

Extended Higgs sectors and their corresponding trilinear scalar couplings

Based mainly on

arXiv:1903.05417 (PLB), 1911.11507 (EPJC), arXiv:2202.03453 (Phys. Rev. Lett.),
arXiv:2305.03015 (EPJC) and ongoing works

in collaboration with Henning Bahl, Martin Gabelmann, Kateryna Radchenko Serdula, Alain Verduras Schaeidt and Georg Weiglein

Johannes Braathen (DESY)

QCD @ LHC 2024,

Universität Freiburg, Germany | 7 October 2024

HELMHOLTZ RESEARCH FOR
GRAND CHALLENGES

DESY.

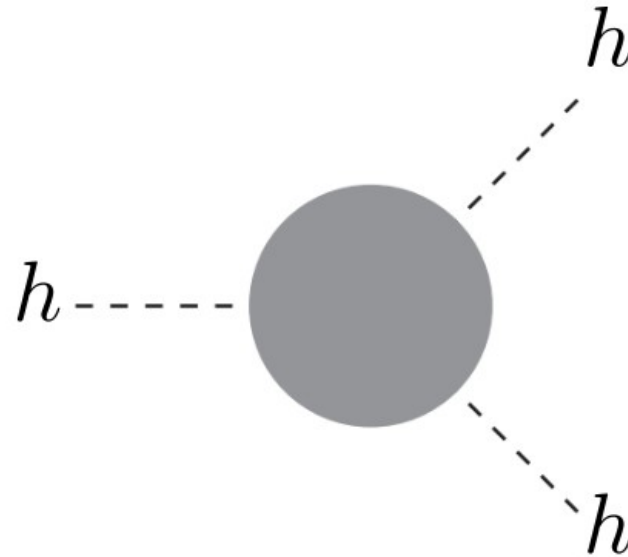
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QUANTUM UNIVERSE



Outline of the talk

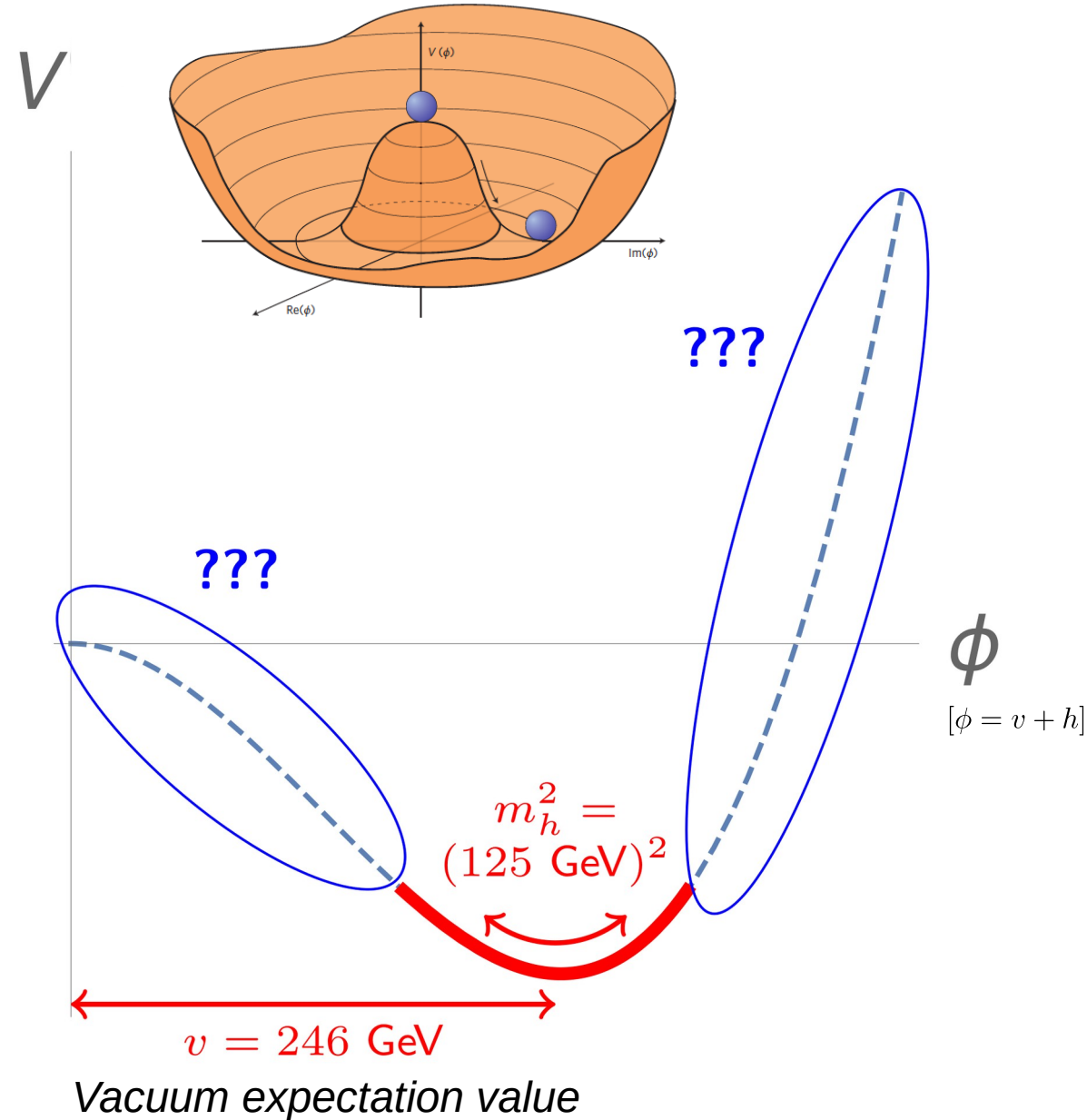
- Introduction: Why study the trilinear Higgs coupling λ_{hhh} and how to access it experimentally
- Calculating λ_{hhh} in BSM models
- How large can λ_{hhh} become for realistic scenarios
- Consequences for di-Higgs production at LHC

Why investigate λ_{hhh} ?



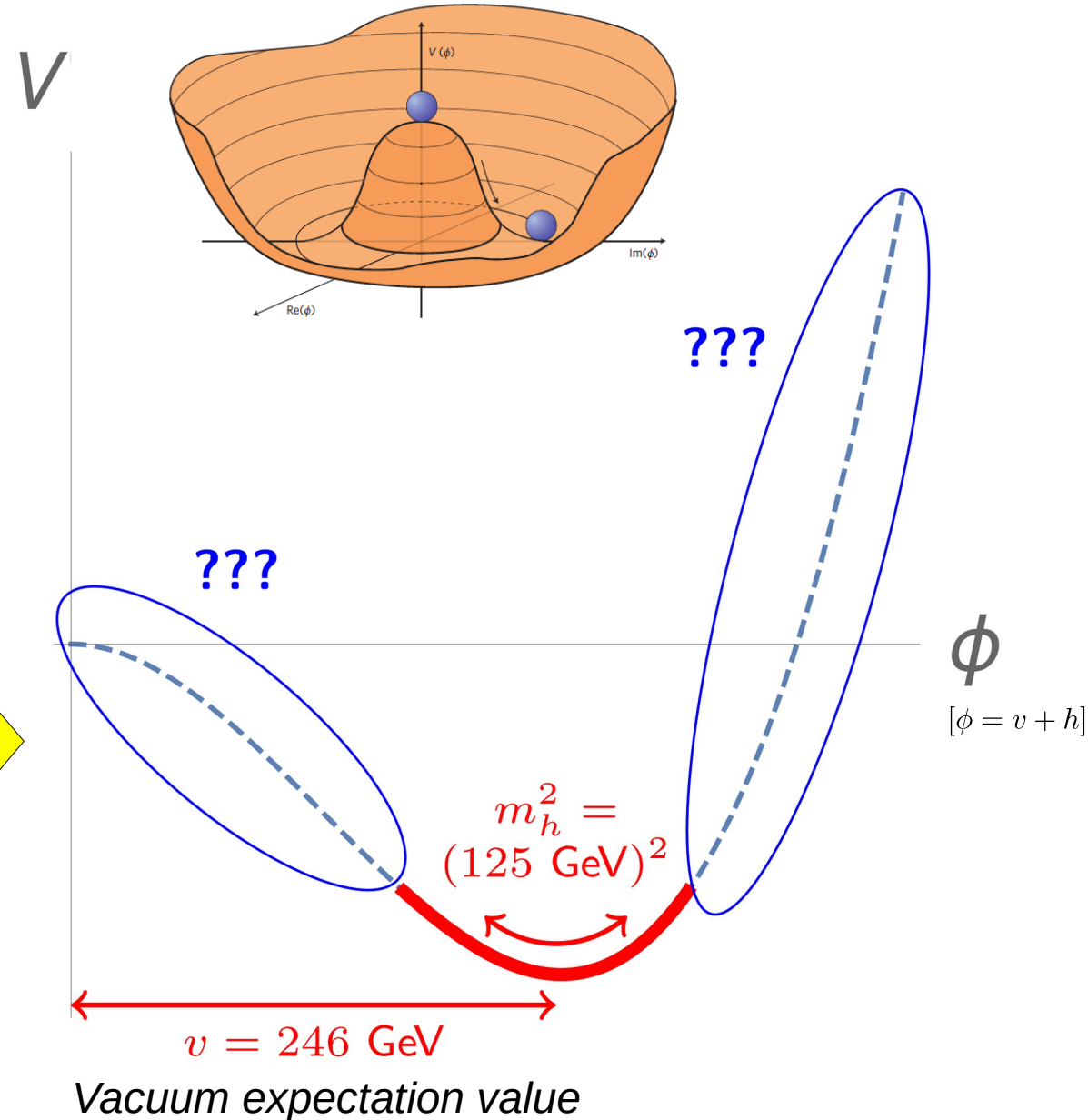
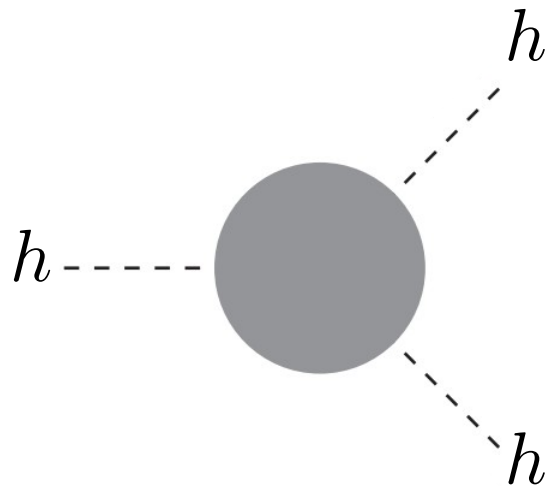
Form of the Higgs potential and trilinear Higgs coupling

- Brout-Englert-Higgs mechanism = **origin of masses of elementary particles** ...
... but very little known about the **Higgs potential** causing the **electroweak phase transition (EWPT)**



Form of the Higgs potential and trilinear Higgs coupling

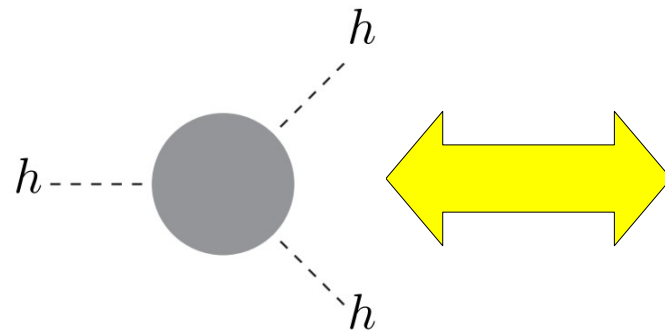
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- Shape of the potential determined by **trilinear Higgs coupling λ_{hhh}**



Form of the Higgs potential and trilinear Higgs coupling

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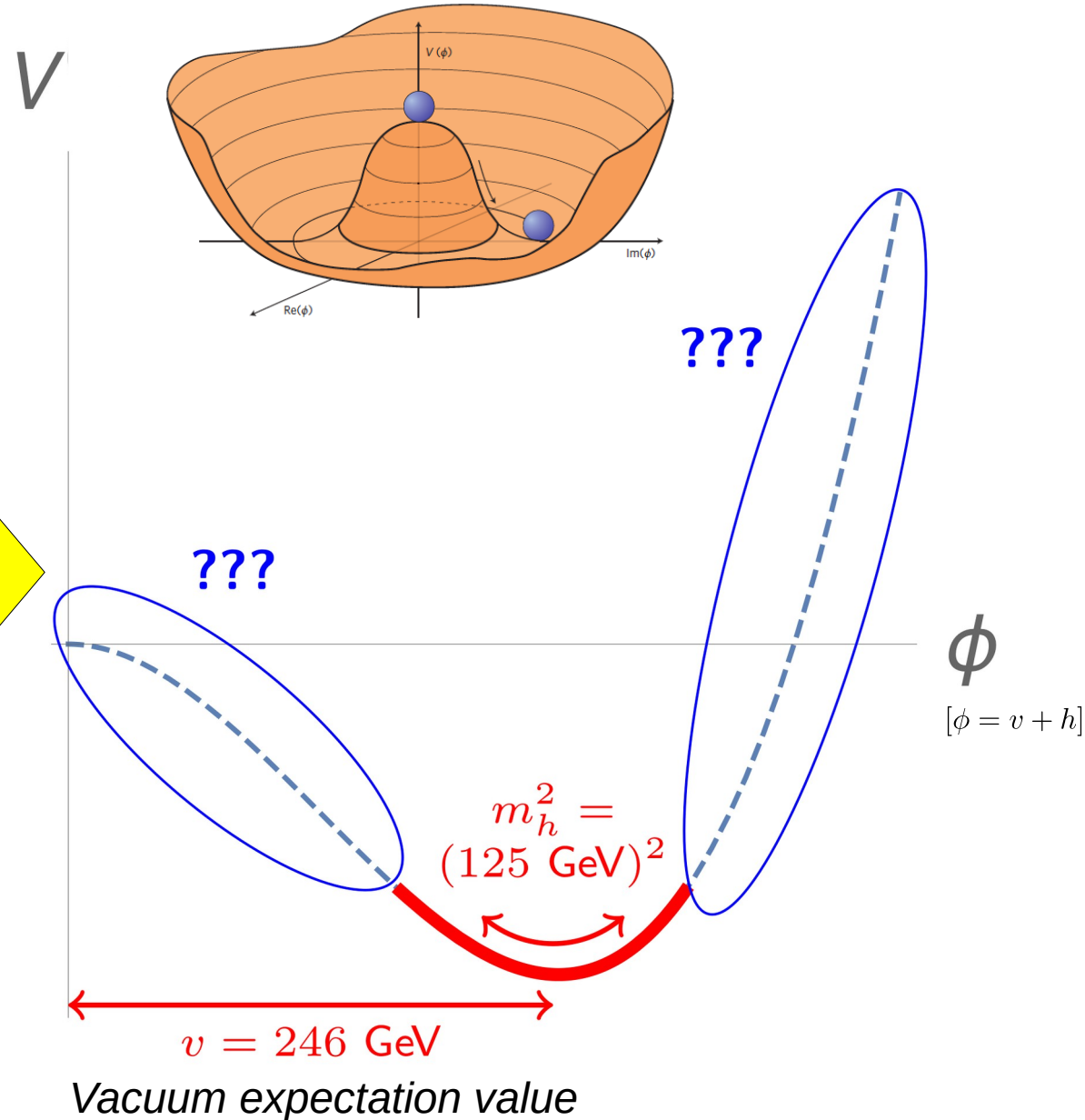


In the SM:
$$V_{SM}^{(0)} = \frac{1}{2} m_h^2 h^2 + \frac{1}{3!} \underbrace{\left(\frac{3m_h^2}{v} \right)}_{\equiv (\lambda_{hhh}^{(0)})^{SM}} h^3 + \frac{1}{4!} \left(\frac{3m_h^2}{v^2} \right) h^4 + \dots$$

In general:

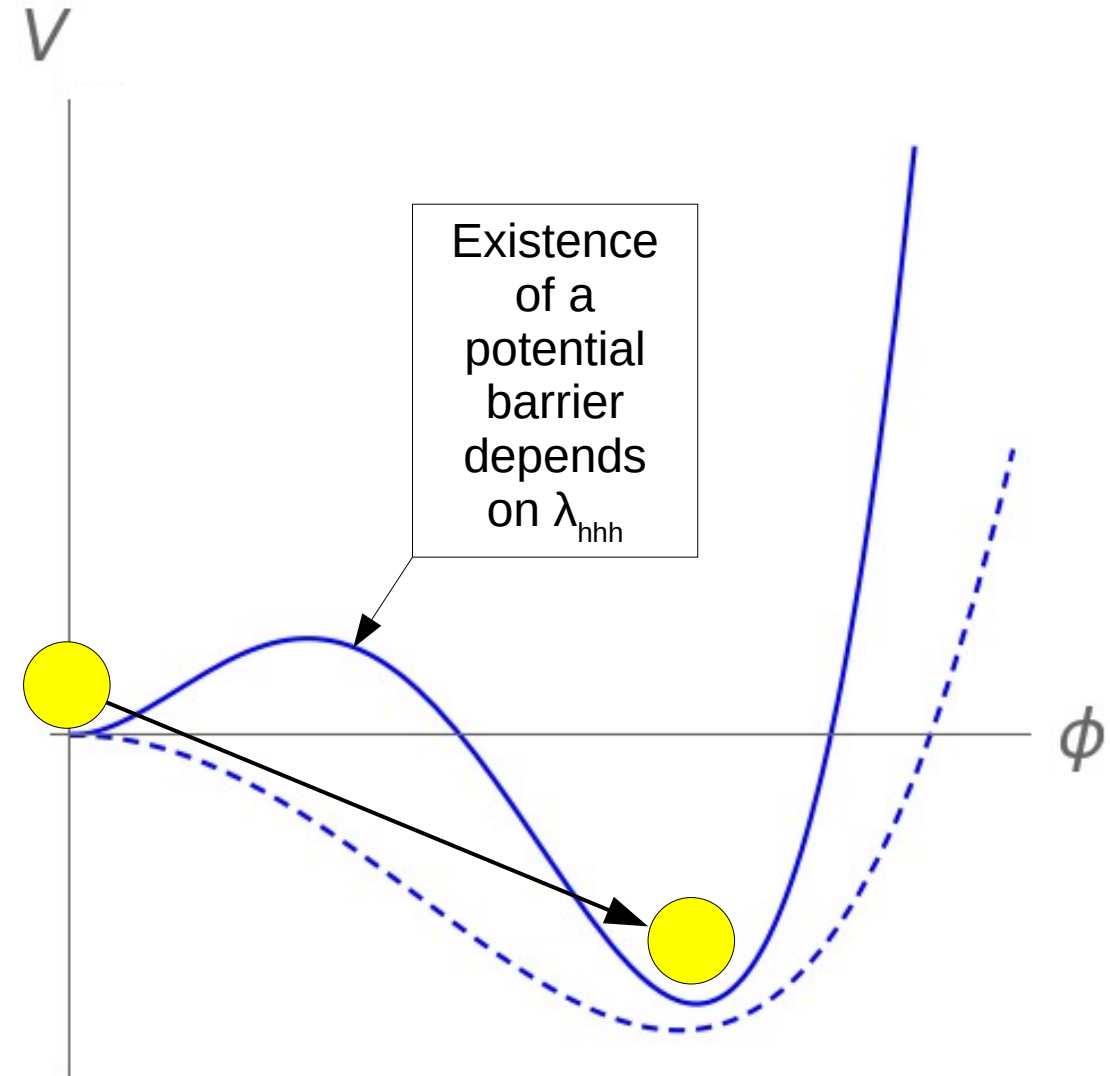
$$V^{(0)} = \frac{1}{2} m_h^2 h^2 + \frac{1}{3!} \overbrace{\kappa_\lambda \left(\frac{3m_h^2}{v} \right)}^{\equiv \lambda_{hhh}} h^3 + \frac{1}{4!} \kappa_{\lambda_4} \left(\frac{3m_h^2}{v^2} \right) h^4 + \dots$$

with $\kappa_\lambda \equiv \lambda_{hhh} / (\lambda_{hhh}^{(0)})^{SM}$



Form of the Higgs potential and baryon asymmetry

- Brout-Englert-Higgs mechanism = **origin of masses of elementary particles** ...
... but very little known about the **Higgs potential** causing the **electroweak phase transition (EWPT)**
- Shape of the potential determined by **trilinear Higgs coupling λ_{hhh}**
- Among **Sakharov conditions** necessary to explain **baryon asymmetry of the Universe via electroweak phase transition (= electroweak baryogenesis)**:
 - **Strong first-order EWPT**
 - barrier in Higgs potential
 - typically significant deviation in λ_{hhh} from SM



Aparté: Form of the Higgs potential – a more realistic picture

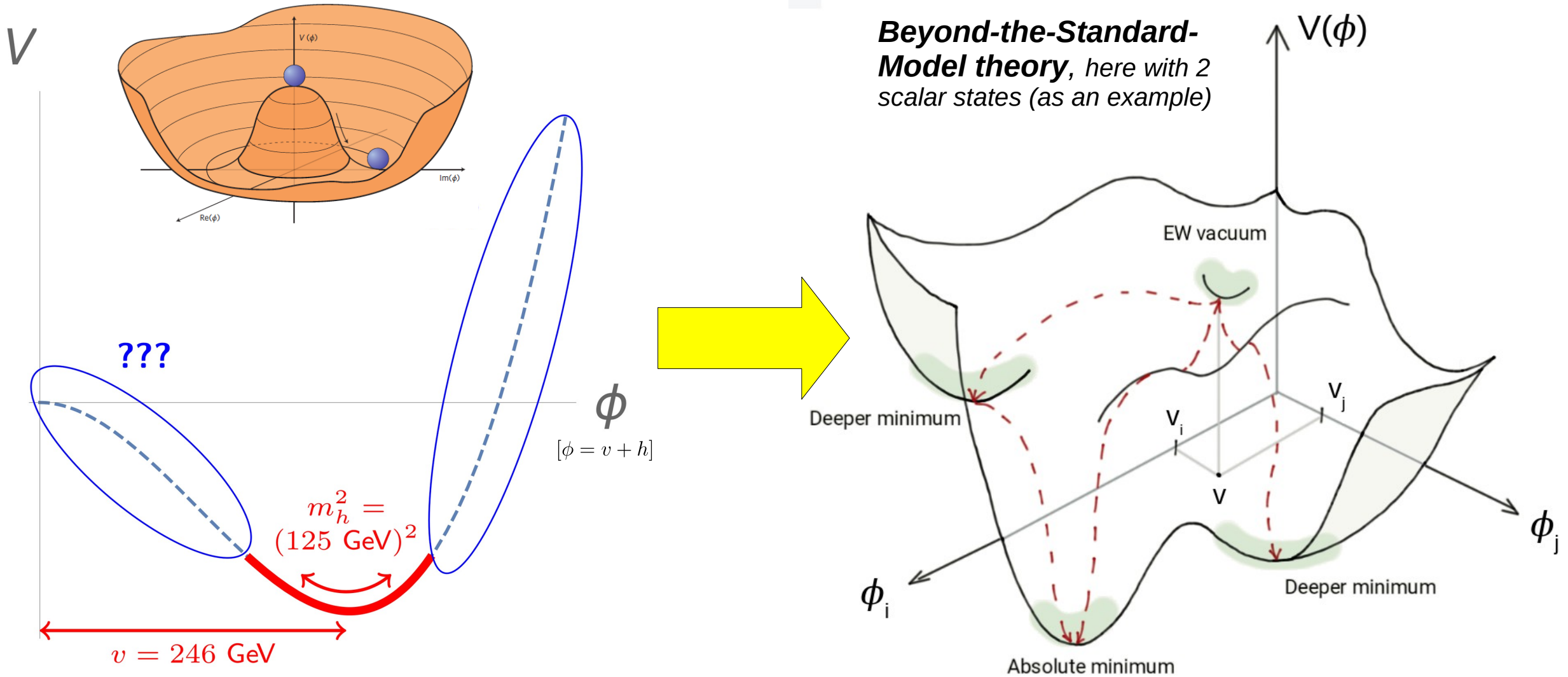
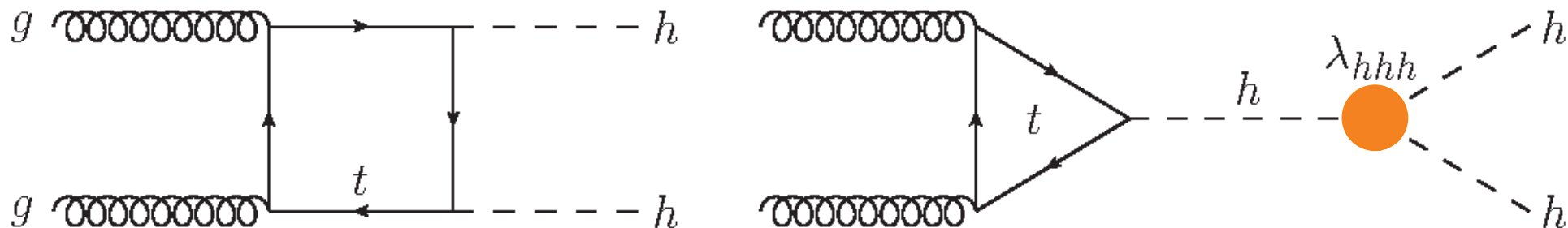


Figure by [K. Radchenko Serdula '24]

Accessing λ_{hhh} experimentally

Accessing λ_{hhh} via di-Higgs production

- Di-Higgs production $\rightarrow \lambda_{hhh}$ enters at leading order (LO) \rightarrow **most direct probe of λ_{hhh}**



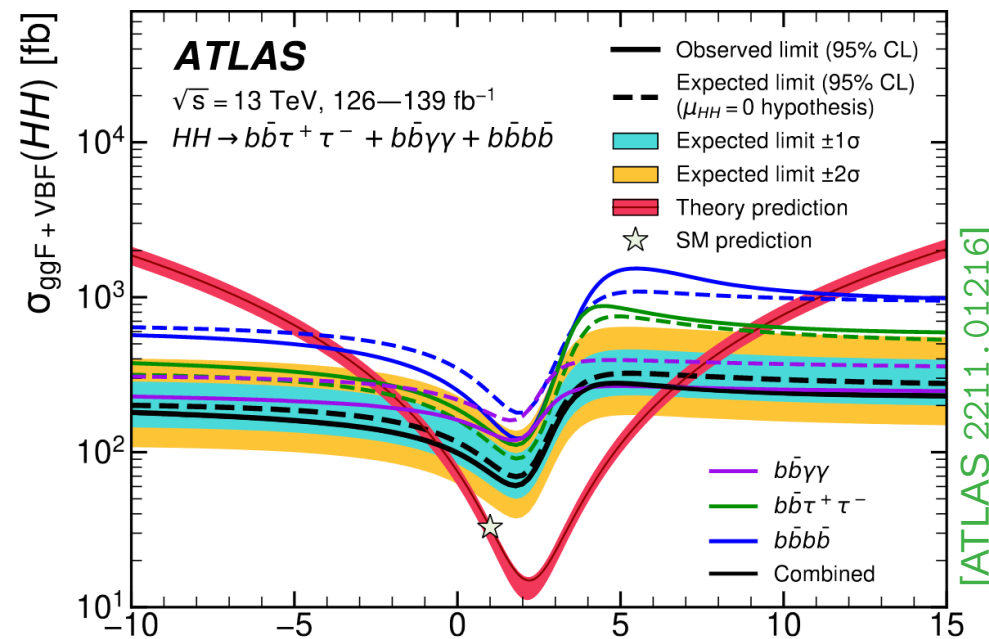
[Note: Single-Higgs production (EW precision observables) $\rightarrow \lambda_{hhh}$ enters at NLO (NNLO)]

- Box and triangle diagrams **interfere destructively**
 \rightarrow small di-Higgs cross-section σ_{hh} in SM

\rightarrow BSM deviation in λ_{hhh} can **significantly alter di-Higgs production!**

- Upper limit on di-Higgs cross-section
 \rightarrow **limits on $\kappa_\lambda \equiv \lambda_{hhh} / (\lambda_{hhh}^{(0)})^{SM}$**

- κ_λ as an *effective coupling*: $\mathcal{L} \supset -\kappa_\lambda \times \frac{3m_h^2}{v^2} \cdot h^3 + \dots$



[ATLAS 2211.01216]

Accessing λ_{hhh} via di-Higgs production

Di- Most recent and reliable results from ATLAS di-Higgs searches [ATLAS-CONF-2024-006] yield the limits:

$$-1.2 < \kappa_\lambda < 7.2 \text{ at 95\% C.L.}$$

(all other κ 's fixed to 1)

Also from [ATLAS PLB '23]:

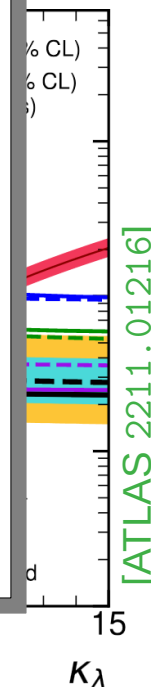
With all other κ 's fixed to 1: $-0.4 < \kappa_\lambda < 6.3$ (95% C.L.)

With κ_t floating: $-1.4 < \kappa_\lambda < 6.1$ (95% C.L.)

CMS: $-1.2 < \kappa_\lambda < 6.5$ at 95% C.L. [CMS '22]

NB: future determination even better (details in backup)

→ Can κ_λ now be used to constrain the parameter space of BSM models?



Calculating λ_{hhh} in models with extended scalar sectors

The Two-Higgs-Doublet Model

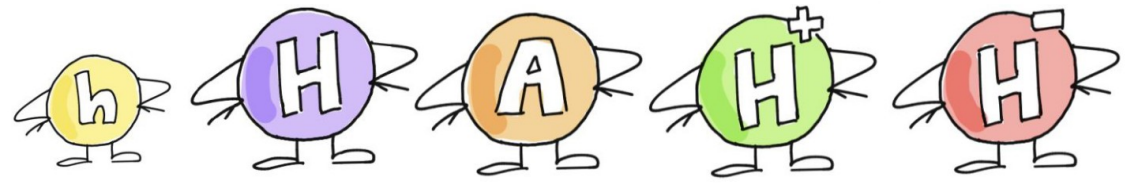


Figure by [K. Radchenko Serdula '24]

- 2 $SU(2)_L$ doublets $\Phi_{1,2}$ of hypercharge $1/2$
- CP-conserving 2HDM, with softly-broken Z_2 symmetry ($\Phi_1 \rightarrow \Phi_1, \Phi_2 \rightarrow -\Phi_2$) to avoid tree-level FCNCs

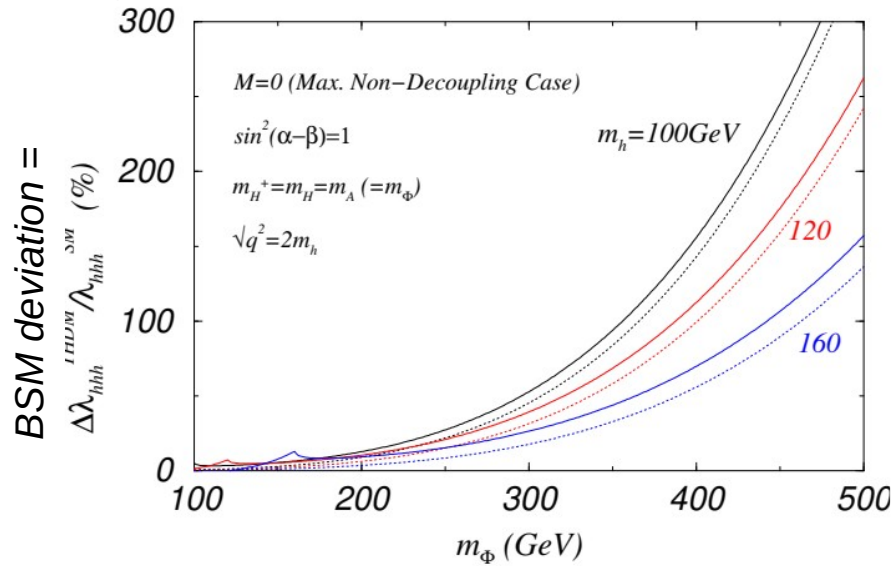
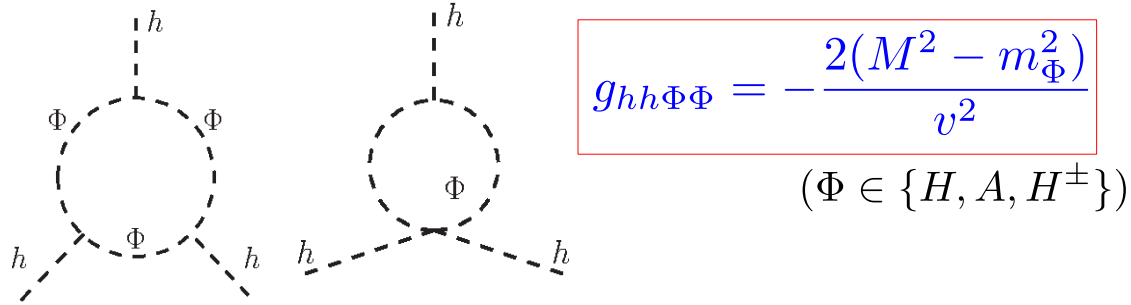
$$V_{2\text{HDM}}^{(0)} = m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2 - m_3^2 (\Phi_2^\dagger \Phi_1 + \Phi_1^\dagger \Phi_2) + \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_2^\dagger \Phi_1|^2 + \frac{\lambda_5}{2} \left((\Phi_2^\dagger \Phi_1)^2 + \text{h.c.} \right)$$

$$v_1^2 + v_2^2 = v^2 = (246 \text{ GeV})^2$$

- Mass eigenstates:**
 - h, H : CP-even Higgs bosons ($h \rightarrow 125\text{-GeV SM-like state}$); A : CP-odd Higgs boson;
 - H^\pm : charged Higgs boson
- BSM parameters:** 3 BSM masses m_H, m_A, m_{H^\pm} , BSM mass scale M (defined by $M^2 \equiv 2m_3^2/s_{2\beta}$), angles α (CP-even Higgs mixing angle) and β (defined by $\tan\beta = v_2/v_1$)
- BSM-scalar masses** take form $m_\Phi^2 = M^2 + \tilde{\lambda}_\Phi v^2$, $\Phi \in \{H, A, H^\pm\}$
- We take the **alignment limit** $\alpha = \beta - \pi/2 \rightarrow$ all Higgs couplings are SM-like at tree level \rightarrow compatible with current experimental data

Mass splitting effects in λ_{hhh}

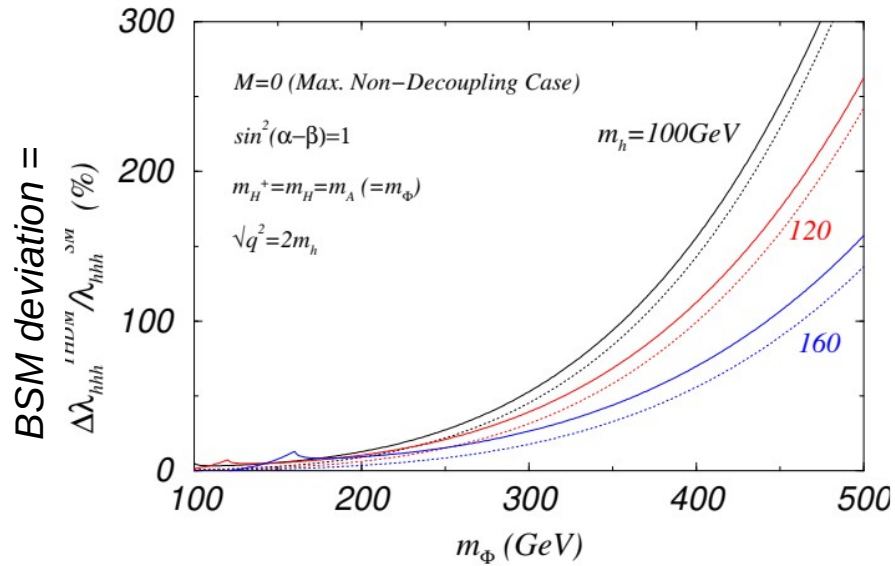
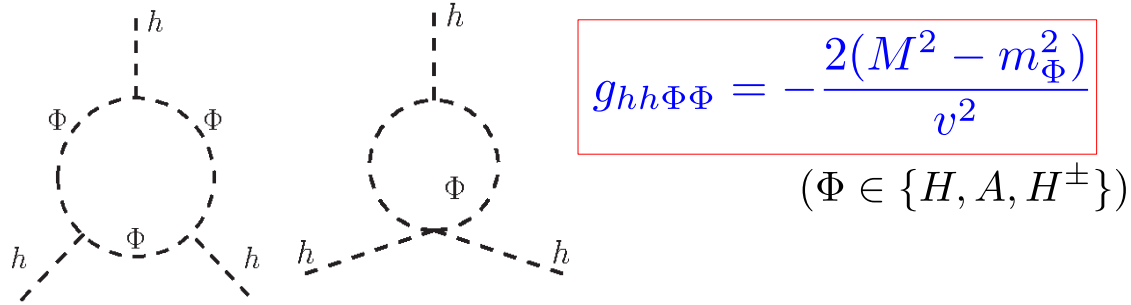
- First investigation of 1L BSM contributions to λ_{hhh} in 2HDM: [Kanemura, (Kiyoura), Okada, Senaha, Yuan '02, '04]



- Deviations of tens/hundreds of % from SM possible, for large $g_{h\Phi\Phi}$ or $g_{hh\Phi\Phi}$ couplings
- Mass splitting effects, now found in various models (2HDM, inert doublet model, singlet extensions, etc.)

