

# Measurement of the $\tau$ anomalous magnetic moment ( $g - 2$ ) at CMS

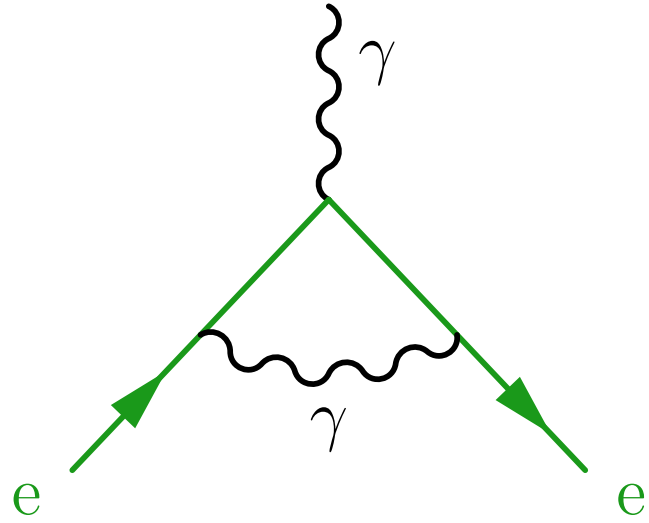
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13/05/2024, UZH Particle Physic Seminar

# Overview

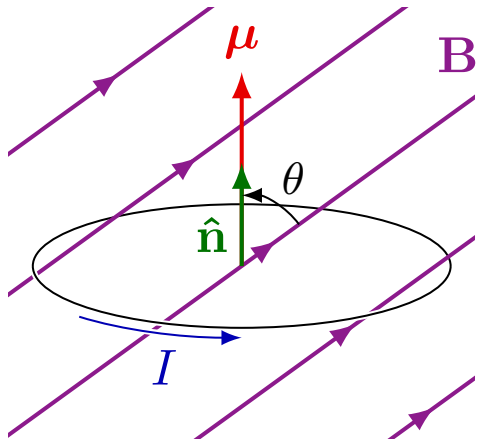
- Introduction
  - Electron & muon
  - Tau
- $\gamma\gamma \rightarrow \tau\tau$  in pp
- Corrections
- Results
  - Observation of  $\gamma\gamma \rightarrow \tau\tau$
  - Constraints on  $a_\tau$  &  $d_\tau$
- Summary



# INTRODUCTION

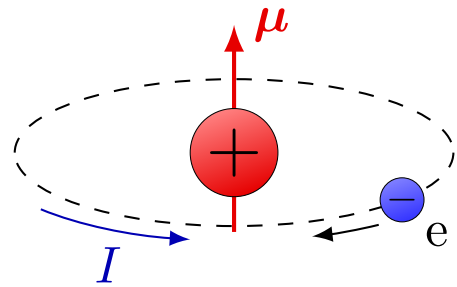
Electron & muon magnetic dipole moment

# Quick recap : What is magnetic momentum ?



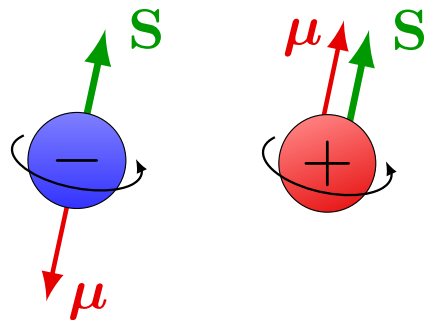
loop of **current**  $I$  in a **B field** experiences a torque

$$\boldsymbol{\tau} = \boldsymbol{\mu} \times \mathbf{B}, \quad \text{with} \quad \boldsymbol{\mu} = IA\hat{\mathbf{n}}$$



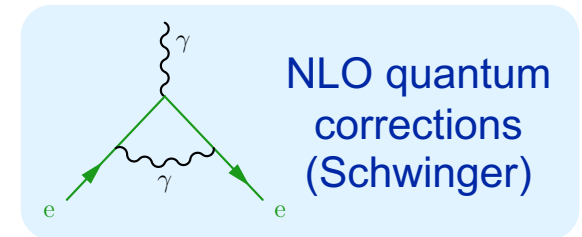
orbiting  $e^-$  is a current

$$\boldsymbol{\mu} = \frac{e}{2m} \mathbf{L}$$



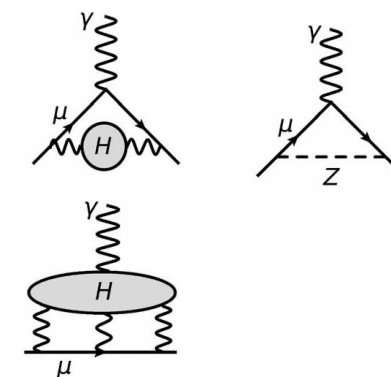
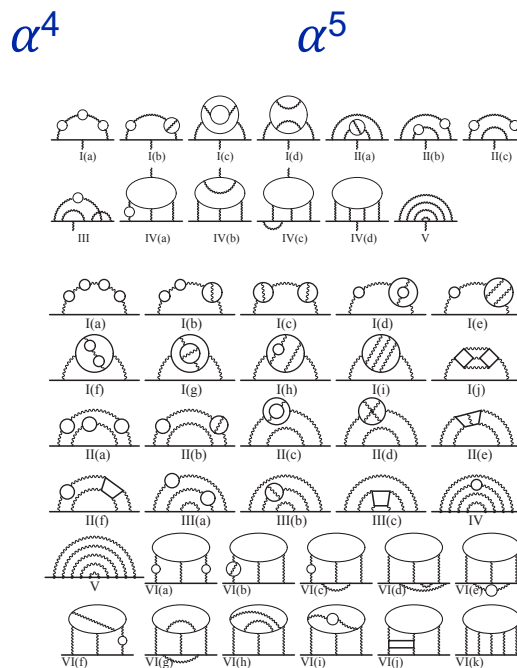
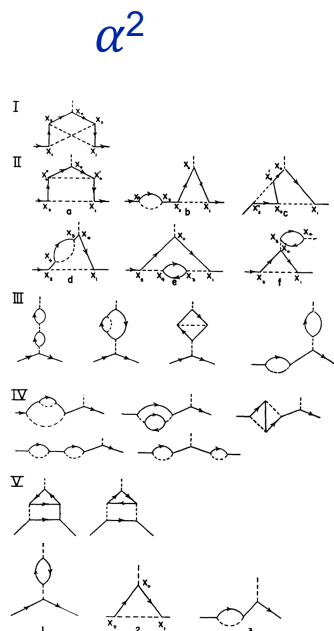
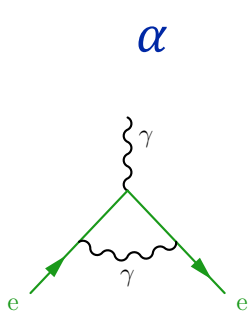
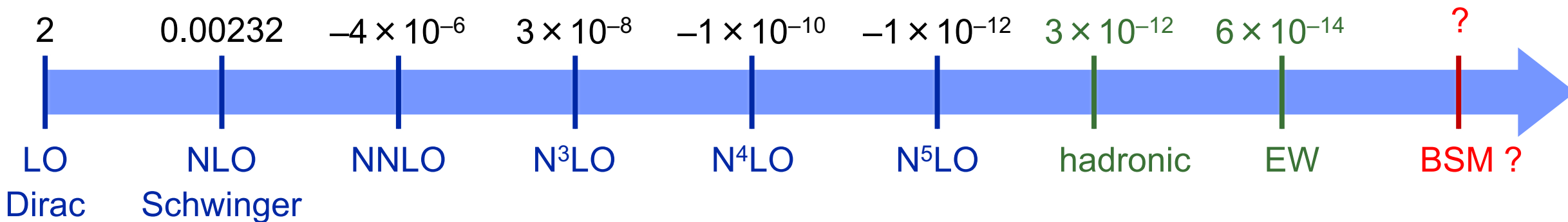
spinning  $e^\pm$  as well !

$$\boldsymbol{\mu}_e = g \frac{e}{2m} \mathbf{S} \longrightarrow \begin{cases} g = 1: \text{classical} \\ g = 2: \text{Dirac} \\ g \approx 2.002: \text{QED} \end{cases}$$



# Quantum corrections to $(g - 2)_e$

$g = 2.002\ 319\ 304\ 361$



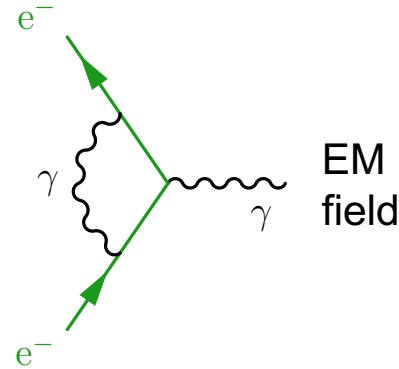
Schwinger (1948)

Karplus & Kroll (1950)  
Sommerfeld, Petermann (1957)

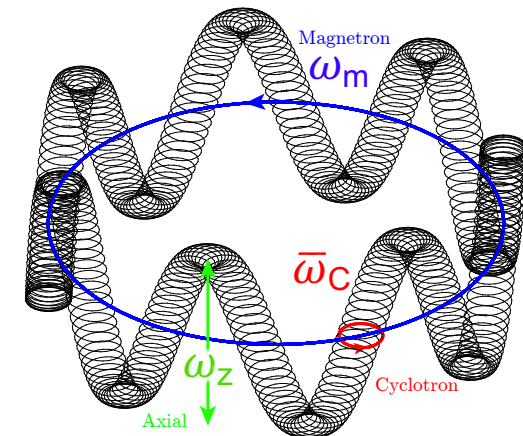
Aoyama et al.

# Quick history: Electron $g - 2$

- **1927**: Dirac equation predicts  
 $g = 2$  (LO)
- **1947–1951**: Kusch & Foley measure  $g > 2$ :  
 $(g - 2)/2 = 0.001\,19\,(5) \sim 4\%$
- **1948**: Schwinger computes  
 $(g - 2)/2 \approx 0.001\,161 \approx \alpha/2\pi$  (NLO)



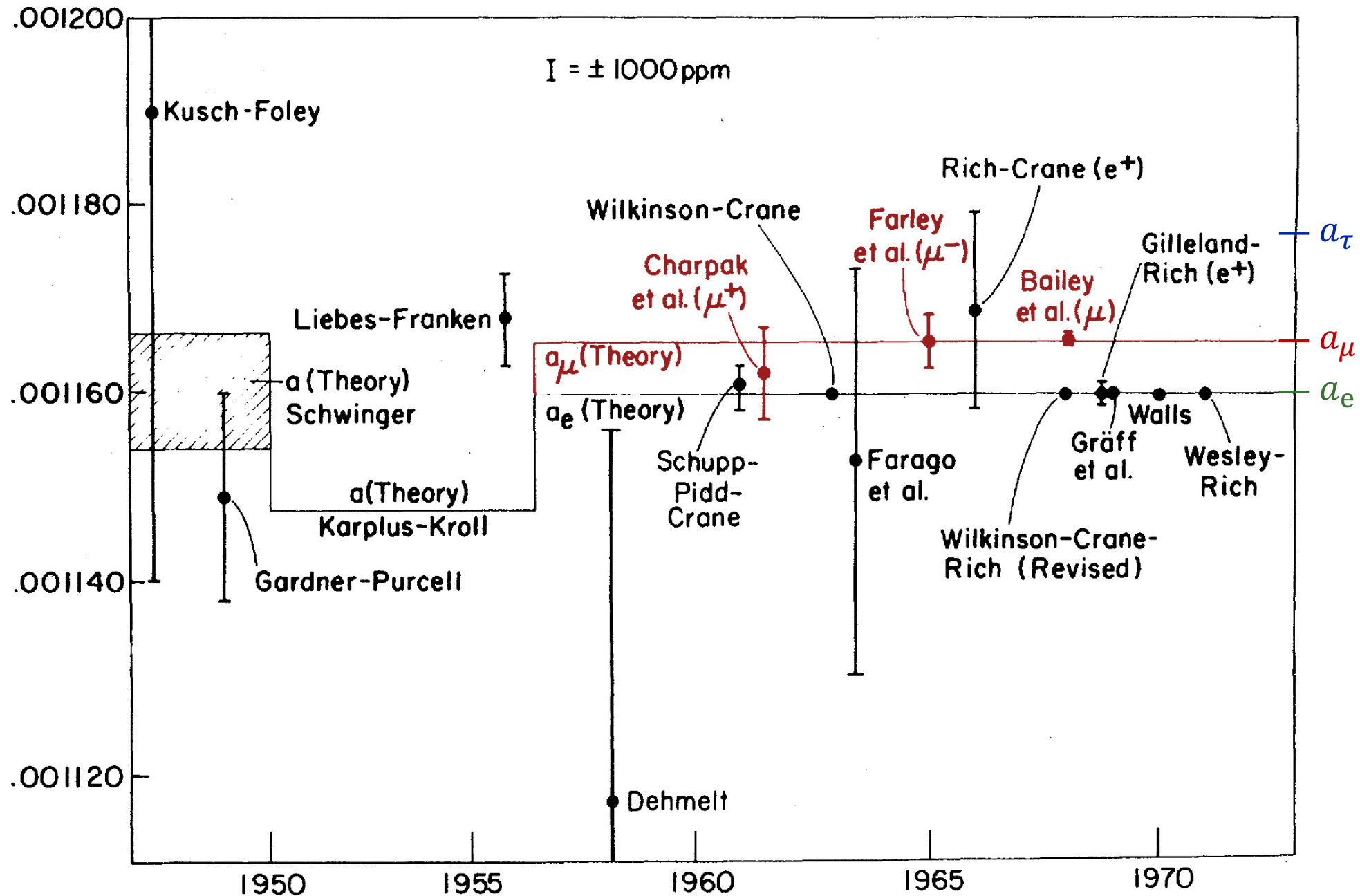
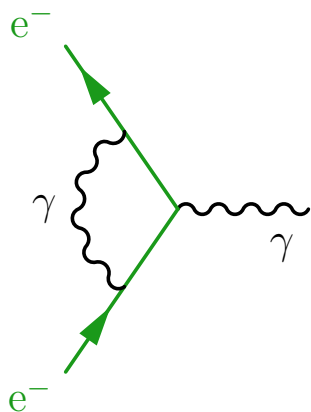
- **1969**: Gräff et. al. with Penning trap  
 $(g - 2)/2 = 0.001\,159\,66\,(30) \sim 300$  ppm
- **1987**: Dehmelt et. al.  
 $(g - 2)/2 = 0.001\,159\,652\,188\,4\,(43) \sim 4$  ppt
- **2006–2022**: Gabrielse et. al.  
 $(g - 2)/2 = 0.001\,159\,652\,180\,59\,(31) \sim 0.13$  ppt



# Status in 1972...

anomalous  
magnetic moment

$$a = \frac{g - 2}{2}$$



The Current Status of the Lepton  $g$  Factors, A. Rich & J.C. Wesley (1972)

<https://journals.aps.org/rmp/abstract/10.1103/RevModPhys.44.250>

$$g = 2 + 2a$$

$$\approx 2.00232$$

“radiative corrections”

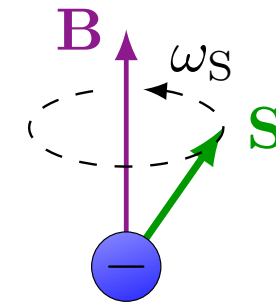
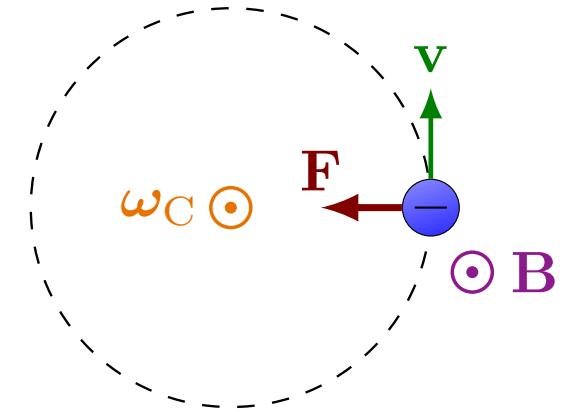
# How to measure $g - 2$ ?

$$\text{cyclotron oscillation } \omega_C = \frac{e}{m} B$$

$$\text{anomalous frequency } \omega_a = \omega_S - \omega_C \sim O(10^{-3})$$

$$\text{Larmor precession } \omega_S = g \frac{e}{2m} B$$

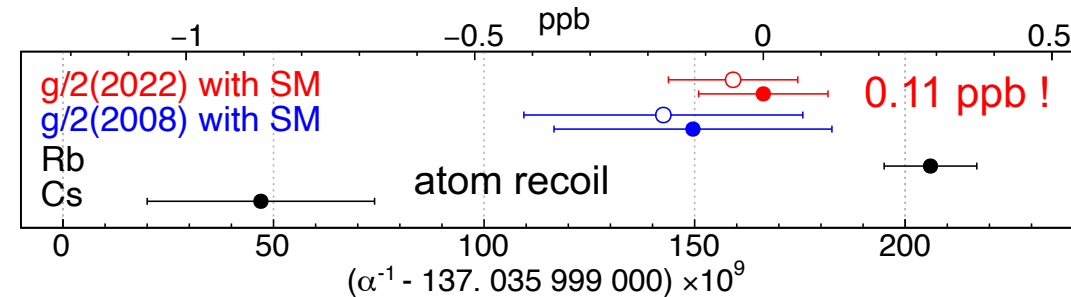
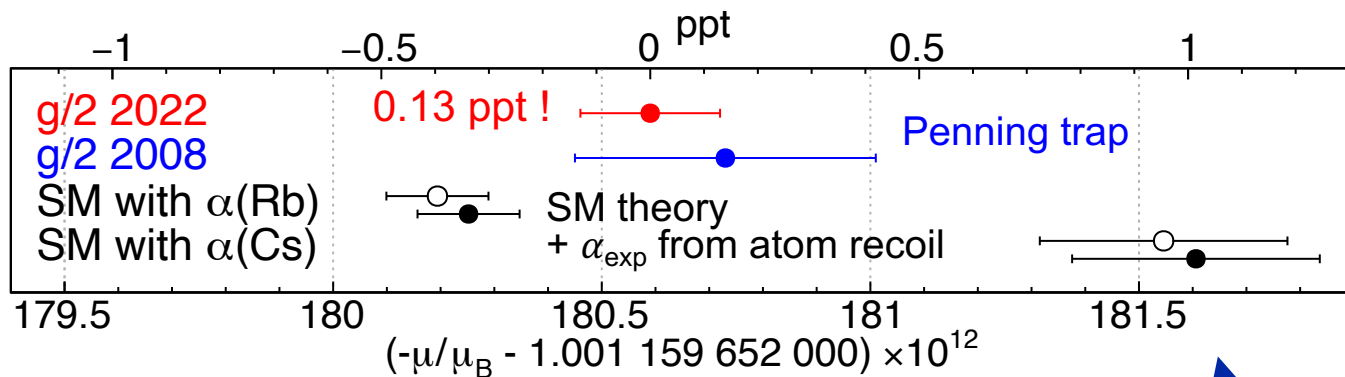
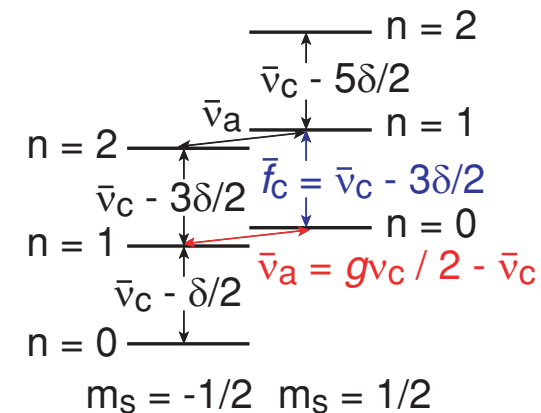
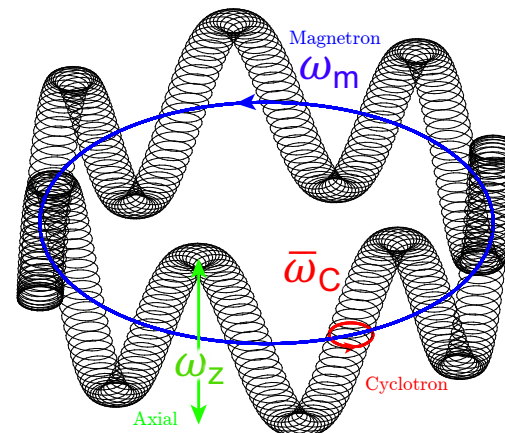
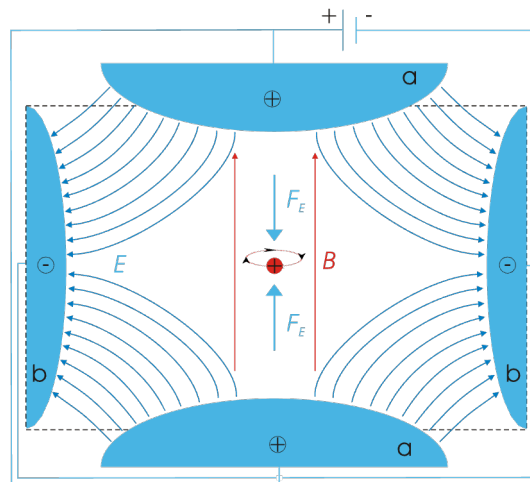
$$\Rightarrow \frac{g}{2} = \frac{\omega_S}{\omega_C} = 1 + \frac{\omega_a}{\omega_C} \text{ by measuring } \omega_a/\omega_C$$





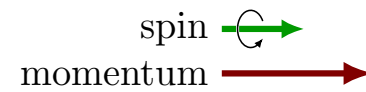
# Measurement of electron $g - 2$ in Penning traps

- oscillate electron in **nonuniform E field**, but **uniform B field**
- measure resonance frequencies



$$\frac{g}{2} = 1 + C_2 \left(\frac{\alpha}{\pi}\right) + C_4 \left(\frac{\alpha}{\pi}\right)^2 + C_6 \left(\frac{\alpha}{\pi}\right)^3 + \dots + a_{\mu, \tau} + a_{\text{had}} + a_{\text{weak}}$$

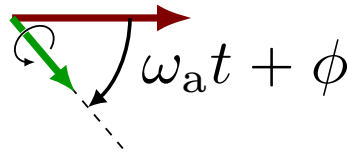
# Measurement of muon $g - 2$ in cyclotrons



- muon lifetime  $\sim 2.2 \mu\text{s}$   
 $\Rightarrow$  use cyclotrons
- spin precesses faster than momentum in cyclotron magnetic field:

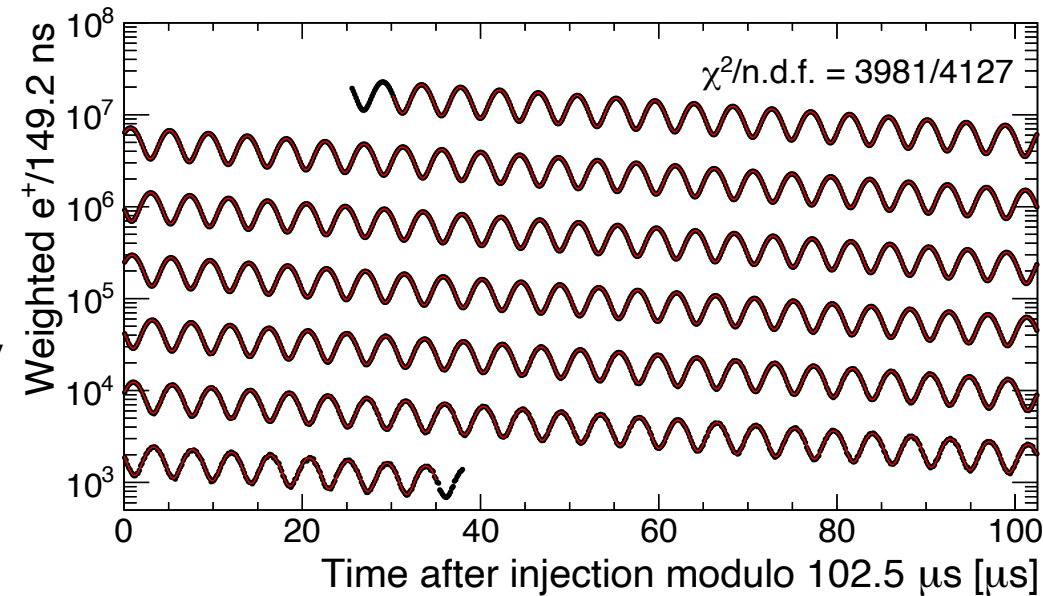
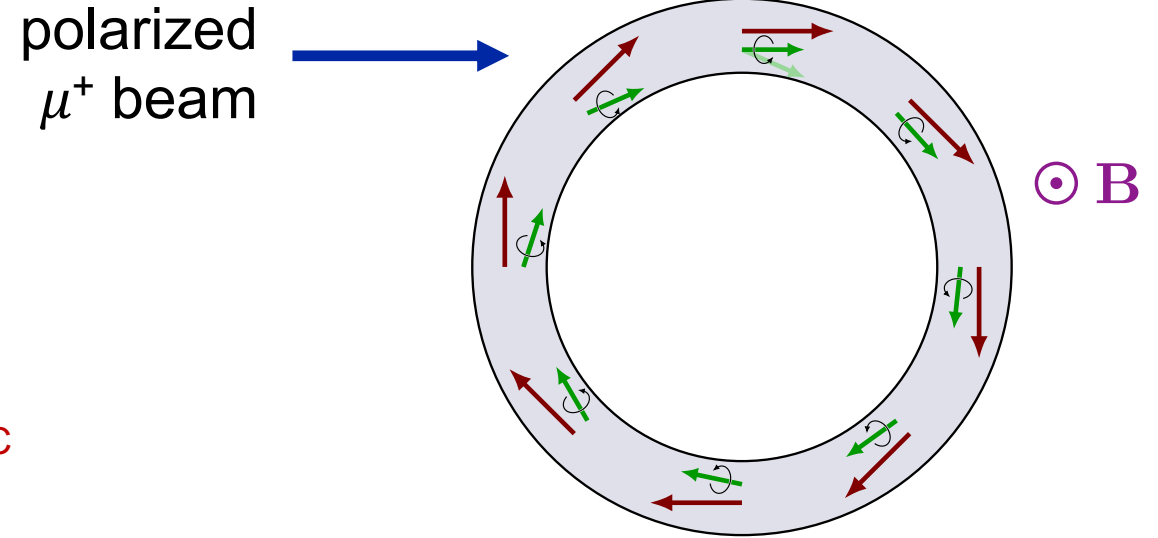
Larmor precession  $\omega_S >$  cyclotron oscillation  $\omega_C$

$$\begin{aligned} \omega_a &= \omega_S - \omega_C \\ &= \frac{g - 2}{2} \frac{e}{m_\mu} B \\ &\sim 230 \text{ kHz} \end{aligned}$$



oscillations in number of  $e^+$  with  $E > 1.8 \text{ GeV}$

- measure oscillation in  $\mu^+ \rightarrow e^+$  energy spectrum

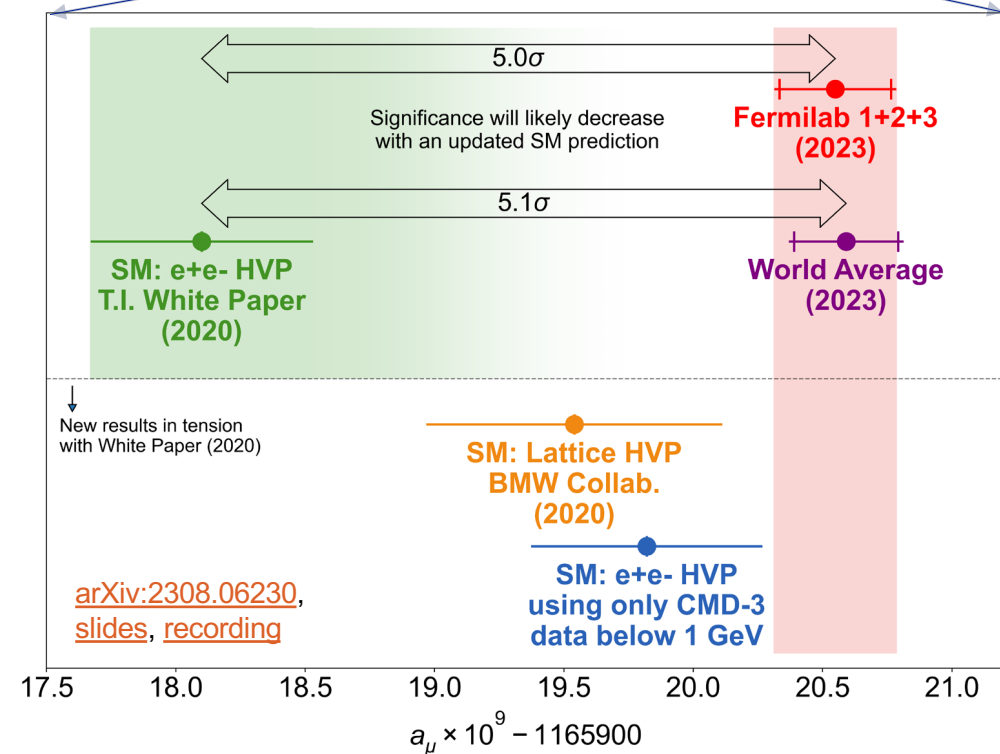
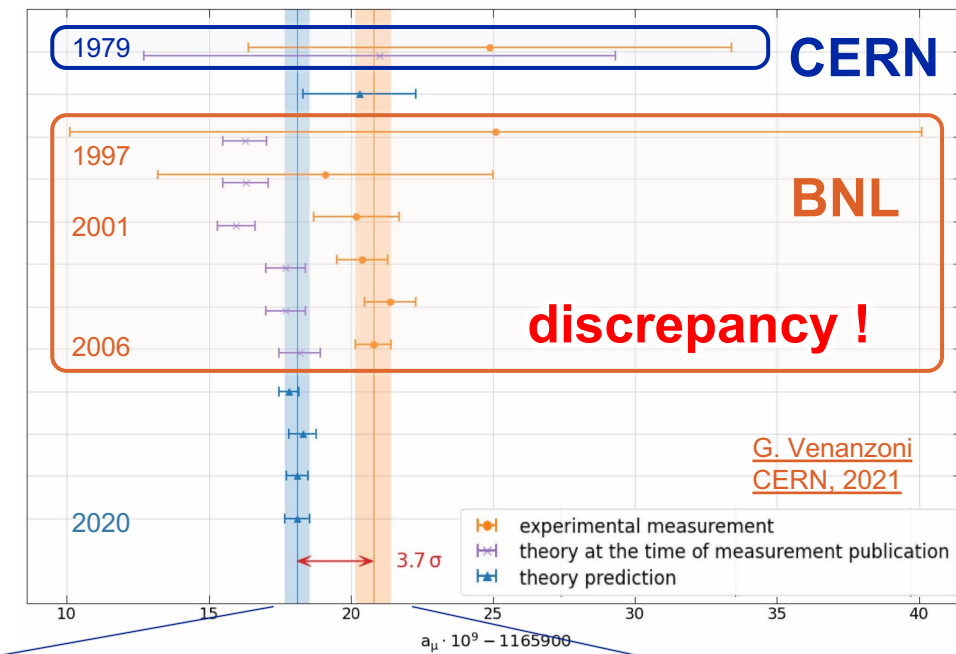


# Quick history: Muon $g - 2$

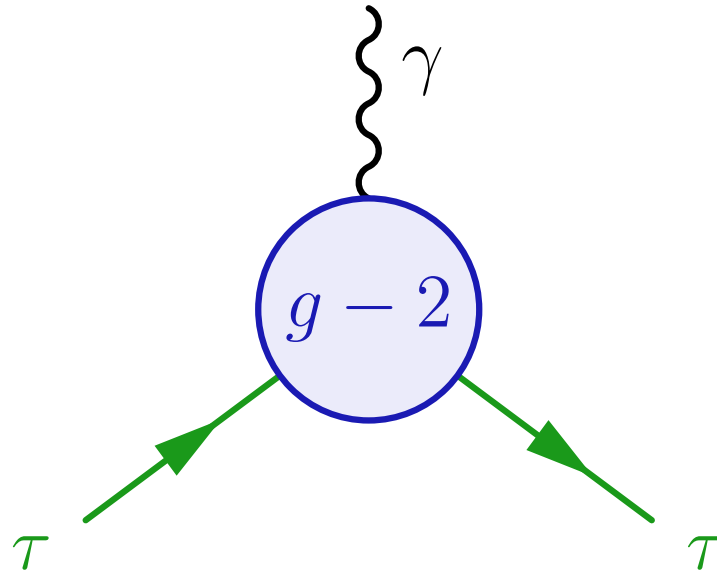
- **CERN:**
  - 1961:  $\sim 0.2\%$
  - 1979:  $\sim 7.30$  ppm
- **BNL:**
  - 1999:  $\sim 1.30$  ppm
  - 2001:  $\sim 0.54$  ppm

$\Rightarrow$  discrepancy with **theory** !
- **FNAL:**
  - 2021:  $\sim 0.46$  ppm
  - 2023:  $\sim 0.20$  ppm

$\Rightarrow$  still tension







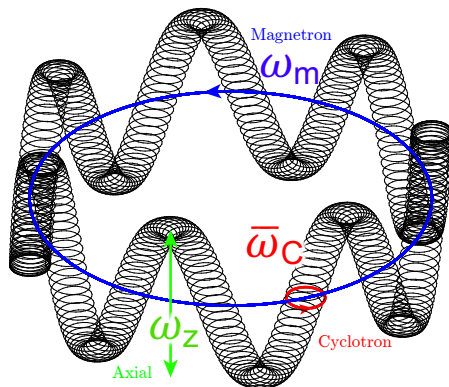
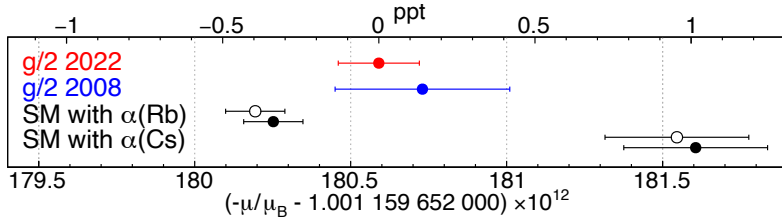
# INTRODUCTION

Tau magnetic moment

# Measurement of lepton $g - 2$

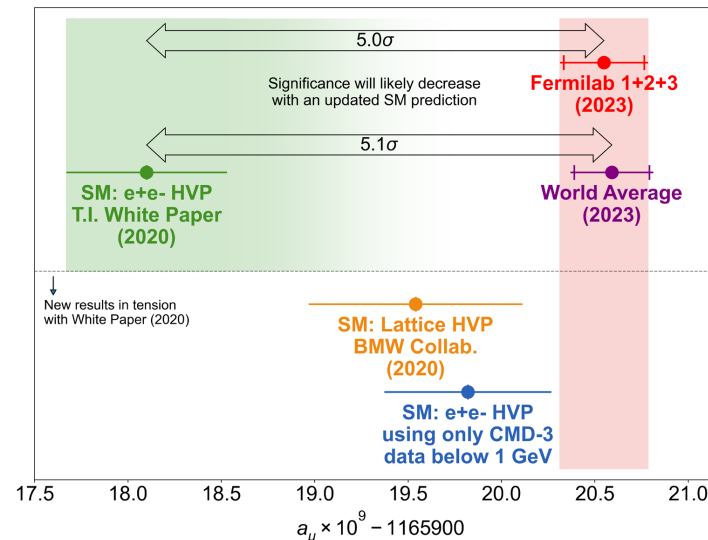
## electron

- stable
- Penning traps
- 0.13 ppt !
- agrees with SM 1 ppt



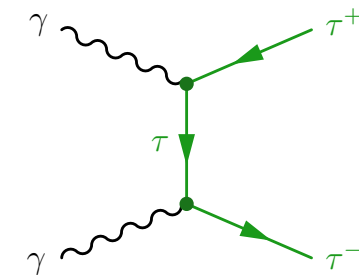
## muon

- lifetime  $\sim 2.2 \times 10^{-6}$  s
- cyclotrons
- 0.20 ppm !
- tension with theory ?



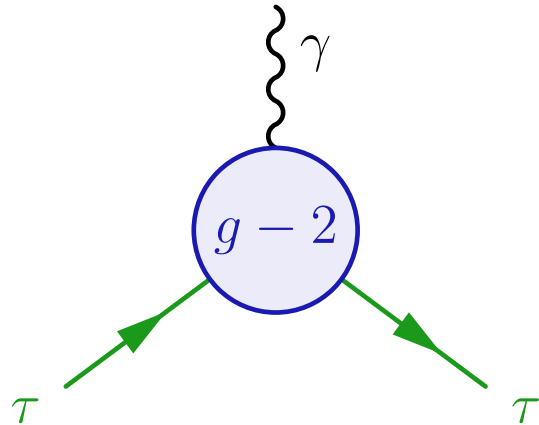
## tau

- lifetime  $\sim 2.9 \times 10^{-13}$  s
- $\gamma\gamma \rightarrow \tau\tau$  process in colliders !
- limit by LEP  $\sim 20$  times Schwinger term
- many **BSMs** predict enhancement e.g.  $O(m_\tau^2/m_\mu^2) \approx 280$
- ⇒ probe for NP ?

