

Triggering Discoveries in High Energy Physics III
9–13 December 2024, Vysoké Tatry, Slovakia

Searching for saturation with large- $|t|$ incoherent J/ψ production at the LHC

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Czech Technical University in Prague

Cepila, JGC, Matas, Ridzikova, PLB 852 (2024) 138613

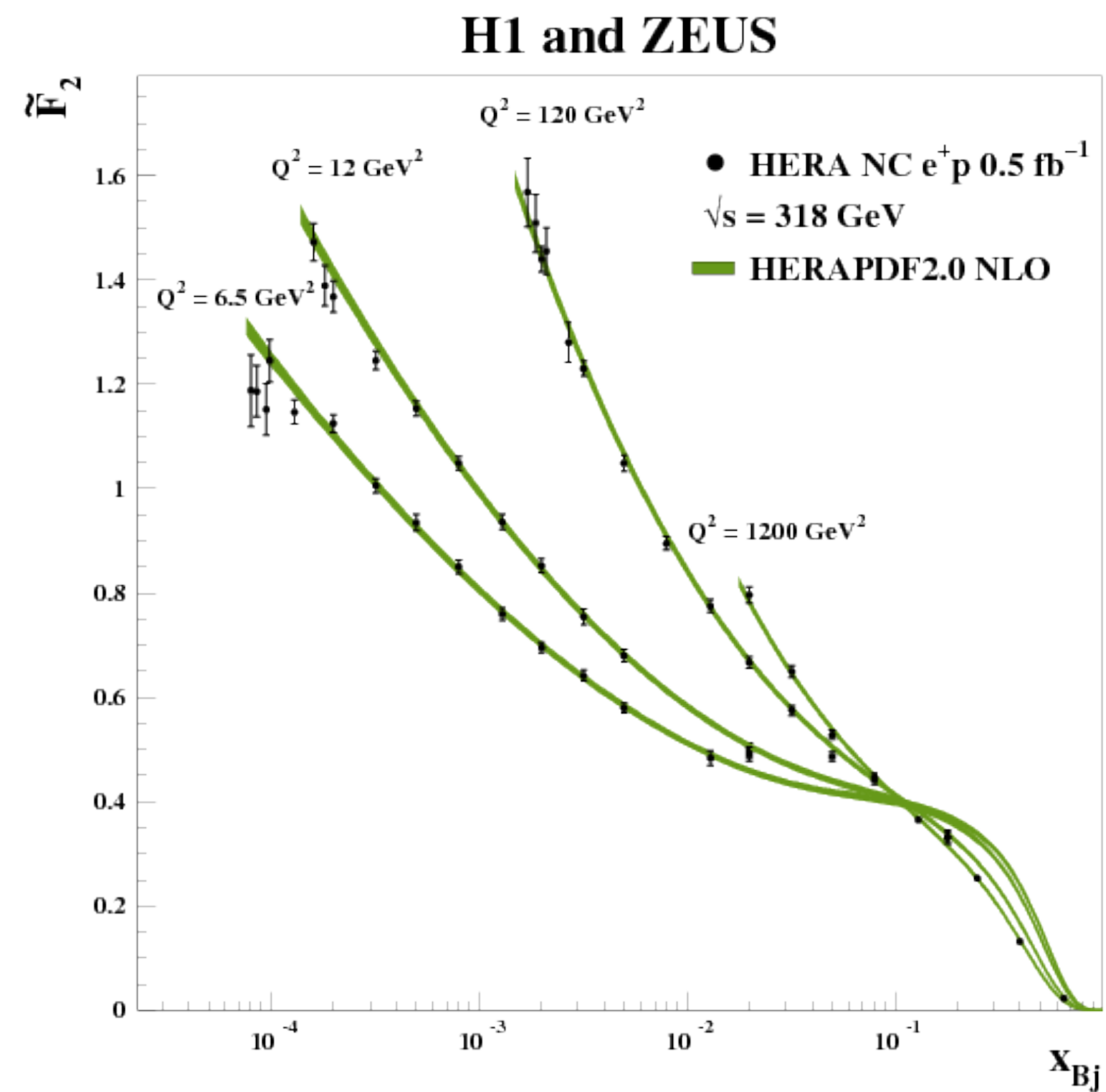


Saturation in QCD

The gluons in the proton

Deep-inelastic scattering

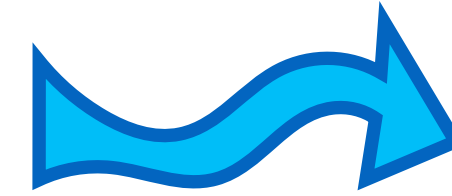
The structure function of the proton grows rapidly at small Bjorken x



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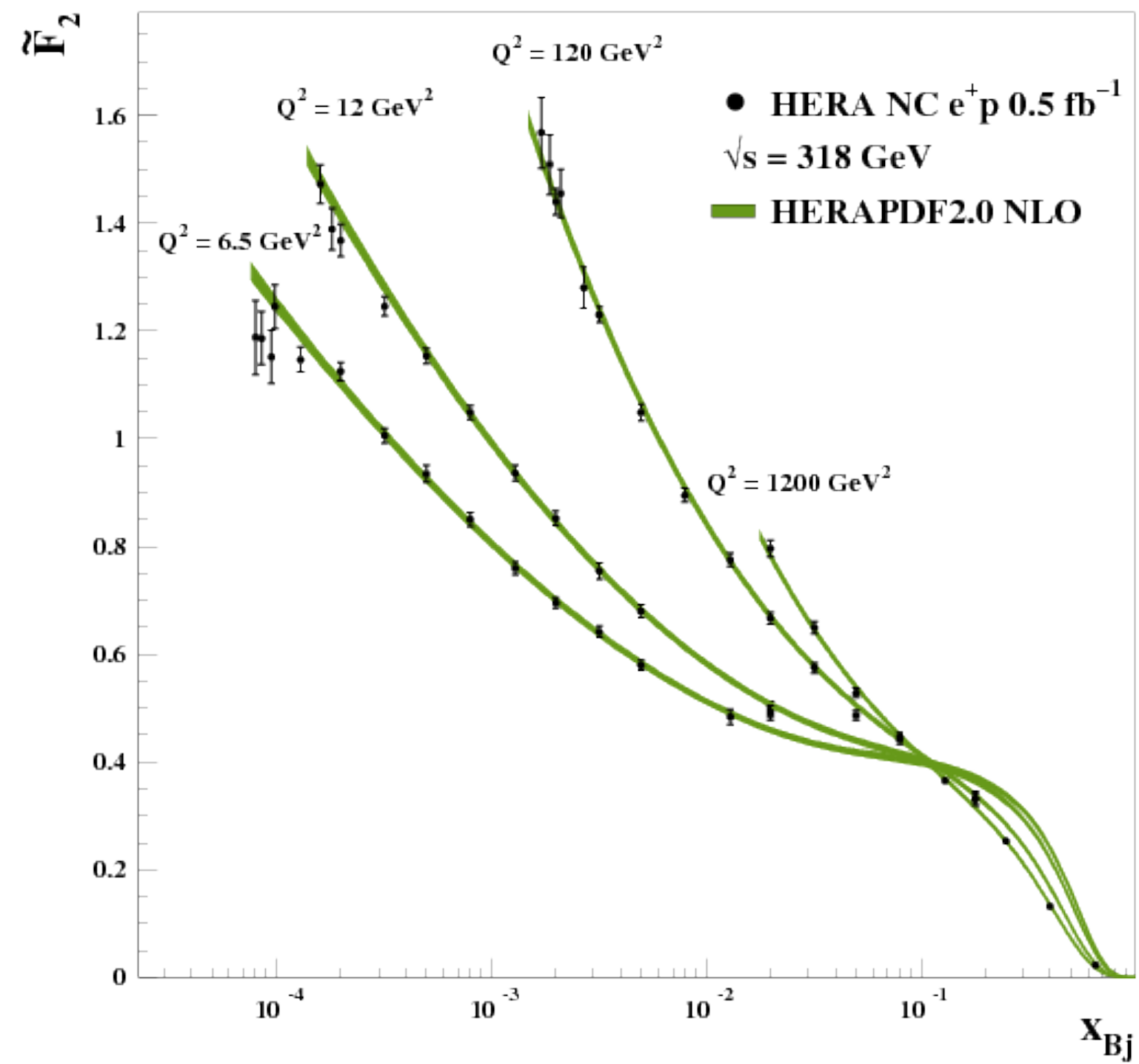
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Quantum chromodynamics

The proton can be seen as formed by **quasi-free** partons: quarks and gluons

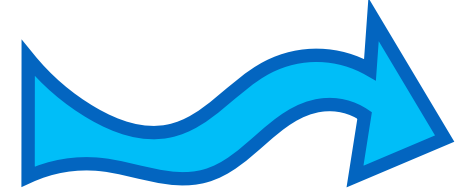
H1 and ZEUS



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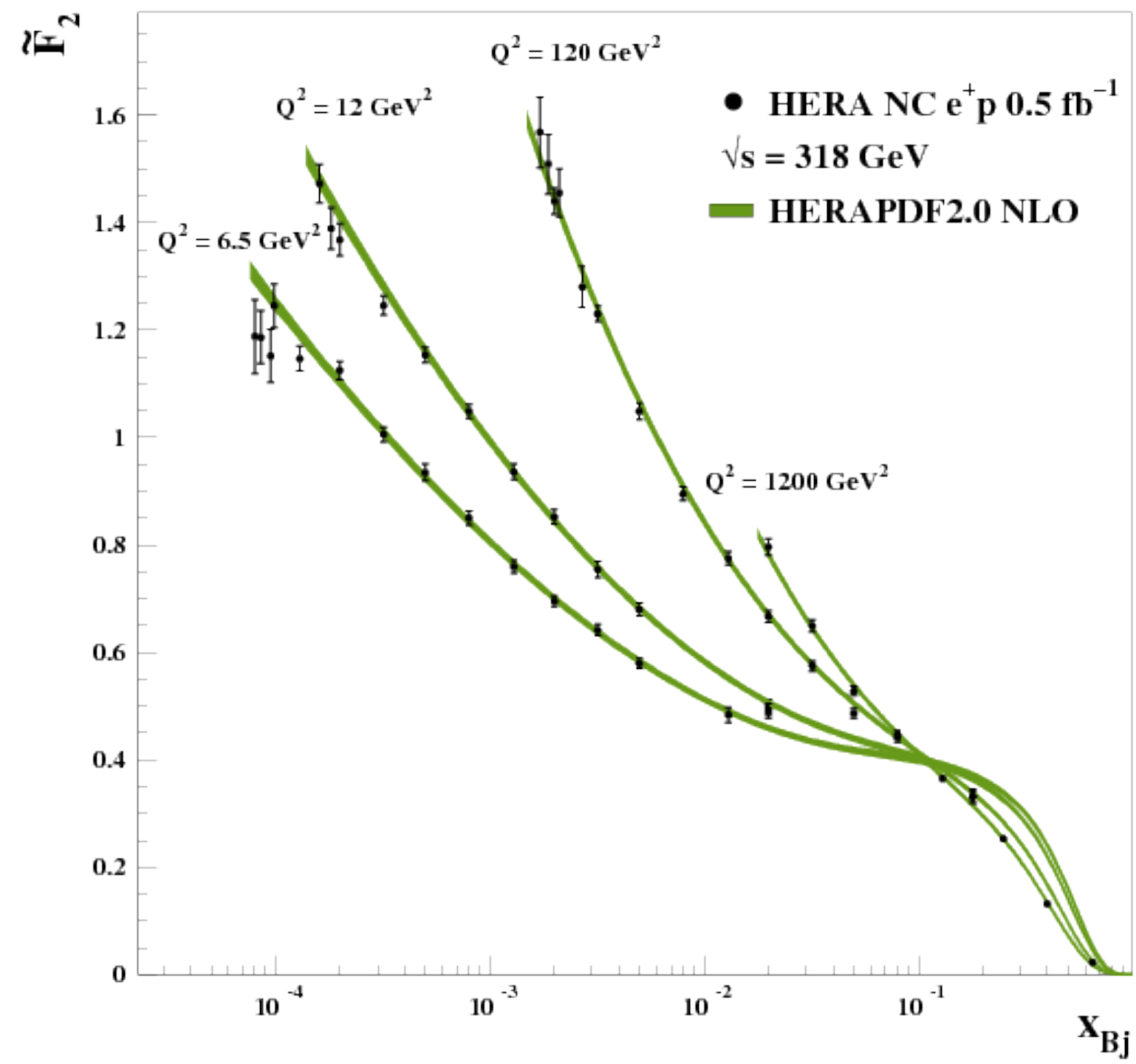
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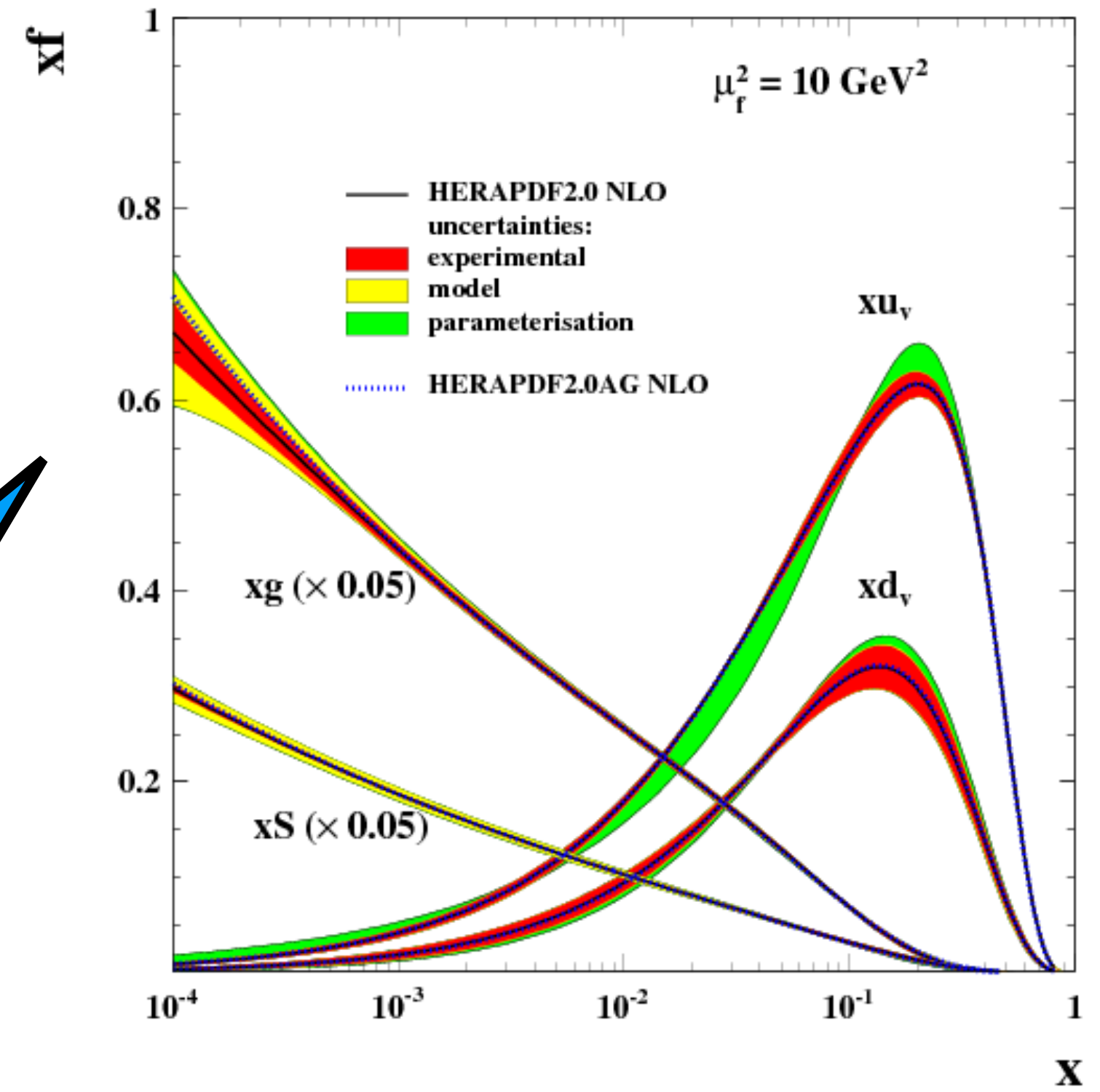
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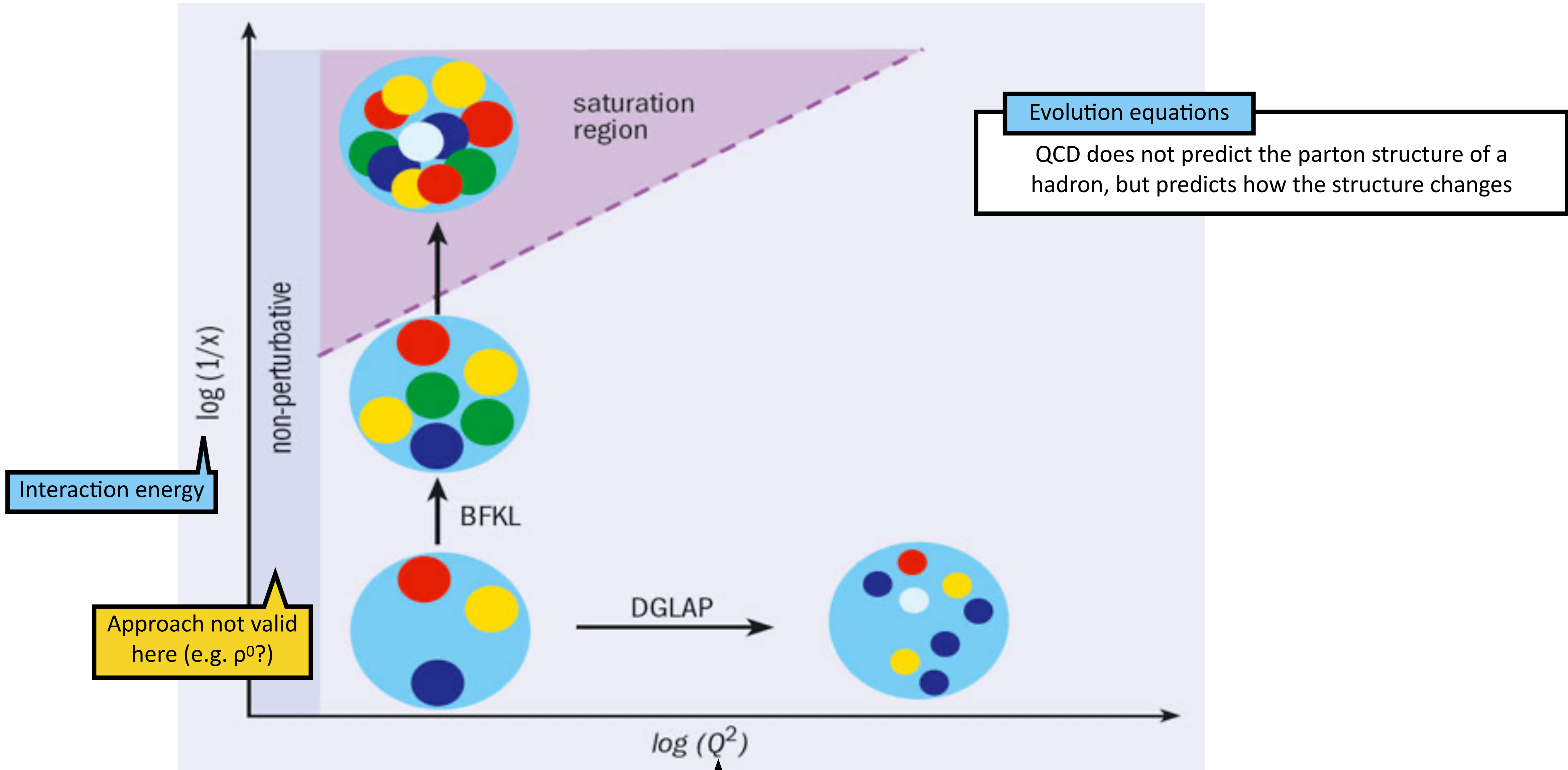


At small Bjorken-x the proton is mainly made of gluons

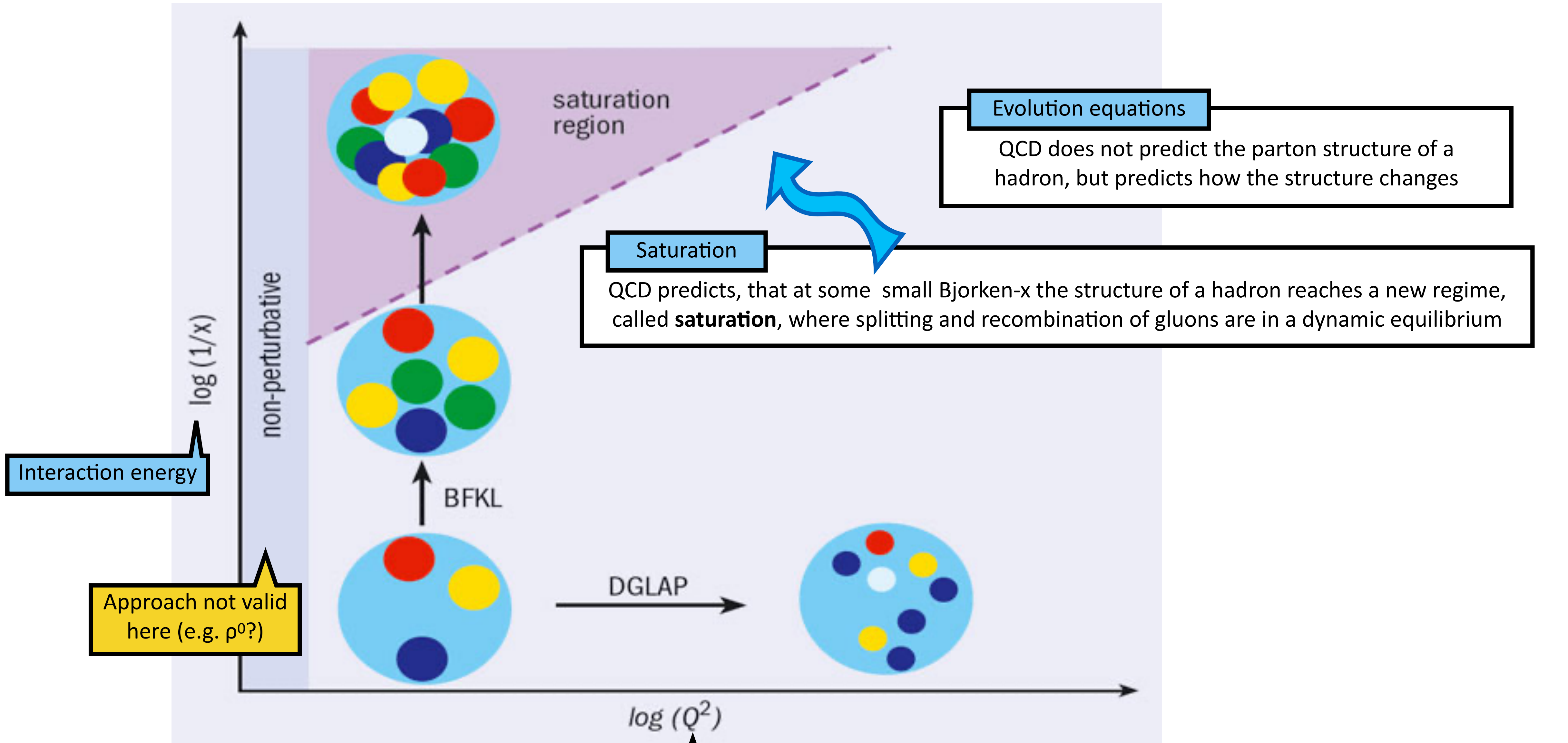
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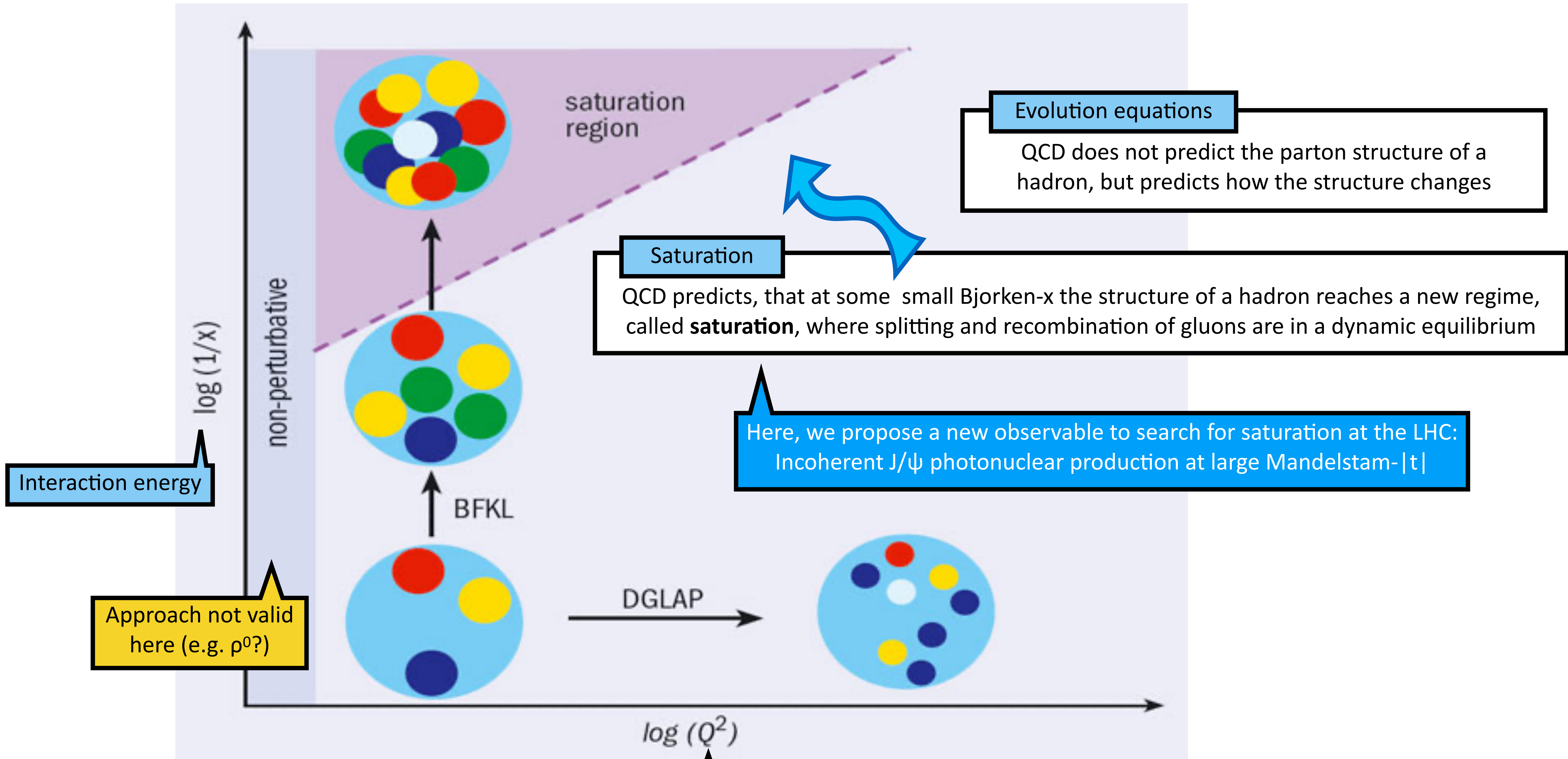
Gluon saturation in QCD



