

Seeded Vacuum Decay

Ian Moss
September 2024

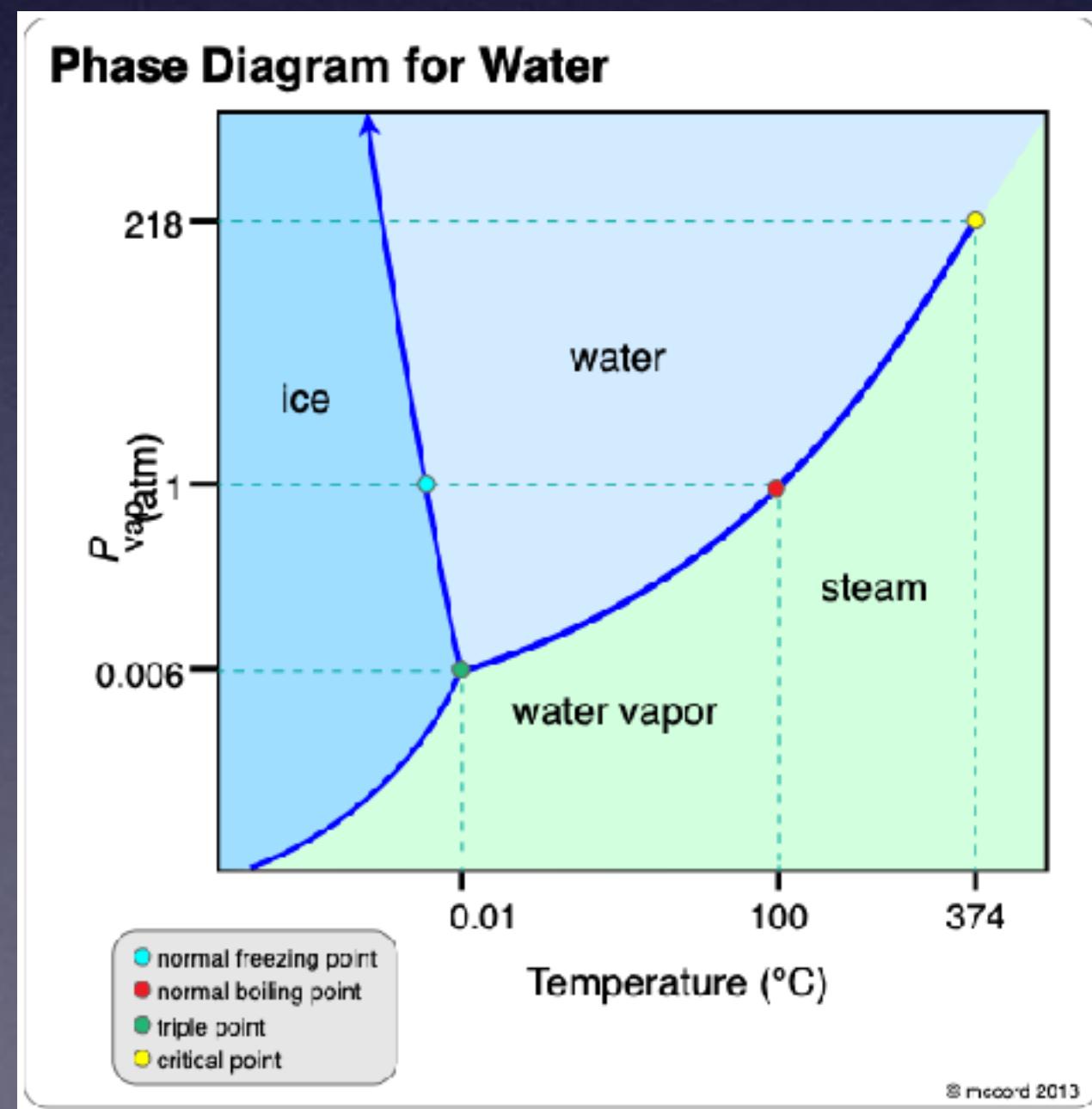
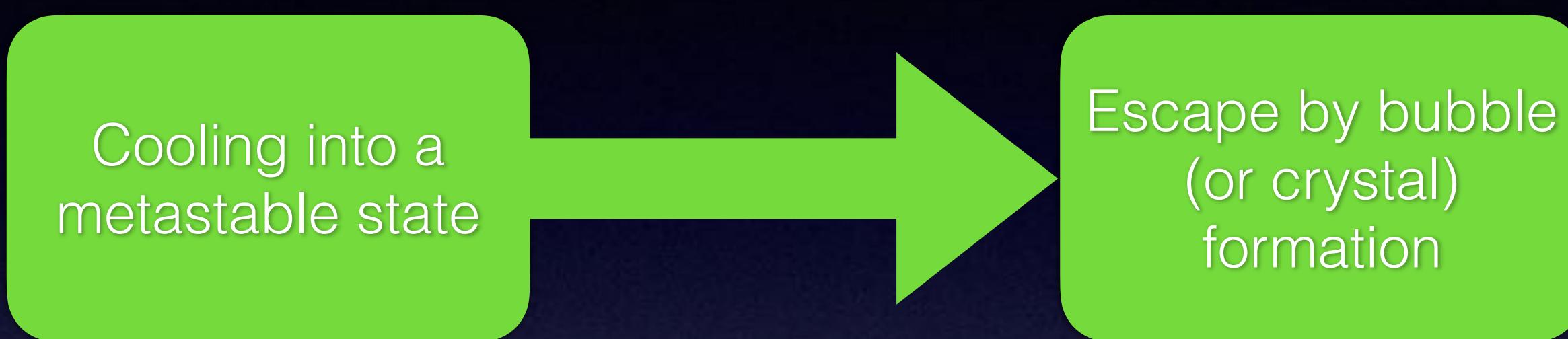


M. Caneletti, I Moss hep-th/2408.12229

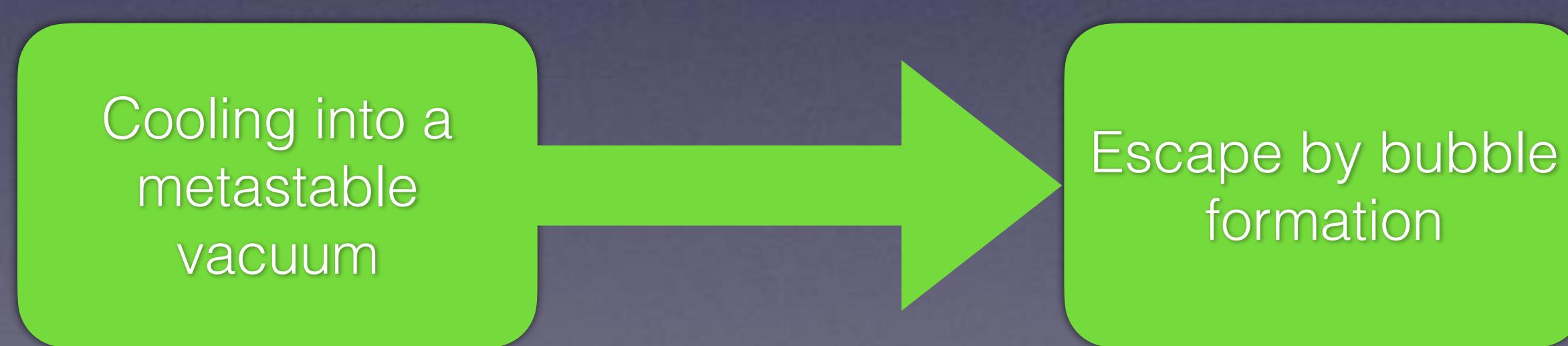
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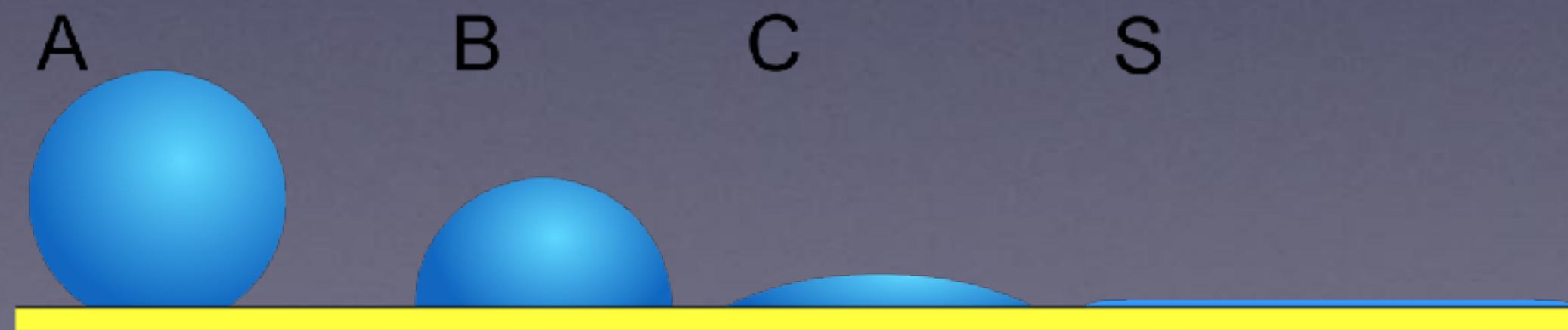
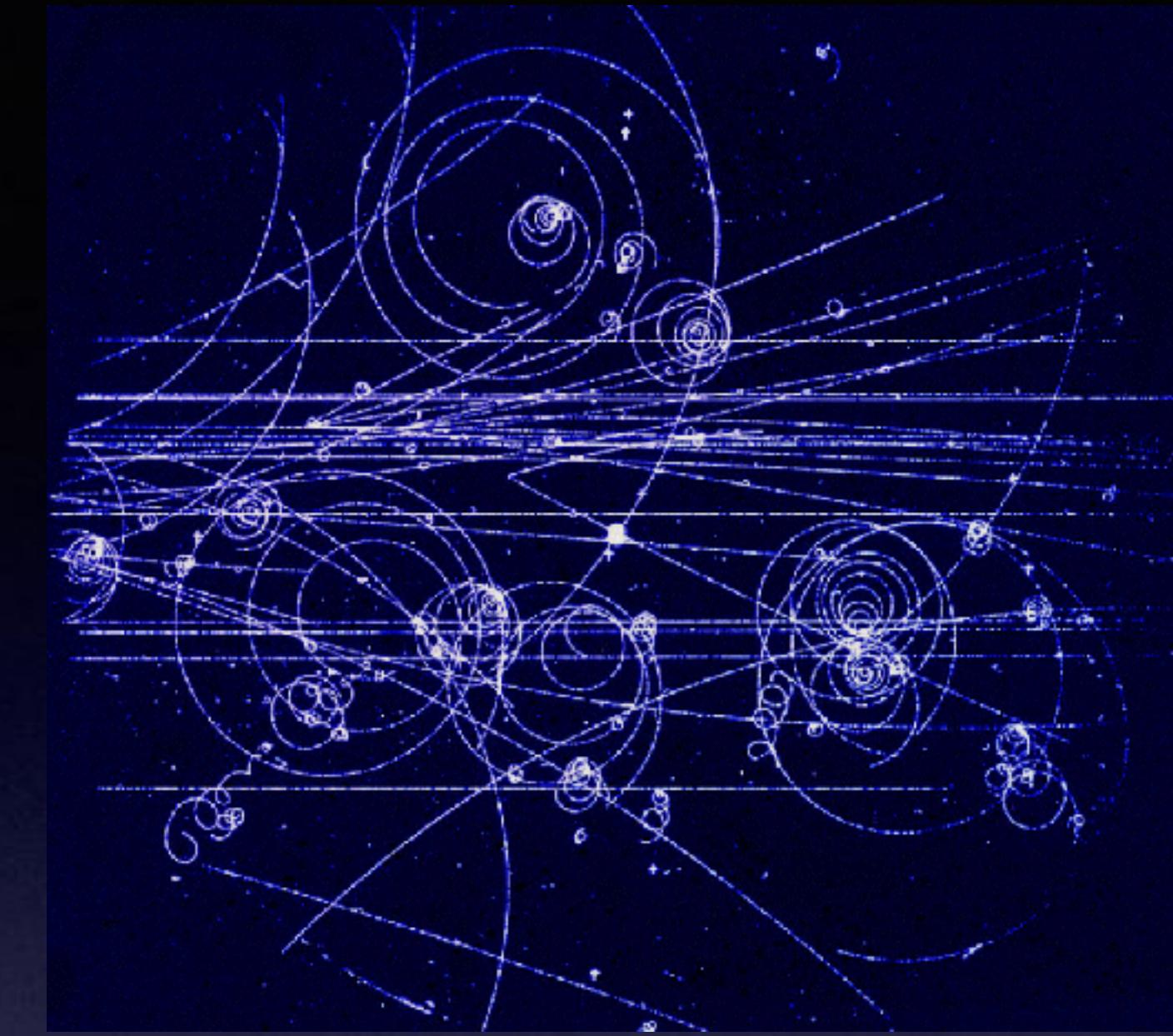
Bubble nucleation