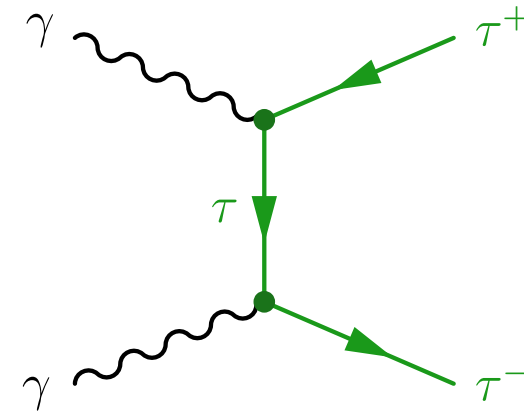


# How to measure the tau $g - 2$

- $a_\tau$  & electric dipole moment  $d_\tau$  can be probed from  $\gamma\tau\tau$  vertex



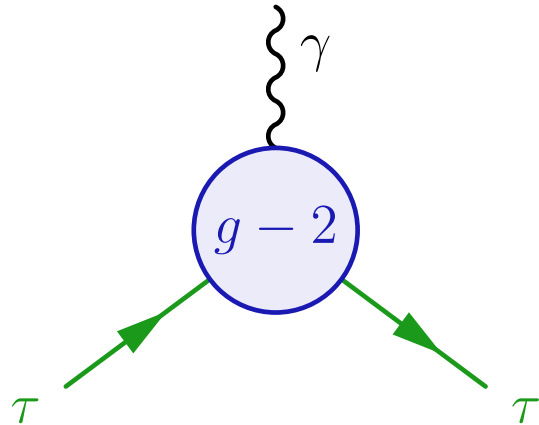
- $\gamma\gamma \rightarrow \tau\tau$  process contains 2  $\gamma\tau\tau$  vertices



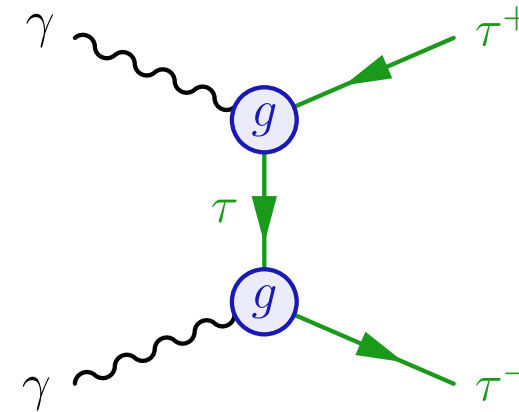
- constraints on electromagnetic moments  $a_\tau$  &  $d_\tau$  from *form factors* or *SMEFT*
- in the SM:  $d_\tau \sim 10^{-37}$  ecm via CP violation in CKM, but could be much larger in BSMs

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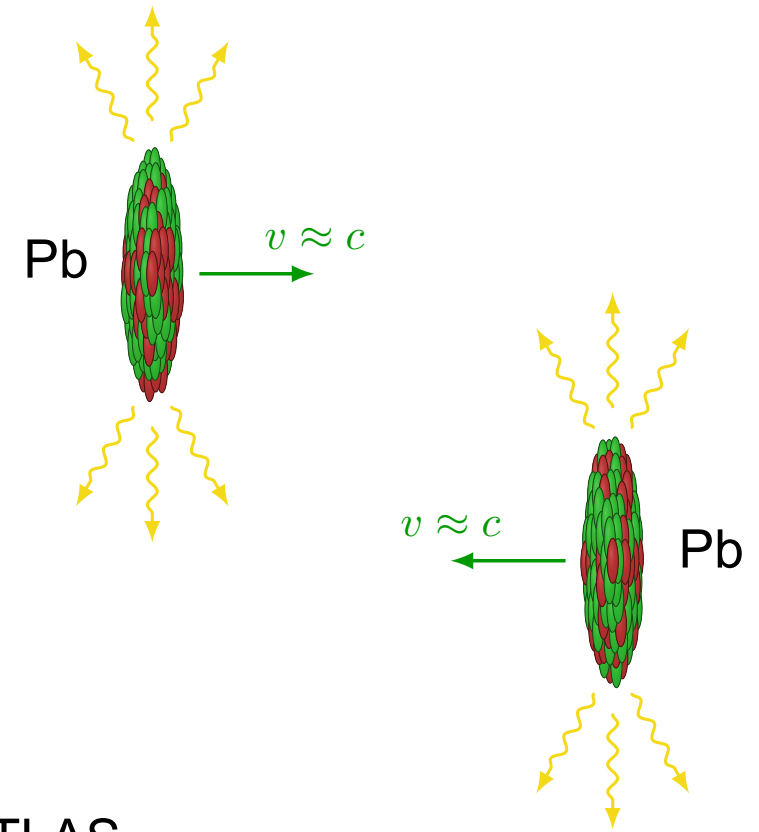


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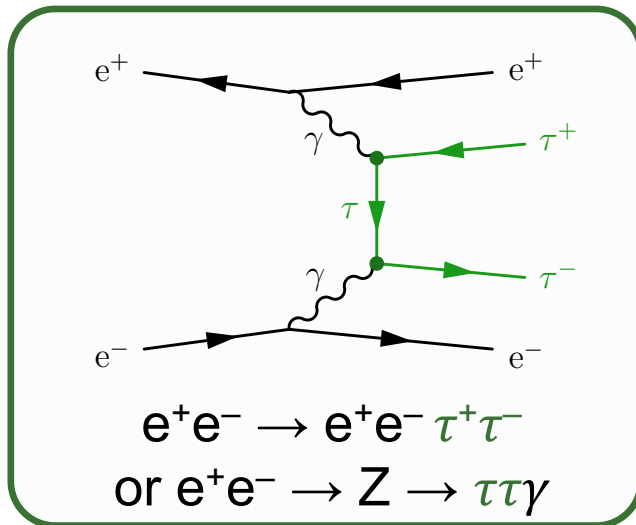


# Photon-induced processes

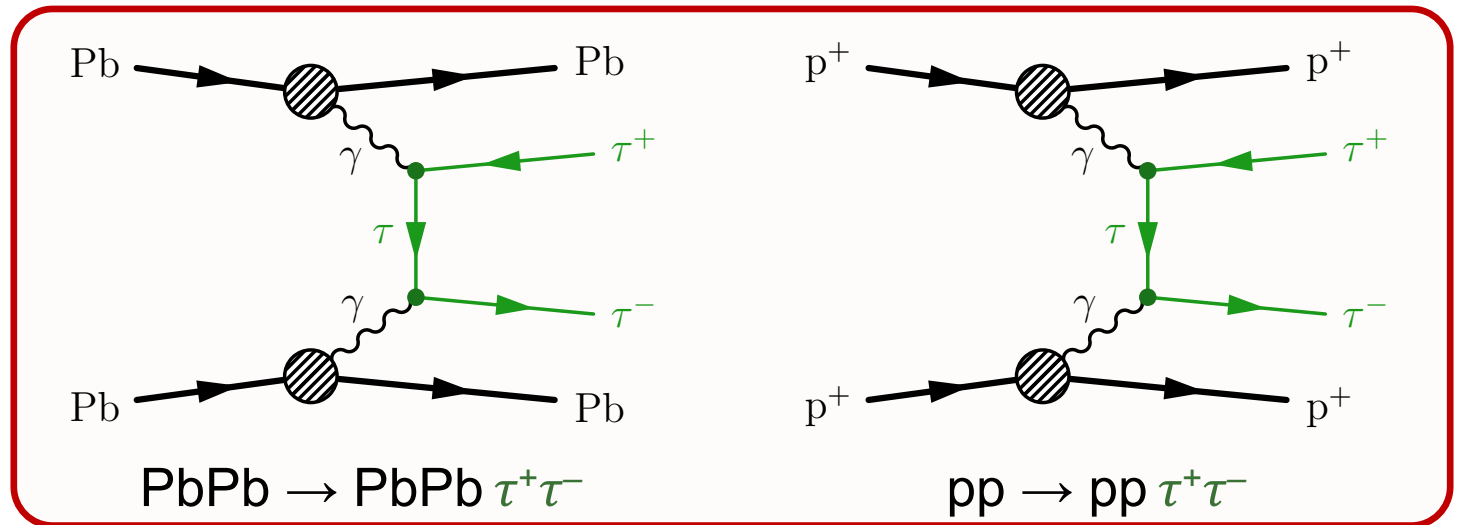
- collide charged particles at high energies  
 $\Rightarrow$  intense **electromagnetic fields**  
 $\Rightarrow$  **photon-photon collisions**
- cross section  $\sigma \propto Z^4$   
 $\Rightarrow$  PbPb collisions enhanced w.r.t. pp



**LEP:** DELPHI, L3, ...

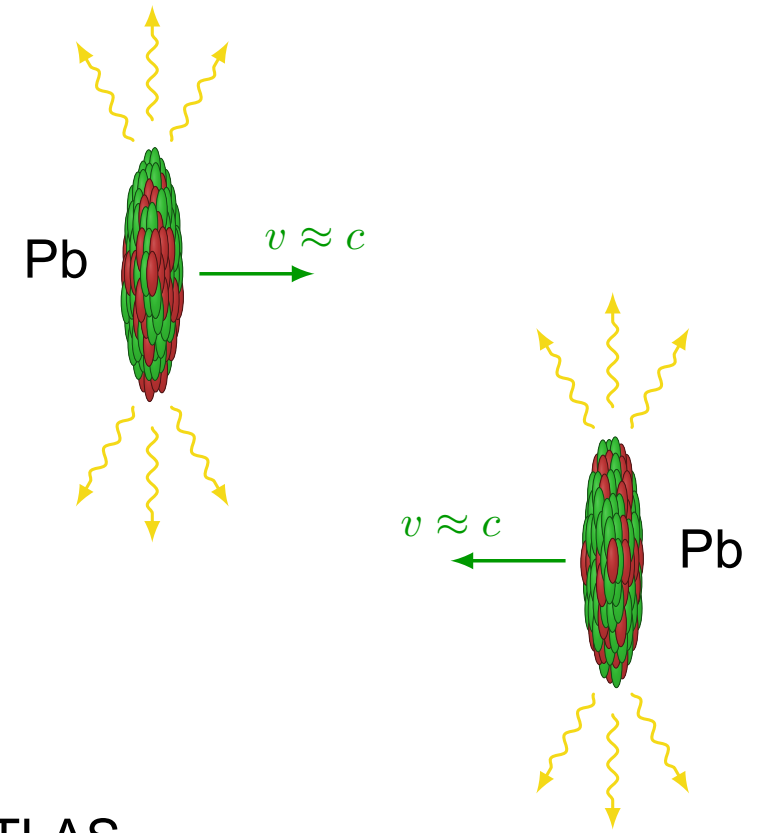


**LHC:** CMS, ATLAS, ...

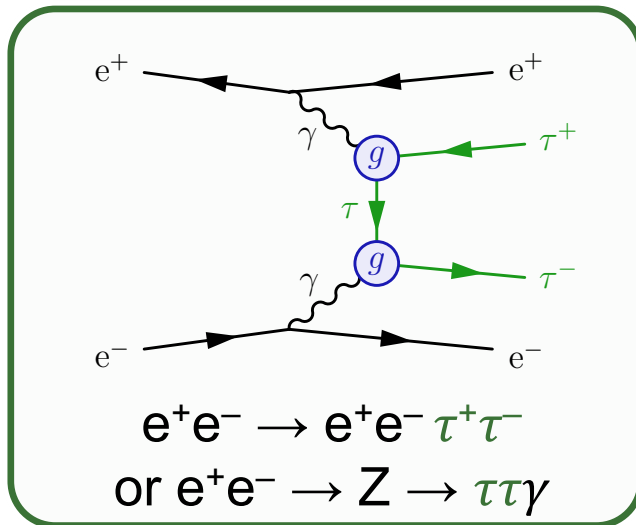


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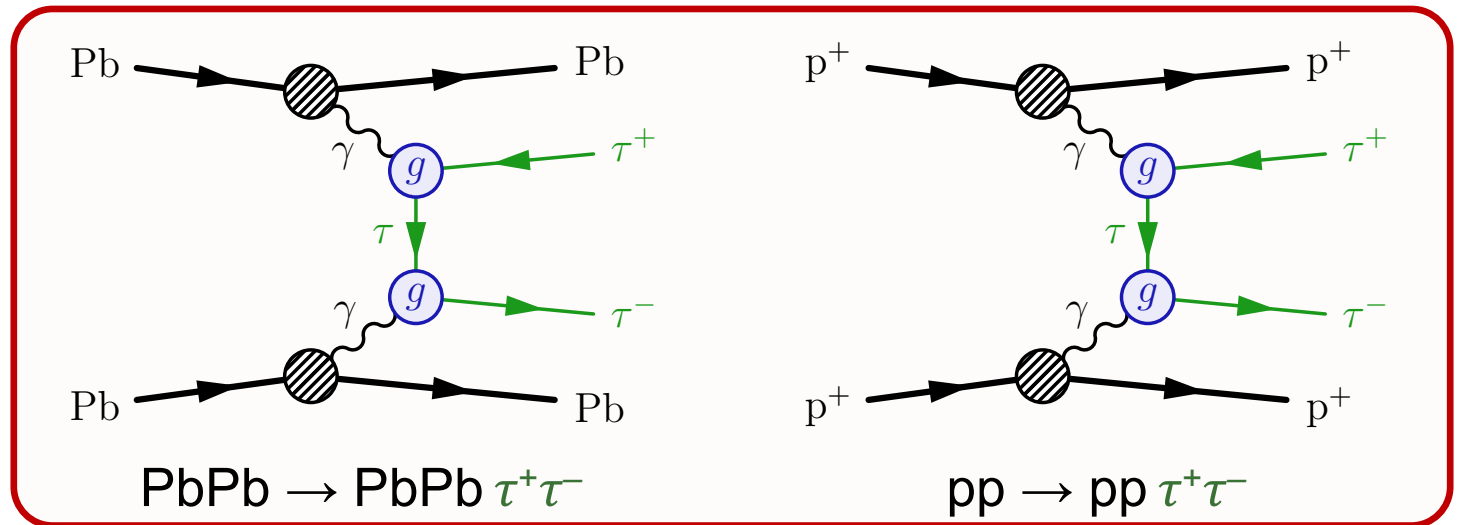
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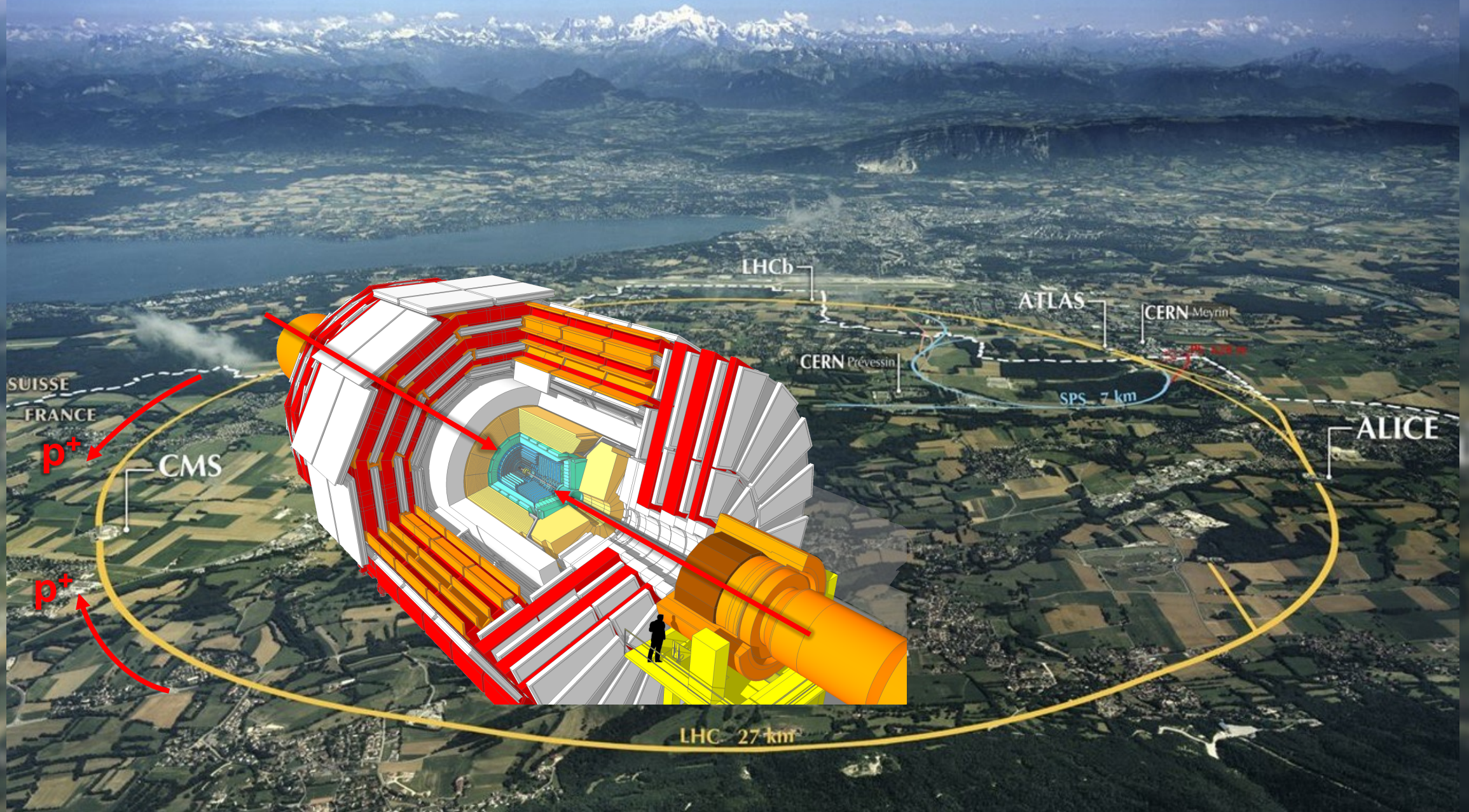


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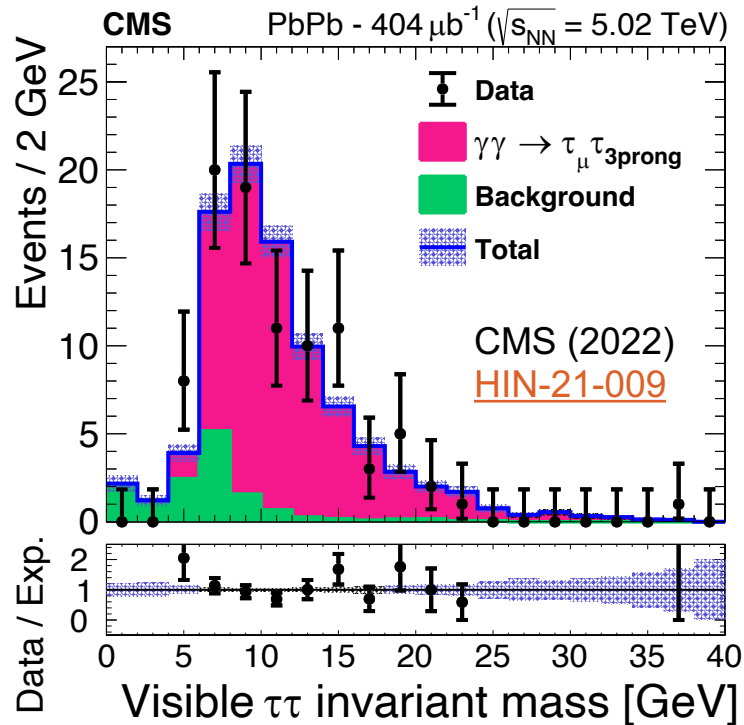
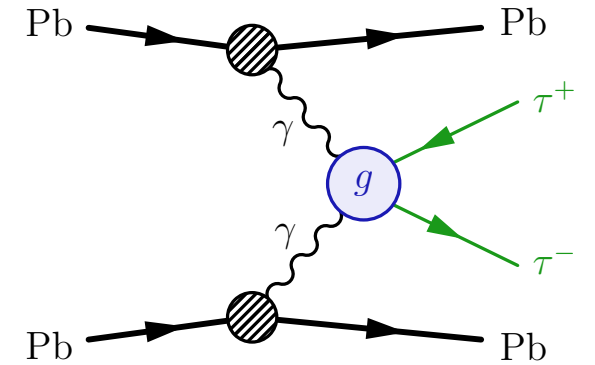
# LHC accelerator

proton collisions @ 13 TeV

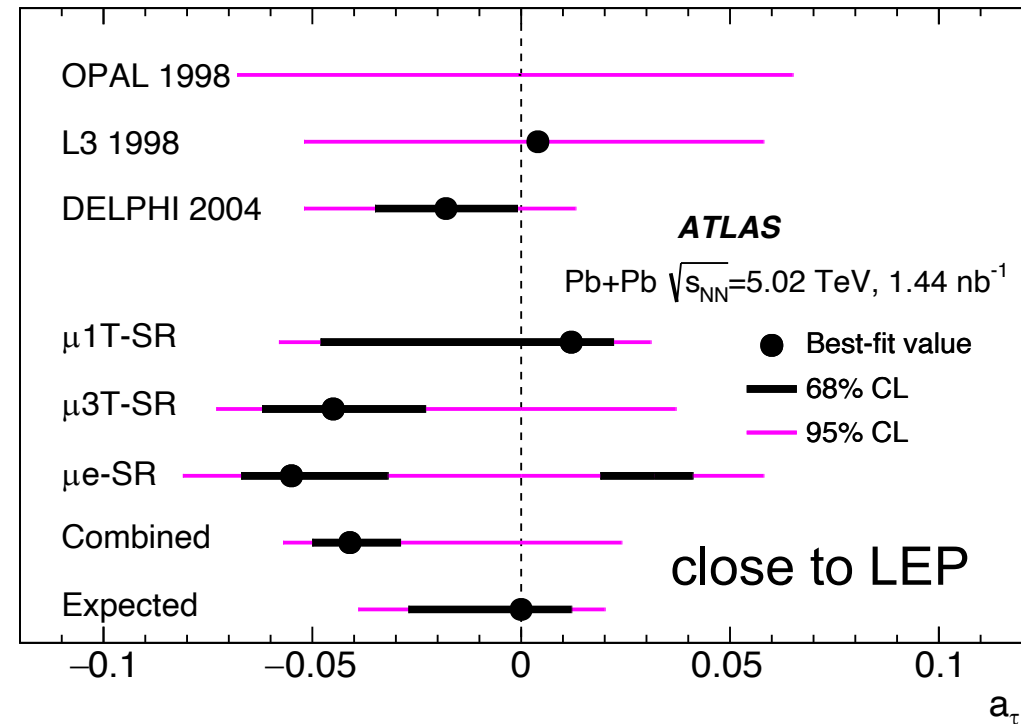


# $\gamma\gamma \rightarrow \tau\tau$ in ultraperipheral PbPb collisions

- 2022: first observed of  $\gamma\gamma \rightarrow \tau\tau$  in PbPb by CMS & ATLAS
- $\sigma \propto Z^4$  enhancement
- clean channel: small backgrounds
- phase space  $m_{\tau\tau} < 40$  GeV



ATLAS (2022) [STDM-2019-19](#)



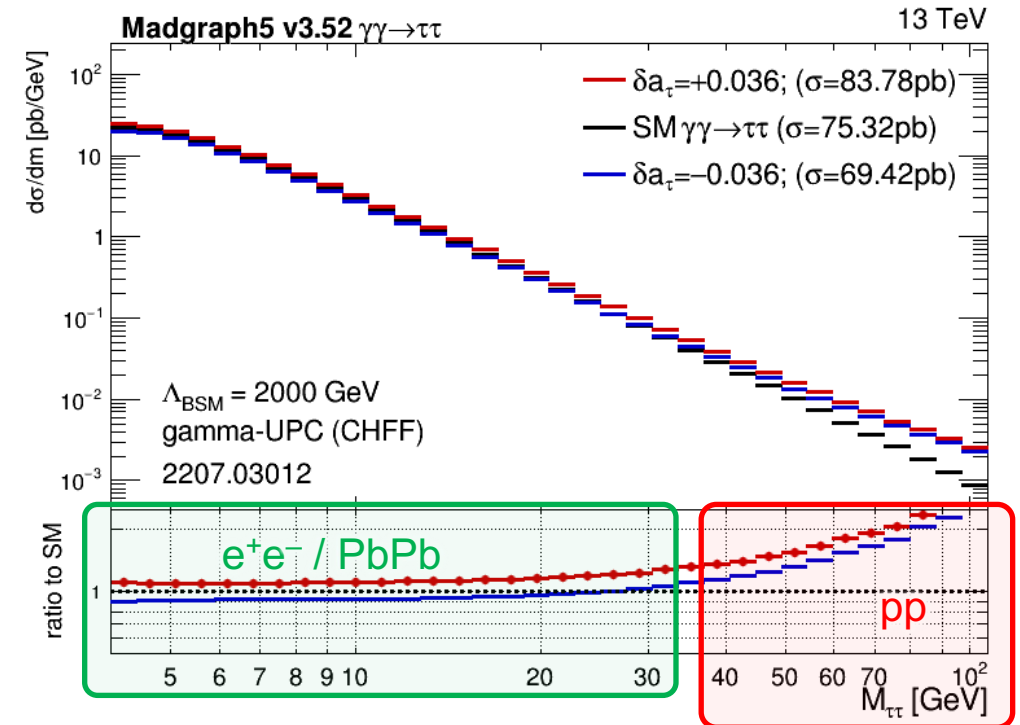
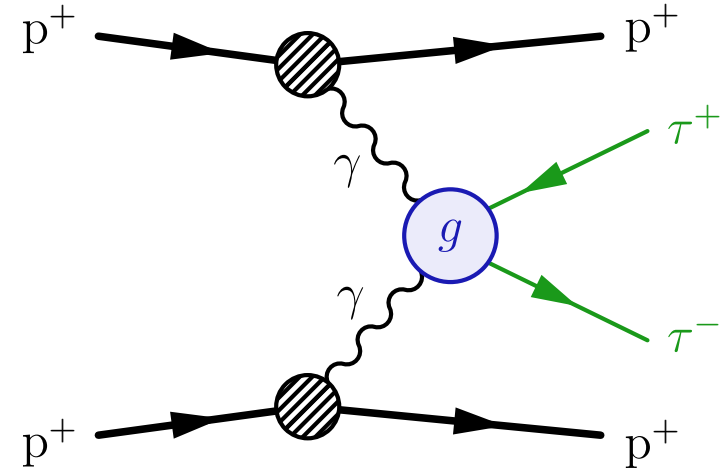
# $\gamma\gamma \rightarrow \tau\tau$ in pp collisions

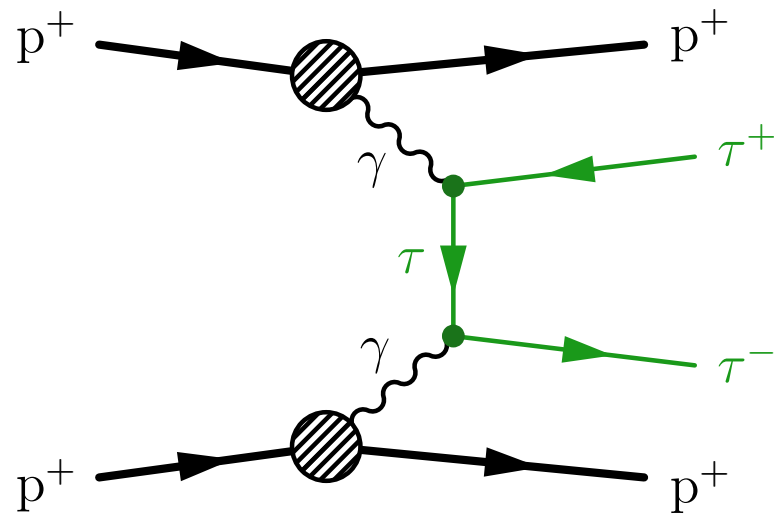
- cons:**

- no  $\sigma \propto Z^4$  enhancement
- soft signal: low acceptance
- large background
- high pileup

- pros:**

- much larger data set:  $\sim O(10^8)$
- much more sensitive to  $a_\tau$  modifications:  
expect large BSM enhancement  
at high  $\tau p_T$  and  $m_{\tau\tau}$

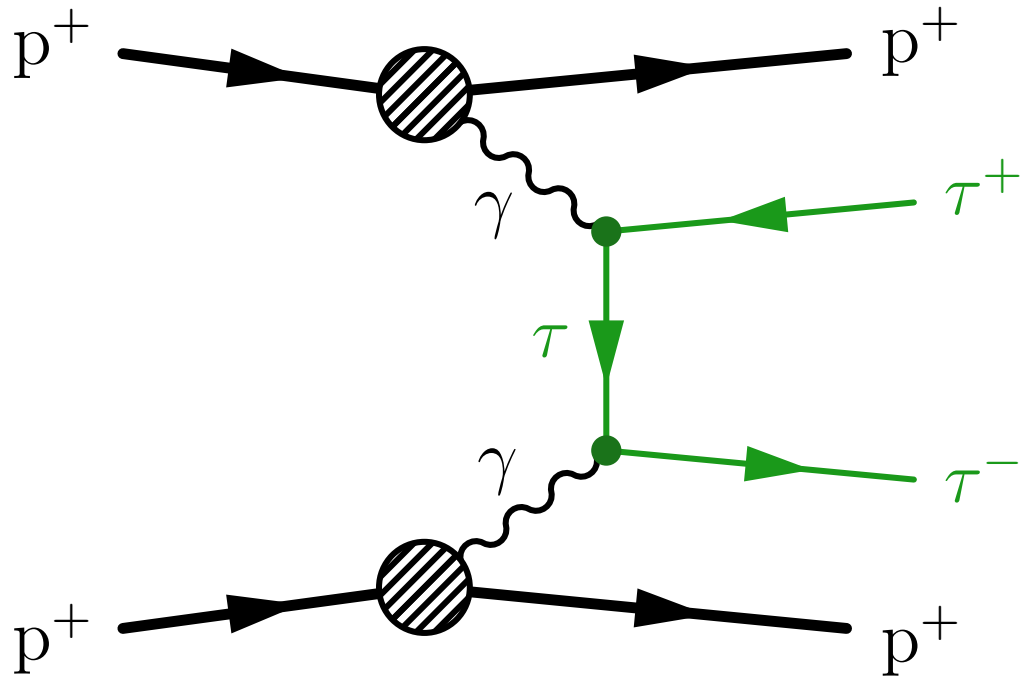




**$\gamma\gamma \rightarrow \tau\tau$  in  $pp$**

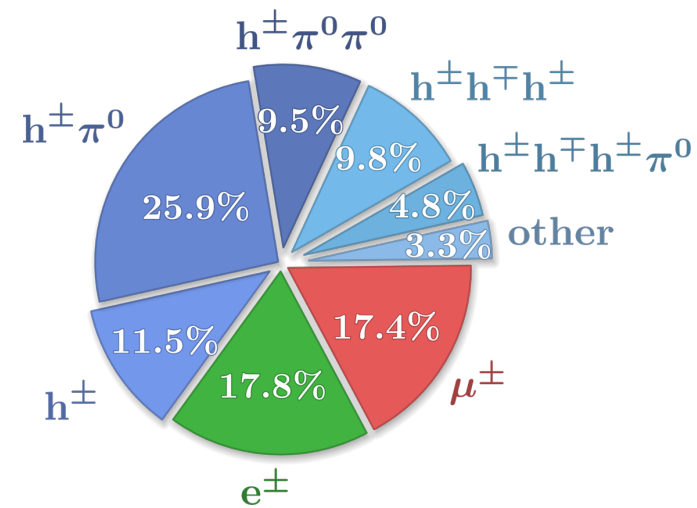
SMP-23-005

# $\gamma\gamma \rightarrow \tau\tau$ signature

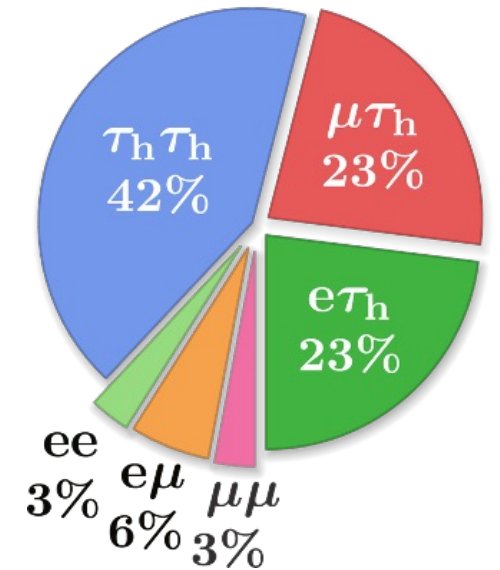


- **2  $\tau$  leptons**

- opposite charge sign
- back-to-back:  $|\Delta\phi| \approx \pi$
- $\tau$  decays:



- $\tau\tau$  decays:



- **2 diffracted protons**

- no hadronic activity close to  $\tau\tau$  vertex

$\tau^- \rightarrow \mu^-$

pile-up



$\tau^+ \rightarrow \pi^+ \pi^- \pi^+$

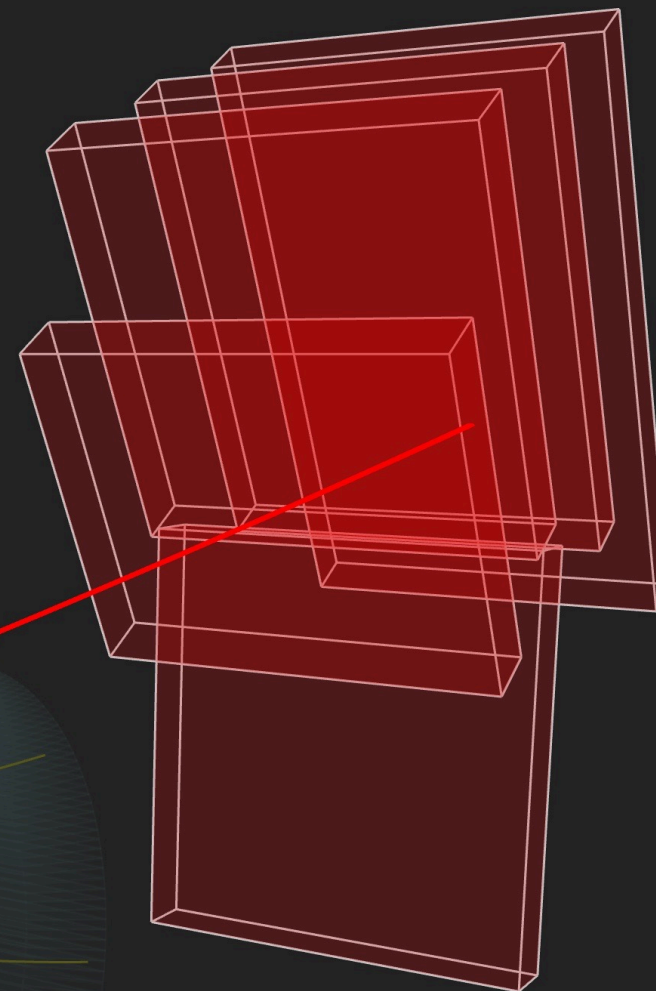
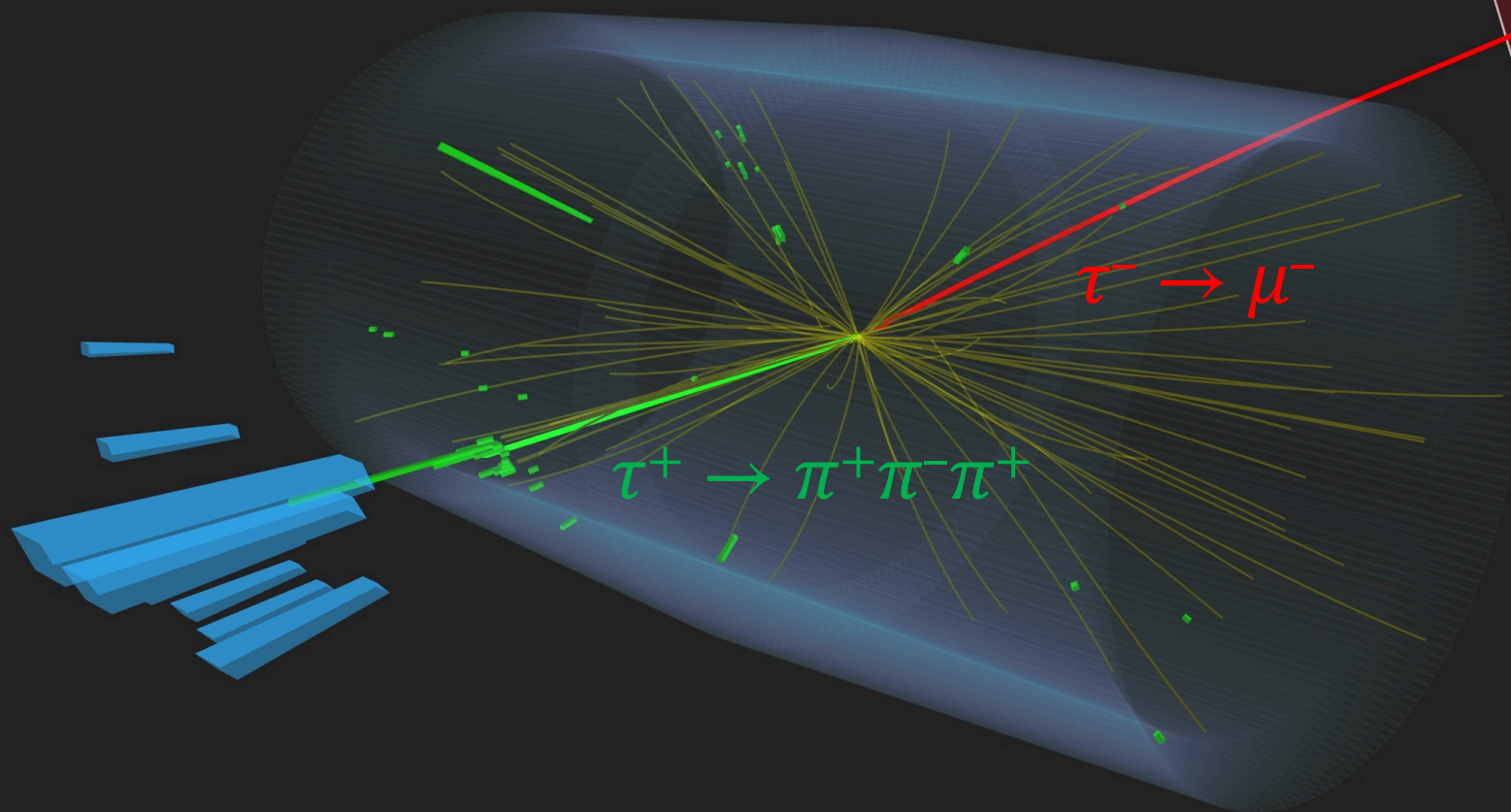