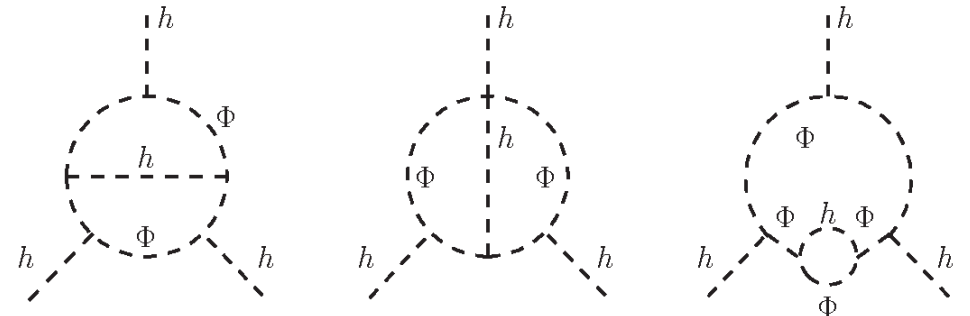
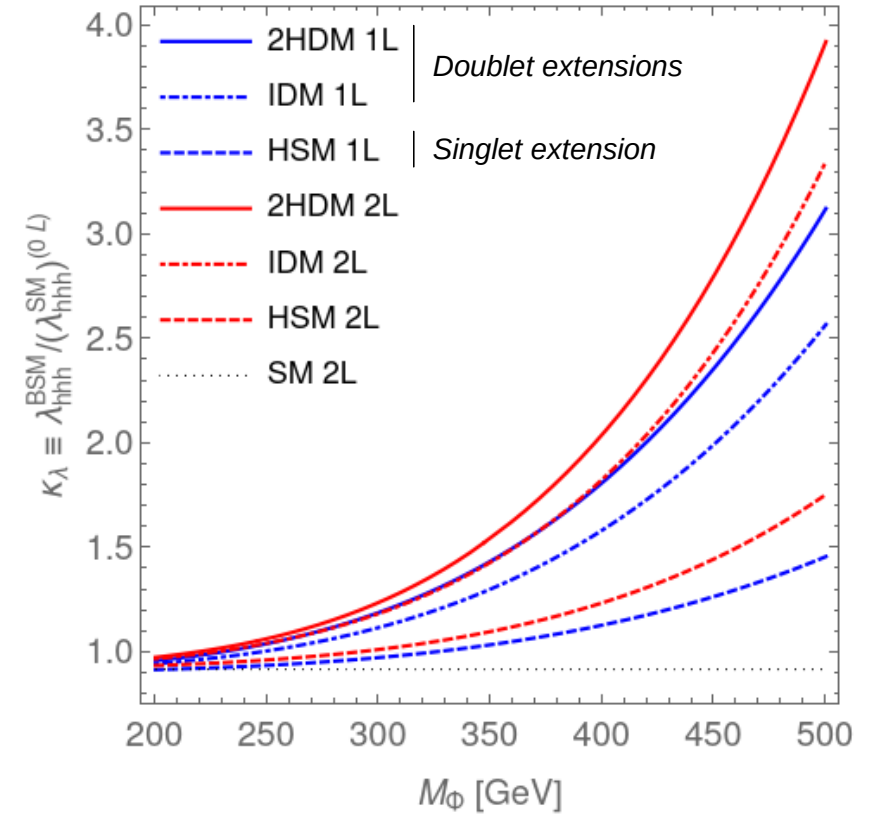
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- Mass splitting effects, now found in various models (2HDM, inert doublet model, singlet extensions, etc.)

- Large effects confirmed at 2L in [JB, Kanemura '19] → leading 2L corrections involving BSM scalars (H, A, H^\pm) and top quark, computed in effective potential approximation



Examples of scalar contributions to λ_{hhh} in aligned 2HDM

BSM scalars:
 $\Phi \in \{H, A, H^\pm\}$
 $m_\Phi^2 = M^2 + \tilde{\lambda}_\Phi v^2$

Coupling/Order	0L	1L	2L	3L
g_{hhhh}		<i>subleading</i> 	<i>subleading</i>	<i>subleading</i>
$g_{(h)h\Phi\Phi}$ $\left[g_{hh\Phi\Phi} = -\frac{2(M^2 - m_\Phi^2)}{v^2} \right]$	-			
$g_{(h)H\Phi\Phi'}$ [$g_{(h)G\Phi\Phi'}$ case similar]	-	-		
$g_{\Phi\Phi\Phi'\Phi'}$ [2 BSM scalars of species Φ , 2 of species Φ']	-	-		

[NB: 1 h can be replaced by a VEV]

→ no further type of coupling entering after 2L

→ for each class of diagrams, perturbative convergence can be checked!

Constraining BSM models with λ_{hhh}

- i. Can we apply the limits on κ_λ , extracted from experimental searches for di-Higgs production, for BSM models?*

- ii. Can large BSM deviations occur for points still allowed in light of theoretical and experimental constraints? If so, how large can they become?*

As a concrete example, we consider an aligned 2HDM

Based on

arXiv:2202.03453 (Phys. Rev. Lett.) in collaboration with Henning Bahl and Georg Weiglein

Can we apply di-Higgs results for the aligned 2HDM?

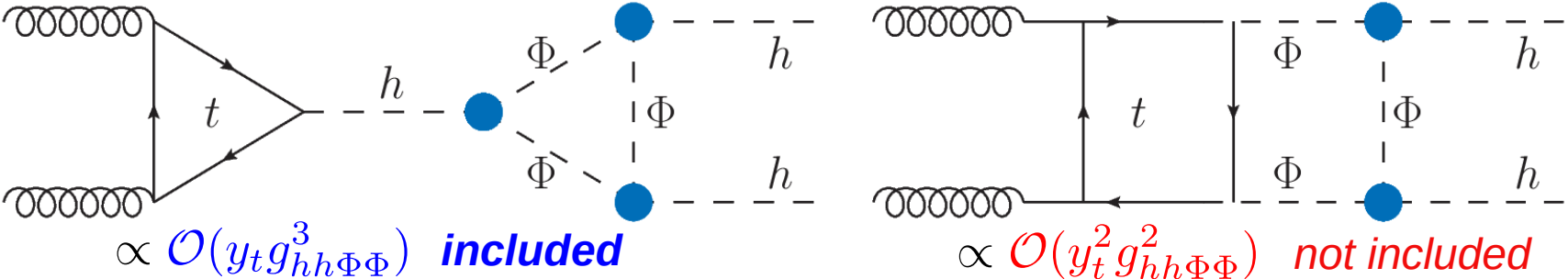
Current strongest limits on κ_λ from ATLAS di-Higgs searches

-1.2 < κ_λ < 7.2 [ATLAS-CONF-2024-006]

[where $\kappa_\lambda \equiv \lambda_{hhh} / (\lambda_{hhh}^{(0)})^{SM}$]

What are the assumptions for the ATLAS limits?

- All other Higgs couplings (to fermions, gauge bosons) are SM-like
 - this is **ensured by the alignment** ✓
- The modification of λ_{hhh} is the only source of deviation of the *non-resonant Higgs-pair production cross section* from the SM



→ We **correctly include all leading BSM effects to di-Higgs production, in powers of $g_{hh\Phi\Phi}$, up to NNLO!** ✓

We can apply the ATLAS limits to our setting!

A parameter scan in the aligned 2HDM

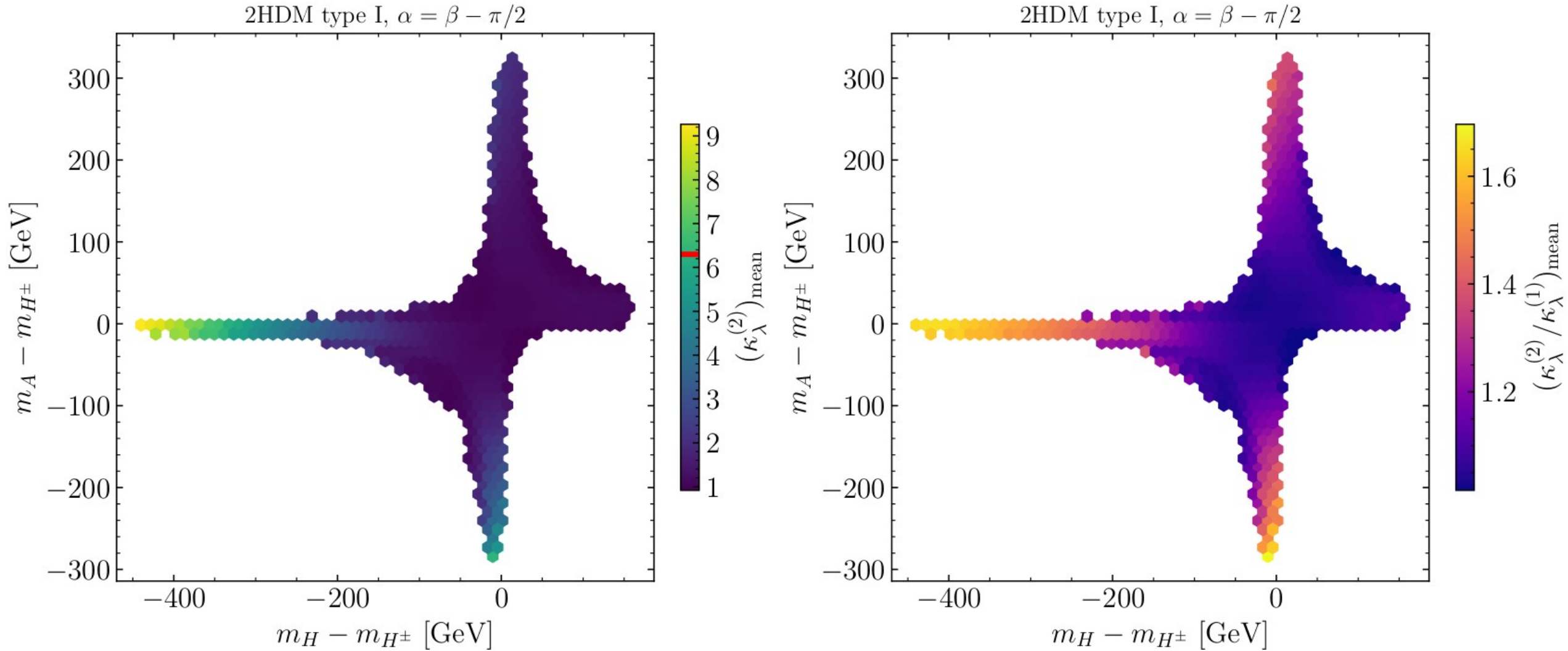
[Bahl, JB, Weiglein PRL '22]

- Our strategy:
 1. **Scan BSM parameter space**, keeping only points passing various theoretical and experimental constraints (*see below*)
 2. Identify regions with **large BSM deviations in λ_{hhh}**
 3. Devise a **benchmark scenario** allowing large deviations and investigate impact of experimental limit on λ_{hhh}
- *Here*: we consider an **aligned 2HDM of type-I**, but similar results expected for other 2HDM types, or other BSM models with extended Higgs sectors
- Constraints in our parameter scan:
 - experimental**
 - 125-GeV Higgs measurements with HiggsSignals
 - Direct searches for BSM scalars with HiggsBounds
 - b-physics constraints, using results from [Gfitter group 1803.01853]
 - EW precision observables, computed at two loops with THDM_EWPOS [Hessenberger, Hollik '16, '22]
 - theoretical**
 - Vacuum stability
 - Boundedness-from-below of the potential
 - NLO perturbative unitarity, using results from [Grinstein et al. 1512.04567], [Cacchio et al. 1609.01290]
- For points passing these constraints, we **compute κ_λ at 1L and 2L**, using results from [JB, Kanemura '19]

Parameter scan results

[Bahl, JB, Weiglein PRL '22]

Mean value for $\kappa_\lambda^{(2)} = (\lambda_{hhh}^{(2)})^{2\text{HDM}} / (\lambda_{hhh}^{(0)})^{\text{SM}}$ [left] and $\kappa_\lambda^{(2)} / \kappa_\lambda^{(1)} = (\lambda_{hhh}^{(2)})^{2\text{HDM}} / (\lambda_{hhh}^{(1)})^{2\text{HDM}}$ [right] in $(m_H - m_{H^\pm}, m_A - m_{H^\pm})$ plane



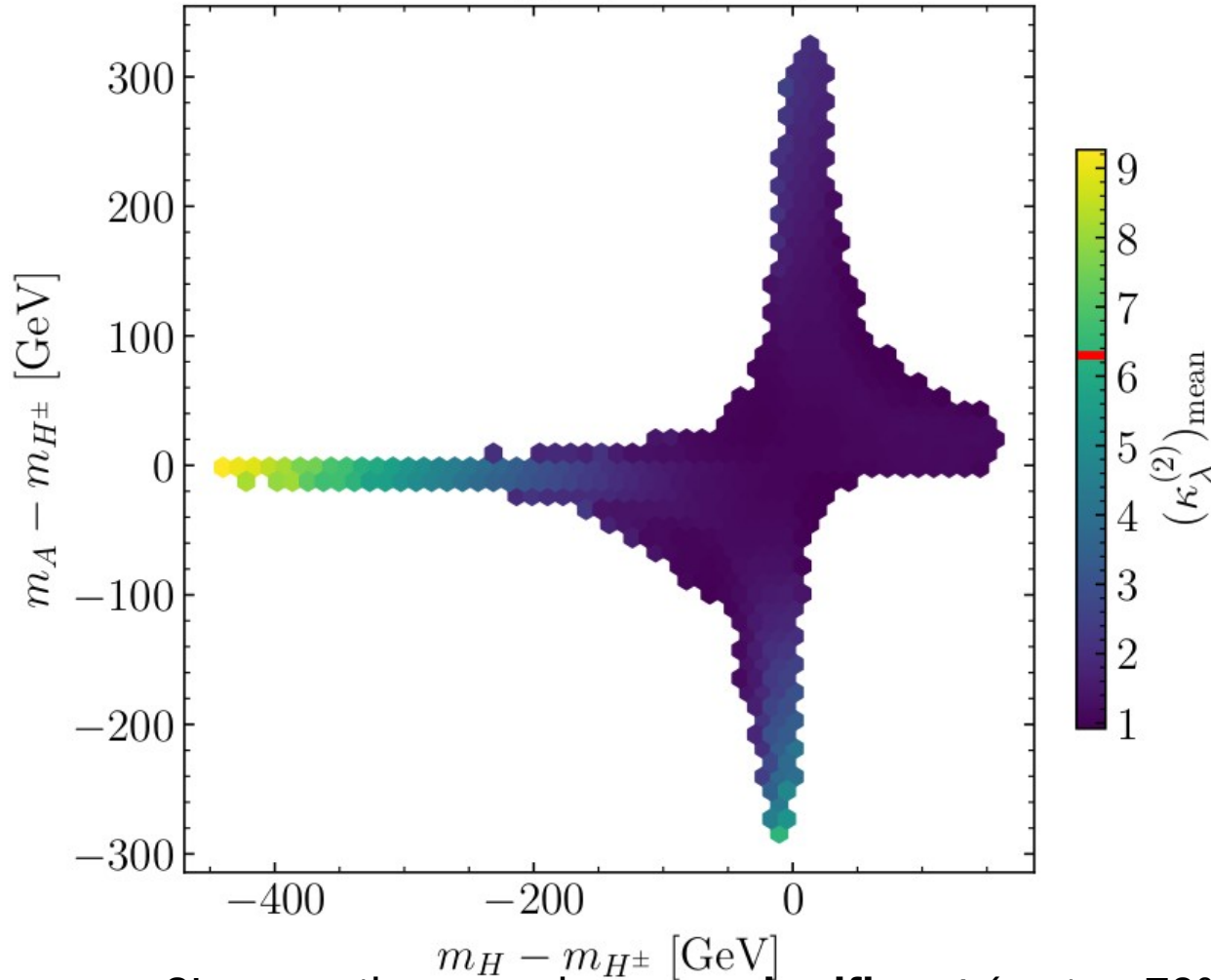
NB: all previously mentioned constraints are fulfilled by the points shown here

Parameter scan results

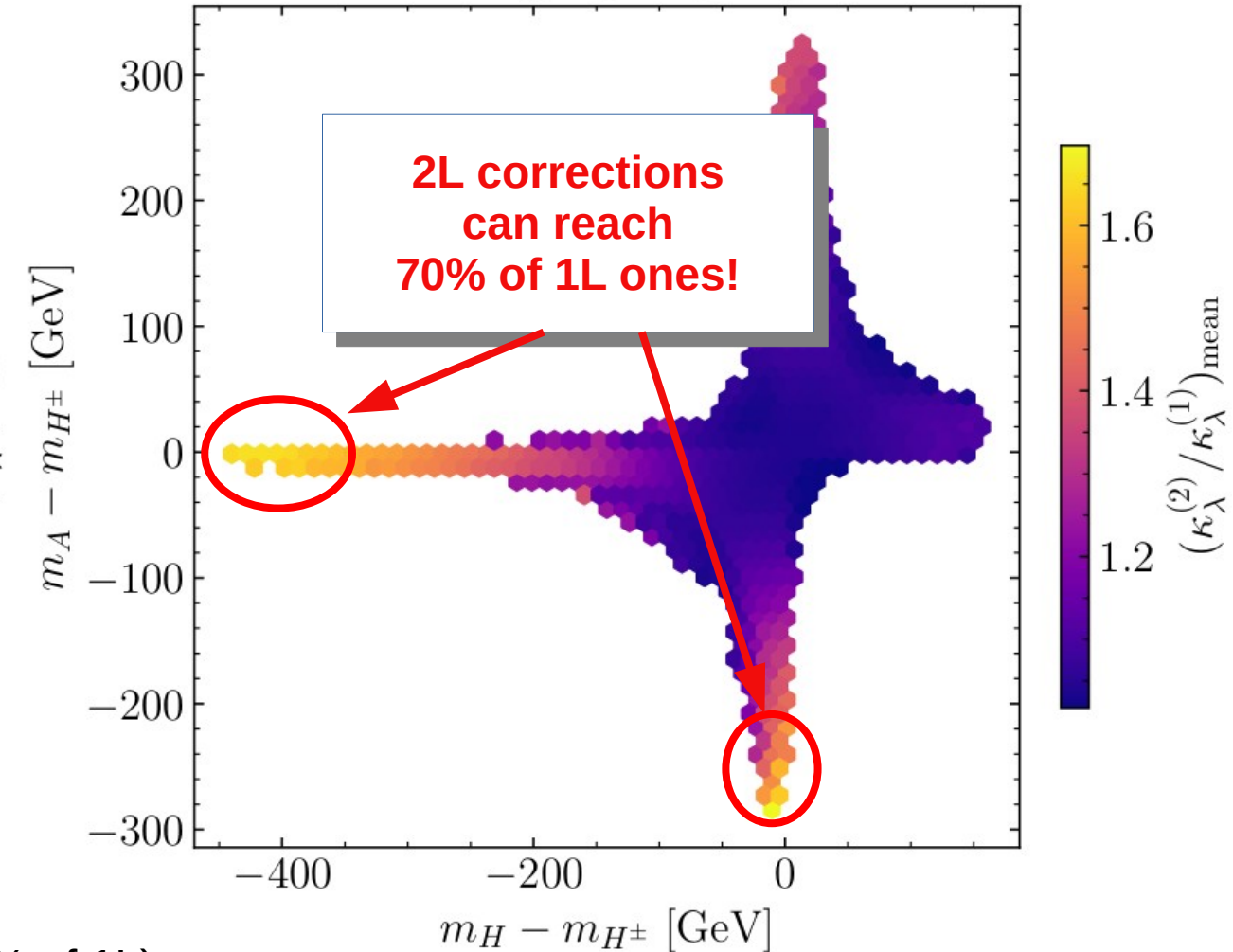
[Bahl, JB, Weiglein PRL '22]

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2HDM type I, $\alpha = \beta - \pi/2$



2HDM type I, $\alpha = \beta - \pi/2$



➤ 2L corrections can become **significant** (up to ~70% of 1L)

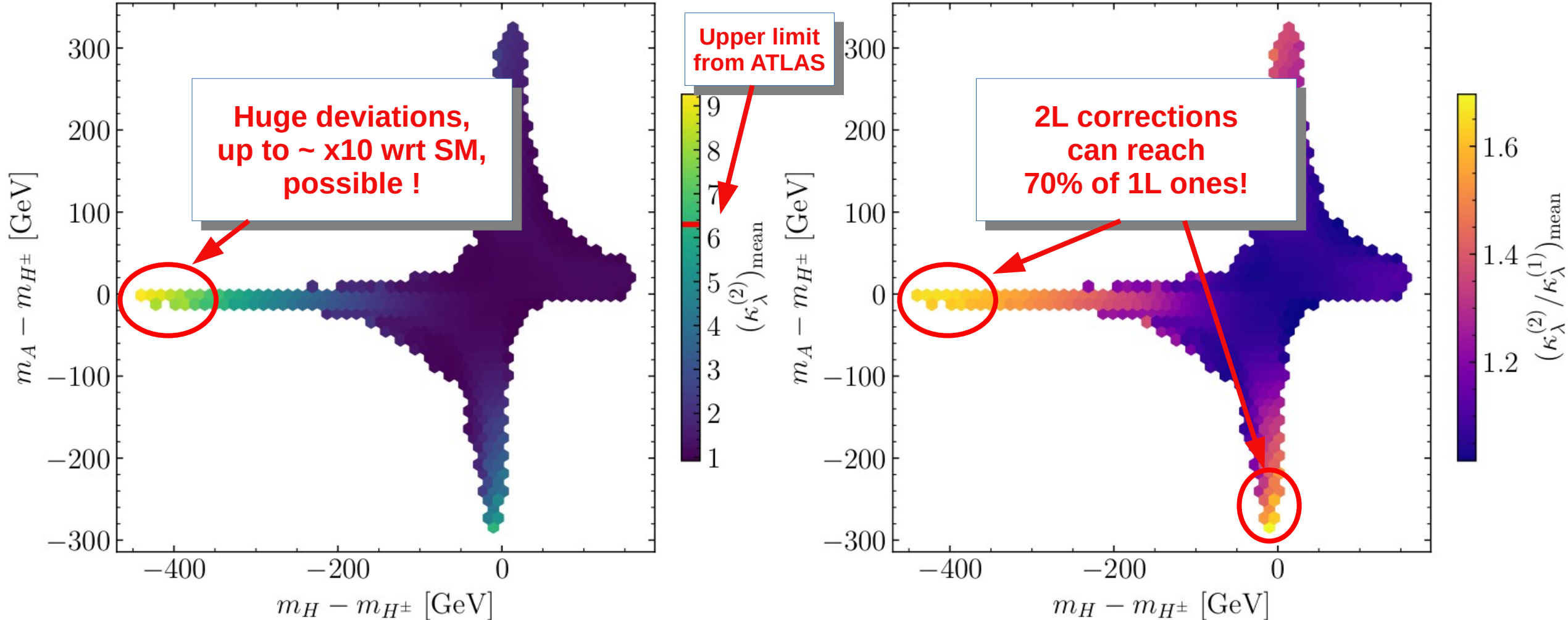
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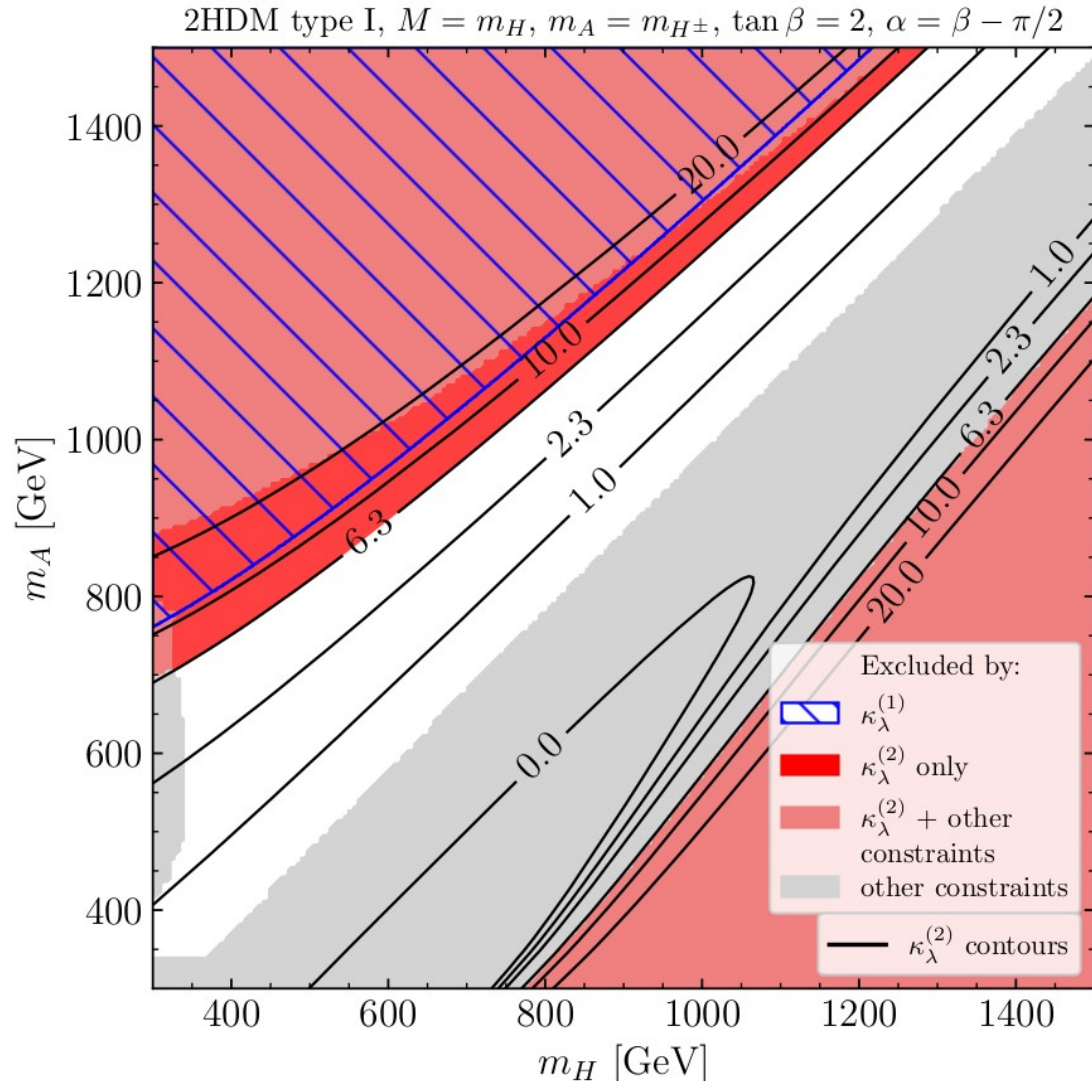
- 2L corrections can become **significant** (up to ~70% of 1L)
- **Huge enhancements** (by a factor ~10) of λ_{hhh} possible for $m_A \sim m_{H^\pm}$ and $m_H \sim M$

A benchmark scenario in the aligned 2HDM

[Bahl, JB, Weiglein PRL '22]

Results shown for aligned 2HDM of type-I, similar for other types (*available in backup*)

We take $m_A = m_{H^\pm}$, $M = m_H$, $\tan\beta = 2$



- **Grey area:** area excluded by other constraints, in particular BSM Higgs searches, boundedness-from-below (BFB), perturbative unitarity
- **Light red area:** area excluded both by other constraints (BFB, perturbative unitarity) and by $\kappa_\lambda^{(2)} > 6.3$ [in region where $\kappa_\lambda^{(2)} < -0.4$ the calculation isn't reliable]
- **Dark red area:** new area that is **excluded ONLY by $\kappa_\lambda^{(2)} > 6.3$** . Would otherwise not be excluded!
- **Blue hatches:** area excluded by $\kappa_\lambda^{(1)} > 6.3 \rightarrow$ impact of including 2L corrections is significant!

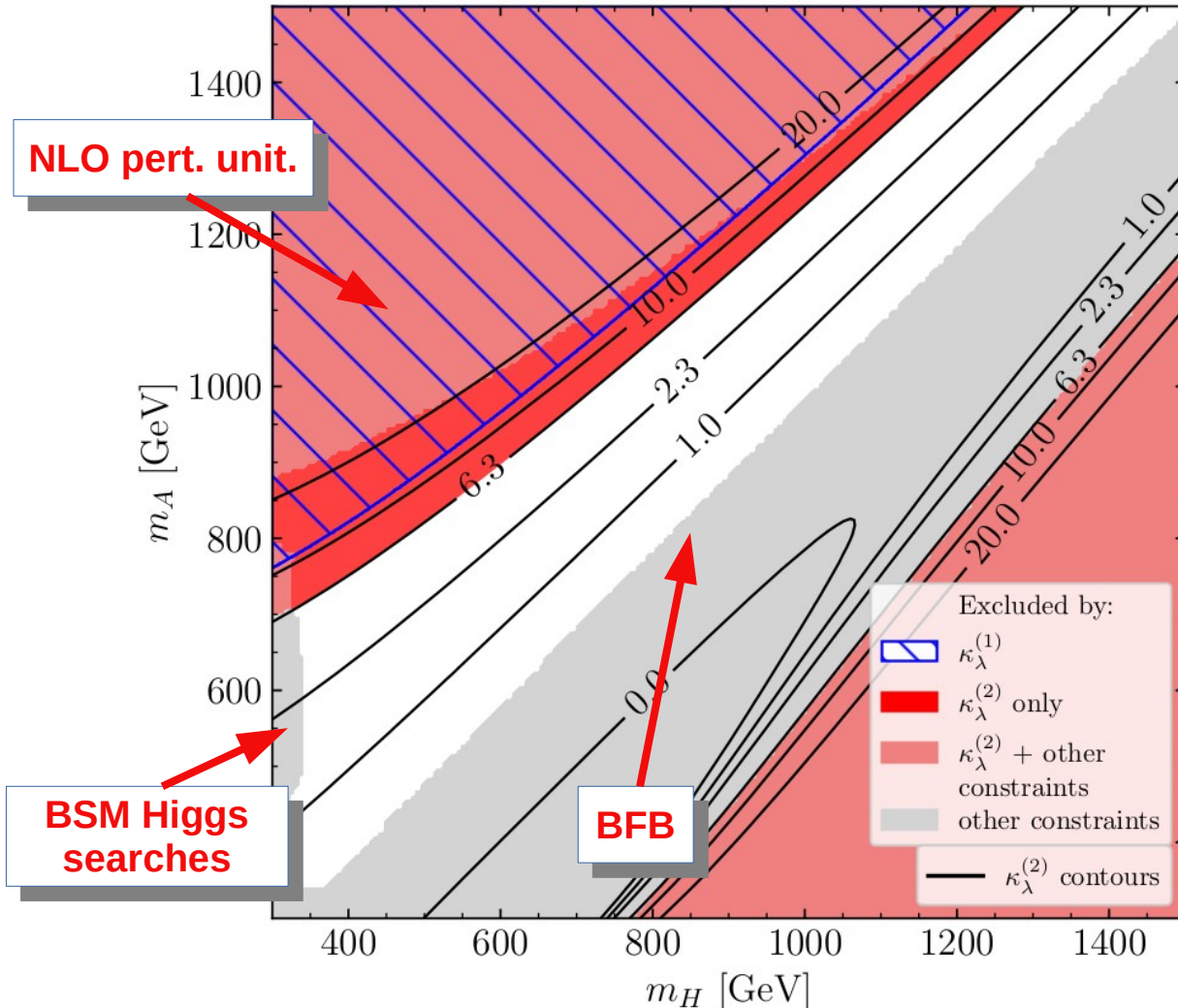
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2HDM type I, $M = m_H$, $m_A = m_{H^\pm}$, $\tan\beta = 2$, $\alpha = \beta - \pi/2$

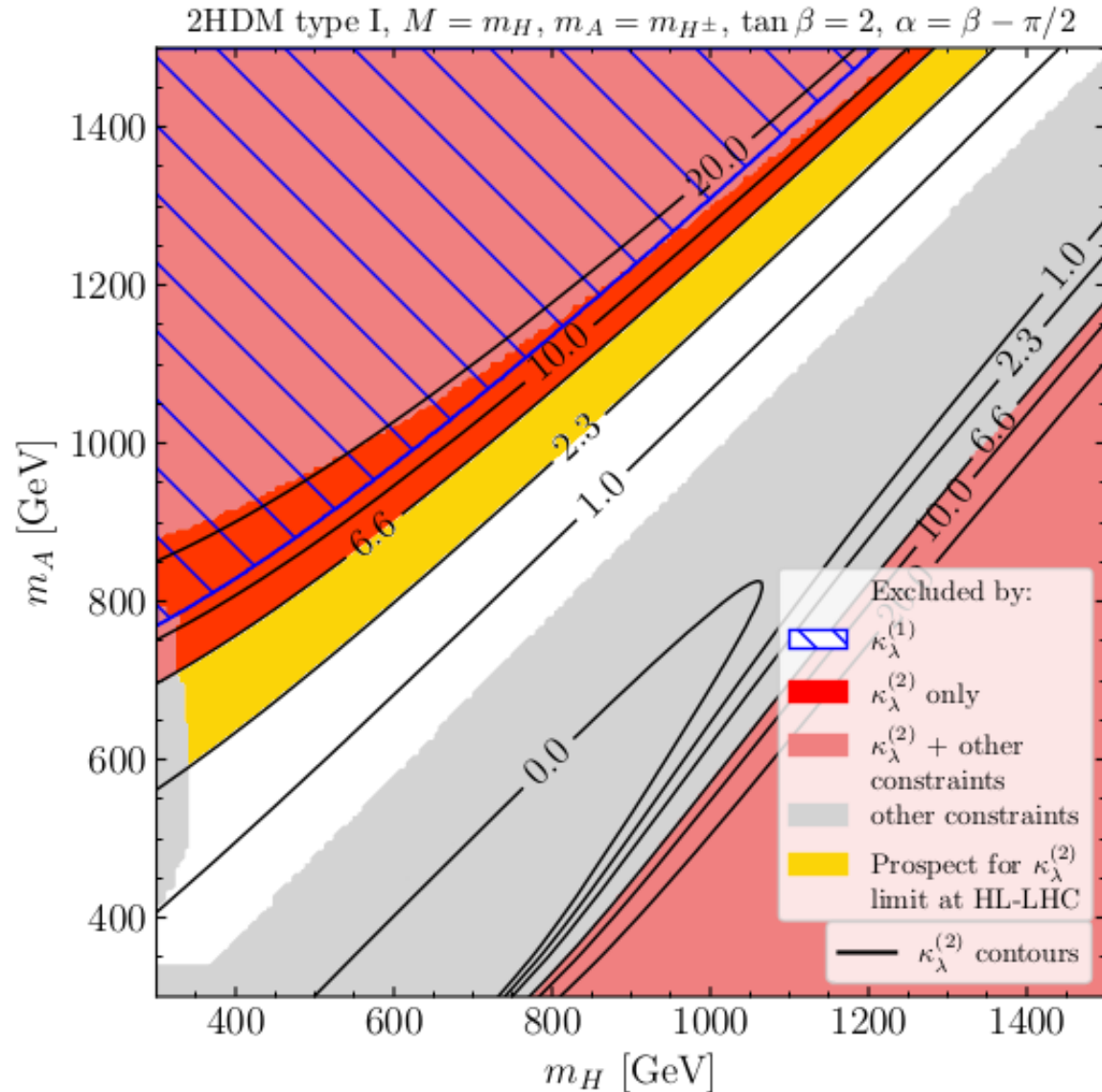


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A benchmark scenario in the aligned 2HDM – future prospects

Suppose for instance the upper bound on κ_λ becomes $\kappa_\lambda < 2.3$

[Bahl, JB, Weiglein '23]



