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Lessons from the Swampland Program

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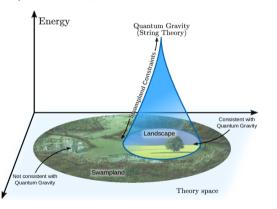
Based on: 2404.01371 with R. Blumenhagen, N. Cribiori and A. Gligovic Review article: 2404.05801

The Swampland Program

Conceptual framework



Consistent set of conjectures motivated mainly (but not exclusively) by string theory. Example reviews: [Palti '18, van Beest, Calderón-Infante, Mirfendereski, Valenzuela '22].



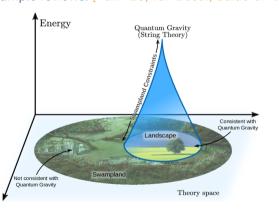
- No Global Symmetries Conjecture
- **Distance Conjecture**
- **Emergent String Conjecture**
- Weak Gravity Conjecture
- (A)dS Distance Conjecture
- Gravitino Conjecture

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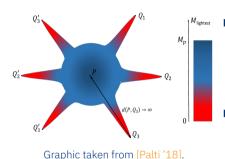
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- ► No Global Symmetries Conjecture
- **▶** Distance Conjecture
- **▶** Emergent String Conjecture
- ▶ Weak Gravity Conjecture
- ► (A)dS Distance Conjecture
- Gravitino Conjecture
- Emergence Proposal

Swampland Ingredients





▶ Distance Conjecture: At an infinite distance in moduli space, a tower of exponentially light states appears [Ooguri, Vafa '06]

$$M(p) \sim M(p_0) e^{-\alpha d(p_0,p)}, \quad \alpha \sim \mathcal{O}(1).$$
 (1)

Emergent String Conjecture: [Lee, Lerche, Weigand '18] $\rightarrow \begin{cases}
\text{decompactification} \\
\text{emergent string limit}
\end{cases}$

Species Scale: The UV cut-off in the presence of many light fields is [Dvali '08]

$$\Lambda_{\rm sp} = \frac{M_{\rm pl}^{(d)}}{N_{\rm sp}^{1/(d-2)}} \,. \tag{2}$$

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Emergence Basics

More recently, [van de Heisteeg, Vafa, Wiesner, Wu '22-'23]

$$S_{\text{corr.},d} \subset \frac{M_{\text{pl}}^{(d)\,d-2}}{2} \int d^d x \sqrt{-g} \left[\sum_n a_n(\phi_i) \frac{\mathcal{O}_n(\mathcal{R})}{M_{\text{pl}}^{(d)\,2n-2}} \right], \quad \frac{1}{\Lambda_{\text{sp}}(\phi_i)^{2n-2}} \simeq \frac{a_n(\phi_i)}{M_{\text{pl}}^{(d)\,2n-2}}. \quad (3)$$

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Emergence Proposal (Strong): The dynamics for all fields are emergent in the infrared by integrating out towers of states down from a scale Λ , below the Planck scale. [Palti '19]

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Emergence Proposal (Strong): The dynamics for all fields are emergent in the infrared by integrating out towers of states down from a scale Λ, below the Planck scale. [Palti '19] Toy models:



[Heidenreich, Reece, Rudelius '18, Grimm, Palti, Valenzuela '18, Lee, Lerche, Weigand '21, Castellano, Herráez, Ibáñez '22, Blumenhagen, Gligovic, AP '23]

Additional connections to topological strings [Hattab, Palti '23-'24].

An M-theoretic Emergence Proposal





Overview

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An M-theoretic Emergence Proposal





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Emergence Proposal (M-theory): In the M-theory limit $M_*R_{11} \gg 1$ with $M_{\mathrm{pl},d}$ kept fixed, a perturbative QG theory arises whose low energy effective description is emerging by integrating out the full **infinite** towers of states with a mass scale parametrically not larger than M_* [Blumenhagen, Cribiori, Gligovic, AP '24].

An M-theoretic Emergence Proposal





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Emergence Proposal (Strong): The dynamics for all fields are emergent in the infrared by integrating out towers of states down from a scale Λ [Palti '19].