CMS Experiment at the LHC, CERN

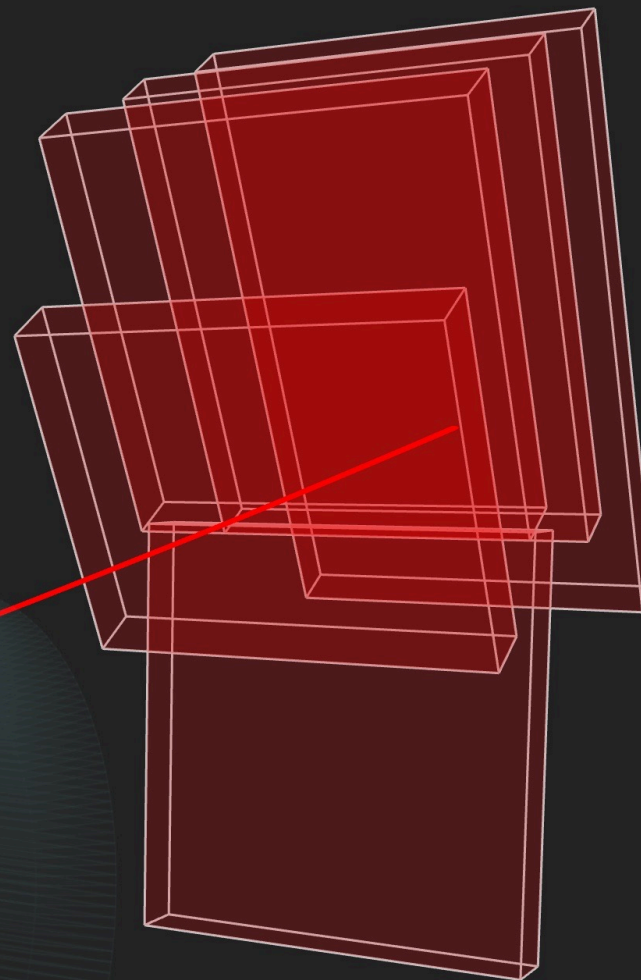
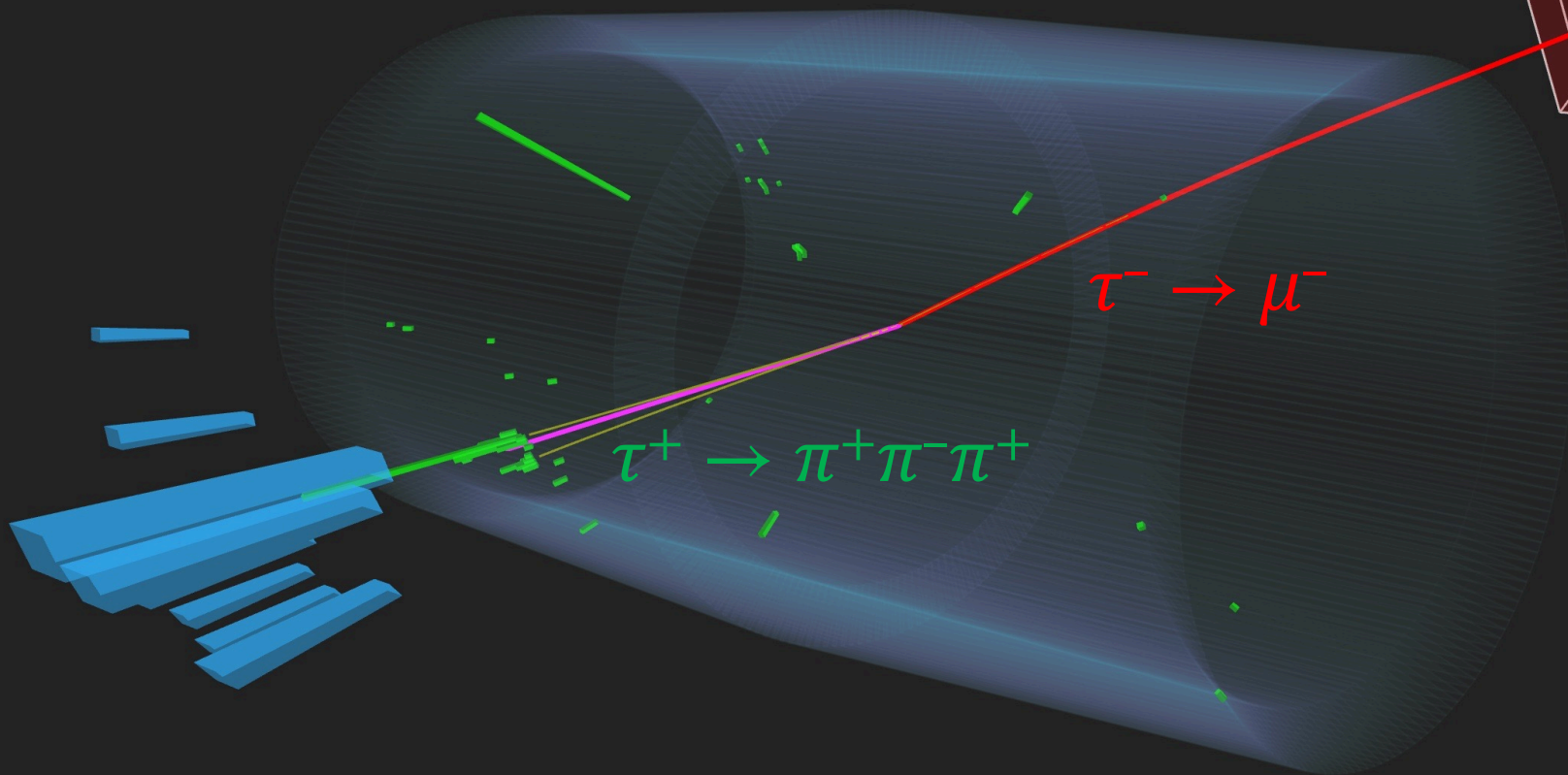
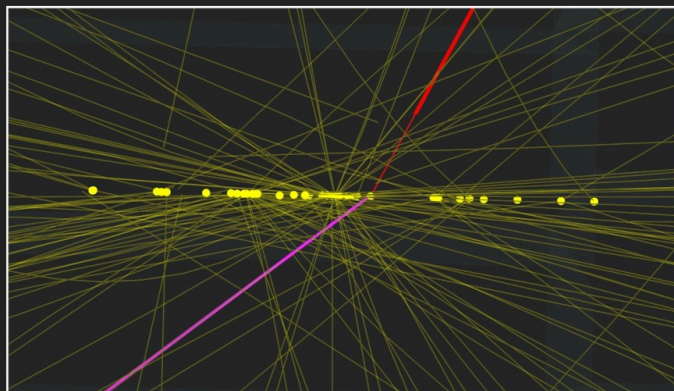
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Run / Event / LS: 315512 / 65277407 / 69



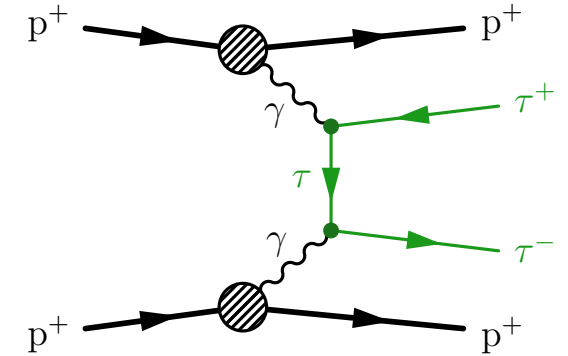


CMS Experiment at the LHC, CERN  
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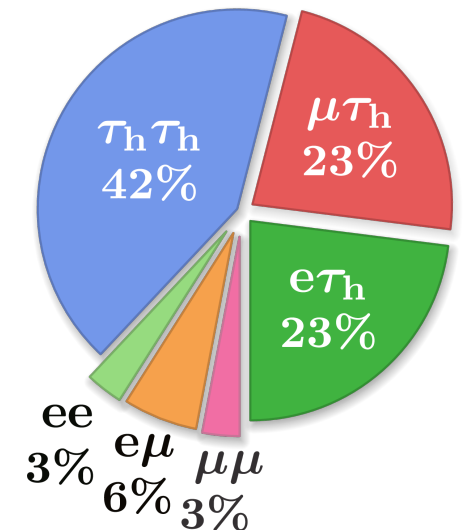


# Strategy to find $\gamma\gamma \rightarrow \tau\tau$ in pp

- select events with opposite sign  $\tau^+\tau^-$ 
  - combine 4  $\tau\tau$  final states:  $e\mu$ ,  $e\tau_h$ ,  $\mu\tau_h$ ,  $\tau_h\tau_h$
  - **exclusivity cuts**:
    - back-to-back:  $|\Delta\phi| \approx \pi$
    - low activity around  $\tau\tau$  vertex (low  $N_{\text{tracks}}$ )
- use  $\mu\mu$  events ( $Z \rightarrow \mu\mu$ ,  $\gamma\gamma \rightarrow \mu\mu$ ) to measure corrections to simulation
- measure  $\gamma\gamma \rightarrow \tau\tau$  from observed  $m_{\tau\tau}$  shape & yield in  $50 < m_{\tau\tau}^{\text{vis}} < 500$  GeV:
  - above  $e^+e^-$  & PbPb ( $m_{\tau\tau} \lesssim 50$  GeV)
  - $m_{\tau\tau}^{\text{vis}} \lesssim 500$  GeV to ensure unitarity in signal samples



$\tau\tau$  decay channels:



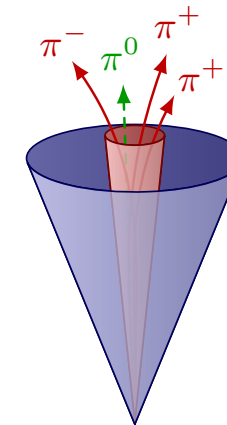
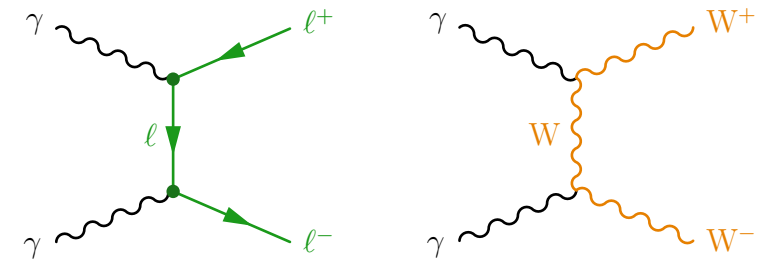
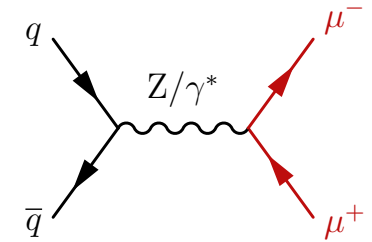
# Backgrounds to $\gamma\gamma \rightarrow \tau\tau$ search

- **MC simulation**

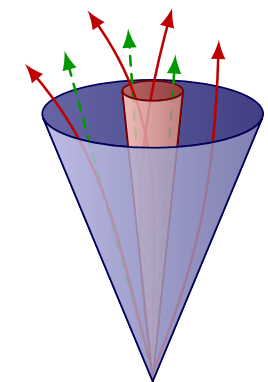
- **Drell–Yan ( $Z/\gamma^* \rightarrow \ell\ell$ ):** dominant at low mass
- **exclusive  $\gamma\gamma \rightarrow ee, \mu\mu, WW$  production**
- **inclusive  $WW$  production (small)**

- **data-driven:** misidentified hadronic jets

- $j \rightarrow \tau_h$ :  $e\tau_h, \mu\tau_h$  &  $\tau_h\tau_h$  channels
- $j \rightarrow e/\mu$ :  $e\mu$  channels



hadronic  
 $\tau_h$  jet

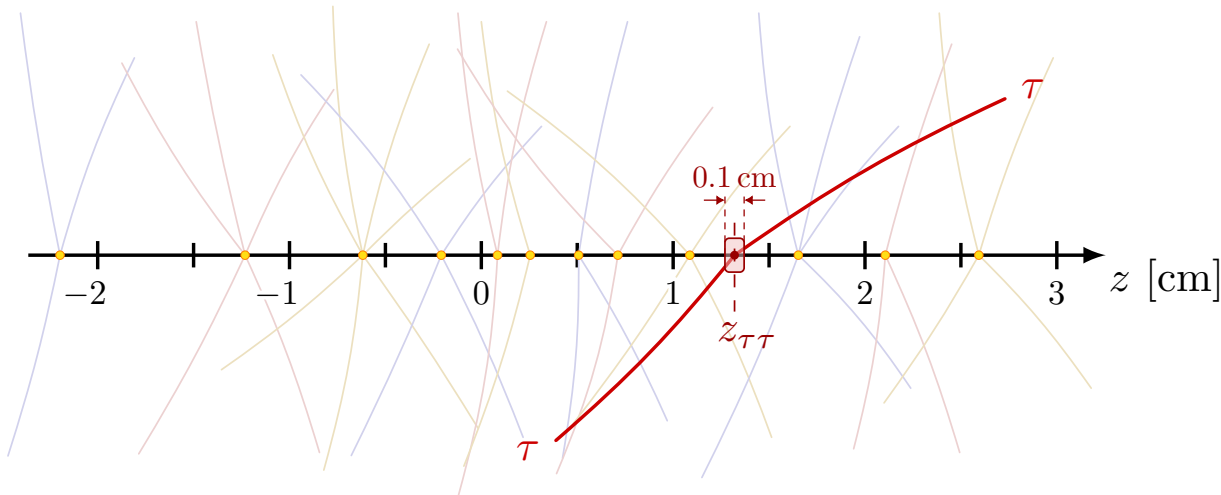


hadronic  
quark/gluon jet

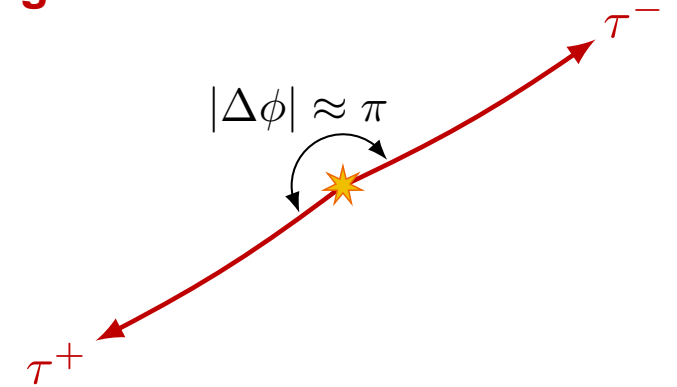
# Exclusivity cuts

define **signal regions** based on exclusivity cuts

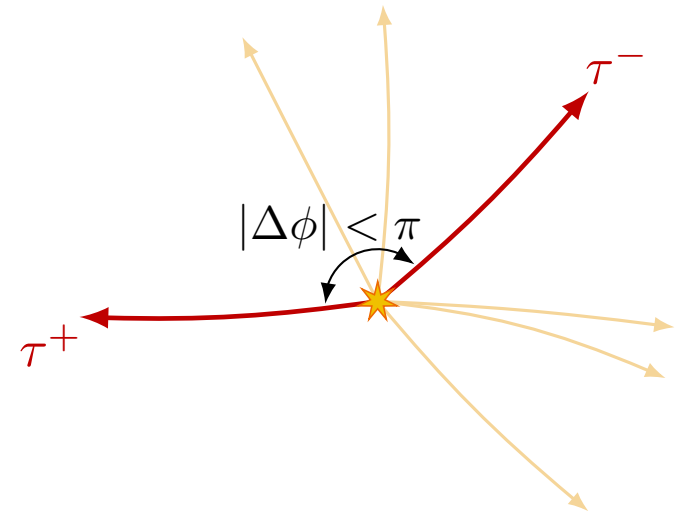
- **acoplanarity**  $A = 1 - \frac{|\Delta\phi|}{\pi}$ 
  - **$A < 0.015$** : >95% signal efficiency, and <30% Drell–Yan efficiency
- $N_{\text{tracks}}$ : count tracks with in **0.1 cm window** around  $\tau\tau$  vertex
  - $\tau\tau$  vertex reconstructed as  $z_{\tau\tau} = \frac{1}{2}(z_{\tau_1} + z_{\tau_2})$
  - **two categories:  $N_{\text{tracks}} = 0$  or  $1$** :  $\approx 75\%$  signal efficiency, and reduces backgrounds (like Drell–Yan) by  $\sim 10^3$



**signal:**



**Drell–Yan background:**



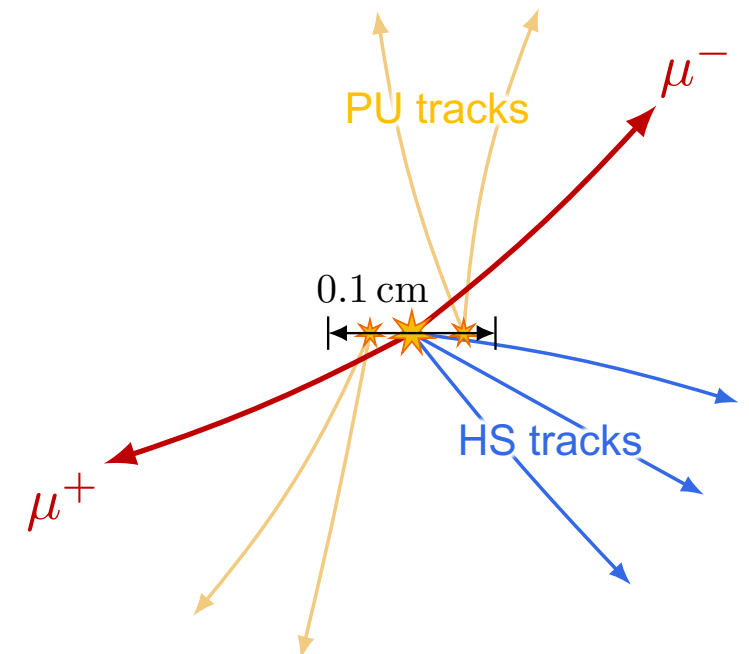
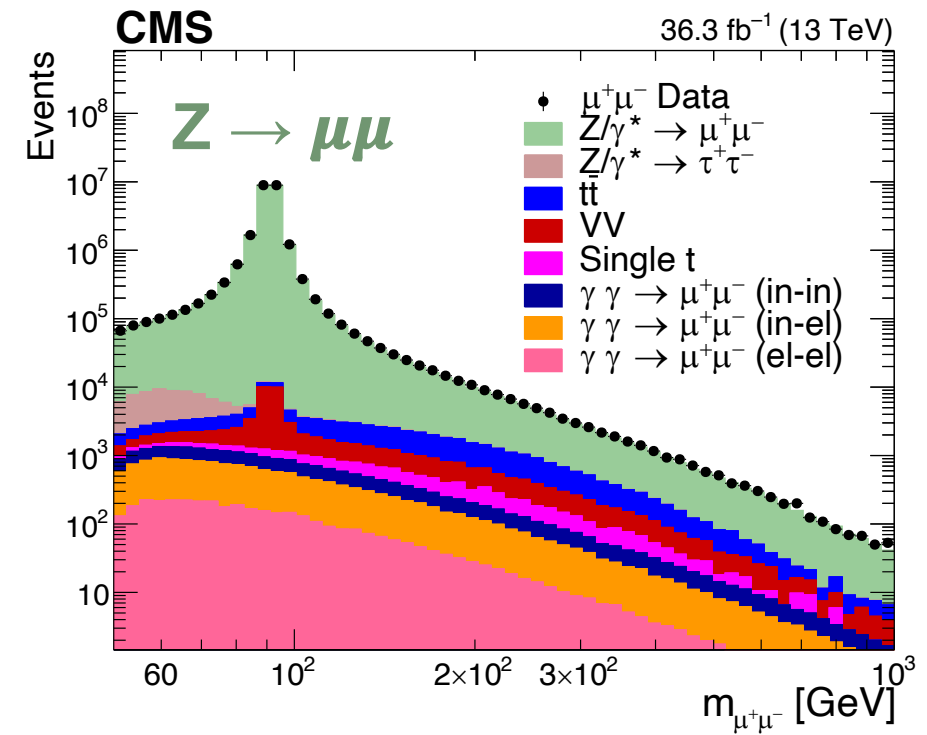
**CORRECTIONS**

# Corrections to simulation

modeling of observed data is not perfect

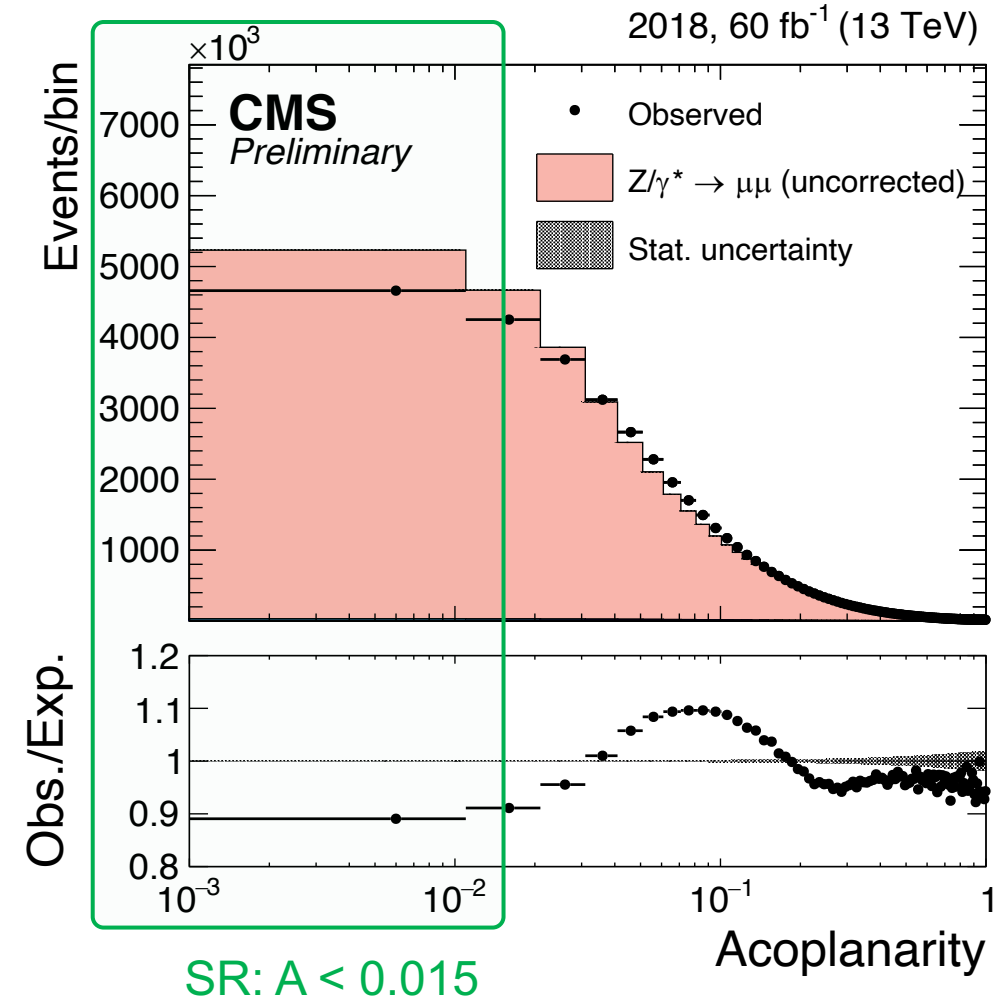
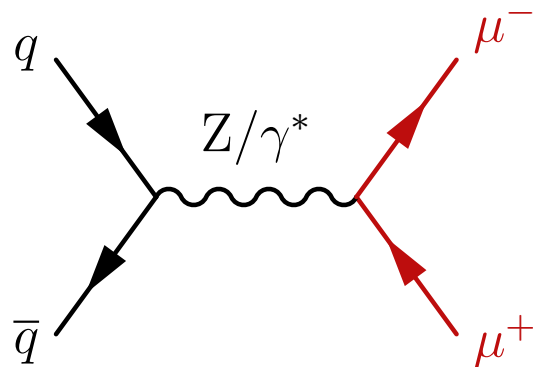
⇒ derive corrections in pure **dimuon ( $\mu\mu$ )** sample

1. **acoplanarity** in **Drell–Yan**
2. **pileup tracks**:  $N_{\text{tracks}}^{\text{PU}}$  in all simulation
3. **hard scattering tracks**:  $N_{\text{tracks}}^{\text{HS}}$  in **Drell–Yan**
4. **nonelastic contributions** of  $\gamma\gamma \rightarrow \ell\ell$  simulation



# 1. Acoplanarity corrections

- Drell–Yan generated by aMC@NLO does not describe well
  - Z boson  $p_T$
  - acoplanarity A
- measure corrections in pure  $Z/\gamma^* \rightarrow \mu\mu$  sample
- apply correction as a function of
  - acoplanarity A
  - leading and subleading muon  $p_T$

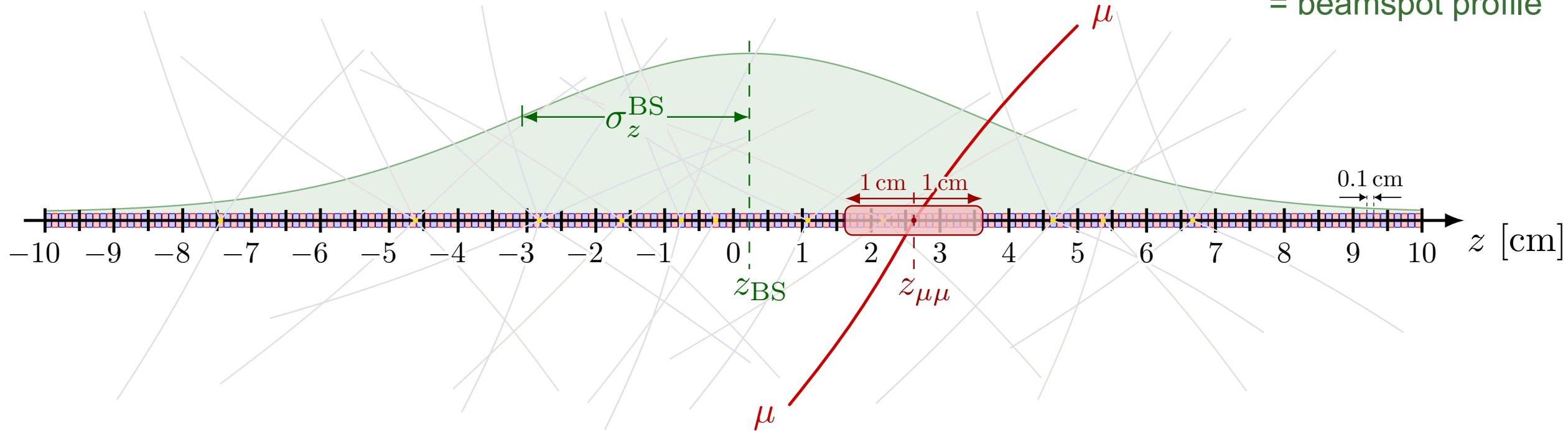




## 2. $N_{\text{tracks}}^{\text{PU}}$ corrections

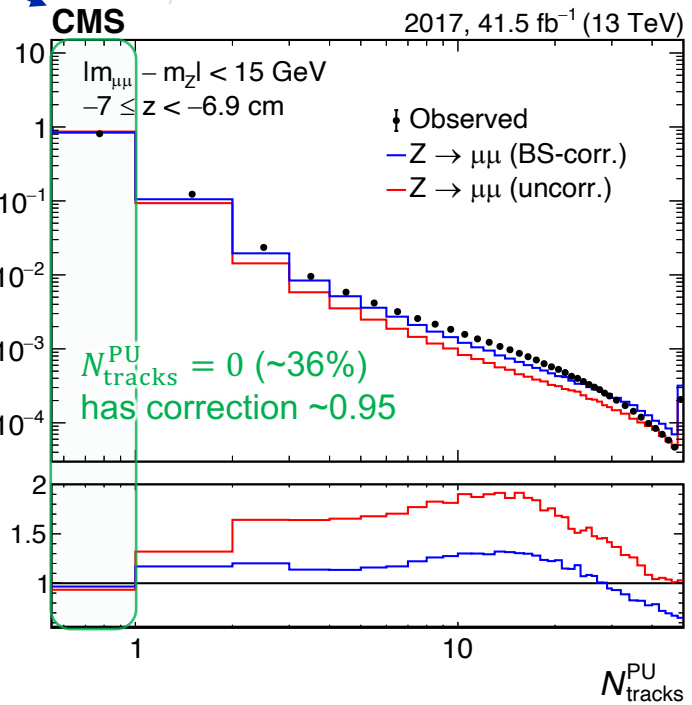
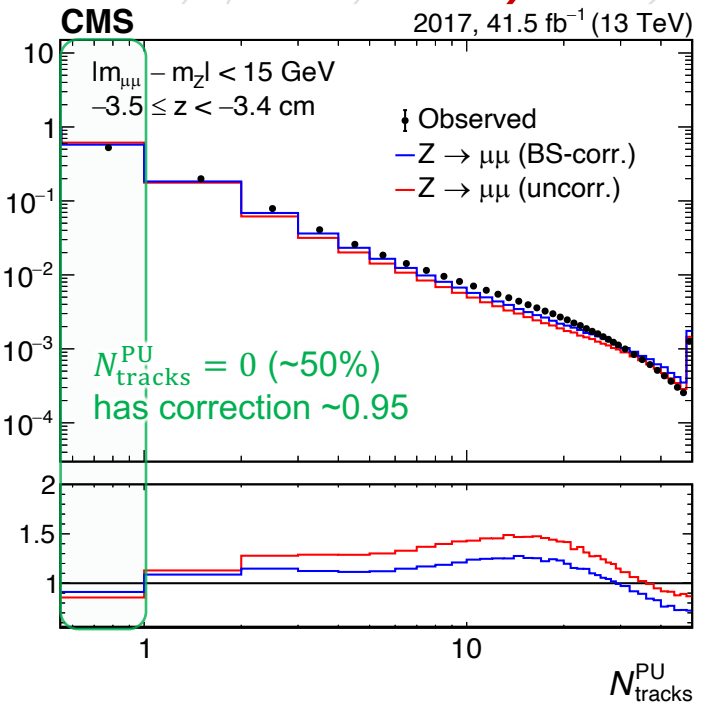
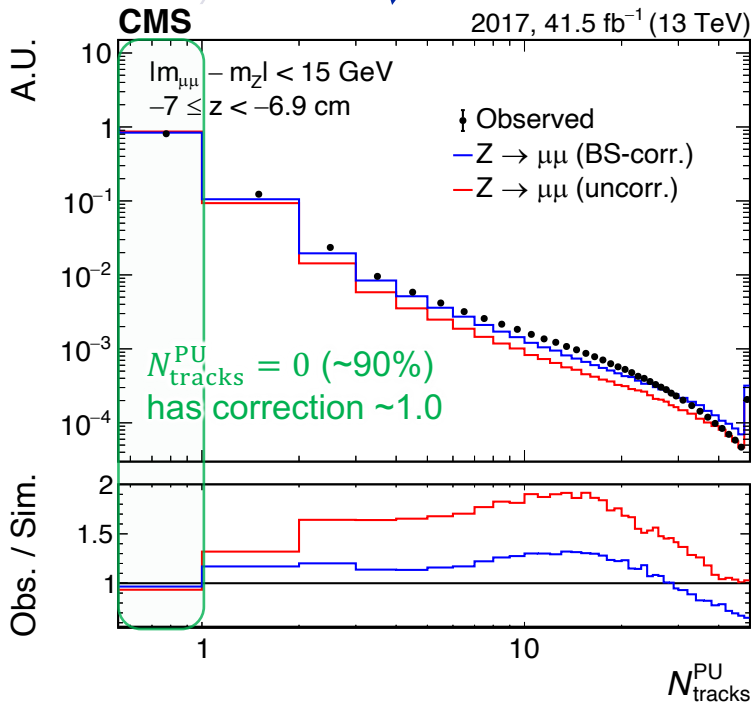
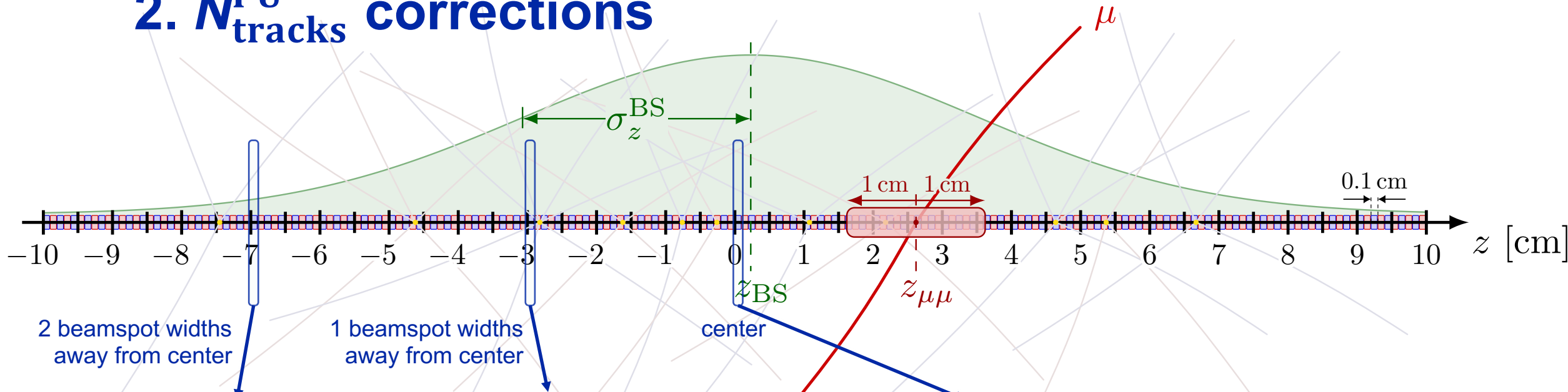
applied to all simulation

gaussian  
= beamspot profile



- use  $Z \rightarrow \mu\mu$  events at Z peak,  $|m_{\mu\mu} - m_Z| < 15$  GeV
- count number of PU tracks in small  $z$  windows (far away from  $\mu\mu$  vertex)
- derive correction from obs. / sim. ratio as a function of  $z$  and  $N_{\text{tracks}}$