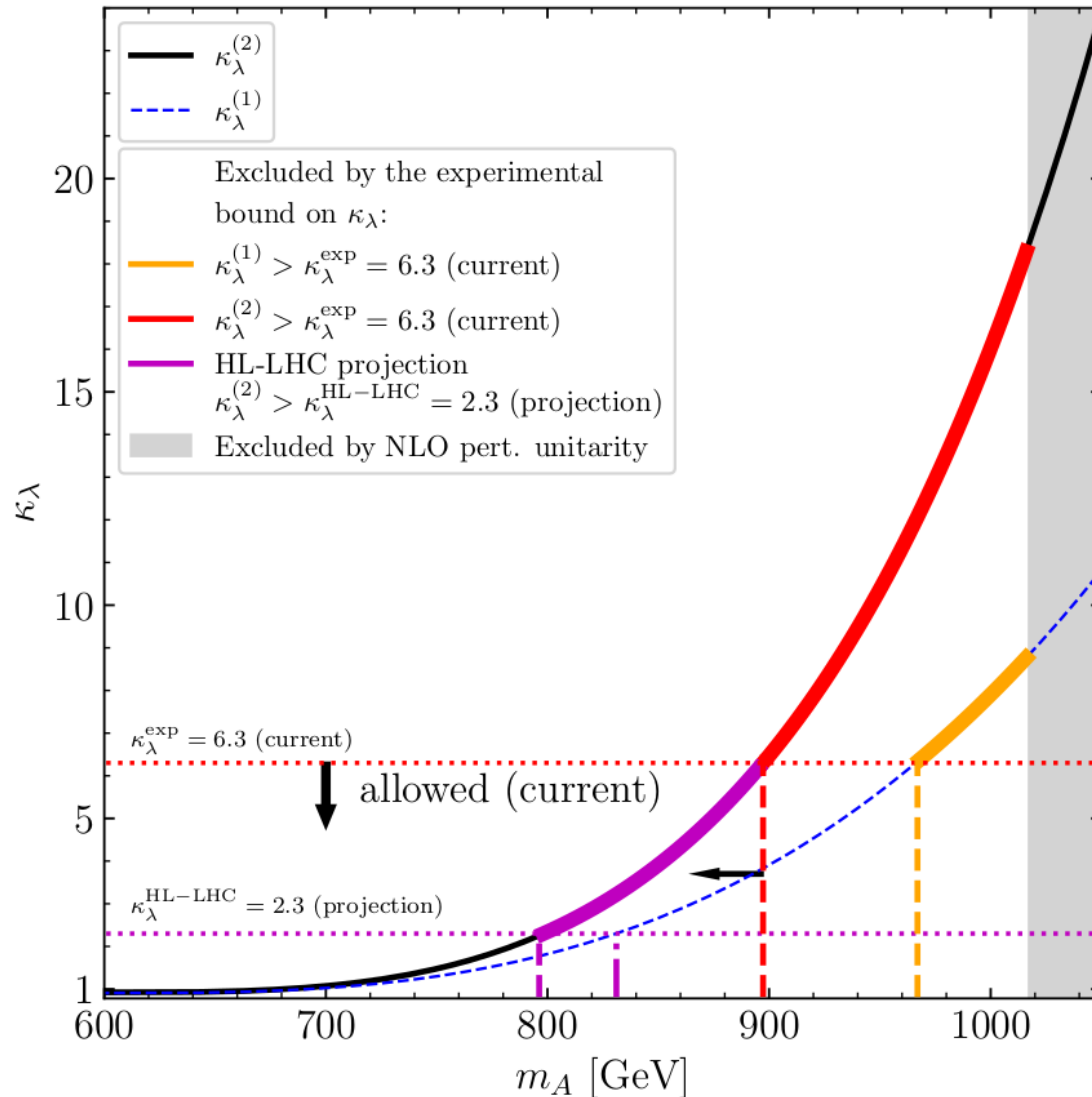
- **Golden area:** additional exclusion if the limit on κ_λ becomes $\kappa_\lambda^{(2)} < 2.3$ (achievable at HL-LHC)
- Of course, **prospects even better with an e⁺e⁻ collider!**
- Experimental constraints, such as Higgs physics, may also become more stringent, however **not** theoretical constraints (like BFB or perturbative unitarity)

A benchmark scenario in the aligned 2HDM – 1D scan

Within the previously shown plane, we fix $M=m_H=600$ GeV, and vary $m_A=m_{H^\pm}$

[Bahl, JB, Weiglein PRL '22]

2HDM type I, $\alpha = \beta - \pi/2$, $m_A = m_{H^\pm}$, $M = m_H = 600$ GeV, $\tan \beta = 2$



- Illustrates the significantly improved reach of the experimental limit when including **2L corrections** in calculation of κ_λ
- A stricter choice for the perturbative unitarity constraint (grey) does not significantly change the region excluded by $\kappa_\lambda^{(2)}$

Mass splitting effects for various BSM models with anyH3

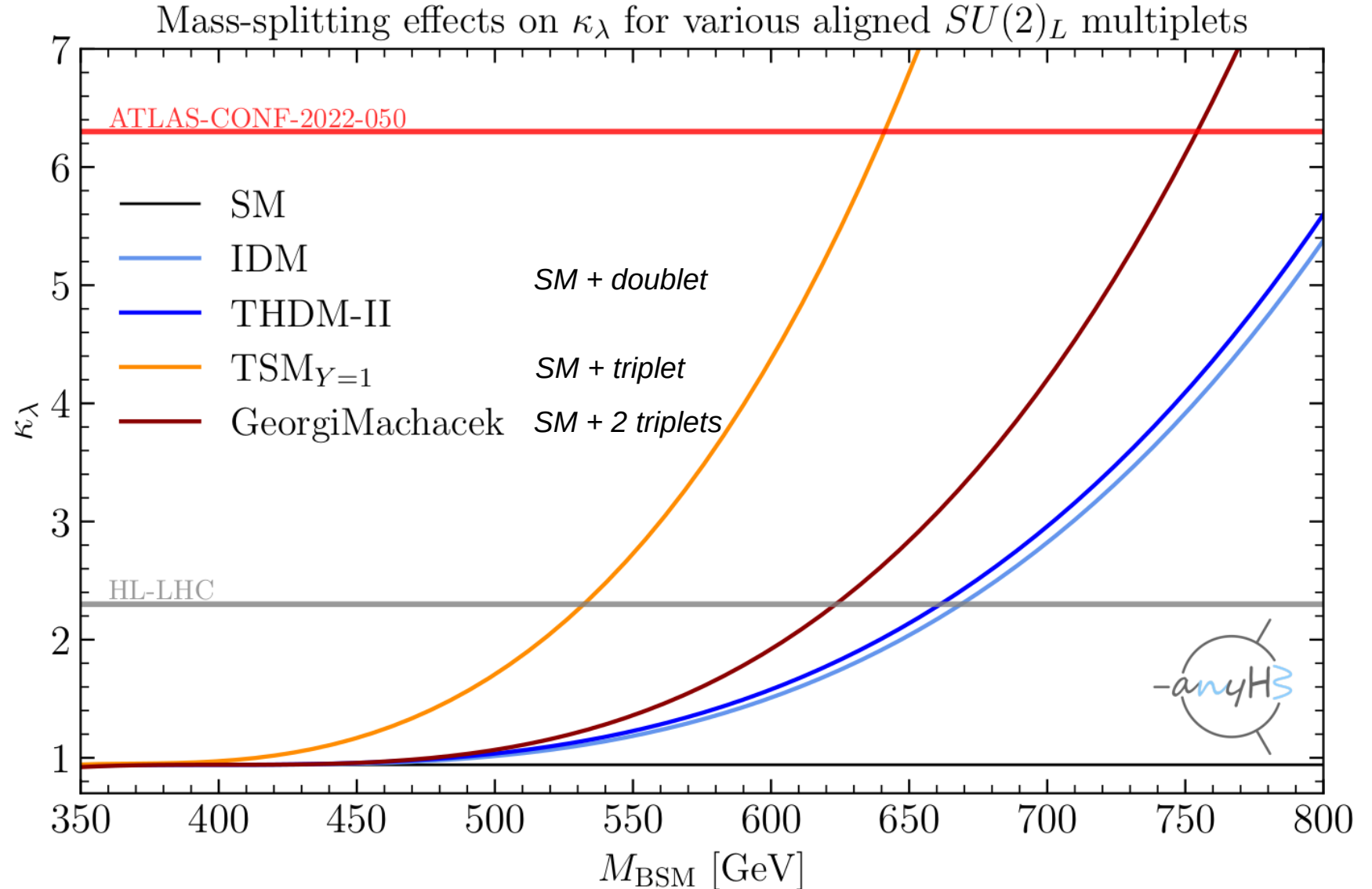
- anyH3 [Bahl, JB, Gabelmann, Weiglein '23]: public tool for full one-loop calculation of λ_{hhh} in arbitrary renormalisable models, using UFO inputs (*more details in backup*)

$$M_{\text{BSM}}^2 = \mathcal{M}^2 + \tilde{\lambda}v^2$$

- Increase M_{BSM} , keeping fixed \mathcal{M}
 - large mass splittings
 - **large BSM effects!**

- Perturbative unitarity checked within anyH3

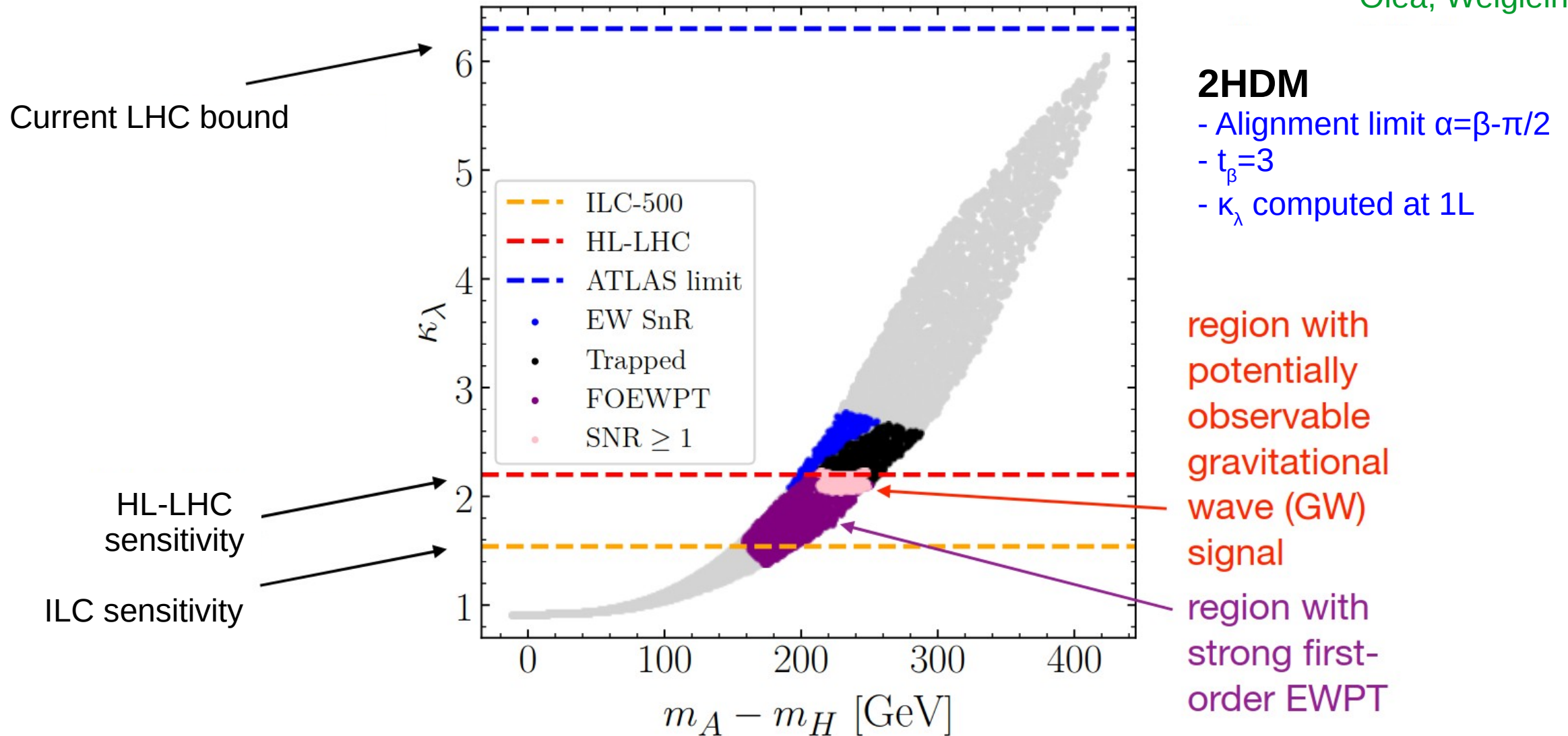
- Constraints on BSM parameter space!**



Here: scenarios with lightest BSM scalar mass + BSM mass param. at 400 GeV; other BSM scalar masses = M_{BSM}

Relation between κ_λ and strong first-order EWPT

[Biekötter, Heinemeyer, No, Olea, Weiglein '22]



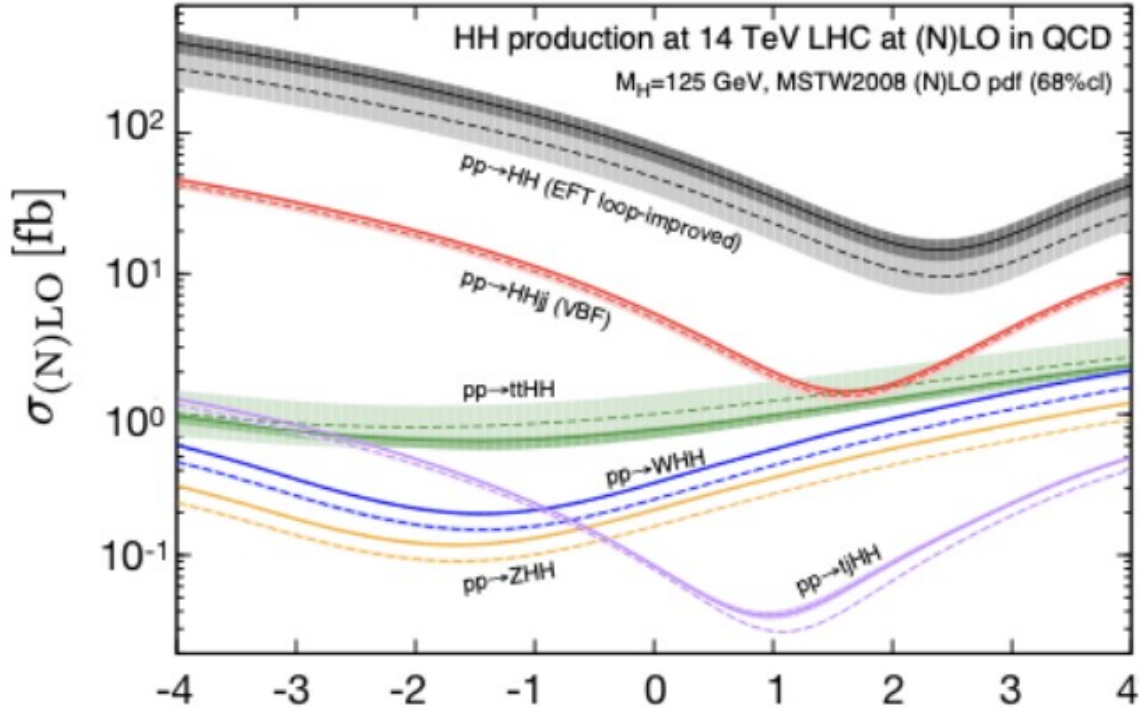
➤ **Region with a strong first-order EWPT and a potentially detectable GW signal is correlated with significant BSM deviation in κ_λ**

Large BSM effects in κ_λ : consequences on di-Higgs production at LHC

Di-Higgs production cross-sections as a function of λ_{hhh}

Plots taken from
[de Blas et al., 1905.03764]

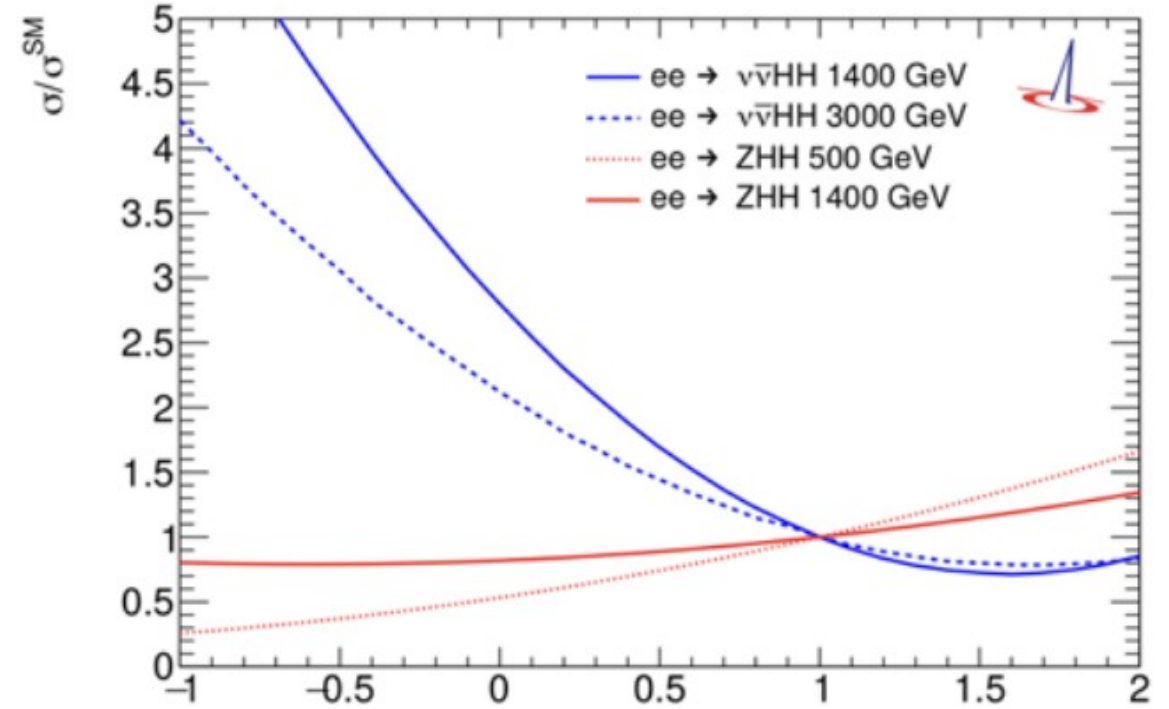
Hadron collider



[Frederix et al., 1401.7340]

$$\lambda_3/\lambda_3^{SM} = \kappa_\lambda$$

e^+e^- collider



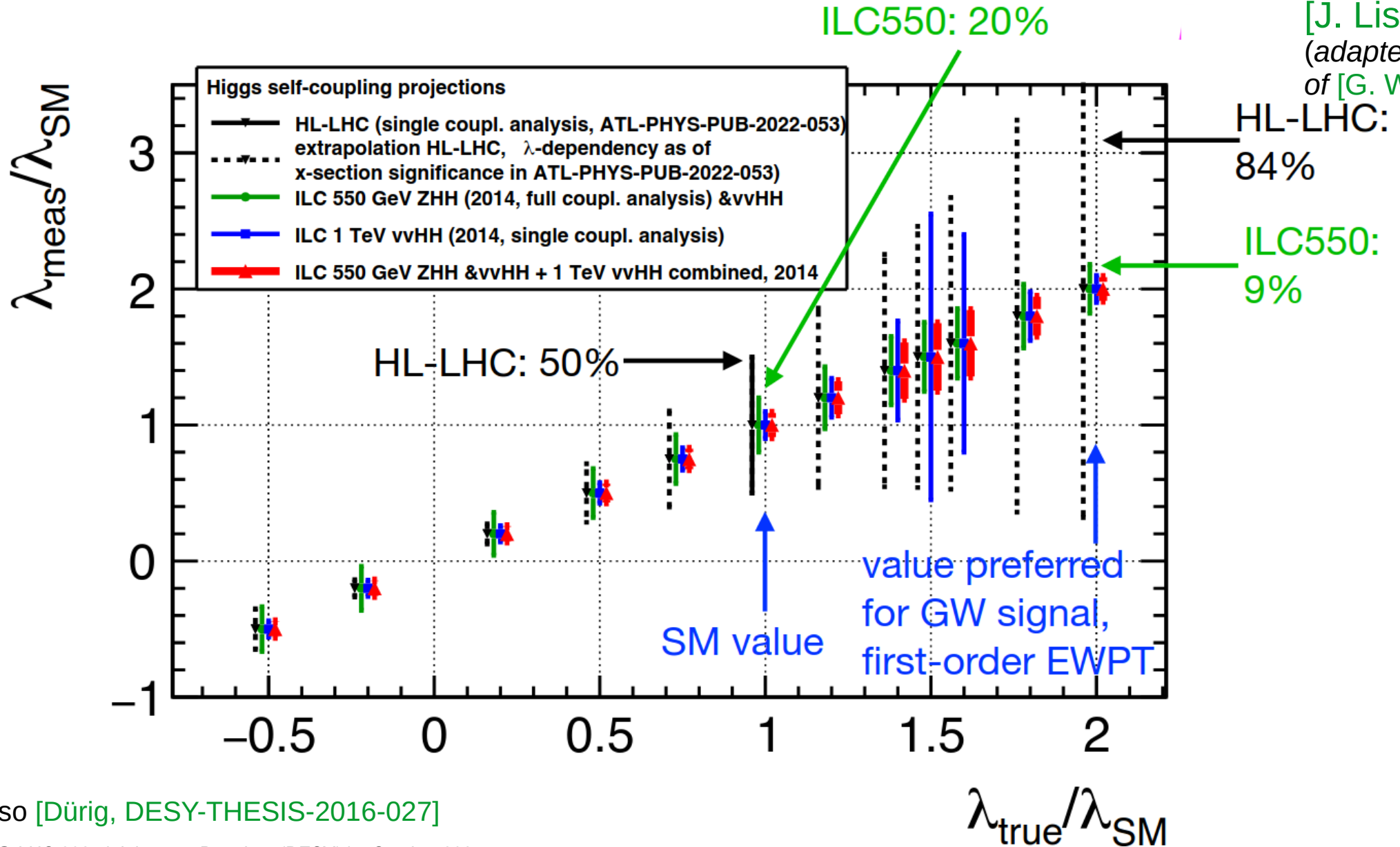
$$\lambda_3/\lambda_3^{SM} = \kappa_\lambda$$



- **BSM deviation in κ_λ modifies the interference between different contributions to di-Higgs production**
- Strong impact on total cross-sections (and also on differential distributions, see later slides)

Precision on the determination of λ_{hhh} as a function of λ_{hhh}

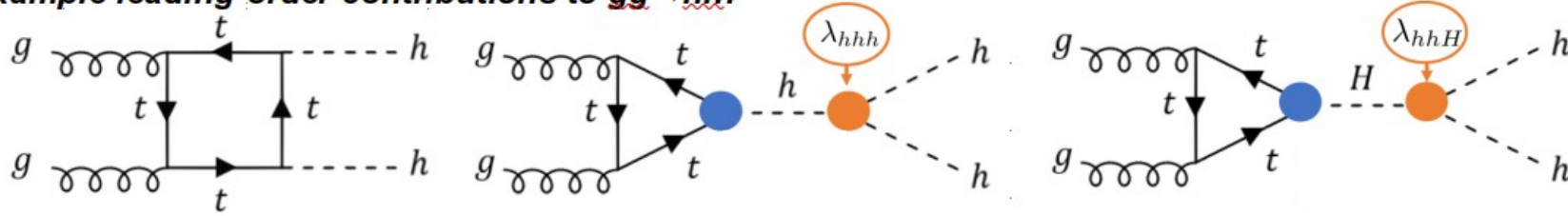
[J. List et al '24]
(adapted from slide of [G. Weiglein '24])



See also [Dürig, DESY-THESIS-2016-027]

Di-Higgs invariant mass distributions

Example leading-order contributions to $gg \rightarrow hh$:

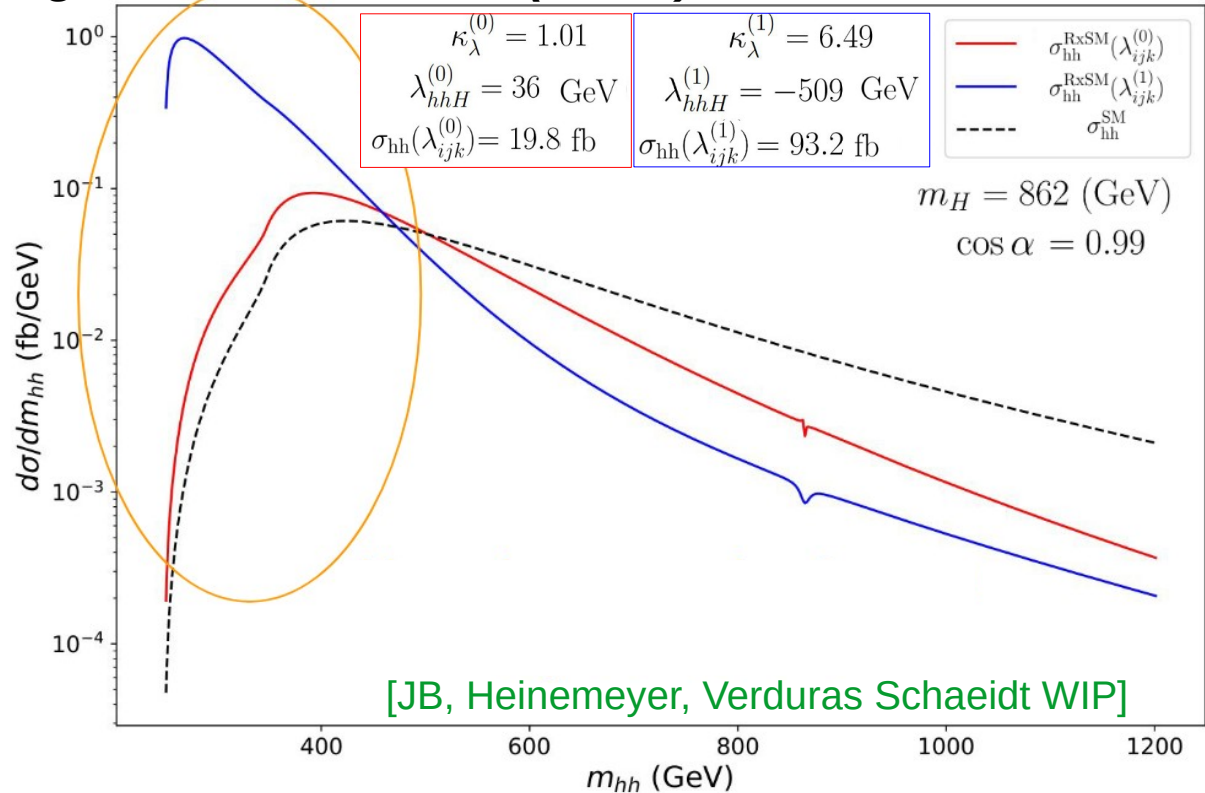


[Diagrams by A. Verduras Schaeidt]

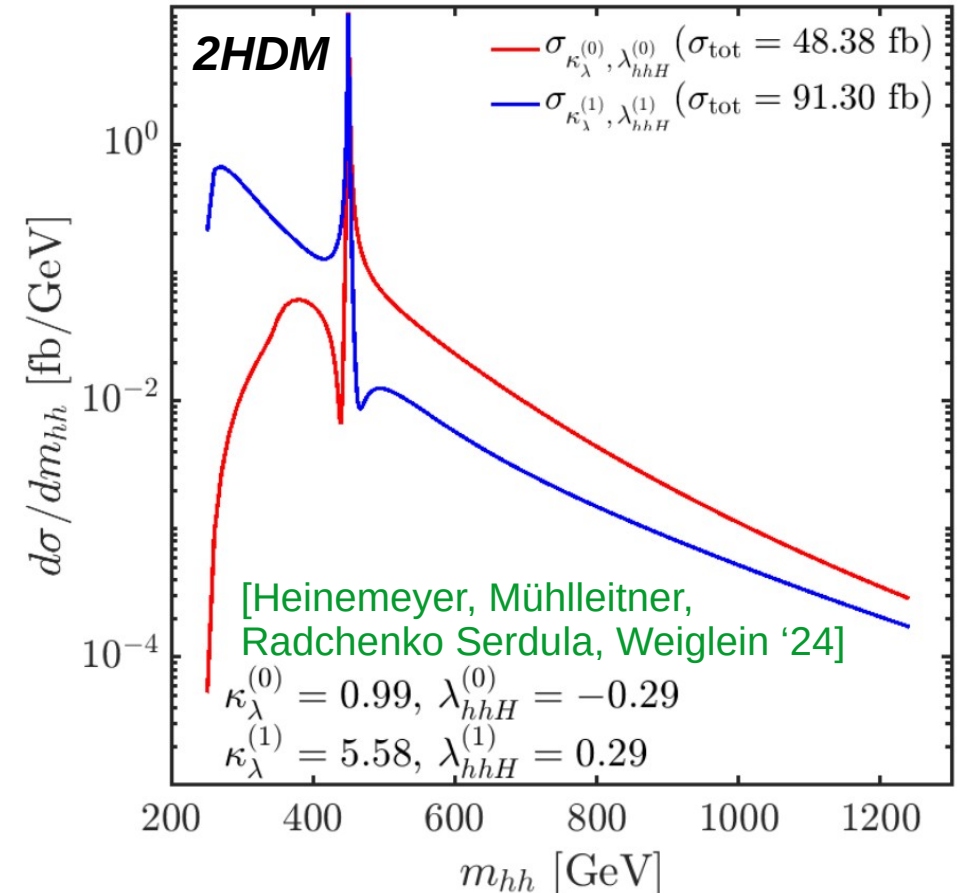
Red: differential distributions (LO) using tree-level trilinear couplings λ_{hhh} and λ_{hhH}

Blue: differential distributions (LO) using loop-corrected trilinear couplings λ_{hhh} and λ_{hhH}

Singlet extension of SM (RxSM)



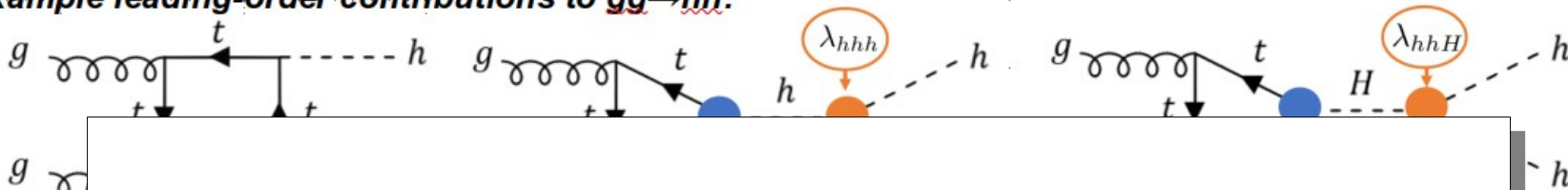
[JB, Heinemeyer, Verduras Schaeidt WIP]



[Heinemeyer, Mühlleitner, Radchenko Serdula, Weiglein '24]

Di-Higgs invariant mass distributions

Example leading-order contributions to $gg \rightarrow hh$:



Red: differential distribution
Blue: differential distribution

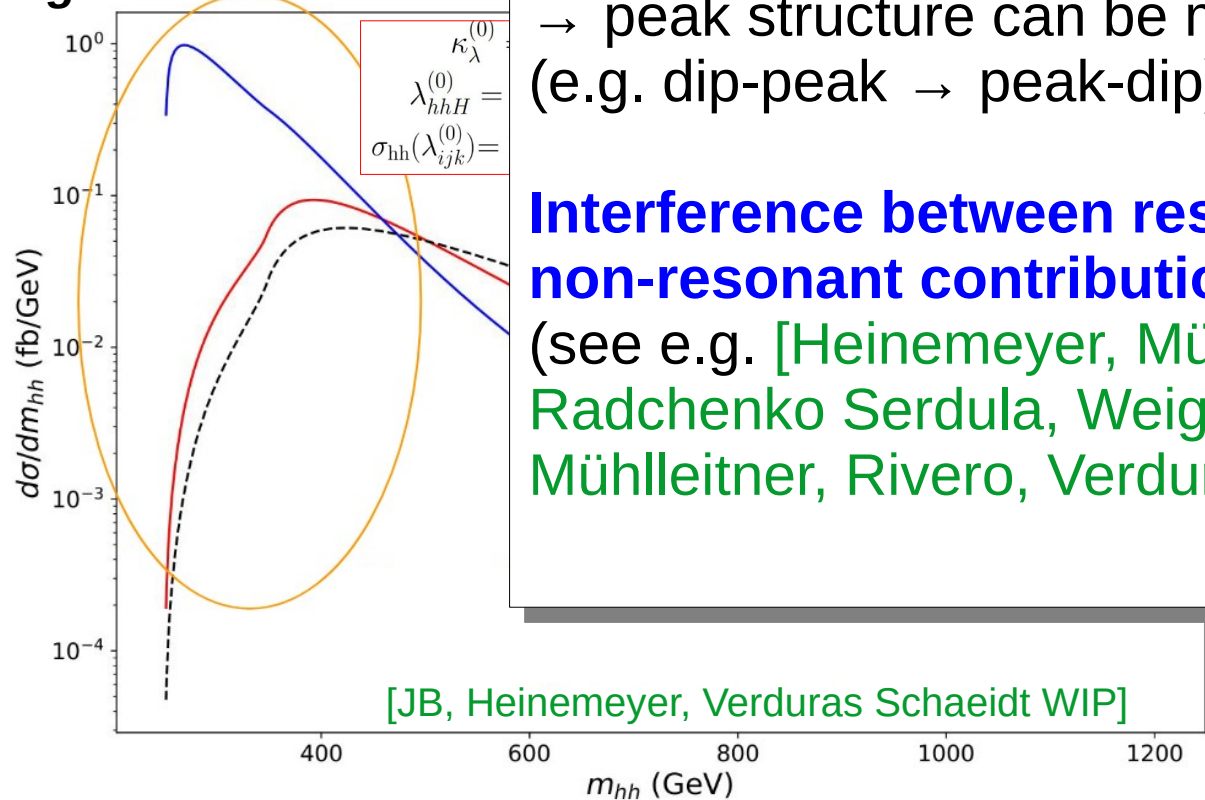
Singlet extension of SM

Strong impact also on differential distributions!

