

A GUT FRAMEWORK FOR ACCIDENTAL DARK MATTER

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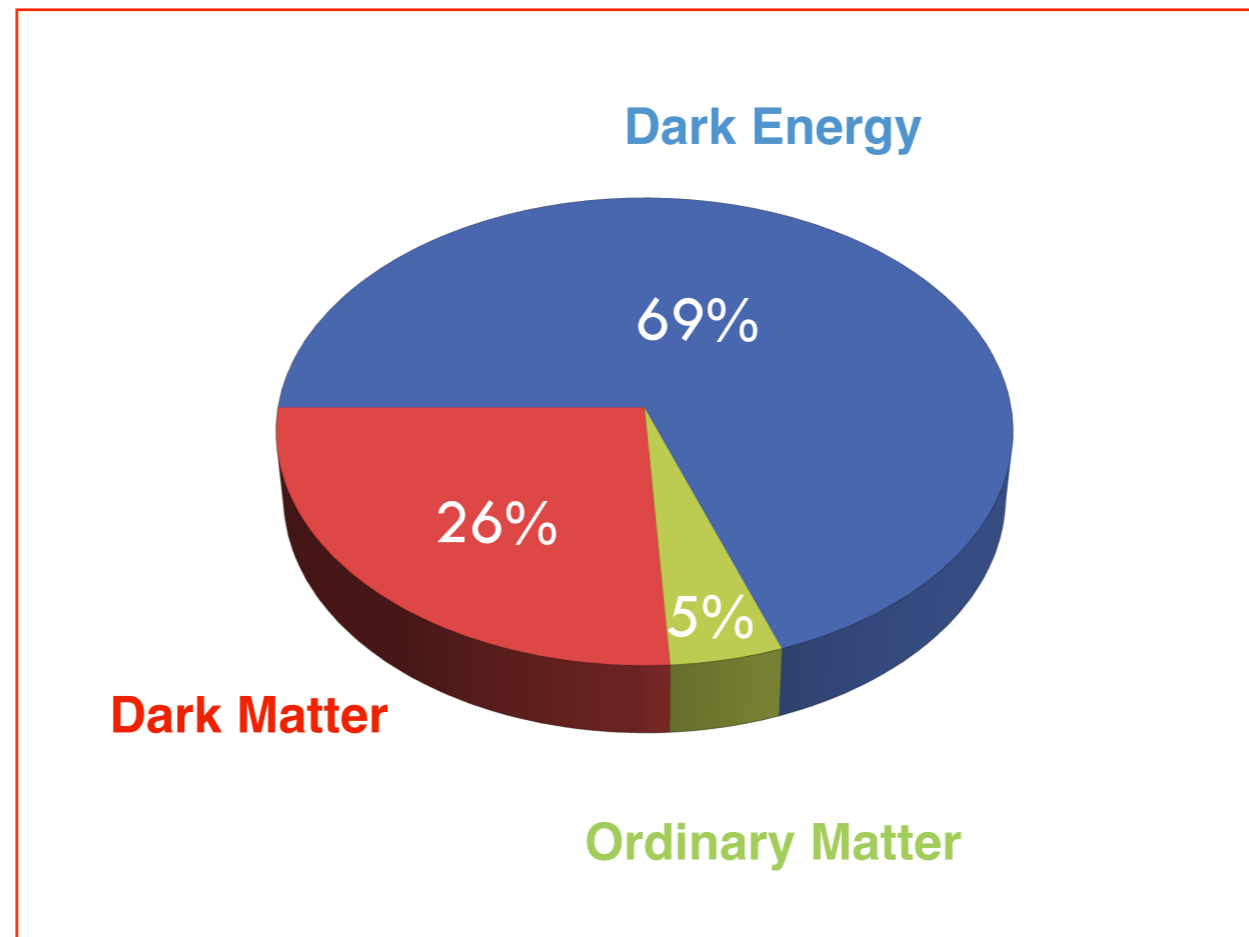
Based on:

S. Bottaro, R.C., S. Verma, work in progress

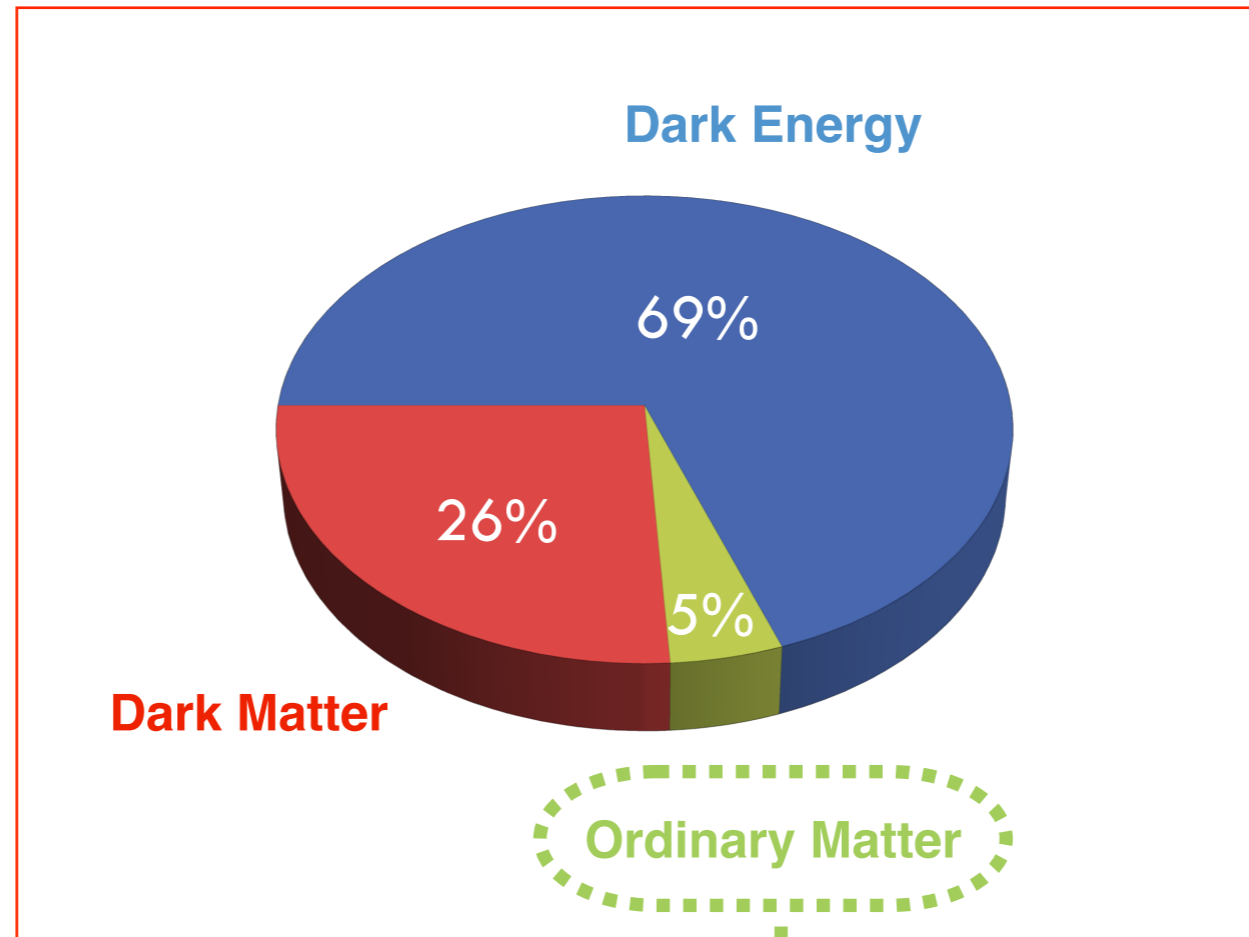
20th Rencontres du Vietnam “*BSM in Particle Physics and Cosmology*”

Quy Nhon, January 7-13, 2024

The Energy Budget of the Universe



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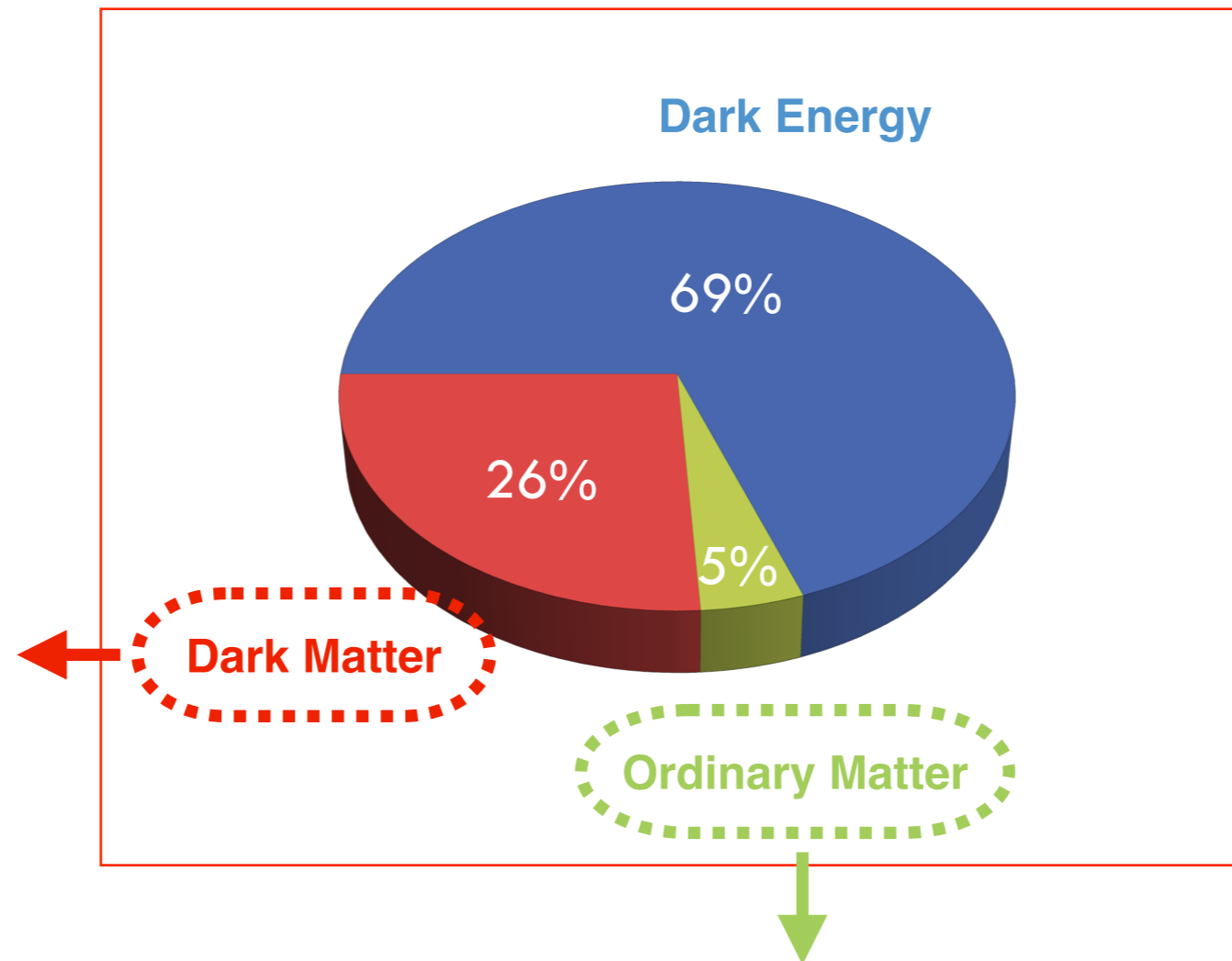


It exists thanks to proton stability, ultimately due to accidental baryon number conservation

The Energy Budget of the Universe



Can Dark Matter be stable due to its own accidental symmetry ?



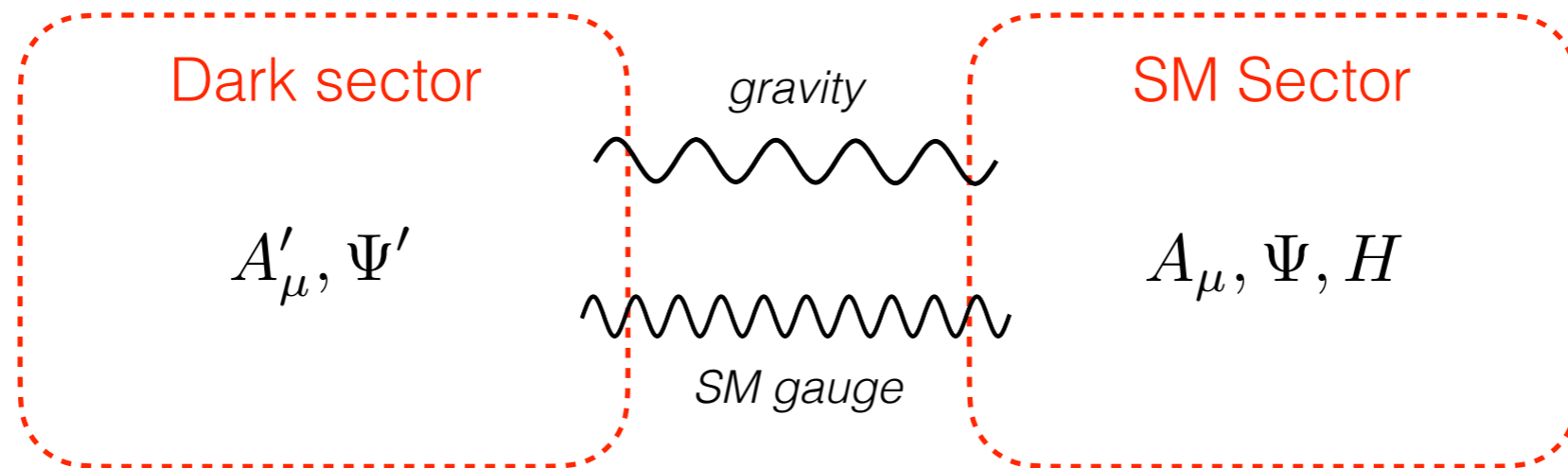
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Accidental vs Exact Global Symmetries



- ▶ Accidental symmetries are only approximate, emerge at low energy (large separation of scales required!) and do not characterize the UV fundamental dynamics
- ▶ Exact global symmetries are believed to be incompatible with quantum gravity and black holes
- ▶ Accidental symmetries are thus more theoretically satisfactory than imposing ad-hoc exact symmetries in the theory

Models of Accidental Dark Matter

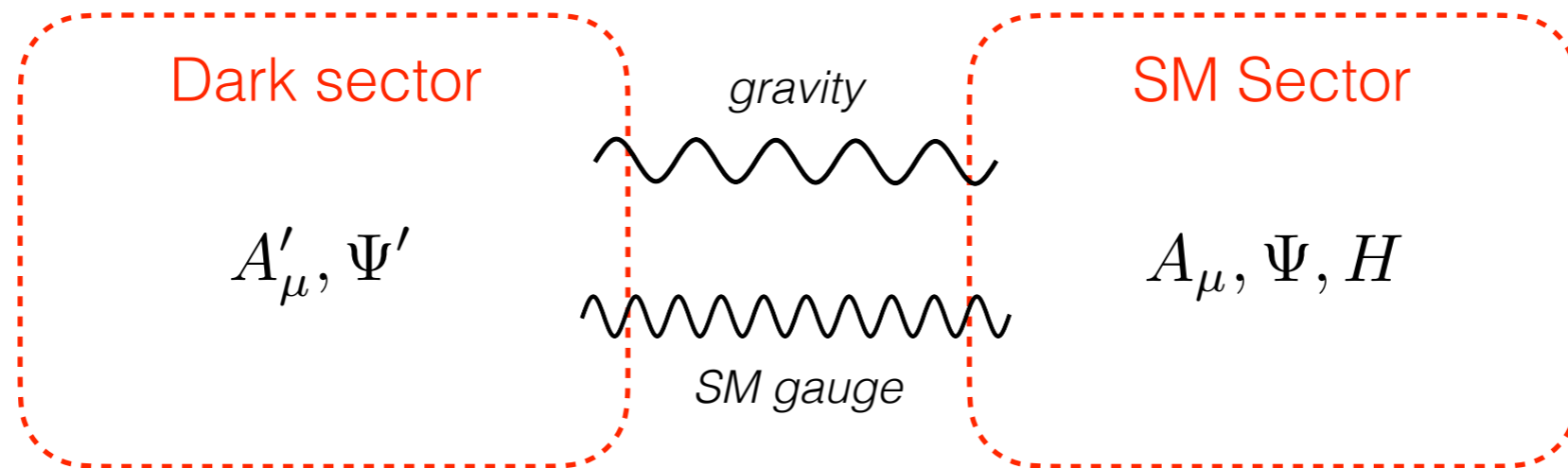


Postulate a new sector with **new matter** and/or **new dynamics**

Requirement:

