## Bootstrapping BSMs



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based on 22II. 12488 [hep-th] with C. Fernandez, F. Riva and F. Sciotti 2307.04729 [hep-th] with T. Ma and F. Sciotti

## Motivation

E $\begin{aligned} & \text { UV completion? } \\ & \text { Effective Field Theory (EFT) }\end{aligned}$
good tool to describe exp. data!

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Usual BSM approach: model by model...
e.g., SM hierarchy problem: MSSM, composite Higgs,...

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## UV completion for a theory of Goldstones

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interesting for

- QCD,
- axions,
- composite Higgs


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## UV completion for a theory of Goldstones

E $\uparrow$ UV completion? $\prod_{\text {simplifying assumption: }}^{\downarrow}$

$\pi^{a}$

as weakly-coupled theories (tree-level) but with infinite higher-spin states

Also aiming strongly-coupled gauge theories (QCD) in the large- $\mathbf{N}_{\mathbf{c}}$ limit:
G. 't Hooft, Nucl. Phys. B 72, 461 (1974)
E. Witten, Nucl. Phys. B 160, 57 (1979)
quarks, gluons $\mathbf{S U}\left(\mathbf{N}_{\mathrm{c}}\right)$
 mesons ( $q \bar{q}$ states), glueballs


## Positivity bounds on (tree-level mediated) amplitudes

Analytical structure of $\mathbf{2 \rightarrow 2}$ amplitudes:
$\mathcal{M}(s, t)$

simple poles due to states in the s-channel:


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$$
\oint \frac{\mathcal{M}(s, t)}{s^{k+1}}=0
$$

## Positivity bounds on (tree-level mediated) amplitudes

This simple structure allows to get dispersion relations:

Cauchy at work:

residue at the origin + sum of residues at the mass poles $=0$
(low-energy EFT parameters related to masses and couplings of mesons)

## Goldstone-Goldstone scattering

J. Albert and L. Rastelli, arXiv: 2203.11950

Lets assume an $\mathbf{S U ( 2 )}$ (isospin) global symmetry


$$
\pi^{a} \in \mathbf{3} \text { massless }
$$

Goldstones from
$S U(2) \otimes S U(2) \rightarrow S U(2)$

Extra condition from large- $\mathrm{N}_{\mathrm{c}}$ QCD:

## Mesons = <br> 

Isospin $=\mathrm{I}=\mathbf{1 / 2} \otimes \mathbf{1 / 2} \mathbf{= 0 , 1}$<br>no I =2 states

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$\mathcal{M}_{s}^{I=2}$
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Working with $\mathcal{M}_{t}^{I=2}(s, u)$
(that cannot have poles in the t-channel)


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Wilson coefficients

$$
\mathcal{M}_{t}^{I=2}(s, u) \rightarrow g_{1,0}^{s, u \rightarrow 0}(s+u)+g_{2,0}\left(s^{2}+u^{2}\right)+g_{2,1} s u+\cdots
$$

Legendre pol. and derivatives (all positive!)

## small u expansion:

$k=1: \quad g_{1,0}+g_{2,1} u+g_{3,1} u^{2}+\ldots=\sum_{i}\left|g_{\pi \pi i}\right|^{2}\left(\frac{P_{J_{i}}(1)}{m_{i}^{2}}+2 \frac{P_{J_{i}}^{\prime}(1)}{m_{i}^{4}} u+2 \frac{P_{J_{i}}^{\prime \prime}(1)}{m_{i}^{6}} u^{2}+\ldots\right)$,
$k=2: \quad g_{2,0}+g_{3,1} u+g_{4,2} u^{2}+\ldots=\sum_{i}\left|g_{\pi \pi i}\right|^{2}\left(\frac{P_{J_{i}}(1)}{m_{i}^{4}}+2 \frac{P_{J_{i}}^{\prime}(1)}{m_{i}^{6}} u+2 \frac{P_{J_{i}}^{\prime \prime}(1)}{m_{i}^{8}} u^{2}+\ldots\right)$,
$k=3: \quad g_{3,0}+g_{4,1} u+g_{5,2} u^{2}+\ldots=\sum_{i}\left|g_{\pi \pi i}\right|^{2}\left(\frac{P_{J_{i}}(1)}{m_{i}^{6}}+2 \frac{P_{J_{i}}^{\prime}(1)}{m_{i}^{8}} u+2 \frac{P_{J_{i}}^{\prime \prime}(1)}{m_{i}^{10}} u^{2}+\ldots\right)$,

