

# Precision calculations in the Higgs sector

**Gudrun Heinrich**

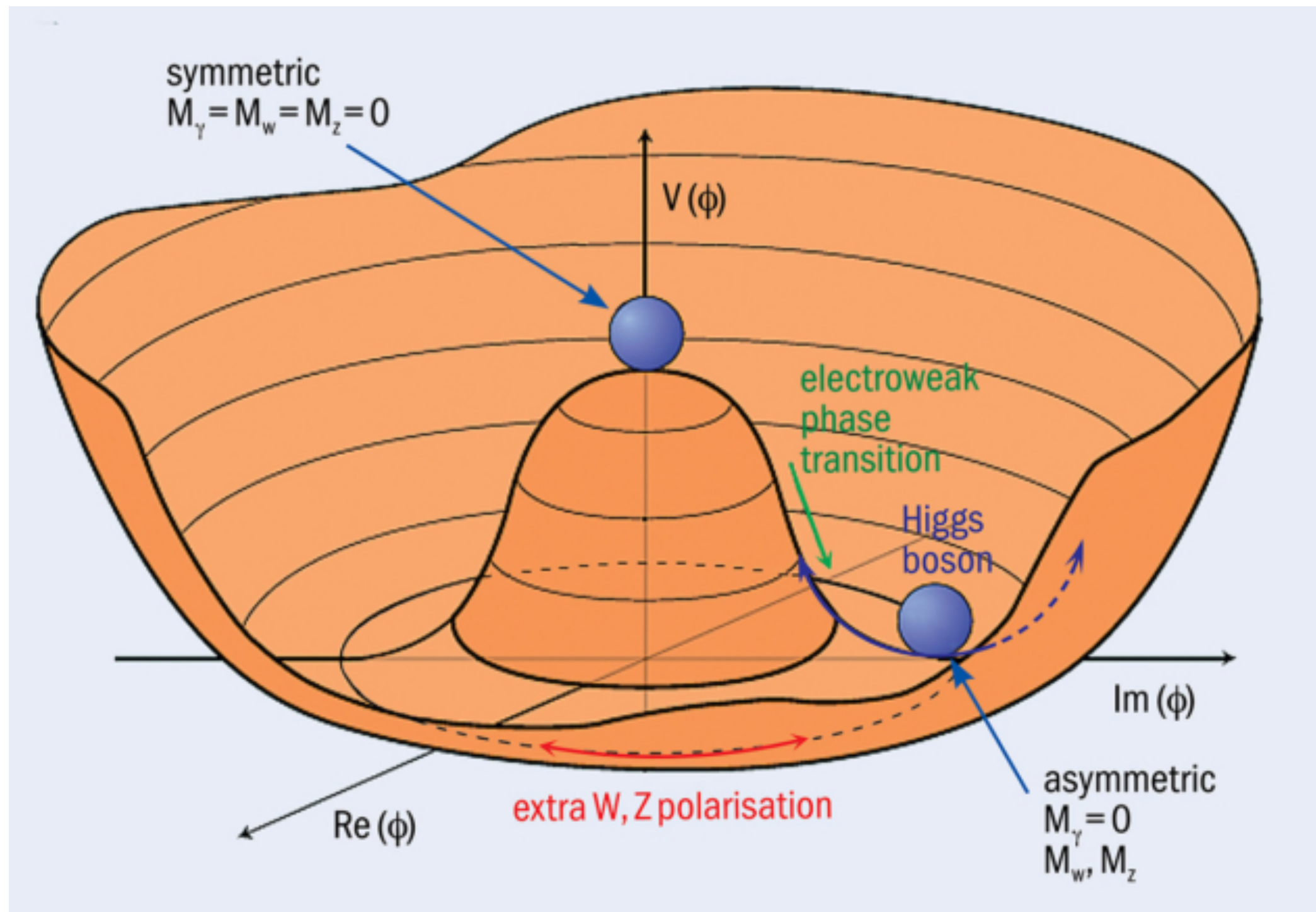
*Institute for Theoretical Physics  
Karlsruhe Institute of Technology*

**QCD@LHC, Freiburg**

October 8, 2024



# Higgs bosons

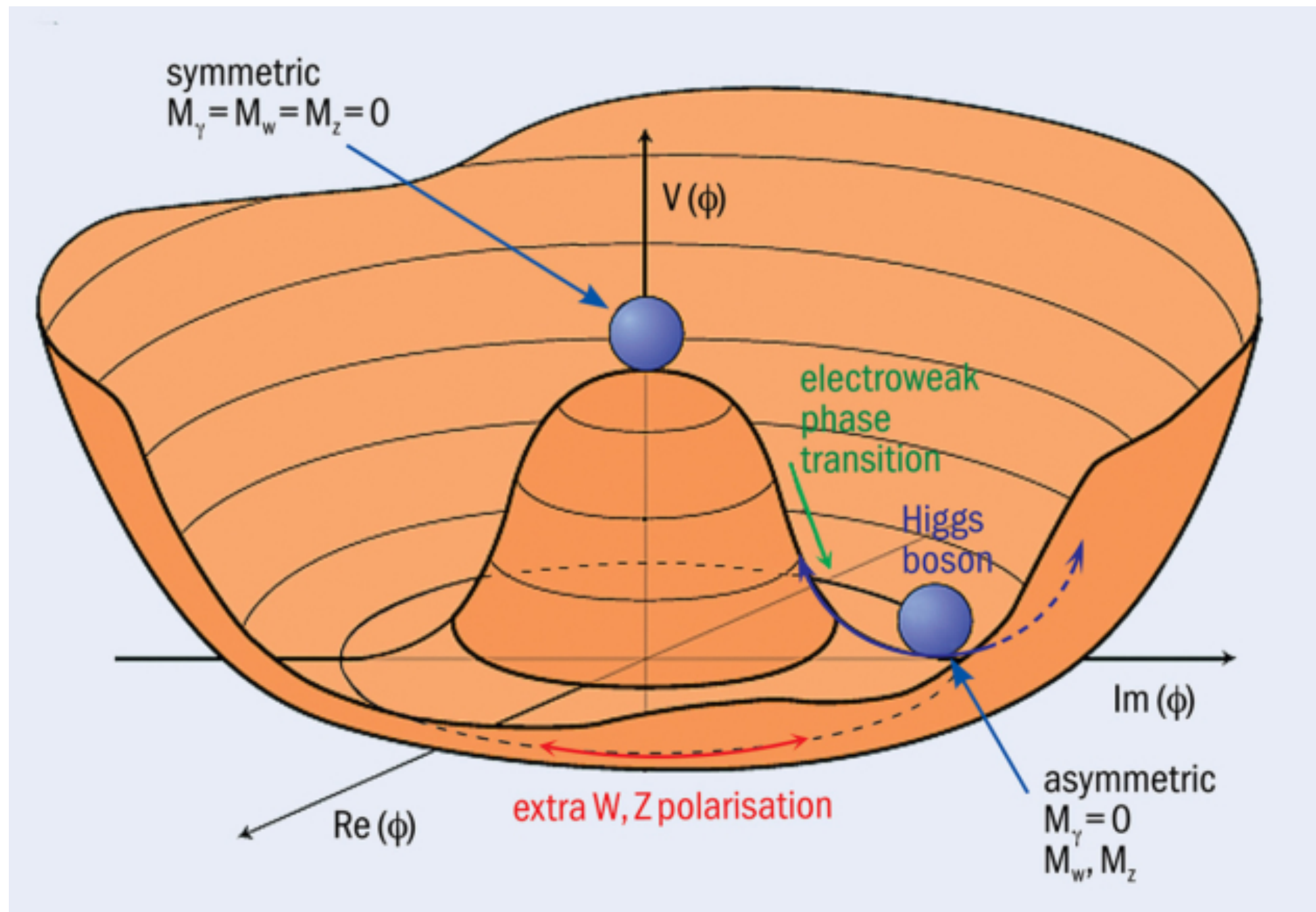


J. Ellis, M. Neubauer, CERN Courier

“We think we have it”

(Rolf Heuer 2012)

# Higgs bosons

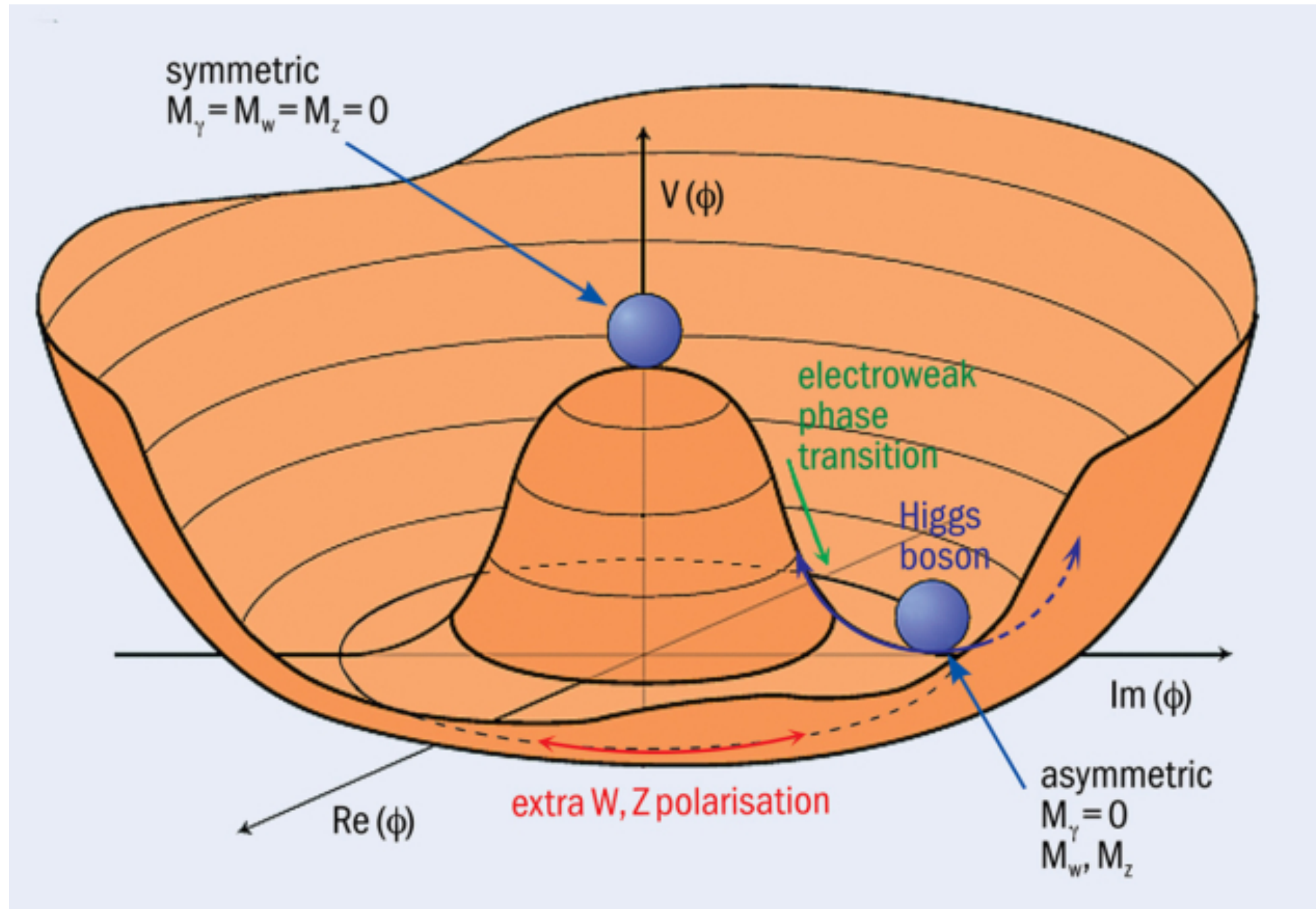


J. Ellis, M. Neubauer, CERN Courier

“We think we have it” ... but it is not the only one ...

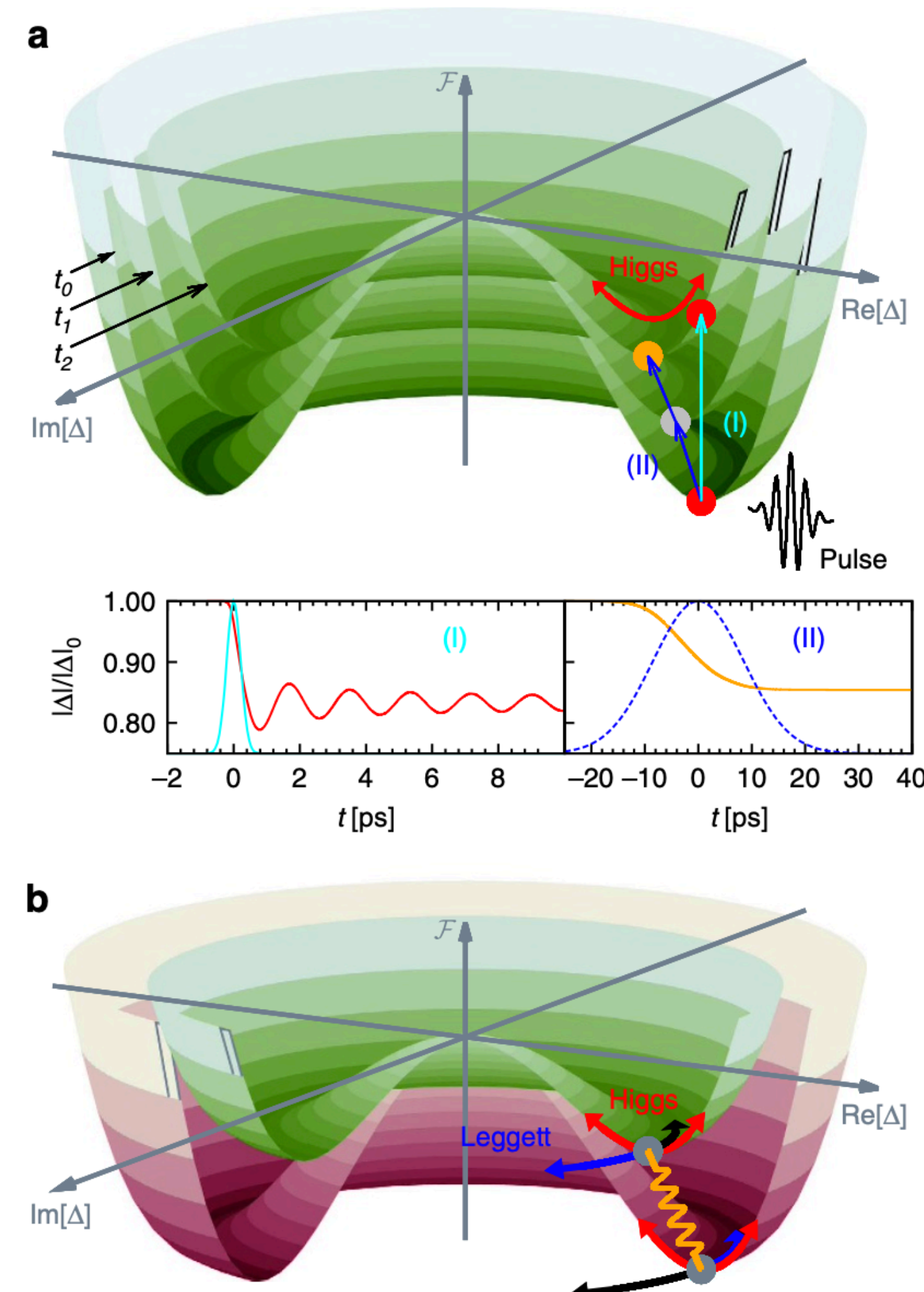
(Rolf Heuer 2012)

# Higgs bosons



J. Ellis, M. Neubauer, CERN Courier

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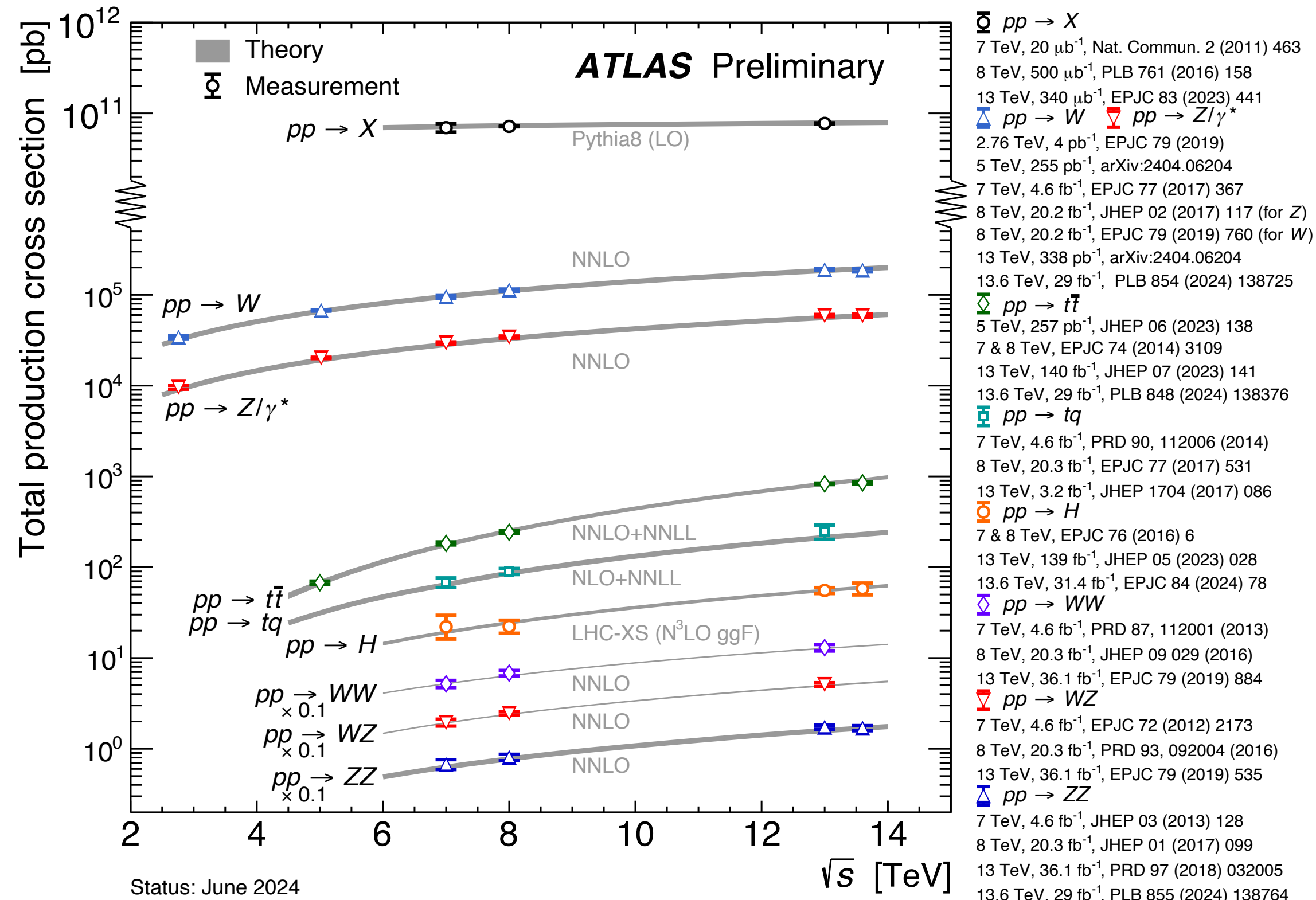


**Figure 1 | Illustration of Leggett and Higgs modes.** (a) Illustration of the excitation process for a one band superconductor. The pump laser pulse

H. Krull et al., Nature Communications 7:11921, 2016

# The LHC as a precision hadron collider

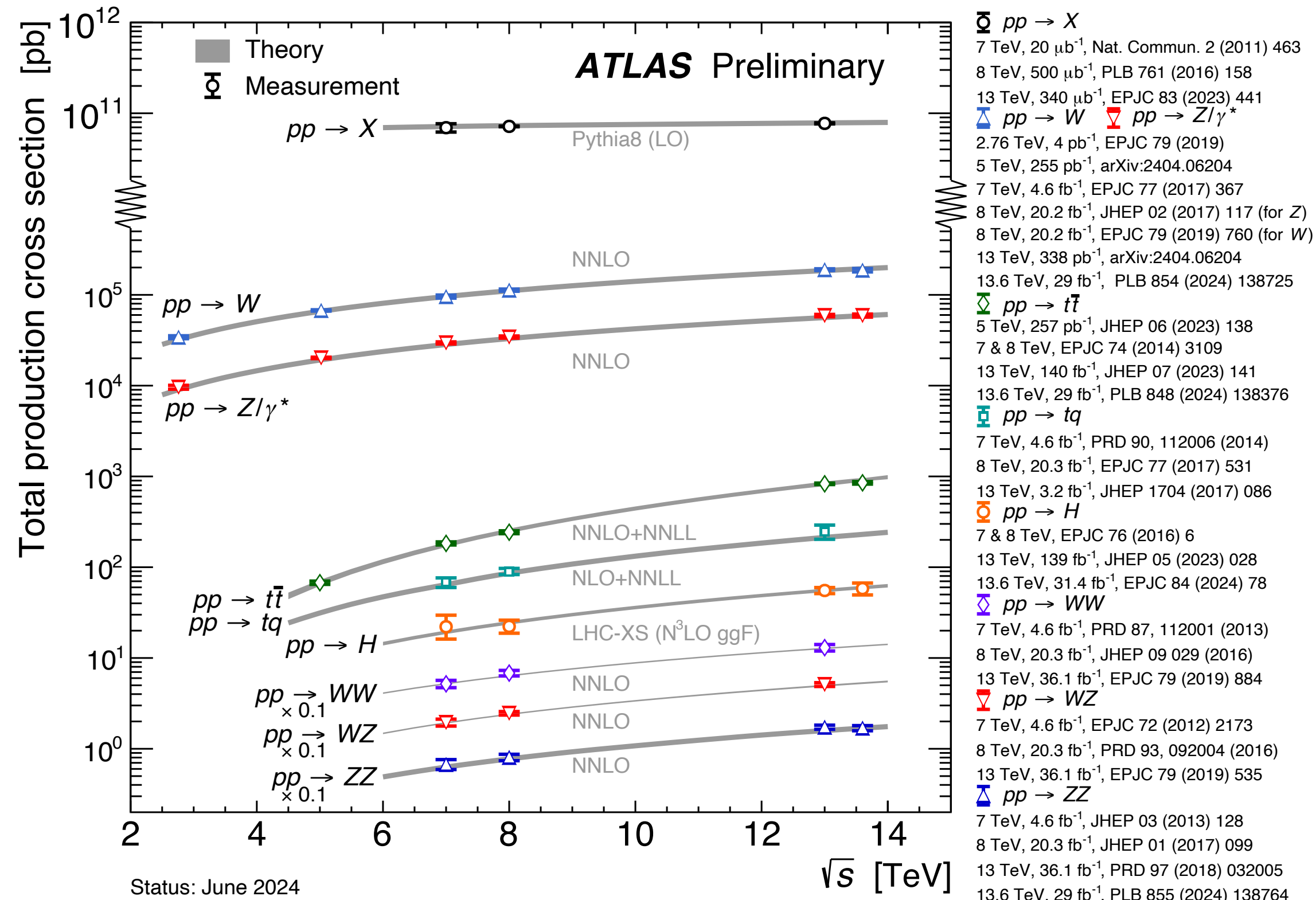
ATL-PHYS-PUB-2024-011



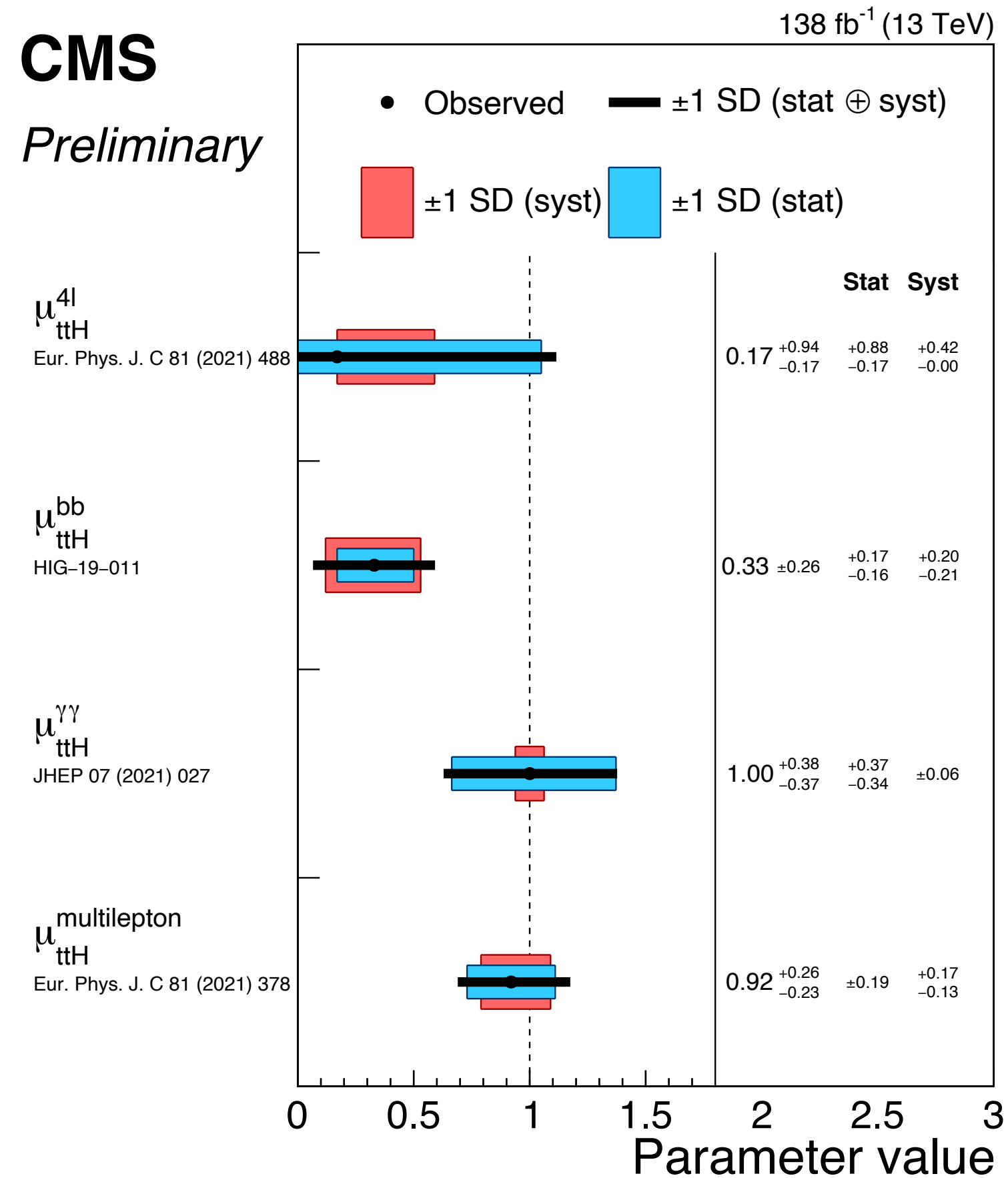
- good news: predictions mostly at NNLO (or higher)

