

Impact of QCD and PDF uncertainties on SM precision measurements (at the LHC)

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on behalf of the ATLAS, CMS, and LHCb collaborations

Oct 10, 2024



Supported by CA22130 - Comprehensive Multiboson Experiment-Theory Action (COMETA)

Topics covered in this talk

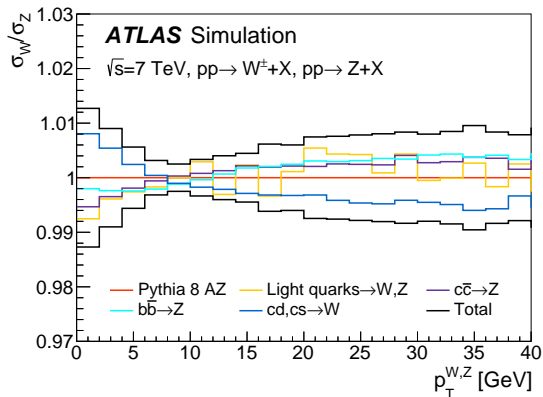
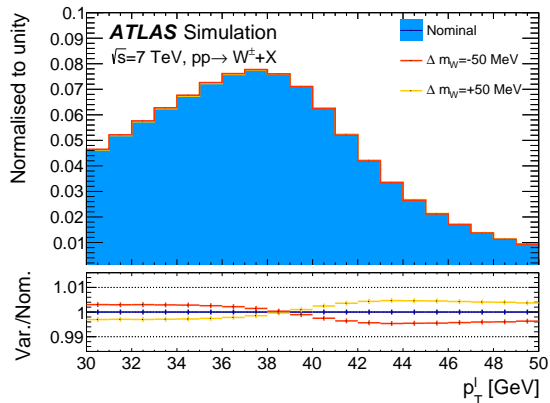
- W boson mass and width
- Weak mixing angle
- Electroweak diboson
- Top quark mass
- Strong coupling α_s
- Higgs → Miha (next talk)

Related plenary talks

- Valentina Guglielmi: Strong coupling measurements at the LHC (Monday)
- Johannes Erdmann: Status of Higgs boson precision measurements (Tuesday)
- Frederic Derue: Status of electroweak parameter measurements (Tuesday)
- Thorsten Kuhl: Recent experimental results on top and heavy-flavour production (Wednesday)
- Miha Muskinja: Impact of QCD and PDF uncertainties on BSM searches (today)
- ...and even more parallel talks!

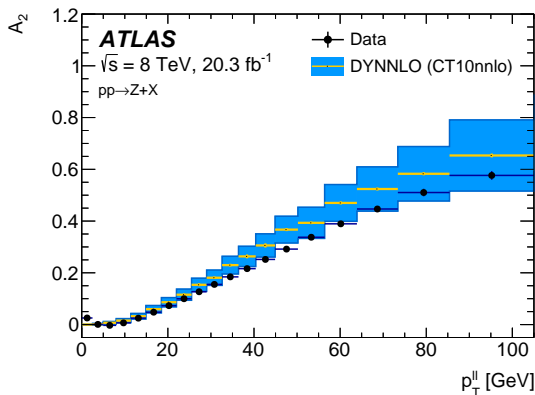
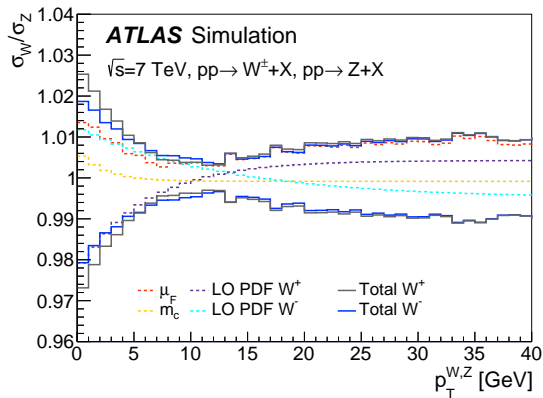
First measurement of the W mass at the LHC (± 19 MeV)

- Measurement of m_W from lepton p_T requires good control of W p_T



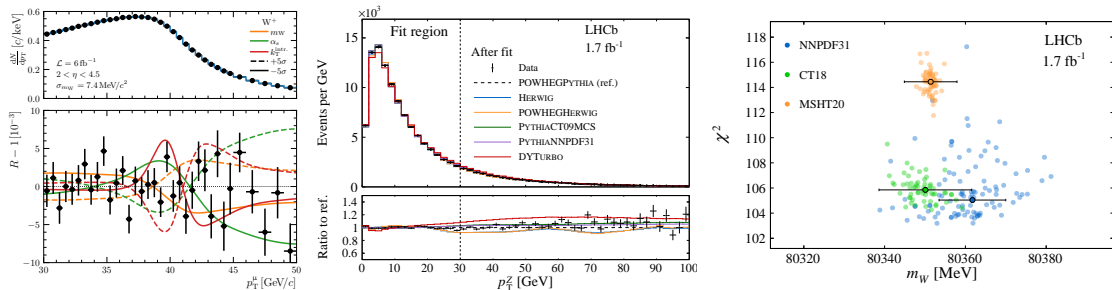
- Prediction by Pythia 8 Tune AZ (LO+ISR MEC), tuned to ATLAS Z p_T data
- Pythia μ_F variations, heavy quark initial states decorrelated between $W/Z \rightarrow \pm 5.0$ MeV
 - Uncorrelated light-quark component would give ± 30 MeV uncertainty (template fit)