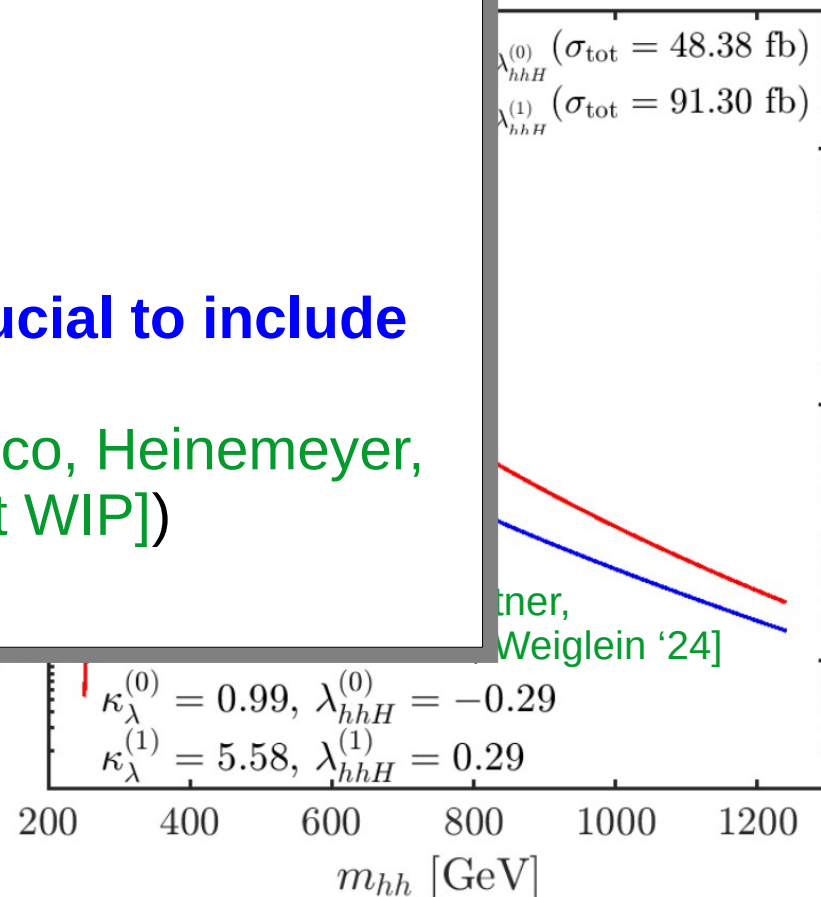
→ change in destructive interference at hh threshold

→ peak structure can be modified (e.g. dip-peak → peak-dip)

Interference between resonant and non-resonant contributions also crucial to include (see e.g. [Heinemeyer, Mühlleitner, Radchenko Serdula, Weiglein '24], [Arco, Heinemeyer, Mühlleitner, Rivero, Verduras Schaeidt WIP])



[JB, Heinemeyer, Verduras Schaeidt WIP]

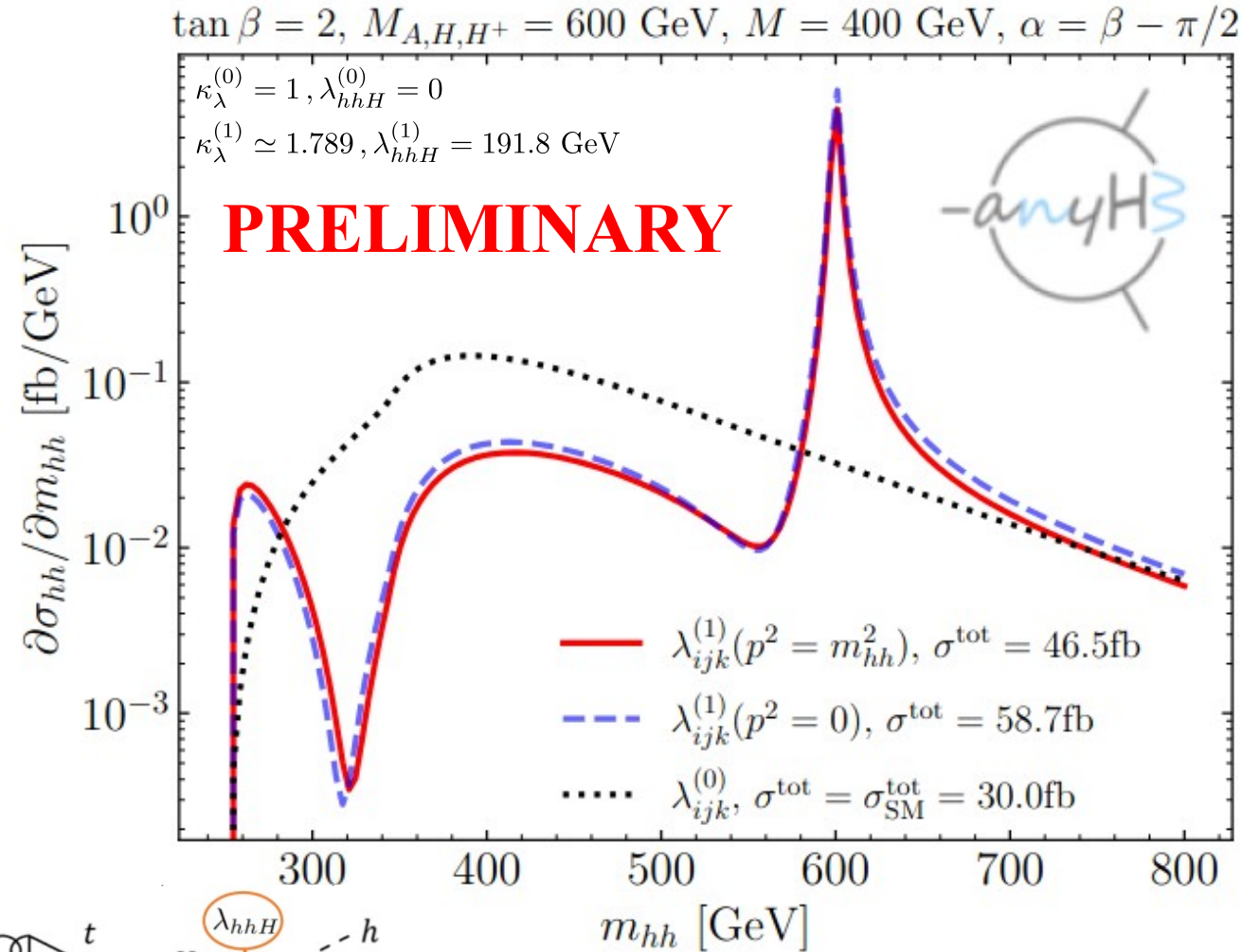
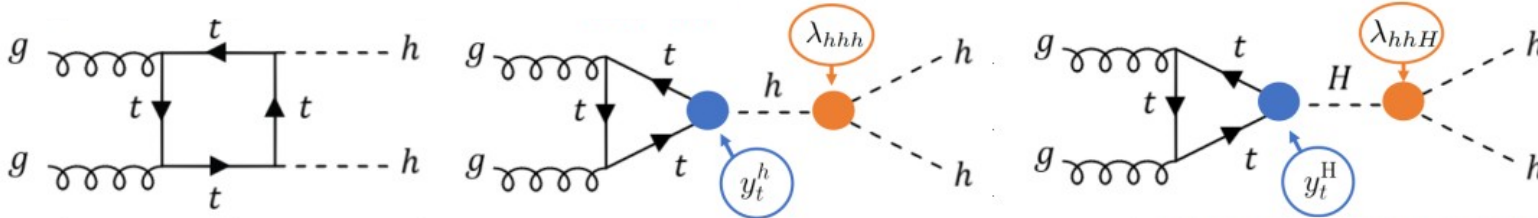


Heinemeyer, Mühlleitner, Radchenko Serdula, Weiglein '24]

Di-Higgs production in arbitrary models: anyHH

[Bahl, JB, Gabelmann, Radchenko Serdula, Weiglein *WIP*]

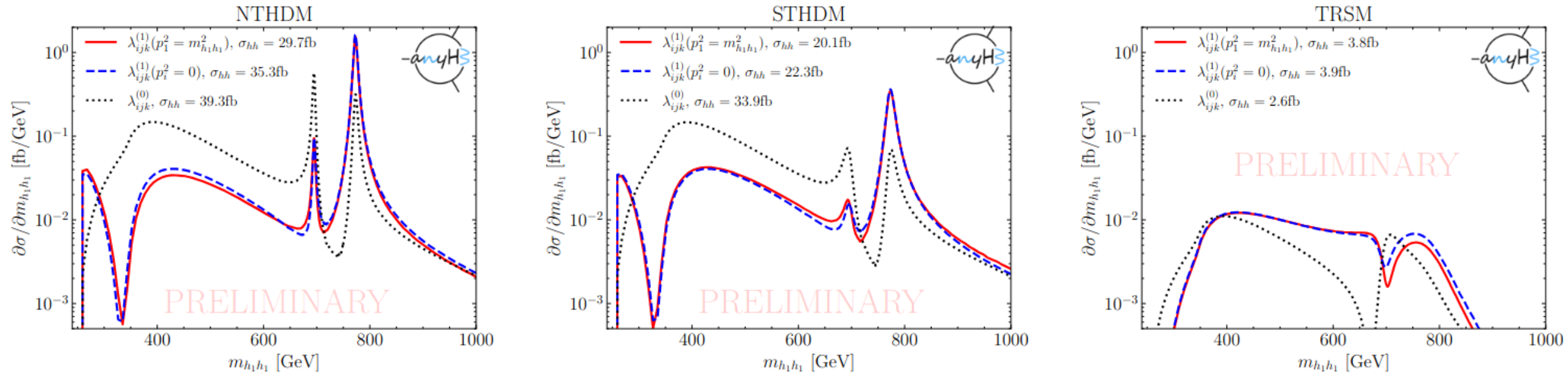
- **anyHH: Total and differential cross-sections** for $gg \rightarrow hh$ including **1L corrections to λ_{ijk}** (computed by anyH3) and **BSM contributions in s-channel**
- Good agreement found with existing results in the literature (e.g. HPair [M. Mühlleitner, M. Spira, et al.]) – *details in backup*
- Here: example in aligned 2HDM
Alignment limit:
 → $\kappa_\lambda^{(0)} = 1; \lambda_{hhH}^{(0)} = 0$
 → **huge impact of loop corrections to λ_{ijk}**
 → **O(20%) impact of momentum in λ_{ijk}**



Ongoing developments: anyHH and link to MadGraph

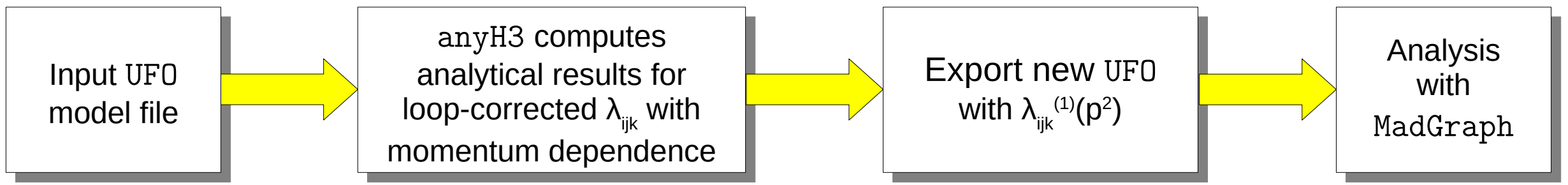
[Bahl, JB, Gabelmann, Radchenko Serdula, Weiglein *WIP*]

- Results available in **various new models** for the 1st time!
(NTHDM = 2HDM + real singlet; STHDM = 2HDM + complex singlet DM; TRSM: two-real singlet model)



(NB: these preliminary plots are meant for illustrations purposes only; not yet for phenomenological studies)

- Link to MadGraph under development:**



Summary

- λ_{hhh} plays a crucial role to probe the **shape of the Higgs potential** and the **nature of the EW phase transition**, and search indirect **signs of New Physics**
- λ_{hhh} can **deviate significantly from SM prediction** (by up to a factor **~ 10**), for otherwise theoretically and experimentally allowed points, due to **mass-splitting effects in radiative corrections involving BSM scalars**
- Current experimental bounds on λ_{hhh} can **already exclude significant parts of otherwise unconstrained BSM parameter space**, and future prospects even better!
- Large BSM deviations in λ_{hhh} , as well as loop corrections to other BSM trilinear scalar couplings, can have a **strong impact on total and differential cross-sections for di-Higgs production**
 - the inclusion of these loop effects in theoretical and experimental analyses is paramount
 - possible with public tools anyH3 and anyHH

Thank you very much for your attention!

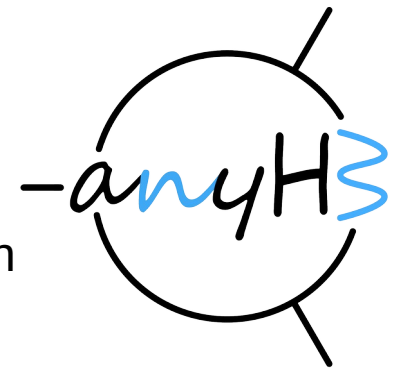
Contact

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Summary – anyH3



Python package anyH3 allows calculation of λ_{hhh} for arbitrary renormalisable theories with

- Full one-loop effects including external-momentum dependence
- Highly flexible choices of renormalisation schemes → predefined or by user
- Uses **UFO** model inputs (generated with SARAH, FeynRules or using custom ones)
- Part of wider **anyBSM framework**, including
 - **anyHH for di-Higgs production at hadron colliders**
 - **Interface to MadGraph planned** to allow direct use in experimental analyses of loop-corrected trilinear scalar couplings
and much more!
- Currently 14 models included (publicly), easy inclusion of further models → **new ideas/requests welcome!**

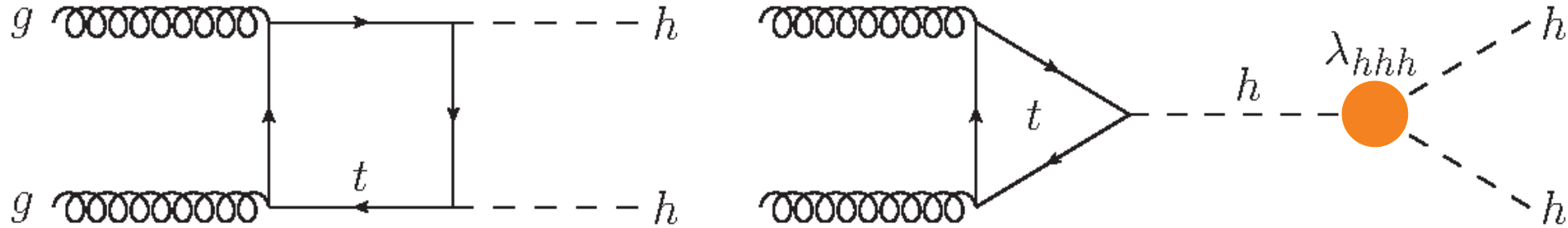
**Get started at <https://anybsm.gitlab.io/>
or directly in terminal with**

```
pip install anyBSM & anyBSM --help !
```

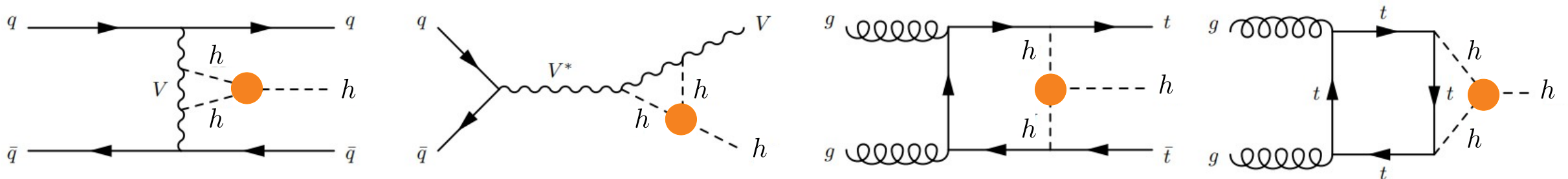
Backup

Experimental probes of λ_{hhh}

- **Double-Higgs production** $\rightarrow \lambda_{hhh}$ enters at leading order (LO) \rightarrow **most direct probe!**

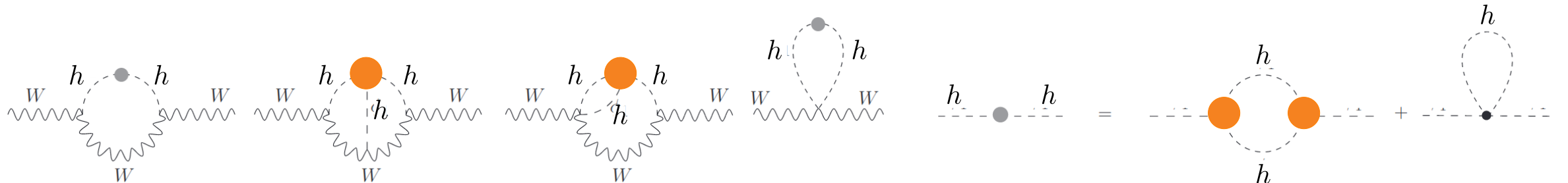


- **Single-Higgs production** $\rightarrow \lambda_{hhh}$ enters at NLO



[Degrassi, Giardino, Maltoni, Pagani '16] [ATLAS-CONF-2019-049]

- **Electroweak Precision Observables (EWPOs)** $\rightarrow \lambda_{hhh}$ enters at NNLO



[Degrassi, Fedele, Giardino '17]

Future determination of λ_{hhh}

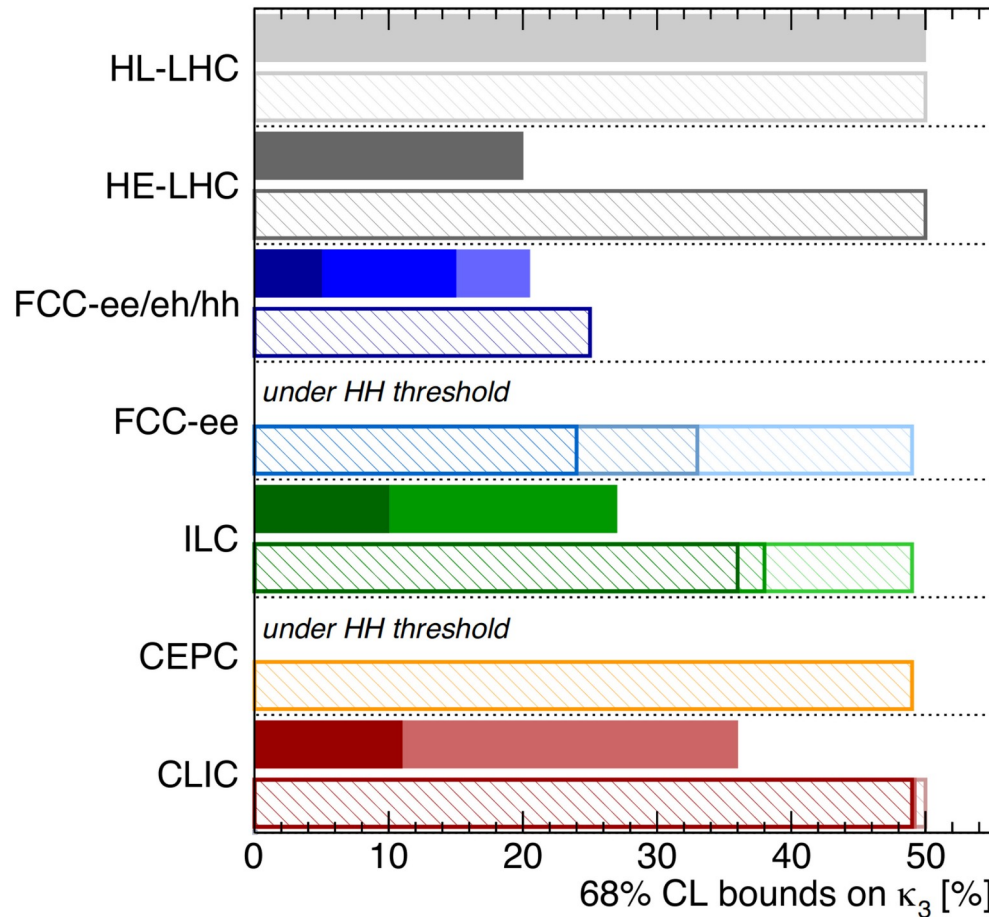
Expected sensitivities in literature, assuming $\lambda_{hhh} = (\lambda_{hhh})^{SM}$

di-Higgs exclusive result

Higgs@FC WG September 2019

di-Higgs	single-Higgs
HL-LHC 50%	HL-LHC 50% (47%)
HE-LHC [10-20]%	HE-LHC 50% (40%)
FCC-ee/eh/hh 5%	FCC-ee/eh/hh 25% (18%)
LE-FCC 15%	LE-FCC n.a.
FCC-eh ₃₅₀₀ -17+24%	FCC-eh ₃₅₀₀ n.a.
	FCC-ee ^{4IP} ₃₆₅ 24% (14%)
	FCC-ee ₃₆₅ 33% (19%)
	FCC-ee ₂₄₀ 49% (19%)
ILC ₁₀₀₀ 10%	ILC ₁₀₀₀ 36% (25%)
ILC ₅₀₀ 27%	ILC ₅₀₀ 38% (27%)
	ILC ₂₅₀ 49% (29%)
	CEPC 49% (17%)
CLIC ₃₀₀₀ -7+11%	CLIC ₃₀₀₀ 49% (35%)
CLIC ₁₅₀₀ 36%	CLIC ₁₅₀₀ 49% (41%)
	CLIC ₃₈₀ 50% (46%)

All future colliders combined with HL-LHC



single-Higgs exclusive

single-Higgs global

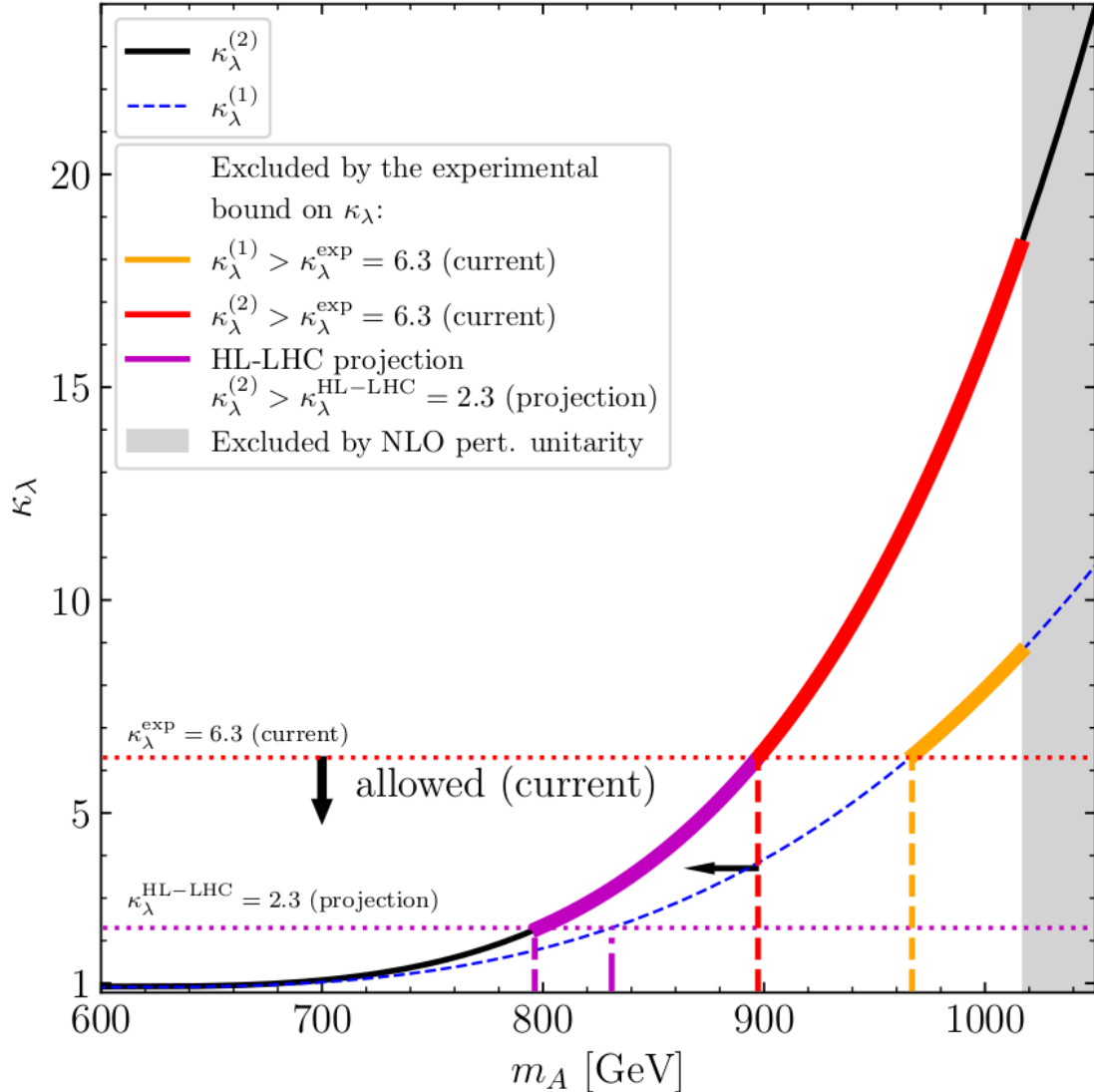
Plot taken from
[de Blas et al., 1905.03764]

see also [Cepeda et al., 1902.00134], [Di Vita et al.1711.03978], [Fujii et al. 1506.05992, 1710.07621, 1908.11299], [Roloff et al., 1901.05897], [Chang et al. 1804.07130,1908.00753], etc.

A benchmark scenario in the aligned 2HDM – 1D scan

[Bahl, JB, Weiglein PRL '22]

2HDM type I, $\alpha = \beta - \pi/2$, $m_A = m_{H^\pm}$, $M = m_H = 600$ GeV, $\tan \beta = 2$



Bound on eigenvalues	$\max(m_A)$ with LO pert. unit.	$\max(m_A)$ with NLO pert. unit.	$\max(m_A)$ with finite $\sqrt{s} \in [3 \text{ TeV}, 10 \text{ TeV}]$
$\max(a_i) < 1$ $\max(\Re(a_i)) < 1$	1161 GeV	1017 GeV	–
$\max(a_i) < 0.5$ $\max(\Re(a_i)) < 0.5$	917 GeV	937 GeV	–
$\max(a_i) < 0.49$ $\max(\Re(a_i)) < 0.49$	911 GeV	933 GeV	–
$\max(a_i) < 0.45$ $\max(\Re(a_i)) < 0.45$	889 GeV	912 GeV	–
			1260 GeV
			929 GeV
			922 GeV
			897 GeV

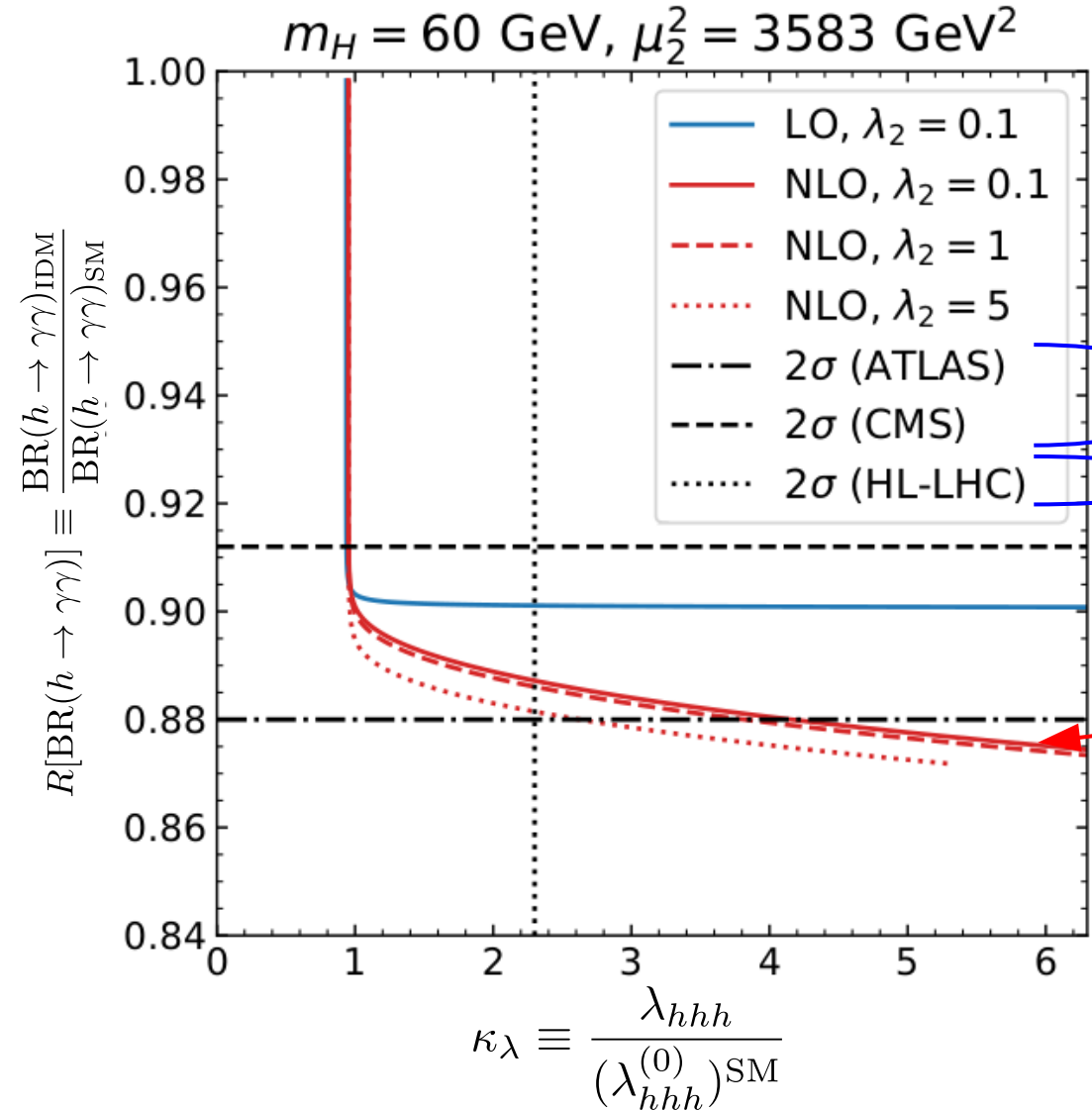
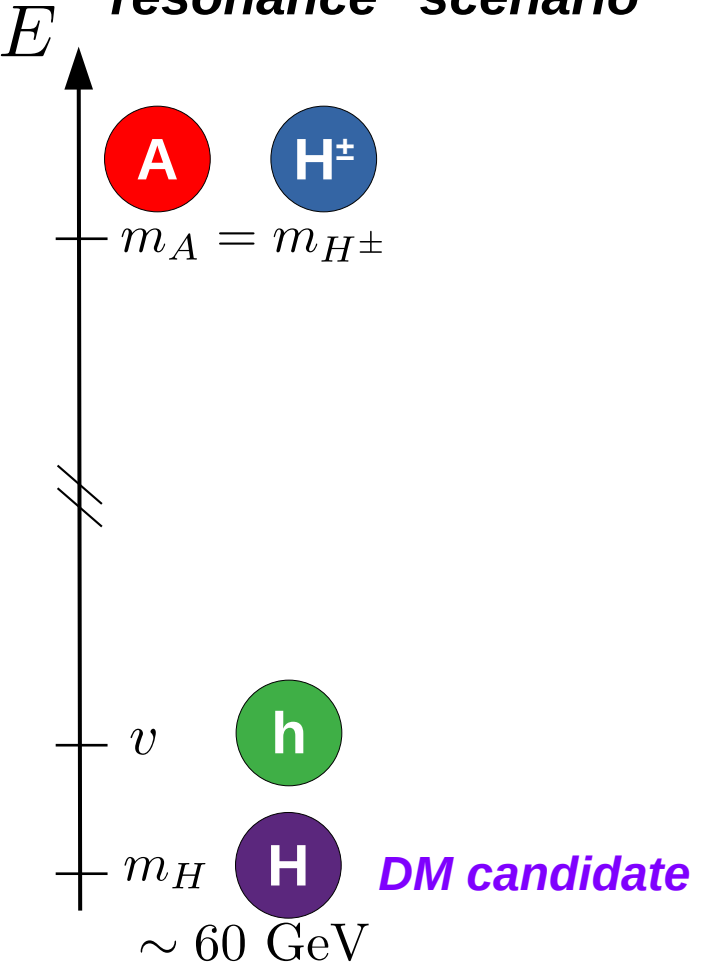
Table 1: Maximal values of m_A allowed in the benchmark scenario under the constraint of perturbative unitarity, at LO and NLO, and for different upper bounds on the $2 \rightarrow 2$ scattering eigenvalues used in the perturbative unitarity constraint. Note that tree-level scattering eigenvalues are all real, so there is no difference between using \max or $\Re(\max)$ for the left column.

Correlation between κ_λ and $BR(h \rightarrow \gamma\gamma)$ at one and two loops

Could BSM Physics be observed first in κ_λ ?

[Aiko, JB, Kanemura '23 + WIP]
+ [JB, Kanemura '19]

Inert Doublet Model in DM-inspired "Higgs resonance" scenario



$[\lambda_2 : \text{inert doublet self-coupling}]$

Expected bounds on $R[BR(h \rightarrow \gamma\gamma)]$ at HL-LHC
Expected bound on κ_λ at HL-LHC

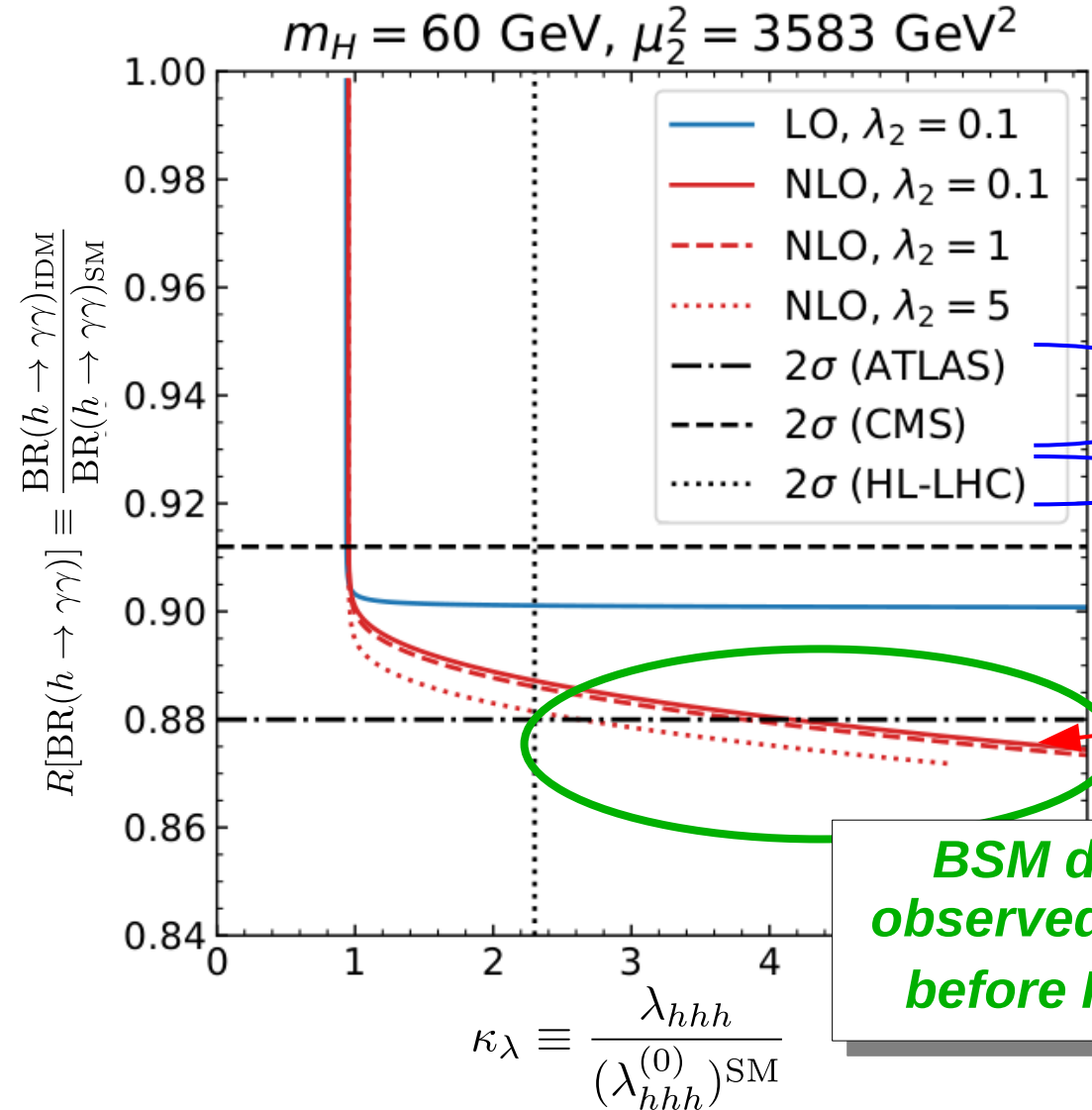
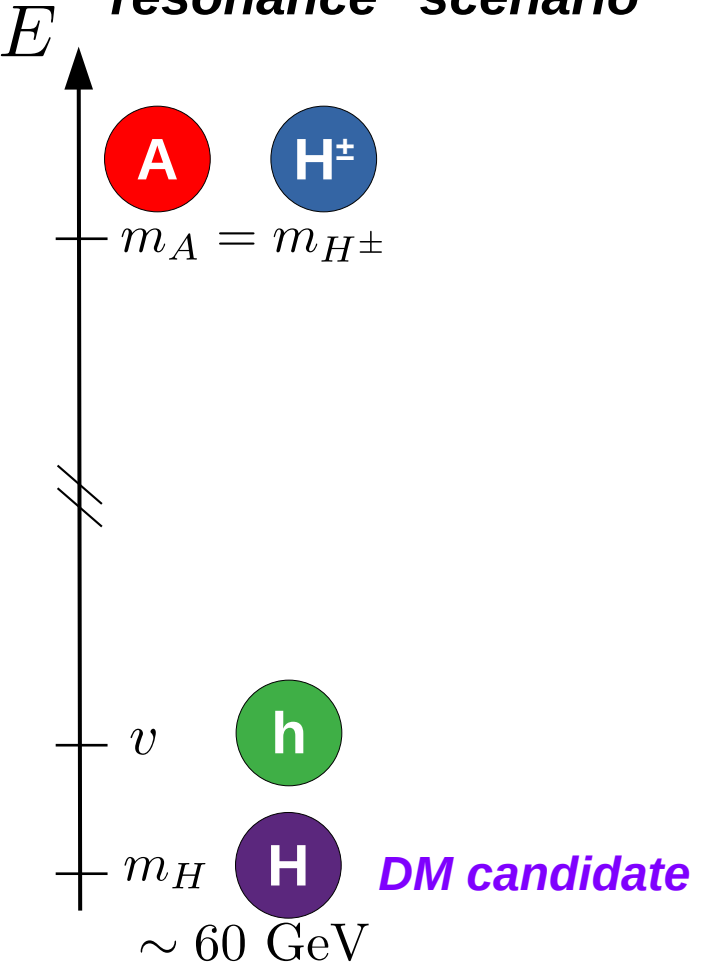
$m_{H^\pm} = m_A$ varied along the curves (until limit from pert. unit.)

