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From lattice QCD to experiment - general introduction

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Baryon weak decays - from experiment to lattice QCD Warsaw, Poland 4-5 March 2024

STR®NG $2:70$

Introduction

- Why do weak baryon decays?
- Baryon asymmetry of the universe requires (Sacharov)
	- C, P and CP violation
	- Out of equilibrium
	- **•** Barvon number violation
- **Generally testing the Standard Model**
- C and P violation in baryons and mesons: late 1950s
- CP-violation in kaons: 1964 (indirect)
- CP-violation in kaons: direct 1999 $(\varepsilon'/\varepsilon)$
- \bullet CP-violation in bottom mesons: > 2001 in lots of places
- CP-violation in charmed mesons: (LHCb 2019)
- all compatible with the Standard Model
- CP-violation in baryons is not observed yet
- $\Lambda_b \to p \pi^-\pi^+\pi^-$ to 3.3 σ (LHCb 2016)

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• What is needed to see CP-violation?

- Need a CP-violating amplitude
- Need another amplitude for it to interfere with
- CP-violation changes from particle to anti-particle
- Strong phases do not
- **Interference leads to observable effects**
- \bullet Baryons ony have direct CP -violation, no particle anti-particle mixing
- So to make theory predictions:
	- Need to know both amplitudes
	- Or look at observables where the "other" amplitude cancels
- Reminder of this talk:
	- \bullet A little bite more about CP-violation and the first steps
	- overview of how these amplitudes are calculated at (low) energies

CP-violation in the Standard Model

• Hidden in the W-couplings:
$$
\frac{g_2}{\sqrt{2}}W^\mu\left(\overline{u}_L \overline{c}_L \overline{t}_L\right) V \gamma_\mu \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix}
$$

- \bullet V is a general 3 by 3 unitary matrix.
- Redefine phases of quark-fields: V_{11} , V_{12} , V_{13} , V_{21} and V_{31} real

$$
V = \left(\begin{array}{ccc} c_1 & -s_1c_3 & -s_1s_3 \\ s_1c_2 & c_1c_2c_3 - s_2s_3e^{i\delta} & c_1c_2s_3 + s_2c_3e^{i\delta} \\ s_1s_2 & c_1s_2c_3 + s_2s_3e^{i\delta} & c_1s_2s_3 - c_2c_3e^{i\delta} \end{array}\right)
$$

- $c_i = \cos \theta_1$, $s_i = \sin \theta_i$
- Unitary implies $\sum_i V_{ik}^* V_{il} = \delta_{il}$
- But need all three generations, otherwise can remove the phase
- CP-violation in SM is small because the angles are small

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Need loops in the SM

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BSM etcetera

 $s \searrow$ μ \swarrow d W Heavy particles can contribute in loop t \bullet γ , g, Z u, c

- Also heavy BSM particles can contribute: tree level and loops
- Competition with suppressed SM contributions allows very good limits
- Might need to know the SM very precisely to detect deviations
- Need to be able to calculate amplitudes \bullet

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Methods of effective field theory

- Separate the problem at different scales
- \bullet High scale: $\geq M_W$
	- Reduce everything to quarks, leptons, gluons, photons
	- Integrate out everything else $(W, Z, top, heavy BSM)$
	- End up with a number of local operators of varying dimensions
	- Can be done using Feynman diagrams or other methods
	- Example: W exchange to $\bar{b}_L \gamma_\mu c_L \bar{u}_L \gamma^\mu d_L$
	- But many more options possible: full classsification: low-energy effective field theory
	- Matching BSM/SM to effective operators
- \bullet Intermediate scale: M_W to hadronic scale
	- Do renormalization group running down
	- Known typically to 2 and sometimes 3 loops
	- Running involves gluons and photons
- These two stages are under control and no problem in principle
- Can be very tedious though

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The underlying problem: the low energy stuff

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- quark-antiquark
- add gluons
- Two body decay