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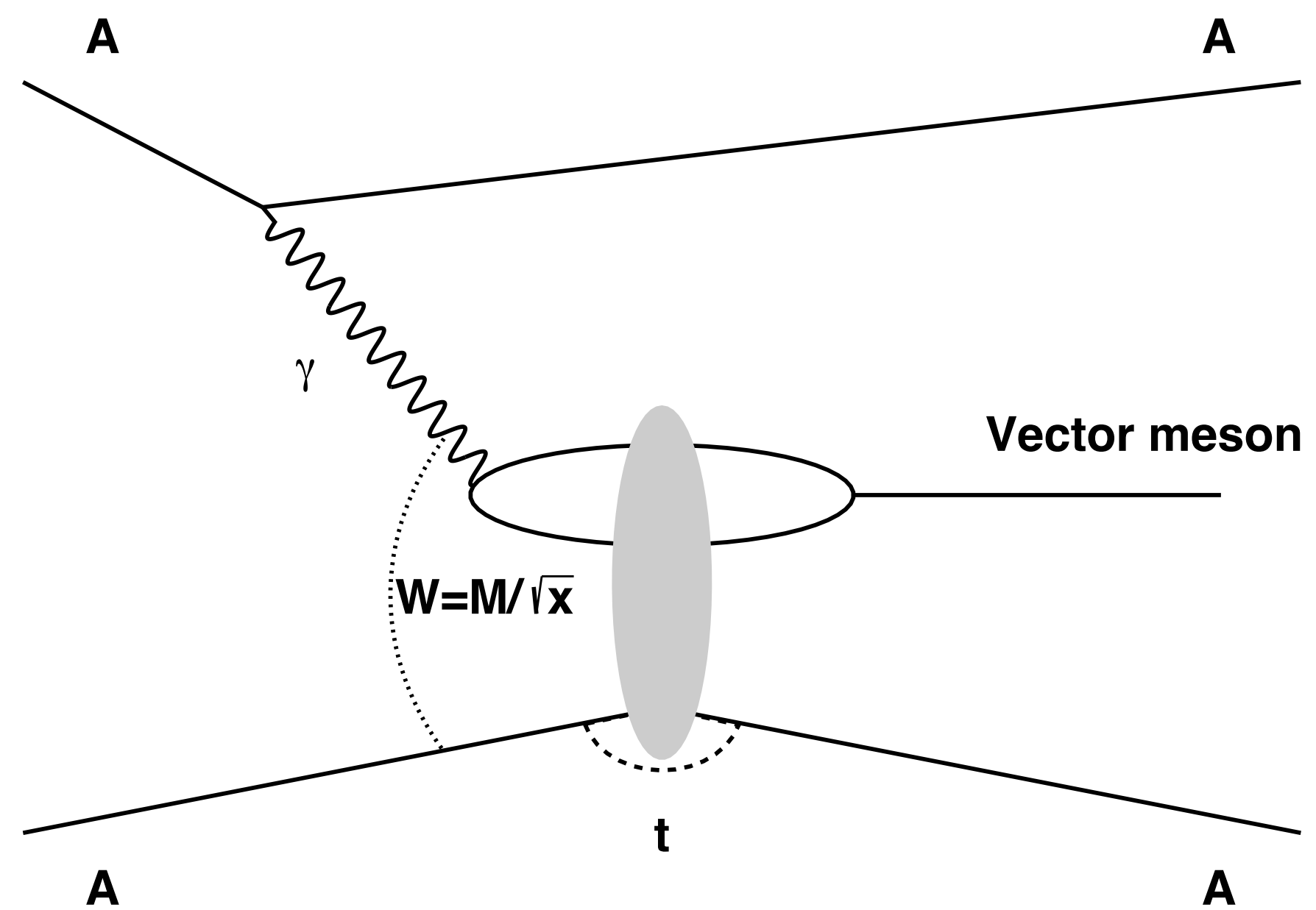


Gluon saturation in QCD

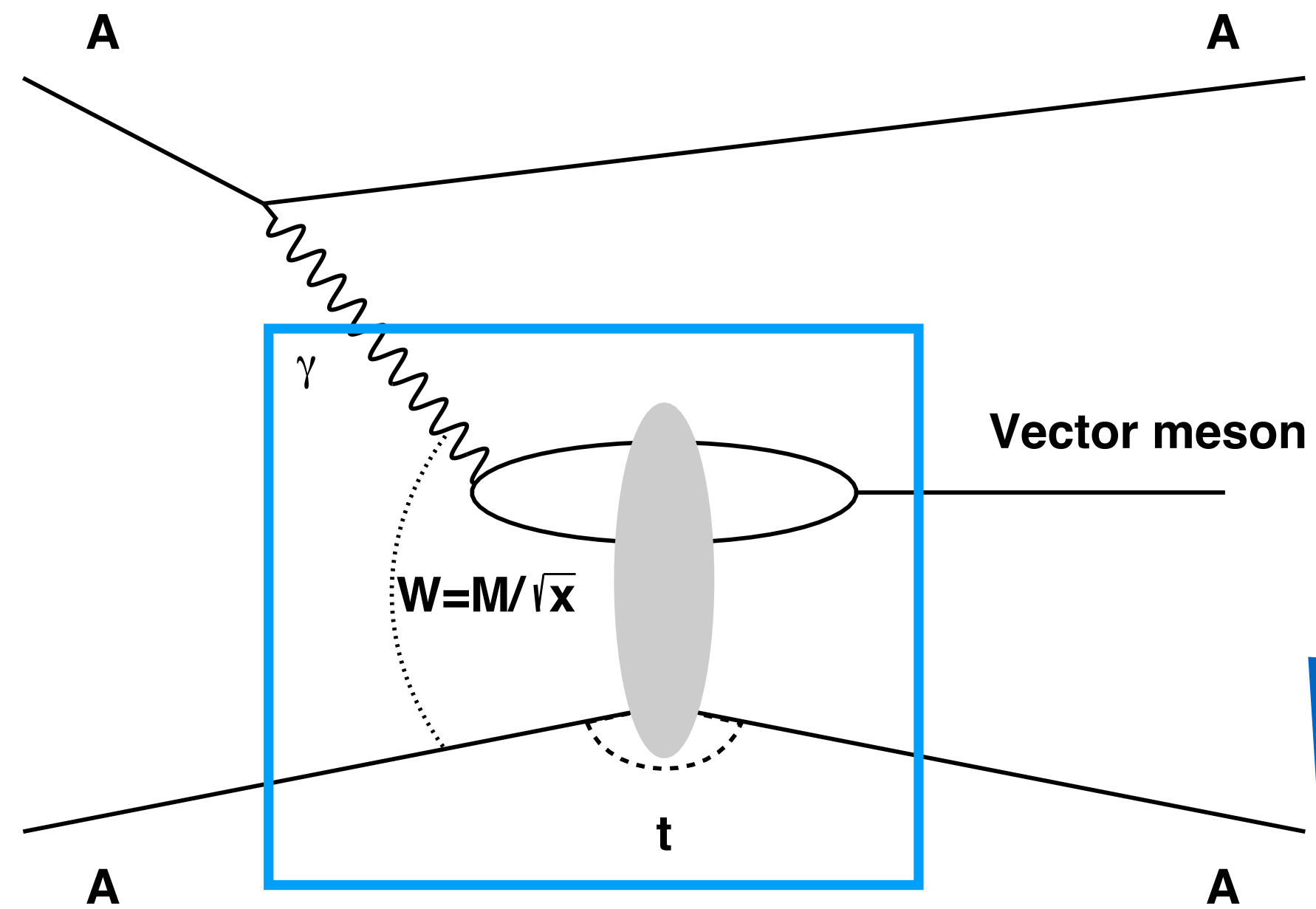


The formalism

Diffractive vector meson photoproduction



Diffractive vector meson photoproduction

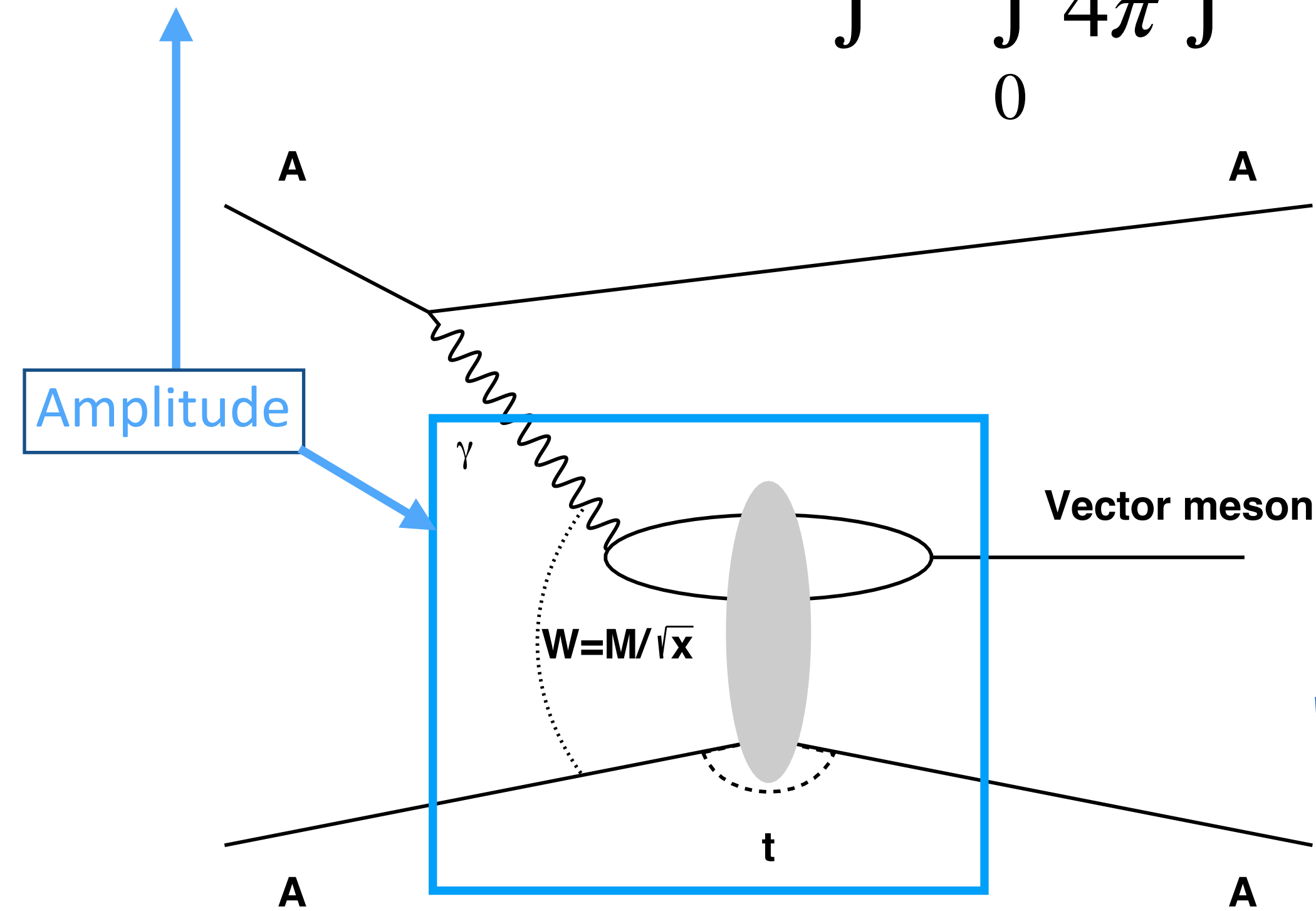


Dipole picture

The photon fluctuates into a long-lived quark-antiquark colour dipole which interacts with the hadronic target and then creates a vector meson

Diffractive vector meson photoproduction

$$\mathcal{A}_{T,L}(x, Q^2, \vec{\Delta}) = i \int d\vec{r} \int_0^1 \frac{dz}{4\pi} \int d\vec{b} |\Psi_\gamma^* \Psi_V|_{T,L} \exp \left[-i \left(\vec{b} - \left(\frac{1}{2} - z \right) \vec{r} \right) \cdot \vec{\Delta} \right] \frac{d\sigma_H^{\text{dip}}}{d\vec{b}}$$



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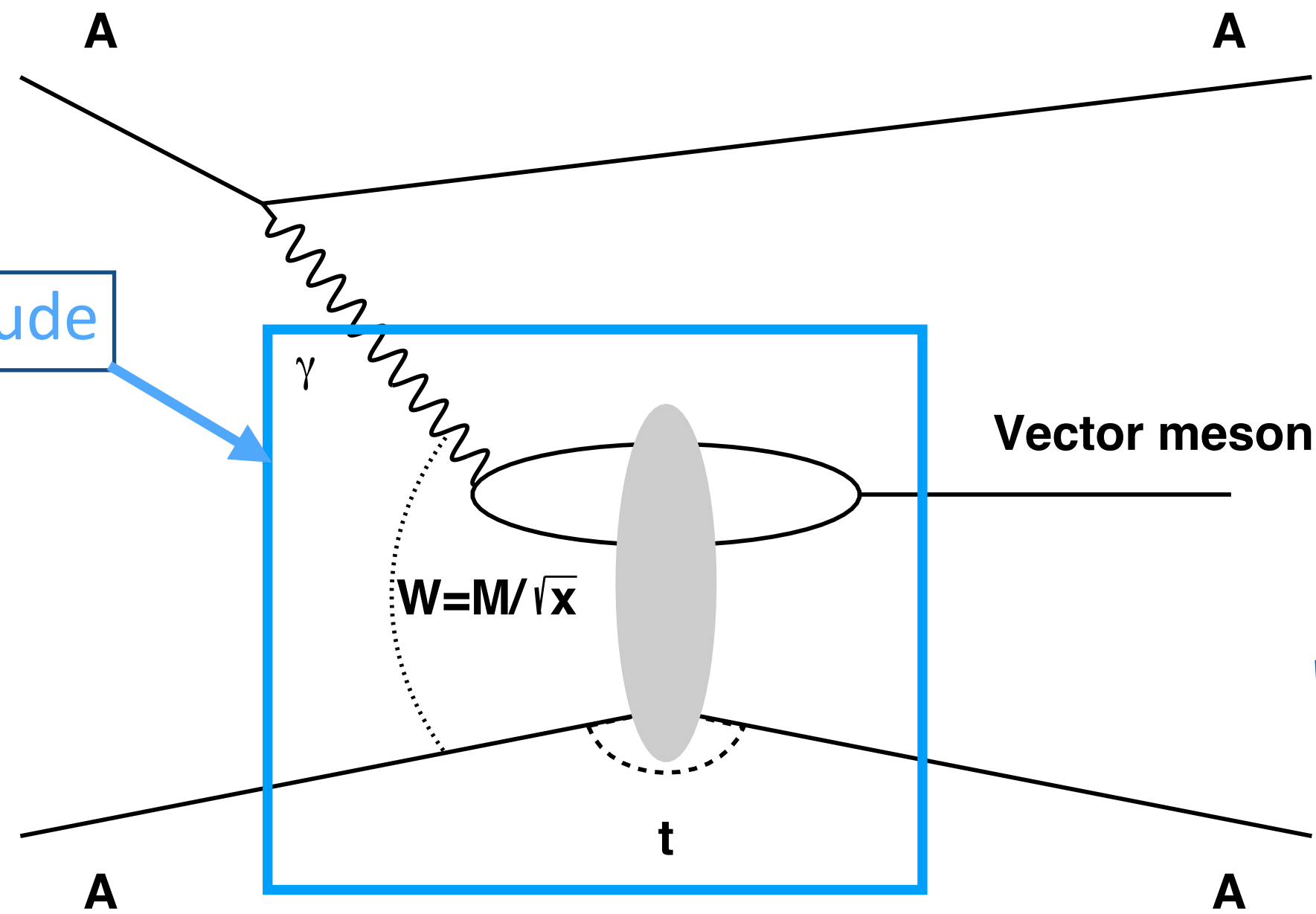
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$\Delta^2 = -t$

Amplitude



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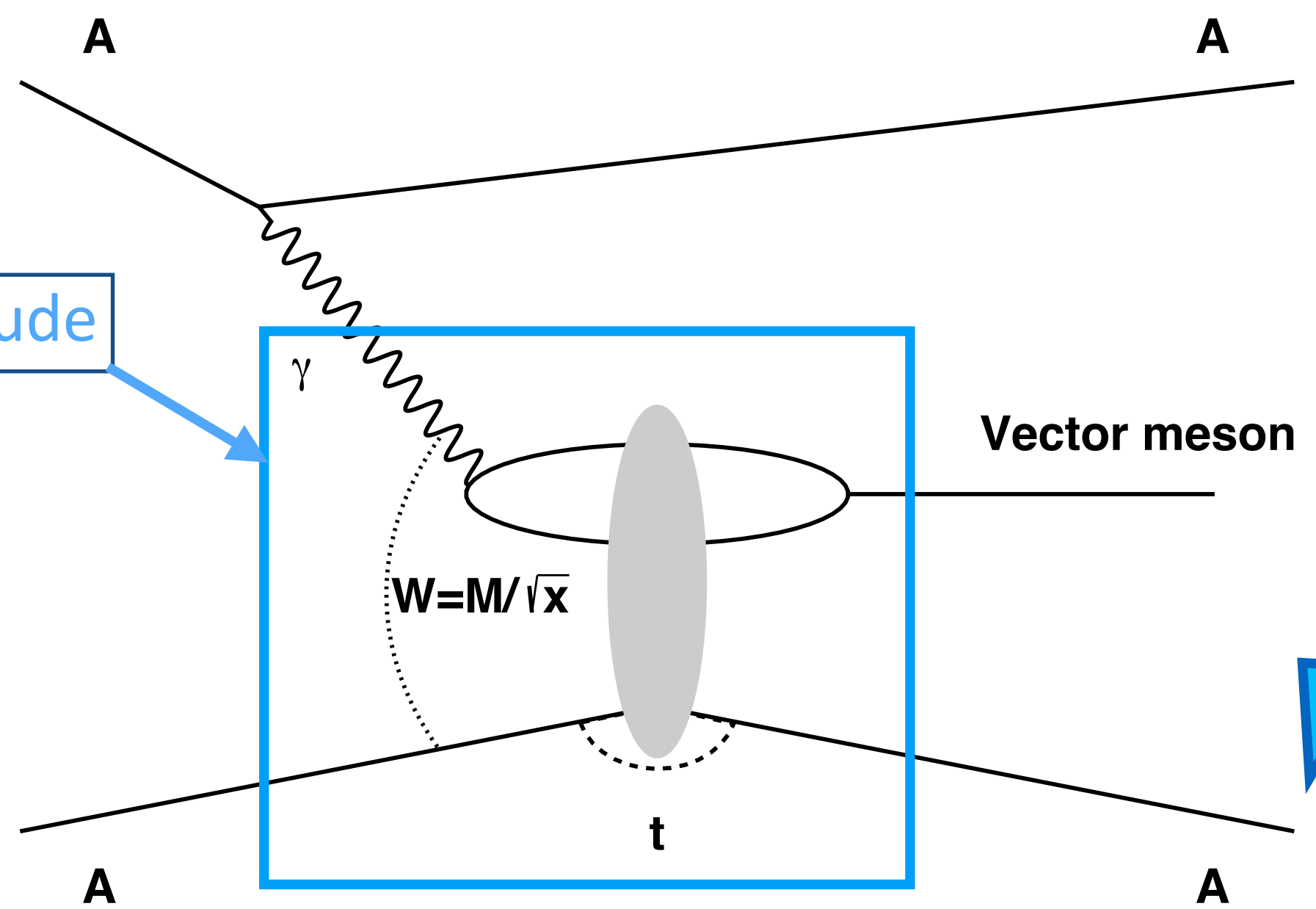
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Dipole size

Quark energy fraction

Amplitude



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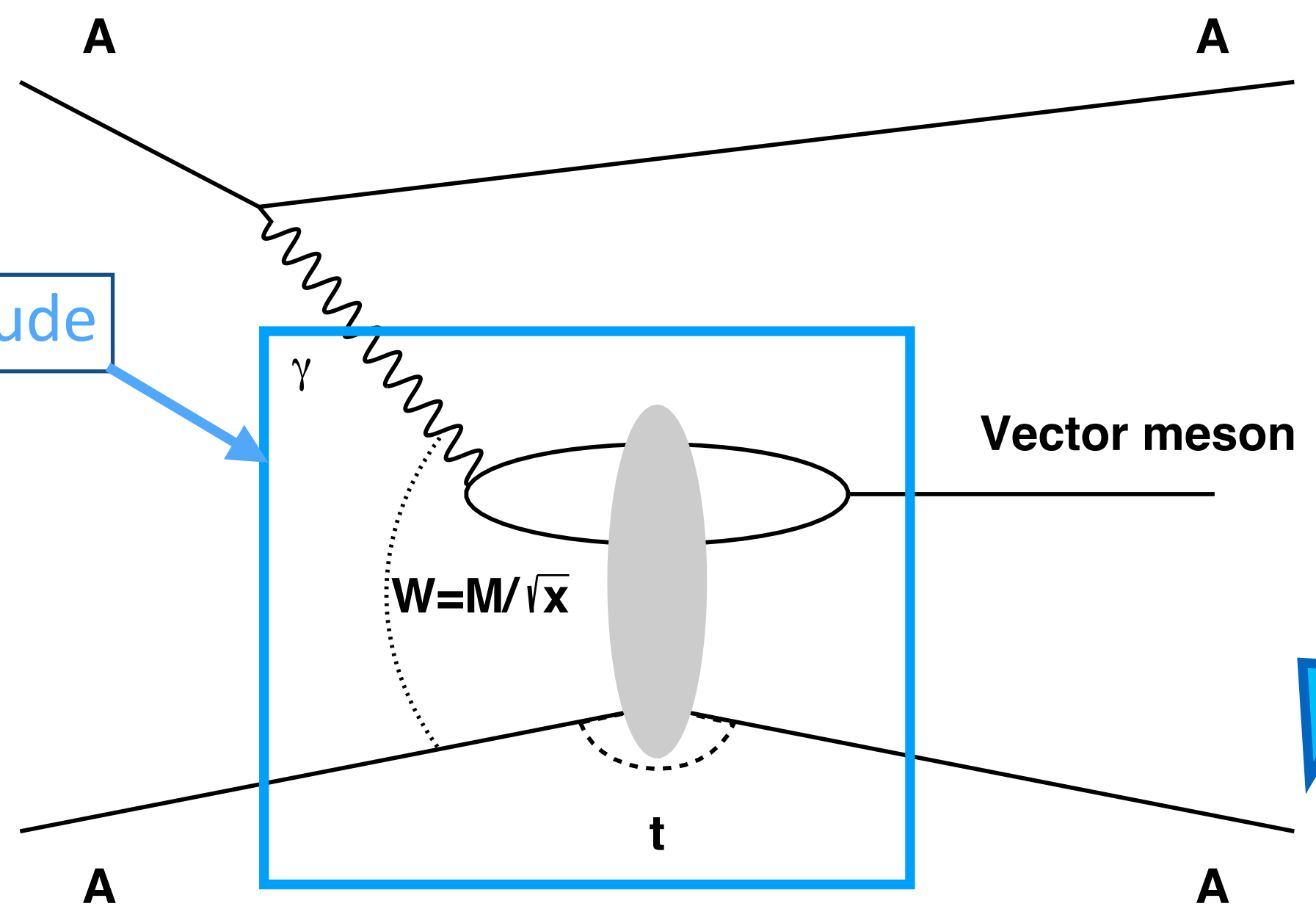
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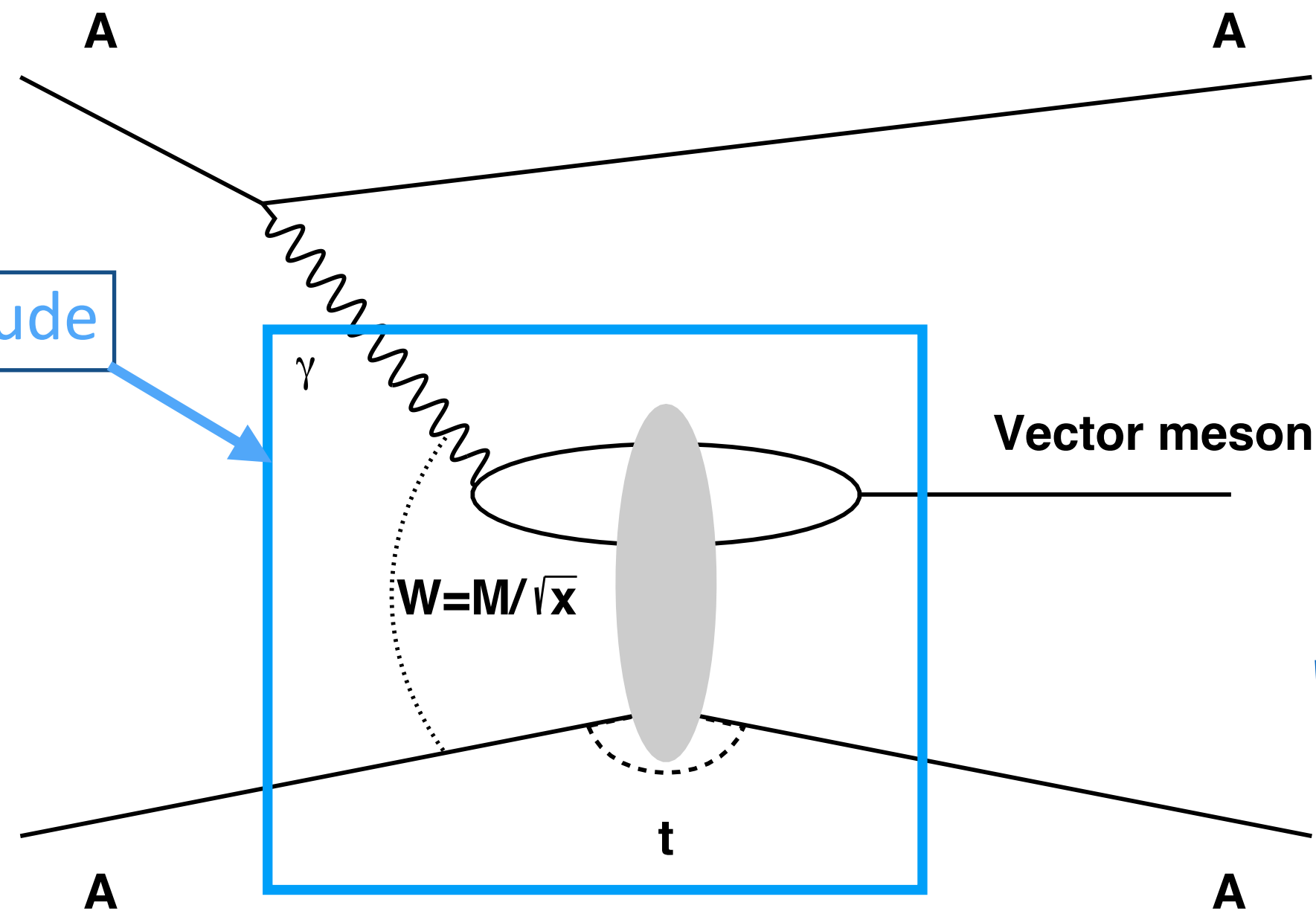
Dipole size

