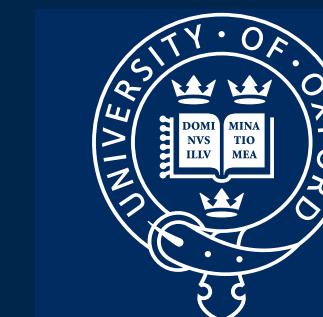


QCD@LHC - FREIBURG - 8th OCTOBER 2024

MiNNLOps EVENT GENERATOR: COLOUR SINGLET PLUS ONE JET EVENTS

SILVIA ZANOLI
University of Oxford

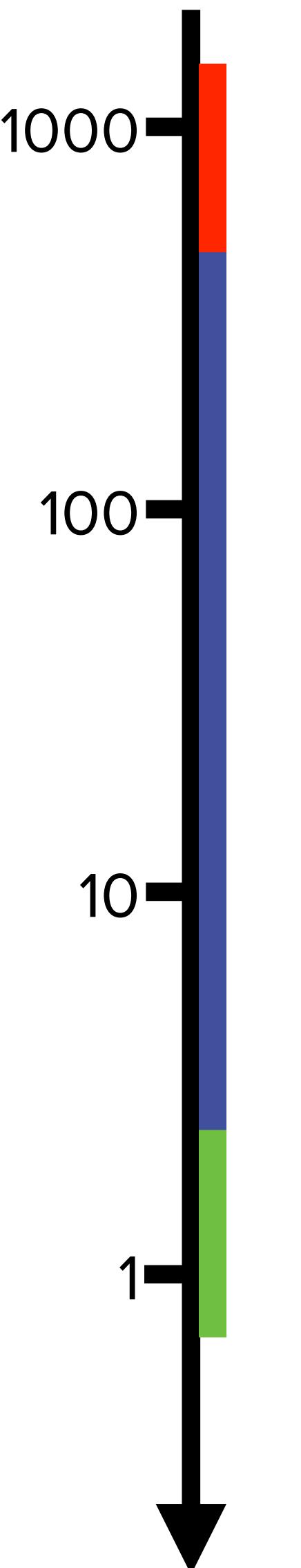
Based on **2402.00596** Ebert, Rottoli, Wiesemann, Zanderighi, **SZ**



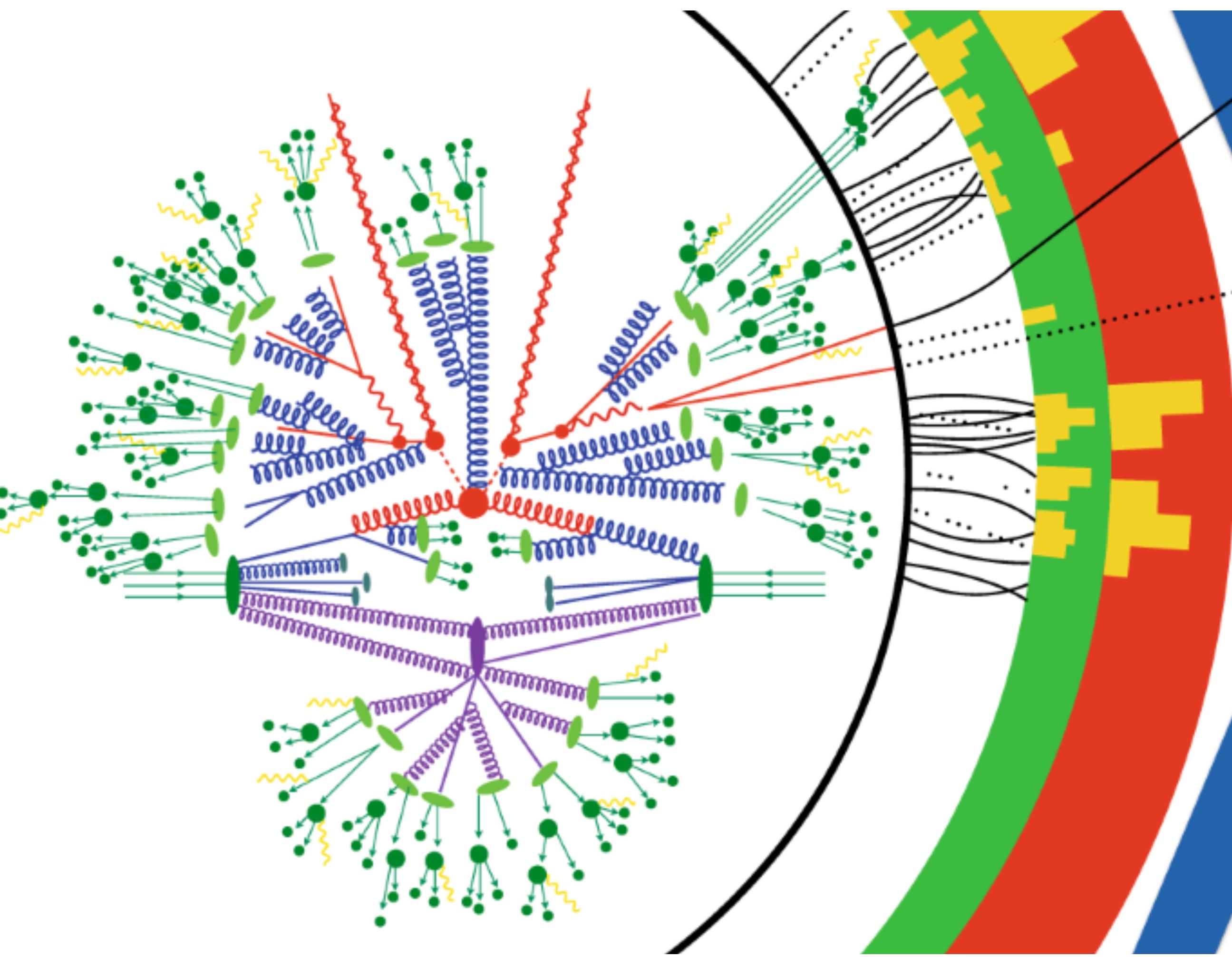
UNIVERSITY OF
OXFORD

LHC EVENT

ENERGY
SCALE [GeV]

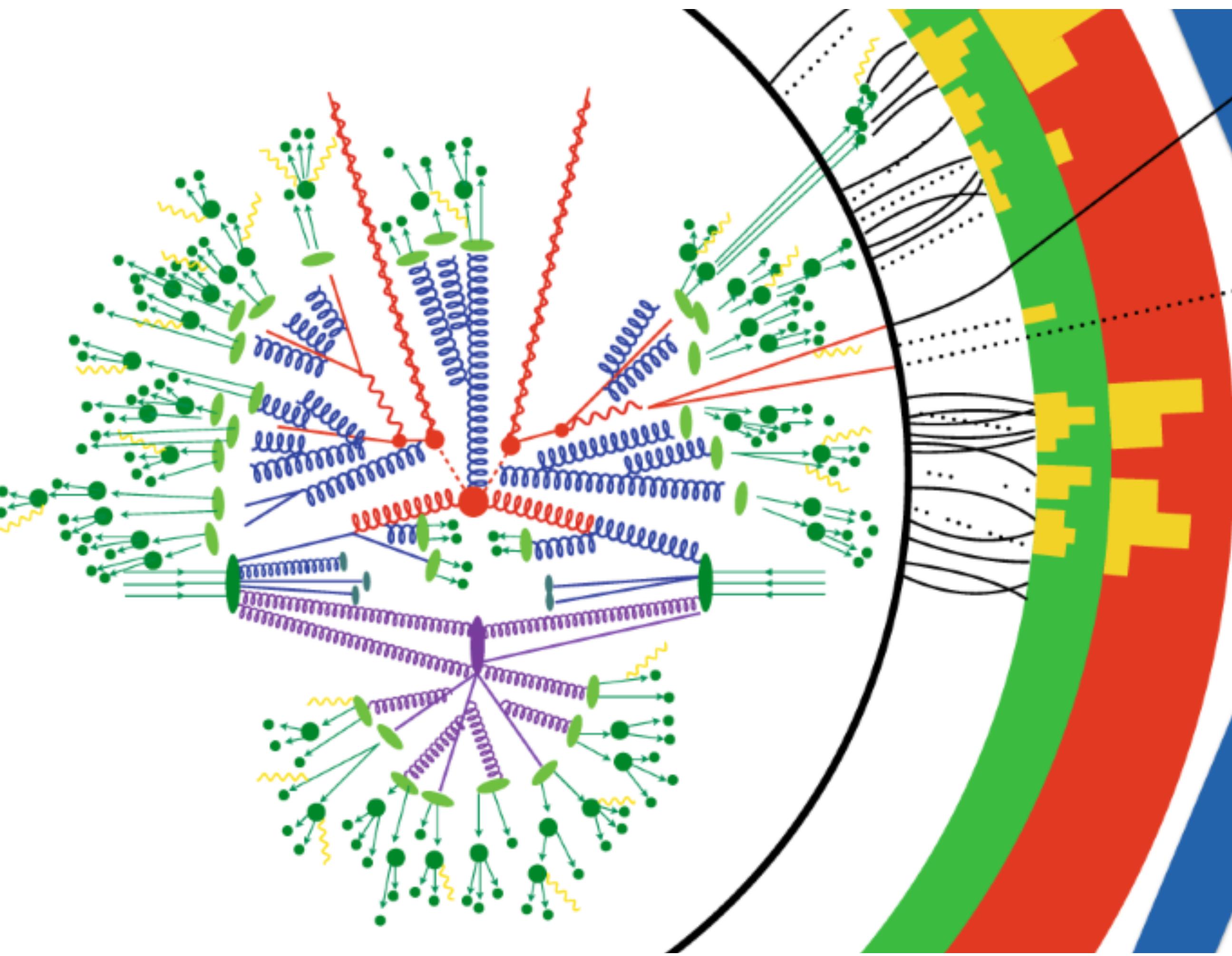
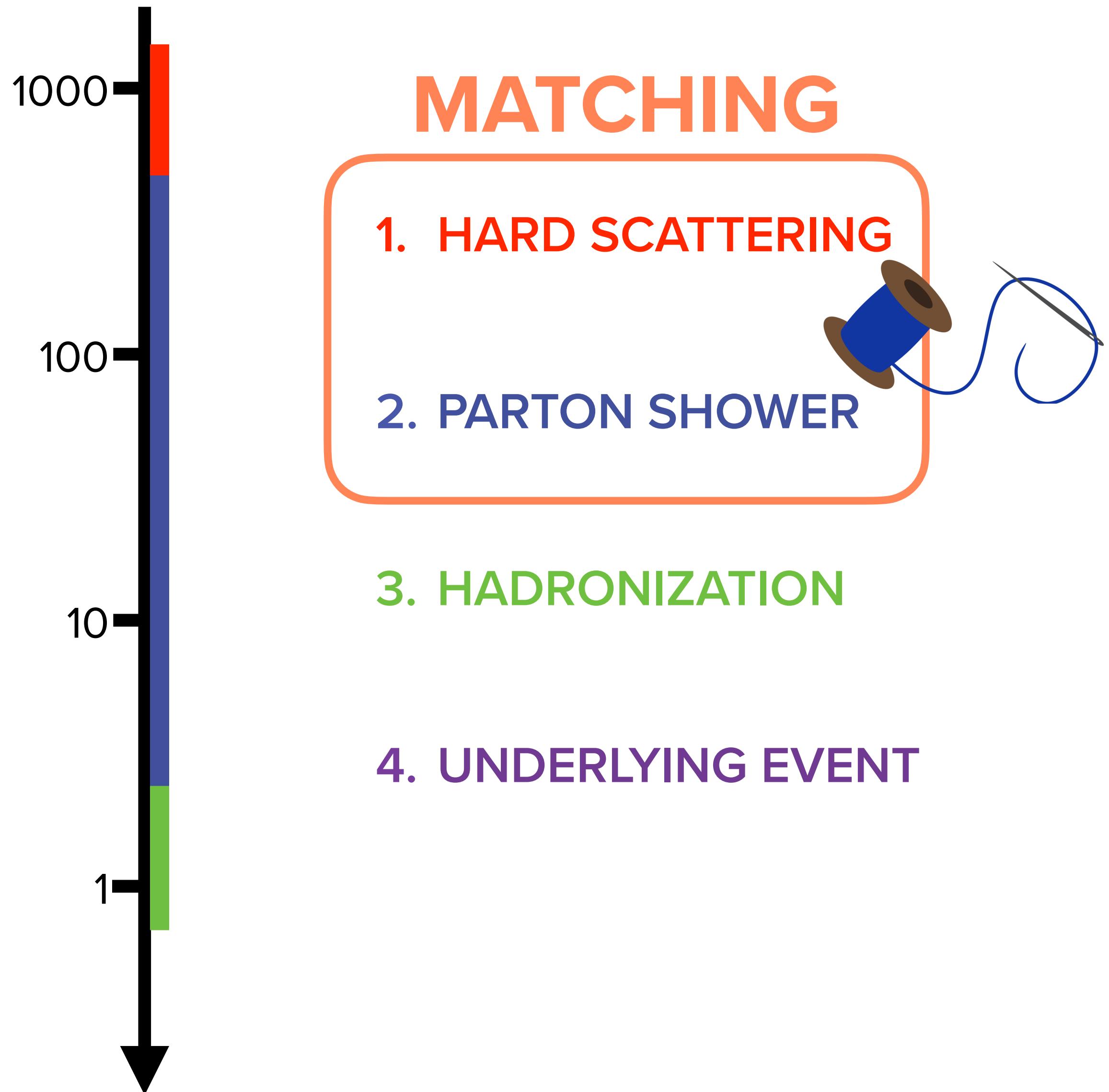


