

Dark Matter from a Conformal Dark Sector

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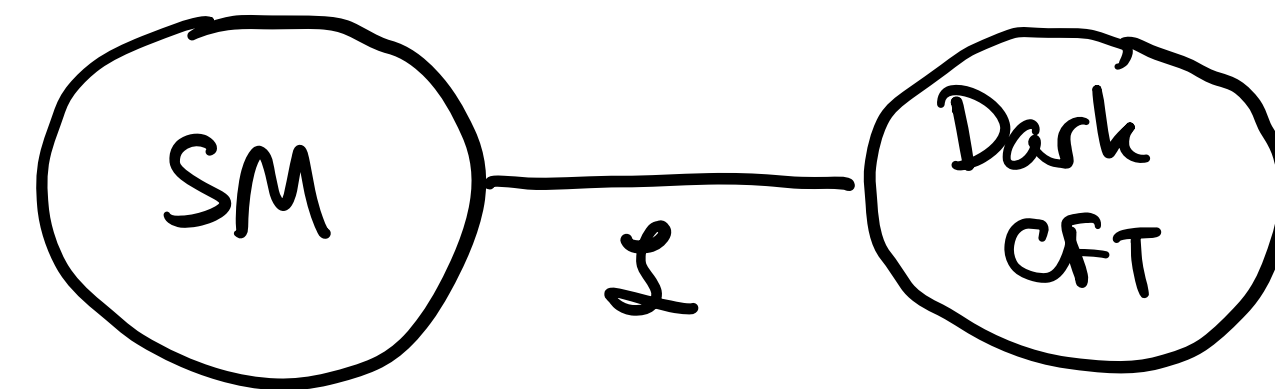
Rencontres du Vietnam, January 8 2024

[Work with Sungwoo Hong and Gowri Kurup, 2207.10093, JHEP]

[+work in progress with Lillian Luo]

Conformal(-ish) Dark Sector

- Conformal field theories seem ubiquitous, appear at interacting fixed points of RG flows
- Consider a dark sector described by a CFT (below some UV cutoff \gg weak scale)
- Can dark matter arise from such a DS?
- Conformal symmetry fixes scaling of CFT energy density in FRW universe: $\rho \propto a^{-4}$
- However DS is generically coupled to the SM, which is not conformal
- This may produce an interesting DM candidate



$$\mathcal{L}_{\text{int}} = \frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^{D-4}} \mathcal{O}_{\text{SM}} \mathcal{O}_{\text{CFT}}$$

Conformal Dark Sector

- In the deep UV, dark sector is a gauge theory, coupled to SM e.g. via

$$\mathcal{L}_{\text{UV}} = \frac{\lambda_{\text{BZ}}}{M_{\text{BZ}}^{d_{\text{SM}}-1}} \mathcal{O}_{\text{SM}} \bar{\Psi} \Psi$$

- DS flows to an interacting IR fixed point (Banks-Zaks) at $\Lambda_{\text{CFT}} < M_{\text{BZ}}$

- Below Λ_{CFT} , the dark sector is a CFT, coupled to SM via

$$\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^{D-4}} \mathcal{O}_{\text{SM}} \mathcal{O}_{\text{CFT}} \quad \lambda_{\text{CFT}} \approx \lambda_{\text{BZ}} \left(\frac{\Lambda_{\text{CFT}}}{M_{\text{BZ}}} \right)^{d_{\text{SM}}-1} \quad D = d + d_{\text{SM}}$$

- “Natural” parameters: $\lambda_{\text{BZ}} \sim \mathcal{O}(1) \rightarrow \lambda_{\text{CFT}} \ll 1$

- CFT is generically strongly coupled, so d is a continuous (non-integer) parameter ($d \geq 1$ from unitarity)

CFT Breaking: Higgs Portal

- For example, consider the “Higgs portal” coupling: $\mathcal{O}_{\text{SM}} = H^\dagger H$
- Below the weak scale: $\mathcal{L} = c \mathcal{O}_{\text{CFT}}$ $c = \frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^{D-4}} \langle \mathcal{O}_{\text{SM}} \rangle.$
- If \mathcal{O}_{CFT} is relevant ($d < 4$), this perturbation grows in the IR, eventually breaking conformal symmetry.
- If no other sources of conformal breaking, the CFT breaking “gap” scale is

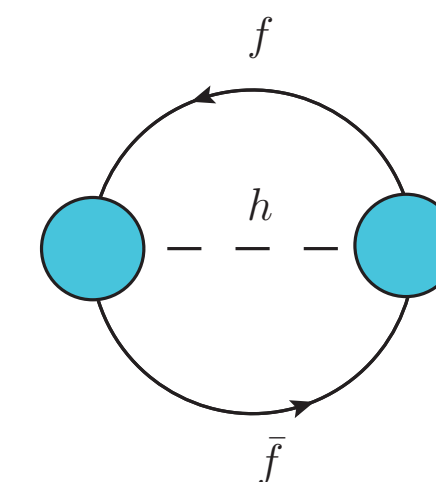
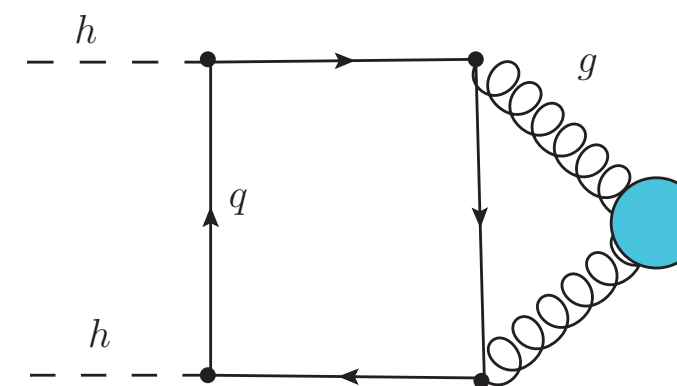
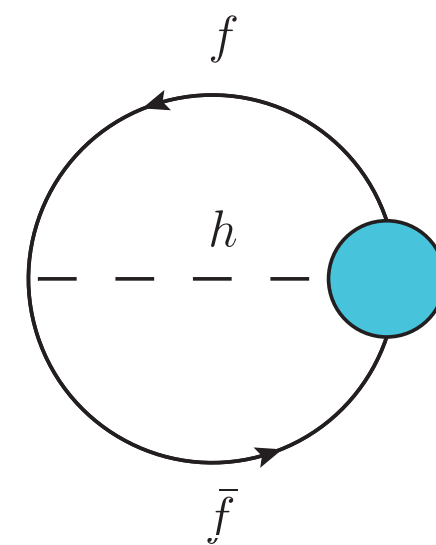
$$M_{\text{gap}} = \left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^{d-2}} v^2 \right)^{\frac{1}{4-d}}$$

- Generically, bound states form below this scale. Cosmologically, bound states behave as particles. If one or more are stable, can be DM.

CFT Breaking: Other Portals

\mathcal{O}_{SM}	\mathcal{O}_{CFT} from $\langle \mathcal{O}_{\text{SM}} \rangle$	Loop-induced \mathcal{O}_{CFT}	Loop-induced \mathcal{O}_{CFT} from $\langle H^\dagger H \rangle$	$\mathcal{O}_{\text{CFT}}^2$
Higgs portal $H^\dagger H$	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^{d-2}} v^2 \right)^{\frac{1}{4-d}}$ ✓	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^{d-2}} \frac{\Lambda_{\text{SM}}^2}{16\pi^2} \right)^{\frac{1}{4-d}}$	—	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^{d-2}} \frac{v}{m_h} \right)^{\frac{1}{2-d}}$
Quark portal $H Q_L^\dagger Q_R$	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} v \Lambda_{\text{QCD}}^3 \right)^{\frac{1}{4-d}}$	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{(\sum_i \kappa_i y_{q_i}) v^2 \Lambda_{\text{SM}}^2}{(16\pi^2)^2} \right)^{\frac{1}{4-d}}$	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{(\sum_i \kappa_i y_{q_i}) v^2 \Lambda_{\text{SM}}^2}{16\pi^2} \right)^{\frac{1}{4-d}}$ ✓	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \sqrt{\frac{\Lambda_{\text{SM}}^4}{(16\pi^2)^2} + \frac{v^4}{16\pi^2}} \right)^{\frac{1}{2-d}}$
Gluon portal $G^{\mu\nu} G_{\mu\nu}$	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \Lambda_{\text{QCD}}^4 \right)^{\frac{1}{4-d}}$	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{\Lambda_{\text{SM}}^4}{16\pi^2} \right)^{\frac{1}{4-d}}$ ✓	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{(\sum_i y_{q_i}^2) \alpha_s v^2 \Lambda_{\text{SM}}^2}{64\pi^3} \right)^{\frac{1}{4-d}}$	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{\Lambda_{\text{SM}}^2}{4\pi} \right)^{\frac{1}{2-d}}$
Lepton portal $H L^\dagger \ell_R$	—	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{(\sum_i \kappa_i y_{\ell_i}) v^2 \Lambda_{\text{SM}}^2}{(16\pi^2)^2} \right)^{\frac{1}{4-d}}$	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{(\sum_i \kappa_i y_{\ell_i}) v^2 \Lambda_{\text{SM}}^2}{16\pi^2} \right)^{\frac{1}{4-d}}$ ✓	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \sqrt{\frac{\Lambda_{\text{SM}}^4}{(16\pi^2)^2} + \frac{v^4}{16\pi^2}} \right)^{\frac{1}{2-d}}$
EW portal $W^{\mu\nu} W_{\mu\nu}$	—	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{\Lambda_{\text{SM}}^4}{16\pi^2} \right)^{\frac{1}{4-d}}$ ✓	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{g^2 v^2 \Lambda_{\text{SM}}^2}{4 \cdot 16\pi^2} \right)^{\frac{1}{4-d}}$	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{\Lambda_{\text{SM}}^2}{4\pi} \right)^{\frac{1}{2-d}}$
EW portal $B^{\mu\nu} B_{\mu\nu}$	—	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{\Lambda_{\text{SM}}^4}{16\pi^2} \right)^{\frac{1}{4-d}}$ ✓	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{g'^2 v^2 \Lambda_{\text{SM}}^2}{4 \cdot 16\pi^2} \right)^{\frac{1}{4-d}}$	$\left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \frac{\Lambda_{\text{SM}}^2}{4\pi} \right)^{\frac{1}{2-d}}$

[Spin-1 portal: Chiu, Hong, Wang, '22]



