

Dark matter detection with superfluid optomechanics

Peter Cox

The University of Melbourne

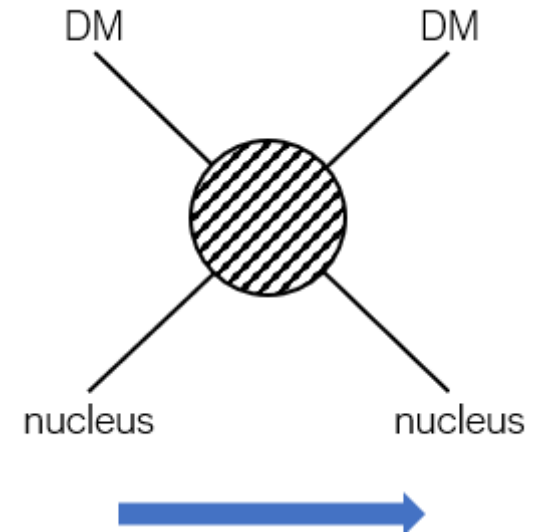
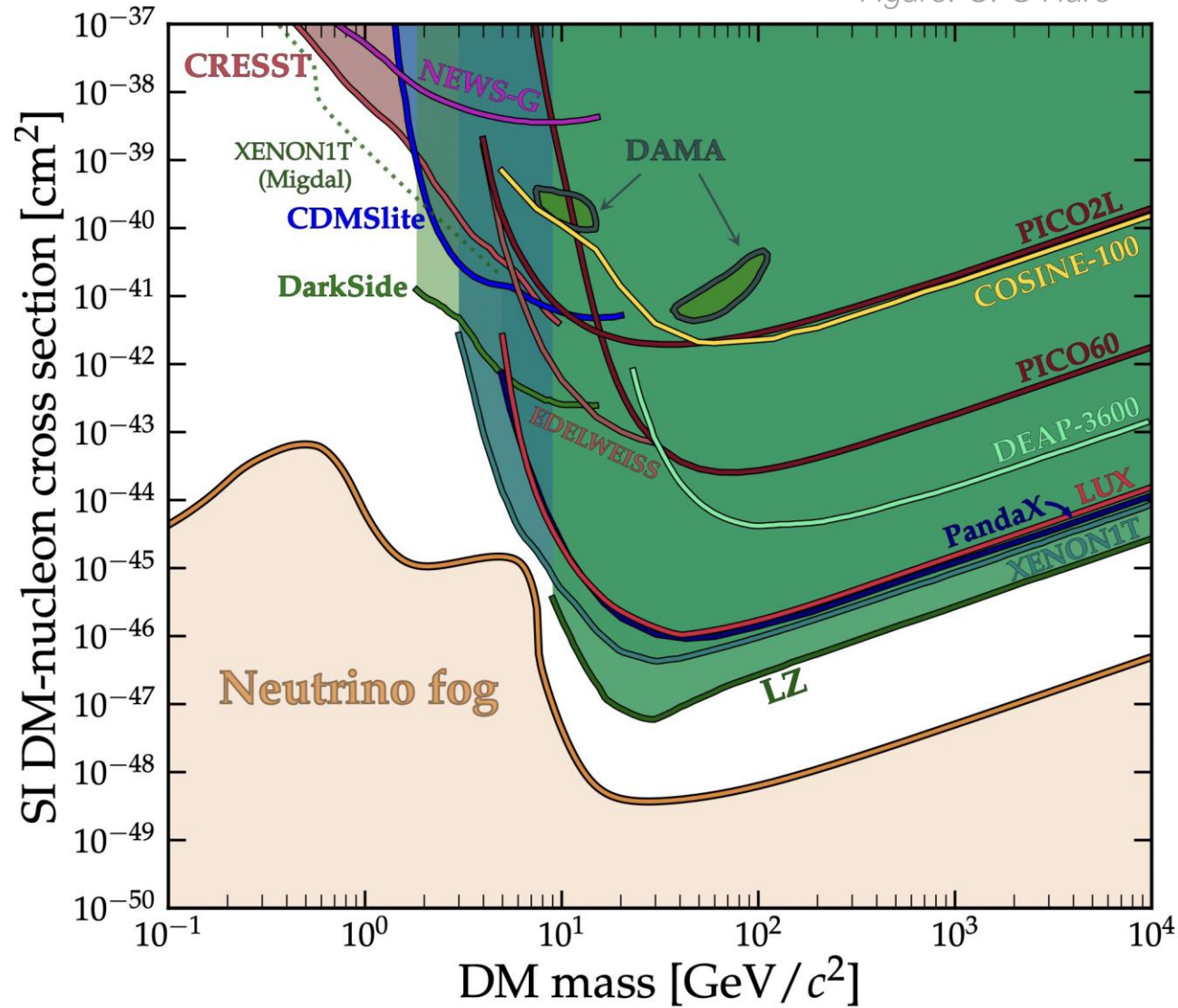
with C. Baker, W. Bowen, M. Dolan, M. Goryachev, G. Harris

arXiv:2306.09726



Direct detection: current status

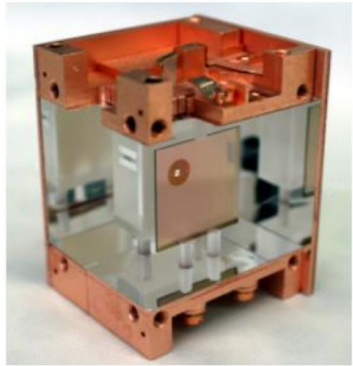
Figure: C. O'Hare



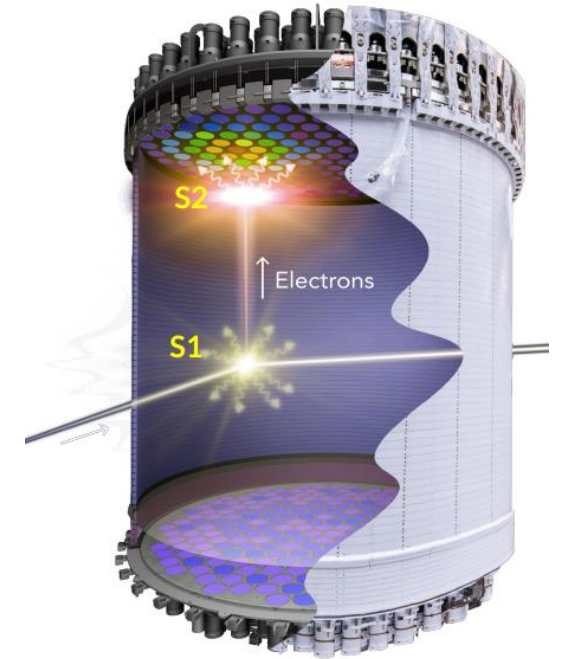
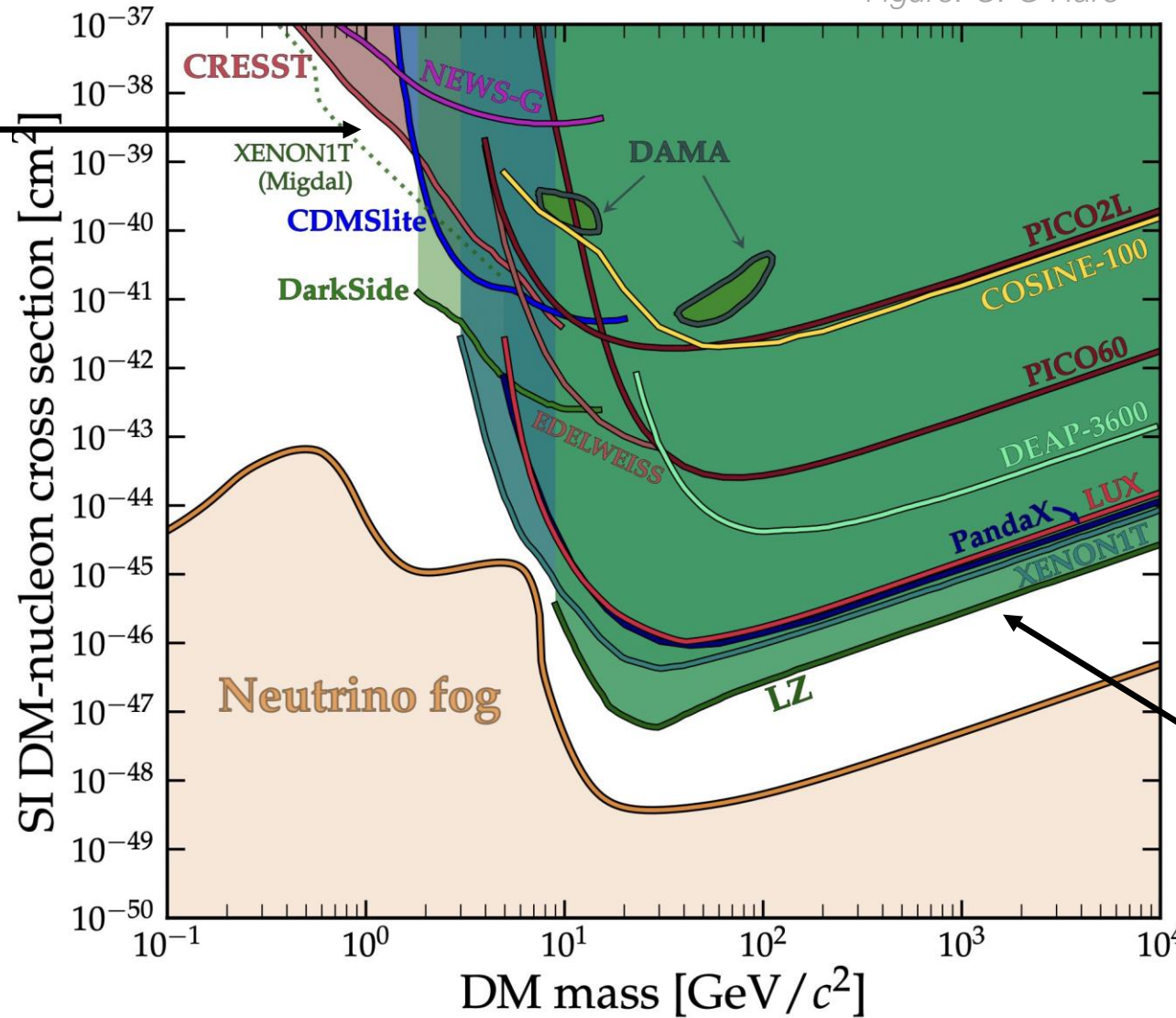
Direct detection: current status

