetimes

#### Questions?

#### Phase/angle parameterization

• ALP- $\tau$  sector:

$$\mathcal{L}_{\tau\ell} = \frac{\partial_{\mu}a}{\Lambda} \left[ C_{\tau\tau} \, \bar{\tau} \gamma^{\mu} \gamma^{5} \tau + \sum_{\ell=e,\mu} \, \bar{\ell} \gamma^{\mu} (V_{\ell\tau} - A_{\ell\tau} \gamma^{5}) \, \tau \right] + H.c.$$

• Useful to rewrite off-diagonal terms (assuming CP symmetry)

$$\overline{\ell}\gamma^{\mu}(V - A\gamma^5)\tau \longrightarrow C\overline{\ell}\gamma^{\mu}(\sin\theta - \cos\theta\gamma^5)\tau$$

where:

$$C = \sqrt{|A|^2 + |V|^2}$$
 Magnitude of coupling

 $\theta = \tan^{-1}(|V|/|A|)$  Parity-violating angle

#### Dark Matter

- If  $m_{\tau} < m_{\chi} < 2m_a$ , dark matter can annihilate to SM through  $\chi \bar{\chi} \to a \to \ell^{\pm} \tau^{\mp}$
- Thermal averaged annihilation cross-section:

$$\langle \sigma v \rangle \sim \frac{C_{\ell\tau}^2 C_{\chi\chi}^2}{\Lambda^4} \frac{m_\tau^2 \left(4m_\chi^2 - m_\tau^2\right)^2}{\left(m_a^2 - 4m_\chi^2\right)^2} \sim 4.4 \times 10^{-26} \,\mathrm{cm}^3 \mathrm{s}^{-1}$$

- Annihilation proceeds in *s*-wave
- If  $m_{\chi} < 10$  GeV, constrained by CMB.
- Can still exist in an asymmetric dark matter scenario
- If  $m_{\chi} > 2m_a$ , dark matter mainly annihilates through  $\chi \bar{\chi} \to aa$

$$\langle \sigma v \rangle \sim \frac{6}{x_{\rm f.o.}} \frac{C_{\chi\chi}^4}{24\pi} \frac{\left(m_{\chi}^2 - m_a^2\right)^2}{\left(2m_{\chi}^2 - m_a^2\right)^4} \left(1 - \frac{m_a^2}{m_{\chi}^2}\right)^{1/2}$$

• Annihilation proceeds in p-wave, no constraints from CMB





arXiv:2110.10698 (M. Bauer, M. Neubert, S. Renner, M. Schnubel, A. Thamm)

- Highly dependent on model parameters
  - As  $C_{\ell\ell} \to 0$ ,  $\tau \to \ell\gamma$  and ,  $\tau \to \ell\ell'$  very suppressed.
  - Weak for  $m_a > m_{ au}$
- Additional limits from Higgs decays (see arXiv:2105.05866 (R.M., H. Davoudiasl, E. Neil, N. Miesch))
- Can one probe  $C_{\tau\ell}$  independent of other couplings?

#### Explanation for $\Delta a_e$ and $\Delta a_\mu$



#### **Production Process**



- $\sigma \propto C_{\ell\tau}^2 Z^2 F(q^2)$ 
  - Production proportional only to off-diagonal coupling
  - Large enhancement from charge of nucleus
  - Suppressed for large  $t = q^2$
  - To produce ALP of mass  $m_a$ , need  $t = (m_a^2/2E_\ell)^2$
  - $F(q^2) = F_{\rm coh}(q^2) + F_{\rm incoh}(q^2)/Z$

# Probing $C_{\tau e}$ : Electron-Ion Collider (EIC)

- High-energy electron and heavy ion beams:
  - In lab frame:  $E_e^{\text{lab}} = 18 \text{ GeV}$ ,  $E_{\text{ion}}^{\text{lab}} = 110 \text{ GeV}/A$
  - In ion frame:  $E_e^{\text{ion}} \approx 4 \text{ TeV}$
  - Luminosity of  $\sim 3-15~{\rm fb^{-1}}$  per nucleon per month
- For clean detector environment, veto on nuclear breakup
  - cut off at  $t = -q^2 = (0.1 \text{ GeV})^2$
  - Can produce ALPs up to mass  $m_a = \sqrt{2E_e\sqrt{t_{\rm max}}} = 30~{\rm GeV}$
- ALP produced on-shell, consider decays  $a \rightarrow e^+ \tau^-$ 
  - Look for LFV signal: identify  $e^+$  and one  $\tau^-$ , veto on  $e^-$
  - Main background: Bethe-Heitler process with  $\tau^+ \rightarrow e^+ \nu \bar{\nu}$ , + loss of electron down the beam pipe.
  - Predicted  $\sim 400$  background events, with  $\sigma \sim 20$
  - Consider only  $\tau \rightarrow 3h$  decays, assume efficiency  $\epsilon_{\tau} = 1\%$  (arXiv:2207.10261).
  - Need to produce  $\sim 30$  signal events for 90% confidence



 $C_{\tau e}$  limits from EIC



- EIC can probe  $C_{\tau e}/\Lambda \sim O(1-10)/\text{TeV}$
- Competitive when  $C_{\tau\tau}/\Lambda < 10^{-1} \, {\rm TeV^{-1}}$
- Can view as complementary constraint:
  - When  $C_{\tau\tau}$  large,  $C_{\tau e}$  constrained with LFV
  - When  $C_{\tau\tau}$  small,  $C_{\tau e}$  constrained through production at EIC

# EIC and electron g - 2 anomalies



- EIC can probe near-chiral LFV explanations for either electron g 2 anomaly (assuming one remains)
- This analysis only considered  $\epsilon_{\tau} \sim 1\%$  and no dedicated background mitigation. A more dedicated analysis could probe a wider range of couplings.
- Also would gain from  $a \rightarrow \chi \chi$  signal

## EIC in the $m_a$ - $\theta$ plane explanation for $g_e - 2$



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- This analysis only considered  $\epsilon_{\tau} \sim 1\%$  and no dedicated background mitigation. A more dedicated analysis could probe a wider range of couplings.
- Would gain more from  $a \rightarrow \chi \chi$  signal

# Probing $C_{\mu\tau}$ : $m_a$ - $\theta$ plane explanation for $g_{\mu} - 2$

- FASER $\nu$ 2 only probes light masses with angle  $\theta \sim \pi/4 + m_{\mu}/m_{\tau}$
- Muon Collider probes entire parameter space