Quark energy fraction

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Photon-dipole wave function

Vector meson wave function

Dipole picture

The photon fluctuates into a long-lived quark-antiquark colour dipole which interacts with the hadronic target and then creates a vector meson

Amplitude

Vector meson

$W = M/\sqrt{x}$

t

A

A

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Impact parameter

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$$\frac{d\sigma_H^{\text{dip}}}{d\vec{b}}$$

Photon-dipole wave function

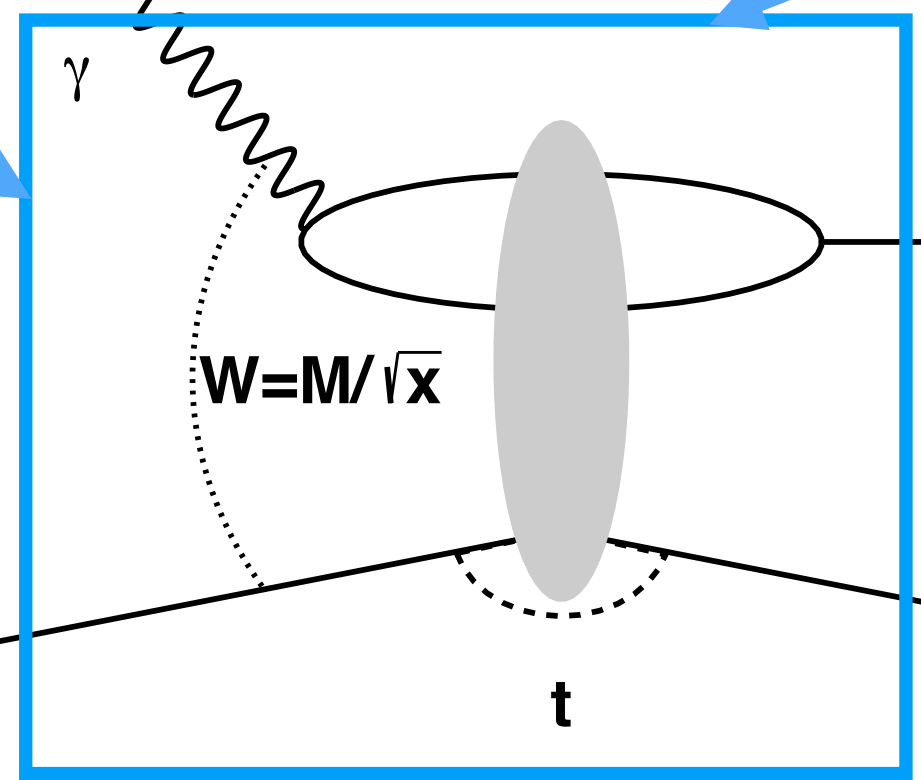
Dipole-hadron cross section, our knowledge of pQCD is encoded here

Vector meson wave function

Dipole picture

The photon fluctuates into a long-lived quark-antiquark colour dipole which interacts with the hadronic target and then creates a vector meson

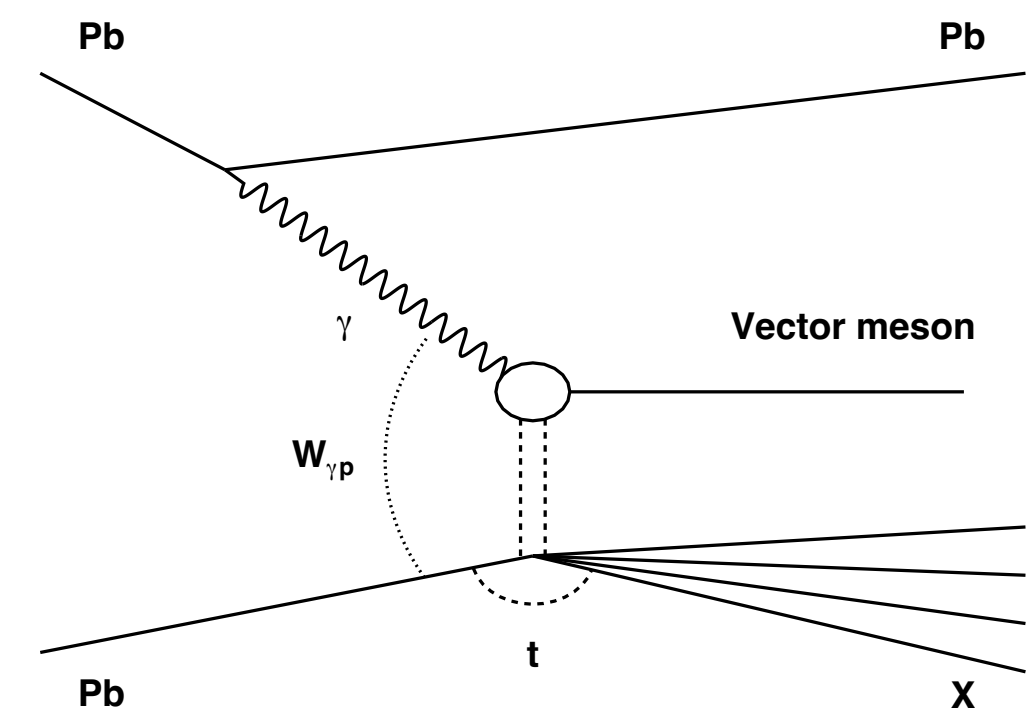
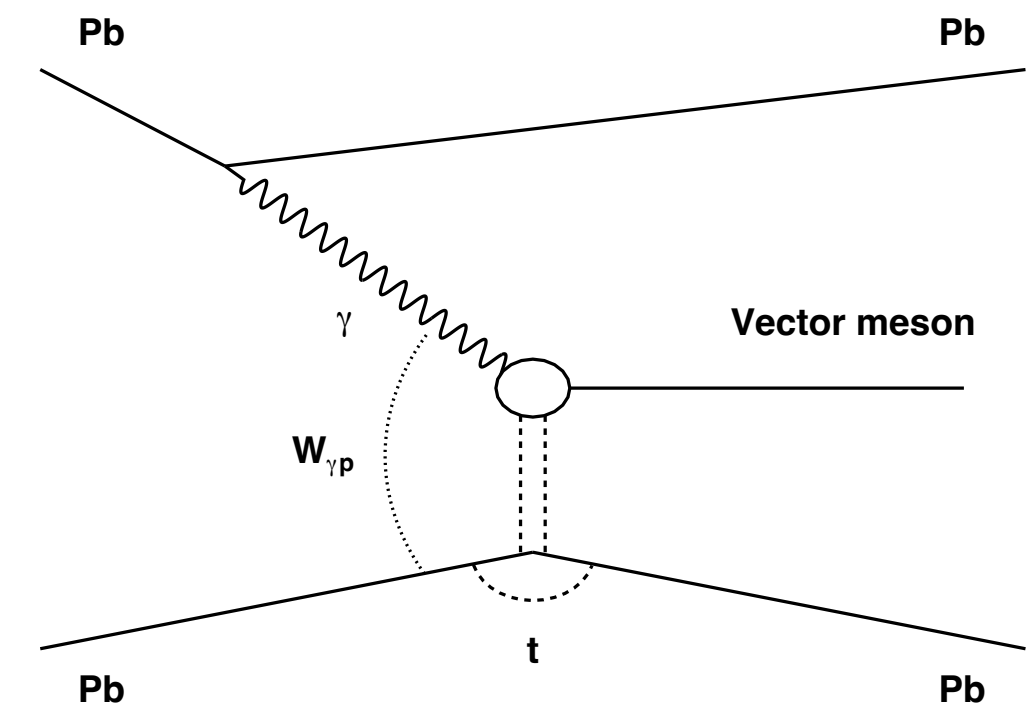
Amplitude



Vector meson

The Good-Walker picture of vector meson photoproduction

Coherent (Exclusive)



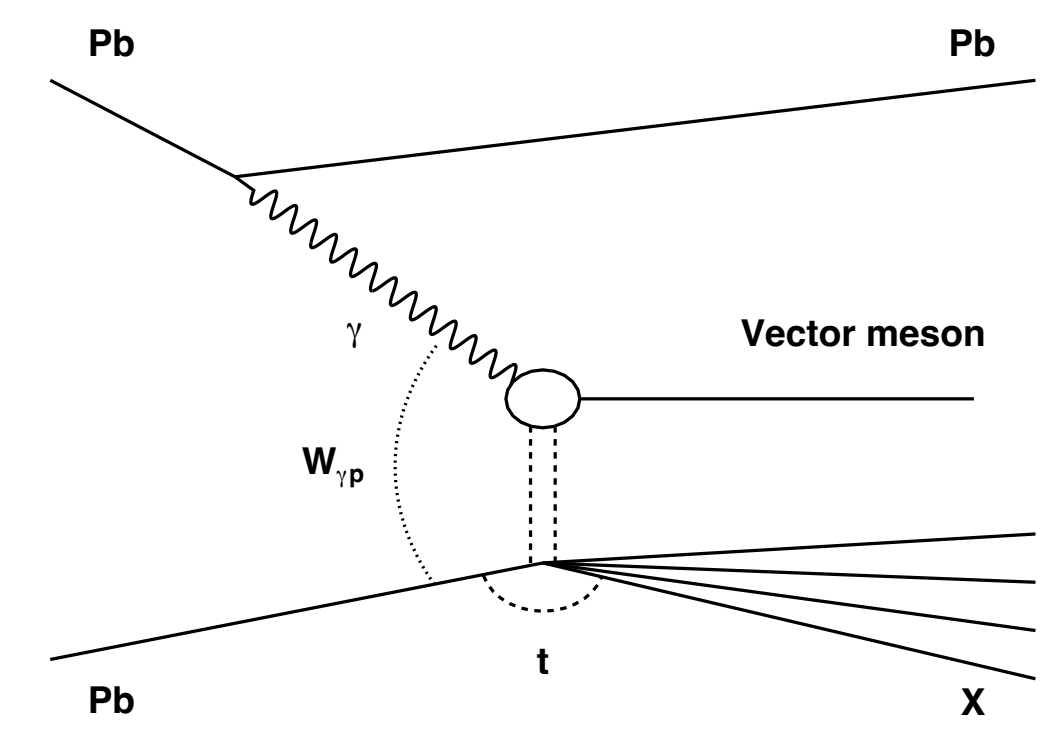
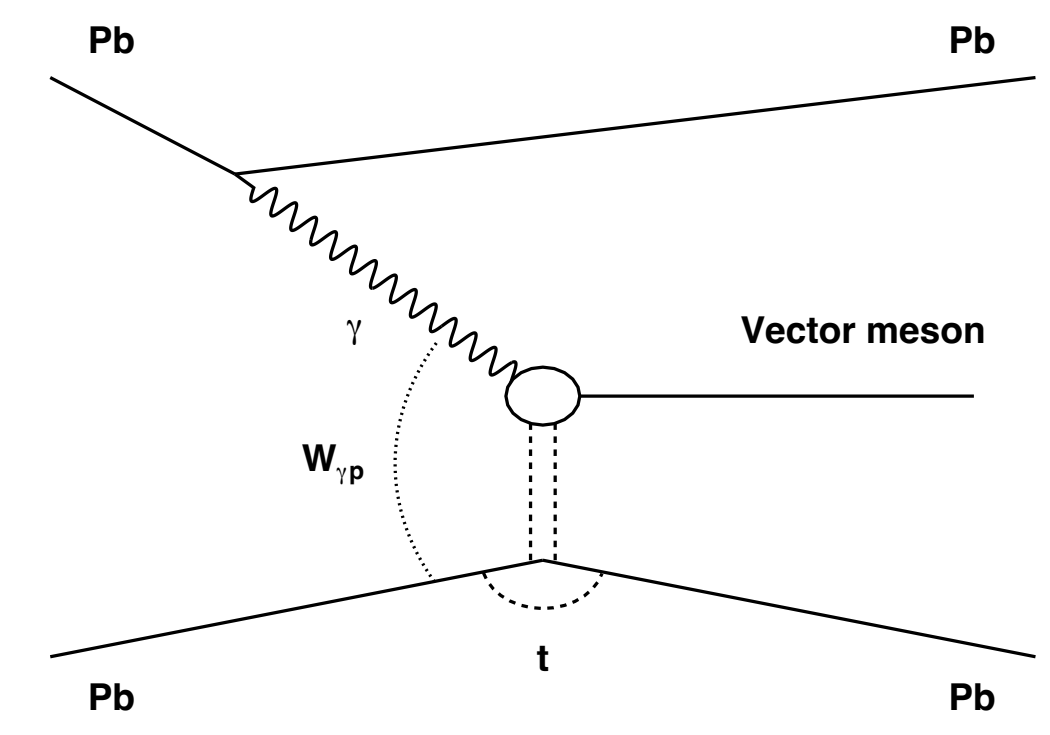
Incoherent (Dissociative)

The Good-Walker picture of vector meson photoproduction

Average over colour configurations

$$\left. \frac{d\sigma^{\gamma^*H \rightarrow VH}}{d|t|} \right|_{T,L} = \frac{\left(R_g^{T,L}\right)^2}{16\pi} \left| \langle \mathcal{A}_{T,L} \rangle \right|^2$$

Coherent (Exclusive)



Incoherent (Dissociative)

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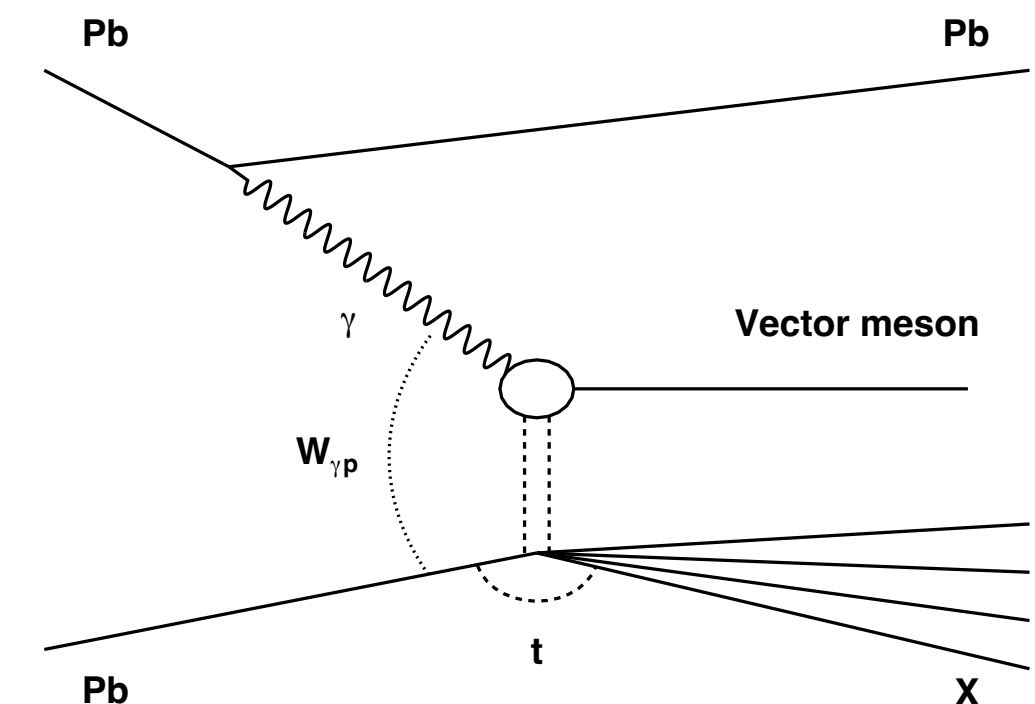
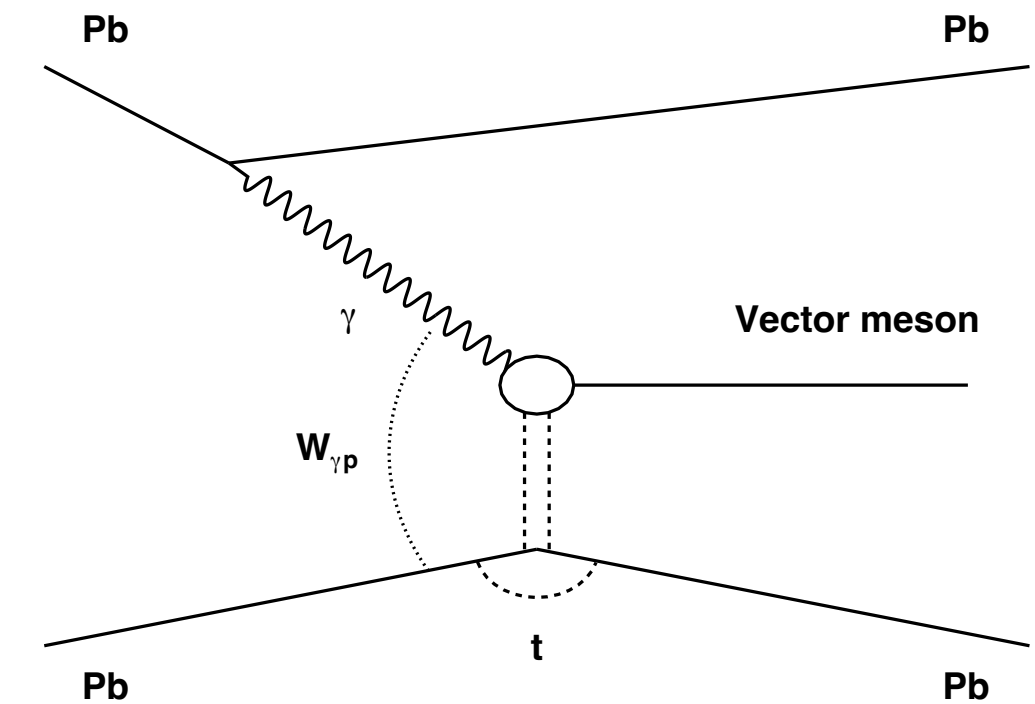
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Variance over colour configurations

$$\left. \frac{d\sigma^{\gamma^*p \rightarrow VY}}{d|t|} \right|_{T,L} = \frac{(R_g^{T,L})^2}{16\pi} \left(\langle |\mathcal{A}_{T,L}|^2 \rangle - |\langle \mathcal{A}_{T,L} \rangle|^2 \right)$$

Coherent (Exclusive)



Incoherent (Dissociative)

The Good-Walker picture of vector meson photoproduction

Average over colour configurations

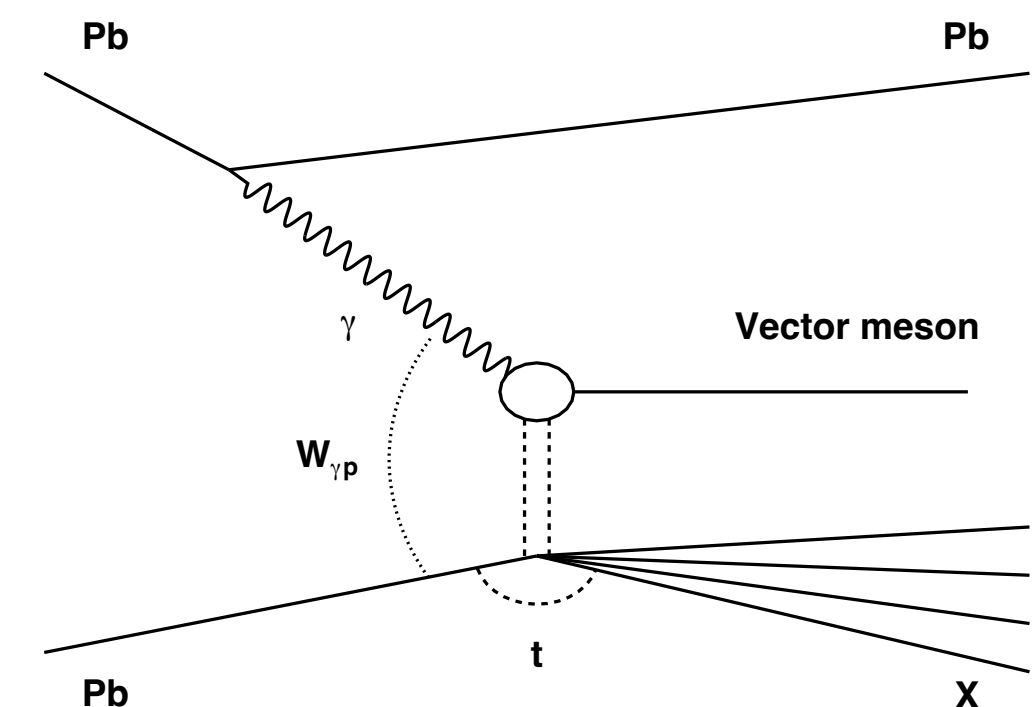
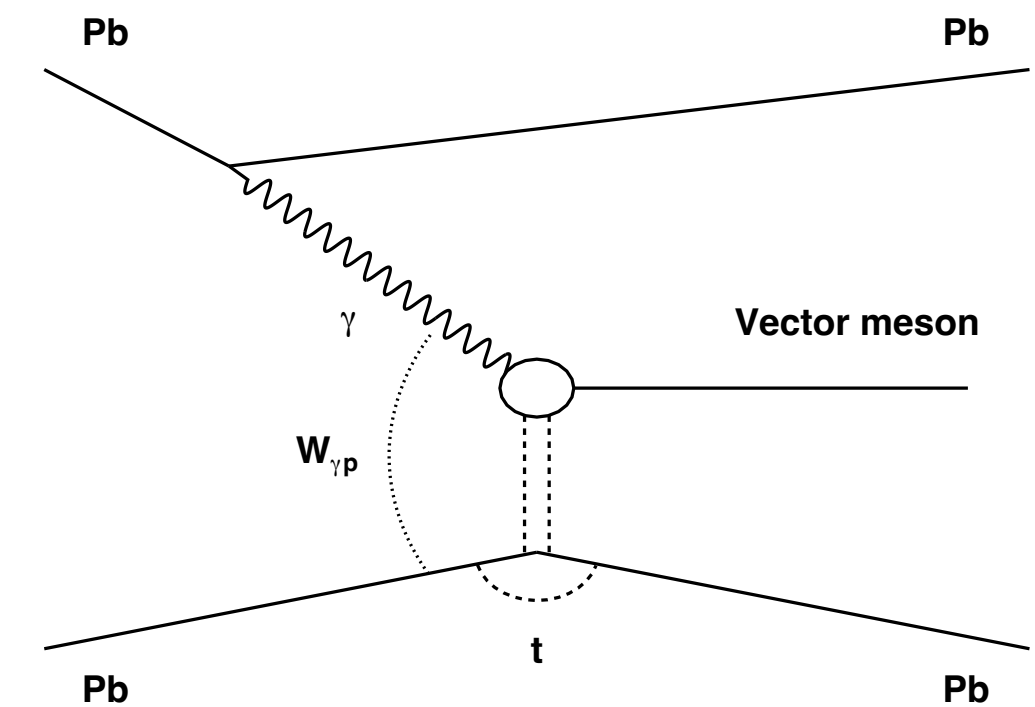
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How to include different configurations in the dipole-hadron cross section?

Coherent (Exclusive)



Incoherent (Dissociative)

The energy-dependent hot-spot model

The dipole cross section in the energy-dependent hot-spot model

Ansatz

The Bjorken- x and impact-parameter dependence of the γp cross section are factorised

The dipole cross section in the energy-dependent hot-spot model

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The Bjorken- x and impact-parameter dependence of the γp cross section are factorised