Figure: C. O'Hare

cryogenic experiments



CRESST

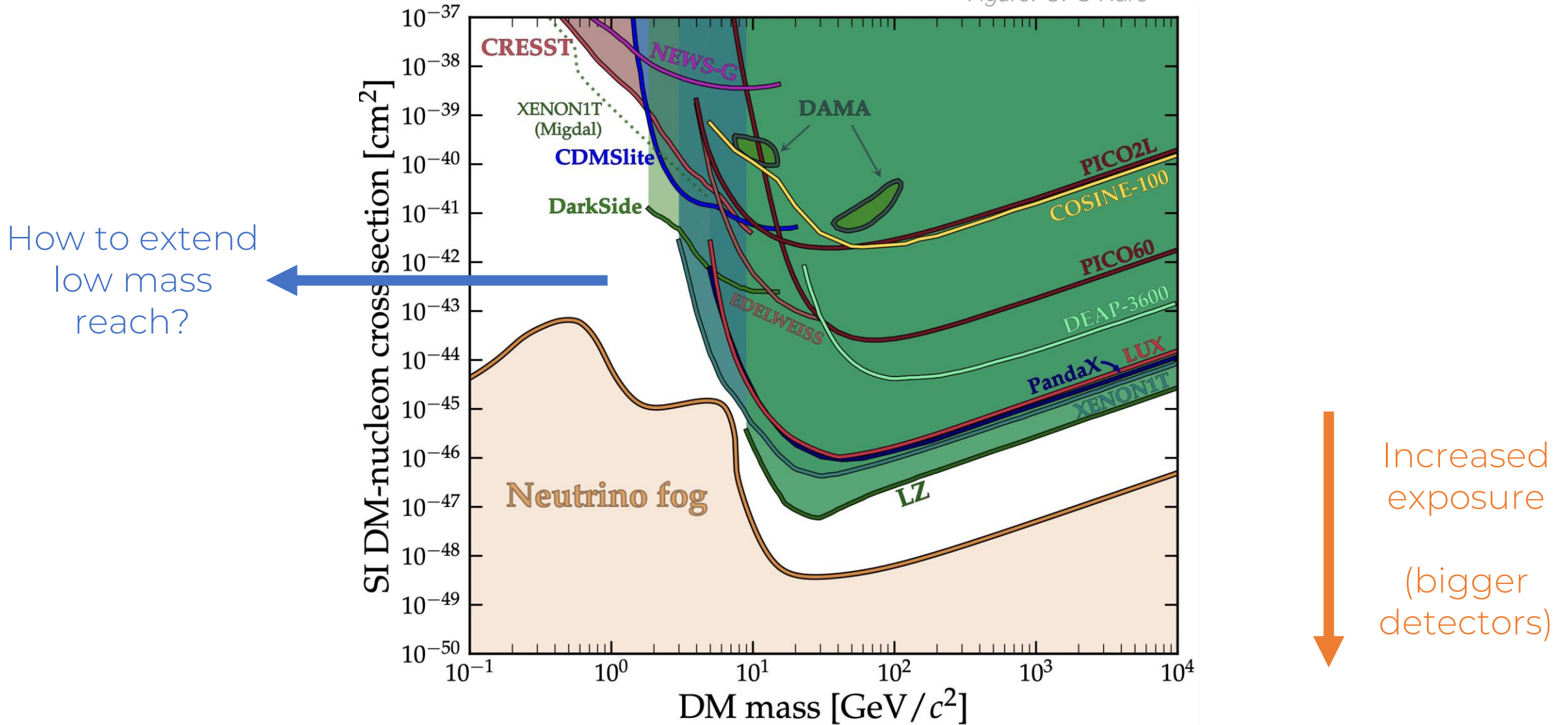


LUX-ZEPPLIN (LZ)

tonne-scale liquid Ar/Xe experiments

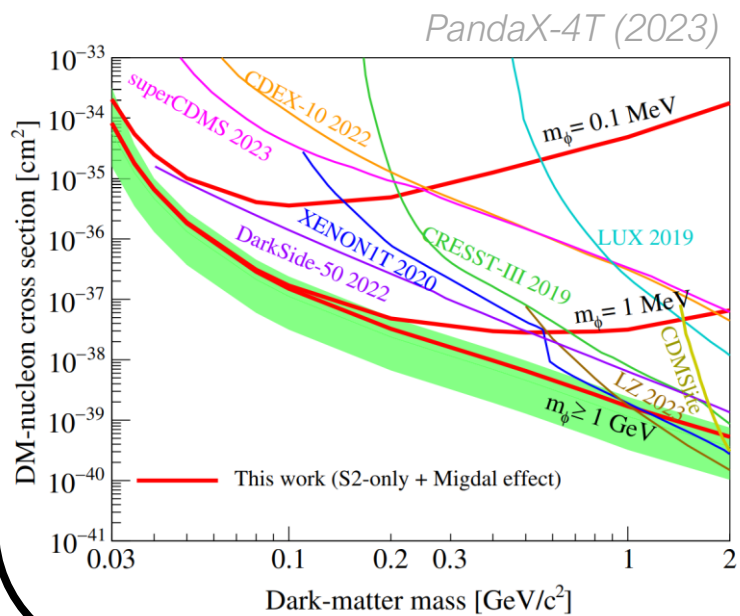
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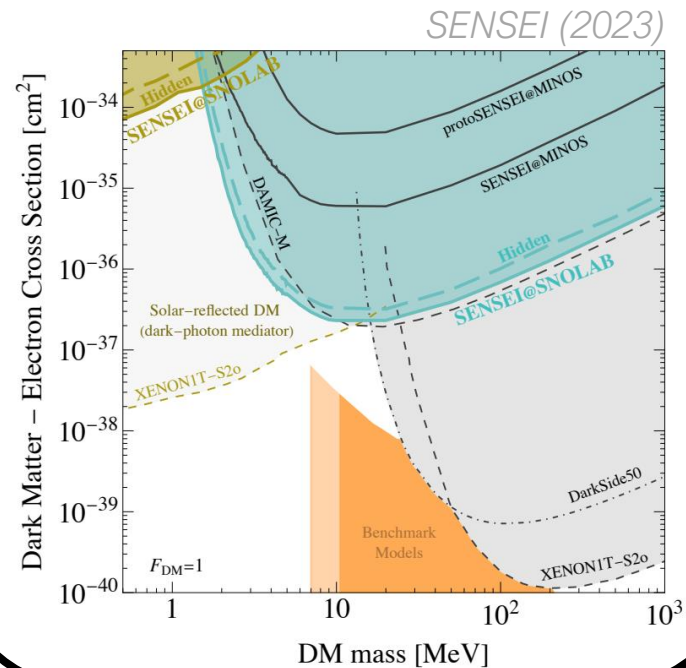


Sub-GeV direct detection

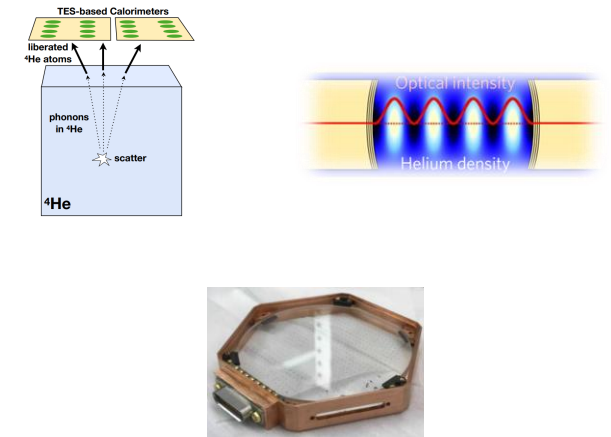
Migdal effect



Electron scattering



Low-threshold detectors



Lots of ideas + R&D

+ DM absorption, boosted DM, ...

