



# Simulation of Signal Propagation in Thin-Gap RPCs

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Based on NIMA Paper:

Simulation of the signal propagation for thin-gap RPC in the ATLAS Phase-II upgrade

For DRD1 WG4

31 Jan 2024

# Outline

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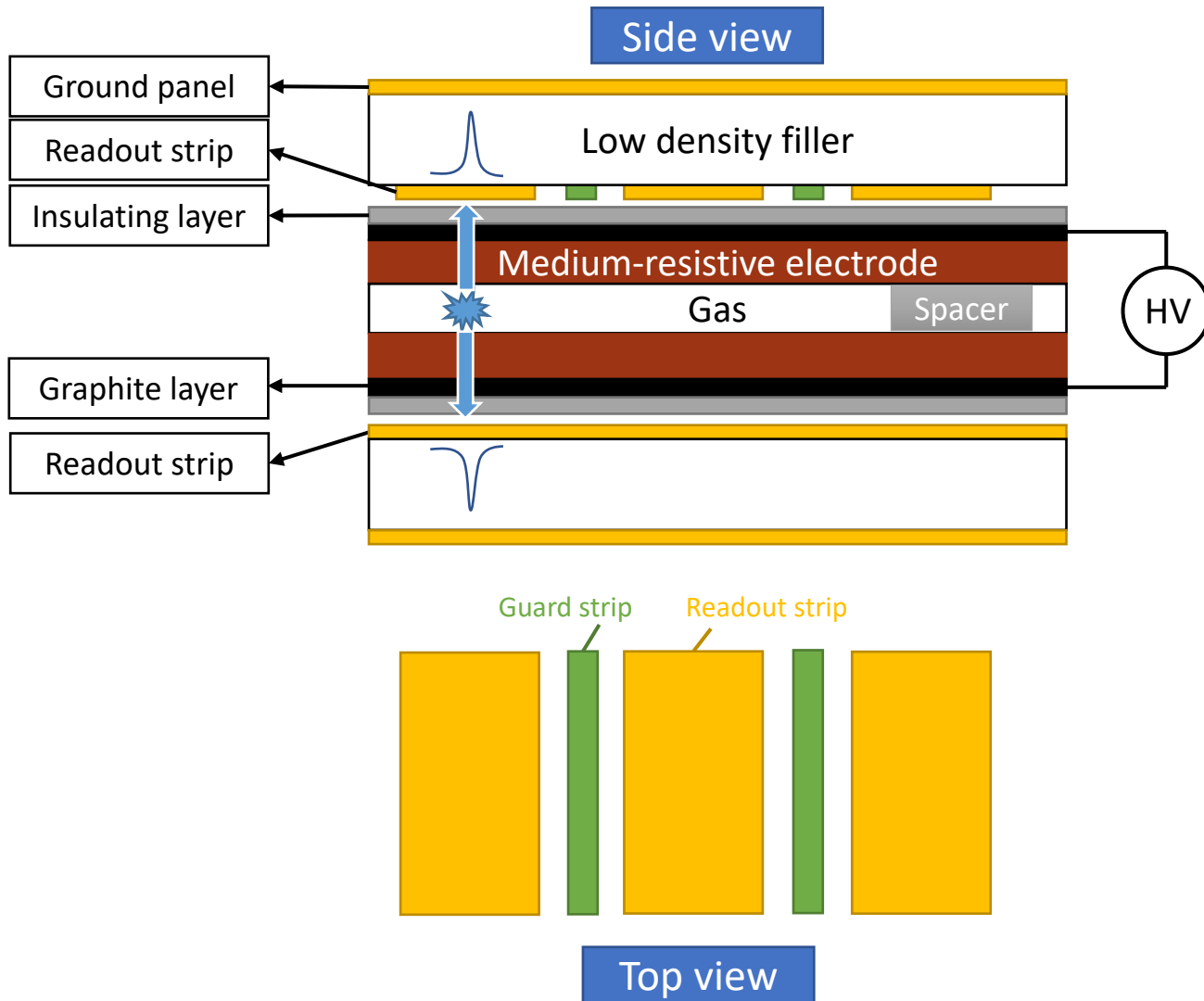
- Introduction
- Transmission simulation
- Measurements & Validation
- Discussions

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# RPC prototype in this talk



- Basic information

- LHC-ATLAS muon-spectrometer component detector
- To be installed at next upgrade