False vacuum decay



Nucleation seeds



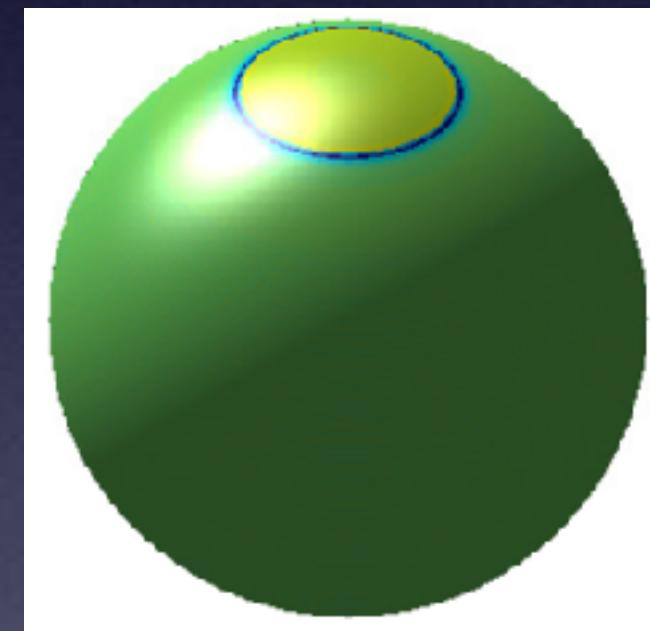
MesserWoland



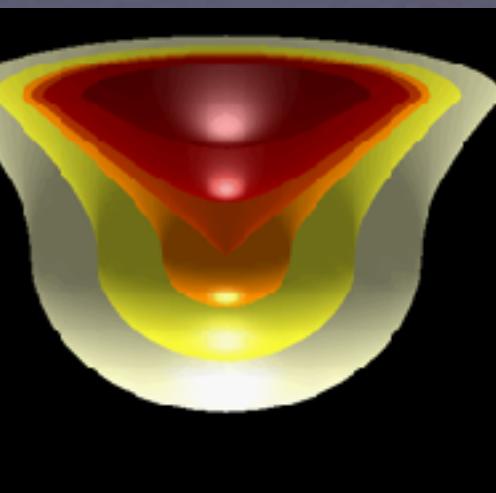
TheBrockenInaGlory

Bubble nucleation in cosmology

CMB distortions

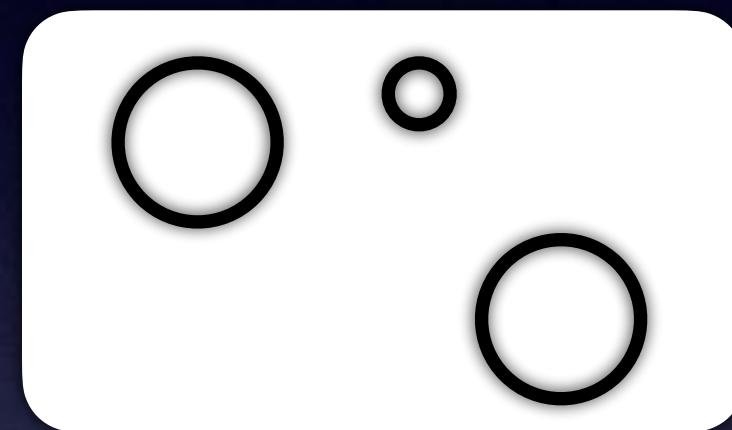


McEwen et al. 1202.2861

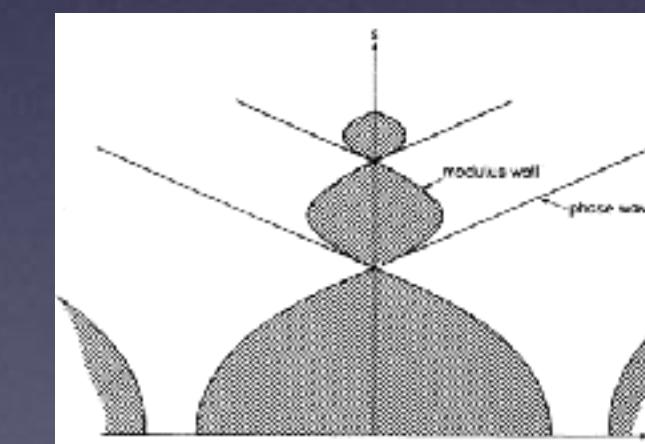


universe from nothing

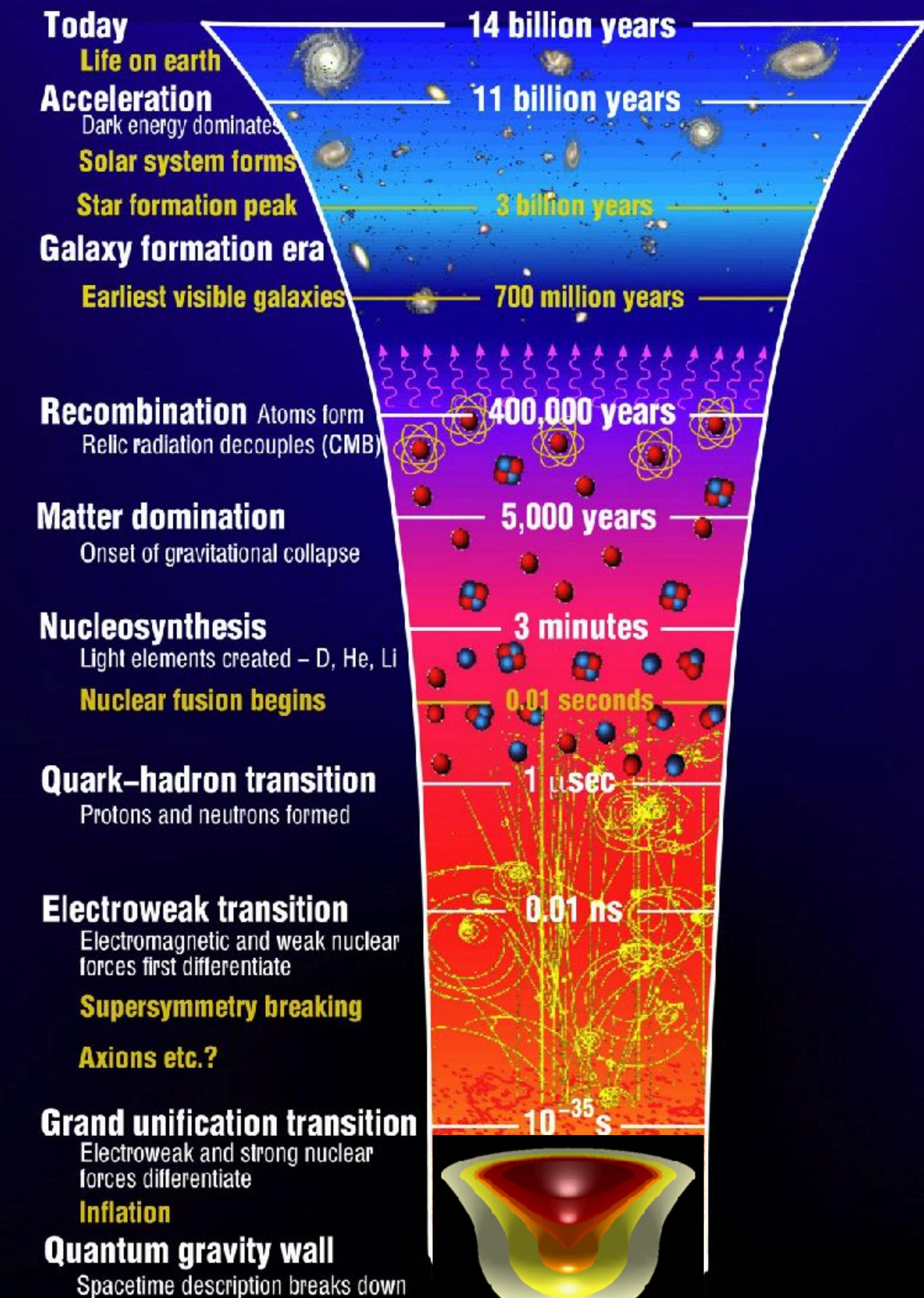
gravitational waves



baryogenesis

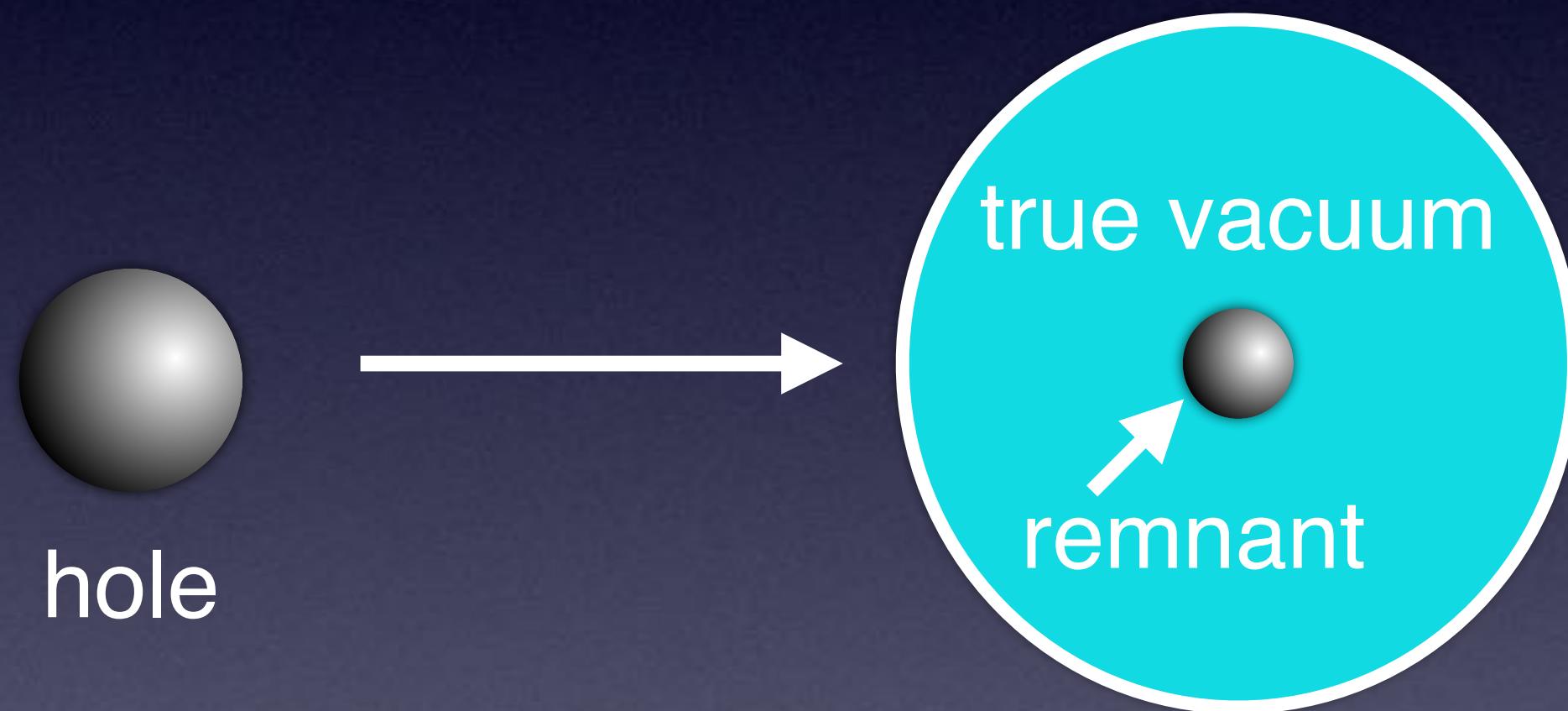


black holes

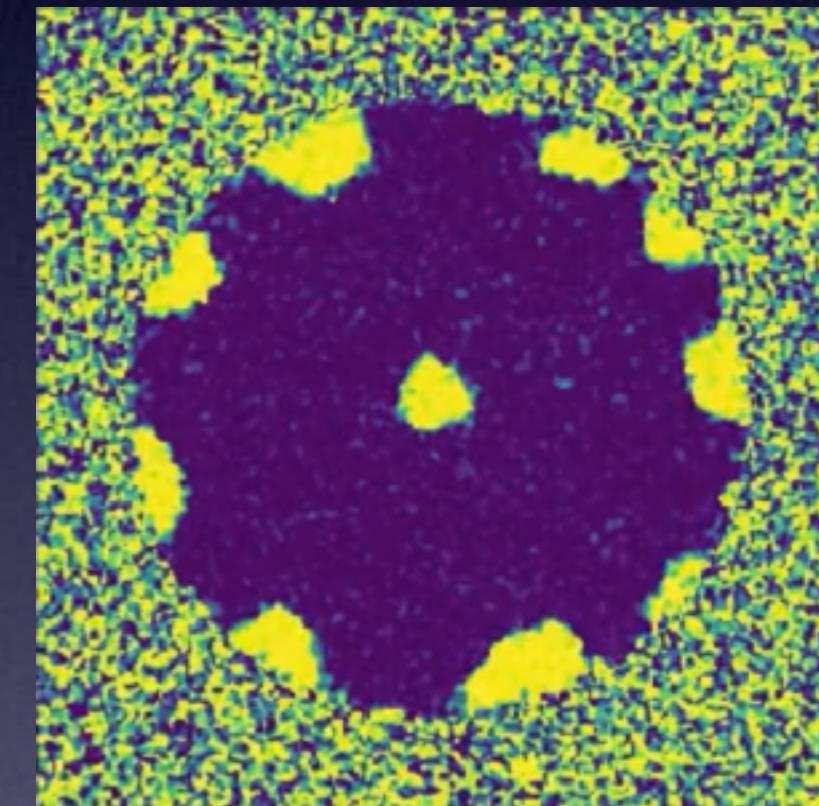


Seeded vacuum decay

Black holes



Vortices



BEC in a trap

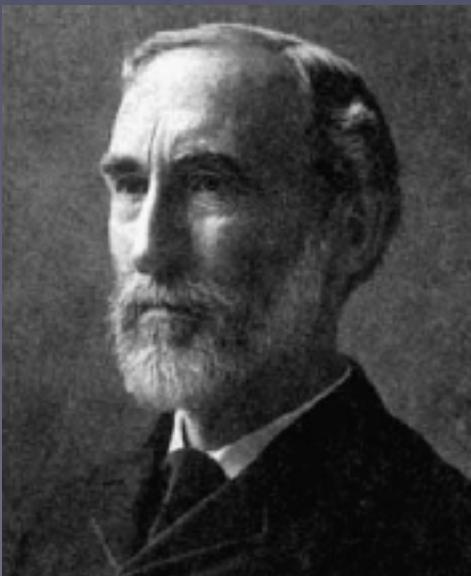
Vortex in the
centre

Critical Nucleation Theory

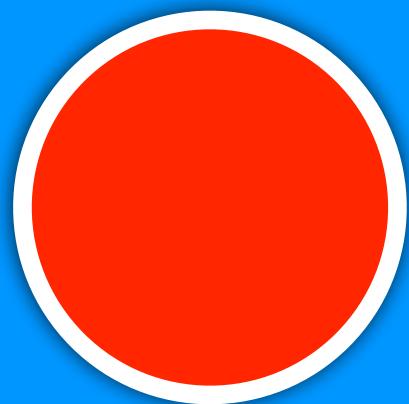
Critical bubbles in a thermal metastable state: Josiah Gibbs 1878!

Probability of a bubble fluctuation $\propto e^{\Delta S/k_B}$

Entropy changes by $\Delta S = -\frac{\Delta E}{T}$



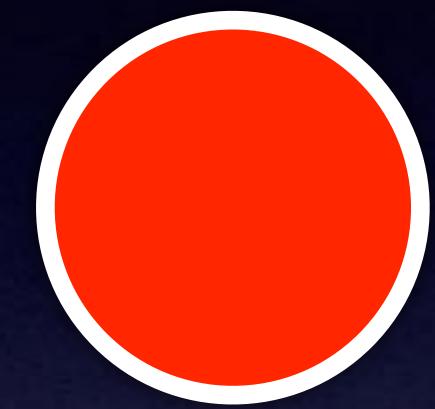
metastable phase



J. W Gibbs, Equilibrium of heterogeneous substances, 1878, p416

Critical Nucleation Theory

$$\Delta E = 4\pi R^2 \sigma - \frac{4}{3}\pi R^3 \epsilon$$