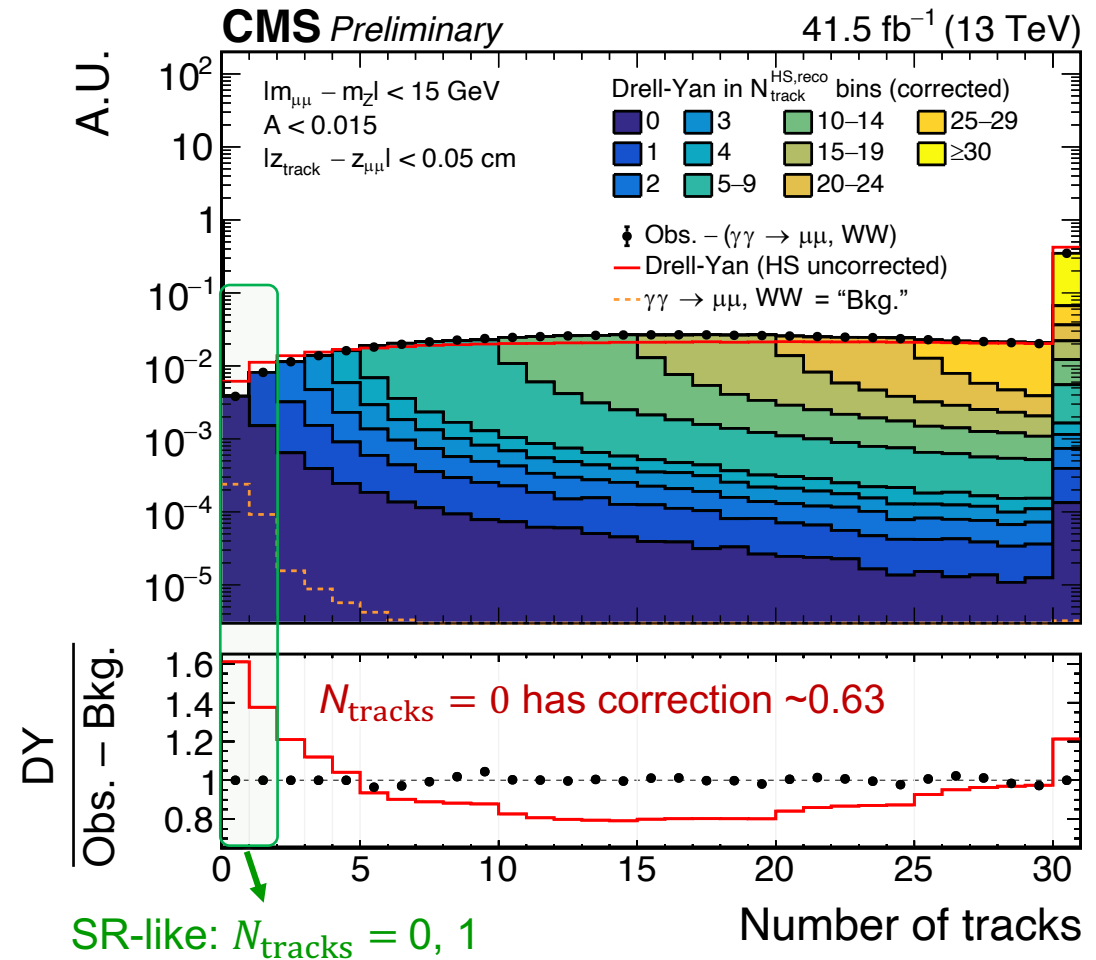
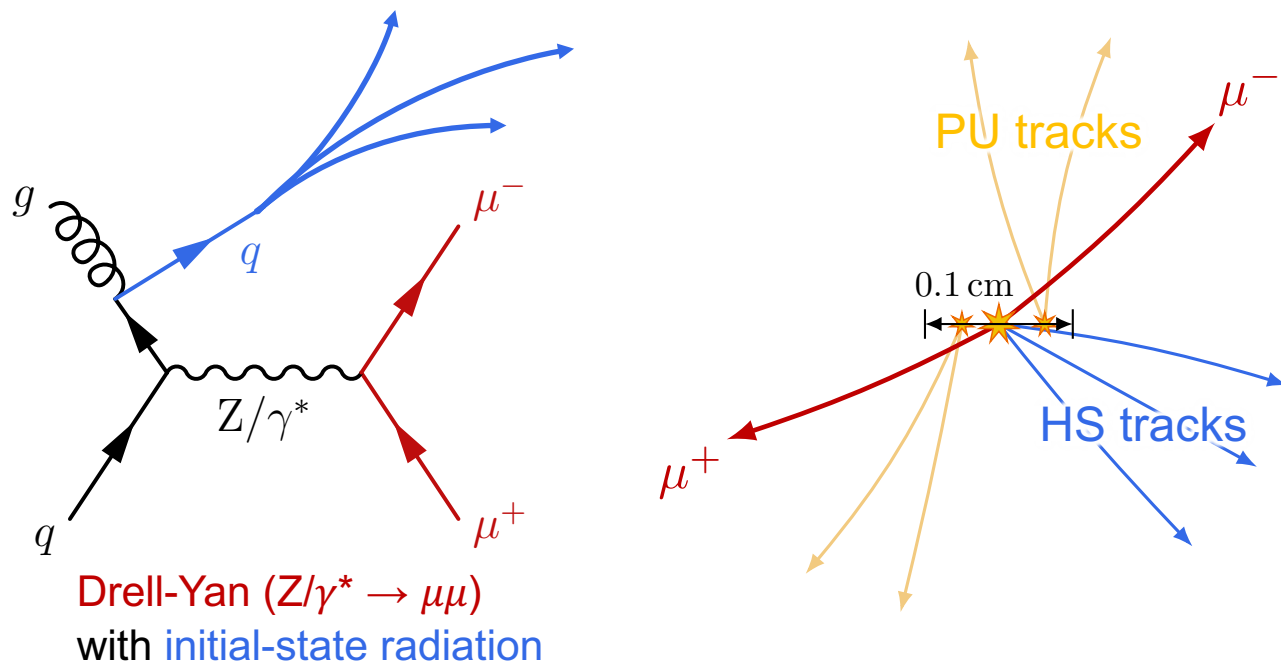
# 2. $N_{\text{tracks}}^{\text{PU}}$ corrections



derive correction from Obs. / Sim.

### 3. $N_{\text{tracks}}^{\text{HS}}$ correction

- use  $Z \rightarrow \mu\mu$  events at Z peak
- count  $N_{\text{tracks}}$  in signal window (0.1 cm) around  $\mu\mu$  vertex
- separate Drell–Yan into bins of  $N_{\text{tracks}}^{\text{HS}}$  by gen-matching reco tracks



$$N_{\text{tracks}} = N_{\text{tracks}}^{\text{HS}} + N_{\text{tracks}}^{\text{PU}}$$

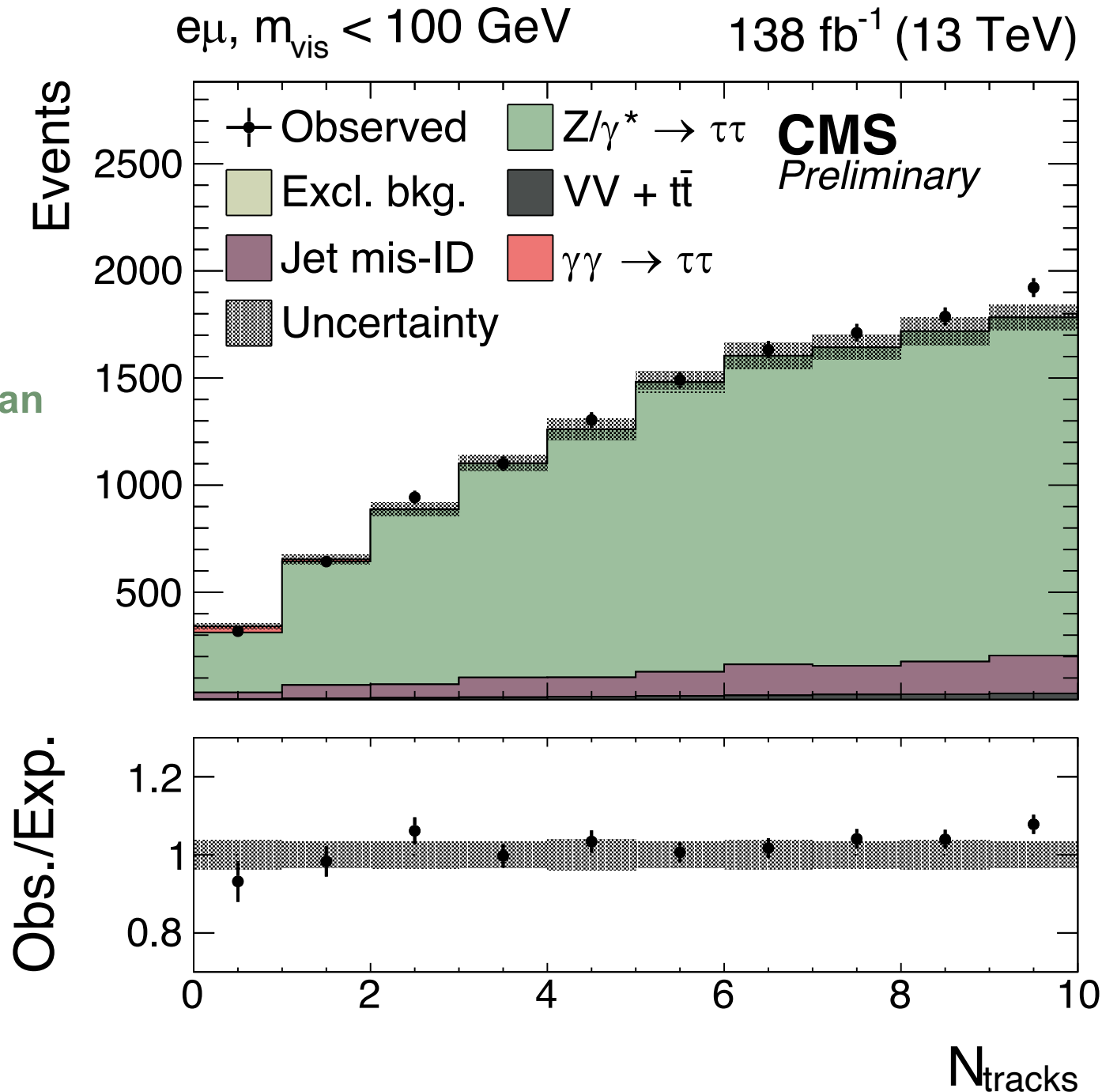
in signal window (0.1 cm)

# After corrections

1. acoplanarity in **Drell–Yan**
2. pileup tracks:  $N_{\text{tracks}}^{\text{PU}}$  in all simulation
3. hard scattering tracks:  $N_{\text{tracks}}^{\text{HS}}$  in **Drell–Yan**

**simulation** describes  
observed data well  
after these corrections !

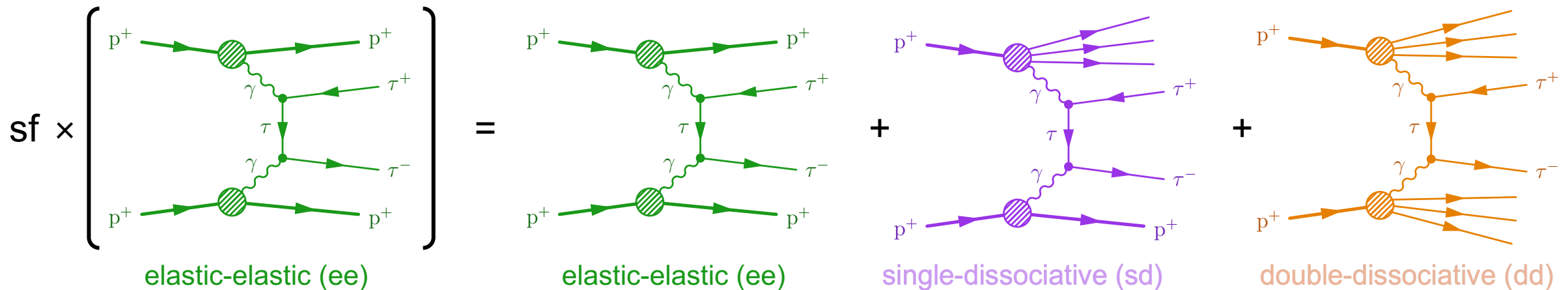
- $m_{\text{vis}}(\tau\tau) < 100$  GeV  
(low signal efficiency)
- in all  $\tau\tau$  final states



# 4. Elastic rescaling

- signal samples only include **elastic-elastic (ee)** process generated by gammaUPC
- **single-dissociative (sd)** and **double-dissociative (dd)** processes not included
  - have larger cross section
  - can have an exclusive signature
- estimate dissociative contributions (incl. higher-order corrections) by rescaling **elastic-elastic  $\gamma\gamma \rightarrow \mu\mu$  signal** in  **$\mu\mu$  data**

$$\Rightarrow \text{measure rescaling factor} = \frac{(\mathbf{ee} + \mathbf{sd} + \mathbf{dd})_{\text{obs}}}{(\mathbf{ee})_{\text{sim}}}$$

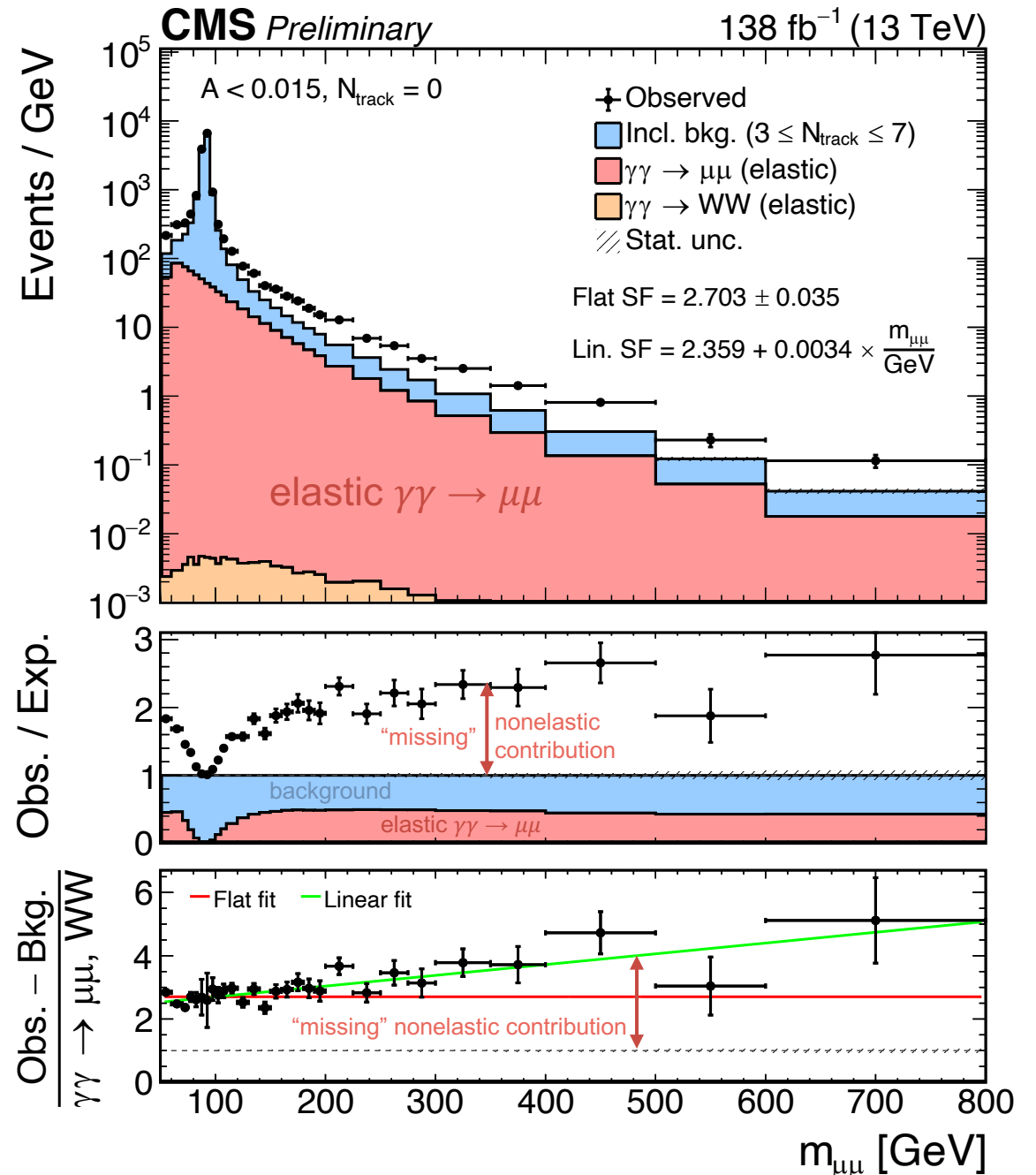


# 4. Elastic rescaling

- rescaling factor measured in  $m_{\mu\mu}$  distribution in dimuon events with  $A < 0.015$  and  $N_{\text{tracks}} = 0$  or 1
- **inclusive background** (mostly Drell–Yan)
  - estimated from data in  $3 \leq N_{\text{tracks}} \leq 7$  region
  - normalized to Z peak
- **elastic  $\gamma\gamma \rightarrow \mu\mu$ /WW “signal”**
  - contributes significantly  $m_{\mu\mu} > 150$  GeV
  - rescale to data to estimate nonelastic contribution
- fits:
  - **linear fit** applied as nominal corrections to all elastic simulation ( $\gamma\gamma \rightarrow ee, \mu\mu, \tau\tau, WW$ )
  - **flat fit (~2.7)** used to obtain uncertainty (conservative)

$$\text{rescaling factor} = \frac{(\text{ee} + \text{sd} + \text{dd})_{\text{obs}}}{(\text{ee})_{\text{sim}}} = \frac{\text{Obs.} - \text{Bkg.}}{\gamma\gamma \rightarrow \mu\mu, WW}$$

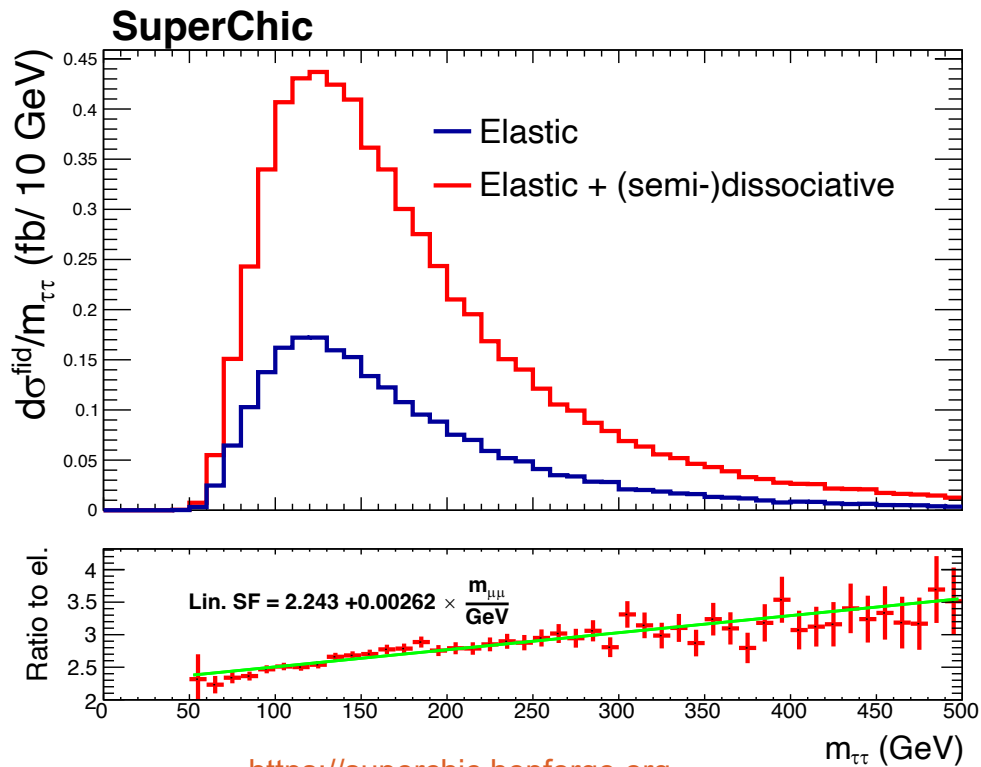
applied to photon-induced simulation ( $\gamma\gamma \rightarrow \ell\ell, WW$ )



# 4. Elastic rescaling

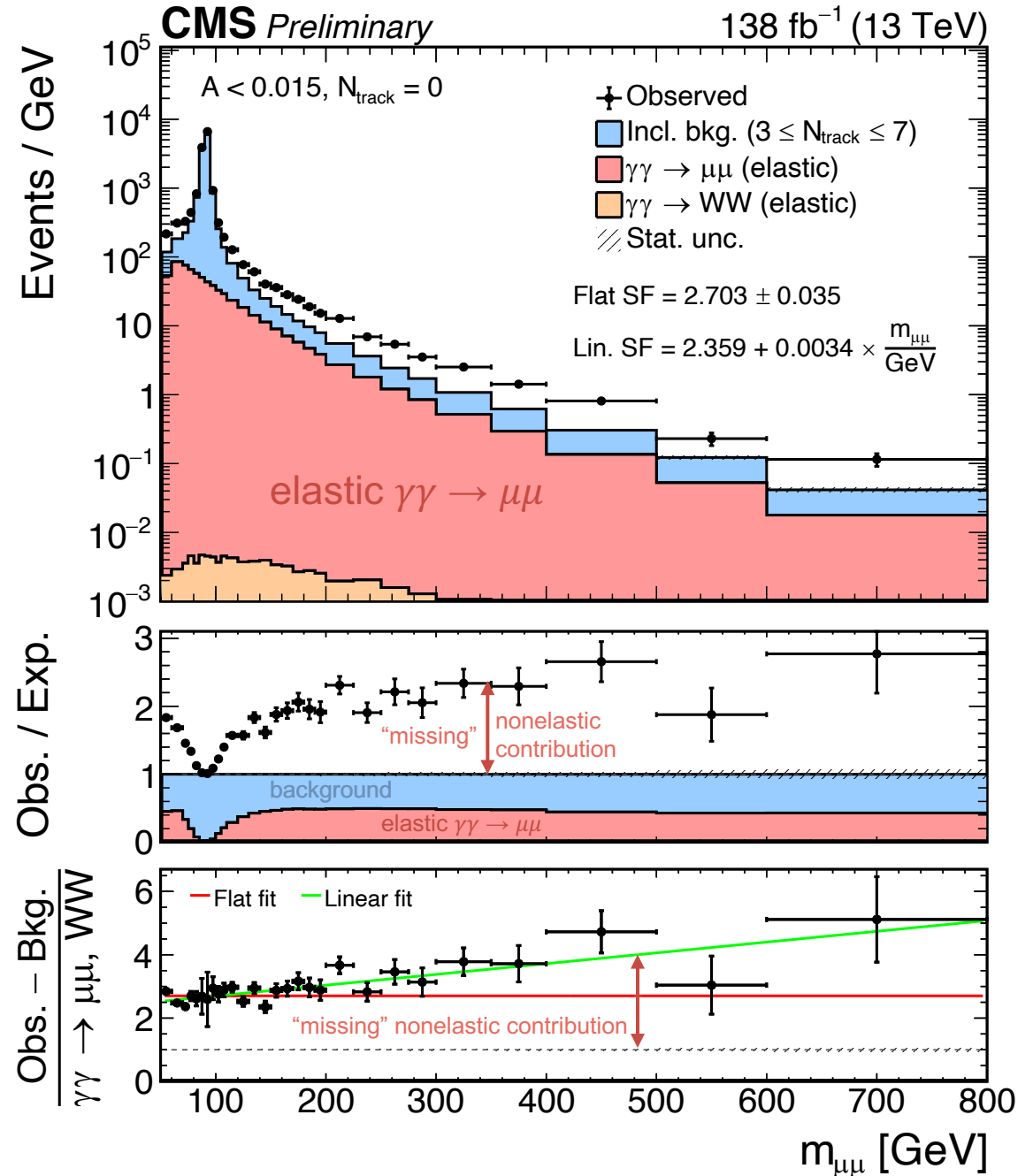
measured rescaling factor consistent with prediction by **SuperChic** generator within uncertainties!

- Measured:  $SF = 2.359 + 0.0032 \times \frac{m_{\mu\mu}}{\text{GeV}}$
- SuperChic:  $SF = 2.243 + 0.0026 \times \frac{m_{\mu\mu}}{\text{GeV}}$



<https://superchic.hepforge.org>

applied to photon-induced simulation ( $\gamma\gamma \rightarrow \ell\ell, WW$ )



# **BACKGROUND ESTIMATION**

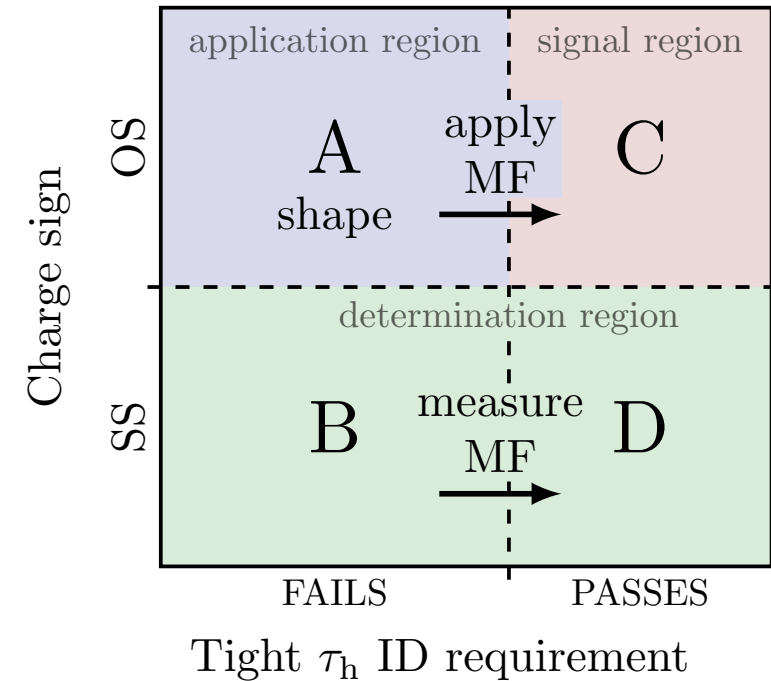


# $j \rightarrow \tau_h$ mis-ID background estimation

- background from  $j \rightarrow \tau_h$  mis-IDs mostly include **QCD multijet** and **W + jets** events
- estimated in a **data-driven** way
- measure “**mis-ID rate**” (**MF**) in several CRs

$$\text{MF} = \frac{N(j \rightarrow \tau_h \text{ passes } \mathbf{tight} \tau_h \text{ ID requirement})}{N(j \rightarrow \tau_h \text{ fails } \mathbf{tight}, \text{ but passes } \mathbf{looser} \tau_h \text{ ID requirement})}$$

- as a function of  $\tau_h p_T$  & decay mode

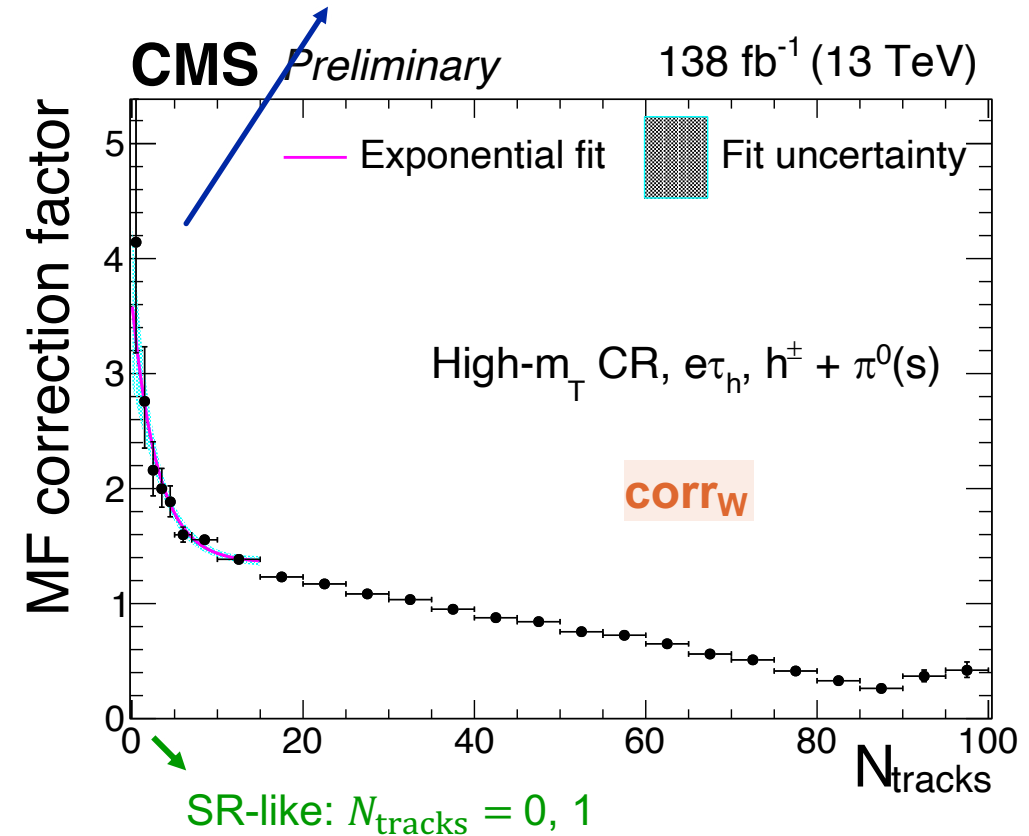


# Corrections to $j \rightarrow \tau_h$ MF in $e\tau_h$ & $\mu\tau_h$

jet is 4 times more likely to pass the tight  $\tau_h$  ID criteria if there is no other track at the vertex

- MFs & corrections measured in separate CRs:
  - $W$  + jets:  $m_T > 75$  GeV
  - QCD: SS,  $m_T < 75$  GeV
- fewer tracks lead to more isolated  $\tau_h$ 
  - ⇒ higher fake rates
  - ⇒ apply **corrections** as a function of  $N_{\text{tracks}}$
- total fake rate “ $j \rightarrow \tau_h$  misidentification factors”:

$$\text{MF} = f_W(m_{\text{vis}}, m_T) \times \text{MF}_W(p_T^{\tau_h}, \text{DM}^{\tau_h}) \times \text{corr}_W(N_{\text{tracks}}, \text{DM}^{\tau_h}) \\ + \left(1 - f_W(m_{\text{vis}}, m_T)\right) \times \text{MF}_{\text{QCD}}(p_T^{\tau_h}, \text{DM}^{\tau_h}) \times \text{corr}_{\text{QCD}}(N_{\text{tracks}}, \text{DM}^{\tau_h})$$



# RESULTS

Observation of  $\gamma\gamma \rightarrow \tau\tau$  in pp

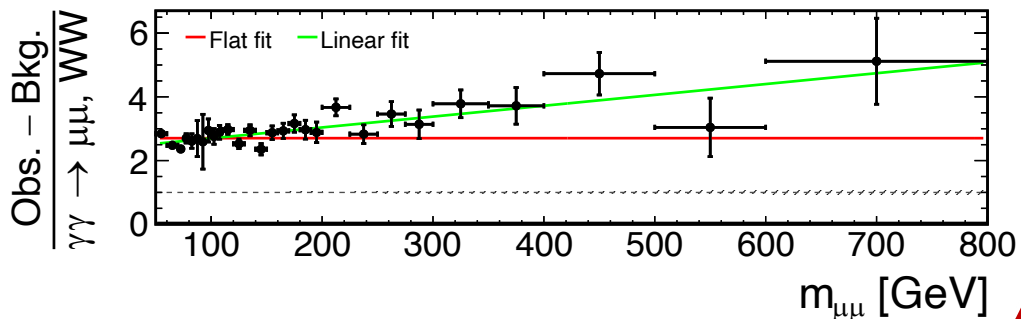
# Leading systematics

CMS Preliminary

138 fb<sup>-1</sup> (13 TeV)

— Fit  ±1 σ impact

$\hat{\mu} = 0.75^{+0.20}_{-0.18}$

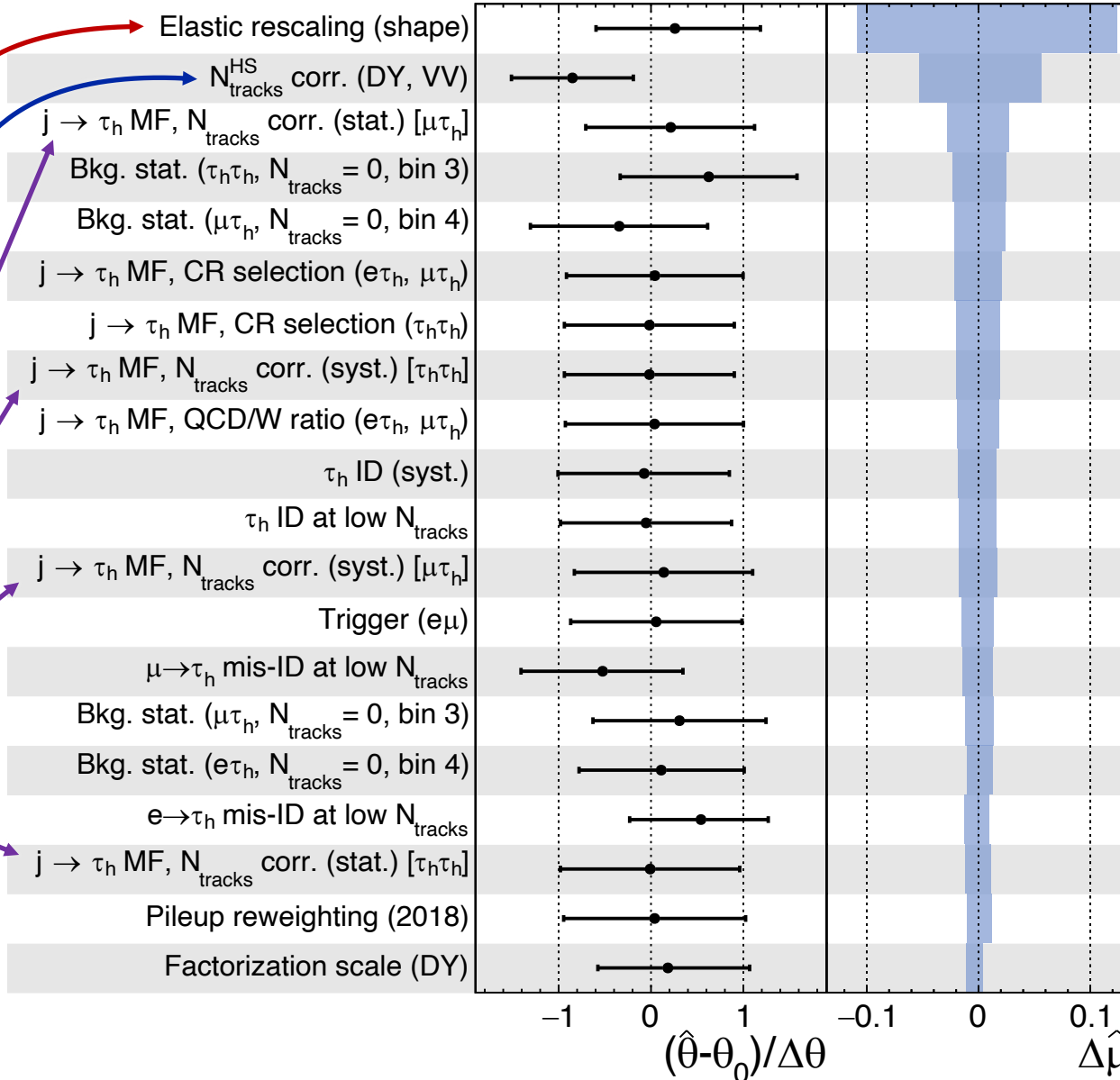


rescaling of elastic simulation ( $\gamma\gamma \rightarrow \ell\ell, WW$ )

