





# **SMEFT in the Higgs Sector Higher Loop Contributions**

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*QCD@LHC, Freiburg, 7 Oct 2024*

Work in collaboration with E. Balzani, G. Degrassi, S. Di Noi, R. Gröber, G. Heinrich, J. Lang



# **SMEFT Framework**



Effects due to heavy New Physics can be parametrized by supplementing the SM Lagrangian with higher-dimensional operators that:

- Respect the symmetries of the SM:  $SU(3) \times SU(2) \times U(1)$  and Lorentz
- **Are built from SM fields**
- Are suppressed by powers of a NP scale  $\Lambda$

$$
\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_{D=5}^{\infty} \frac{1}{\Lambda^{D-4}} \mathcal{C}_i^{(D)} \mathcal{O}_i^{(D)}
$$

**The Lagrangian is built without knowing the underlying UV theory (Bottom-up approach)** 

- **The Wilson Coefficients can probe classes of UV models all at once**
- This talk: SMEFT at D=6  $\rightarrow$  Operators defined in the Warsaw basis [Grzadkowski et al. 1008.4884]

# **Light-Quark Yukawa Couplings at the LHC**



Projected bounds on coupling modifiers  $\kappa_q = y_q/y_q^{SM}$  at <code>HL-LHC</code>  $\,$  [de Blas et al. - 1905.03764]

 $\kappa_u < 560$ ;  $\kappa_d < 260$ ;  $\kappa_s < 13$ ;  $\kappa_c < 1.2$ 

**Alternative: sensitivity from specific processes** 

- Higgs decays (mainly charm) - Higgs+jet  $\rightarrow$  diff. distributions [Bishara et al. - 1606.09253; Soreq et al. - 1606.09621; Bonner, Logan - 1608.04376] [Bodwin et al. - 1306.5770; Kagan et al – 1406.1722; König, Neubert – 1505.03870; Alte et al. - 1609.06310]

See talk by A. Raspiareza

- Other approaches [Aguilar-Saavedra et al. - 2008.12538, Falkowski et al. - 2011.09551; Vignaroli – 2205.09449; Yu - 1609.06592]
- HH production [Alasfar, Corral Lopez, Gröber 1909.05279; Alasfar et al. 2207.04157]

Off-shell Higgs production with H → ZZ → 4l decay [Balzani, Gröber, MV - 2304.09772] Evidence at LHC [CMS - 2202.06923; ATLAS - 2304.01532] See also [Zhou - 1505.06369]

# **Light-Quark Yukawas in SMEFT**



D=6

■ We are interested in modifications of the Yukawa sector via D=6 operators

$$
\textsf{SM}\quad \left|\ \mathcal{L}_y=-y_{ij}^u\bar{Q}_L^i\tilde{\phi}u_R^j-y_{ij}^d\bar{Q}_L^i\phi d_R^j+\text{ h.c.}\ \right|
$$

$$
\Delta \mathcal{L}_y = \frac{\phi^{\dagger} \phi}{\Lambda^2} \left( (C_{u\phi})_{ij} \bar{Q}_L^i \tilde{\phi} u_R^j + (C_{d\phi})_{ij} \bar{Q}_L^i \phi d_R^j + \text{ h.c.} \right)
$$

After EWSB and rotation to mass basis, Lagrangian for Higgs coupling to quarks is

$$
\mathcal{L} \supset g_{hq_i\bar{q}_j} \bar{q}_j q_i h + g_{hhq_i\bar{q}_j} \bar{q}_j q_i h^2 + g_{hhhq_i\bar{q}_j} \bar{q}_j q_i h^3
$$
\n
$$
g_{hq_i\bar{q}_j} = \frac{m_q}{v} \delta_{ij} \left[ -\frac{1}{\sqrt{2}} \frac{v^2}{\Lambda^2} (\tilde{C}_{q\phi})_{ij}, \right] g_{hhq_i\bar{q}_j} = \frac{3}{-\frac{3}{2\sqrt{2}} \Lambda^2} (\tilde{C}_{q\phi})_{ij}, \quad g_{hhhq_i\bar{q}_j} = \frac{1}{-\frac{1}{2\sqrt{2}} \Lambda^2} (\tilde{C}_{q\phi})_{ij}
$$