The underlying problem

- Flavour and Hadron Physics: need structure of hadrons
- Why is this so difficult?
- $\textsf{QED} \,\, \mathcal{L} = \overline{\psi} \gamma_\mu \left(\partial^\mu \textit{ieA}^\mu \right) \psi \frac{1}{4}$ $\frac{1}{4}F_{\mu\nu}F^{\mu\nu}$
- QCD: $\overline{q}\gamma_\mu$ $\left(\partial^\mu i\frac{g}{2}\right)$ $\frac{g}{2}G^{\mu}\big)$ $q-\frac{1}{8}$ $\frac{1}{8} {\rm tr} \left(\mathsf{G}_{\mu\nu} \mathsf{G}^{\mu\nu} \right)$
- $G_{\mu} = G_{\mu}^{a} \lambda^{a}$ is a matrix
- \bullet $F_{\mu\nu} = \partial_{\mu}A_{\nu} \partial_{\nu}A_{\mu}$
- $G_{\mu\nu} = \partial_{\mu} G_{\nu} \partial_{\nu} G_{\mu} i g (G_{\mu} G_{\nu} G_{\nu} G_{\mu})$
- gluons interact with themselves
- $e(\mu)$ smaller for smaller μ , $g(\mu)$ larger for smaller μ
- QCD: low scales no perturbation theory possible

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The low-energy step

- So simple QCD perturbation theory does not work
- What else?
- **•** Lattice QCD
- QCD and other sum rules (light-cone sum rules)
- Using dispersion relations
- Schwinger-Dyson equations
- Effective field theor(y)(ies)
- Symmetries
- Models

· · ·

 \bullet

- \bullet Large N_c
- **•** Find observables where most of the difficulties cancel

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- Rest of the talk: giving some indications of strenghts and weaknesses of the different methods (i.e. get everyone angry at me)
- In particular I will not discuss all the extra improvements that are used in practice
- **•** Different observables call for different methods
- **•** Cross checks are always valuable

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Lattice QCD

A recommended read:

Lattice QCD: A Guide for people who want results, Christine Davies, hep-lat/0509046 [hep-lat]

- From first principles (in principle) (there are often extrapolations and other assumptions inherent in the analysis)
- Take the functional integral of QCD and integrate it numerically
- Discretize space and time and take a finite volume
- Go to Euclidean space or imaginary time
- The last two-points are needed to be able to do the functional integral numerically

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Lattice QCD

- Φ $\hbar c = 197.3$ MeV fm
- Lattice spacing a needs to be such that $1/a$ is scale significantly above 1 GeV: match to perturbative QCD
- \bullet The lattice size L must belarge enough so that (all) the hadrons "fit": need to be several fm.
- E.g. $1/a = 2$ GeV and $L = 4$ fm requires about 40 points in each direction
- Also explains why charm quark is difficult (but there are ways around it for some cases)
- The b-quark is typically treated as static (via HQET or NRQCD) but then needs $1/m_b$ corrections.
- Fast moving particles also difficult: wavelengths similar to lattice spacing
- **•** State of the art: $96^3 \times 144$

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Lattice QCD: matrix elements of operators

- Calculate numerically vacuum expectation values: $\langle O_1(x_1) \dots O_n(x_n) \rangle$
- \bullet From this (LSZ theorem for the theorists) get lots of physical quantities
- Hard work in lattice QCD summarized in a few words:
	- \bullet finding good O_i for the observable
	- Finding ways to get the vacuum expectation values calculated as accurately as possible

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Lattice QCD: masses and decay constants

Two-point functions
$$
\langle O_1(0, \vec{0})O_2(\tau, \vec{0}) \rangle = \sum_i f_{1i} f_{2i} e^{-E_i \tau}
$$

- **o** the sum is over all states *i*
- ALL: also multiparticle states, states with momentum,. . .
- $f_{1i} = \langle O_1|i\rangle$
- **Can get energies and couplings of states**
- Large τ dominated by E_0 : get at the mass and coupling constants of the ground state.
- Example: O_i axial current: pion mass and decay constants
- Possible problems;
	- Need large τ : lattice length must be big enough (neglect around the end of the world)
	- Excited state contamination can happen
	- Typically: at small τ : $a \neq 0$ artefacts; at large τ : noise