Dark Sector contains (at least) one DM candidate that is cosmologically stable due to one of its accidental symmetries

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Accidental symmetries easily obtained from strongly-coupled dark sectors

If symmetry broken by operator with dimension D:

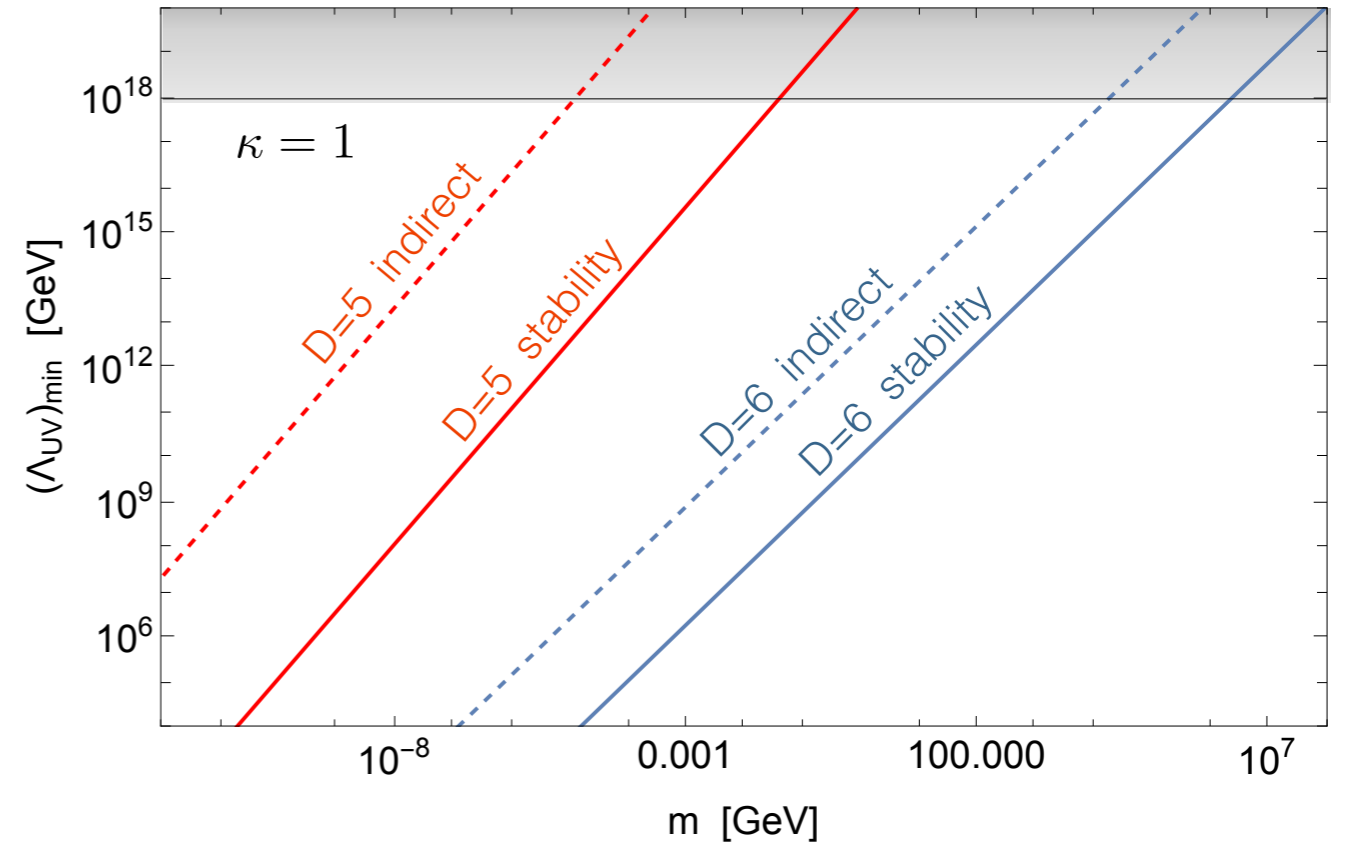
$$\Gamma \sim \frac{\kappa^2}{8\pi} \frac{m^{2D-7}}{\Lambda_{UV}^{2D-8}}$$

Cosmological stability:

$$\tau \gtrsim 10^{17} \text{ sec}$$

Bounds from CMB, 21cm, DM indirect detection:

$$\tau \gtrsim 10^{28} \text{ sec}$$



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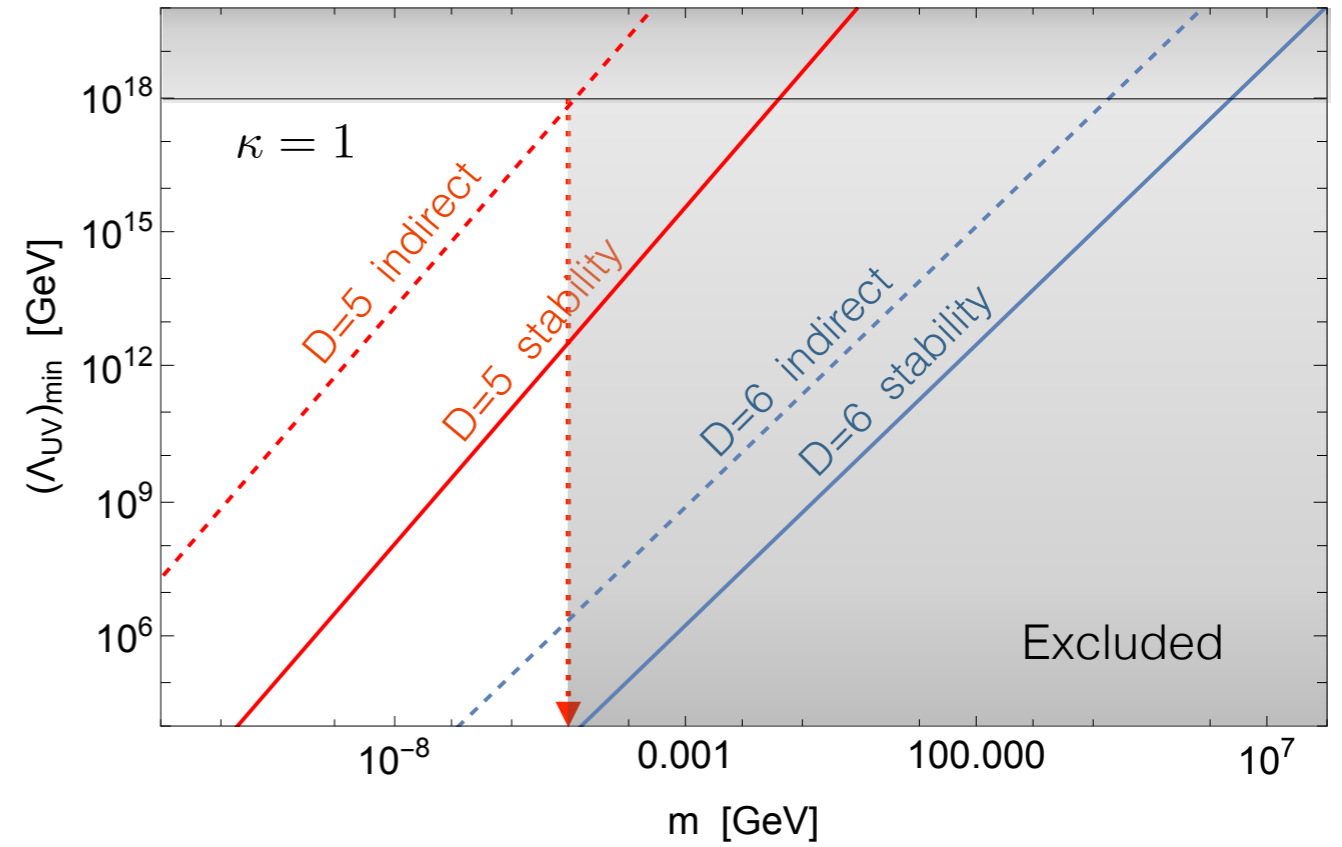
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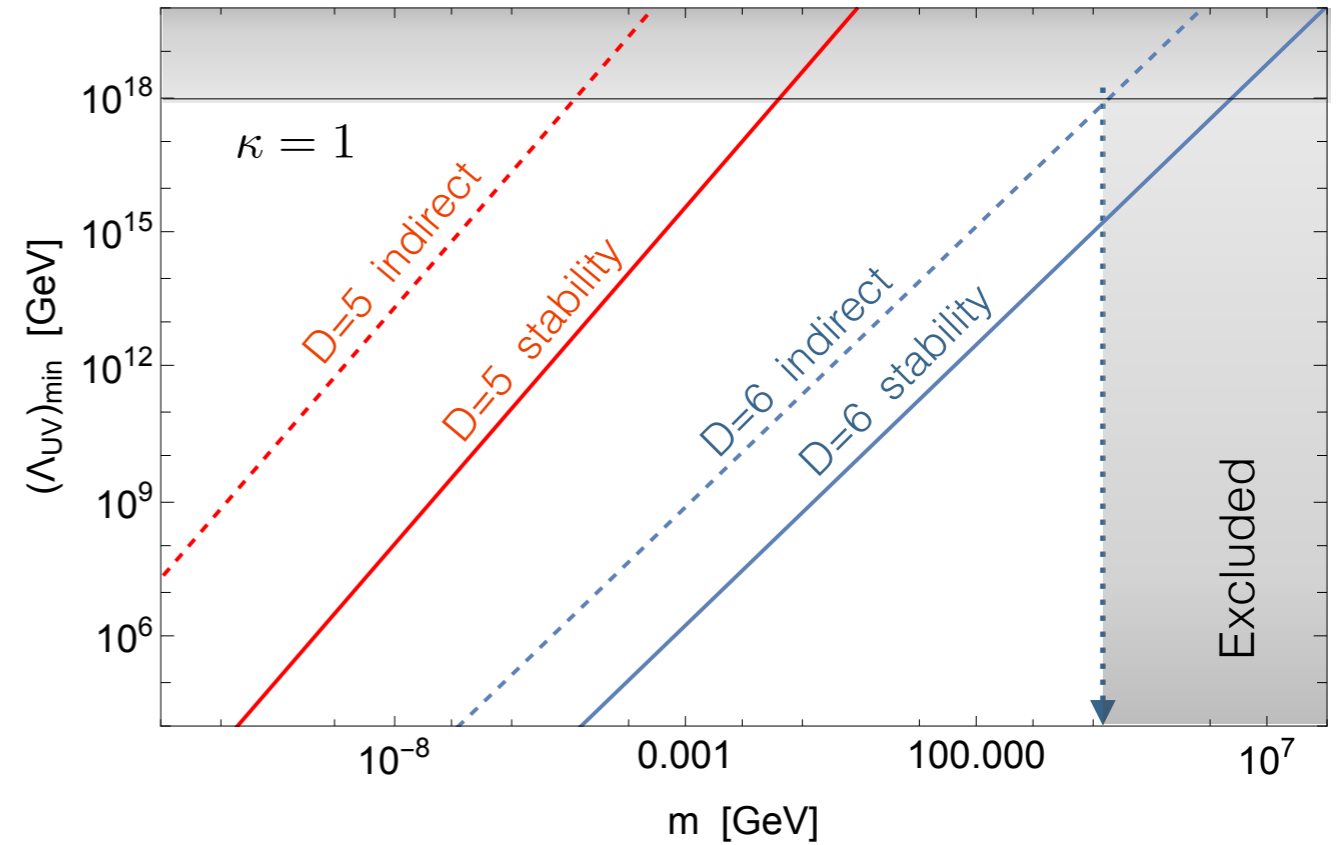
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- ▶ D=5 requires $m_{DM} \lesssim 10 \text{ keV}$
 - too light for a SM-charged sector

- ▶ D=6 requires $m_{DM} \lesssim 100 \text{ TeV}$
 - sufficiently heavy for SM-charged sector to have escaped detection
 - DM with $m_{DM} \sim 50 \text{ TeV}$ can be a thermal relic if strongly coupled

Dark Matter Sector: Vector-like Confining Gauge Theory

Kilic, Okui, Sundrum JHEP 1002 (2010) 018

Antipin, Redi, Strumia, Vigianni JHEP 1507 (2015) 039

Mitridate, Redi, Smirnov, Strumia, JHEP 10 (2017) 210

Gauge Group = $G_{DC} \times G_{SM}$ where $G_{DC} = SU(N)_{DC}$ or $SO(N)_{DC}$

Dark 'quarks' $Q = (\square, r)$ of $G_{DC} \times G_{SM}$, Dirac/Majorana if (\square, r) is complex/real

$$\mathcal{L} = -\frac{1}{4g_{DC}^2} \mathcal{G}_{\mu\nu}^2 + \bar{Q} (i\not{D} - M) Q + y \bar{Q} H Q + h.c.$$

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- Accidental dark baryon number $U(1)_{DB}$, broken at $D \geq 6$

Lightest dark baryon stable and good DM candidate $\mathcal{B} \sim (QQ \cdots Q)$

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Lightest dark baryon stable and good DM candidate $\mathcal{B} \sim (QQ \cdots Q)$

- Accidental species numbers, broken at $D \geq 5$

Long-lived mesons not good DM candidates, must decay before BBN $\pi \sim \bar{Q}_i Q_j$

Request: DM model must be embeddable into SU(5) GUT

$$\mathcal{L}_{DM} = -\frac{1}{4g_{DC}^2} \mathcal{G}_{\mu\nu}^2 + \sum_i \bar{Q}^i (i\not{D} - m_Q) Q^j + y_{ij}^L \bar{Q}^i H P_L Q^j + y_{ij}^R \bar{Q}^i H P_R Q^j + \text{h.c.}$$



sum over SU(5)
fragments

Q^i	$SU(5)$	SM Quantum Numbers
N	1	$(1, 1, 0)$
$D \oplus L$	$\bar{5}$	$(\bar{3}, 1, 1/3) \oplus (1, 2, -1/2)$
$U \oplus E \oplus Q$	10	$(\bar{3}, 1, -2/3) \oplus (1, 1, 1) \oplus (3, 2, 1/6)$
$Q \oplus T \oplus S$	15	$(3, 2, 1/6) \oplus (1, 3, 1) \oplus (6, 1, -2/3)$
$V \oplus G \oplus X \oplus N$	24	$(1, 3, 0) \oplus (8, 1, 0) \oplus (\bar{3}, 2, 5/6) \oplus (1, 1, 0)$