$$\frac{d\sigma_p^{\text{dip}}}{d\vec{b}} = \sigma_0 N(x, r) T_p(\vec{b})$$

Target profile

The dipole-target amplitude

The dipole cross section in the energy-dependent hot-spot model

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Target profile

Different configurations are taken into account in the profile distribution

The dipole-target amplitude

The dipole amplitude in the energy-dependent hot-spot model

GBW model

$$N(x, r) = \left[1 - \exp\left(-\frac{r^2 Q_s^2(x)}{4}\right) \right]$$

The dipole amplitude in the energy-dependent hot-spot model

GBW model

Saturation scale

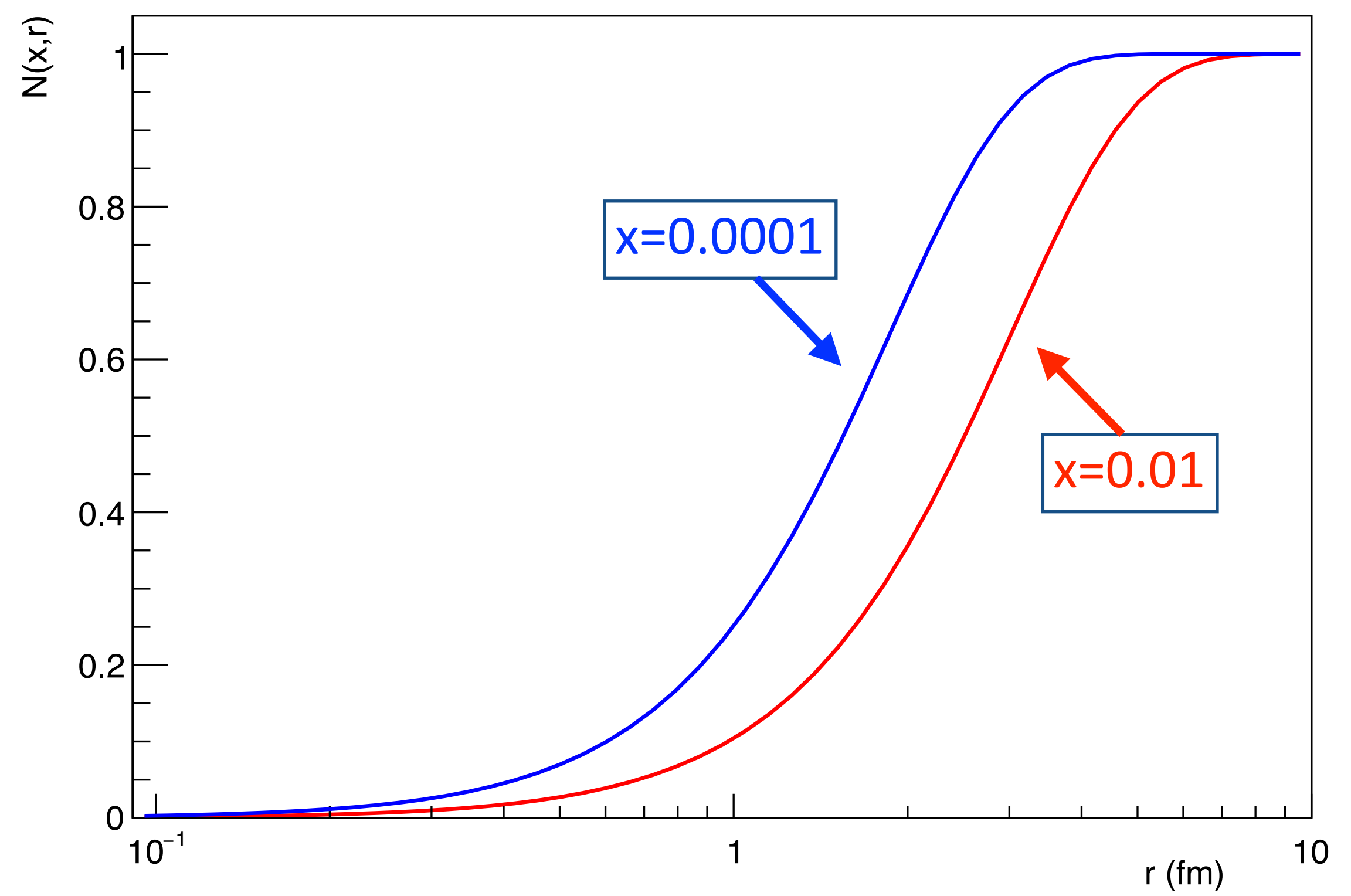
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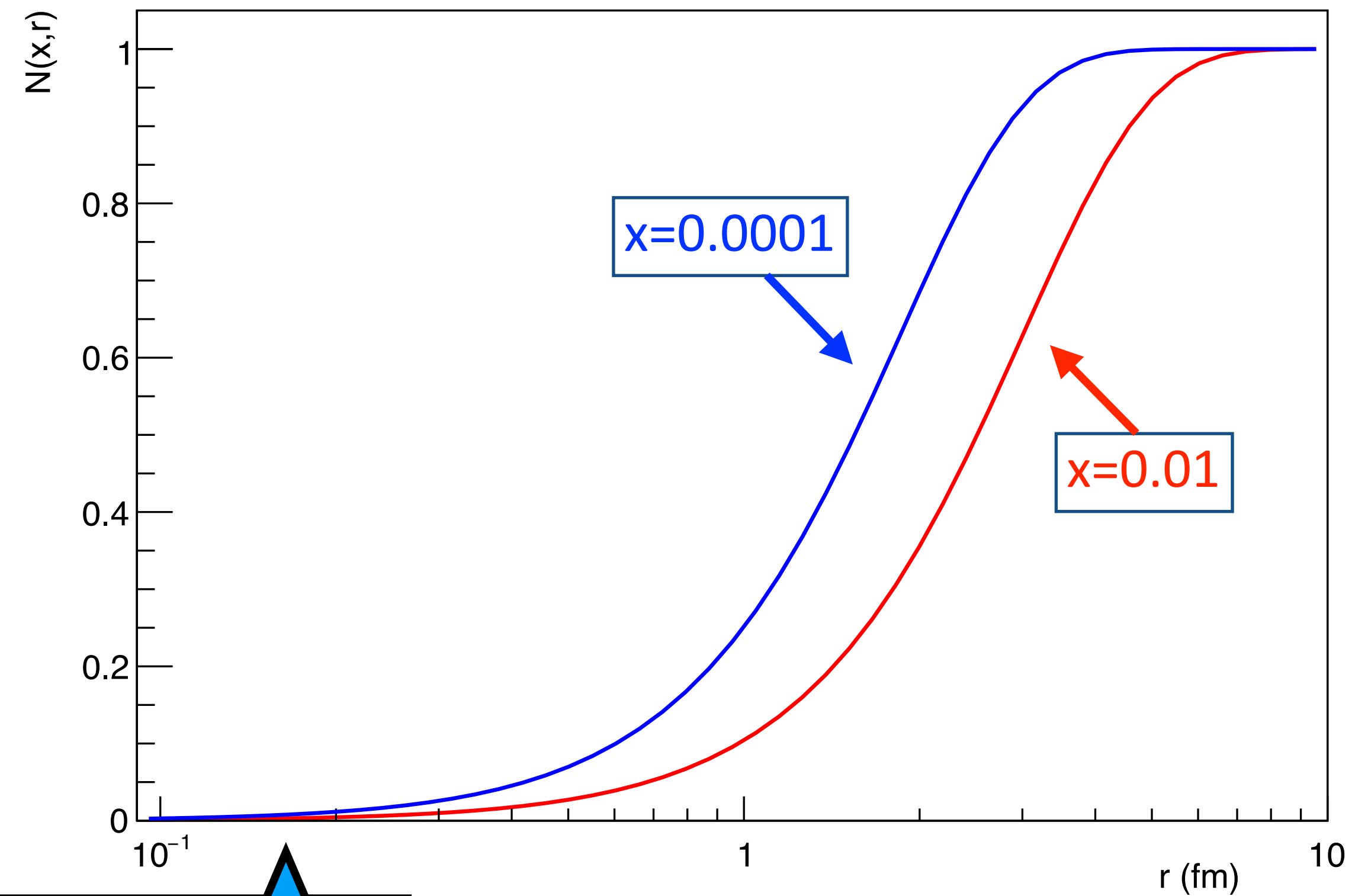


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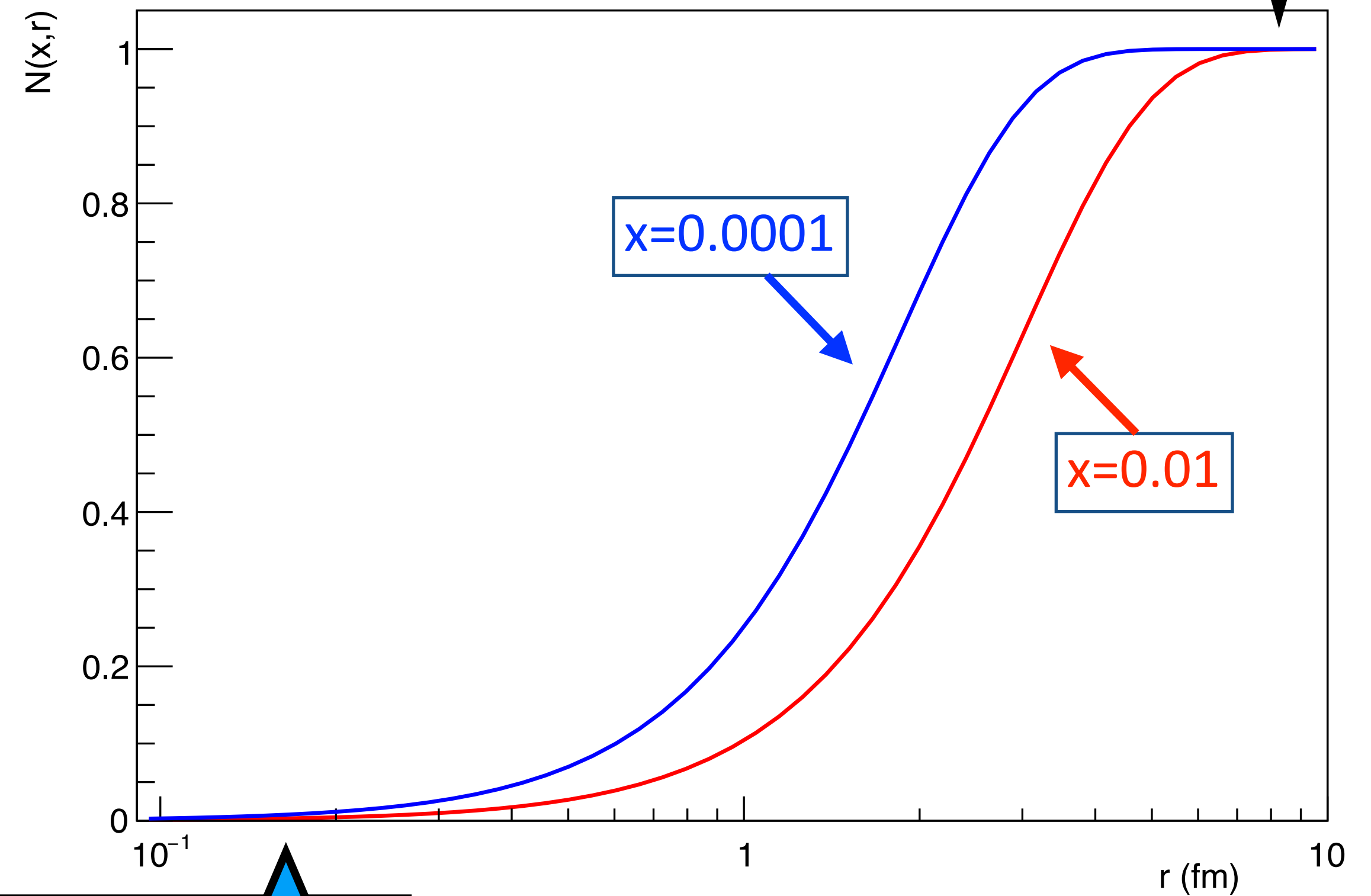
For small values of r ,
 N goes to zero

The dipole amplitude in the energy-dependent hot-spot model

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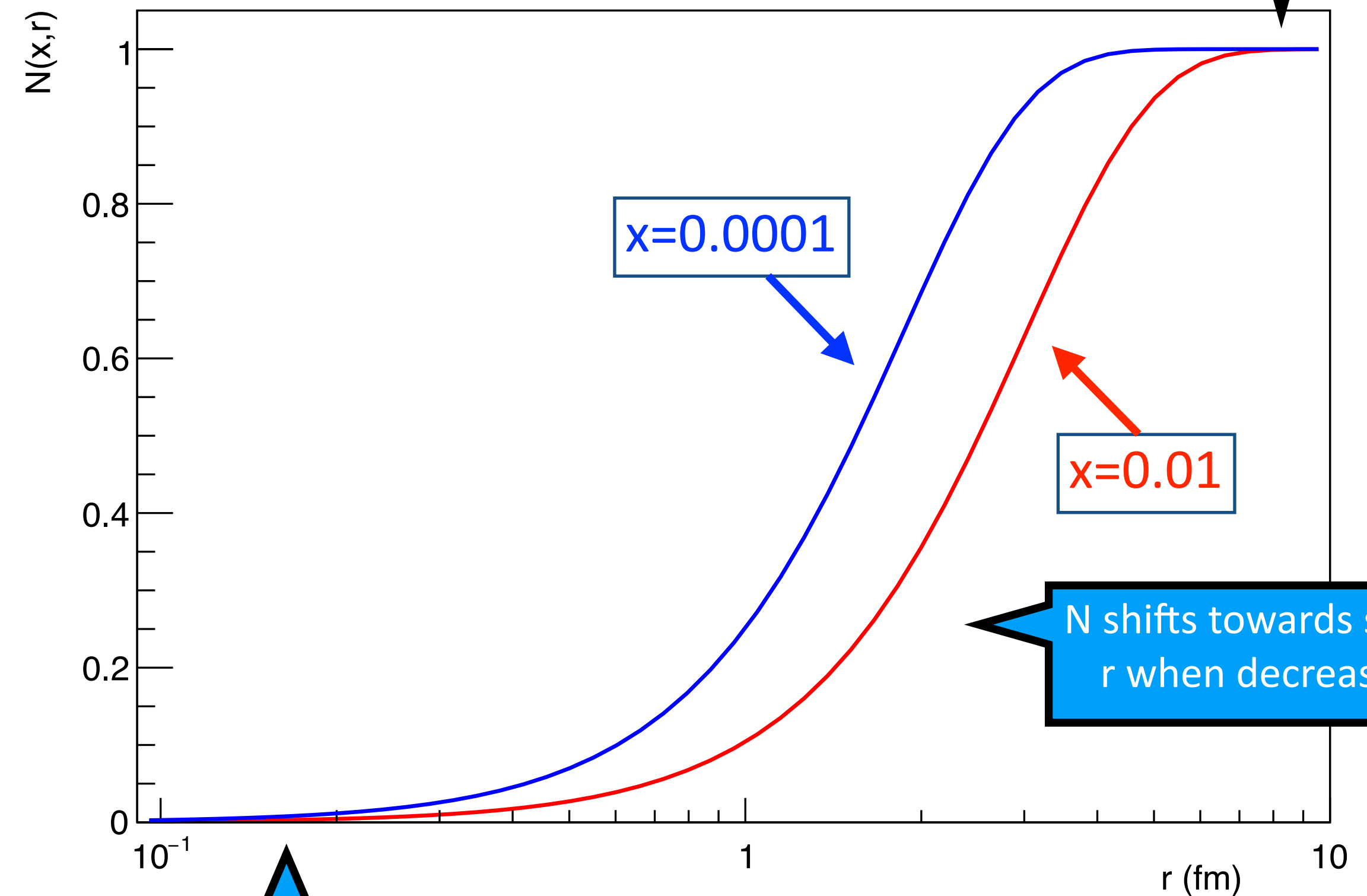
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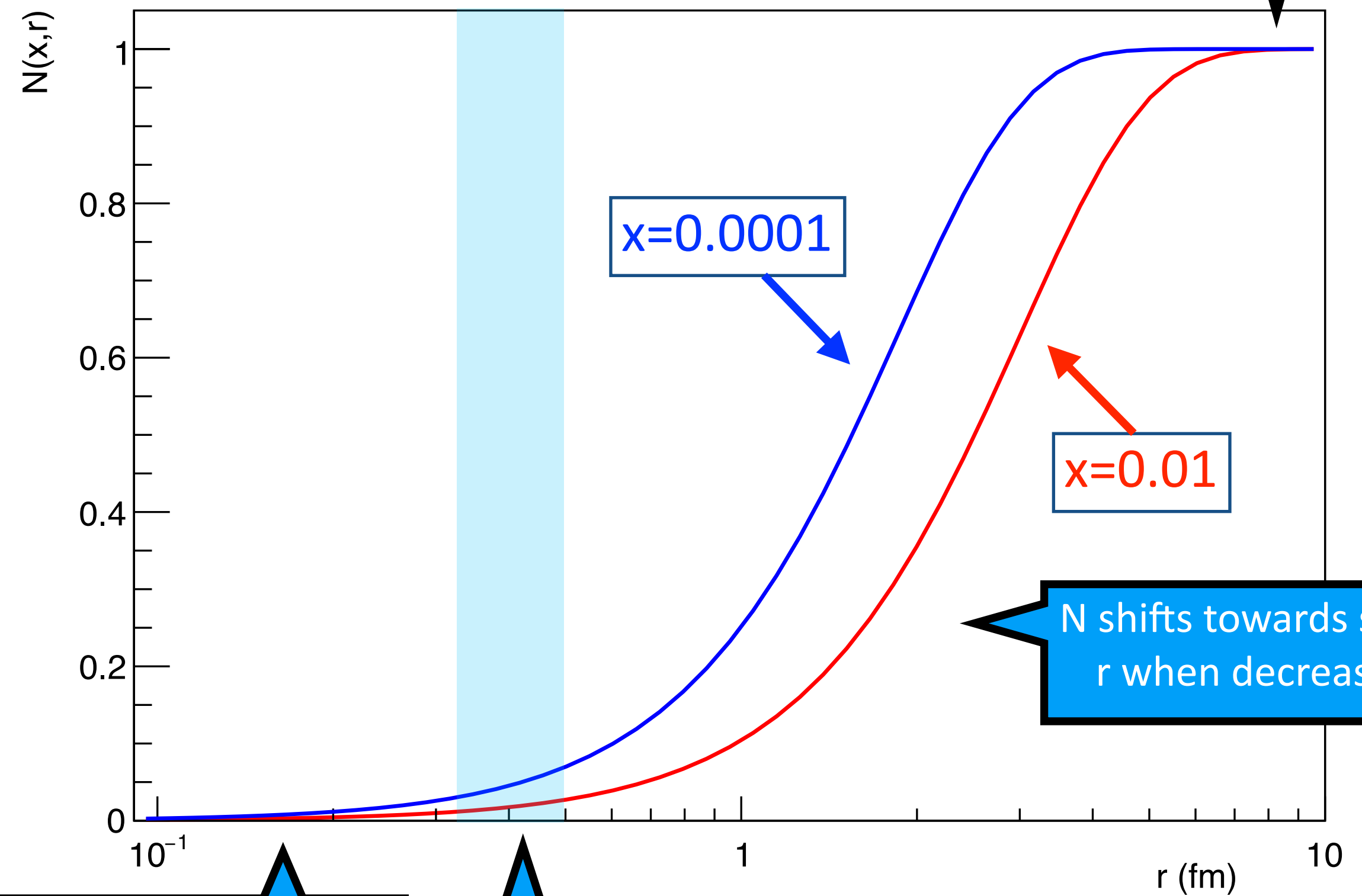


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GBW model

Saturation scale

$$N(x, r) = \left[1 - \exp\left(-\frac{r^2 Q_s^2(x)}{4}\right) \right]$$



For small values of r , N goes to zero

The wave functions "select" a range in r

N shifts towards smaller r when decreasing x

For large values of r , N saturates

The proton profile in the energy-dependent hot-spot model

The proton is made off a certain number of hot spots

$$T_p(\vec{b}) = \frac{1}{N_{\text{hs}}} \sum_{i=1}^{N_{\text{hs}}} T_{\text{hs}}(\vec{b} - \vec{b}_i)$$

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The proton is made off a certain number of hot spots

The number of hot spots at a given Bjorken x varies e-b-e and grows with decreasing x

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The positions of the hot spots are obtained e-b-e from a Gaussian distribution representing the proton

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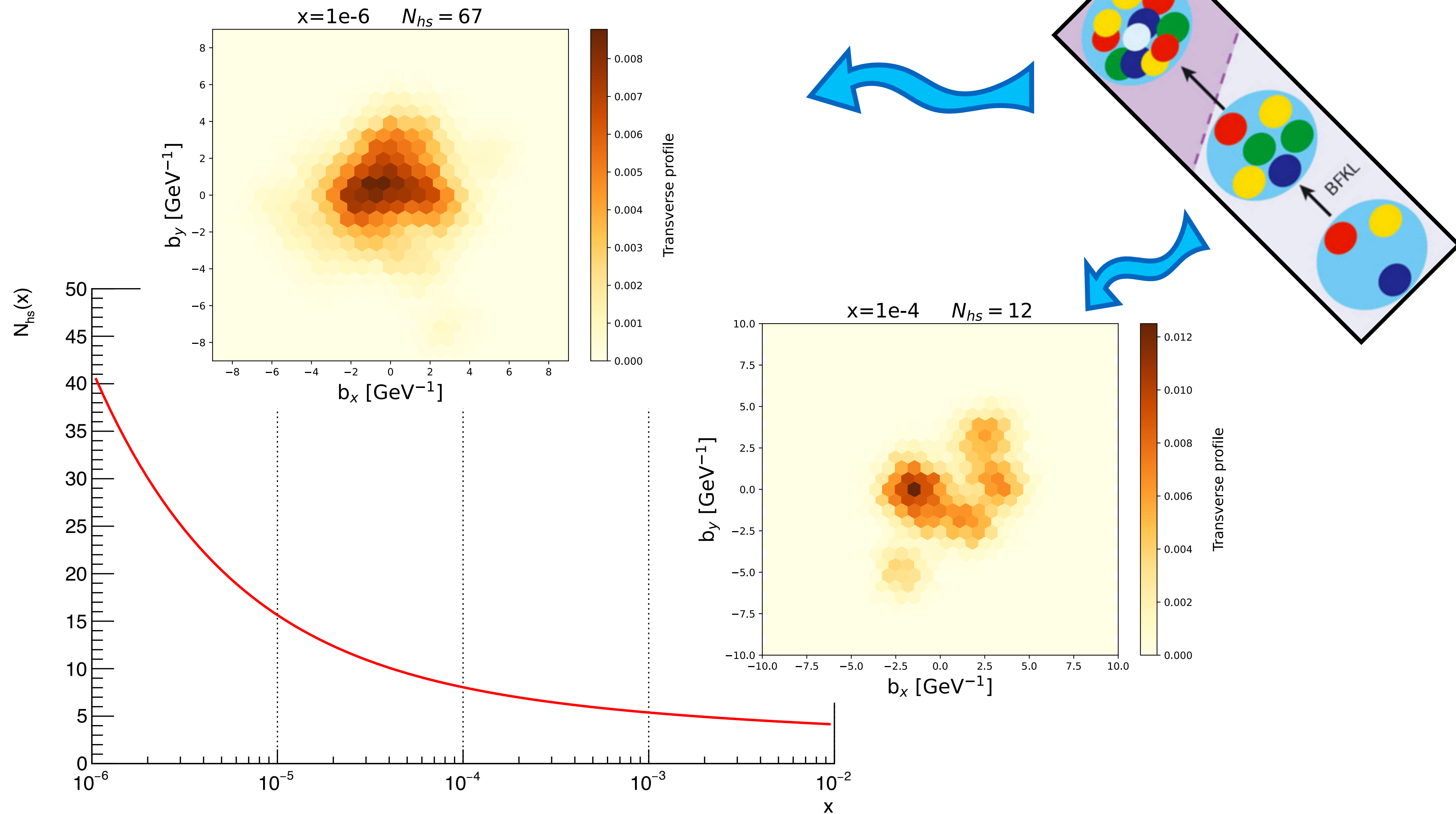
$$T_{\text{hs}}(\vec{b} - \vec{b}_i) = \frac{1}{2\pi B_{\text{hs}}} \exp\left(-\frac{(\vec{b} - \vec{b}_i)^2}{2B_{\text{hs}}}\right)$$