Hadronic Phase EFT

- Below the gap scale, dark sector has particle-like excitations. To be specific, we assume the following (partly QCD-inspired) features:
- Lightest hadron is a pseudo-scalar particle, “dark pion”
- Dark pion is a pNGB, $r = m_{\text{DM}}/M_{\text{gap}}$ is a free (radiatively stable) parameter
- Dark pion is stable, plays the role of DM (no anomaly w.r.t. SM)
- Scalar or vector “dark rho” with mass $\sim M_{\text{gap}}$
- Rho-pion interactions from symmetry: e.g. $\mathcal{L} \sim g_* \rho^\mu \left(\chi^\dagger \partial_\mu \chi + \text{h.c.} \right)$

Hadronic Phase EFT

- DM elastic self-scattering is mediated by dark rho exchanges:

$$\sigma_{\text{SI}} \sim \frac{g_\star^4}{8\pi M_{\text{gap}}^2} \sim \frac{r^6}{8\pi M_{\text{gap}}^2} \text{ (scalar rho),} \quad \text{or} \quad \sim \frac{r^2}{8\pi M_{\text{gap}}^2} \text{ (vector rho)}$$

- Recall that SM-CFT coupling is $\mathcal{L}_{\text{int}} = \frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^{D-4}} \mathcal{O}_{\text{SM}} \mathcal{O}_{\text{CFT}}$

- Symmetries restrict which states can be created by :

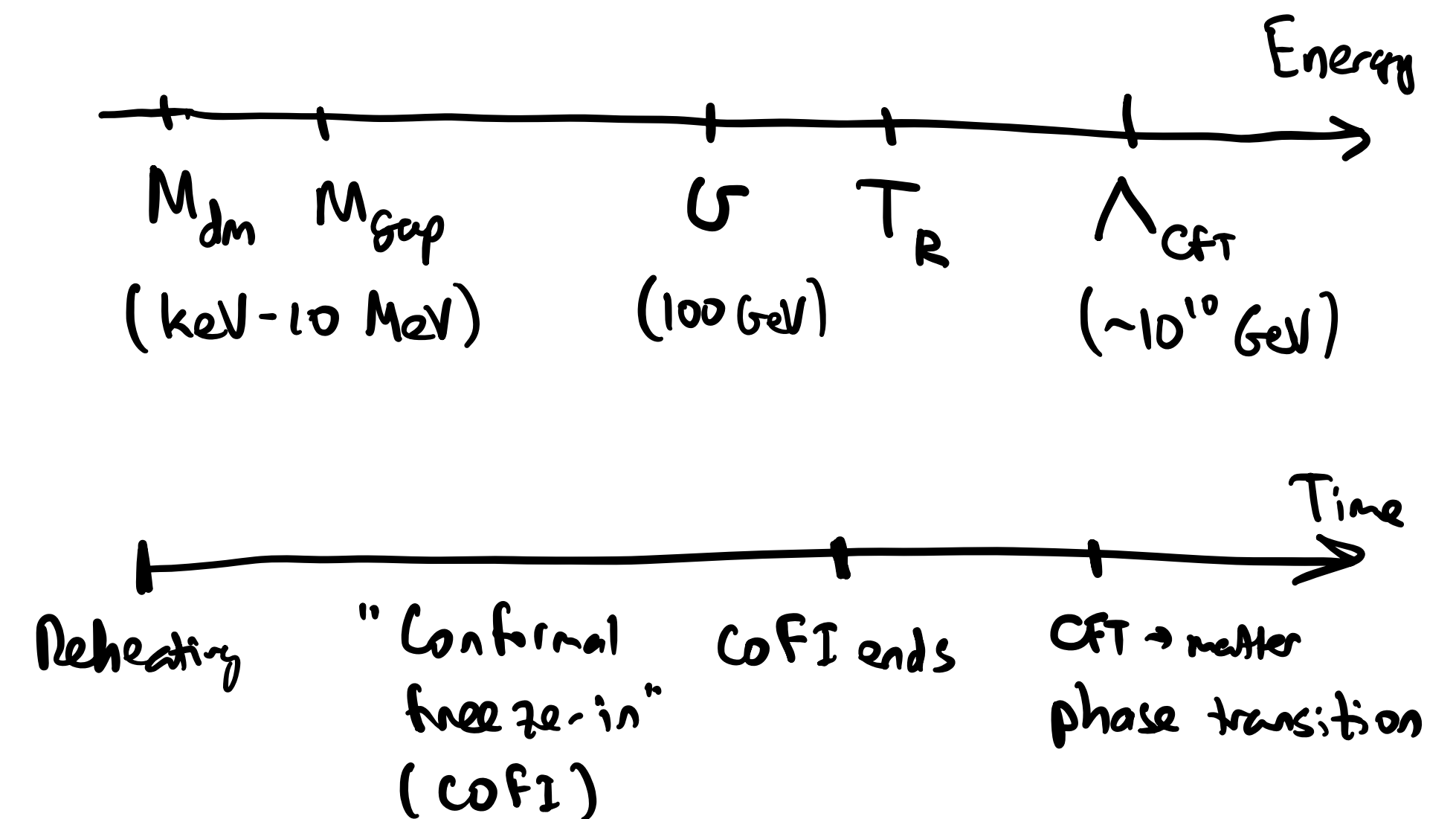
$$\mathcal{O}_{\text{CFT}} \longrightarrow \frac{M_{\text{gap}}^{d-1}}{g_\star} \phi \quad \mathcal{O}_{\text{CFT}} \sim \partial_\mu \rho^\mu \quad \mathcal{O}_{\text{CFT}} \sim (\partial\chi)^2$$

- Dark rho mediates DM-SM interactions: for example for lepton portal

$$\mathcal{L} \sim \frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^d} \left(H L^\dagger \ell_R \right) \mathcal{O}_{\text{CFT}} \rightarrow \frac{\lambda_{\text{CFT}} v M_{\text{gap}}^{d-1}}{\sqrt{2} g_\star \Lambda_{\text{CFT}}^d} (\bar{e}e) \phi + \frac{g_\star}{M_{\text{gap}}} \phi (\partial\chi)^2$$

Cosmological History

- Phase transition (conformal plasma \rightarrow bound states) in the dark sector at $T_{\text{dark}} \sim M_{\text{gap}}$
- Assume that 100% of energy in the dark sector before the transition is converted to DM
- If dark sector is in thermal equilibrium with SM before the phase transition, observed DM density requires $m_{\text{dm}} \sim 100 \text{ eV}$ - hot DM!
- Freeze-in scenario: $T_{\text{dark}} < T_{\text{SM}}$
- As always with freeze-in, assume that dark sector is not reheated after inflation, populated slowly by SM interactions



Conformal Freeze-In

- Energy transfer from SM to dark sector occurs when dark sector is conformal

- CFT energy evolves according to $\frac{d\rho_{\text{CFT}}}{dt} + 4H\rho_{\text{CFT}} = \Gamma_E(\text{SM} \rightarrow \text{CFT})$

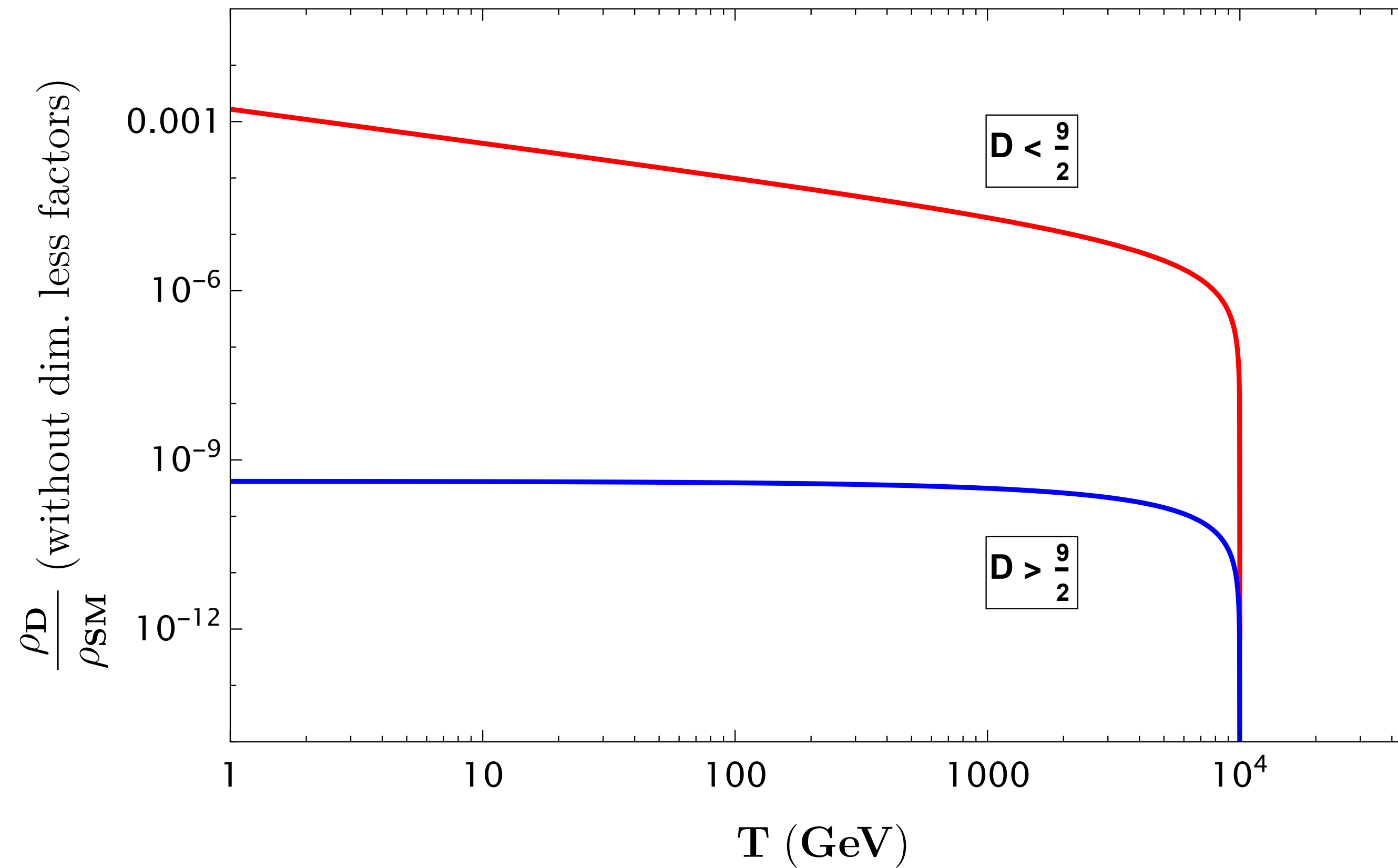
- Dimensional analysis (if $T_{\text{SM}} \gg$ all mass scales): $\Gamma_E(\text{SM} \rightarrow \text{CFT}) \sim \frac{\lambda_{\text{CFT}}^2}{\Lambda_{\text{CFT}}^{2(D-4)}} T_{\text{SM}}^{2D-3}$.