1. HARD SCATTERING
2. PARTON SHOWER
3. HADRONIZATION
4. UNDERLYING EVENT



LHC EVENT

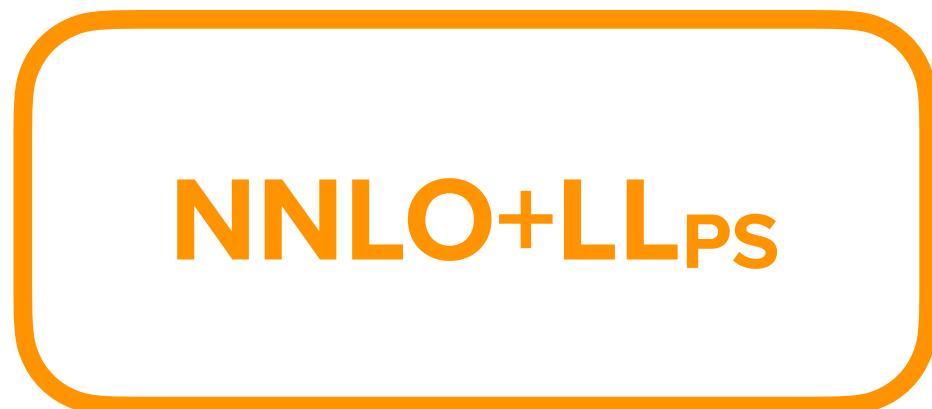
ENERGY
SCALE [GeV]



MATCHING



- A **solved problem** for long time.
- Completely understood and **fully automatized**.
- Two main approaches available: POWHEG [Nason '04; Frixione, Nason, Oleari '07; Alioli, Nason, Oleari, Re '10] and MC@NLO [Frixione, Webber '02].

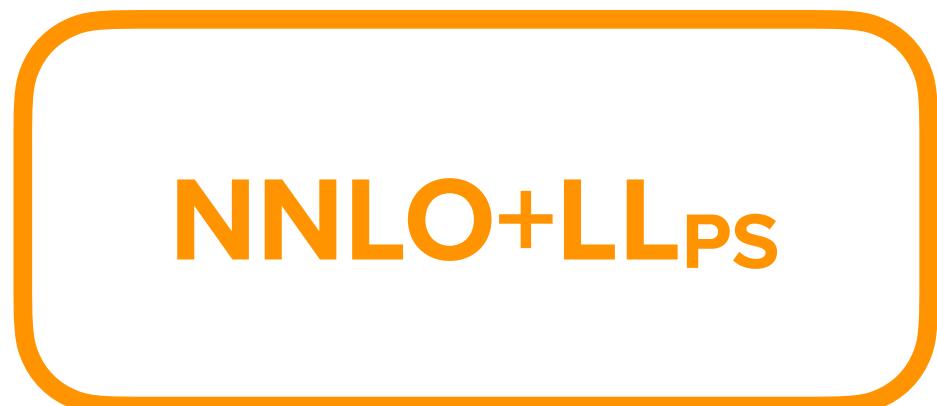
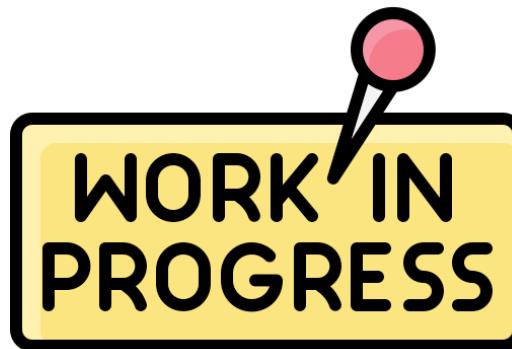


- **State-of-the-art** for precision LHC phenomenology.
- Lots of ongoing effort, **many processes already implemented**.
- Two main methods available: MiNNLO_{PS} [Monni, Nason, Re, Wiesemann, Zanderighi '19] and Geneva [Alioli, Bauer, Berggren, Tackmann, Walsh, Zuberi '13, + subsequent papers].

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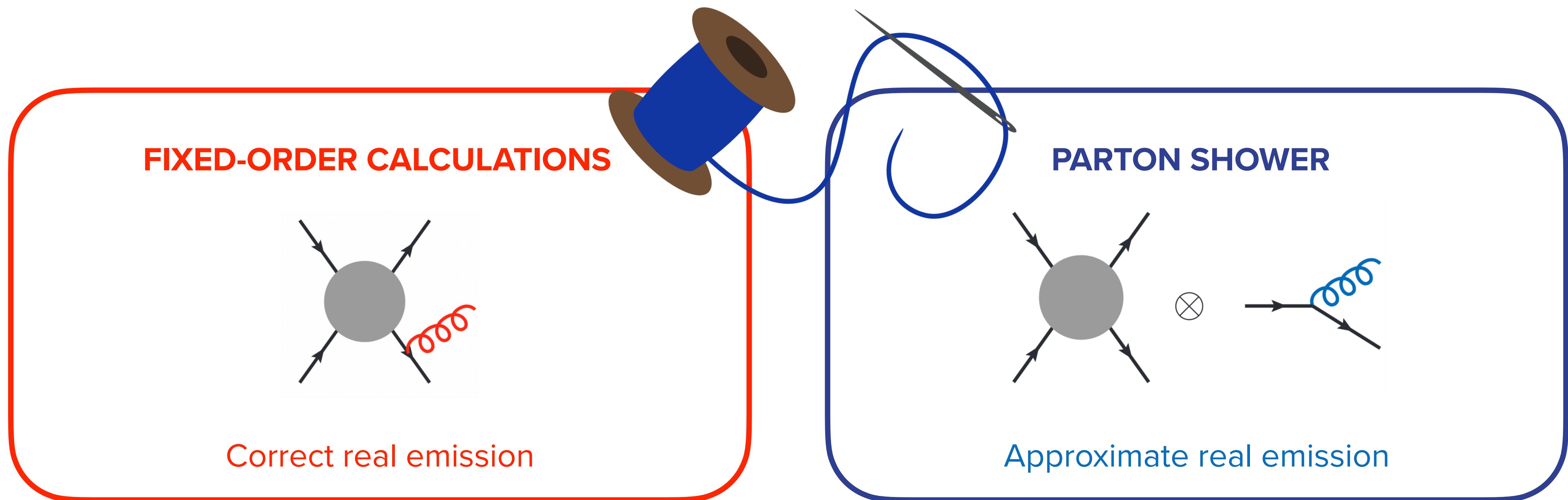


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Logarithmically accurate showers are now available, but matching is still under investigation (at NLO). The method I am presenting today does not directly apply to matching with NLL showers!

WHAT'S THE PROBLEM?



!! DOUBLE COUNTING !!

THE POWHEG METHOD

[Nason '04;
Frixione, Nason, Oleari '07;
Alioli, Nason, Oleari, Re '10]

Master Formula

$$d\sigma_{\text{pwg}} = d\Phi_F \bar{B}(\Phi_F) \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{T,\text{rad}}) \frac{R(\Phi_F, \Phi_{\text{rad}})}{B(\Phi_F)} \right\}$$

NLO NORMALIZATION (= xs)

$$\bar{B}(\Phi_F) = B(\Phi_F) + V(\Phi_F) + \int d\Phi_{\text{rad}} [R(\Phi_{FJ}) - C(\Phi_{FJ})]$$

FIRST (= hardest) EMISSION
obtained with the correct matrix element R/B

$$\Delta(p_T) = \exp \left\{ - \int d\Phi'_{\text{rad}} \frac{R(\Phi_F, \Phi'_{\text{rad}})}{B(\Phi_F)} \Theta(p'_T - p_T) \right\}$$

When using a p_T -ordered shower (most common option, like PYTHIA), we apply a p_T -veto: all the emissions produced by the shower must be softer than the first emission produced by POWHEG.

THE MiNNLO_{PS} METHOD

[Monni, Nason, Re, Wiesemann, Zanderighi '19]

Master Formula

$$d\sigma_F^{\text{MiNNLO}_\text{PS}} = d\Phi_{\text{FJ}} \bar{B}^{\text{MiNNLO}_\text{PS}}(\Phi_{\text{FJ}}) \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{\text{T,rad}}) \frac{R(\Phi_{\text{FJ}}, \Phi_{\text{rad}})}{B(\Phi_{\text{FJ}})} \right\}$$

NNLO NORMALIZATION (= xs)

SECOND EMISSION
obtained à la POWHEG

$$\bar{B}^{\text{MiNNLO}_\text{PS}}(\Phi_{\text{FJ}}) =$$

THE MiNNLO_{PS} METHOD

[Monni, Nason, Re, Wiesemann, Zanderighi '19]

Master Formula

$$d\sigma_F^{\text{MiNNLO}_\text{PS}} = d\Phi_{FJ} \bar{B}^{\text{MiNNLO}_\text{PS}}(\Phi_{FJ}) \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{T,\text{rad}}) \frac{R(\Phi_{FJ}, \Phi_{\text{rad}})}{B(\Phi_{FJ})} \right\}$$

NNLO NORMALIZATION (= xs)

SECOND EMISSION
obtained à la POWHEG

$$\bar{B}^{\text{MiNNLO}_\text{PS}}(\Phi_{FJ}) = \left(B(\Phi_{FJ}) + V(\Phi_{FJ}) + \int d\Phi_{\text{rad}} R(\Phi_{FJJ}) \right)$$

↓
Born FJ

↓
Virtual+Real
on FJ

! DIVERGENT

THE MiNNLO_{PS} METHOD

[Monni, Nason, Re, Wiesemann, Zanderighi '19]

Master Formula

$$d\sigma_F^{\text{MiNNLO}_\text{PS}} = d\Phi_{FJ} \bar{B}^{\text{MiNNLO}_\text{PS}}(\Phi_{FJ}) \left\{ \Delta_{\text{pwg}}(\Lambda_{\text{pwg}}) + \int d\Phi_{\text{rad}} \Delta_{\text{pwg}}(p_{T,\text{rad}}) \frac{R(\Phi_{FJ}, \Phi_{\text{rad}})}{B(\Phi_{FJ})} \right\}$$