# The LHC as a precision hadron collider

ATL-PHYS-PUB-2024-011



## CMS Preliminary

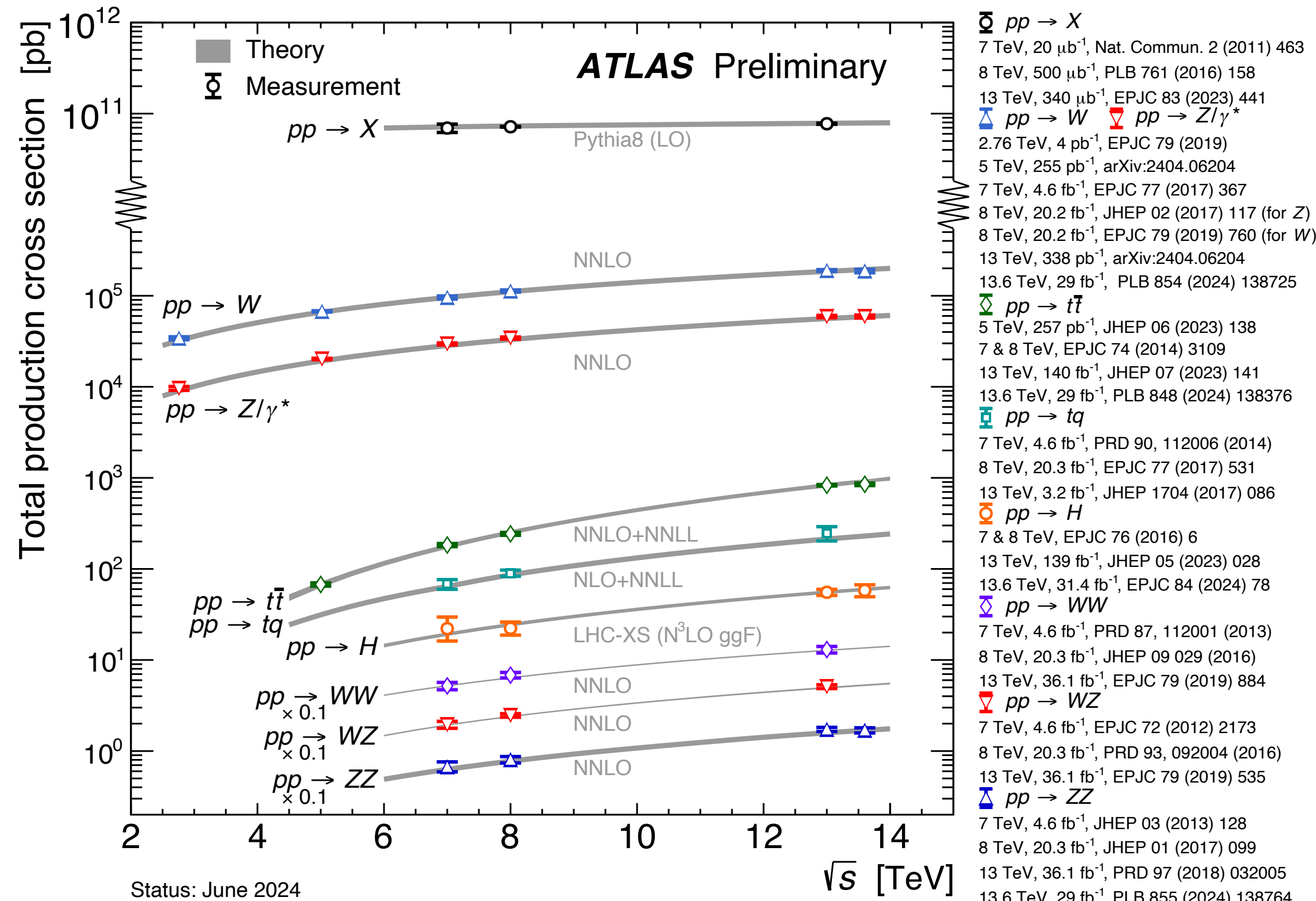


2207.00043 (Nature)

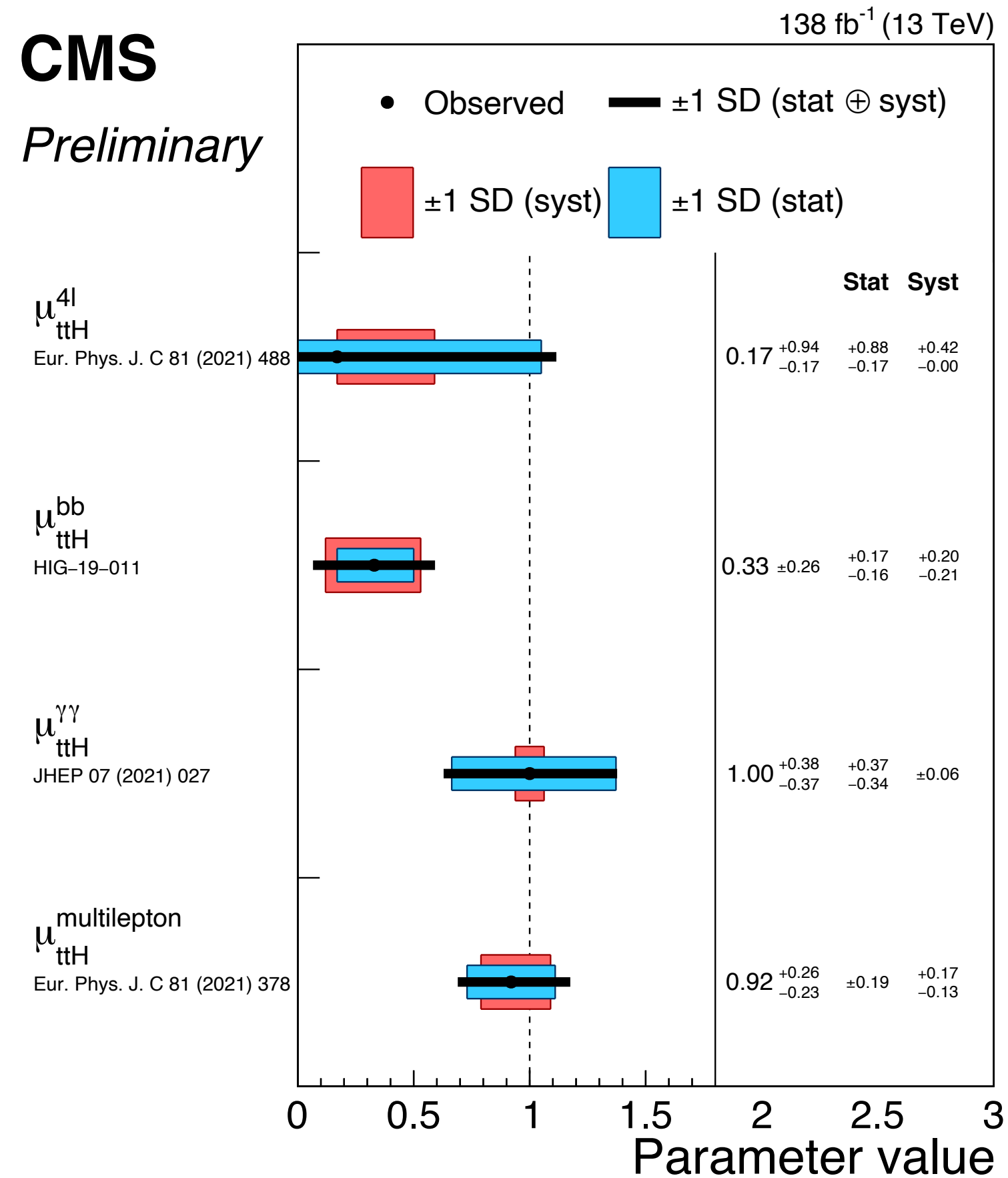
- good news: predictions mostly at NNLO (or higher)
- bad (?) news: need higher precision in both data and predictions to clearly identify deviations from the SM

# The LHC as a precision hadron collider

ATL-PHYS-PUB-2024-011



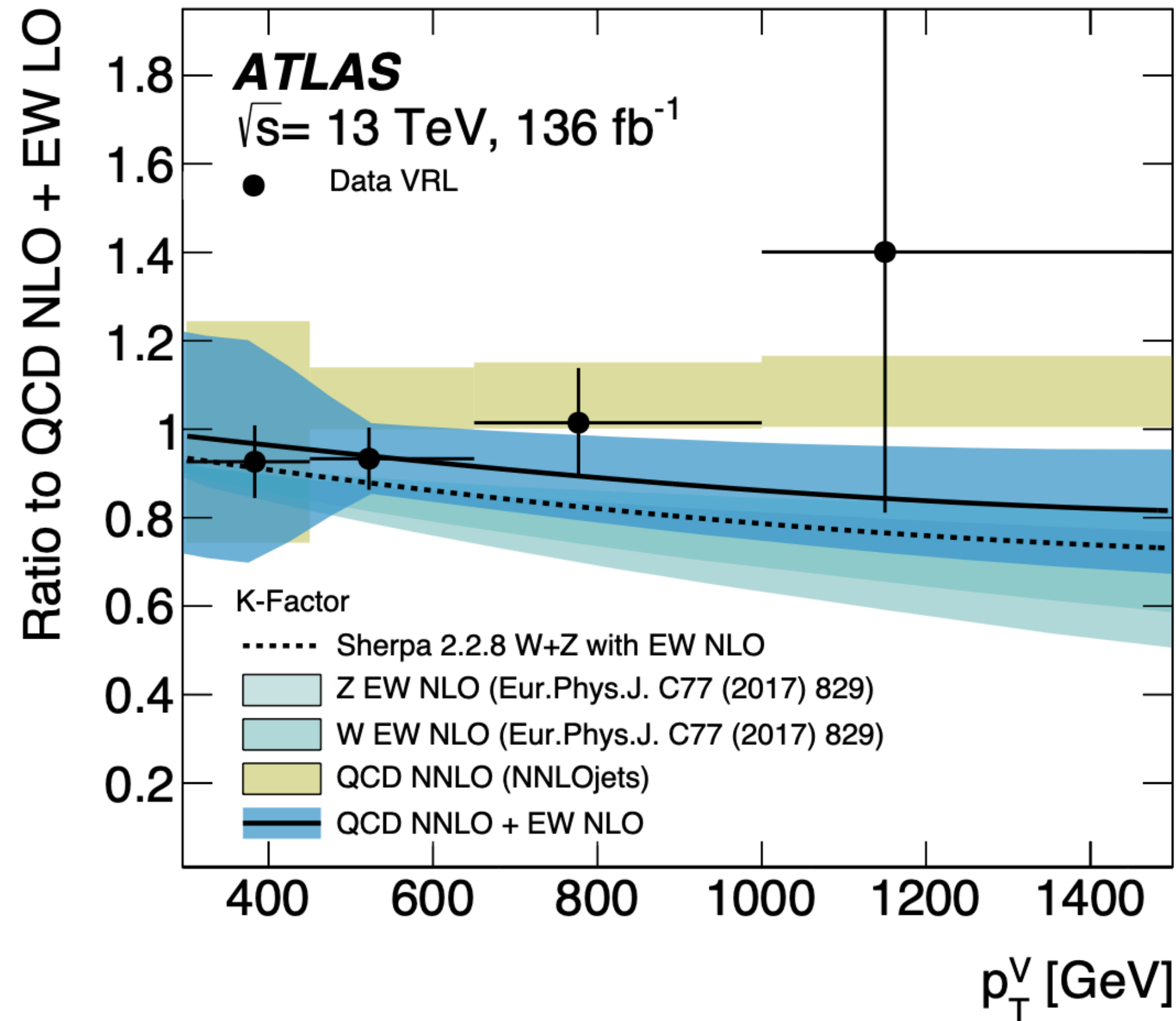
## CMS Preliminary



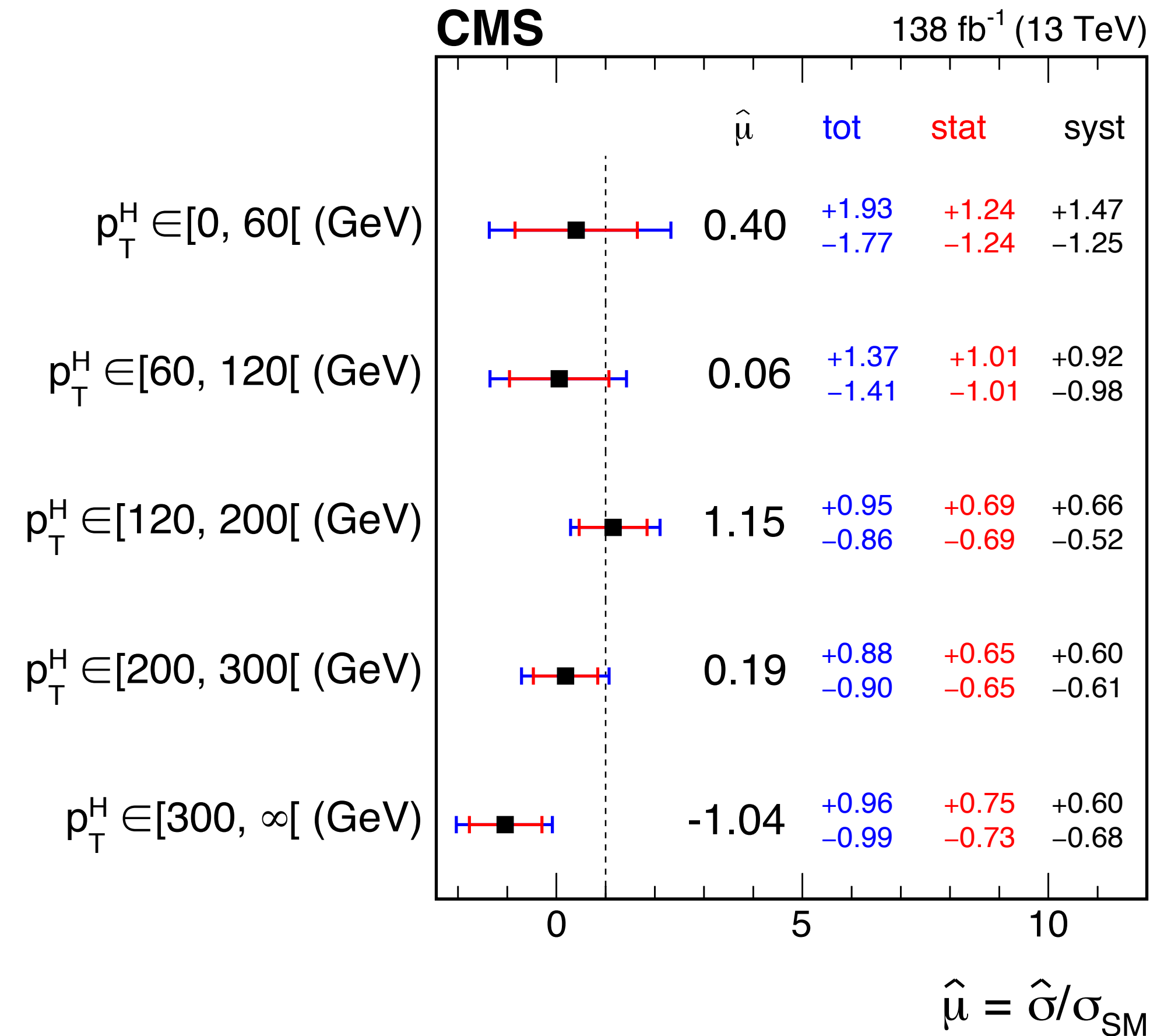
2207.00043 (Nature)

- good news: predictions mostly at NNLO (or higher)
- bad (?) news: need higher precision in both data and predictions to clearly identify deviations from the SM
- HL-LHC will decrease statistical uncertainties substantially → **prime time for precision calculations!**

# Beyond total cross sections



2111.08340



CERN-EP-2024-179

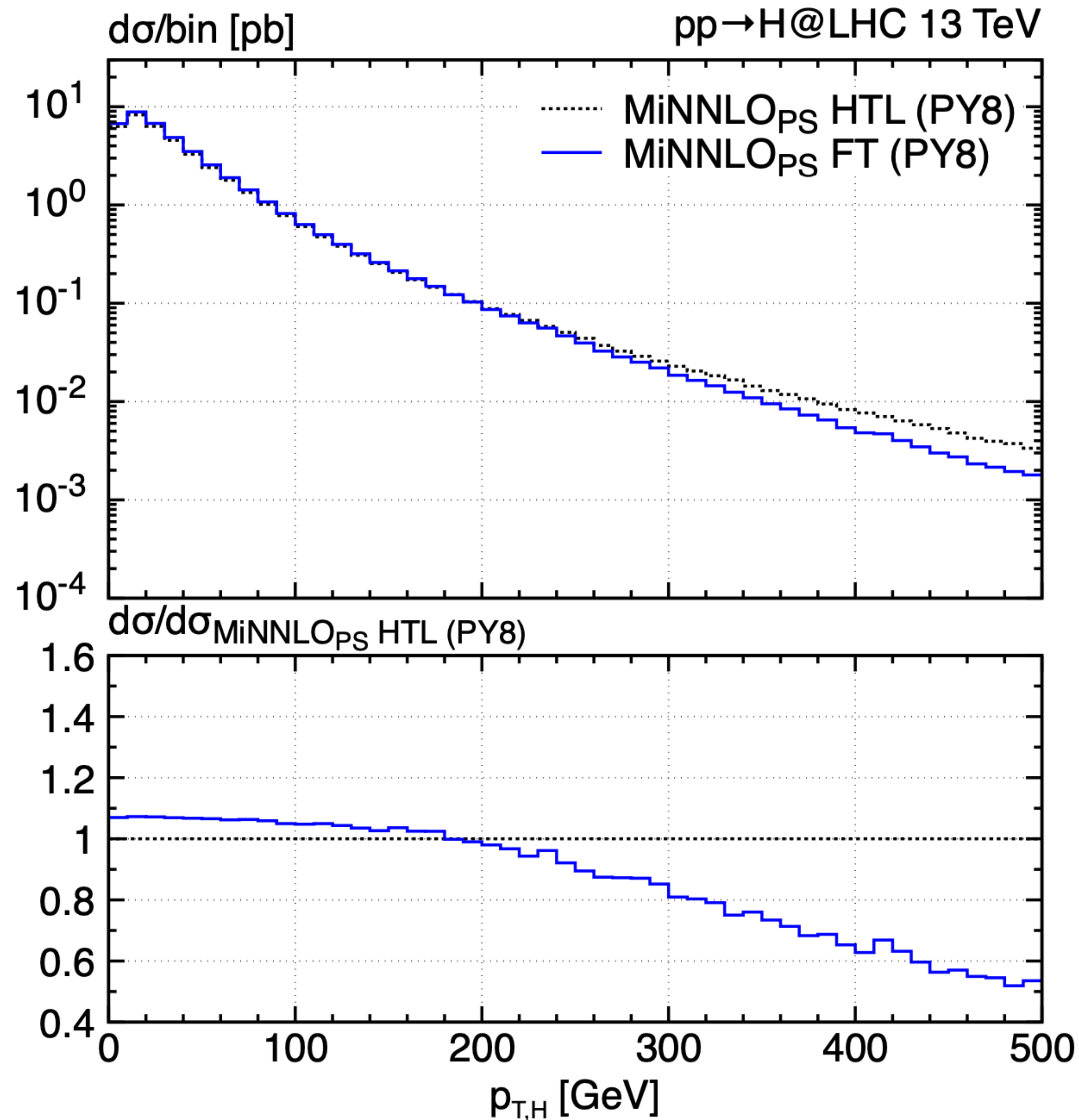
more differential information than total cross section is important



# Outline

- focus on recent results in:
  - gluon fusion Higgs production
  - Higgs + jet production
  - VBF Higgs production
  - ttH production
  - Higgs boson pair production in gluon fusion
- not covered: VH, tH, bbH, couplings to 2nd generation, HHH, ...
- apologies for the biased and incomplete selection