Correlation between κ_λ and $\text{BR}(h \rightarrow \gamma\gamma)$ at one and two loops

Could BSM Physics be observed first in κ_λ ?

[Aiko, JB, Kanemura '23 + WIP]
+ [JB, Kanemura '19]

Inert Doublet Model in DM-inspired "Higgs resonance" scenario



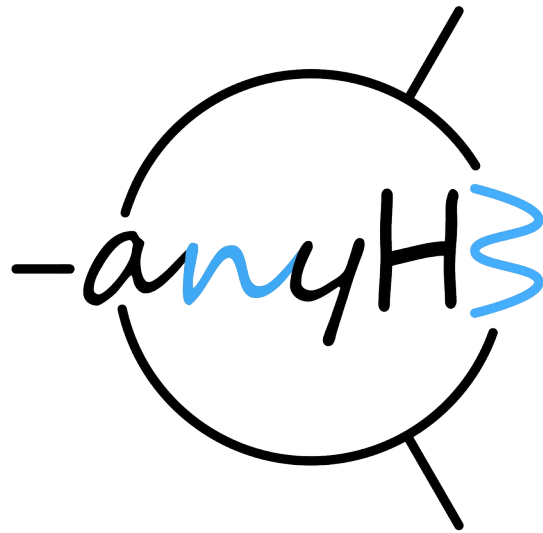
$[\lambda_2 : \text{inert doublet self-coupling}]$

Expected bounds on $R[\text{BR}(h \rightarrow \gamma\gamma)]$ at HL-LHC
Expected bound on κ_λ at HL-LHC

$m_{H^\pm} = m_A$ varied along the curves (until limit from pert. unit.)

BSM deviation observed first in κ_λ , before $\Gamma(h \rightarrow \gamma\gamma)$!

Generic predictions for λ_{hhh}

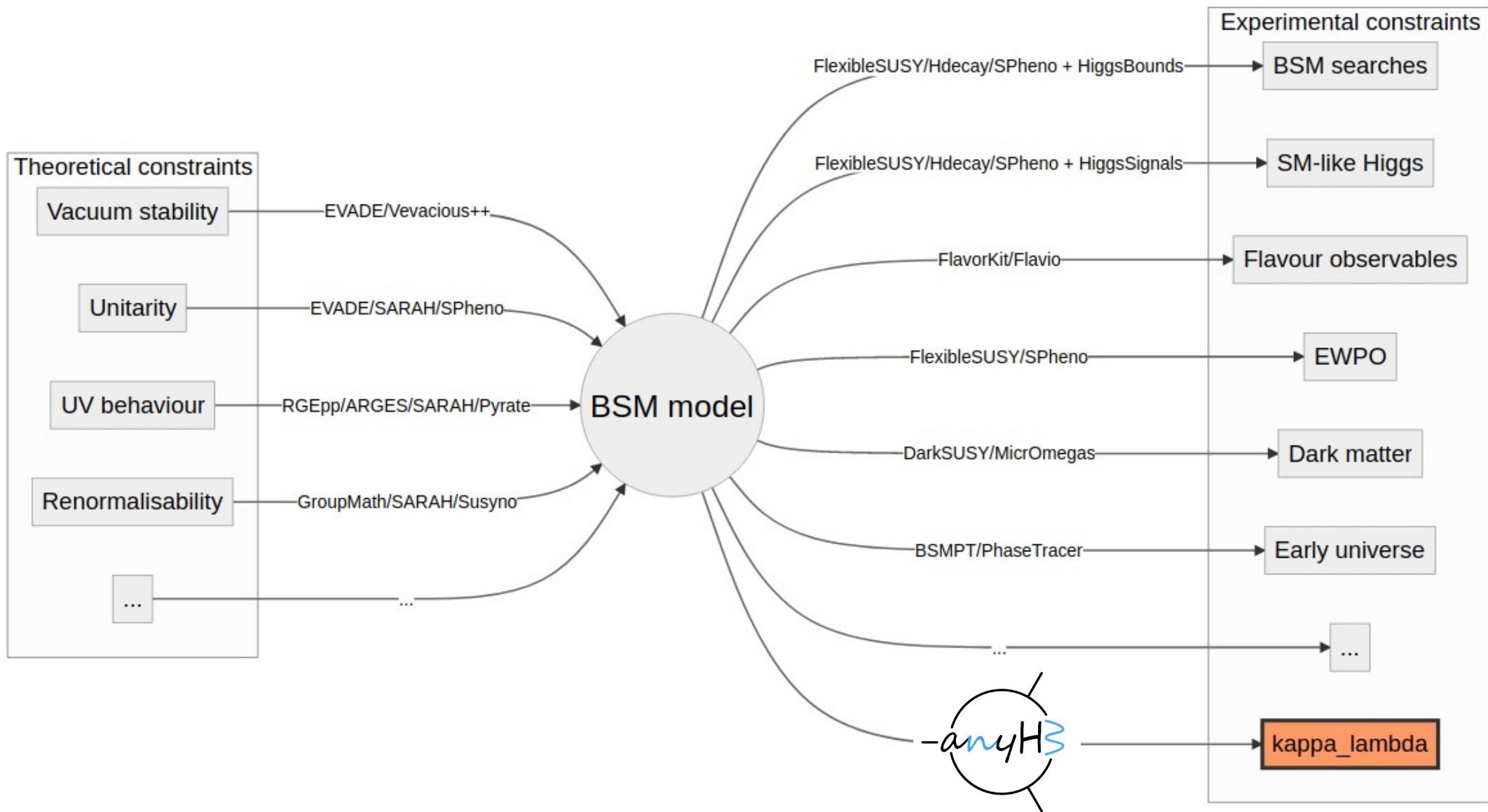


Based on

arXiv:2305.03015 (EPJC) + WIP

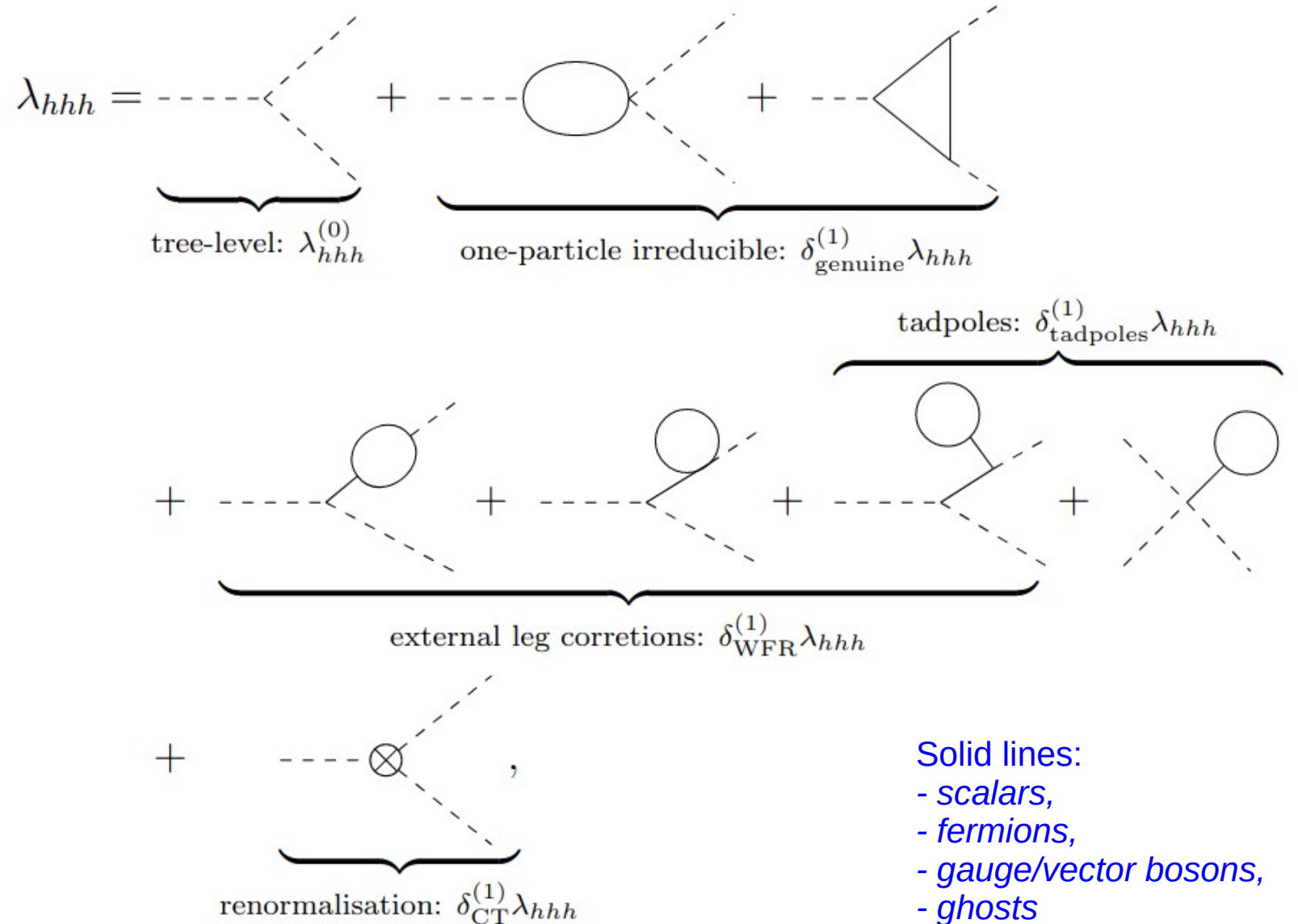
in collaboration with Henning Bahl, Martin Gabelmann, Kateryna Radchenko Serdula and Georg Weiglein

λ_{hhh} within the landscape of automated tools



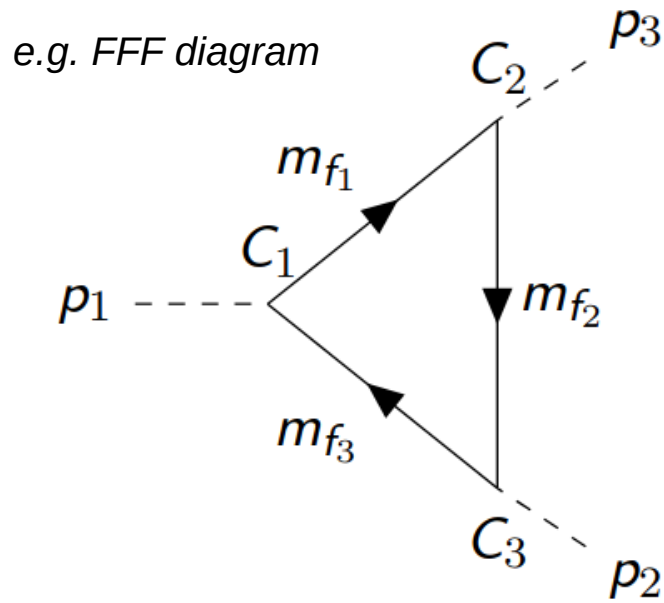
Full one-loop calculation of λ_{hhh} with anyH3: how does it work?

- Generic results applied to concrete (B)SM model, using inputs in UFO format
[Degrande et al., '11], [Darmé et al. '23]
- Loop functions evaluated via COLLIER [Denner et al '16] interface, pyCollier
- Restrictions on **particles** and/or **topologies** possible
- Renormalisation performed automatically** (*more in backup*)



Computing λ_{hhh} in general renormalisable theories: method

Our method: we derive and implement analytic results for **generic diagrams**, i.e. assuming generic



For evaluation:

- Apply to concrete (B)SM model, using inputs in UFO format [Degrande et al., '11], [Darmé et al. '23]
- Evaluate loop functions via COLLIER [Denner et al '16] interface, pyCollier
- All included in public tool anyH3 [Bahl, JB, Gabelmann, Weiglein '23]

- Couplings $C_i = C_i^L P_L + C_i^R P_R$, where $P_{L,R} \equiv \frac{1}{2}(1 \mp \gamma_5)$
- Masses on the internal lines m_{fi} , $i=1,2,3$
- External momenta p_i , $i=1,2,3$

$$\begin{aligned}
 &= 2\mathbf{B0}(p_3^2, m_2^2, m_3^2)(C_1^L(C_2^L C_3^R m_{f1} + C_2^R C_3^R m_{f2} + C_2^R C_3^L m_{f3}) + C_1^R(C_2^R C_3^L m_{f1} + \\
 &C_2^L C_3^L m_{f2} + C_2^L C_3^R m_{f3})) + m_{f1} \mathbf{C0}(p_2^2, p_3^2, p_1^2, m_1^2, m_3^2, m_2^2)((C_1^L C_2^L C_3^R + \\
 &C_1^R C_2^R C_3^L)(p_1^2 + p_2^2 - p_3^2) + 2(C_1^L C_2^L C_3^L + C_1^R C_2^R C_3^R)m_{f2} m_{f3} + \\
 &2m_{f1}(C_1^L(C_2^L C_3^R m_{f1} + C_2^R C_3^R m_{f2} + C_2^R C_3^L m_{f3}) + C_1^R(C_2^R C_3^L m_{f1} + C_2^L C_3^L m_{f2} + \\
 &C_2^L C_3^R m_{f3}))) + \mathbf{C1}(p_2^2, p_3^2, p_1^2, m_1^2, m_3^2, m_2^2)(2p_2^2(C_1^L C_3^R(C_2^L m_{f1} + C_2^R m_{f2}) + \\
 &C_1^R C_3^L(C_2^R m_{f1} + C_2^L m_{f2})) + (p_1^2 + p_2^2 - p_3^2)((C_1^L C_2^L C_3^R + C_1^R C_2^R C_3^L)m_{f1} + \\
 &(C_1^L C_2^R C_3^L + C_1^R C_2^L C_3^R)m_{f3})) + \mathbf{C2}(p_2^2, p_3^2, p_1^2, m_1^2, m_3^2, m_2^2)((p_1^2 + p_2^2 - \\
 &p_3^2)(C_1^L C_3^R(C_2^L m_{f1} + C_2^R m_{f2}) + C_1^R C_3^L(C_2^R m_{f1} + C_2^L m_{f2})) + 2p_1^2((C_1^L C_2^L C_3^R + \\
 &C_1^R C_2^R C_3^L)m_{f1} + (C_1^L C_2^R C_3^L + C_1^R C_2^L C_3^R)m_{f3}))
 \end{aligned}$$

(B0, C0, C1, C2: loop functions)

Flexible choice of renormalisation schemes

$$\delta_{\text{CT}}^{(1)} \lambda_{hhh} = \text{---} \otimes \text{---} = ?$$

➤ **1L calculation** → renormalisation of all parameters entering λ_{hhh} at tree-level

➤ In general:

$$(\lambda_{hhh}^{(0)})^{\text{BSM}} = (\lambda_{hhh}^{(0)})^{\text{BSM}} \left(\underbrace{m_h \simeq 125 \text{ GeV}, v \simeq 246 \text{ GeV}}_{\text{SM sector}}, \underbrace{m_{\Phi_i}}_{\text{BSM}}, \underbrace{\alpha_i}_{\text{BSM}}, \underbrace{v_i}_{\text{BSM}}, \underbrace{g_i}_{\text{indep.}} \right)$$

masses
mixing angles
VEVs
BSM coups.

➤ Most automated codes: $\overline{\text{MS}}/\overline{\text{DR}}$ only

➤ **anyH3**: much more flexibility, following **user choice**:

- **SM sector** (m_h, v): fully OS or $\overline{\text{MS}}/\overline{\text{DR}}$
- **BSM masses**: OS or $\overline{\text{MS}}/\overline{\text{DR}}$
- **Additional couplings/vevs/mixings**: by default $\overline{\text{MS}}$, but **user-defined ren. conditions** also possible!

$$\delta_{\text{CT}}^{(1)} \lambda_{hhh} = \sum_x \left(\frac{\partial}{\partial x} (\lambda_{hhh}^{(0)})^{\text{BSM}} \right) \delta^{\text{CT}} x, \quad \text{with } x \in \{m_h, v, m_{\Phi_i}, v_i, \alpha_i, g_i, \text{etc.}\}$$

Renormalised in $\overline{\text{MS}}$, OS, in custom schemes, etc.

(Default) Renormalization choice of $(v^{\text{SM}})^{\text{OS}}$ and $(m_i^2)^{\text{OS}}$

> $v^{\text{OS}} \equiv \frac{2M_W^{\text{OS}}}{e} \sqrt{1 - \frac{M_W^{2\text{OS}}}{M_Z^{2\text{OS}}}}$ with

• $\delta^{(1)} M_V^{2\text{OS}} = \frac{\Pi_V^{(1),T}}{M_V^{2\text{OS}}}(p^2 = M_V^{2\text{OS}})$, $V = W, Z$

• $\delta^{(1)} e^{\text{OS}} = \frac{1}{2} \dot{\Pi}_\gamma(p^2 = 0) + \text{sign}(\sin \theta_W) \frac{\sin \theta_W}{M_Z^2 \cos \theta_W} \Pi_{\gamma Z}(p^2 = 0)$

> attention (i): $\rho^{\text{tree-level}} \neq 1 \rightarrow$ further CTs needed (depends on the model)

\rightarrow ability to define *custom* renormalisation conditions

> scalar masses: $m_i^{\text{OS}} = m_i^{\text{pole}}$

• $\delta^{\text{OS}} m_i^2 = -\widetilde{\text{Re}} \Sigma_{h_i}^{(1)}|_{p^2=m_i^2}$

• $\delta^{\text{OS}} Z_i = \widetilde{\text{Re}} \frac{\partial}{\partial p^2} \Sigma_{h_i}^{(1)}|_{p^2=m_i^2}$

> attention (ii): scalar mixing may also require further CTs/tree-level relations

All bosonic one- & two-point functions and their derivatives for general QFTs are required for flexible OS renormalisation.

Features of anyH3, so far

- Import/conversion of any UFO model
- Definition of renormalisation schemes

```
# schemes.yml
```

```
renormalization_schemes:
```

```
MS:
```

```
  SM_names:
```

```
    Higgs-Boson: h1
```

```
  VEV_counterterm: MS
```

```
  mass_counterterms:
```

```
    h1: MS
```

```
    h2: MS
```

```
OS:
```

```
  SM_names:
```

```
    Higgs-Boson: h1
```

```
  VEV_counterterm: OS
```

```
  custom_CT_hhh: 'dbetaH =
```

```
f"({Sigma('Hm1','Hm2',momentum='0')} +  
{Sigma('Hm1','Hm2',momentum='MHm2**2')})/ -  
(2*MHm2**2)"
```

```
  dTanBeta = f"({dbetaH})/cos(betaH)**2"
```

```
  ...
```

*(extract from
schemes.yml
for 2HDM)*

- Analytical / numerical / LaTeX outputs

- **3 user interfaces:**

- Python library

```
from anyBSM import anyH3  
myfancymodel = anyH3('path/to/UFO/model')  
result = myfancymodel.lambdahhh()
```

- Command line

- Mathematica interface

- **Perturbative unitarity checks** available (at tree level and in high-energy limit for now)

- Can be used together with a spectrum generator and **handles SLHA format**

- Efficient **caching** available

- Lots more!

New results I: mass-splitting effects in various BSM models

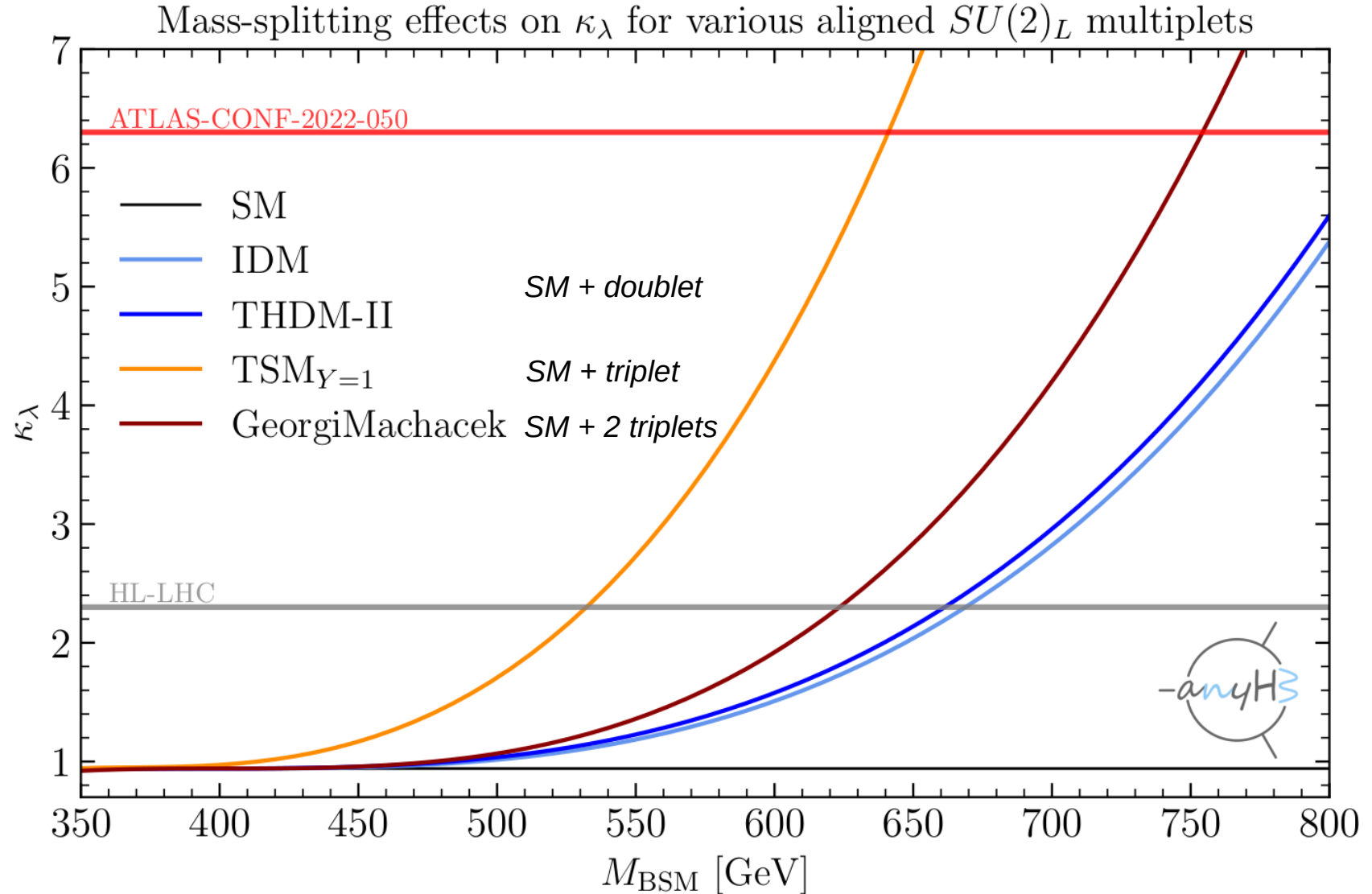
- Consider the non-decoupling limit in several BSM models

$$M_{\text{BSM}}^2 = \mathcal{M}^2 + \tilde{\lambda}v^2$$

- Increase M_{BSM} , keeping \mathcal{M} fixed
 - large mass splittings
 - **large BSM effects!**

- Perturbative unitarity checked with anyPerturbativeUnitarity

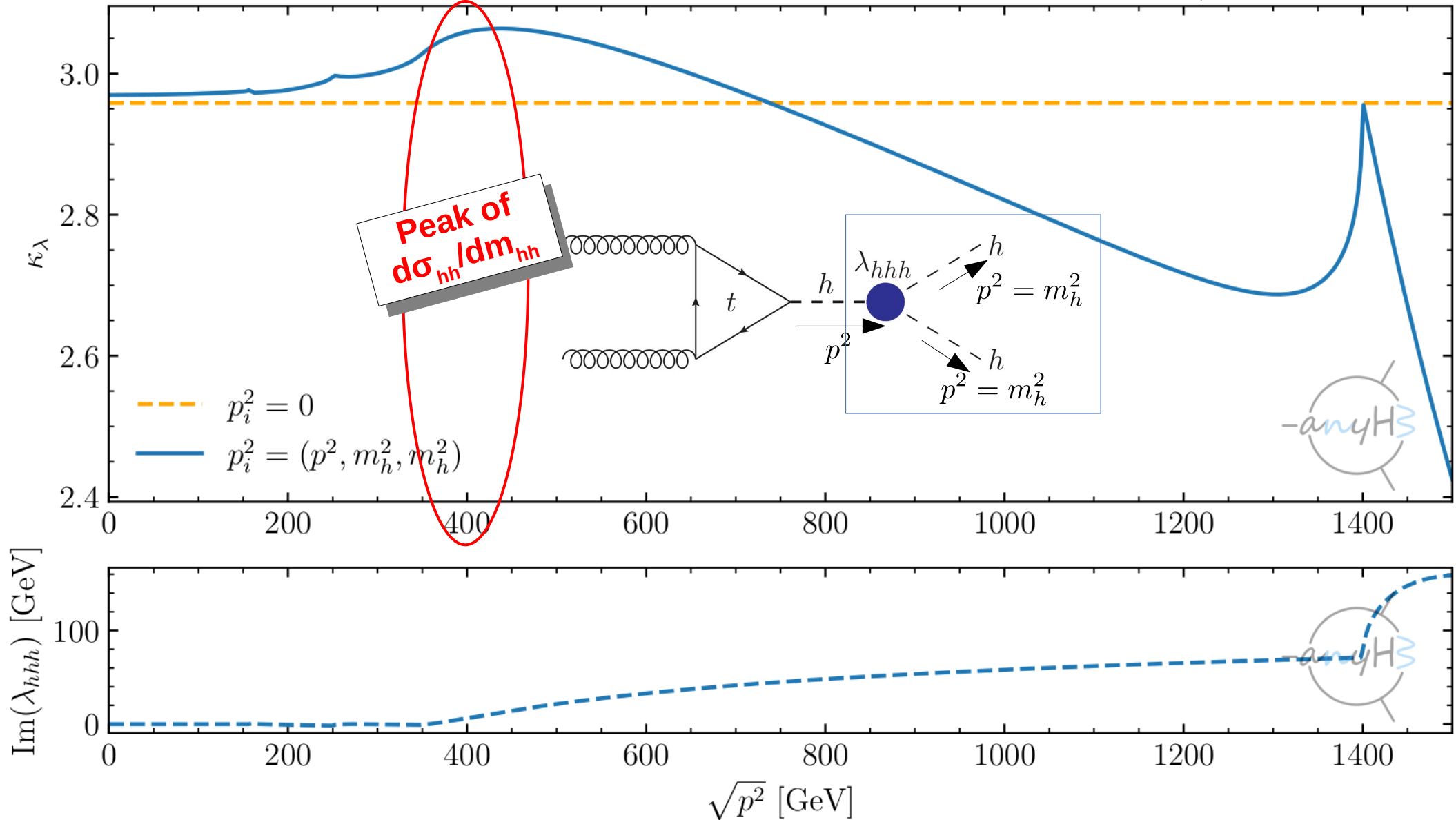
- Constraints on BSM parameter space!**



Here: scenarios with lightest BSM scalar mass & BSM mass param. at 400 GeV; other BSM scalar masses = M_{BSM}

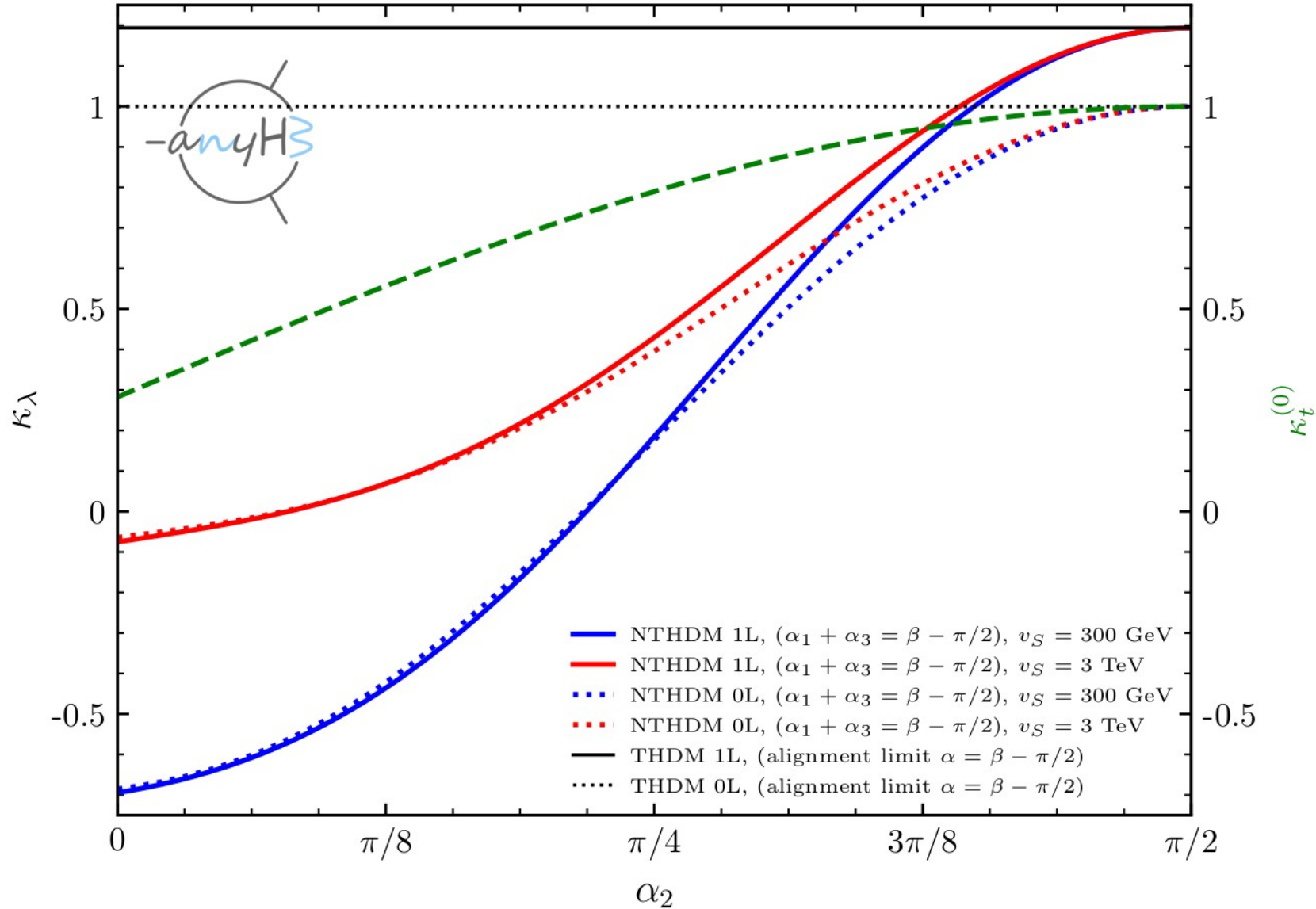
New results II: momentum dependence in the 2HDM

THDM-I: $m_H = M = 400 \text{ GeV}$, $m_A = m_{H^\pm} = 700 \text{ GeV}$, $t_\beta = 2$



More new results with anyH3: an example in the N2HDM

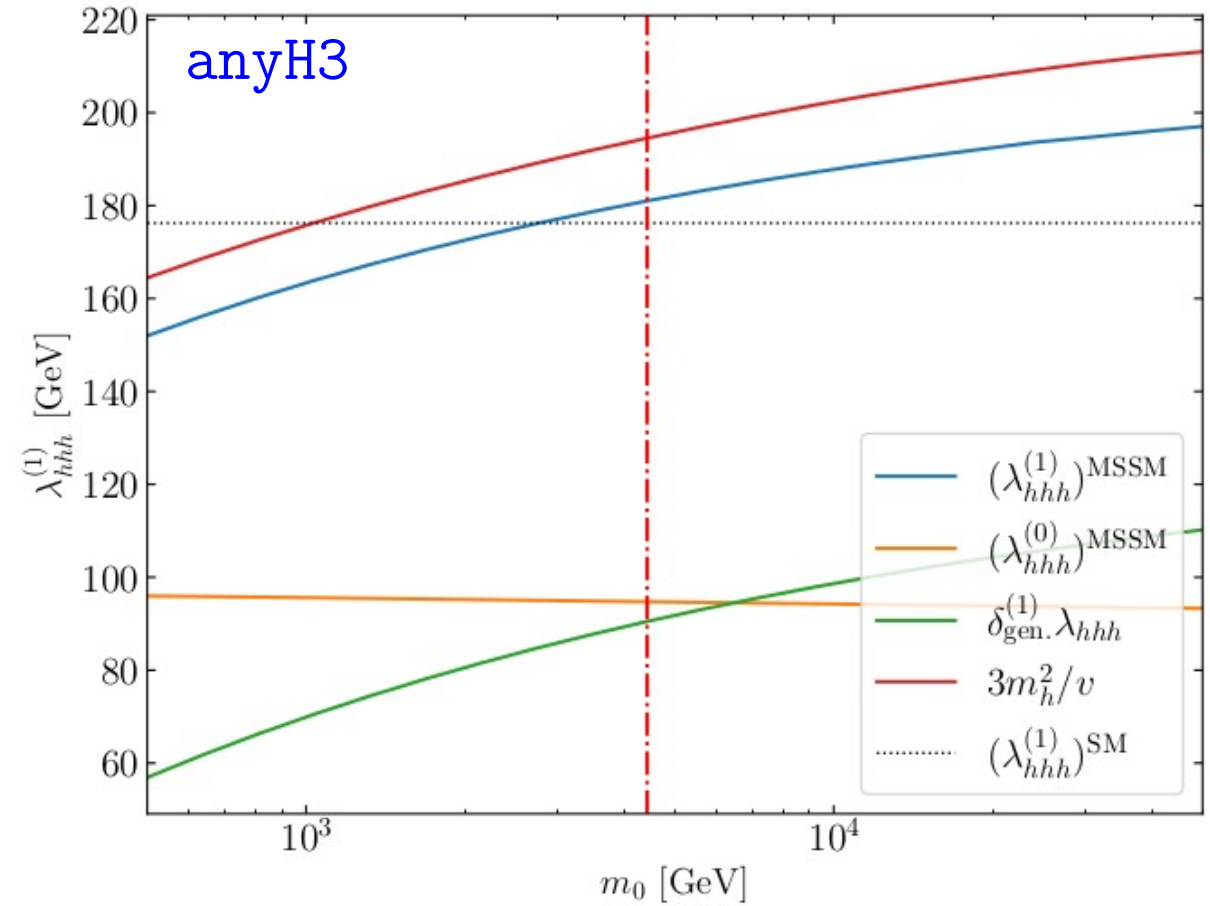
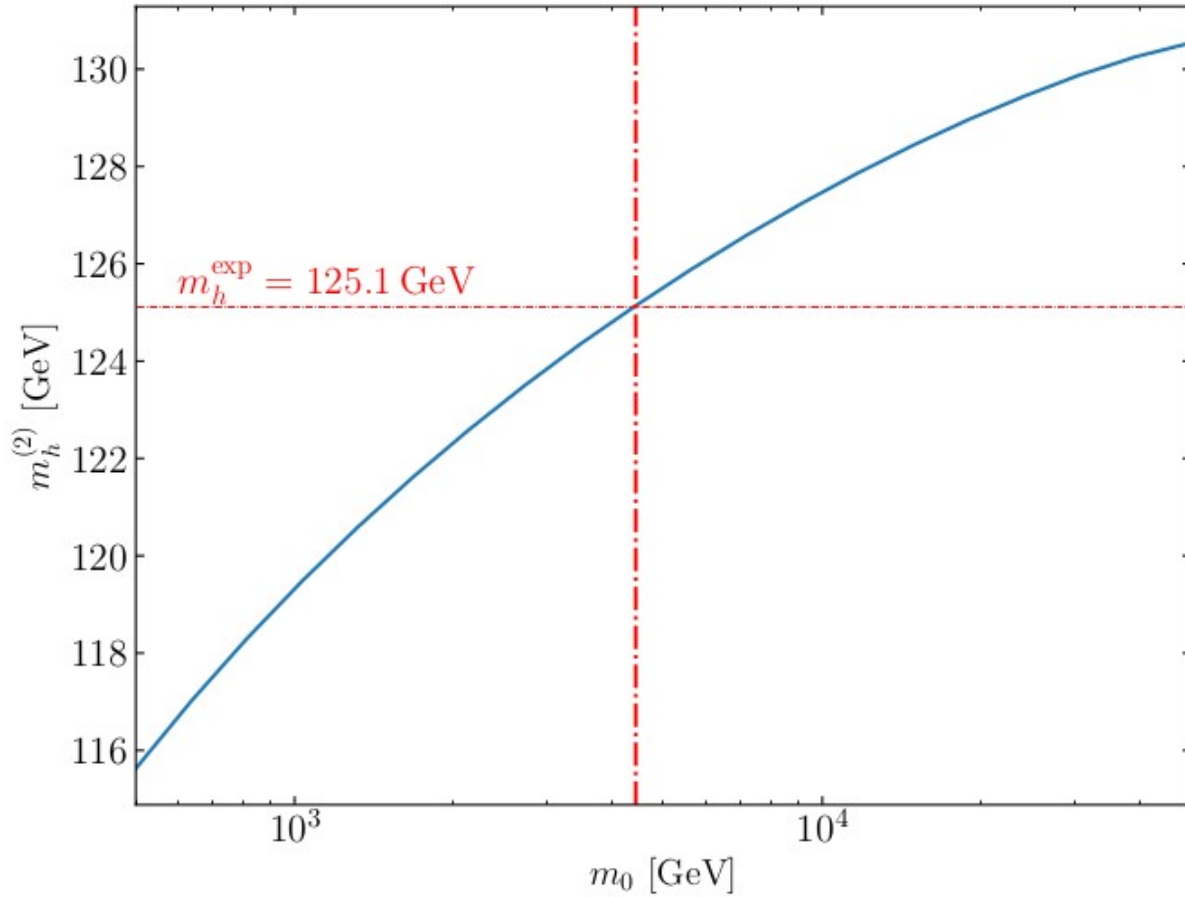
NTHDM: $m_{h_2} = 125.1$ GeV, $m_{h_1} = m_{h_3} = m_A = m_{H^\pm} = 300$ GeV, $\tilde{\mu} = 100$ GeV, $t_\beta = 2$