- Solution to Boltzmann equation:

$$\rho_{\text{CFT}} \sim \frac{M_{\text{pl}}}{\Lambda_{\text{CFT}}^{2D-8}} \left[T^4 \left(\frac{T_R^{2D-9} - T^{2D-9}}{2D-9} \right) \right]$$

- IR-dominated (“true freeze-in”) for $D < 9/2$, otherwise (mildly) depends on T_R

Conformal Freeze-In



Conformal Freeze-In: Higgs Portal

- A more detailed calculation can be performed using Georgi's "unparticle" approach
- For example, in the Higgs portal:

$$\begin{aligned}
 n_h \langle \Gamma(h \rightarrow \text{CFT}) E \rangle &= \iint d\Pi_h \underline{d\Pi_{\text{CFT}}} f_h (2\pi)^4 \delta^4(p_h - P) E_h |\mathcal{M}|^2. \\
 &= \iint \frac{d^3\vec{p}_h}{(2\pi)^3 2E_h} \frac{d^4P}{(2\pi)^4} e^{-\beta E_h} (2\pi)^4 \delta^4(p_h - P) \underline{A_d} (P^2)^{d-2} E_h \frac{v^2}{4} \frac{\lambda_{\text{CFT}}^2}{\Lambda_{\text{CFT}}^{2d-4}} \\
 &= \frac{f_d \lambda_{\text{CFT}}^2 v^2 m_h^{2(d-1)} T}{\Lambda_{\text{CFT}}^{2d-4}} K_2(m_h/T). \quad \longrightarrow \quad \rho_{\text{CFT}}(T) = \frac{2M_* f_d \lambda_{\text{CFT}}^2}{3\sqrt{g_*(T)} v} \left(\frac{m_h}{\Lambda_{\text{CFT}}}\right)^{2d-4} T^4 \left(\frac{v^3}{T^3} - 1\right)
 \end{aligned}$$

$$A_d = \frac{16\pi^{5/2}}{(2\pi)^{2d}} \frac{\Gamma(d+1/2)}{\Gamma(d-1)\Gamma(2d)}.$$

$$f_d = A_d/16\pi^2$$

Conformal Freeze-In: Higgs Portal

- Strong interactions in the CFT thermalize the transferred energy:

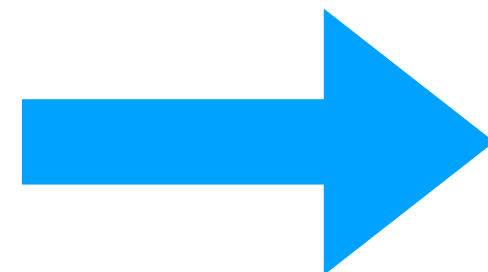
$$\rho_{\text{CFT}} = AT_D^4, A \sim 1 \dots 10$$

- Freeze-in stops when $T_D \sim m_{\text{dm}}$:

$$T_m^4 = A m_{\text{DM}}^4 \left[\frac{2M_* f_d \lambda_{\text{CFT}}^2 g_*(T_m)}{3(g_*(m_h))^{3/2} v} \left(\frac{m_h}{\Lambda_{\text{CFT}}} \right)^{2d-4} \left(\frac{v^3}{m_h^3} - 1 \right) \right]^{-1}$$

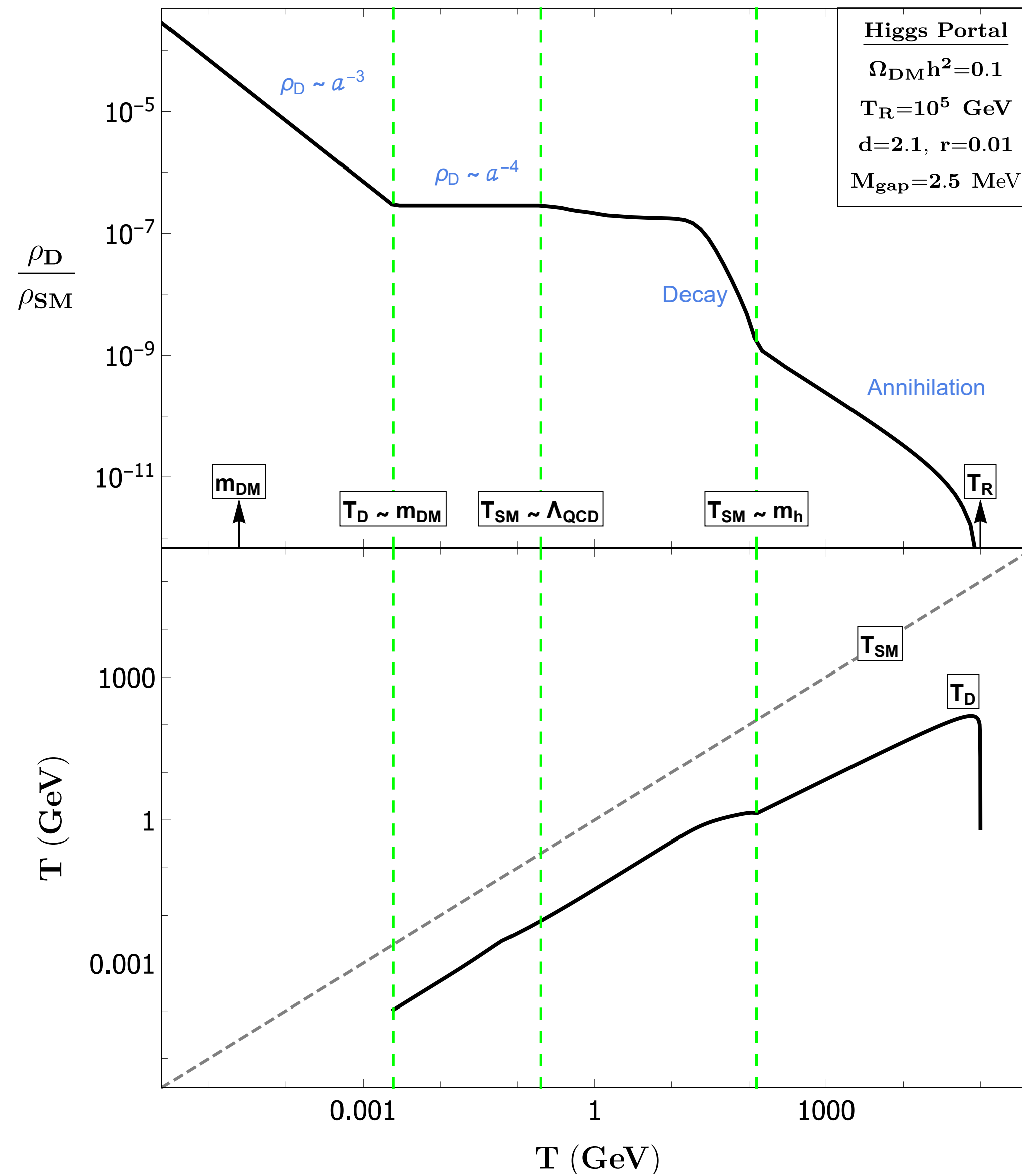
- Current DM energy density:

$$\rho_{\text{DM}}(T_0) = A m_{\text{DM}}^4 \frac{g_*(T_0) T_0^3}{g_*(T_m) T_m^3}$$

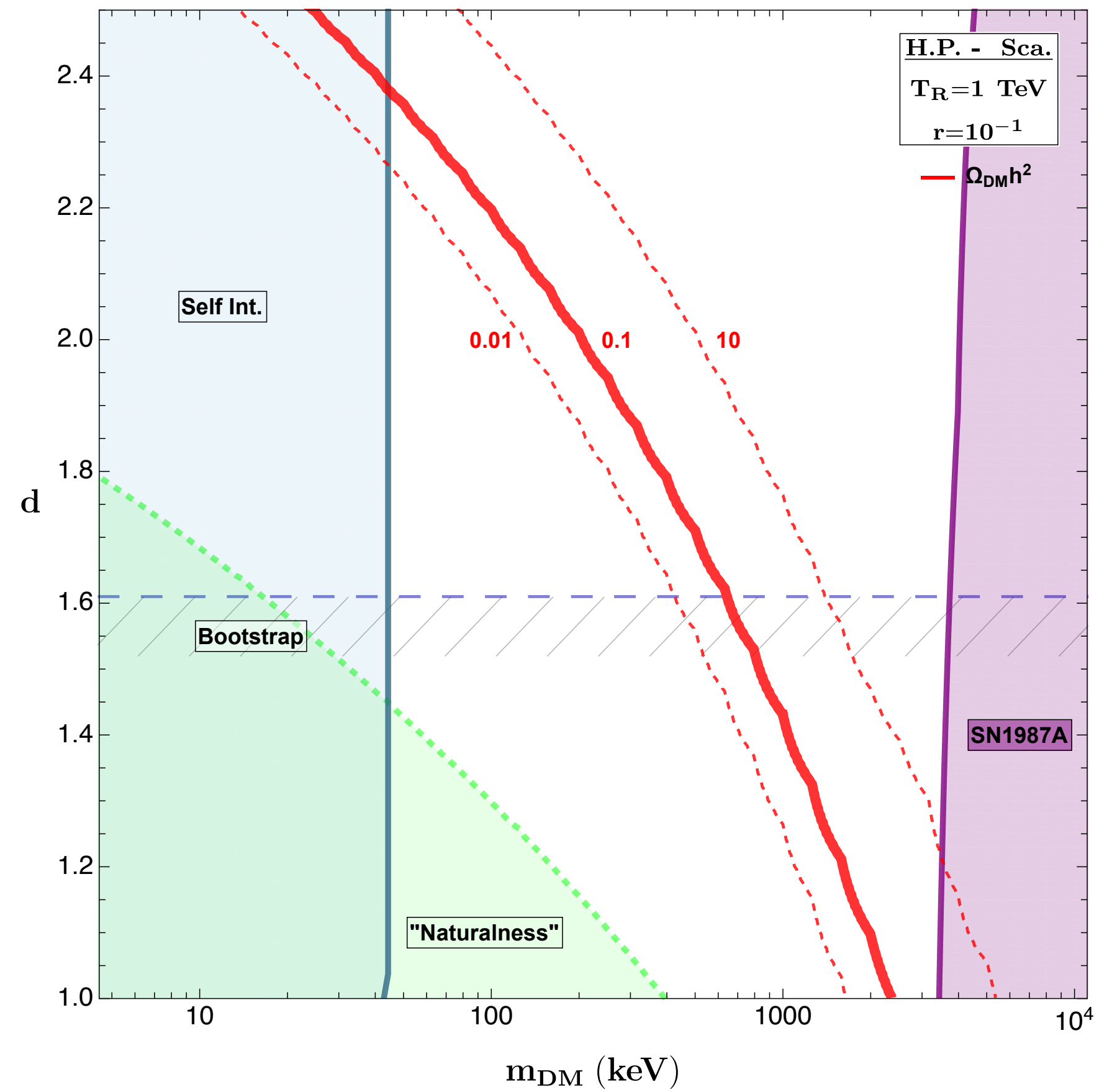


$$\frac{\Omega_{\text{DM}} h^2}{0.1} = \left[\frac{m_{\text{DM}}}{1 \text{ MeV}} \right] \left[\frac{\left(A f_d^3 g_*^{-9/2} \right)^{1/4}}{10^{-5}} \right] \left[\frac{\left(\frac{M_{\text{gap}}}{m_h} \right)^{\left(6 - \frac{3d}{2} \right)}}{10^{-12}} \right]$$