- PDFs uncertainties are the largest: CT10nnlo eigenvectors (± 7.4 MeV)
 - \oplus comparison to MMHT14 and CT14 (± 3.8 MeV)



- Uncertainty on angular coefficients A_i from measurement in Z data (5.8 MeV)

- Simultaneous fit of W mass, ISR α_s , and intrinsic k_t [arXiv 1907.09958](#)



- p_T model: Powheg+Pythia vs Pythia vs Powheg+Herwig $\rightarrow \pm 11$ MeV (after fit)
 - Common intrinsic k_t but ISR α_s decorrelated between W and Z
- PDFs: average of NNPDF3.1, CT18, and MSHT20 $\rightarrow \pm 9$ MeV
- A_i at NNLO but A_3 would be ± 30 MeV. Included in fit $\rightarrow \pm 10$ MeV
- Anti-correlation of LHCb and GPDs, $\rho \simeq -0.5$ [arXiv 1508.06954](#) [arXiv 2308.09417](#)

Post-CDF W mass world combination

- All results shifted to set of common PDF sets
- Combined with BLUE method for each PDF
- With CDF: largest uncertainty from PDFs

All experiments (4 d.o.f.)				
PDF set	m_W	σ_{PDF}	χ^2	$p(\chi^2, n)$
ABMP16	80392.7 ± 7.5	3.2	29	0.0008%
CT14	80393.0 ± 10.9	7.1	16	0.3%
CT18	80394.6 ± 11.5	7.7	15	0.5%
MMHT2014	80398.0 ± 9.2	5.8	17	0.2%
MSHT20	80395.1 ± 9.3	5.8	16	0.3%
NNPDF3.1	80403.0 ± 8.7	5.3	23	0.1%
NNPDF4.0	80403.1 ± 8.9	5.3	28	0.001%

nominal

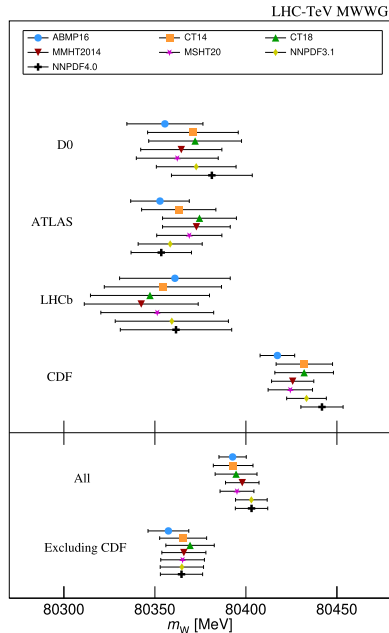
largest difference

- ABMP: smallest uncertainty due to anti-correlation between ATLAS $W_{+/-}$
- 10 MeV between lowest and highest
- W/o CDF: PDF down, total up, fit improved

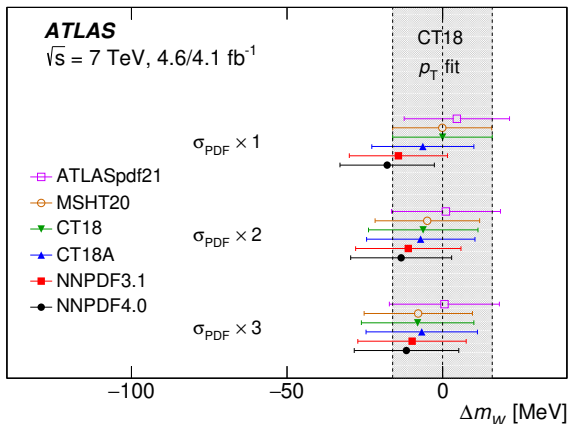
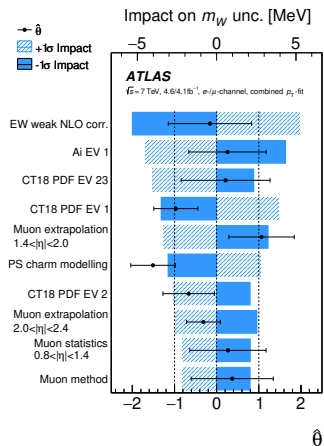
CT18	80369.2 ± 13.3	6.2	0.5	92%
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nominal