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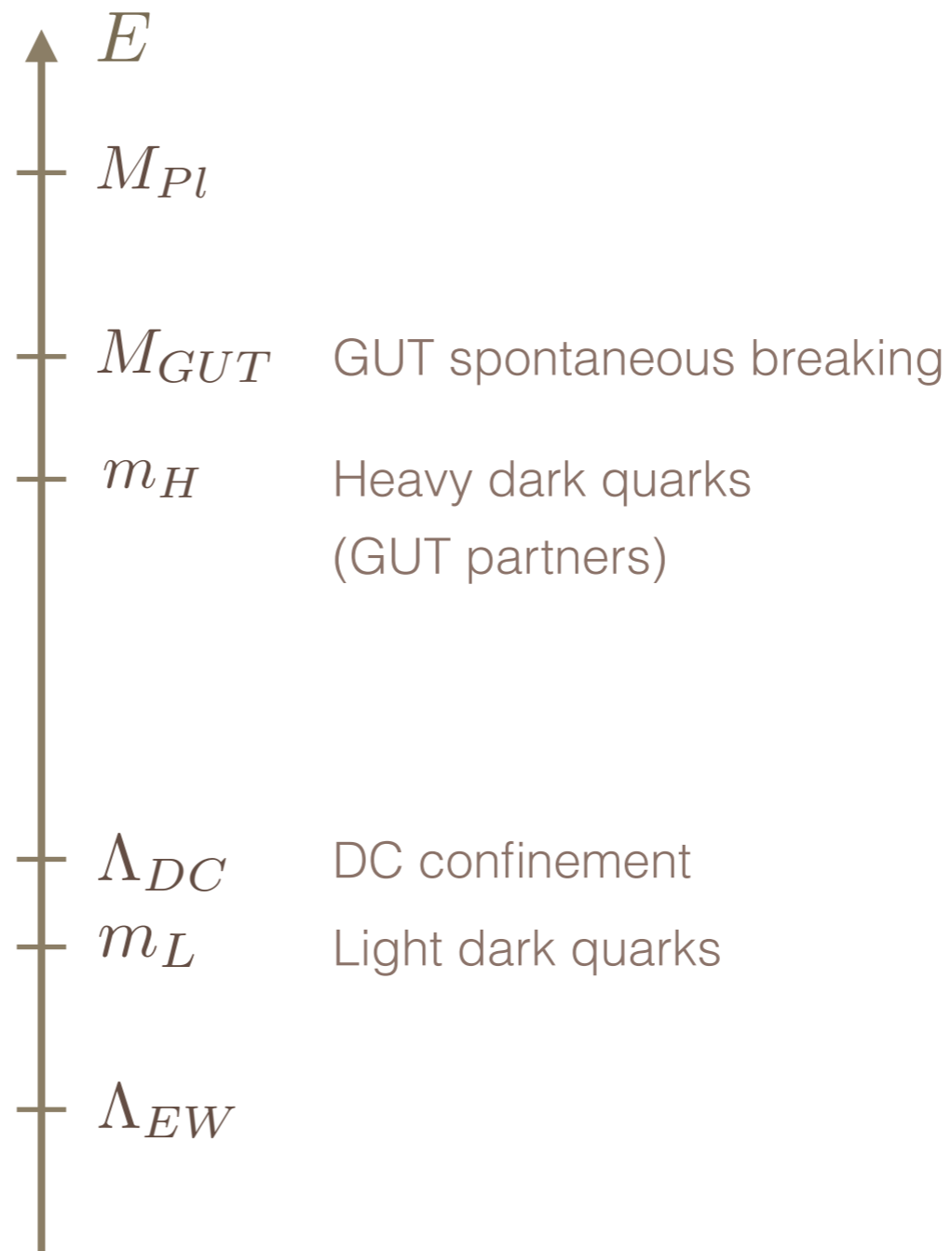
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Example: $Q + \tilde{D}$ model with $G_{DC} = SU(3)_{DC}$

- 1 Yukawa: $\mathcal{L}_Y = \bar{Q} H \tilde{D} + h.c.$ No accidental species number
- DM candidate: $QQ\tilde{D}$