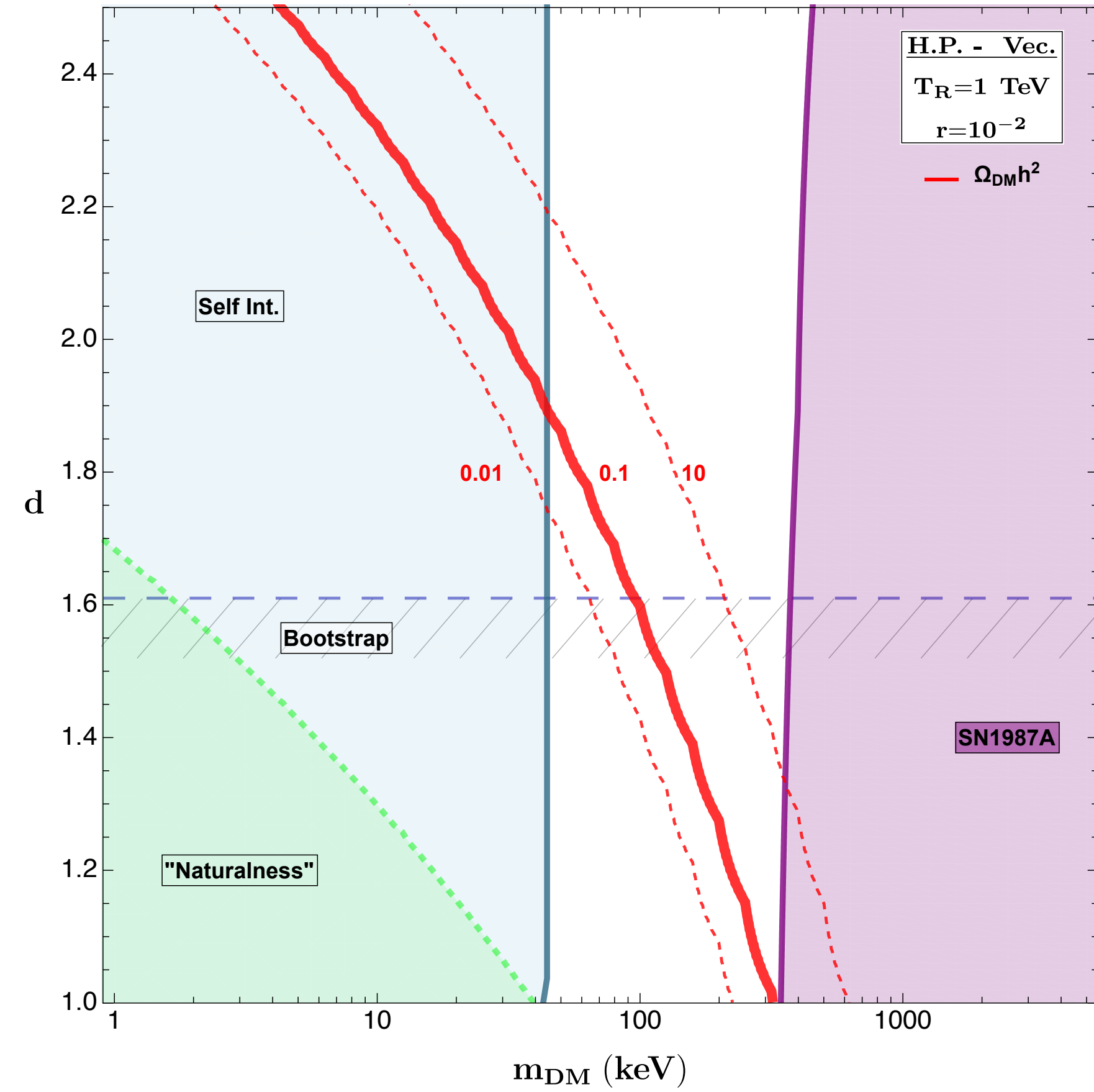
Conformal Freeze-In: Higgs Portal



Results: Higgs Portal $\mathcal{O}_{\text{SM}} = H^\dagger H$



scalar ρ dominant

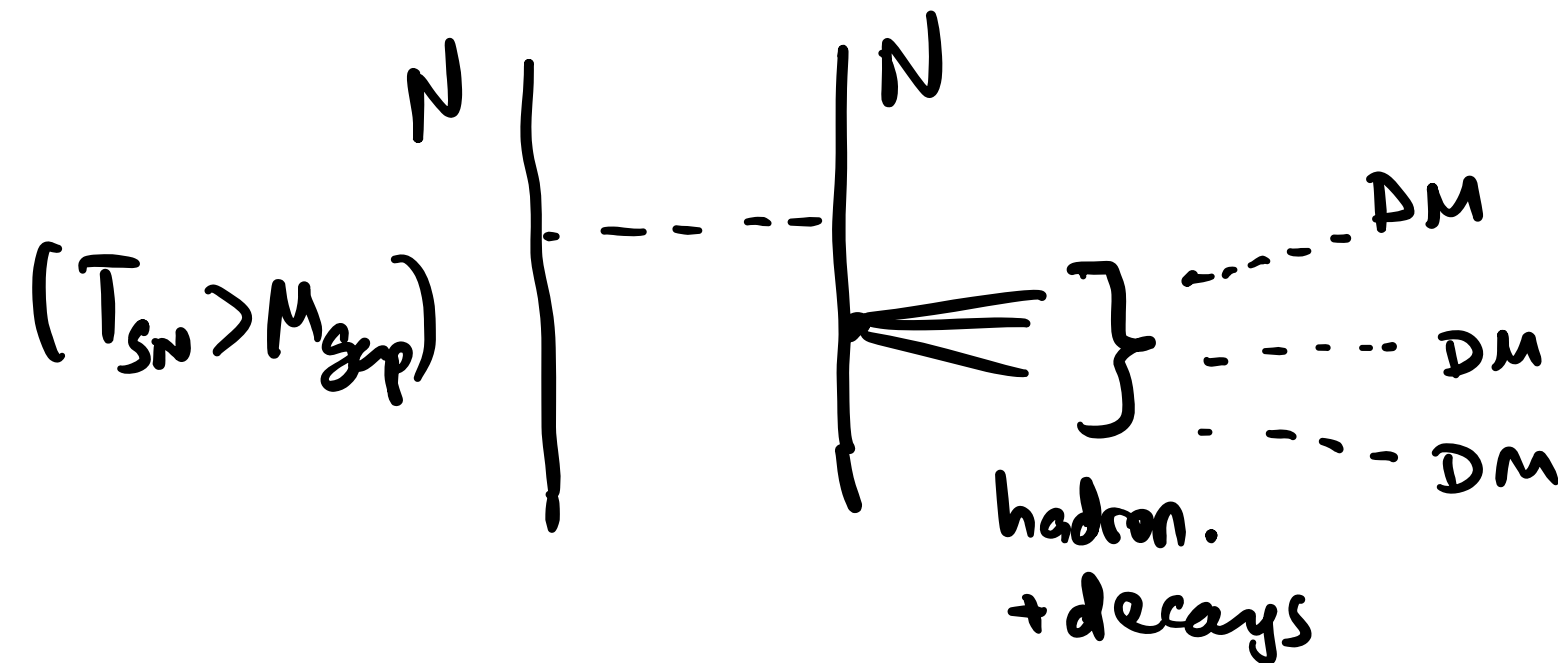


vector ρ dominant

Supernova Bounds

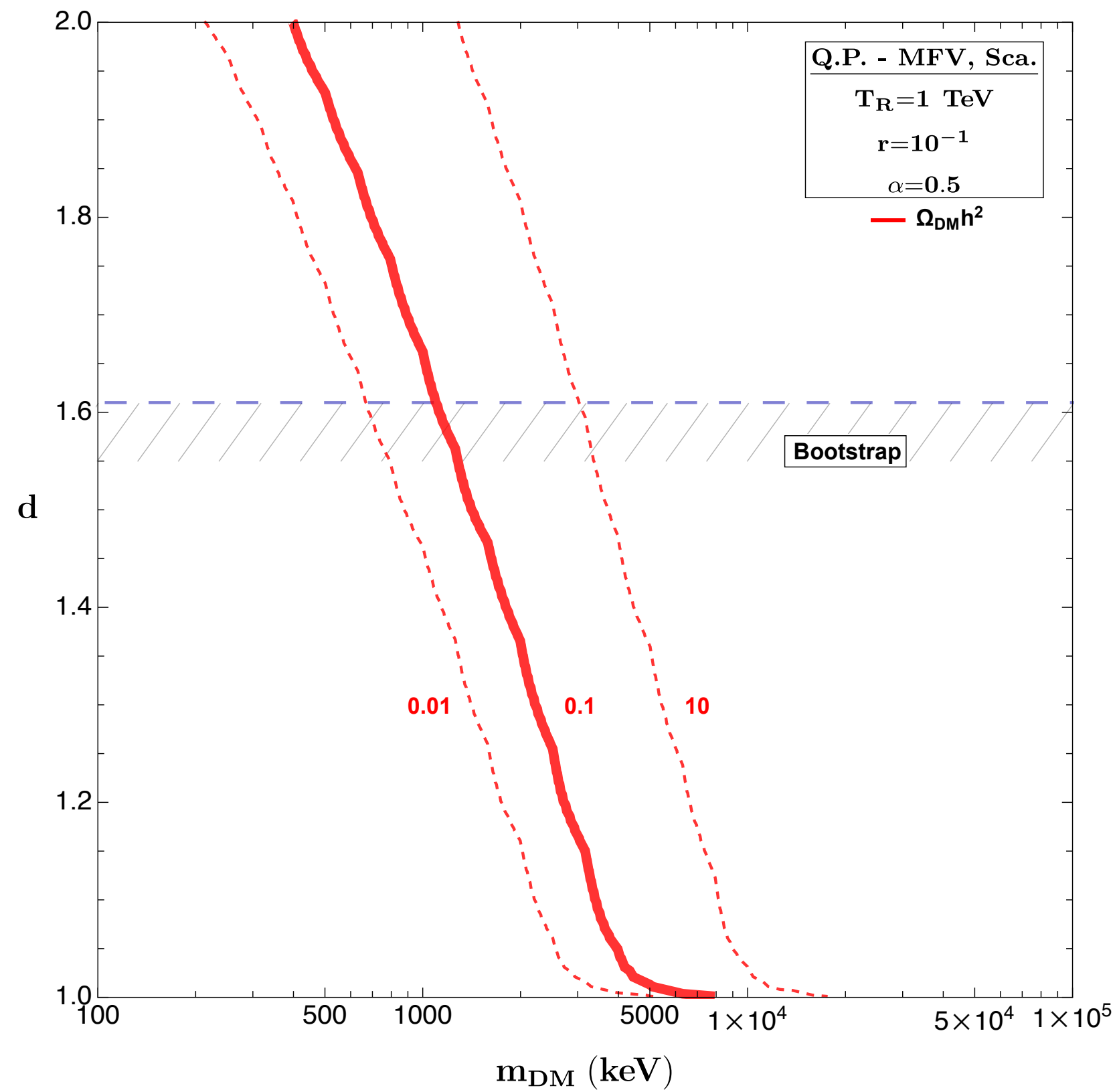
- Effective Lagrangian relevant for SN core:

$$\mathcal{L} \sim \frac{\lambda_{\text{CFT}} v}{\sqrt{2}\Lambda_{\text{CFT}}^{d-2}} h \mathcal{O}_{\text{CFT}} + \frac{\alpha_s}{12\pi v} h G_{\mu\nu}^a G^{\mu\nu a} \quad \longrightarrow \quad \mathcal{L} \sim C_G^{(N)} \left(\frac{\alpha_s}{6\sqrt{2}\pi} \right) \left(\frac{M_{\text{gap}}^{4-d}}{v^2 m_h^2} \right) \bar{N} N \mathcal{O}_{\text{CFT}}$$

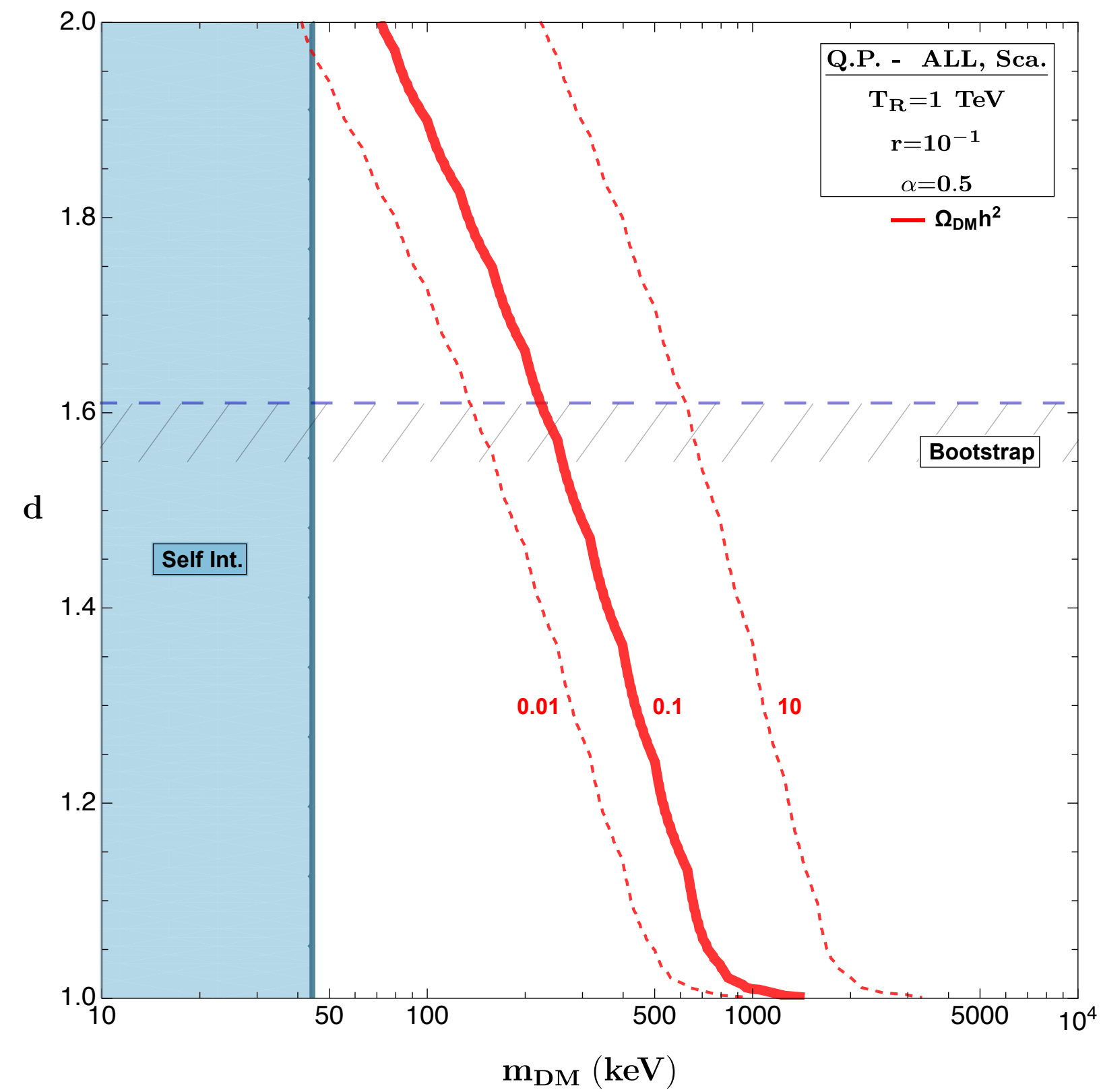


- Production: Use Georgi's trick to evaluate inclusive production rate if $T_{\text{SN}} > M_{\text{gap}}$ or use hadronic CFT to compute DM pair-production in nucleon collisions if $T_{\text{SN}} < M_{\text{gap}}$
- Trapping: Use hadronic EFT to evaluate DM mean free path in the SN core