If we assume flavor-diagonal couplings $\rightarrow \;\; g_{hq\overline{q}}=\kappa_{q} \frac{m_{q}}{n_{q}}$ 

# **Enhancing Light Yukawas in** *pp→ZZ*



- Negligible effects in ggF  $\rightarrow$  treated as SM
- Largest modifications in qq-channel
- **NP** in coupling with PDFs
	- $\rightarrow$  focus only on first generation



# **Off-Shell Higgs Production**



 $|\tilde{C}_{d\phi}/(1 \text{ TeV}^2) = 0.45| |\tilde{C}_{u\phi}/(1 \text{ TeV}^2) = 0.21|$ 



# **Kinematic Discriminants**

[Campbell et al. - 1311.3589; CMS – 2202.06923; Haisch, Koole – 2111.12589, ...]



$$
D_s^d = \log_{10}\left(\frac{P_{d\bar{d}}^{sig}}{P_{q\bar{q}}^{back} + P_{gg}^{back}}\right)
$$

$$
P_{ij}(v) = \frac{1}{\sigma_{ij \to 4\ell}} \int dx_1 dx_2 \delta(x_1 x_2 E_{CMS}^2 - m_{4\ell}^2) f_i(x_1) f_j(x_2) \hat{\sigma}_{ij}(x_1, x_2, v)
$$

- For  $D_s^d$  > 2 selects basically only events from signal process
- Not possible to distinguish between  $d\bar{d} \rightarrow h^*$  and  $u\bar{u} \rightarrow h^*$



[Balzani, Gröber, MV - 2304.09772]

# **Comparison with Previous Studies**



Shape analysis on  $D_s^d$  distributions – off-shell region defined by  $m_{\mathrm{ZZ}} \! > \! 250 \, \mathrm{GeV}$ 

Consider only the  $ZZ \rightarrow 4$  final state



[Balzani, Gröber, MV - 2304.09772]

# **Higgs Probes of Trilinear Coupling**

**HH production has the best sensitivity** See talk by N. P. Readioff



#### $\sigma$  $\sigma$  $t, b$  $t, b$  $\sigma$  $\sigma$

 $V(h) = \frac{m_H^2}{2}h^2 + \lambda_3 v h^3 + \frac{\lambda_4}{4}h^4$ 

### Single-Higgs measurements are helpful, too

[McCullough - 1312.3322; Gorbahn, Haisch – 1607.03773; Degrassi, Giardino, Maltoni, Pagani – 1607.04251; Bizon, Gorbahn, Haisch, Zanderighi – 1610.05771; Maltoni, Pagani, Shivaji, Zhao – 1709.08649; Di Vita, Grojean, Panico, Riembau, Vantalon – 1704.01953; Degrassi, Vitti - 1912.06429]

### In this case,  $\lambda_3$  enters via loop contributions



# **Trilinear coupling in**  $H \rightarrow Z\gamma$

[Degrassi, Vitti - 1912.06429]

Recent evidence in [ATLAS, CMS - 2309,03501]

**The trilinear coupling enters at two loops** 

**Amplitude obtained from a Taylor expansion in the external momenta** 

$$
\frac{q_1^2}{4m^2}, \frac{q_2^2}{4m^2}, \frac{q_1 \cdot q_2}{4m^2} \ll 1 \qquad m = m_H, m_t, m_W, m_Z
$$

After the expansion 
$$
q_1^2 = 0
$$
,  $q_2^2 = m_Z^2$ ,  $q_1 \cdot q_2 = (m_H^2 - m_Z^2)/2$ 

Sensitivity comparable to other single-Higgs processes

[Degrassi, Giardino, Maltoni, Pagani – 1607.04251]