- use linear fit to estimate uncertainty
- dominant systematic

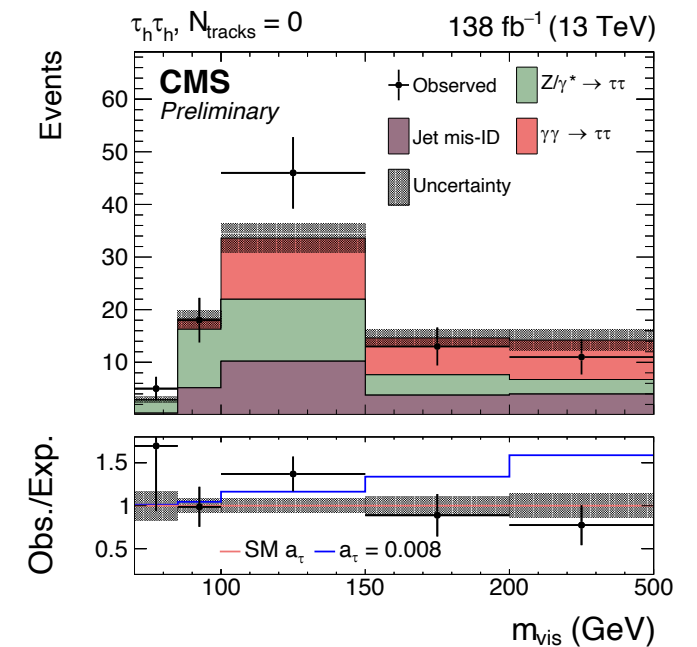
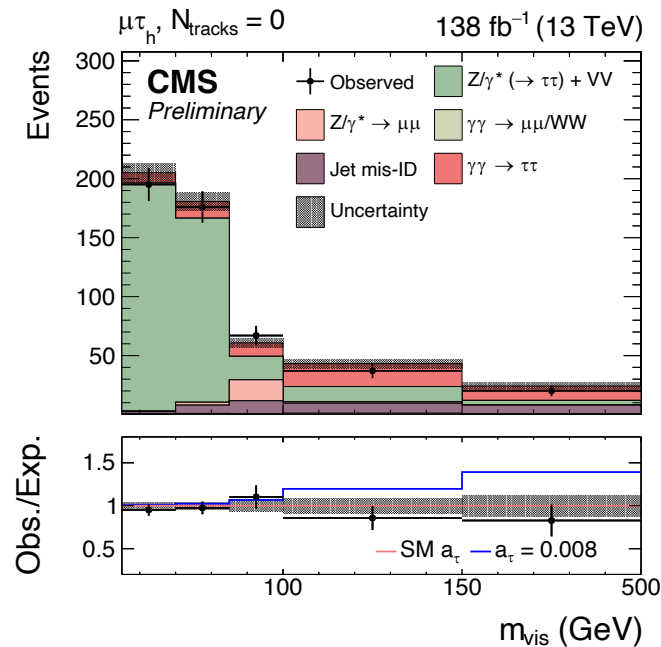
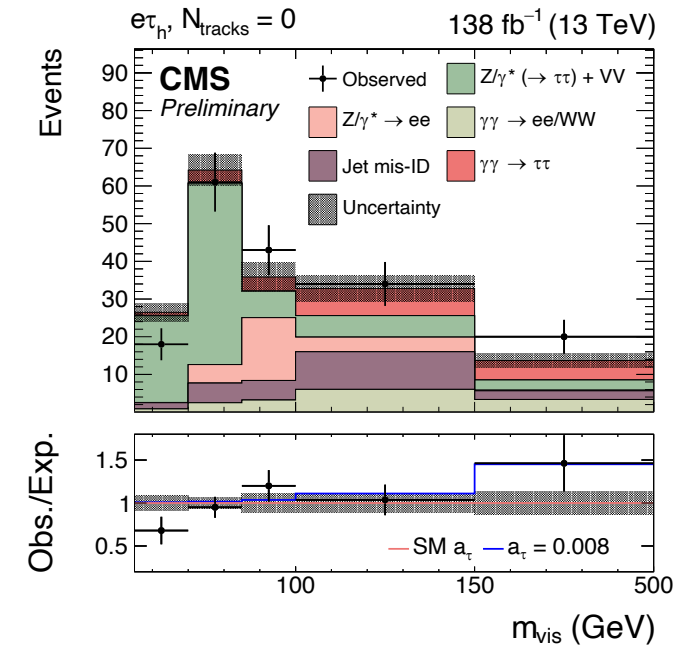
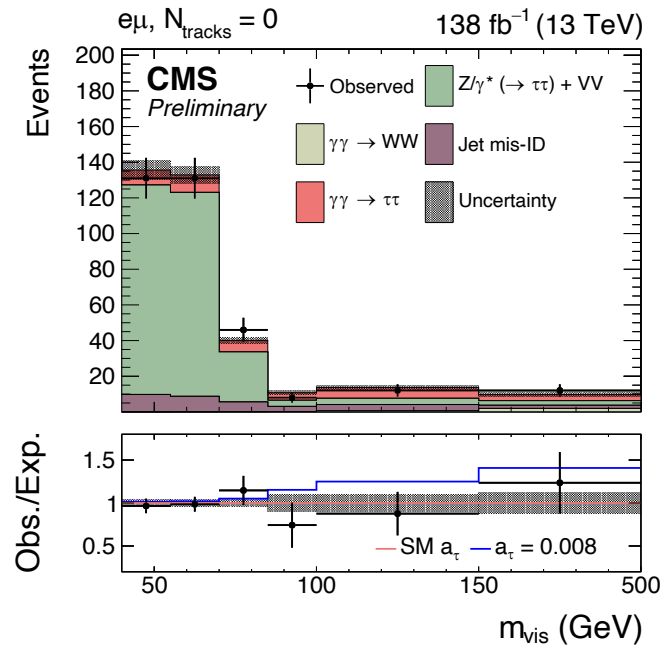
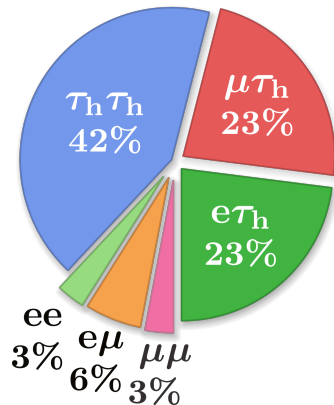
$N_{\text{tracks}}^{\text{HS}}$  correction in Drell–Yan  
(~6.5% in  $N_{\text{tracks}} = 0$ )

$N_{\text{tracks}}$  extrapolation to  $j \rightarrow \tau_h$  mis-ID rate  
(up to ~20%)



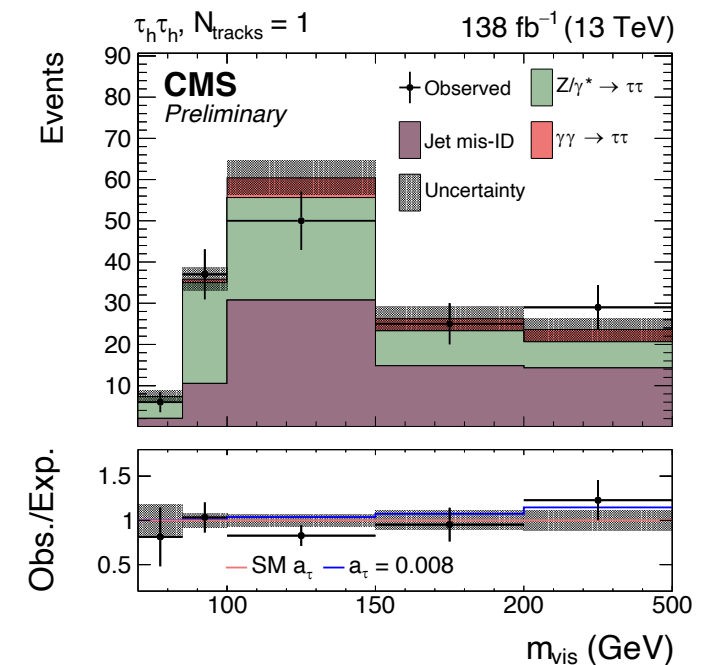
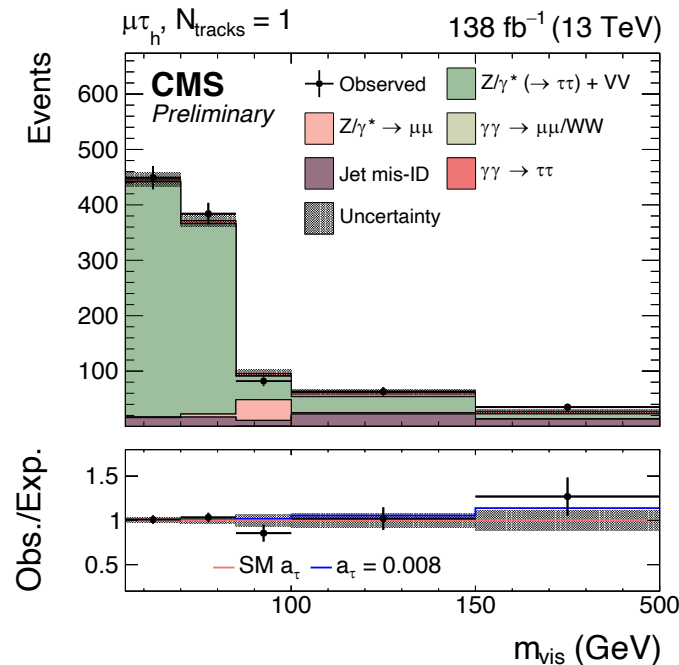
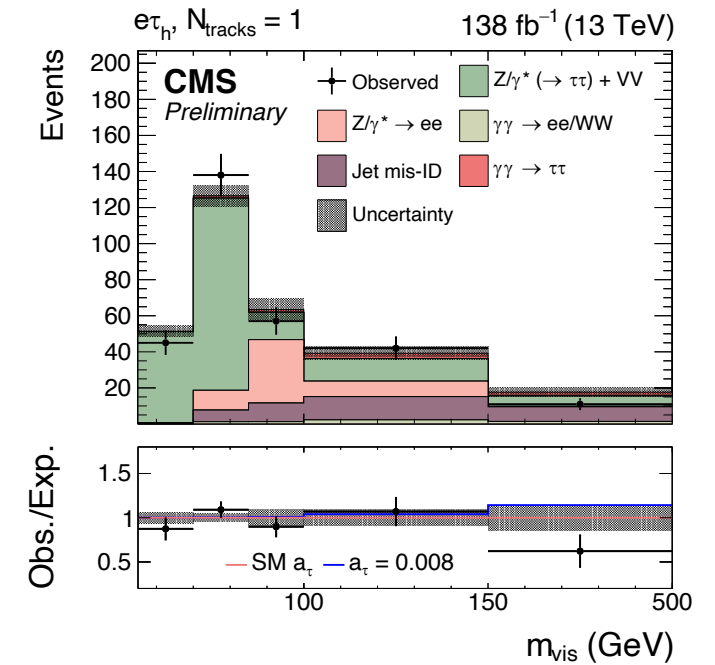
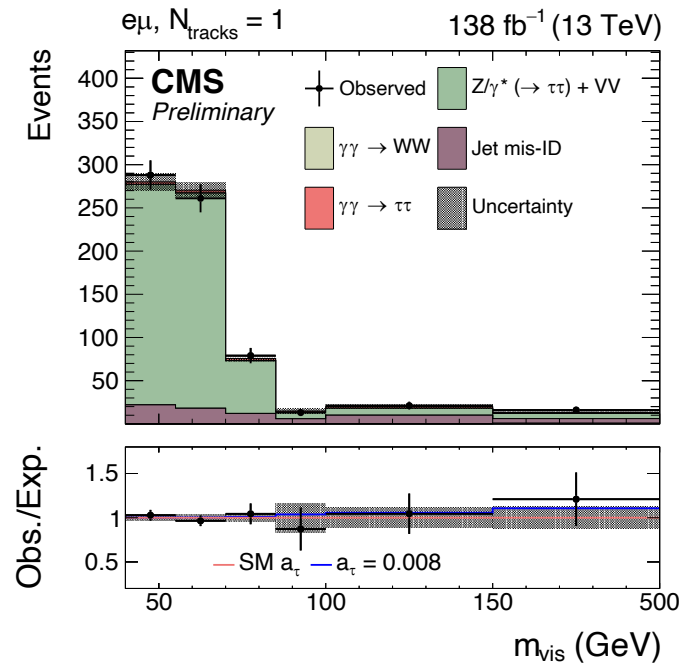
# SR with $N_{\text{tracks}} = 0$

- after maximum-likelihood fit to observed data
- assuming SM  $a_\tau$  &  $d_\tau$
- signal clearly visible in high  $m_{\text{vis}}(\tau\tau)$  bins



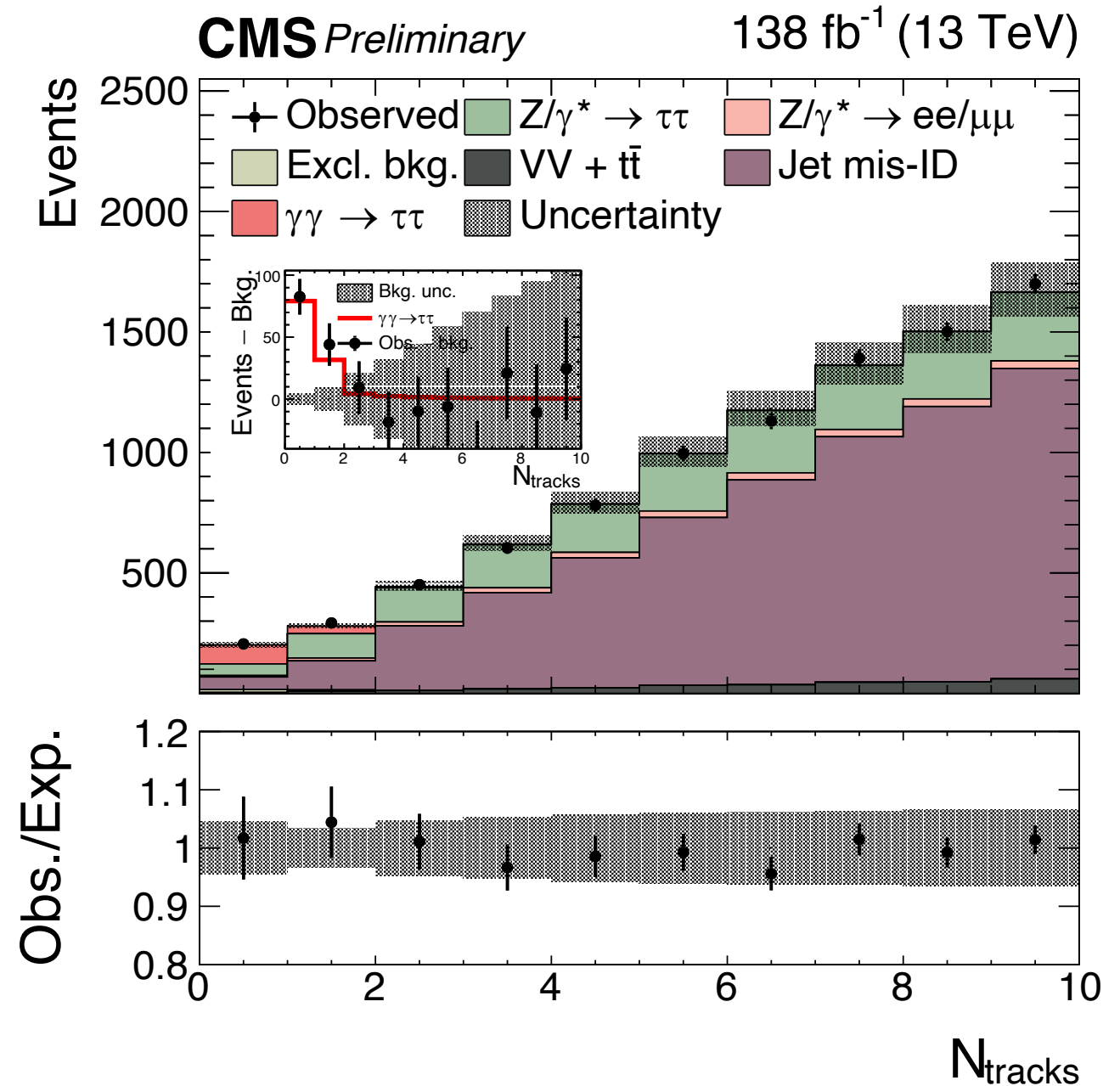
# SR with $N_{\text{tracks}} = 1$

- after maximum-likelihood fit to observed data
- assuming SM  $a_\tau$  &  $d_\tau$
- lower **signal efficiency**, but
  - still adds sensitivity
  - allows for validation of background modeling



# $N_{\text{tracks}}$ distributions

- same selections as SR, but
  - allowing  $N_{\text{track}} < 10$
  - $m_{\text{vis}} > 100 \text{ GeV}$
- combination of
  - all  $\tau\tau$  channels
  - all data-taking years
- very nice modeling of  $N_{\text{track}}$  !
- **signal clearly visible**



# First observation of $\gamma\gamma \rightarrow \tau\tau$ in pp collisions !

- combined observed significance of  **$5.3\sigma$**  ( $6.5\sigma$  expected) assuming SM  $a_\tau$

$\Rightarrow$  *first observation of  $\gamma\gamma \rightarrow \tau\tau$  in pp !*

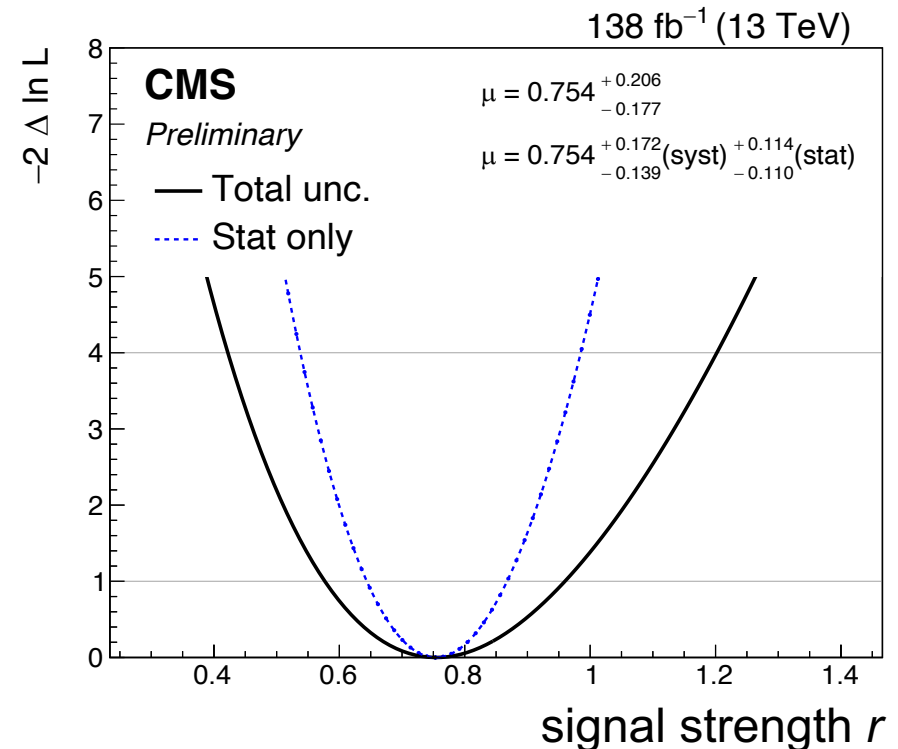
- combined **signal strength**

$$r = 0.75^{+0.21}_{-0.18}$$

w.r.t. gammaUPC elastic prediction

× rescaling measured in  $\mu\mu$  data

$\tau\tau$ channel	Observed	Expected
$e\mu$	$2.3\sigma$	$3.2\sigma$
$e\tau_h$	$3.0\sigma$	$2.1\sigma$
$\mu\tau_h$	$2.1\sigma$	$3.9\sigma$
$\tau_h\tau_h$	$3.4\sigma$	$3.9\sigma$
Combined	$5.3\sigma$	$6.5\sigma$





# RESULTS

Constraints on  $a_\tau$  &  $d_\tau$

# EFT interpretation to constrain $a_\tau$

- previous analyses used form factors ([DELPHI](#), [ATLAS](#), [CMS](#)), but we use an [SMEFT approach](#) (equivalent for  $q^2 \rightarrow 0$ )
- deviations of  $\delta a_\tau$  &  $\delta d_\tau$  from the SM can be parametrized in terms of a BSM Lagrangian with **dim-6 operators** with **NP scale  $\Lambda$** :

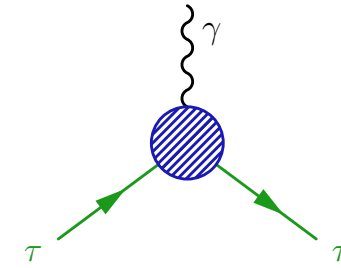
$$\mathcal{L}_{\text{BSM}} = \bar{L}_\tau \sigma^{\mu\nu} \tau_R H \left[ \frac{C_{\tau B}}{\Lambda^2} B_{\mu\nu} + \frac{C_{\tau W}}{\Lambda^2} W_{\mu\nu} \right]$$

- contributions to  $a_\tau$  &  $d_\tau$  are linearly dependent to the *complex* Wilson coefficients:

$$\delta a_\tau = \frac{2m_\tau \sqrt{2}v}{e \Lambda^2} \text{Re}[\cos \theta_W C_{\tau B} - \sin \theta_W C_{\tau W}]$$

$$\delta d_\tau = \frac{\sqrt{2}v}{\Lambda^2} \text{Im}[\cos \theta_W C_{\tau B} - \sin \theta_W C_{\tau W}]$$

- scan  $a_\tau$  &  $d_\tau$  values in  $\gamma\gamma \rightarrow \tau\tau$  signal samples:
  - by scanning  $C_{\tau B}$  and  $C_{\tau W}$  in matrix element reweighting
  - varying  $a_\tau$  or  $d_\tau$  changes the cross section and  $m_{\tau\tau}$  distribution
  - we fix  $\Lambda = 2 \text{ TeV}$  (although result *independent* of choice of  $\Lambda$ )

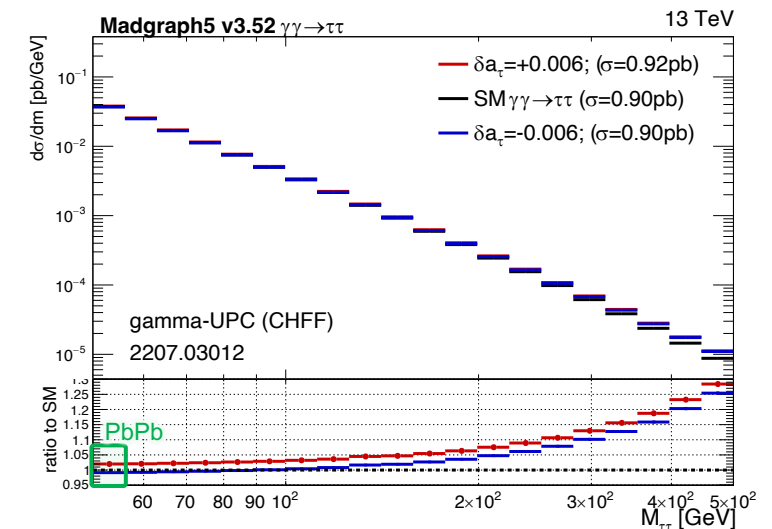


$$a_\tau^{\text{SM}} \approx 0.001177$$

$$a_\tau = \frac{g-2}{2} = a_\tau^{\text{SM}} + \delta a_\tau$$

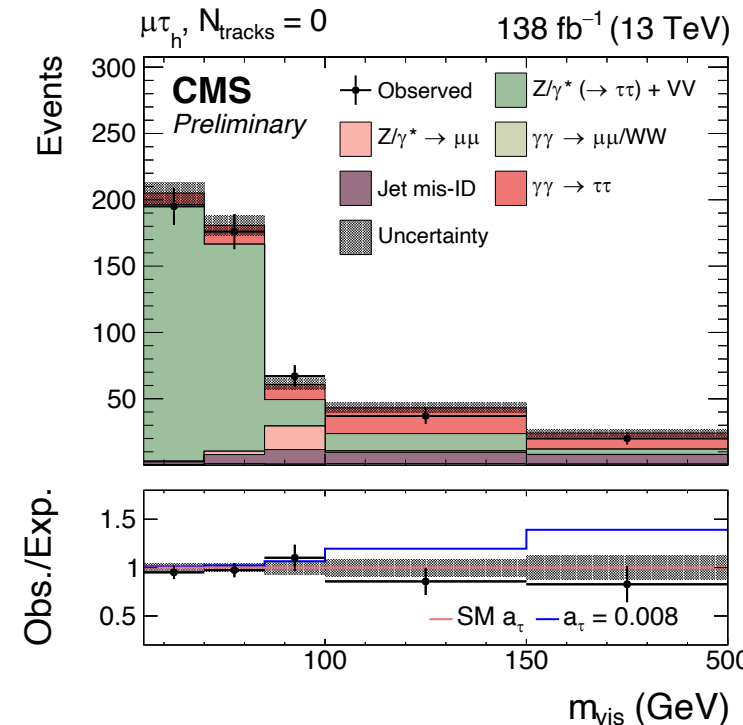
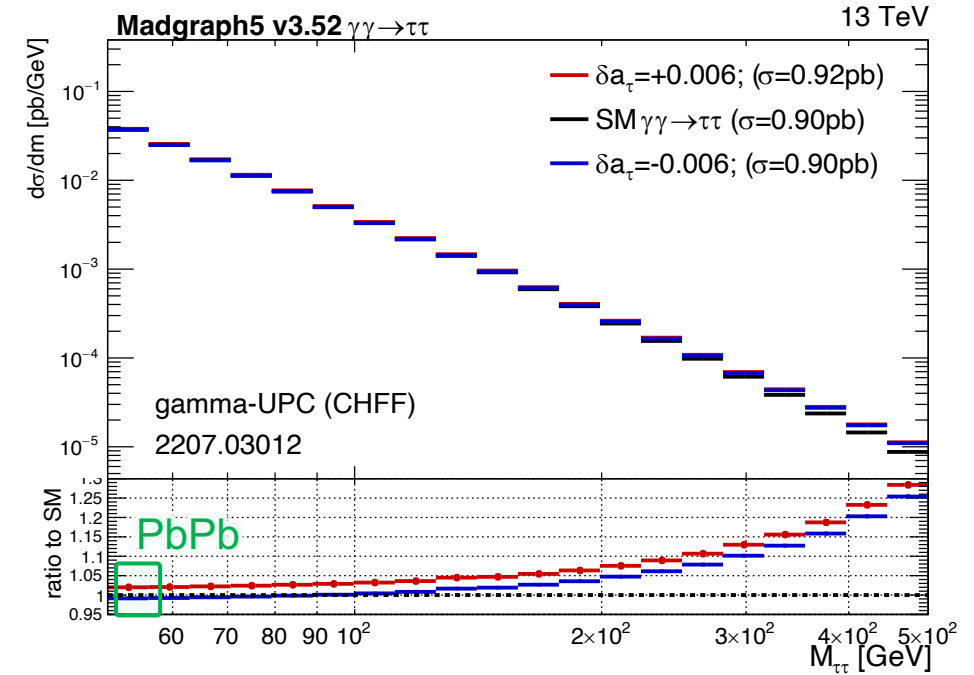
CP violation in CKM:  
 $d_\tau^{\text{SM}} \approx 10^{-37} \text{ ecm}$

some BSMs predict:  
 $d_\tau \approx 10^{-19} \text{ ecm}$



# How BSM in $a_\tau$ affects $\gamma\gamma \rightarrow \tau\tau$

- at  $m_{\tau\tau} > 100$  GeV:
  - cross section grows with  $m_{\tau\tau}$
  - for both  $\delta a_\tau > 0$  &  $\delta a_\tau < 0$
- constrain  $a_\tau$  by measuring the **yield** and  $m_{\tau\tau}$  distribution of  $\gamma\gamma \rightarrow \tau\tau$
- pp data looks at  $m_{\tau\tau} > 50$  GeV  $\Rightarrow$  better sensitivity than PbPb !

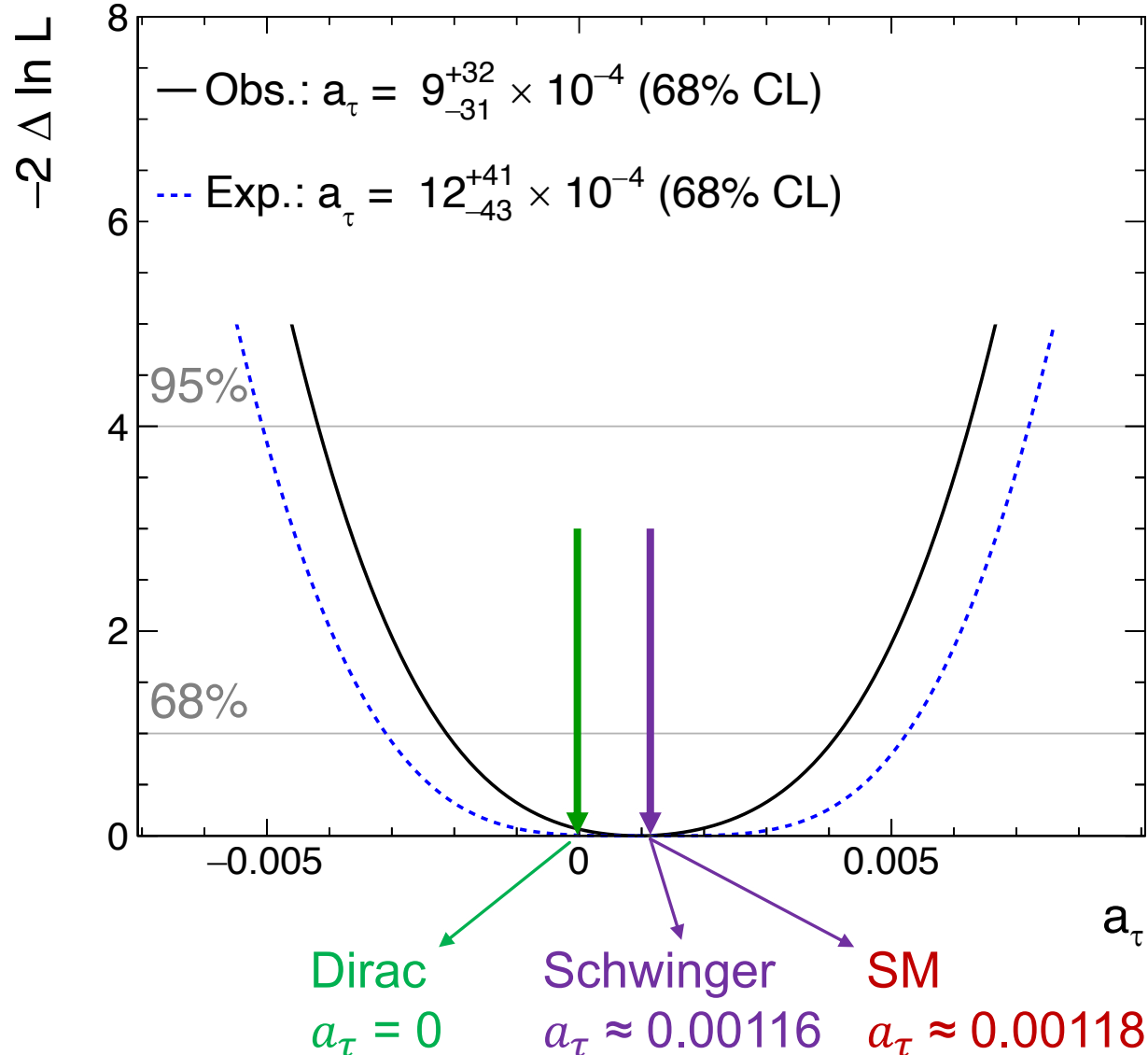


differences increase with  $m_{\tau\tau}$

# Constraints on $a_\tau$

**CMS Preliminary**

138 fb<sup>-1</sup> (13 TeV)



- fit all  $m_{\tau\tau}$  distributions
- scan likelihood over  $a_\tau$
- small  $\gamma\gamma \rightarrow \tau\tau$  deficit observed  
⇒ tighter constrain than expected
- but compatible with the SM

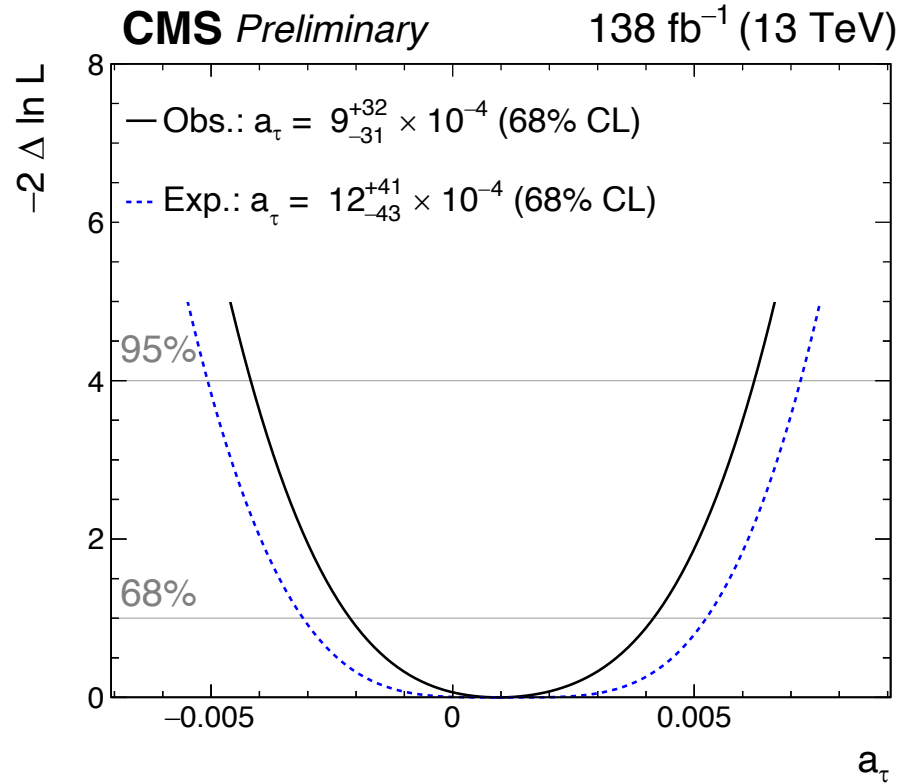
Schwinger:  $a_\tau = 0.001\ 161\ 4$

SM:  $a_\tau = 0.001\ 177\ 21(5)$

our result:  $a_\tau = 0.0009\ (32)$

⇒ uncertainty  $\sim 3 \times$  Schwinger !

# Constraints on $a_\tau$



- **SM:**  $a_\tau = 0.001\ 177\ 21(5)$
- **DELPHI:**  $a_\tau = -0.018 \pm 0.017$
- **ATLAS:**  $a_\tau = -0.041 +0.012 -0.009$
- **CMS HIN:**  $a_\tau = 0.001 +0.055 -0.089$
- **our result:**  $a_\tau = 0.0009 +0.0032 -0.0031$

~2.7x above SM, >5x better than LEP !

