

AdS₃ vacua through Exceptional Field Theory

Camille Eloy

GenHET meeting in String Theory, 29th April 2024

Joint work with G. Larios, H. Samtleben, M. Galli and E. Malek

[arXiv:2011.11658, arXiv:2111.01167, arXiv:2306.12487, arXiv:2309.03261, arXiv:2405.xxx]



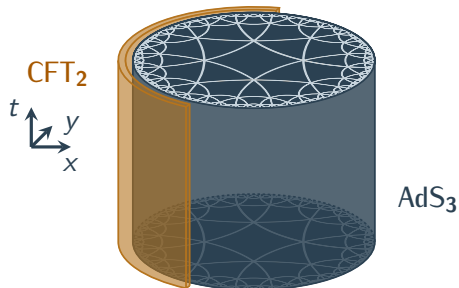
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Motivations

Bulk
Supergravity
on $\text{AdS} \times \mathcal{M}$

\Updownarrow

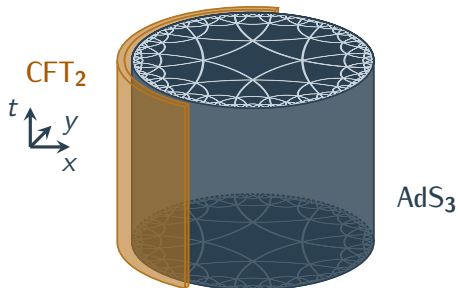
Boundary
Conformal fields
theory (CFT)



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 Supergravity
 on $\text{AdS} \times \mathcal{M}$

\Updownarrow

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Field operator map: $(\phi, m) \longleftrightarrow (\mathcal{O}, \Delta)$

$$\left\langle \exp \left(\int d^d x \mathcal{O} \phi^{(0)} \right) \right\rangle_{\text{CFT}} = e^{-S_{\text{sugra}}[\phi]} \Big|_{\text{boundary}},$$

Recent progress in understanding $\text{AdS}_3/\text{CFT}_2$:

$$\text{AdS}_3 \times \mathcal{S}^3 \times \mathcal{S}^3 \times \mathcal{S}^1 \longleftrightarrow \text{WZW on } \text{Sym}^N(\text{SU}(2) \times \text{U}(1))$$

[Eberhardt, Gaberdiel, Li (2017)]

$$\text{AdS}_3 \times \mathcal{S}^3 \times \text{T}^4 \longleftrightarrow \text{WZW on } \text{Sym}^N(\text{T}^4)$$

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Continuous deformations preserving the conformal symmetry.

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Operator \mathcal{O} with $\Delta = 2$

AdS
Scalar field ϕ with $m = 0$

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compact manifold



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Example: fields on $\text{AdS}_3 \times S^1$ $\varphi^{(4d)}(x^\mu, y) = \sum_n \phi_n^{(3d)}(x^\mu) e^{iny/R}$.

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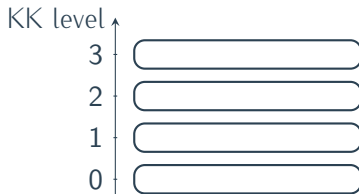
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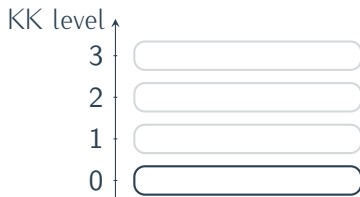
Compactification leads to towers of
massive **Kaluza-Klein** modes.



Consistent truncations

Consistent truncation:

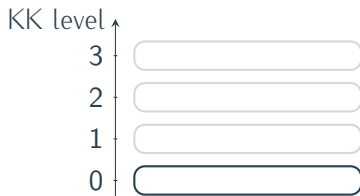
Restriction to a finite subset of KK modes such that every solution of the truncated theory defines a solution of the full theory.