- Thin-gap RPC

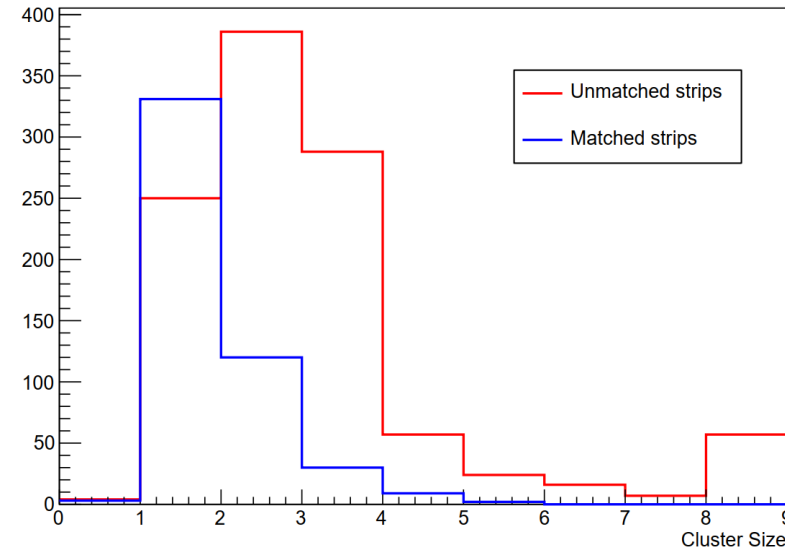
- 1 mm gas gap

- Panel layout

- 25 mm strip width + 2 mm spacing
- 0.8 mm guard strip

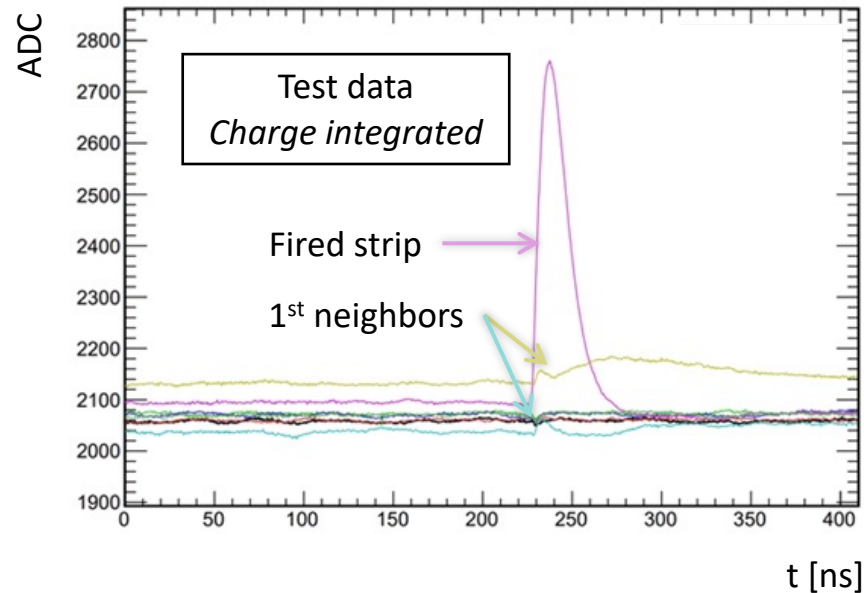
# Multiplicity in RPC readout

- Current configuration to limit multiplicity:
  - ✓ Higher graphite layer resistivity
  - ✓ Guard strip
  - ✓ Optimized termination
- Potential improvements:
  - More delicate impedance matching
  - Crosstalk mitigation
  - Transmission simulation provides guidance



Termination optimization

*From ATLAS MS Phase-II Upgrade TDR*



Crosstalk signal observed on neighboring strips

*X.Y. Xie, et.al, A new approach in simulating RPC and searching for the causes of large cluster size of RPC, 2019 JINST 14 C09012*

# Lossless Multi-conductor transmission line (MTL) for RPC

## • Transmission model

- Induced charge treated as a point-like current source  $I_0$  on the fired strip:

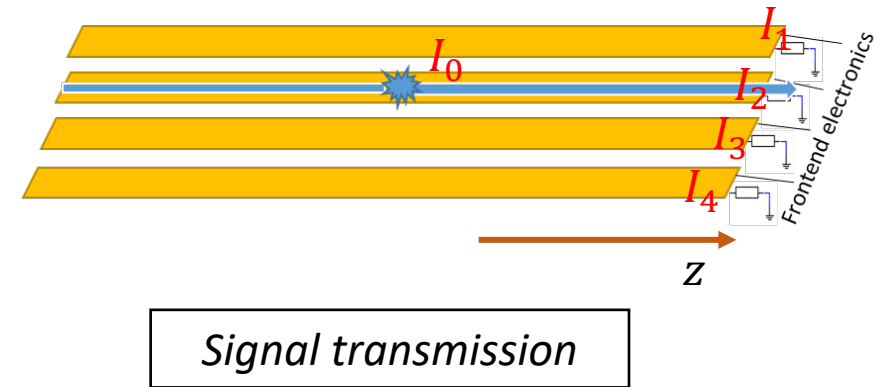
$$\vec{I}(t, z_0) = \begin{pmatrix} 0 \\ I_0(t) \\ 0 \\ 0 \end{pmatrix}$$

- Collected signal at frontend **distorted**:

$$\vec{I}(t, L) = \begin{pmatrix} I_1(t) \\ I_2(t) \\ I_3(t) \\ I_4(t) \end{pmatrix}$$

## • Issues of interest

- Calculate signal distortions using PRC modelling
  - Reflection and crosstalk
- Find distortion mitigation methods



*Theory assumptions:*

- ✓ 'Transparent' graphite layer
- ✓ Resistance of copper ignored

# MTL simulation tools

- Fundamental formulae:

$$\frac{d^2}{dz^2} \vec{V}(z, t) = \hat{L} \hat{C} \frac{d^2}{dt^2} \vec{V}(z, t)$$
$$\frac{d^2}{dz^2} \vec{I}(z, t) = \hat{C} \hat{L} \frac{d^2}{dt^2} \vec{I}(z, t)$$

- $\hat{C}, \hat{L}$ : capacitance and inductance matrices of parallel readout strips

- $\hat{C} = \begin{pmatrix} C_{gnd} & -C_m \\ -C_m & C_{gnd} \end{pmatrix}; \hat{L} = \begin{pmatrix} L_{gnd} & L_m \\ L_m & L_{gnd} \end{pmatrix}$

- Given by **Maxwell**

- $\vec{V}(z, t), \vec{I}(z, t)$ : vectors of signal

- $\vec{V} = \hat{Z} \vec{I}$ ,  $\hat{Z}$  impedance matrix
- Solved using **Mathematica**