The hot spots have a Gaussian shape in impact parameter

The number of hot spots in the proton in the energy-dependent hot-spot model

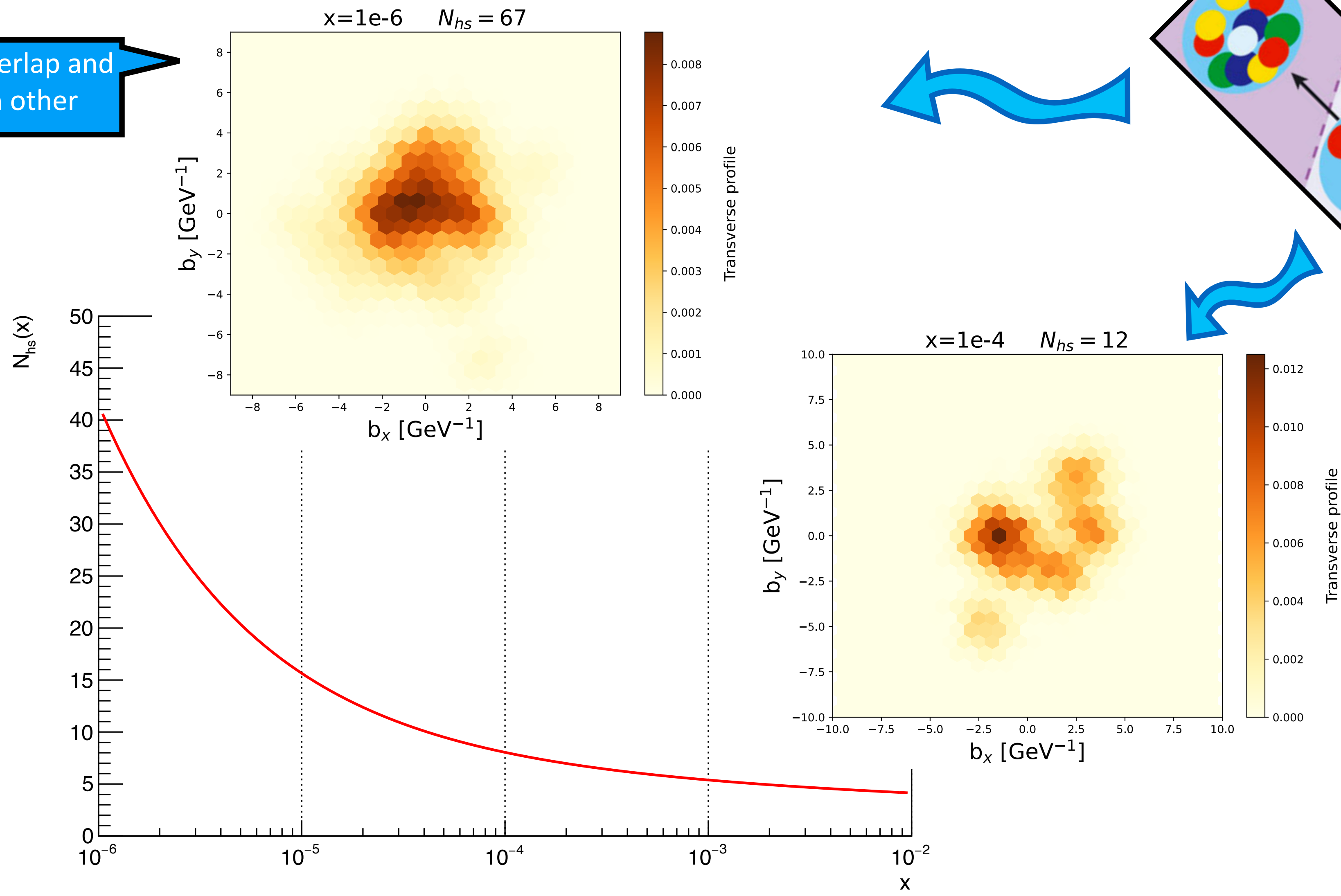


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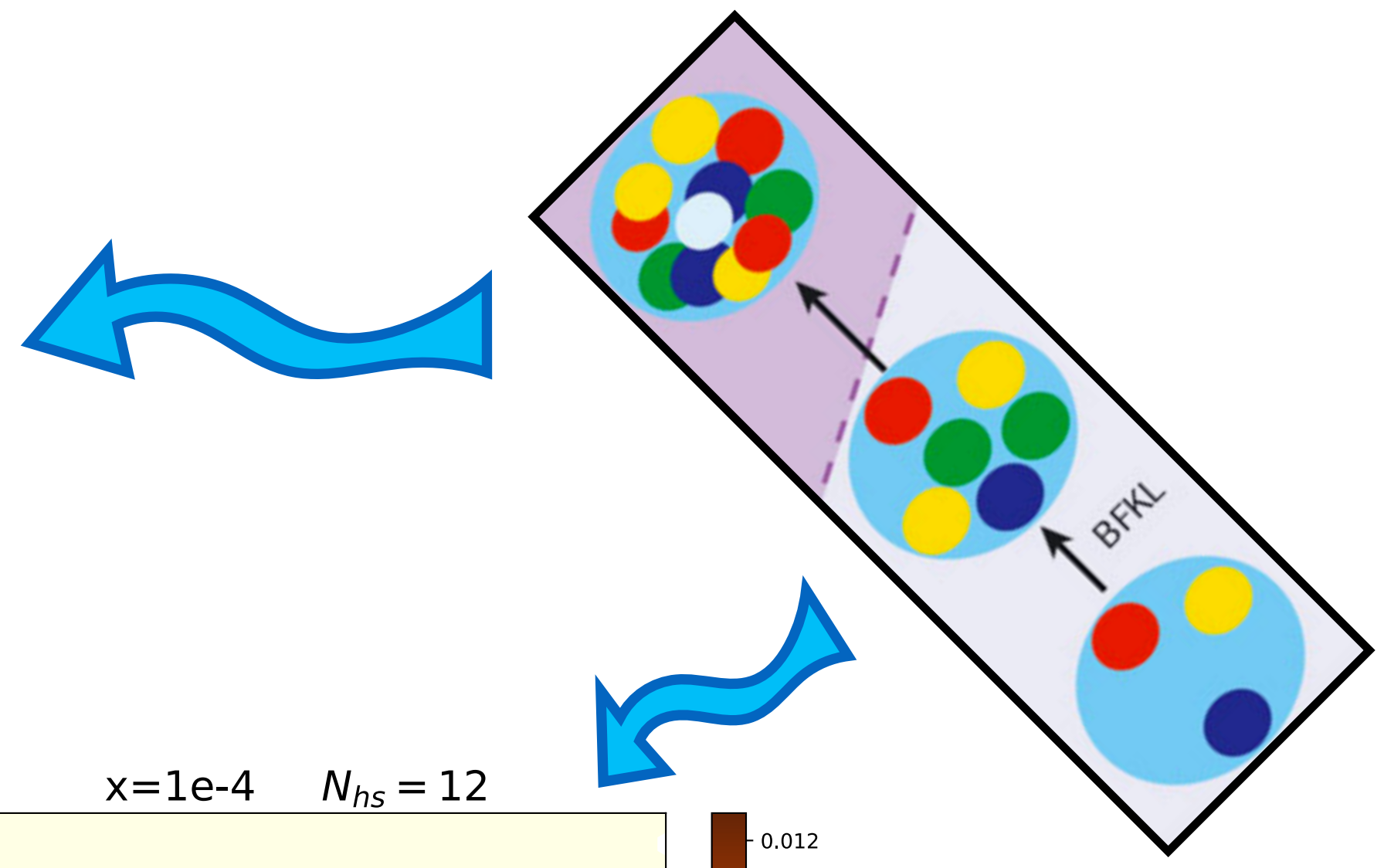
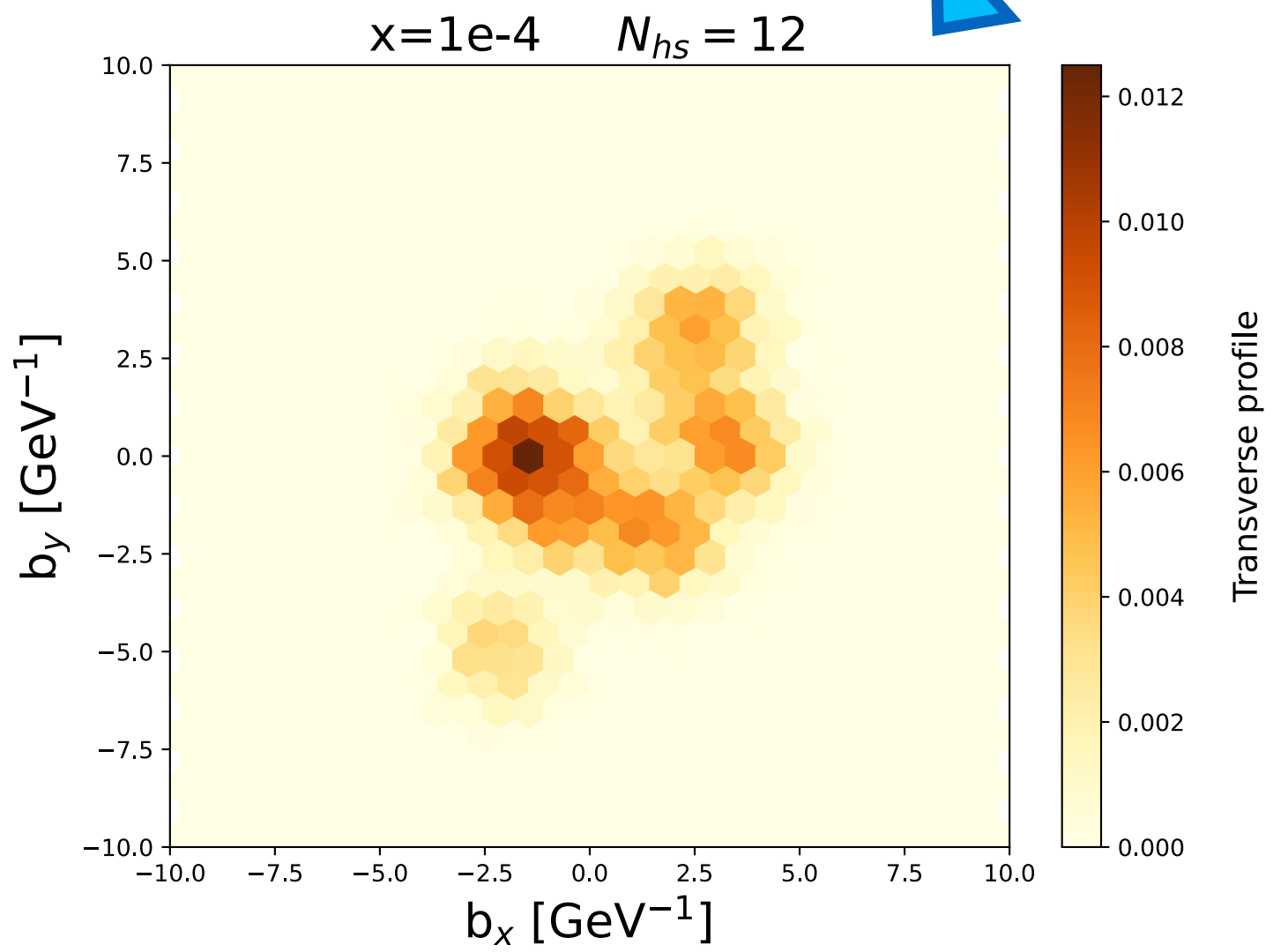
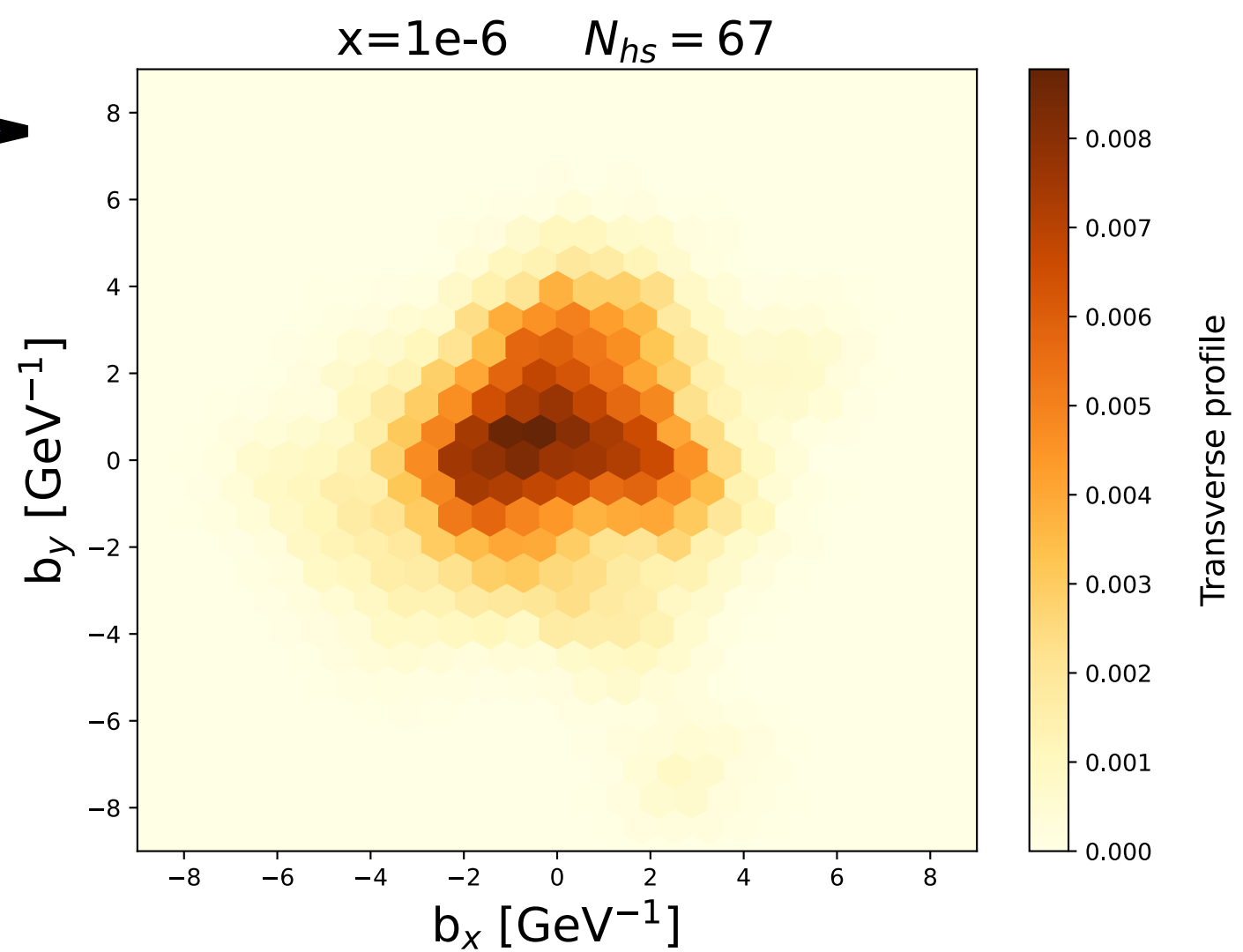
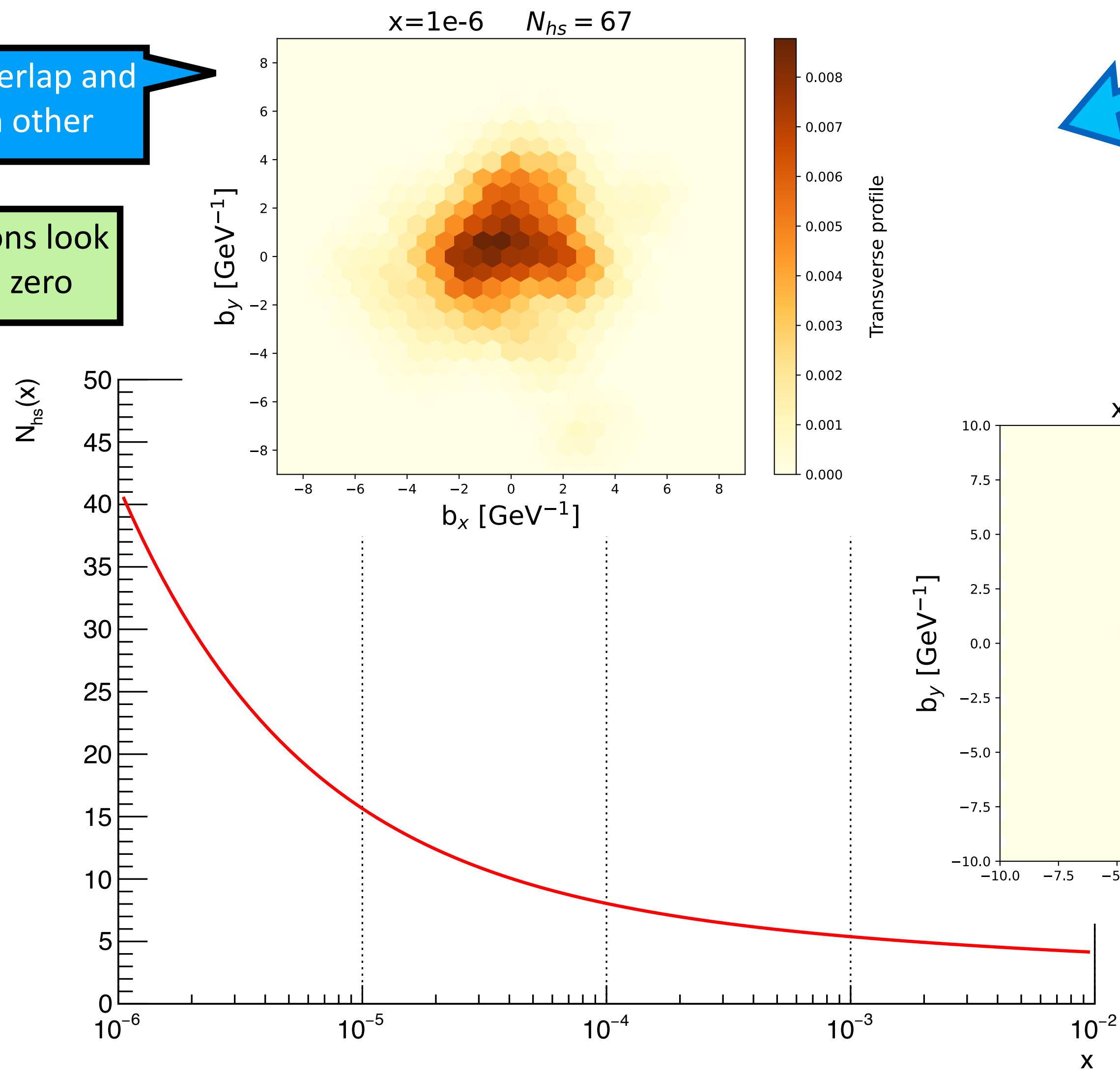
At small Bjorken-x the hot spots overlap and all configurations resemble each other



The number of hot spots in the proton in the energy-dependent hot-spot model

At small Bjorken-x the hot spots overlap and all configurations resemble each other

In the limit where all configurations look the same, the variance goes to zero



The nucleus profile in the energy-dependent hot-spot model

Nuclei are made of nucleons, which are made of hot spots

Position of nucleons sampled from a Woods-Saxon profile

$$T_{\text{Pb}}(\vec{b}) = \frac{1}{2\pi B_p} \sum_{j=1}^{A=208} \exp\left(-\frac{(\vec{b} - \vec{b}_j)^2}{2B_p}\right)$$

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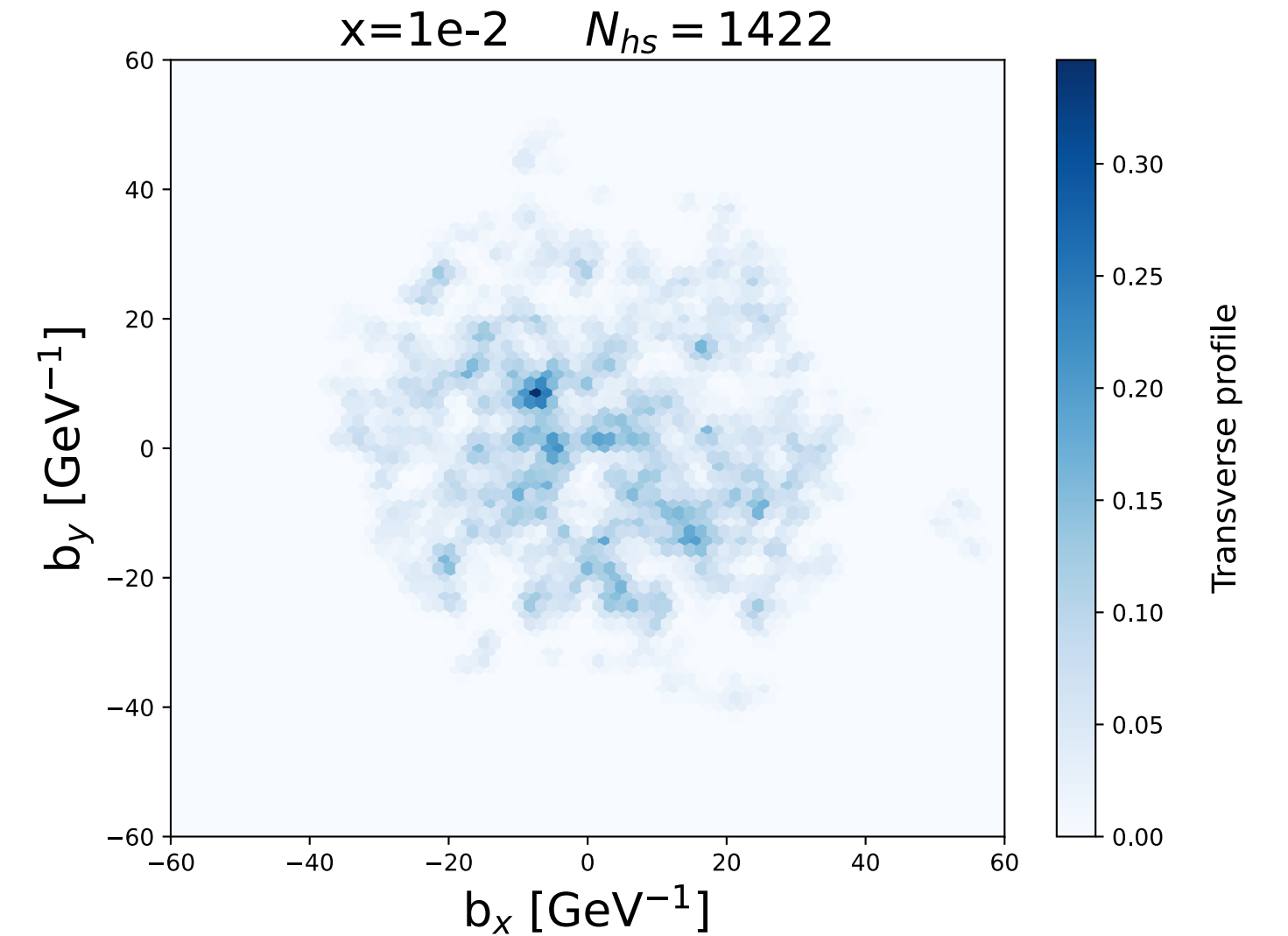
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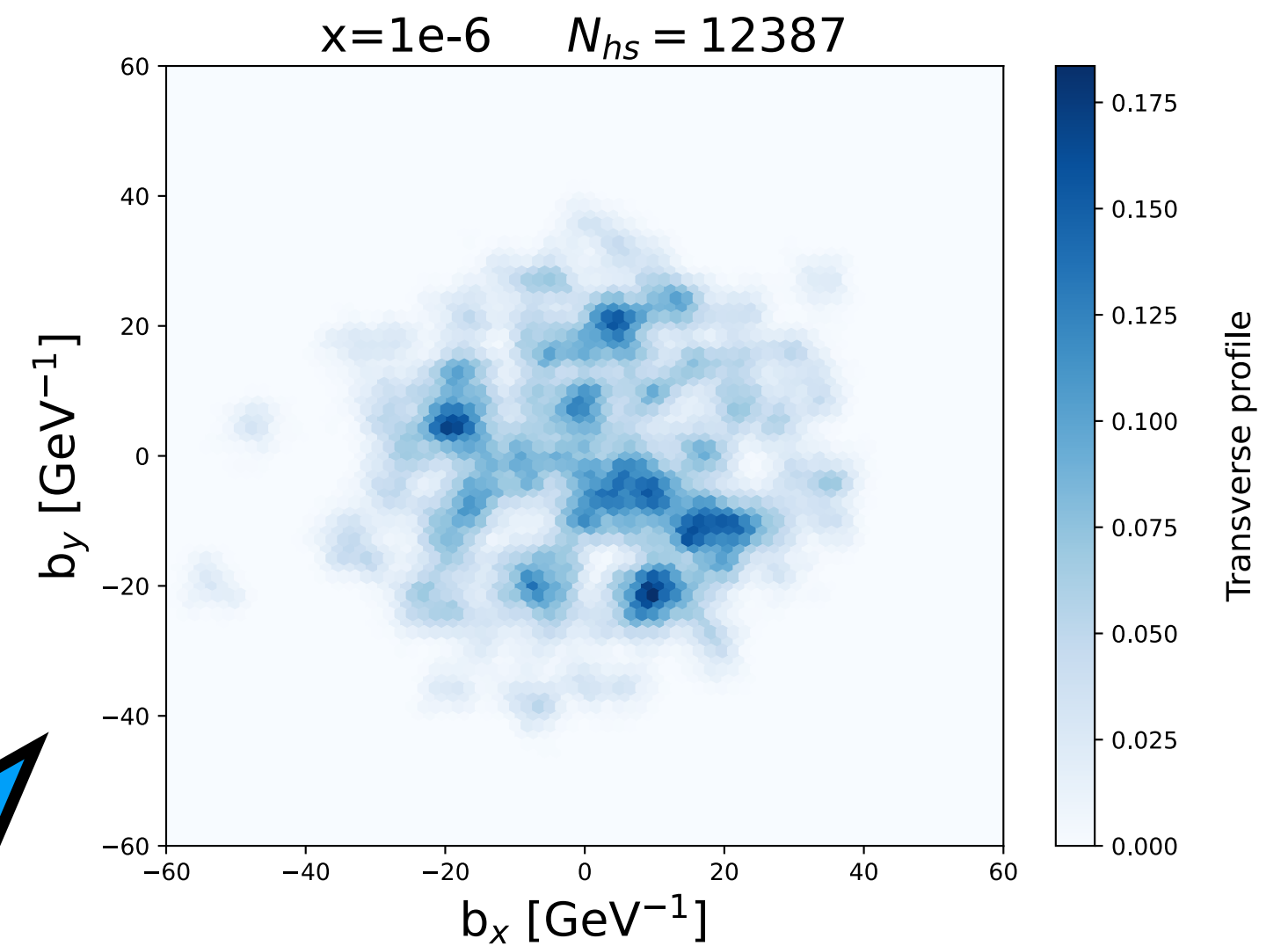
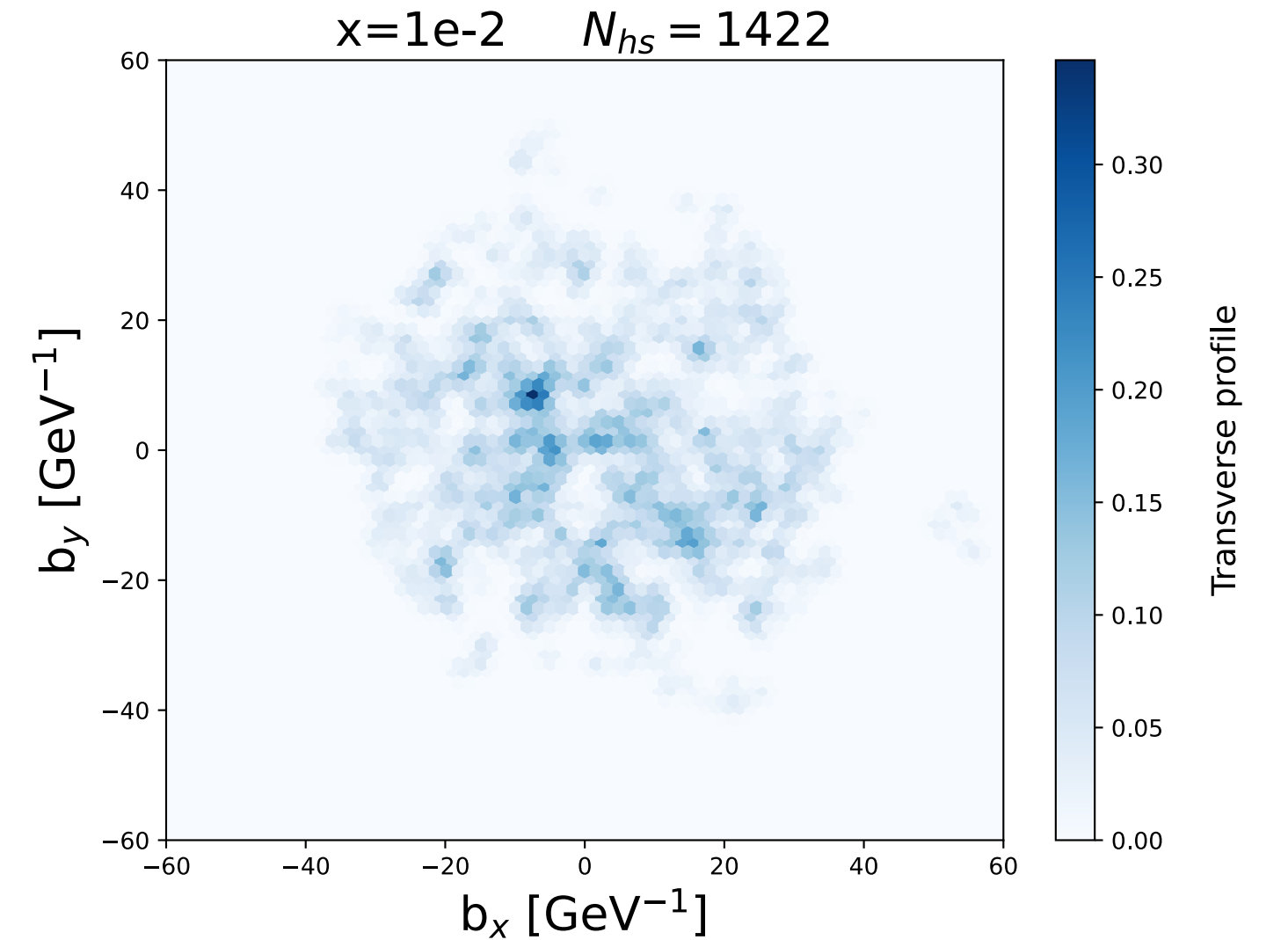
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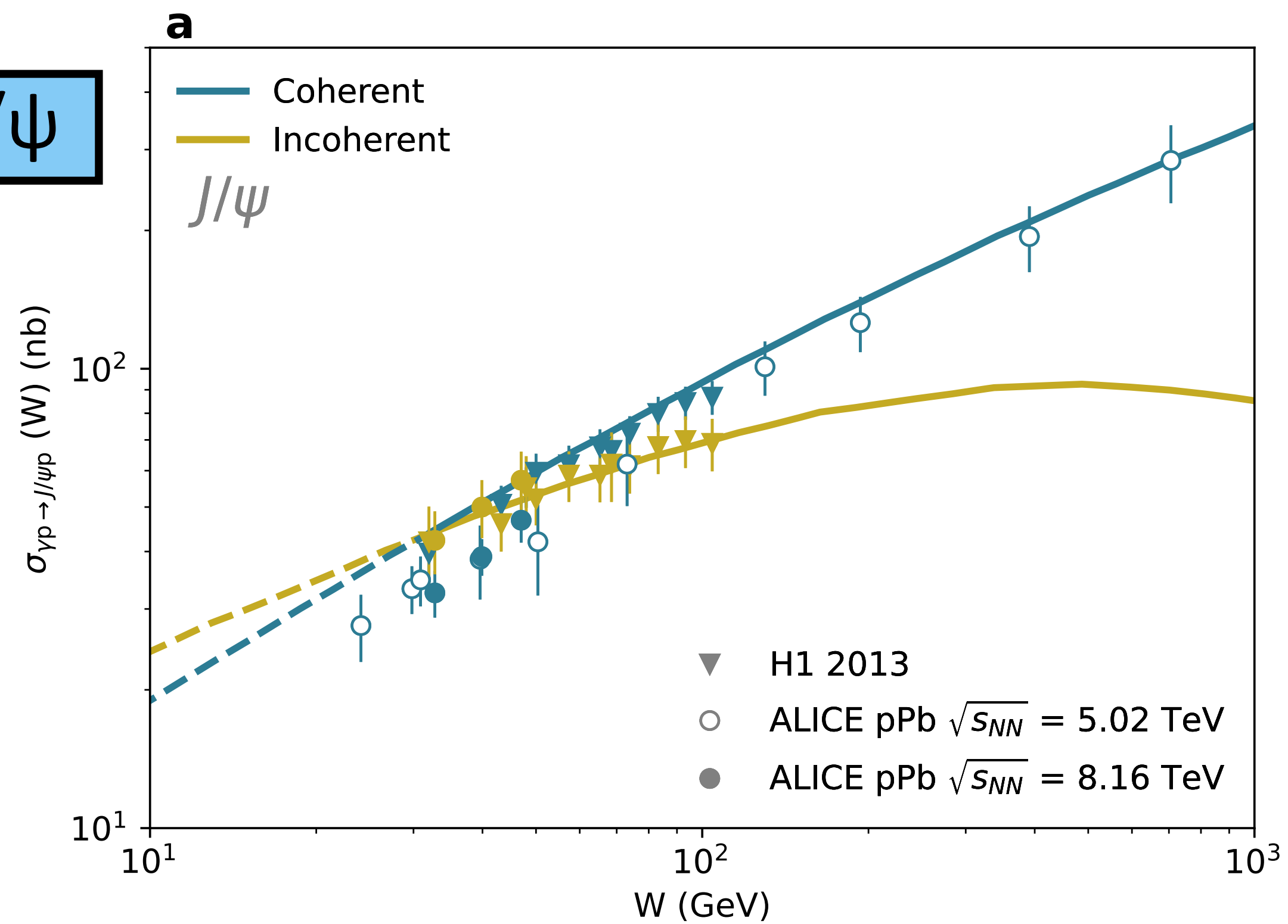
For nuclear targets, in our model the hot spots start to overlap locally