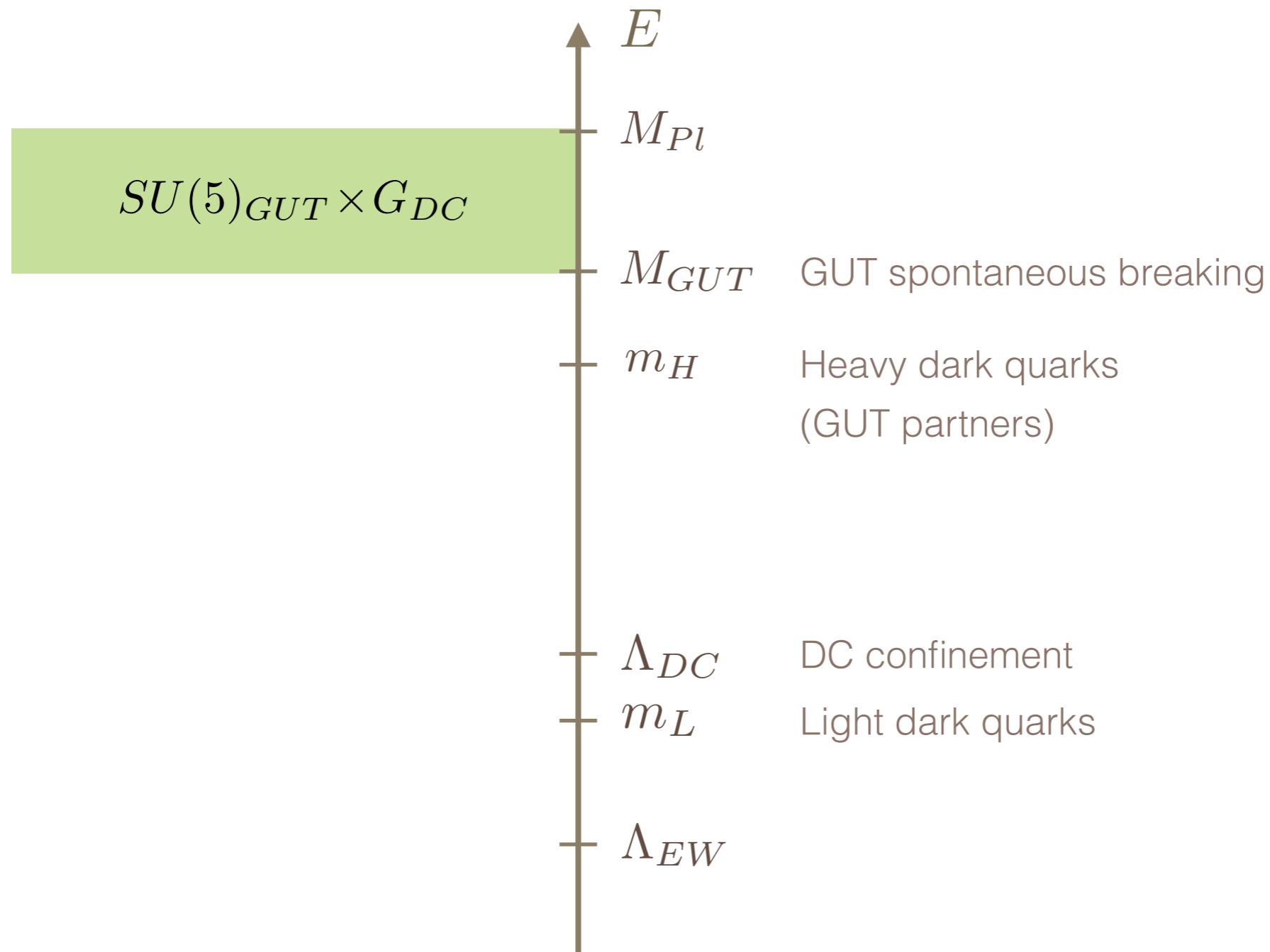
UV completing DM models into SU(5) GUT

Bottaro, R.C., Verma, work in progress



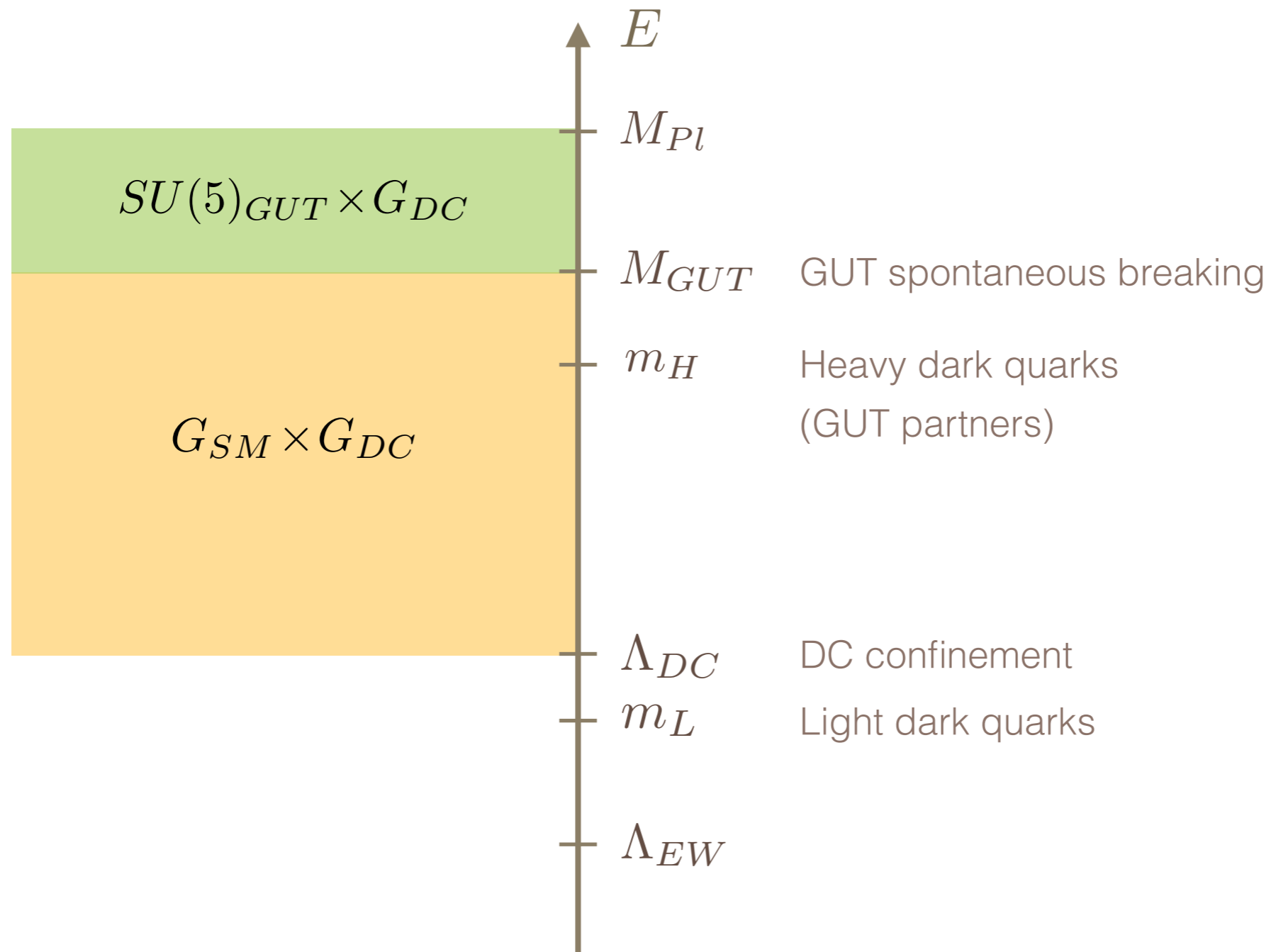
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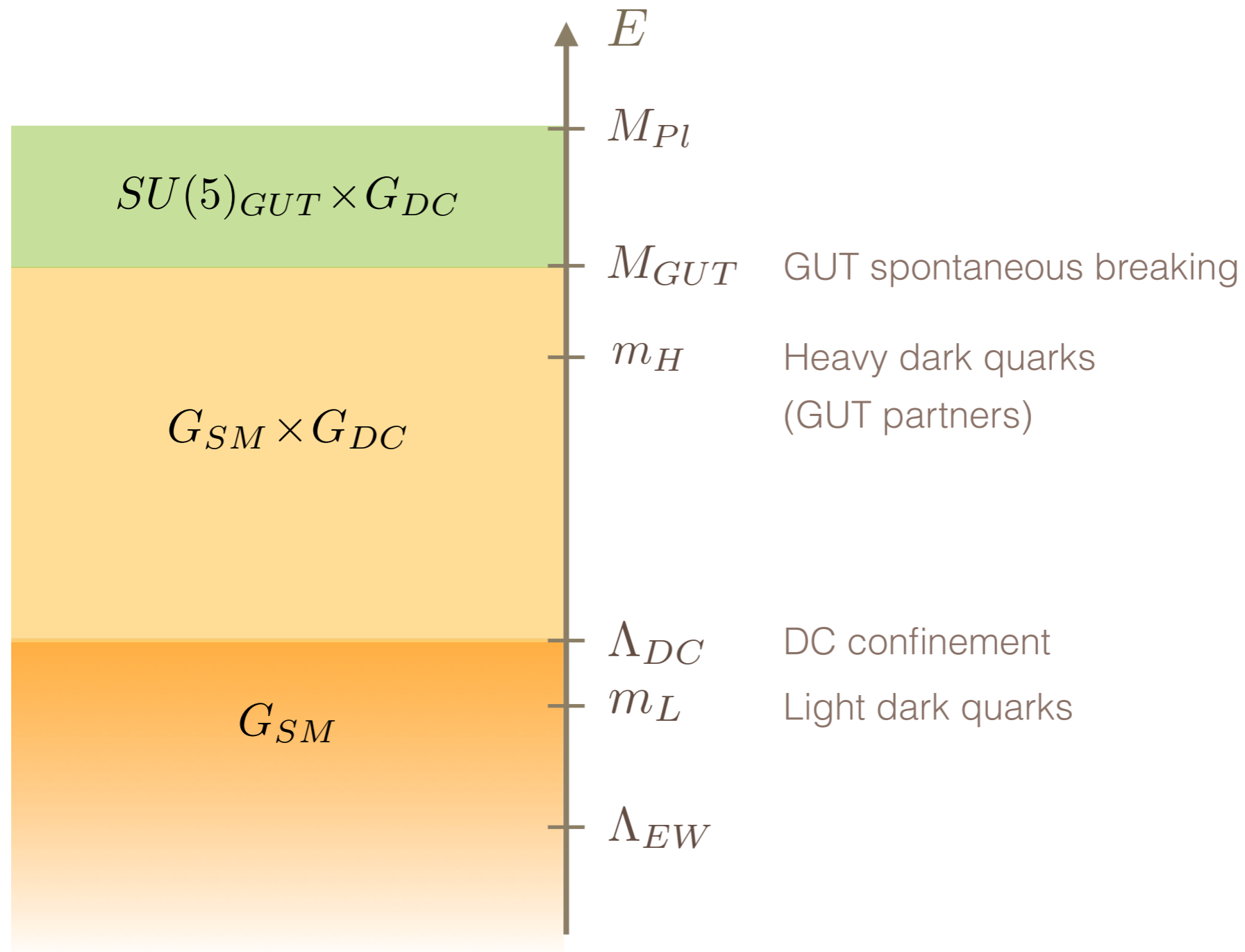
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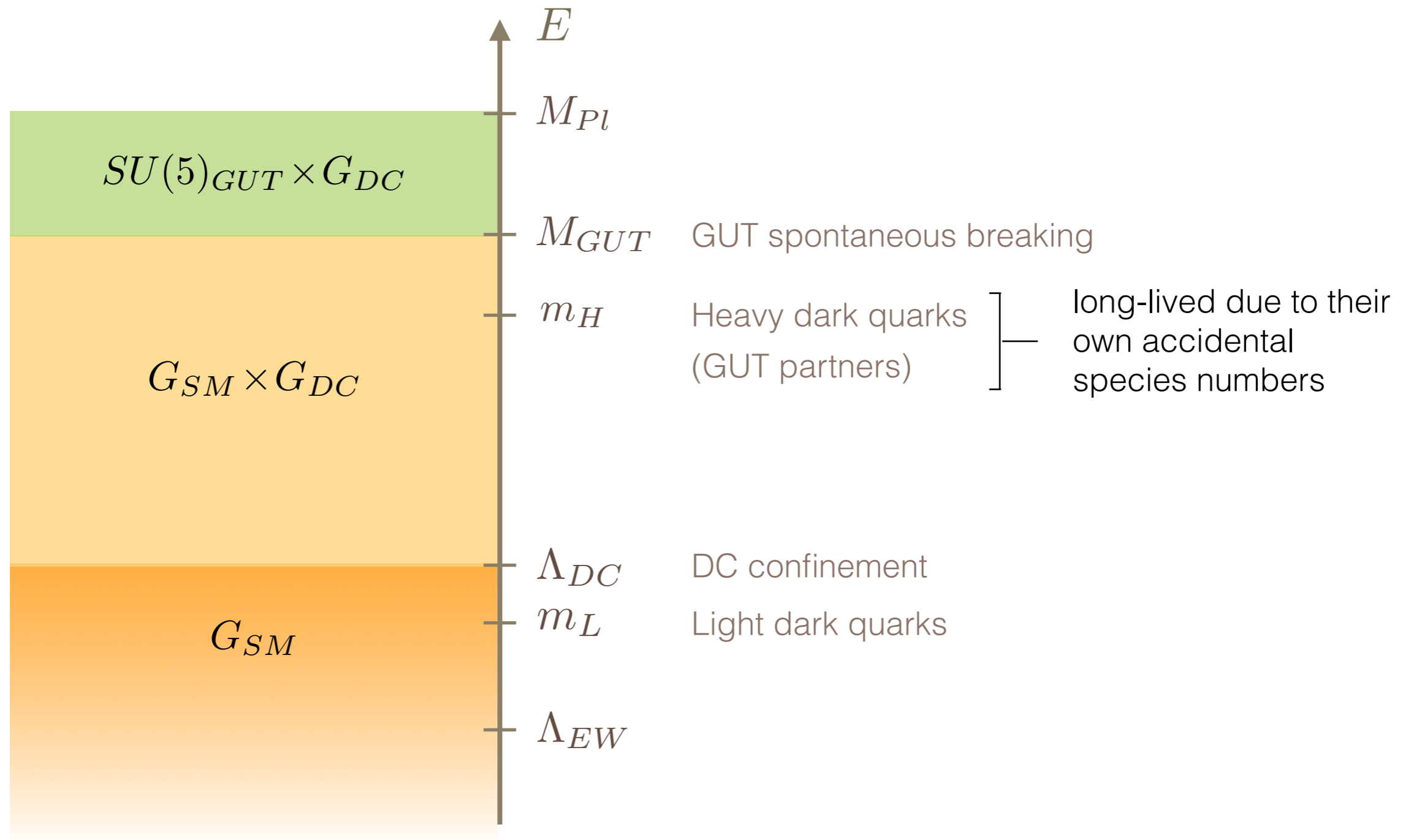
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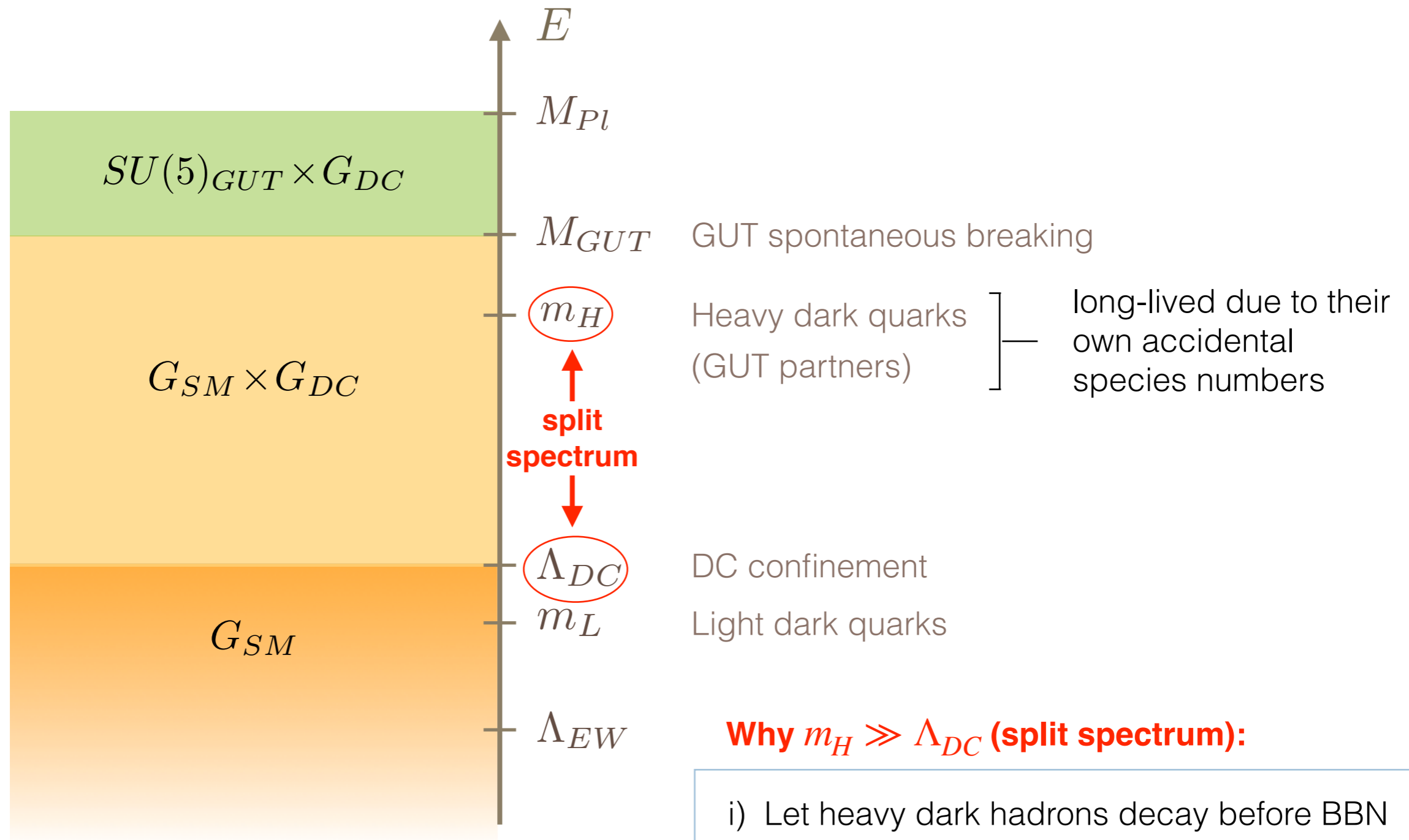
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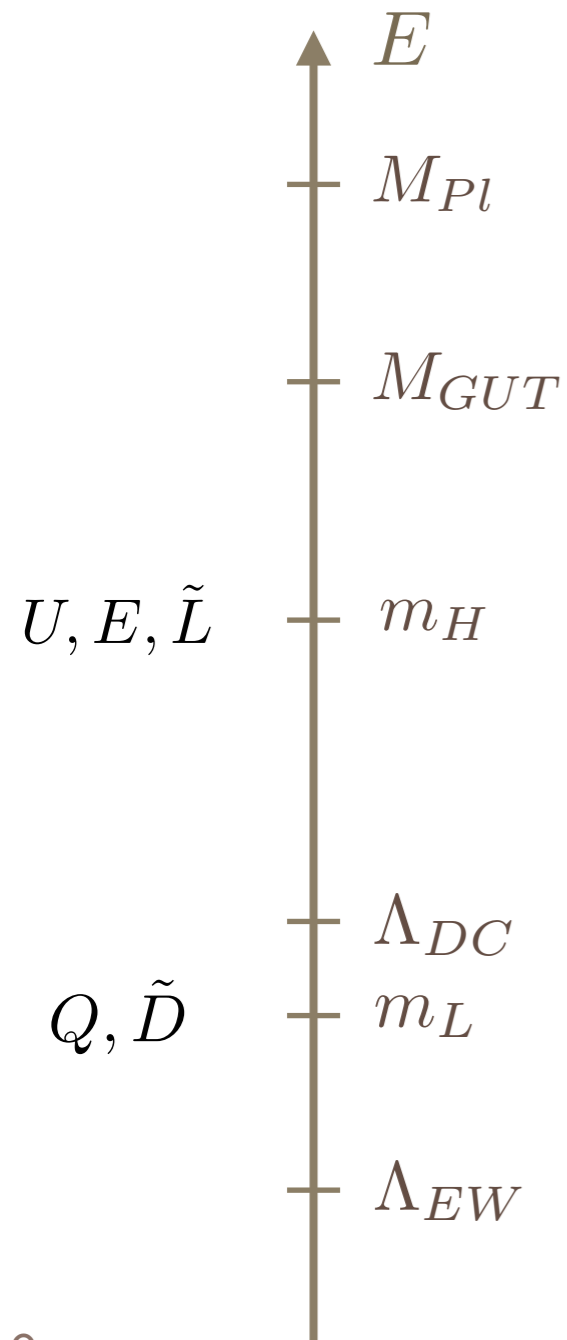


Mass Spectrum and Naturalness

Ex: $Q + \tilde{D}$ model from $5 \oplus 10$ GUT theory

$$\psi_5 = \tilde{D} \oplus \tilde{L} \quad \psi_{10} = Q \oplus U \oplus E$$

$$\mathcal{L} \supset -m_5 \bar{\psi}_5 \psi_5 - m_{10} \bar{\psi}_{10} \psi_{10} - y_5 \bar{\psi}_5 \Phi_{24} \psi_5 - y_{10} \bar{\psi}_{10} \Phi_{24} \psi_{10} \\ - y_L \bar{\psi}_5 \phi_5^\dagger P_R \psi_{10} - y_R \bar{\psi}_5 \phi_5^\dagger P_L \psi_{10} + h.c.$$

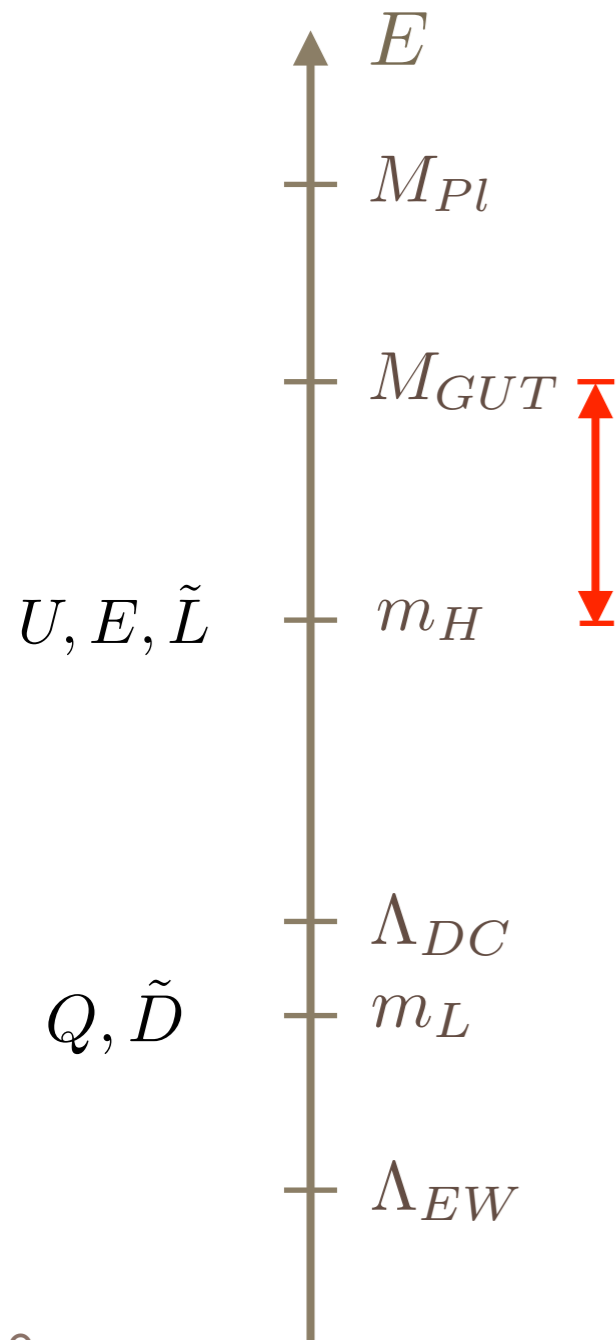


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Hierarchy $m_{U,E,\tilde{L}} \ll M_{GUT}$ is technically natural for $y_5, y_{10} \ll 1$

$m_{5,10}, y_{5,10}$ are the only spurions under $U(1)_L \times U(1)_R$:

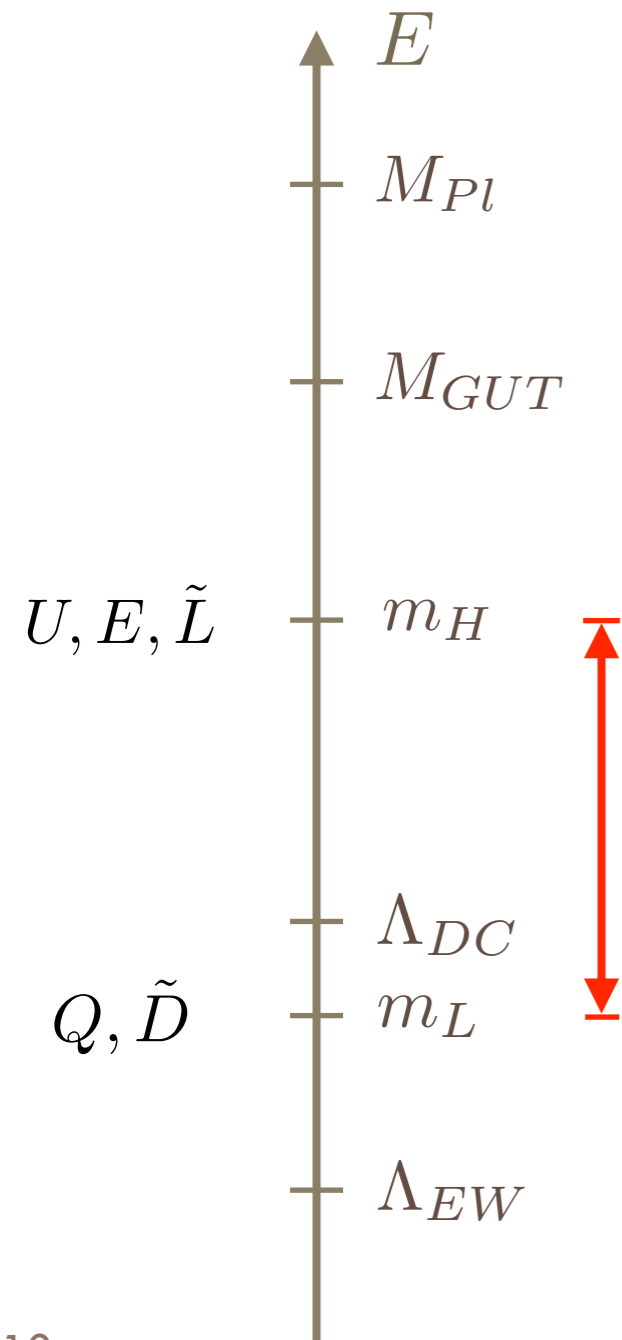
$$U(1)_L : \begin{cases} \psi_{5L} \rightarrow e^{i\alpha} \psi_{5L} \\ \psi_{10R} \rightarrow e^{i\alpha} \psi_{10R} \end{cases} \quad U(1)_R : \begin{cases} \psi_{5R} \rightarrow e^{i\beta} \psi_{5R} \\ \psi_{10L} \rightarrow e^{i\beta} \psi_{10L} \end{cases}$$