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\end{array}
$$

$$
\begin{aligned}
& g_{n, 0}= \sum_{i} \frac{g_{i \pi \pi}^{2}}{m_{i}^{2 n}} \begin{array}{c}
\text { all states } \\
\text { contribute } \\
\text { positively! }
\end{array} \\
& g_{n+1,1}=\sum_{i} \frac{g_{i \pi \pi}^{2} J_{i}\left(J_{i}+1\right)}{m_{i}^{2(n+1)}} \\
& \Rightarrow \text { the larger the } J, \\
& \text { the smaller } g_{i m \pi} / m_{i}
\end{aligned}
$$

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\vdots &
\end{array}
$$

due to crossing, overconstrained system!
infinite constraints in the spectrum and couplings

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\text { e.g. } \quad \sum_{i} \frac{\left|g_{\pi \pi i}\right|^{2}}{m_{i}^{6}} J_{i}\left(J_{i}+1\right)\left(J_{i}-2\right)\left(J_{i}+3\right)=0
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k=3: & g_{3,0}+g_{4,} u+g_{5}, 2 u^{2}+\ldots=\sum_{i}\left|g_{\pi \pi i}\right|^{2}\left(\frac{P_{J_{i}}(1)}{m_{i}^{6}}+2 \frac{P_{J_{i}}^{\prime}(1)}{m_{i}^{8}} u+2 \frac{P_{J_{i}}^{\prime \prime}(1)}{m_{i}^{10}} u^{2}+\ldots\right),
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due to crossing, overconstrained system!
infinite constraints in the spectrum and couplings

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\text { e.g. } \quad \sum_{i} \frac{\left|g_{\pi \pi i}\right|^{2}}{m_{i}^{6}} J_{i}\left(J_{i}+1\right)\left(J_{i}-2\right)\left(J_{i}+3\right)=0
$$

also from dispersion relations at fixed $t$

## Implications of Positivity bounds

Lets assume at $|s| \rightarrow \infty$ \& either t or u fixed:

$$
\frac{\mathcal{M}_{t}^{I=2}(s, u)}{s \quad k_{\min }=1} \rightarrow 0
$$

expected from Regge theory

## Infinite set of Sum Rules:

$\sum_{i} \frac{\left|g_{\pi \pi i}\right|^{2}}{m_{i}^{6}} J_{i}\left(J_{i}+1\right)\left(J_{i}-2\right)\left(J_{i}+3\right)=0$
$\sum_{i} \frac{\left|g_{\pi \pi i}\right|^{2}}{m_{i}^{10}} J_{i}\left(J_{i}-1\right)\left(J_{i}+1\right)\left(J_{i}+2\right)\left(J_{i}^{2}+J_{i}-15\right)=0$
$\sum_{i} \frac{\left|g_{\pi \pi i}\right|^{2}}{m_{i}^{14}} J_{i}\left(J_{i}-2\right)\left(J_{i}-1\right)\left(J_{i}+1\right)\left(J_{i}+2\right)\left(J_{i}+3\right)\left(J_{i}^{2}+J_{i}-28\right)=0$