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Light States: Transverse M2, M5 branes carrying KK momentum

$$R_{11} \to \lambda R_{11}, \quad M_* \to \frac{M_*}{\lambda^{\frac{1}{d-1}}}, \quad R_I \to \lambda^{\frac{1}{d-1}} R_I, \quad M_{D0} \sim \frac{M_{\rm pl}^{(d)}}{\lambda}, \quad M_{D2,NS5} \sim \frac{M_{\rm pl}^{(d)}}{\lambda^{1/(d-1)}}.$$
 (5)

Similarities: BFSS matrix model [Banks, Fischler, Shenker, Susskind '97].

R⁴ couplings

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GGV approach

M-theory on a (k + 1) torus of volume $r_{11}V_k$

$$S_{R^4} \simeq M_*^{d-8} \int d^d x \sqrt{-g} \, r_{11} \mathcal{V}_k \, a_d \, t_8 t_8 \, R^4 \,, \quad k = 10 - d.$$
 (6)

The **1/2 BPS saturated** coefficient a_d is known [Green, Gutperle, Vanhove '97]

$$a_{10-k} \simeq \frac{2\pi}{r_{11} \mathcal{V}_k} \sum_{m_I \in \mathbb{Z}} \int_0^\infty \frac{dt}{t^{\frac{4-k}{2}}} e^{-\pi t \sum_{I,J=1}^k m_I G_{(k+1)}^{IJ} m_J}. \tag{7}$$

Regularization: Poisson resummation over all integers and T-duality for $\hat{m}_I=0$.

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What more can we learn?

Testing the Emergence Proposal in M-theory





Extend the Ansatz of GGV to the **full spectrum** of **light** 1/2 BPS particle states

$$a_d \simeq \frac{2\pi}{r_{11}\mathcal{V}_k} \hat{\sum}_{N^A, m \in \mathbb{Z}} \int_0^\infty \frac{dt}{t^{\frac{d-6}{2}}} \, \delta(\text{BPS}) \, \exp\left(-\pi t \, N^A \mathcal{M}_{AB} N^B - \pi t \, \frac{m^2}{r_{11}^2}\right). \tag{8}$$

Regularization: UV cutoff + ζ -functions [Blumenhagen, Cribiori, Gligovic, AP '23].

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ightharpoonup d = 10: We can only have particle-like KK modes, just like GGV.

$$a_{10} \simeq \frac{2\pi}{r_{11}} \sum_{m \neq 0} \int_{\epsilon}^{\infty} \frac{dt}{t^2} e^{-\pi t \frac{m^2}{r_{11}^2}} \simeq \frac{2\zeta(3)}{r_{11}^3},$$
 (9)

using

$$\int_{\epsilon}^{\infty} \frac{dt}{t^2} e^{-\pi t A} = \frac{1}{\epsilon} + \pi A \left(\log(\pi A \epsilon) + \gamma_E - 1 \right) + \mathcal{O}(\epsilon). \tag{10}$$

Downside: The (constant) one-loop term is missing.

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Testing the Emergence Proposal in M-theory

ightharpoonup d = 9: Similar behavior (no **light** wrapped branes)

$$a_9 \simeq \frac{2\zeta(3)}{r_{11}^3} + \frac{8\pi}{r_{11}^2 r_1} \sum_{m \neq 0} \sum_{m \geq 0} \left| \frac{m}{m_1} \right| K_1 \left(2\pi |m| m_1 \frac{r_1}{r_{11}} \right). \tag{11}$$

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▶ d = 8: Also light wrapped M2-branes satisfying [Obers, Pioline '99]

$$\sum_{J} n_{IJ} m_{J} = 0 \rightarrow \mathcal{M}^{2} = n_{12}^{2} t_{12}^{2} + \frac{m^{2}}{r_{11}^{2}}, \quad t_{12} = r_{1} r_{2}.$$
 (12)