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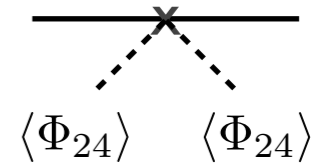
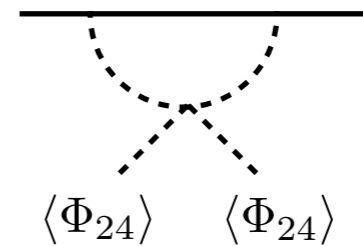


Hierarchy $m_{Q, \tilde{D}} \ll m_{U, E, \tilde{L}}$ requires *two* fine tunings

$$\bar{\psi}_5 \mathcal{M}_5 \psi_5$$

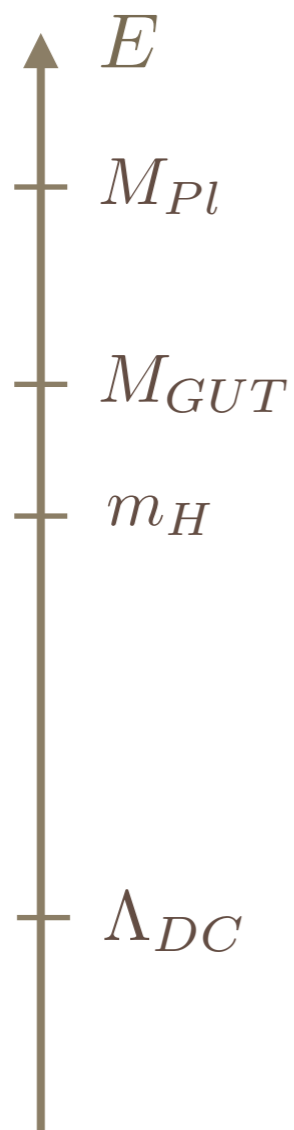
$$\mathcal{M}_5 = m_1 \mathbb{1} + m_{24} \langle \Phi_{24} \rangle$$

$$-\frac{2}{5} - \sqrt{\frac{6}{5}} \frac{m_1}{m_{24}} \simeq \frac{m_{\tilde{D}}}{m_{\tilde{L}}} \ll 1$$



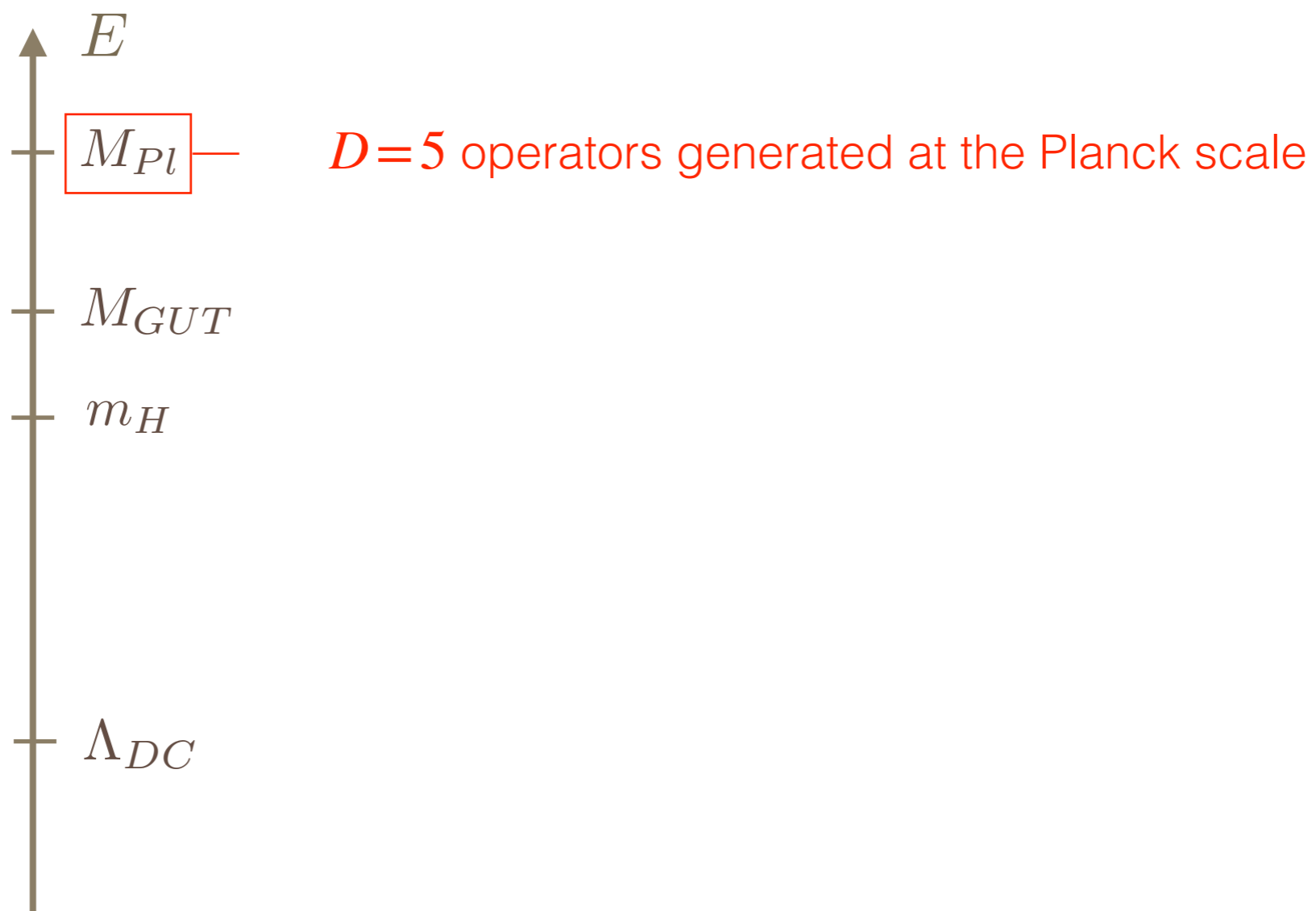
Viable Species Number-Breaking Operators

- All long-lived mesons must decay before BBN $\tau \sim \left(\frac{\kappa^2 m^{2D-7}}{8\pi \Lambda_{UV}^{2D-8}} \right)^{-1} < 1 \text{ sec}$



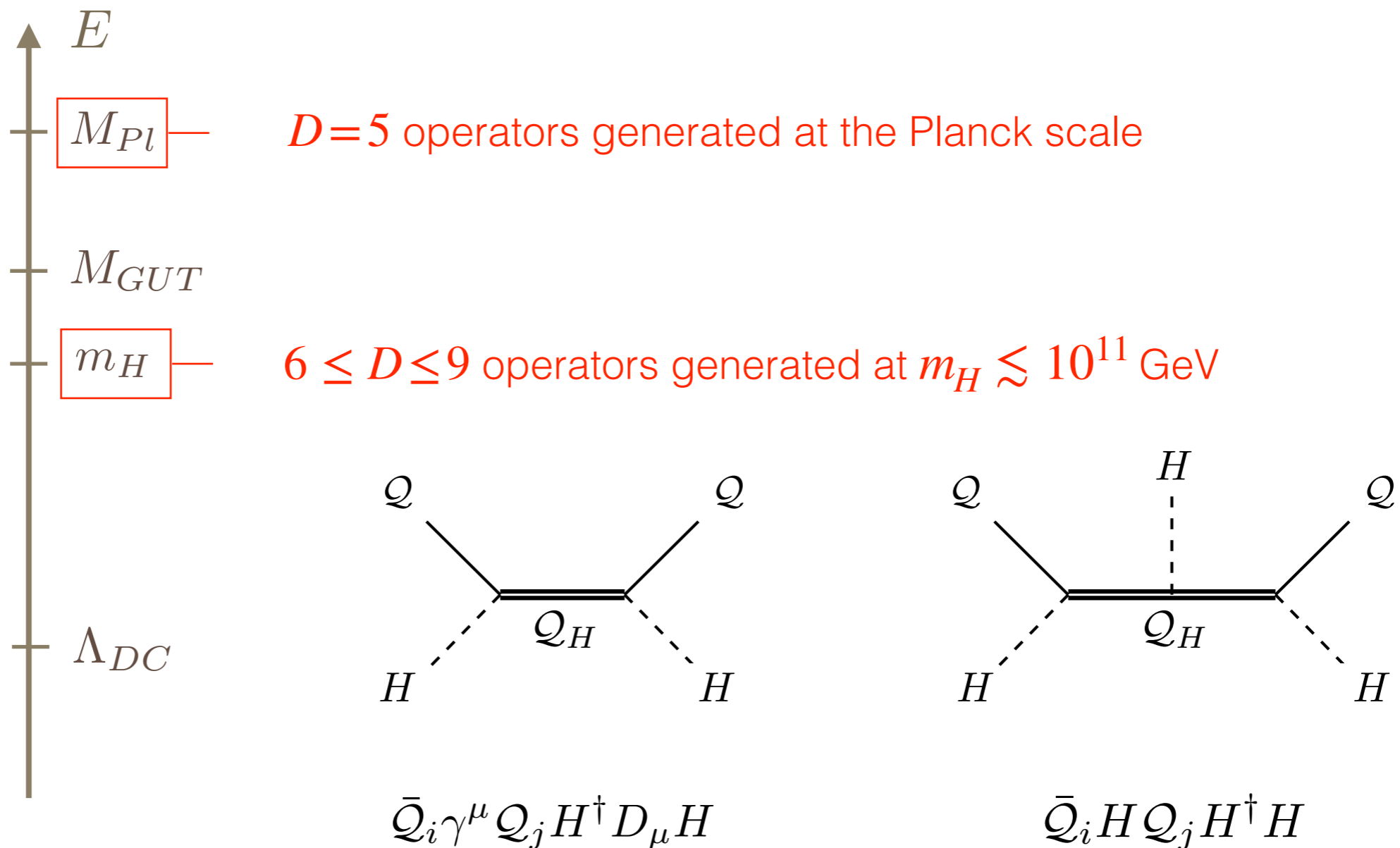
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Minimal Parent Theories

- For each DM model one can identify one or more Minimal Parent Theories

Minimal Parent Theory = minimal GUT field content that reproduces the field content of the low-energy theory *and breaks all its accidental species numbers.*

Acceptable Minimal Parent Theories have

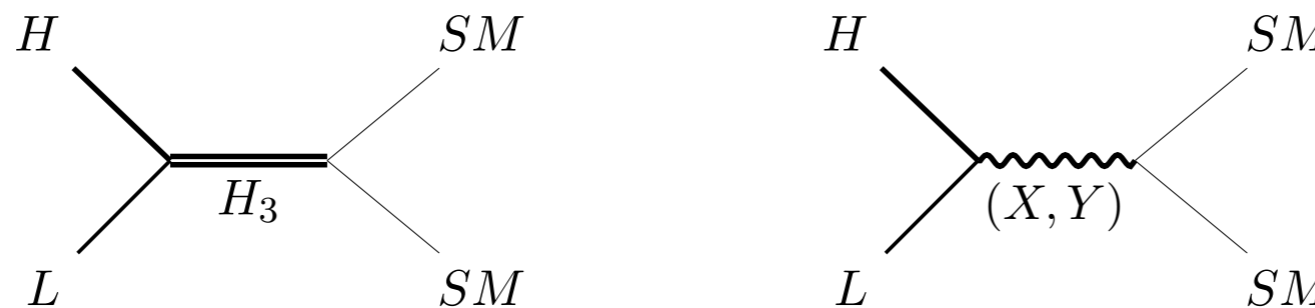
- i) no accidental species numbers
- OR
- ii) accidental species numbers broken at the D=5 level; the inherited species numbers of the low-energy theory must also be broken at the D=5 level

Minimal Parent Theories

- Example: $Q \oplus \tilde{D} \rightarrow 10 \oplus 5$

- ▶ GUT theory has 1 Yukawa $\mathcal{L}_Y = \bar{\psi}_{10} \phi_5^\dagger \psi_5 + h.c.$ hence no accidental species number
- ▶ DM sector ($Q + \tilde{D}$) has 1 Yukawa $\mathcal{L}_Y = \bar{Q} H \tilde{D} + h.c.$ hence no accidental species number
- ▶ Theory below MGUT has 3 more fields ($U + E + \tilde{L}$) and 1 more Yukawa $\mathcal{L}_Y \supset \bar{E} H \tilde{L}$

Two accidental species numbers ($U(1)_{DL}, U(1)_U$), heavy hadrons are metastable and decay through D=6 operators generated at the GUT scale



Selecting Viable Theories

We select theories that satisfy the following criteria:

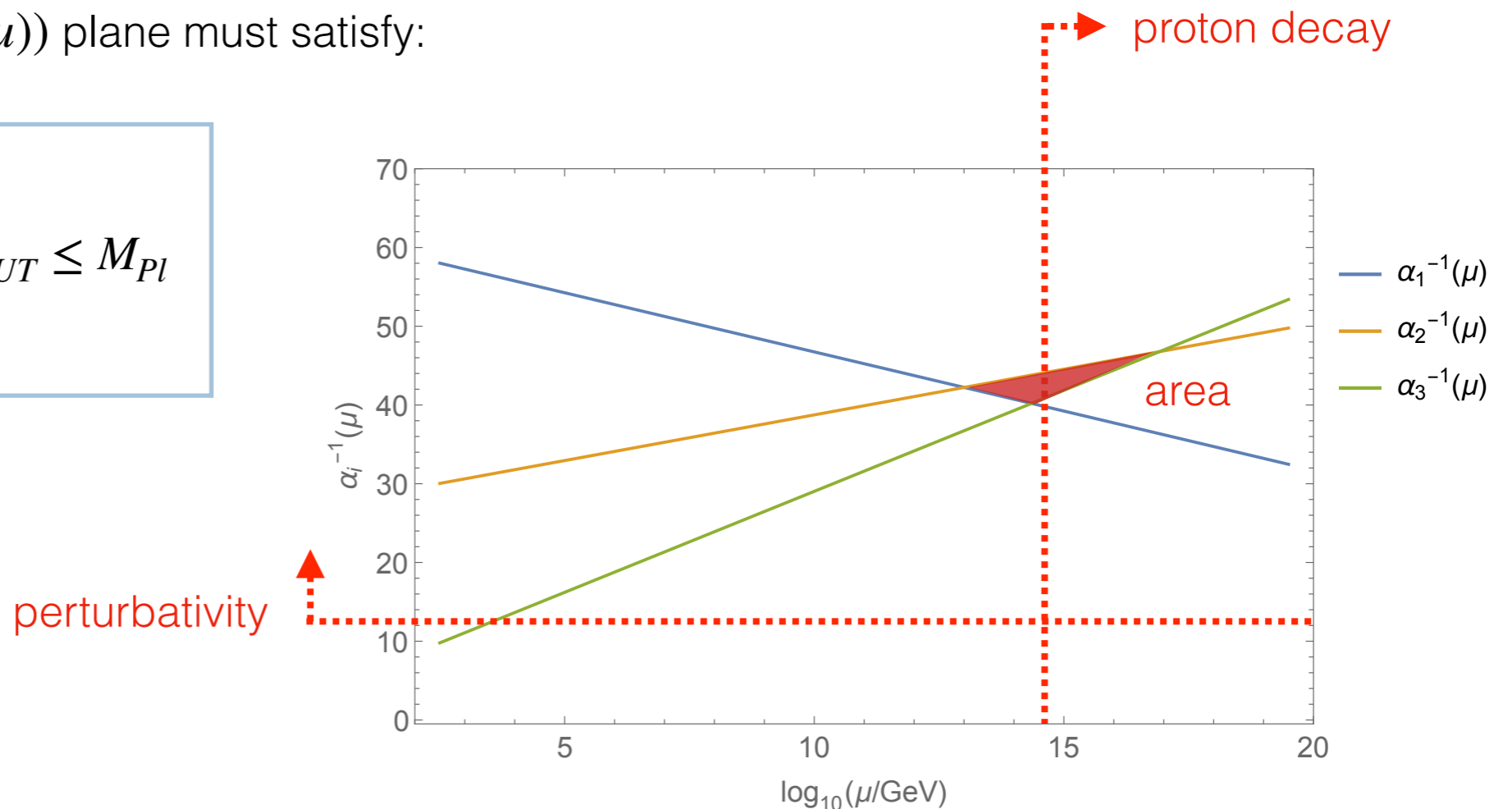
1. $SU(N_{DC})$ must confine
2. Light quark sector must contain a viable DM candidate
3. No Landau poles of $SU(5)_{GUT} \times SU(N_{DC})$ below M_{Pl}
4. Quality of unification as in the SM or better;