σ surface tension

ϵ energy density lower

Critical case

$$\frac{d\Delta E}{dR} = 0 \quad R_c = \frac{2\sigma}{\epsilon}$$

$$\text{Nucleation rate} \quad \Gamma = \frac{N}{R_c^3} \frac{k_B T}{h} \left(\frac{\Delta E_c}{k_B T} \right)^{1/2} e^{-\Delta E_c / k_B T}$$

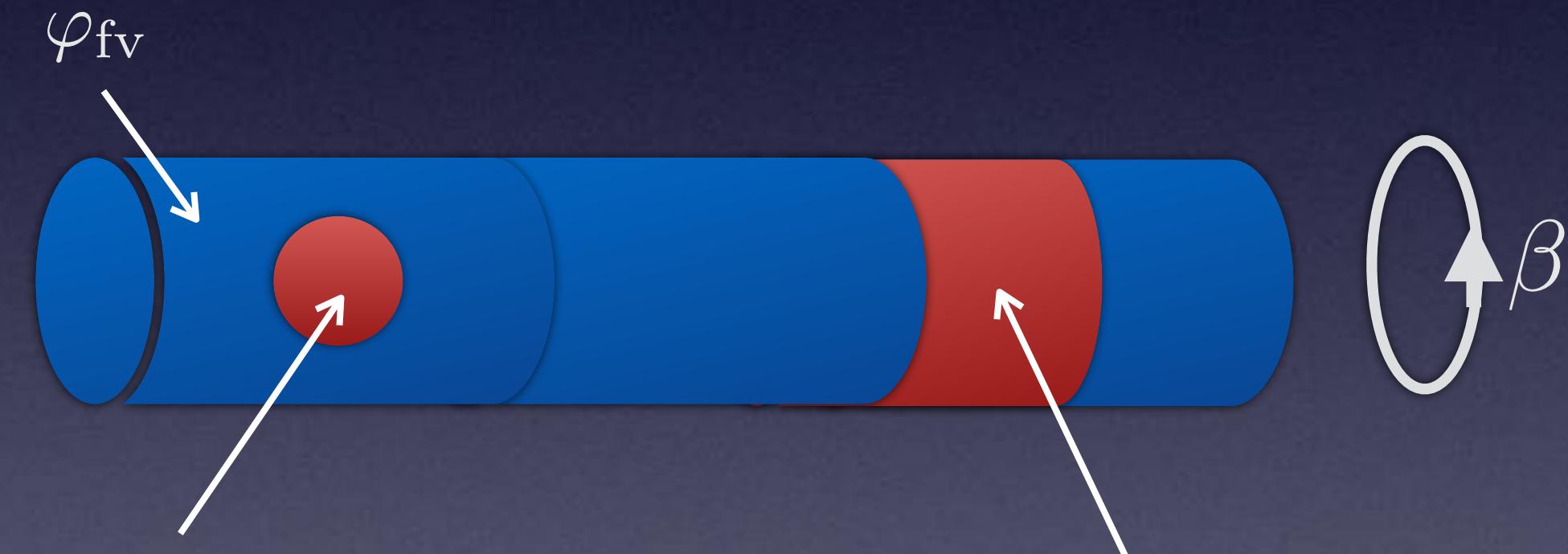
$\Delta S/k_B$

False vacuum decay

In quantum field theory, replace the bubble by a ‘bounce’ instanton, a solution to the field equations with **imaginary** time τ .

$$S_E = \int \left\{ \frac{1}{2} \nabla \varphi^2 + V(\varphi) \right\}$$

local potential minimum



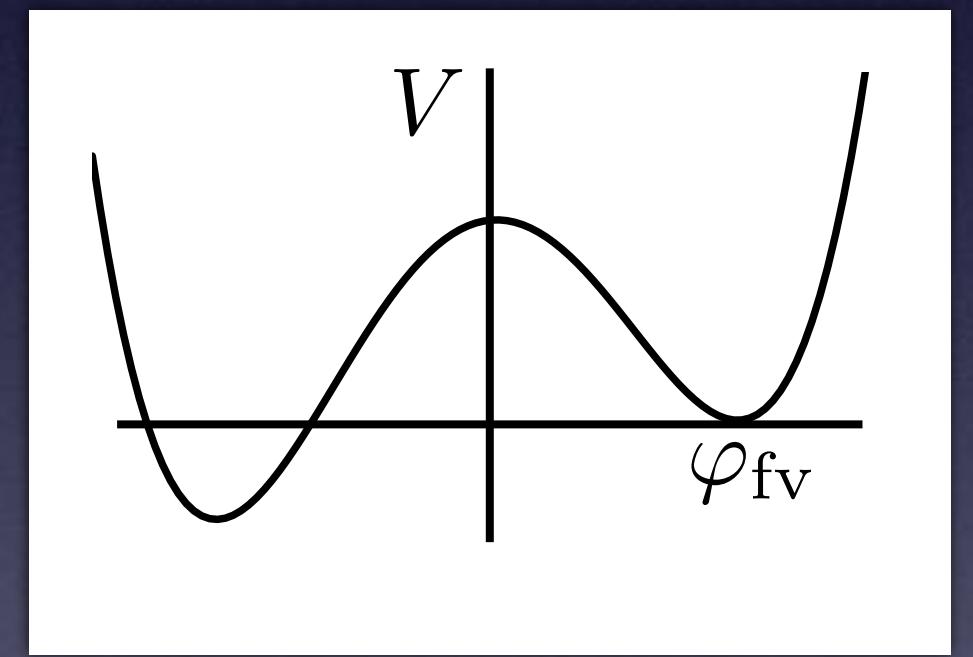
false vacuum decay

$$\varphi = \varphi(\sqrt{x^2 + \tau^2})$$

false vacuum decay
at finite temperature

$$\varphi = \varphi(x)$$

$$\beta = \hbar/k_B T$$



Coleman, Phys Rev D15 2929 1977

False vacuum decay rate

$$\Gamma = \left| \frac{\det' S_E''[\varphi_b]}{\det S_E''[\varphi_{fv}]} \right|^{-1/2} \left(\frac{S_E[\varphi_b]}{2\pi\hbar} \right)^{n/2} e^{-S_E[\varphi_b]/\hbar}$$

product of the eigenvalues

excluded zero modes (translations)

inertial frame?

correlations?

renormalisation?