## Infinite set of Sum Rules:

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\begin{aligned}
& \left.\left.\sum_{i} \frac{\left|g_{\pi \pi i}\right|^{2}}{m_{i}^{6}} J_{i} \right\rvert\, J_{i}+1\right)\left(J_{i}-2\right)\left(J_{i}+3\right)=0 \\
& \left.\sum_{i} \frac{\left|g_{\pi \pi i}\right|^{2}}{m_{i}^{10}} J_{i}\right\}\left(J_{i}-1\right)\left(J_{i}+1\right)\left(J_{i}+2\right)\left(J_{i}^{2}+J_{i}-15\right)=0 \\
& \sum_{i} \frac{\left|g_{\pi \pi i}\right|^{2}}{m_{i}^{14}} \underbrace{}_{J_{i}\left(J J_{i}-2\right)\left(J_{i}-1\right)\left(J_{i}+1\right)\left(J_{i}+2\right)\left(J_{i}+3\right)\left(J_{i}^{2}+J_{i}-28\right)=0}
\end{aligned}
$$

$J_{i}=0$ states satisfy all constraints
possible UV completion:
Theory of Scalars (Higgs mechanism)


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$$
\frac{\left|g_{\pi \pi 1}\right|^{2}}{m_{J=1}^{6}}=9 \frac{\left|g_{\pi \pi 3}\right|^{2}}{m_{J=3}^{6}}+35 \frac{\left|g_{\pi \pi 4}\right|^{2}}{m_{J=4}^{6}}+\cdots
$$

spin-1 must be in the spectrum with the largest coupling

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Vector Meson Dominance (VMD),
assumed in the past to explain QCD experimental data

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spin- $\mathbf{3}$ must be in the spectrum

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non-scalar UV completions require all spin states with couplings to pions decreasing with $J$

From the constraints, we find numerically $\left(-50\right.$ constraint, $\left.J_{\text {max }}-1000\right)$ :

## Upper bound on couplings

(normalized to $m_{i}^{2} / F_{\pi}^{2}$ )

| J | $\left\|g_{\pi \pi i}\right\|^{2}$ |
| :--- | :--- |
| 1 | 0.78 |
| 2 | 0.18 |
| 3 | 0.03 |

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| 2 | 0.18 | $\longrightarrow$ | 0.18 |
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## Constraints on Wilson coefficients

$\mathcal{L}=\frac{F_{\pi}^{2}}{4} \operatorname{Tr}\left(\partial_{\mu} U^{\dagger} \partial^{\mu} U\right)+L_{1} \operatorname{Tr}^{2}\left(\partial_{\mu} U^{\dagger} \partial^{\mu} U\right)+L_{2} \operatorname{Tr}\left(\partial_{\mu} U^{\dagger} \partial_{\nu} U\right) \operatorname{Tr}\left(\partial^{\mu} U^{\dagger} \partial^{\nu} U\right)+L_{3} \operatorname{Tr}\left(\partial_{\mu} U^{\dagger} \partial^{\mu} U \partial_{\nu} U^{\dagger} \partial^{\nu} U\right)$

$$
\mathbf{e}^{\mathbf{i} \sigma^{\mathbf{a}} \pi^{\mathbf{a}} / \mathbf{F}_{\pi}}
$$

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(S) $\left.\mathbf{S}^{2}\right): \quad \tilde{g}_{2,0}=4\left(2 L_{1}+3 L_{2}+L_{3}\right) \frac{M^{2}}{F_{\pi}^{2}}, \quad \tilde{g}_{2,1}=16 L_{2} \frac{M^{2}}{F_{\pi}^{2}}$

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"Polyhedronal"
bounds


EFTs are
"EFT-hedron"

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mass of the 1st meson


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\mathcal{L}=\frac{F_{\pi}^{2}}{4} \operatorname{Tr}\left(\partial_{\mu} U^{\dagger} \partial^{\mu} U\right)+L_{1} \operatorname{Tr}^{2}\left(\partial_{\mu} U^{\dagger} \partial^{\mu} U\right)+L_{2} \operatorname{Tr}\left(\partial_{\mu} U^{\dagger} \partial_{\nu} U\right) \operatorname{Tr}\left(\partial^{\mu} U^{\dagger} \partial^{\nu} U\right)+L_{3} \operatorname{Tr}\left(\partial_{\mu} U^{\dagger} \partial^{\mu} U \partial_{\nu} U^{\dagger} \partial^{\nu} U\right)
$$

