

Status of electroweak parameters measurements

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on behalf of the ATLAS, CMS and LHCb Collaborations



- introduction
- m_W, Γ_W
- $\sin^2(\theta_W)$
- $\Gamma(Z \rightarrow \text{inv})$
- m_{top}

Introduction

- Rich variety of electroweak interaction derived from symmetry principles
- Mass of electroweak gauge bosons and interaction strength predicted precisely from g, g', v, λ

$$SU(2)_L \times U(1)_Y \\ \Rightarrow W^+, W^-, Z, \gamma$$

Parameters of the Standard Model

- four input parameters, e.g. α_{QED}, G_F, m_Z and m_H
- interconnected with each other
 - at Tree level

$$m_W = \frac{gv}{2}, m_Z = \frac{\sqrt{g^2 + g'^2} v}{2}, \sin^2 \theta_W = \frac{g^2}{g^2 + g'^2} = 1 - m_W^2 / m_Z^2, G_F = \frac{\sqrt{2} g^2}{8 m_W^2}$$

- at leading order $\sin^2 \theta_{eff}^l \propto (1 - g_v / g_a)$ related to the real effective (leptonic) vector and axial-vector couplings of the Z boson

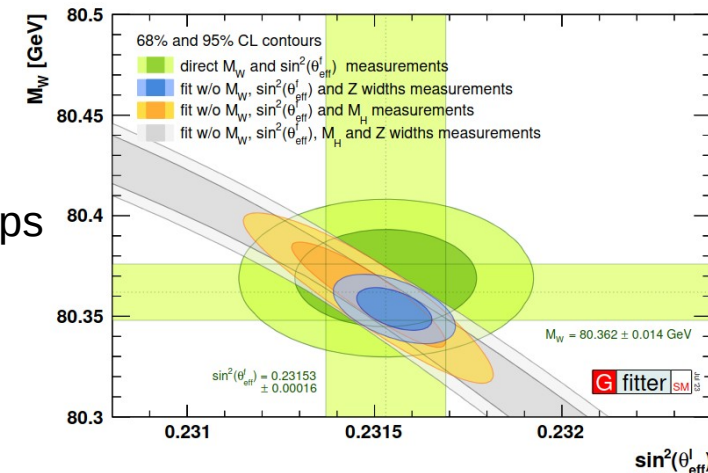
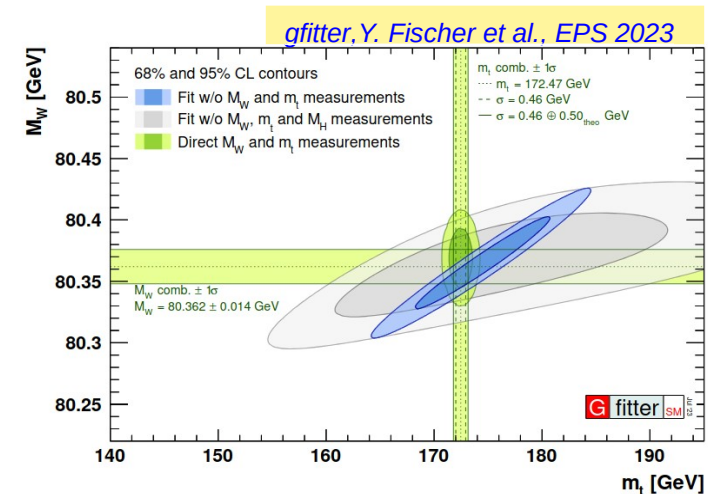
- at higher orders

$$m_W = \left(\frac{\pi \alpha_{QED}}{\sqrt{2} G_F} \right)^{1/2} \frac{\sqrt{1 + \Delta r}}{\sin \theta_W}, \sin^2 \theta_{eff}^l = \kappa \sin^2 \theta_W, \kappa \sim 1.037$$

- radiative corrections Δr modify propagator and decay vertices
 - sensitivity to a wide range of physics through quantum loops
 - largest contributions from $m_t^2, \log(m_H)$

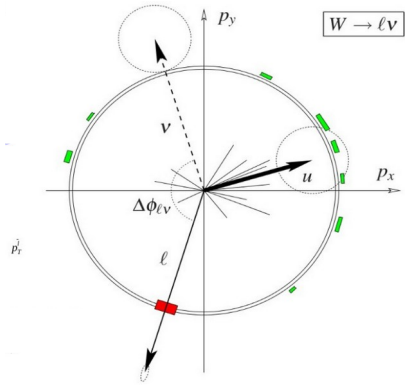
Precision measurements

- test self-consistency of SM theory in global EW fits
- tensions could be signs of BSM effects

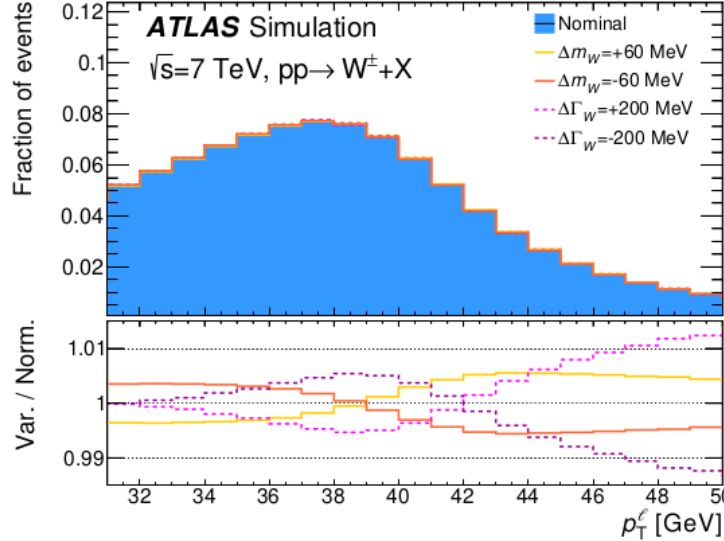


Measurement of the W boson mass and width

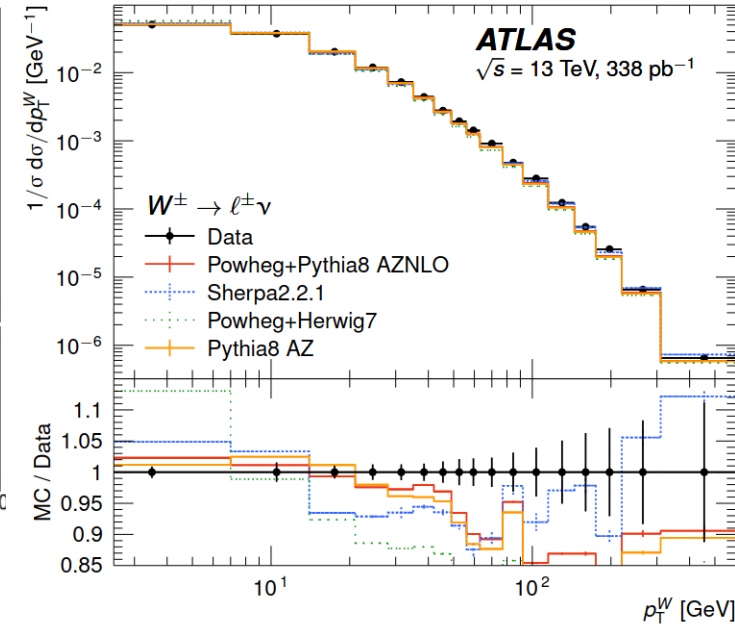
arXiv:0901.0512



arXiv:2403.15085



arXiv:2404.06204



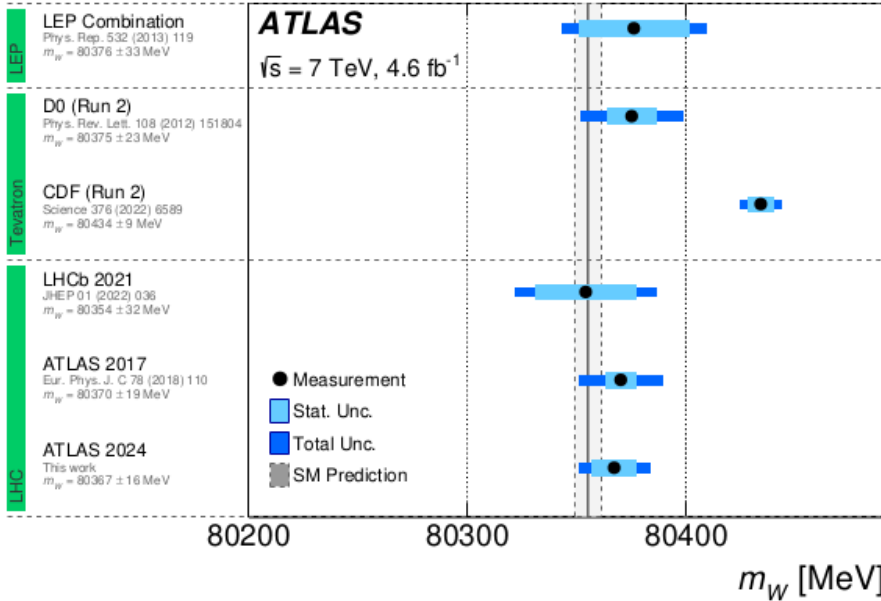
● ATLAS

- revisit 2011 (7 TeV) data, favourable experimental environment for measurement of m_W
- measured from p_T^ℓ and m_T^W distributions in $W \rightarrow \ell\nu$ decays
- checks of p_T^W modelling in dedicated measurements
- more modern PDF sets : CT18 (was CT10nnlo)
- small update to uncertainties for higher-order electroweak corrections
- key change : use profile likelihood fit (was χ^2 fit)
 - constrain systematic uncertainties in situ
 - directly determine their correlations
 - challenge: m_W now also correlated with some syst. variations
- extensive validation of method to avoid biases