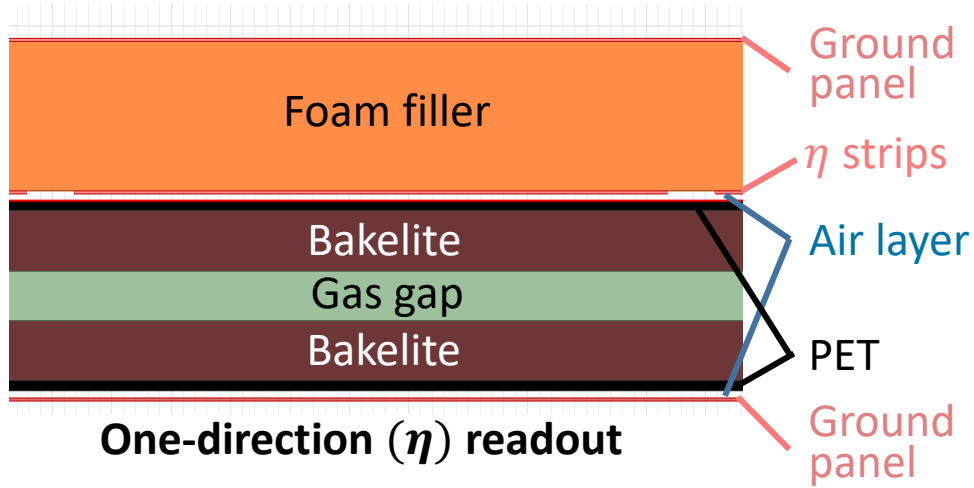
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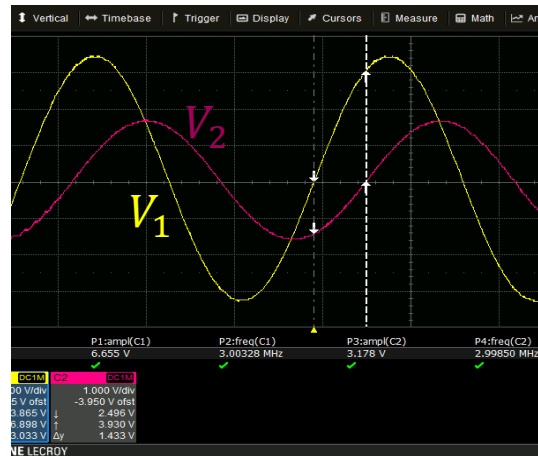
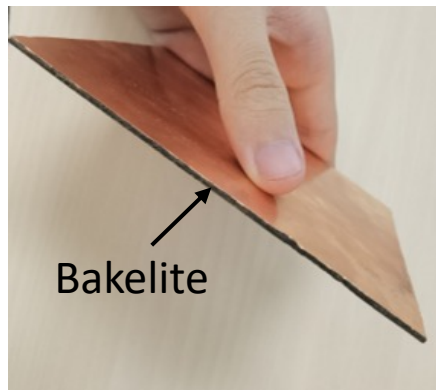
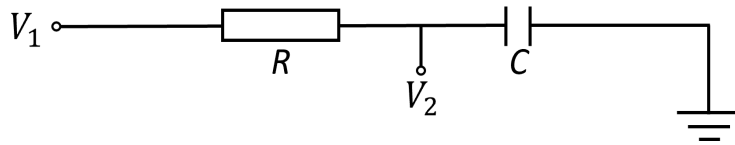
- Introduction
- **Transmission simulation**
- Measurements & Validation
- Discussions



# Maxwell-2D setup



	Layer	Material	Thickness [mm]	Relative permittivity
Gas chamber	Gas gap	Gas mixture	1.0	1
	Electrode	Bakelite	1.2	5.2
	Insulator	PET	0.2	3.7
	Extra air layer	Air	0.15	1
Readout panel	Filler	Foam	3.1	1
	Ground panel/Strips	Copper	0.05	N/A

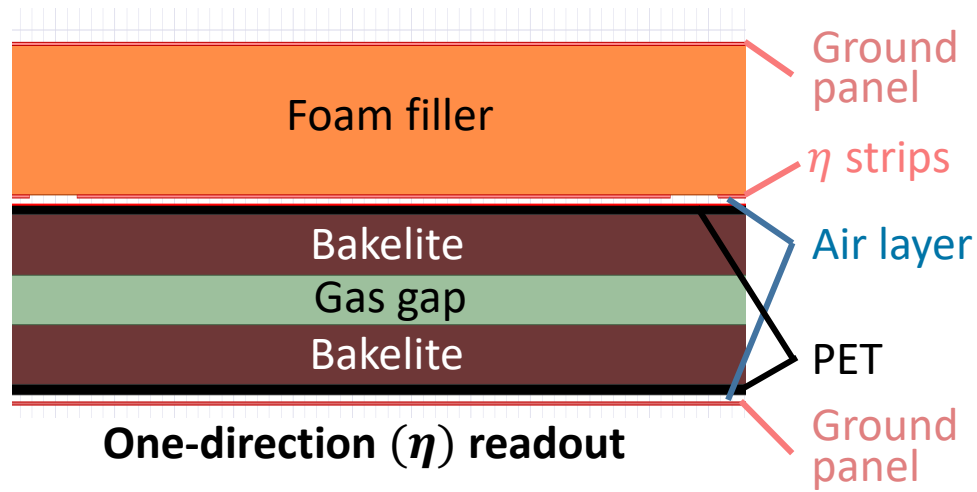


## • Permittivity measurement

- Conductor with bakelite medium
- $V_1, V_2$  connected to oscilloscope
- $\Rightarrow \epsilon_r(\text{bakelite}) = 5.2$

Transmission simulation

# Maxwell-2D setup



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- **Spacer indicator**

- Thickness: 0.15 mm
- Air layer between readout strips and gas chamber

# Maxwell results: $\hat{C}$ ; $\hat{L}$ ; $\hat{Z}$ matrices

- Simplest case: One-direction ( $\eta$ ) parallel readout

- $\hat{C} = \begin{pmatrix} 229.5 & -12.4 & 0 \\ -12.4 & 229.5 & -12.4 \\ 0 & -12.4 & 229.5 \end{pmatrix}$  [pF/m]

- $\hat{L} = \begin{pmatrix} 153.9 & 5.4 & 0 \\ 5.4 & 153.9 & 5.4 \\ 0 & 5.4 & 153.9 \end{pmatrix}$  [nH/m]

- Note:  $C_{13}, C_{31}, L_{13}, L_{31}$  negligible


$$\hat{v}^{-2} = \hat{M}^{-1} \hat{C} \hat{L} \hat{M} ; \hat{Z} = \hat{L} \hat{M} \hat{v} \hat{M}^{-1}$$