## CMS

138 fb<sup>-1</sup> (13 TeV)

• Observed — 68% CL — 95% CL

### OPAL

$ee \rightarrow Z \rightarrow \tau\tau\gamma$   
PLB 434 (1998) 188

### L3

$ee \rightarrow Z \rightarrow \tau\tau\gamma$   
PLB 434 (1998) 169

### DELPHI

$\gamma\gamma \rightarrow \tau\tau$  ( $\gamma$  from e)  
EPJC 35 (2004) 159

### ATLAS

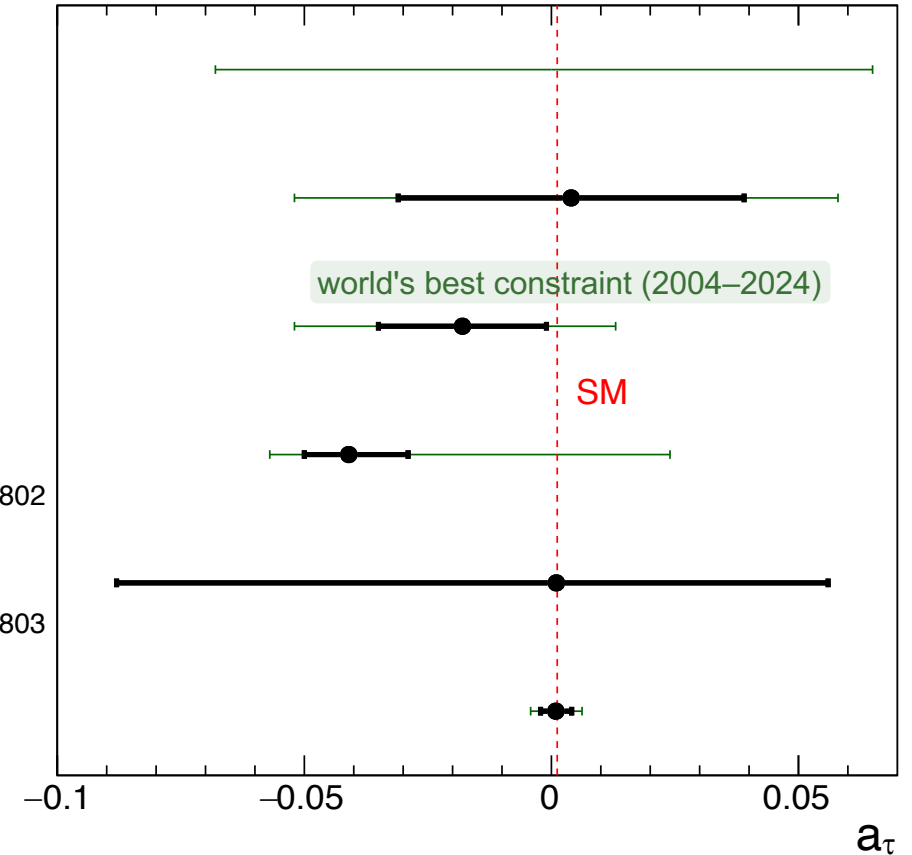
$\gamma\gamma \rightarrow \tau\tau$  ( $\gamma$  from Pb)  
PRL 131 (2023) 151802

### CMS

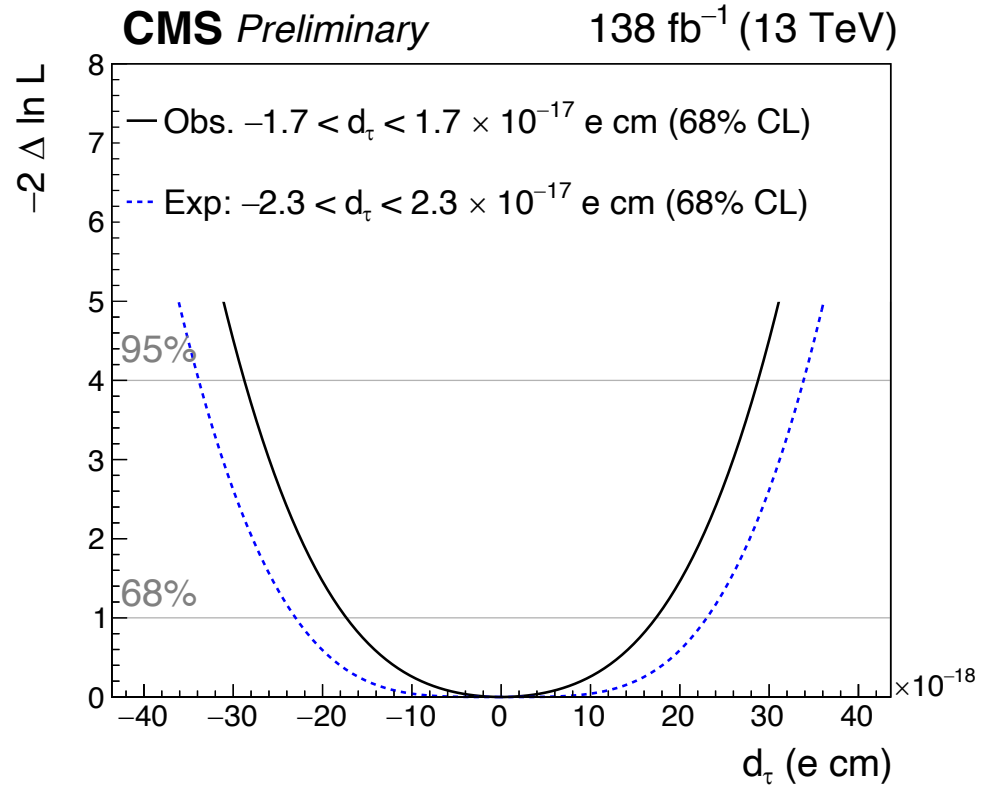
$\gamma\gamma \rightarrow \tau\tau$  ( $\gamma$  from Pb)  
PRL 131 (2023) 151803

### CMS

$\gamma\gamma \rightarrow \tau\tau$  ( $\gamma$  from p)  
This result



# Constraints on $d_\tau$



## OPAL

$ee \rightarrow Z \rightarrow \tau\tau\gamma$   
 PLB 431 (1998) 188

## L3

$ee \rightarrow \tau\tau\gamma$   
 PLB 434 (1998) 169

## ARGUS

$ee \rightarrow \gamma^* \rightarrow \tau\tau$   
 PLB 485 (2000) 37

## Belle

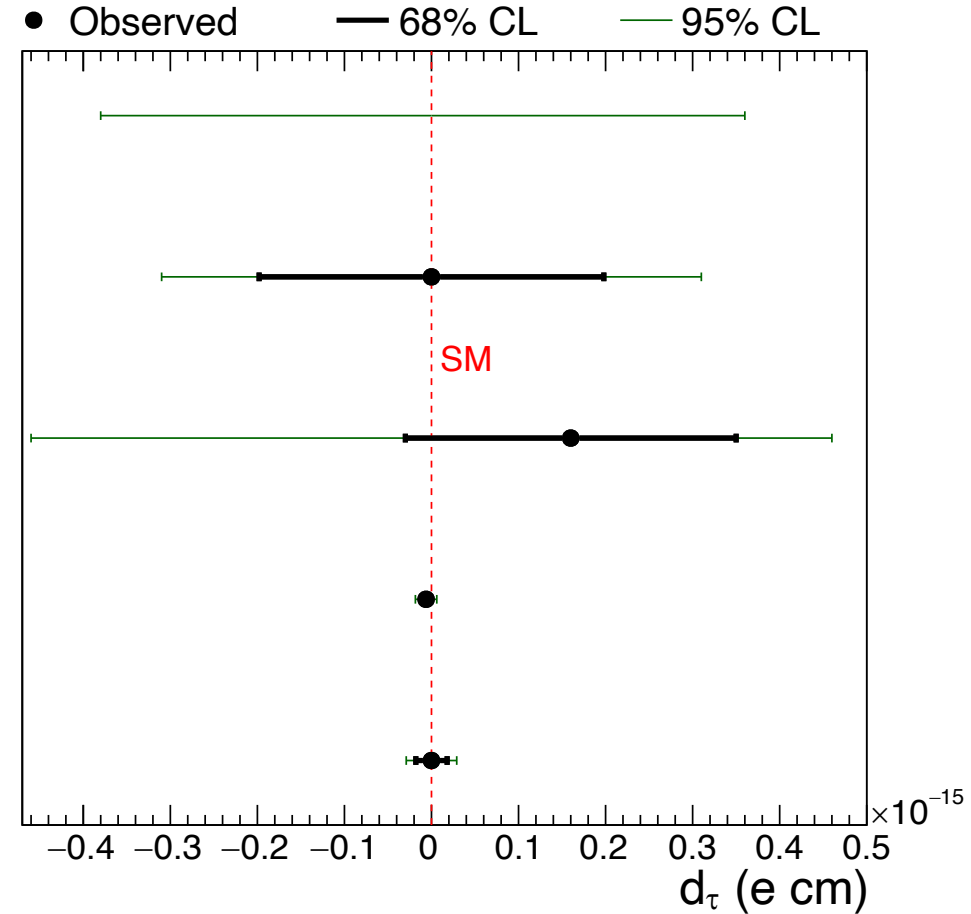
$ee \rightarrow \gamma^* \rightarrow \tau\tau$   
 JHEP 04 (2022) 110

## CMS

$\gamma\gamma \rightarrow \tau\tau$  ( $\gamma$  from p)  
 This result

## CMS

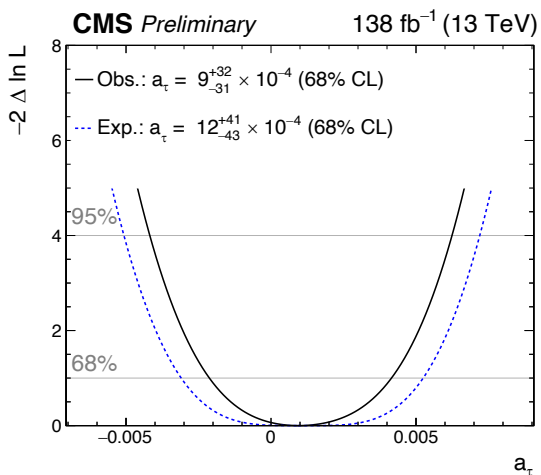
138 fb<sup>-1</sup> (13 TeV)



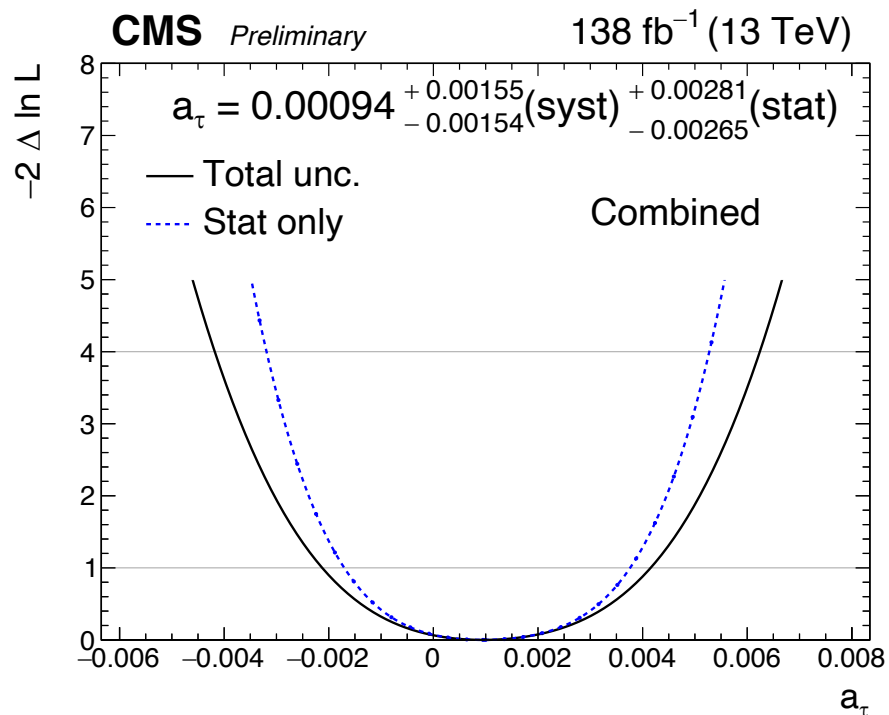
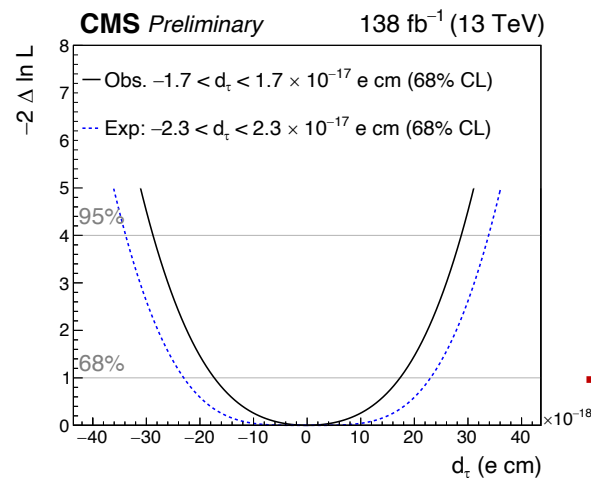
- SM:  $d_\tau \sim 10^{-37}$  ecm (due to CPV in CKM)
- Belle:  $-1.85 < d_\tau < 0.61 \times 10^{-17}$  ecm (95%)
- our result:  $-1.70 < d_\tau < 1.70 \times 10^{-17}$  ecm (68%)

approaching Belle !

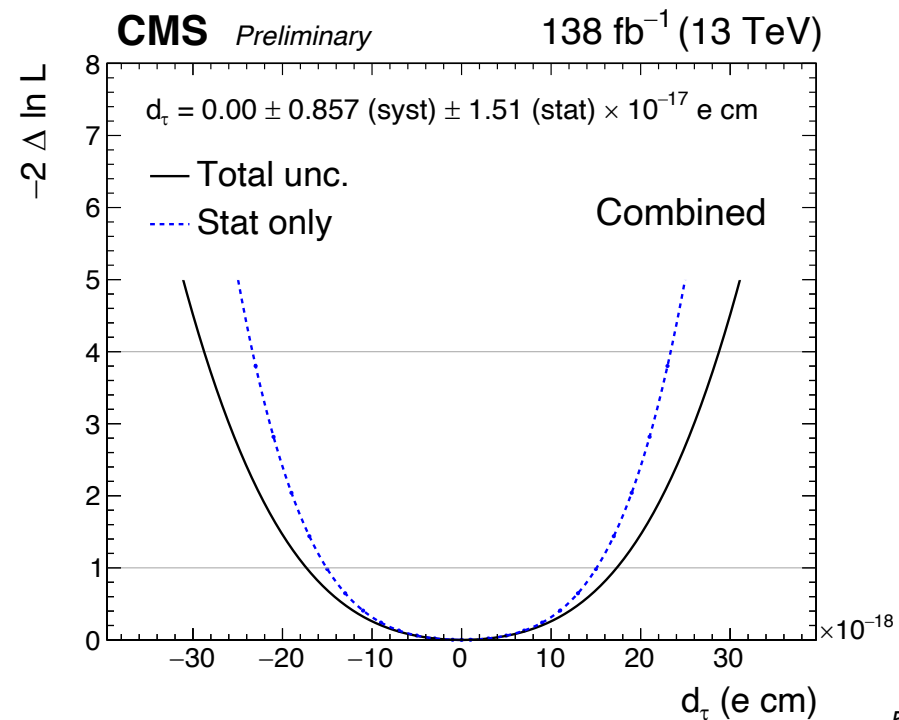
# NLL breakdown by stat. & syst.



measurements mostly statistically limited !



breakdowns of likelihood profiles into **stat.** & **syst.** components



# Constraints on Wilson coefficients

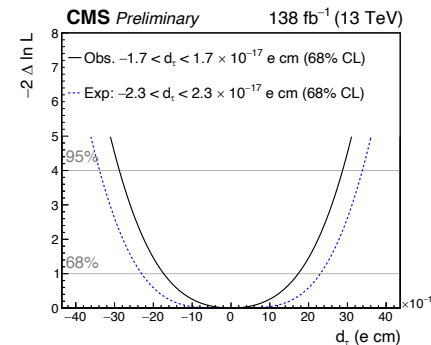
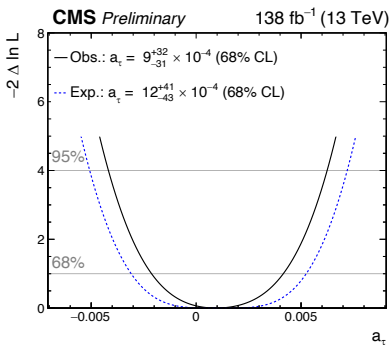
$$a_\tau = a_\tau^{\text{SM}} + \delta a_\tau = \frac{g-2}{2}$$

$$d_\tau = d_\tau^{\text{SM}} + \delta d_\tau$$

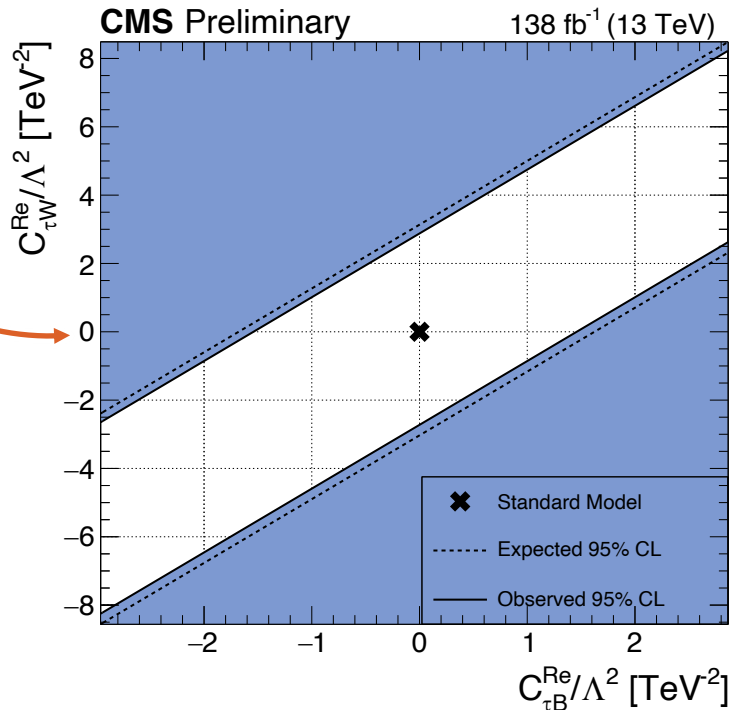
recast results to make exclusion of  $C_{\tau B}/\Lambda^2$  vs.  $C_{\tau W}/\Lambda^2$ :

$$\delta a_\tau = \frac{2m_\tau \sqrt{2}v}{e \Lambda^2} \text{Re}[\cos \theta_W C_{\tau B} - \sin \theta_W C_{\tau W}]$$

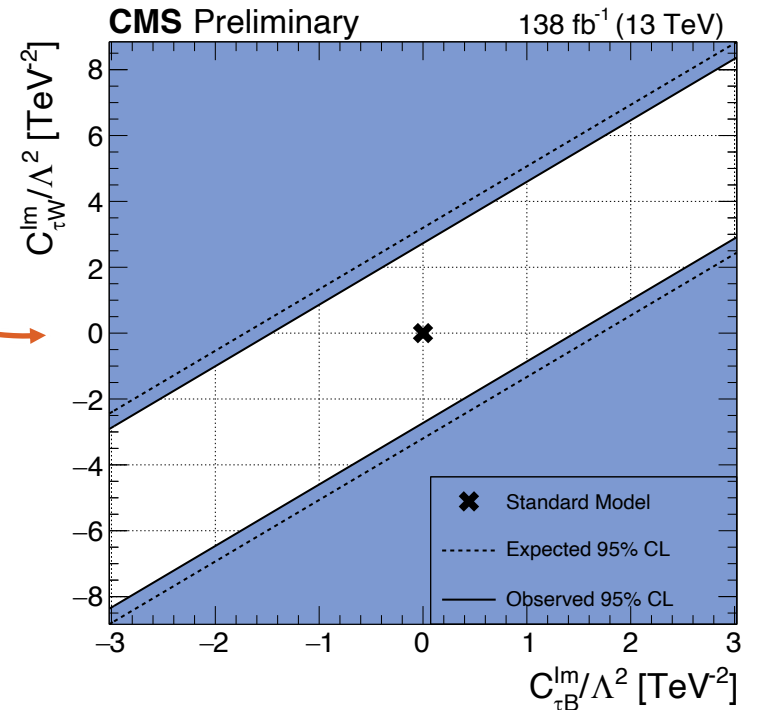
$$\delta d_\tau = \frac{\sqrt{2}v}{\Lambda^2} \text{Im}[\cos \theta_W C_{\tau B} - \sin \theta_W C_{\tau W}]$$



real part:

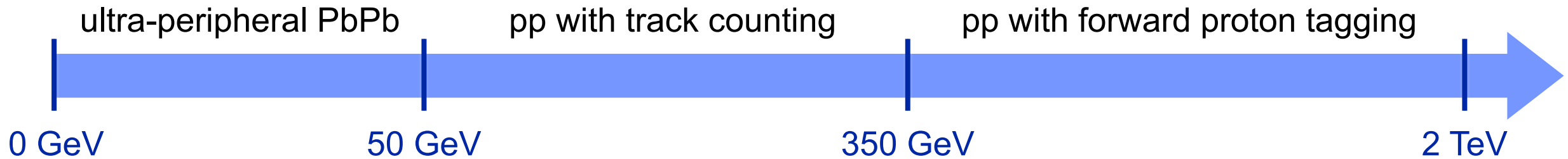
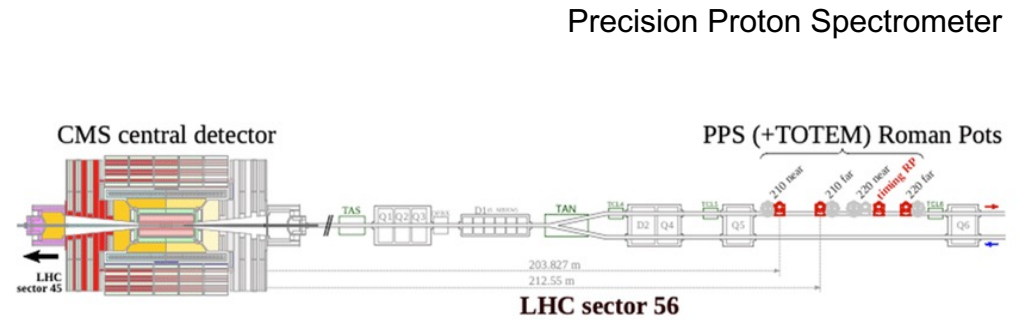
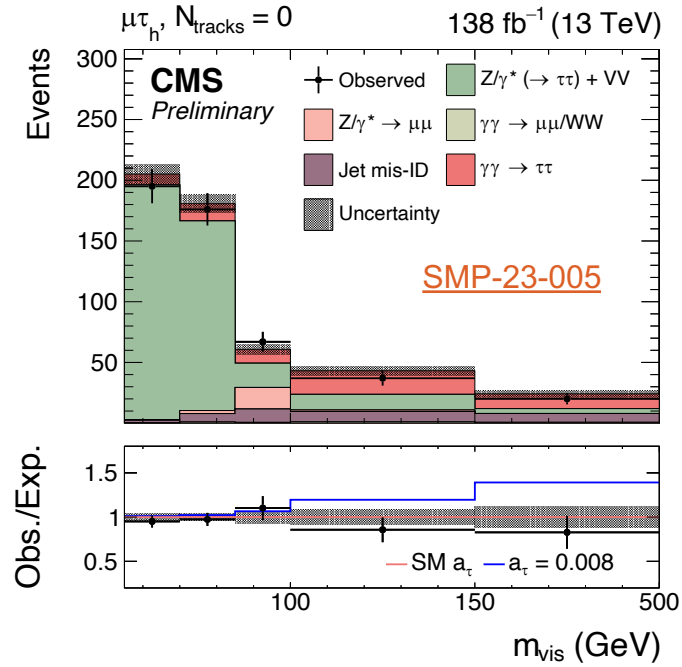
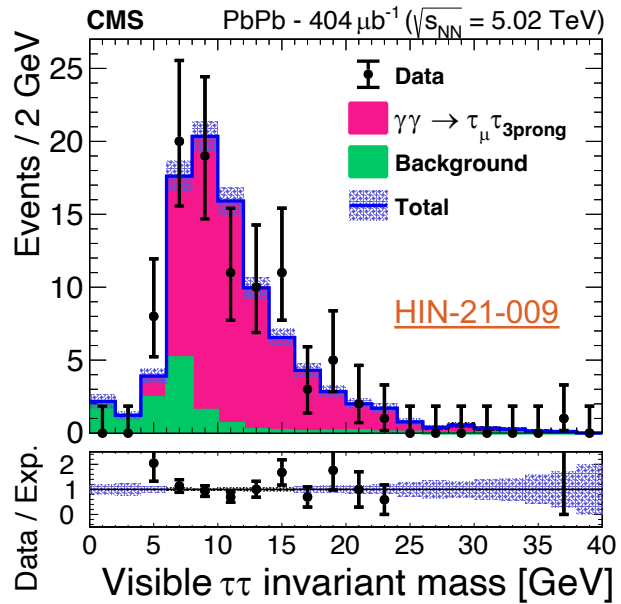


imaginary part:





# Bigger picture



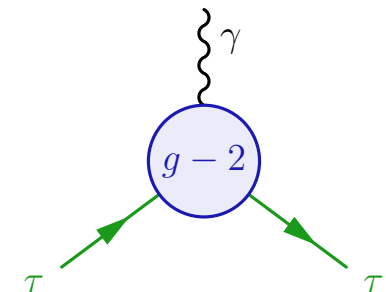
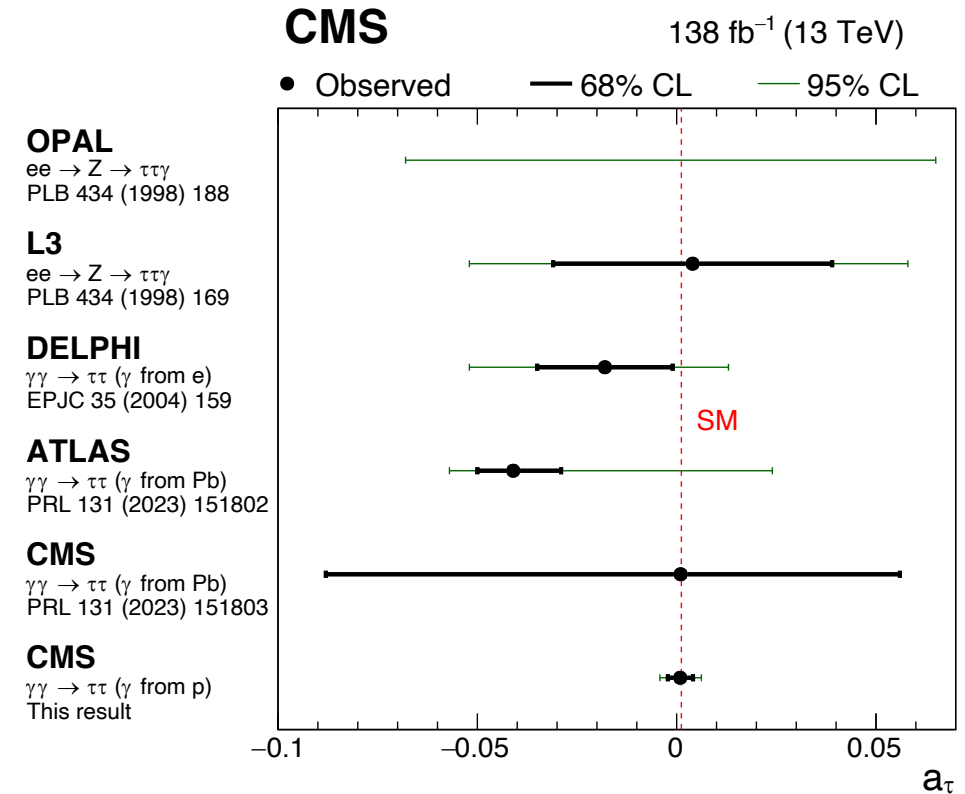
# **SUMMARY**

# Summary

- measuring the electromagnetic momenta the electron and muon has a long & interesting history
  - $(g - 2)_e$  @ 0.13 ppt in Penning traps
  - $(g - 2)_\mu$  @ 0.20 ppm in cyclotrons
- $(g - 2)_\tau$  has strong potential to search new physics
- new preliminary result in **pp** by CMS ([SMP-23-005](#)) puts strong constraints on  $a_\tau$  &  $d_\tau$ 
  - using exclusivity cuts on **acoplanarity** &  $N_{\text{tracks}}$
  - from shape and yield in  $m_{\tau\tau} > 50$  GeV
  - full Run-2 UL data analyzed in 4  $\tau\tau$  final states
- first-time observation of  $\gamma\gamma \rightarrow \tau\tau$  process in pp ( $5.3\sigma$ ) and constraints on
  - $a_\tau$ : > 5x better than LEP
  - $d_\tau$ : same order as Belle

$$a_\tau = 0.0009 +0.0032 -0.0031$$

$$g_\tau = 2.0018 +0.0064 -0.0062 \text{ (0.3\%)}$$



# References

## Theory & phenomenology

- gammaUPC (2022) [arXiv:2207.03012](#)
- Beresford, Liu (2020) [arXiv:1908.05180](#)
- Dynal et al. (2020) [arXiv:2002.05503](#)
- Haisch et al. (2023) [arXiv:2307.14133](#)
- Beresford et al (2024) [arXiv:2403.06336](#)

## Experiment

- $a_e$  Penning Trap (2023) [arXiv:2209.13084](#)
- $a_\mu$  FNAL (2023) [arXiv:2308.06230](#)
- $a_\tau$  DELPHI (2004) [arXiv:hep-ex/0406010](#)
- $d_\tau$  Belle (2022) [arXiv:2108.11543](#)
- $\gamma\gamma \rightarrow WW$  ATLAS (2021) [arXiv:2010.04019](#)
- $\gamma\gamma \rightarrow ee$  ATLAS (2023) [arXiv:2207.12781](#)
- $\gamma\gamma \rightarrow tt$  CMS (2023) [arXiv:23w10.11231](#)

$(g-2)_\tau$  with UPC PbPb ( $m_{\tau\tau} < 50$  GeV):

- $a_\tau$  CMS (2022) [HIN-21-009](#)
- $a_\tau$  ATLAS (2022) [STDM-2019-19](#)

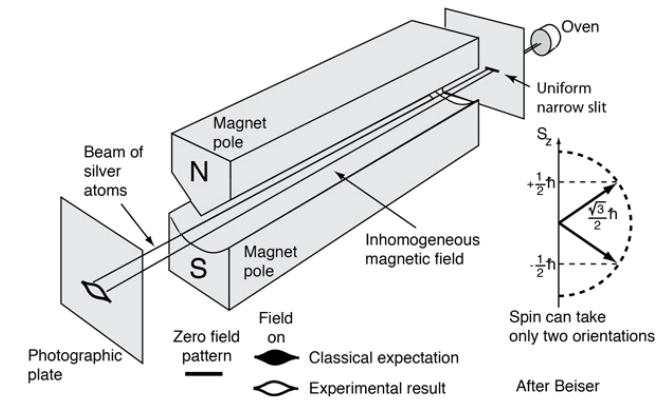
$(g-2)_\tau$  with pp ( $50 < m_{\tau\tau} < 500$  GeV):

- $a_\tau$  CMS (2024) [PAS-SMP-23-005](#)
  - talks: [LHC seminar](#), [Moriond](#)
  - press: [CMS](#), [CERN](#), [Courier](#)

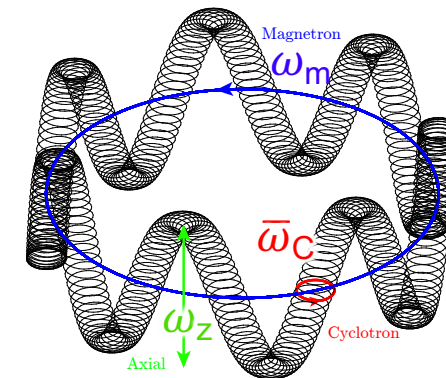
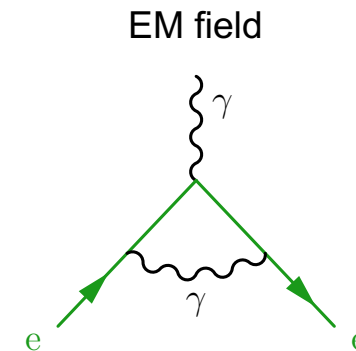
**BACK UP**

# Quick history: Electron spin & g – 2

- **1922**: Stern & Gerlach discover Ag atoms in B field separate discretely
- **1925**: Uhlenbeck & Goudsmit introduce electron spin to explain spectroscopy (Zeeman effect)
- **1927**: Phipps & Taylor confirm electron spin in SG experiment with H atoms

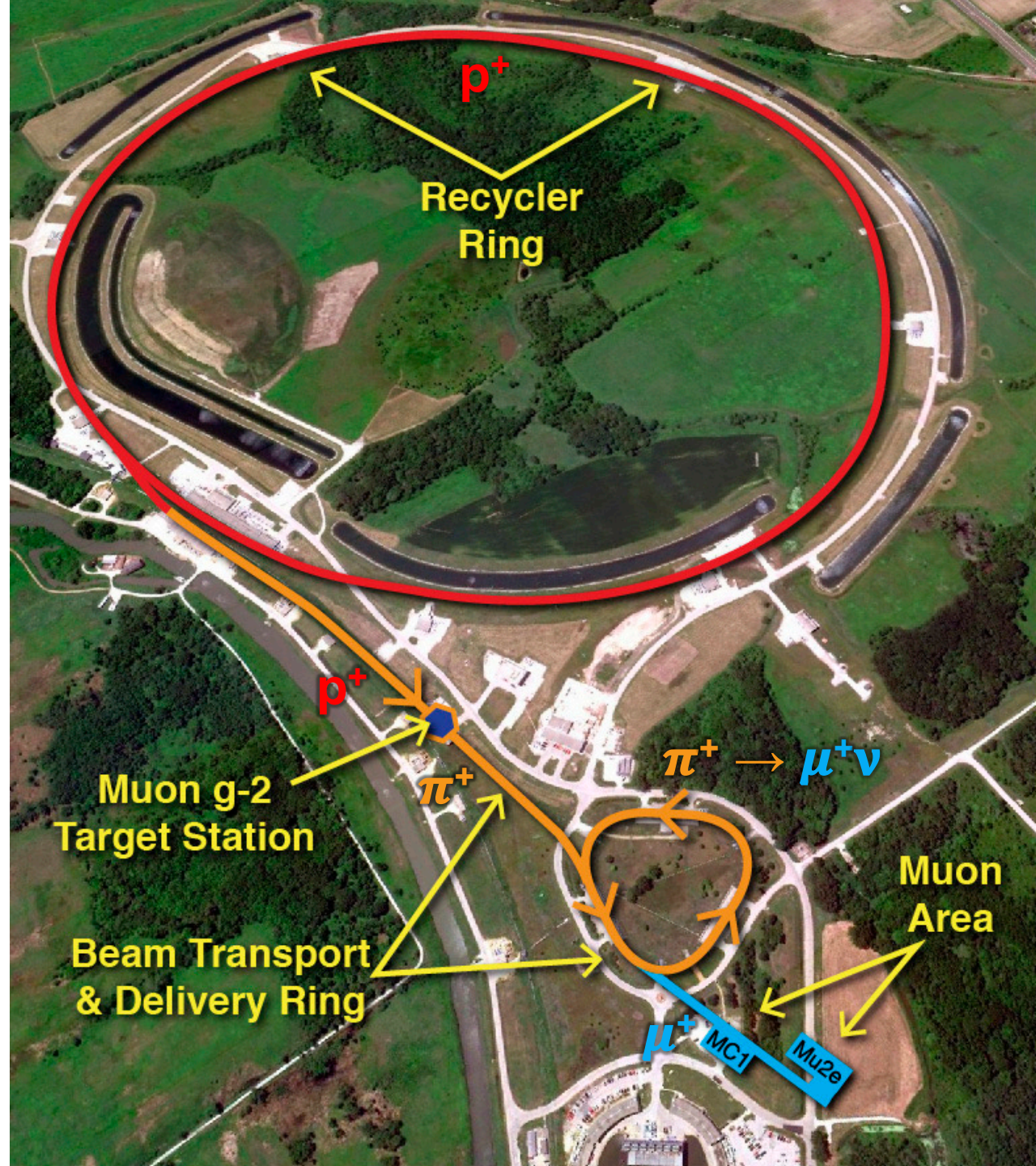


- **1927**: Dirac equation predicts  $g = 2$
- **1947–1951**: Kusch & Foley measure  $g > 2$  with Ga atoms:  
 $(g - 2)/2 = 0.001\,19(5) \sim 4\%$
- **1948**: Schwinger computes  
 $(g - 2)/2 \approx 0.001\,161 = \alpha/2\pi$
- **1969**: Gräff et. al. with Penning trap  
 $(g - 2)/2 = 0.001\,159\,66(30) \sim 300 \text{ ppm}$
- **1987**: Dehmelt et. al. improve  
 $(g - 2)/2 = 0.001\,159\,652\,188\,4(43) \sim 4 \text{ ppt}$
- **2006–2008**: Gabrielse et. al. improve  
 $(g - 2)/2 = 0.001\,159\,652\,180\,73(28) \sim 0.2 \text{ ppt}$





# Fermilab Muon campus

- Recycler provides bunches of  $10^{12}$  **protons** @ 8 GeV
- nickel-iron target: produce  $\pi^+$  @  $\sim 3.11$  GeV
- purify in delivery ring and let decay to **polarized  $\mu^+$  beam**

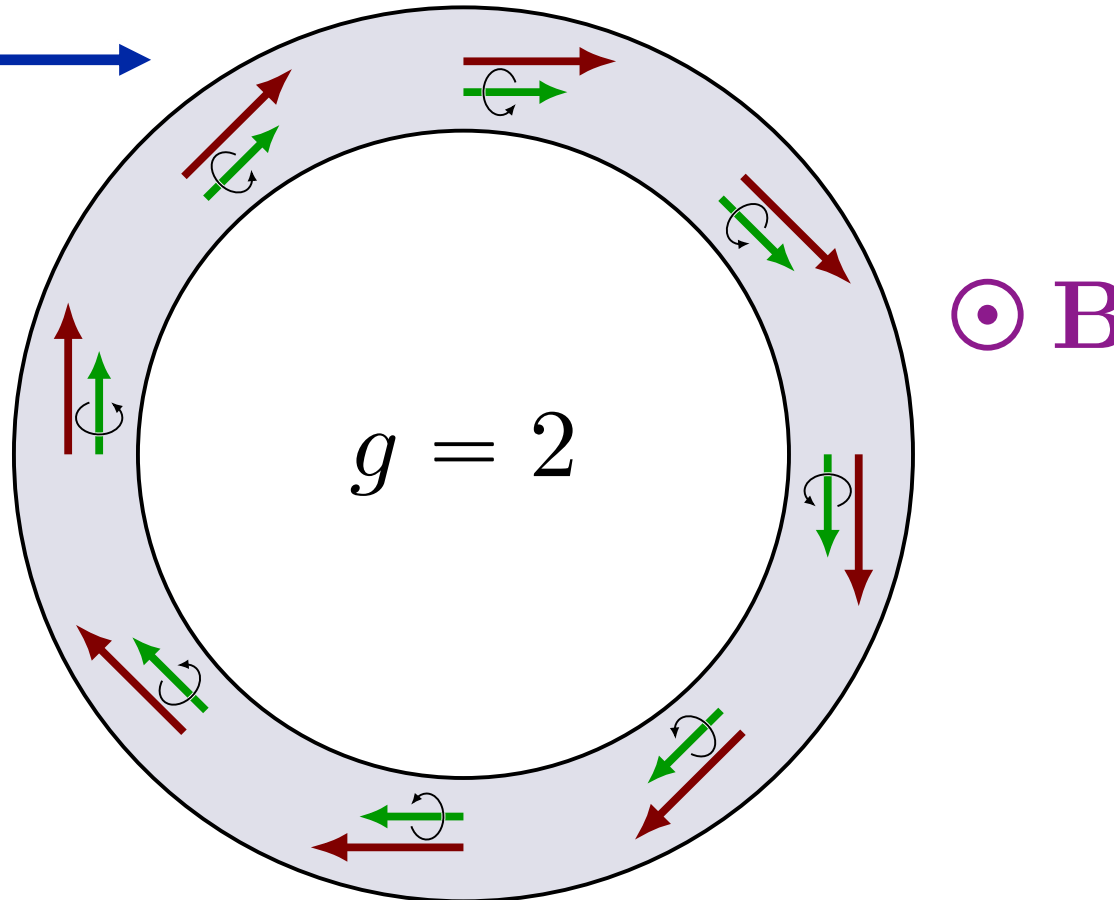


# Muon g – 2 main idea

spin   
 momentum 

polarized  $\mu^+$  beam 



$$\begin{aligned}\omega_a &= \omega_S - \omega_C \\ &= \frac{g - 2}{2} \frac{e}{m_\mu} B \\ &= 0\end{aligned}$$