Dark matter detection with superfluid ^4He

Lanou, Maris & Seidel '87

Guo & McKinsey '13

Ito & Seidel '13

Hertel+ '18

Upcoming experiments using superfluid helium-4 target: *HeRALD*, *DELIGHT*

Primary signal: *quantum evaporation*

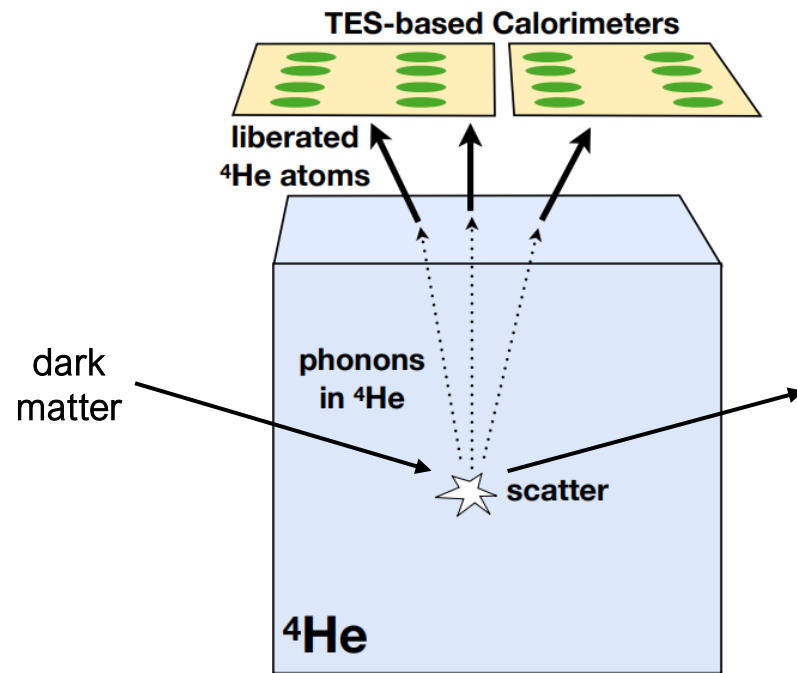


Figure: Herald Collaboration

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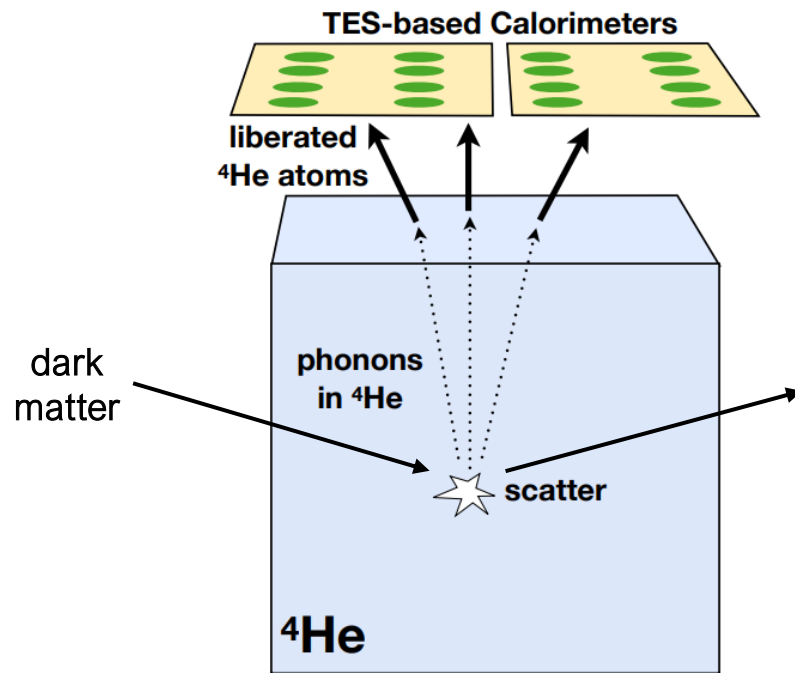


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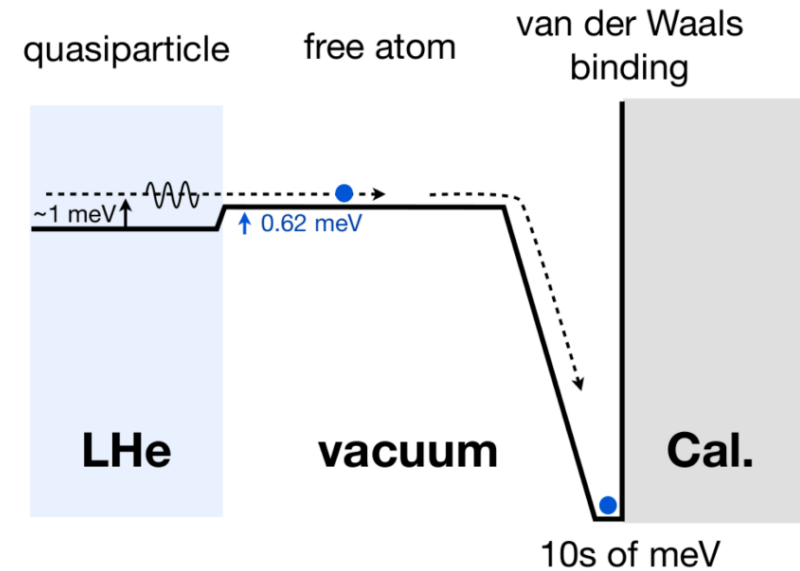


Figure: D. McKinsey

Adsorption onto surface amplifies signal

Dark matter detection with superfluid ^4He

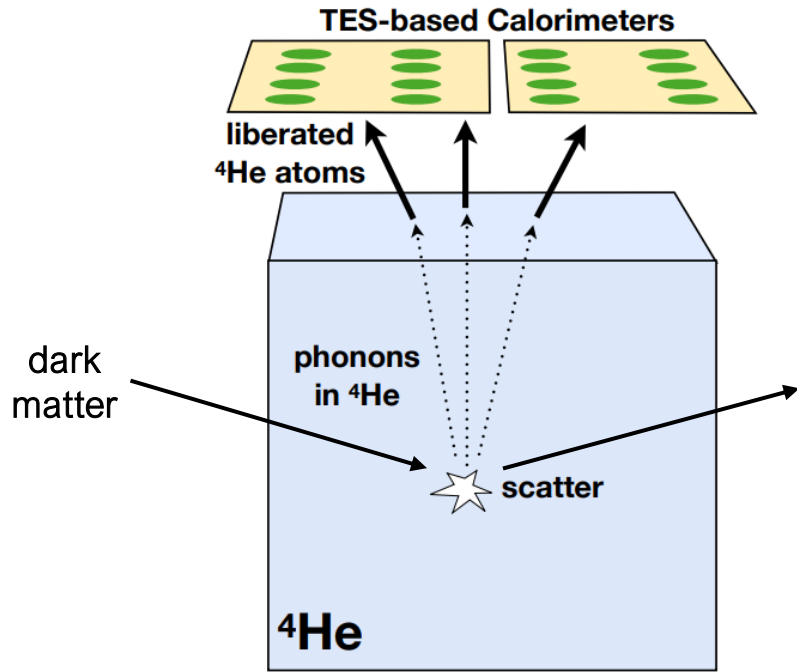
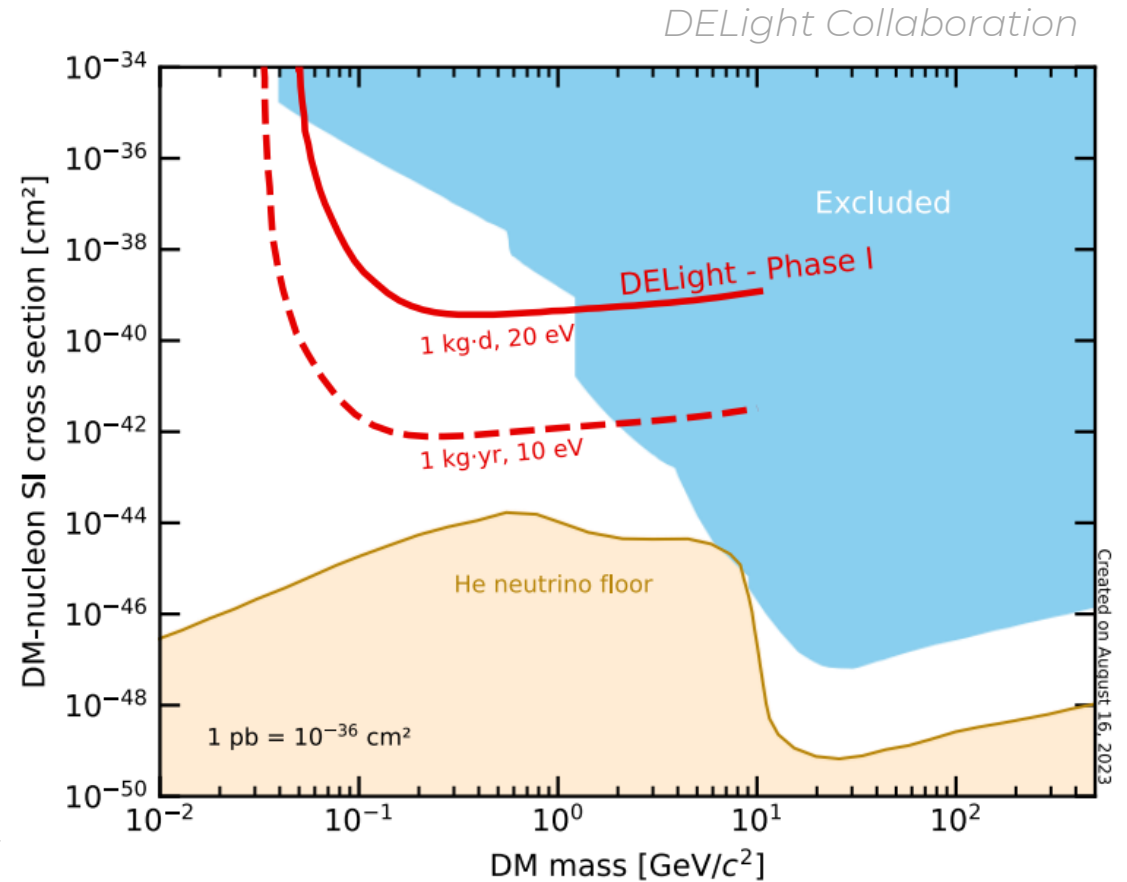