Triangle in the $(\mu, \alpha^{-1}(\mu))$ plane must satisfy:

$$\text{Area} \leq \text{Area}^{\text{SM}}$$

$$6.5 \times 10^{14} \text{GeV} \leq M_{GUT} \leq M_{Pl}$$

$$\alpha_{GUT} < 4\pi$$



We find only two viable theories:

- $Q \oplus \tilde{D}$

Minimal Parent theory: $10 \oplus 5$

$$7 \times 10^6 \text{ GeV} < m_H < 5 \times 10^{14} \text{ GeV}$$

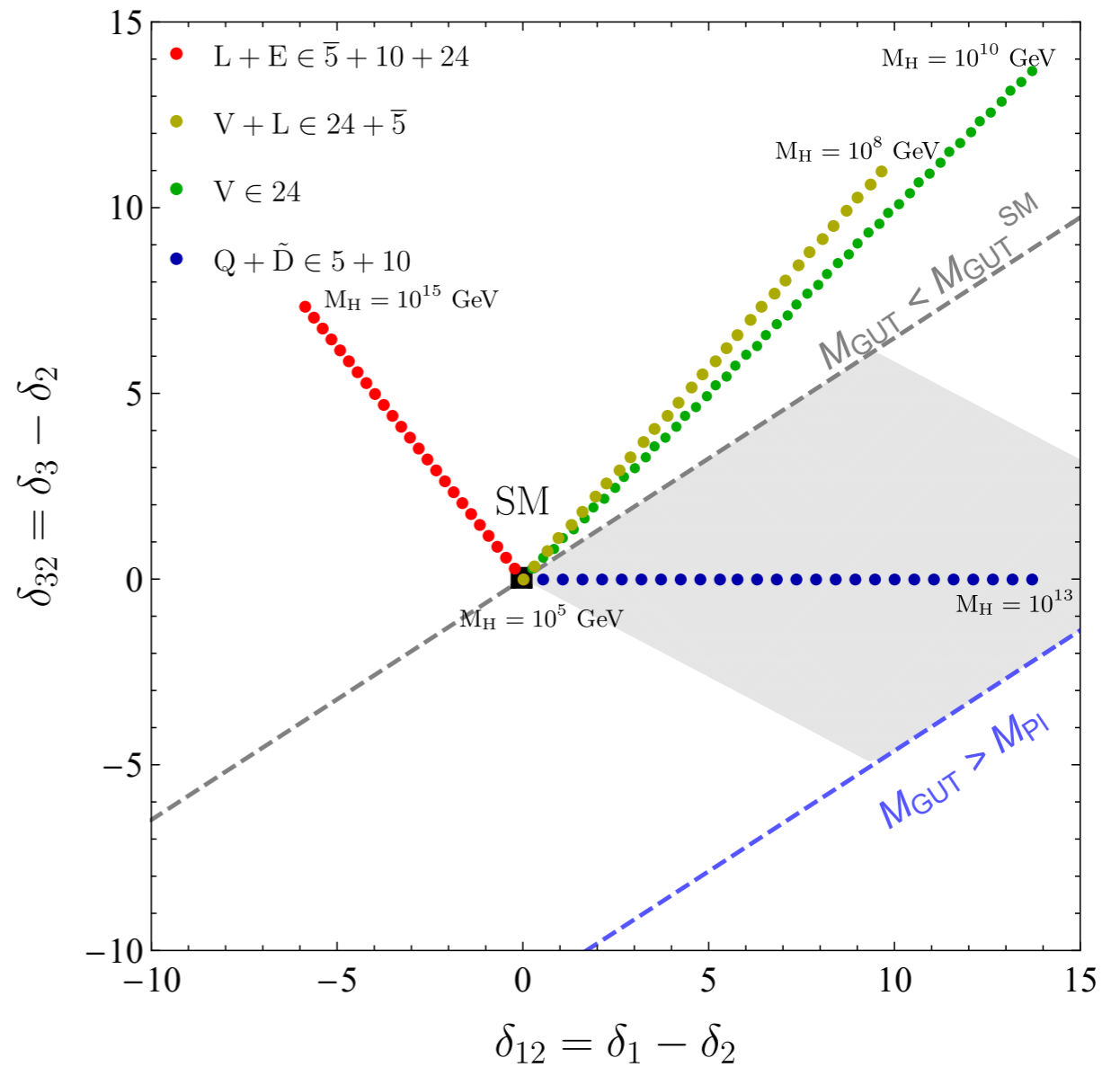
Minimal Parent theory: $15 \oplus 5$

$$4 \times 10^{11} \text{ GeV} < m_H < 5 \times 10^{14} \text{ GeV}$$

- N

Minimal Parent theory: 24

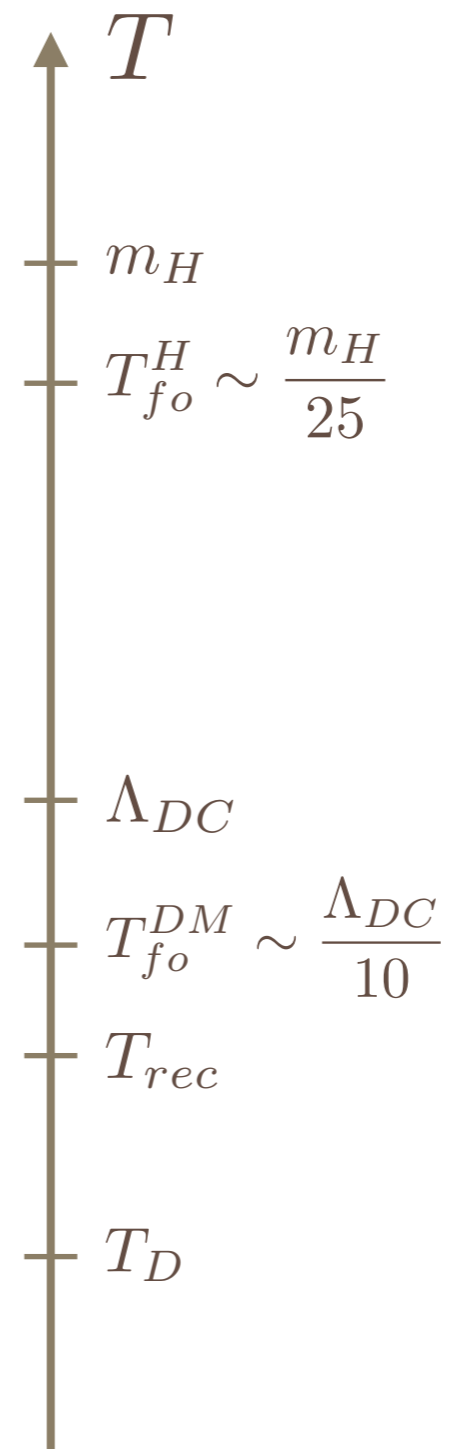
$$m_H > 10^9 \text{ GeV}$$



$$\alpha_i(\mu)^{-1} = \alpha_i(M_Z)^{-1} - \frac{b_i^{\text{SM}}}{2\pi} \log \frac{\mu}{M_Z} + \delta_i$$

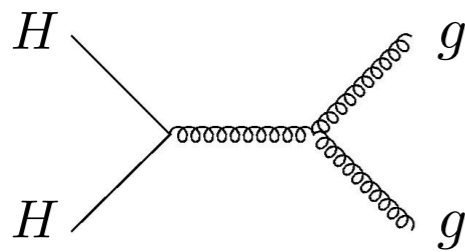
$$\delta_i = -\frac{\Delta\beta_i^L}{2\pi} \log \frac{\mu}{\Lambda_{DC}} - \frac{\Delta\beta^H}{2\pi} \log \frac{\mu}{m_H}$$

Thermal history of the dark color states

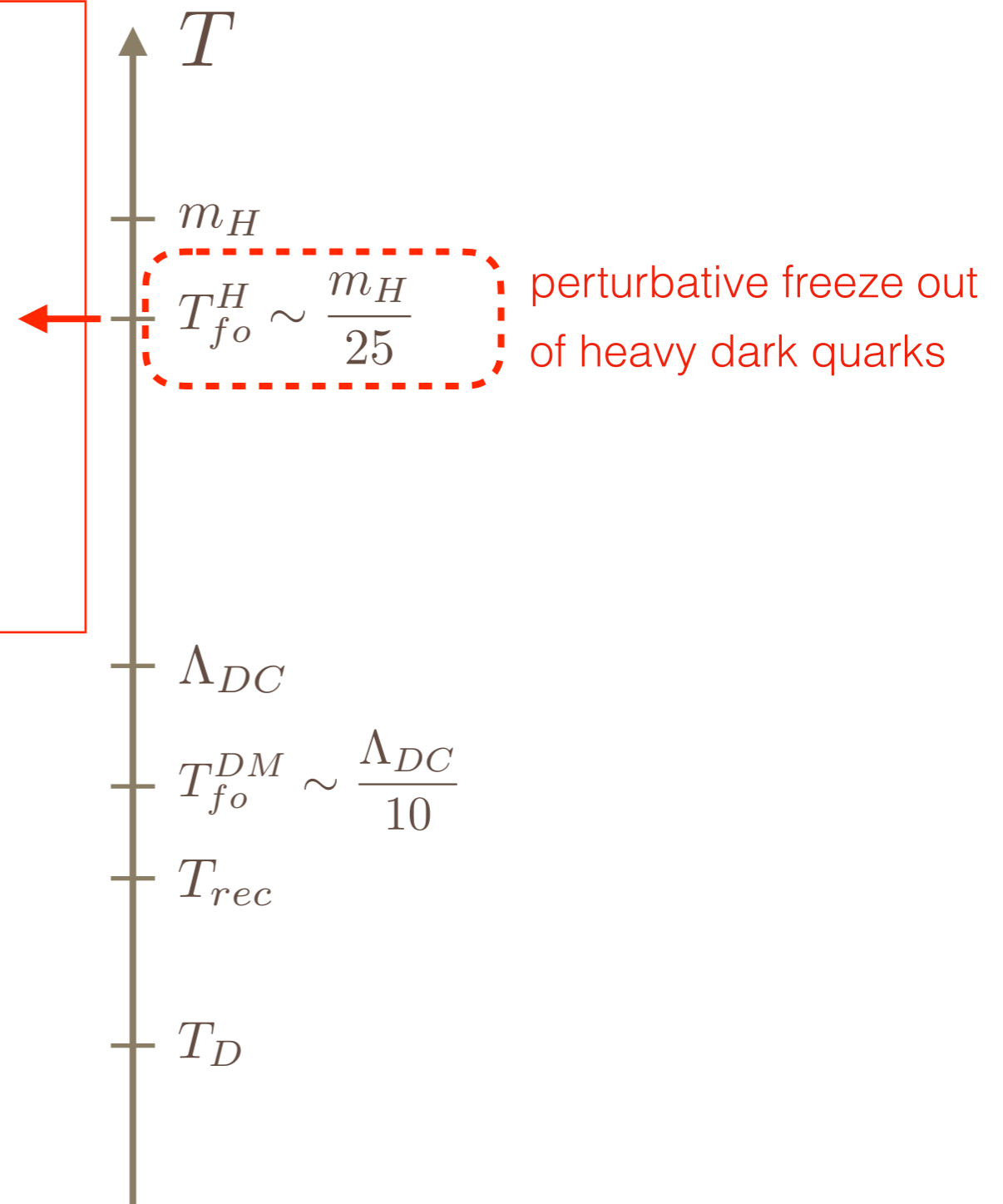


Thermal history of the dark color states

At $T \sim m_H/25$ heavy dark quarks undergo a first perturbative freeze out



$$\langle \sigma v \rangle \sim \frac{\pi \alpha_{DC}^2}{m_H^2}$$



Thermal history of the dark color states

At temperatures of order Λ_{DC} various types of dark color bound states are formed:

- ▶ Light hadrons

$L\bar{L}\bar{L}, L\bar{L}$

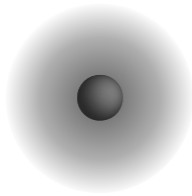


$$r_0 \sim 1/\Lambda_{DC}$$

$$m \sim \Lambda_{DC}$$

- ▶ Hybrid hadrons

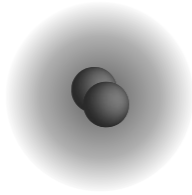
$H\bar{L}\bar{L}, H\bar{L}$
(type I)



$$r_0 \sim 1/\Lambda_{DC}$$

$$m \sim m_H + O(\Lambda_{DC})$$

$H\bar{H}\bar{L}$
(type II)

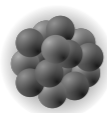


$$r_0 \sim 1/\Lambda_{DC}$$

$$m \sim 2m_H + O(m_H\alpha_{DC}^2)$$

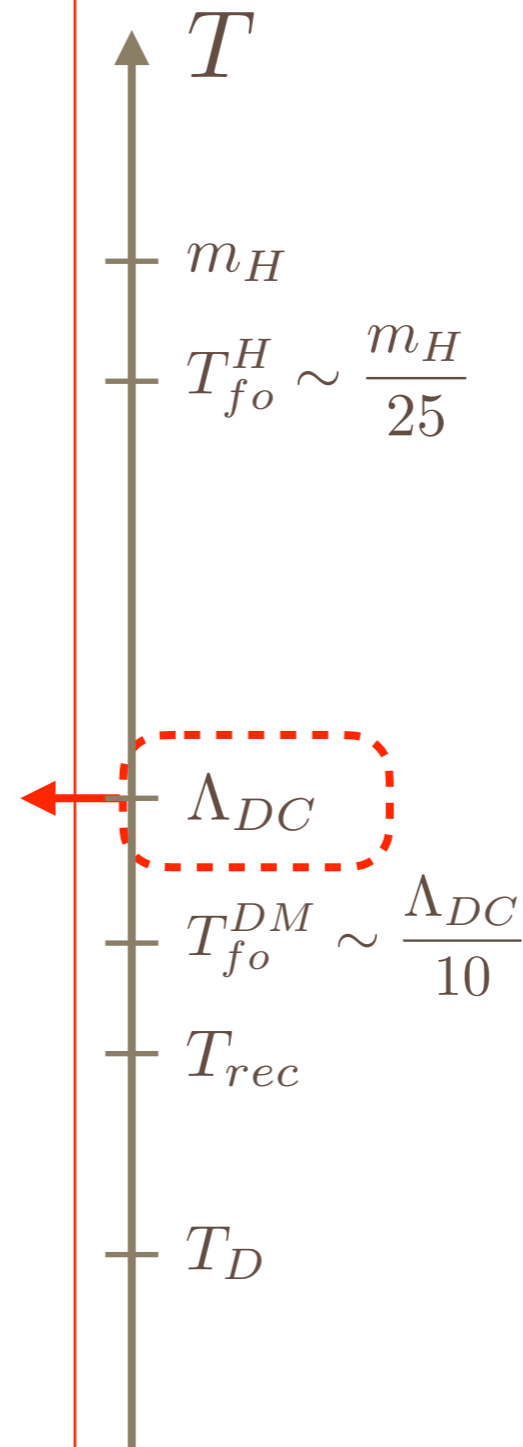
- ▶ Heavy (perturbative) hadrons

$H\bar{H}\bar{H}, \bar{H}\bar{H}$
(type III)