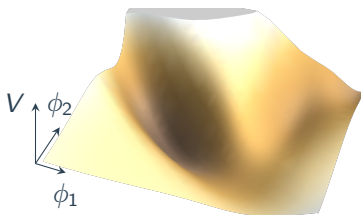
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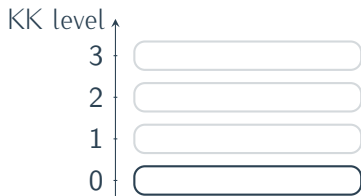
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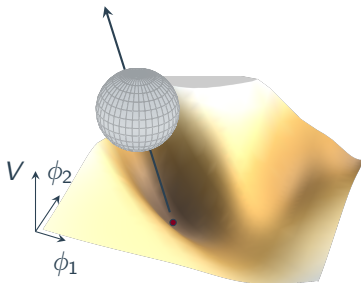
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10d uplift:

$\text{AdS}_3 \times \mathcal{M}_1$

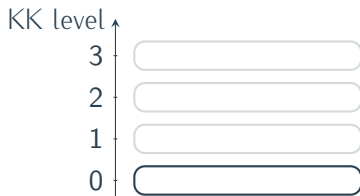


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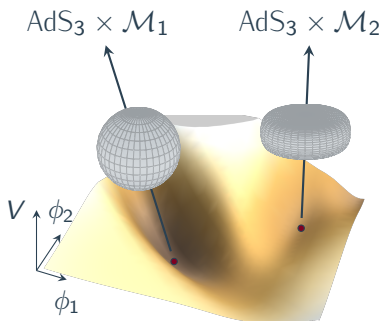
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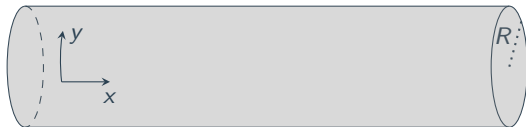


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Duality symmetries

Dualities: novel symmetries arising when string theory is compactified.

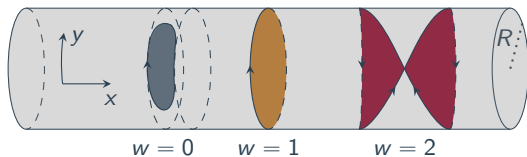
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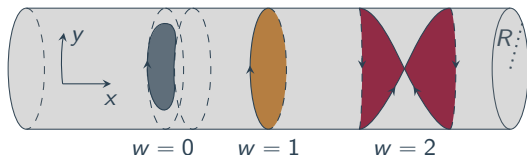
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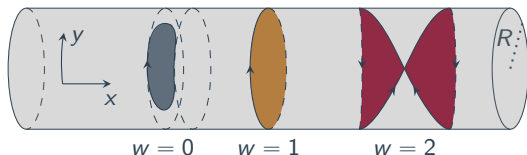
Winding number: w
Momentum along y : p

$$\text{Energy: } M^2 = \frac{p^2}{R^2} + \frac{w^2 R^2}{\alpha'^2} \implies \text{invariant under } \begin{cases} R \rightarrow \alpha'/R, \\ w \leftrightarrow p. \end{cases}$$

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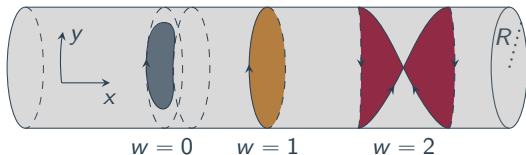
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U duality: Further symmetry enhancement. For type II: $E_{d+1(d+1)}$.

Exceptional Field Theory

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⇒ relevant framework to implement dualities!

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Today:

- Duality symmetries provide powerful tools to study the AdS/CFT correspondence,
- Exceptional Field Theory makes it possible to build consistent truncation and compute Kaluza–Klein spectra.

From 10d to 3d and $E_{8(8)}$ ExFT

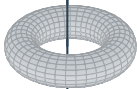
From IIB to maximal supergravity in 3d

$$\begin{array}{l} \text{10d IIB sugra} \\ \mathcal{N} = (2, 0) \end{array} \quad e^{-1} \mathcal{L}_{\text{IIB}} = e^{-\phi} \hat{R} - e^{-\phi} \partial_{\hat{\mu}} \hat{\phi} \partial^{\hat{\mu}} \hat{\phi} - \frac{1}{12} G_{\hat{\mu}\hat{\nu}\hat{\rho}}^{\alpha} M_{\alpha\beta} G^{\beta\hat{\mu}\hat{\nu}\hat{\rho}} + \dots$$

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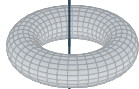


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$E_{8(8)}$ global symmetry
 after **dualization/reorganisation** of the fields.