Our ansatz implies that the contribution to the R^4 coupling is

$$a_{8,D2/D0} \simeq \frac{2\pi}{r_{11}t_{12}} \sum_{n_{12} \neq 0} \sum_{m \in \mathbb{Z}} \int_{\epsilon}^{\infty} \frac{dt}{t} e^{-\pi t \left(n_{12}^2 t_{12}^2 + \frac{m^2}{r_{11}^2}\right)} \to$$
 (13)

$$a_{8,D2/D0} \simeq \frac{2\pi}{r_{11}t_{12}} \left(\frac{\pi}{3} r_{11} t_{12} + 4 \sum_{n_{12},m>0} \frac{1}{n_{12}} e^{-2\pi n_{12} m r_{11}t_{12}} \right) = -\frac{2\pi}{r_{11}t_{12}} \log \left(|\eta(ir_{11}t_{12})|^4 \right).$$

(14)

Testing the Emergence Proposal in M-theory





Adding the KK contribution

$$a_{8,D0} \simeq \frac{2\zeta(3)}{r_{11}^3} - \frac{2\pi}{r_{11}t_{12}} \log \left(r_{11}r_2^2 |\eta(iu)|^4 \right) + \frac{8\pi}{r_{11}^2} \sum_{\substack{m>0\\(m_1,m_2)\neq(0,0)}} \frac{m \, K_1 \left(2\pi \frac{m}{r_{11}} \sqrt{m_1^2 r_1^2 + m_2^2 r_2^2} \right)}{\sqrt{m_1^2 r_1^2 + m_2^2 r_2^2}}$$

$$(15)$$

where we have used
$$\int_{\epsilon}^{\infty} \frac{dt}{t} e^{-tA} = -\gamma_E - \log(\epsilon A) + \mathcal{O}(\epsilon). \tag{16}$$

We thus obtain the **complete** result in 8d!

Similarly in 7d!

Can this be checked further?

Testing the Emergence Proposal in M-theory





Adding the KK contribution

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 \blacktriangleright The pattern: **constant terms** \leftrightarrow **extended objects** persists in d=6.7 and in the emergent string limit in this duality frame.

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Testing the Emergence Proposal in M-theory

▶ The instanton contributions can be generally determined.

Particle states	Instantons
$(D0, \mathrm{KK}_{(K)})$	$ED0_{(K)}$
$(D2_{(IJ)}, \mathrm{KK}_{(K)})$	$ED2_{(IJK)}$
$(NS5_{(IJKLM)}, \mathrm{KK}_{(N)})$	ENS5 _(IJKLMN)
$(D2_{(IJ)},D0)$	$EF1_{(IJ)}$
$(NS5_{(IJKLM)}, D0)$	ED4 _(IJKLM)
$(NS5_{(IJKLM)}, D2_{(LM)})$	$ED2_{(IJK)}$

$$M_{\rm pl} = {\rm const}$$

Our results are consistent with more formal results [Kiritsis, Pioline '97, Obers, Pioline '99, Green, Russo, Vanhove '10].

pert. string theory		desert		M-theory
$g_s \ll 1$		$g_s = \mathcal{O}(1)$		$g_s \gg 1$
$a_d = \frac{c_0}{g_s^2} + \underbrace{\left(c_1 + \mathcal{O}(e^{-S_{ws}})\right)}_{\text{one-loop}} + \mathcal{O}(e^{-S_{st}})$	=	$\mathcal{E}_{\Lambda_{E_{k+1}},s=\frac{k}{2}-1}^{E_{k+1(k+1)}}$	=	$\mathcal{E}_{\Lambda_{E_k}\oplus 1,s=\frac{k}{2}-1}^{E_{k(k)}}$

Summary and Outlook





Testing the **M-theoretic Emergence Proposal**, we extended the ansatz of [Green, Gutperle, Vanhove '97] to the **full spectrum** of **light** 1/2 BPS particle states

$$a_d \simeq \frac{2\pi}{r_{11} \mathcal{V}_k} \hat{\sum}_{N^A, m \in \mathbb{Z}} \int_0^\infty \frac{dt}{t^{\frac{d-6}{2}}} \, \delta(\text{BPS}) \, \exp\left(-\pi t \, N^A \mathcal{M}_{AB} N^B - \pi t \, \frac{m^2}{r_{11}^2}\right). \tag{17}$$

Regularization: UV cutoff, minimal subtraction and ζ -function regularization.