- $\hat{v} = \begin{pmatrix} 237 & 0 & 0 \\ 0 & 240 & 0 \\ 0 & 0 & 243 \end{pmatrix}$  [mm/ns]

- $\bar{v} = 240$  mm/ns ;  $\Delta v = 3$  mm/ns

- $\hat{Z} = \begin{pmatrix} 18.3 & 0.8 & 0.04 \\ 0.8 & 18.3 & 0.8 \\ 0.04 & 0.8 & 18.3 \end{pmatrix}$  [ $\Omega$ ]

## Counterparts in experiment

- Leading order elements:

- $C_{11} ; L_{11} \Rightarrow Z_{11}$ , impedance
- Impedance decides matching resistors

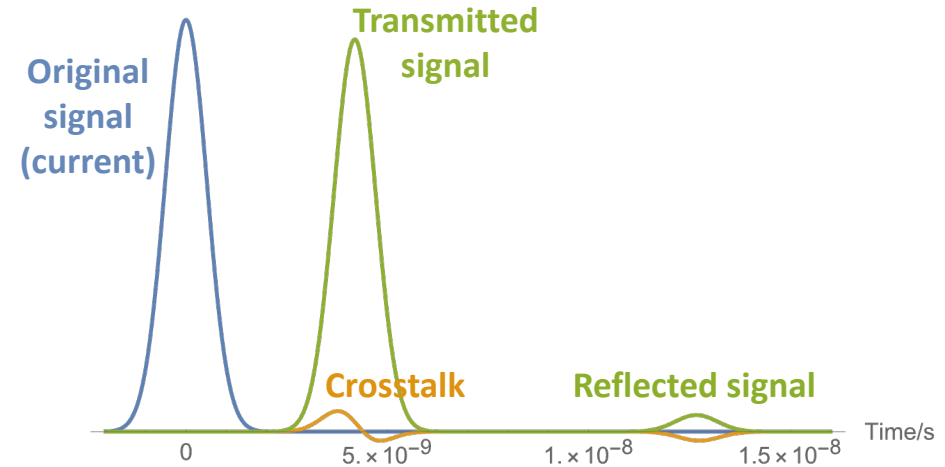
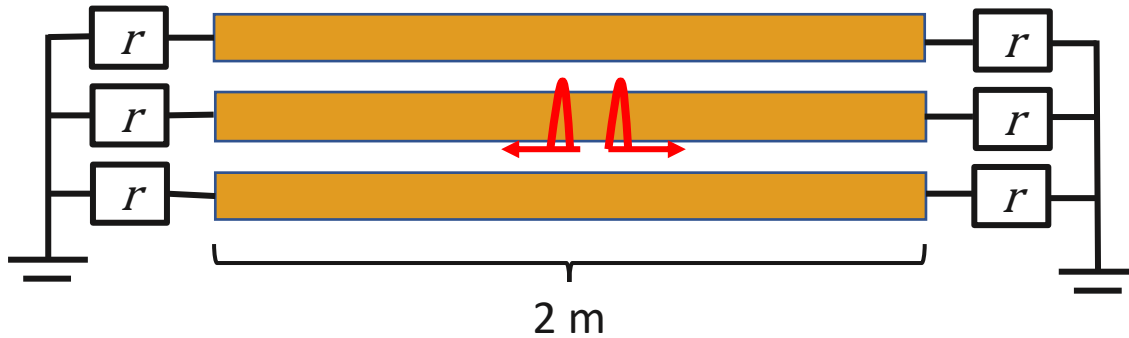
- $\hat{Y} = \hat{Z}^{-1}, \hat{R} = \begin{pmatrix} (\sum_i Y_{1i})^{-1} & \dots & -(Y_{1N})^{-1} \\ \vdots & \ddots & \vdots \\ -(Y_{N1})^{-1} & \dots & (\sum_i Y_{Ni})^{-1} \end{pmatrix}$

- $\hat{R} = \begin{pmatrix} 20 & 400 & 400,000 \\ 400 & 20 & 400 \\ 400,000 & 400 & 20 \end{pmatrix}$  [ $\Omega$ ]

- Sub-leading order elements:

- $C_{12} ; L_{12} \Rightarrow \Delta v$ , dispersion
- Dispersion decides the level of crosstalk

# Mathematica results in time-domain



- Example setup:

- 3 strips, middle strip fired
- Input 1.22 ns FWHM gaussian pulse
- Matching resistor  $r = 20 \Omega$  on both ends
- No guard strips equipped

	Normalized Charge	Normalized Amplitude
Original	1	1
Transmitted	95.6%	95.3%
Crosstalk	0	6.0%
Reflected	4.4%	3.9%