(s) $\left.\mathbf{S}^{2}\right): \quad \tilde{g}_{2,0}=4\left(2 L_{1}+3 L_{2}+L_{3}\right) \frac{M^{2}}{F_{\pi}^{2}}, \quad \tilde{g}_{2,1}=16 L_{2} \frac{M^{2}}{F_{\pi}^{2}}$
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$$
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$$

Amazingly, related to the fact that


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Experimental
QCD data

## Explaining the success of holography

## AdS/QCD: 5D model for QCD mesons

$S U(2)_{L} \times S U(2)_{R} \quad$ model with only $\mathbf{s}=0,1$ fields:
Erlich+Katz+Son+Stephanov 05
Da Rold+Pomarol 05

$$
\mathcal{L}_{5}=\frac{M_{5}}{2} \operatorname{Tr}\left[-L_{M N} L^{M N}-R_{M N} R^{M N}+\left|D_{M} \Phi\right|^{2}+3|\Phi|^{2}\right]
$$

|  | Experiment | $\mathrm{AdS}_{5}$ | Deviation |
| :---: | :---: | :---: | :---: |
| $m_{\rho}$ | 775 | 824 | $+6 \%$ |
| $m_{a_{1}}$ | 1230 | 1347 | $+10 \%$ |
| $m_{\omega}$ | 782 | 824 | $+5 \%$ |
| $F_{\rho}$ | 153 | 169 | $+11 \%$ |
| $F_{\omega} / F_{\rho}$ | 0.88 | 0.94 | $+7 \%$ |
| $F_{\pi}$ | 87 | 88 | $+1 \%$ |
| $g_{\rho \pi \pi}$ | 6.0 | 5.4 | $-10 \%$ |
| $L_{9}$ | $6.9 \cdot 10^{-3}$ | $6.2 \cdot 10^{-3}$ | $-10 \%$ |
| $L_{10}$ | $-5.2 \cdot 10^{-3}$ | $-6.2 \cdot 10^{-3}$ | $-12 \%$ |
| $\Gamma(\omega \rightarrow \pi \gamma)$ | 0.75 | 0.81 | $+8 \%$ |
| $\Gamma(\omega \rightarrow 3 \pi)$ | 7.5 | 6.7 | $-11 \%$ |
| $\Gamma(\rho \rightarrow \pi \gamma)$ | 0.068 | 0.077 | $+13 \%$ |
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Success understood from the above analysis: J>I mesons contribute little to low-energy observables

## Similar structure for higher-order Wilson coeff.

## $O\left(s^{3}\right):$



## UV completions for models of Goldstones



## UV completions for models of Goldstones



## U(I)A axial anomaly

Introducing the $\eta^{\prime}$ (Goldstone of an anomalous symmetry):

$$
\begin{aligned}
& U(2) \otimes U(2) \rightarrow U(2) \\
& \quad \longrightarrow S U(2) \otimes S U(2) \otimes U(I)_{A} \otimes U(I)
\end{aligned}
$$

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- Adding external gauge-bosons:

$$
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$$



two qL, QR model

a) It cannot be mediated by scalars

> axial anomaly discards theories with only scalar resonances
b) Bounded

## How a bound on the anomaly arises:



## How a bound on the anomaly arises:



Amazingly, a bound can be extended in general (from positivity):


$$
\kappa \sqrt{\frac{2 F_{\pi}^{2}}{\mathcal{P}}}
$$



spin-I coupling to pions


## Weak gravity conjecture (WGC)-like bound

$$
G \leq 10.6618 e^{2}+0.0367 g_{0,1}
$$

## Bounds on the anomaly in susy models:

$$
\begin{aligned}
& \begin{array}{l}
\left\langle\hat{\jmath}_{\mu}(x) \hat{\jmath}_{\nu}(y) \hat{\jmath}_{\rho}(z)\right\rangle \xlongequal{\hat{\jmath}_{\mu}=\frac{2 \pi^{2}}{\sqrt{3 \tau}} j_{\mu}}{ }_{\text {bounds }} D_{\mu \nu \rho}(x, y, z)
\end{array} \\
& 1909.11676
\end{aligned}
$$