Measurement of the W boson mass and width

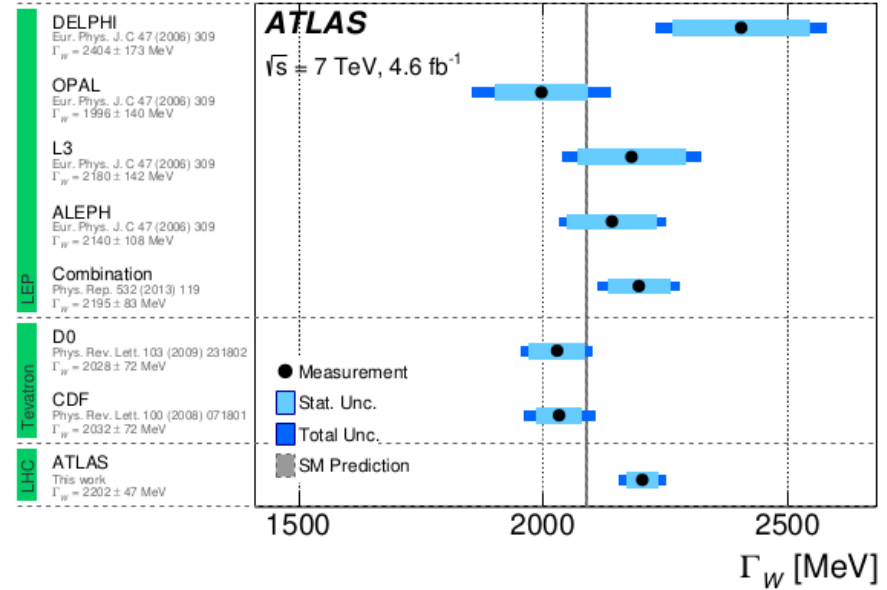
Overview of m_W measurements

arXiv:2403.15085



Unc. [MeV]	Total	Stat.	Syst.	PDF	A_i	Backg.	EW	e	μ	u_T	Lumi	Γ_W	PS
p_T^ℓ	16.2	11.1	11.8	4.9	3.5	1.7	5.6	5.9	5.4	0.9	1.1	0.1	1.5
m_T	24.4	11.4	21.6	11.7	4.7	4.1	4.9	6.7	6.0	11.4	2.5	0.2	7.0
Combined	15.9	9.8	12.5	5.7	3.7	2.0	5.4	6.0	5.4	2.3	1.3	0.1	2.3

Overview of Γ_W measurements



Unc. [MeV]	Total	Stat.	Syst.	PDF	A_i	Backg.	EW	e	μ	u_T	Lumi	m_W	PS
p_T^ℓ	72	27	66	21	14	10	5	13	12	12	10	6	55
m_T	48	36	32	5	7	10	3	13	9	18	9	6	12
Combined	47	32	34	7	8	9	3	13	9	17	9	6	18

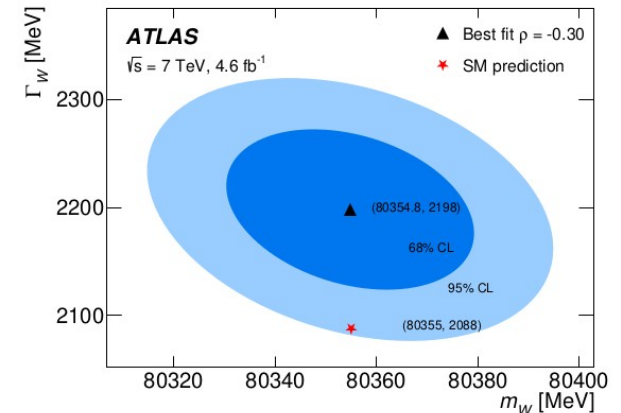
○ separate measurement of mass and width :

$$m_W = 80366.5 \pm 15.9 \text{ MeV}$$

$$\Gamma_W = 2202 \pm 47 \text{ MeV}$$

○ ... as well as simultaneous extraction

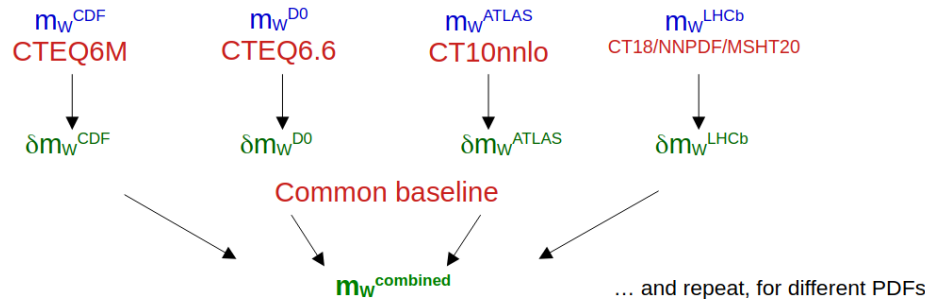
○ most precise single-experiment measurement of Γ_W



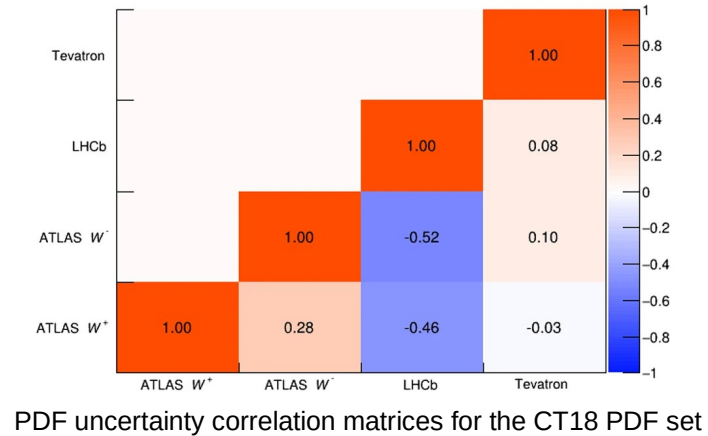
Measurement of the W boson mass m_W

- **Combination « ATLAS, LHCb, D0, CDF »** EPJ C (2024) 84:451

- measurements performed at different times, using different baseline PDFs and QCD tools : existing result extrapolated to a common baseline
- two-step procedure :
 - correct to common theory and modelling
 - combine including correlations (proton structure)



*M. Boonekamp, LHC EW WG
General Meeting, July 2024*



LHCb : m_W determination in the forward acceptance strongly suppresses the PDF uncertainty in an LHC m_W average due to complementary geometry. It is only a 2016 dataset analysis, with a full Run 2 analysis still possibly coming ! JHEP 01 (2022) 036

$$m_W = 80364 \pm 32 \text{ MeV}$$

Tension between « ATLAS, LHCb, D0 » combination and CDF W mass is of 3.6σ

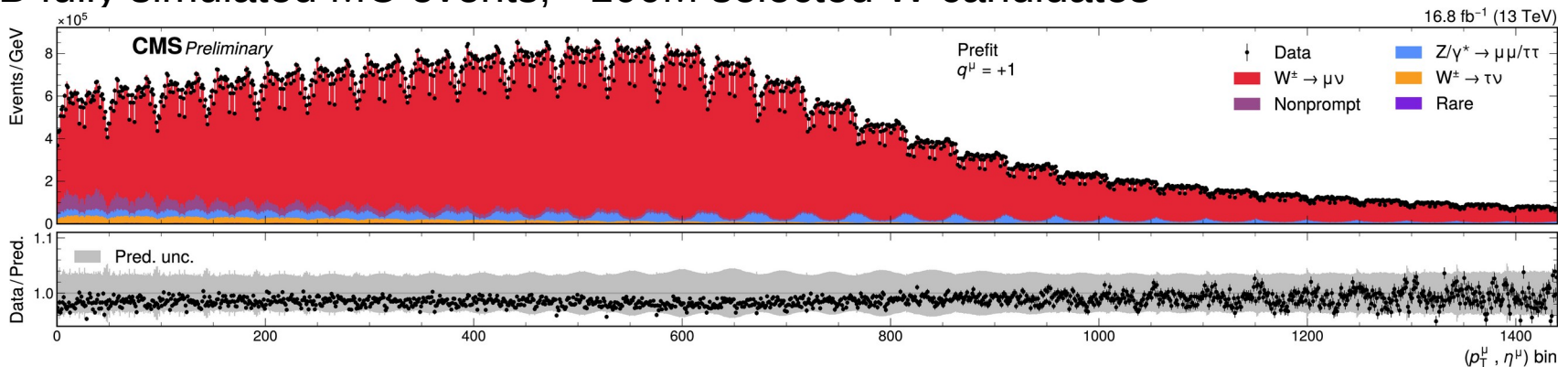
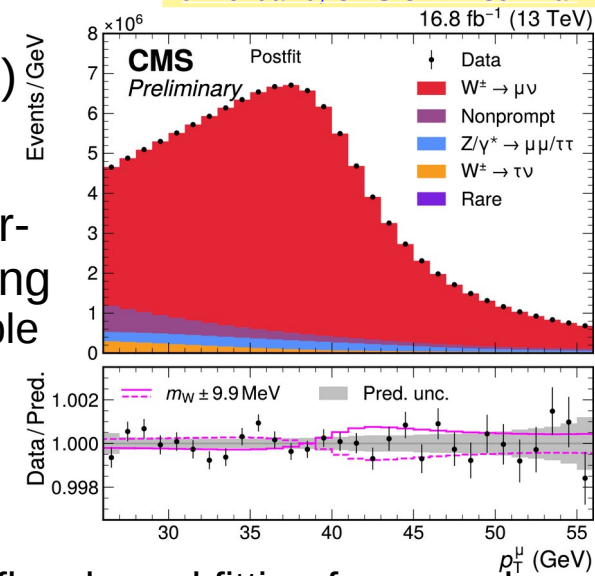
$$\text{« ATLAS, LHCb, D0 » : } m_W = 80369.2 \pm 13.3 \text{ MeV}$$