NNLO NORMALIZATION (= xs)

SECOND EMISSION
obtained à la POWHEG

$$\bar{B}^{\text{MiNNLO}_\text{PS}}(\Phi_{FJ}) = e^{-\tilde{S}(p_T)} \left(B(\Phi_{FJ}) (1 + \alpha_s \tilde{S}^{(1)}) + V(\Phi_{FJ}) + \int d\Phi_{\text{rad}} R(\Phi_{FJ}) \right)$$

Sudakov form factor



Correct NLO on FJ

Virtual+Real
on FJ

F@NNLO+PS

NLO

NLO

LO

PS (LL)

$$\tilde{S}(p_T) = \int_{p_T^2}^{Q^2} \frac{dq^2}{q^2} \left[A \log \frac{Q^2}{q^2} + B \right]$$

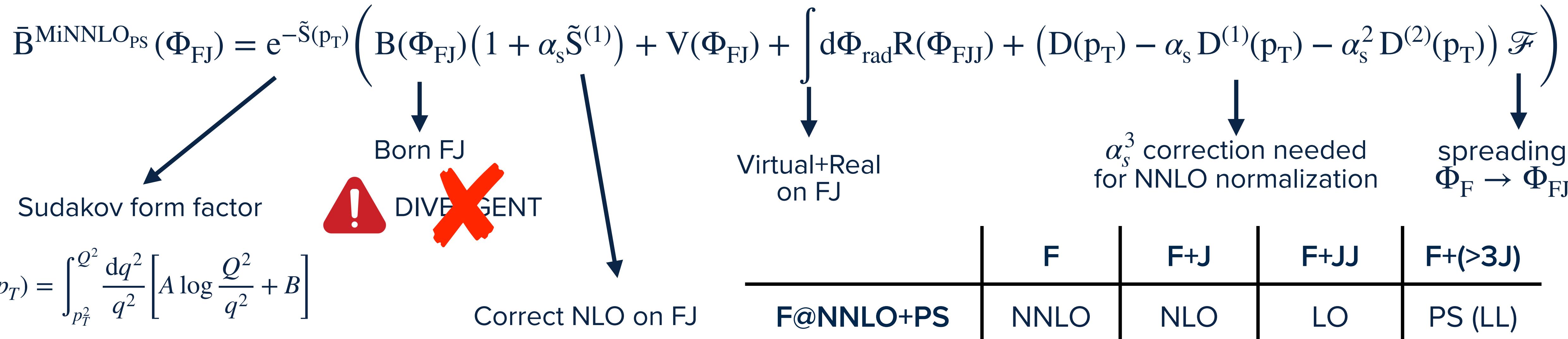
THE MiNNLO_{PS} METHOD

[Monni, Nason, Re, Wiesemann, Zanderighi '19]

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NNLO NORMALIZATION (= xs)

SECOND EMISSION
obtained à la POWHEG

THE MINNLO_{PS} METHOD

- Analytic all-order formula:

$$\frac{d\sigma}{d\Phi_F dp_T} = \frac{d\sigma^{\text{sing}}}{d\Phi_F dp_T} + R(p_T) = \frac{d}{dp_T} \left\{ e^{-\tilde{S}(p_T)} \mathcal{L}(p_T) \right\} + R(p_T) = e^{-\tilde{S}(p_T)} \left[D(p_T) + \frac{R(p_T)}{e^{-\tilde{S}(p_T)}} \right]$$

$$D(p_T) \equiv - \frac{d\tilde{S}(p_T)}{dp_T} \mathcal{L}(p_T) + \frac{d\mathcal{L}p_T}{dp_T}$$

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- Combine with FJ fixed-order $d\sigma_{\text{FJ}}$ and expand up to α_s^3 : 
- $\mu_R = \mu_F = p_T$

$$d\sigma_F = d\sigma_F^{\text{sing}} + [d\sigma_{\text{FJ}}]_{\text{f.o.}} - [d\sigma_F^{\text{sing}}]_{\text{f.o.}} = e^{-\tilde{S}(p_T)} \left\{ D + \underbrace{\frac{[d\sigma_{\text{FJ}}]_{\text{f.o.}}}{[e^{-\tilde{S}(p_T)}]_{\text{f.o.}}} - \frac{[d\sigma_F^{\text{sing}}]_{\text{f.o.}}}{[e^{-\tilde{S}(p_T)}]_{\text{f.o.}}}}_{1 - \alpha_s \tilde{S}^{(1)}} - \alpha_s D^{(1)}(p_T) - \alpha_s^2 D^{(2)}(p_T) \right\}$$

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$$\bar{B}^{\text{MiNNLO}_{\text{PS}}}(\Phi_{\text{FJ}}) = e^{-\tilde{S}(p_T)} \left(B(\Phi_{\text{FJ}}) (1 + \alpha_s \tilde{S}^{(1)}) + V(\Phi_{\text{FJ}}) + \int d\Phi_{\text{rad}} R(\Phi_{\text{FJ}}) + (D(p_T) - \alpha_s D^{(1)}(p_T) - \alpha_s^2 D^{(2)}(p_T)) \mathcal{F} \right)$$

WHAT CAN WE DO WITH MiNNLOps?

2 → 1 PROCESSES

- H** [1908.06987, 2407.01354] ✓
- Z** [1908.06987] ✓
- W** [2006.04133] ✓
- bb**→**H** [2402.04025]

2 → 2 PROCESSES

- Z γ** [2010.10478] ✓
- $\gamma\gamma$** [2204.12602] ✓
- ZZ** [2108.05337] ✓
- VH (H→bb)** [2112.04168]
- (+SMEFT [2204.00663])
- WW** [2103.12077] ✓
- WZ** [2208.12660] ✓

INCLUSION NLO EW

- WZ** [2208.12660] ✓
- Z** ongoing

QQ PRODUCTION

- tt** [2012.14267, 2112.12135] ✓
- bb** [2112.04168]

QQF PRODUCTION

- bbZ** [2404.08598]

THIS TALK!

EXTENSION TO PROCESSES WITH JETS

[2402.00596]

✓ = publicly available at <https://powhegbox.mib.infn.it/>

MiNNLO_{PS} FOR PROCESSES WITH JETS

- We now aim to target NNLO+PS accuracy in processes with a jet.
- N-jettiness (τ_N) is a suitable observable to study processes with jets, and the resummation is known at a sufficient order for a NNLO+PS accurate formalism.

τ_N represents how “N-jet-like” an event looks.

$$\tau_N = \frac{2}{Q^2} \sum_k \min\{q_a \cdot p_k, q_b \cdot p_k, q_1 \cdot p_k, \dots, q_N \cdot p_k\}$$

q_a, q_b = incoming particles
 q_i = signal jets
 p_k = hadronic fs particles

$\tau_N \rightarrow 0$: exactly N jet in the event

$\tau_N \rightarrow 1$: the event has hard radiation between the N signal jets

THE PLAN

MiNNLO_{PS}-p_T: NNLO accuracy on F



MiNNLO_{PS}-τ₀: NNLO accuracy on F



MiNNLO_{PS}-τ₁: NNLO accuracy on FJ

THE PLAN

MiNNLO_{PS}-p_T: NNLO accuracy on F



MiNNLO_{PS}-τ₀: NNLO accuracy on F



- Theoretical formalism
- Implementation for H/Z production
- Phenomenological analysis



- **Problems in the matching with the shower**
- **Large discrepancies in the 1 jet bin for H production**