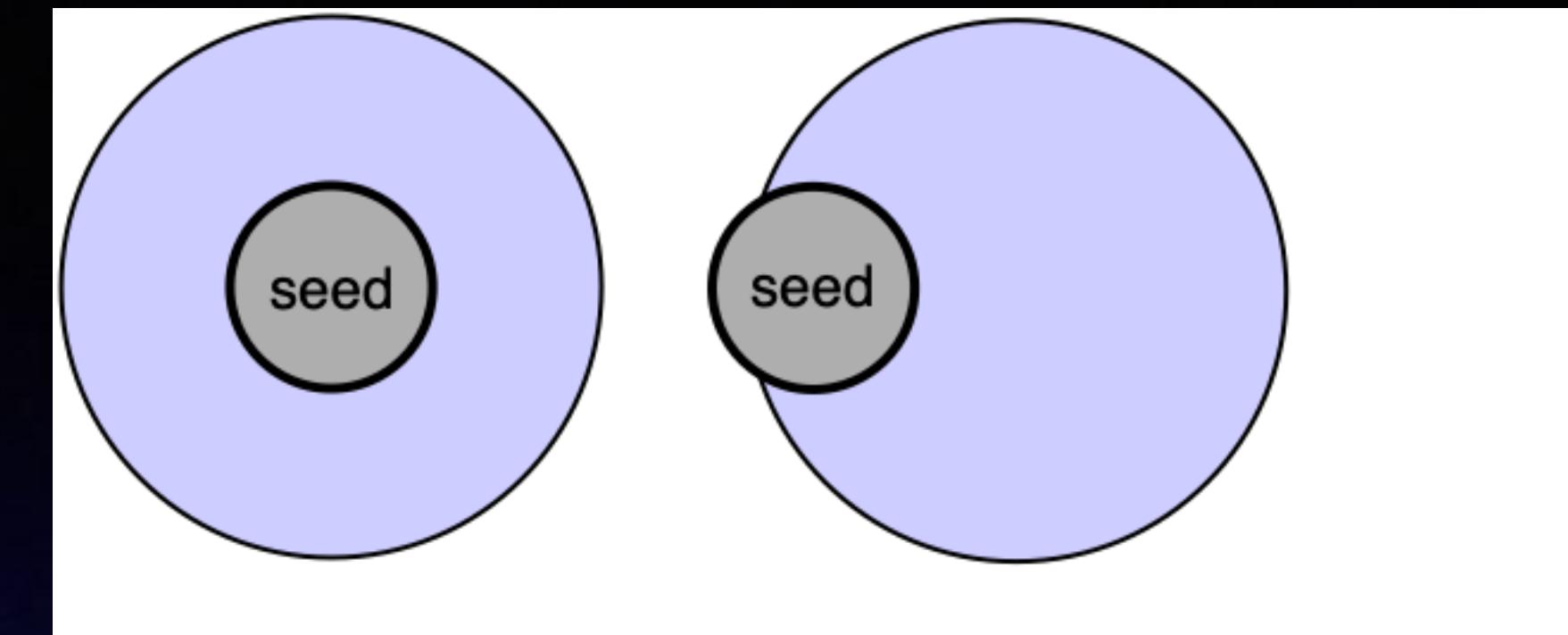
does some other process dominate vacuum decay?

big difference between QFT and QM of single particles

exists?
singular?

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graph TD; Gamma["\Gamma = \left| \frac{\det' S_E''[\varphi_b]}{\det S_E''[\varphi_{fv}]} \right|^{-1/2} \left( \frac{S_E[\varphi_b]}{2\pi\hbar} \right)^{n/2} e^{-S_E[\varphi_b]/\hbar}"]; Gamma -- "product of the eigenvalues" --> Prod["product of the eigenvalues"]; Gamma -- "excluded zero modes (translations)" --> Trans["excluded zero modes (translations)"]; Gamma -- "inertial frame?" --> Inertial["inertial frame?"]; Gamma -- "correlations?" --> Correlations["correlations?"]; Gamma -- "renormalisation?" --> Renormalisation["renormalisation?"]; Gamma -- "exists? singular?" --> Exist["exists? singular?"]; Gamma -- "does some other process dominate vacuum decay?" --> OtherProcess["does some other process dominate vacuum decay?"]; Gamma -- "big difference between QFT and QM of single particles" --> QFTQM["big difference between QFT and QM of single particles"];
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Seeded nucleation



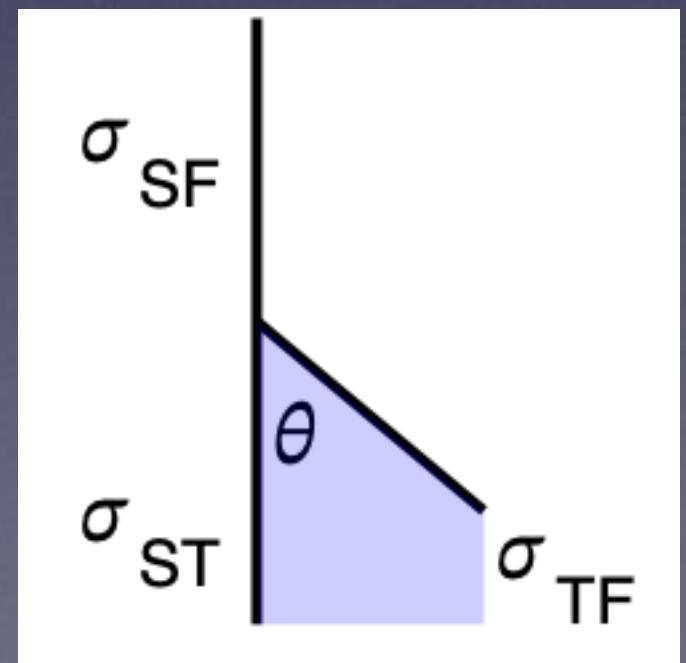
Laplace's relation

$$\frac{1}{R_1} + \frac{1}{R_2} = \frac{\epsilon}{\sigma_{TF}}$$

$$R = \frac{2R_1 R_2}{R_1 + R_2} = \frac{2\epsilon}{\sigma_{TF}}$$

Young's equation

$$\cos \theta = \frac{\sigma_{SF} - \sigma_{ST}}{\sigma_{FT}}$$



σ_{ST} between the seed and the true vacuum phase
 σ_{SF} between the seed and the false vacuum phase
 σ_{TF} between the true and the false vacuum phase

Seeded nucleation rates

$$\Gamma = \frac{N}{R_c^3} \frac{k_B T}{h} \left(\frac{\Delta E_c}{k_B T} \right)^{1/2} e^{-\Delta E_c / k_B T}$$

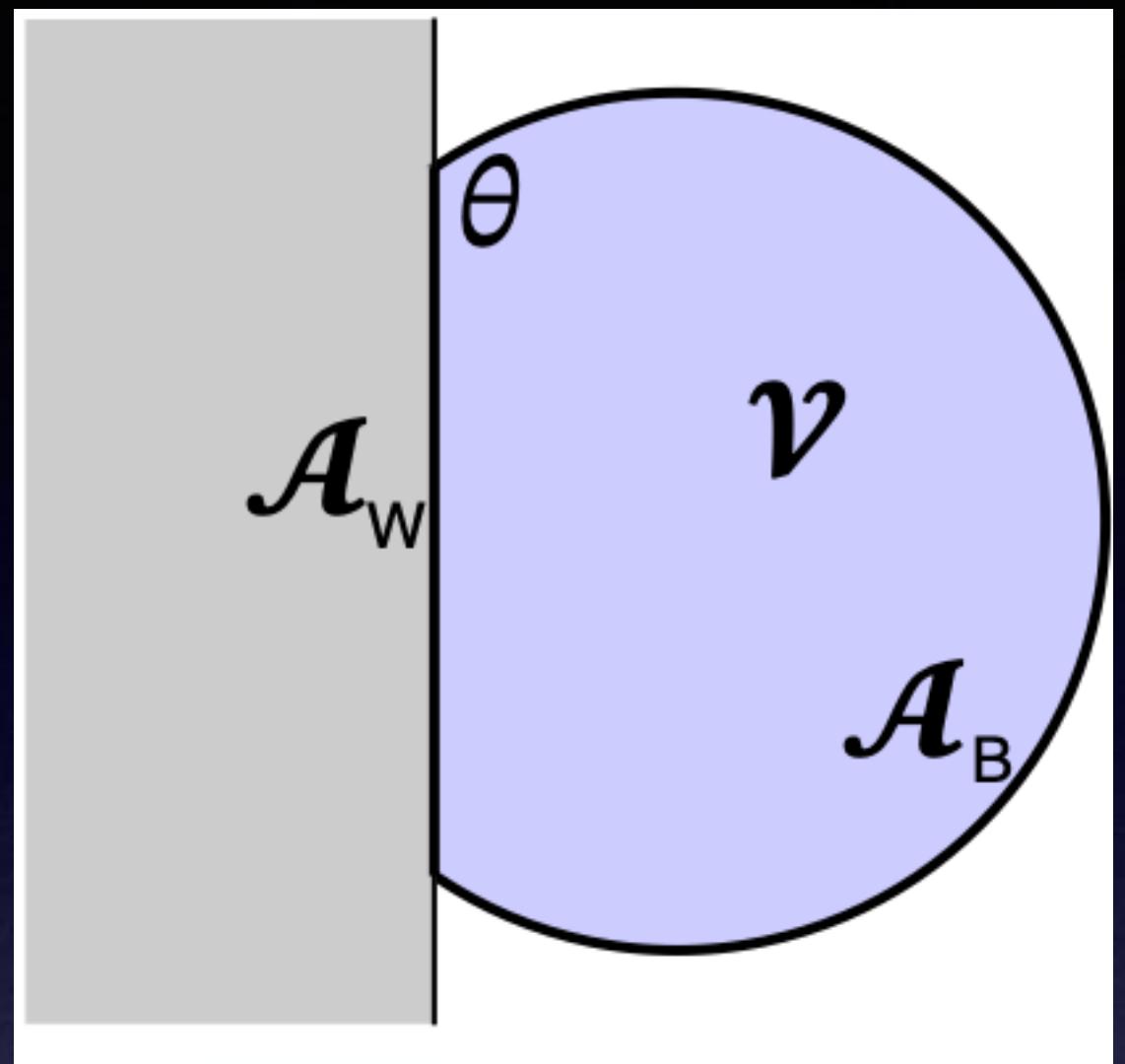
The energy difference between bubble and no bubble is

$$\Delta E = \mathcal{A}_W \sigma_{ST} + \mathcal{A}_B \sigma_{FT} - \mathcal{A}_W \sigma_{SF} - \epsilon \mathcal{V}.$$

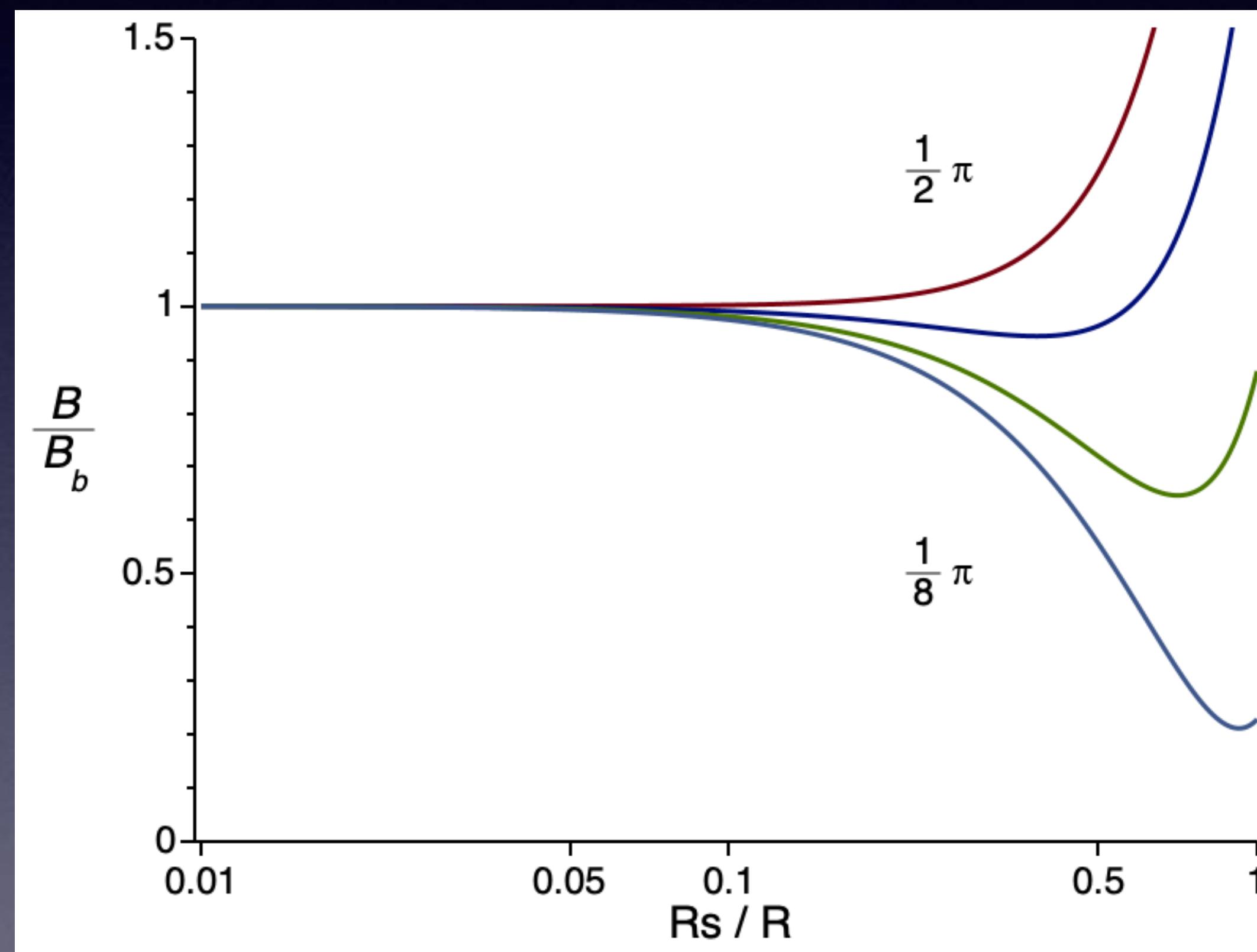
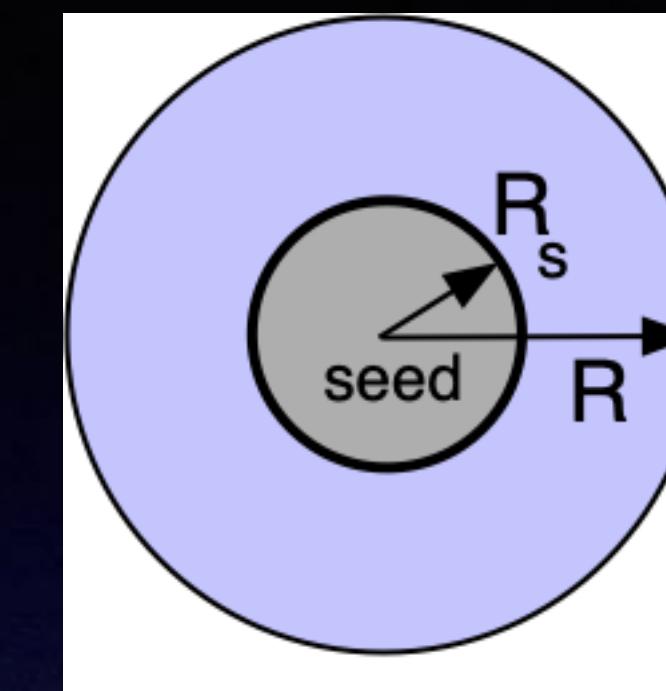
Young's relation implies