- 12 MeV difference between lowest and highest



- Fit to lepton p_T , treating all uncertainties as nuisance parameters

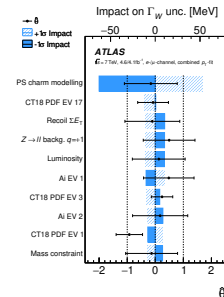
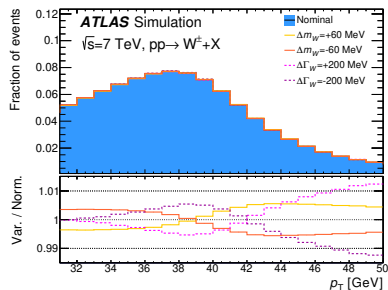


- Reduction of PDF uncertainty from 7.4 (CT10) to 4.9 MeV (profiled CT18)
- Difference between PDF sets: up to 18 MeV
 - Reducible by inflating prefit uncertainties but not applied by default

Measurement of the W width

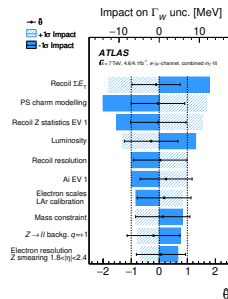
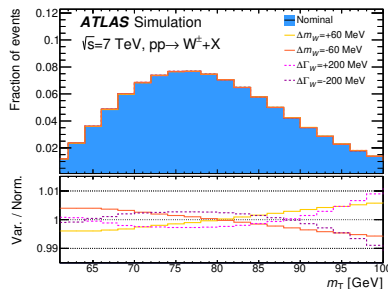
W width from lepton p_T

- Huge uncertainty from charm modeling ($m_c \pm 0.5$ GeV)
- Cannot be distinguished from width variation!
- ~~Change systematic variation~~
Consider different observable



W width from transverse mass m_T

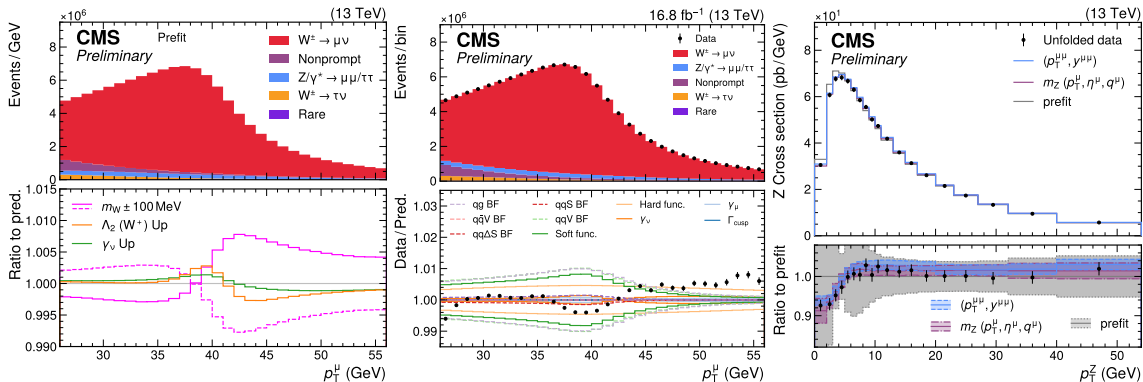
- Impact of charm modeling reduced by factor 4



Combined value mostly m_T

- Total uncertainty ± 47 MeV

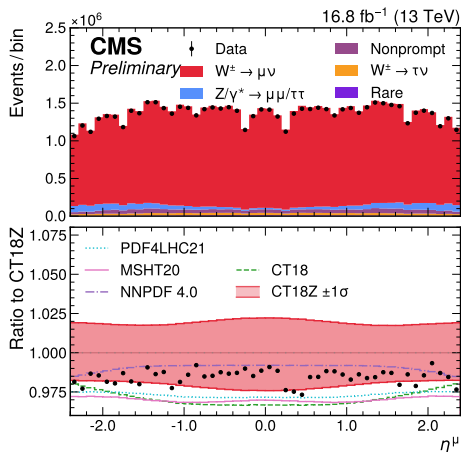
- Full profile likelihood fit to lepton p_T and η
- Prediction: MiNNLO reweighted to SCETlib+DYTurbo N³LL+NNLO
- TNP's instead of scale variations for resummation Tackmann $\rightarrow p_T^W$ uncertainty ± 2 MeV



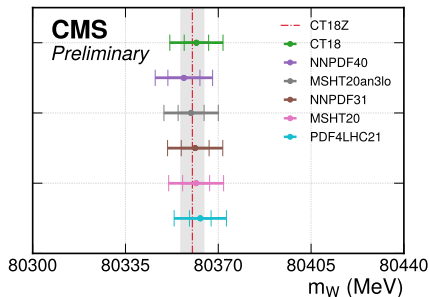
- W-like Z: one muon treated as neutrino \rightarrow good agreement in p_T^Z and m_Z
- MiNNLO scale uncertainties on $A_i \rightarrow \pm 3.2$ MeV, larger than p_T^W now