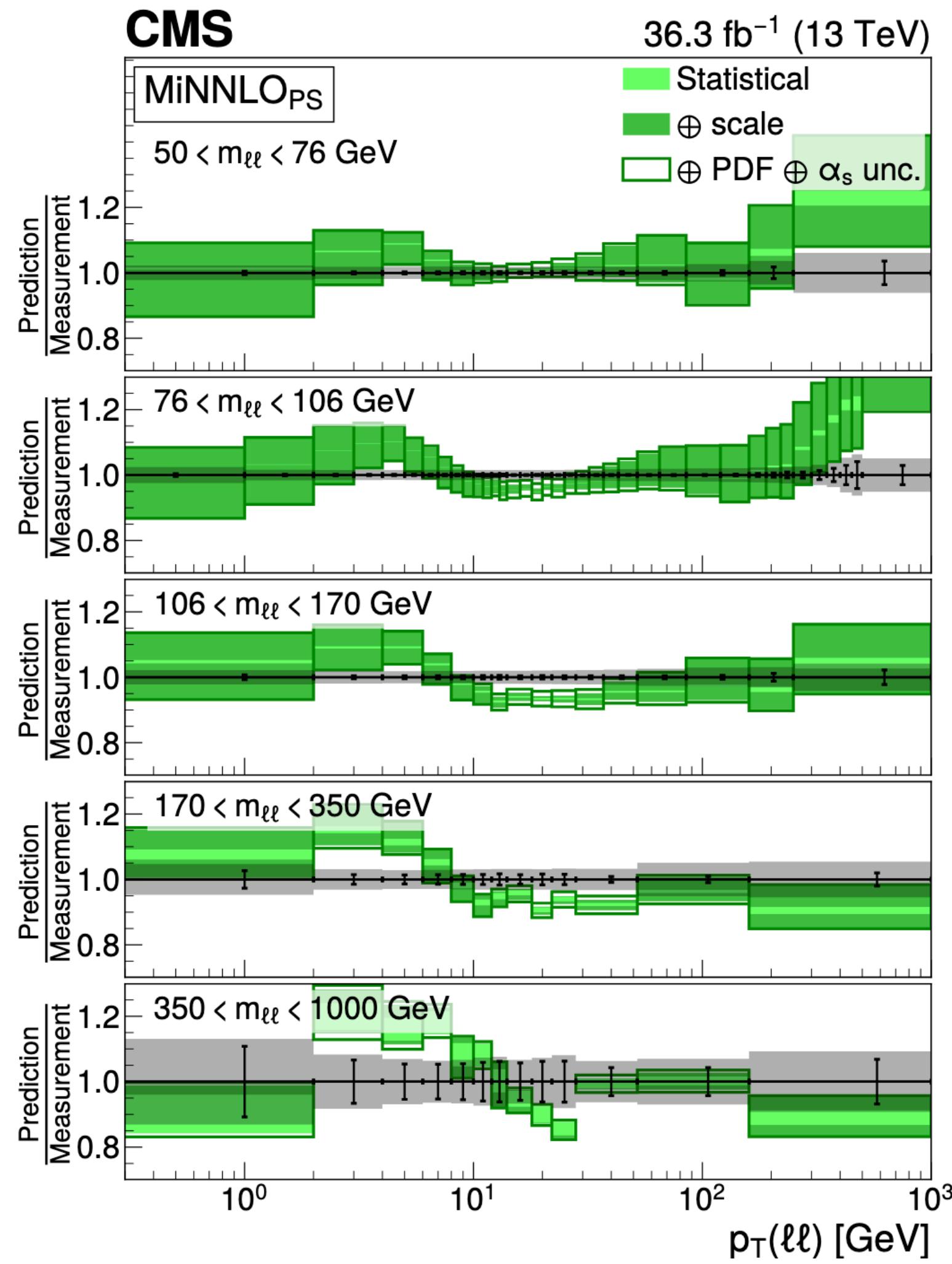
MiNNLO_{PS}-τ₁: NNLO accuracy on FJ



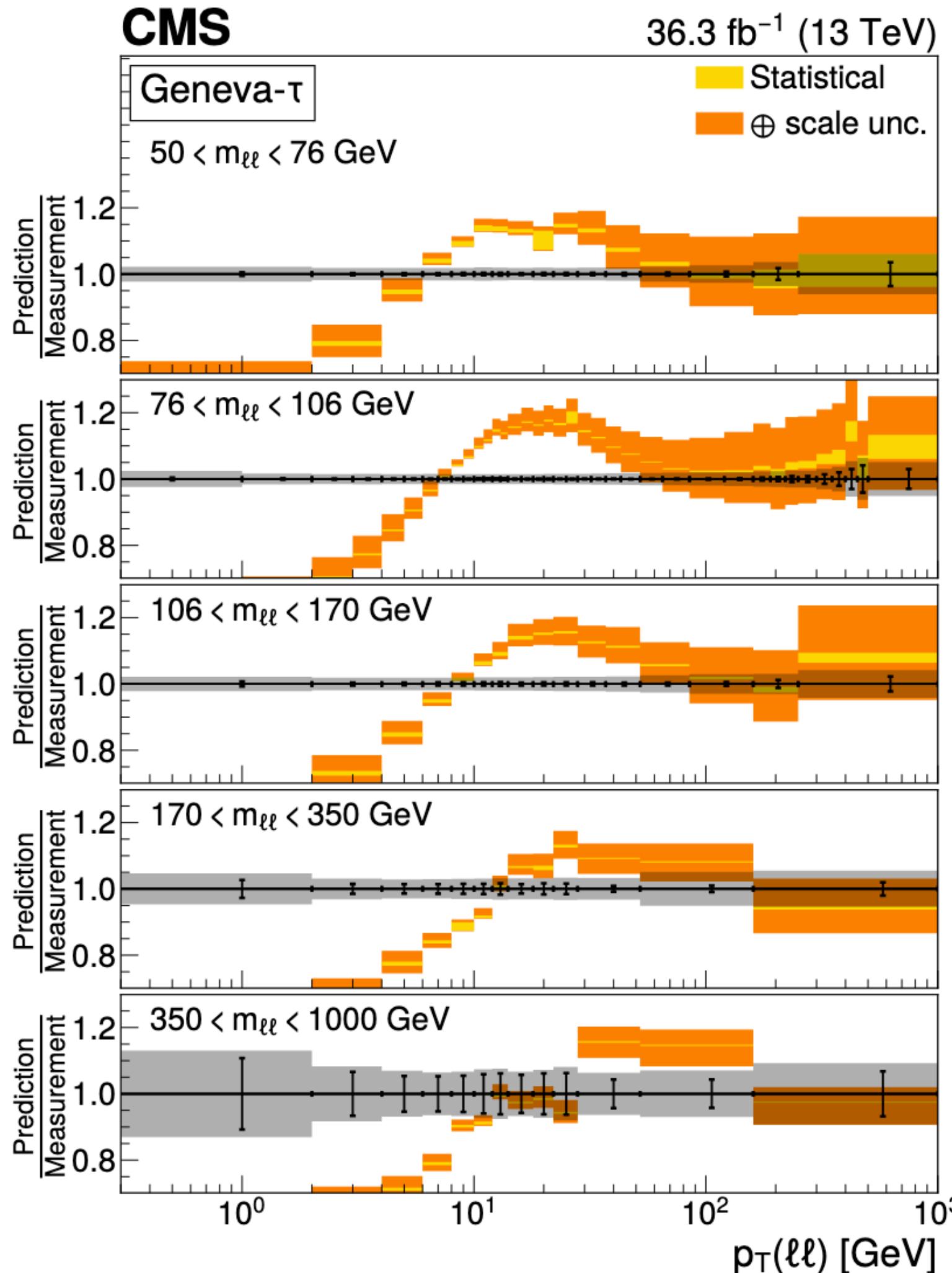
- Theoretical formalism

DY - CMS 2205.04897

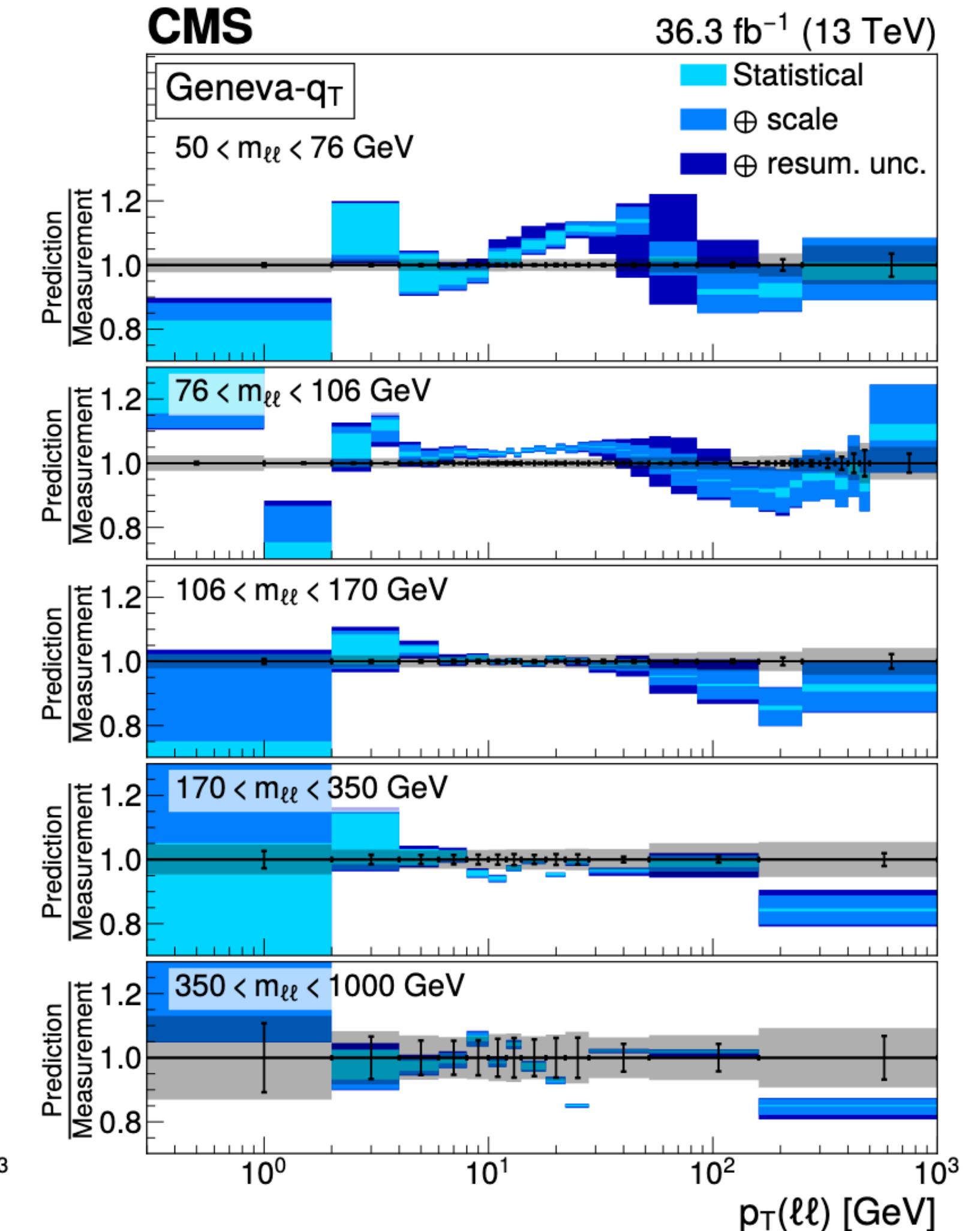
MiNNLO_{PS}-p_T



GENEVA- τ_0



GENEVA-p_T



THE MiNNLO_{PS}- τ_0 METHOD

[Ebert, Rottoli, Wiesemann, Zanderighi, SZ '24]

- We start from the factorization formula of 0-jettiness at NNLL' (for 1-jettiness, include also jet function)

$$\frac{d\sigma}{d\Phi_F d\tau_0} = \frac{d\sigma^{\text{sing}}}{d\Phi_F d\tau_0} + R_f(\tau_0)$$

$$\frac{d\sigma^{\text{sing}}}{d\Phi_F d\tau_0} = \sum_{a,b} \frac{d|M_{a,b}|^2}{d\Phi_F} H_{a,b}(Q, \mu) \int dt_a dt_b B_a(t_a, x_a, \mu) B_b(t_b, x_b, \mu) S\left(\tau_0 - \frac{t_a}{Q} - \frac{t_b}{Q}, \mu\right)$$

- We evolve and expand all the needed ingredients in order to obtain:
- We follow all the steps presented for MiNNLO_{PS}- p_T to obtain:

$$\frac{d\sigma^{\text{sing}}}{d\Phi_F d\tau_0} = \frac{d}{d\tau_0} \left(e^{-\tilde{S}(\tau_0)} \mathcal{L}(\tau_0) \right)$$

$$\bar{B}^{\text{MiNNLO}_{\text{PS}}}(\Phi_{FJ}) = e^{-\tilde{S}(\tau_0)} \left(B(\Phi_{FJ}) (1 + \alpha_s \tilde{S}^{(1)}) + V(\Phi_{FJ}) + \int d\Phi_{\text{rad}} R(\Phi_{FJJ}) + (D(\tau_0) - \alpha_s D^{(1)}(\tau_0) - \alpha_s^2 D^{(2)}(\tau_0)) \mathcal{F} \right)$$

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The logarithmic structure in transverse momentum and jettiness resummation is different!
The MiNNLO_{PS} formulae in the two cases are the same in the structure, but contain different ingredients.

MATCHING WITH THE SHOWER

[Ebert, Rottoli, Wiesemann, Zanderighi, SZ '24]

The accuracy of the parton shower is not fully preserved because we rely on the POWHEG formalism.

Fix this issue requires a deep **modification of the POWHEG method**, mainly modifying the mappings and/or including truncated-vetoed showers. **We plan to implement these changes when matching with NLL accurate showers.**