Measurement of the W boson mass

• CMS

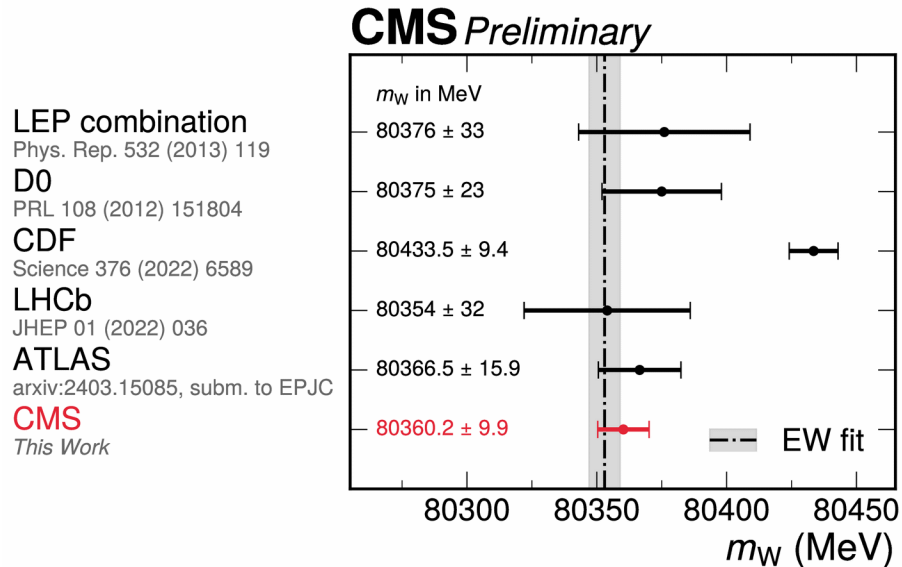
- use well-understood subset of 13 TeV data: 16.8 fb^{-1} from later part of 2016 run (~ 30 mean interactions per crossing)
 - focus on muon channel and kinematics
 - larger experimental syst. for electrons and hadronic recoil
- strategy : exploit large dataset, accurate modeling of uncertainties for maximal in-situ constraints on theoretical modeling
 - reserve Z data as independent cross-check as much as possible
 - muon calibration from J/ψ , validated with Z
 - in-situ constraints on theory modeling from W data itself, independent validation with Z
- m_W extracted from profile likelihood fit to μ (η , p_T , charge)
 - thousands of bins and systematic variations ; optimized Tensorflow-based fitting framework
- building on experimental techniques, tools, and experience from W-like m_Z measurement (2016) and W rapidity-helicity measurement (2020) which established strong in-situ constraints on PDFs from charged lepton kinematics
- 4B fully simulated MC events, $>100\text{M}$ selected W candidates

CMS-PAS-SMP-23-002
J. Bendavid, CMS CERN seminar



Measurement of the W boson mass

CMS-PAS-SMP-23-002
J. Bendavid, CMS CERN seminar

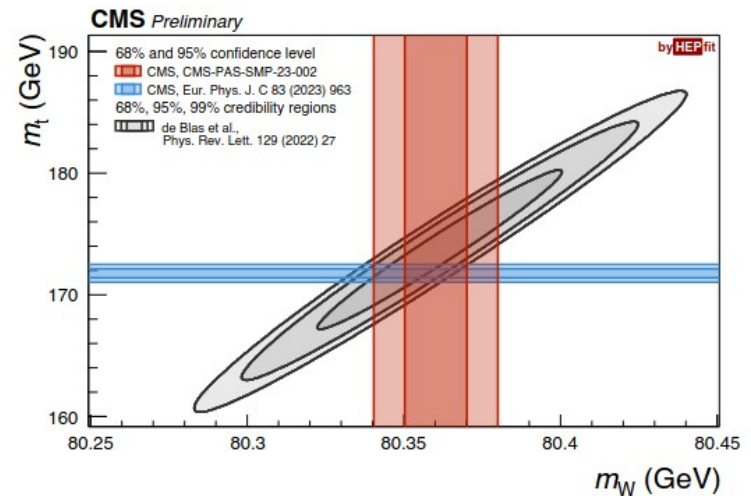


$$m_W = 80360.2 \pm 9.9 \text{ MeV}$$

- first m_W measurement from CMS
- in agreement with the SM prediction
- measurement is performed with $\sim 10\%$ of Run 2 data
- major advances in experimental and theoretical techniques from the basis for further improved precision and additional measurements in the future

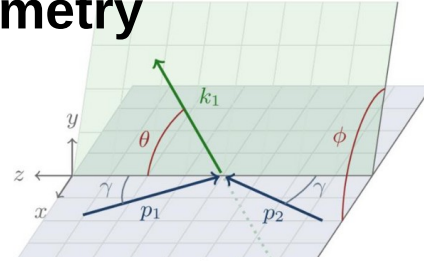
Source of uncertainty	Impact (MeV)			
	Nominal		Global	
	in m_Z	in m_W	in m_Z	in m_W
Muon momentum scale	5.6	4.8	5.3	4.4
Muon reco. efficiency	3.8	3.0	3.0	2.3
W and Z angular coeffs.	4.9	3.3	4.5	3.0
Higher-order EW	2.2	2.0	2.2	1.9
p_T^V modeling	1.7	2.0	1.0	0.8
PDF	2.4	4.4	1.9	2.8
Nonprompt background	–	3.2	–	1.7
Integrated luminosity	0.3	0.1	0.2	0.1
MC sample size	2.5	1.5	3.6	3.8
Data sample size	6.9	2.4	10.1	6.0
Total uncertainty	13.5	9.9	13.5	9.9

Towards the electroweak fit precision



Measurement of the effective weak mixing angle

lepton plane



• Measurement of $pp \rightarrow Z/\gamma^* \rightarrow \ell^+ \ell^-$ Forward-Backward asymmetry

- use Collins-Soper frame (Z boson at rest)
 - z axis defined by quark direction
 - using final state leptons angular distribution

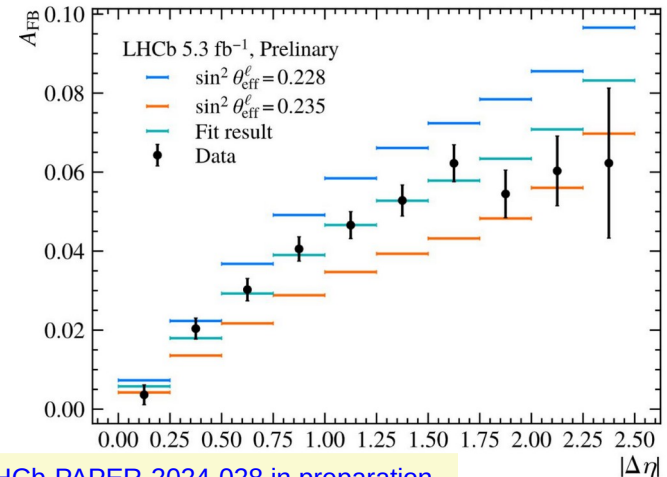
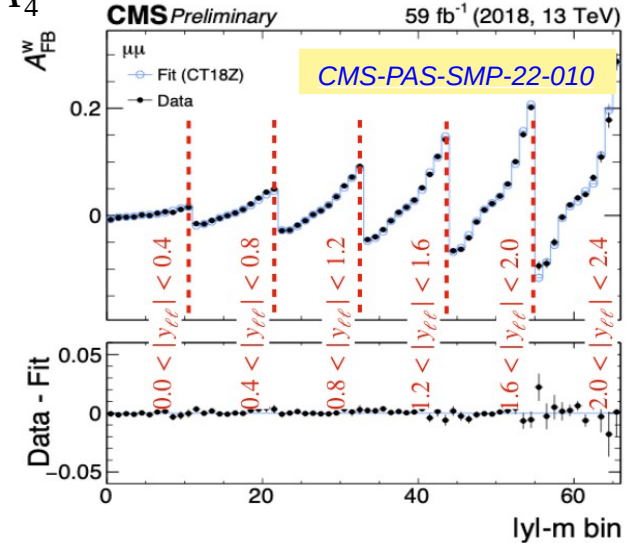
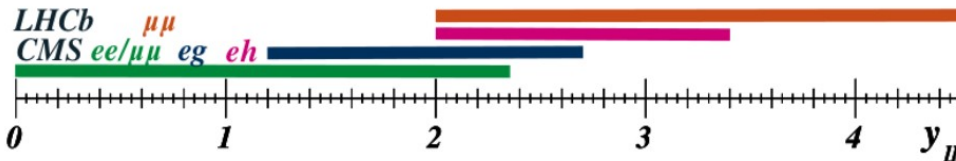
$$\frac{d\sigma}{d\cos\theta} \sim 1 + \cos^2\theta + \frac{1}{2} A_0 (1 - 2\cos^2\theta) + A_4 \cos\theta, \quad A_{FB} = \frac{3}{8} A_4$$

- the Forward-Backward asymmetry A_{FB} increases with the Z boson rapidity
 - only valence quarks contribute to the A_{FB}
 - ambiguity in quark direction resolved through rapidity-dependent measurement

- experimentally defined as

$$A_{FB} = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)} \quad A_{FB} = \frac{N(\eta^- > \eta^+) - N(\eta^- < \eta^+)}{N(\eta^- > \eta^+) + N(\eta^- < \eta^+)}$$

- reconstruction of muons in CMS up to $|\eta| < 2.4$
- 3 categories for electrons : « e » tracker only ($|\eta| < 2.5$), «g» in FCAL ($2.5 < |\eta| < 2.87$), «h» in forward HCAL ($2.5 < |\eta| < 2.87$),
- high quality muon reconstruction in LHCb in $2.0 < |\eta| < 4.5$

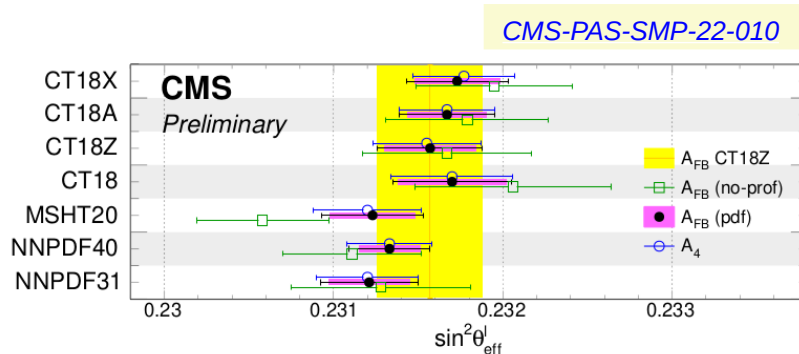


LHCb-PAPER-2024-028 in preparation
([link to CERN seminar](#))