Predictions: energy dependence

Energy dependence for γp collisions

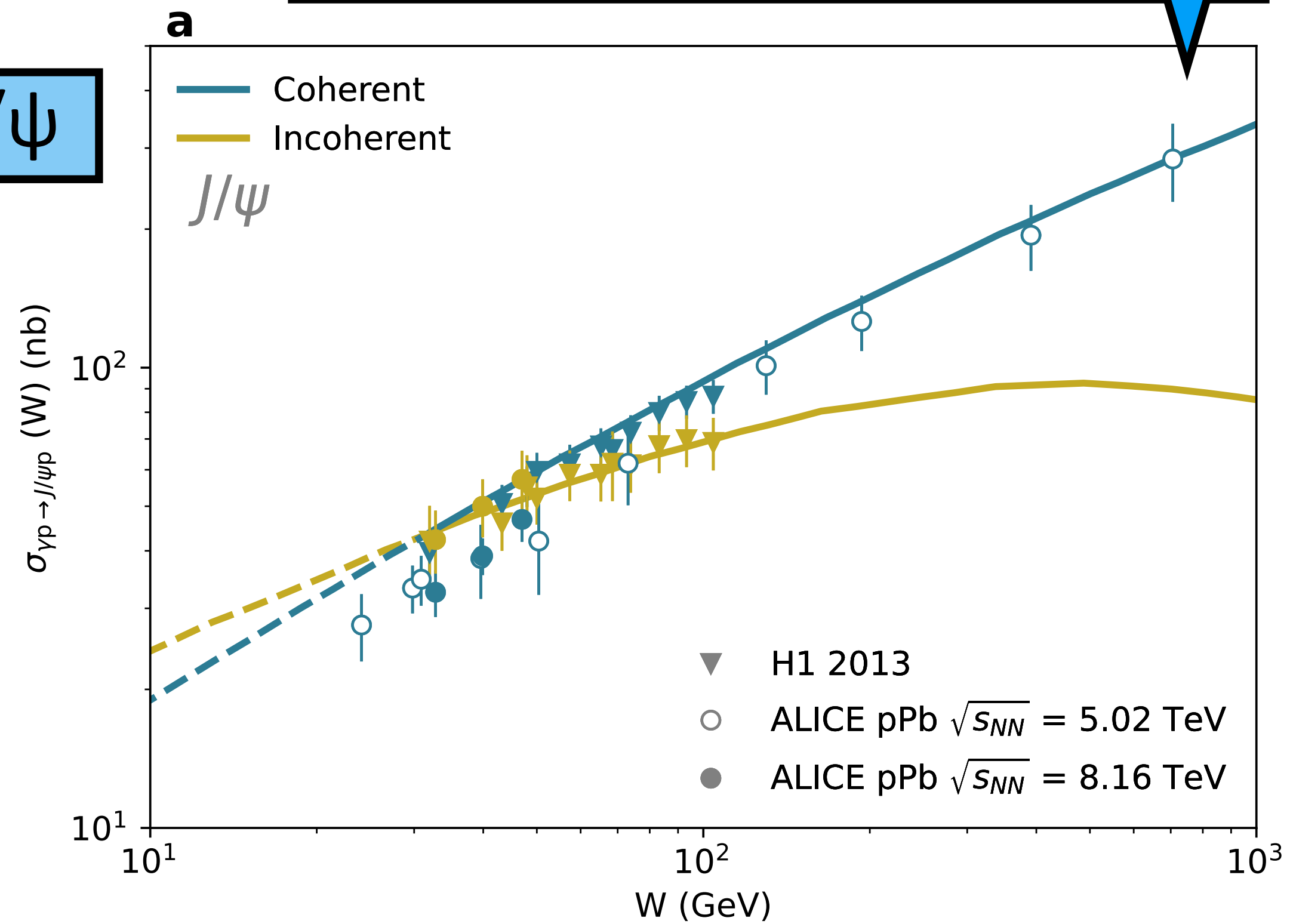
J/ ψ



Energy dependence for γp collisions

The coherent (exclusive) cross section rises with energy showing no obvious saturation behaviour

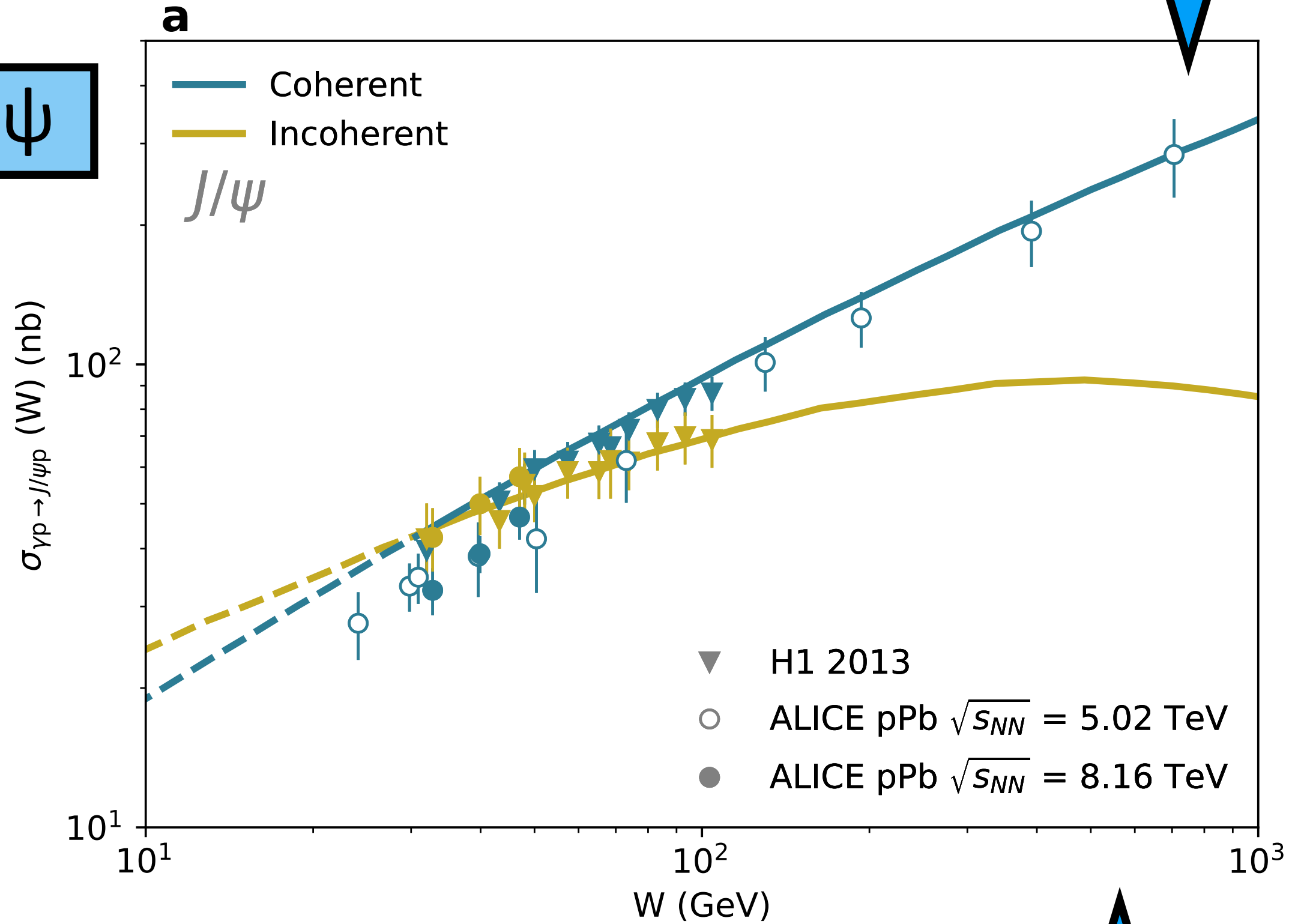
J/ψ



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J/ψ

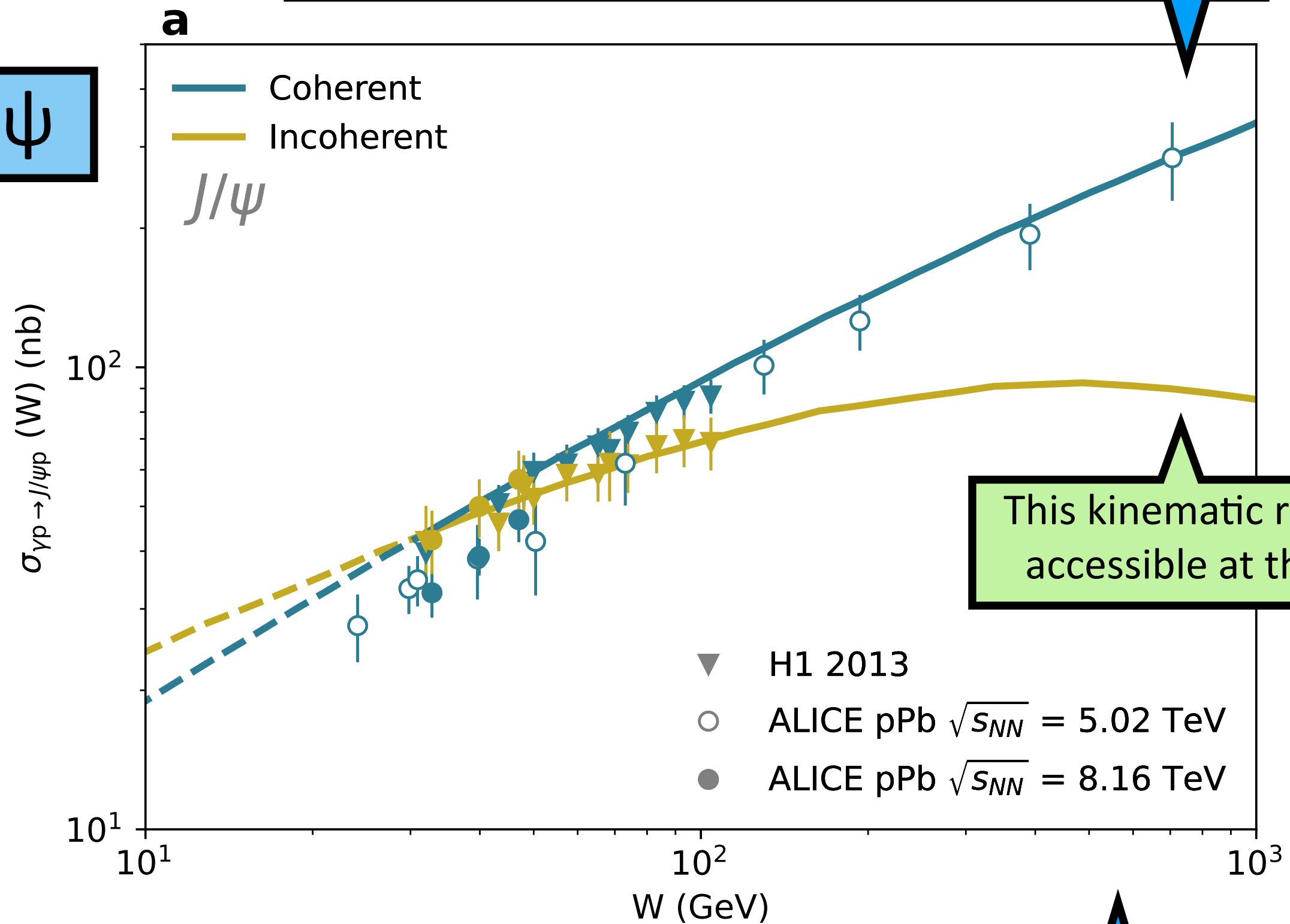


The incoherent (dissociative) cross section is predicted to reach a maximum and then decrease with increasing energy

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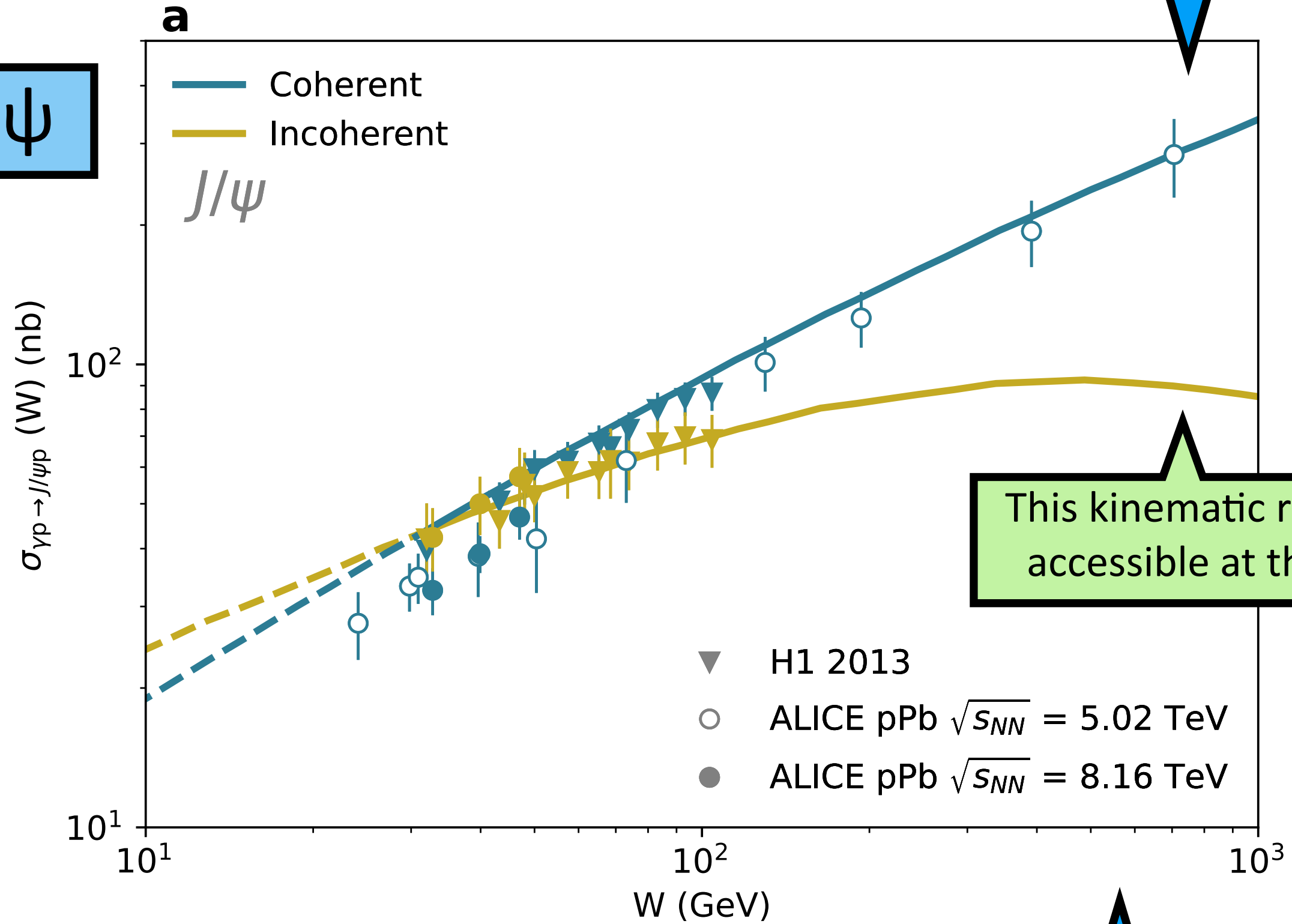


This kinematic region is accessible at the LHC

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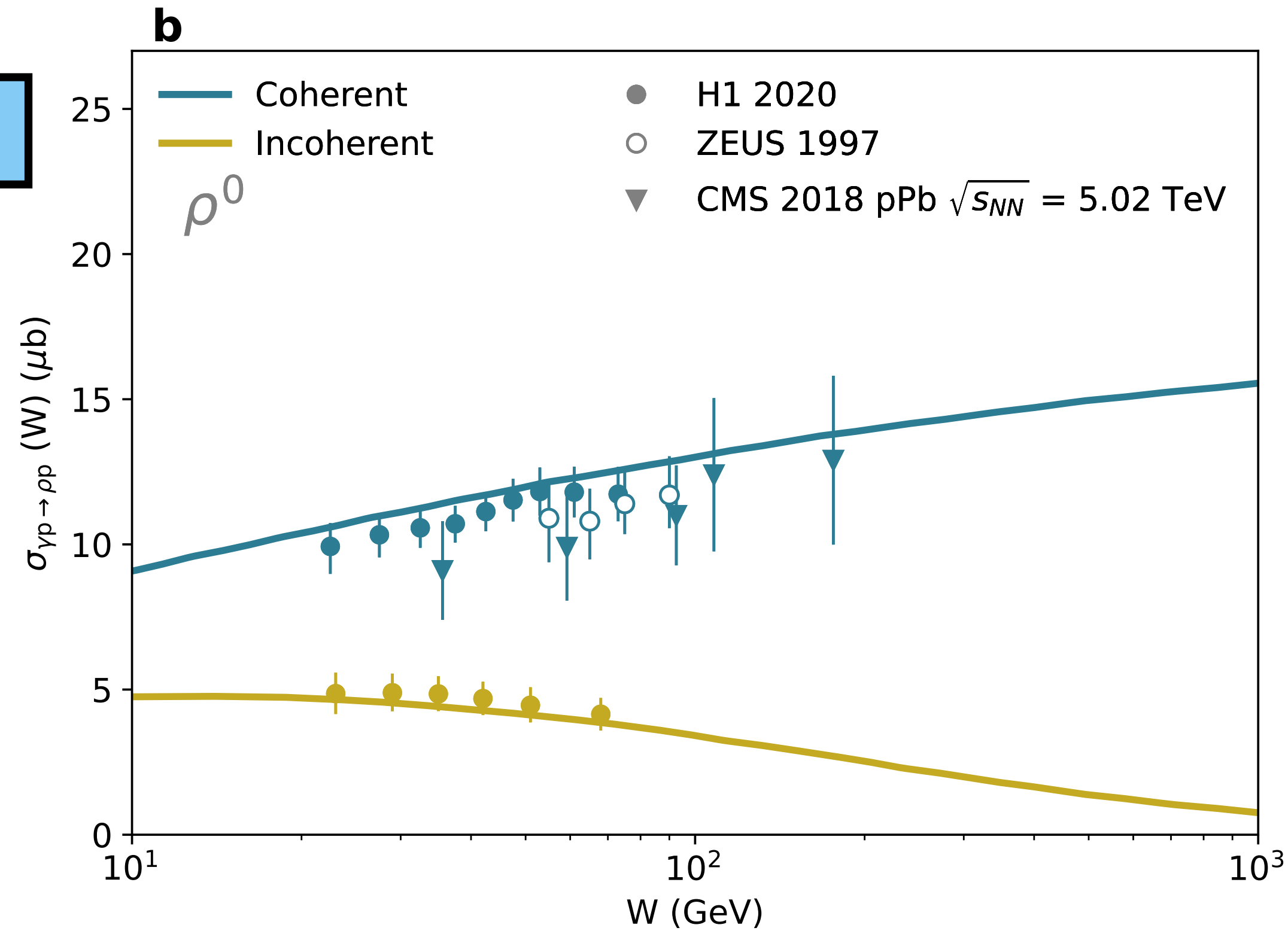


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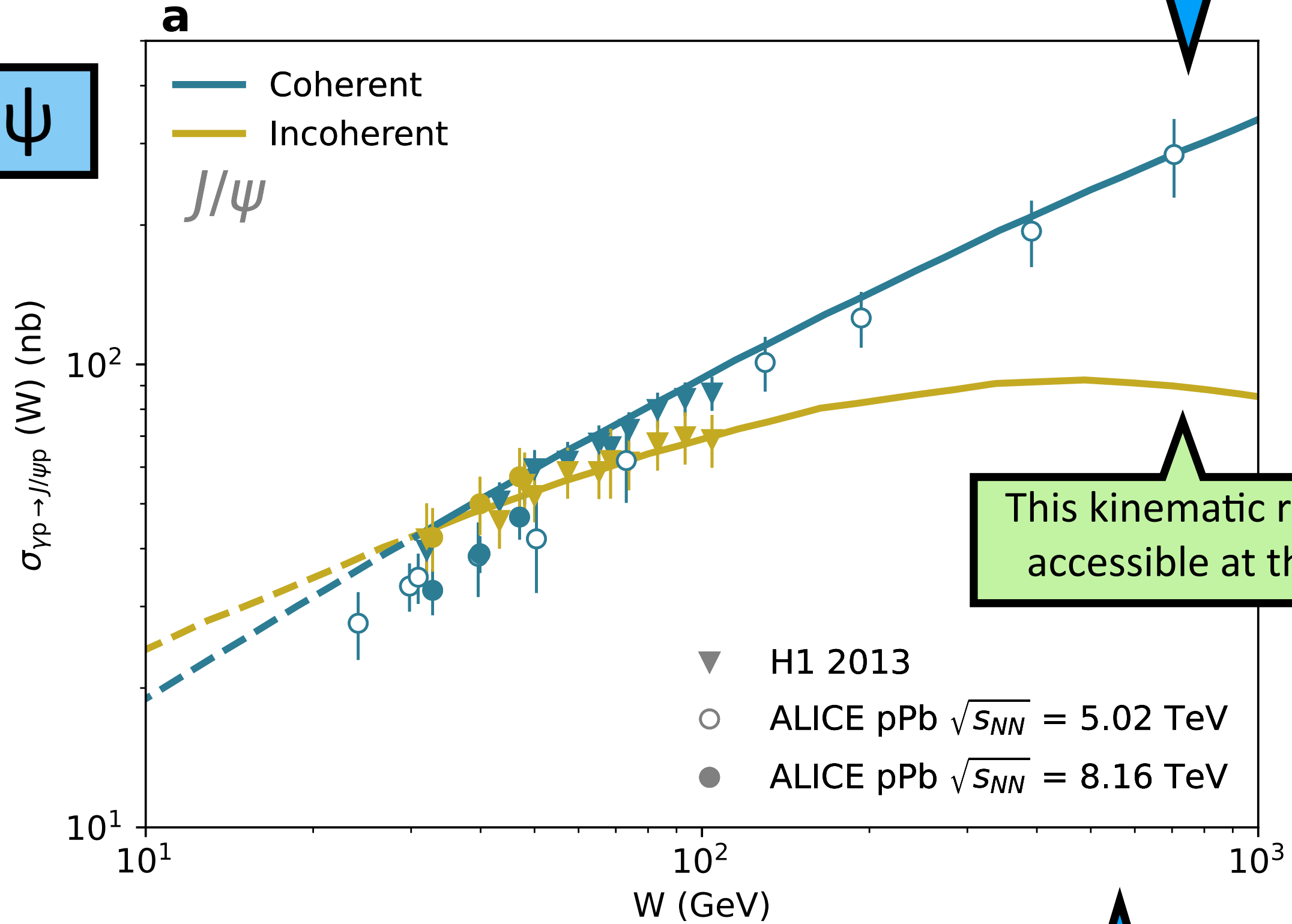
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ρ^0