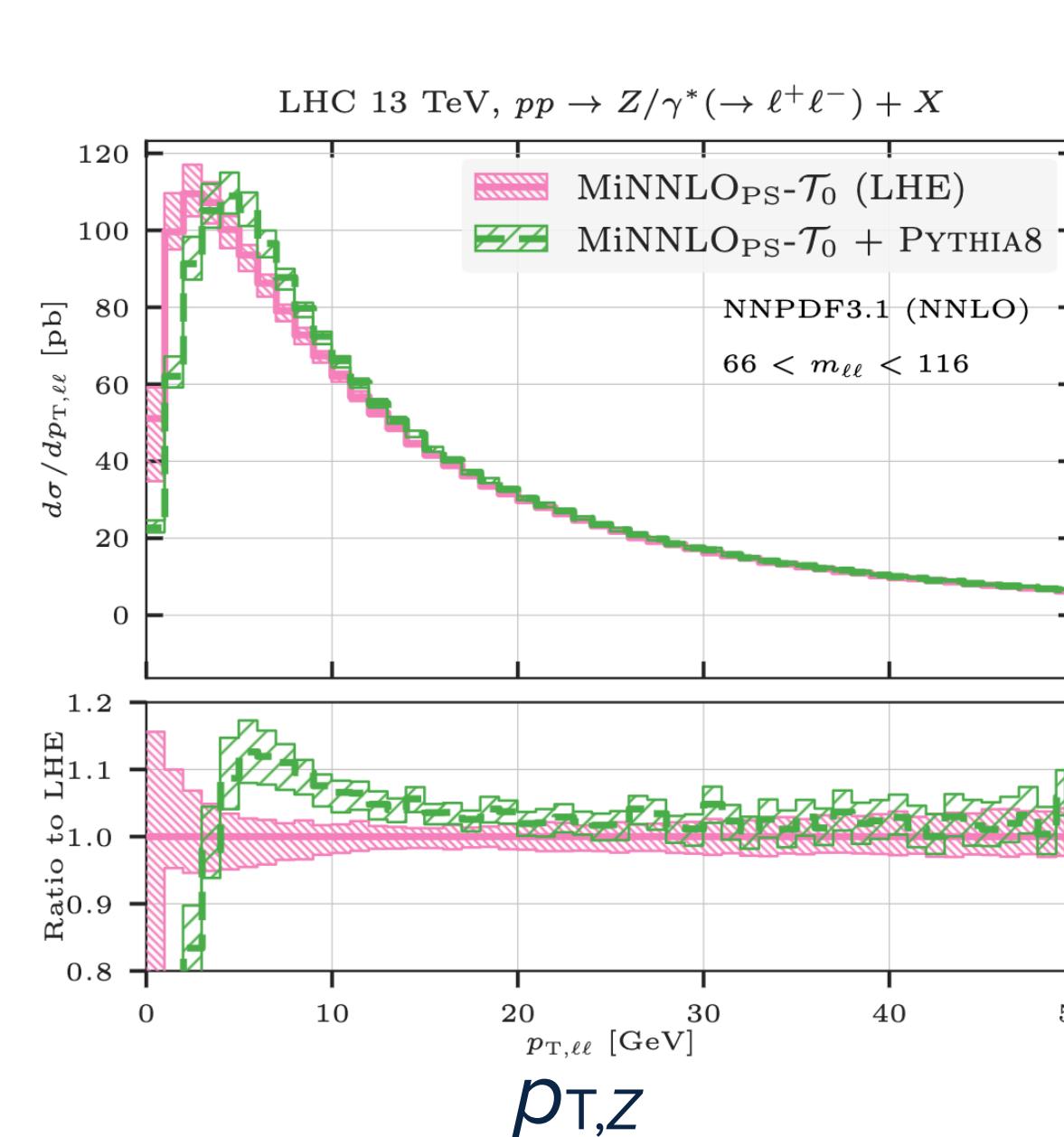
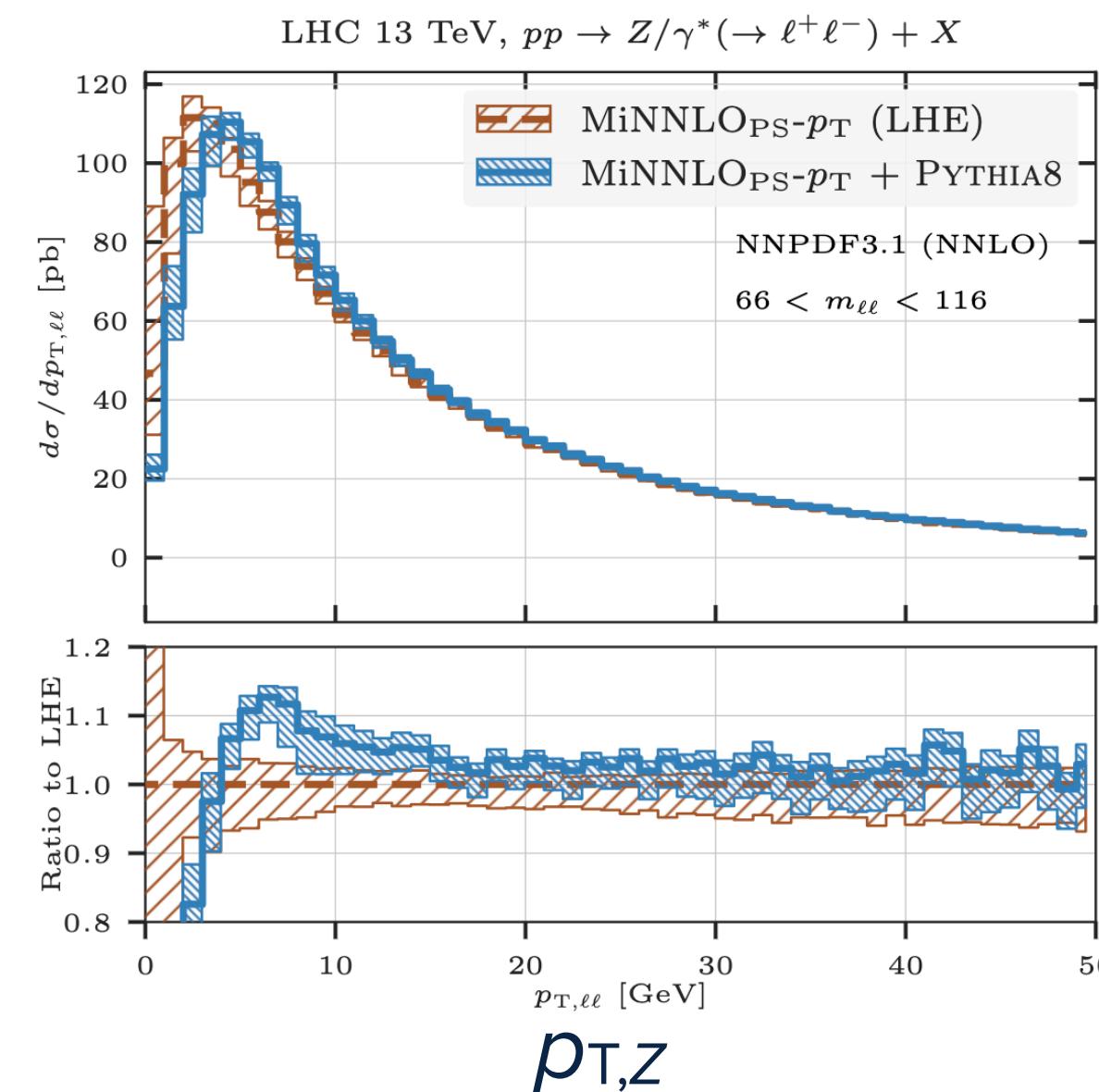
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Our results are anyway reliable because the showers effects are small and they have the same impact in MiNNLO_{PS}- p_T and MiNNLO_{PS}- τ_0 .



- █ MiNNLO_{PS}- p_T (LHE)
- █ MiNNLO_{PS}- p_T (PY8)
- █ MiNNLO_{PS}- τ_0 (LHE)
- █ MiNNLO_{PS}- τ_0 (PY8)

CROSS SECTIONS

[Ebert, Rottoli, Wiesemann, Zanderighi, SZ '24]



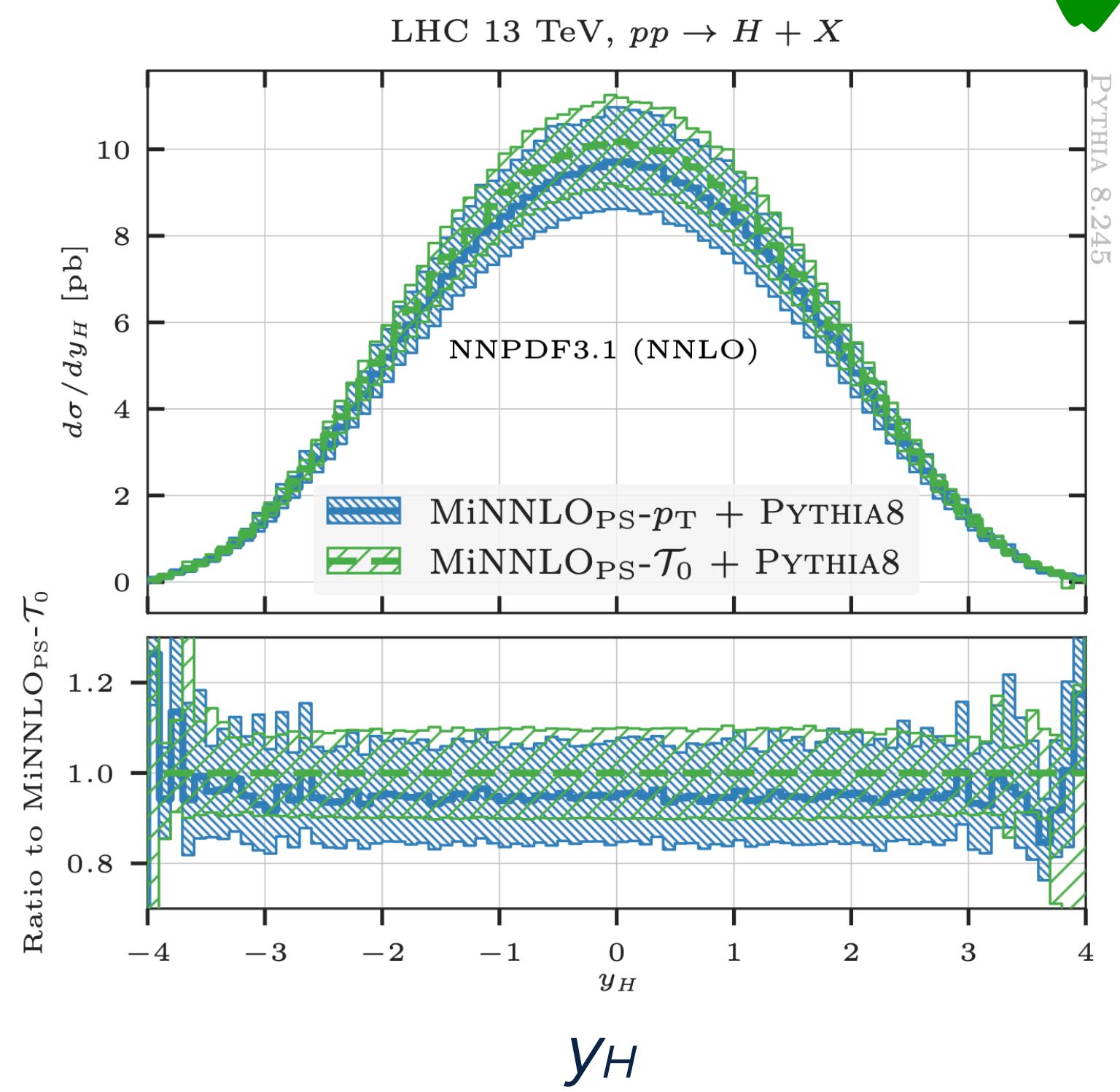
	$pp \rightarrow H$ (on-shell)		$pp \rightarrow Z \rightarrow \ell^+ \ell^-$	
	σ [pb]	$\sigma/\sigma_{\text{NNLO}}$	σ [fb]	$\sigma/\sigma_{\text{NNLO}}$
NNLO	$40.32(2)^{+10.7\%}_{-10.4\%}$	1.000	$1919(1)^{+0.9\%}_{-1.1\%}$	1.000
MiNNLO _{PS} - p_T	$39.33(1)^{+12.2\%}_{-11.0\%}$	0.975	$1907(2)^{+1.1\%}_{-1.2\%}$	0.994
MiNNLO _{PS} - \mathcal{T}_0	$41.56(2)^{+9.4\%}_{-10.1\%}$	1.031	$1925(1)^{+1.2\%}_{-1.2\%}$	1.003

NOTE: the two MiNNLOPS descriptions differ by terms beyond accuracy, so they are expected to agree within error bands.