W mass at CMS (± 9.9 MeV): PDF treatment

- CT18Z as default PDF, profiling the eigenvectors $\rightarrow \pm 4.4$ MeV
- Derive scale factors to cover m_W extracted with all other PDF sets



PDF set	Scale factor	Impact in m_W (MeV)	
		Original σ_{PDF}	Scaled σ_{PDF}
CT18Z	–	4.4	
CT18	–	4.6	
PDF4LHC21	–	4.1	
MSHT20	1.5	4.3	5.1
MSHT20aN3LO	1.5	4.2	4.9
NNPDF3.1	3.0	3.2	5.3
NNPDF4.0	5.0	2.4	6.0



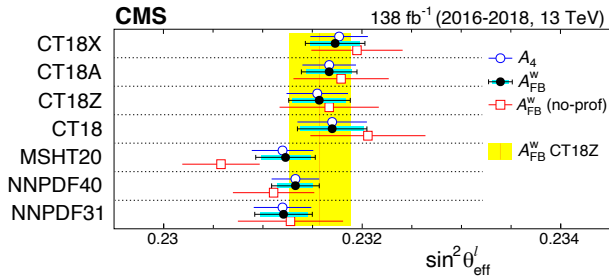
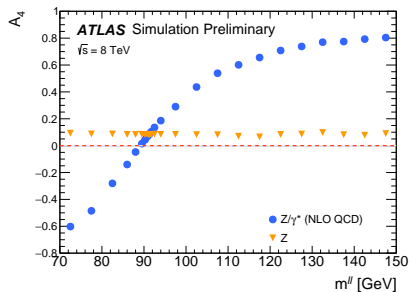
- Very good consistency between PDF sets even before scaling, owed to η^μ
- Difference CT18 vs NNPDF4.0 reduced from 5 MeV to 3 MeV

Weak mixing angle at ATLAS and CMS

- Measured by Z/γ^* forward-backward asymmetry, need to infer initial state
- Less dilution at higher Z rapidity \rightarrow use electrons in forward calorimeters

7 TeV **ATLAS** **STDM-2011-34** (total $\pm 12 \times 10^{-4}$) \rightarrow 8 TeV **ATLAS** **CONF-2018-037** (total $\pm 3.6 \times 10^{-4}$)

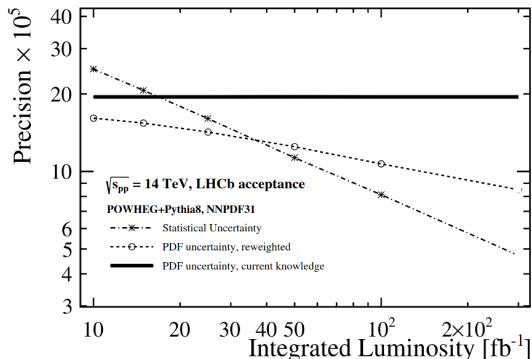
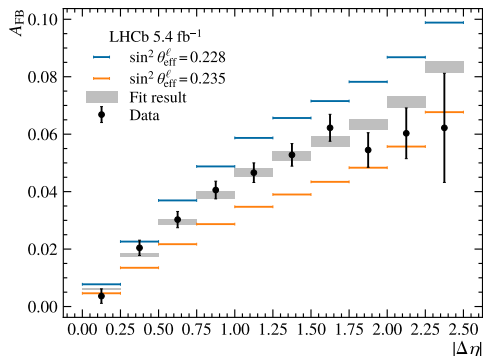
- PDF treatment: ATLAS-epWZ12 ($\pm 9 \times 10^{-4}$) \rightarrow MMHT14 ($\pm 2.4 \times 10^{-4}$)



13 TeV measurement **CMS** **SMP-22-010** (total $\pm 3.1 \times 10^{-4}$)

- PDF profiling \rightarrow reduction of differences, decrease of individual PDF uncertainties
- Central value with CT18Z ($\pm 2.7 \times 10^{-4}$), covers other PDF sets

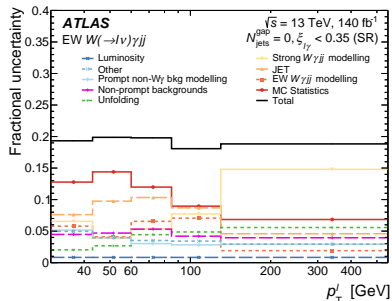
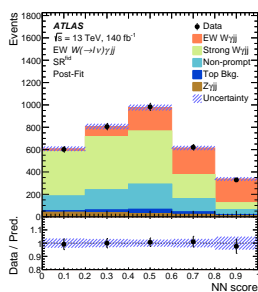
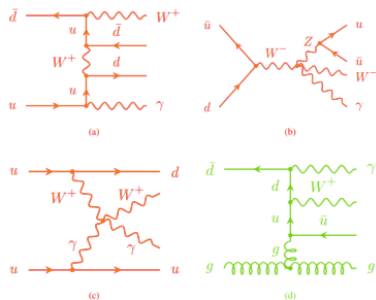
- Advantage: muon reconstruction in the forward region ($2.0 < \eta < 4.5$)
- 7+8 TeV: NNPDF2.3 $\rightarrow \pm 4.3 \times 10^{-4}$ (total $\pm 10.6 \times 10^{-4}$)
- 13 TeV: average of NNPDF3.1, CT18, and MSHT20 $\rightarrow \pm 2.1 \times 10^{-4}$ (total $\pm 4.9 \times 10^{-4}$)