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Connection to SMEFT: calculation using

$$
V^{NP} = \sum_{n=1}^{N} c_{2n} (\Phi^{\dagger} \Phi)^n, \qquad \Phi = \begin{pmatrix} \phi^+ \\ \frac{1}{\sqrt{2}} (v + h + i\phi_2) \end{pmatrix}
$$

When truncating at  $n \leq 3$  recover SMEFT with only  $\mathcal{O}_{\phi} = (\Phi^{\dagger} \Phi)^3$  switched on



# **4-top operators in the SMEFT**

**Loosely constrained, difficult to access directly** 

Constraints possible from

Top-quark data

[Zhang – 1708.05928 D'Hondt, Mariotti, Mimasu, Moortgat, Zhang – 1807.02130 Hartland, Maltoni, Nocera, Rojo, Slade, Vryonidou, Zhang – 1901.05965 Brivio, Bruggisser, Maltoni, Moutafis, Plehn, Vryonidou, Westhoff, Zhang - 1910.0366 Ellis, Madigan, Mimasu, Sanz You – 2012.02779 SMEFiT Collaboration – 2105.00006 Degrande, Rosenfeld, Vasquez - 2402.06528 Celada, Giani, ter Hoeve, Mantani, Rojo, Rossia, Thomas, Vryonidou - 2404.12809]

### EWPOs

[Dawson, Giardino – 2201.09887; de Blas, Chala, Santiago - 1507.00757]



$$
\mathcal{L}_{4t} = \frac{\mathcal{C}_{QQ}^{(1)}}{\Lambda^2} \left( \bar{Q}_L \gamma_\mu Q_L \right) \left( \bar{Q}_L \gamma^\mu Q_L \right) \n+ \frac{\mathcal{C}_{QQ}^{(3)}}{\Lambda^2} \left( \bar{Q}_L \tau^I \gamma_\mu Q_L \right) \left( \bar{Q}_L \tau^I \gamma^\mu Q_L \right) \n+ \frac{\mathcal{C}_{QL}^{(1)}}{\Lambda^2} \left( \bar{Q}_L \gamma_\mu Q_L \right) \left( \bar{t}_R \gamma^\mu t_R \right) \n+ \frac{\mathcal{C}_{QL}^{(8)}}{\Lambda^2} \left( \bar{Q}_L T^A \gamma_\mu Q_L \right) \left( \bar{t}_R T^A \gamma^\mu t_R \right) \n+ \frac{\mathcal{C}_{tt}}{\Lambda^2} \left( \bar{t}_R \gamma_\mu t_R \right) \left( \bar{t}_R \gamma^\mu t_R \right) .
$$

# **Single-Higgs Processes and 4-top Operators**



Competitive bounds from single-Higgs production and decay [Alasfar, de Blas, Gröber - 2202.02333]

 $\{qq \to H; t\bar{t}H; H \to \gamma\gamma; H \to qq; H \to b\bar{b}\}$ 

 $\Box$   $\mathcal{O}_\phi$  included in the fit  $\rightarrow$  bounds on Higgs trilinear coupling become less stringent



HH production discussed in [Heinrich, Lang - 2311.15004; 2409.19578]

In both cases the 4-top operators can enter at two loops

#### **4-top Operators in** *gg→H*   $g$  are  $g$  are  $q_{\lambda}$ 000  $-h$  $-h$  $-h$  $g_{QQ}$  $g_{Q\ Q}$  $g$  allered

**4-top operators involve chiral projectors**  $\Rightarrow$  treatment of  $\gamma$ <sup>5</sup> required in Dim Reg

 $\gamma^5 = i\gamma^0\gamma^1\gamma^2\gamma^3 \Rightarrow$  Intrisically 4-dimensional object

In  $D\neq 4$ , the following properties cannot be satisfied at the same time

■ Anticommutativity  $\Rightarrow \{\gamma^5, \gamma^\mu\} = 0$ 

Cyclicity of Trace

$$
\mathbf{Tr}[\gamma^{\mu}\gamma^{\nu}\gamma^{\rho}\gamma^{\sigma}\gamma^{5}] = 4i \ \varepsilon^{\mu\nu\rho\sigma}
$$