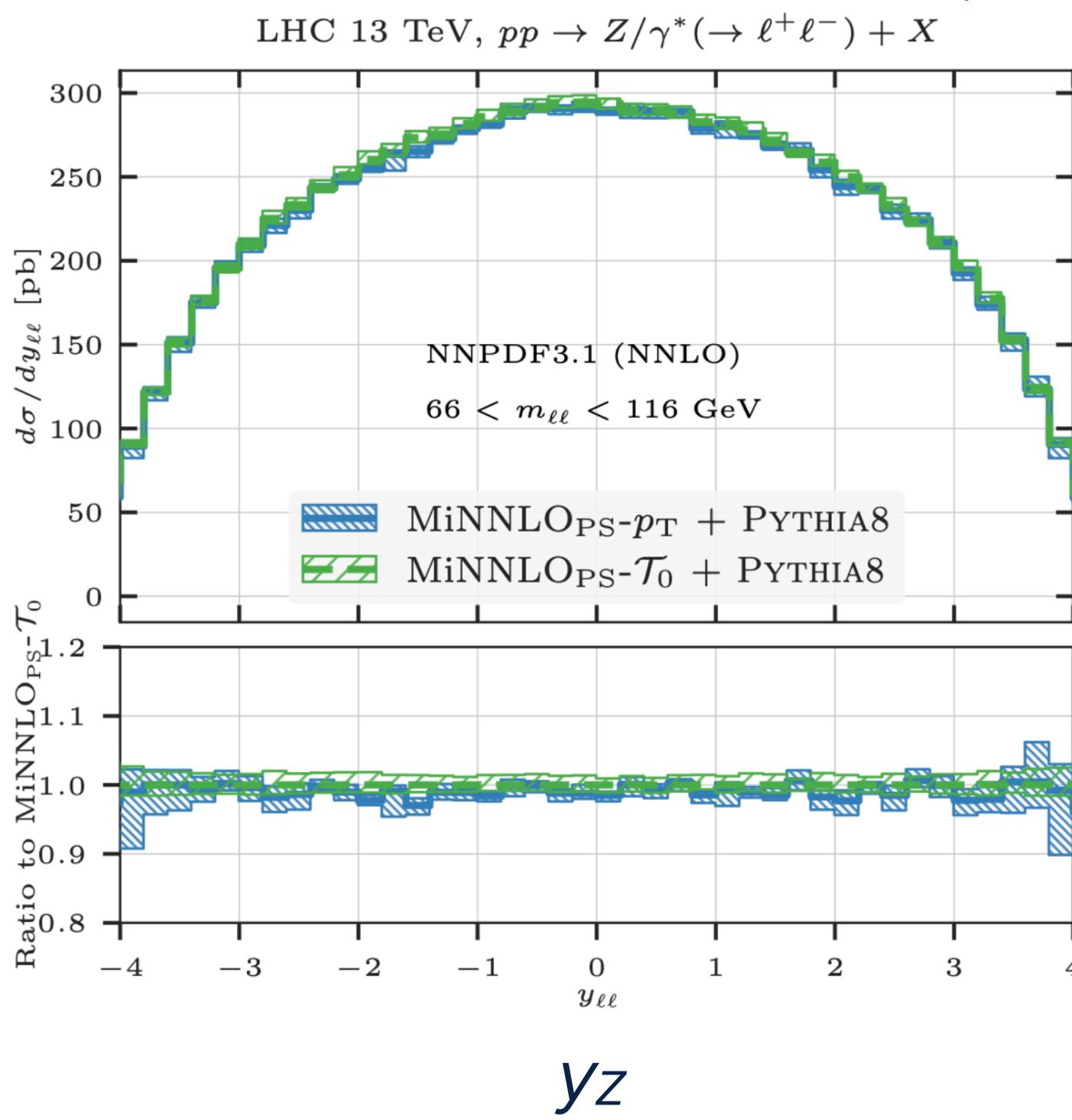
NNLO OBSERVABLES

[Ebert, Rottoli, Wiesemann, Zanderighi, SZ '24]

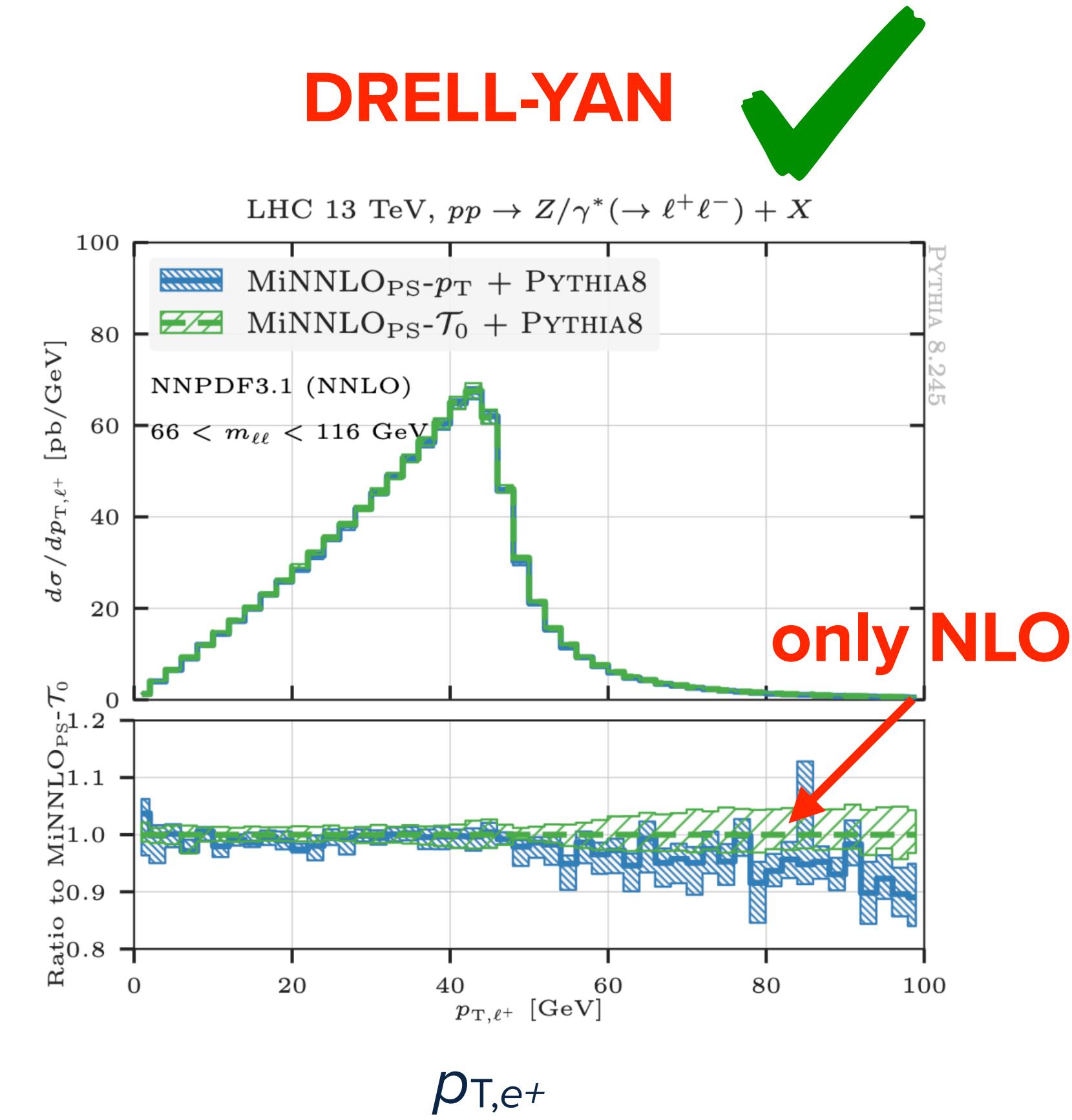
H PRODUCTION



DRELL-YAN



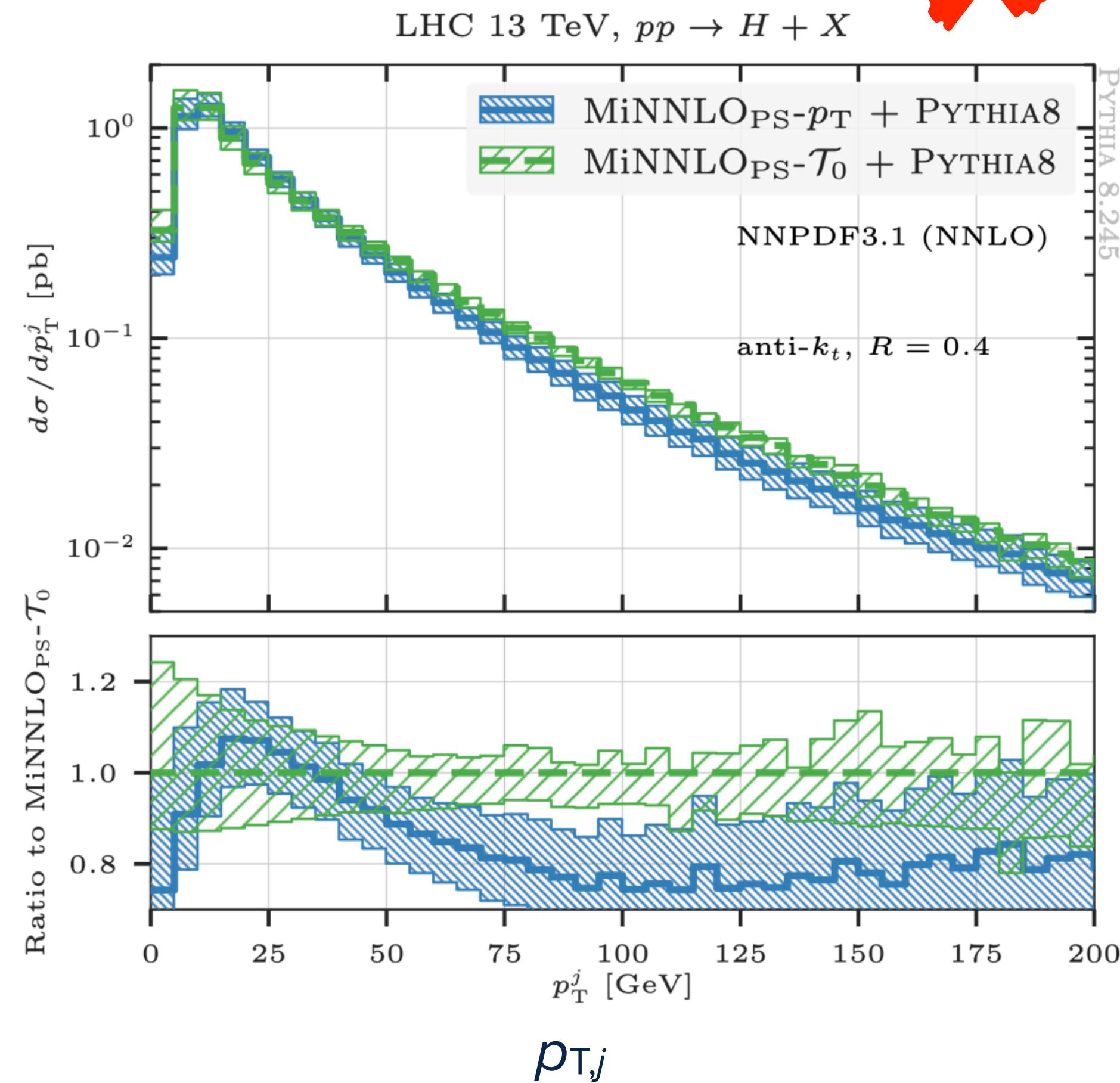
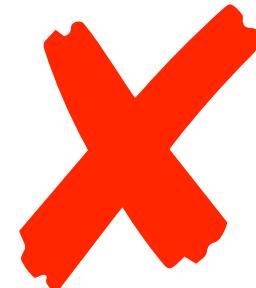
DRELL-YAN