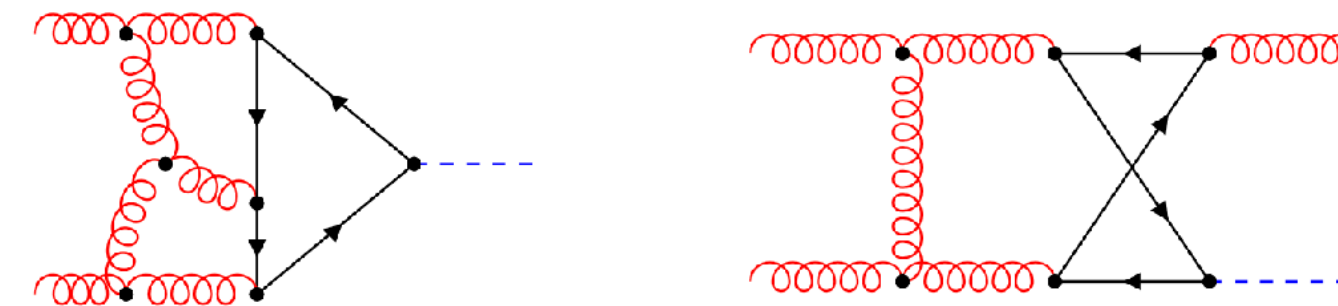
# Higgs production at NNLO+PS



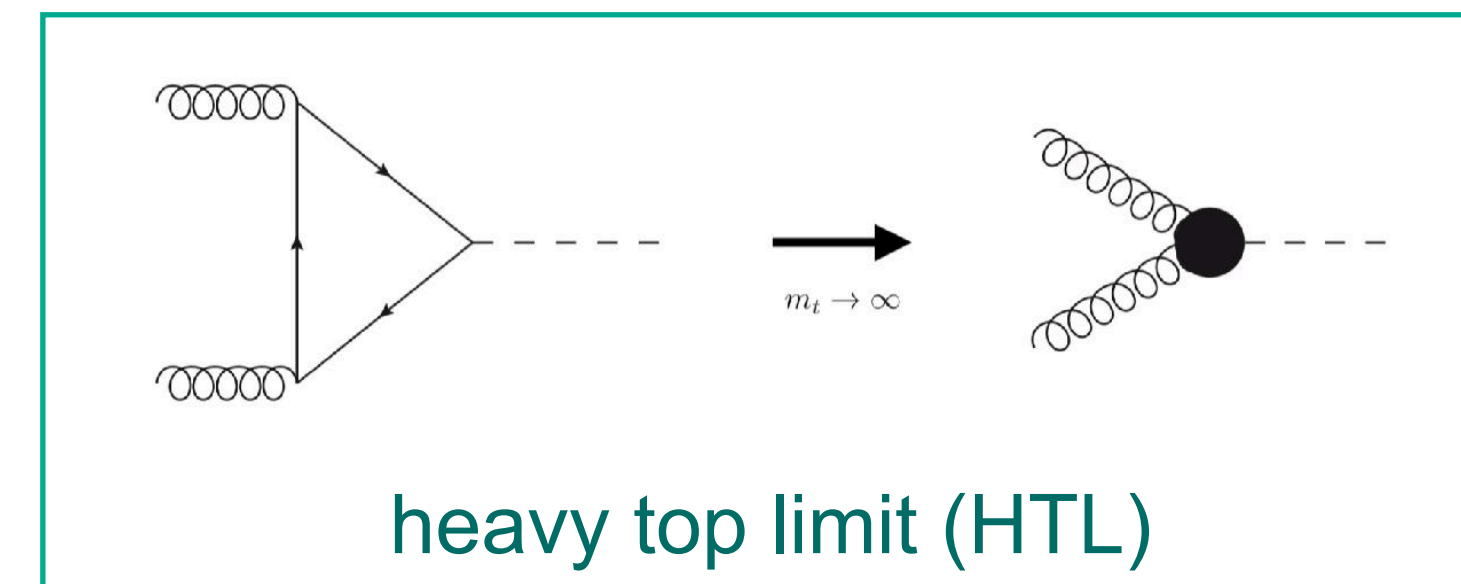
Niggetiedt, Wiesemann 2407.01354

includes  $gg \rightarrow H$  up to 3 loops and  $pp \rightarrow H + \text{jet}$  up to two loops with full top mass dependence

Czakon, Harlander, Klappert, Niggetiedt '20



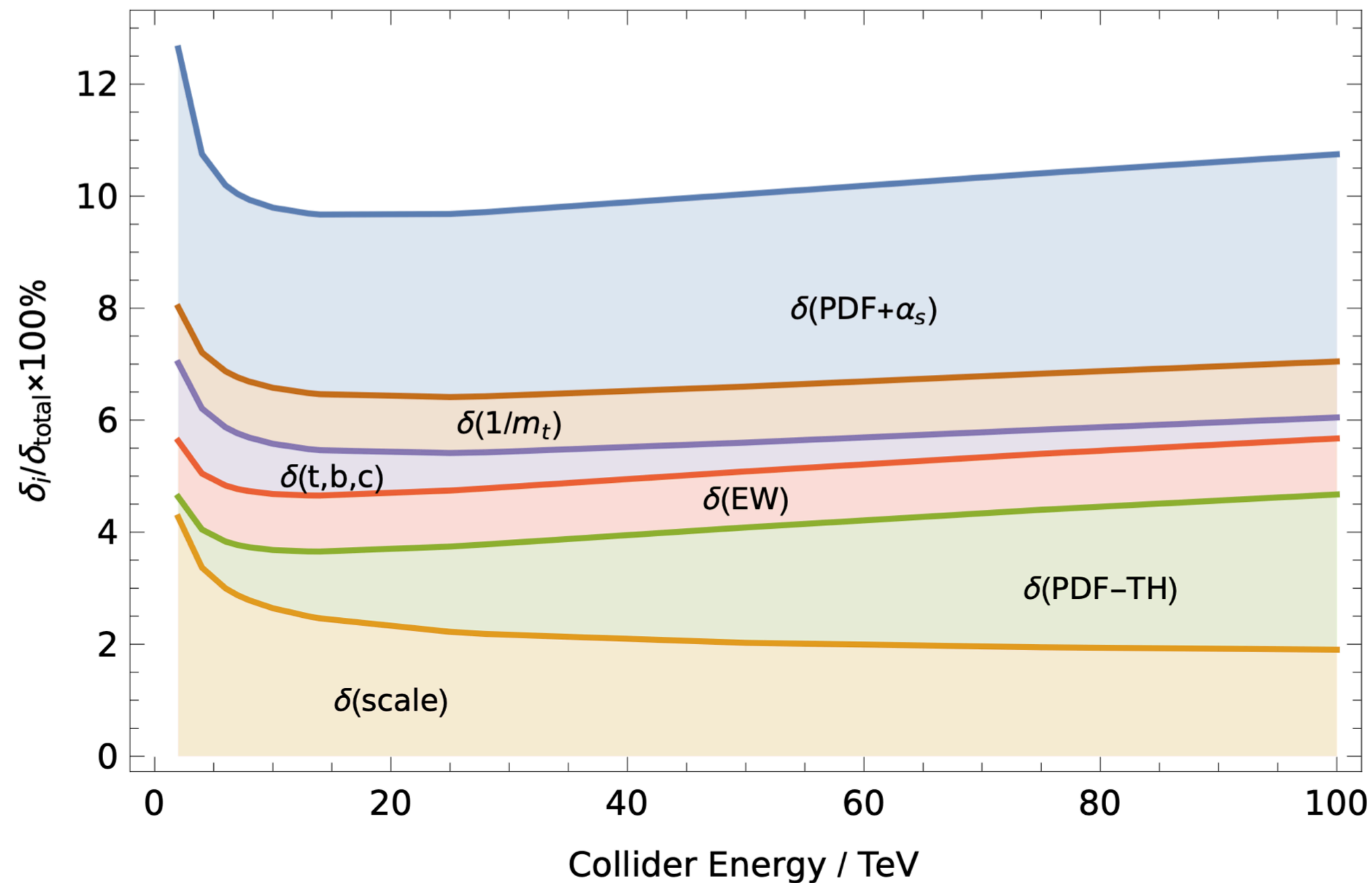
uses  $\text{MiNNLO}_{\text{PS}}$  Monni, Nason, Re, Wiesemann, Zanderighi 1908.06987



more than 40% difference between **full theory (FT)** and heavy top limit (HTL) in tail of  $p_{T,H}$  distribution

# Higgs production in gluon fusion

uncertainty budget 6 years ago Dulat, Lazopoulos, Mistlberger '18  
N3LO in heavy top limit

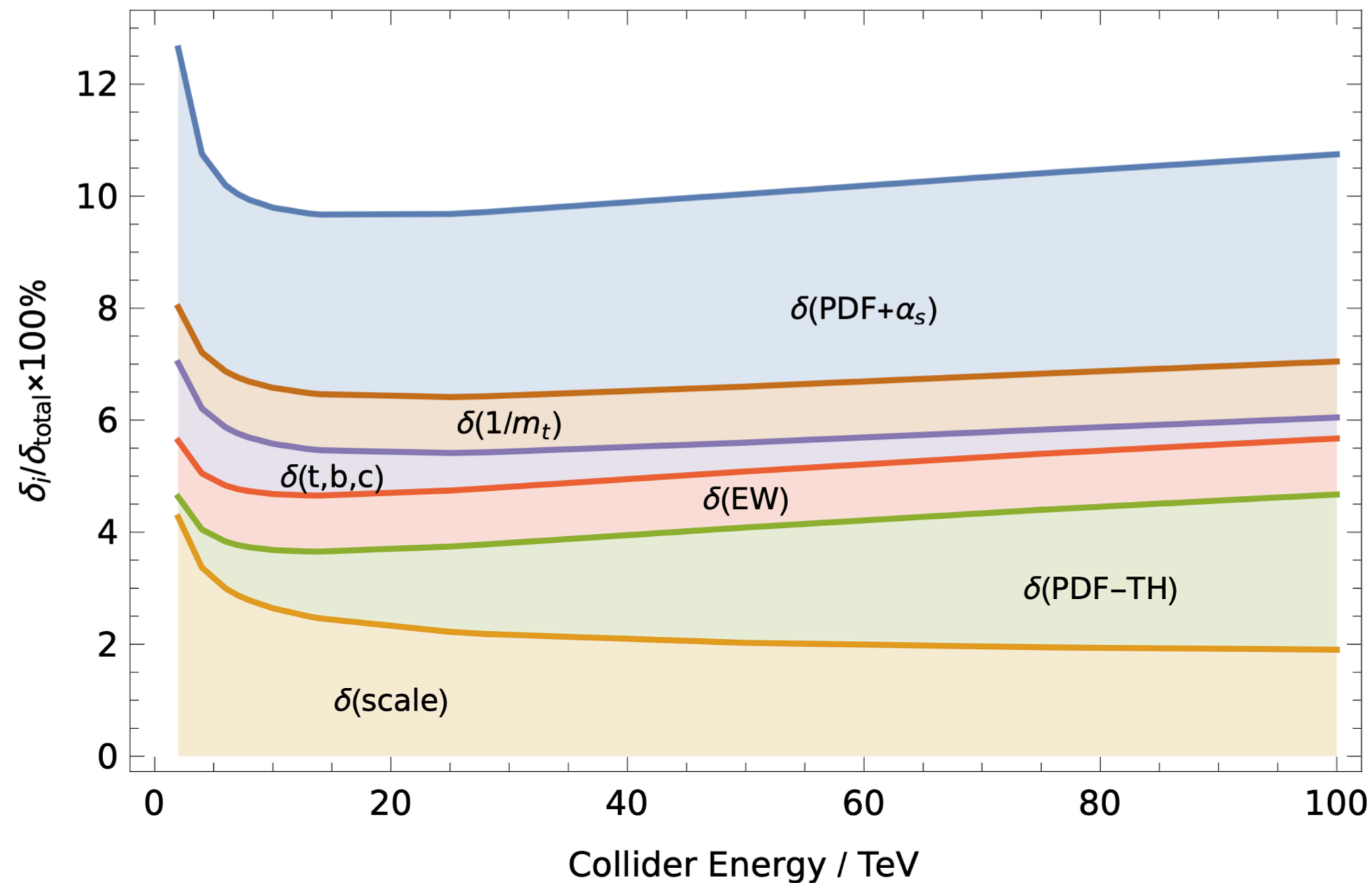


see PDF sessions and talk by Valentina Guglielmi

basically removed (NNLO with full top mass)  
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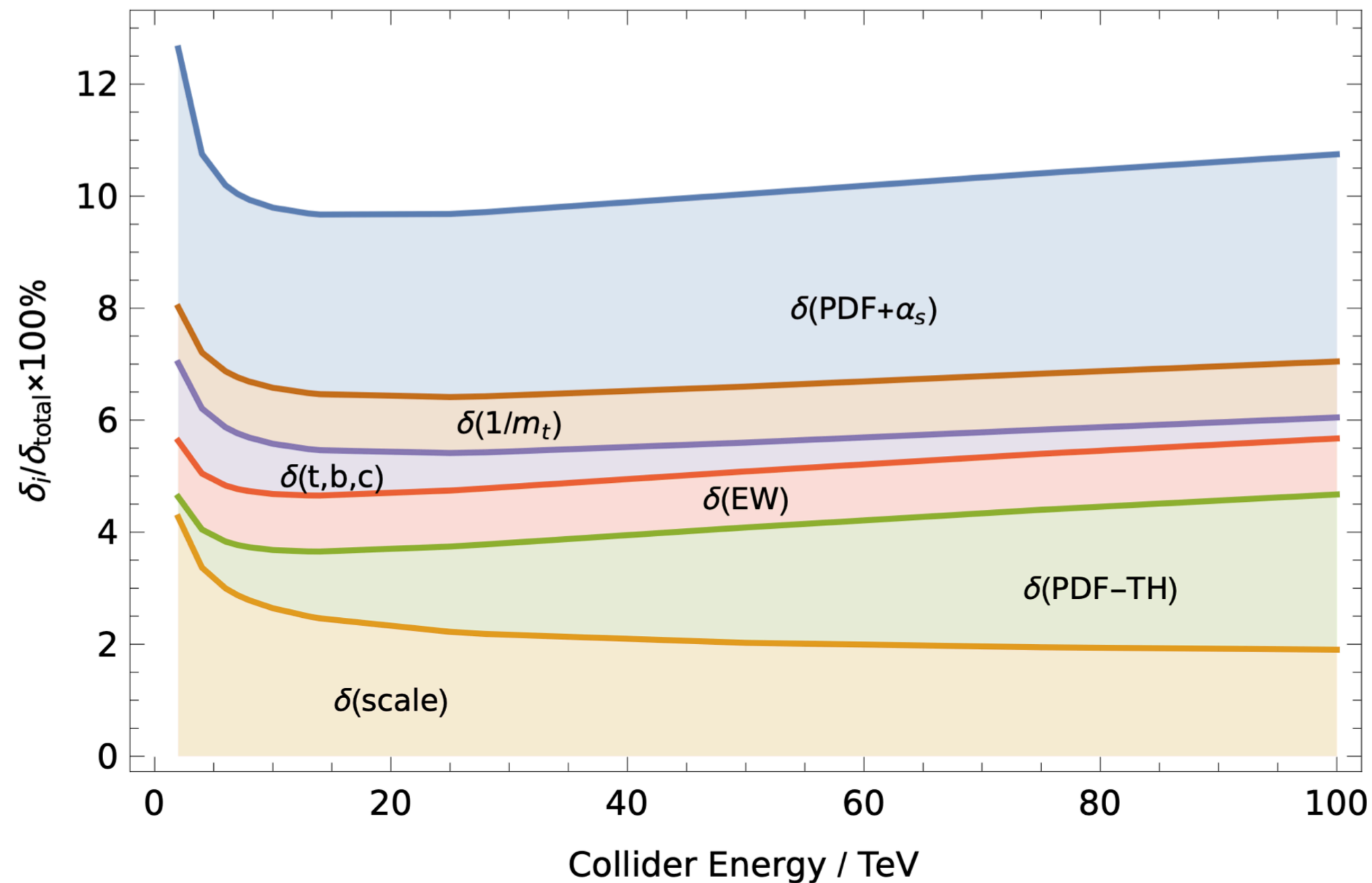
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t-b interference at NNLO calculated recently  
Czakon, Eschment, Niggetiedt, Poncelet, Schellenberger '23, '24

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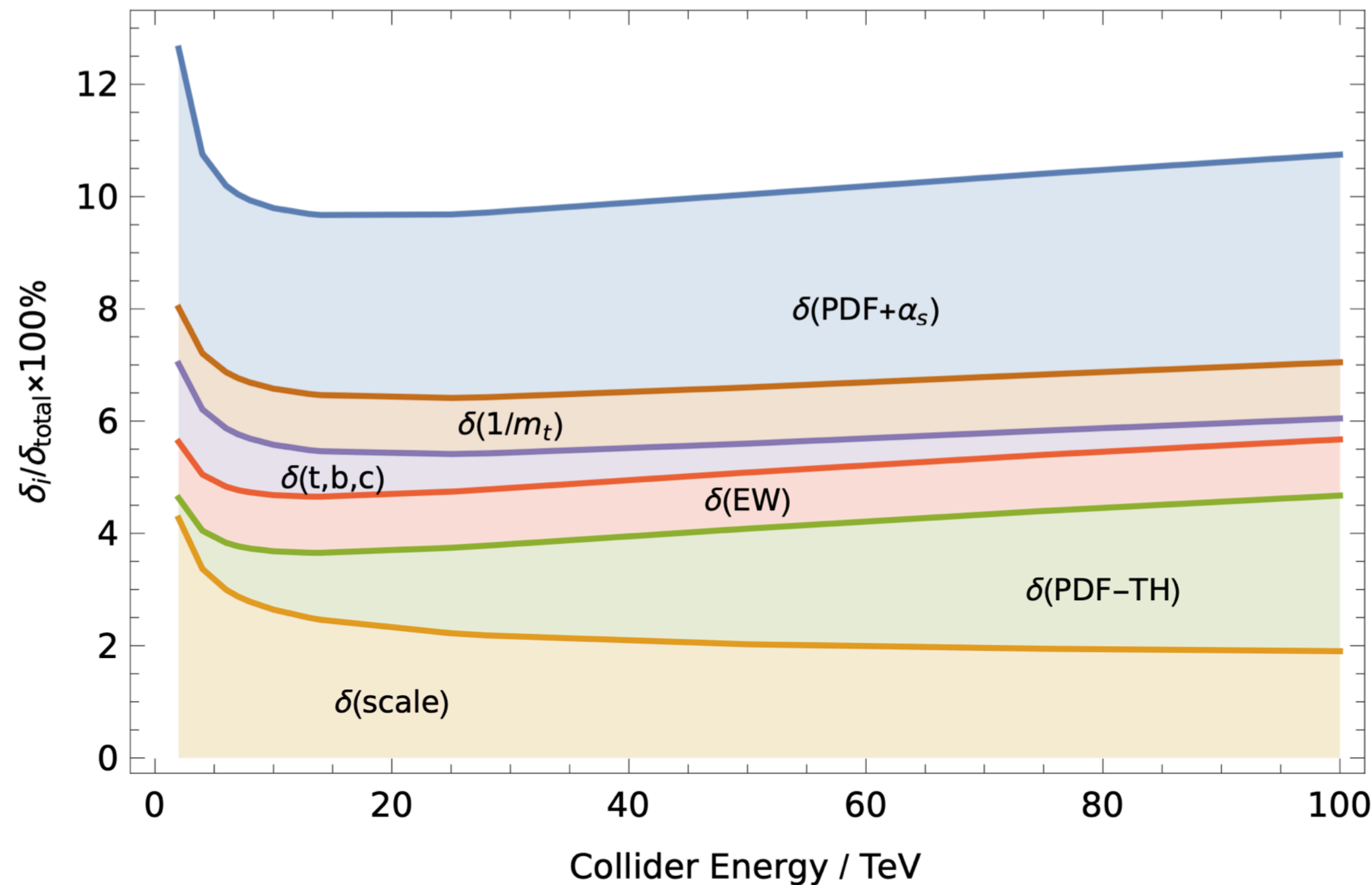
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reduced to 0.6%

Bechetti et al '20, '21, Bonetti et al '18, '20, '22

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Bechetti et al '20, '21, Bonetti et al '18, '20, '22

mismatch between PDF (NNLO) and ME (N3LO)

towards N3LO PDFs: MSHT 2207.04739,

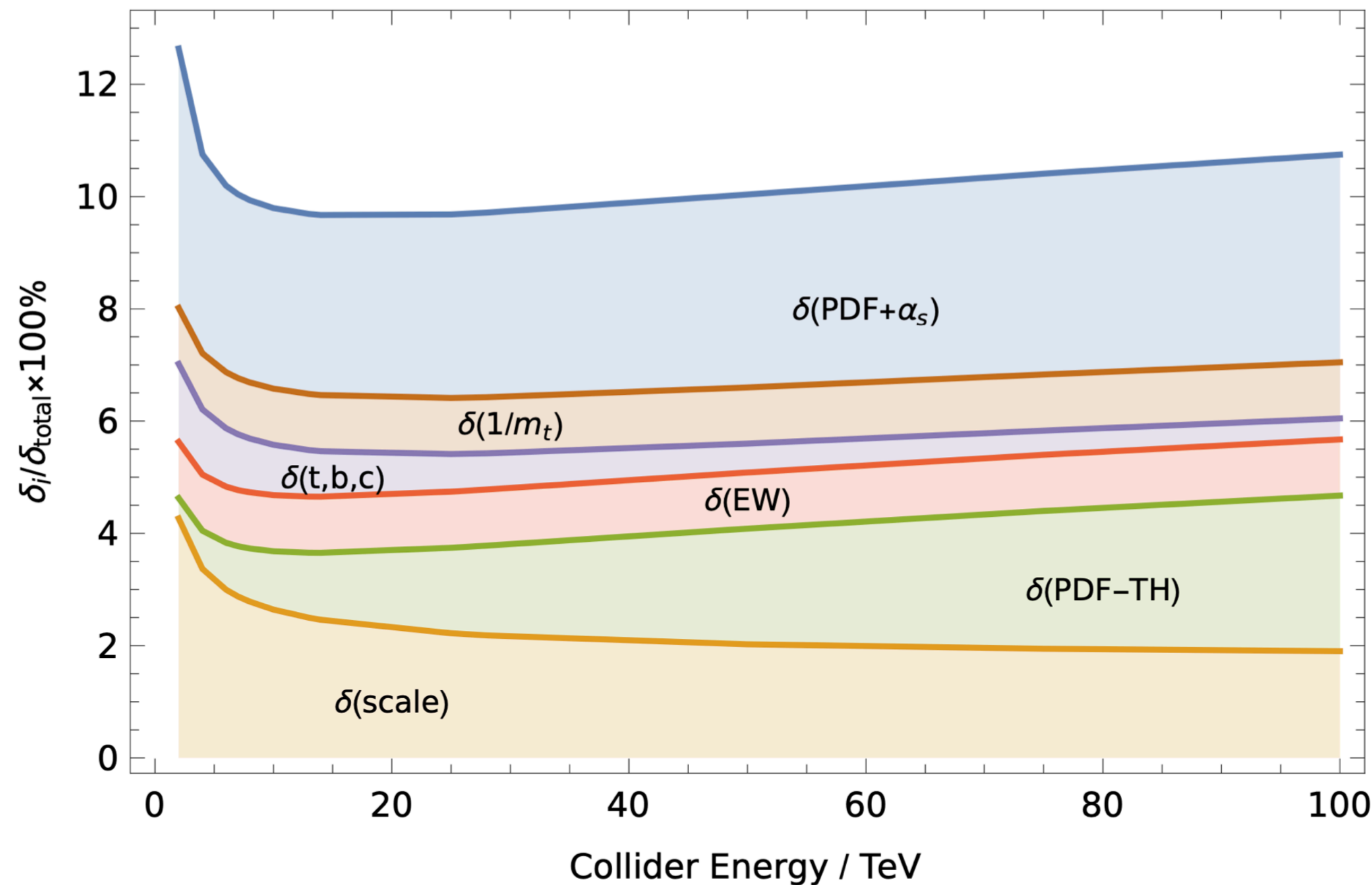
NNPDF4.0 2402.18635, Cooper-Sarkar et al. 2406.16188,