Vast(!) literature of approaches to address this. We considered two cases

# **Continuation Schemes for**  $\gamma^5$



### **Naive Dim Reg (NDR)**

[Chanowitz, Furman, Hinchliffe ('79)] [ 't Hooft, Veltman ('72);

Extend  $\{\gamma^5, \gamma^\mu\} = 0$  to  $D \neq 4$ 

Computationally convenient

Cyclicity of trace lost

**Breitenlohner, Maison, 't Hooft, Veltman (BMHV)**

Breitenlohner, Maison ('79)]

Split the Dirac algebra

$$
\begin{split} \gamma^{(D)}_{\mu} &= \gamma^{(4)}_{\mu} + \gamma^{(D-4)}_{\mu}, \\ \{\gamma^{(4)}_{\mu}, \gamma_{5}\} &= 0, \quad [\gamma^{(D-4)}_{\mu}, \gamma_{5}] = 0 \end{split}
$$

Algebraically consistent

### Breaking of chiral WIs

[Larin - 9302240 Bélusca-Maı̈to, Ilakovac, Kühler, Mador-Božinović, Stöckinger, Weißwange - 2303.09120 Cornella, Feruglio, Vecchi - 2205.10381]

Physical observables will be independent of the  $\gamma^5$  scheme, but intermediate expressions will differ by  $\mathcal{O}(\varepsilon)$  contributions

# **Scheme-Dependent Contributions**

[Di Noi, Gröber, Heinrich, Lang, MV - 2310.18221]

Scheme-dependent pole in the gluon-top vertex modification



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[Di Noi, Gröber, Heinrich, Lang, MV - 2310.18221]

Scheme-dependent pole in the gluon-top vertex modification

$$
g \text{ sequence}
$$
\n
$$
g \text{ where } g \text{ is a nonline}
$$
\n
$$
K_{tG} = \begin{cases}\n\frac{\sqrt{2}m_t g_s}{16\pi^2 v} & \text{(NDR)} \\
0 & \text{(BMHV)}\n\end{cases}
$$
\n
$$
K_{tG} = \begin{cases}\n\frac{\sqrt{2}m_t g_s}{16\pi^2 v} & \text{(NDR)} \\
0 & \text{(BMHV)}\n\end{cases}
$$
\n
$$
16\pi^2 \mu \frac{dC_{\phi G}}{d\mu} = -4\sqrt{2}g_{h\bar{t}t}g_s \left(\frac{C_{tG}}{C_{tG}} + K_{tG} \left(\frac{C_{Qt}^{(1)} - \frac{1}{6}C_{Qt}^{(8)}}{6Q_{tG}}\right)\right)
$$
\n
$$
g \text{ The Minkting, Manobar, Trott} = 1308.2627; 1310.4838; 1312.2014
$$

### **Scheme-Dependent Parameters**

 $\blacksquare$  Observed in  $b \rightarrow s \, \gamma \, (g)$  in the context of Weak EFT

[Ciuchini, Franco, Reina, Silvestrini – 9311357; Ciuchini, Franco, Martinelli, Reina, Silvestrini – 9307364; Buras, Misiak, Munz, Pokorski – 9311345 Herrlich, Nierste - 9412375]