## Conclusions

- Crossing + Analyticity + Unitarity allow to get information on possible UV completions of theories of Goldstones:

- Predicts a "EFT-hedron" structure


## Conclusions

- Crossing + Analyticity + Unitarity allow to get information on possible UV completions of theories of Goldstones:

- Axial anomaly can discriminate between the two possibilities

Bounded from above:

$$
\frac{\kappa}{\sqrt{\mathcal{P} / F_{\pi}^{2}}} \leq \frac{1}{\sqrt{2}}
$$

$\Rightarrow$ potential interest to constrain DM scenarios (e.g. SIMPs)

- Gravitational anomaly?


## RESTRICTED AREA

## MONITORED BY VIDEO CAMERA

$$
0=\sum_{i} \frac{\left|g_{\pi \pi i}\right|^{2}}{m_{i}^{2 n}}(\underbrace{\left.\frac{2^{n-1}}{(n-1)!} P_{J_{i}}^{(n-1)}(1)-\mathcal{J}_{i}^{2}\right)}_{\mathcal{X}_{n, 1}} \quad \begin{array}{ll} 
& n=2,3,4, \ldots \\
J^{2} \equiv J(J+1)
\end{array}
$$




Lets assume at $s \rightarrow \infty$ and either t or u fixed:

$$
\frac{\mathcal{M}_{t}^{I=2}(s, u)}{s^{2}} \rightarrow 0
$$



## C The su-models

Let us consider the most general theory of a degenerate spectrum that contributes to the fourpion amplitude $\mathcal{M}(s, u)[7,8]$. This means that all states have equal mass $m$, and therefore the denominator of this amplitude is fixed to be $\mathcal{M}(s, u) \propto 1 /\left(\left(s-m^{2}\right)\left(u-m^{2}\right)\right)$. If we further demand that Eq. (6a) and Eq. (6b) are satisfied for $k_{\min }=1$, we are led to

$$
\begin{equation*}
\mathcal{M}(s, u)=\frac{a_{1} m^{4}+a_{2} m^{2}(s+u)+a_{3} s u}{\left(s-m^{2}\right)\left(u-m^{2}\right)} \tag{91}
\end{equation*}
$$

where $a_{i}$ are constants. The Adler's zero condition fixes $a_{1}=0$. Then, aside from a global multiplicative factor, the amplitude has only one free parameter. We can write it as

$$
\begin{equation*}
\mathcal{M}_{1}^{(s u)}(s, u)=\frac{m^{2}(s+u)+\lambda s u}{\left(s-m^{2}\right)\left(u-m^{2}\right)} \tag{92}
\end{equation*}
$$

where the possible values of $\lambda$ are determined by unitarity. Indeed, imposing the positivity of the residues of Eq. (92), we obtain

$$
\begin{equation*}
-2 \leq \lambda \leq \frac{2 \ln 2-1}{1-\ln 2} \tag{93}
\end{equation*}
$$

In the limiting case $\lambda=-2$, the residues of all $J>0$ states are zero, and we are left with the scalar amplitude Eq. (22). In the other limit,

$$
\begin{equation*}
\lambda=\frac{2 \ln 2-1}{1-\ln 2} \simeq 1.26 \tag{94}
\end{equation*}
$$