Fields: $g_{\mu\nu}(x)$, $M_{\bar{M}\bar{N}}(x) \in E_{8(8)}/SO(16)$

$$e^{-1} \mathcal{L}_{3d} = R + \frac{1}{240} \partial_{\mu} M_{\bar{M}\bar{N}} \partial_{\mu} M^{\bar{M}\bar{N}}$$

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Gauging $G \subset E_{8(8)}$ through an **embedding tensor** $X_{\bar{M}\bar{N}}$:
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- Internal coordinate dependence \implies non-abelian gauge structure:

$$E_{8(8)} \text{ generalised diffeomorphisms } \mathcal{L}_{(\Lambda, \Sigma)}^{E_{8(8)}}.$$

- Duality-covariant w.r.t. $E_{8(8)}$: $D_\mu = \partial_\mu - \mathcal{L}_{(\mathcal{A}_\mu, \mathcal{B}_\mu)}^{E_{8(8)}}$

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IIB SUGRA

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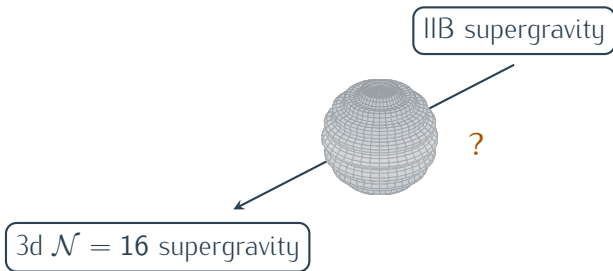
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Consistent truncation and Kaluza–Klein spectra within ExFT

General idea

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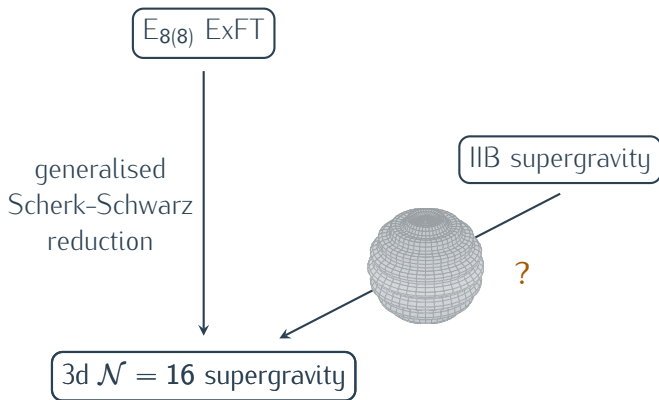
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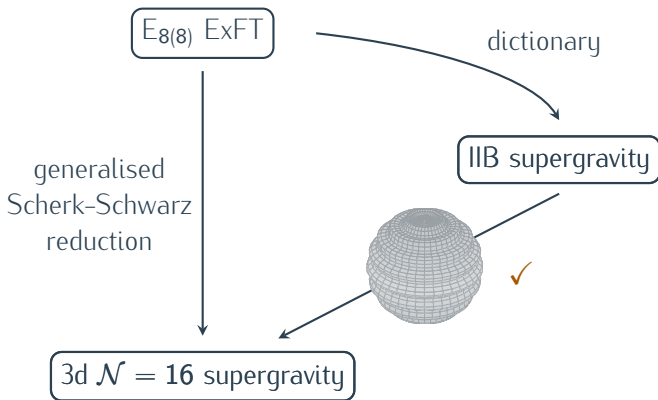
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Generalized Scherk-Schwarz ansätze in terms of twist matrix $U_M^{\tilde{M}} \in E_{8(8)}$ and scale factor ρ :

$$\begin{cases} \mathcal{M}_{MN}(x, Y) = U_M^{\tilde{M}}(Y) U_N^{\tilde{N}}(Y) M_{\tilde{M}\tilde{N}}(x), \\ \mathcal{A}_\mu^M(x, Y) = \rho(Y)^{-1} (U^{-1})_{\tilde{M}}^M(Y) \mathcal{A}_\mu^{\tilde{M}}(x). \end{cases}$$

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Consistency conditions:

$$\text{EOM}_{\text{ExFT}} \left[\mathcal{A}_\mu(x, Y) \right] = U(Y) \cdot \text{EOM}_{3d} \left[\mathcal{A}_\mu(x) \right].$$

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Generalized Scherk–Schwarz ansätze in terms of twist matrix $U_M^{\tilde{M}} \in E_{8(8)}$ and scale factor ρ :

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Embedding tensor of the 3d theory!