Quark Portal $\mathcal{O}_{\text{SM}} = H Q^\dagger q$



MFV couplings

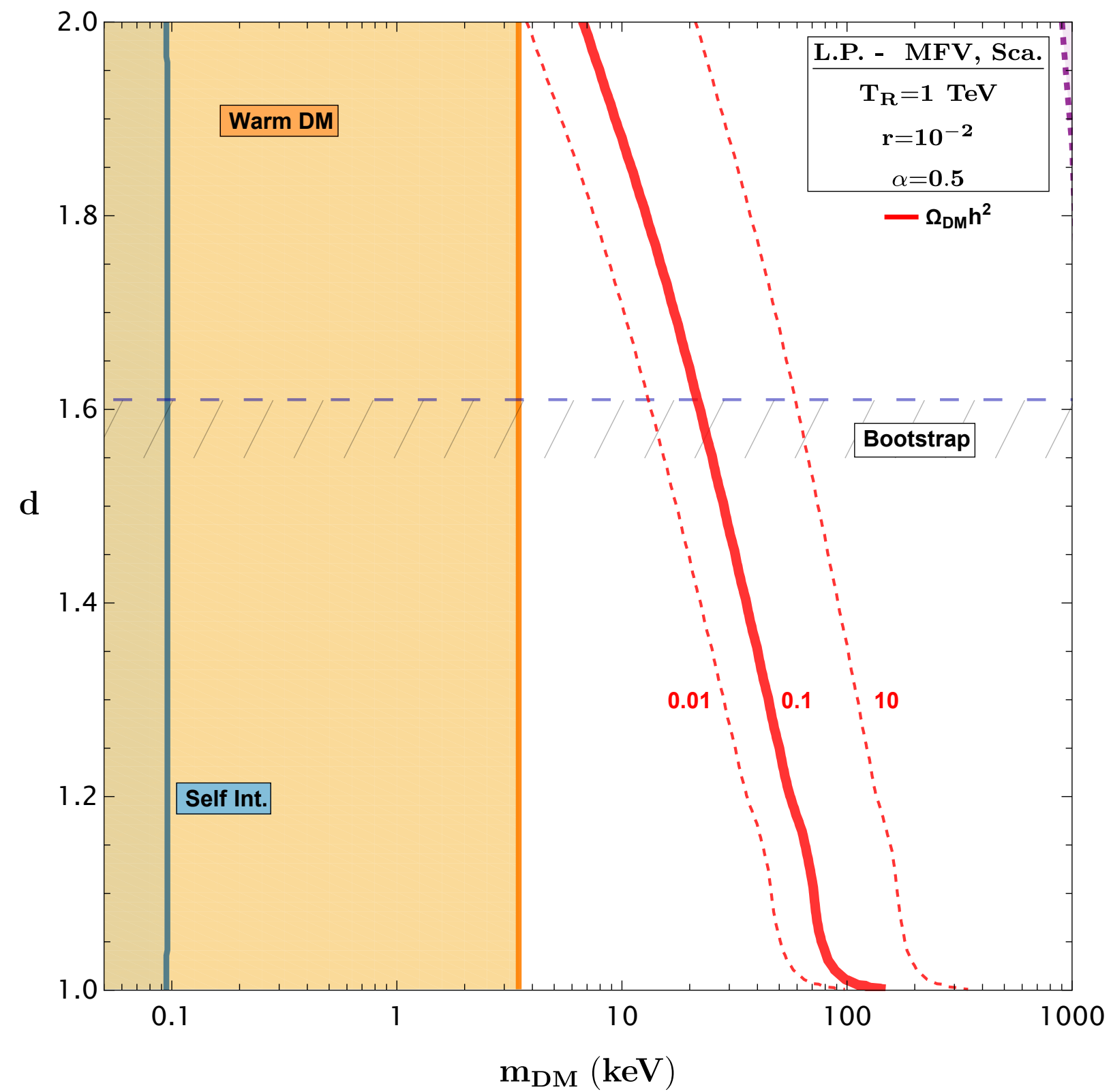


Flavor-diagonal couplings

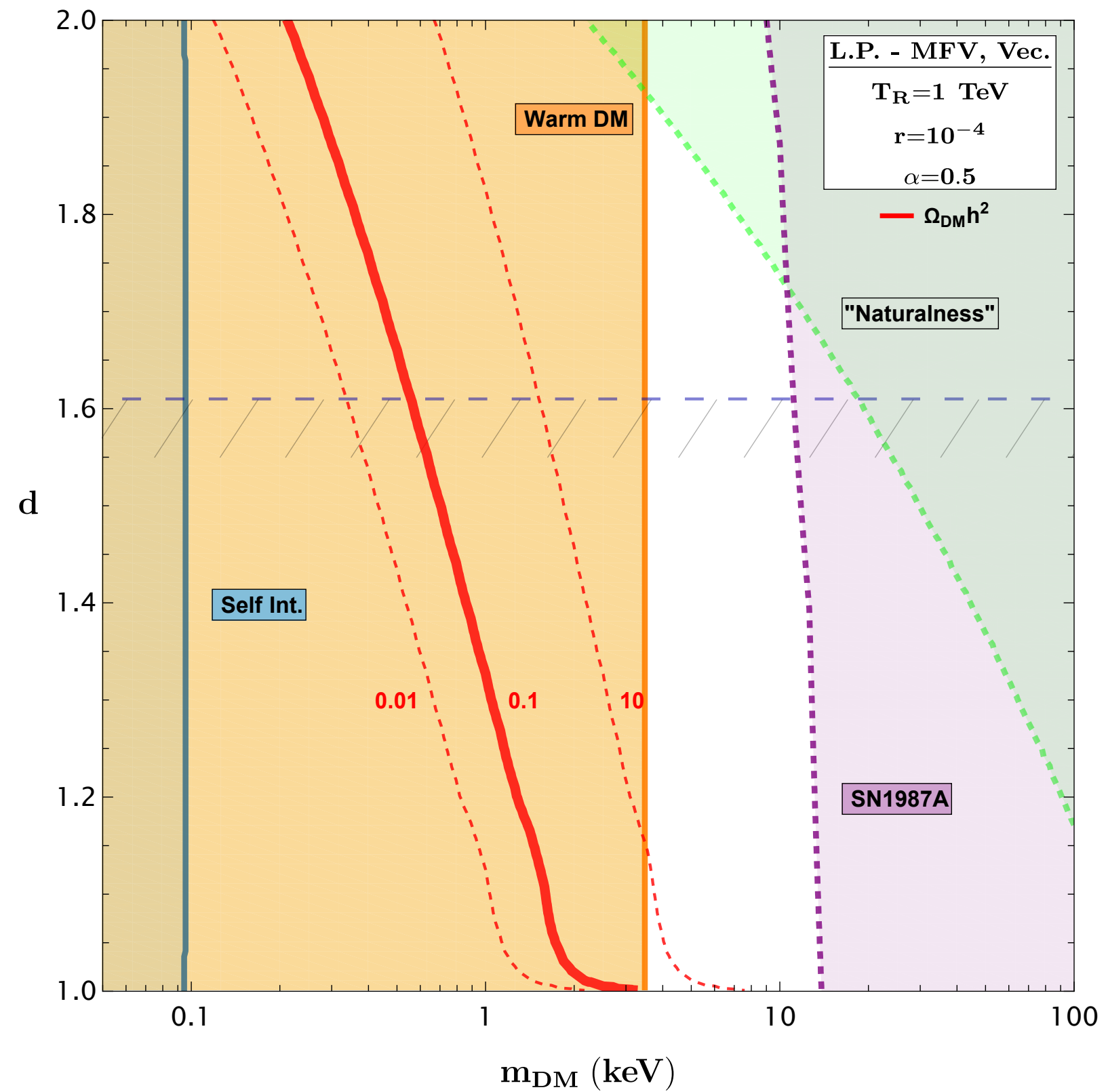
[scalar rho dominant]

Lepton Portal

$$\mathcal{O}_{\text{SM}} = HL^\dagger \ell_R$$



scalar rho dominant

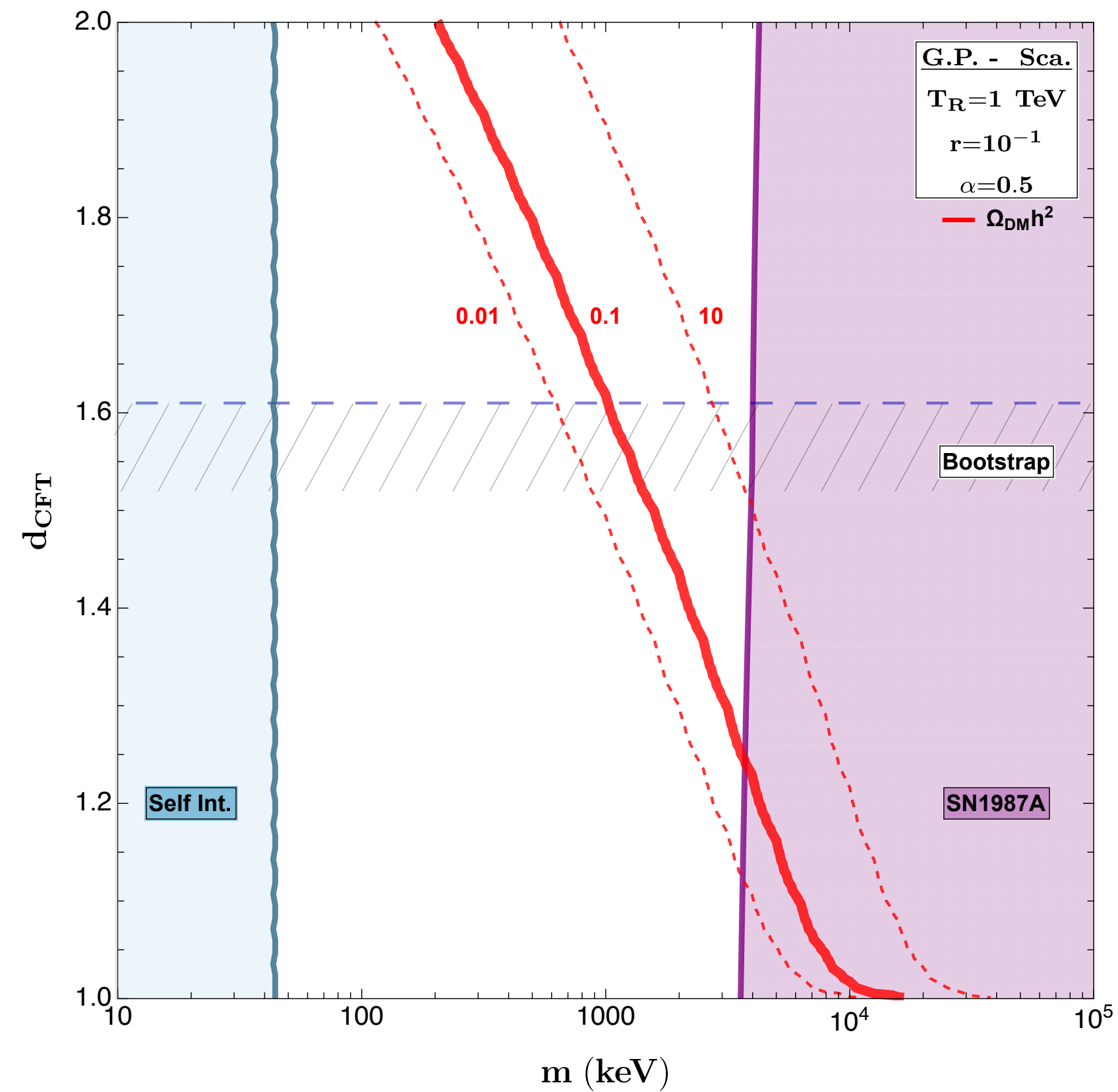


vector rho dominant

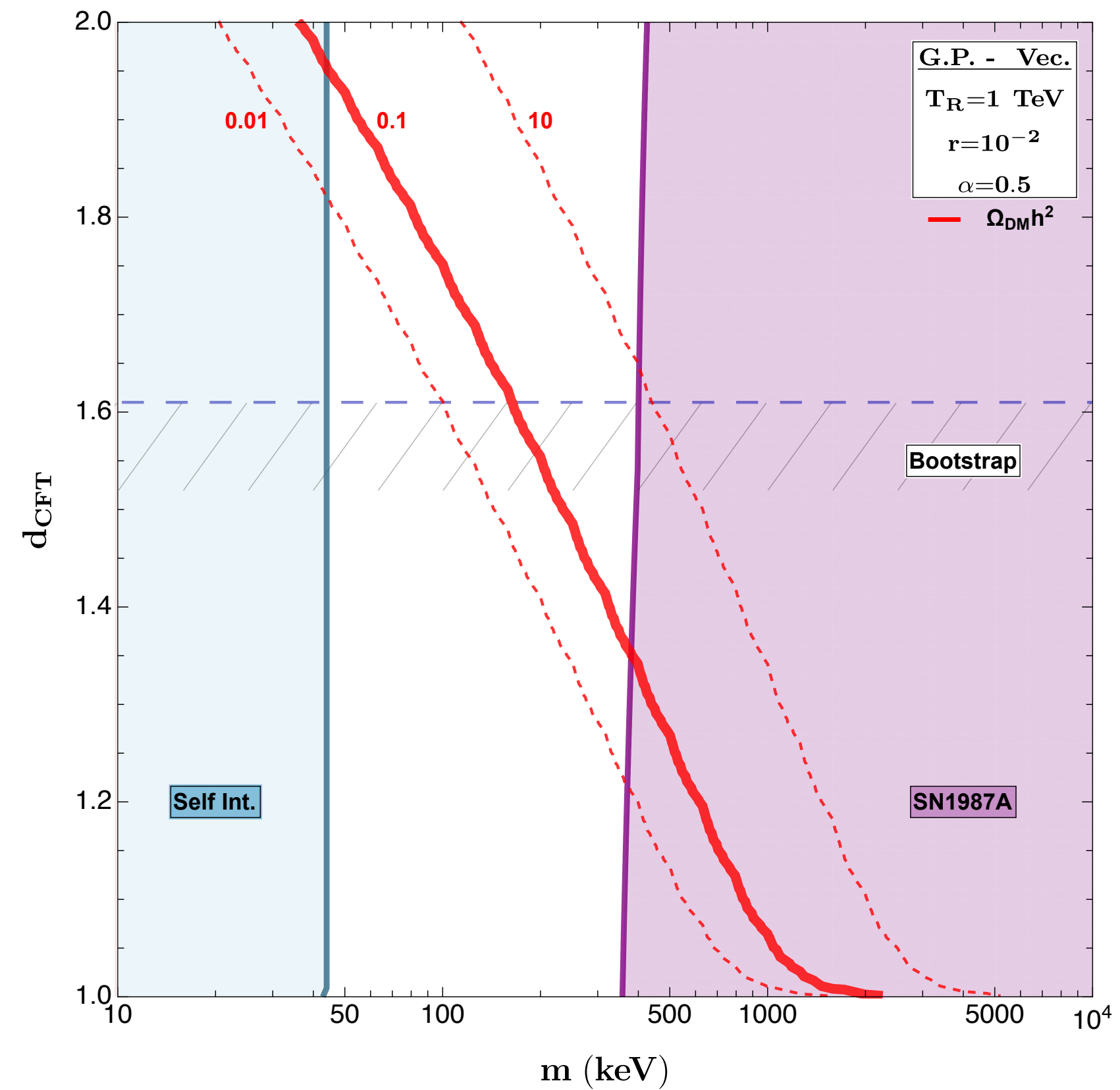
[MFV couplings]