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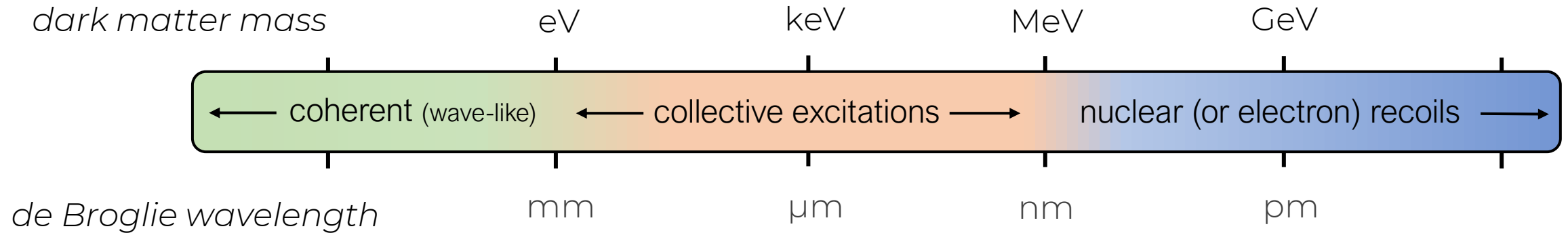
Initial sensitivity to DM masses of 10s-100s MeV

Ongoing R&D towards lower threshold calorimeters:

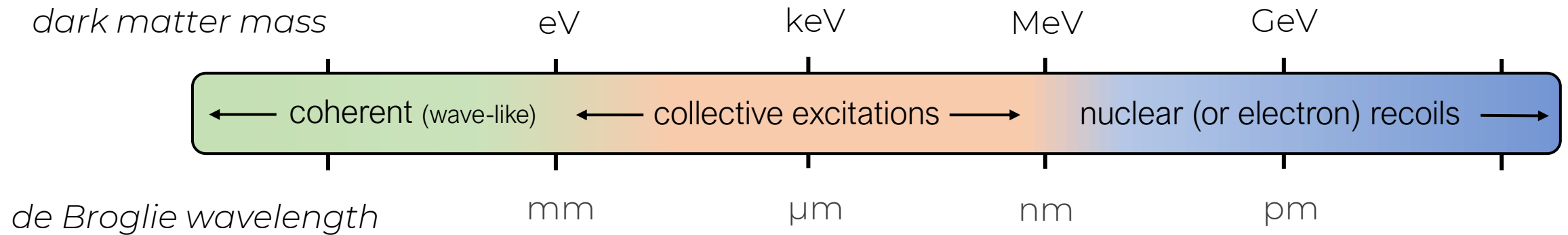
- HeRALD (transition edge sensors)
- DELIGHT (magnetic micro-calorimeter)



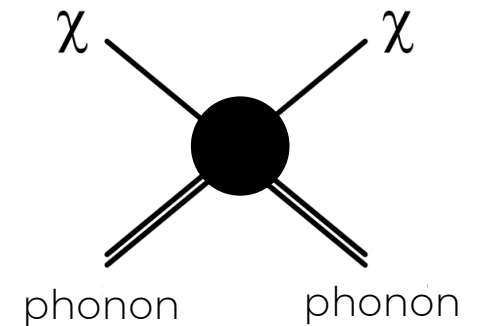
Sub-MeV direct detection: collective excitations



Sub-MeV direct detection: collective excitations



Sub-MeV mass DM interacts directly with *collective excitations*
(e.g. phonons)



Superfluid ^4He collective modes (phonons/rotons)

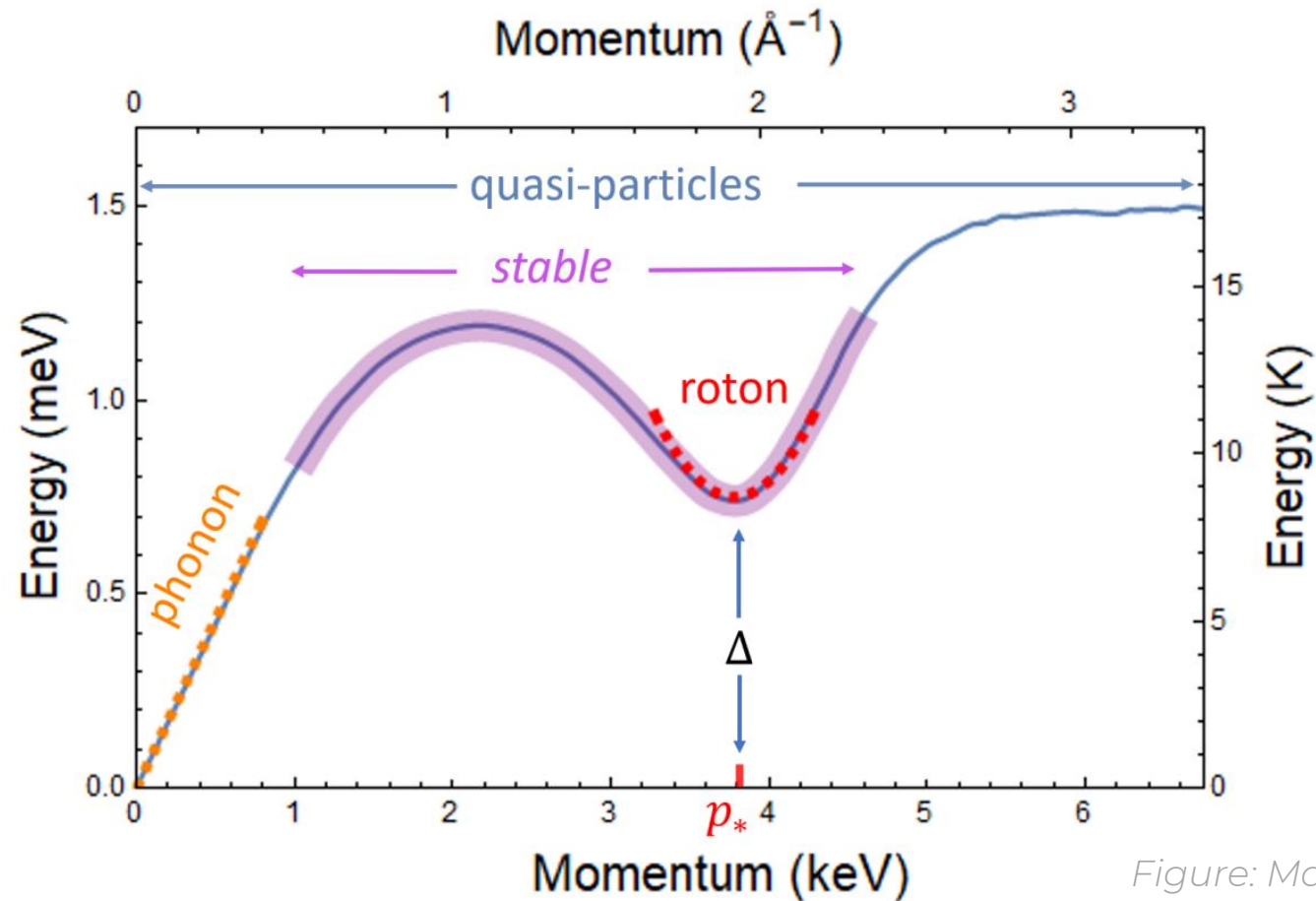


Figure: Matchev et. al '21

Long-lived/stable collective excitations

Superfluid phonon EFT

Son '02
Nicolis '11

Low-energy phonons in superfluid described by effective field theory

- Nambu-Goldstone bosons of spontaneously broken $U(1)$ particle number

$$\Phi(x) \rightarrow \Phi(x) + \alpha$$

$$\langle \Phi(x) \rangle = \mu t$$

$\mu =$ chemical
potential

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$$\Phi(x) \rightarrow \Phi(x) + \alpha \qquad \langle \Phi(x) \rangle = \mu t \qquad \mu = \text{chemical potential}$$

- VEV breaks internal $U(1)$, Lorentz boosts & time translations
- Preserves linear combination $H - \mu N$

Superfluid phonon EFT

*Son '02
Nicolis '11*

Most general Lagrangian consistent with shift symmetry:

$$\mathcal{L} = P(X)$$

$$X = \sqrt{\partial^\mu \Phi \partial_\mu \Phi}$$

Superfluid phonon EFT

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Most general Lagrangian consistent with shift symmetry:

$$\mathcal{L} = P(X)$$

$$X = \sqrt{\partial^\mu \Phi \partial_\mu \Phi} \xrightarrow{\Phi = \mu t} \mu$$