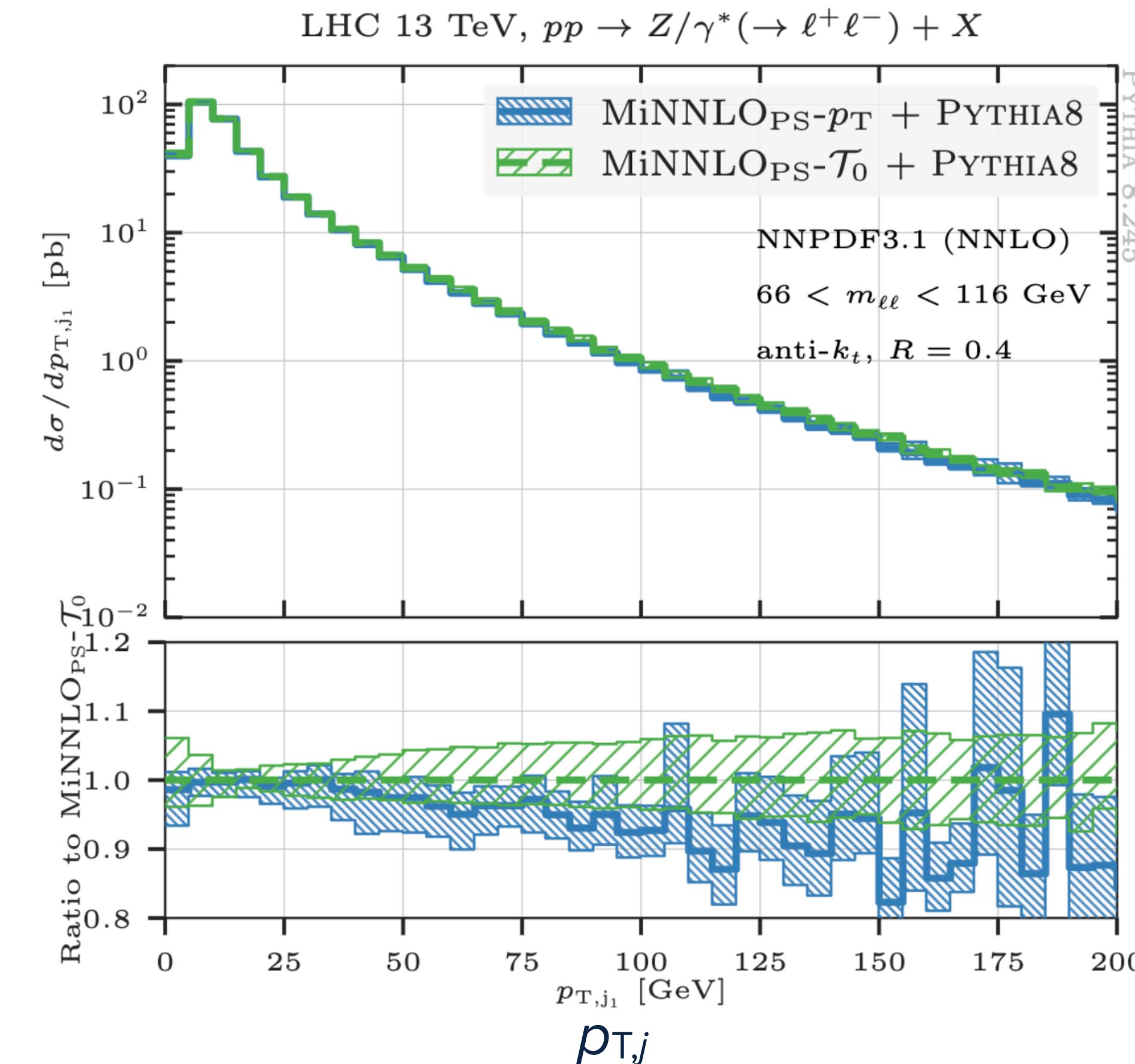
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H PRODUCTION



DRELL-YAN

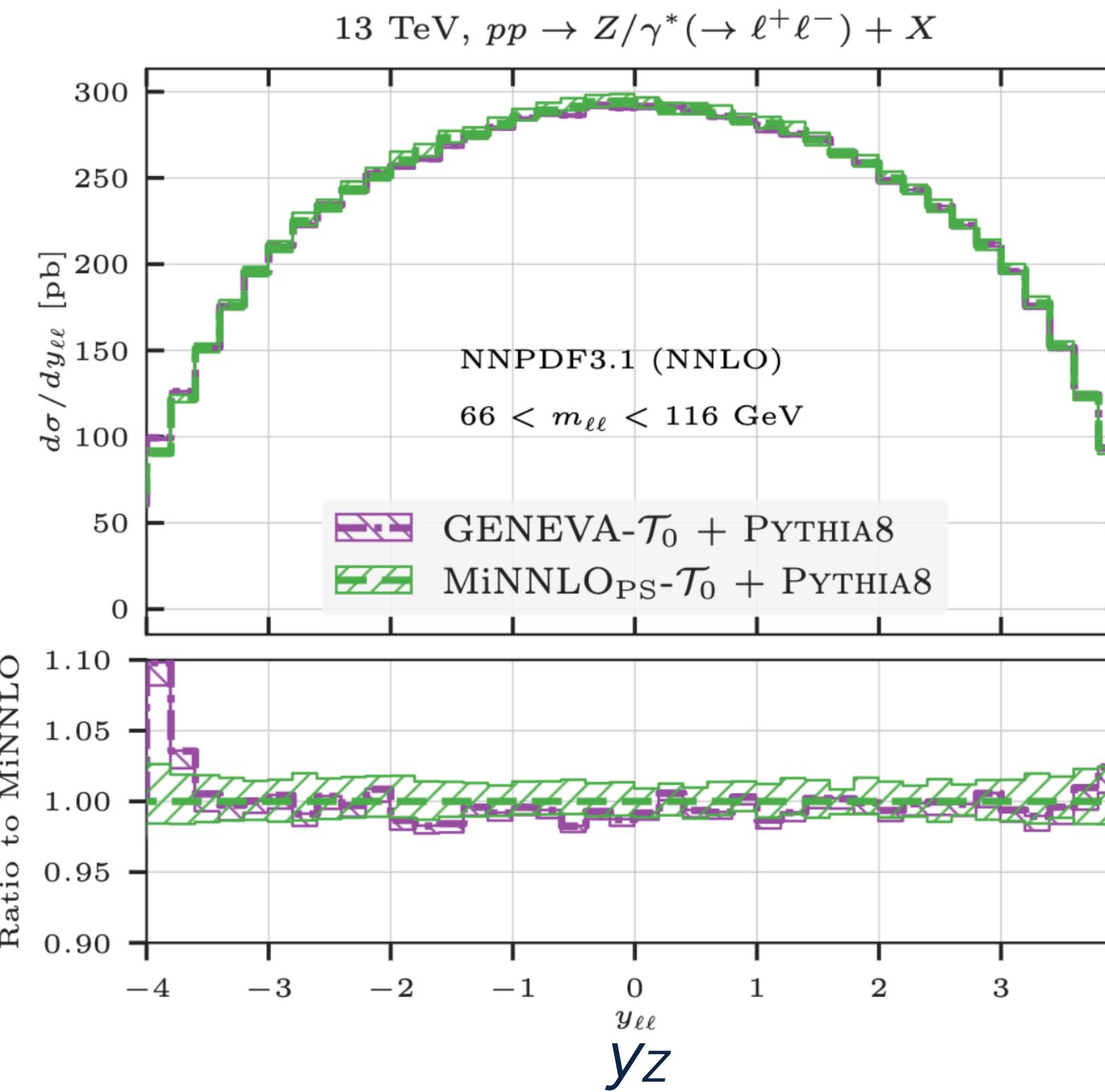


Large differences between MiNNLO- p_{T} and MiNNLO- τ_0 for H production **not covered by scale variation.**

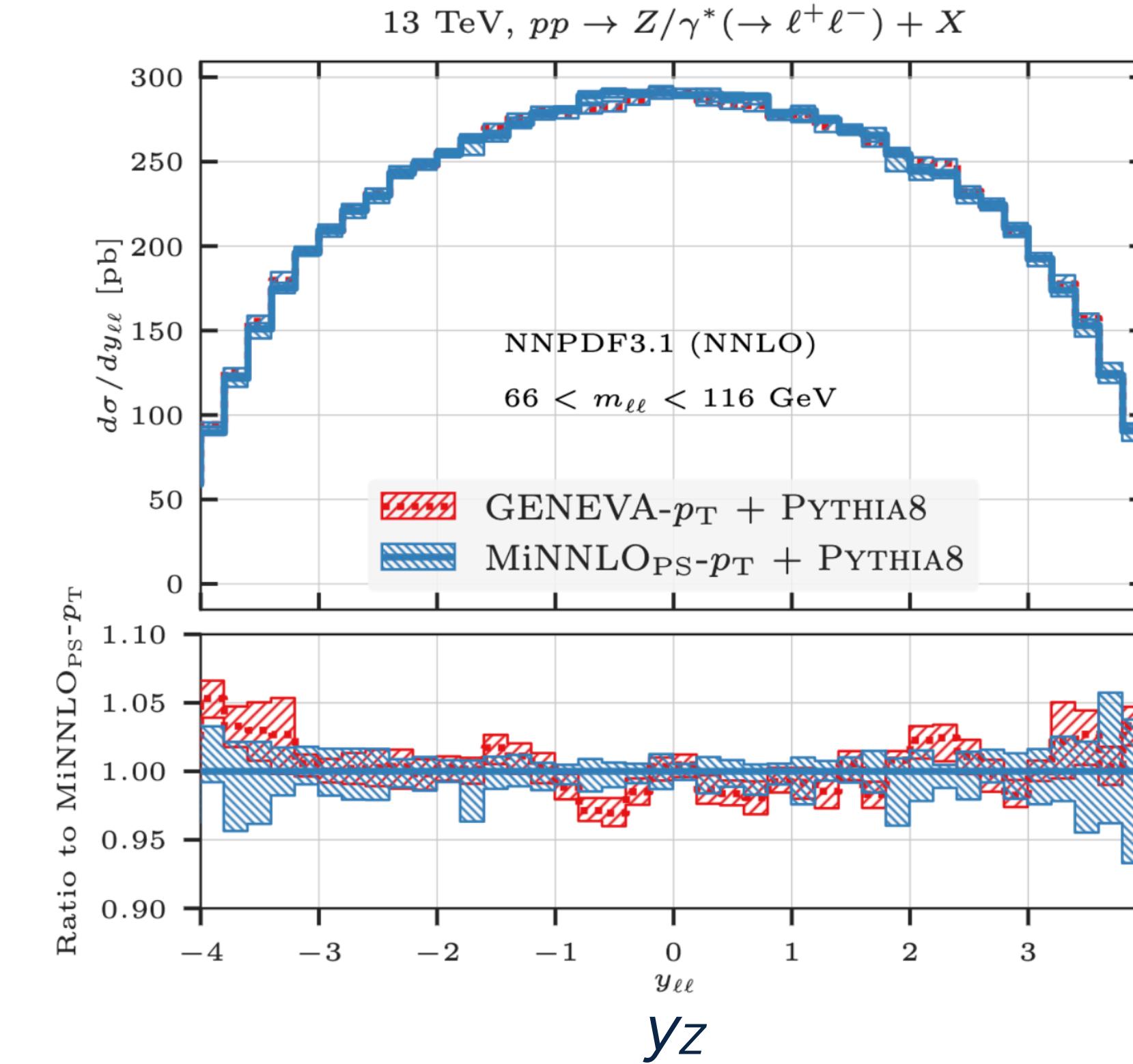
COMPARISON WITH GENEVA - DY

[Ebert, Rottoli, Wiesemann, Zanderighi, SZ '24]