$$r_0 \sim 1/(\alpha_{DC}m_H)$$

$$m \sim n m_H + O(m_H\alpha_{DC}^2)$$



dark color confinement

Thermal history of the dark color states

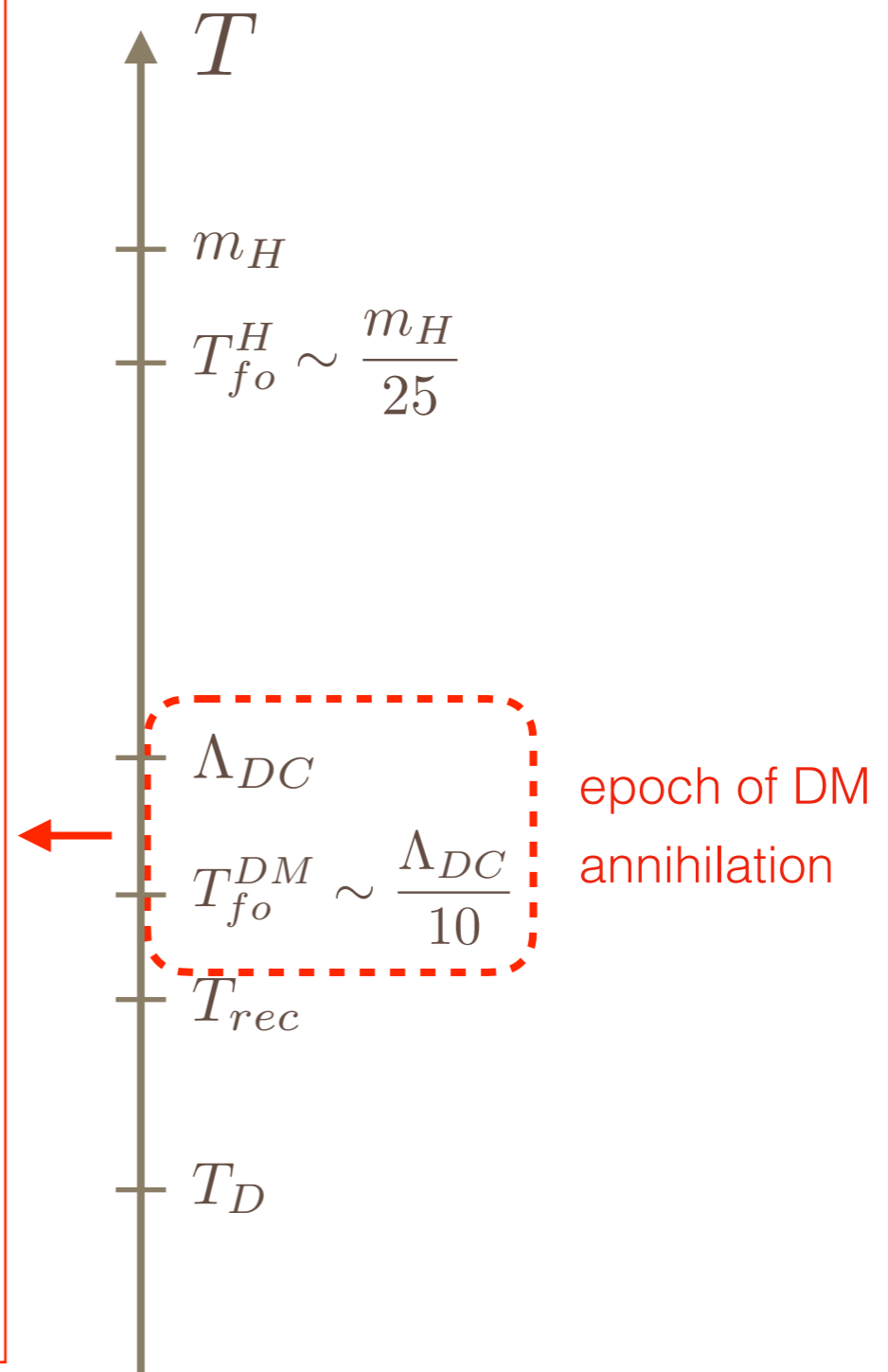
At $T \lesssim \Lambda_{DC}$ dark baryons have an epoch of annihilation into dark mesons with large non-perturbative cross section



These reactions go out of equilibrium at temperatures $T \sim \Lambda_{DC}/10$ leaving a thermal abundance of DM

$$\Omega_B \leq \Omega_{DM} \Rightarrow \Lambda_{DC} \lesssim 100 \text{ TeV}$$

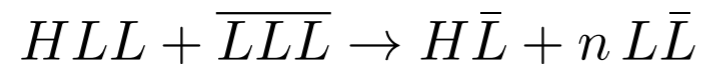
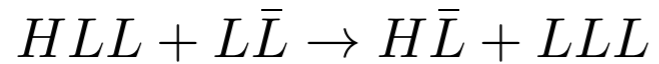
[K. Griest, M. Kamionkowski, PRL 64 (1990) 615
Antipin, Redi, Strumia, Vigiani JHEP 1507 (2015) 039]



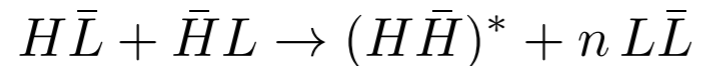
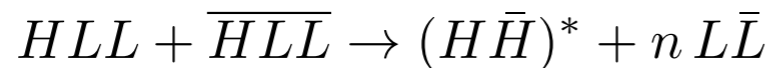
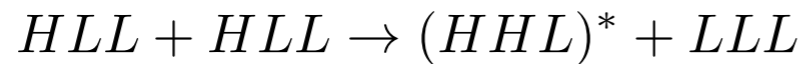
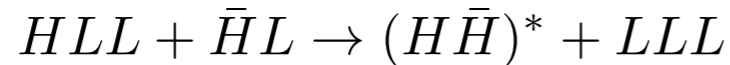
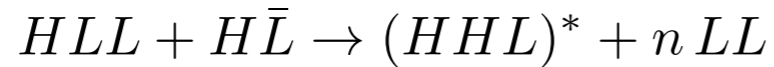
Thermal history of the dark color states

For $T_{rec} \lesssim T \lesssim \Lambda_{DC}$ various reactions change the abundance of heavy hadrons:

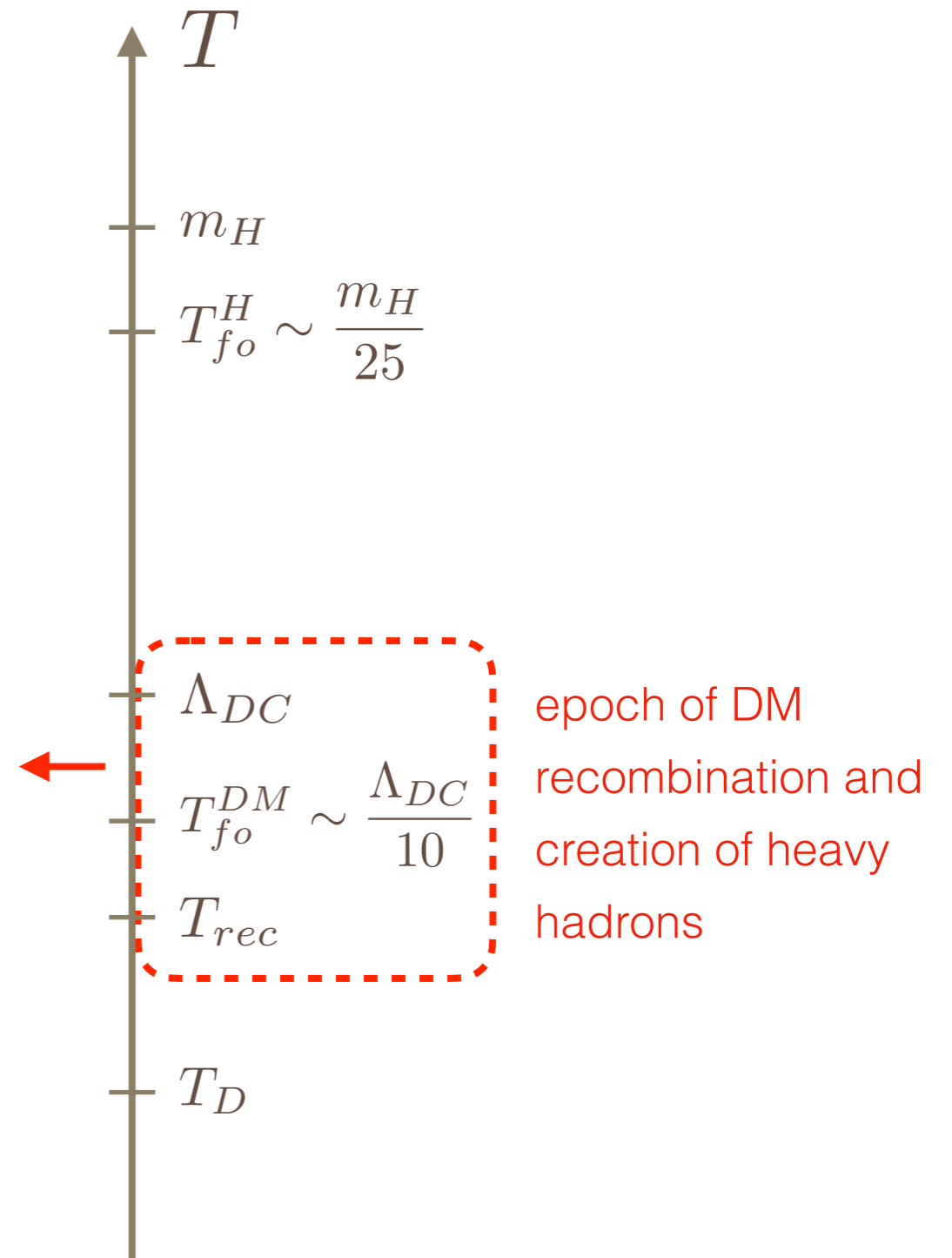
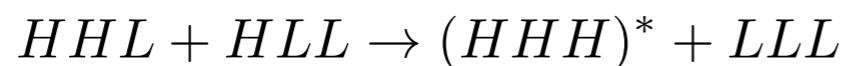
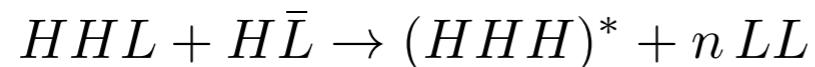
- ▶ Recombination of Type-I hybrids



- ▶ Type-I + Type-I \rightarrow Type-II



- ▶ Type-II + Type-I \rightarrow Type-III



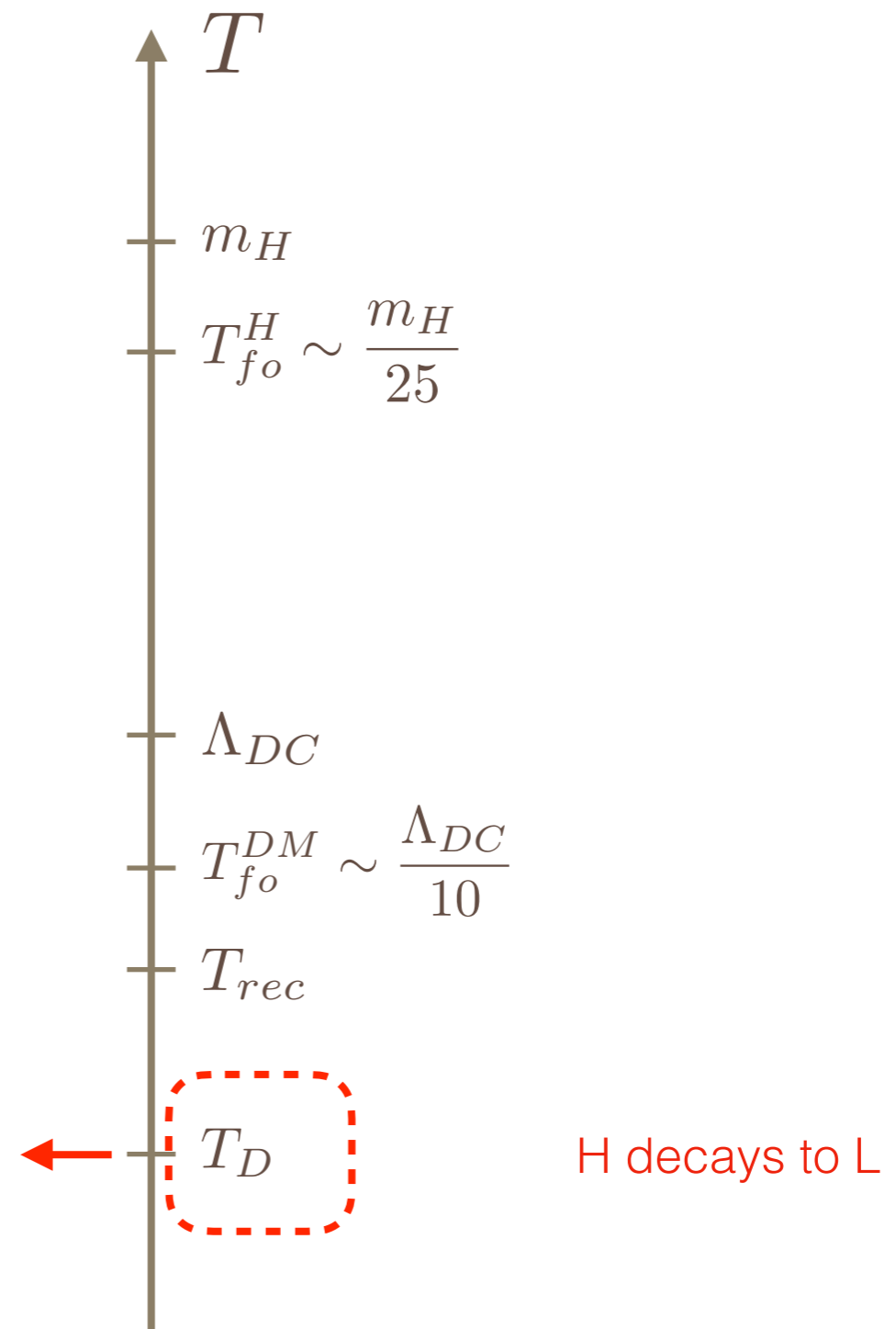
Thermal history of the dark color states

Heavy dark quarks H decay into L through $D=6$ operators generated at M_{GUT}

$$\Gamma_{H \rightarrow L} \sim \frac{g_{GUT}^4}{192\pi^3} \frac{m_H^5}{M_{GUT}^4}$$