Measurement of the effective weak mixing angle

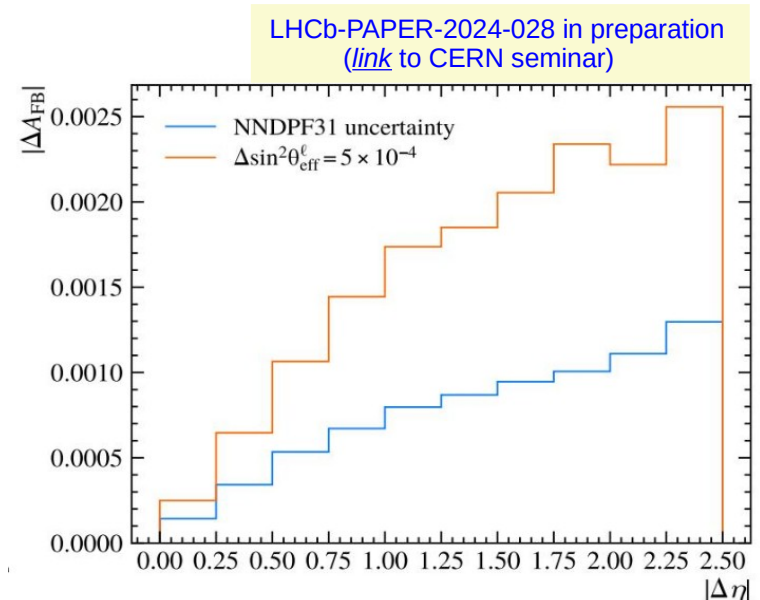
• CMS

- total uncertainty dominated by PDFs
- PDF reweighted/profiled in fit of A_{FB} and A_4 to determine $\sin^2 \theta_{eff}^\ell$
 - reduces PDF uncertainties by a factor of 2
 - results in better agreement between different PDF sets
- CT18Z chosen as ‘default’ pdf set before unblinding
 - its uncertainty covers best other central values



• LHCb

- the uncertainty from the PDF is estimated following the prescription provided by the groups responsible for each of the PDF sets used
- considering variations in the PDF “replicas”
- the PDF uncertainty \ll statistical uncertainty ($\sim 4.4 \times 10^{-4}$) because of the use of the LHCb acceptance
- don't need to use profiling to reduce the PDF uncertainty



Measurement of the effective weak mixing angle

LHCb-PAPER-2024-028 in preparation
 ([link](#) to CERN seminar)

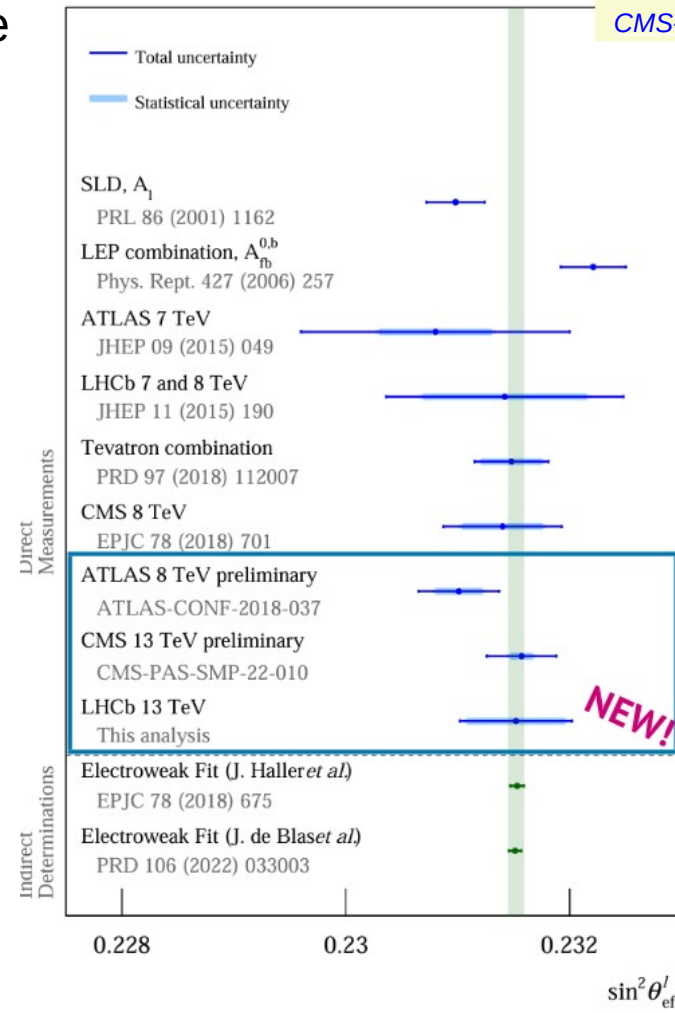
CMS-PAS-SMP-22-010

• Precise measurements from hadron colliders

- precisions comparable to the most precise single measurements at LEP A_{FB}^b and SLD A_{LR} determination

- to be compared to calculation from SM using precise experimental inputs

$$\sin^2 \theta_{eff}^\ell = 0.23155 \pm 0.00004 \text{ (SM)}$$



$$\text{CMS : } \sin^2 \theta_{eff}^\ell = 0.23157 \pm 0.00010 \text{ (stat)} \pm 0.00015 \text{ (syst)} \pm 0.00009 \text{ (theo)} \pm 0.00027 \text{ (PDF)}$$

$$\text{LHCb : } \sin^2 \theta_{eff}^\ell = 0.23152 \pm 0.00044 \text{ (stat)} \pm 0.00005 \text{ (syst)} \pm 0.00022 \text{ (theo/PDF)}$$

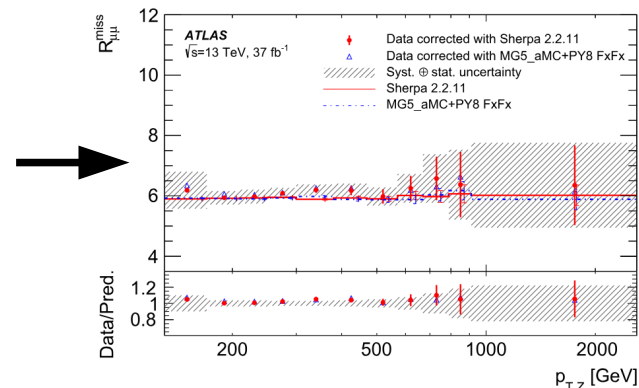
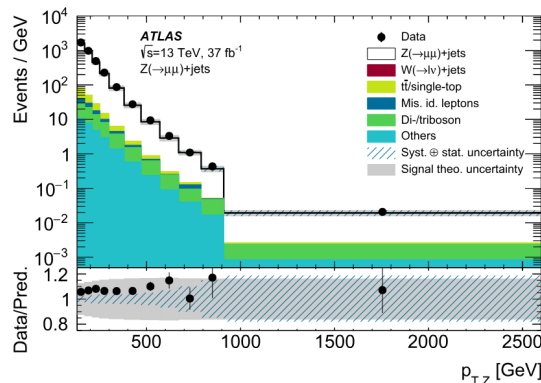
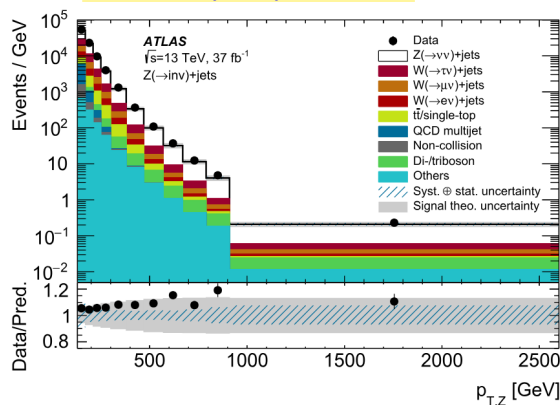
Z boson invisible width

- Width of Z boson for decays into invisible states $\Gamma(Z \rightarrow \text{inv})$ sensitive to
 - number of light neutrinos ($m_\nu < m_Z/2$)
 - potential BSM contributions from new particles

1. correct $Z \rightarrow \text{inv}$ and $Z \rightarrow \ell\ell$ to common phase-space
2. take ratio
3. fit constant \hat{R}^{miss}

$$R^{\text{miss}}(p_{T,Z}) \equiv \left(\frac{d\sigma(Z(\rightarrow \text{inv}) + \text{jets})}{dp_{T,Z}} \right) / \left(\frac{d\sigma(Z(\rightarrow \ell\ell) + \text{jets})}{dp_{T,Z}} \right)$$

PLB 854 (2024) 138705



Z boson invisible width

Convert fitted constant to Z boson invisible width by combining with $Z \rightarrow \ell\ell$ width measurement from LEP