$$\Delta E = (\mathcal{A}_B - \mathcal{A}_W \cos \theta) \sigma_{FT} - \epsilon \mathcal{V}$$

$$\cos \theta = \frac{\sigma_{SF} - \sigma_{ST}}{\sigma_{FT}}$$

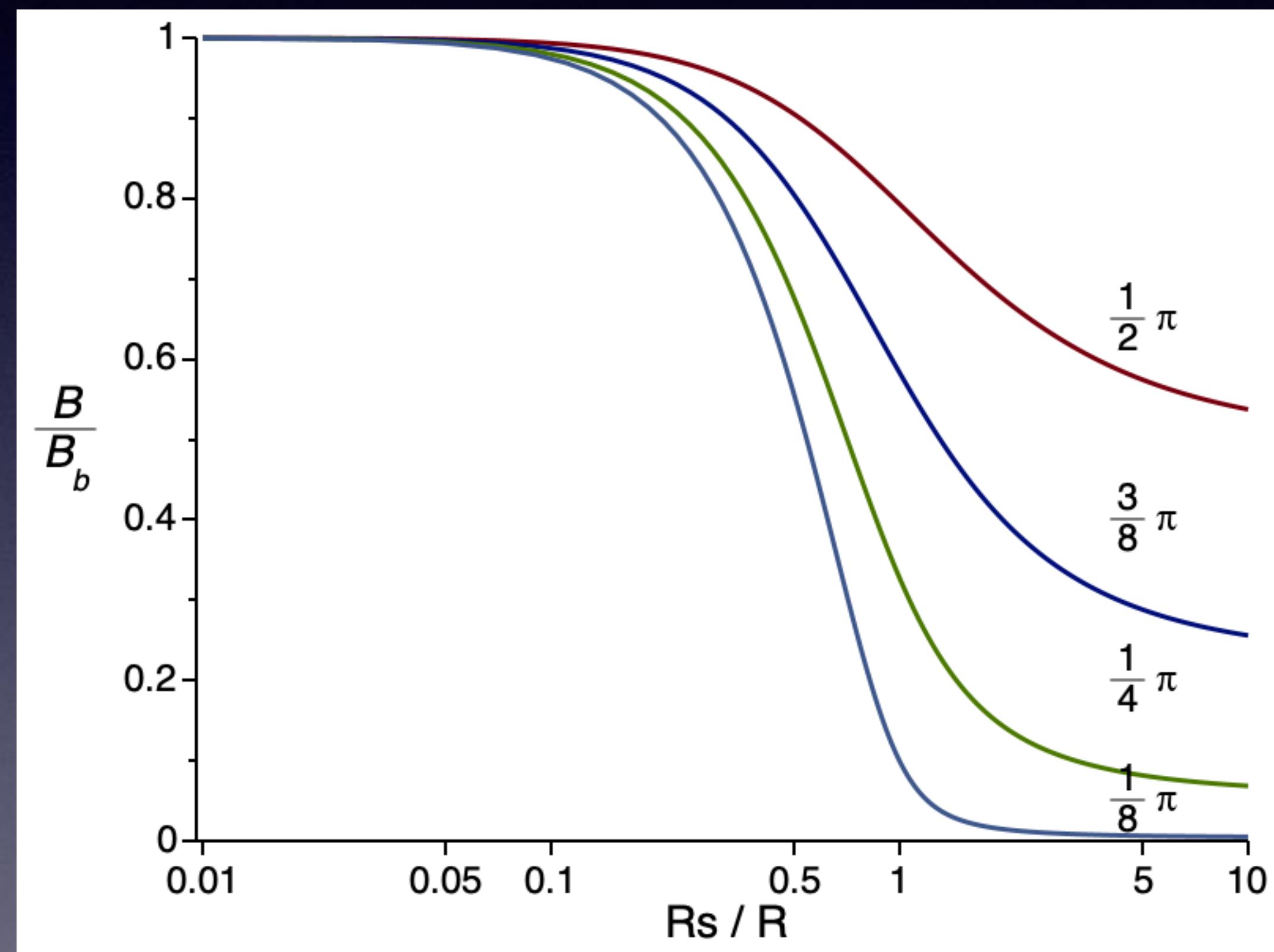
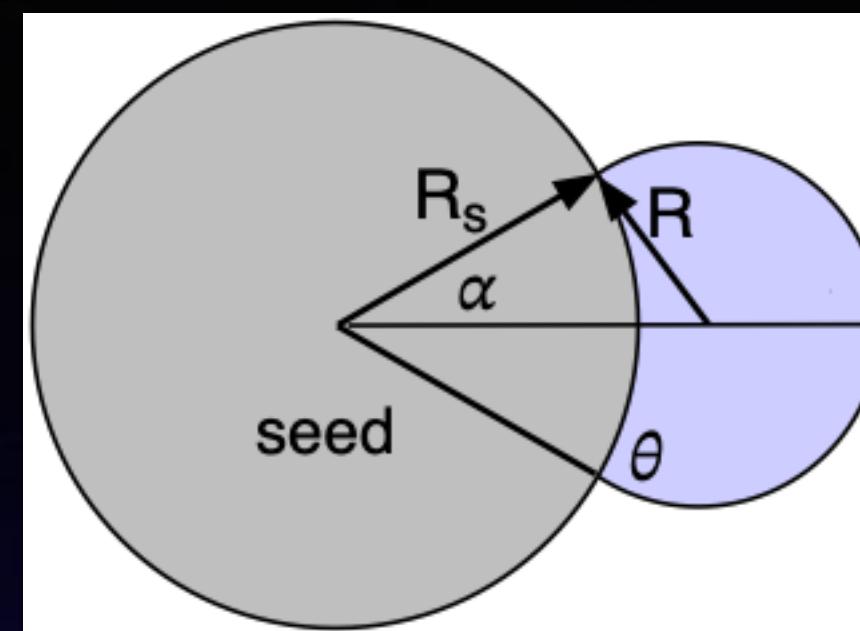


Seeded nucleation rates: interstitial



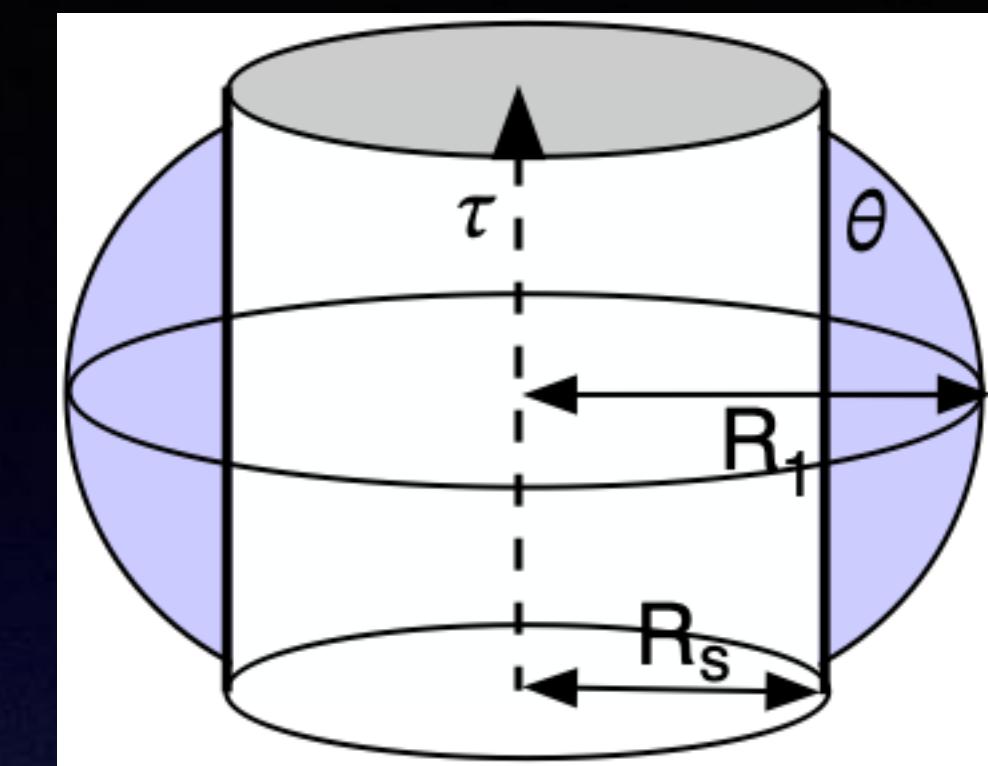
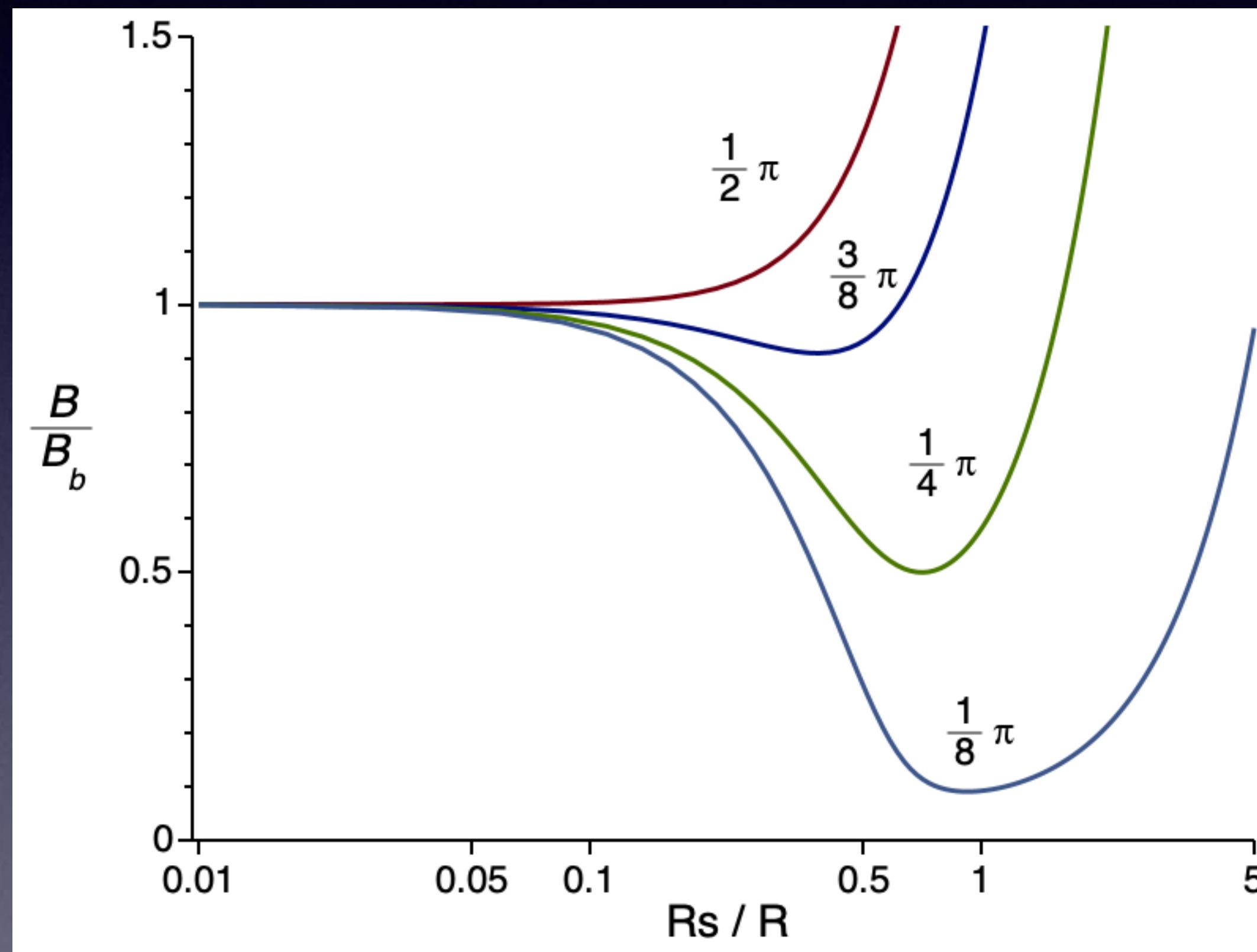
$$B = \Delta E / k_b T$$