- ▶ Decays occurring at $T_D > T_{fo}^{DM}$ do not affect the DM abundance
- ▶ Decays occurring after BBN are subject to strong constraints and excluded
- ▶ Decays occurring at $T_{BBN} < T_D < T_{fo}^{DM}$ give an extra non-thermal contribution to the DM abundance

$$Y_{DM} = Y_{DM}^T + e^{-t_{fo}/\tau_H} \cdot f_B \cdot Y_H$$



Thermal history of the dark color states

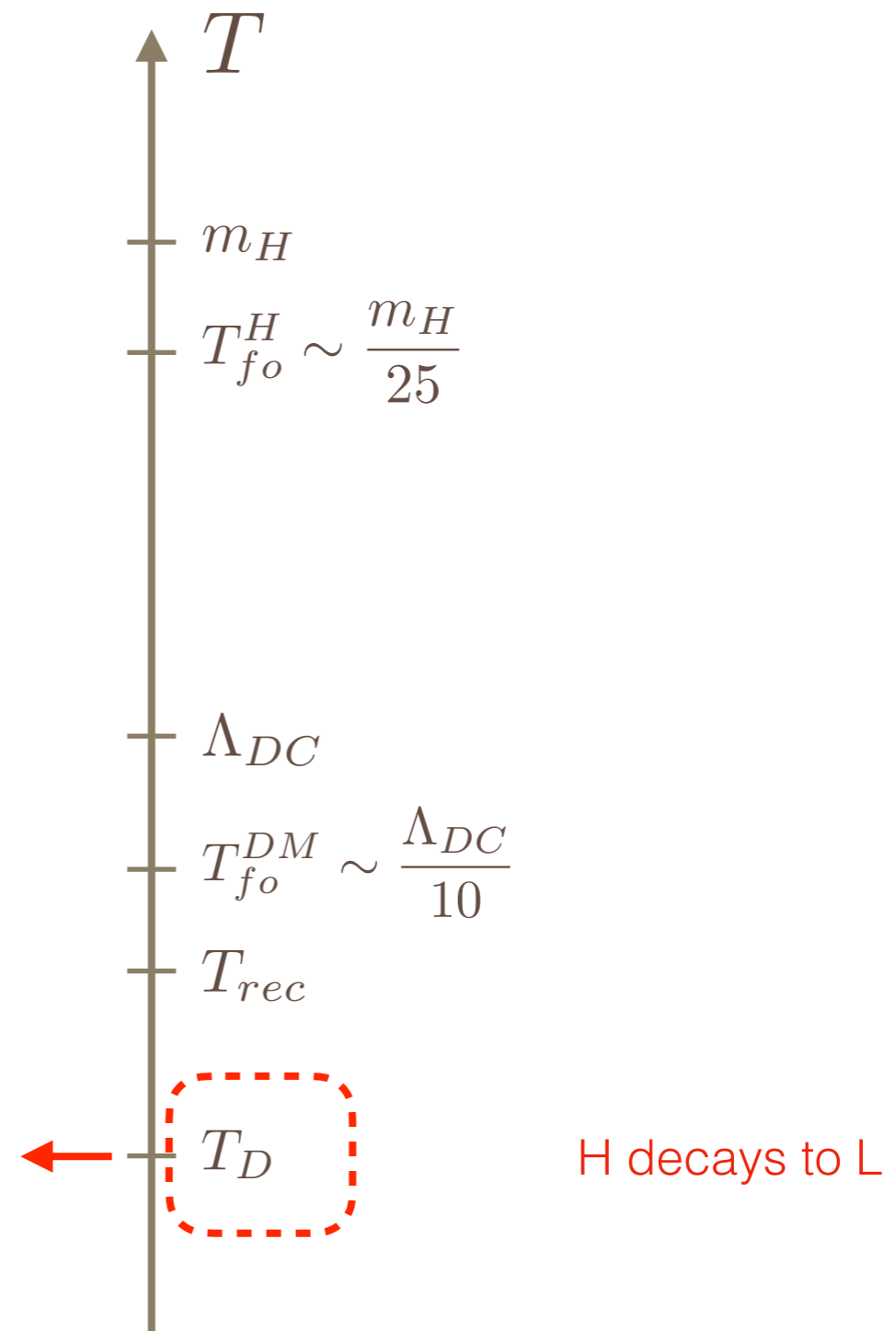
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DM thermal abundance



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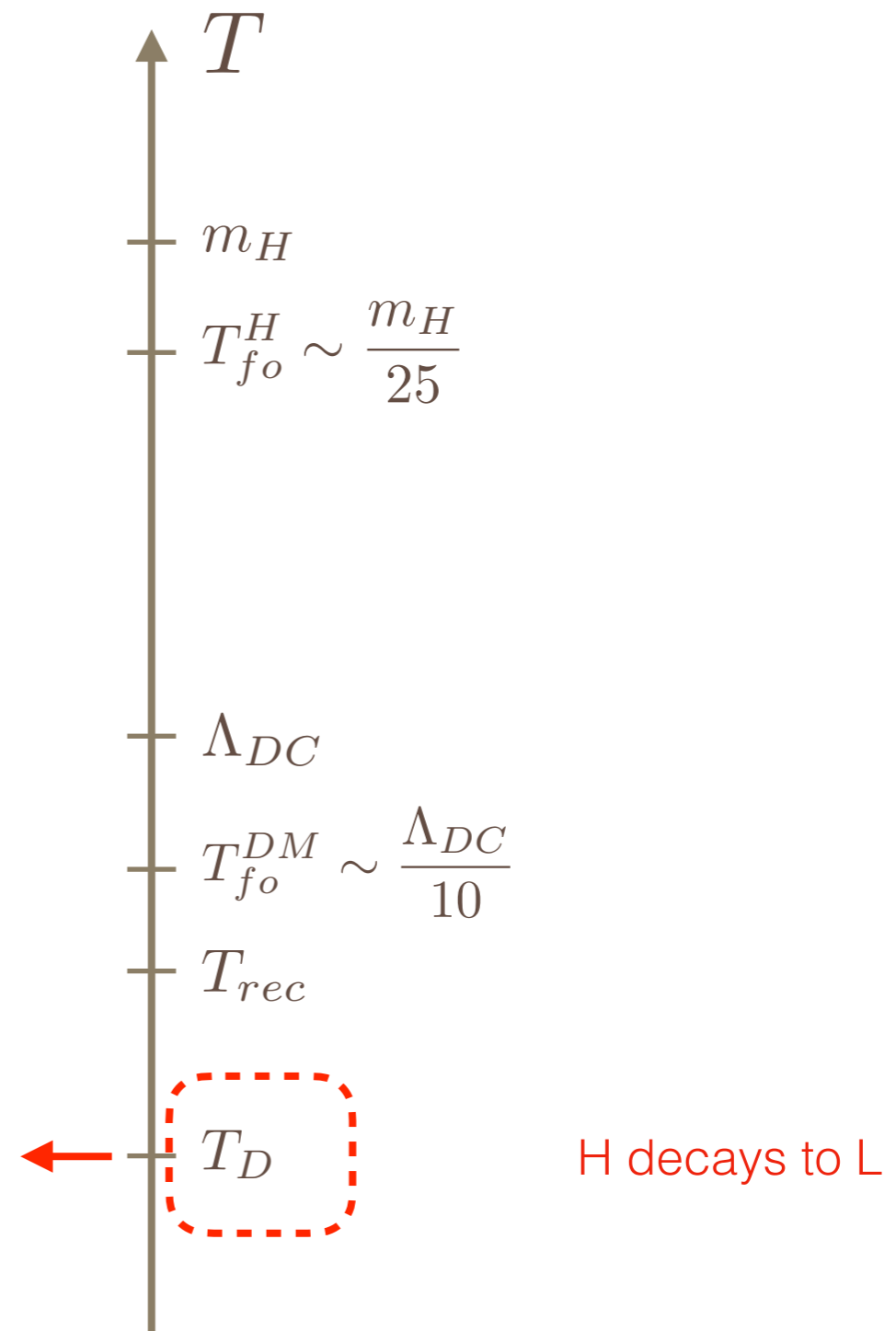
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DM thermal abundance
fraction of heavy baryons over all heavy hadrons at end of recombination

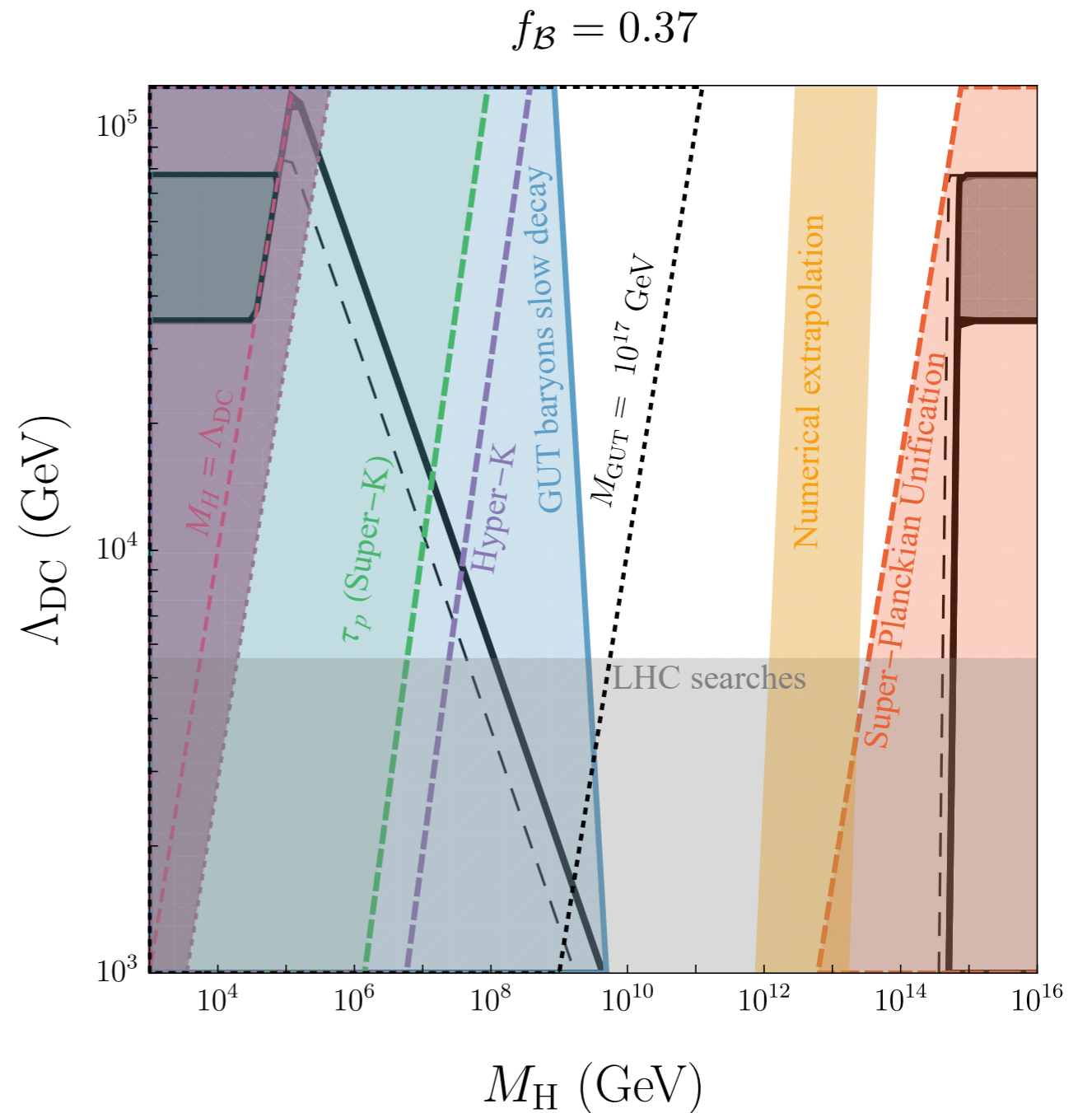


Non-thermal contribution to DM from recombination and decays of heavy hadrons can be much larger than the thermal one and overclose the Universe

$$Y_{DM} = Y_{DM}^T + e^{-t_{fo}/\tau_H} \cdot f_B \cdot Y_H$$

$$Y_H \sim \frac{x_{fo}^H}{M_{Pl} m_H \sigma_H} \sim \frac{25 m_H}{\pi M_{Pl} \alpha_{DC}^2}$$

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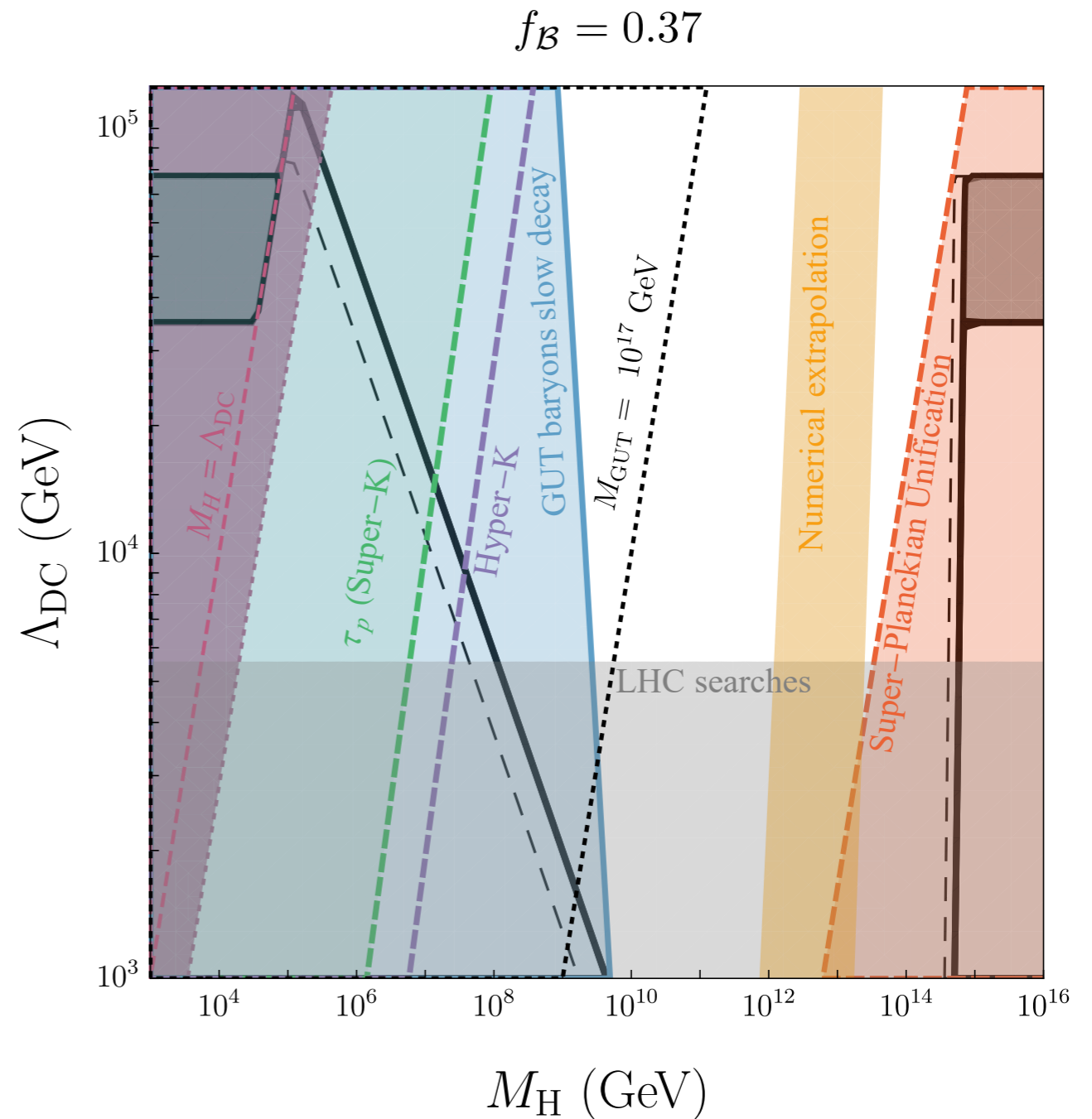


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👉 Moral: model excluded unless reheating temperature is lower than m_H , so that sector of heavy dark quarks is not populated

Conclusions

- Accidental DM + SU(5) GUT realized by very few models, among which:
 - $SU(3)_{DC}$, $\Psi = Q \oplus \tilde{D} \rightarrow 10 \oplus 5 / 15 \oplus 5$
 - $SU(3)_{DC}$, $\Psi = N \rightarrow 24$
 - $SU(3)_{DC}$, $\Psi = L \oplus E \rightarrow \bar{5} \oplus 10 \oplus 5 \oplus 24$ (with split heavy quark spectrum)
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- Non-thermal contribution to DM from heavy baryons is too large and overcloses the universe. Prediction: reheating temperature lower than m_H
- Dark confinement scale $\Lambda_{DC} \simeq 100 \text{ TeV}$ too large to produce dark hadrons at colliders. Potentially observable signals (indirect detection): i) DM decays via D=6 operators; ii) DM annihilations

Outlook

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