- **N2HDM = 2HDM + real singlet**
- CP-even sector: 3 states h_1, h_2, h_3 , with 3 mixing angles $\alpha_1, \alpha_2, \alpha_3$
- Here $\alpha_2 \rightarrow \pi/2 \rightarrow$ recover 2HDM (itself in alignment limit)
- We can study e.g. the relative sign of κ_λ and $\kappa_t \rightarrow$ affects double-Higgs production
- κ_t too far away from 1 excluded

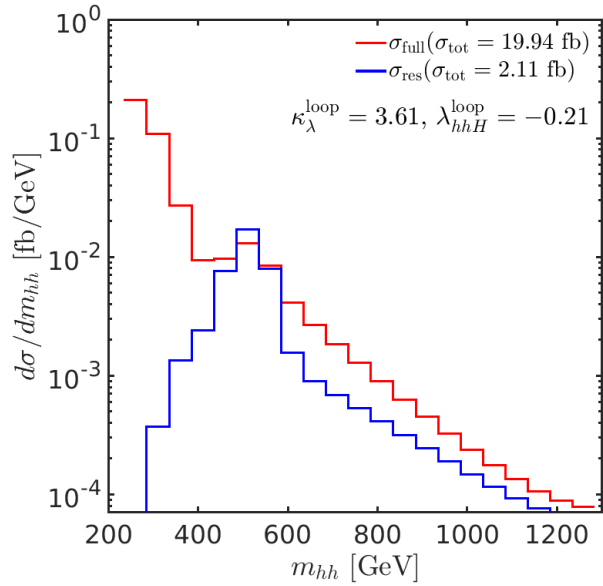
Full one-loop calculation of λ_{hhh} in the MSSM

CMSSM, $m_0 = m_{1/2} = -A_0$, $\tan\beta = 10$, $\text{sgn}(\mu) = 1$, with m_h computed at 2L in SPheno



- Example for a very simple version of the constrained MSSM → BSM parameters m_0 , $m_{1/2}$, A_0 , $\text{sgn}(\mu)$, $\tan\beta$
- For each point, M_h computed at 2L with SPheno, and SLHA output of SPheno used as input of anyH3

Ongoing developments in anyBSM



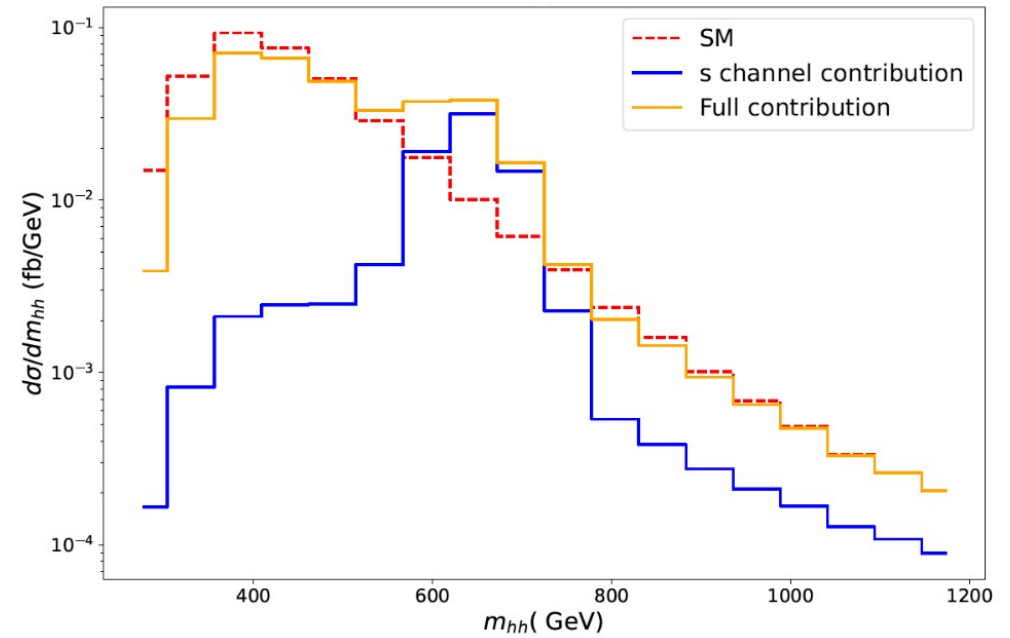
Left: 2HDM

[Heinemeyer, Mühlleitner, Radchenko Serdula, Weiglein '24]

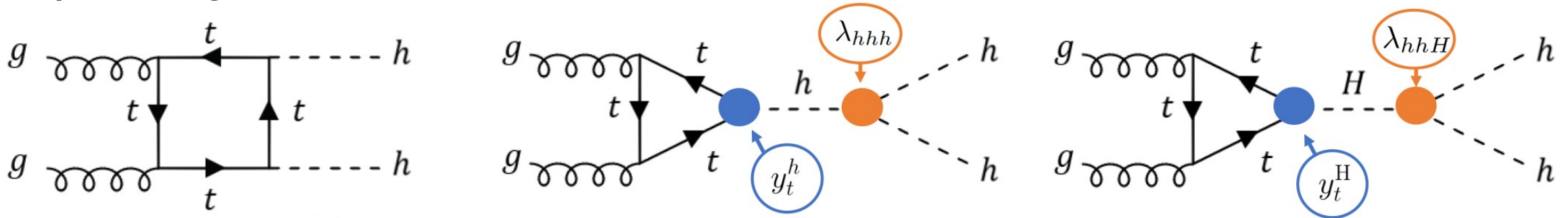
plot from talk of K. Radchenko Serdula at 20th LHC Higgs WG workshop

Right: singlet extension

[Arco, Heinemeyer, Mühlleitner, Rivero, Verduras WIP]



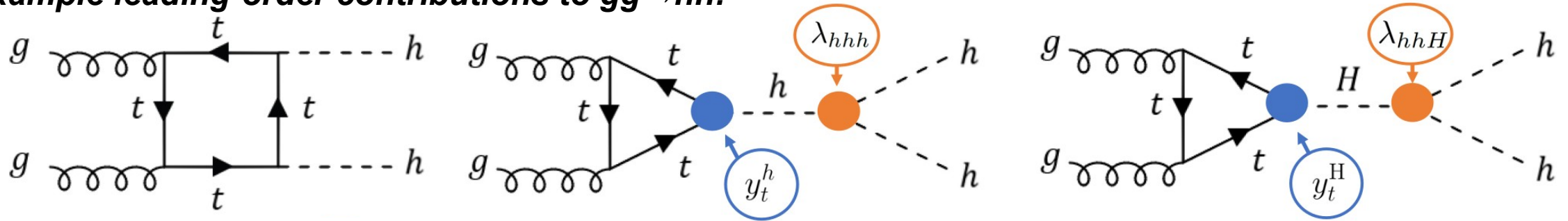
Example leading-order contributions:



[Figure by A. Verduras]

Ongoing developments in anyBSM: anyLambdaijk and anyHH

Example leading-order contributions to $gg \rightarrow hh$:

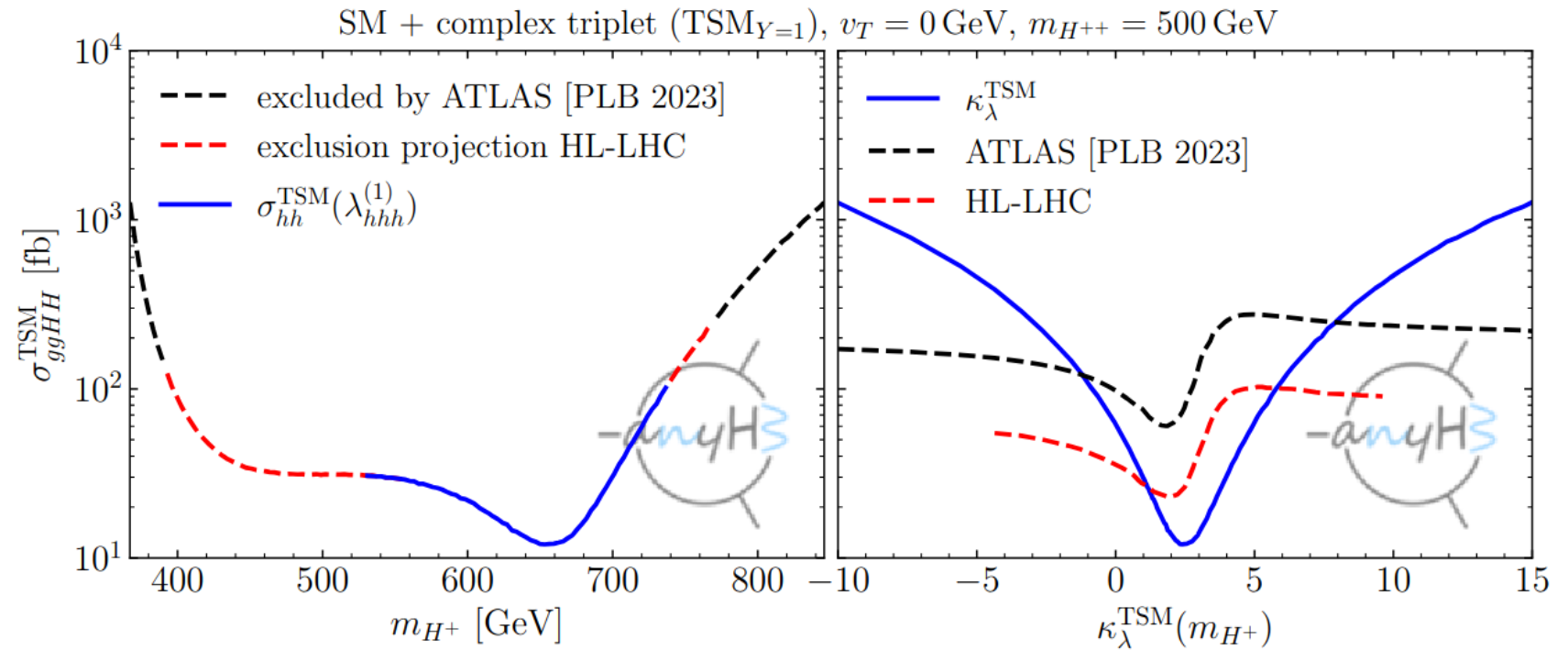


[Diagrams by A. Verduras Schaeidt]

Having predictions for di-Higgs production, including **all (i.e. resonant + non-resonant) contributions + 1L corrections to trilinear scalar couplings in arbitrary models** would be highly desirable

→ new modules anyLambdaijk and anyHH

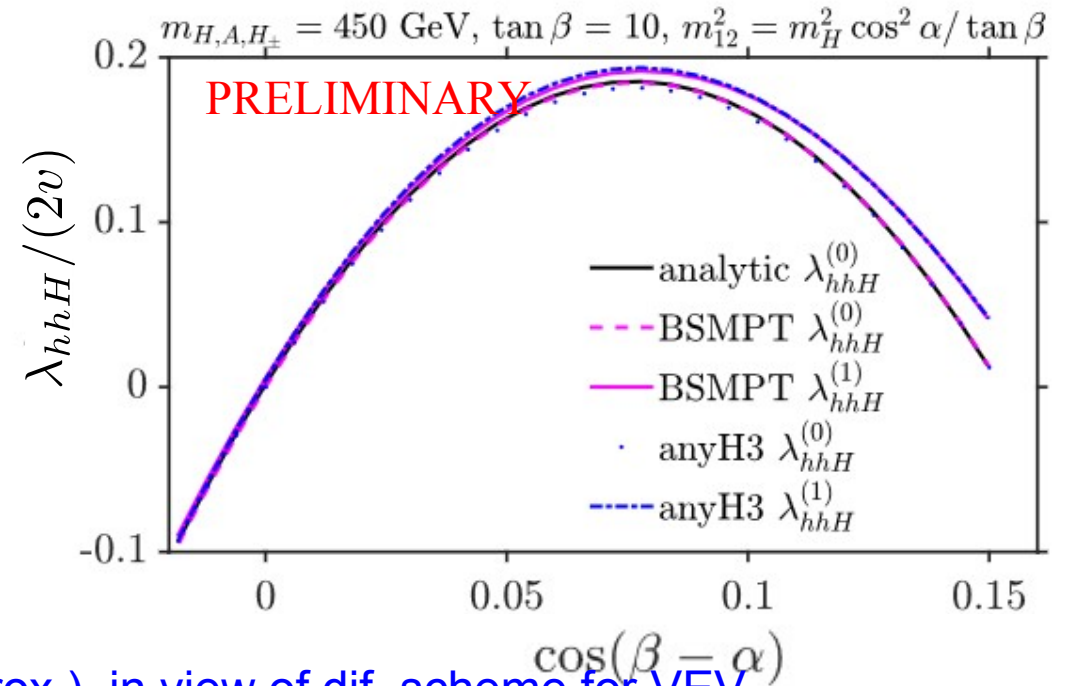
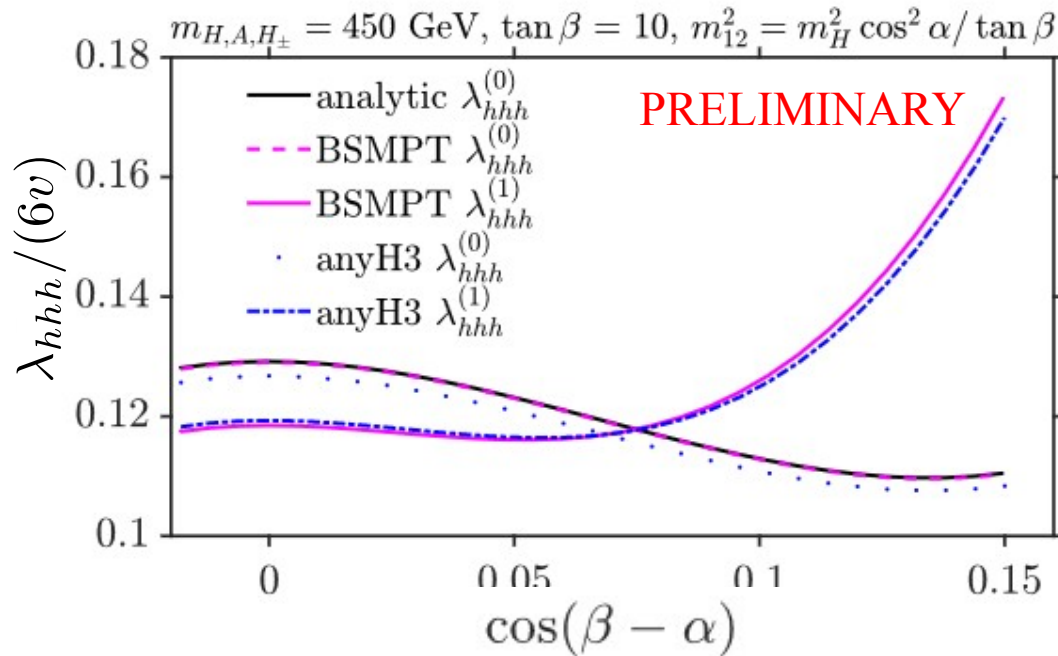
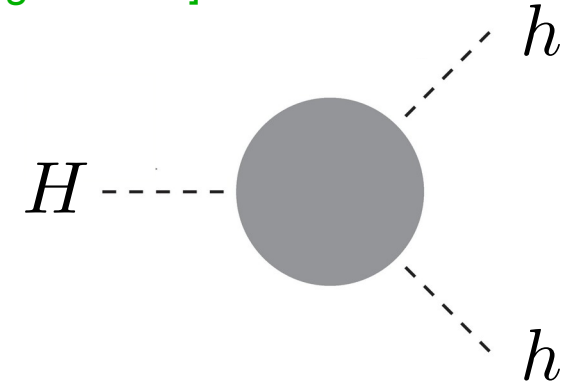
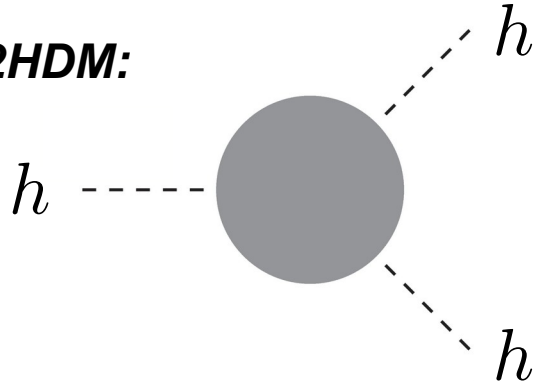
[Bahl, Braathen, Gabelmann, Radchenko Serdula, GW WIP]



Ongoing developments: anyLami_{jk}

[Bahl, JB, Gabelmann, Radchenko Serdula, Weiglein *WIP*]

Example in a 2HDM:



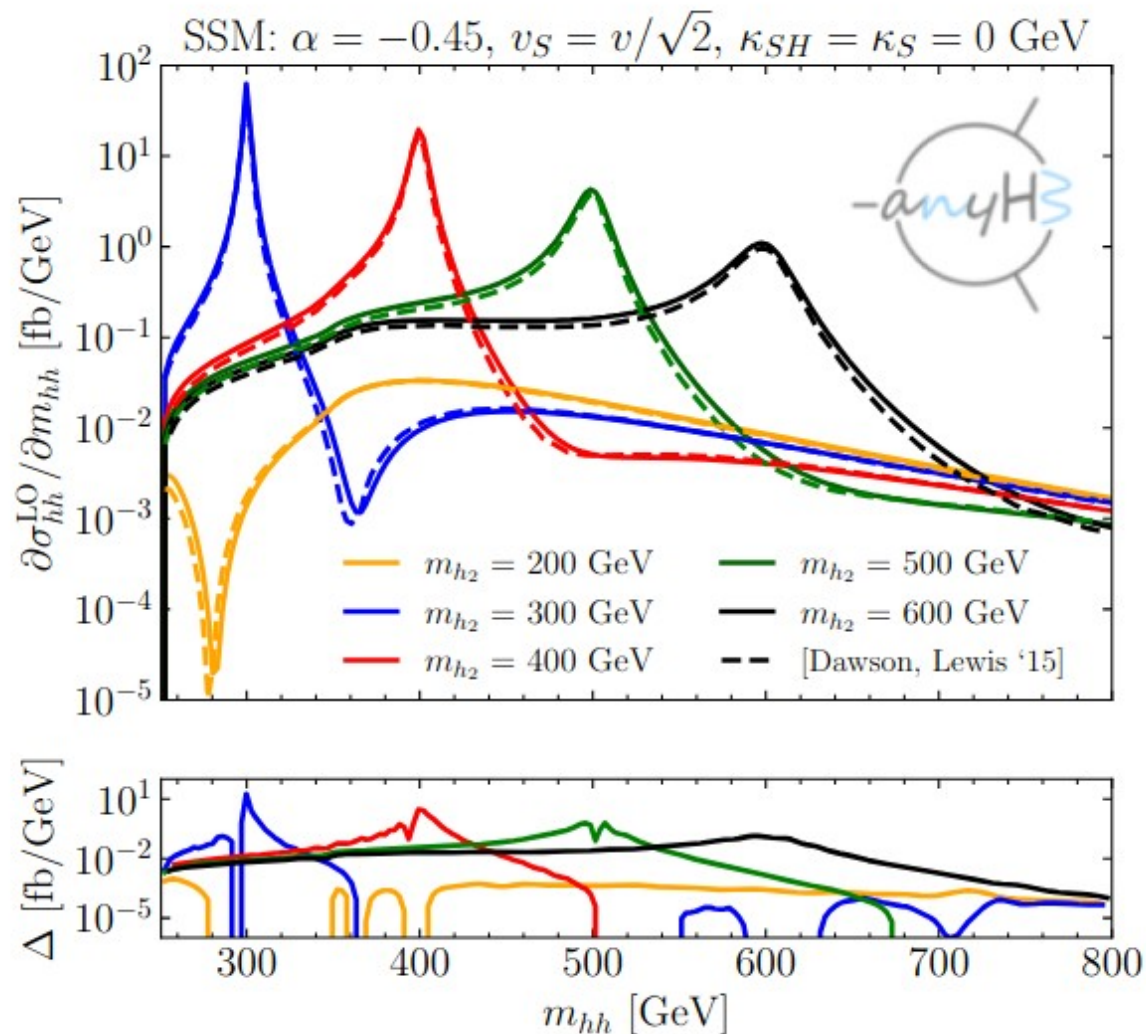
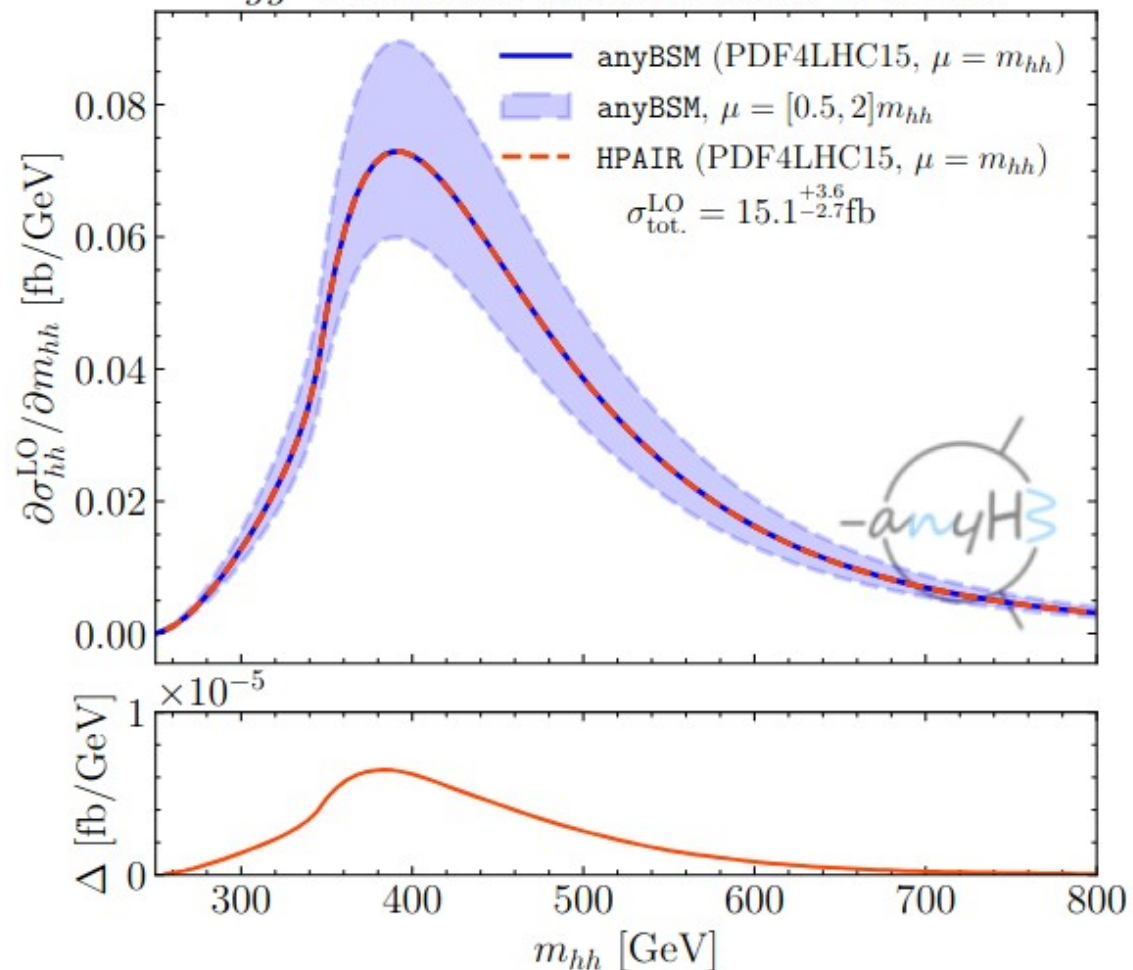
→ excellent agreement with BSMPT results (in eff. pot. approx.), in view of dif. scheme for VEV

→ full OS schemes for λ_{hhh} and λ_{hhH} couplings worked out in 2HDM [Bahl, JB, Gabelmann, Radchenko Serdula, Weiglein], RxSM [JB, Heinemeyer, Verduras Schaeidt], and more [Bosse, JB, Gabelmann, Hannig, Weiglein]!

Ongoing developments: tests of anyHH with leading order trilinear couplings

$$\Delta \equiv \left| \partial\sigma_{hh}^{\text{LO}} / \partial m_{hh}(\text{HPAIR}) - \partial\sigma_{hh}^{\text{LO}} / \partial m_{hh}(\text{anyHH}) \right|$$

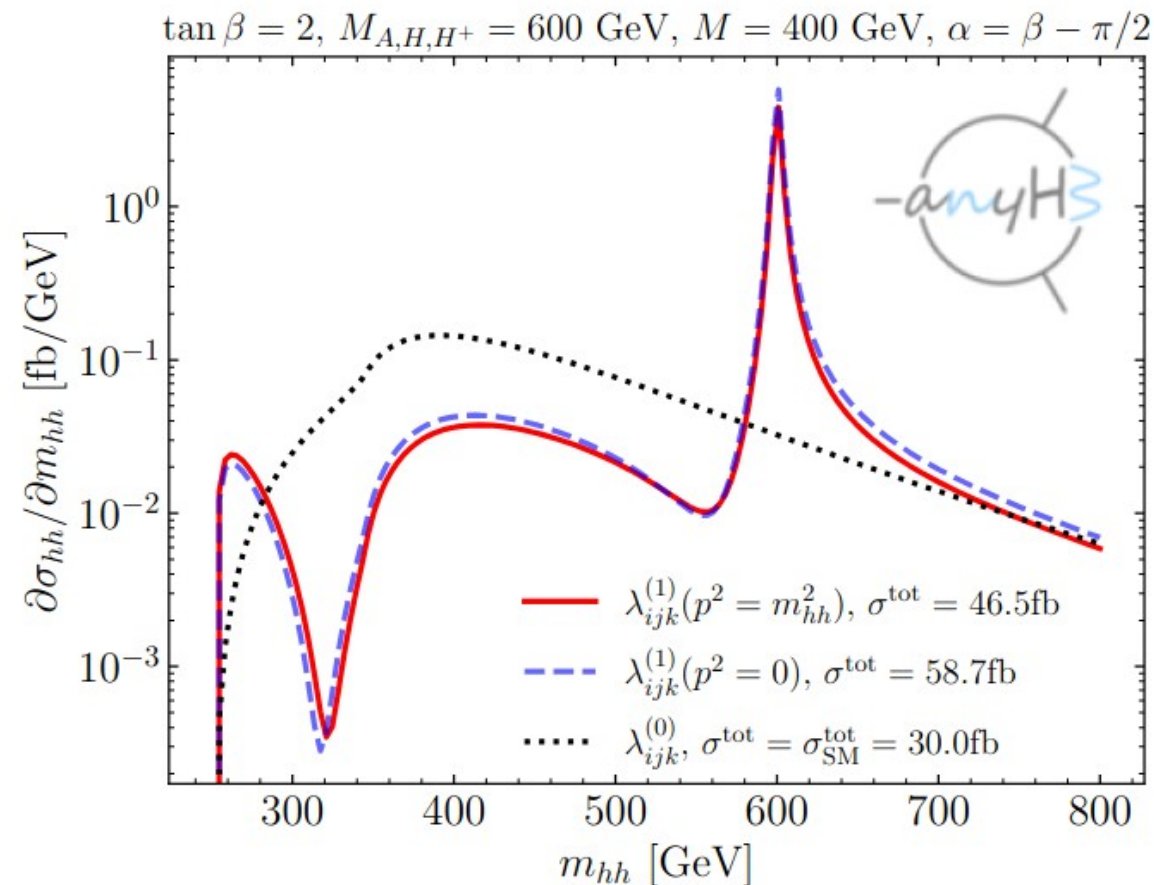
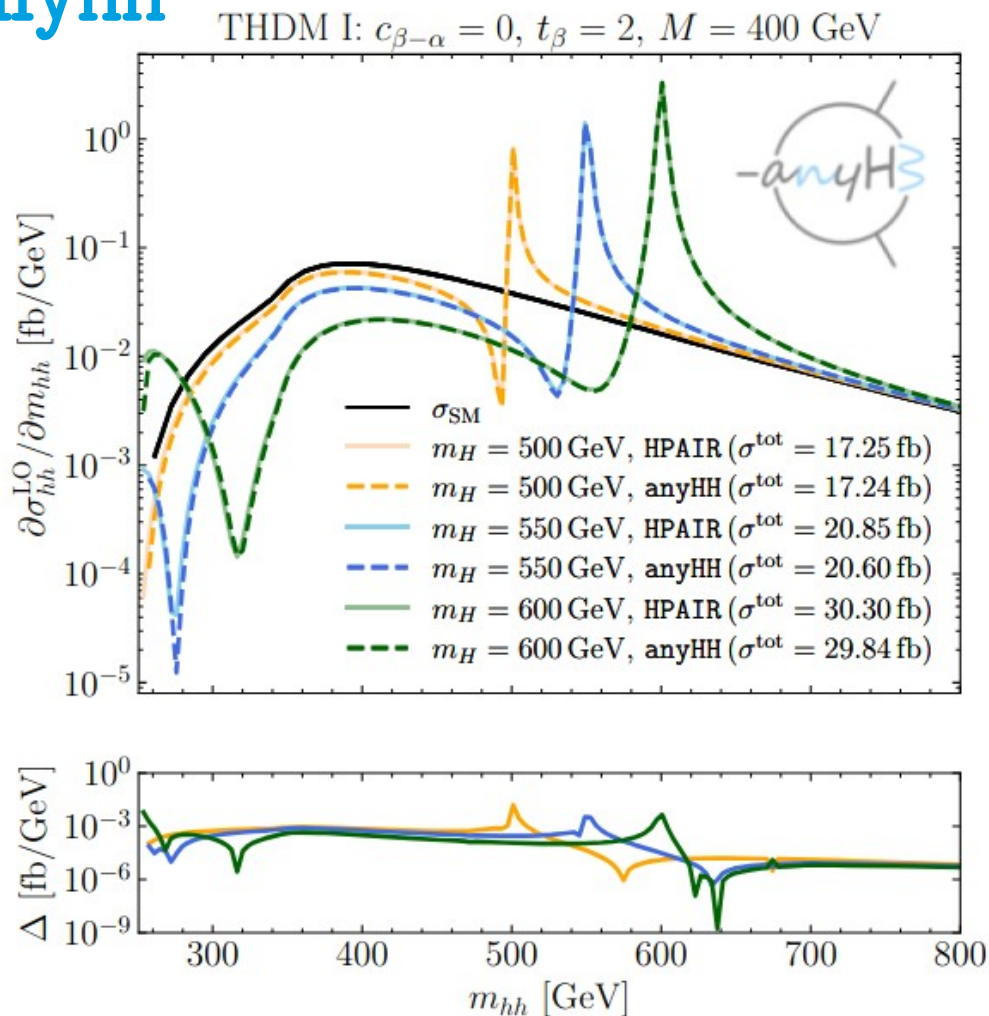
$gg \rightarrow hh$ in the Standard Model @ 14 TeV



- Excellent agreement with LO HPAIR result, once one ensures that running of α_s + choice of PDFs are same

- Very good agreement results of [Dawson, Lewis '15] for singlet extension of SM (remaining difference because PDF sets can't be taken to be the same)

Ongoing developments: tests and new results in 2HDM with anyHH



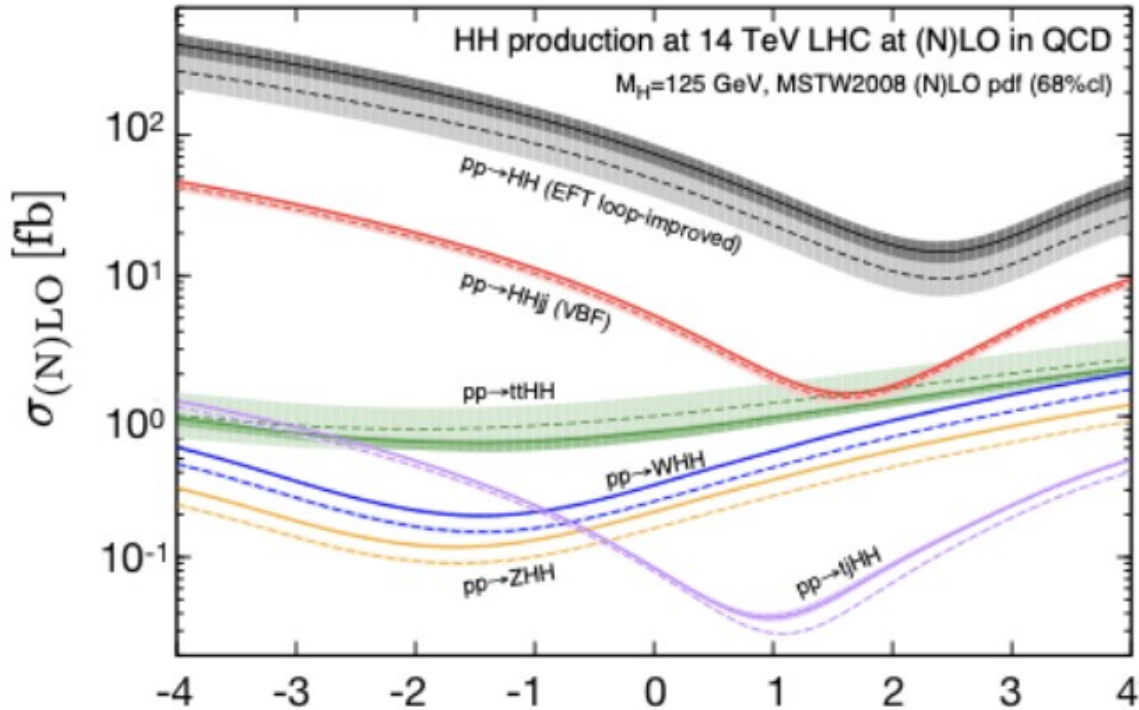
Very good agreement with HPAIR, using one-loop trilinear scalar couplings computed by anyH3/anyLambdaijk, for 2HDM benchmarks (here in alignment limit)

- Strong impact of inclusion of one-loop corrections to trilinear scalar couplings on differential distribution
- Impact of momentum dependence of trilinear scalar couplings (only possible with anyHH, not with HPAIR) can be as large as 20% on total cross-section

Di-Higgs production cross-sections as a function of λ_{hhh}

Plots taken from
[de Blas et al., 1905.03764]