- Dominated by statistical uncertainty, great prospects with more data

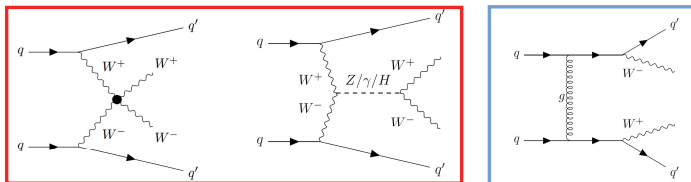
Remark for all $\sin^2 \theta$ measurements: $A_{4/FB}$ fully unfolded, available for reinterpretation

- QCD uncertainties relevant in EW measurements where QCD-induced subtracted
- Using NN to isolate EW from QCD-induced in VBS-enhanced phase space
→ observation of electroweak $W\gamma jj$, measured fiducial and differential cross sections



- Strong $W\gamma jj$ modeling uncertainties large at high lepton p_T
 - Sherpa NLO scale uncertainties, Sherpa vs MadGraph5_aMCatNLO
- Corresponding CMS measurement CMS SMP-21-011

■ Observation of electroweak W^+W^- production

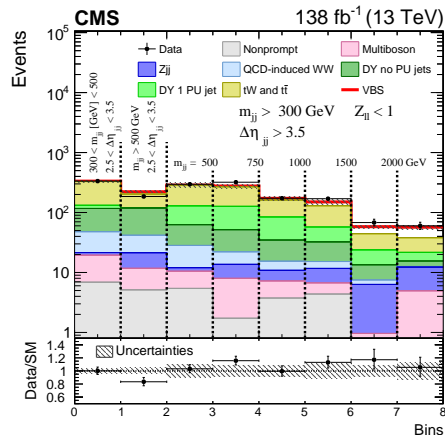


■ Selected uncertainties

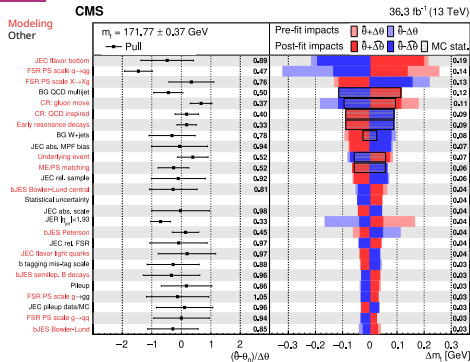
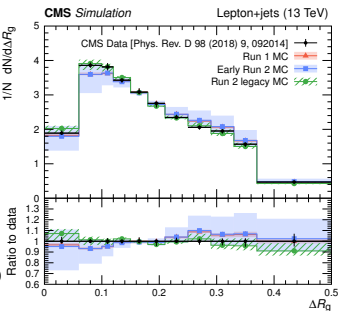
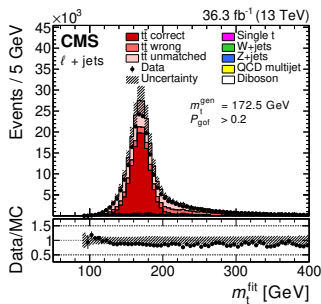
- Leading uncertainty: statistical (14.9%)
- $t\bar{t}$ scale variation (NLO, 5.1%)
- VBS signal scale variation ($WWjj$ @LO, 4.9%)
- QCD-induced scale variation (WW @NNLO, 2.1%)

■ Modeling might become limiting factor in the future

■ Corresponding ATLAS paper [ATLAS](#) [STDM-2022-06](#)



- Direct m_t measurements fit reconstructed top mass peak
- Progress in top quark modeling: switched to NLO generators, improved tunes, using parton shower weights for uncertainties