Gluon Portal

$$\mathcal{O}_{\text{SM}} = G^{\mu\nu} G_{\mu\nu}$$

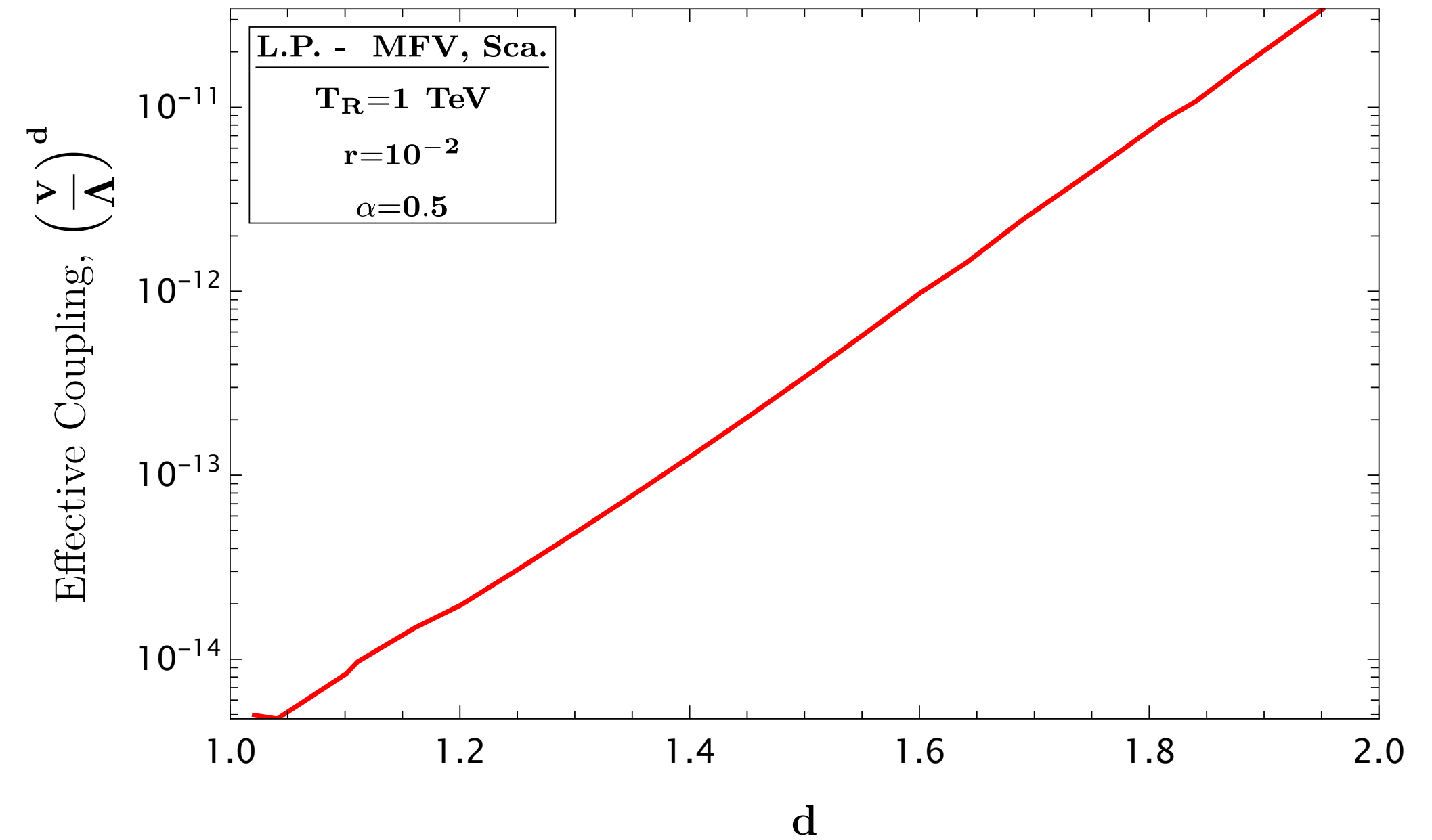
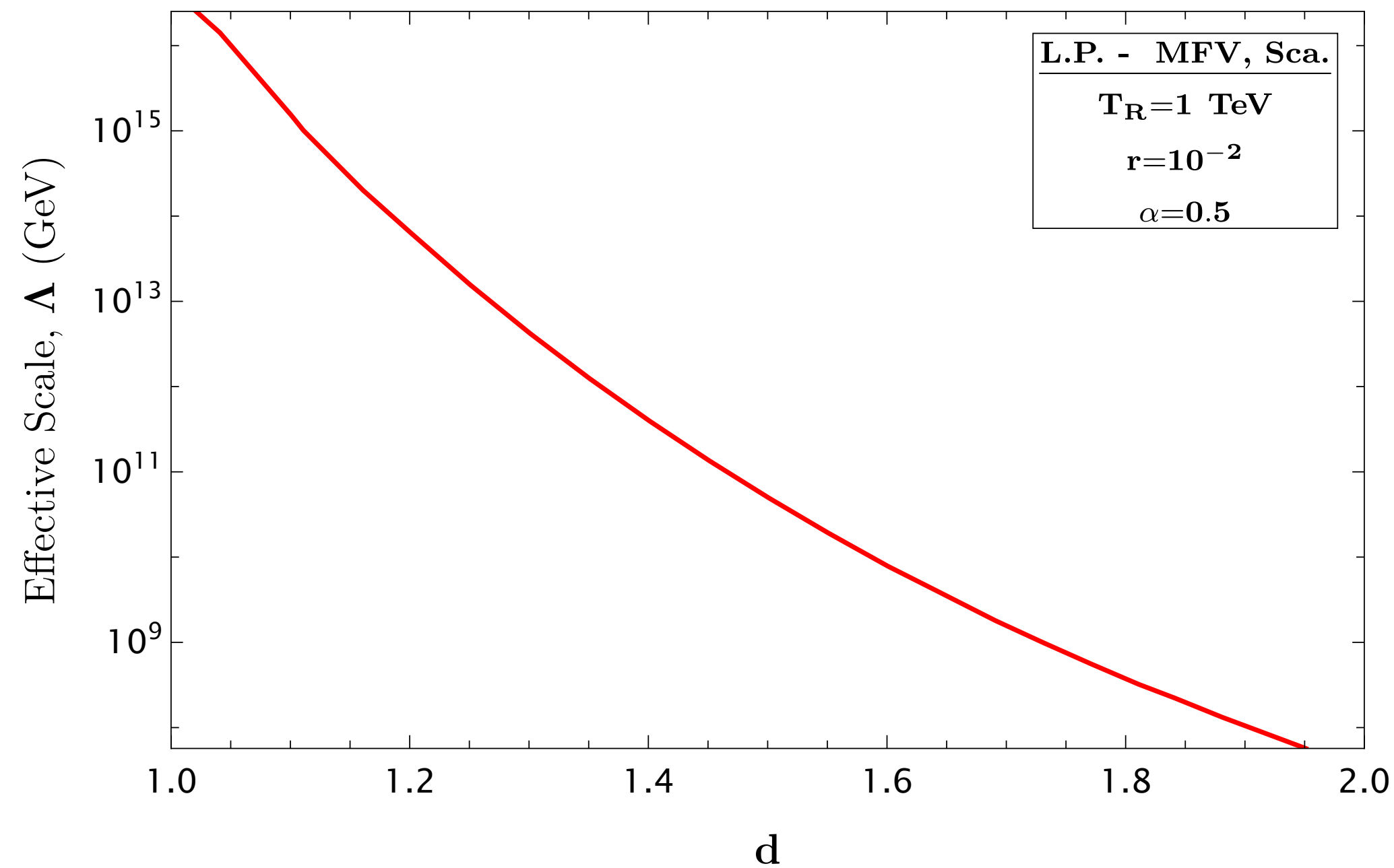


scalar rho dominant



vector rho dominant

DM-SM Couplings

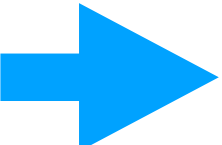


$$\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^{D-4}} \mathcal{O}_{\text{SM}} \mathcal{O}_{\text{CFT}}$$

[Example: MFV Lepton Portal]

➔ $\Lambda = (\lambda_{\text{CFT}})^{-\frac{1}{D-4}} \cdot \Lambda_{\text{CFT}} \sim 10^{10} - 10^{15} \text{ GeV}$

Observational Signatures?