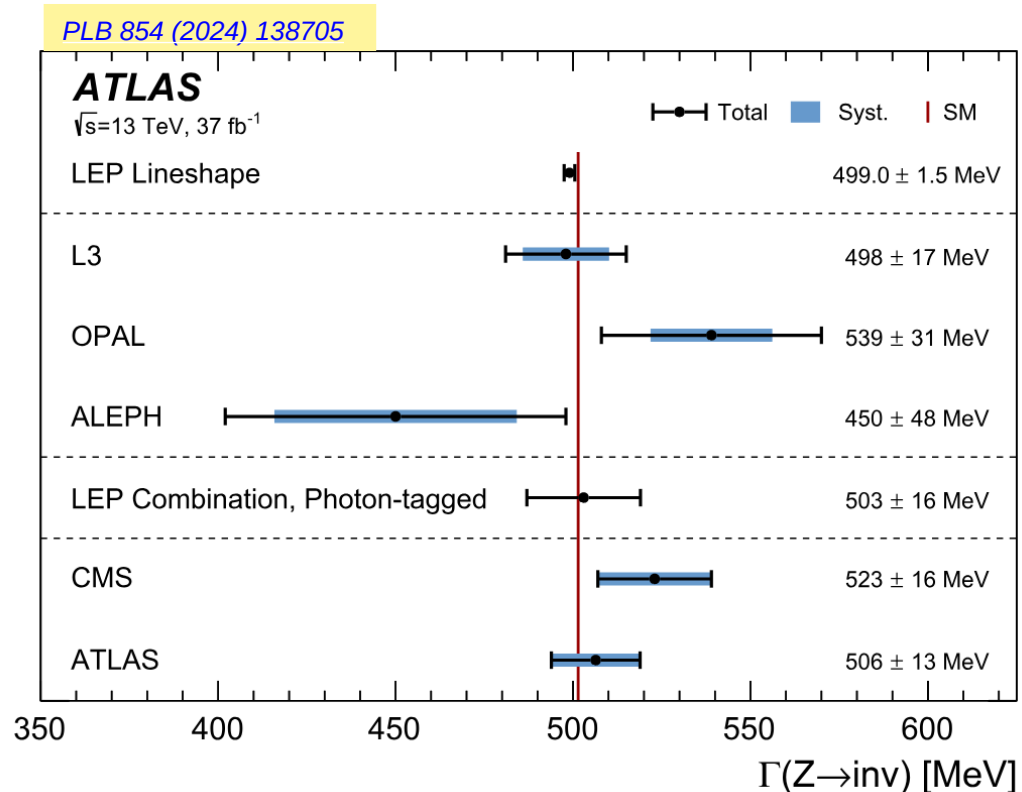
$$\Gamma(Z \rightarrow \text{inv}) = \hat{R}^{\text{miss}} \cdot \Gamma(Z \rightarrow \ell\ell)$$

Most precise recoil-based result

Precision limited by lepton systematic uncertainties in $Z \rightarrow \ell\ell$ events

ATLAS : $\Gamma(Z \rightarrow \text{inv}) = 506 \pm 13 \text{ MeV}$

CMS : $\Gamma(Z \rightarrow \text{inv}) = 523 \pm 16 \text{ MeV}$



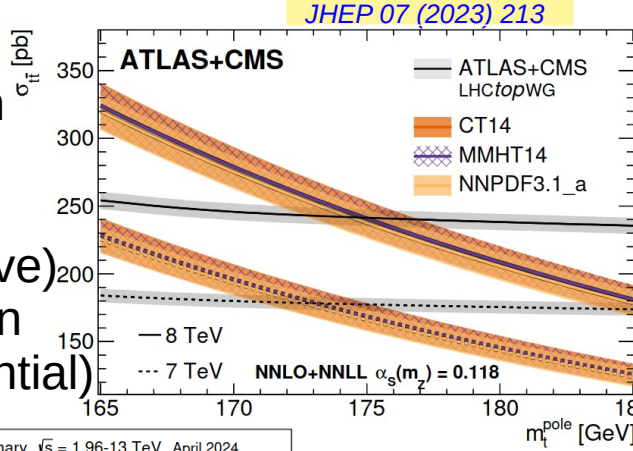
PLB 854 (2024) 138705

Phys. Lett. B 842 (2023) 137563

Measuring the top-quark mass m_t

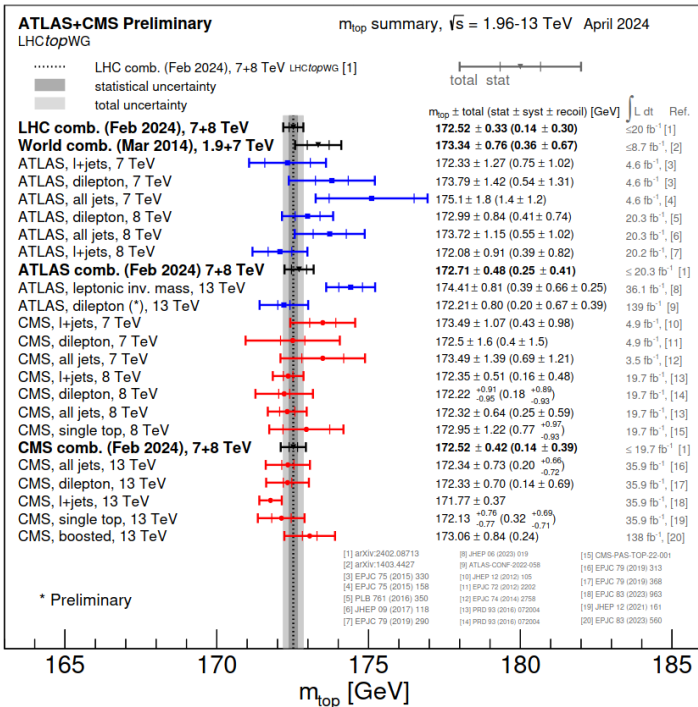
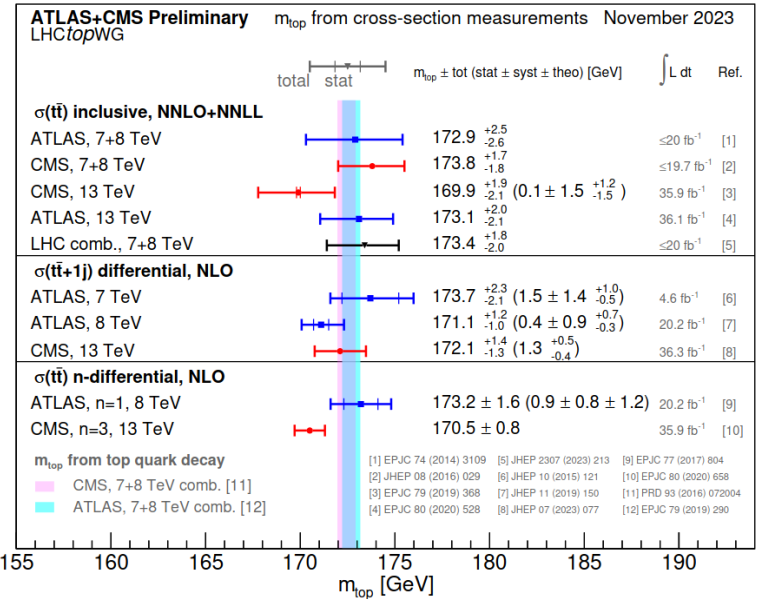
- Significant improvements over the past years
 - better calibrations, alternative techniques, improved theoretical modelling
 - more than 40 publications by ATLAS and CMS collaborations

- « Indirect »
 - from cross-section measurements
 - ~1% precision on pole mass (inclusive)
 - ~0.4% precision on pole mass (differential)



JHEP 07 (2023) 213

LHCTopWG SummaryPlots



- « Direct »

- extract m_t from decay products (l +jets, $l\bar{l}$)
 - ~0.2% precision
- single most precised measurements @13 TeV

CMS l +jet : $m_t = 171.77 \pm 0.37$ GeV

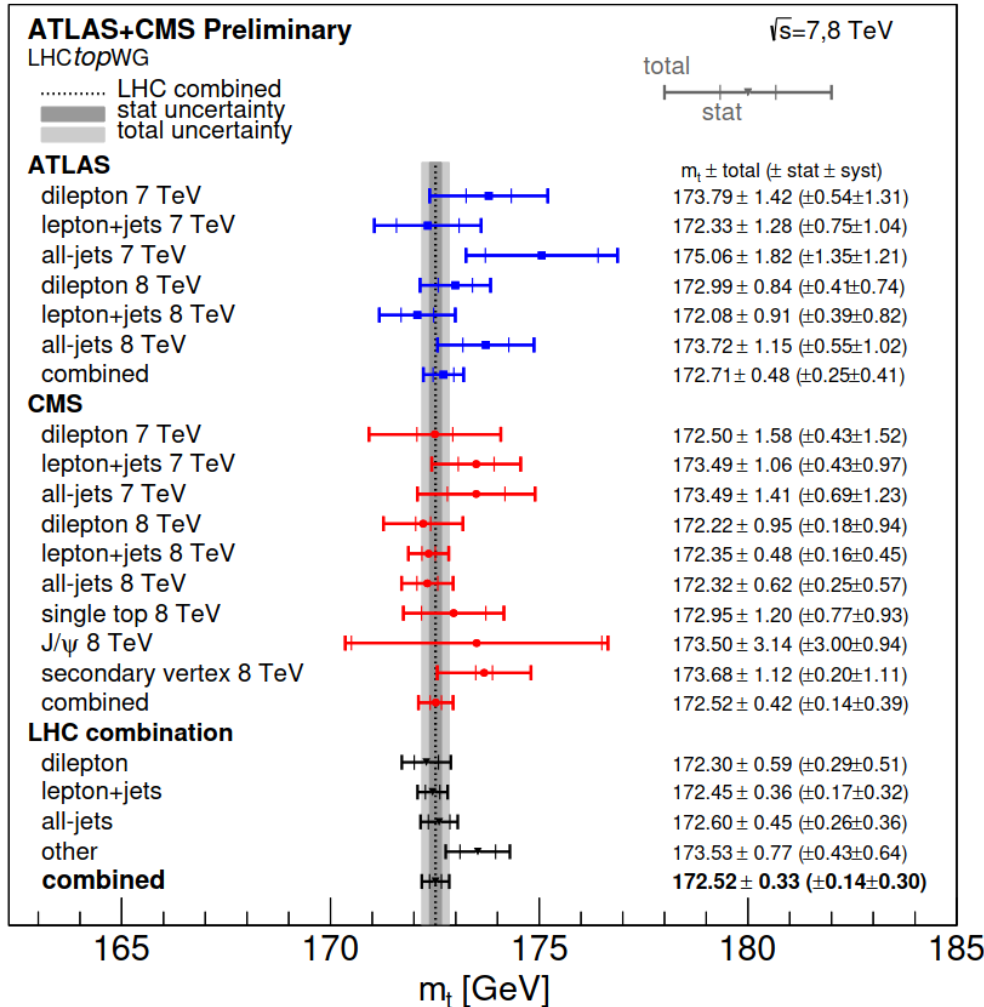
EPJC 83 (2023) 963

ATLAS $l\bar{l}$: $m_t = 172.21 \pm 0.80$ GeV

ATLAS-CONF-2022-058

Measuring top-quark mass m_t : Run 1 combination

A combination of fifteen top-quark mass measurements performed by the ATLAS and CMS experiments at the LHC