Seeded nucleation rates: edge



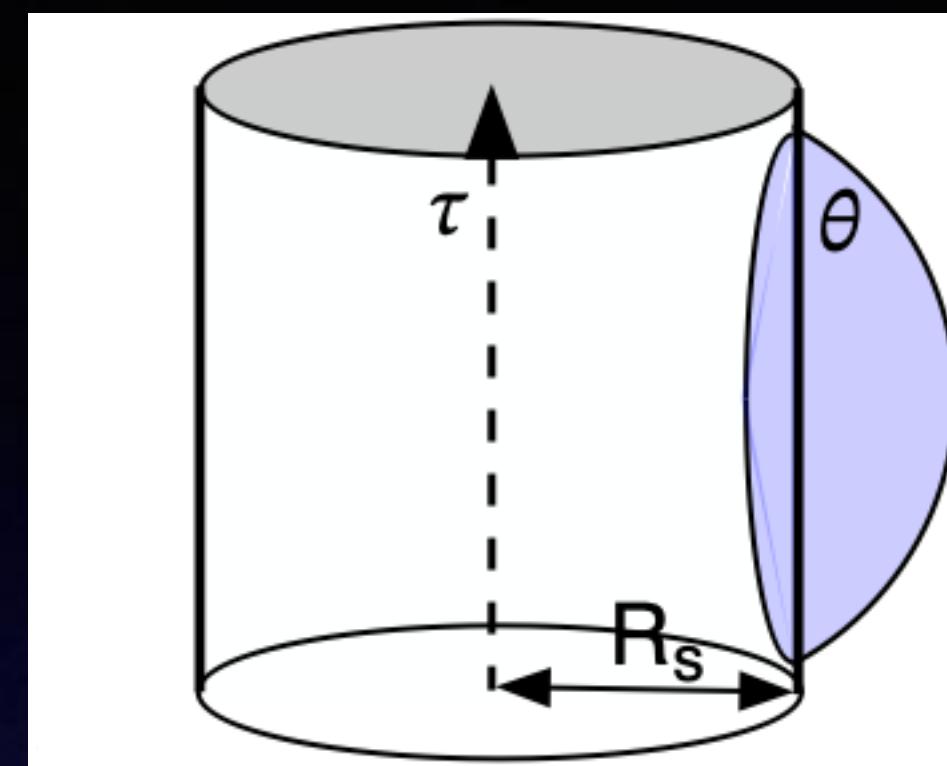
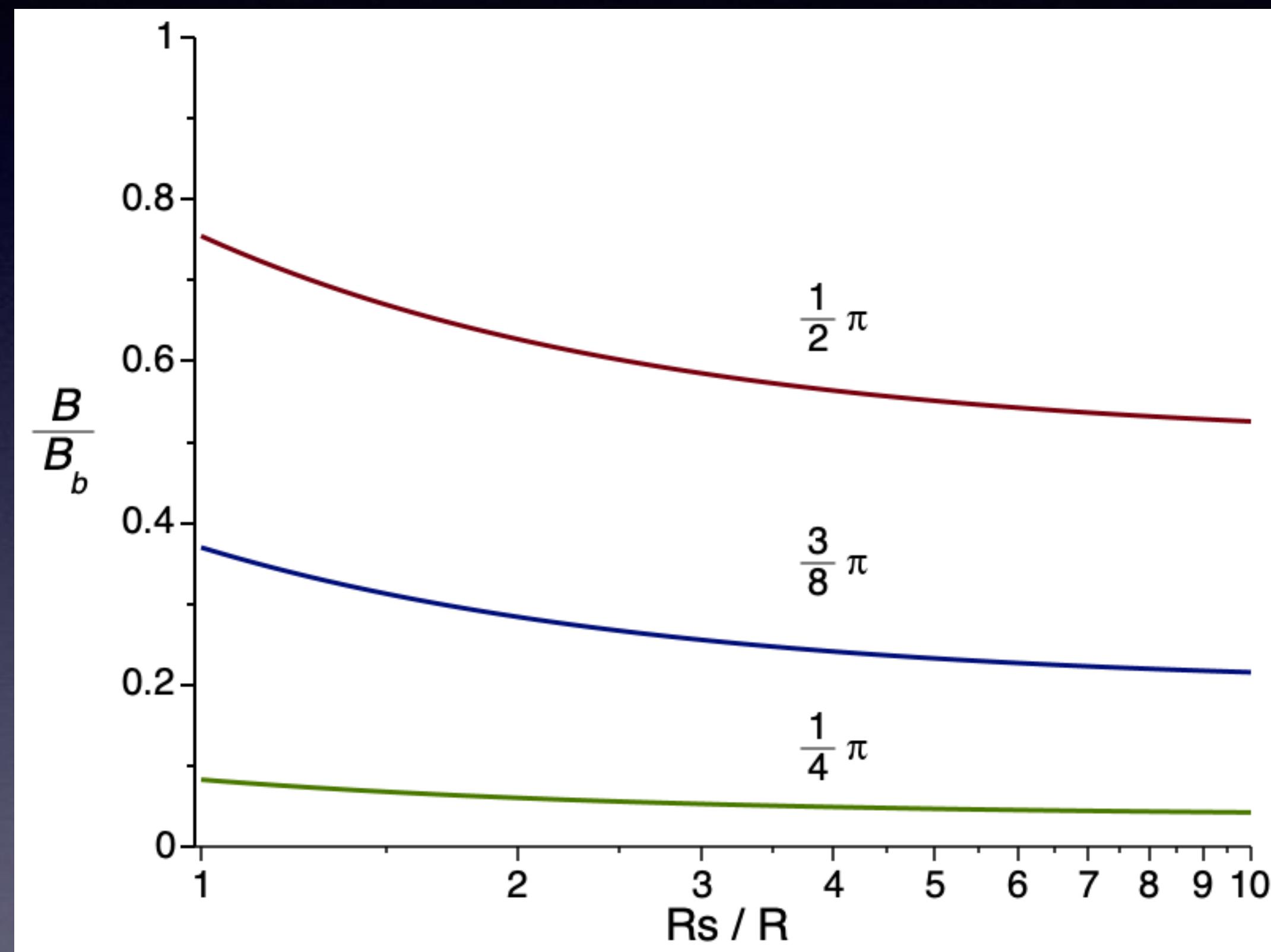
$$B = \Delta E / k_b T$$