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Lattice QCD: form factors

- Form factors: need a matrix element like $\langle i|O_W|i\rangle = f_{Wii}$
- Get from $\langle O_1(0)O_W(\tau_W)O_2(\tau_2)\rangle=\sum_{ij}f_{1i}f_{2j}f_{Wij}e^{-E_i\tau_W}e^{-E_j(\tau_2-\tau_W)}+\sum_i f_{1i}f_{2i}e^{-E_i\tau_2}$
- So need to get the ground state in two legs
- The problems from previous page are amplified
- States should not move too fast so B-decays limited to maximal q^2

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Lattice QCD: multi particle final states

- Problem when looking at scattering and multi (i.e. 2 or more) final states (note leptons don't count)
- Energy is not conserved so the lowest possible state with the same quantum numbers will dominate
- **•** Scattering is in Minkowski: need to relate to Euclidean observables
- Problem for 2-body scattering: Lüscher: via volume dependence of energy levels
- Decays: Lellouch-Lüscher: same but with an insertion of the decay operator
- Three body: active research area

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Lattice QCD and Baryons: added problems

- Three quark vs quark-antiquark: operators typically more complicated
- Baryons are bigger: need larger lattices
- Excited states closer by than for mesons
- NOISE MUCH LARGER

Explanation (long known):

- quantity x via $\langle x \rangle$; error is via $\langle x^2 \rangle \langle x \rangle^2$
- baryons: $\left\langle N^{\dagger}(0)N(\tau)\right\rangle \sim e^{-m_N\tau}$
- Noise $\langle N^{\dagger}(0)N(0) N^{\dagger}(\tau)N(\tau)\rangle \sim e^{-E_0\tau}$
- But $N^\dagger N$ couples to purely mesonic states and $E_0 < m_B$
- signal to noise decays as $e^{-(m_B-E_0)\tau}$: exponentially worse

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- Form factors: simple ones and near the largest q^2 : very good
- **•** Two body scattering for light mesons: starting to be good
- Weak decays if not via form factors: only starting
- \bullet Note: B - B mixing is like a form factor
- I summarized a large community (\geq 500 for a big conference) working for a long time (≥ 40 years) here in a few slides
- I also stuck to lattice topics related to what we might want to do

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Light cone quantization Brodsky, Pauli, Phys.Rept. 301 (1998) 299-486 [hep-ph/9705477]

- \bullet Only physical degrees of freedom (ie no ghosts \dots)
- Wave functions are expanded in Fock states: partons directly visible
- The perturbative vacuum is the physical vacuum
- In principle allows for a competing numerical nonperturbative method
- Was a very active field 1990s
- Main (unsolved) difficulty: dealing with the zero mode This is where all the trouble of spontaneous symmetry breaking and confinement hides in this approach

Note: this not quark models on the light cone

 \bullet Now often combined with holography (Brodsky, de Téramond,...)

LUND Lattice QCD

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Other full QCD only

QCD, Finite Energy Sum Rules, . . .

• Circle and residue points: perturbative QCD

Axis: data and/or resonance saturation

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Dispersion relations and unitarity

- Again Cauchy's theorem
- But now choose $f(z)$ e.g. a decay or scattering amplitude
- \bullet s, t, u: more parameters
- Unitarity $1 = S^{\dagger}S = 1 + T^{\dagger}T + i(T T^{\dagger})$
- Due to the cuts: phases provide constraints
- Integral equations for the amplitudes
- Questions: subtraction constants, experimental input for phases, asymptotic behaviour

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Schwinger-Dyson equations

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• Idea
$$
(\phi^3)
$$
: $- \bullet$ = $-$ + $-$

- Full three-point function involves full four-point function
- **Four involves five.**
- An infinite set of consistency equations
- Need to truncate: here the model aspects start
- Need for a starting ansatz to make life bearable (usually a full gluon propagator)
- Usually kept at the "quenched" approximation

Effective Field Theory (EFT)

- **•** gap in the spectrum \implies separation of scales
- with the lower degrees of freedom, build the most general effective Lagrangian
- $\bullet \infty \#$ parameters
- Where did my predictivity go?
- $\bullet \implies$ Need some ordering principle: power counting Higher orders suppressed by powers of $1/\Lambda$
- Taylor series expansion does not work (convergence radius is zero when massless modes are present)
- Continuum of excitation states need to be taken into account
- Use field theory and loops