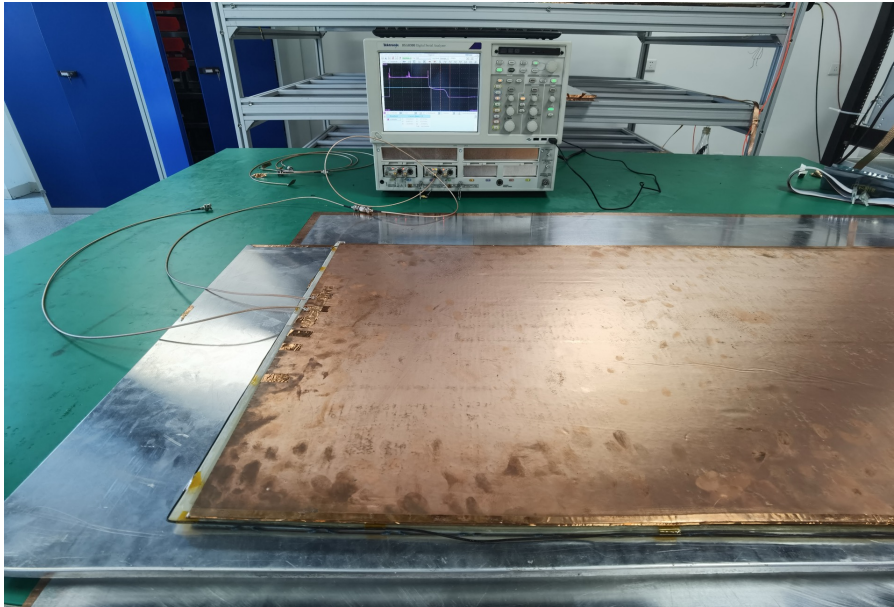
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- **Measurements & Validation**
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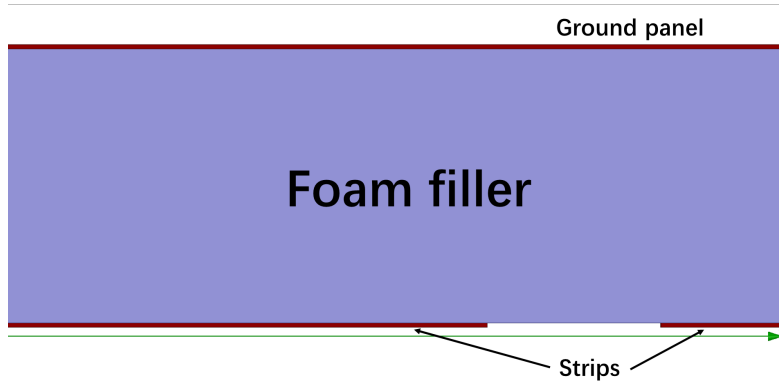
# Leading order: impedance measurement

- Device: Tektronix DSA8300
  - As TDR (Time Domain Reflectometry)
- Experiment setup:
  - Thin-gap RPC size: 1 m × 0.5 m
  - Far-end grounded



# Leading order validation results

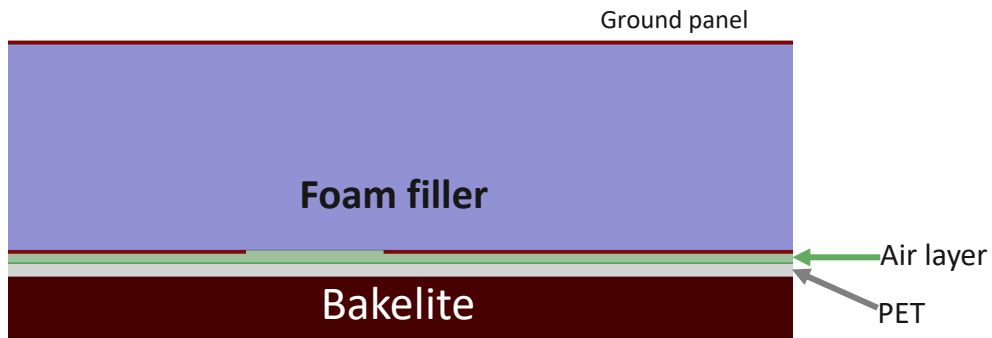
- Case 1: bare strip



Impedance [ $\Omega$ ]	Bare strip	Assembled
Measurement	32.2	18.5
Simulation	32.3	$18.3 \pm 0.4$

- Case 2: assembled RPC

- Only  $\eta$  panel
- $110 \text{ kg/m}^2$  pressure



✓ Good agreement between simulation & measurement

# Sub-leading order: crosstalk & S-parameter

- Crosstalk sensitive to off-diagonal elements

$$\hat{C} = \begin{pmatrix} C_{11} & -C_{12} \\ -C_{21} & C_{22} \end{pmatrix}; \hat{L} = \begin{pmatrix} L_{11} & L_{12} \\ L_{21} & L_{22} \end{pmatrix}$$

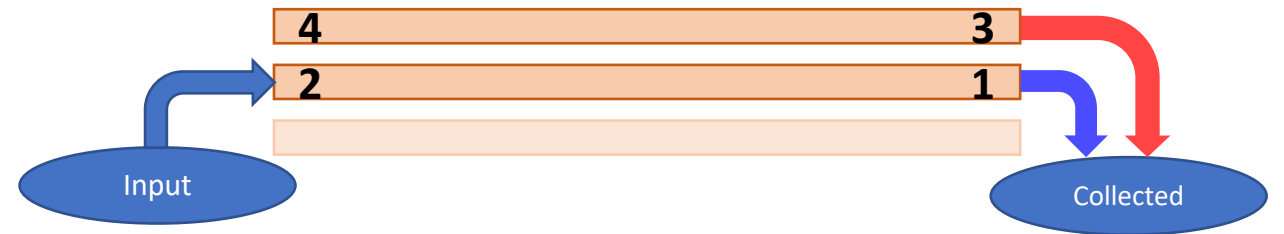
$$C_{12} \ll C_{11}; L_{12} \ll L_{11} \Rightarrow Z \approx \sqrt{L_{11}/C_{11}}$$

- S-parameter definition:

$$S_{13}(f) = \frac{Amp_3(f)}{Amp_1(f)}$$

- $Amp_3$  → neighbouring strip collected signal
- $Amp_1$  → fired strip collected signal
- Note: phase information ignored