False vacuum decay: interstitial

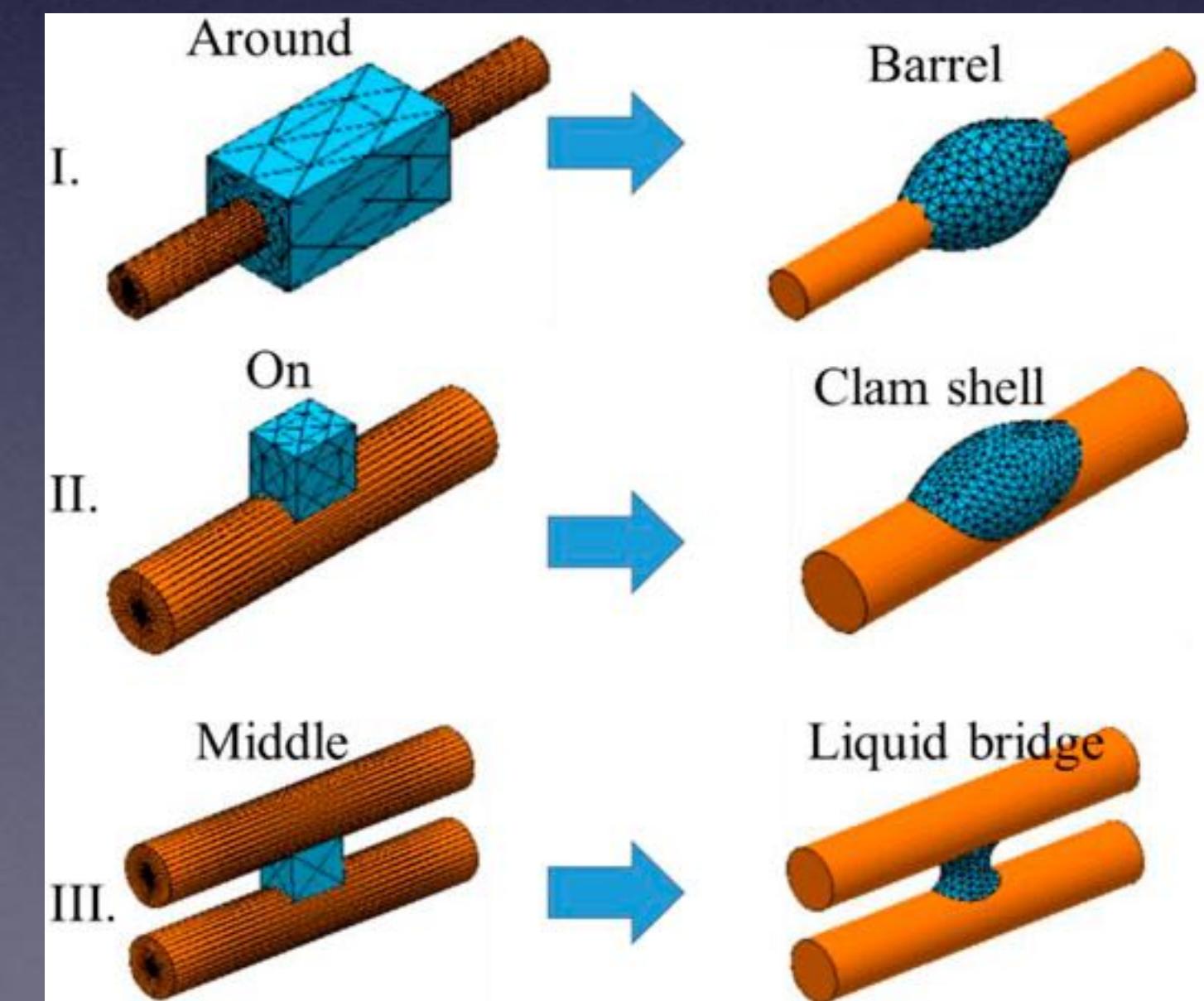


$$B = \Delta S_E / \hbar$$

False vacuum decay: edge

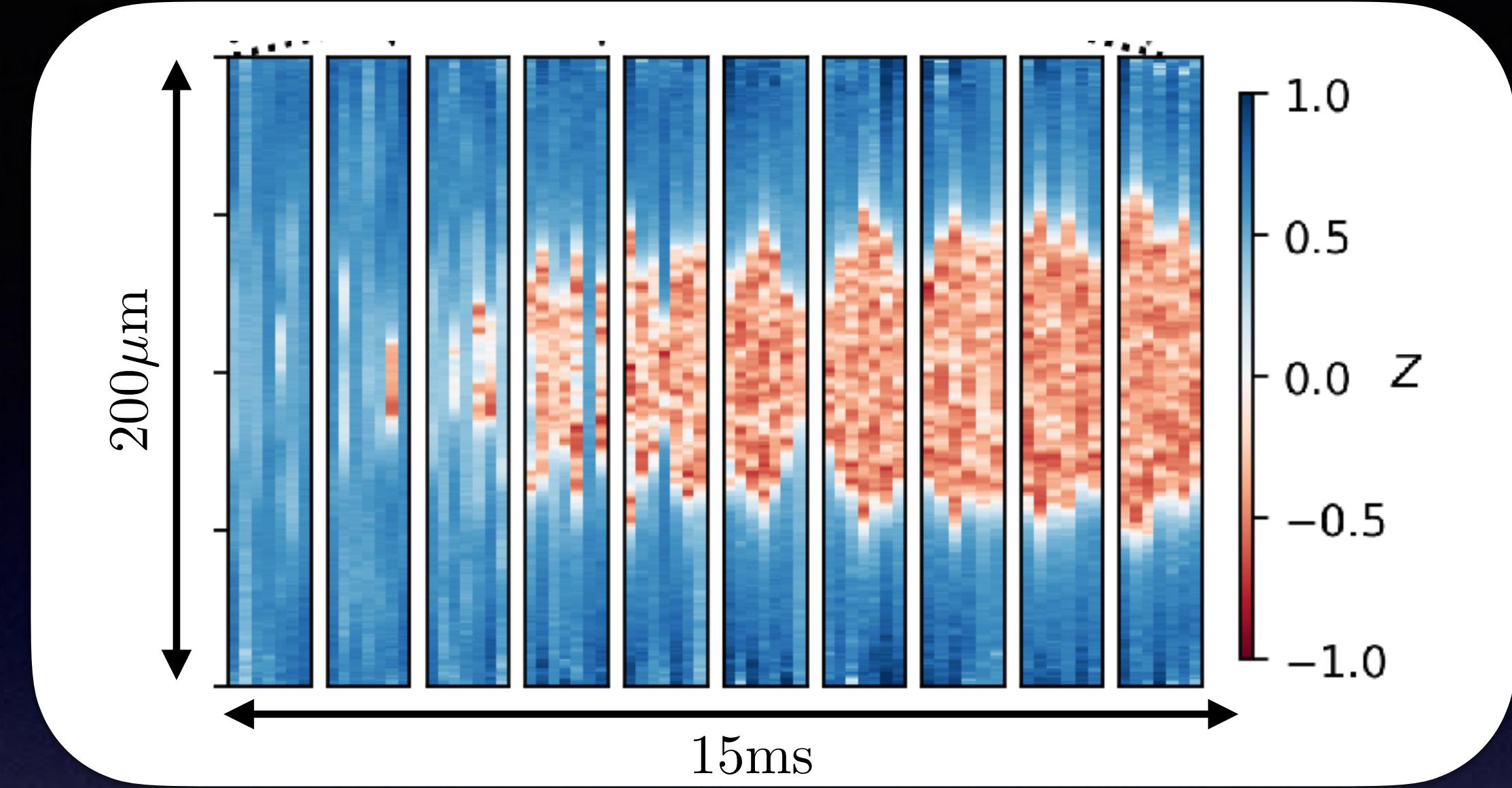


$$B = \Delta S_E / \hbar$$

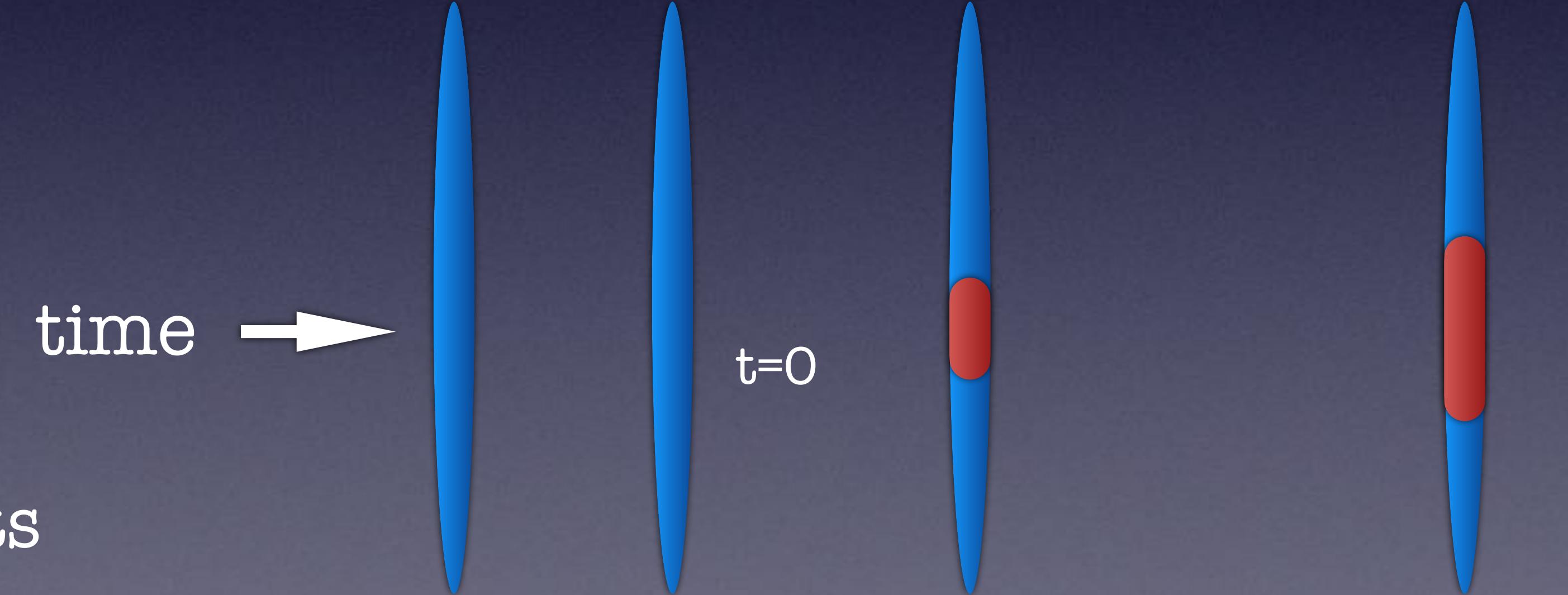


False Vacuum Decay in the Lab (Trento)

A Zenesini, A Berti, R Cominotti, C Rogora, IG Moss, TP Billam, I Carusotto, G Lamporesi, A Recati, G Ferrari arXiv:2305.05225



Ferromagnetic
bubbles in a two-
component
sodium BEC



Nucleation rate fits
theory

FalseVacuum Decay in the Lab

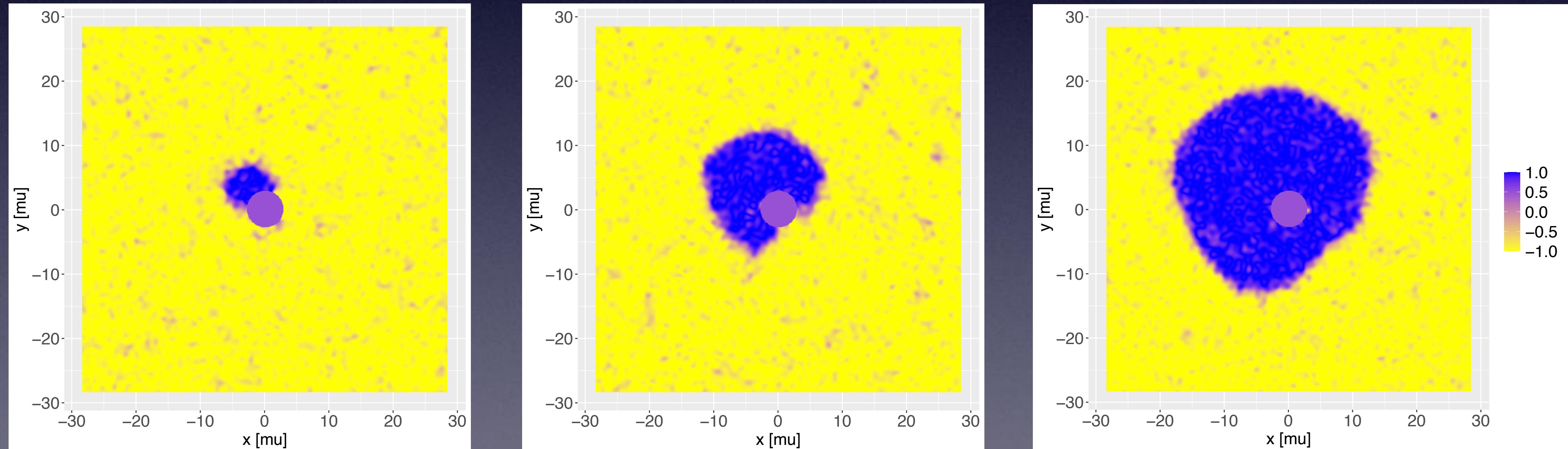
species	$ F,m_F\rangle$ states	effective field	status
sodium 23	$ 1,-1\rangle, 2,-2\rangle$	magnetisation	1D, finite T
potassium 39	$ 1,0\rangle, 1,-1\rangle$	relative phase	2D under construction
rubidium 87	$ 1,1\rangle, 1,0\rangle, 1,-1\rangle$	relative phase	theory only

Seeded FalseVacuum Decay simulations: K39 in 2D

Real-time evolution uses the Stochastic Projected Gross Pitaevski equation

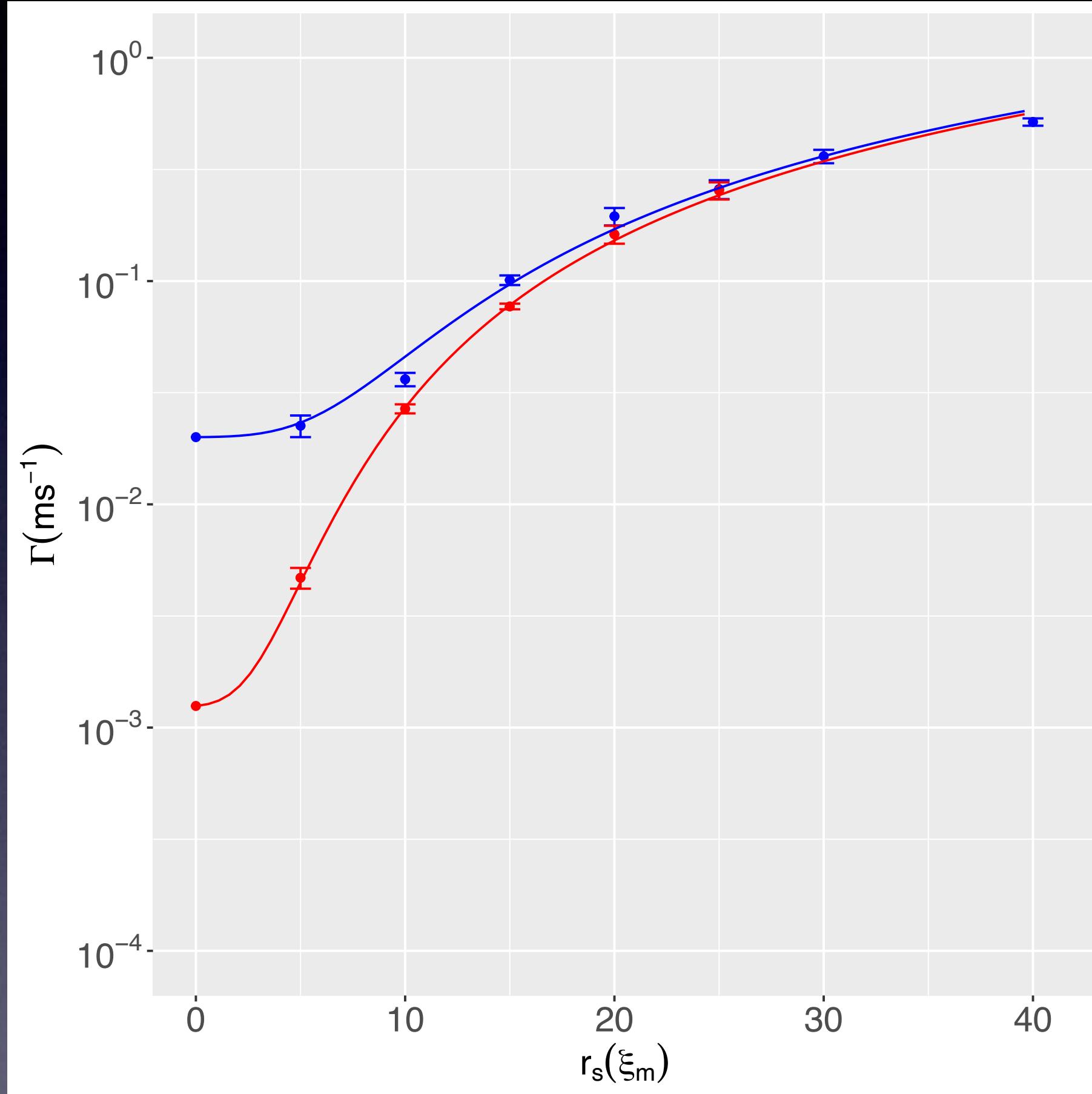
$$i\hbar \frac{\partial \psi_i}{\partial t} = \mathcal{P} \left\{ (1 + i\gamma) \frac{\partial H}{\partial \bar{\psi}_i} + \eta_i \right\}$$