- DM-SM Couplings are too weak for production at colliders, direct/indirect detection (common feature of freeze-in models)
- DM mass in the 10 keV-1 MeV range  free-streaming at scales accessible with future improved large-scale structure data
- CFT->matter phase transition in the dark sector at $T \sim M_{\text{gap}}$
- No structures smaller than Hubble scale at the time of the phase transition can be formed
- Stochastic gravitational wave production if first-order phase transition (unfortunately $\Omega_{GW} \propto (T_{\text{dark}}/T_{\text{SM}})^8$)

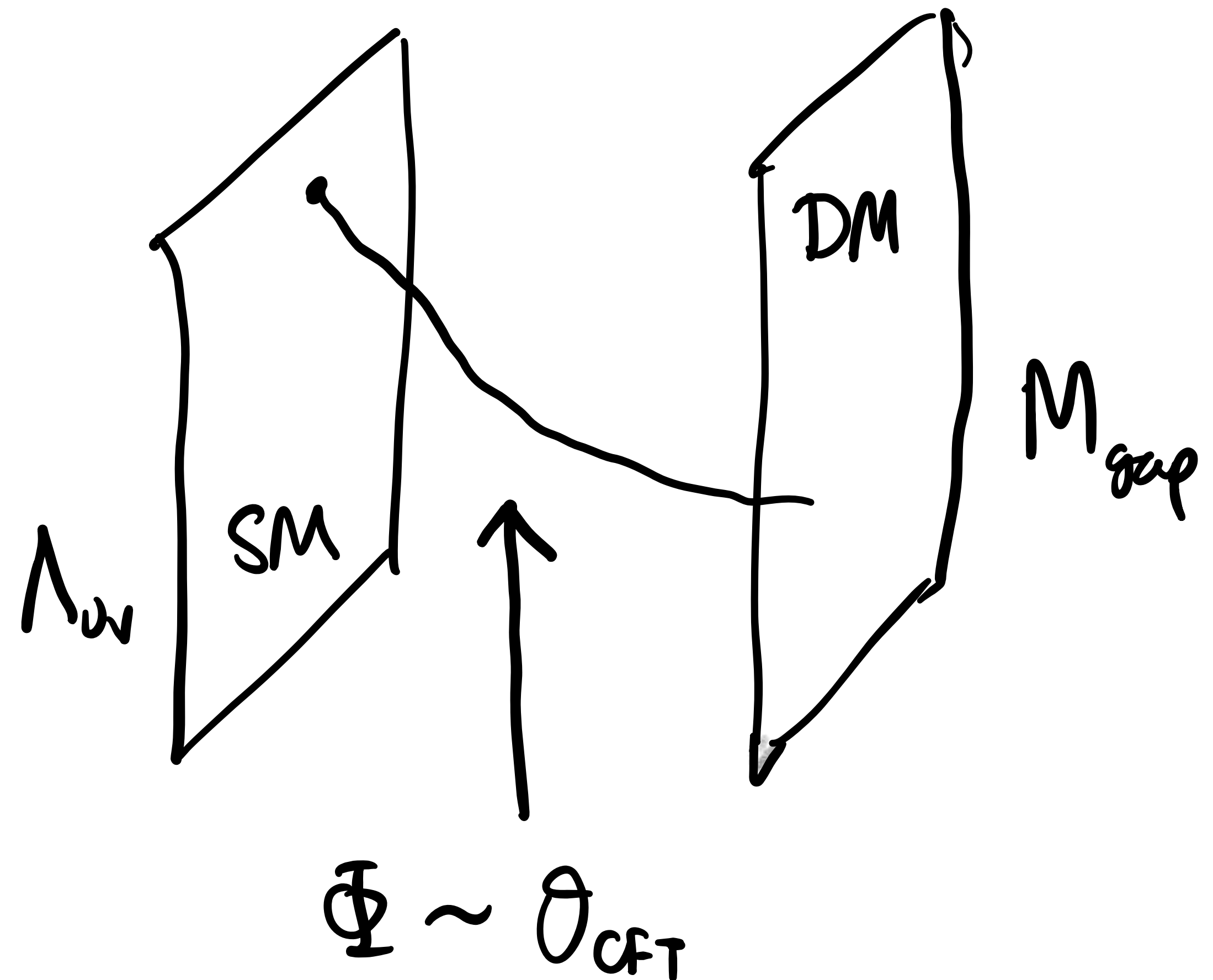
Summary

\mathcal{O}_{SM}	DM Mass (Scalar Mediator)	DM Mass (Vector Mediator)	Dominant CFT Deformation	Dominant Production Mode
$H^\dagger H$	0.4 - 1.2 MeV	40 - 400 keV	Tree-level	$h \rightarrow \text{CFT}$
$HQ^\dagger q$	1st: SN All: 0.1 - 1 MeV MFV: 0.5 - 5 MeV	1st: SN All: 50 - 200 keV MFV: 0.1 - 1 MeV	Radiative mixing	$q\bar{q} \rightarrow \text{CFT}$
$HL^\dagger \ell_R$	1st: WDM All: 3 - 10 keV MFV: 10 - 100 keV	1st: WDM All: WDM MFV: WDM	Radiative mixing	$\ell\bar{\ell} \rightarrow \text{CFT}$
$G^{\mu\nu} G_{\mu\nu}$	0.2 - 2 MeV	50 - 400 keV	Radiative direct	$gg \rightarrow \text{CFT}$
$B^{\mu\nu} B_{\mu\nu}$	0.1 - 10 MeV	0.05 - 1 MeV	Radiative direct	$\gamma\gamma \rightarrow \text{CFT}$

5D Dual: Relevant Dilaton

[work in progress with Lillian Luo]

- AdS/CFT correspondence indicates that the above setup has a 5D dual: AdS slice, SM on UV brane, DM IR-localized
- \mathcal{O}_{CFT} is dual to a bulk scalar field
- Key feature of COFI: Conformal symmetry breaking in the SM determines the scale of CFT breaking in the IR
- In 5D: Physics on the UV brane sets up the position of the IR brane
- Realized explicitly in “Relevant Dilaton Stabilization” models (constructed for EW/Planck hierarchy stabilization)



[Csaki, Geller, Heller-Algazi, Ismail, '23]

5D Dual: Relevant Dilaton

- In relevant dilation model, bulk action is

$$S_{\Phi} = \int d^4x dy \sqrt{g} \left[\frac{1}{2} g^{MN} \partial_M \Phi \partial_N \Phi - \frac{1}{2} m^2 \Phi^2 - \frac{\sqrt{g_{\text{ind}}}}{\sqrt{g}} V_{\text{UV}}(\Phi) \delta(y) - \frac{\sqrt{g_{\text{ind}}}}{\sqrt{g}} V_{\text{IR}}(\Phi) \delta(y - y_c) \right]$$

$$V_{\text{UV}}(\Phi) = \frac{1}{2} m_{\text{UV}} \Phi^2 + \gamma k^{5/2} \Phi,$$

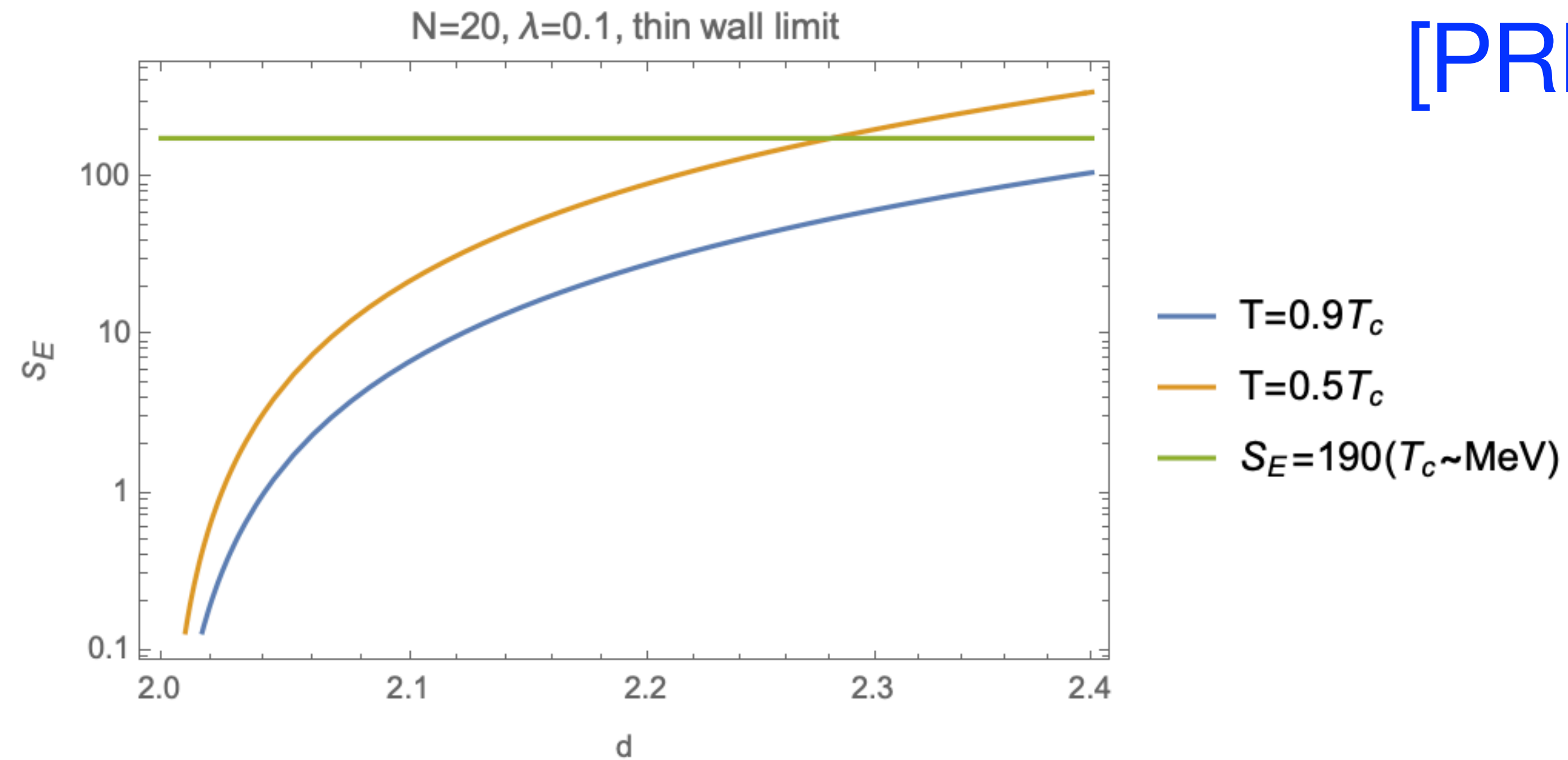
$$V_{\text{IR}}(\Phi) = \frac{1}{2} m_{\text{IR}} \Phi^2$$

- The UV-brane tadpole term serves as a source for the bulk field
- Minimizing the bulk action fixes the location of the IR brane (or equivalently dilation vev):

$$\chi \equiv k e^{-k y_c} \quad \langle \chi \rangle = k \left(\frac{\lambda_{2\nu\nu}}{2\lambda} \right)^{1/(4-2\nu)} \quad \longleftrightarrow \quad M_{\text{gap}} = \left(\frac{\lambda_{\text{CFT}}}{\Lambda_{\text{CFT}}^{d-2}} v^2 \right)^{\frac{1}{4-d}}$$

in COFI (Higgs portal)

5D dual: Phase Transition



[PRELIMINARY!]

- Preliminary conclusion: First-order transition completes promptly at $T_{PT} \sim M_{\text{gap}}$
- Gravitational wave production is under investigation

Conclusions

- Dark Sector described by a CFT is a natural and generic possibility
- Coupling of DS to SM necessarily breaks Conformal symmetry
- If coupling is via relevant CFT operator, low-energy phase is non-conformal → can contain dark matter
- Conformal Freeze-In (COFI): DS is populated from SM when it is in conformal phase, then undergoes a phase transition in which DM particles are created
- Produces viable DM candidate with mass in the 10 keV-10 MeV range
- Very feeble interactions of DM with SM, but large-scale structure signatures are possible
- Dark Sector phase transition/Gravitational wave production can be studied using 5D dual