Falcioni et al 2302.07593, Guan et al. 2408.03019,

Gehrmann, Manteuffel, Sotnikov, Yang '23, '24

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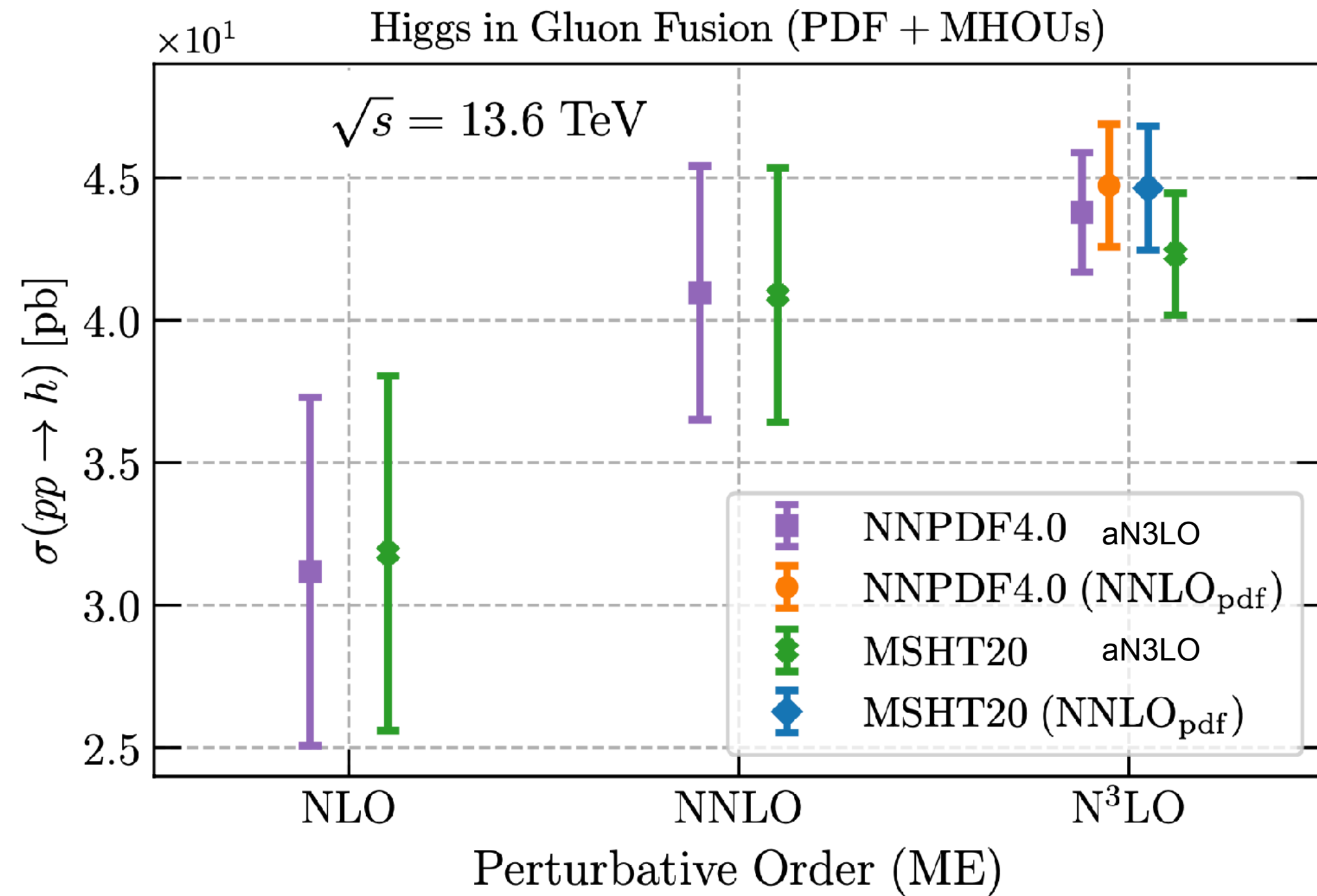
Falcioni et al 2302.07593, Guan et al. 2408.03019,

Gehrmann, Manteuffel, Sotnikov, Yang '23, '24

N4LO soft-virtual approx. Das, Moch, Vogt '20;

4-loop form factor Lee, Manteuffel, Schabinger, Smirnov, Smirnov Steinhauser '22, '23

# approximate N3LO PDFs

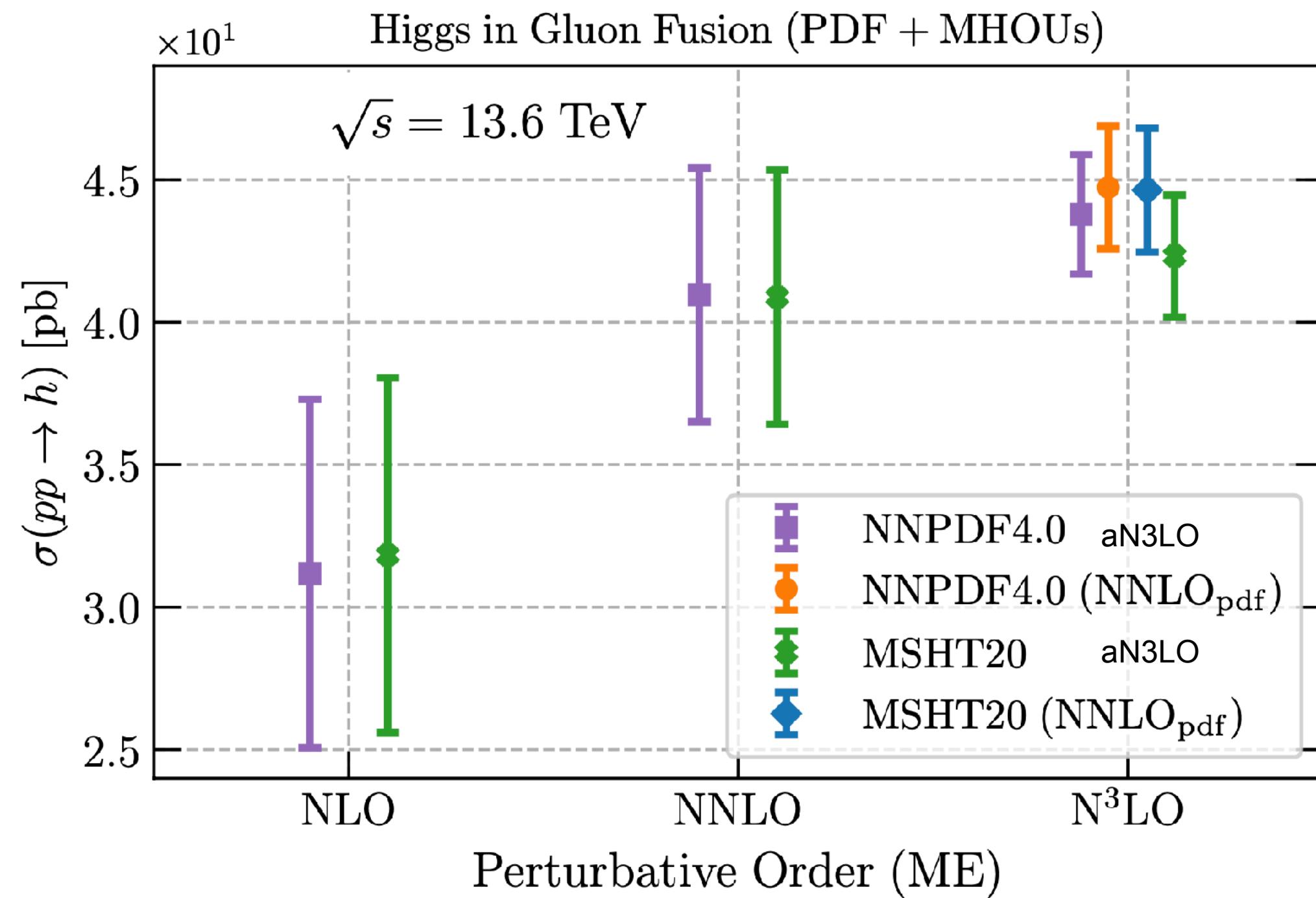


NNPDF collaboration, 2402.18635

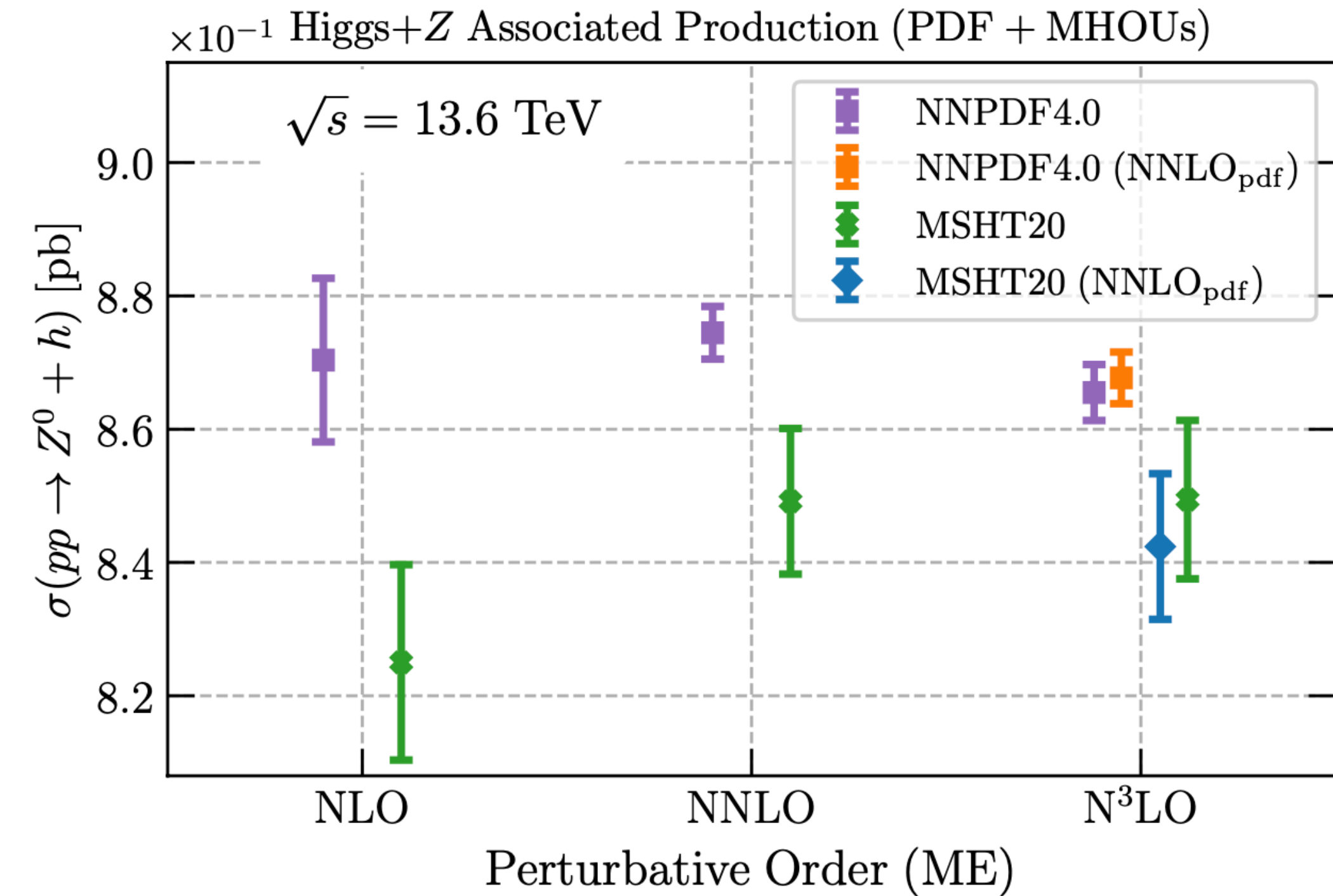
ggF: reasonable agreement with different PDF sets



# approximate N3LO PDFs



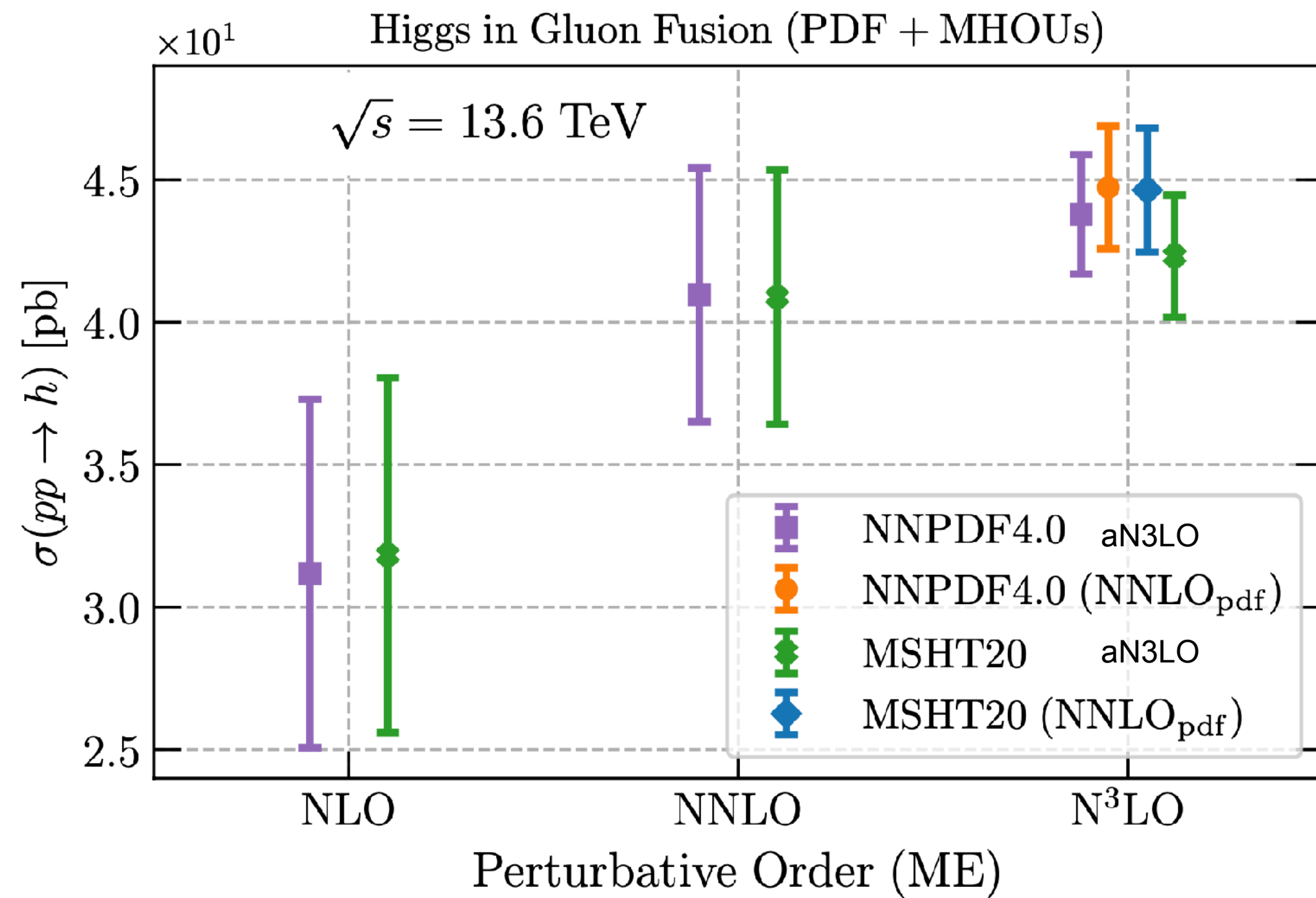
NNPDF collaboration, 2402.18635



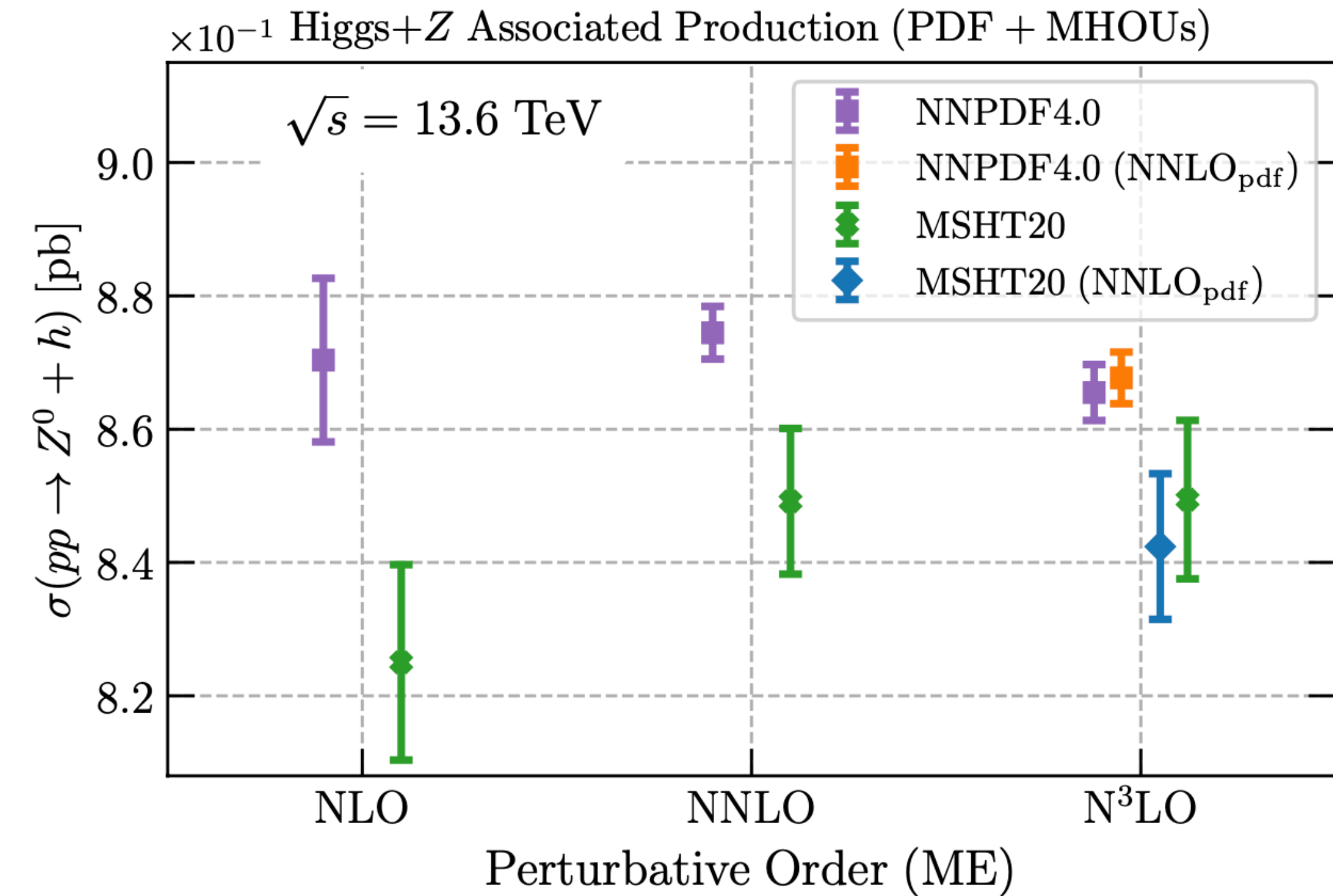
ggF: reasonable agreement with different PDF sets

less so for H+Z production

# approximate N3LO PDFs



NNPDF collaboration, 2402.18635



ggF: reasonable agreement with different PDF sets

less so for H+Z production

see talks by Tongzhi Yang, Sven Moch, and PDF sessions Tuesday and Thursday

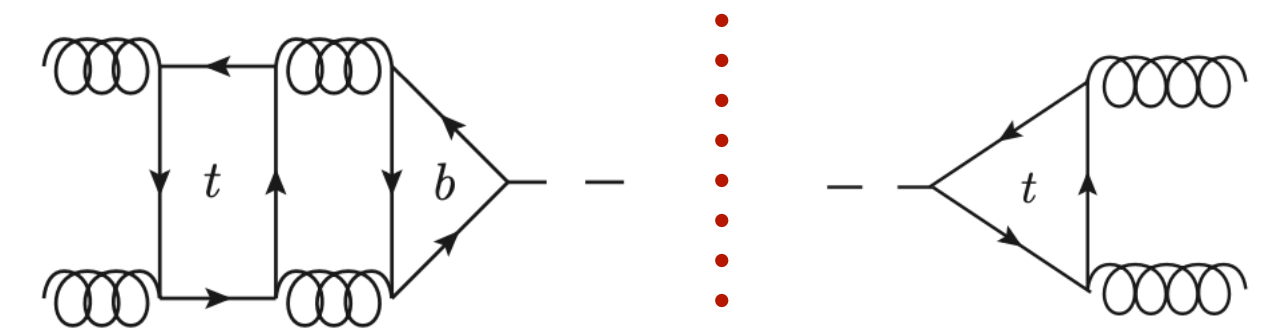
# Higgs production in gluon fusion

**new:** top-bottom interference effects at NNLO

Pietrulewicz, Stahlhofen 2302.06623

Niggetiedt, Usowitsch 2312.05297 (3-loop form factor with 3 mass scales)

Czakon, Eschment, Niggetiedt, Poncelet, Schellenberger 2312.09896 (t-b interference), 2407.12413 (OS vs MSbar, 4FS/5FS)

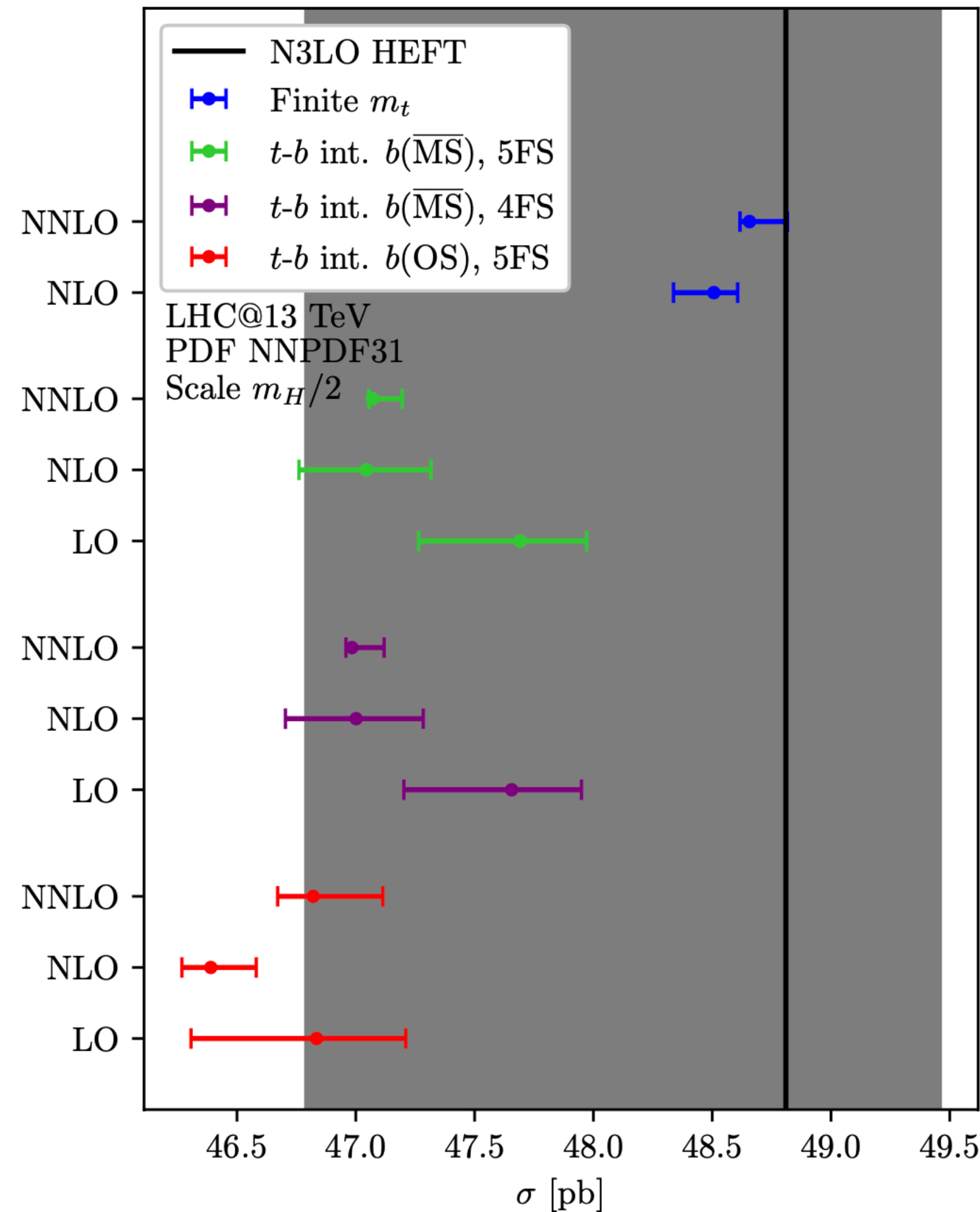


Order	$\sigma_{\text{HEFT}}$ [pb]	$(\sigma_t - \sigma_{\text{HEFT}})$ [pb]	$\sigma_{t \times b}$ [pb]	$\sigma_{t \times b} / \sigma_{\text{HEFT}}$ [%]
$\sqrt{s} = 13 \text{ TeV}$				
$\mathcal{O}(\alpha_s^2)$	+16.30	–	–1.975	
LO	$16.30^{+4.36}_{-3.10}$	–	$-1.98^{+0.38}_{-0.53}$	–12
$\mathcal{O}(\alpha_s^3)$	+21.14	–0.303	–0.446(1)	
NLO	$37.44^{+8.42}_{-6.29}$	$-0.303^{+0.10}_{-0.17}$	$-2.42^{+0.19}_{-0.12}$	$-6.5^{+0.9}_{-0.8}$
$\mathcal{O}(\alpha_s^4)$	+9.72	+0.147(1)	+0.434(8)	
NNLO	$47.16^{+4.21}_{-4.77}$	$-0.156(1)^{+0.13}_{-0.03}$	$-1.99(1)^{+0.30}_{-0.15}$	$-4.2^{+0.9}_{-0.8}$