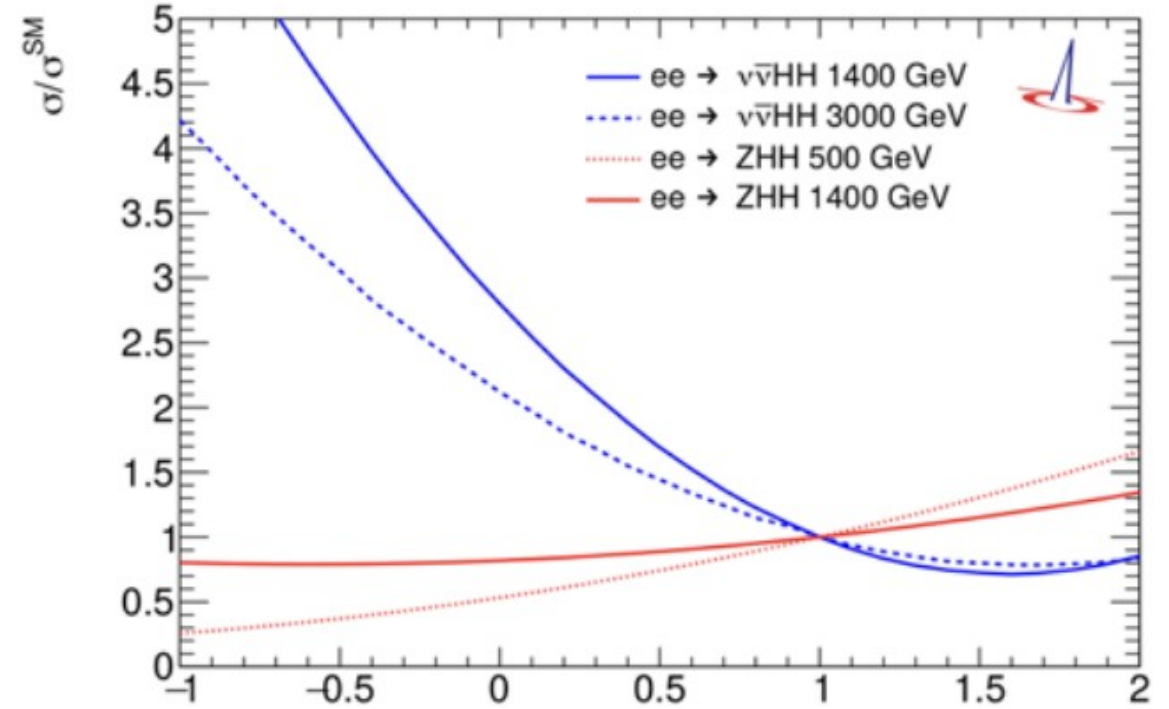
Hadron collider



[Frederix et al., 1401.7340]

$$\lambda_3/\lambda_3^{SM} = \kappa_\lambda$$

e^+e^- collider



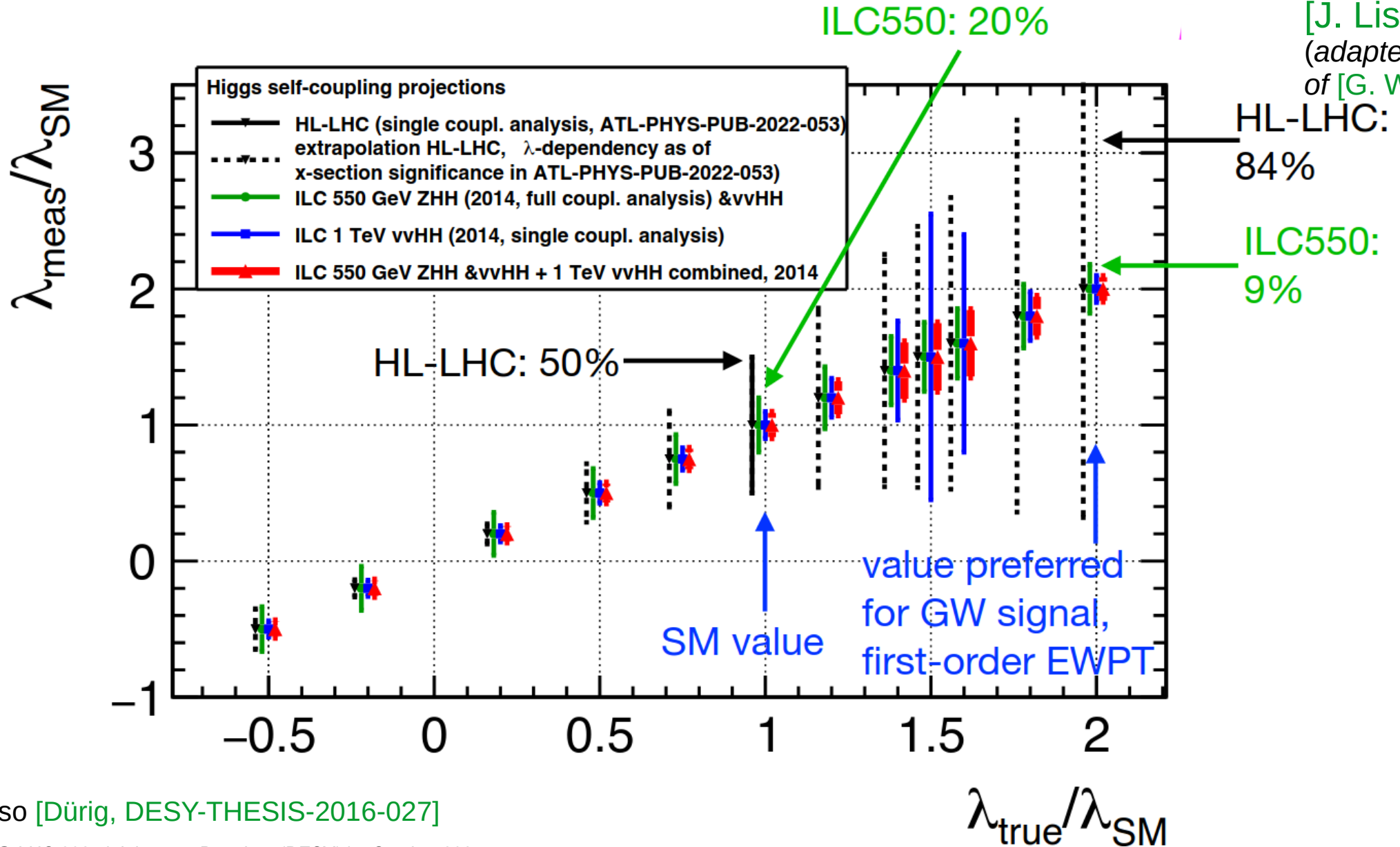
$$\lambda_3/\lambda_3^{SM} = \kappa_\lambda$$



- **BSM deviation in κ_λ modifies the interference between different contributions to di-Higgs production**
- Strong impact on total cross-sections (and also on differential distributions, see later slides)

Precision on the determination of λ_{hhh} as a function of λ_{hhh}

[J. List et al '24]
(adapted from slide of [G. Weiglein '24])



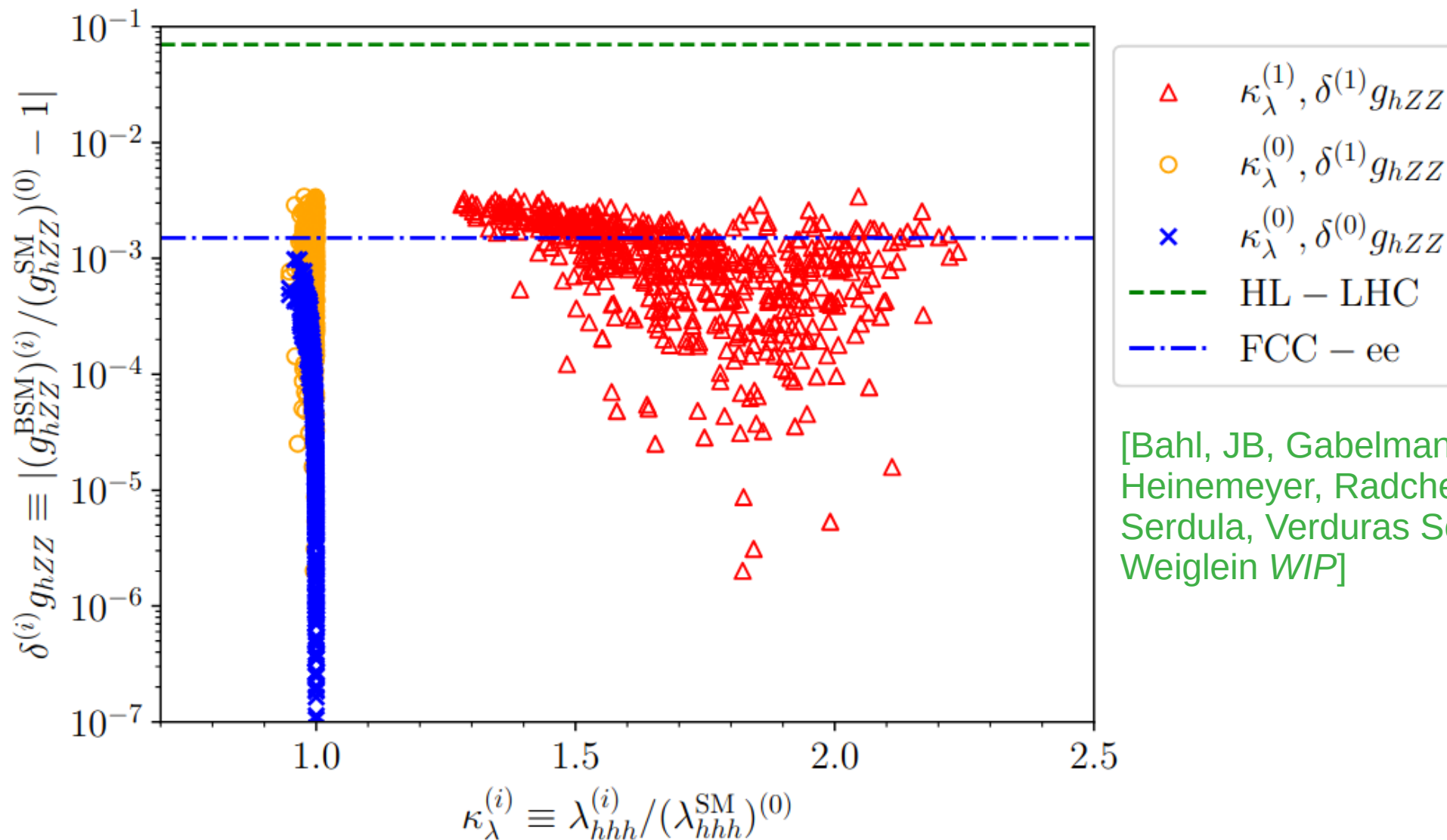
See also [Dürig, DESY-THESIS-2016-027]

Correlation between κ_λ and g_{hZZ} at tree level and one loop

Could BSM Physics be observed first in κ_λ ?

2HDM type II

All points shown here feature a strong first-order EWPT



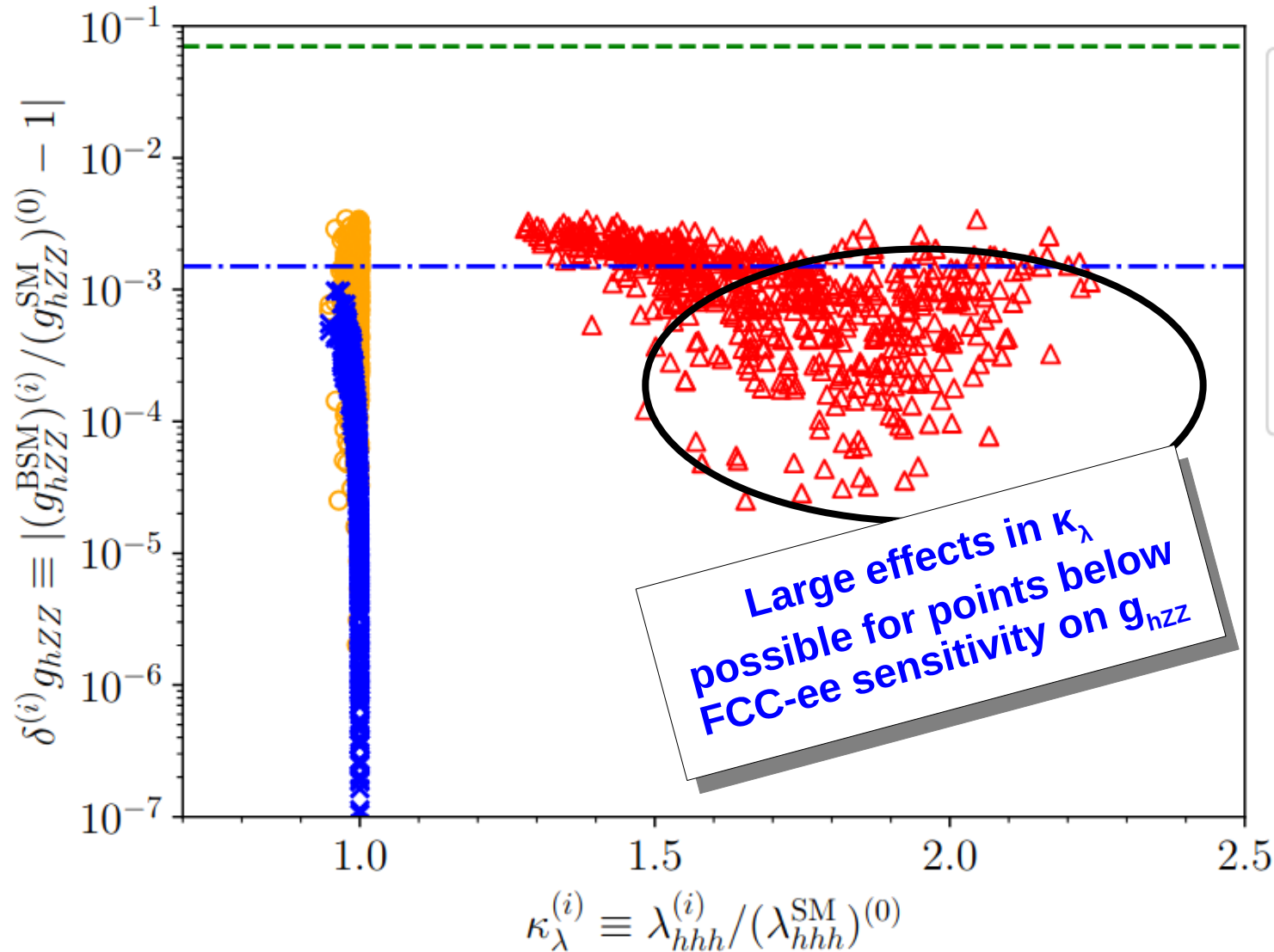
[Bahl, JB, Gabelmann, Heinemeyer, Radchenko, Serdula, Verduras Schaeidt, Weiglein *WIP*]

Correlation between κ_λ and g_{hZZ} at tree level and one loop

Could BSM Physics be observed first in κ_λ ?

2HDM type II

All points shown here feature a strong first-order EWPT



[Bahl, JB, Gabelmann, Heinemeyer, Radchenko, Serdula, Verduras Schaeidt, Weiglein WIP]

A word on EFTs

Effects in κ_λ much larger than in other Higgs couplings can also be understood in terms of EFT/dimensional analysis

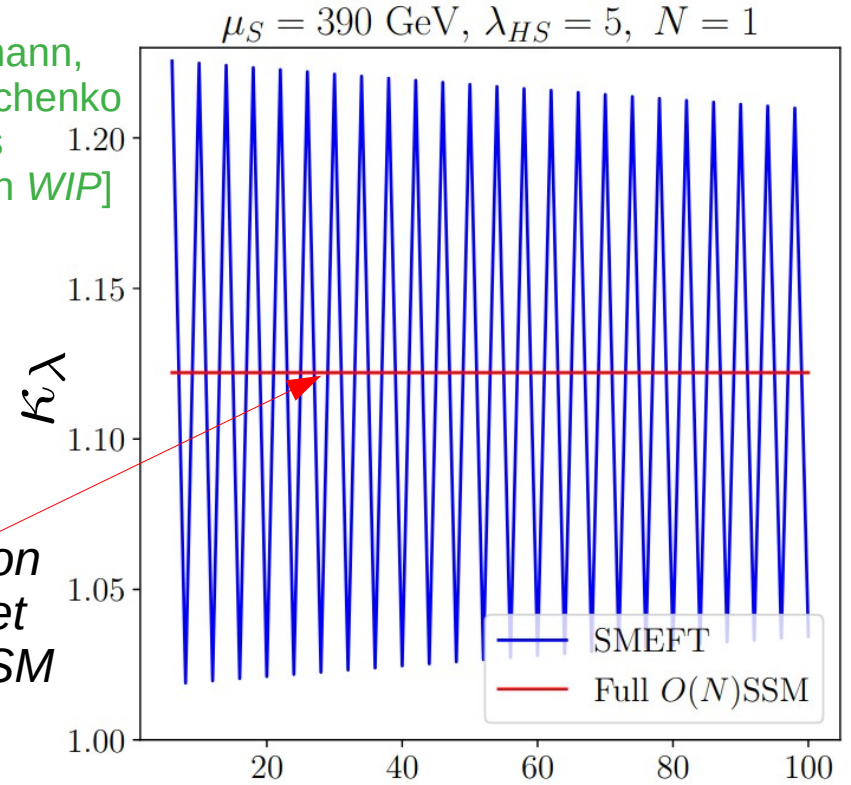
See e.g. [Durieux, McCullough, Salvioni 2022] and [McCullough @ LCWS'24]

$$\left| \frac{\delta_{h^3}}{\delta_{hVV}} \right| \lesssim \min \left\{ \left(\frac{4\pi v}{m_h} \right)^2, \left(\frac{M_{\text{BSM}}}{m_h} \right)^2 \right\}$$

Deviation in λ_{hhh} ~ 600
 Deviation in g_{hVV}

E.g. an additional scalar of $M \sim 300\text{-}500$ GeV is not necessarily excluded by experimental searches, but is also not well captured by SMEFT!
 → one should use **Higgs EFT** (HEFT) instead

[Bahl, JB, Gabelmann, Heinemeyer, Radchenko, Serdula, Verduras, Schaeidt, Weiglein *WIP*]



Full calculation (1L) in singlet extension of SM

But beware also about the **range of applicability** of different EFTs!

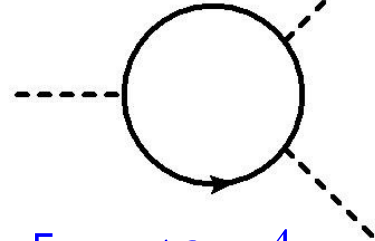
$$\mathcal{L}_{\text{SMEFT}} \supset \sum_{n>3} c^{(2n)} \frac{|\Phi|^{2n}}{\Lambda^{2n-4}}$$

n
 Order to which we do the calculation in SMEFT

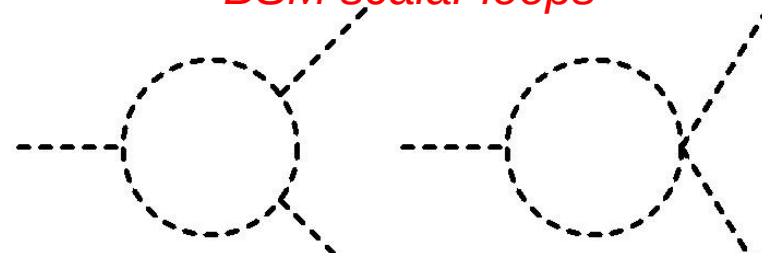
One-loop mass-splitting effects

- Leading one-loop corrections to λ_{hhh} in models with extended sectors (like 2HDM):

SM top quark loop



BSM scalar loops



$$\delta^{(1)} \lambda_{hhh} \supset \frac{1}{16\pi^2} \left[-\frac{48m_t^4}{v^3} + \sum_{\Phi} \frac{4n_{\Phi} m_{\Phi}^4}{v^3} \left(1 - \frac{\mathcal{M}^2}{m_{\Phi}^2} \right)^3 \right]$$

First found in 2HDM:
[Kanemura, Kiyoura,
Okada, Senaha, Yuan '02]

\mathcal{M} : BSM mass scale, e.g. soft breaking scale M of Z_2 symmetry in 2HDM

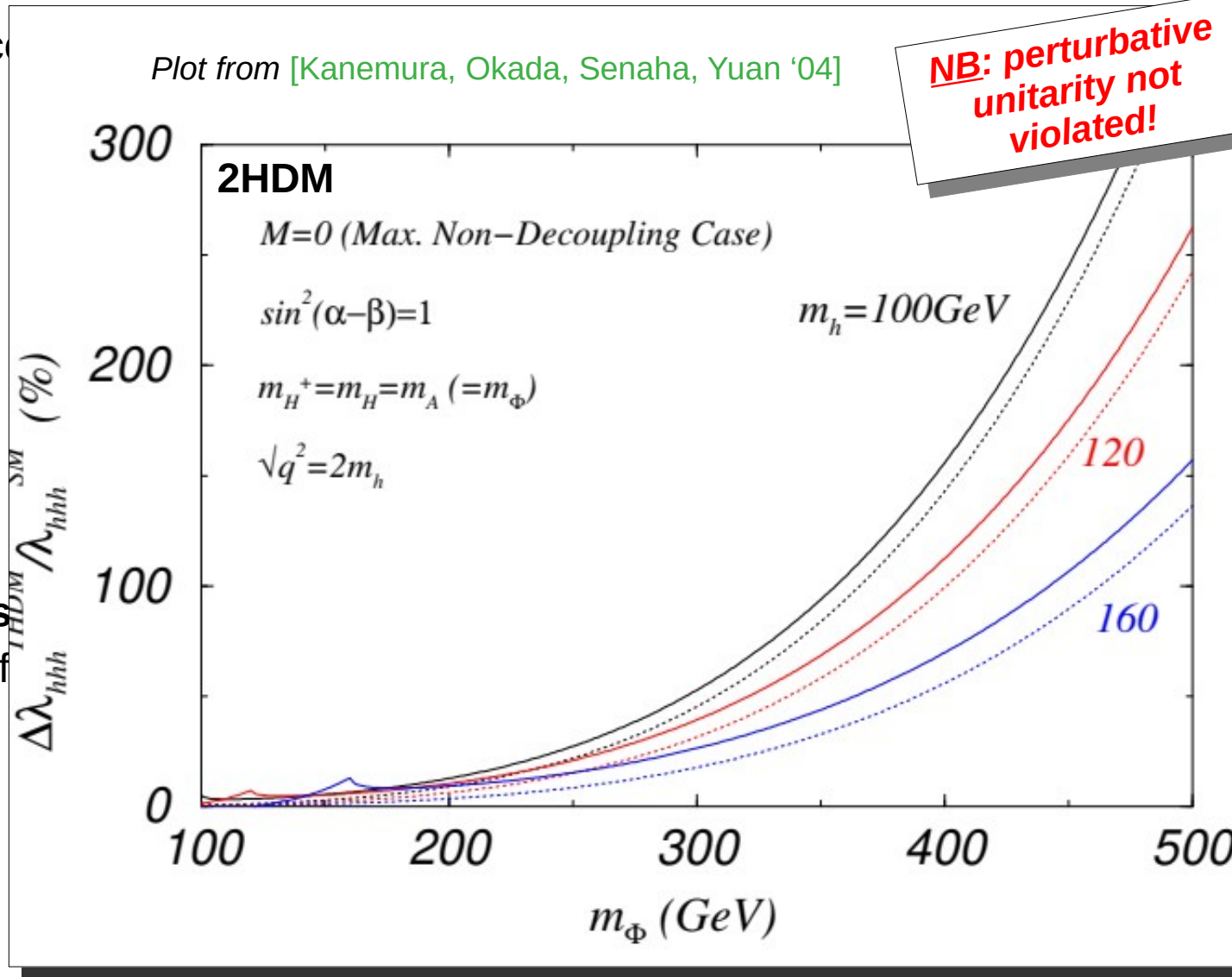
n_{Φ} : # of d.o.f of field Φ

- Size of new effects depends on how the BSM scalars acquire their mass: $m_{\Phi}^2 \sim \mathcal{M}^2 + \tilde{\lambda}v^2$

$$\left(1 - \frac{\mathcal{M}^2}{m_{\Phi}^2} \right)^3 \longrightarrow \begin{cases} 0, & \text{for } \mathcal{M}^2 \gg \tilde{\lambda}v^2 \\ 1, & \text{for } \mathcal{M}^2 \ll \tilde{\lambda}v^2 \end{cases} \longrightarrow \text{Huge BSM effects possible!}$$

One-loop mass-splitting effects

Leading one-loop c



First found in 2HDM:
 [Kanemura, Kiyoura,
 Okada, Senaha, Yuan '02]

$$\delta^{(1)} \lambda_{hhh} \supset$$

\mathcal{M} : BSM mass
 n_Φ : # of d.o.f of

Size of new effects

$$\lambda^2 + \tilde{\lambda} v^2$$

Huge BSM effects possible!

Two-loop calculation of λ_{hhh}

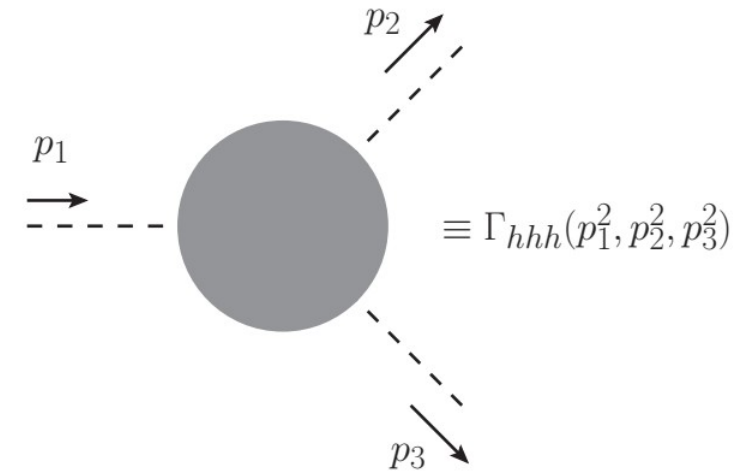
Goal: How large can the two-loop corrections to λ_{hhh} become?

Based on

[arXiv:1903.05417 \(PLB\)](#) and [arXiv:1911.11507 \(EPJC\)](#) in collaboration with Shinya Kanemura

An effective Higgs trilinear coupling

- In principle: consider 3-point function Γ_{hhh}
but this is momentum dependent → **very difficult beyond one loop**



- Instead, consider an **effective trilinear coupling**

$$\lambda_{hhh} \equiv \left. \frac{\partial^3 V_{\text{eff}}}{\partial h^3} \right|_{\text{min}}$$

entering the coupling modifier

$$\kappa_\lambda = \frac{\lambda_{hhh}}{(\lambda_{hhh}^{(0)})^{\text{SM}}} \quad \text{with } (\lambda_{hhh}^{(0)})^{\text{SM}} = \frac{3m_h^2}{v}$$

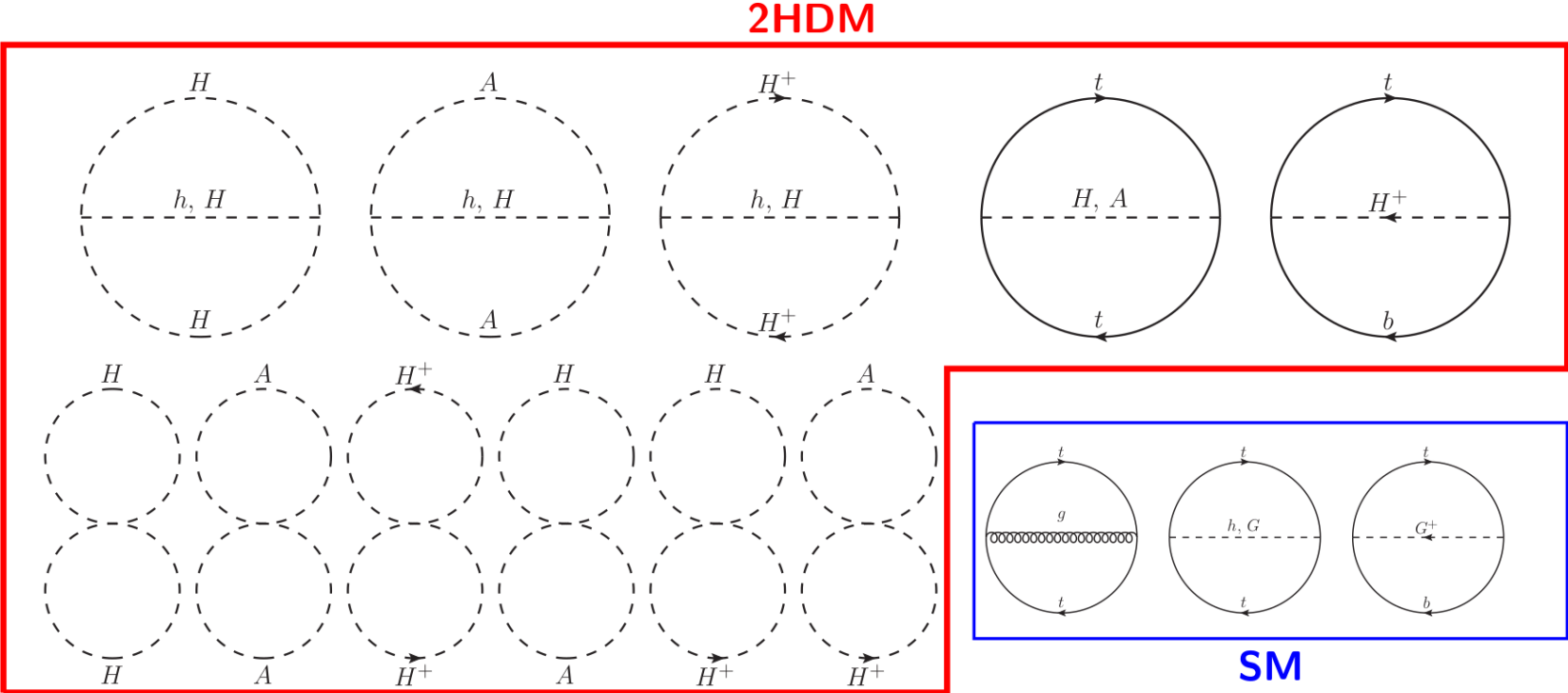
constrained by experiments (*applicability of this assumption discussed later*)

Our effective-potential calculation

[JB, Kanemura '19]

➤ **Step 1:** compute $V_{\text{eff}} = V^{(0)} + \frac{1}{16\pi^2} V^{(1)} + \frac{1}{(16\pi^2)^2} V^{(2)}$ ($\overline{\text{MS}}$ result)

- ➔ $V^{(2)}$: 1PI vacuum bubbles
- ➔ *Dominant BSM contributions to $V^{(2)}$* = diagrams involving **heavy BSM scalars and top quark**
- ➔ **Neglect masses of light states** (SM-like Higgs, light fermions, ...)



Our effective-potential calculation

[JB, Kanemura '19]

➤ **Step 1:** compute $V_{\text{eff}} = V^{(0)} + \frac{1}{16\pi^2} V^{(1)} + \frac{1}{(16\pi^2)^2} V^{(2)}$ ($\overline{\text{MS}}$ result)

➔ $V^{(2)}$: 1PI vacuum bubbles

➔ *Dominant BSM contributions to $V^{(2)}$* = diagrams involving **heavy BSM scalars and top quark**

➤ **Step 2:** derive an effective trilinear coupling

$$\lambda_{hhh} \equiv \left. \frac{\partial^3 V_{\text{eff}}}{\partial h^3} \right|_{\text{min.}} = \frac{3[M_h^2]_{V_{\text{eff}}}}{v} + \left[\frac{\partial^3}{\partial h^3} - \frac{3}{v} \left(\frac{\partial^2}{\partial h^2} - \frac{1}{v} \frac{\partial}{\partial h} \right) \right] \Delta V \Big|_{\text{min.}}$$

($\overline{\text{MS}}$ result too)

*Express tree-level
result in terms of
effective-potential
Higgs mass*

Our effective-potential calculation

[JB, Kanemura '19]

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→ $V^{(2)}$: 1PI vacuum bubbles

→ *Dominant BSM contributions to $V^{(2)}$* = diagrams involving **heavy BSM scalars and top quark**

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($\overline{\text{MS}}$ result too)

➤ **Step 3:** conversion from $\overline{\text{MS}}$ to OS scheme

→ Express result in terms of **pole masses**: M_t, M_h, M_Φ ($\Phi=H,A,H^\pm$); OS Higgs VEV $v_{\text{phys}} = \frac{1}{\sqrt{\sqrt{2}G_F}}$

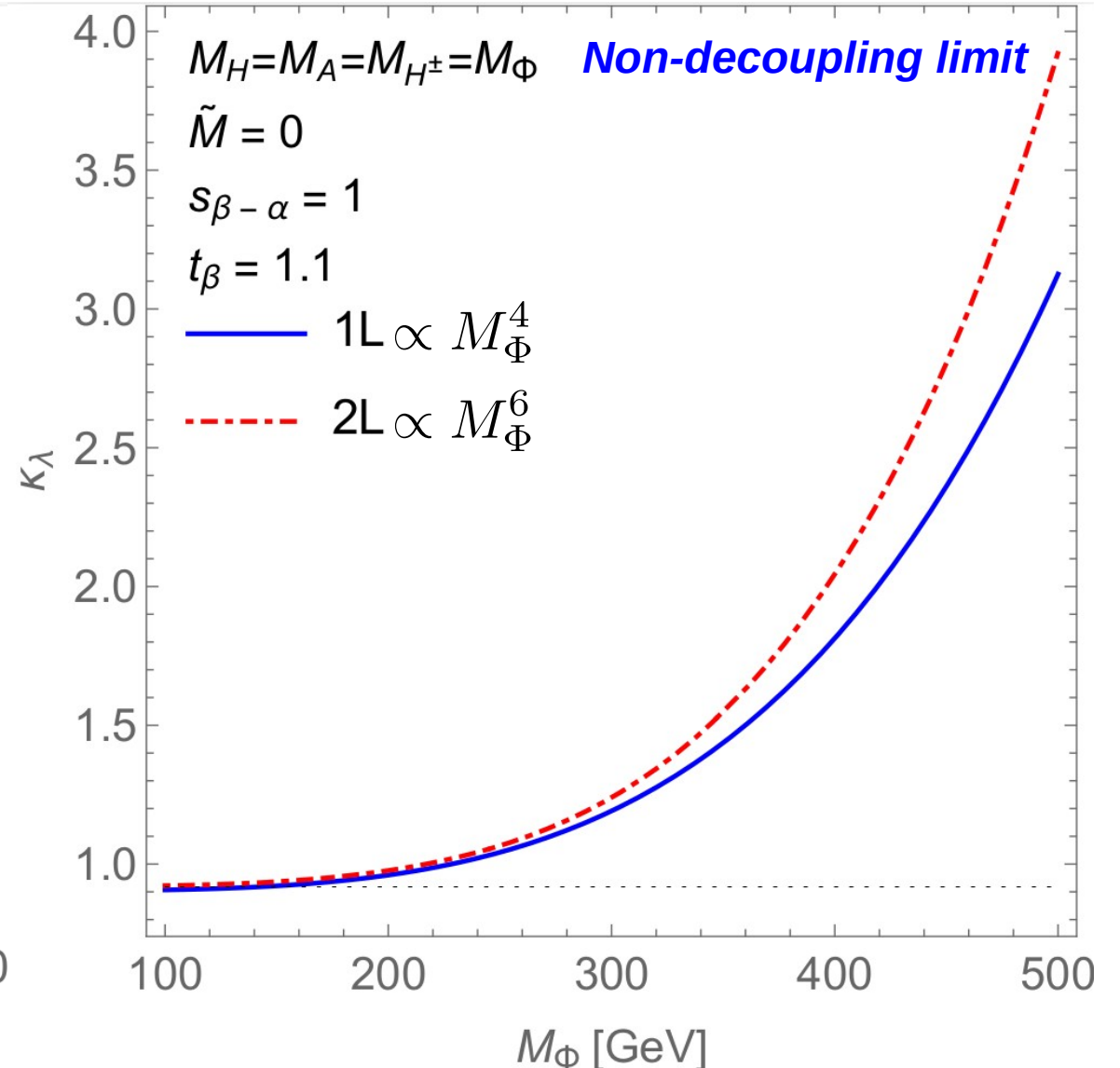
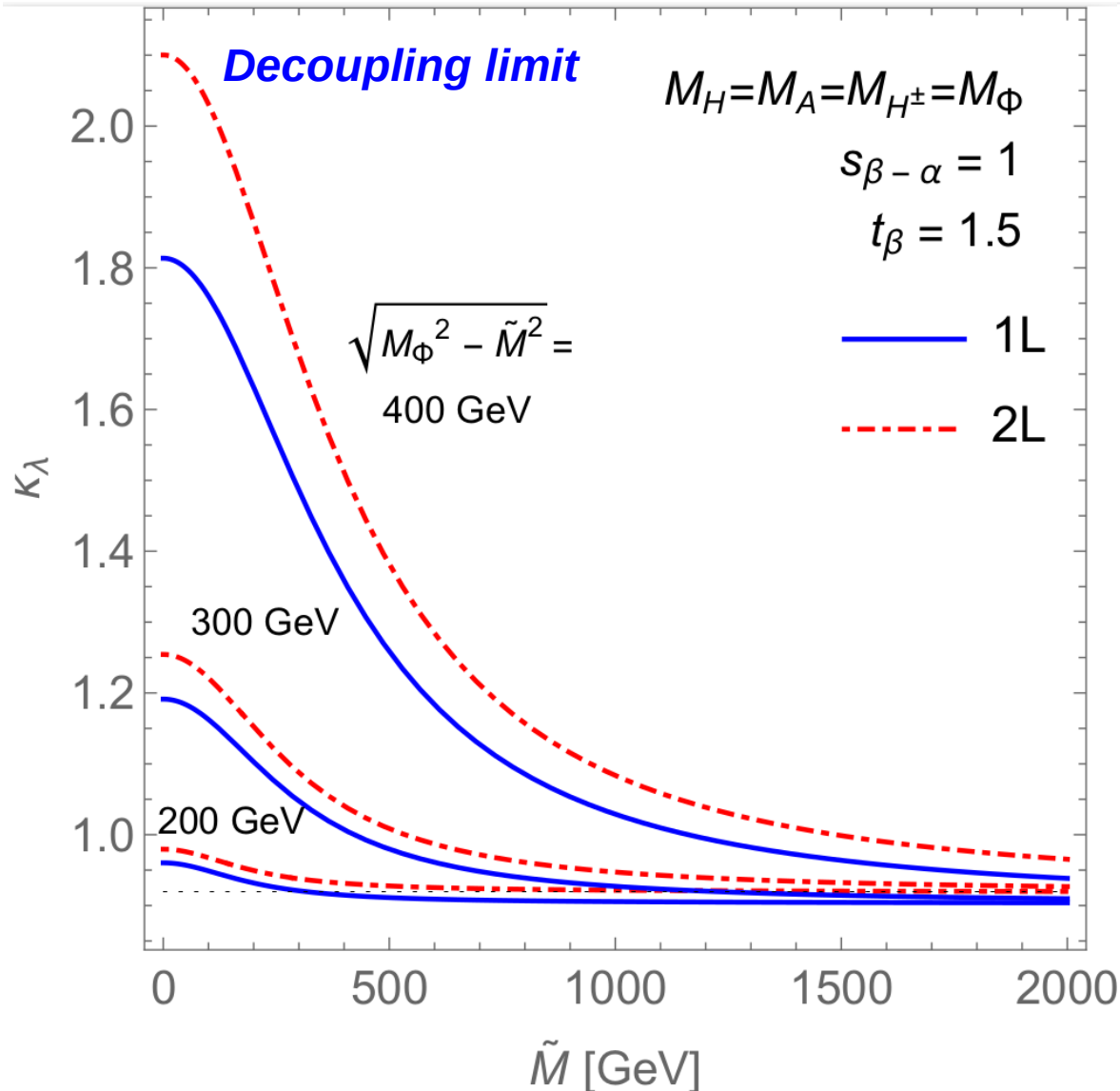
→ Include **finite WFR**: $\hat{\lambda}_{hhh} = (Z_h^{\text{OS}} / Z_h^{\overline{\text{MS}}})^{3/2} \lambda_{hhh}$