Energy dependence for γp collisions

J/ψ

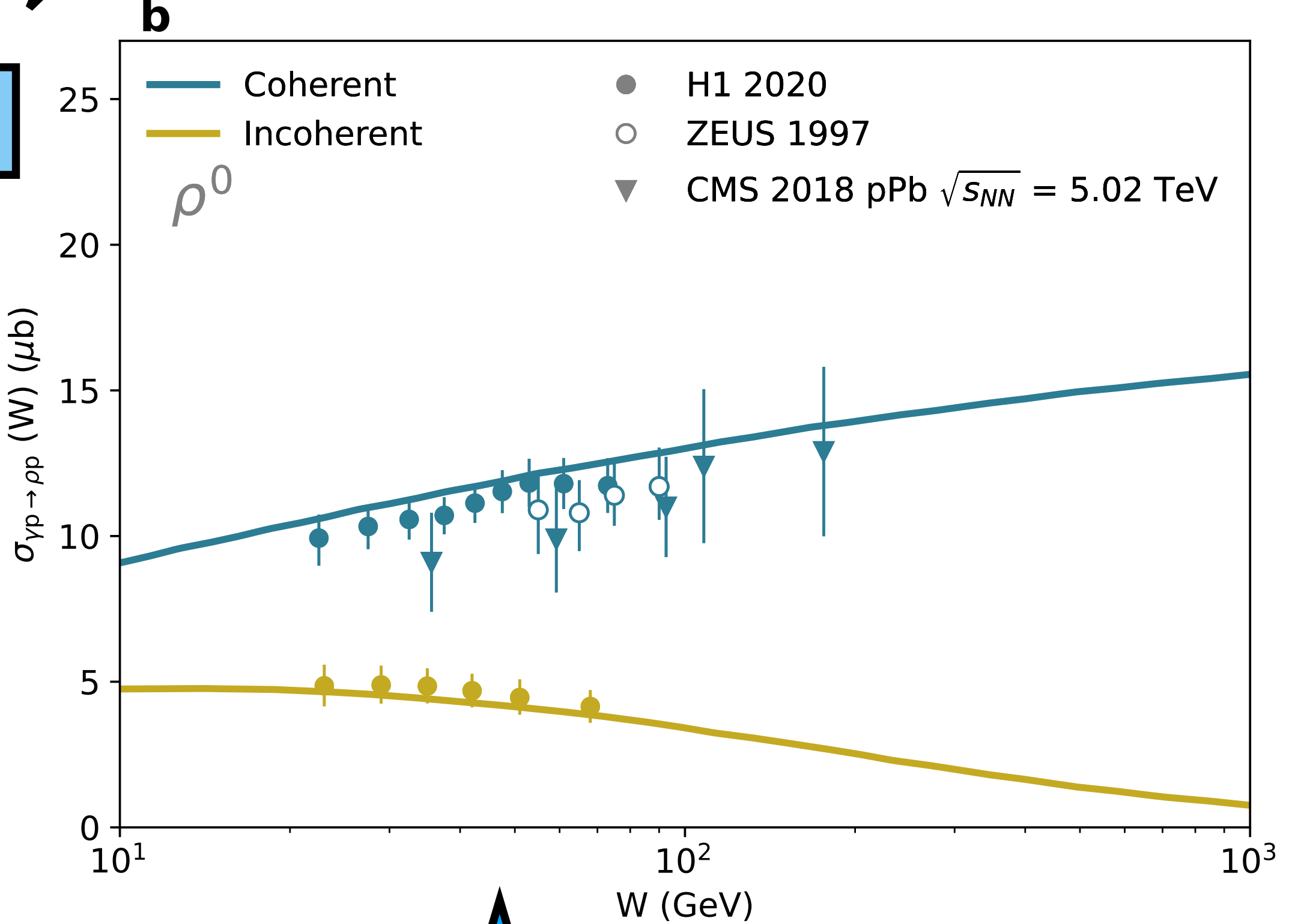


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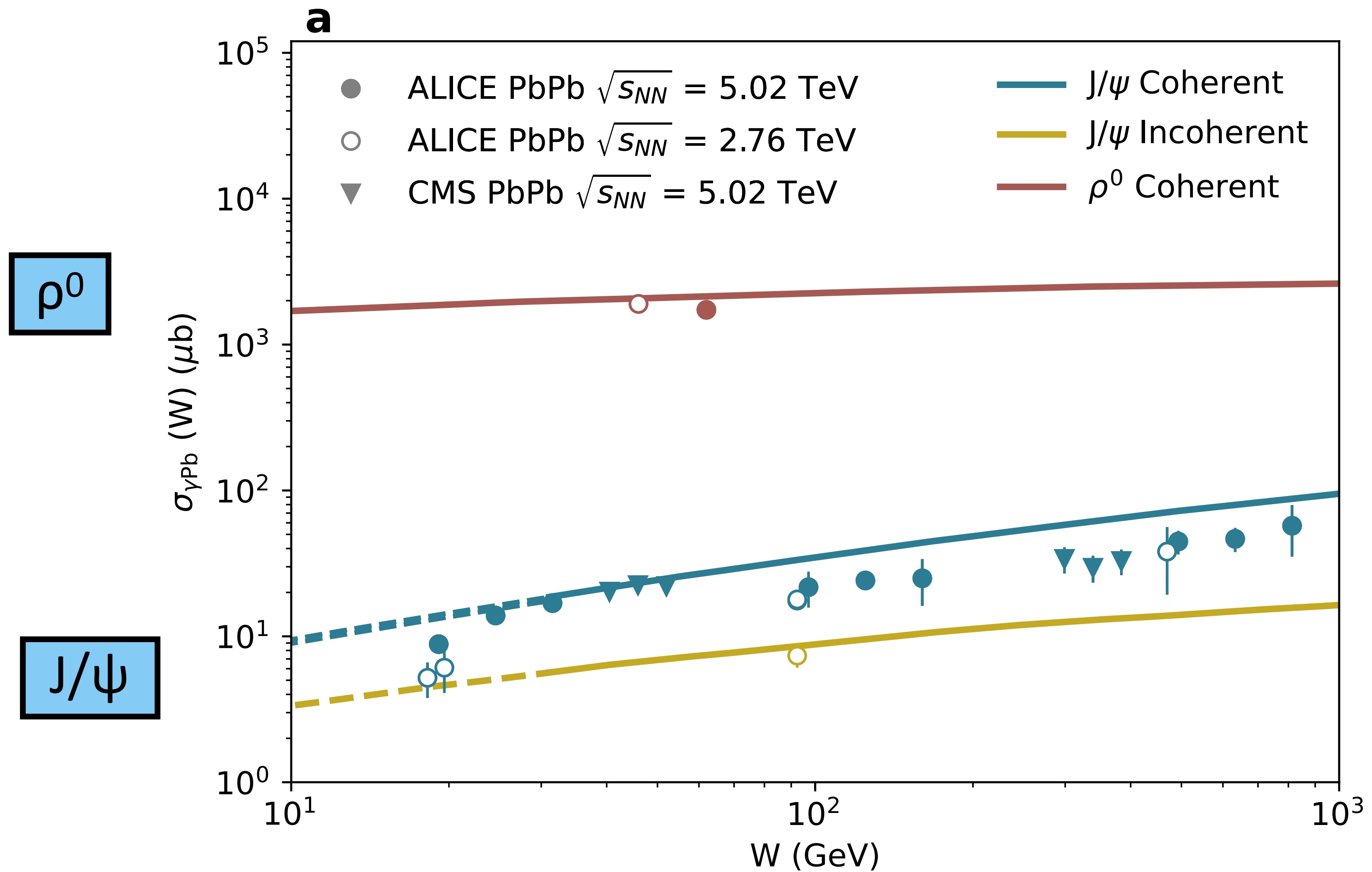
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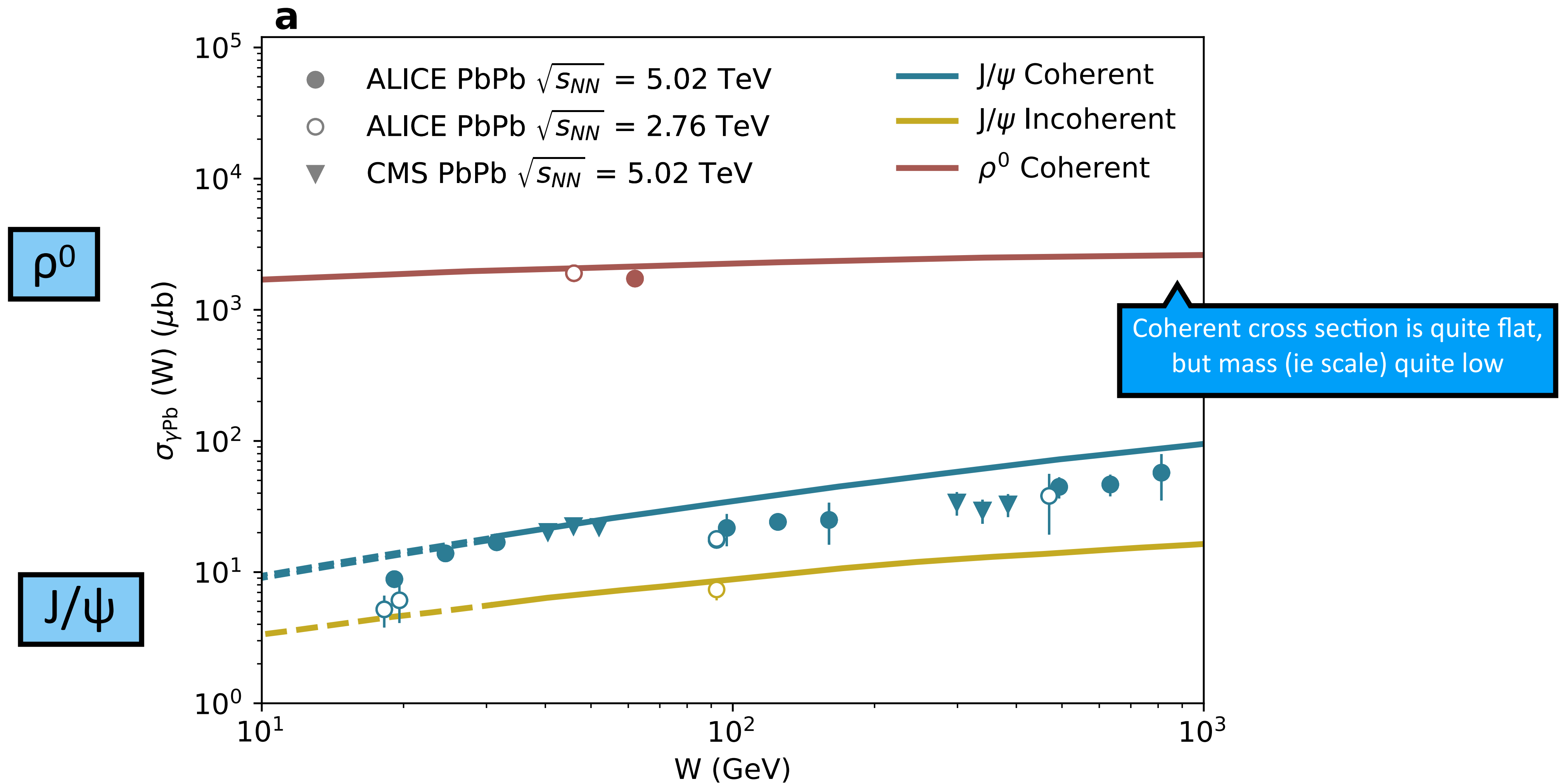
Is this mass scale in the perturbative region?

The incoherent (dissociative) cross section is decreasing according to HERA data, but there are some caveats

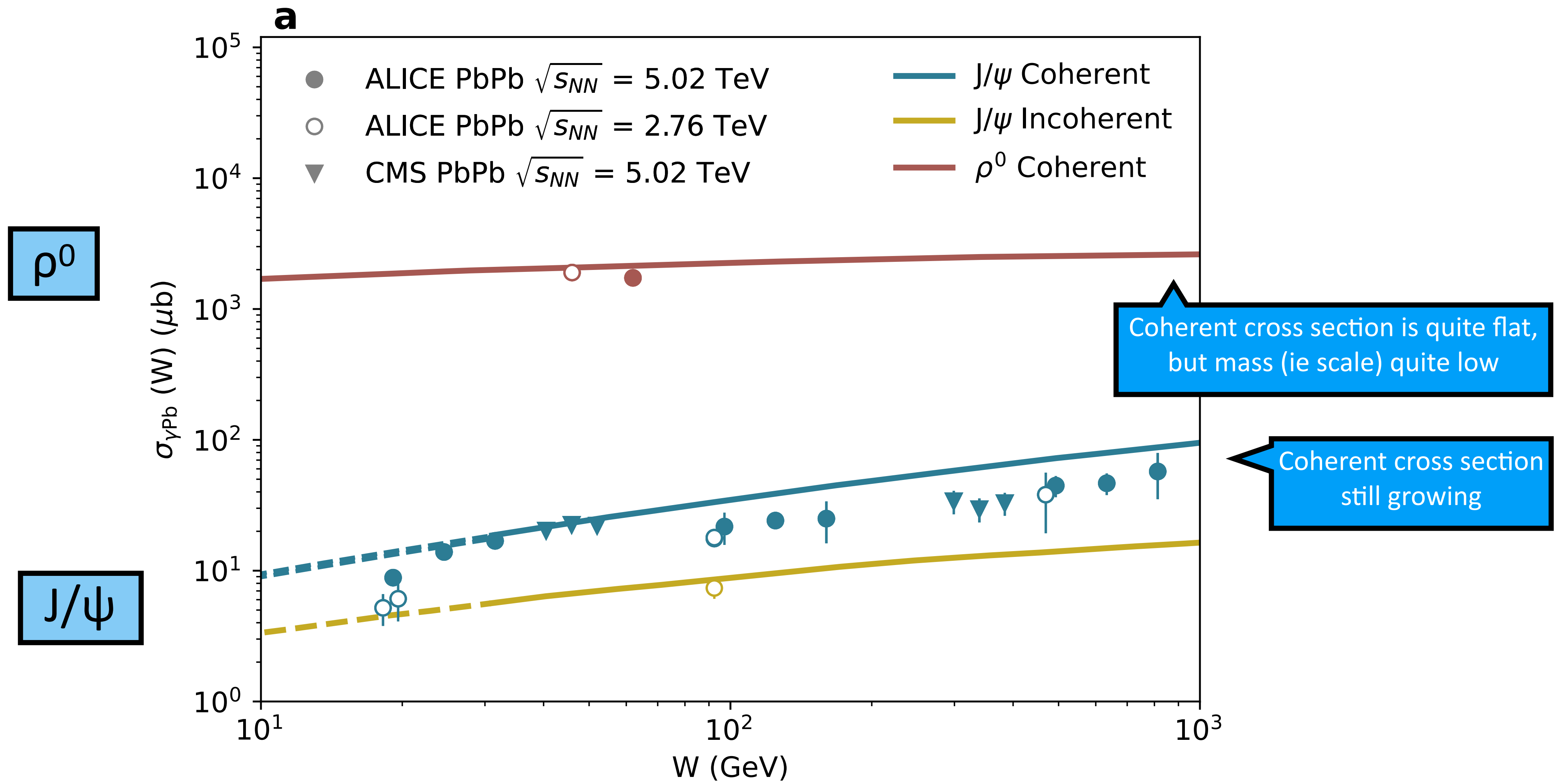
Energy dependence for γ Pb collisions



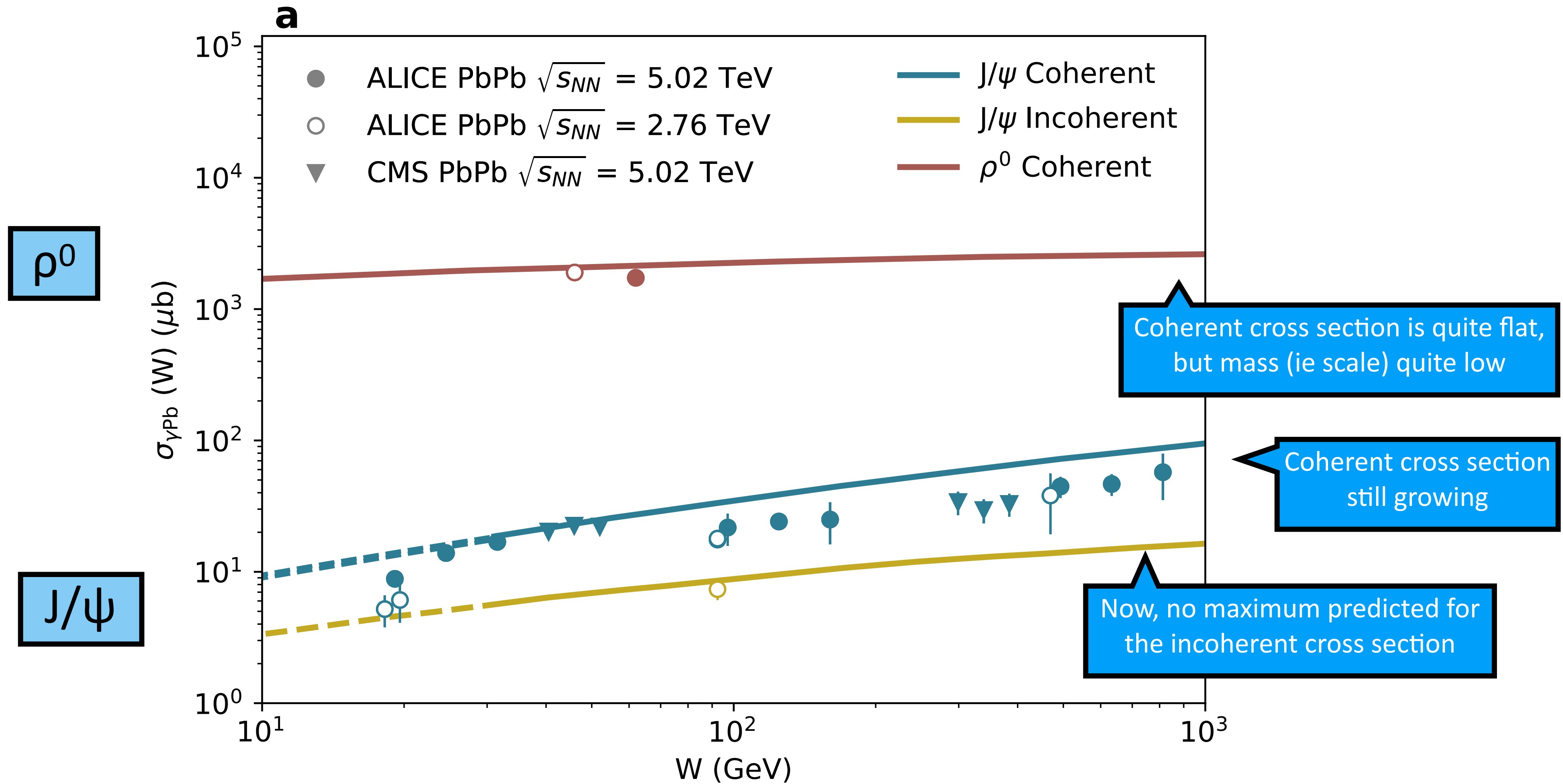
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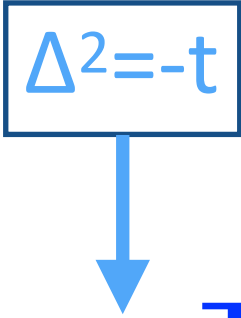


Energy dependence for γ Pb collisions

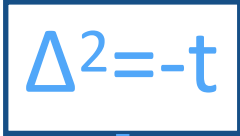


Predictions: Mandelstam-t dependence

Mandelstam-t and impact parameter

$$\mathcal{A}_{\text{T,L}}(x, Q^2, \vec{\Delta}) = i \int d\vec{r} \int_0^1 \frac{dz}{4\pi} \int d\vec{b} | \Psi_\gamma^* \Psi_V |_{\text{T,L}} \exp \left[-i \left(\vec{b} - \left(\frac{1}{2} - z \right) \vec{r} \right) \cdot \vec{\Delta} \right] \frac{d\sigma_{\text{H}}^{\text{dip}}}{d\vec{b}}$$


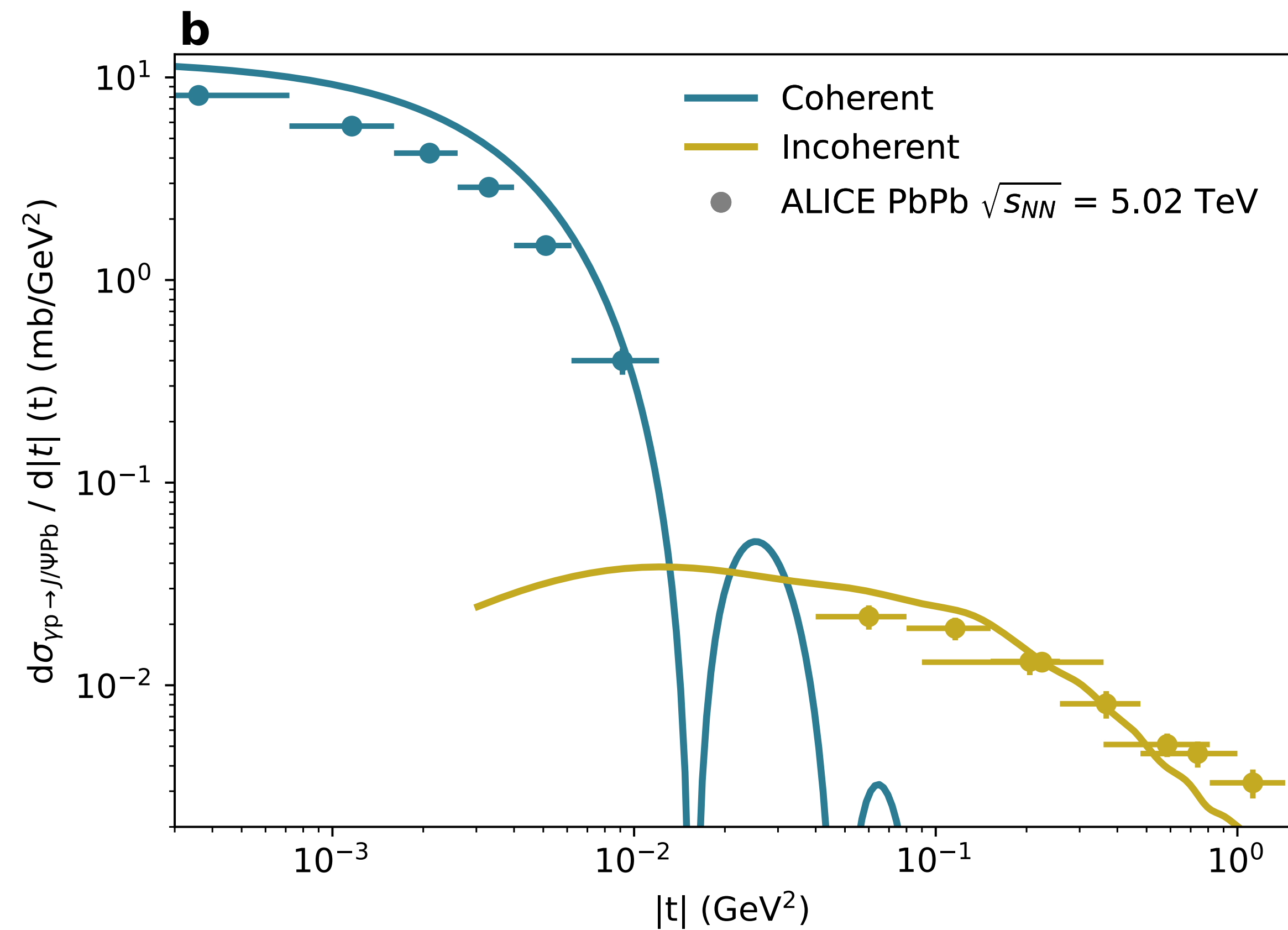
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Impact parameter is Fourier conjugate to the momentum transferred at the hadron vertex
 →
 different ranges in Mandelstam-t are sensitive to different size scales in the impact-parameter plane

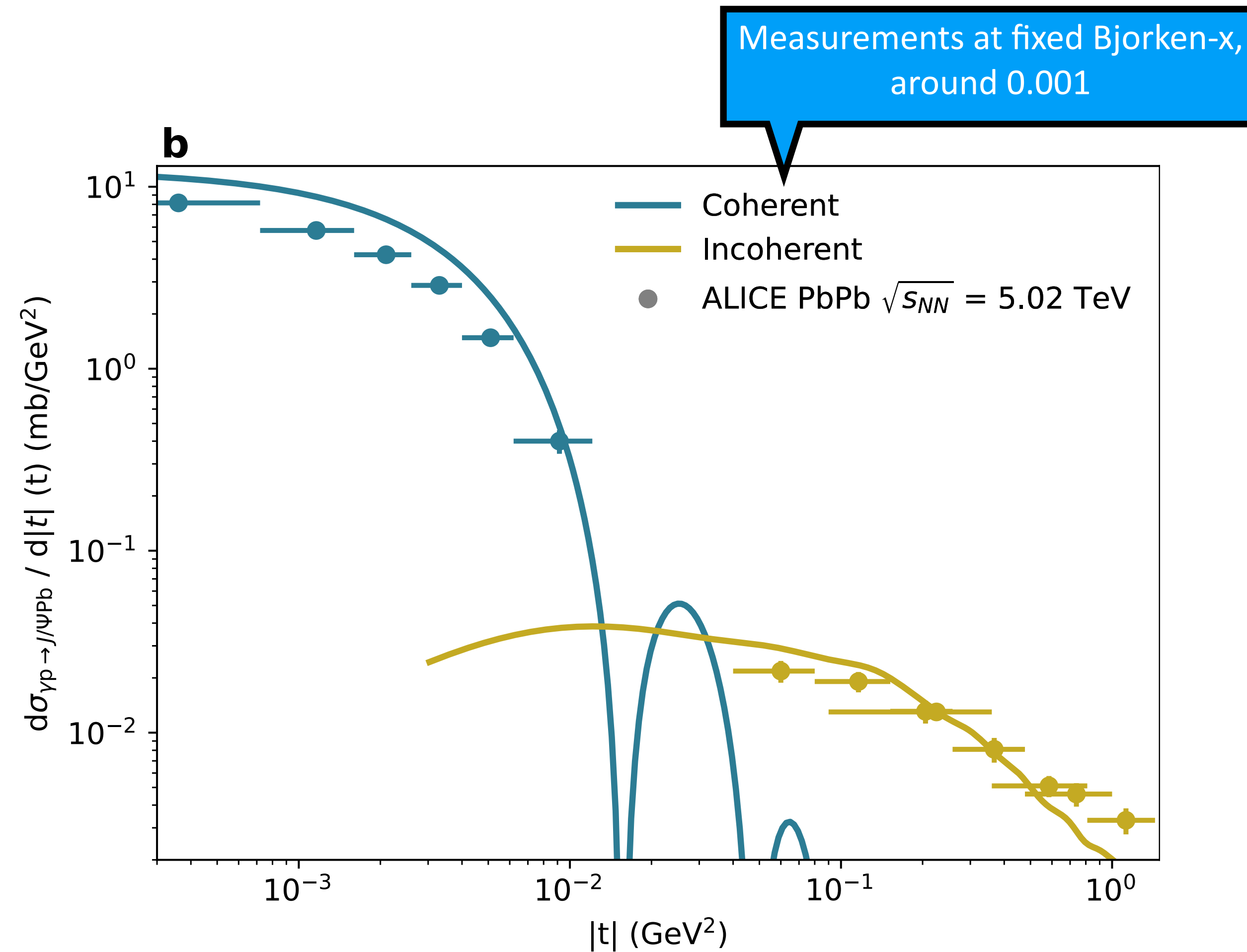
Mandelstam-t dependence for γ Pb collisions