[LHCtopWG Summary Plots](#)
Phys. Rev. Lett. **132**, 261902

- using BLUE^[1], calculate or estimate the correlation between measurements, then calculates the corresponding uncertainty on the physics parameter
- ATLAS inputs 6 measurements, CMS the same channels plus single top, J/ ψ and secondary vertex at 8TeV
- to see compatibility run “simultaneous” BLUE with two m_t parameters, $m_t(\text{ATLAS})$ and $m_t(\text{CMS})$, excellent agreement
- resulting precision is below 2 per mil
- 31% improvement over most precise single input

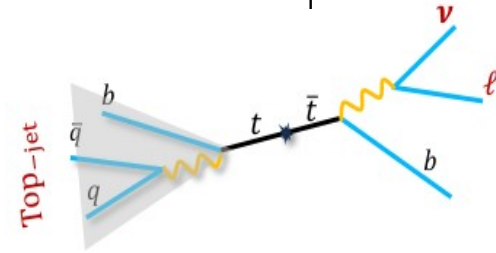
[1] Nucl. Inst. and Meth. A 270 (1988) 110

$m_t = 172.52 \pm 0.14 \text{ (stat)} \pm 0.30 \text{ (syst)} \text{ GeV}$, with a total uncertainty of 0.33 GeV

Measuring m_t : boosted channels

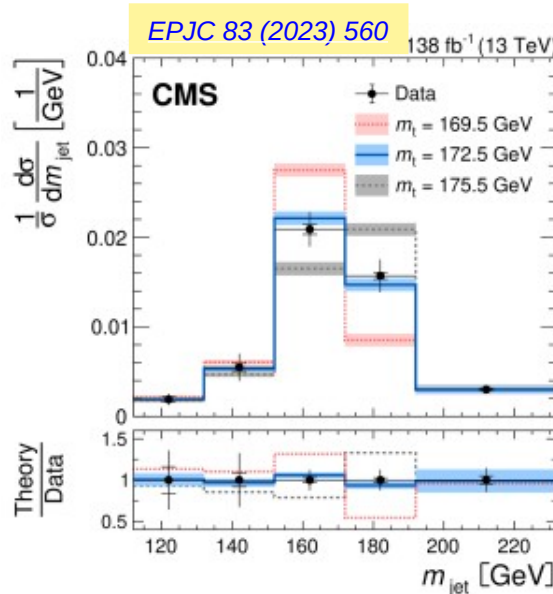
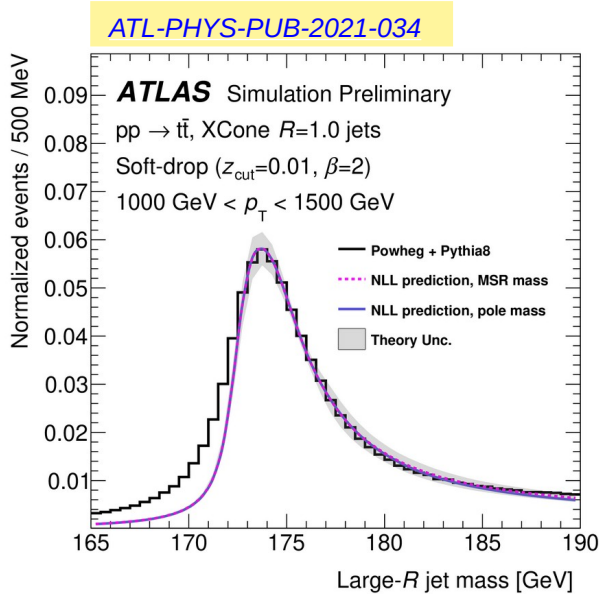
• Direct measurements from top-quark decays

- extract well defined m_t from boosted top-jet using large-radius jet : $m^2(\text{jet}) = (\sum p_i)^2$
- compare measurement to well defined field theory parameter
 - no additional uncertainty for $m_{top}^{MC} \rightarrow m_{top}^{MSR}$
- phase-space of theory and experiment different
 - calculations only at $p_T \geq 750$ GeV and experiment at $p_T \geq 400$ GeV



• CMS

- improved jet reconstruction in Run 2 \Rightarrow improvement in jet resolution
- unfolding, differential cross-section measurement
- reduced dominant uncertainties : calibration of Jet Mass Scale, modeling of FSR

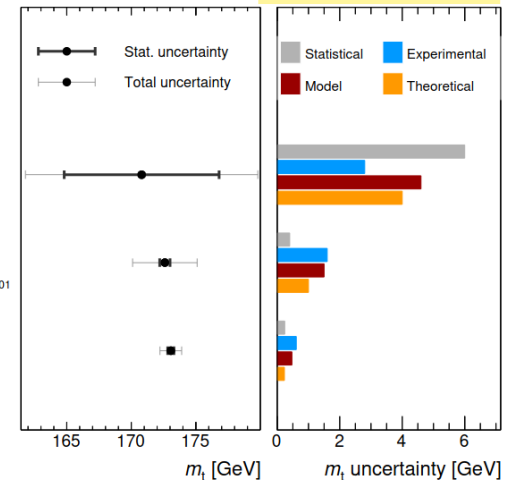


CMS

8 TeV (19.7 fb^{-1})
 $m_t = 170.8 \pm 9.0 \text{ GeV}$
 Eur. Phys. J. C 77 (2017) 467

13 TeV (35.9 fb^{-1})
 $m_t = 172.6 \pm 2.5 \text{ GeV}$
 Phys. Rev. Lett. 124 (2020) 202001

13 TeV (138 fb^{-1})
 $m_t = 173.06 \pm 0.84 \text{ GeV}$
 Eur. Phys. J. C 83 (2023) 560



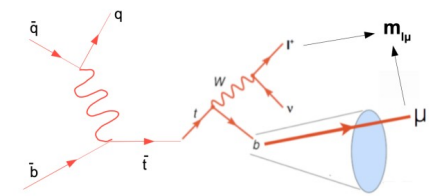
$$\Delta^{MSR} = m_t^{MC} - m_t^{MSR}(1 \text{ GeV}) = 80_{-400}^{+350} \text{ MeV}$$

$$m_t = 173.06 \pm 0.84 \text{ GeV}$$

Measuring m_t : alternative channels

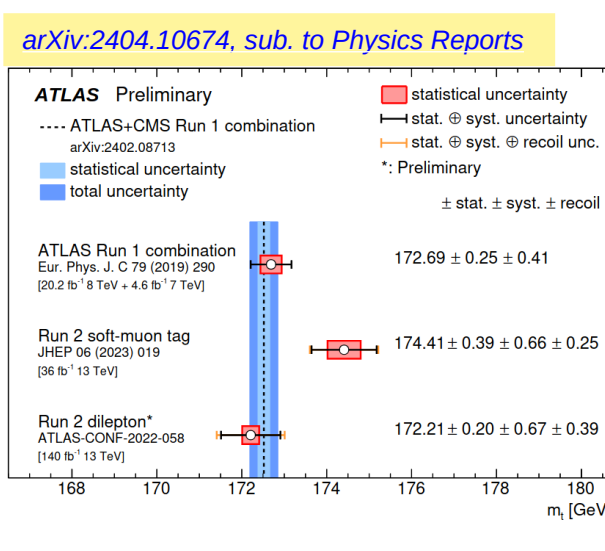
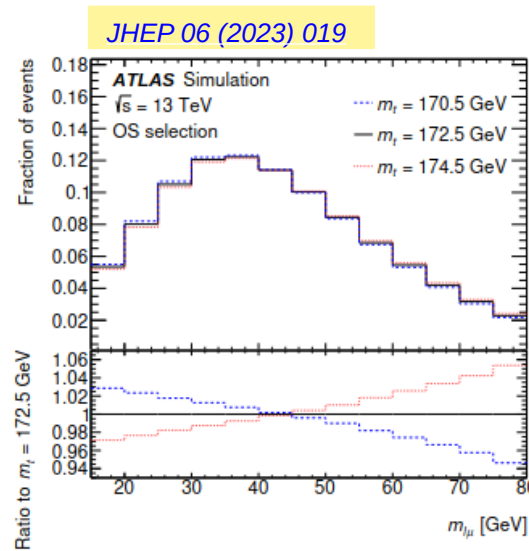
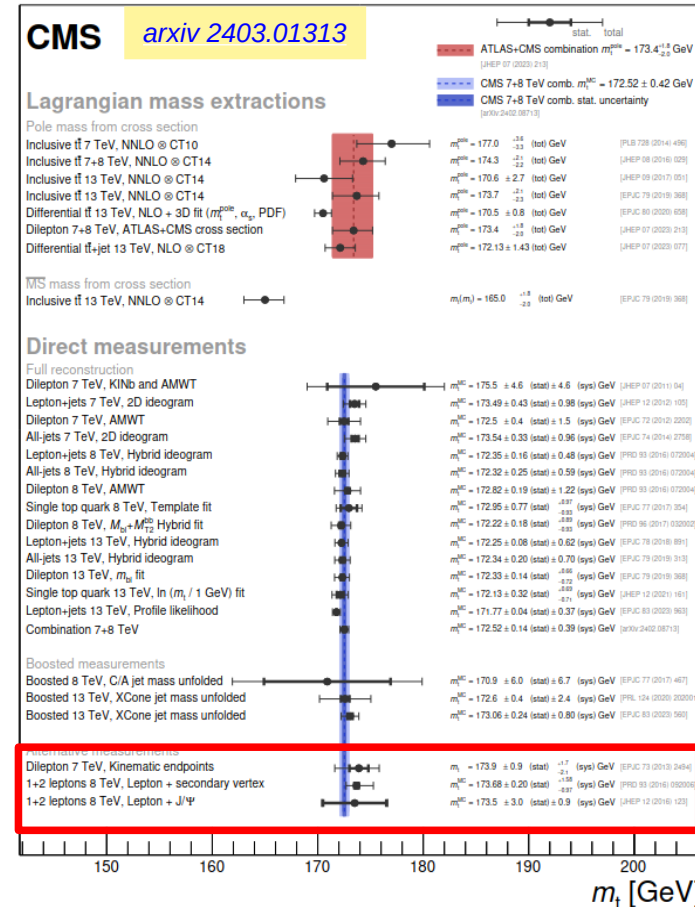
Direct measurements from top-quark decays