- $S_{13}(f)$  represents crosstalk level



- S-parameter property

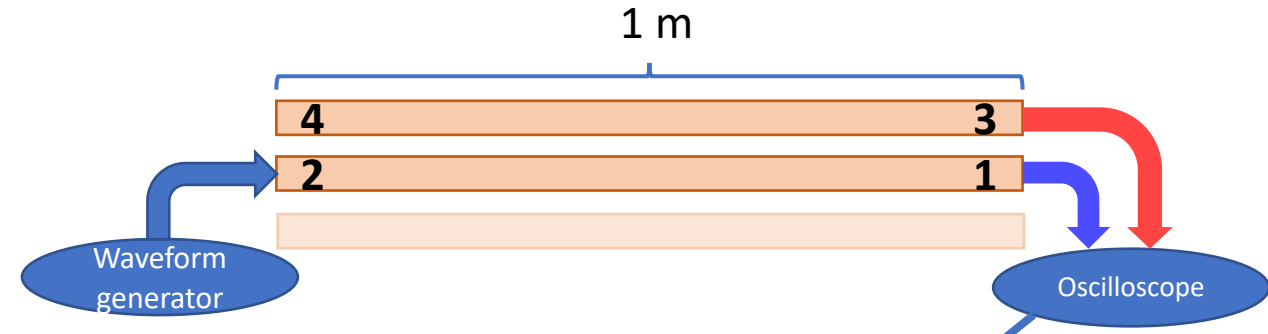
- Equals 0 when  $f \ll$  the characteristic frequency  $f_c$  of the system
- **Not** dependent on signal shape or amplitude
- Reflection on the fired strip also included in calculation



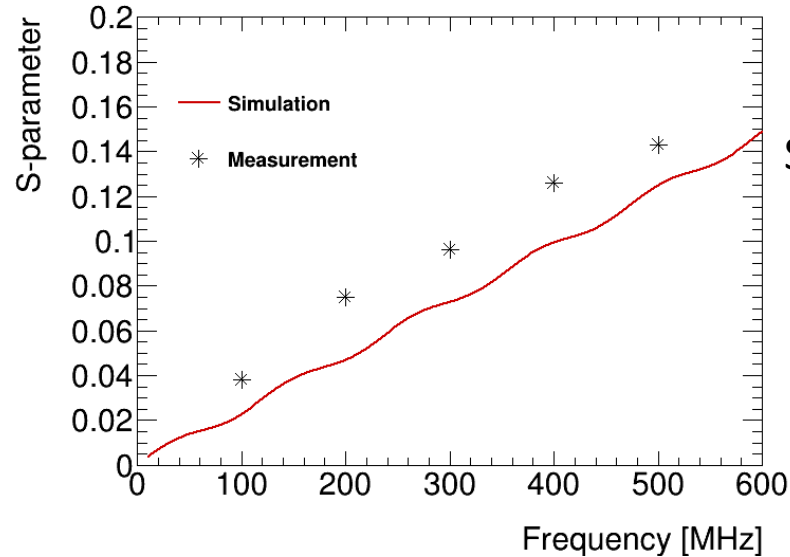
# Sub-leading order validation results

## • Experiment setup

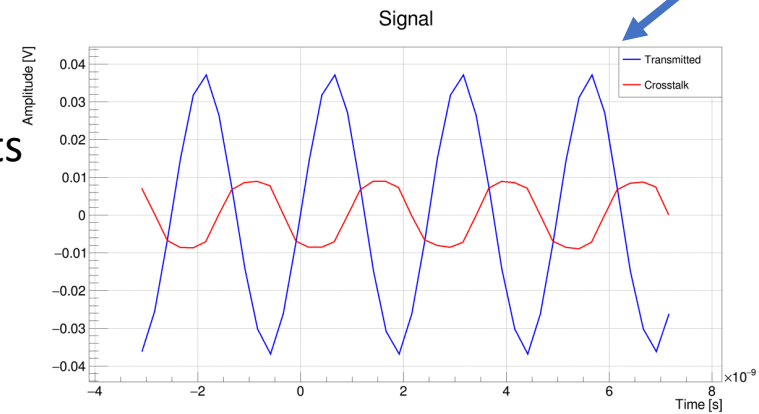
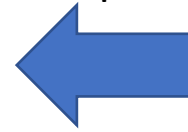
- Device:
  - Waveform generator: Tabor WX2182C
  - Oscilloscope: Lecroy 3104z, 1 GHz bandwidth
- RPC:
  - 1 m × 0.5 m size, only  $\eta$  panel
  - 20  $\Omega$  matching resistor
  - 110 kg/m<sup>2</sup> pressure



## • Results



Scan 5 points



Sinewave fit for  $Amp_1$  and  $Amp_3$

*Measurement and simulation roughly consistent*

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# Discussion: $\eta - \eta$ readout

- Potential readout for ATLAS Phase II upgrade

- From time difference to position

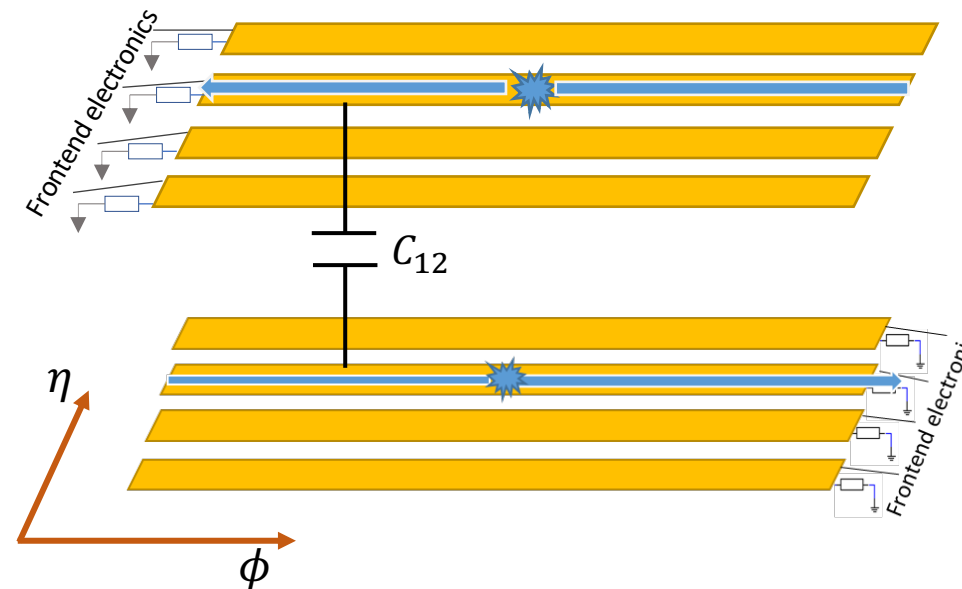
- Capacitance matrix:

$$\hat{C}_{\eta-\eta} = \begin{pmatrix} 228.9 & -115.1 \\ -115.1 & 228.9 \end{pmatrix}$$