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$$\begin{cases} \mathcal{M}_{MN}(x, Y) = U_M^{\bar{M}}(Y) U_N^{\bar{N}}(Y) \mathcal{Y}_\Sigma(Y) M_{\bar{M}\bar{N}}^\Sigma(x), \\ \mathcal{A}_\mu^M(x, Y) = \rho(Y)^{-1} (U^{-1})_{\bar{M}}^M(Y) \mathcal{Y}_\Sigma(Y) A_\mu^{\bar{M}\Sigma}(x), \end{cases}$$

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$$M_{\bar{N}}^{\bar{M}\Sigma \Omega} = \left(\eta^{\bar{M}\bar{P}} + \delta^{\bar{M}\bar{P}} \right) \left(X_{\bar{P}\bar{N}} \delta^{\Sigma\Omega} + f_{\bar{P}\bar{N}}^{\bar{Q}} \mathcal{T}_{\bar{Q}}^{\Sigma\Omega} \right).$$

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⇒ access to KK spectrum around any vacuum in the potential!

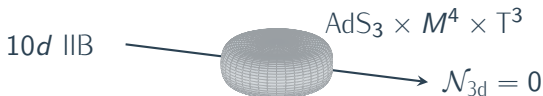
Example: $\text{AdS}_3 \times \mathcal{S}^3 \times T^4$

(ω, ζ) deformation of the $AdS_3 \times S^3 \times T^4$ vacuum:



Remaining isometries: $U(1)_L \times U(1)_R \times U(1)^4$.

(ω, ζ) deformation of the AdS₃ × S³ × T⁴ vacuum:



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$$e^{\hat{\phi}} = \Delta^2,$$

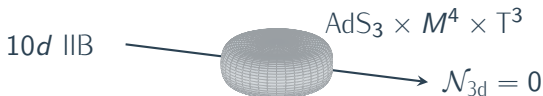
$$d\hat{s}^2 = ds^2(\text{AdS}_3) + ds^2(M_{\omega, \zeta}^3) + \delta_{ij} dy^i dy^j + [dy^7 + e^\omega \zeta \Delta^4 (\cos^2 \alpha d\beta - \sin^2 \alpha d\gamma)]^2,$$

$$\hat{H}_{(3)} = 2\text{Vol}(\text{AdS}_3) + \sin(2\alpha) \Delta^8 e^{2\omega} d\alpha \wedge (d\beta + \zeta dy^7) \wedge ((\zeta^2 + e^{-2\omega})d\gamma - \zeta dy^7),$$

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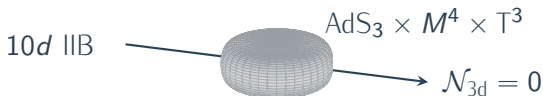
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Effect on the spectrum:

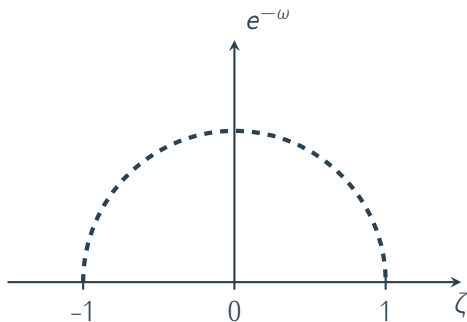
$$(\Delta = \dots + \sqrt{\dots + \sum (2\pi p_a)^2})$$

$$\sum (2\pi p_a)^2 \longrightarrow \sum (2\pi p_a)^2 + \frac{e^{2\omega}}{4} \left((q_L - q_R) + (q_L + q_R) (e^{-2\omega} + \zeta^2) + 4\pi p_T \zeta \right)^2 - q_L^2$$