- alternative measurements \Rightarrow sensitive to different systematics



ATLAS

- construct templates of leptonic-only $m_{l\mu}$, lepton from W and soft μ from a b-hadron
 - smaller sensitivity to jet energy scale & resolution
 - less sensitivity to top-quark production modeling than previously showed measurement
- binned-template profile likelihood fit used to find best value for m_t , systematics included as Gaussian-constrained nuisance parameters



$m_t = 174.41 \pm 0.39$ (stat.) ± 0.66 (syst.) ± 0.25 (recoil) GeV

“Alternative”: limited by modeling of b-quark fragmentation

Summary

- Numerous results of precision electroweak physics released in the last 12 months!
- The LHC is competing with previous machines in electroweak precision
- Facilitated by large datasets, detailed understanding of the detectors, dedicated reconstruction techniques and state-of-the-art theory predictions
- New measurements of key electroweak parameters
 m_W (precision at 0.2 per mil), Γ_W and $\sin^2 \theta_{eff}^\ell$
- They join precision probes in improving our understanding of electroweak symmetry breaking
 - top-quark mass measurements in different channels, with increasing precision ATLAS+CMS Run-1 combination lead to a precision already around 0.3 GeV (precision below 2 per mil)
 - precise measurements of $\Gamma(Z \rightarrow inv)$

Backup slides

Introduction

● Parameters of the Standard Model

○ at Tree level, simple relations after BEH mechanism with $\phi = \begin{pmatrix} 0 \\ v/2 \end{pmatrix}$

- $m_W = \frac{gv}{2} \quad m_Z = \frac{\sqrt{g^2 + g'^2} v}{2}$

○ radiative corrections Δr modify propagator and decay vertices

- sensitivity to a wide range of physics through quantum loops
- largest contributions from m_t , $\log(m_H)$

$$G_F \propto \frac{g^2}{m_W^2} \quad m_W = \left(\frac{\pi \alpha_{QED}}{\sqrt{2} G_F} \right)^{1/2} \frac{\sqrt{1 + \Delta r}}{\sin \theta_W}$$

$$\sin^2 \theta_{\text{eff}}^\ell = \kappa \sin^2 \theta_W, \quad \kappa \sim 1.037 \quad \sin^2 \theta_W = 1 - m_W^2 / m_Z^2$$

2

● Precision measurements

- test self-consistency of SM theory in global EW fits
- tensions could be signs of BSM effects
- probe BSM beyond reach of searches

Measurement of the W boson mass m_W

- **The W boson mass in proton collisions**

- incomplete kinematics (due to missing neutrino)
 - no invariant mass; rely on measured quantities, and exploit momentum conservation in the transverse plane

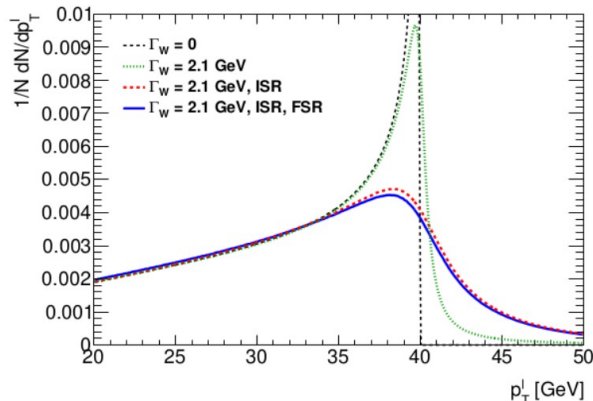
- event representation

- main signature : electron or muon \vec{p}_T^ℓ
- recoil : sum of « everything else » reconstructed in the calorimeters $\vec{u}_T = \sum E_T^i \Rightarrow$ a measure of $p_T^{W,Z}$
- derived quantitiesⁱ

$$\vec{p}_T^{\text{miss}} = -(\vec{p}_T^\ell + \vec{u}_T) \quad m_T = \sqrt{2 p_T^\ell p_T^{\text{miss}} (1 - \cos \Delta \phi)}$$

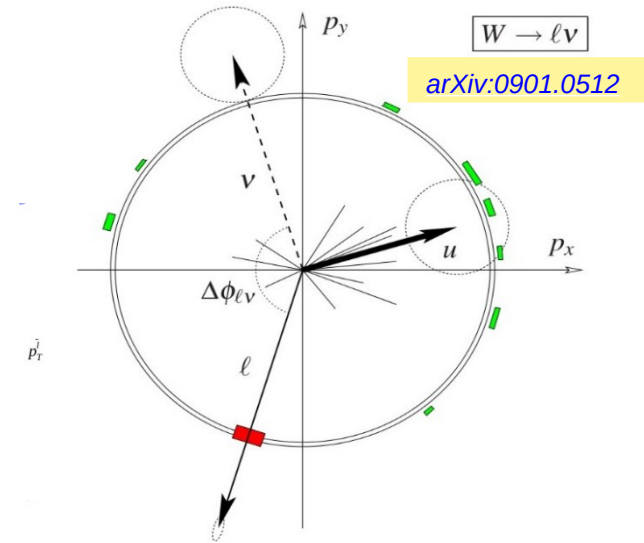
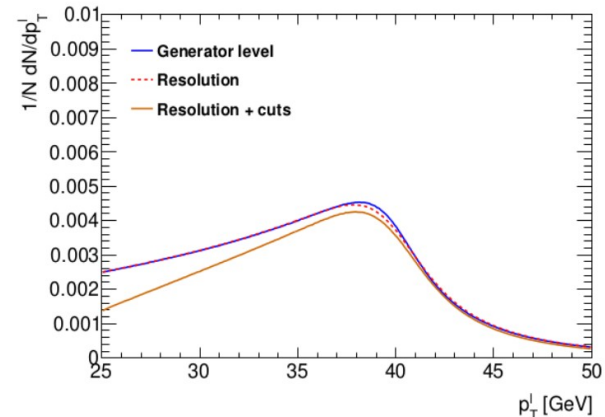
- physics correction :

- Γ_W , QCD and QED ISR and FSR, PDFs, ...
- all carry uncertainties to be quantified !



- detector effects, with uncertainties

- lepton calibration and resolution; Missing ET resolution $\sim 5 - 15$ GeV
- efficiencies and acceptance $\sim 15\%$ (with non-trivial kinematic dependence !)

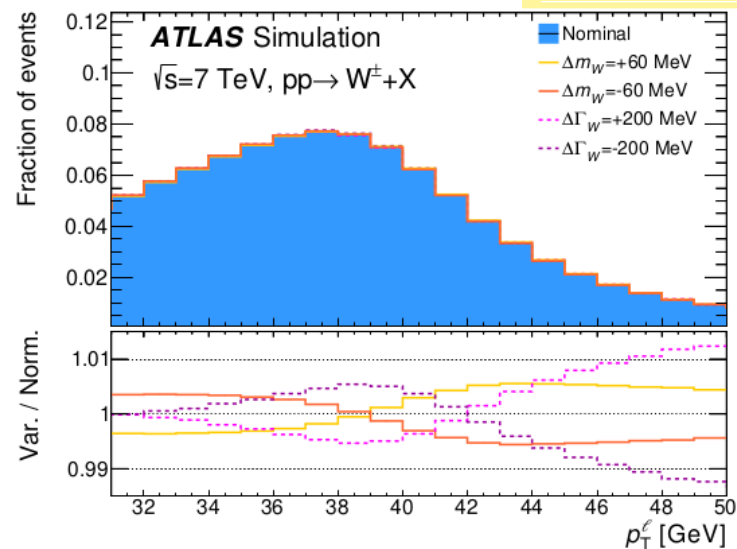


Measurement of the W boson mass m_W

arXiv:2403.15085

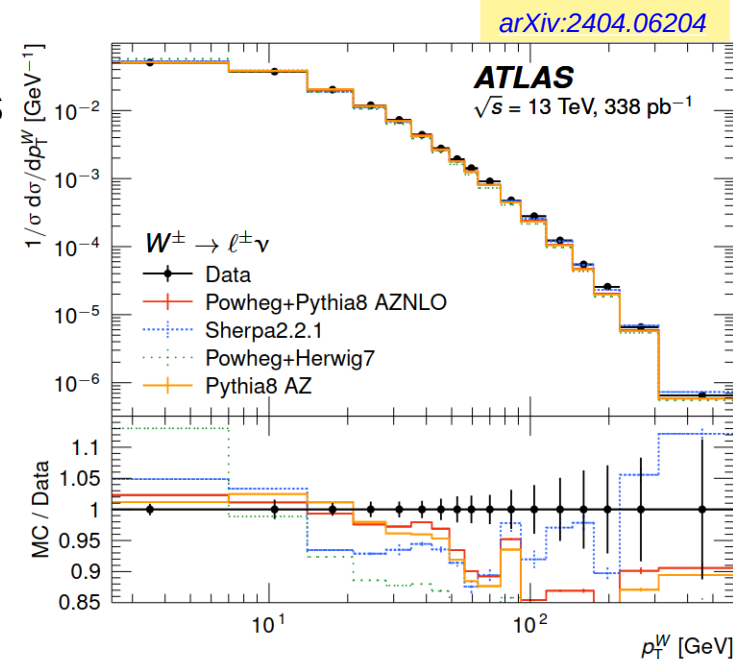
● ATLAS

- revisit 2011 (7 TeV) data, favourable experimental environment for measurement of m_W
- unchanged from previous analysis
 - 15 M $W \rightarrow e\nu$ and $W \rightarrow \mu\nu$ candidates
 - lepton p_T : Jacobian edge at $m_W/2$
 - transverse mass m_T : Jacobian edge at m_W , more sensitive to Γ_W in tails
 - template fits using kinematic observables sensitive to m_W and Γ_W