$g = 2 \Rightarrow$  Larmor precession  $\omega_S \approx 6.7$  MHz = cyclotron oscillation  $\omega_C \approx 6.7$  MHz

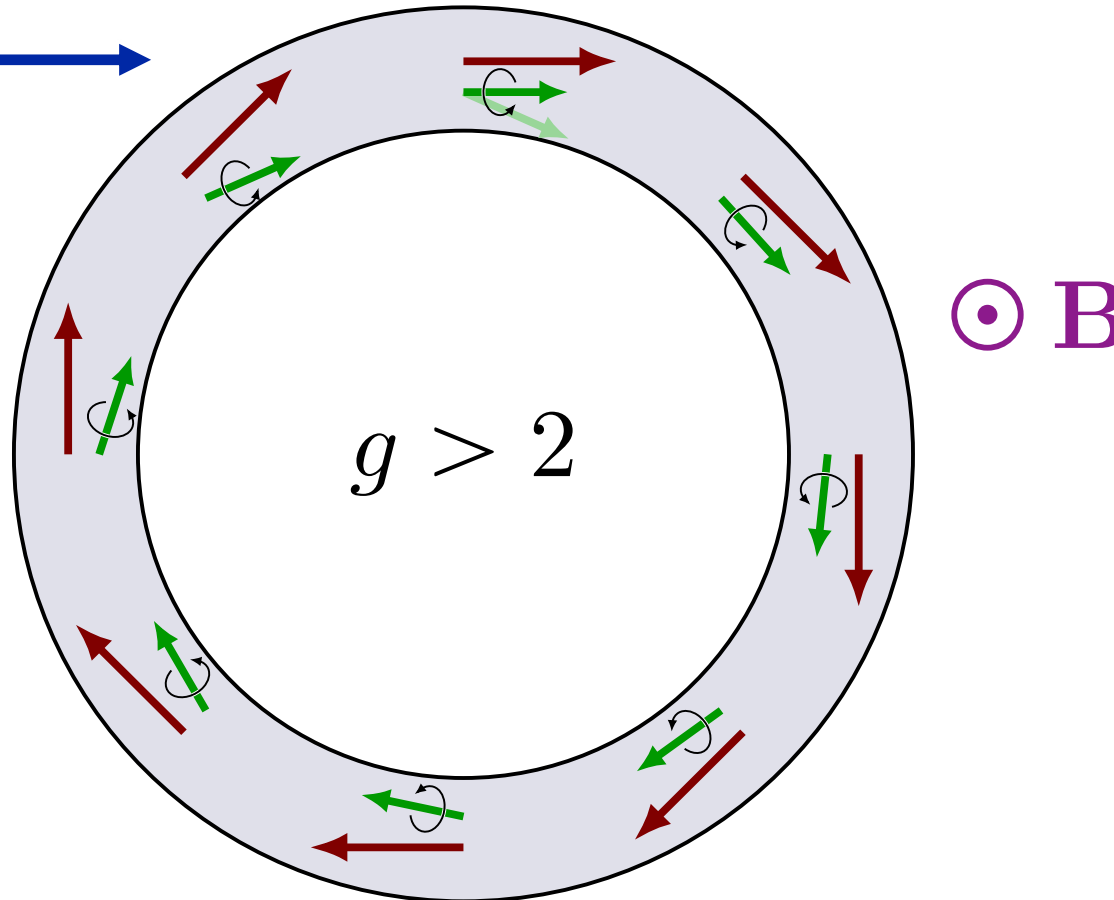
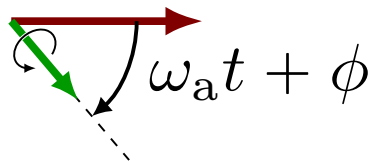


# Muon g – 2 main idea

spin   
momentum 

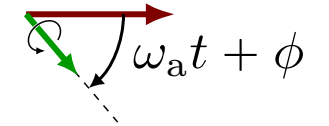
polarized  $\mu^+$  beam 

$$\begin{aligned}\omega_a &= \omega_S - \omega_C \\ &= \frac{g - 2}{2} \frac{e}{m_\mu} B \\ &\sim 230 \text{ kHz}\end{aligned}$$



$g > 2 \Rightarrow$  Larmor precession  $\omega_S >$  cyclotron oscillation  $\omega_C$   
 $\sim 6.93 \text{ MHz}$   $\sim 6.7 \text{ MHz}$

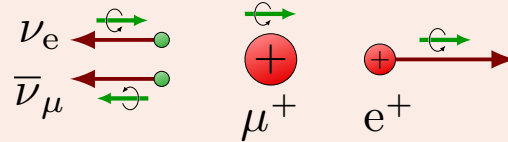
# Positron measurement



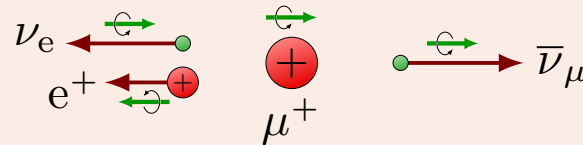
$$N(t) = N_0 e^{-t/\tau} (1 + A(E) \cos(\omega_a t + \phi))$$

rest frame

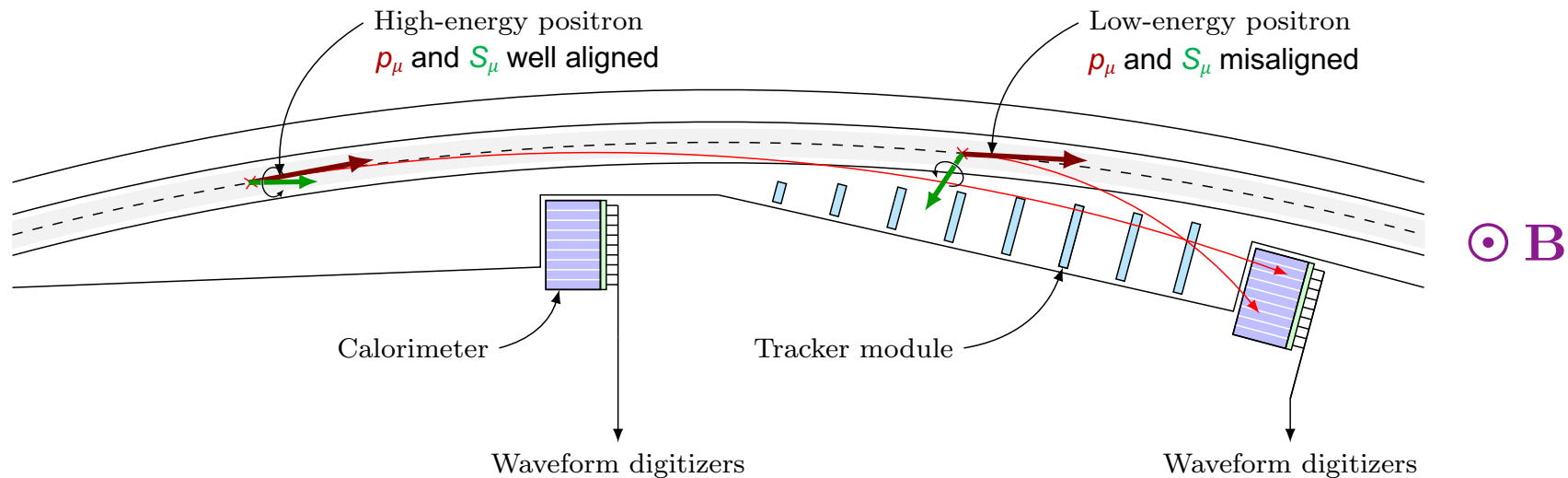
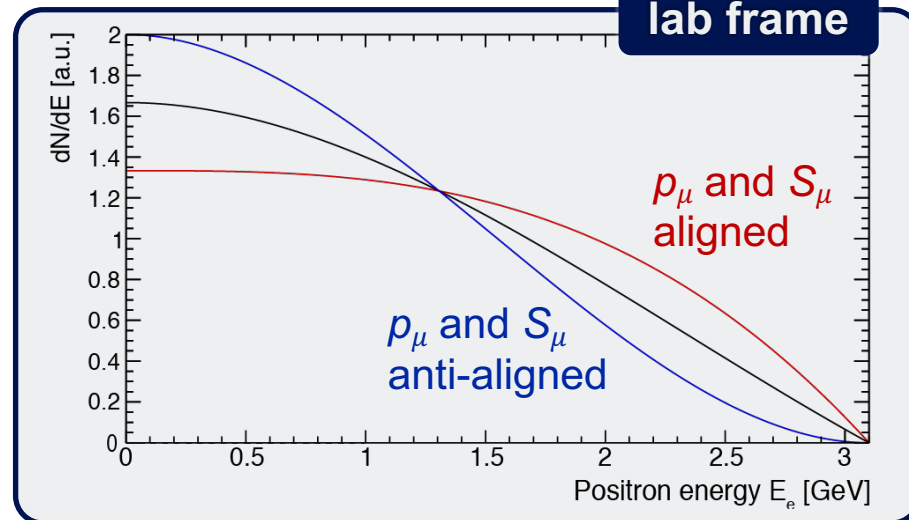
e<sup>+</sup> parallel:  
maximal E<sub>e</sub>



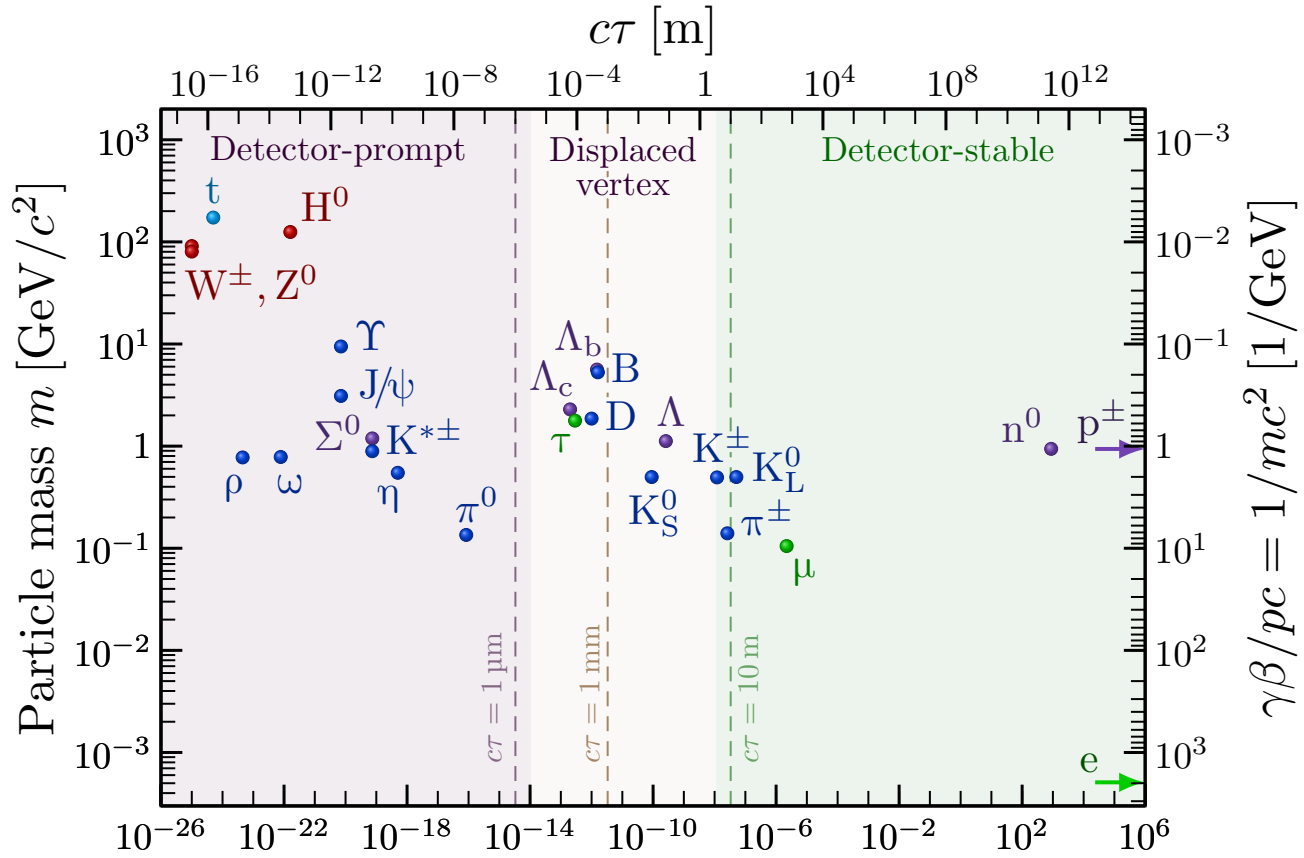
e<sup>+</sup> anti-parallel:  
minimum E<sub>e</sub>



lab frame



# Lepton lifetimes



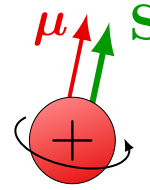
decay length not measurable      Proper lifetime  $\tau$  [s]      particles travel into the detector  
 decay vertex displaced from production vertex

tau lifetime  $\tau = 2.9 \times 10^{-13}$  s  
 $\Rightarrow \gamma c\tau \sim 1$  mm (20 GeV)  
 $\Rightarrow$  secondary vertex

	three generations of matter (fermions)			interactions / forces (bosons)	
	I	II	III		
QUARKS	mass $\approx 2.2$ MeV charge $+2/3$ spin $1/2$ <b>u</b> up	mass $\approx 1.3$ GeV charge $+2/3$ spin $1/2$ <b>c</b> charm	mass $\approx 173$ GeV charge $+2/3$ spin $1/2$ <b>t</b> top	0 0 1 <b>g</b> gluon	mass $\approx 125$ GeV 0 0 0 <b>H</b> Higgs SCALAR BOSONS
	mass $\approx 4.7$ MeV charge $-1/3$ spin $1/2$ <b>d</b> down	mass $\approx 96$ MeV charge $-1/3$ spin $1/2$ <b>s</b> strange	mass $\approx 4.2$ GeV charge $-1/3$ spin $1/2$ <b>b</b> bottom	0 0 1 <b><math>\gamma</math></b> photon	
	mass $\approx 0.511$ MeV charge $-1$ spin $1/2$ <b>e</b> electron	mass $\approx 106$ MeV charge $-1$ spin $1/2$ <b><math>\mu</math></b> muon	mass $\approx 1.777$ GeV charge $-1$ spin $1/2$ <b><math>\tau</math></b> tau	mass $\approx 80.4$ GeV charge $\pm 1$ spin 1 <b>W</b> W boson	
LEPTONS	mass $< 1.0$ eV charge 0 spin $1/2$ <b><math>\nu_e</math></b> electron neutrino	mass $< 0.17$ eV charge 0 spin $1/2$ <b><math>\nu_\mu</math></b> muon neutrino	mass $< 18.2$ MeV charge 0 spin $1/2$ <b><math>\nu_\tau</math></b> tau neutrino	mass $\approx 91.2$ GeV charge 0 spin 1 <b>Z</b> Z boson	GAUGE BOSONS VECTOR BOSONS

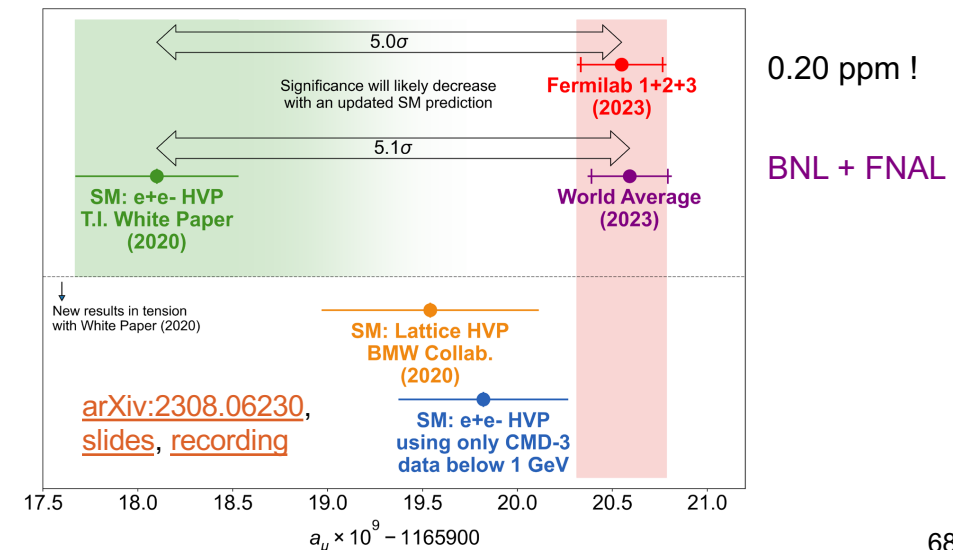
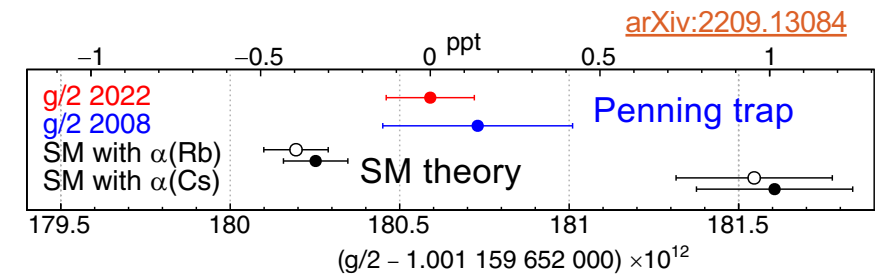
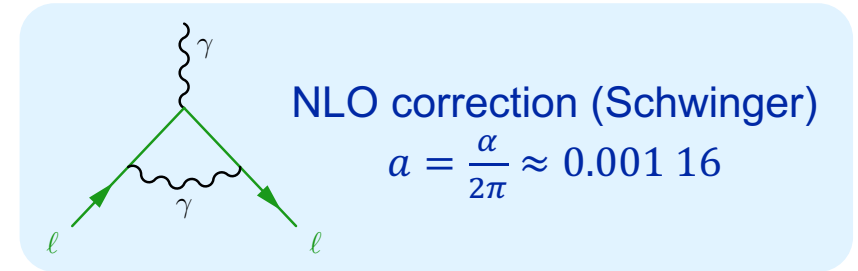
Note: time dilation: decay length  $L = \gamma\beta c\tau$ , with  $\gamma\beta = p/mc$

# What is $g - 2$ ?

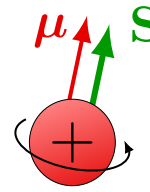


$$\mu = g \frac{e}{2m} \mathbf{S} \longrightarrow \begin{cases} g = 1: \text{classical} \\ g = 2: \text{Dirac} \\ g \approx 2.002: \text{QED} \end{cases}$$

- particles with spin  $\mathbf{S}$  have a **magnetic moment  $\mu$**
- obtains quantum corrections with gyromagnetic factor / “g-factor”  $g \approx 2.002\ 32$  for spin  $\frac{1}{2}$   
 $\Rightarrow$  **anomalous magnetic moment  $a = \frac{g-2}{2} \approx 0.001\ 16$**
- measurements of  $(g - 2)_e$  in Penning traps are the “most precise in physics”
- measurements of  $(g - 2)_\mu$  in storage rings are in longstanding tension with theoretical computations

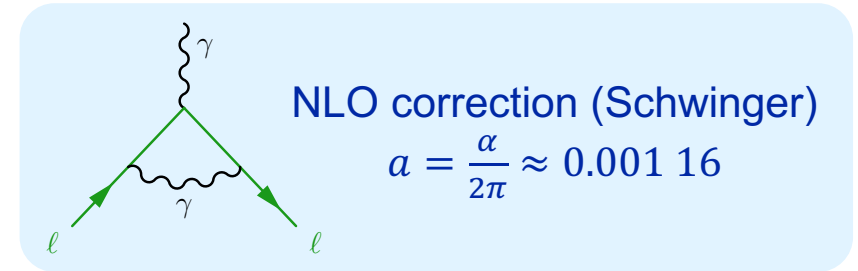


# What is $g - 2$ ?

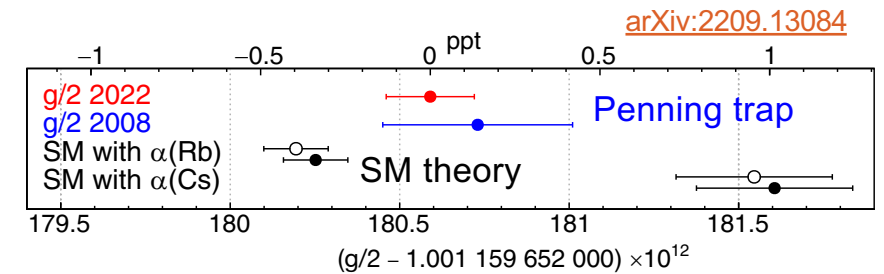


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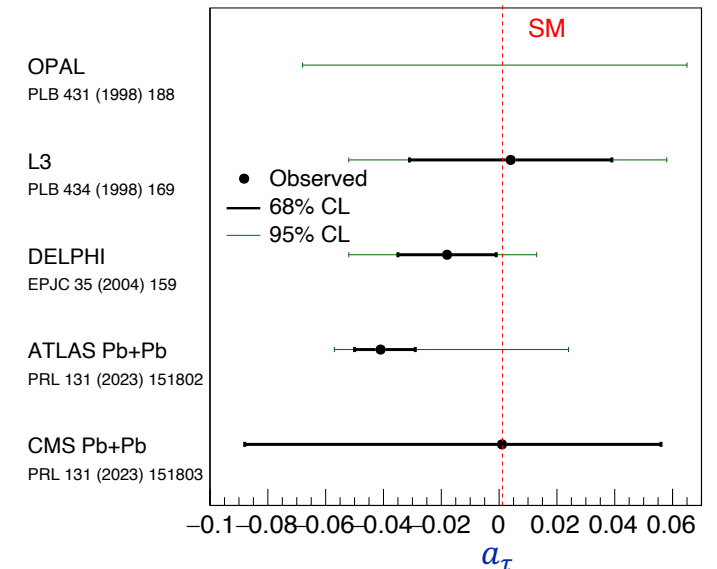
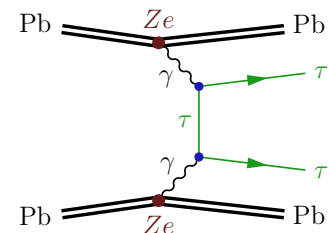


- measurements of  $(g - 2)_e$  in Penning traps are the "most precise in physics"
- measurements of  $(g - 2)_\mu$  in storage rings are in longstanding tension with theoretical computations
- constraints on  $(g - 2)_\tau$  in  $e^+e^-$  or PbPb collisions:
  - DELPHI@LEP:  $-0.052 < a_\tau < 0.013$  (95% CL)
  - CMS HIN:  $-0.088 < a_\tau < 0.056$  (68% CL)
  - ATLAS HIN:  $-0.057 < a_\tau < 0.024$  (95% CL)



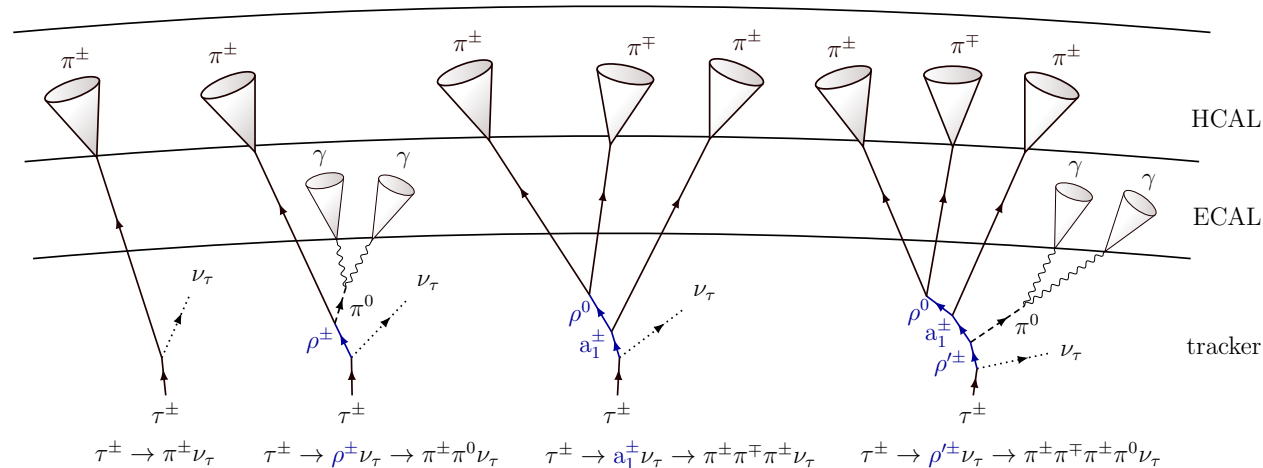
- many **BSMs** predict **enhancement for  $\tau$  lepton**  
 e.g. Yukawa-like coupling:  $\frac{m_\tau^2}{m_\mu^2} \approx 280$   
 $\Rightarrow$  probe for NP ?

world's best since 2004



# Object reconstruction & selection

- **e**: MVA WP80,  $p_T > 15$  GeV,  $|\eta| < 2.5$
- **$\mu$** : medium ID, medium isolation,  $p_T > 10$  GeV,  $|\eta| < 2.4$
- **$\tau_h$** : HPS,  $p_T > 30$  GeV,  $|\eta| < 2.3$ , DeepTau v2p1 (VSe, VSmu, VSjet), four decay modes:



- **MET**: PFMET reconstruction
- **tracks**: charged PFCandidate collection in miniAOD,  $p_T > 0.5$  GeV,  $|\eta| < 2.5$

# Inclusive pre-selections

	$e\mu$	$e\tau_h$	$\mu\tau_h$	$\tau_h\tau_h$	$\mu\mu$
$p_T^e$ (GeV)	$> 15/24$	$> 25 - 33$	—	—	—
$ \eta^e $	$< 2.5$	$< 2.1 - 2.5$	—	—	—
$p_T^\mu$ (GeV)	$> 24/15$	—	$> 21 - 29$	—	$> 26 - 29/10$
$ \eta^\mu $	$< 2.4$	—	$< 2.1 - 2.4$	—	—
$p_T^{\tau_h}$ (GeV)	—	$> 30 - 35$	$> 30 - 32$	$> 40$	—
$ \eta^{\tau_h} $	—	$< 2.1 - 2.3$	$< 2.1 - 2.3$	$< 2.1$	—
$m_{\mu\mu}$ (GeV)	—	—	—	—	$> 50$
OS	yes	yes	yes	yes	yes
$ d_z(\ell, \ell') $ (cm)	$< 0.1$	$< 0.1$	$< 0.1$	$< 0.1$	$< 0.1$
$\Delta R(\ell, \ell')$	$> 0.5$	$> 0.5$	$> 0.5$	$> 0.5$	$> 0.5$
$m_T(e/\mu, \vec{p}_T^{\text{miss}})$ (GeV)	—	$< 75$	$< 75$	—	—

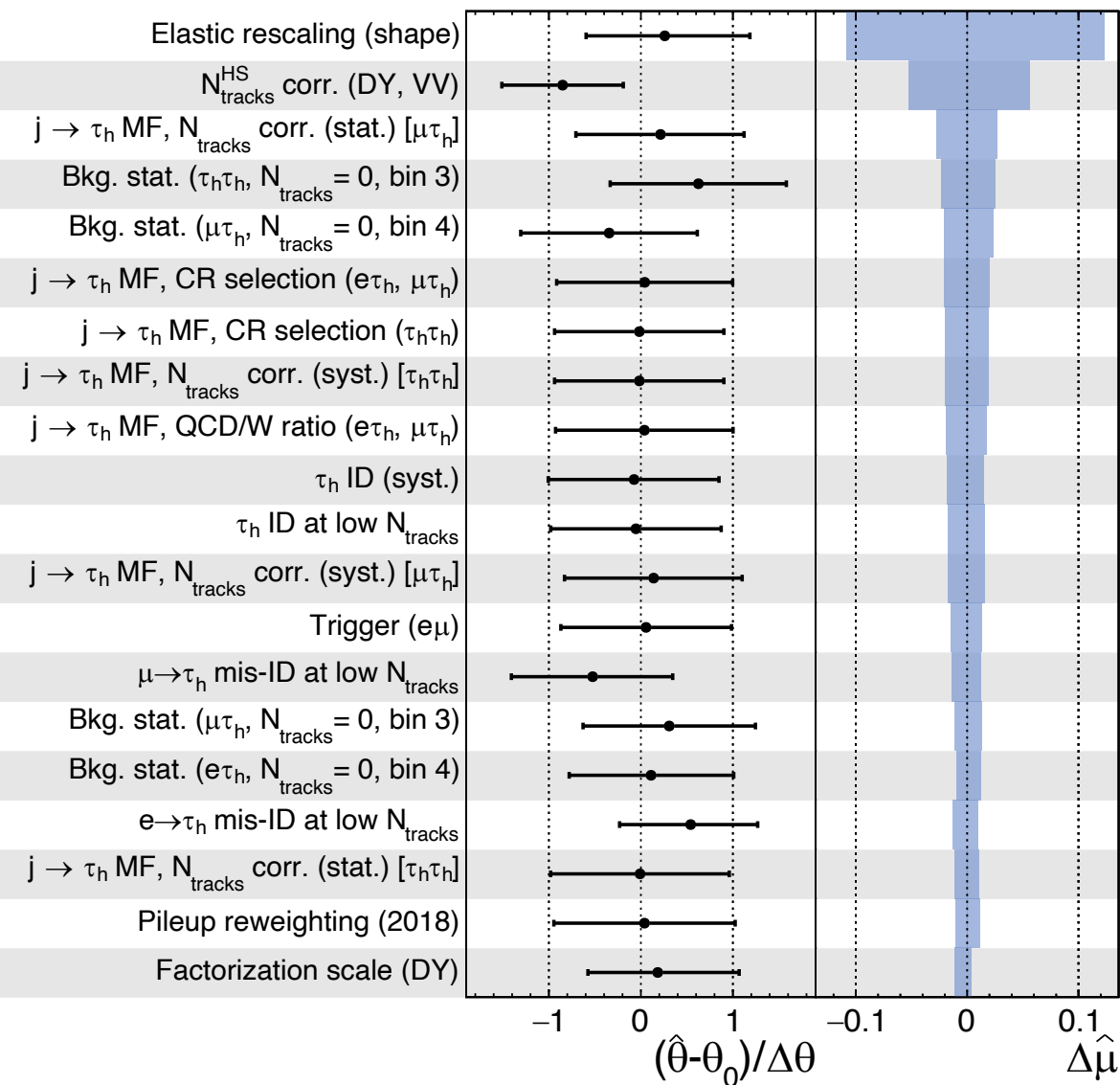
# Systematics

CMS Preliminary

138 fb<sup>-1</sup> (13 TeV)

→ Fit  ±1 σ impact

$\hat{\mu} = 0.75^{+0.20}_{-0.18}$



Uncertainty	Process	Magnitude
Luminosity	All simulations	1.6%
DY cross section	DY	2%
Inclusive diboson cross section	WW, WZ, ZZ	5%
e ID, iso, trigger	All simulations	up to 2%
e ID low- $N_{\text{tracks}}$ correction	All simulations	1%
$\mu$ ID, iso, trigger	All simulations	< 2%
$\tau_h$ ID	All simulations	1–5%
$\tau_h$ trigger	All simulations	up to 5%
$e \rightarrow \tau_h$ mis-ID	$Z/\gamma^* \rightarrow ee$ and $\gamma\gamma \rightarrow ee$	< 10%
$\mu \rightarrow \tau_h$ ID	$Z/\gamma^* \rightarrow \mu\mu$ and $\gamma\gamma \rightarrow \mu\mu$	< 10%
$\tau_h$ energy scale	All simulations	< 1.2%
$e \rightarrow \tau_h$ energy scale	$Z/\gamma^* \rightarrow ee$ and $\gamma\gamma \rightarrow ee$	< 5%
$\mu \rightarrow \tau_h$ energy scale	$Z/\gamma^* \rightarrow \mu\mu$ and $\gamma\gamma \rightarrow \mu\mu$	< 1%
$\tau_h$ ID low- $N_{\text{tracks}}$ correction	All simulations	2.1%
e ID low- $N_{\text{tracks}}$ correction	All simulations	2.0%
$e \rightarrow \tau_h$ ID low- $N_{\text{tracks}}$ correction	$Z/\gamma^* \rightarrow ee$ and $\gamma\gamma \rightarrow ee$	22%
$\mu \rightarrow \tau_h$ ID low- $N_{\text{tracks}}$ correction	$Z/\gamma^* \rightarrow \mu\mu$ and $\gamma\gamma \rightarrow \mu\mu$	15%
$N_{\text{tracks}}^{\text{PU}}$ reweighting	All simulations	2%
$N_{\text{tracks}}^{\text{HS}}$ reweighting	DY and inclusive VV	1.5–6.5%
Acoplanarity correction	DY	5%
DY extrapolation from $N_{\text{tracks}} < 10$	DY simulation	1.4–2.0%
$\mu_R, \mu_f$	DY simulation	Shape
PDF	DY simulation	Shape
jet $\rightarrow \tau_h$ MF, extrapolation with $p_T^{\tau_h}$	jet $\rightarrow \tau_h$ mis-ID bkg.	< 50%
jet $\rightarrow \tau_h$ MF, $N_{\text{tracks}}$ extrapolation (stat.)	jet $\rightarrow \tau_h$ mis-ID bkg.	6–18%
jet $\rightarrow \tau_h$ MF, inversion of CR selection	jet $\rightarrow \tau_h$ mis-ID bkg.	< 10%
jet $\rightarrow \tau_h$ MF, $x^{\text{QCD}}$ fraction	jet $\rightarrow \tau_h$ mis-ID bkg.	9%
jet $\rightarrow \tau_h$ MF, $N_{\text{tracks}}$ extrapolation (syst.)	jet $\rightarrow \tau_h$ mis-ID bkg.	< 10%
jet $\rightarrow e/\mu$ OS-to-SS (stat.)	jet $\rightarrow e/\mu$ mis-ID bkg.	< 20%
jet $\rightarrow e/\mu$ OS-to-SS (syst.)	jet $\rightarrow e/\mu$ mis-ID bkg.	10%
jet $\rightarrow e/\mu$ OS-to-SS $N_{\text{tracks}}$ extrapolation	jet $\rightarrow e/\mu$ mis-ID bkg.	8%
Elastic rescaling (stat.)	$\gamma\gamma \rightarrow \tau\tau/\mu\mu/ee, WW$	1.3–3.7%
Elastic rescaling (syst., shape)	$\gamma\gamma \rightarrow \tau\tau/\mu\mu/ee, WW$	Mass-dependent
Limited statistics	All processes	Bin-dependent
Pileup reweighting	All simulations	Event-dependent