## D The Lovelace-Shapiro amplitude

The Lovelace-Shapiro (LS) amplitude for the scattering of four pions is defined as [26, 27]

$$
\begin{equation*}
\mathcal{M}^{(\mathrm{LS})}(s, u)=\frac{\Gamma(1-\alpha(s)) \Gamma(1-\alpha(u))}{\Gamma(1-\alpha(s)-\alpha(u))} \tag{105}
\end{equation*}
$$

where $\alpha(s)=\alpha_{0}+\alpha^{\prime} s$ is referred as the Regge trajectory. We will fix the values of $\alpha_{0}$ and $\alpha^{\prime}$ by requiring that Eq. (106) satisfies the Adler zero condition, $\mathcal{M}^{(\mathrm{LS})}(s, u) \rightarrow 0$ for $s, u \rightarrow 0$, and that the first pole of Eq. (106) occurs for $s=m_{\rho}^{2}$. These two conditions lead to $\alpha_{0}=1 / 2$ and $\alpha^{\prime}=1 /\left(2 m_{\rho}^{2}\right)[66]$ and then we can write

$$
\begin{equation*}
\mathcal{M}^{(\mathrm{LS})}(s, u)=\frac{\Gamma\left(\frac{1}{2}-\frac{s}{2 m_{\rho}^{2}}\right) \Gamma\left(\frac{1}{2}-\frac{u}{2 m_{\rho}^{2}}\right)}{\Gamma\left(\frac{t}{2 m_{\rho}^{2}}\right)} . \tag{106}
\end{equation*}
$$

By looking at the poles of Eq. (106), one can see that the LS amplitude corresponds to a theory of higher-spin states with masses

$$
\begin{equation*}
m_{n}^{2}=m_{\rho}^{2}(2 n+1), \quad n=0,1,2, \ldots \tag{107}
\end{equation*}
$$

For a given $n$, there are at most $n+1$ states with $\operatorname{spin} J=0,1, \ldots, n+1$. Furthermore, Eq. (106) satisfies the condition Eq. (6a) and Eq. (6b) with $k_{\min }=1$.

## E The Coon amplitude

The Lovelace-Shapiro amplitude presented in Appendix D can be generalized to a larger class of amplitudes depending on an additional parameter $q$. This is the so-called Coon amplitude, which was first proposed in $[28]^{11}$ :

$$
\begin{equation*}
\mathcal{M}_{q}(s, u)=C(\sigma, \tau, q) \prod_{n=0}^{\infty} \frac{\left(1-q^{n+1}\right)\left(\sigma \tau-q^{n+1}\right)}{\left(\sigma-q^{n+1}\right)\left(\tau-q^{n+1}\right)} \tag{118}
\end{equation*}
$$

where $\sigma=1+(q-1)\left(\alpha_{0}+\alpha^{\prime} s\right)$ and $\tau=1+(q-1)\left(\alpha_{0}+\alpha^{\prime} u\right)$. As explained in Appendix D, we take $\alpha_{0}=1 / 2$ and $\alpha^{\prime}=1 /\left(2 m_{\rho}^{2}\right)$. The parameter $q$ takes values between 0 and 1 , and in the limit $q \rightarrow 1$ we recover the LS amplitude Eq. (106). There is some freedom in the choice of the prefactor $C$, as long as it satisfies $\lim _{q \rightarrow 1} C(\sigma, \tau, q)=1$.

The Coon amplitude has an infinite number of simple poles at

$$
\begin{equation*}
s_{n}=m_{\rho}^{2} \frac{1+q-2 q^{n+1}}{1-q}, \quad n=0,1,2, \ldots \tag{119}
\end{equation*}
$$

## Impact on BSM searches at the LHC

Higgs as a Pseudo-Goldtone boson:

Indirect probes:

deviations in Higgs coupling

Direct probes:


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Direct probes:

$$
\overbrace{\bar{q}}^{q^{\prime}} \sim_{g_{*}^{\prime}}^{w^{\prime}}{ }_{\substack{\prime}}^{w^{\prime}}
$$


e.g. I502.0I70I [hep-th]

## Impact on BSM searches at the LHC

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