● Improvement since first measurement

- checks of p_T^W modelling in dedicated measurements
- update to QCD background estimation
- more modern PDF sets: CT18 (was CT10nnlo)
- small update to uncertainties for higher-order electroweak corrections
- key change: profile likelihood fit
 - constrain systematic uncertainties in situ
 - directly determine their correlations
 - challenge: m_W now also correlated with some syst. variations \rightarrow extensive validation of method to avoid biases

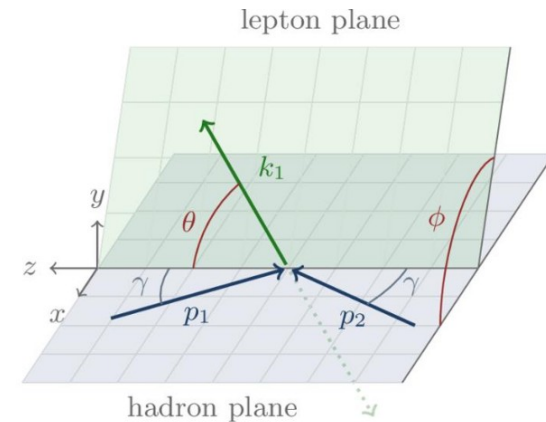


arXiv:2404.06204

Measurement of the effective weak mixing angle

• Measurement of $pp \rightarrow Z/\gamma^* \rightarrow \ell^+\ell^-$ Forward-Backward asymmetry

- the Forward-Backward asymmetry A_{FB} increases with the Z boson rapidity
 - only valence quarks contribute to the A_{FB}
 - the forward region direction is given by the valence quark i.e. the system boost direction
- use Collins-Soper frame
 - z axis defined by quark direction
 - using final state leptons angular distribution in this frame



$$\frac{d\sigma}{d\cos\theta} \sim 1 + \cos^2\theta + \frac{1}{2}A_0(1 - 2\cos^2\theta) + A_4\cos\theta \quad A_{FB} = \frac{3}{8}A_4$$

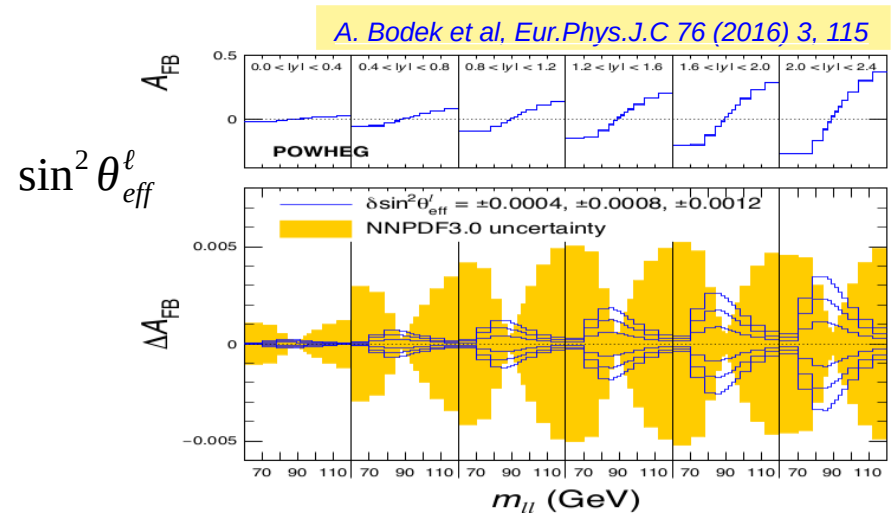
- at the Z peak, A_{FB} yields a measurement of

- strong PDF dependence

- experimentally defined as

$$A_{FB} = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)}$$

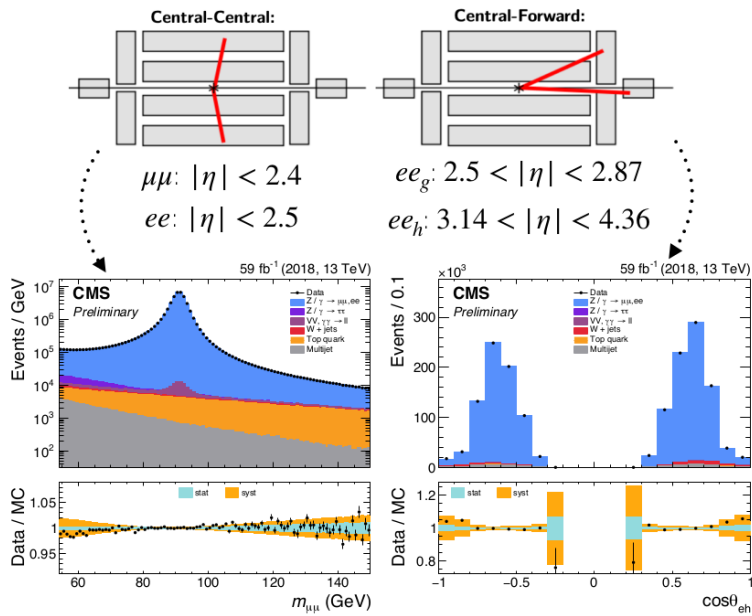
$$A_{FB} = \frac{N(\eta^- > \eta^+) - N(\eta^- < \eta^+)}{N(\eta^- > \eta^+) + N(\eta^- < \eta^+)}$$



Measurement of the effective weak mixing angle

• CMS analysis strategy

- full Run 2 dataset (137 fb⁻¹)



- background events

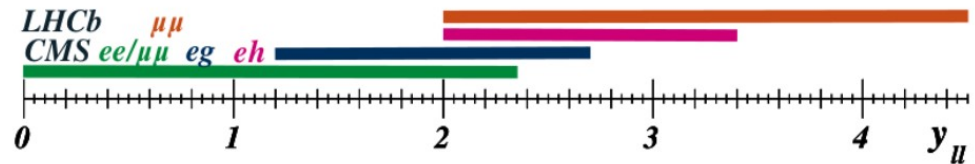
- QCD multijets,
- W+jets, ...
- others (MC samples)

- systematic uncertainties

- experimental : MC stat., efficiency, momentum calibration. backgrounds
- theory : QCD scales, pT(μ), QED FSR virtual EW, **PDFs**

• LHCb analysis strategy

- 2016-2018 dataset (5.3 fb⁻¹)
 - measure A_{FB} in tens interval of $|\Delta\eta|$ up to $|\Delta\eta| < 2.5$ using $Z \rightarrow \mu\mu$ decays
 - identified μ candidate matched to a single muon trigger path in a fiducial region $2.0 < |\eta_\mu| < 4.5$, $p_T(\mu) > 20$ GeV
- $66 < m(\mu\mu) < 116$ GeV



- background events

- HF backgrounds are suppressed to the % level by a muon impact parameter requirement
- hadronic background suppressed to the % level by an isolation requirement and muon track fit requirement

- yields

- roughly 860k events are selected

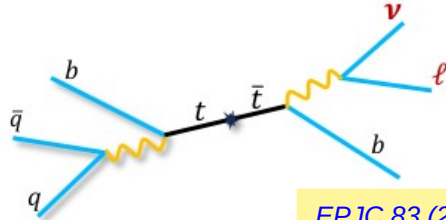
Measuring m_t : direct measurements

- « Direct » measurements from top-quark decays
 - better precision ; extract m_t from decay products

LHCtopWGSummaryPlots
Phys. Rev. Lett. 132, 261902

• CMS

- most precise individual measurement performed in ℓ +jets channel
- construct m_t from three jets
- m_{top}^{MC} from minimizing a negative log-likelihood



EPJC 83 (2023) 963

$$m_t = 171.77 \pm 0.37 \text{ GeV}$$

• ATLAS

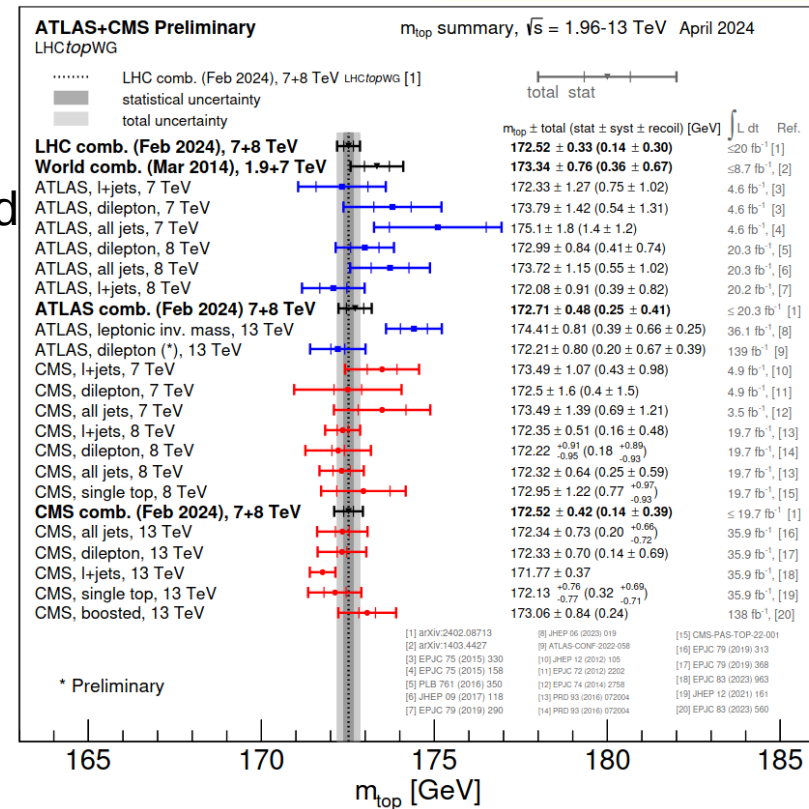
- most precise individual measurement performed in $\ell\ell$ +jets channel
- construct templates of m_{lb}
- m_{top}^{MC} from template fits on data

ATLAS-CONF-2022-058

$$m_t = 172.21 \pm 0.20(\text{stat}) \pm 0.67(\text{syst}) \pm 0.39(\text{recoil}) \text{ GeV}$$

• Combination 7-8 TeV

$$m_t = 172.52 \pm 0.33 \text{ GeV}$$



“Conventional” biggest challenges are JES uncertainties and b-JES calibration