# Signal simulation

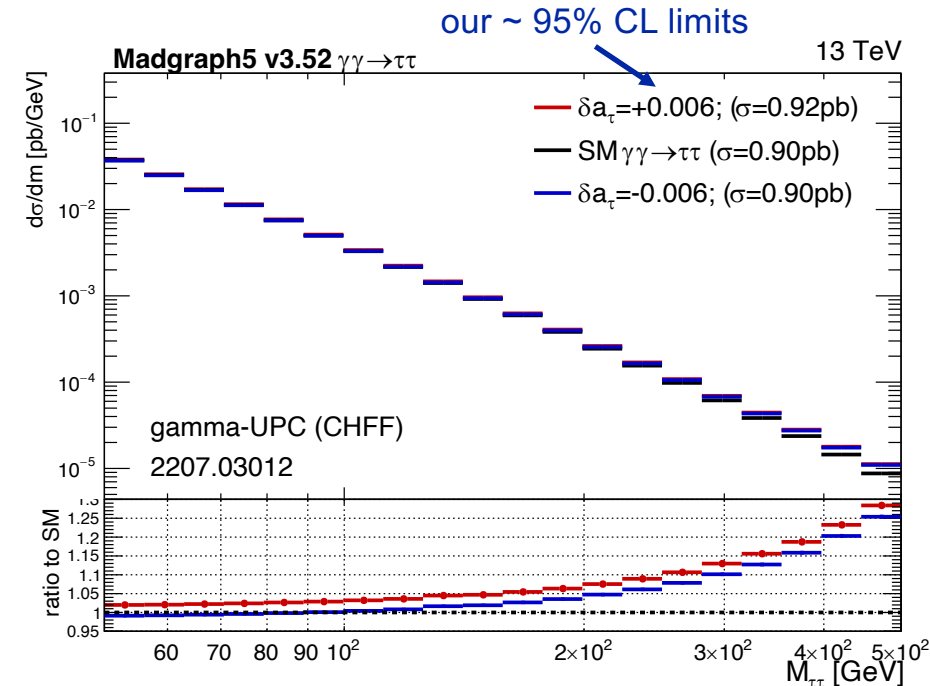
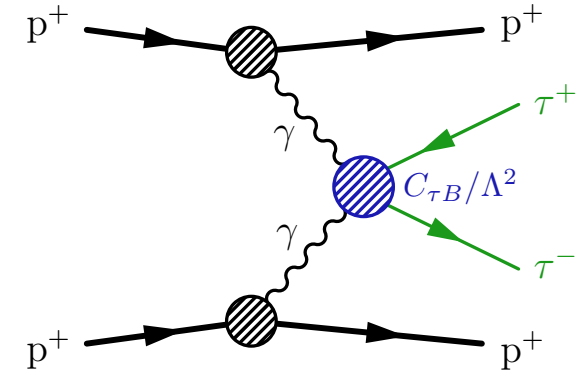
- **elastic-elastic events** are generated using gammaUPC generator with  $k_t$  smearing ([arXiv:2207.03012](https://arxiv.org/abs/2207.03012))
- charged form factors to correct the photon flux are used (recommended by gammaUPC authors)
- $a_\tau$  &  $d_\tau$  interpretation using the **EFT approach** with the [SMEFTsim](https://github.com/STSC/SM-EFTsim) package, simplifying with  $C_{\tau W} = 0$ :

$$\delta a_\tau \propto \frac{\text{Re}[C_{\tau B}]}{\Lambda^2}, \quad \delta d_\tau \propto \frac{\text{Im}[C_{\tau B}]}{\Lambda^2}$$

- scan  $a_\tau$  &  $d_\tau$  values through matrix element reweighting in two *independent* 1D grids of 100 points for  $C_{\tau B}$ :

$$\text{Re}[C_{\tau B}] \in [-40, 40], \quad \text{Im}[C_{\tau B}] \in [-40, 40]$$

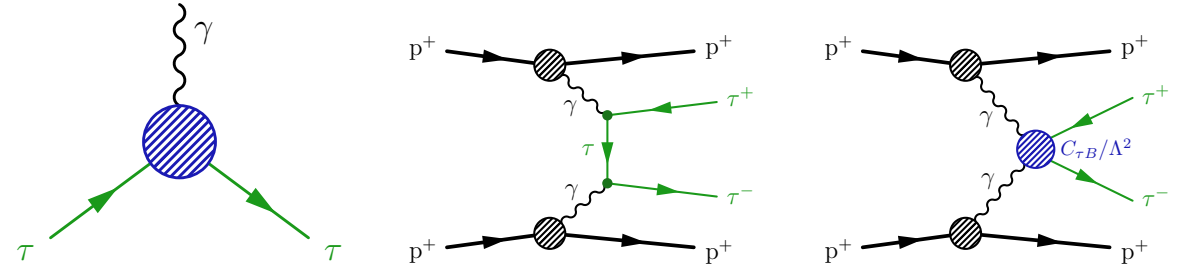
- varying  $a_\tau$  or  $d_\tau$  changes the cross section and  $m_{\tau\tau}$  distribution
- hadronized using Pythia 8.24, switching off multi-parton interaction
- result *independent* of choice of  $\Lambda$ , because  $C_{\tau B}$  and  $C_{\tau W}$  scale with  $\Lambda^2$ , but we fix  $\Lambda = 2 \text{ TeV}$  in event generation



# Form factors vs. EFTs

in the **SM Lagrangian** electromagnetic moments arise from:

$$\mathcal{L} \supset \mathcal{L}_{\tau\tau\gamma} = \frac{1}{2} \bar{\tau} \sigma^{\mu\nu} \left( a_\tau \frac{e}{2m_\tau} - i d_\tau \gamma_5 \right) \tau_R F_{\mu\nu}$$



$$\text{spin tensor } \sigma_{\mu\nu} = \frac{i}{2} [\gamma_\mu, \gamma_\nu]$$

- previous analyses by [DELPHI](#) & [ATLAS](#) used **form factors** to parametrize the  $\gamma\tau\tau$  vertex:

$$\Gamma_\mu(q^2) = ie \left[ F_1(q^2) \gamma_\mu + \frac{1}{2m_\tau} (iF_2(q^2) + F_3(q^2) \gamma_5) \sigma_{\mu\nu} q^\nu \right]$$

- $F_1(q^2)$  parametrises the vector part of the electromagnetic current and is identified at zero-momentum transfer ( $q^2 = 0$ ) with the electric charge  $e$ , implying  $F_1(0) = 1$
- the asymptotic values of the form factors ( $q^2 \rightarrow 0$ ) are the electromagnetic moments  $a_\tau$  and  $d_\tau$ :

$$a_\tau = \frac{F_2(0)}{e}$$

$$d_\tau = \frac{F_3(0)}{2m_\tau}$$

- the virtualities of exchanged photons in  $\gamma\gamma \rightarrow \ell\ell$ :
  - PbPb UPC :  $Q_{1,2}^2 \lesssim 0.001 \text{ GeV}^2$
  - pp:  $Q_{1,2}^2 \lesssim 0.08 \text{ GeV}^2$
  - LEP  $e^+e^-$ :  $Q_{1,2}^2 < 1 \text{ GeV}^2$

- we use **SMEFT model** to parametrize deviations  $a_\tau$  and  $d_\tau$  from the SM can be parametrized in terms of a BSM Lagrangian with **dim-6 operators** with **NP scale  $\Lambda$** :

$$\mathcal{L}_{\text{BSM}} = \bar{L}_\tau \sigma^{\mu\nu} \tau_R H \left[ \frac{C_{\tau B}}{\Lambda^2} B_{\mu\nu} + \frac{C_{\tau W}}{\Lambda^2} W_{\mu\nu} \right]$$

- after symmetry breaking:

$$\mathcal{L}_{\text{BSM}} \supset \mathcal{L}_{\tau\tau\gamma}^{\text{BSM}} = \bar{\tau}_L \sigma^{\mu\nu} \tau_R \frac{v}{\sqrt{2}\Lambda^2} [\cos\theta_W C_{\tau B} - \sin\theta_W C_{\tau W}] F_{\mu\nu}$$

- $\gamma\tau\tau$  vertex:

$$\Gamma_\mu(q^2) = ie \left[ \dots + \frac{1}{2m_\tau} \frac{v}{\sqrt{2}\Lambda^2} [\cos\theta_W C_{\tau B} - \sin\theta_W C_{\tau W}] \frac{2m_\tau}{e} (i + \gamma_5) \sigma_{\mu\nu} q^\nu \right]$$

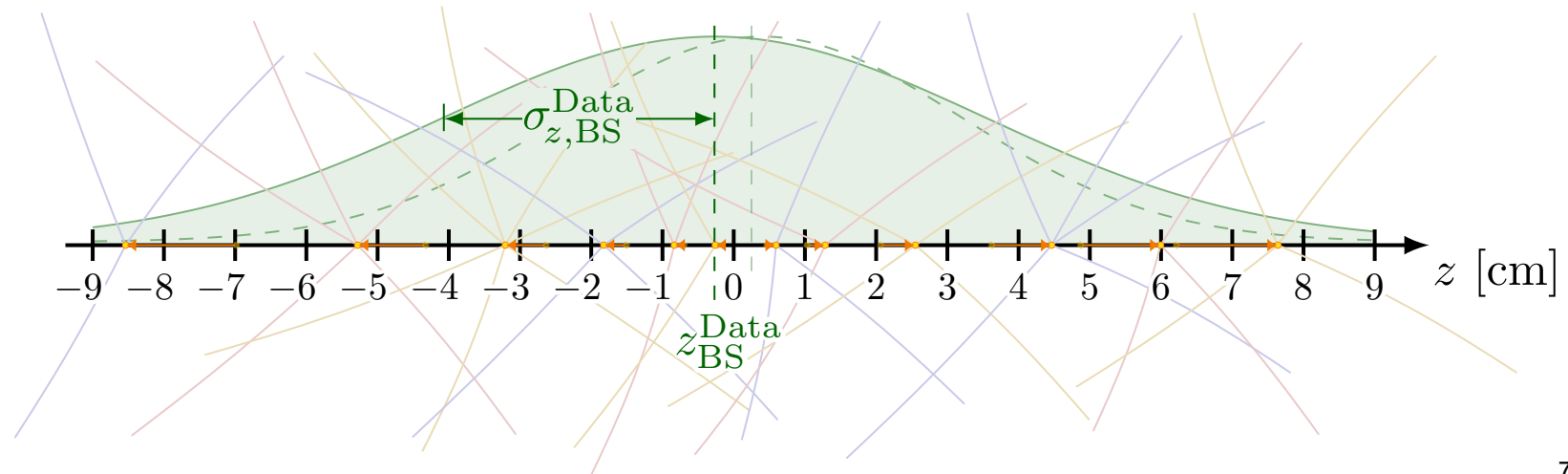
- then  $\delta a_\tau$  &  $\delta d_\tau$  are linearly dependent through the *complex* Wilson coefficients:

$$\delta a_\tau = \frac{2m_\tau \sqrt{2}v}{e \Lambda^2} \text{Re}[\cos\theta_W C_{\tau B} - \sin\theta_W C_{\tau W}]$$

$$\delta d_\tau = \frac{\sqrt{2}v}{\Lambda^2} \text{Im}[\cos\theta_W C_{\tau B} - \sin\theta_W C_{\tau W}]$$

# Beamspot smearing to pileup tracks

- **simulated events** have a *fixed* beamspot  $z$  position and width for a given era
- **in data**, beamspot  $z$  position and width are *run-dependent*
- to each simulated event, randomly assign a **BS position**  $z_{\text{data}}^{\text{BS}}$  & a **BS width**  $\sigma_{\text{data}}^{\text{BS}}$  by sampling the BS distributions in data
- correct  $z$  position of the pileup tracks
  - smear:  $z^{\text{corr}} = z_{\text{MC}}^{\text{BS}} + \frac{\sigma_{\text{MC}}^{\text{BS}}}{\sigma_{\text{data}}^{\text{BS}}} (z - z_{\text{MC}}^{\text{BS}})$
  - shift:  $z^{\text{corr}} = z + (z_{\text{data}}^{\text{BS}} - z_{\text{MC}}^{\text{BS}})$

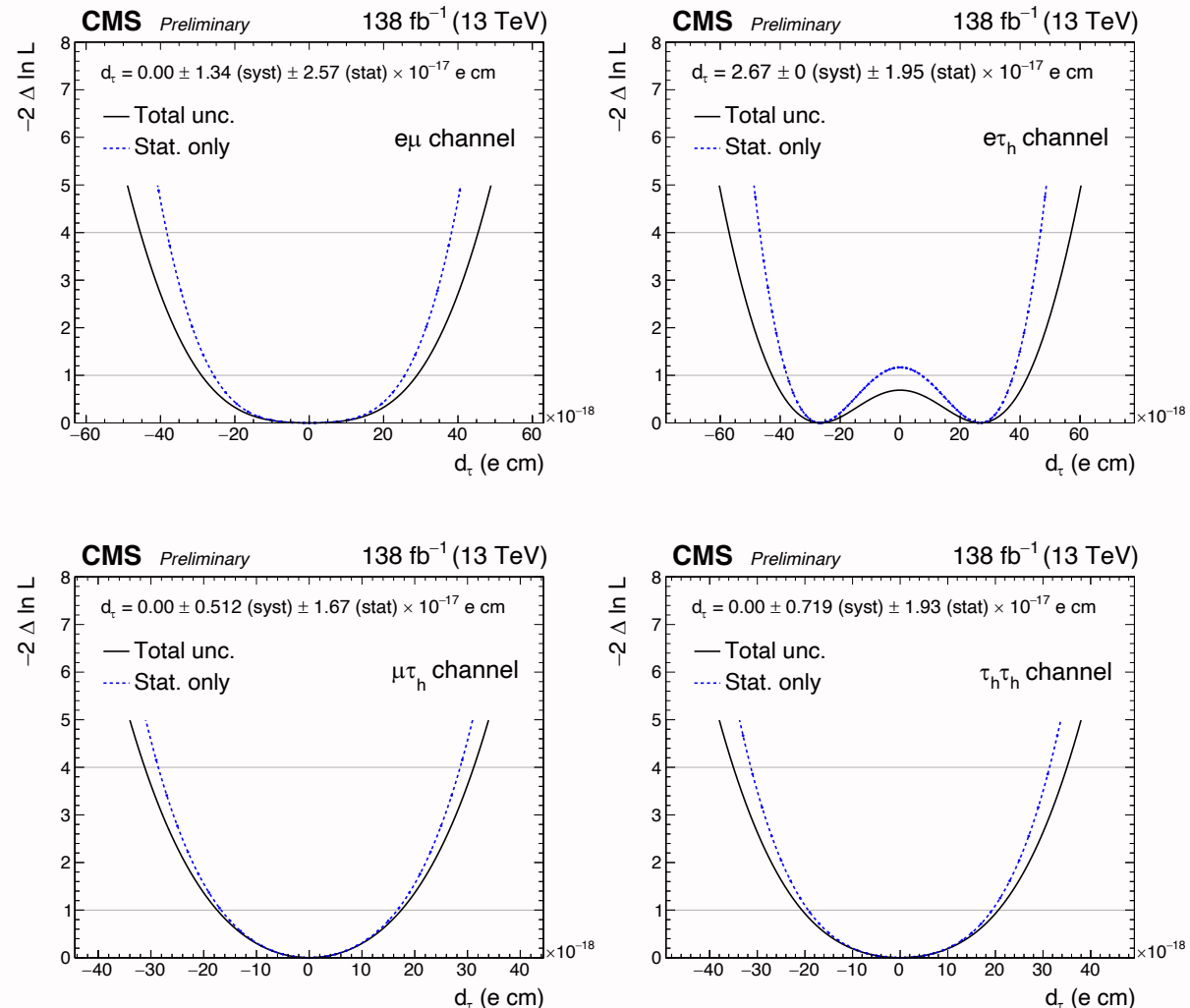
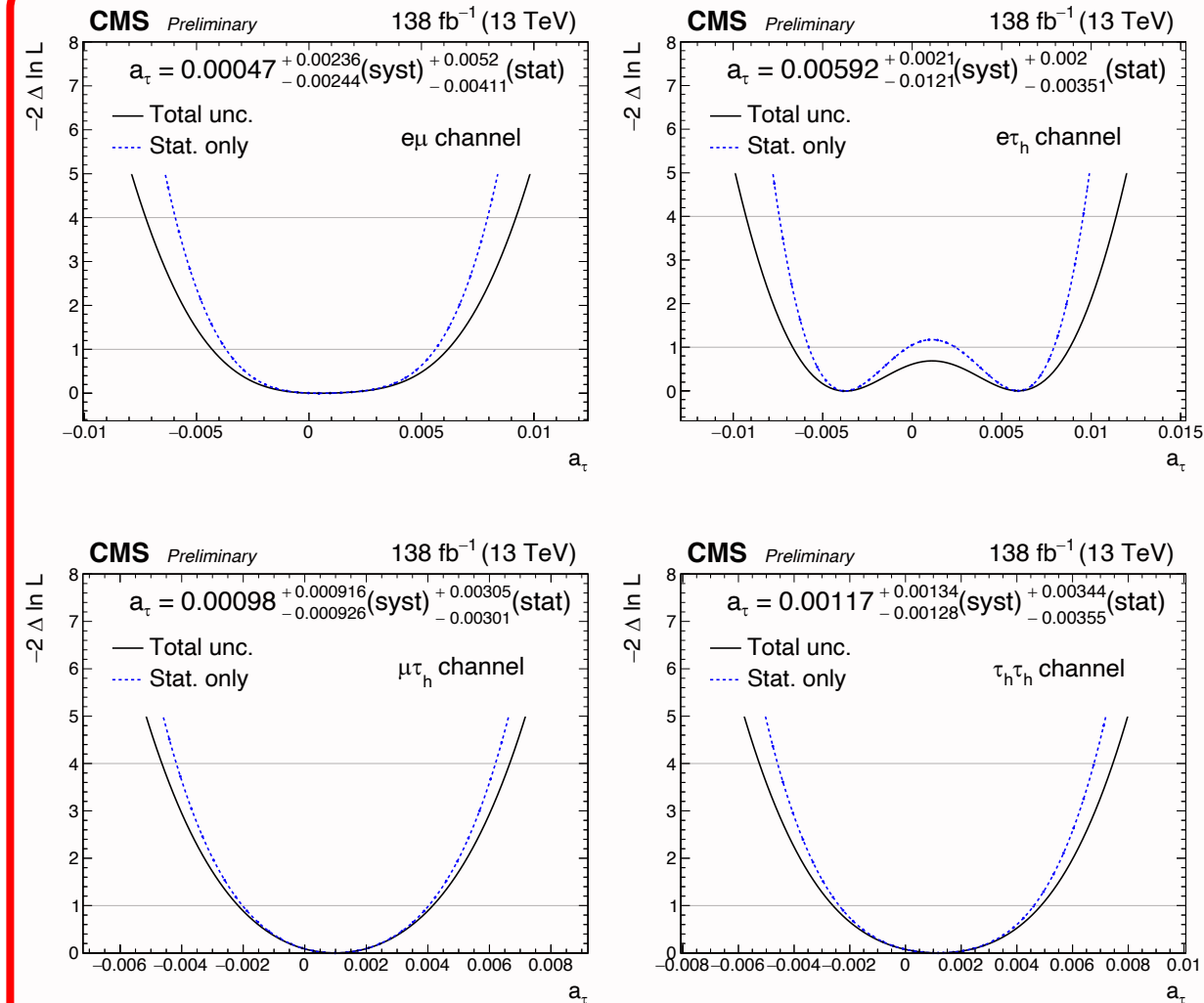


# NLL breakdowns by channel

double minima caused by small excess in  $e\tau_h$  and the fact that BSM deviations go in the same direction

$a_\tau$

$d_\tau$



# Form factors vs. EFTs

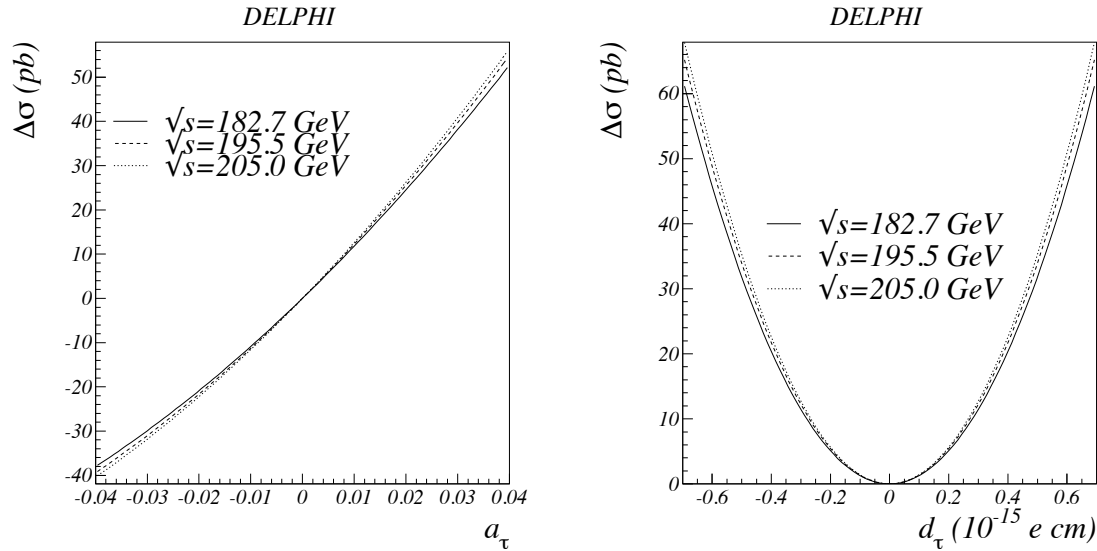


Figure 7: Total cross-section change as a function of anomalous magnetic moment and as a function of electric dipole moment.

DELPHI (2004) [arXiv:hep-ex/0406010](https://arxiv.org/abs/hep-ex/0406010)

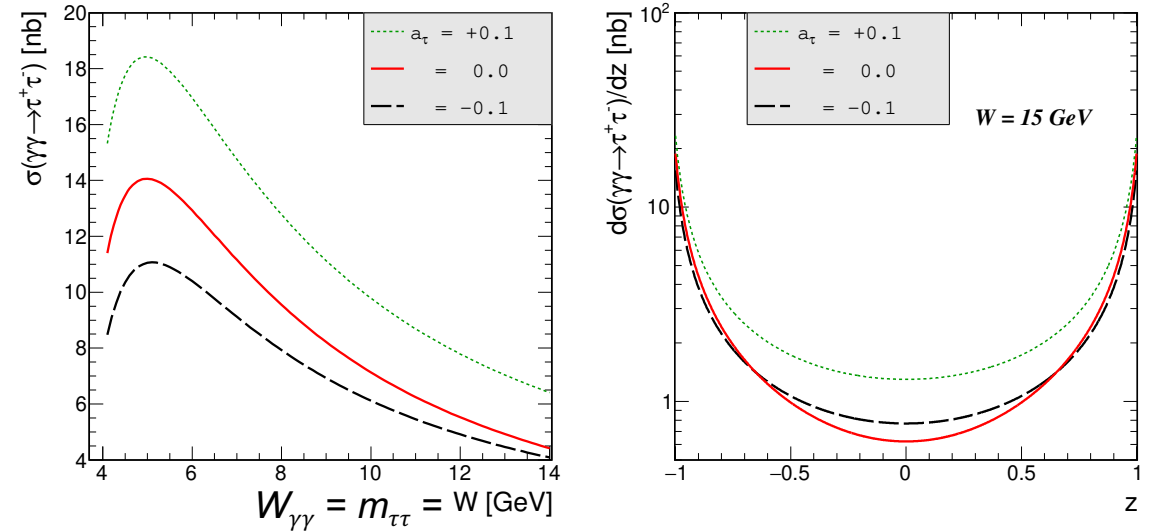
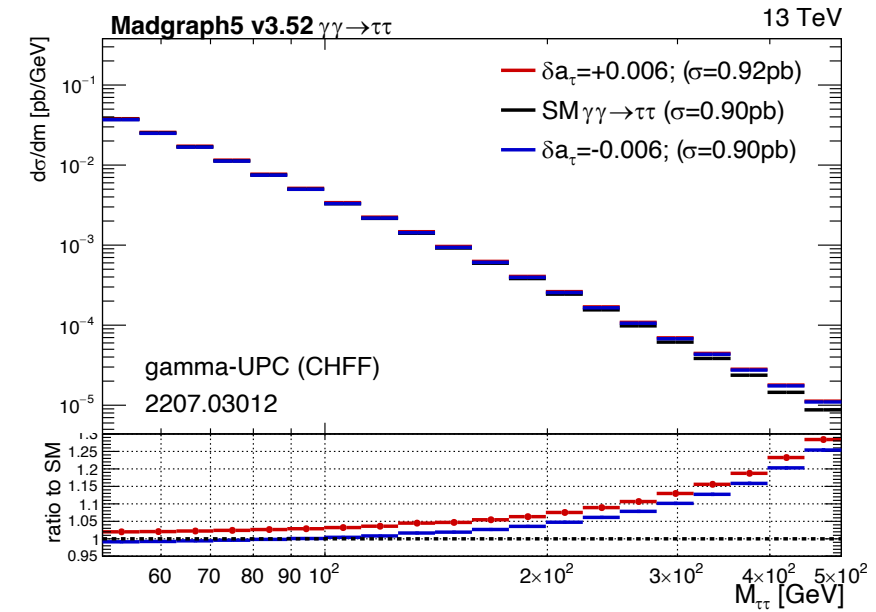


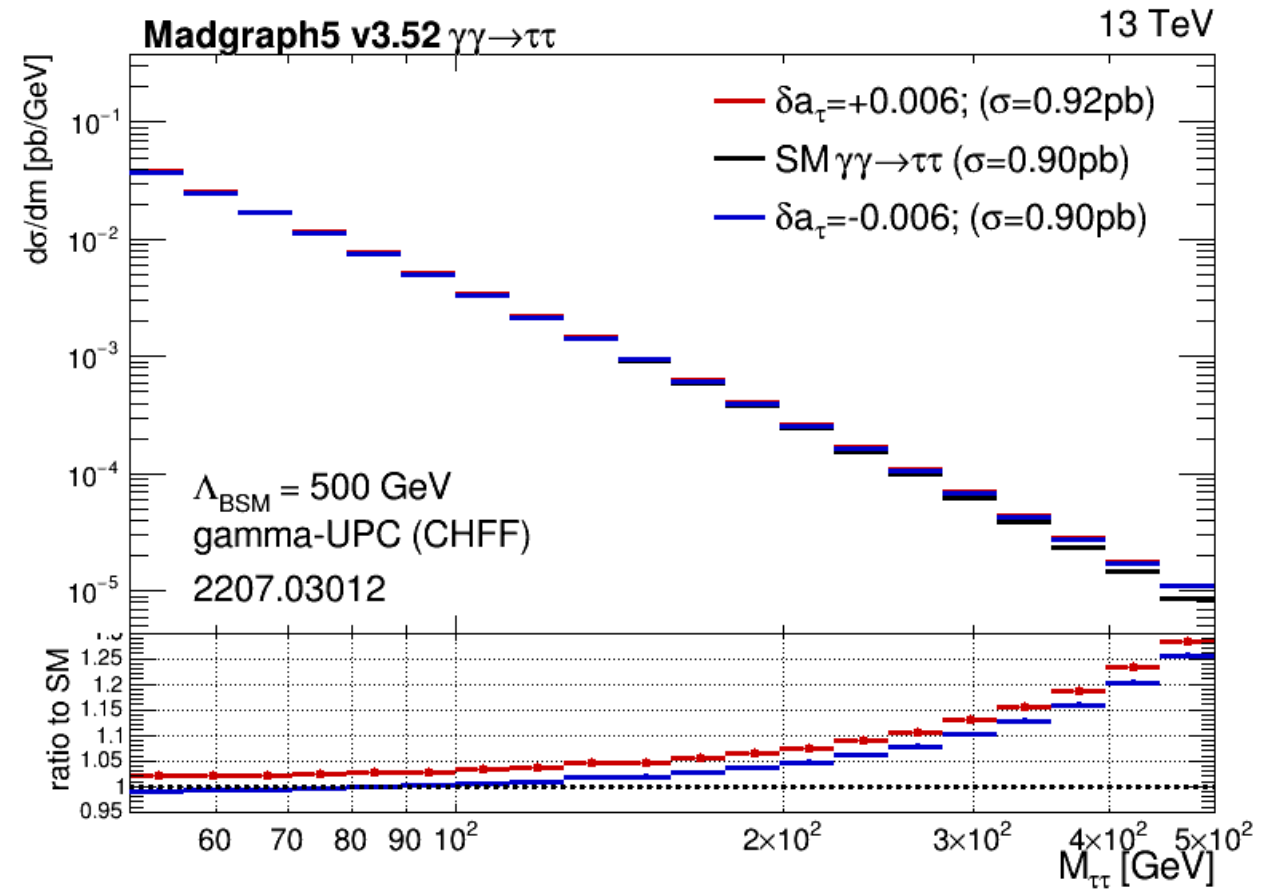
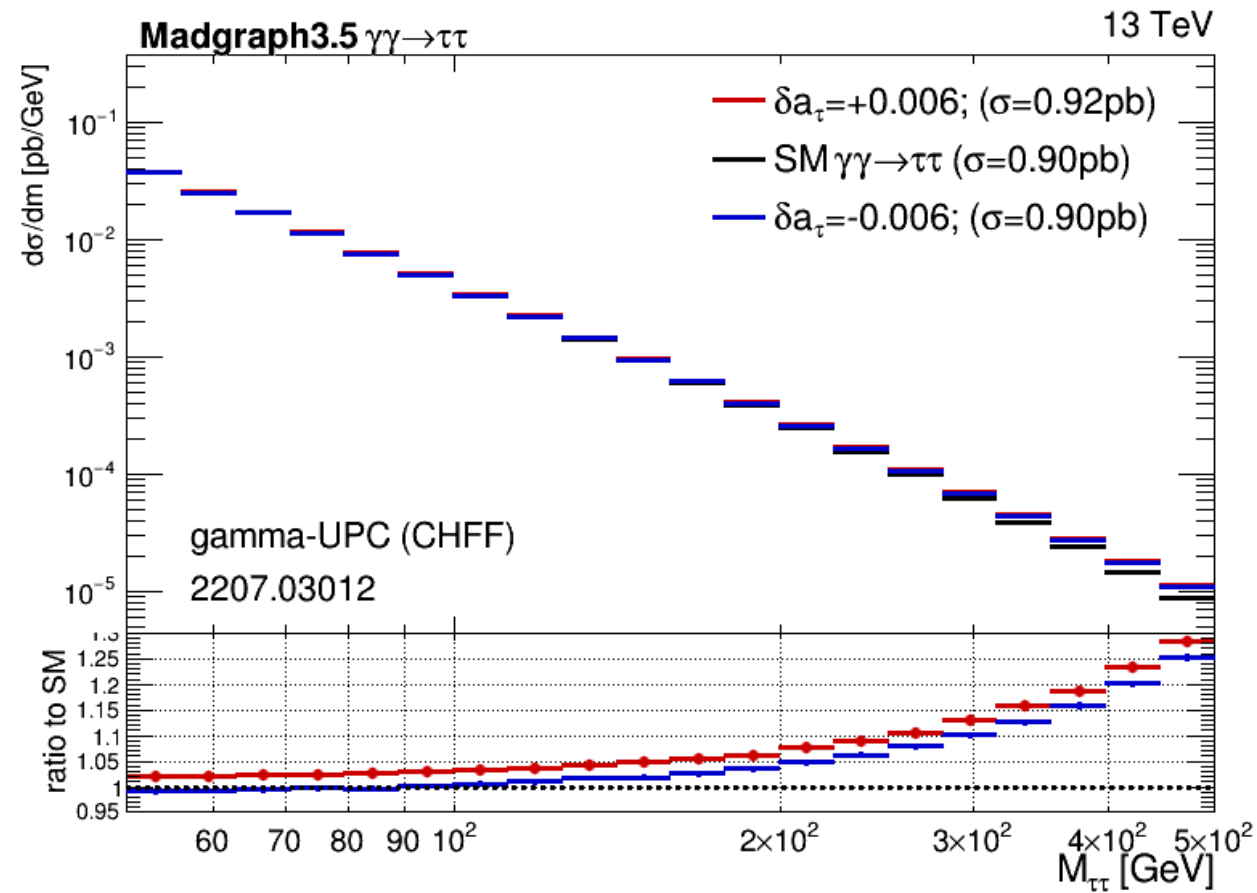
FIG. 1. Elementary cross section for  $\gamma\gamma \rightarrow \tau^+\tau^-$  process as a function of  $W_{\gamma\gamma} = m_{\tau\tau}$  (left) and as a function of  $z = \cos\theta$  for  $W_{\gamma\gamma} = 15$  GeV (right).

Dynal et al. (2020) [arXiv:2002.05503](https://arxiv.org/abs/2002.05503)

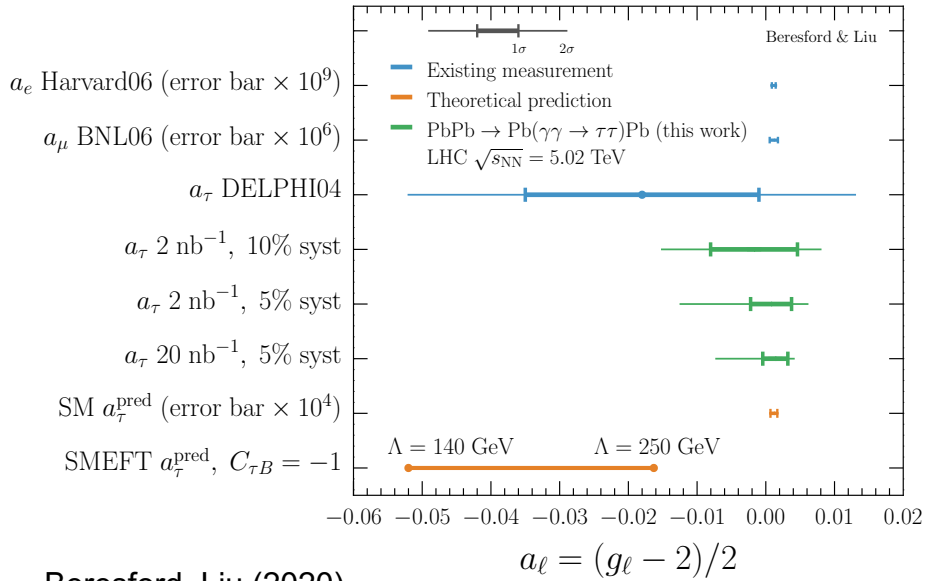
- BSM Scale dependence:**

$$\mathcal{L}_{BSM} = \bar{L}_\tau \sigma^{\mu\nu} \tau_R H \left[ \frac{C_{\tau B}}{\Lambda^2} B_{\mu\nu} + \frac{C_{\tau W}}{\Lambda^2} W_{\mu\nu} \right], \text{ if } C_{\tau W} = 0 \text{ then } \delta\alpha_\tau = \frac{2m_\tau}{e} \text{Re}(C_{\tau B}) \frac{\sqrt{2}v \cdot \cos\theta_W}{\Lambda^2}$$

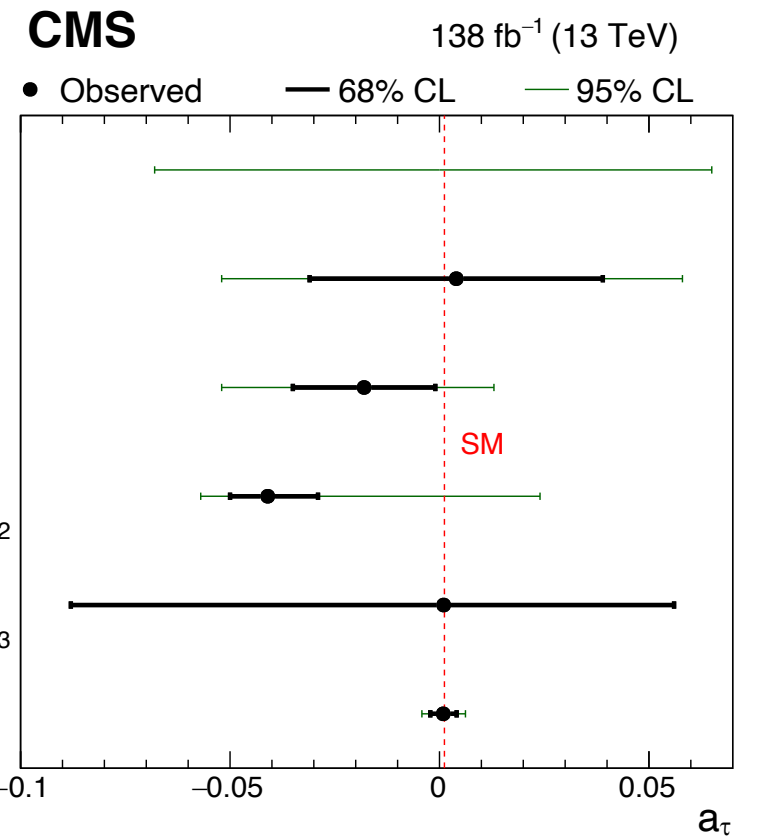
Two options tested:  $C_{\tau W} = 6.7$ ,  $\Lambda = 2\text{TeV}$  and  $C_{\tau W} = 6.7/16$ ,  $\Lambda = 500\text{GeV}$



# $a_\tau$ comparisons



Beresford, Liu (2020)  
[arXiv:1908.05180](https://arxiv.org/abs/1908.05180)



ATLAS (2022) [STDM-2019-19](https://arxiv.org/abs/2019.11.01)