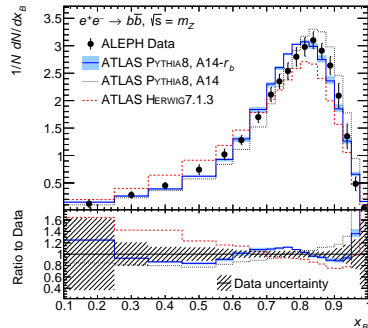
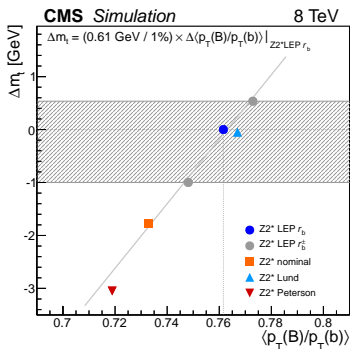
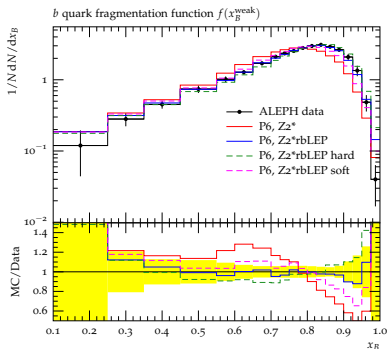


- PDF negligible but leading uncertainties from QCD modeling: Pythia vs Herwig b jet response, FSR scale, color reconnection
- Can we expect higher precision in top decays from NLL showers?

Top quark mass: alternative measurements

- Circumvent jet energy scale uncertainty by using heavy hadrons and leptons
- Large b fragmentation uncertainties in Run 1 CMS measurements

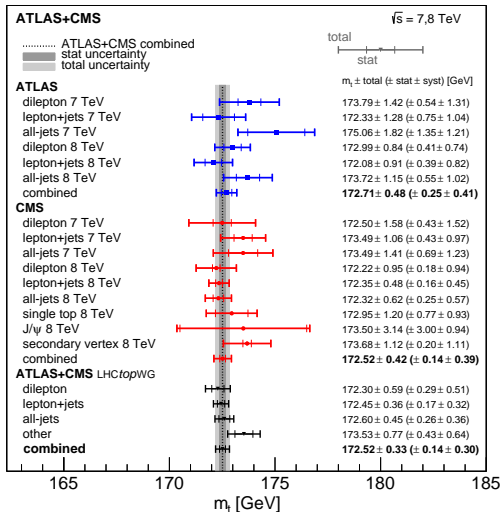
■ $m_{\text{SecVtx},\ell} \rightarrow {}^{+1.00}_{-0.64} \text{ GeV (bfrag)}$ CMS TOP-12-030 , $m_{J/\psi,\ell} \rightarrow \pm 0.3 \text{ GeV (bfrag)}$ CMS TOP-15-014



- ATLAS measurement using $m_{\ell\mu}$ with soft μ from b hadron decay ATLAS TOPQ-2017-17
 - Different approach of fitting LEP measurements $\rightarrow \pm 0.19 \text{ GeV (bfrag)}$
 - Leading uncertainties from b,c-hadron decay BRs ($\pm 0.40 \text{ GeV}$) and FSR recoil ($\pm 0.25 \text{ GeV}$)
- For all: no standard FSR variations evaluated, huge statistical uncertainties for J/ ψ

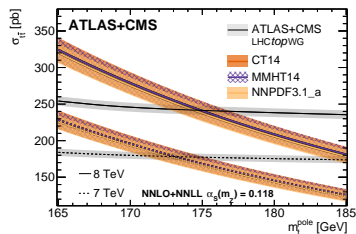
LHC Run 1 combination (direct+alternative)

- Most precise direct value from ATLAS+CMS Run 1 combination $\rightarrow \pm 0.33$ GeV
- CR uncertainty reduced, likely to be effect from limited sample size in each measurement

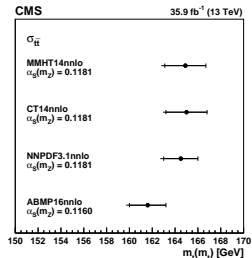


Uncertainty category	Uncertainty impact [GeV]		
	LHC	ATLAS	CMS
b-JES	0.18	0.17	0.25
b tagging	0.09	0.16	0.03
ME generator	0.08	0.13	0.14
JES 1	0.08	0.18	0.06
JES 2	0.08	0.11	0.10
Method	0.07	0.06	0.09
CMS b hadron β	0.07	—	0.12
QCD radiation	0.06	0.07	0.10
Leptons	0.05	0.08	0.07
JER	0.05	0.09	0.02
CMS top quark p_T	0.05	—	0.07
Background (data)	0.05	0.04	0.06
Color reconnection	0.04	0.08	0.03
Underlying event	0.04	0.03	0.05
g-JES	0.03	0.02	0.04
Background (MC)	0.03	0.07	0.01
Other	0.03	0.06	0.01
l-JES	0.03	0.01	0.05
CMS JES 1	0.03	—	0.04
Pileup	0.03	0.07	0.03
JES 3	0.02	0.07	0.01
Hadronization	0.02	0.01	0.01
p_T^{miss}	0.02	0.04	0.01
PDF	0.02	0.06	<0.01
Trigger	0.01	0.01	0.01
Total systematic	0.30	0.41	0.39
Statistical	0.14	0.25	0.14
Total	0.33	0.48	0.42