“local chemical potential”

$P(X)$ is identified as the pressure of the superfluid

$$T^{\mu\nu} \Big|_{\Phi = \mu t} = \mu n \delta_0^\mu \delta_0^\nu - \eta^{\mu\nu} P(\mu)$$

Superfluid phonon EFT

Son '02
Nicolis '11

Most general Lagrangian consistent with shift symmetry:

$$\mathcal{L} = P(X) \quad X = \sqrt{\partial^\mu \Phi \partial_\mu \Phi}$$

Nambu-Goldstone phonon: $\Phi(x, t) = \mu t + \sqrt{\frac{\mu c_s^2}{\bar{n}}} \phi(x, t)$

$$\mathcal{L} = \frac{1}{2} \dot{\phi}^2 - \frac{c_s^2}{2} (\nabla \phi)^2 + \lambda_3 \dot{\phi} (\nabla \phi)^2 + \mathcal{O}(\phi^4)$$

Sound speed, couplings can be expressed in terms of derivatives of $P(\mu)$

Dark matter – phonon interactions

Acanfora, Esposito, Pelosa '19

Consider spin-independent DM-nucleon interaction

\Rightarrow DM couples to He number density $n = \frac{P'(X)}{X} \partial^0 \Phi$

$$\mathcal{L}_{\text{int}} = g_\chi n \chi^2$$

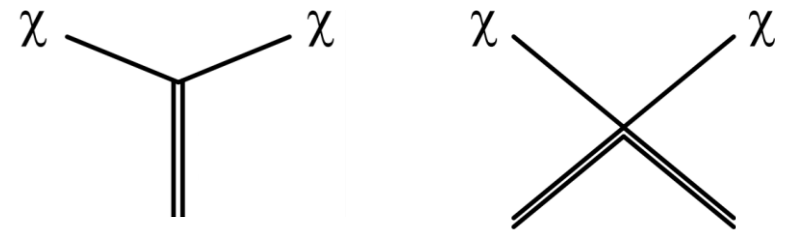
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$$\begin{aligned} \mathcal{L}_{\text{int}} &= g_\chi n \chi^2 \\ &= g_\chi \left(\bar{n} + \sqrt{\frac{\bar{n}}{\mu c_s^2}} \dot{\phi} + \lambda_3 (\nabla \phi)^2 + \dots \right) \chi^2 \end{aligned}$$



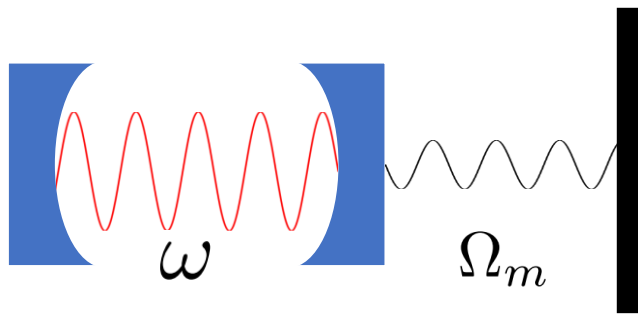
Detecting phonons - cavity optomechanics

Basic idea: optomechanical systems can be single phonon detectors

Detecting phonons - cavity optomechanics

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Toy model:



$$H = \Omega_m b_m^\dagger b_m + \left(\omega_0 + \frac{\partial \omega}{\partial x} x \right) a^\dagger a$$

phonon

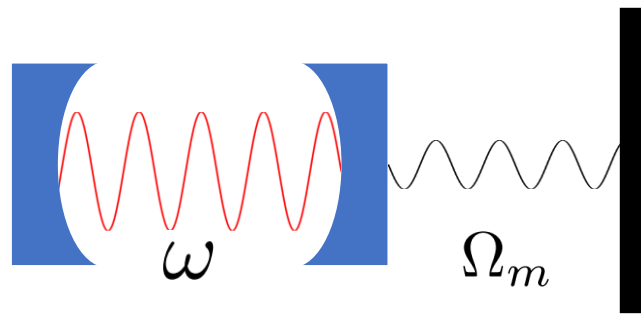
photon

Optical resonance frequency depends on cavity length

Detecting phonons - cavity optomechanics

Basic idea: optomechanical systems can be single phonon detectors

Toy model:



$$\begin{aligned} H &= \Omega_m b_m^\dagger b_m + \left(\omega_0 + \frac{\partial \omega}{\partial x} x \right) a^\dagger a \\ &= \Omega_m b_m^\dagger b_m + \left(\omega_0 + g_0 (b_m + b_m^\dagger) \right) a^\dagger a \end{aligned}$$

phonon

photon

optomechanical coupling

Superfluid cavity optomechanics

superfluid ^4He filled optical cavity

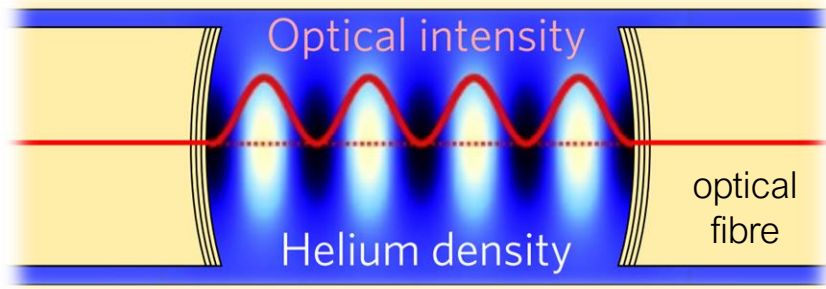


Figure: Kashkanova+ '16

Mechanical mode: phonons in superfluid

Optomechanical interaction due to
change in refractive index

Superfluid cavity optomechanics

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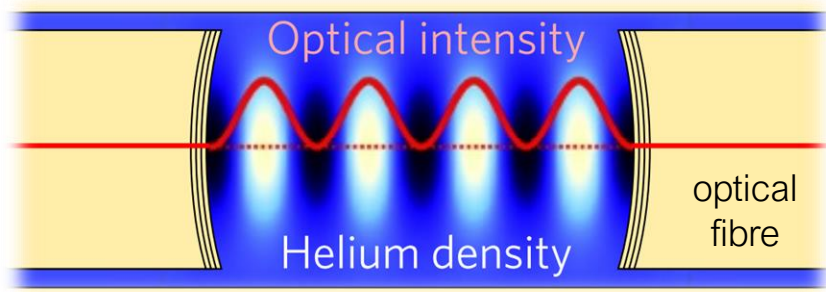


Figure: Kashkanova+ '16

$$H_{\text{OM}} = -g_0(a_{\gamma_1}^\dagger a_{\gamma_2} b_m^\dagger + \text{h.c.})$$

optomechanical coupling photons phonon

Energy-momentum conservation:

$$\Omega_m = \omega_{\gamma_2} - \omega_{\gamma_1} \ll \omega_{\gamma_{1,2}}$$

$$\lambda_m \approx \lambda_\gamma / 2$$

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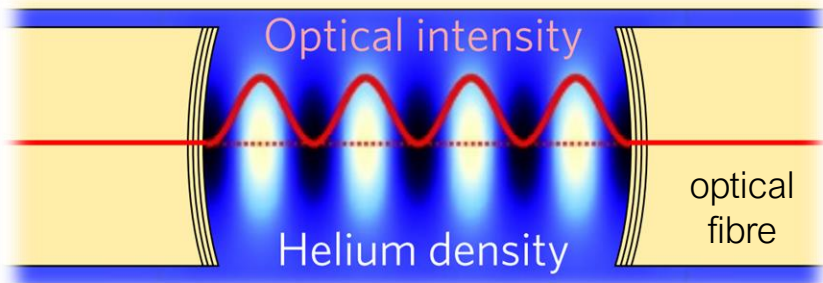


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Optomechanical interaction converts
 $\sim\mu\text{eV}$ phonons into detectable $\sim\text{eV}$ photons

$$H_{\text{OM}} = -g_0(a_{\gamma_1}^\dagger a_{\gamma_2} b_m^\dagger + \text{h.c.})$$
$$\rightarrow -g_0 \sqrt{N_1} (a_{\gamma_2} b_m^\dagger + \text{h.c.})$$

pump laser enhances small g_0

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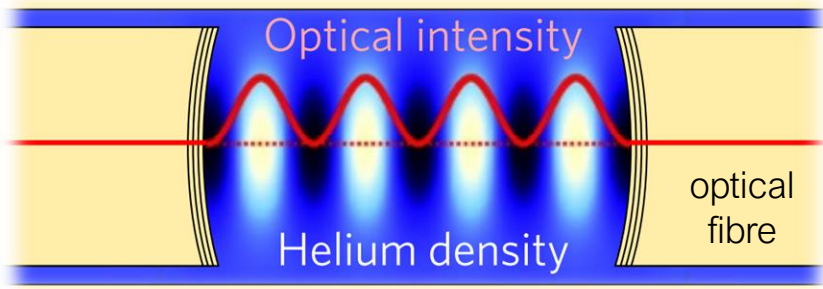


Figure: Kashkanova+ '16

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Optomechanical systems have demonstrated μeV phonon counting