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Upshots:

- \triangleright Self-consistently getting full results in d=7,8. Precise instanton predictions.
- ▶ Providing physical interpretation for previously ambiguous terms.
- ► Connecting the work of [Obers, Pioline '99] to the swampland framework.

Future directions:

- ► Microscopic structure of other physical amplitudes, e.g. *F*⁴ terms?
- ► Non 1/2 BPS quantities?
- ► M(-atrix) model implications?



Back-up Slide: 8d calculation in perturbative string theory

The Kaluza-Klein contribution is

$$a_8^{1-\text{loop},(1)} \simeq \frac{2\pi}{\vartheta_{12}} \sum_{(m_1, m_2) \neq (0, 0)} \int_0^\infty \frac{dt}{t} e^{-\pi t \left(\frac{m_1^2}{\rho_1^2} + \frac{m_2^2}{\rho_2^2}\right)},$$
(18)

$$\int_0^\infty \frac{dx}{x^{1-\nu}} e^{-\frac{b}{x} - cx} = 2 \left| \frac{b}{c} \right|^{\frac{\nu}{2}} K_{\nu} \left(2\sqrt{|b c|} \right), \qquad \int_{\epsilon}^\infty \frac{dt}{t} e^{-tA} = -\gamma_E - \log(\epsilon A) + \mathcal{O}(\epsilon). \quad (19)$$

With $\epsilon \to \tilde{\epsilon} = \epsilon \, 4\pi e^{-\gamma_E}$, this gives rise to

$$a_8^{1-\text{loop},(1)} \simeq -\frac{2\pi}{\vartheta_{12}} \log \left(\rho_2^2 |\eta(iu)|^4 \right).$$
 (20)

Meanwhile, defining $\alpha = (1,0), (0,1), (1,1)$, the winding sector contributes as

$$a_8^{1-\text{loop},(2)} = -\frac{2\pi}{\vartheta_{12}} \log \left(|\eta(i\vartheta_{12})|^4 \right) . \tag{21}$$

We get the full one-loop result!

Back-up Slide: Example of an NS5-brane contribution

The full set of BPS conditions is [Obers, Pioline '99]

$$\sum_{J} n_{IJ} m_{J} = 0 , \quad n_{[IJ} n_{KL]} + \sum_{P} m_{P} n_{PIJKL} = 0 , \quad n_{I[J} n_{KLMNP]} = 0 .$$
 (22)

An example of such a solution is the configuration

$$(n_{45}, m_1) = P(-\tilde{\nu}_5, \tilde{n}_{23}), \quad (n_{15}, m_4) = Q(\tilde{\nu}_5, \tilde{n}_{23}), \quad (n_{14}, m_5) = R(-\tilde{\nu}_5, \tilde{n}_{23}), \quad (23)$$

where $P, Q, R \in \mathbb{Z}$. This contributes as

$$a_5^{\text{typ}} \simeq \frac{2\pi}{r_{11}t_{12345}} \sum_{\tilde{n}_{23}, \tilde{r}_5 \in \mathbb{Z}} \sum_{N > 0} \sum_{P, Q, R, m \in \mathbb{Z}} \int_0^\infty dt \, t^{\frac{1}{2}} e^{-\pi t \left(N^2 t_{23}^2 L^2 + \frac{m^2}{r_{11}^2} + \left(\frac{p^2}{r_1^2} + \frac{Q^2}{r_4^2} + \frac{P^2}{r_5^2}\right) L^2\right)}$$
(24)

$$\simeq 2\pi \sum_{\tilde{n}_{23}, \tilde{\nu}_5 \in \mathbb{Z}} \sum_{N>0} \sum_{(P,Q,R,m) \neq (0,0,0,0)} \frac{1}{SL^2} e^{-2\pi NS}, \quad L = \sqrt{\tilde{\nu}_5^2 t_{145}^2 + \tilde{n}_{23}^2}, \tag{25}$$

$$S = \sqrt{P^2 t_{123}^2 + Q^2 t_{234}^2 + R^2 t_{235}^2 + m^2 \left(\tilde{n}_{23}^2 (r_{11} t_{23})^2 + \tilde{\nu}_5^2 (r_{11} t_{12345})^2 \right)} \,.$$