- Measured and predicted $\sigma_{t\bar{t}}$ have different dependence on m_t
- Extract m_t in well-defined mass scheme from intersection



Δm_t^{pole} (GeV)	$\sqrt{s} = 7$ TeV	$\sqrt{s} = 8$ TeV
Data statistics	0.6	0.3
Analysis systematics	0.8	0.9
Integrated luminosity	0.7	1.2
LHC beam energy	0.7	0.6
PDF+ α_s	1.8	1.7
QCD scale choice	+0.9 -1.2	+0.9 -1.3

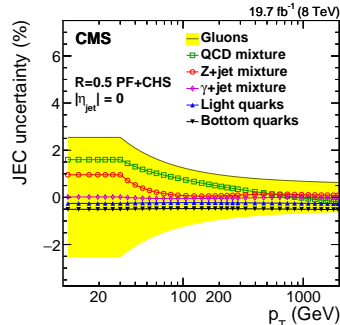
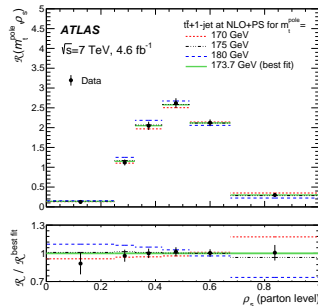


- Largest uncertainties from PDF+ α_s and QCD scale (NNLO+NNLL)
 - No breakdown given but $\alpha_s \pm 0.001$ may account for ± 1.5 GeV in m_t
- Most precise result: ATLAS+CMS Run 1 combination: $m_t = 173.4_{-2.0}^{+1.8}$ GeV (NNPDF3.1)
- CMS 13 TeV: 3 GeV downward shift with ABMP16 which uses a lower value of α_s
 - pole mass results envelope the direct measurements

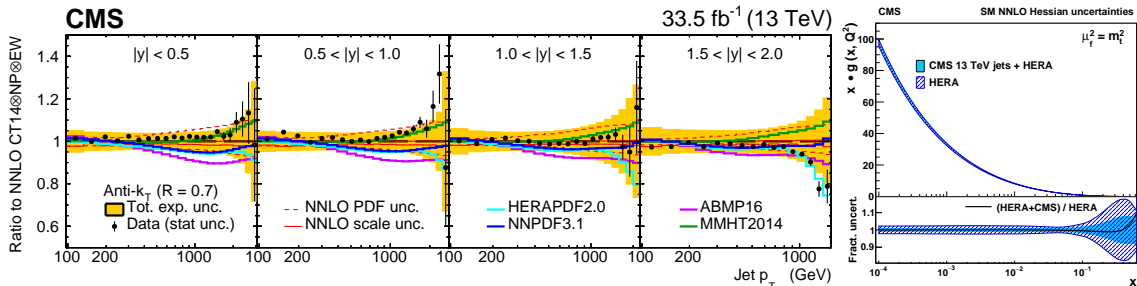
Pole mass from $t\bar{t}$ + jet

- Using mass-sensitive observable $\rho = 2m_0/m(t\bar{t} + \text{jet})$
- ATLAS measurement at 7 TeV
 - $m_t = 173.7 \pm 1.5$ (stat) ± 1.4 (syst) $_{-0.5}^{+1.0}$ (theory)
 - Large QCD scale uncertainty from NLO $t\bar{t}$ + jet ($_{-0.44}^{+0.93}$ GeV), using fixed scale $\mu = m_t$
- CMS measurement at 13 TeV
 - Dynamic QCD scale choice $H_T^B/2 \rightarrow_{-0.43}^{+0.51}$ GeV
 - Largest uncertainty from gluon jet response CMS JME-13-004
 - $m_t = 172.93 \pm 1.36$ GeV (ABM16),
 $m_t = 172.13 \pm 1.43$ GeV (CT18) \leftarrow 0.8 GeV difference

→ wishlist: NNLO calculation, resolve PDF discrepancy, resolve light-quark vs gluon jet response (Pythia vs Herwig)

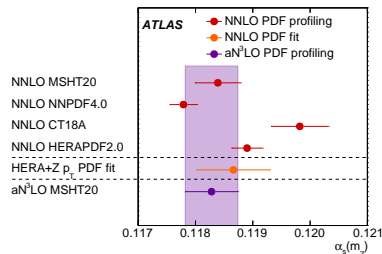
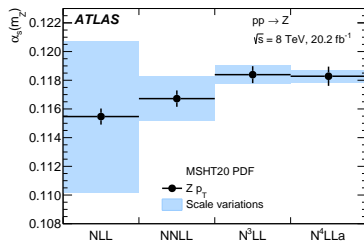
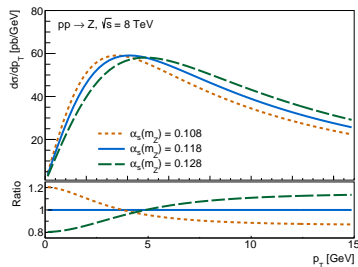