(e.g. Patil et. al. '22)

$$H_{\text{OM}} = -g_0(a_{\gamma_1}^\dagger a_{\gamma_2} b_m^\dagger + \text{h.c.})$$
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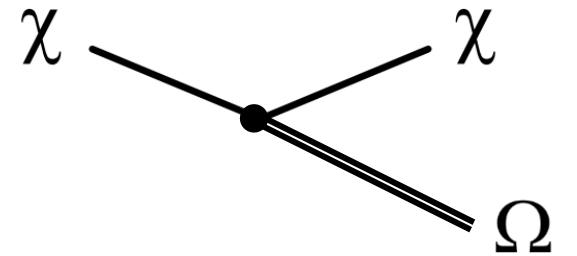
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Narrow-band detection

Superfluid optomechanical systems as dark matter detectors:

- ✓ exceptional low-energy sensitivity ($\sim \mu\text{eV}$)
 - ✗ narrow-band detector (single phonon energy)
- ➔ Very low dark matter scattering rate due to restricted phase space



Narrow-band detection & phonon lasing

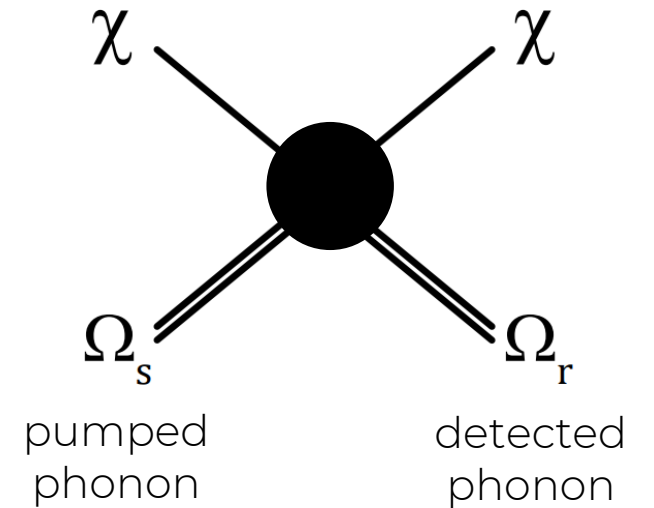
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Solution: *Phonon lasing*

- *Stimulated* scattering rate (proportional to phonon occupation number)
- Achieved via optomechanical interaction



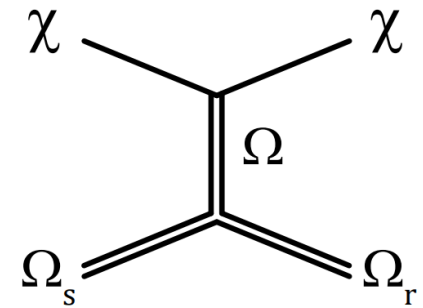
Scattering rate

Initial state phonon number density

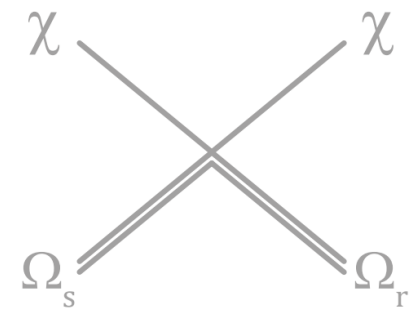
$$R \propto \frac{\rho_\chi \sigma_\chi n}{m_\chi^3} n_s Q^2 \frac{\Omega_r \Omega_s}{m_{\text{He}}^2 c_s^4} \frac{(1 + \gamma_G)^2}{1}$$

Acoustic quality factor: $Q = \Omega_m / \Gamma_m$

3-phonon coupling



resonantly enhanced



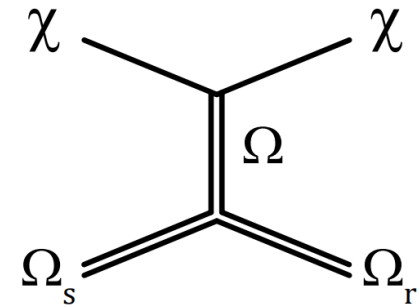
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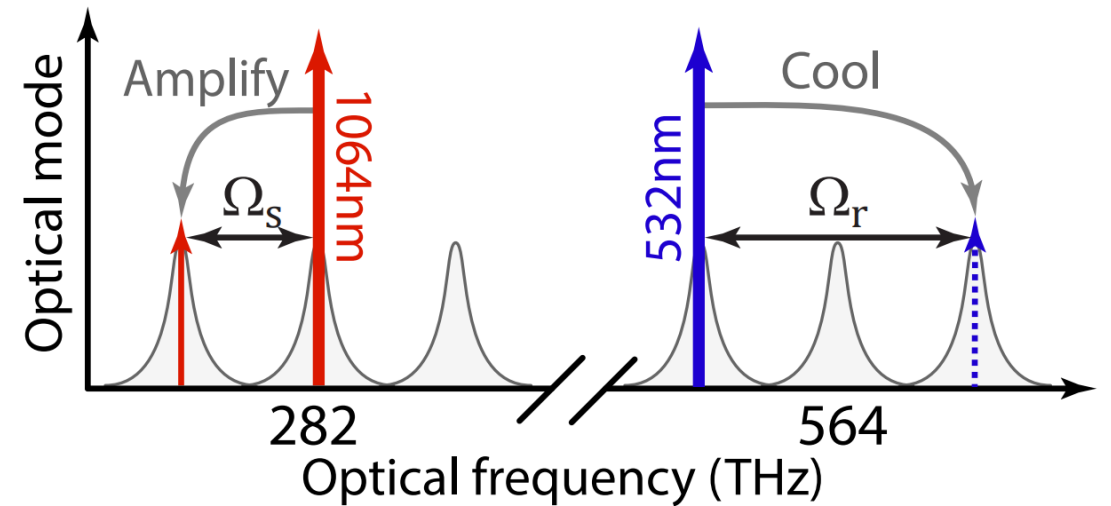
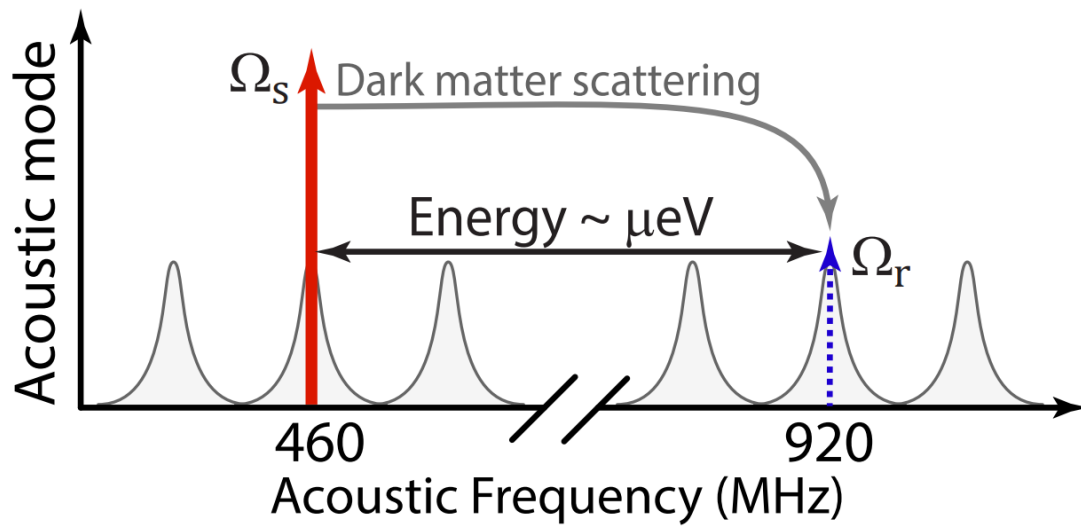
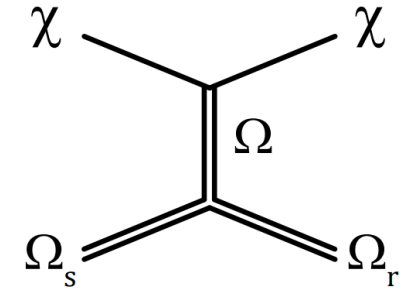


Scattering is between specific initial *and final* phonon states:

- I. Scattering is at fixed momentum transfer: $q = (\Omega_r - \Omega_m) / c_s \sim \text{eV}$
- II. Event rate *doesn't* scale with detector volume (resolved mode regime)