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--- SUSY locus
 $\zeta^2 = 1 - e^{-2\omega}$
 $\mathcal{N}_{3d} = (0, 4)$

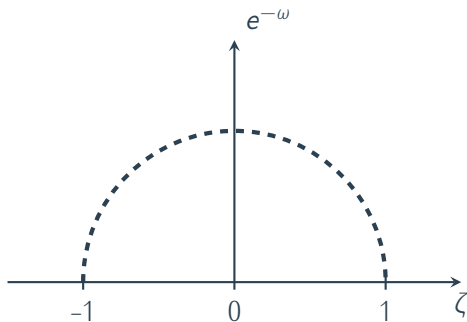
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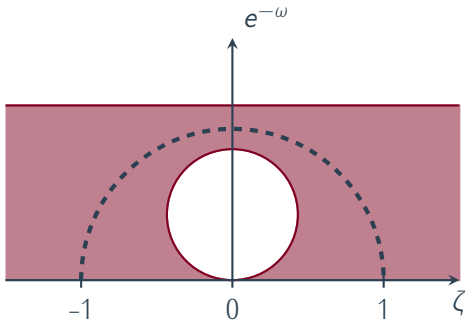
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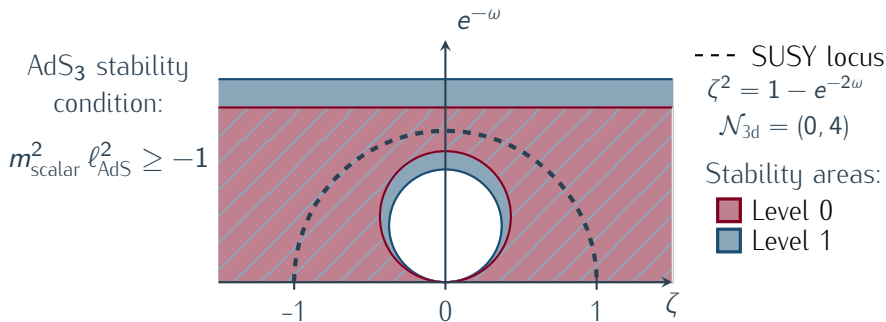
Stability areas:

■ Level 0

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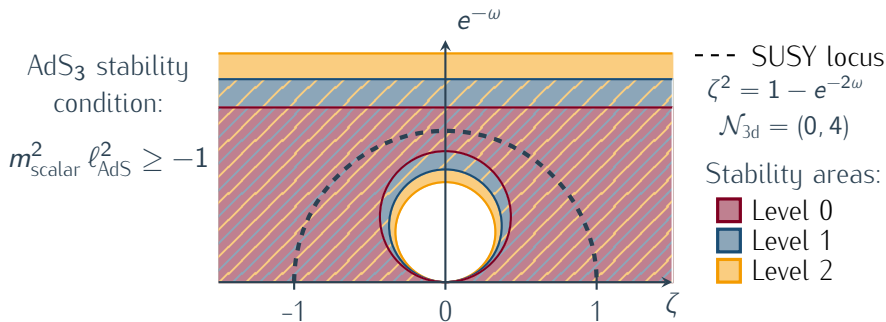
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First example of a full family of non-SUSY (pert.) stable AdS₃ vacua.

Conclusion and perspectives

- ExFT gives efficient tools for the analysis of consistent truncations and Kaluza-Klein spectra.

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- ExFT gives efficient tools for the analysis of consistent truncations and Kaluza–Klein spectra.
- New families of AdS_3 vacua, with supersymmetric subfamilies and non-susy BF stability
 \implies first candidates for $2d$ non-supersymmetric holographic conformal manifold.
- Up to 15 deformation parameters, for $\mathcal{S}^3 \times T^4$ and $\mathcal{S}^3 \times \mathcal{S}^3 \times \mathcal{S}^1$, including TsT.
- Described by $J\bar{J}$ deformations of the worldsheet theory.
- CFT? Possible non-pert. decay channel? Cubic couplings?

Thanks for listening!