- 7 TeV: $\alpha_s = 0.1185 \pm 0.0028$ (CT10) $_{-0.0024}^{+0.0053}$ (NLO scale) ± 0.0019 (exp+NP)
- 8 TeV: $\alpha_s = 0.1164_{-0.0029}^{+0.0025}$ (CT10) $_{-0.0028}^{+0.0053}$ (NLO scale) $_{-0.0015}^{+0.0014}$ (exp+NP)
 - HERA+CMS result: $\alpha_s = 0.1185_{-0.0016}^{+0.0002}$ (model+param) $_{-0.0018}^{+0.0022}$ (NLO scale) $_{-0.0021}^{+0.0019}$ (exp)
 - Smaller QCD scale uncertainties due to consistent treatment in PDF and theory prediction



- 13 TeV: main result now HERA+CMS full QCD fit at NNLO
 - $\alpha_s = 0.1170 \pm 0.0007$ (model+param) ± 0.0008 (NNLO scale) ± 0.0014 (exp)
 - Jet energy response to gluons starts to become an important factor
 - new parton showers, or clever idea for calibration?

- Measurement of Z p_T and rapidity in full phase space (without lepton cuts)
- Fitted using N³LO+aN⁴LL prediction, profiling MSHT20 PDFs $\rightarrow \alpha_s = 0.1183 \pm 0.0009$
 - Experimental ± 0.44 , PDF ± 0.51 , scale variation $\pm 0.42 \times 10^{-3}$



- **Cross-check fits** at N³LO+N³LL, profiling NNLO PDFs
 - MSHT20 in agreement with NNPDF4.0 and HERAPDF2.0 within PDF uncertainties
 - Value extracted with CT18A significantly higher (0.1198)
- **HERA+ATLAS fit** $\rightarrow \alpha_s = 0.1187 \pm 0.0010$ with ± 0.0006 from PDF

Summary: W mass and weak mixing angle

- LHC is a precision machine!
- W boson mass: uncertainties balanced between experimental and modeling

LEP combination
Phys. Rep. 532 (2013) 119

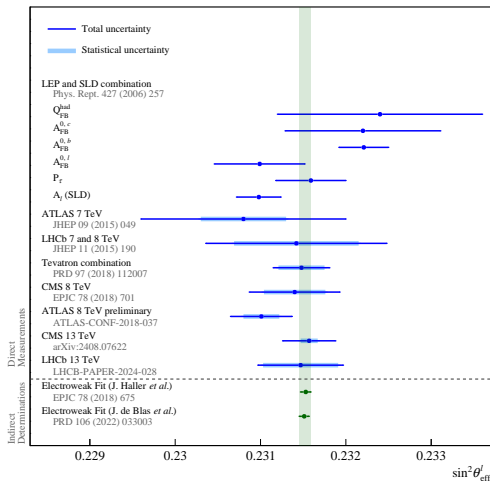
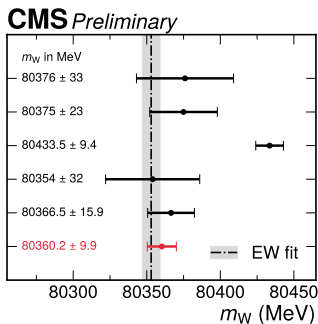
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Science 376 (2022) 6589

LHCb
JHEP 01 (2022) 036

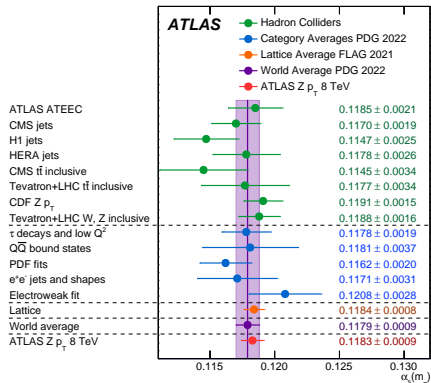
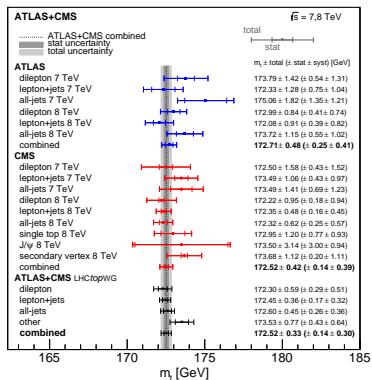
ATLAS
arxiv:2403.15085, subm. to EPJ C

CMS
This Work



- Weak mixing angle: precision limited by PDFs, good prospects for LHCb with more data

Summary: top quark mass and strong coupling



- **Direct m_t** : limited by modeling of top quark decay and scheme uncertainty
- **m_t from cross section**: large uncertainties from PDF, α_s , and QCD scale (NNLO+NNLL)
- **α_s** : dominated by theory and modeling, genuine detector effects becoming smaller

⇒ further improve precision by collaboration between theory and LHC experiments!