Obtain scheme-independent predictions via a finite renormalization of the parameters

$$
\mathcal{C}_{tG}^{\text{NDR}} = \mathcal{C}_{tG}^{\text{BMHV}} - \left(\mathcal{C}_{Qt}^{(1)} - \frac{1}{6}\mathcal{C}_{Qt}^{(8)}\right) \frac{\sqrt{2}g_{h\bar{t}t}g_s}{16\pi^2},
$$
\n
$$
g_{h\bar{t}t}^{\text{NDR}} = g_{h\bar{t}t}^{\text{BMHV}} - g_{h\bar{t}t} \left(\mathcal{C}_{Qt}^{(1)} + \frac{4}{3}\mathcal{C}_{Qt}^{(8)}\right) \frac{(m_h^2 - 6m_t^2)}{16\pi^2\Lambda^2},
$$
\n
$$
m_t^{\text{NDR}} = m_t^{\text{BMHV}} + \left(\mathcal{C}_{Qt}^{(1)} + \frac{4}{3}\mathcal{C}_{Qt}^{(8)}\right) \frac{m_t^3}{8\pi^2\Lambda^2}.
$$

**Confirmed by matching onto UV toy models in the two schemes** 

**Possibility to map predictions between schemes while remaining in the bottom-up approach** 

# **Loop- and Tree-Generated Operators**



What does "higher loop" mean in SMEFT?

In the SM, the definition is clear (just look at the Feynman diagram)

- In the SMEFT NP degrees of freedom are integrated out
- If the underlying UV theory is weakly coupled and renormalizable, there are classes of SMEFT operators that can be only generated from loop diagrams in the UV [Arzt, Einhorn, Wudka – 9405214]

The WC of these loop-generated operators will include a suppression due to a loop factor [Buchalla, Heinrich, Müller-Salditt, Pandler - 2204.11808]



5–7: Fermion Bilinears  $(\psi^2)$ 

[Isidori, Wilsch, Wyler - 2303.16922]



### **Scheme-Dependent Parameters**



**IF**  $\mathcal{O}_{tG}$  is loop-generated, the shift is of the same order of magnitude of the 4-top contribution

$$
\begin{split} &\frac{\mathcal{C}_{tG}^{\text{NDR}}}{16\pi^2} = \mathcal{C}_{\frac{tG}{16\pi^2}}^{\text{BMHV}} - \left(\mathcal{C}_{Qt}^{(1)} - \frac{1}{6}\mathcal{C}_{Qt}^{(8)}\right) \frac{\sqrt{2}g_{h\bar{t}t}g_s}{16\pi^2},\\ &g_{h\bar{t}t}^{\text{NDR}} = g_{h\bar{t}t}^{\text{BMHV}} - g_{h\bar{t}t} \left(\mathcal{C}_{Qt}^{(1)} + \frac{4}{3}\mathcal{C}_{Qt}^{(8)}\right) \frac{(m_h^2 - 6m_t^2)}{16\pi^2\Lambda^2},\\ &m_t^{\text{NDR}} = m_t^{\text{BMHV}} + \left(\mathcal{C}_{Qt}^{(1)} + \frac{4}{3}\mathcal{C}_{Qt}^{(8)}\right) \frac{m_t^3}{8\pi^2\Lambda^2}. \end{split}
$$

**Shifts for other parameters are higher-order in the loop counting** 



# **Summary**



■ Light-Yukawa probes discussed within the SMEFT framework

- Highlighted the potential of loop effects in Higgs processes to put competitive/complementary constraints on
	- Higgs self-coupling
	- 4-top operators
- Higher-loop contributions require additional care in the the choice of calculational schemes employed
- Importance of being inclusive when choosing the set of operators, also because constraints on WCs may be scheme-dependent



### **Thank you for your attention!**

### **Finite mixing @ 1 Loop for 4-top operators**





# Effect of  $\gamma^5$ -scheme on  $gg$  → HH





(NDR used for all contributions) (4-top contribution computed in BMHV)

# **Light Yukawas - Phenomenological Analysis**

Shape analysis on  $D_s^d$  distributions – off-shell region defined by  $m_{\mathrm{ZZ}} \! > \! 250 \, \mathrm{GeV}$ 

Consider only the  $ZZ \rightarrow 4$  final state

Efficiency factors obtained from MadGraph based on experimental cuts ( $p_T > 10 \,\text{GeV}$ ,  $|\eta| < 2.5$ )



# **Consistency of EFT Analysis**

Sensitivity is not affected (much) by the choice of invariant mass range