J/ ψ



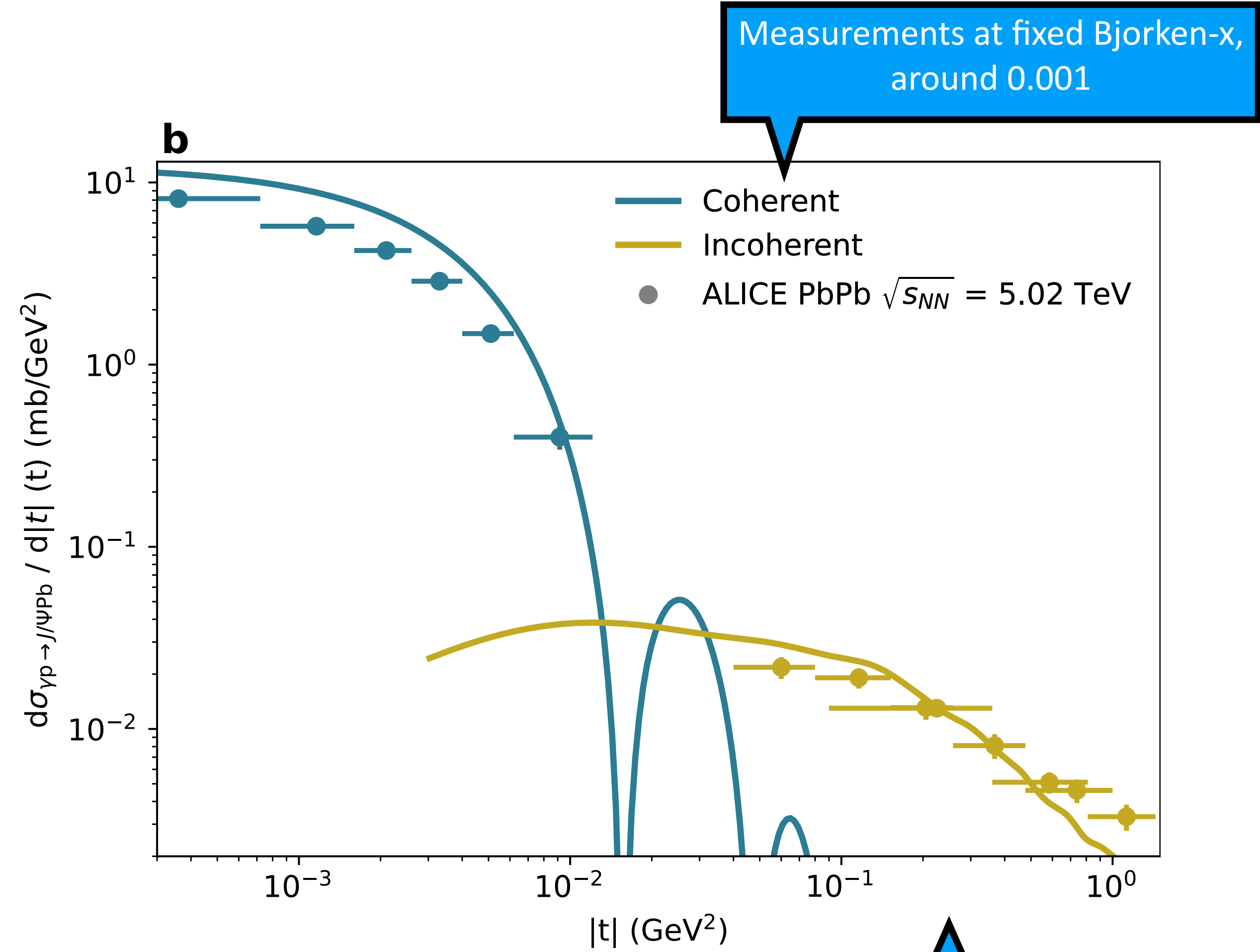
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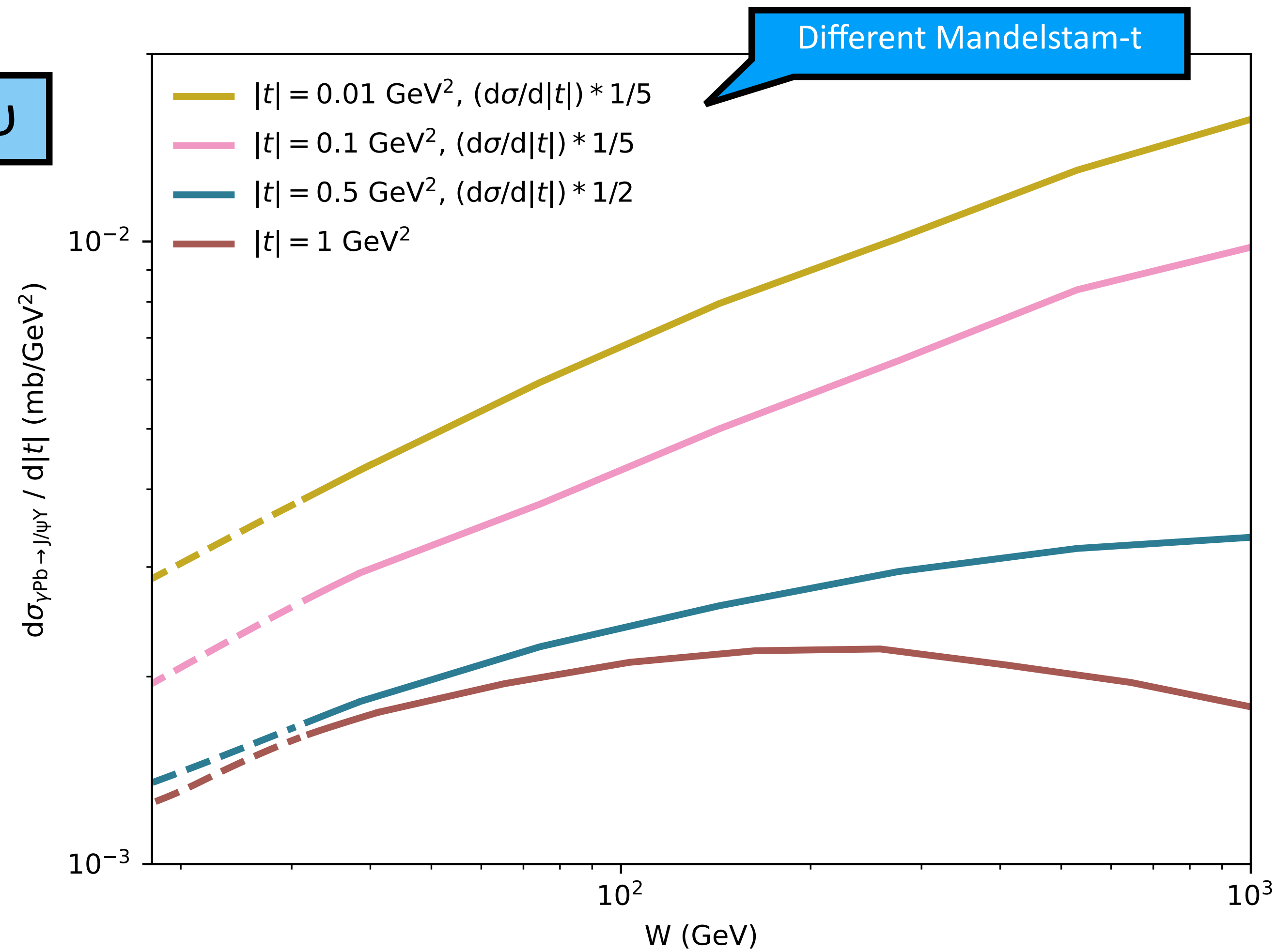


LHC data covers three orders of magnitude in Mandelstam-t

Saturation signature at high $|t|$

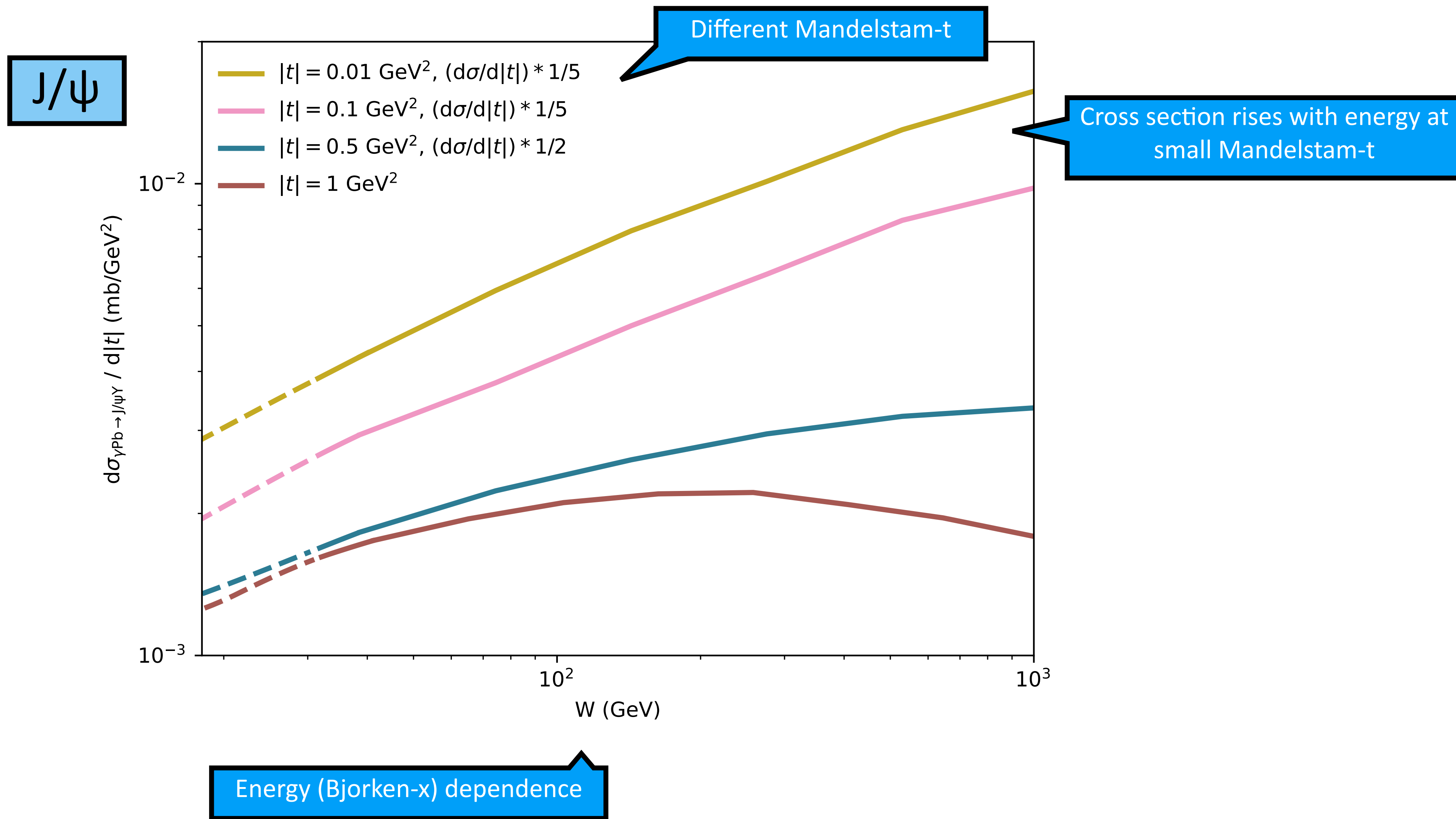
Scanning size scales in the impact-parameter plane

J/ψ

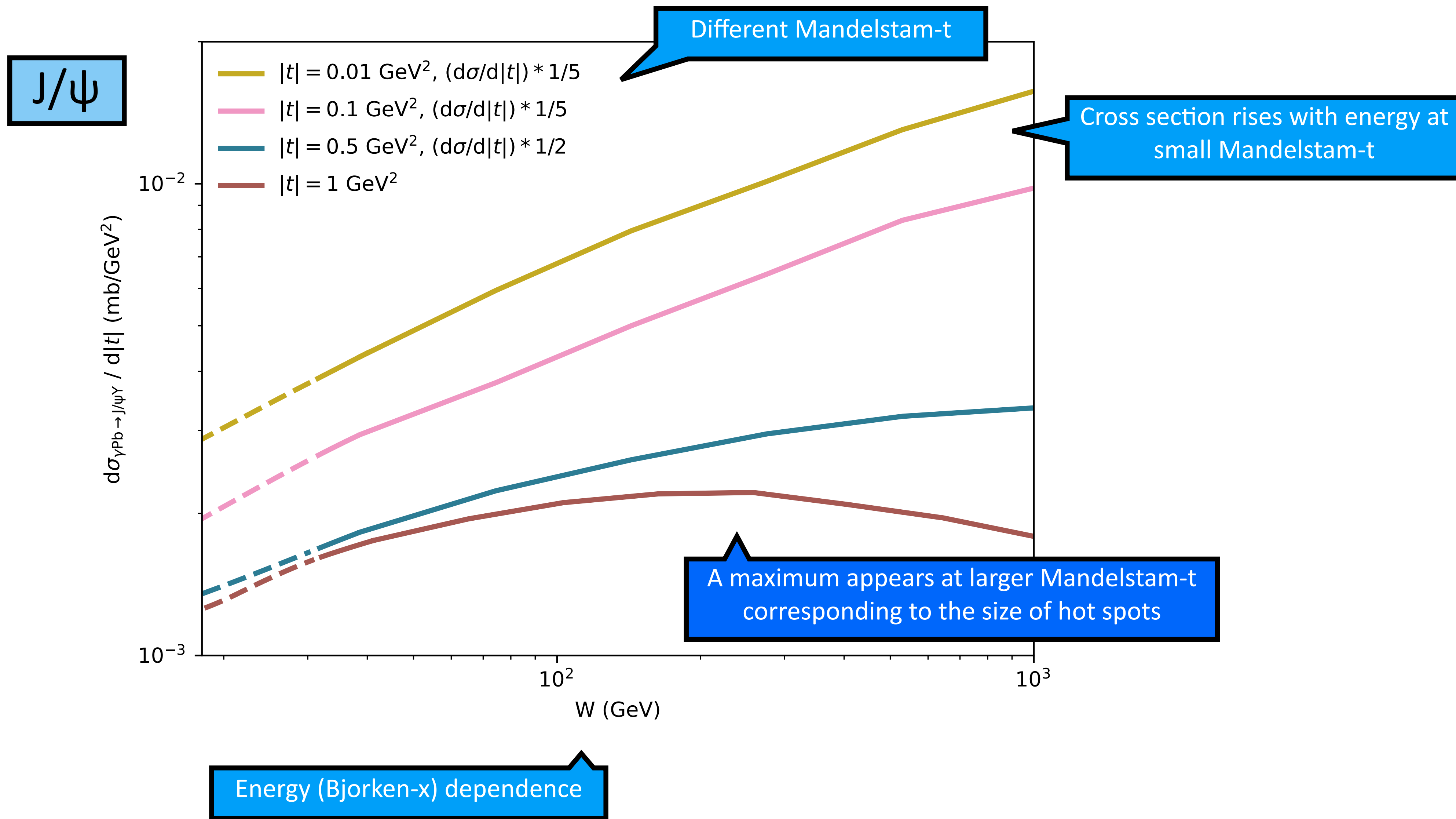


Energy (Bjorken-x) dependence

Scanning size scales in the impact-parameter plane

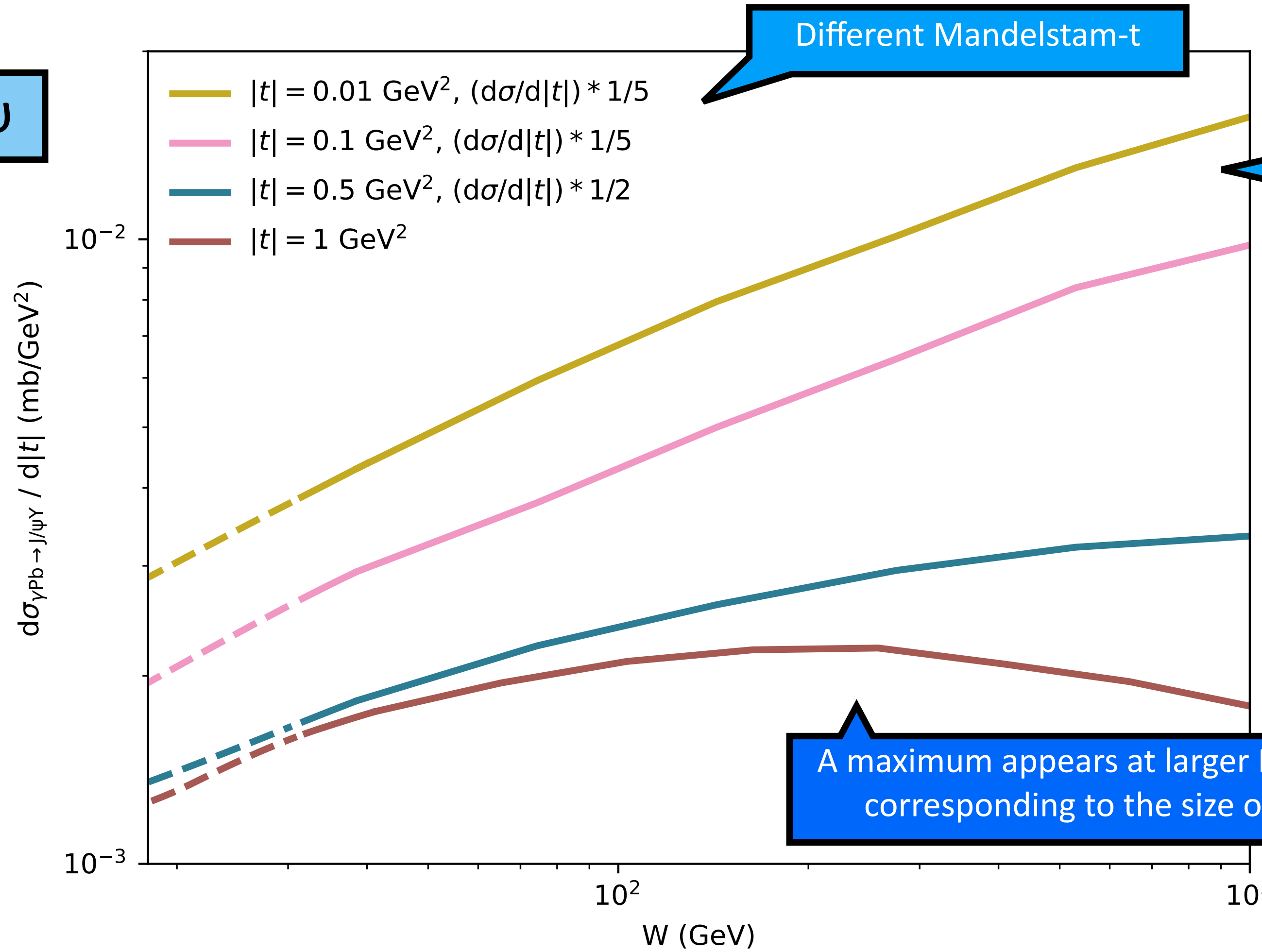


Scanning size scales in the impact-parameter plane



Scanning size scales in the impact-parameter plane

J/ψ

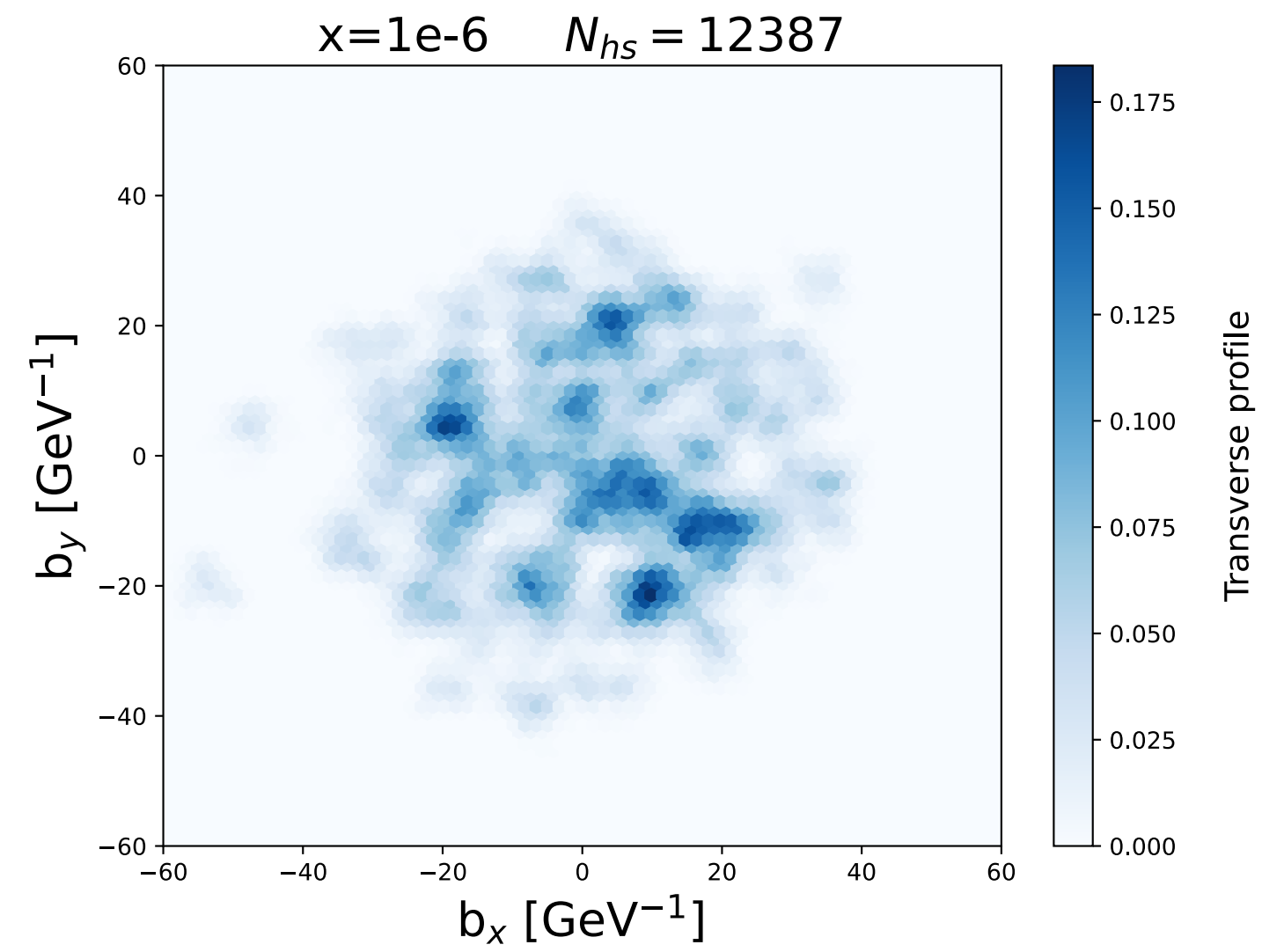


Different Mandelstam-t

Cross section rises with energy at small Mandelstam-t

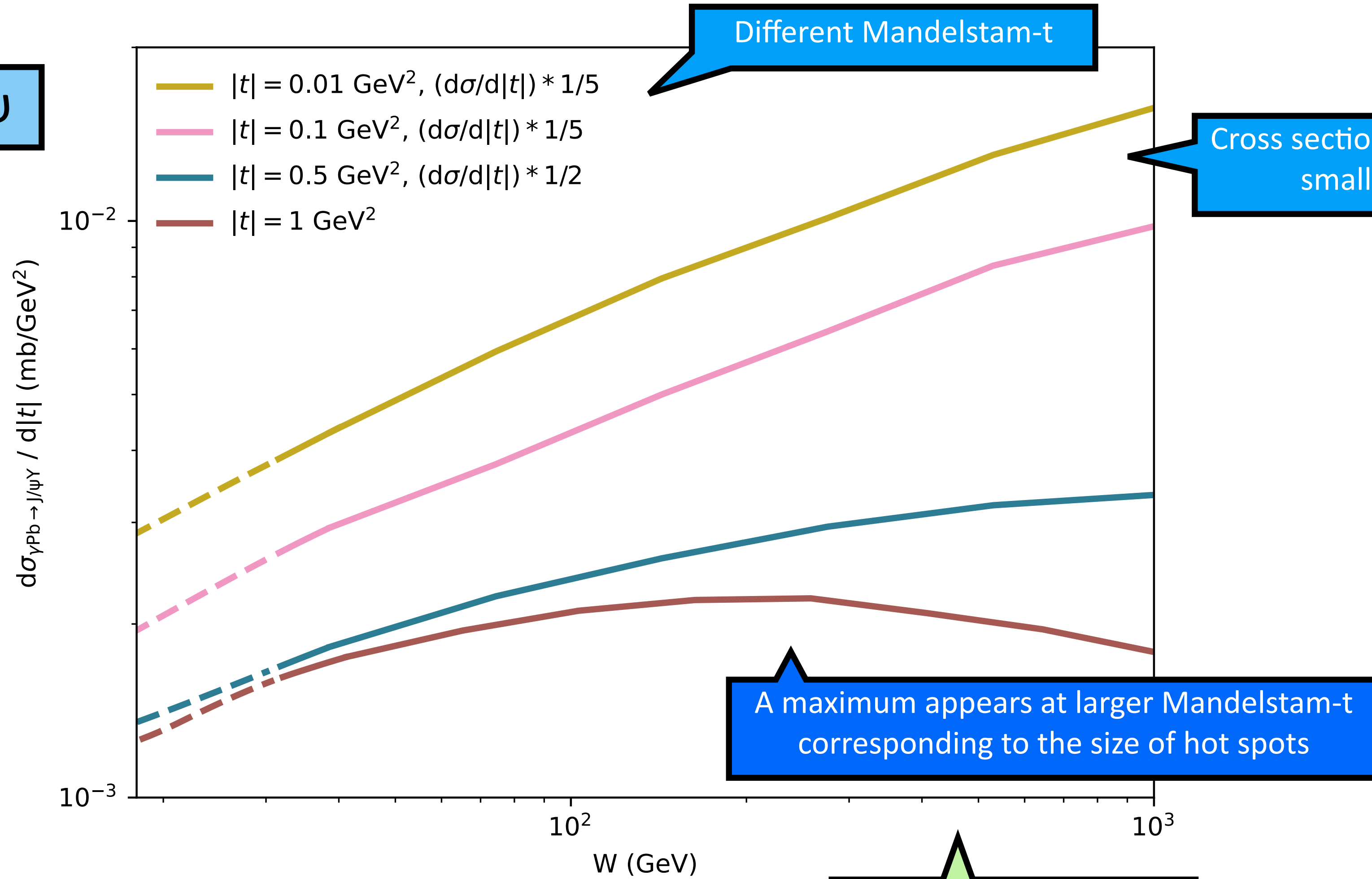
A maximum appears at larger Mandelstam-t corresponding to the size of hot spots

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J/ψ



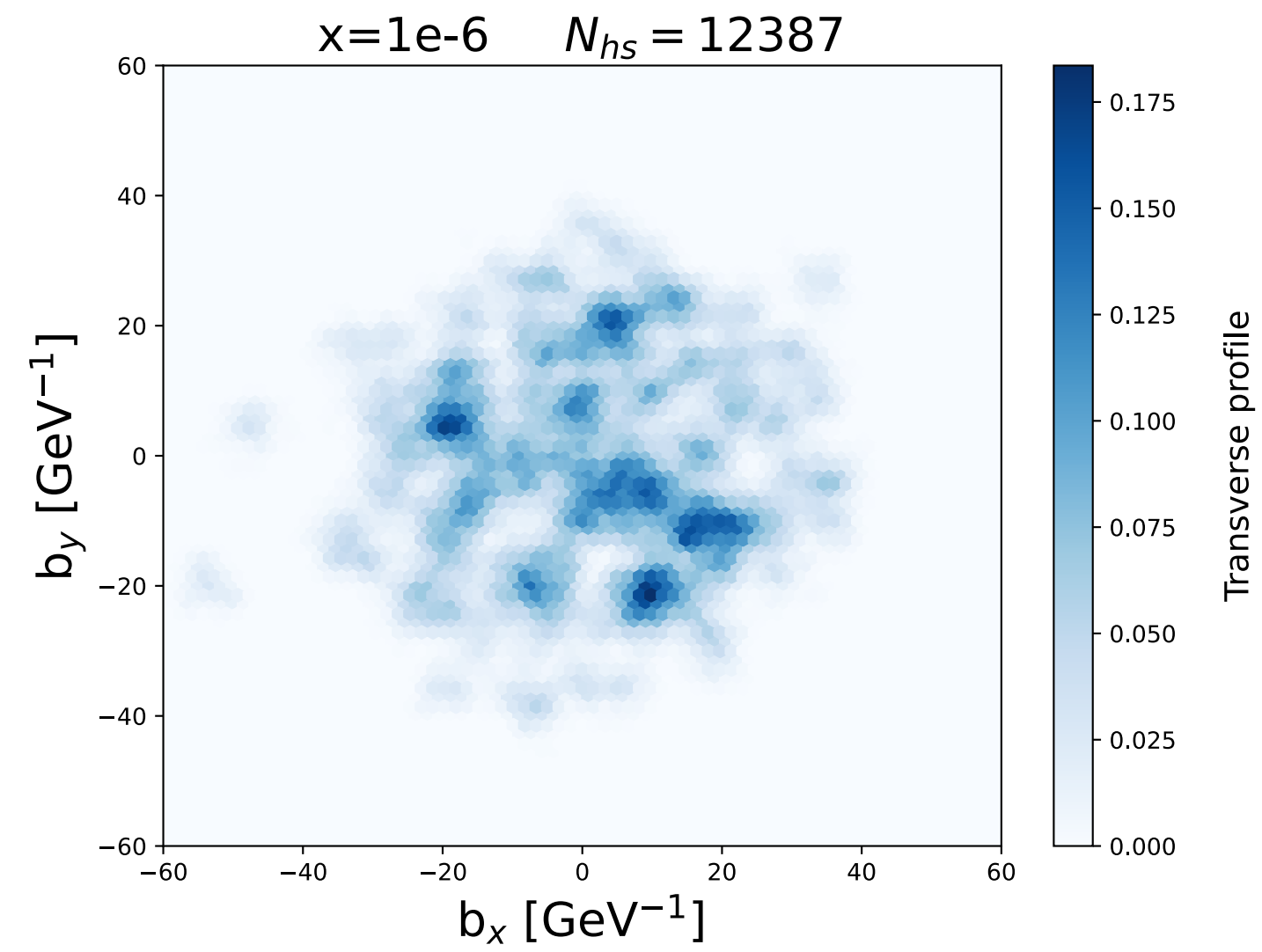
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Deep-inelastic scattering

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LHC

We propose to use incoherent J/ψ at large Mandelstam- t to search for the onset of saturation at the LHC