Optomechanical detection

Dark matter detector requires optomechanical control of *two* acoustic modes

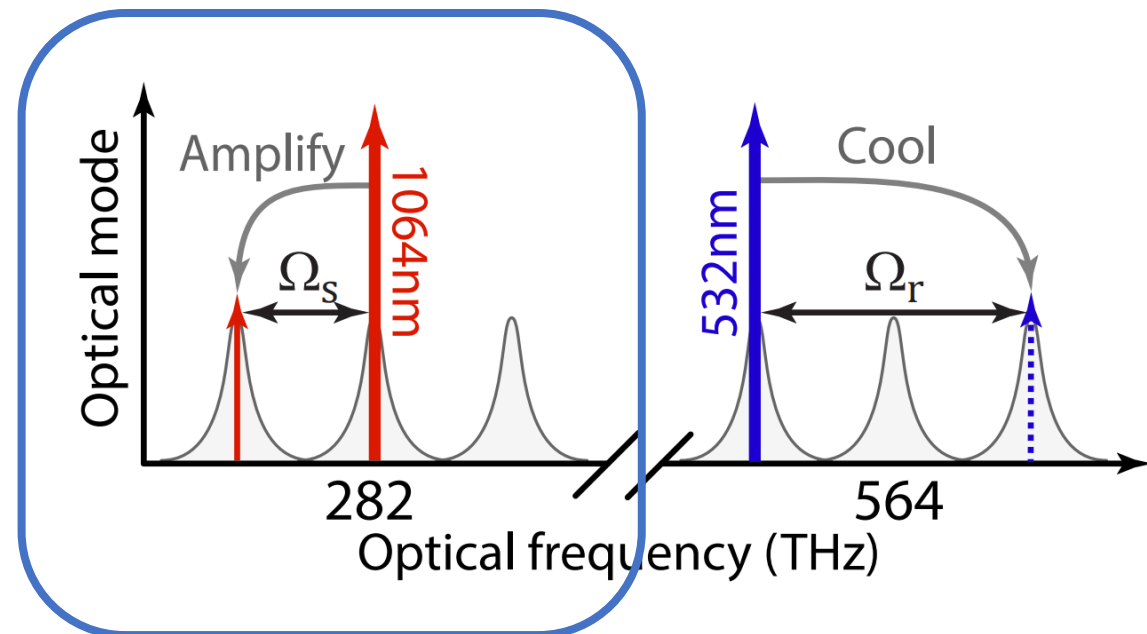
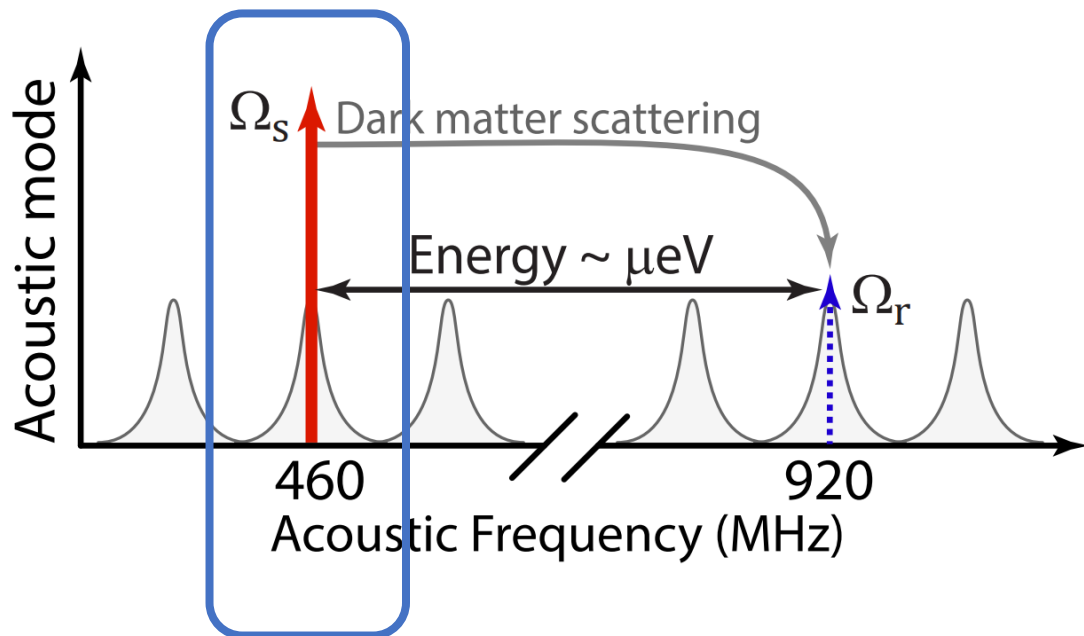
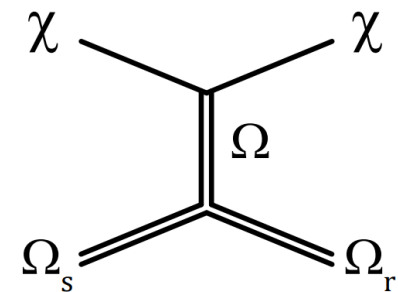


Optomechanical detection

1

Phonon lasing

Lower-energy phonon mode Ω_s populated via optomechanical interaction

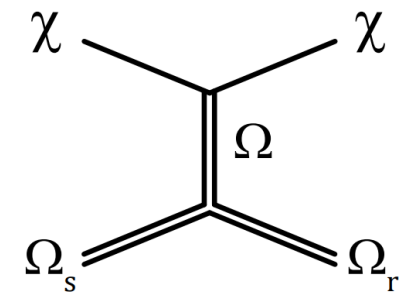
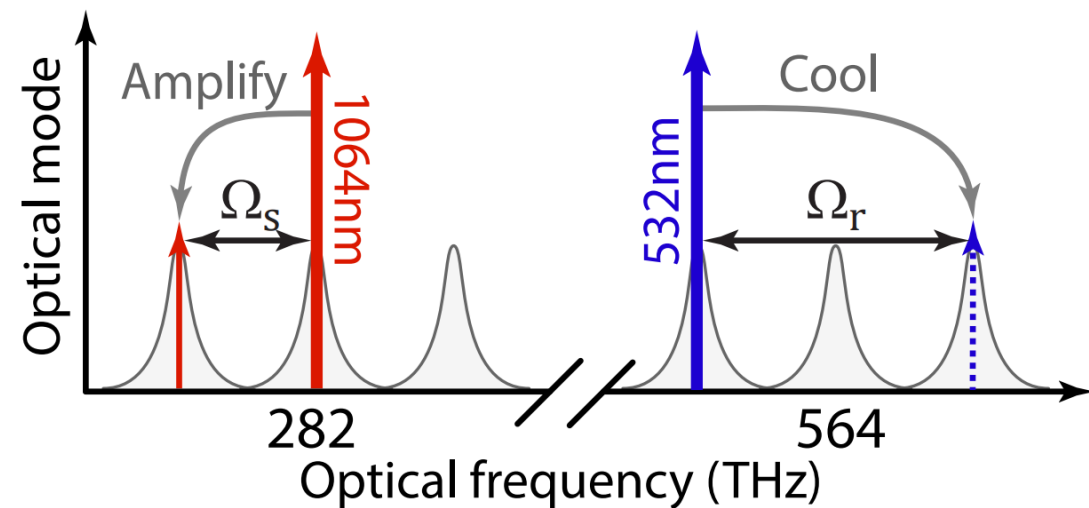
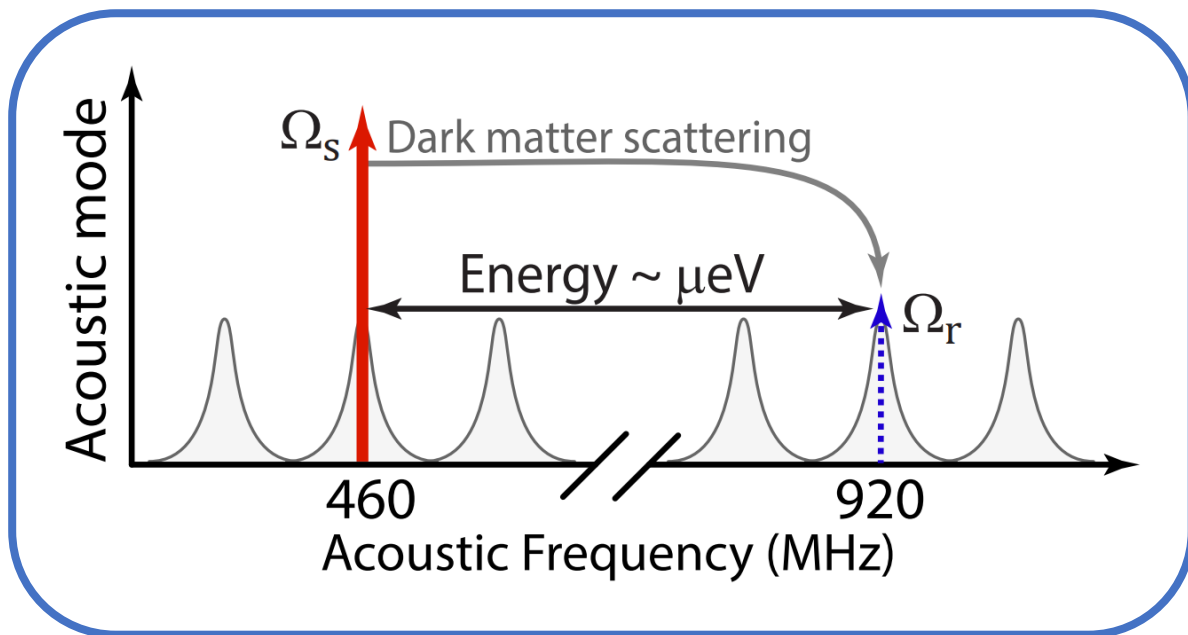