M. Niggetiedt, HP2 2024

t-b interference effect larger than pure top mass effect, also larger than NLO scale uncertainties

# on-shell versus $\overline{\text{MS}}$ scheme



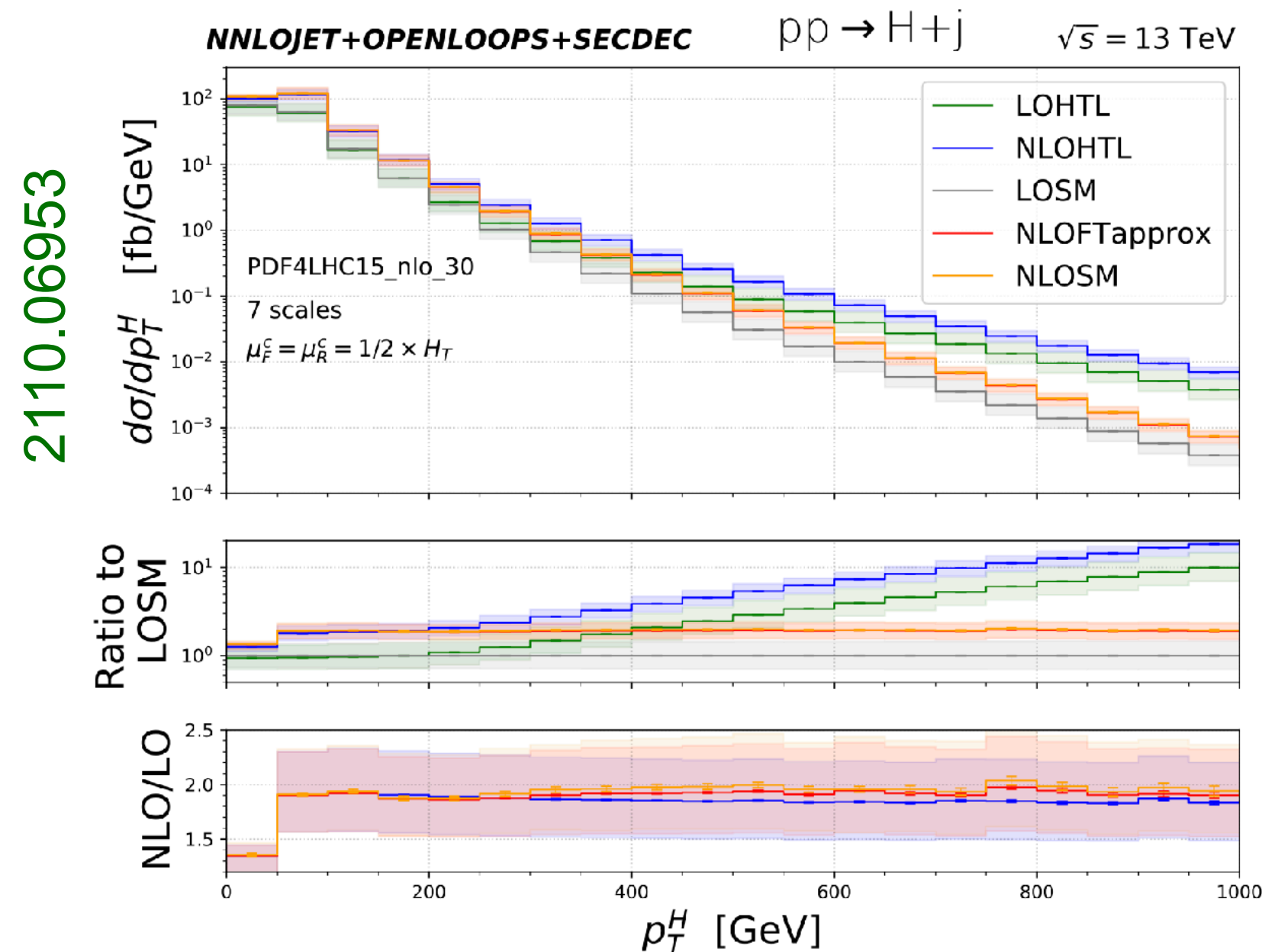
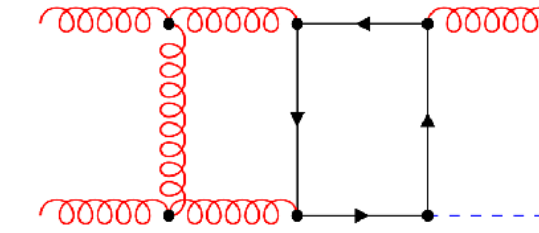
Tom Schellenberger, P3H YS Meeting 2024

- better perturbative convergence for  $b$  in  $\overline{\text{MS}}$  scheme
- difference between 4 flavour scheme and 5 flavour scheme rather small

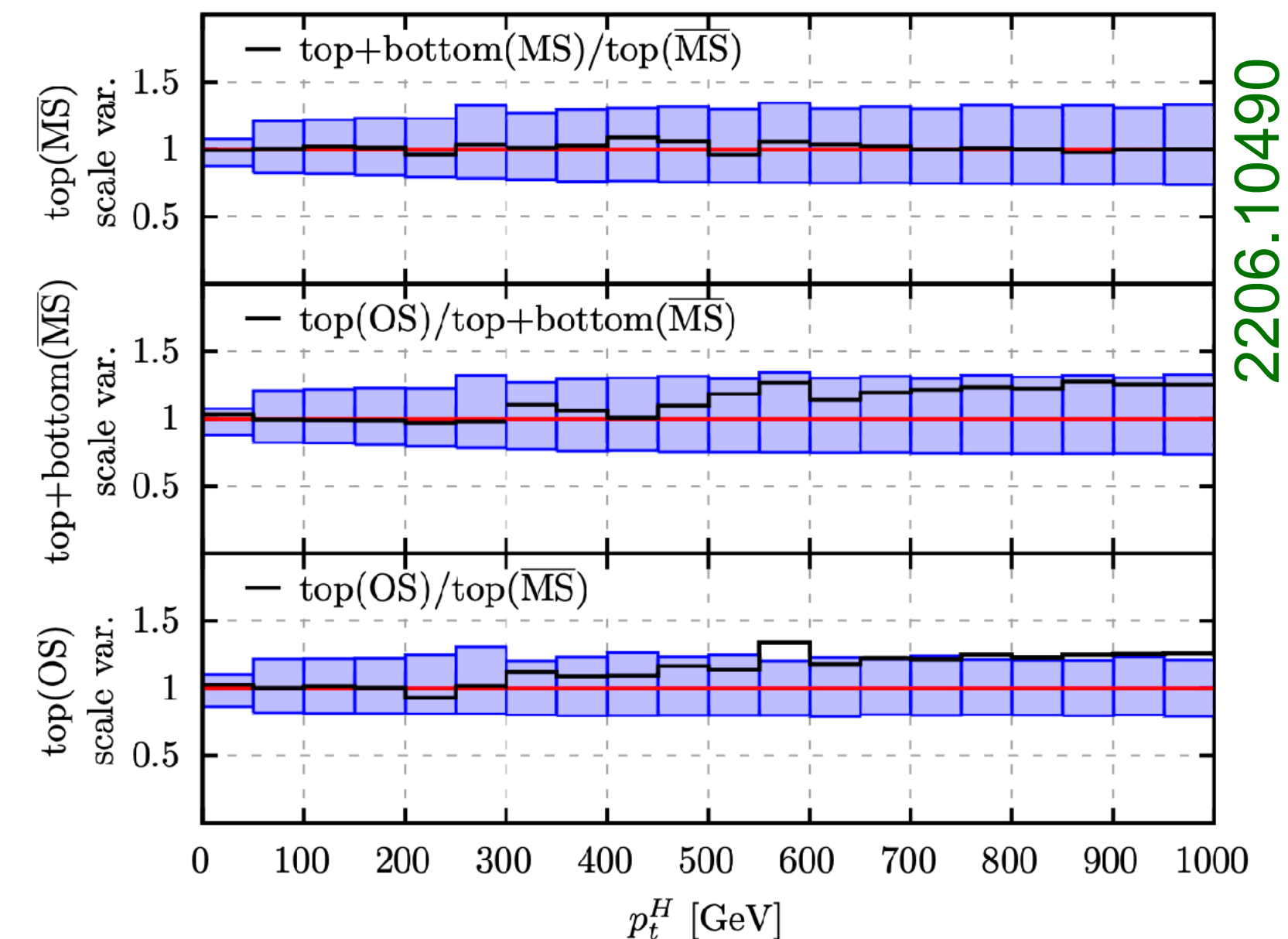
(HEFT here means heavy top limit, rescaled with full LO)

# Higgs+jet (with mass dependence)

- NLO QCD (numerically) [Jones, Kerner, Luisoni 1802.00349](#)
- boosted Higgs, NLO QCD+NNLO HTL, generators [Becker, Caola et al. \(HXSWG note\) 2005.07762, SciPost 2024](#)
- top mass effects in H+jet and H+2jets [Chen, Huss, Jones, Kerner, Lang, Lindert, Zhang 2110.06953](#)
- NLO QCD including bottom mass: [Bonciani, Del Duca, Frellesvig, Hidding, Hirschi 2206.10490](#);  
[Czakon, Eschment, Niggetiedt, Poncelet, Schellenberger 2312.09896, 2407.12413](#) (ingredient of ggH NNLO)
- EW corrections to ggHg in the large- $m_t$  limit: [Davies, Schönwald, Steinhauser, Zhang 2308.01355](#)



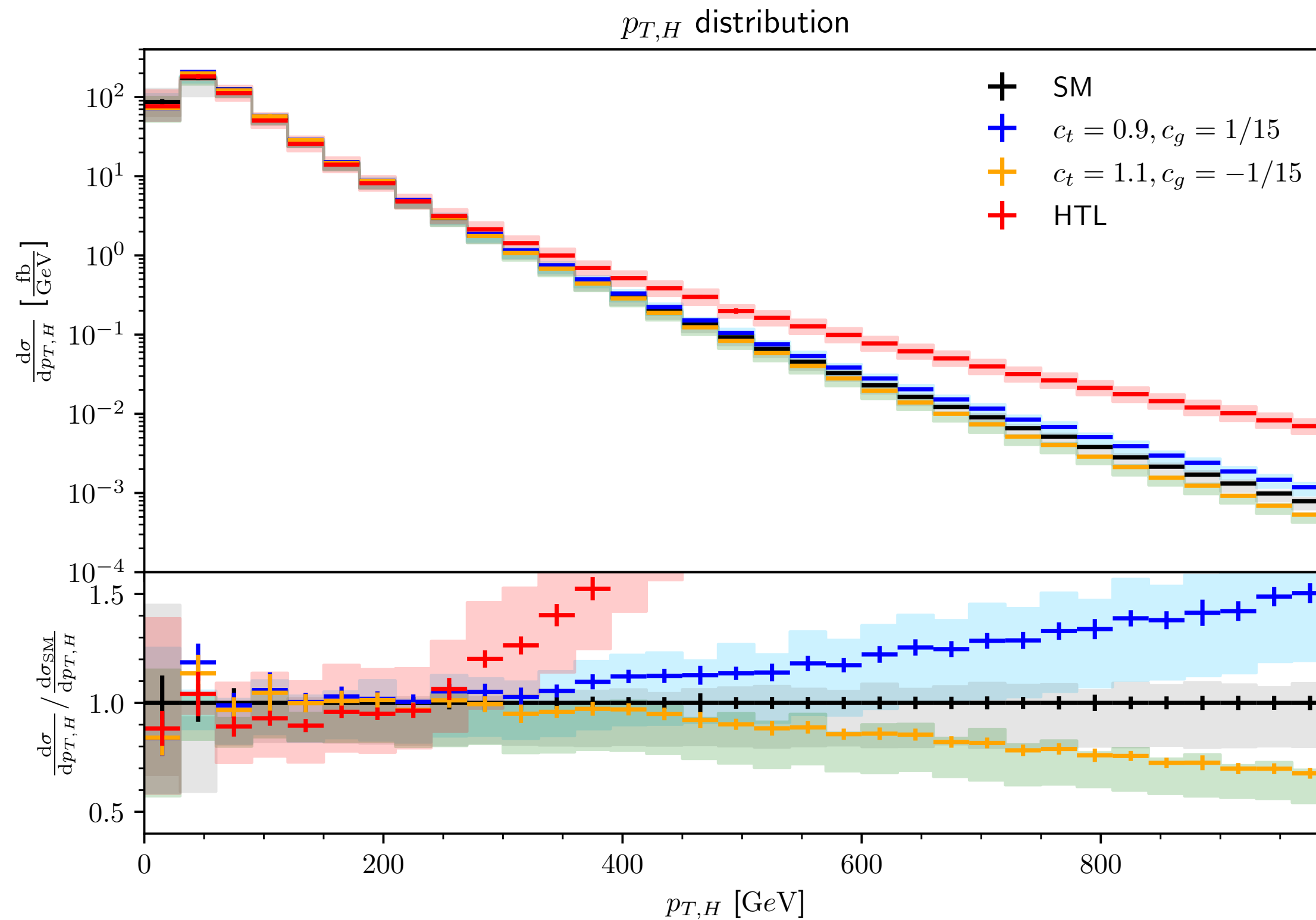
- large difference to heavy top limit at large  $p_{T,H}$
- **full NLO** and **FTapprox** (virtual part in HTL) very similar  
will this also be true for H+2j ?
- difference top on-shell vs MSbar starts to exceed scale uncertainties at large  $p_{T,H}$



# boosted Higgs at NLO with anomalous couplings

Campillo, GH, Kerner, Kunz 2409.05728 (based on SM NLO calculation of Jones, Kerner, Luisoni '18)

NLO with full top mass including anomalous couplings

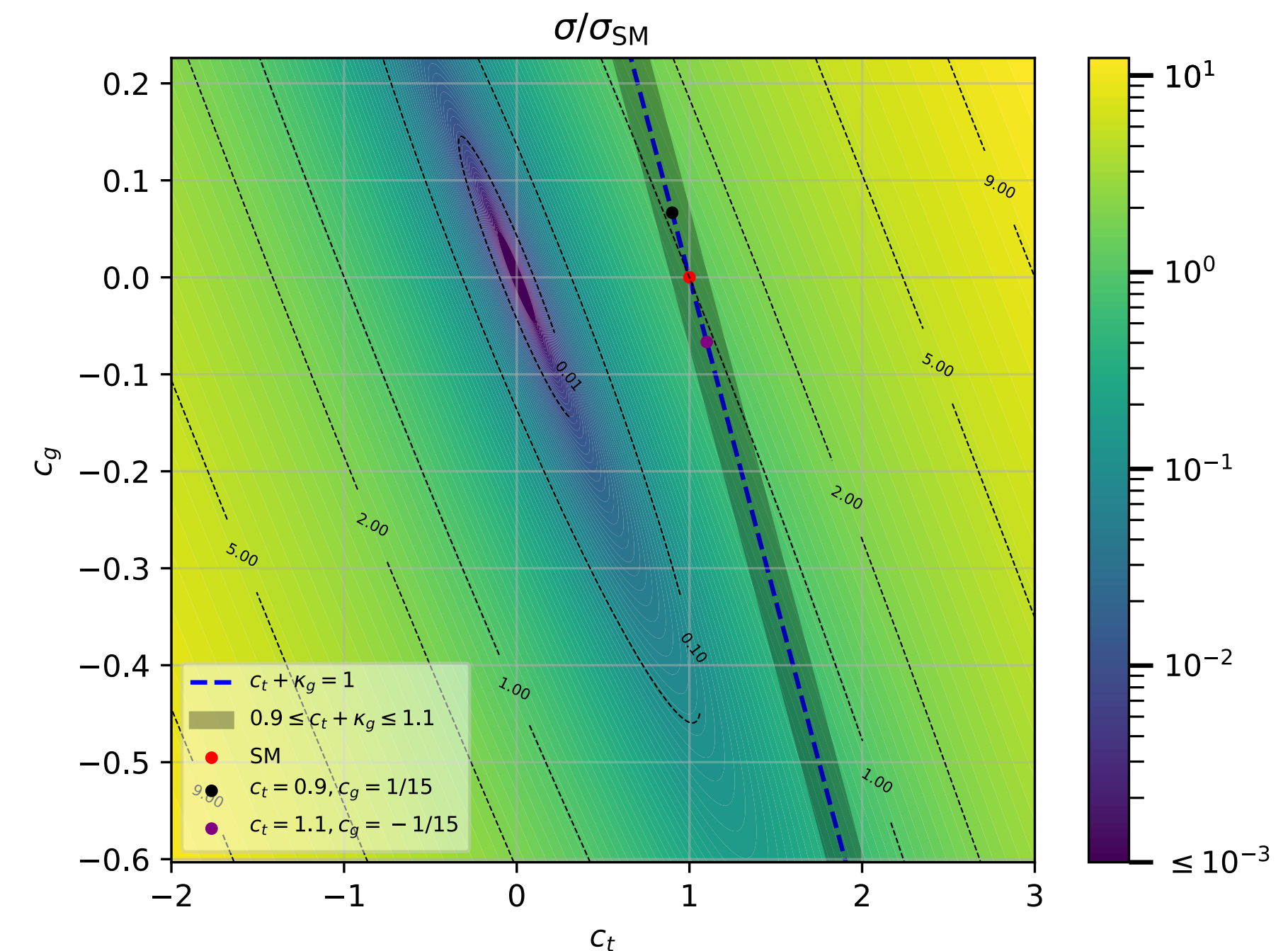


effects of  $c_t, c_g$  exceed scale uncertainties at large  $p_{T,H}$

$p_{T,H}$ cut [GeV]	$\sigma_{EFT}/\sigma_{SM}$	
	LO	NLO
200	$1.021 \pm 0.002$	$1.02 \pm 0.02$
400	$1.118 \pm 0.007$	$1.11 \pm 0.01$
600	$1.251 \pm 0.012$	$1.23 \pm 0.01$
800	$1.407 \pm 0.016$	$1.37 \pm 0.02$

$(c_t, c_g) = (0.9, 1/15)$

40% effect for highly boosted Higgs



# Towards N3LO Higgs+jet production in the HTL

- at NLO scale uncertainties are  $\sim 15\%$
- at NNLO in the HTL still  $O(10\%)$  uncertainties
- also addresses N3LO V+jet production

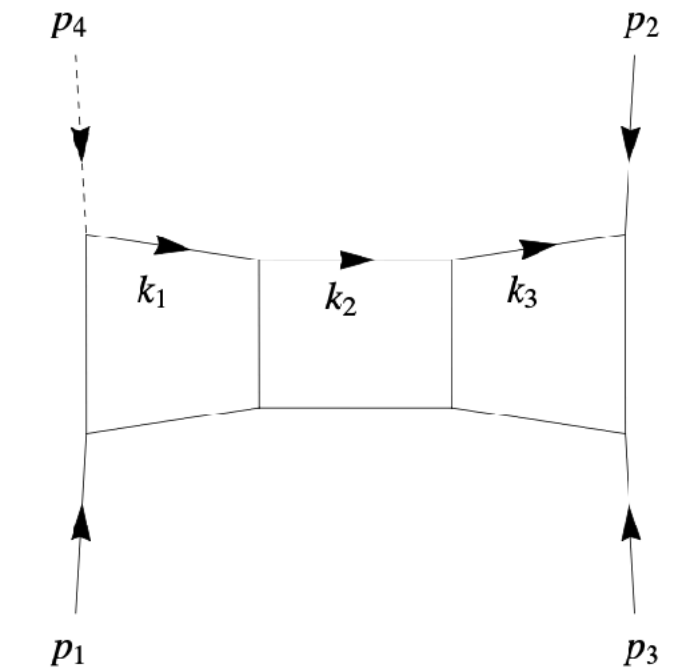
## planar diagrams:

Di Vita, Mastrolia, Schubert, Yundin '14;  
Canko, Syrrakos '21,

Gehrmann, Jakubcik, Mella, Syrrakos, Tancredi 2307.15405

NNLO to higher order in epsilon

Gehrmann, Jakubcik, Mella, Syrrakos, Tancredi 2301.10849



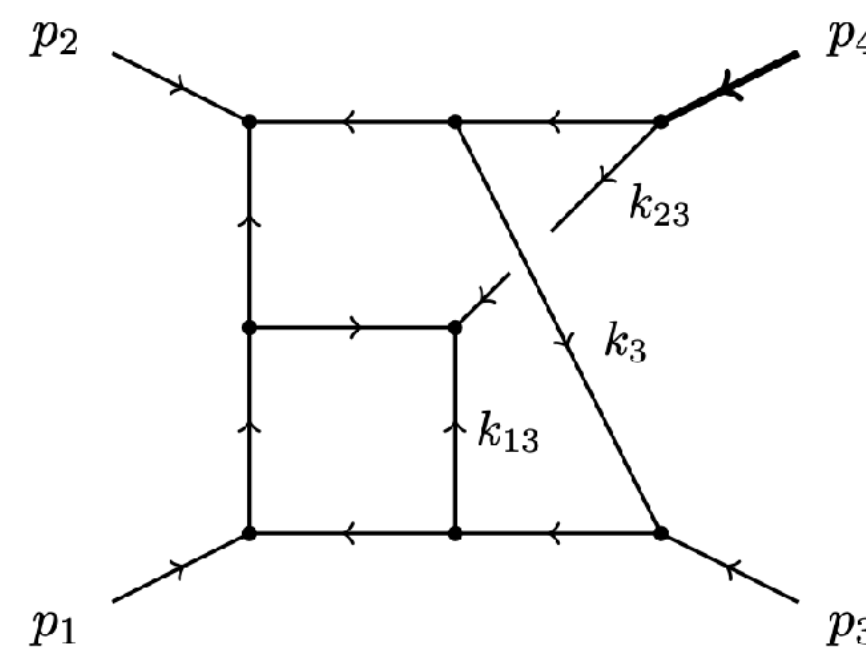
## non-planar diagrams:

Henn, Lim, Torres-Bobadilla '23

Syrrakos, Canko '23

Aliaj, Papathanasiou '24

Cesare Carlo Mella, Loops&Legs 2024



see talk by Lorenzo Tancredi

# VBF Higgs production

Asteriadis, Behring, Melnikov, Novikov, Röntsch 2407.09363

NNLO corrections to both, production and decay  $H \rightarrow b\bar{b}$

large negative corrections, depending on pT cuts on b-jets

scale variation  $\frac{2\mu_0}{\mu_0/2}$  in WBF

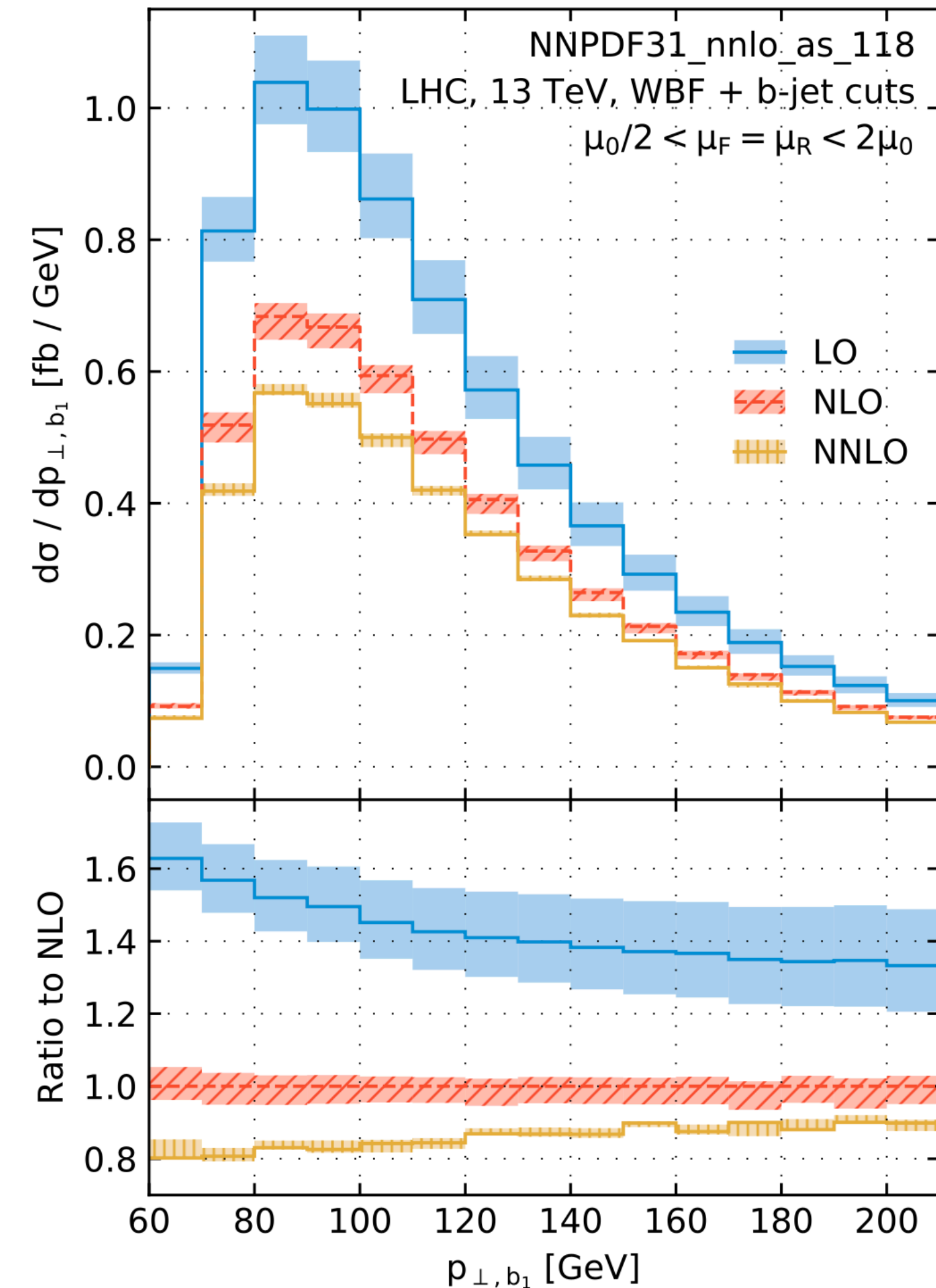


$$\sigma^{\text{LO}} = 75.6_{-5.6}^{+6.5} \text{ fb} \quad (\pm 9\%)$$

$$\sigma^{\text{NLO}} = 52.4_{-2.6}^{+1.5} \text{ fb} \quad (-31\% \pm 3\%)$$

$$\sigma^{\text{NNLO}} = 44.6_{-0.6}^{+0.9} \text{ fb} \quad (-10\% \pm 1\%)$$

Ivan Novikov, P3H YS Meeting '24





# ttH production

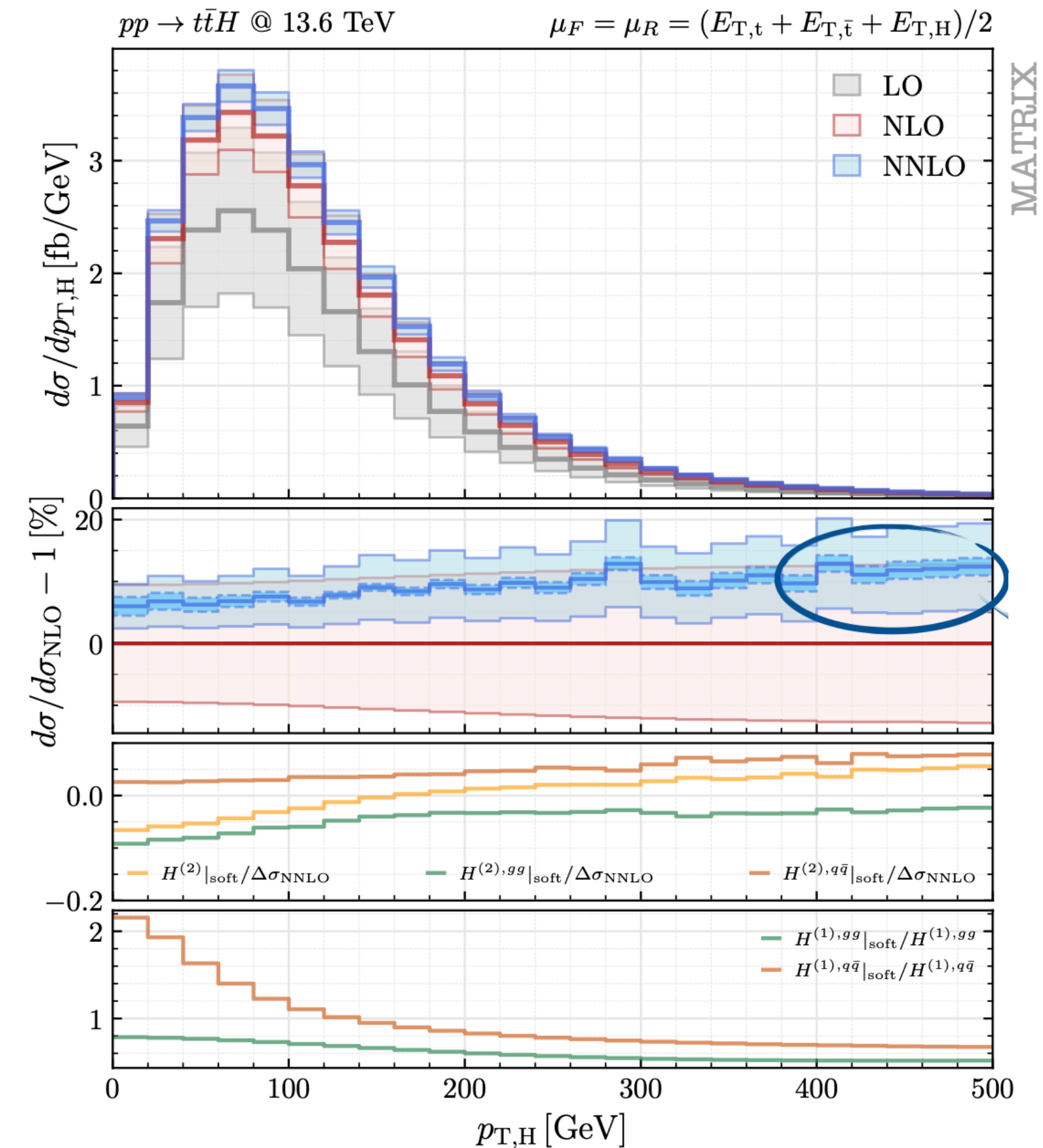
Catani, Devoto, Grazzini, Kallweit, Mazzitelli, Savioni '22, '24

4% increase at NNLO, reduction of scale uncertainties

$\sigma$ [pb]	$\sqrt{s} = 13$ TeV	$\sqrt{s} = 100$ TeV
$\sigma_{\text{LO}}$	$0.3910^{+31.3\%}_{-22.2\%}$	$25.38^{+21.1\%}_{-16.0\%}$
$\sigma_{\text{NLO}}$	$0.4875^{+5.6\%}_{-9.1\%}$	$36.43^{+9.4\%}_{-8.7\%}$
$\sigma_{\text{NNLO}}$	$0.5070 (31)^{+0.9\%}_{-3.0\%}$	$37.20(25)^{+0.1\%}_{-2.2\%}$

- soft approximation + “massification” for 2-loop virtual amplitude
- uncertainty due to approximate 2-loop amplitude estimated to  $\sim 1\%$  for total cross section
- can be larger in tail of  $p_{T,H}$  distribution (at NLO  $\sim 8\%$ )

## first differential NNLO results



Chiara Savioni, HP2 2024

# 2-loop pentagon amplitudes

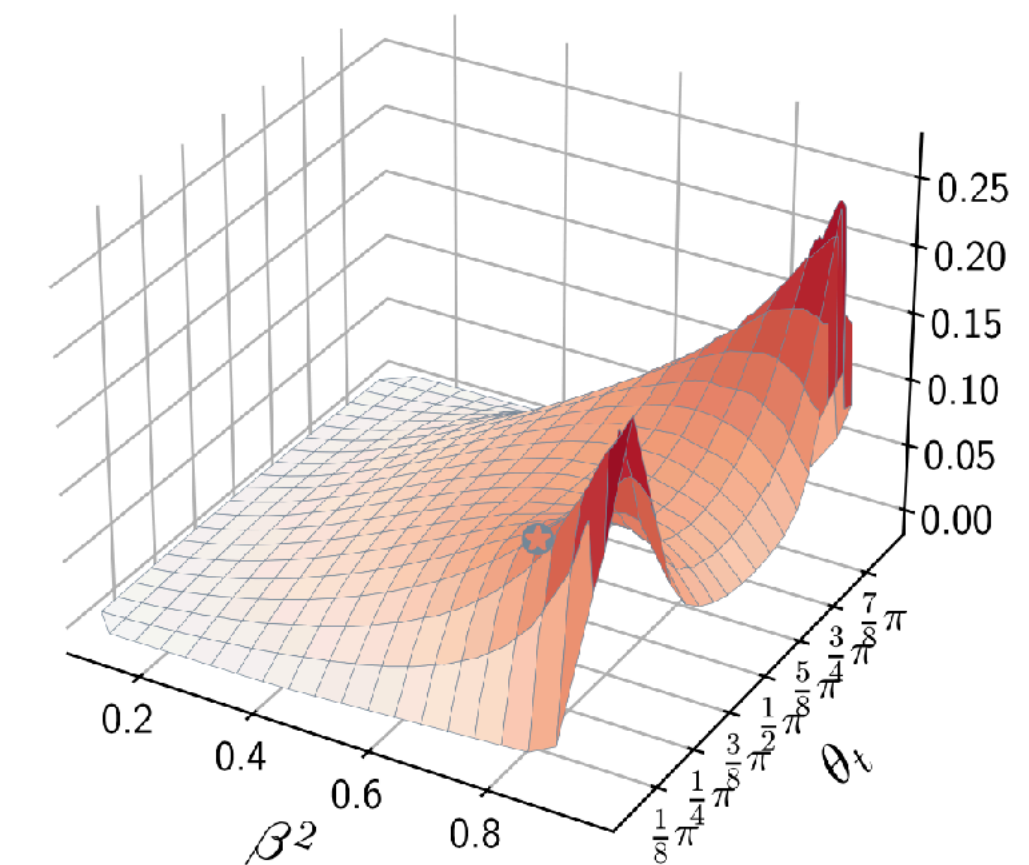
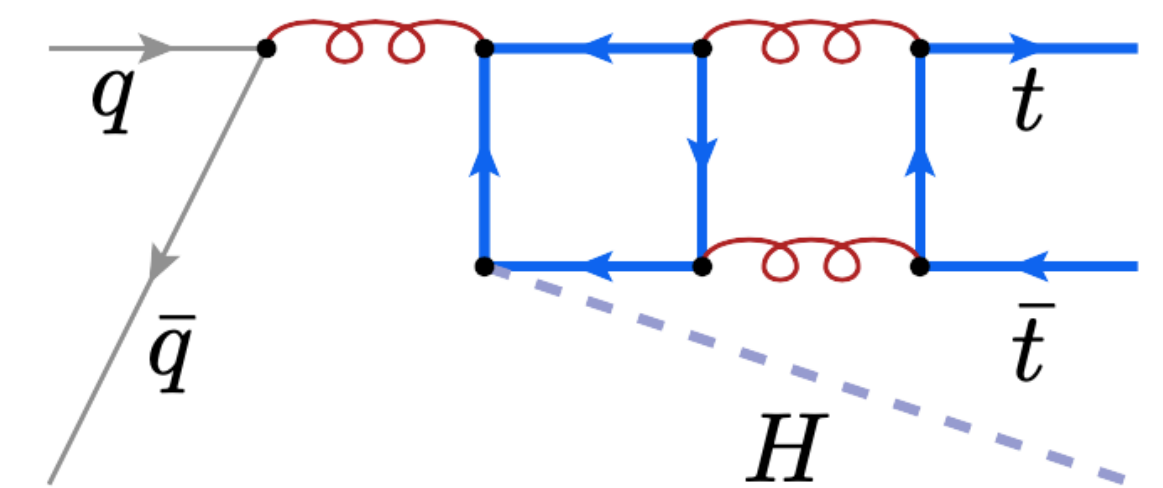
Results for **massless** 5-point amplitudes are known, physical results with **1 off-shell leg** also exist

Abreu, Agarwal, Badger, Becchetti, Caola, Chicherin, Chawdry, Czakon, De Laurentis, Gambuti, Gehrmann, Hartanto, Henn, Ita, Kallweit, Klinkert, Kryz, Lo Presti, Page, Peraro, Poncelet, Ma, Manteuffel, Mazzitelli, Mitov, Sotnikov, Tancredi, Wiesemann, Zhang, Zoia, ...

**2-loop 5-point amplitudes: 5 kinematic scales, for ttH in addition 2 masses**

## ttH @2-loops partial results:

- t  $\rightarrow$  H fragmentation functions [Brancaccio, Czakon, Generet, Krämer, Mück, 2106.06516](#)
- infrared pole coefficients [Chen, Ma, Wang, Yang, Ye, 2202.02913](#)
- leading colour contributions to amplitudes with light-quark loops  
[Febres Cordero, Figueiredo, Kraus, Page, Reina, 2312.08131](#)
- 1-loop to order  $\epsilon^2$  [Buccioni, Kreer, Liu, Tancredi, 2312.10013](#)
- high-energy limit, numerically [Wang, Xia, Yang, Ye, 2402.00431](#)
- Nf-part in quark channel, numerically [Agarwal, GH, Jones, Kerner, Klein, Lang, Magerya, Olsson, 2402.03301](#)



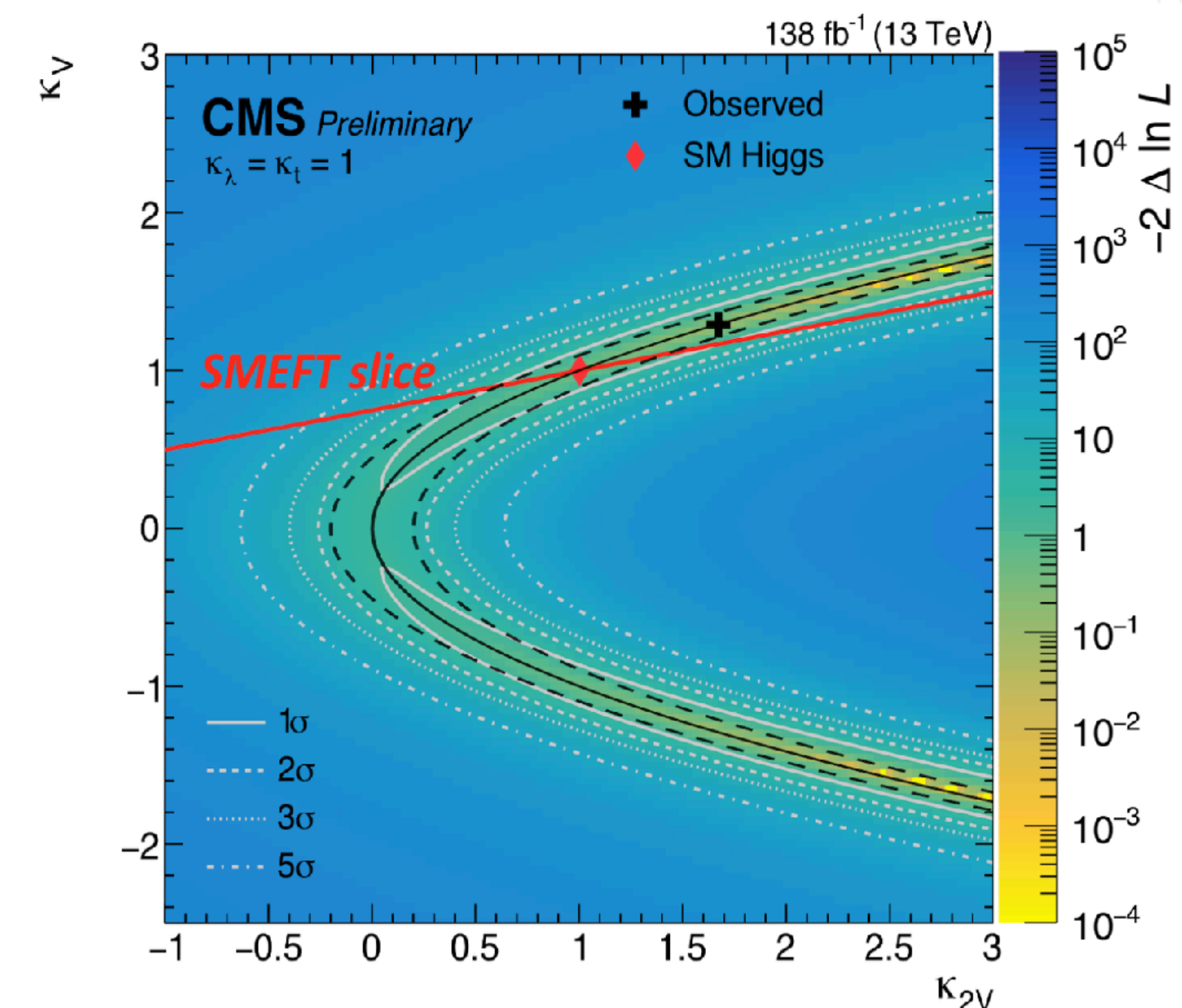
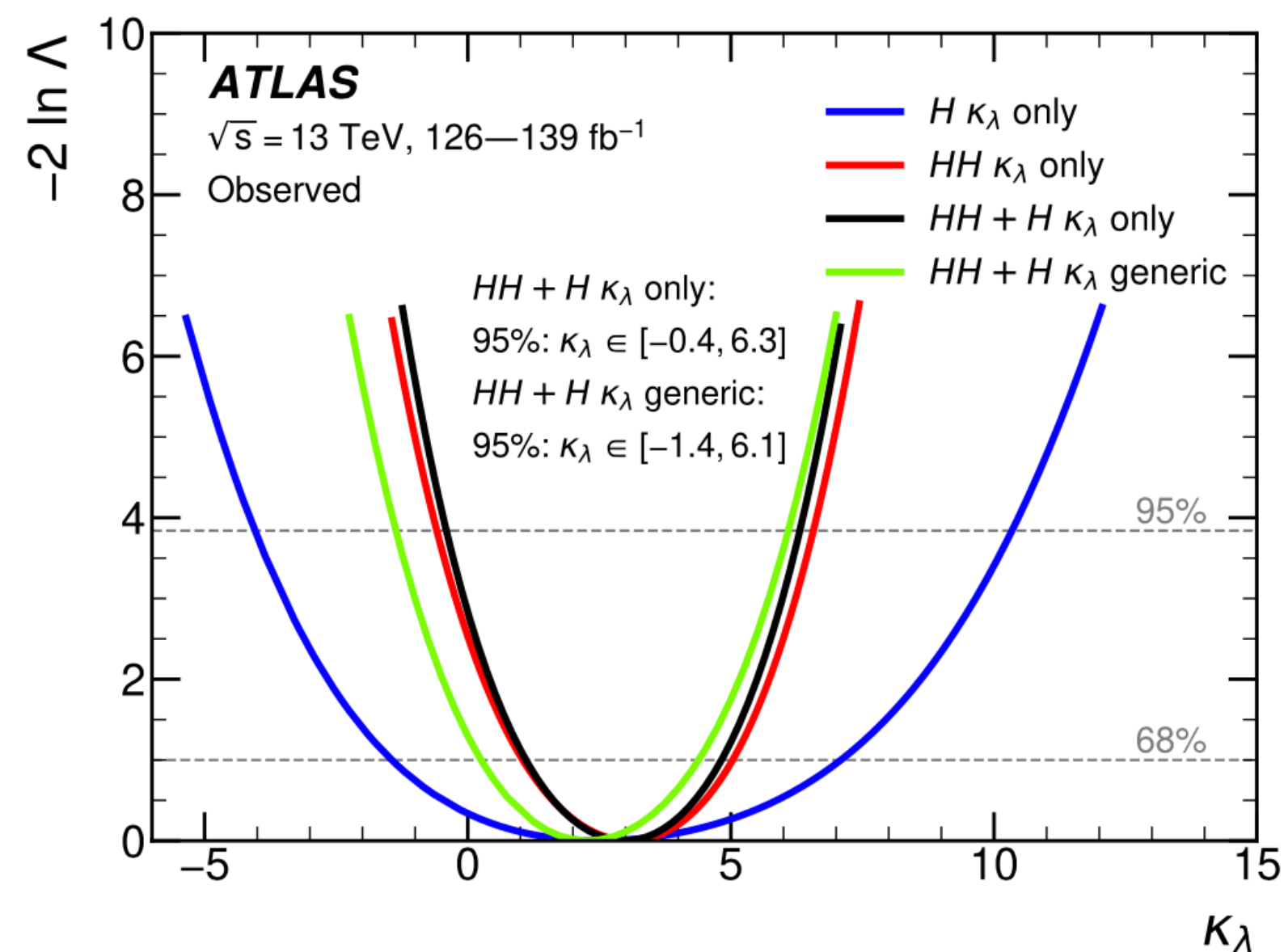
talk by Vitaly Magerya  
this afternoon

# Higgs boson pair production

prime process to explore the Higgs potential

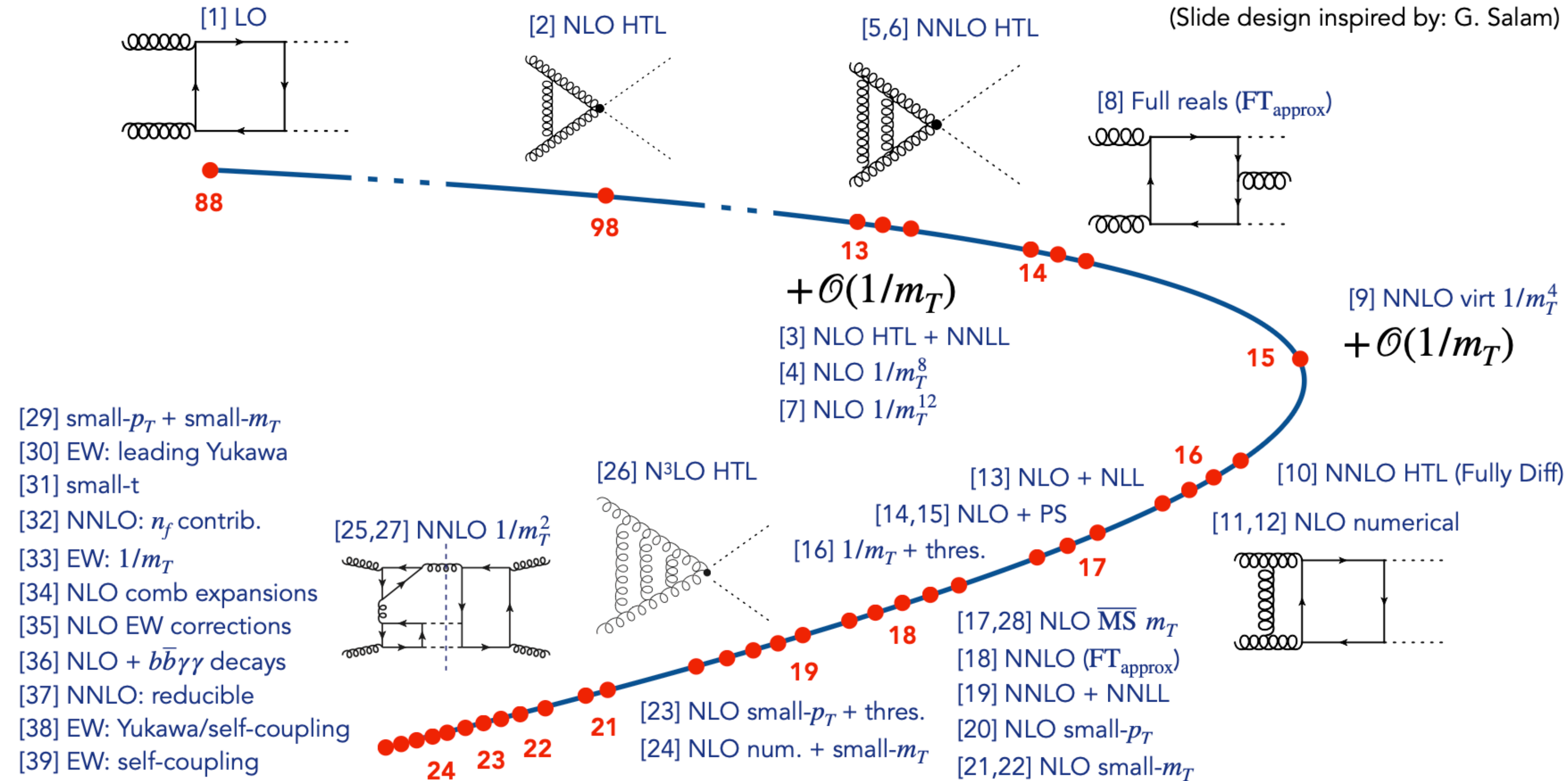
at energies much larger than the electroweak scale:  $V(\Phi) = ?$

after EW symmetry breaking:  $V(h) \sim \frac{1}{2} \underbrace{(2v^2 \lambda)}_{m_h^2} h^2 + v\lambda h^3 + \frac{\lambda}{8} h^4 + \dots ?$