MiNNLO_{PS}- τ_0 vs GENEVA- τ_0



MiNNLO_{PS}- p_T vs GENEVA- p_T

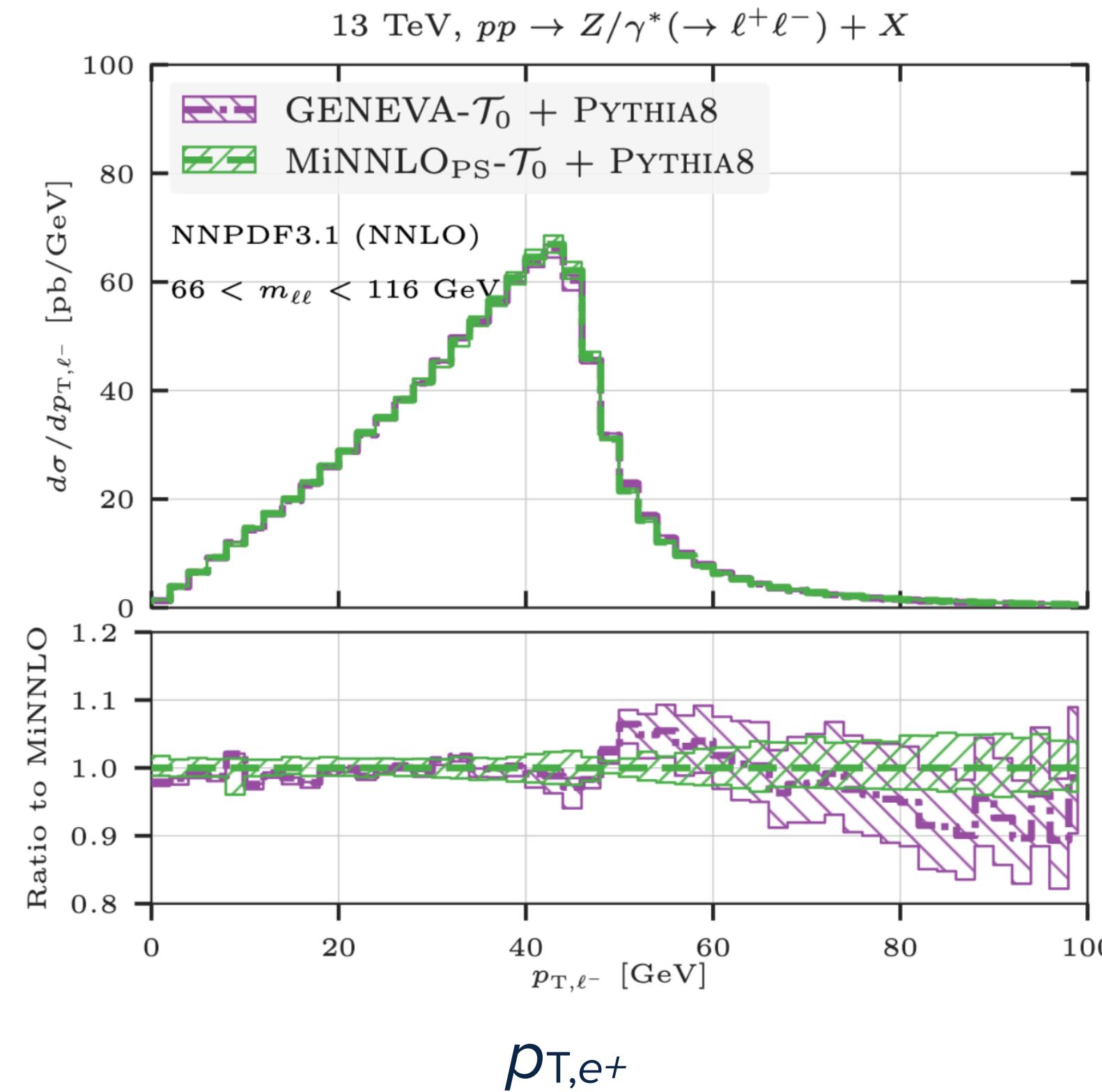


NOTE: GENEVA error bars are obtained through 3-point scale variation.

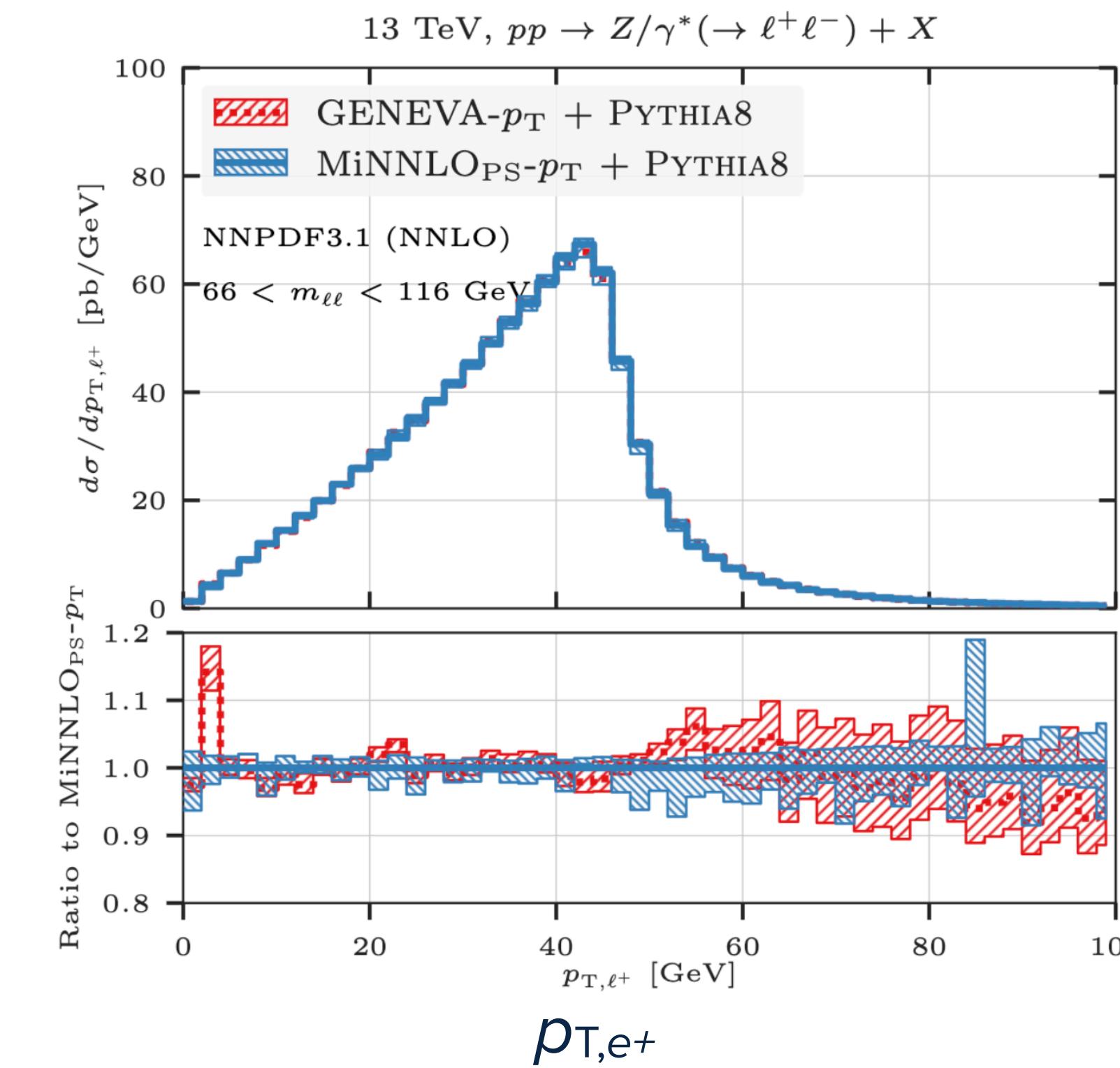
COMPARISON WITH GENEVA - DY

[Ebert, Rottoli, Wiesemann, Zanderighi, SZ '24]

MiNNLO_{PS}- τ_0 vs GENEVA- τ_0



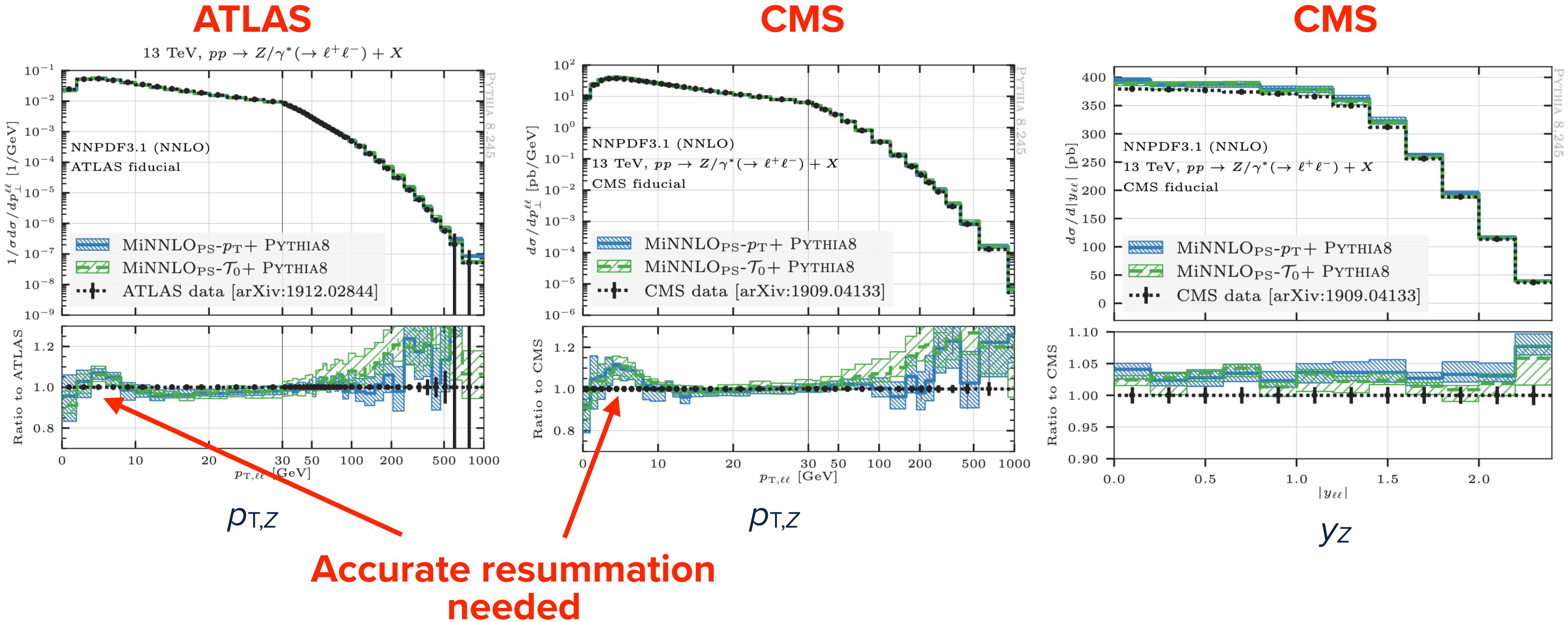
MiNNLO_{PS}- p_T vs GENEVA- p_T



NOTE: GENEVA error bars are obtained through 3-point scale variation.

COMPARISON WITH DY DATA ✓

[Ebert, Rottoli, Wiesemann, Zanderighi, SZ '24]



Good agreement (1-2 σ) between MiNNLO_{PS} predictions and data.

SUMMARY

- **NNLO+PS** accuracy is the **state-of-the art** for precision physics at the LHC.
- **The MiNNLO_{PS} method is a powerful framework** to reach this accuracy.
- **Extending MiNNLO_{PS} to processes with jets is not trivial.**
 - **MiNNLO_{PS} based on 0-jettiness resummation:** I presented the theoretical formalism and discussed phenomenological results for Higgs production and Drell-Yan process. We found **very good agreement for NNLO observables, while discrepancies are present for NLO ones (in the Higgs case).**
 - The **comparison with GENEVA shows a nice agreement between the two methods**, both for the p_T and the jettiness formalisms.
 - **We obtained a good agreement with ATLAS and CMS data.**
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Thank you!