The components represent two Zeeman levels of the BEC. The relative phase (plotted) undergoes false vacuum decay.



Simulated thermal bubble nucleation around a circular seed for a two dimensional BEC.

Seeded False Vacuum Decay: comparison with theory



Seeded rate: $\Gamma_s = A_s R_s B_s^{1/2} e^{-B_s}$

Where $B_s \equiv B_s(B_b, R_s, R, \theta)$

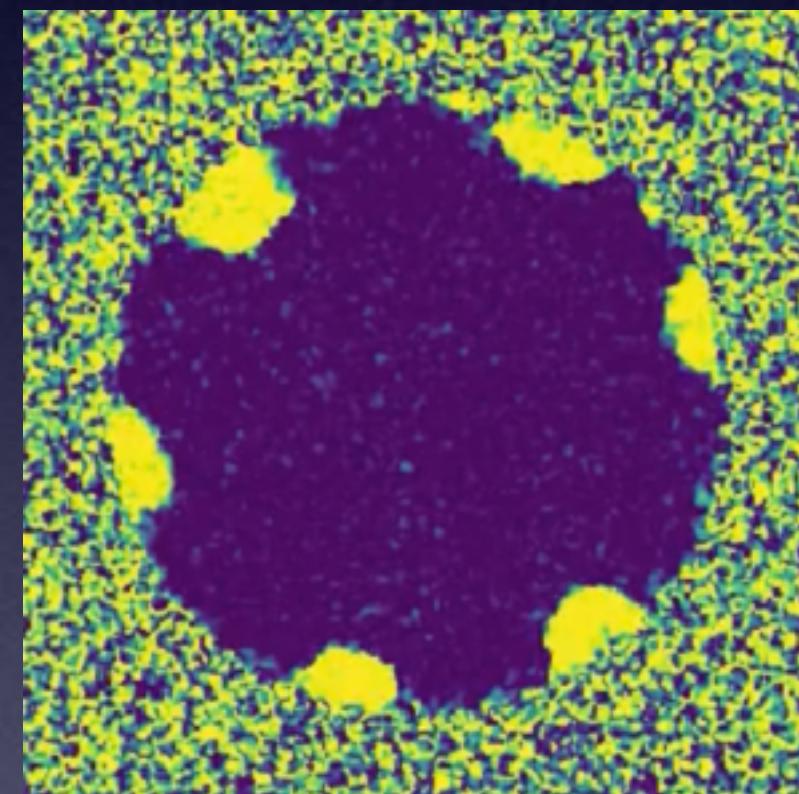
Unseeded rate: $\Gamma_b = A_b L^2 B_b e^{-B_b}$

Total rate: $\Gamma = \Gamma_s + \Gamma_b$

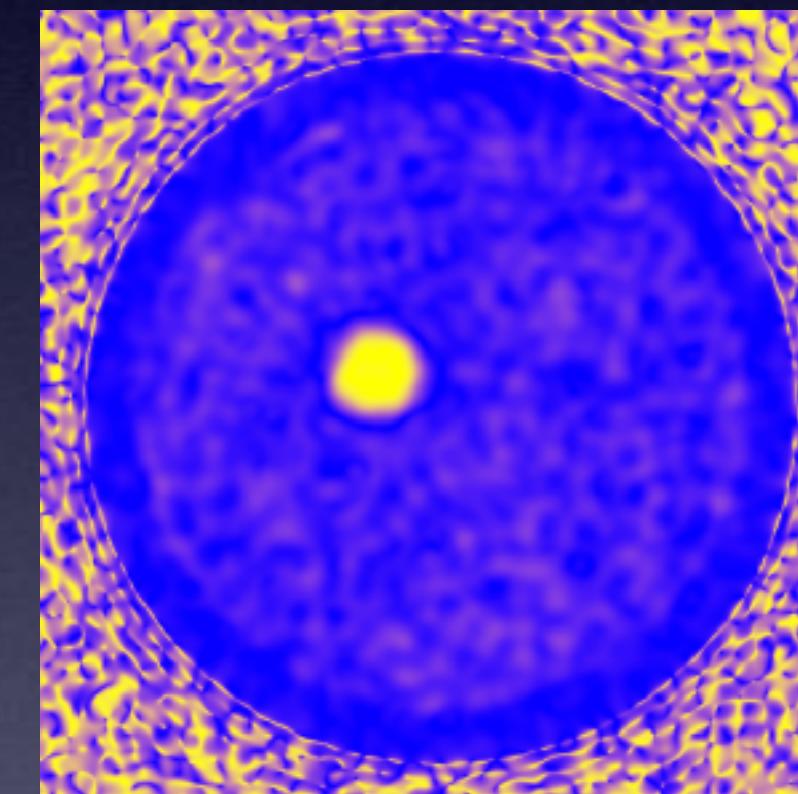
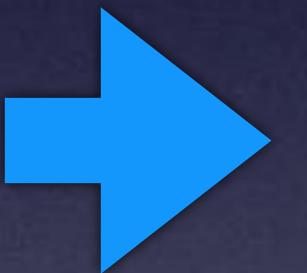
The fit gives $R = 9.2 \xi_m$ ($\xi_m \approx 0.2 \mu\text{m}$)

Bubble nucleation rate plotted as a function of the seed radius. The upper curve is for a periodic box of side $L=400$ and the lower curve $L=200$.

False Vacuum Decay in a trapping potential



hydrophobic coating

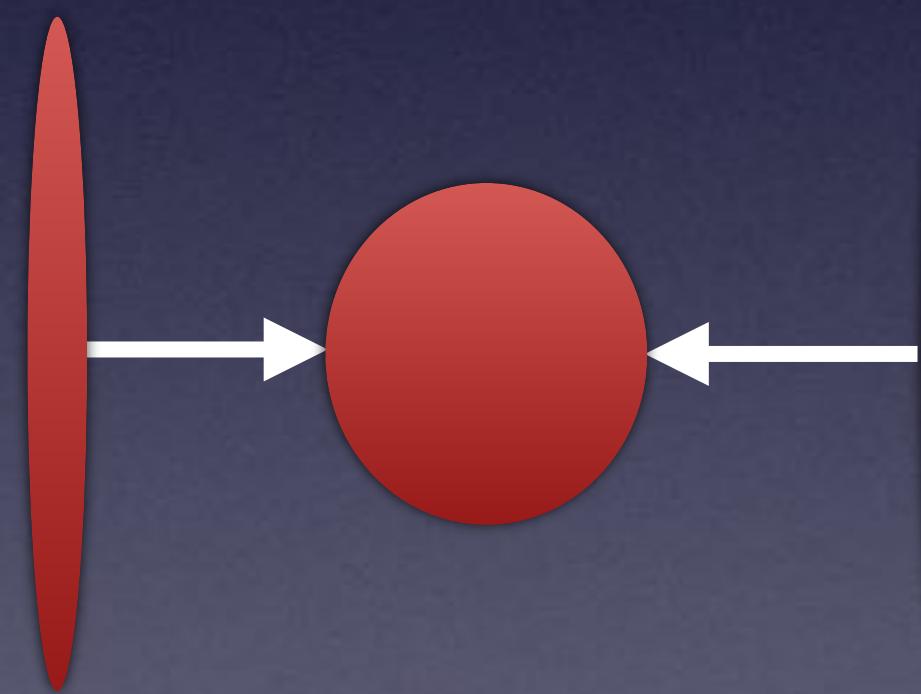


False Vacuum Decay and particle collisions

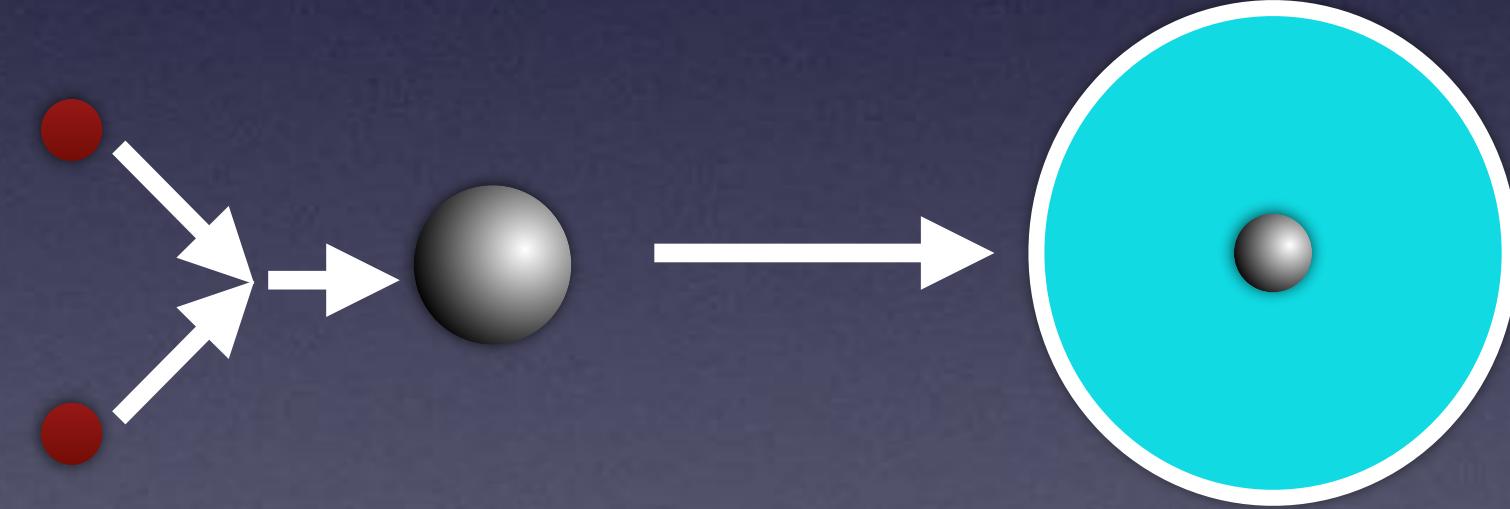
Could particle collisions cause vacuum decay today?

Most results have been 1+1 dimensions - but geometry is important

energy and size



heavy ion collisions



Cuspinera, Gregory, Marshall, Moss 1803.02871

From fantasy to reality?

We have seen the first experimental test of false vacuum decay at finite temperature in a BEC.

False vacuum decay is a non-perturbative quantum field theory phenomenon that may be important in understanding the origin of the universe.

Seeded nucleation may play a role in the early universe and future analogue vacuum decay experiments.

End