→ Prescription for M to ensure **proper decoupling** with $M_\Phi^2 = \tilde{M}^2 + \tilde{\lambda}_\Phi v^2$ and $\tilde{M} \rightarrow \infty$

Our results in the aligned 2HDM

[JB, Kanemura '19]

Taking degenerate BSM scalar masses: $M_\Phi = M_H = M_A = M_{H^\pm}$



$\overline{\text{MS}}$ to OS scheme conversion

- V_{eff} : we use expressions in MS scheme hence results for λ_{hhh} also in $\overline{\text{MS}}$ scheme
- We include finite counterterms to express the Higgs trilinear coupling in terms of physical quantities

$$\underbrace{m_X^2}_{\overline{\text{MS}}} = \underbrace{M_X^2}_{\text{pole}} - \Re[\Pi_{XX}^{\text{fin.}}(p^2 = M_X^2)], \quad v^2 = \underbrace{(\sqrt{2}G_F)^{-1}}_{\equiv v_{\text{OS}}^2} + \frac{3M_t^2}{16\pi^2} \left(2 \log \frac{M_t^2}{Q^2} - 1\right) + \dots$$

- Also we include finite WFR effects \rightarrow OS scheme

$$\underbrace{\hat{\lambda}_{hhh}}_{\text{OS}} = \underbrace{\left(\frac{Z_h^{\text{OS}}}{Z_h^{\overline{\text{MS}}}}\right)^{3/2}}_{\text{finite WFR}} \underbrace{\lambda_{hhh}}_{\overline{\text{MS}}} = - \underbrace{\Gamma_{hhh}(0, 0, 0)}_{\text{3-pt. func.}}$$

MS to OS scheme conversion

- ▶ OS result is obtained as

$$\hat{\lambda}_{hhh} = \underbrace{\left(\frac{Z_h^{\text{OS}}}{Z_h^{\overline{\text{MS}}}} \right)^{3/2}}_{\text{inclusion of WFR}} \times \underbrace{\lambda_{hhh}}_{\substack{\overline{\text{MS}} \text{ parameters} \\ \text{replaced by OS ones}}}$$

- ▶ Let's suppose (for simplicity) that λ_{hhh} only depends on one parameter x , as

$$\lambda_{hhh} = f^{(0)}(x^{\overline{\text{MS}}}) + \kappa f^{(1)}(x^{\overline{\text{MS}}}) + \kappa^2 f^{(2)}(x^{\overline{\text{MS}}}) \quad \left(\kappa = \frac{1}{16\pi^2} \right)$$

and

$$x^{\overline{\text{MS}}} = X^{\text{OS}} + \kappa \delta^{(1)} x + \kappa^2 \delta^{(2)} x$$

then in terms of OS parameters

$$\lambda_{hhh} = f^{(0)}(X^{\text{OS}}) + \kappa \left[f^{(1)}(X^{\text{OS}}) + \cancel{\frac{\partial f^{(0)}}{\partial x}(X^{\text{OS}}) \delta^{(1)} x} \right] \\ + \kappa^2 \left[f^{(2)}(X^{\text{OS}}) + \frac{\partial f^{(1)}}{\partial x}(X^{\text{OS}}) \delta^{(1)} x + \cancel{\frac{\partial f^{(0)}}{\partial x}(X^{\text{OS}}) \delta^{(2)} x} + \cancel{\frac{\partial^2 f^{(0)}}{\partial x^2}(X^{\text{OS}}) (\delta^{(1)} x)^2} \right]$$

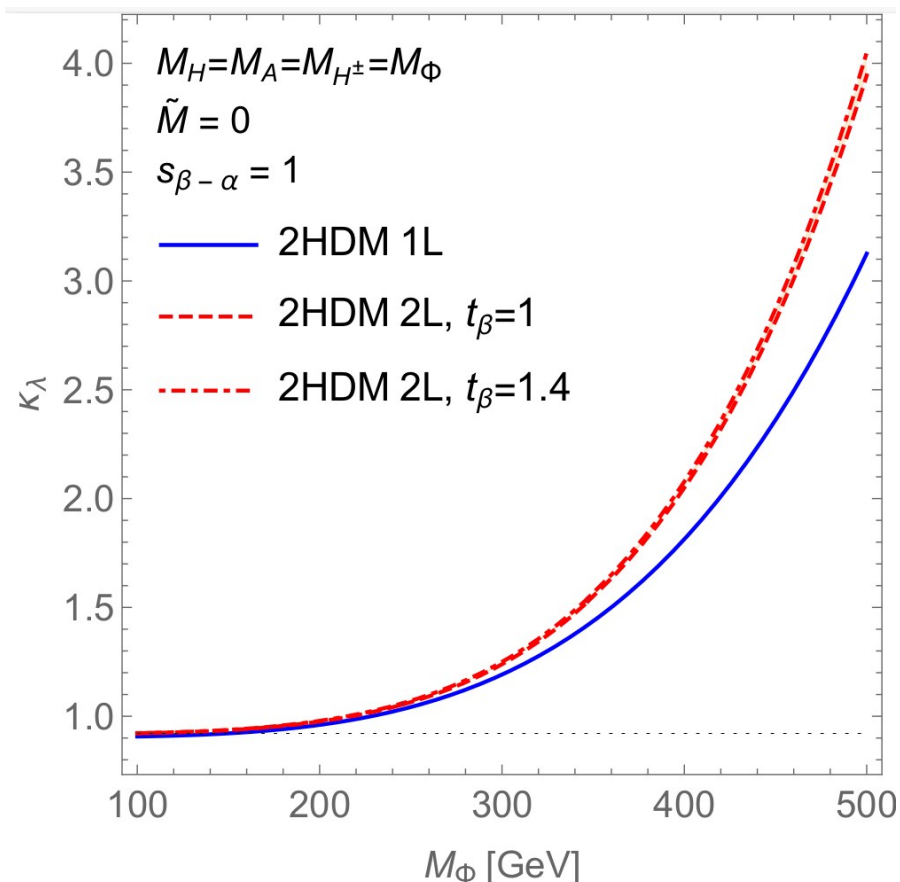
because we neglect m_h in the loop corrections and $\lambda_{hhh}^{(0)} = 3m_h^2/v$ (in absence of mixing)

λ_{hhh} at two loops in more models

[JB, Kanemura '19]

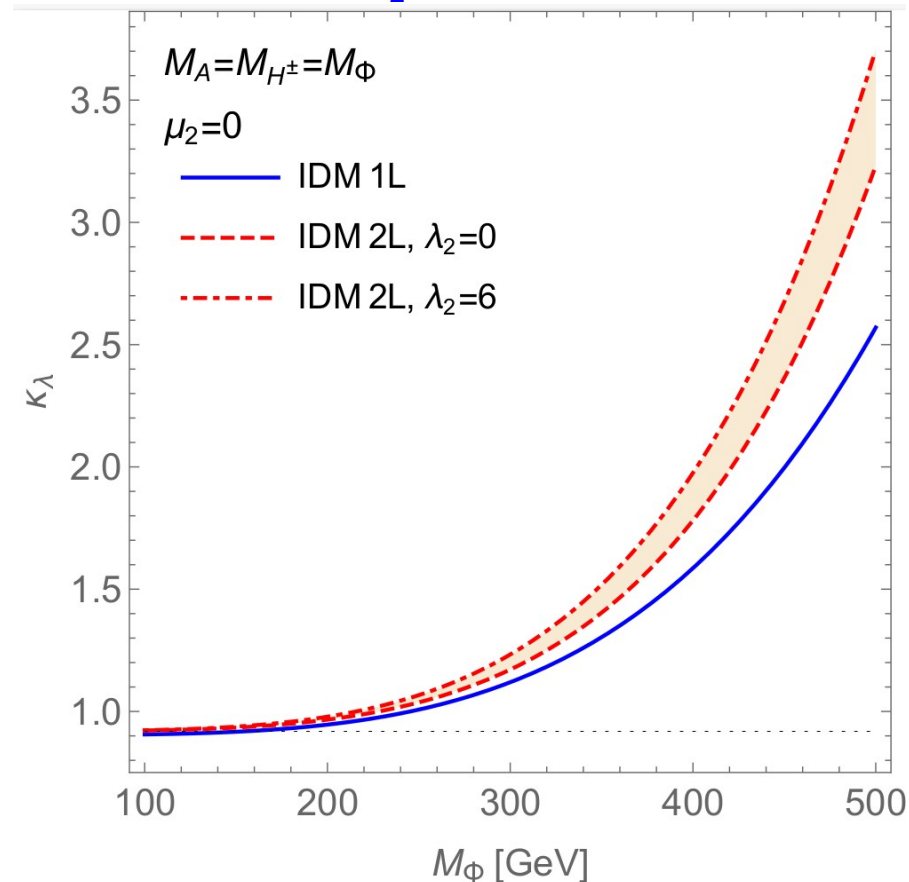
- Calculations in several other models: *Inert Doublet Model (IDM)*, *singlet extension of SM*
- Each model contains a **new parameter appearing from two loops**:

Aligned 2HDM \rightarrow $\tan\beta$



$\tan\beta$ constrained by perturbative unitarity
 \rightarrow only small effects

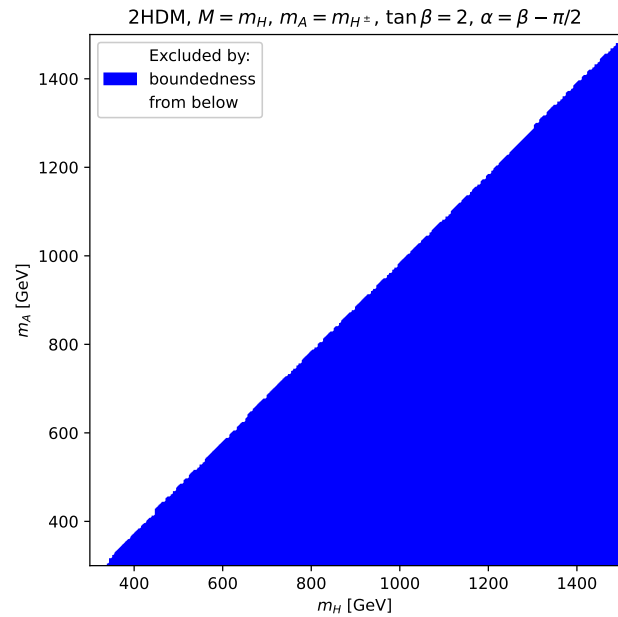
IDM \rightarrow λ_2 (quartic coupling of inert doublet)



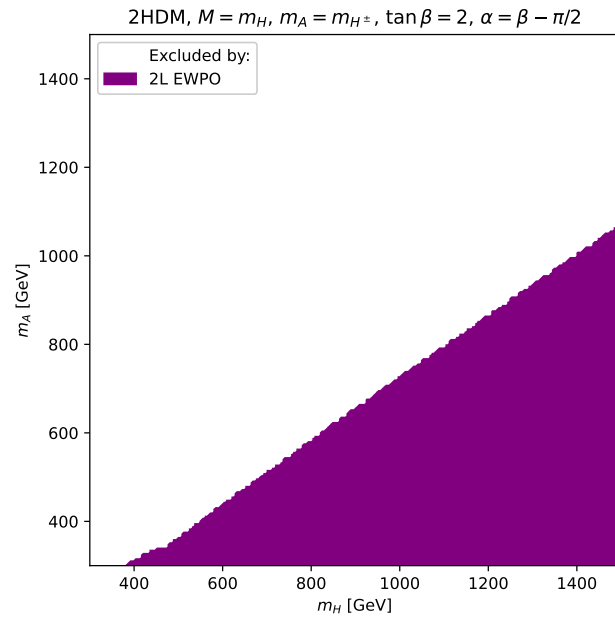
λ_2 is less constrained \rightarrow **enhancement is possible**
 (but 2L effects remain well smaller than 1L ones)

2HDM benchmark plane – individual theoretical constraints

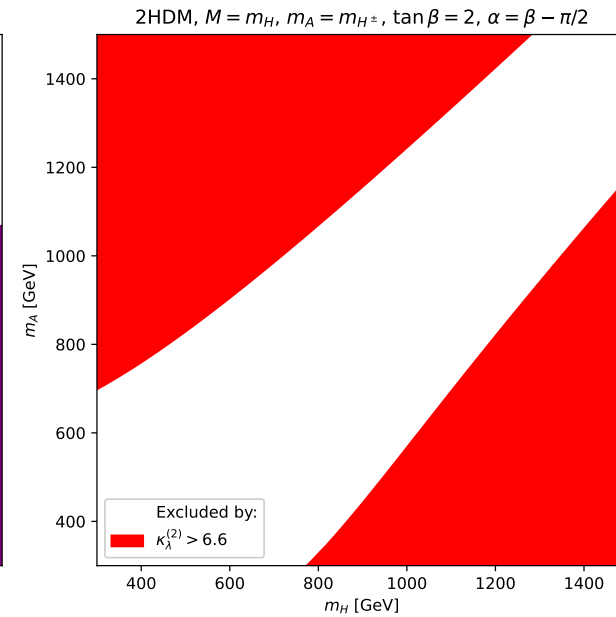
Constraints shown below are independent of 2HDM type



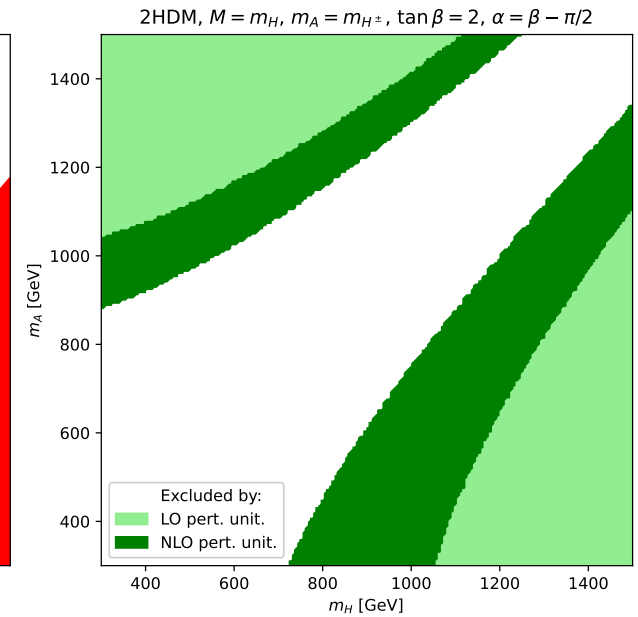
Boundedness from below



EW precision observables computed at 2L



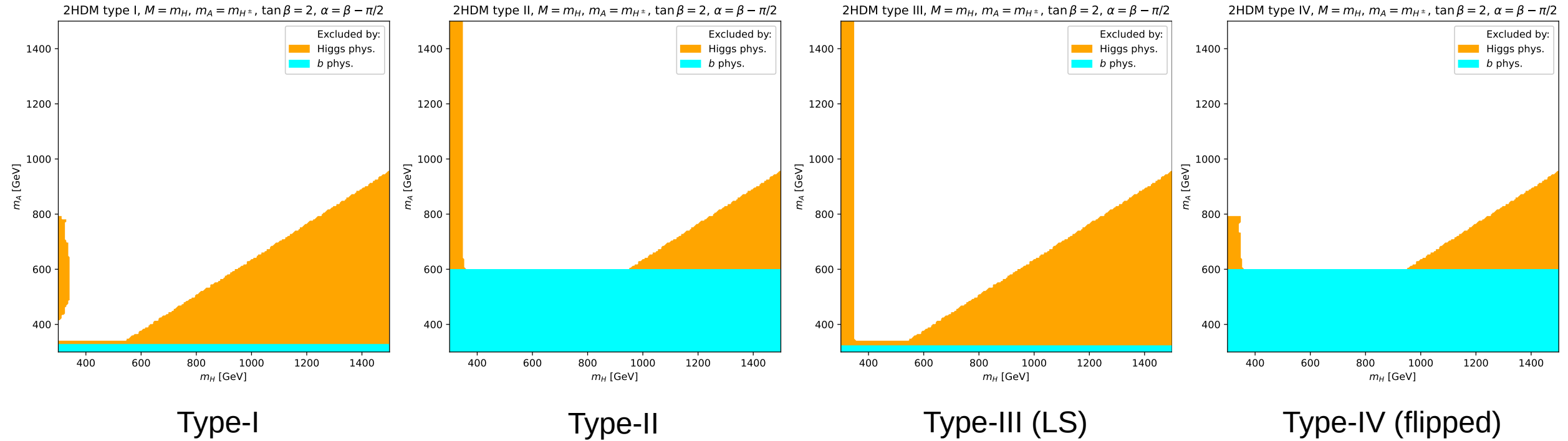
$\kappa_\lambda^{(2)} > 6.6$



Perturbative unitarity at (N)LO

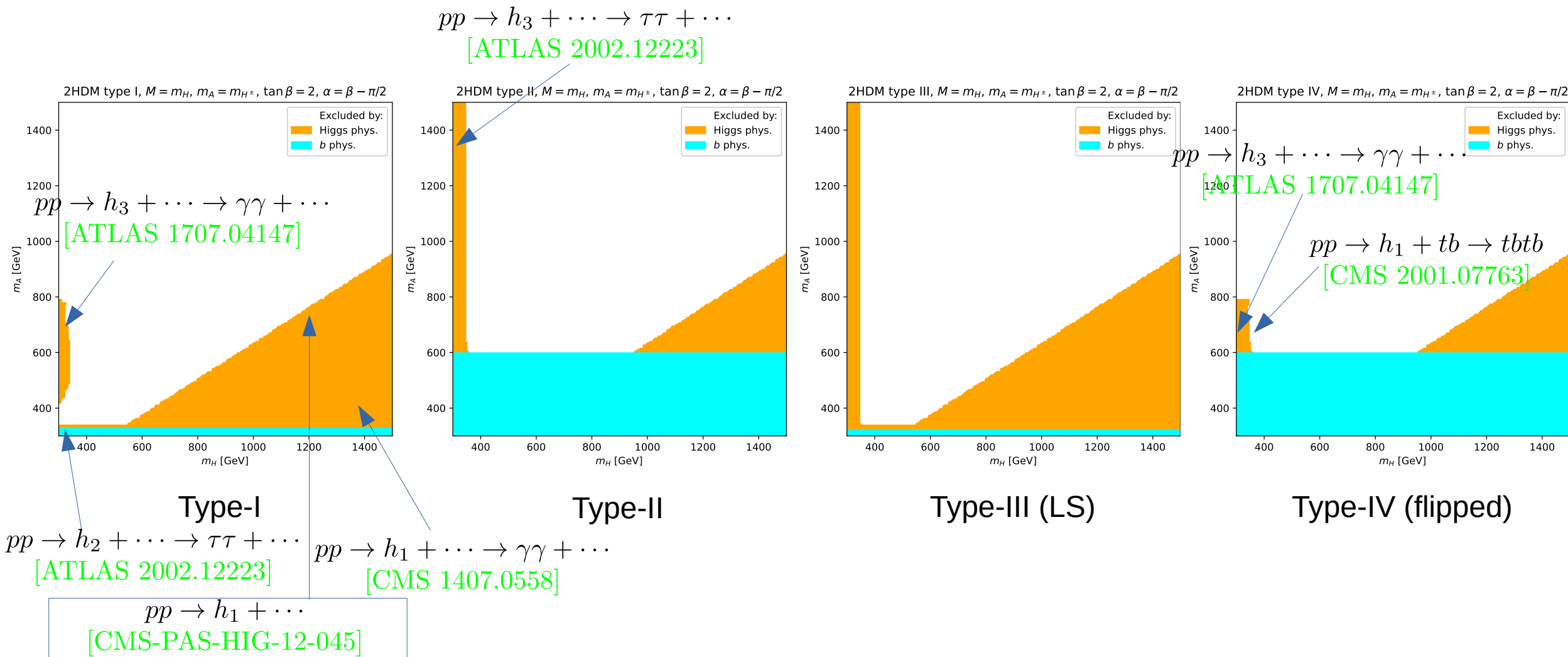
2HDM benchmark plane – experimental constraints

i.e. Higgs physics (via HiggsBounds and HiggsSignals) and b physics (from [Gfitter group 1803.01853])

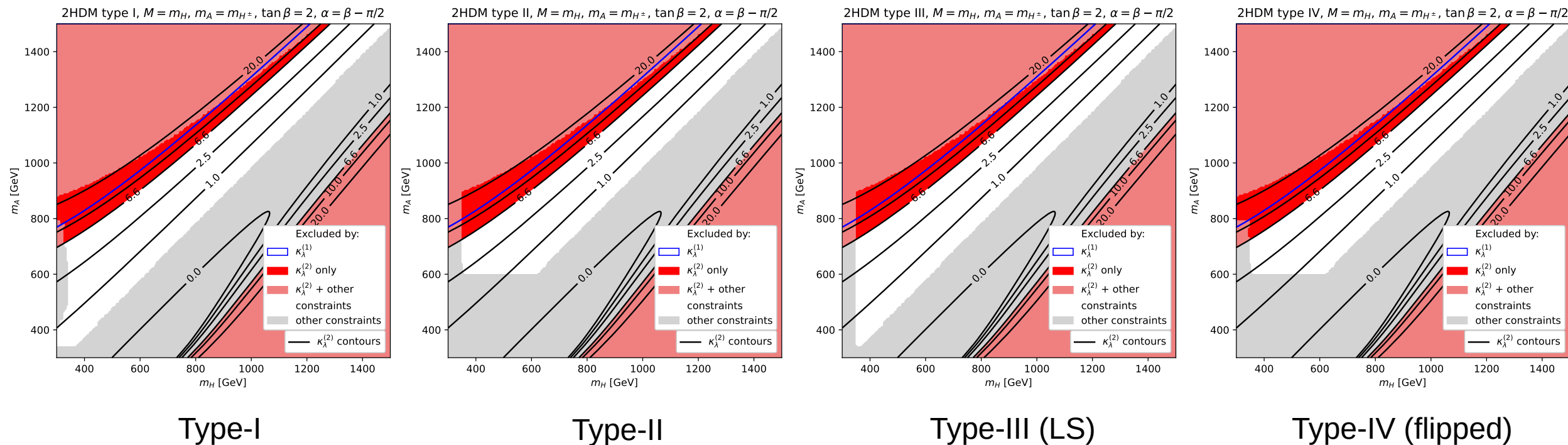


2HDM benchmark plane – experimental constraints

i.e. Higgs physics (via HiggsBounds and HiggsSignals) and b physics (from [Gfitter group 1803.01853])



2HDM benchmark plane – results for all types



Baryogenesis

Observed Baryon Asymmetry of the Universe (BAU)

$$\eta \equiv \frac{n_b - n_{\bar{b}}}{n_\gamma} \simeq 6.1 \times 10^{-10} \quad [\text{Planck '18}]$$

n_b : baryon no. density
 $n_{\bar{b}}$: antibaryon no. density
 n_γ : photon no. density

Sakharov conditions [Sakharov '67] for a theory to explain BAU:

- 1) Baryon number violation
- 2) C and CP violation
- 3) Loss of thermal equilibrium

In the SM

- Sphaleron transitions (break B+L)
- C violation (SM is chiral), but **not enough CP violation**
- **No loss of th. eq.** → in SM, the EWPT is a **crossover**

SM cannot reproduce the BAU → **BSM physics needed!**

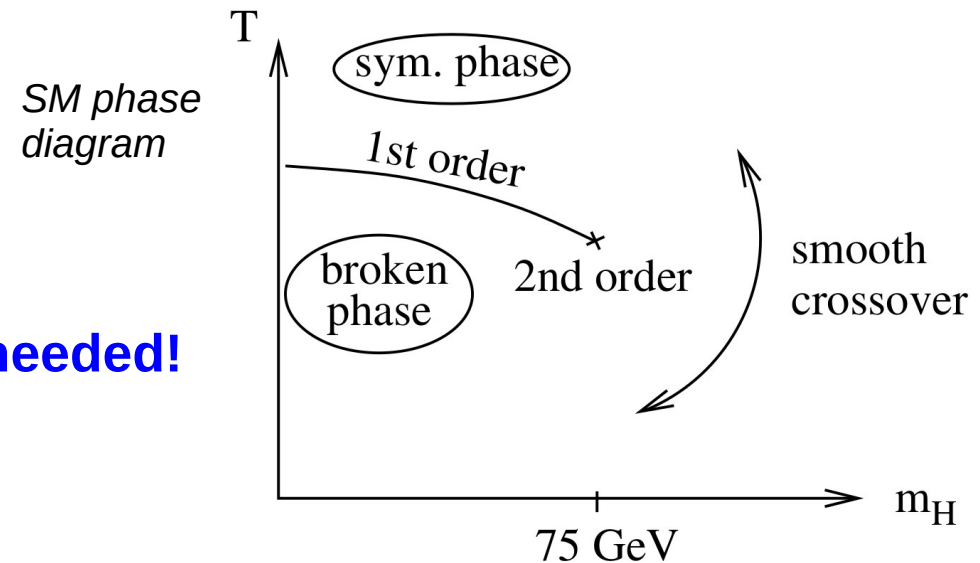


Figure from [Cline '06]

Electroweak Baryogenesis

- Many scenarios proposed, including:
 - Grand Unified Theories
 - Leptogenesis
 - **Electroweak Baryogenesis (EWBG)** [Kuzmin, Rubakov, Shaposhnikov, '85], [Cohen, Kaplan, Nelson '93]
- **Sakharov conditions** in EWBG
 - 1) Baryon number violation → Sphaleron transitions (break B+L)
 - 2) C and CP violation → C violation + **CP violation in extended Higgs sector**
 - 3) Loss of thermal equilibrium → **Loss of th. eq. via a strong 1st order EWPT**

The Higgs potential and the Electroweak Phase Transition

Possible thermal history of the Higgs potential:

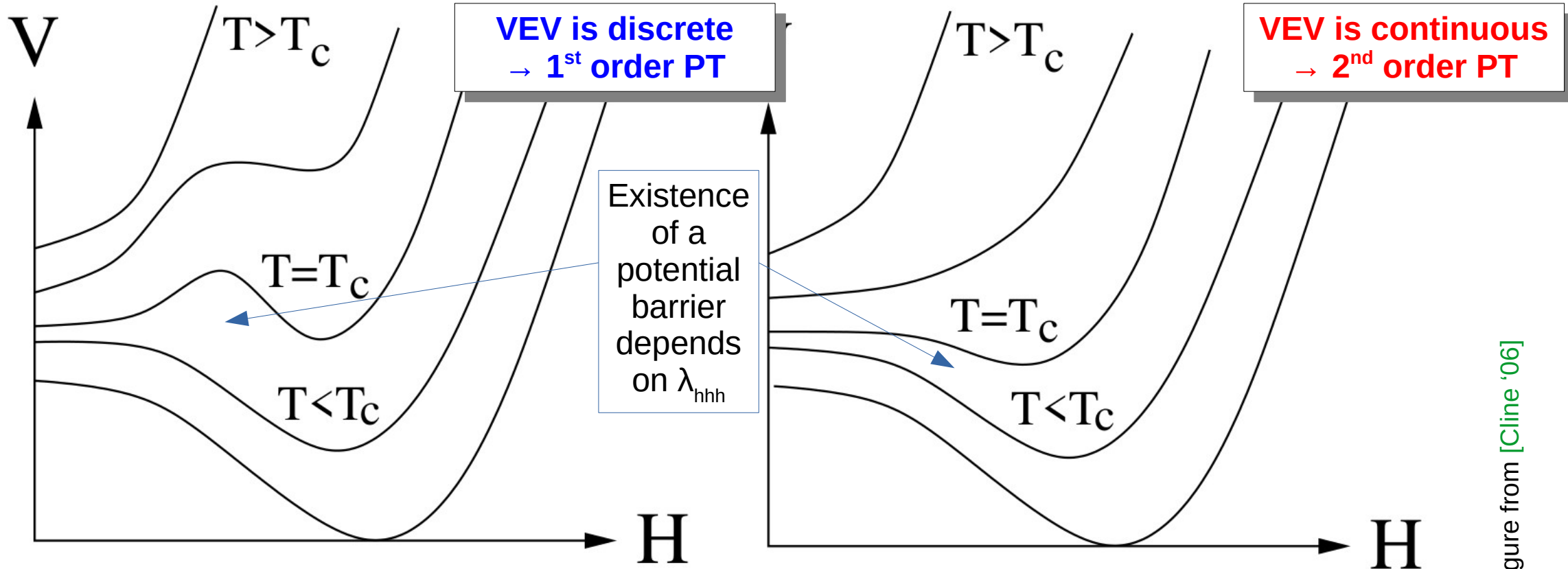


Figure from [Cline '06]

➤ λ_{hhh} determines the nature of the EWPT!

⇒ deviation of λ_{hhh} from its SM prediction typically needed to have a strongly first-order EWPT

[Grojean, Servant, Wells '04], [Kanemura, Okada, Senaha '04]

⇒ required for **electroweak baryogenesis** scenario

Electroweak Baryogenesis – a brief sketch

➤ **Sakharov conditions** in EWBG

1) Baryon number violation

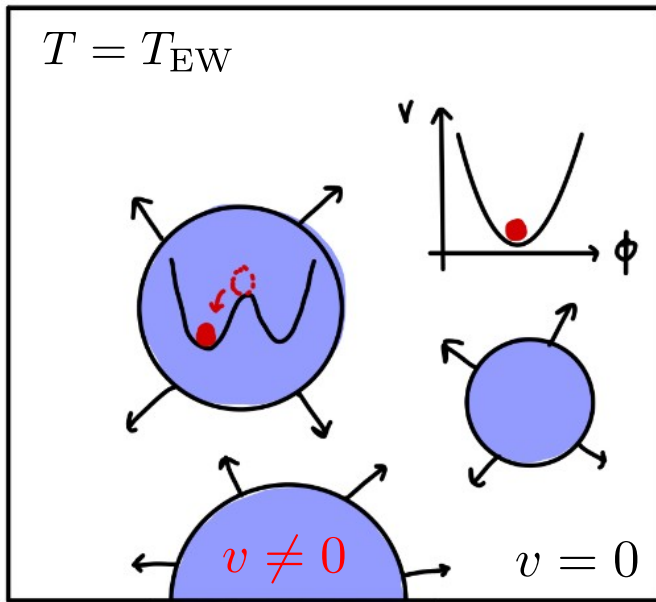
2) C and CP violation

3) Loss of thermal equilibrium

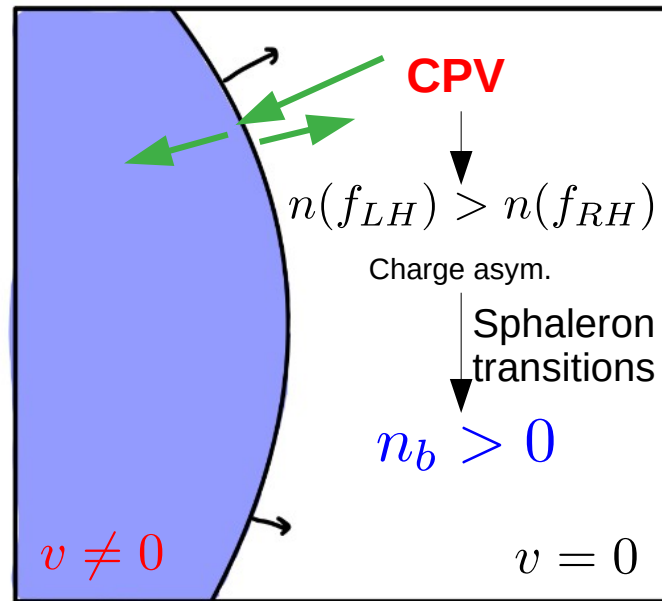
→ Sphaleron transitions (break B+L)

→ C violation + CP violation in extended Higgs sector

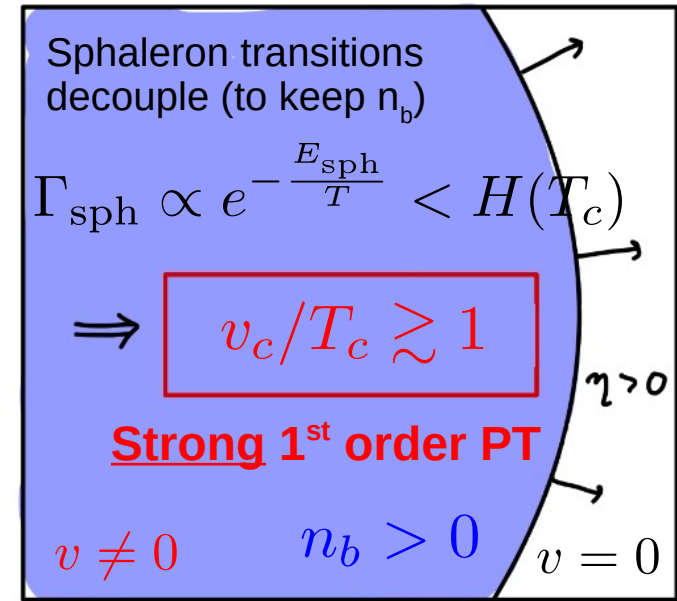
→ Loss of th. eq. via a strong 1st order EWPT



1) Bubble nucleation



2) Baryon number generation



3) Baryon number conservation

➤ EWBG only involves phenomena around the EW scale → **testable in the foreseeable future**

via λ_{hhh} , collider searches, gravitational waves or primordial black holes (sourced by 1st order EWPT)

Figure adapted from [Biermann '22]