- $C_{12}, C_{21}$ : face-to-face capacitance

- Impedance:

	$\eta - \phi$	$\eta - \eta$
Geometry	Adjacent	Face-to-face
Impedance	$\hat{Z} = \begin{pmatrix} 18.3 & 0.8 \\ 0.8 & 18.3 \end{pmatrix}$	$\hat{Z} = \begin{pmatrix} 22 & 10 \\ 10 & 22 \end{pmatrix}$
Termination network	$\hat{R} = \begin{pmatrix} 20 & 400 \\ 400 & 20 \end{pmatrix}$	$\hat{R} = \begin{pmatrix} 32 & 42 \\ 42 & 32 \end{pmatrix}$

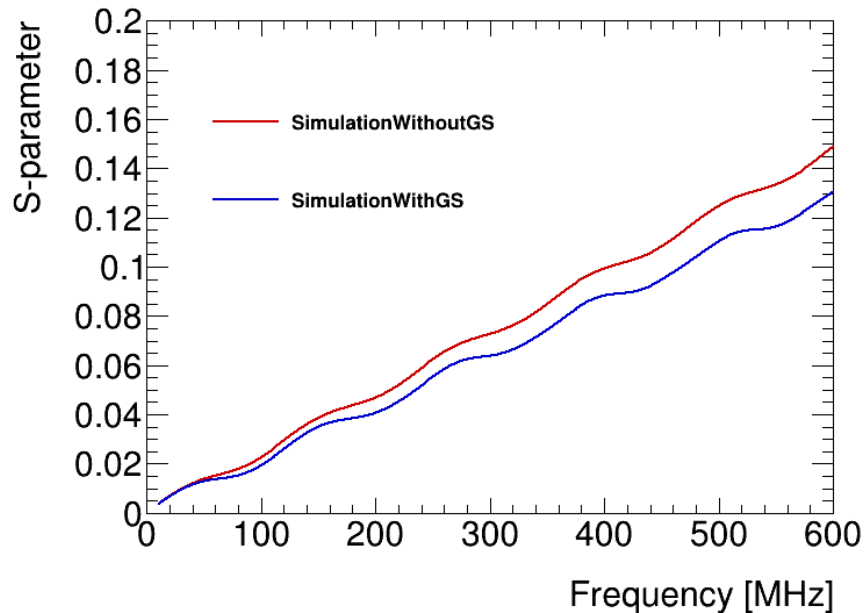


- First order termination **would be insufficient**

# Discussion: different geometry designs

- Guard strip

- Strip impedance  $18.3 \Omega$ , guard strip impedance  $100 \Omega$  ( simulated )
- Crosstalk amplitude drops from 6%  $\rightarrow$  5.1%
  - 1.22 ns FWHM gaussian pulse
  - 1 m transmission distance



✓ *Guard strip slightly reduces crosstalk*

- Pitches and electrode thickness

- Different pitch (2 mm spacing kept)

Width [mm]	Crosstalk amplitude (no guard strip)	Impedance [ $\Omega$ ]
35	3.8%	14.4
31	4.2%	16.0
27	6.0%	18.3
23	6.8%	21.2
20	7.5%	23.4

- Bakelite thickness

Thickness [mm]	Crosstalk amplitude (no guard strip)	Impedance [ $\Omega$ ]
1.2	6.0%	18.3
1.4	6.8%	18.7

# Summary and outlook

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- MTL simulation method and its validation is presented
  - Leading order: simulated impedance agrees with measurement
  - Sub-leading order: S-parameter simulation roughly agrees with measurement
- Suitable for matching resistors selection
- Different readout schemes could be investigated via this method