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Examples of low-energy EFTs

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• Chiral perturbation theory

• Heavy quark effective theory

- Combinations of the above
- Main drawbacks:
	- many parameters, often unknown
	- Not always (often?) in range of validity
- Beware: Just because it says chiral perturbation theory or effective field theory doesn't mean it is (they are not protected trade marks)

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Effective Lagrangians

- Basic degrees of freedom: hadron fields beyond the pseudoscalars
- Beware of product (mis)labelling
	- Chiral Perturbation Theory
	- Chiral Effective Theory
	- Are very popular names and "de vlag dekt niet altijd de lading" since they are not protected names (free flag doesn't make free bottom)
- Note field redefinitions: same Lagrangian can look very different
- Hope: find a simple Lagrangian and then refine it
- A full classification attempt: Resonance chiral theory (R_XT) , also attempts to go to one-loop.
- This includes e.g. also hidden local symmetry implementations of the vectors
- **•** many other partially successful attempts
- In some ways holography belongs to this class as well
- Difficult to find a proper power counting (so not EFT)

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Models with "Quarks"

- Nonrelativistic constituent quark models: understanding the spectrum (fill up octets and nonets)
- Chiral quark model: quarks plus pseudo-scalars, no confinement
- Nambu-Jona-Lasinio models: Quarks with a four quark interaction
	- Has spontaneous chiral symmetry breaking

 $=$ \longrightarrow +

Produces a constituent quark mass from a gap equation:

- mesons from a bubble sum
- Mesons but no confinement

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- Add vector-like four quark interactions \implies vectors and axial-vertex
- Add a 't Hooft vertex to get η' better (or a variation on that vertex)
- make the vertex non-local
- Add Polyakov loop
- Many more variations possible
- Usually large N_c or tree level at the "meson" level
- Some attempts to go beyond that: many difficulties and not clear if it ever yielded something useful

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Holography or AdS/QCD

- Holography: put a 3D picture in a 2D film
- Lots of (supersymmetric) theories have very unexpected properties
- \bullet $N = 4$ Super Yang-Mills dual to five dimensional string theory
- Many more examples known (Maldacena, Polyakov,. . .)
- The four dimensional theory lives on a boundary of the five dimensional one
- Conjecture: same is true for QCD
- Write a low-energy Lagrangian in the five dimensional theory (mesonic and /or baryons)
- Choose the (global in four dimensions) symmetry and including a choice of fields
- Top down: start from a stringy construction
- Bottom up: simply choose a five-dimensional model

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Holography

- \bullet Space is Minkowski \times a line
- Line has one end: UV point, where the four dimensional fields live
- On that point: connection with QCD operators as boundary conditions
- For each operator: introduce a five-dimensional bulk field
- Need boundary condition "at the othe other end"
- Hard wall: put a finite length
- Soft wall: infinite length but fields must decay sufficiently fast
- Eigenmodes in the fifth dimension: an infinite number of resonances with the same spin

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- Simplest model: Hirn-Sanz: vector+axial-vector fields
	- \bullet Boundary conditions at large L: put in QCD VEV
	- Contains the pseudscalar (nonet) and an infinite number of vector and axial-vectors
- Erlich, Katz, Son, Stephanov and Da Rold Pomerol
	- Scalar-Pseudoscalar-vector-axial-vector fields: an infinite number of these
	- Allows for input of quark masses: boundary condition at the UV end
	- QCD VEV again at the IR (large L) end
- Can add many more fields
- Baryons: use either skyrmions in the mesonic theory or add explicit fermion fields

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Holography: advantages, disadvantages

- Results do depend on the choice of model
- Nonleptonic decays difficult as well in this approach (Master thesis of Jack Borthwick was my start on this)
- Some connection with QCD but still a model and there is a certain variation in predictions

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- • Why we want to study CP-violation
- \bullet Baryons give us more information beyond what we have (just mentioned really)
- Overview of lattice QCD
- Lightning overview of other methods
- Be aware of the advantages and drawbacks of what you use \bullet
- \bullet Do the best you can, sometimes using a model is all you can do
- Often best results by combining several methods

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