# Overview

(Slide design inspired by: G. Salam)



Stephen Jones  
Higgs Hunting 2024

[1] Glover, van der Bij 88; [2] Dawson, Dittmaier, Spira 98; [3] Shao, Li, Li, Wang 13; [4] Grigo, Hoff, Melnikov, Steinhauser 13; [5] de Florian, Mazzitelli 13; [6] Grigo, Melnikov, Steinhauser 14; [7] Grigo, Hoff 14; [8] Maltoni, Vryonidou, Zaro 14; [9] Grigo, Hoff, Steinhauser 15; [10] de Florian, Grazzini, Hanga, Kallweit, Lindert, Maierhöfer, Mazzitelli, Rathlev 16; [11] Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Schubert, Zirke 16; [12] Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Zirke 16; [13] Ferrera, Pires 16; [14] Heinrich, SPJ, Kerner, Luisoni, Vryonidou 17; [15] SPJ, Kuttimalai 17; [16] Gröber, Maier, Rauh 17; [17] Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher 18; [18] Grazzini, Heinrich, SPJ, Kallweit, Kerner, Lindert, Mazzitelli 18; [19] de Florian, Mazzitelli 18; [20] Bonciani, Degrassi, Giardino, Gröber 18; [21] Davies, Mishima, Steinhauser, Wellmann 18, 18; [22] Mishima 18; [23] Gröber, Maier, Rauh 19; [24] Davies, Heinrich, SPJ, Kerner, Mishima, Steinhauser, David Wellmann 19; [25] Davies, Steinhauser 19; [26] Chen, Li, Shao, Wang 19, 19; [27] Davies, Herren, Mishima, Steinhauser 19, 21; [28] Baglio, Campanario, Glaus, Mühlleitner, Ronca, Spira 21; [29] Bellafronte, Degrassi, Giardino, Gröber, Vitti 22; [30] Davies, Mishima, Schönwald, Steinhauser, Zhang 22; [31] Davies, Mishima, Schönwald, Steinhauser 23; [32] Davies, Schönwald, Steinhauser 23; [33] Davies, Schönwald, Steinhauser, Zhang 23; [34] Bagnaschi, Degrassi, Gröber 23; [35] Bi, Huang, Huang, Ma Yu 23 [36] Li, Si, Wang, Zhang, Zhao 24; [37] Davies, Schönwald, Steinhauser, Vitti 24; [38] Heinrich, SPJ, Kerner, Stone, Vestner [39] Li, Si, Wang, Zhang, Zhao 24

# ggHH: higher order QCD corrections in the SM

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**NLO full  $m_t$**

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Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher '18

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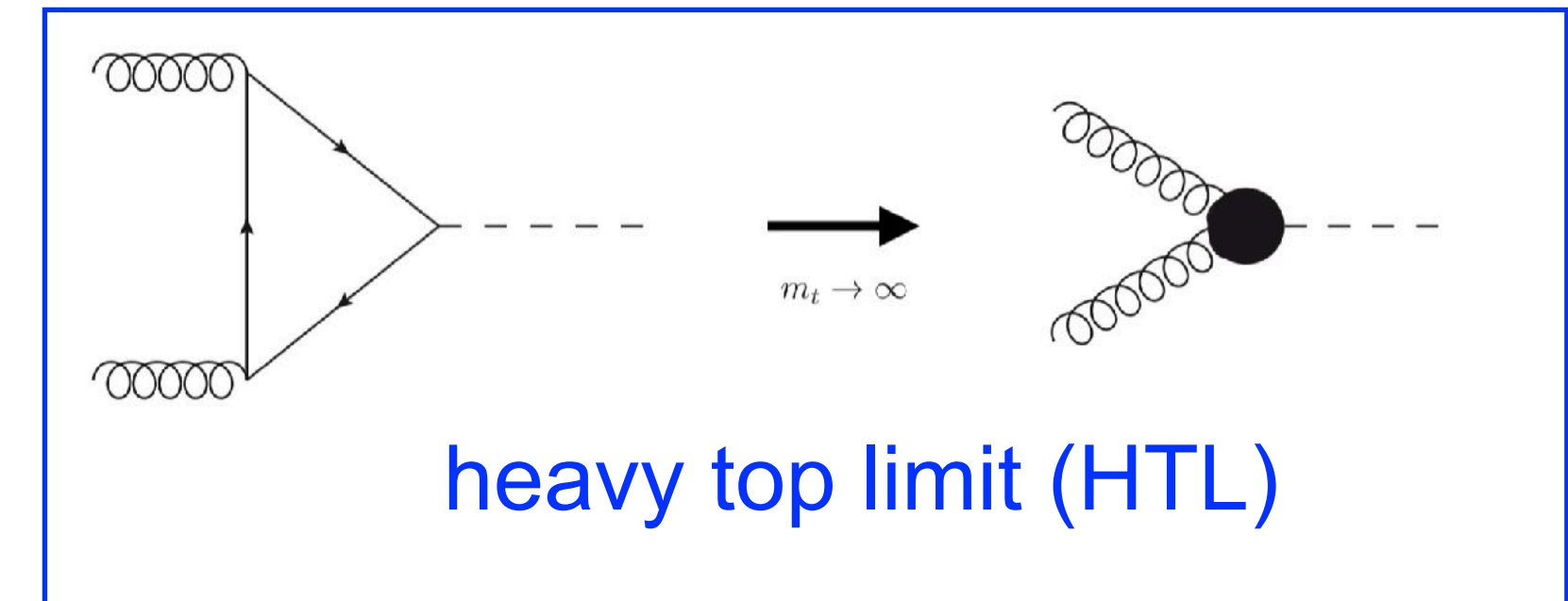
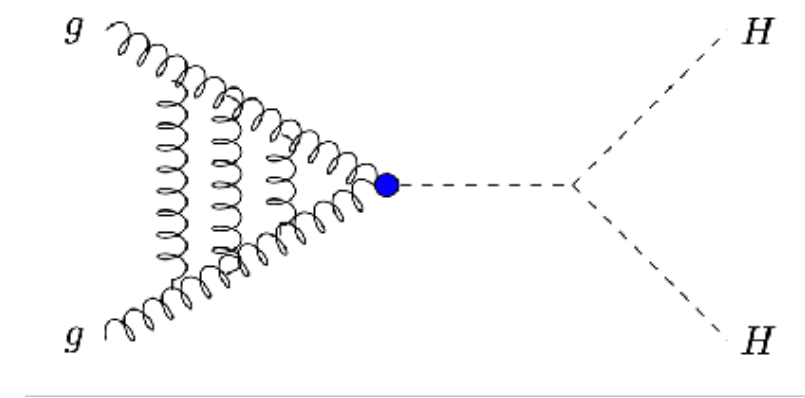
$NNLO_{FTapprox}$  Grazzini, Kallweit, GH, Jones,  
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inclusion of top quark mass dependence except in virtual  $\mathcal{O}(\alpha_s^3)$

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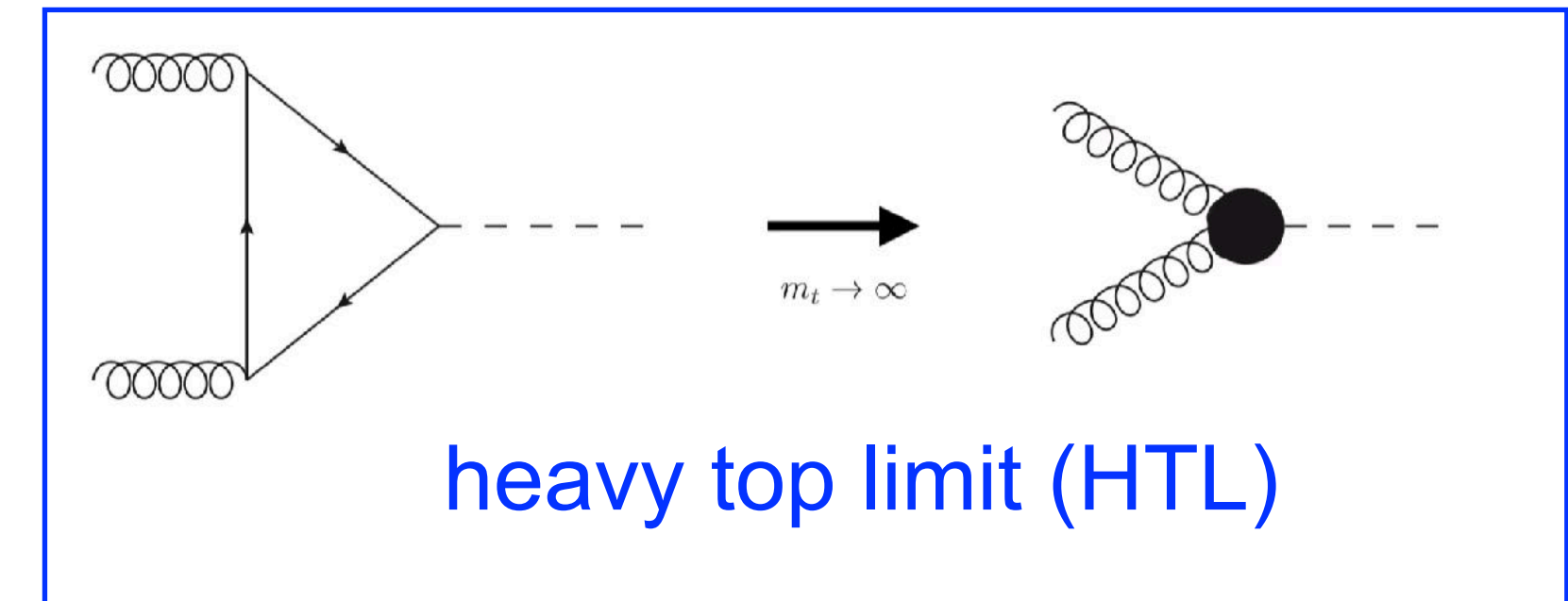
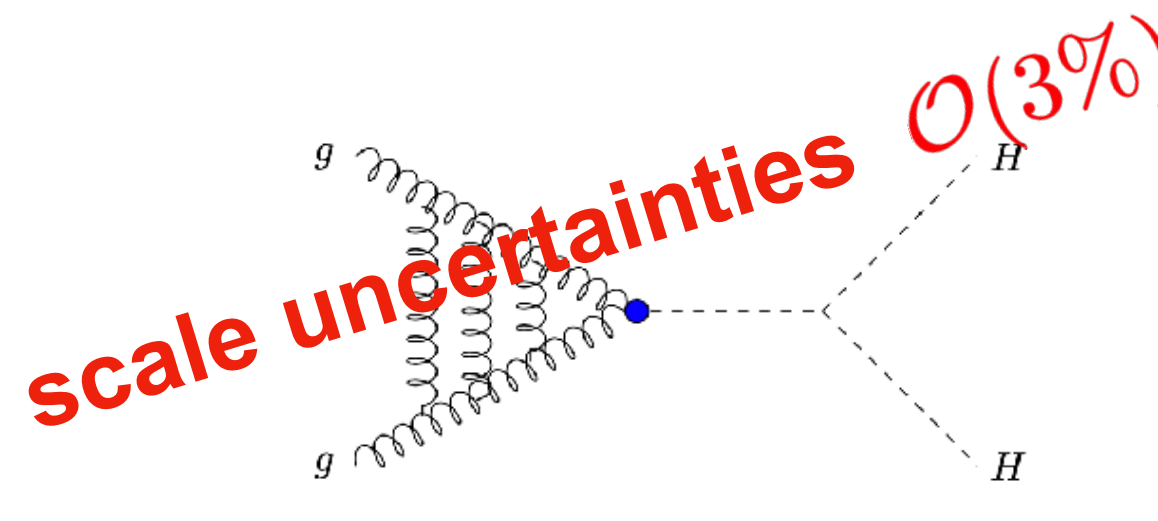
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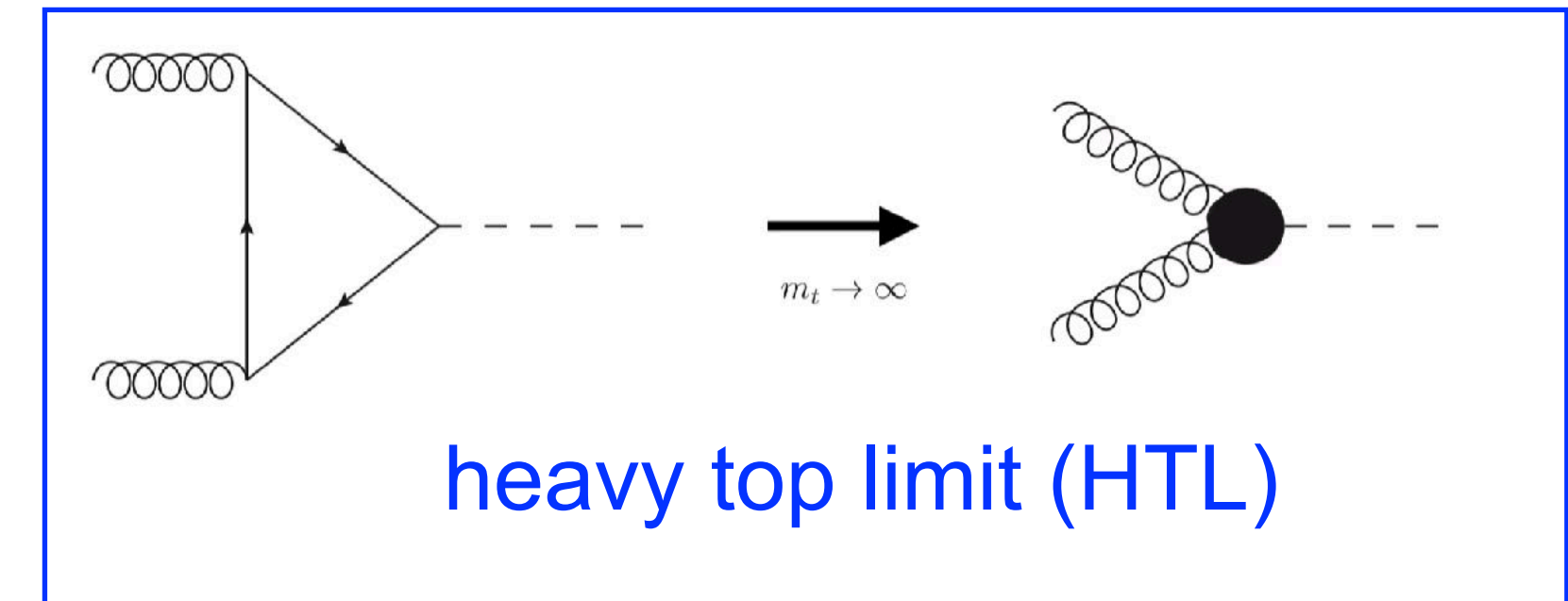
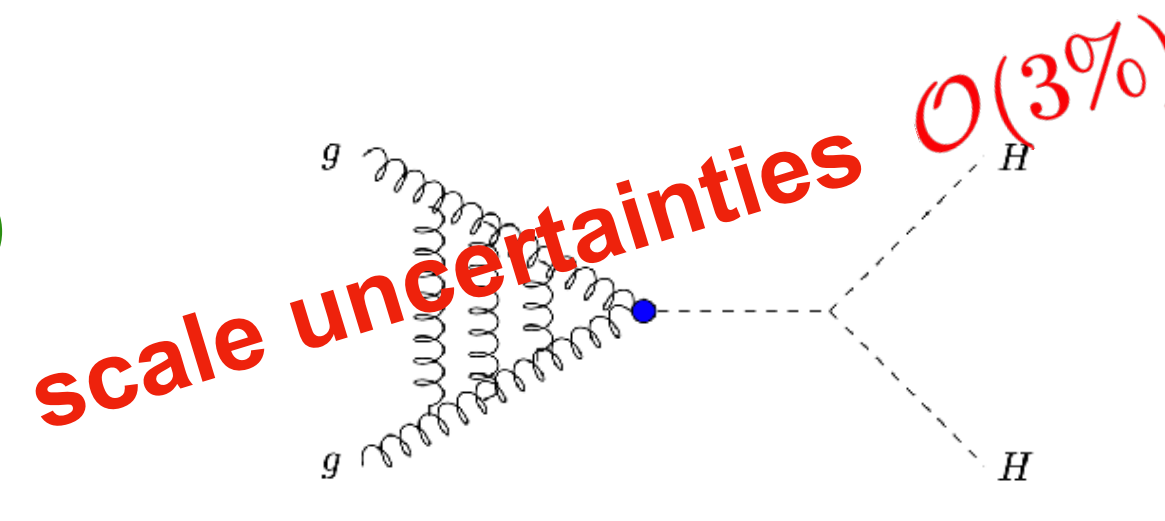
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residual missing top mass effects estimated to  $\mathcal{O}(5\%)$

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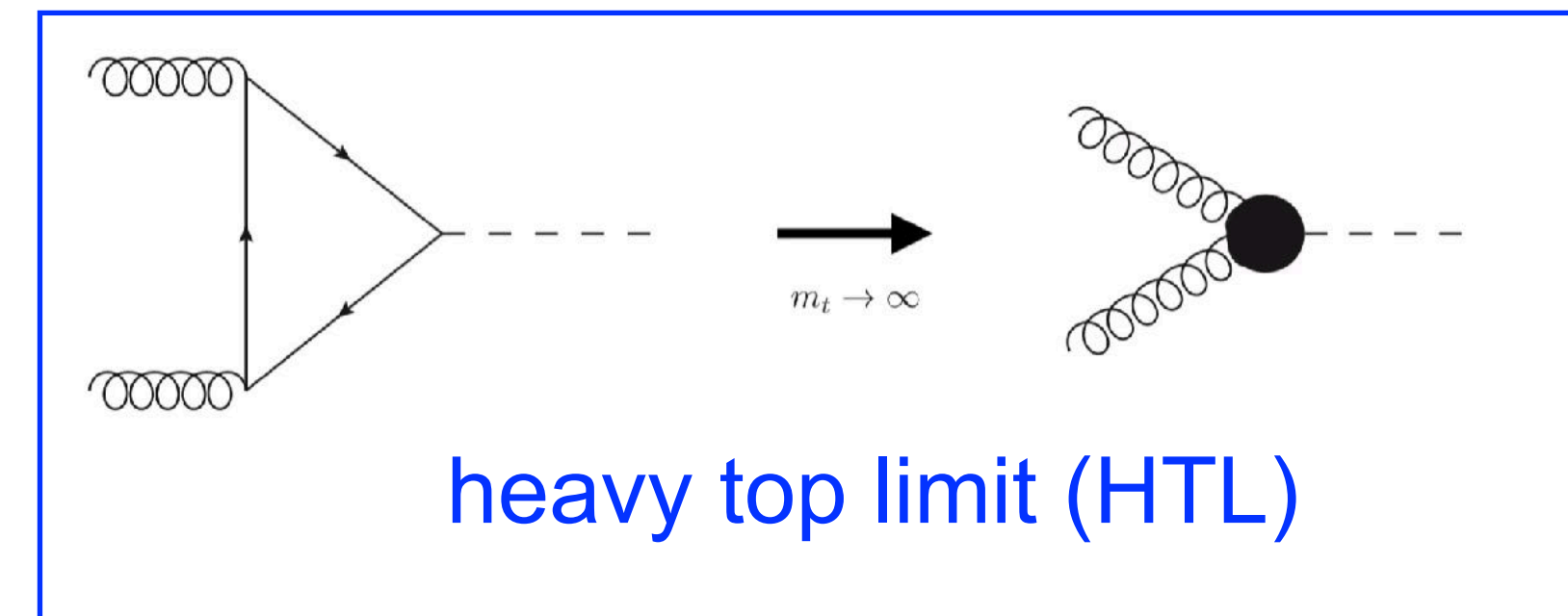
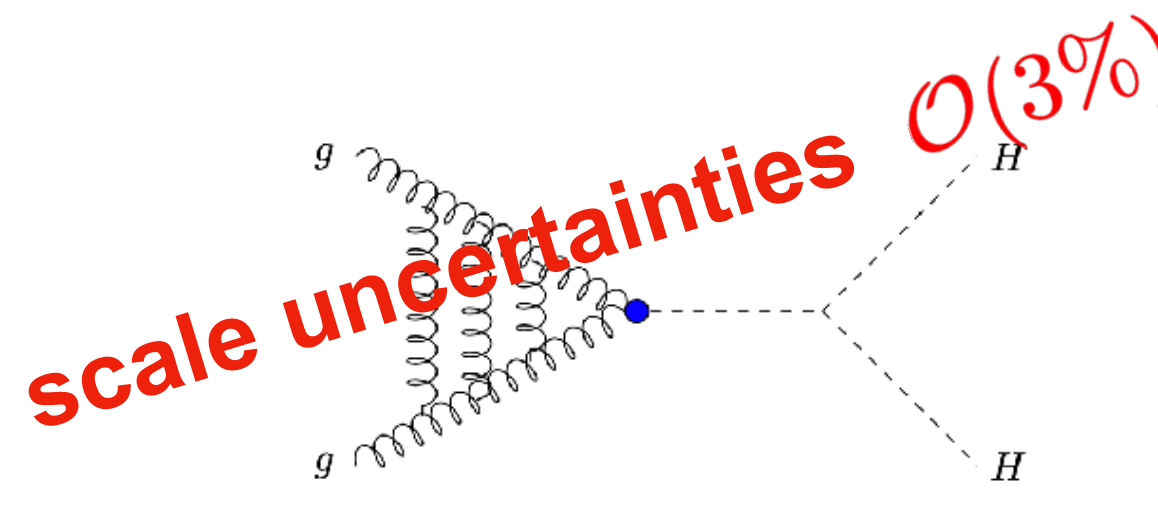
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uncertainty due to top mass scheme  $\mathcal{O}(20\%)$