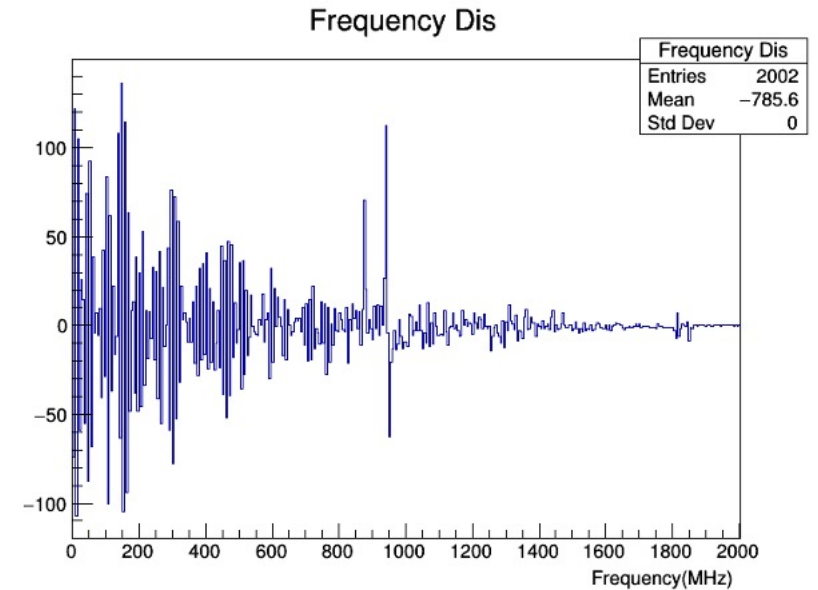
# Backup

# Key reference:

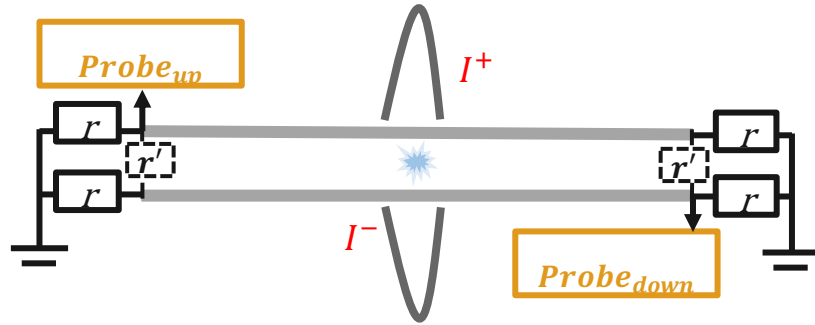
$$\vec{V}_T(t) = \frac{1 + \hat{\Gamma}_0}{2} \sum_{j=0}^{\infty} (\hat{\Gamma}_D \hat{\Gamma}_0)^j \left\{ \hat{Z}_c \hat{M} \begin{pmatrix} \hat{M}_{1n}^{-1} I \left( t - \frac{y_0 + 2jD}{v_1} \right) \\ \vdots \\ \hat{M}_{Nn}^{-1} I \left( t - \frac{y_0 + 2jD}{v_N} \right) \end{pmatrix} \right. \\ \left. + \hat{\Gamma}_D \hat{Z}_c \hat{M} \begin{pmatrix} \hat{M}_{1n}^{-1} I \left( t - \frac{2(j+1)D - y_0}{v_1} \right) \\ \vdots \\ \hat{M}_{Nn}^{-1} I \left( t - \frac{2(j+1)D - y_0}{v_N} \right) \end{pmatrix} \right\} \quad (10)$$

where  $\vec{V}_T(t)$  is the  $N$ -dimensional array of voltages measured by a readout system placed at  $y=0$  when the  $N$ -strip structure is excited along line  $n$  by a current  $I(t)$  originated at position  $y=y_0$ . The sum extends over all  $j$  reflections. The reflection matrices at the near-end ( $y=0$ ) and at the far-end ( $y=D$ ) are defined as

$$\Gamma_0 = \frac{\hat{Z}_0 - \hat{Z}_c}{\hat{Z}_0 + \hat{Z}_c}, \quad \Gamma_D = \frac{\hat{Z}_D - \hat{Z}_c}{\hat{Z}_D + \hat{Z}_c}. \quad (11)$$



# $\eta - \eta$ readout

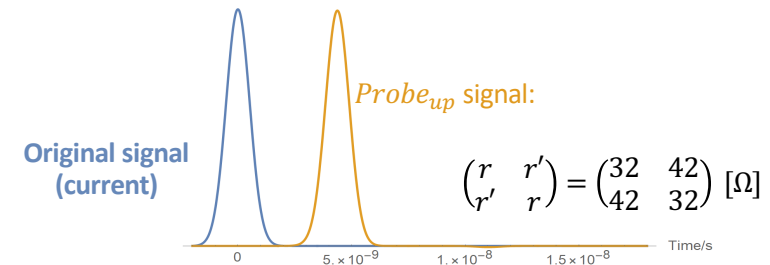
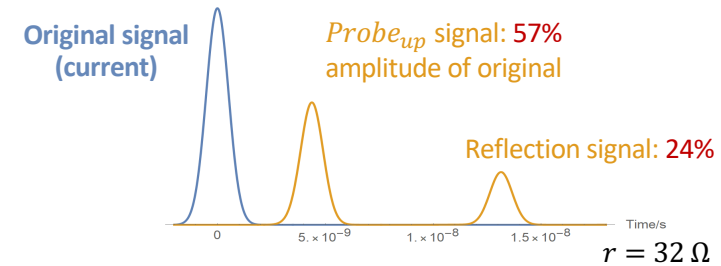
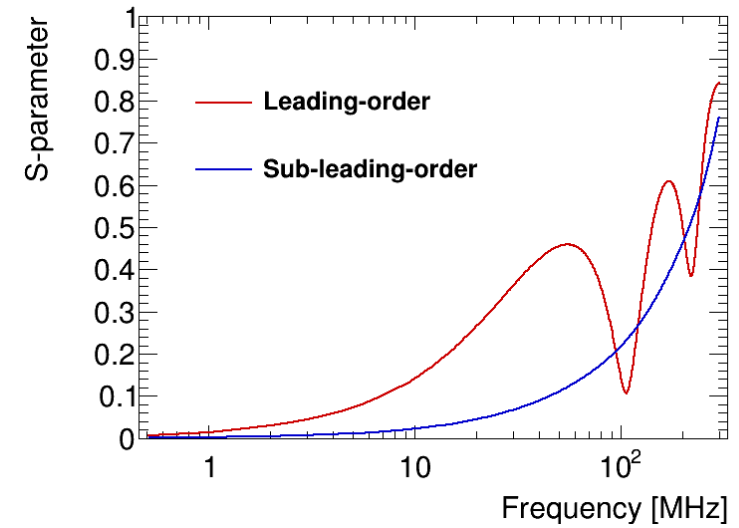


- S-parameter

- Characteristic frequency  $f_c \cong 100$  MHz
  - Crosstalk is comparable with main signal
- Ill matching at only leading-order termination

- Countermeasure

- Include next-to-leading-order termination
  - Connect face-to-face strips with  $r'$
  - $r = 32 \Omega$ ;  $r' = 42 \Omega$
- Consider the minus current source on the other strip
  - $I^+$  and  $I^-$  together contribute to the total collected current





# $\eta - \phi$ readout

- Pulse signal test

- 2 ns width pulse from waveform generator
- 1 m transmission distance

- Results

- Crosstalk amplitude is about 6.6%
- $\eta - \phi$  readout crosstalk amplitude is **not significantly higher** than single  $\eta$  readout
  - Note: the lower limit of the pulse width of this waveform generator is 2 ns
- $\eta - \phi$  scheme introduces a more complex shape in crosstalk