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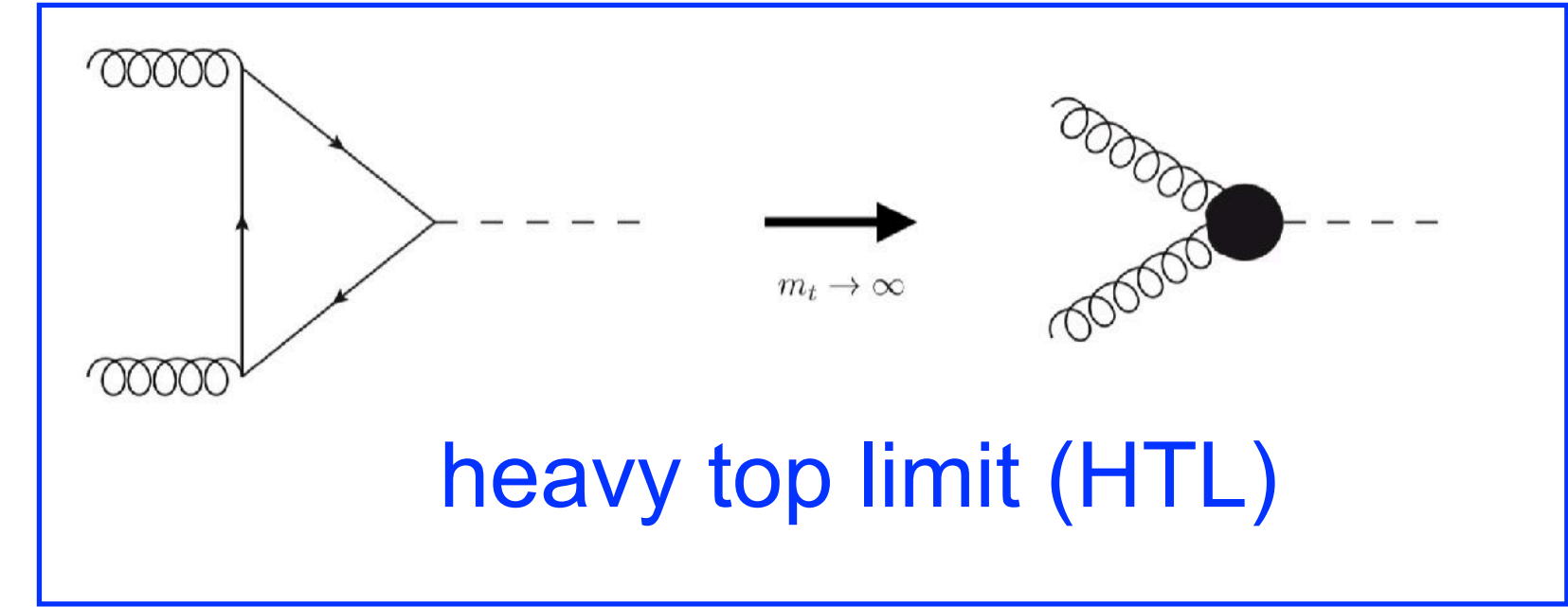
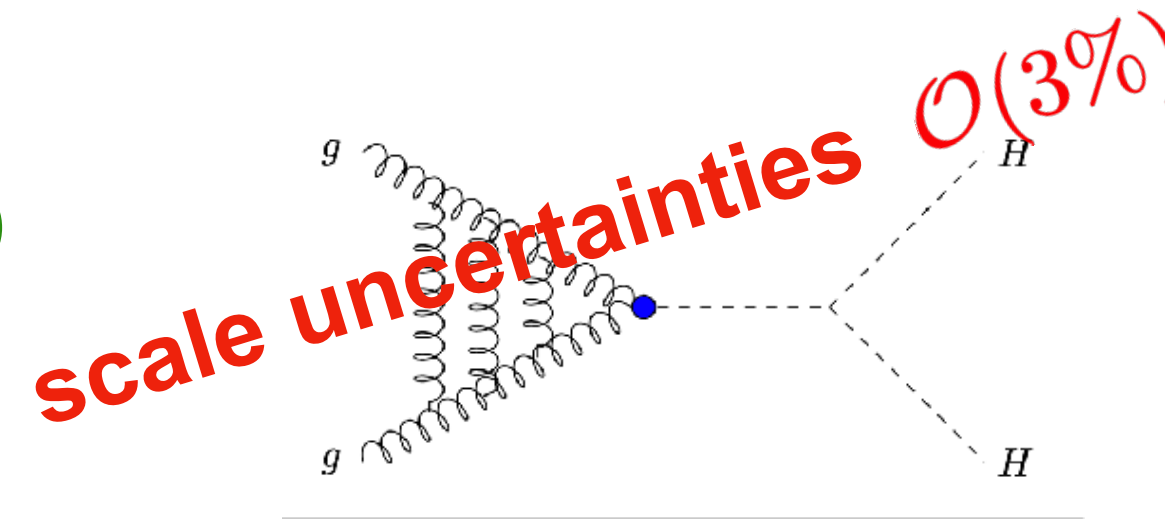
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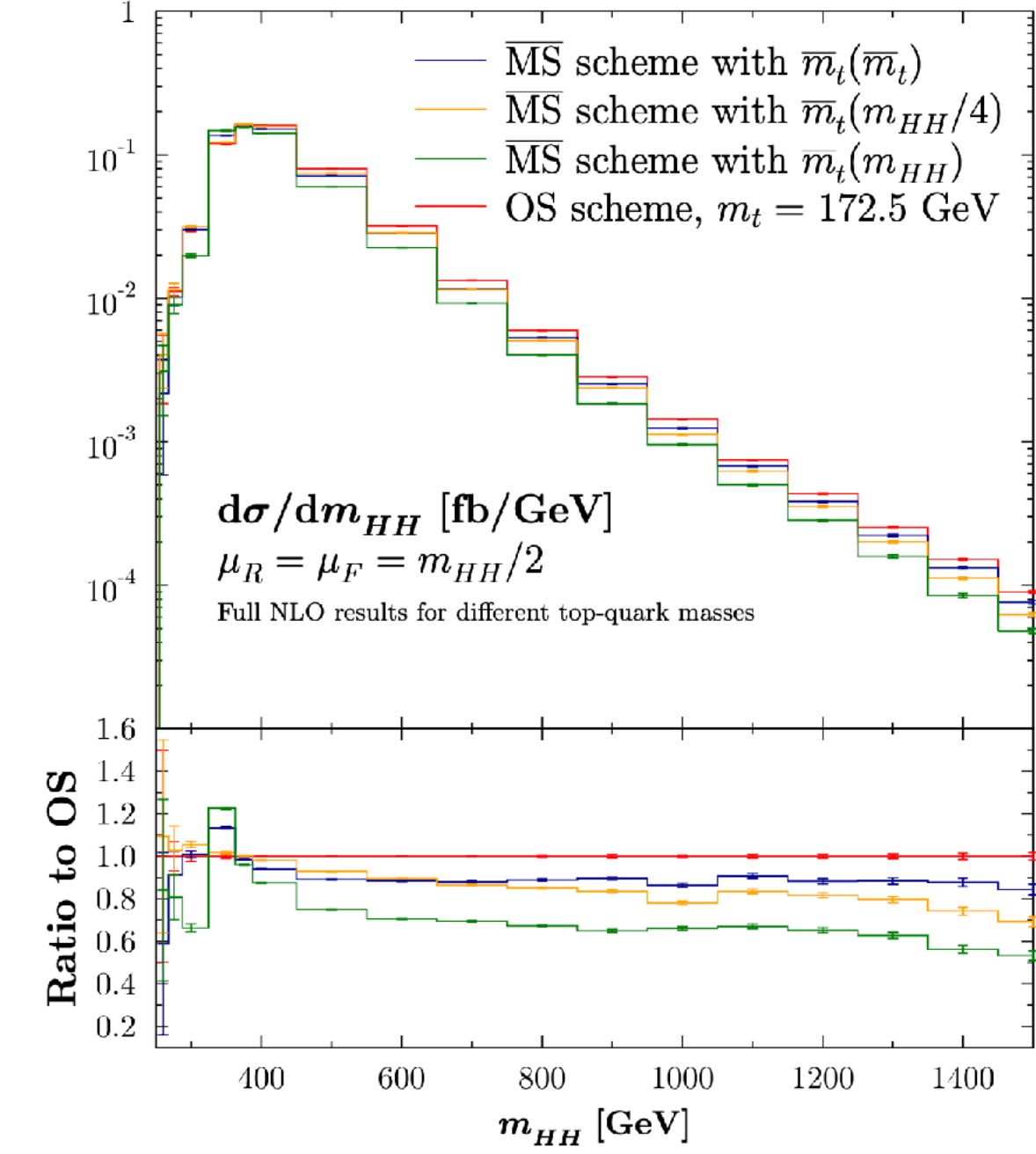
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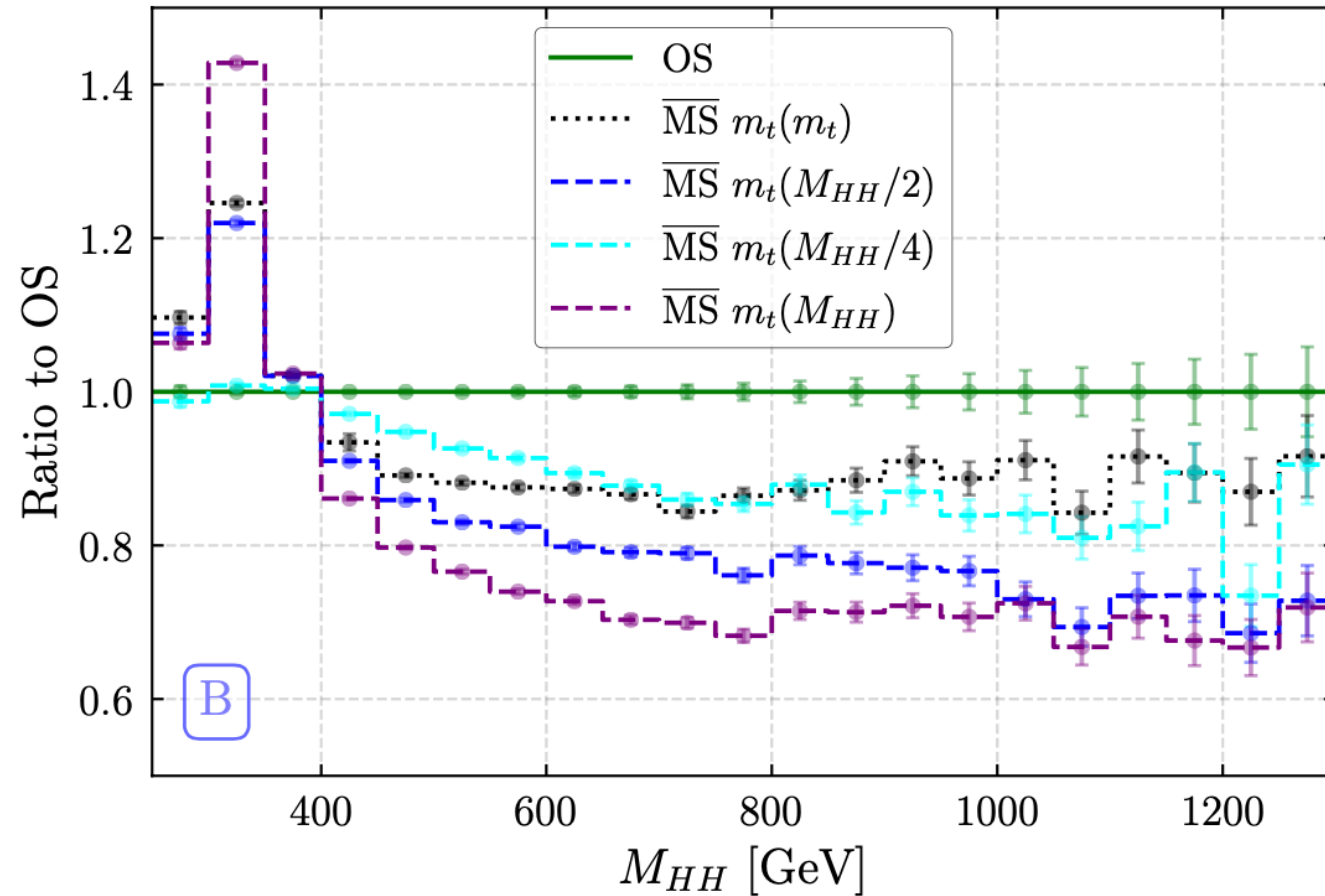
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gg → HH at NLO QCD | √s = 14 TeV | PDF4LHC15



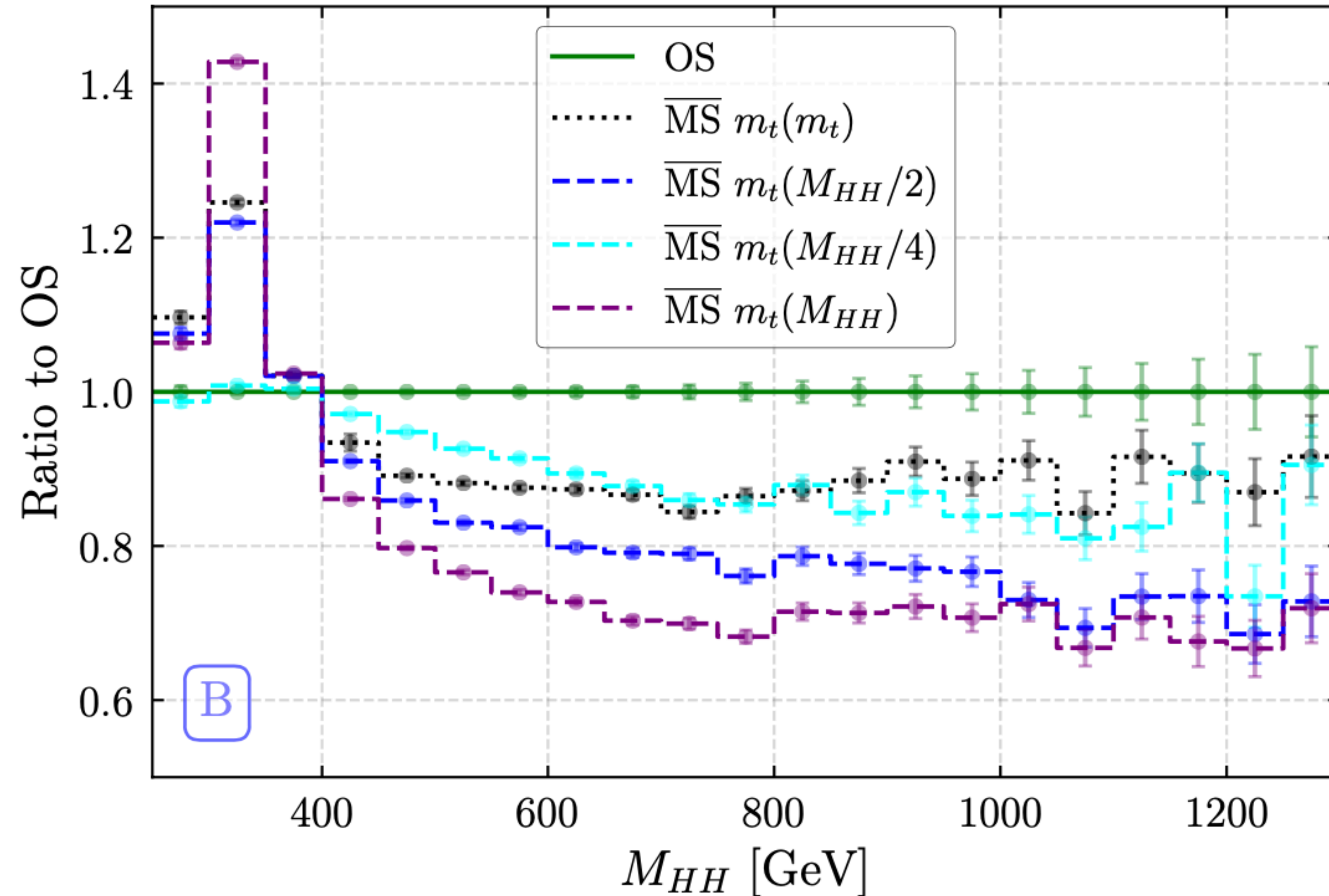
# scheme uncertainties (top mass)



PDF +  $\alpha_s$  uncertainties  $\sim 2.3\%$

Bagnaschi, Degrassi, Gröber 2309.10525

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top mass scheme uncertainty currently  
largest uncertainty in  
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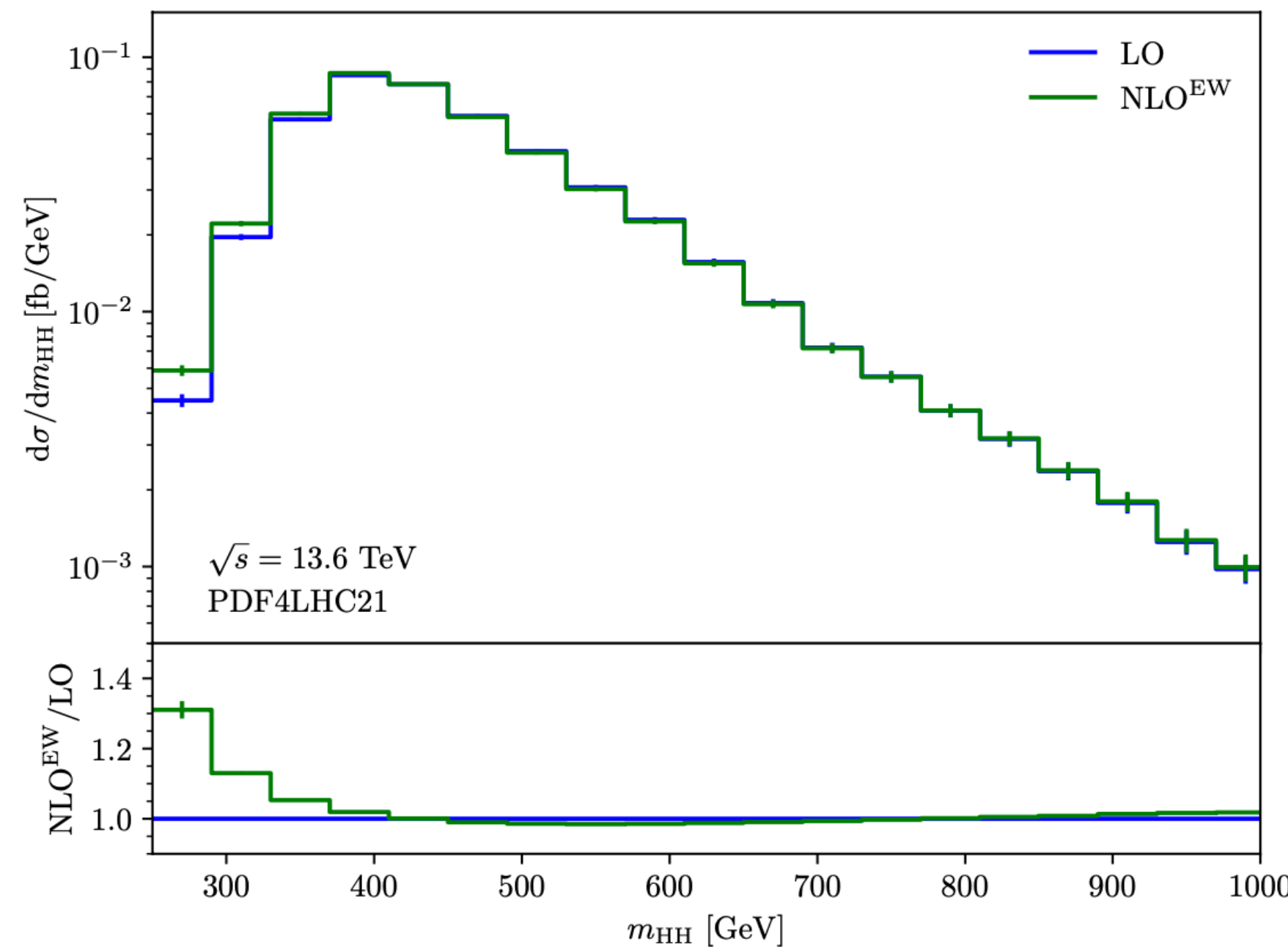
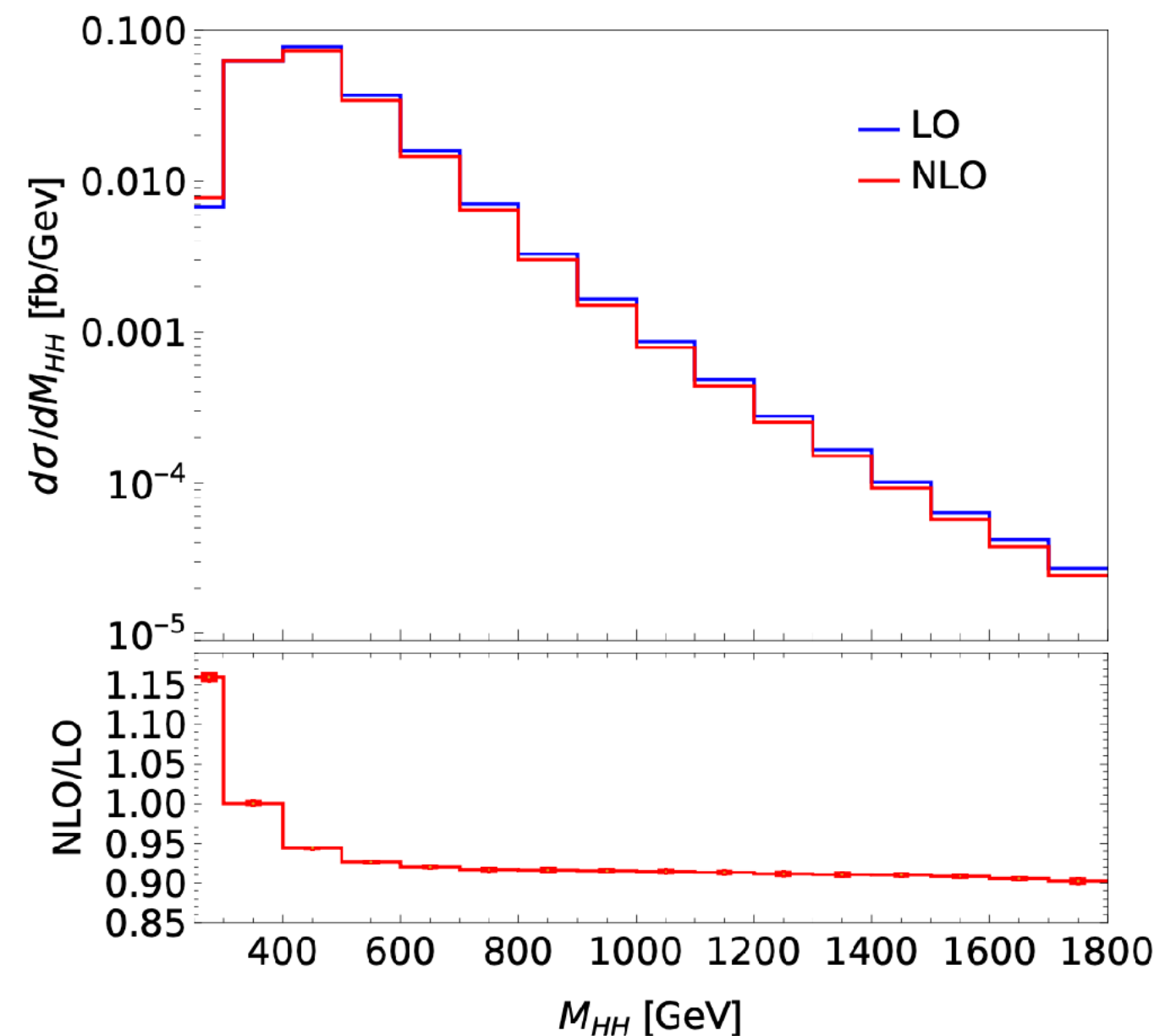
Bagnaschi, Degrandi, Gröber 2309.10525

# NLO electroweak corrections to ggHH

full EW: [Bi, Huang, Huang, Ma, Yu '23](#)

Yukawa- and Higgs self-coupling type corrections:

[GH, Jones, Kerner, Stone, Vestner '24](#)



see also

heavy top limit, high energy expansion

[Davies, Mishima, Schönwald, Steinhauser, Zhang '22](#)

Yukawa coupling corrections in (partial) HTL

[Mühlleitner, Schlenk, Spira '22](#)

full EW in large- $m_t$  expansion '23

+ factorisable contributions '24

[Davies, Schönwald, Steinhauser, Zhang](#)

cancellations between gauge-boson and Yukawa-type corrections

partial EW corrections, with coupling modifiers:

[Borowka, Duhr, Maltoni, Pagani, Shivaji, Zhao '18](#); [Bizon, Haisch, Rottoli '18, '24](#)

see talks by [Huai-Min Yu](#),  
[Johannes Braaten](#)

# Summary & outlook

- The Higgs boson is our youngest particle (time since discovery) and the most peculiar particle (the only elementary scalar so far)
- Precision calculations are necessary to identify deviations from the SM predictions as new physics and to make the case for future colliders; in addition we keep learning about the structure of Quantum Field Theories
- Technical frontiers are 2-loop 5-point with several mass scales, 3-loop 4-point ... (loops+legs+masses  $\geq 7$ ), combining QCD corrections with EW corrections, EW schemes, treatment of heavy quarks (e.g. mass renormalisation schemes), parton shower matching beyond NLO, power corrections, PDFs, ... lots of progress!
- Conceptual frontiers are ...



Guess what's under the fog from the features peaking out of the fog ...