Optomechanical detection

2

Scattering

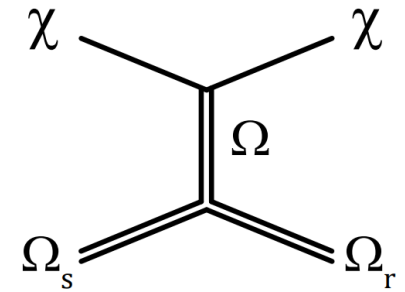
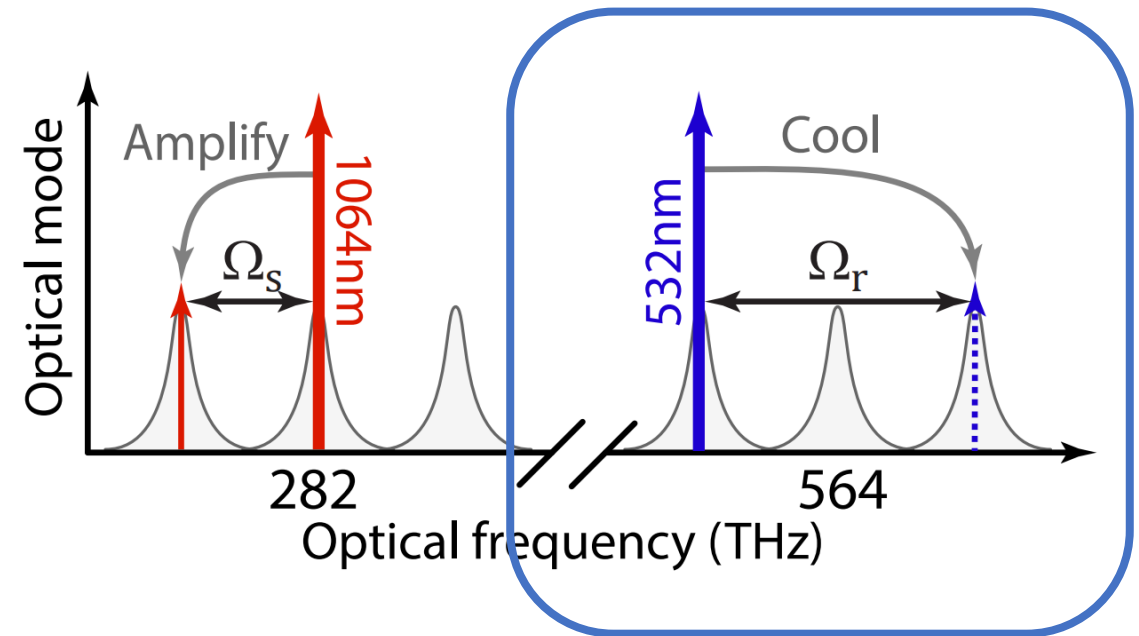
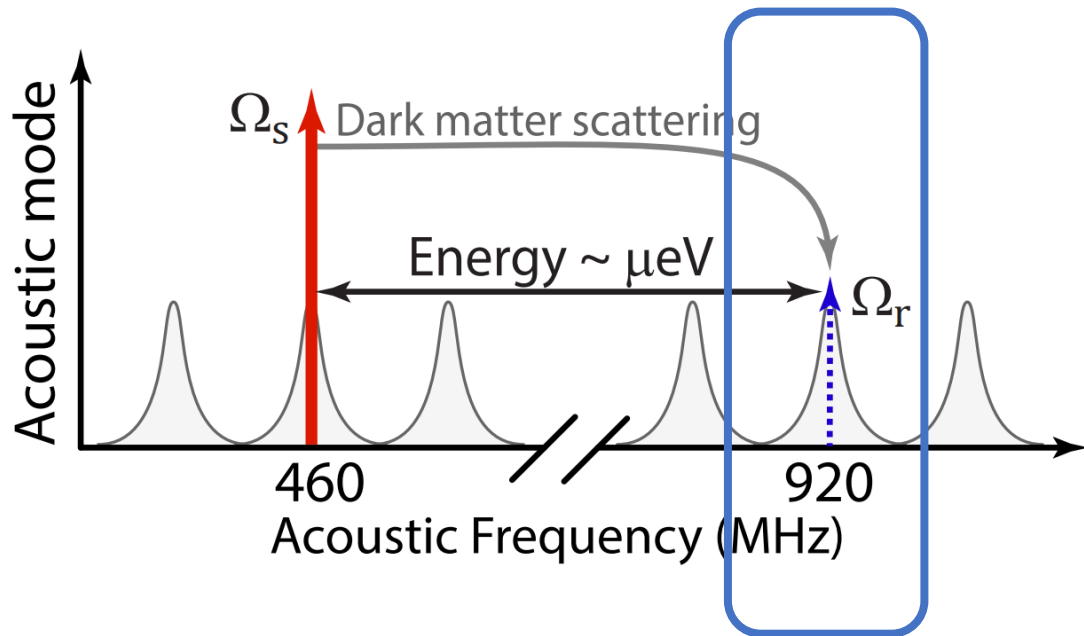
Stimulated dark matter scattering excites higher energy phonon mode



Optomechanical detection

3 Conversion & amplification

Optomechanical conversion of Ω_r phonon to higher energy photon

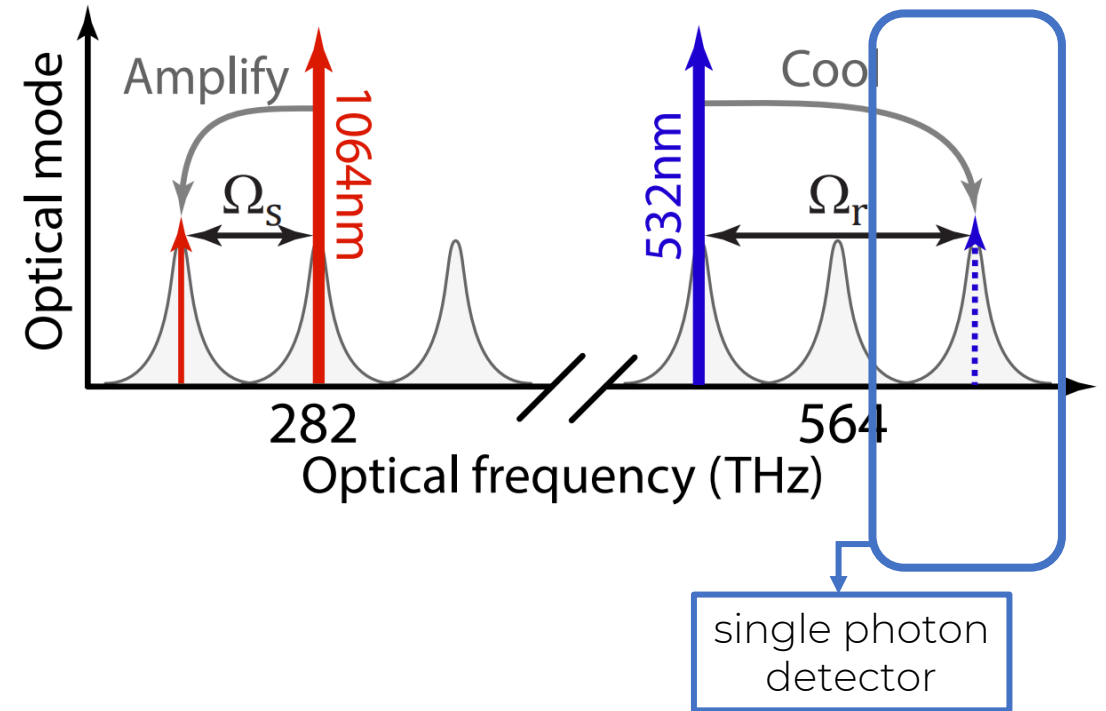
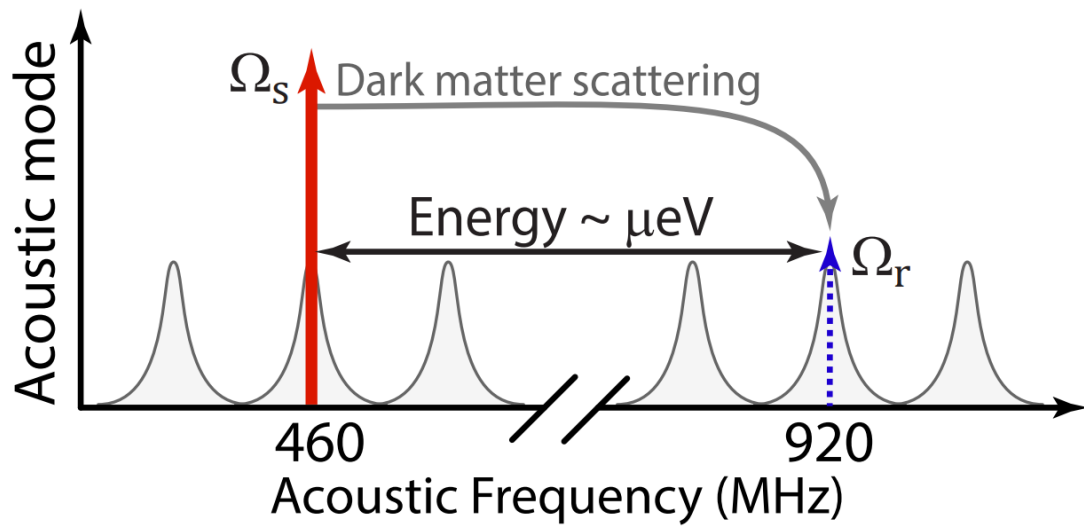
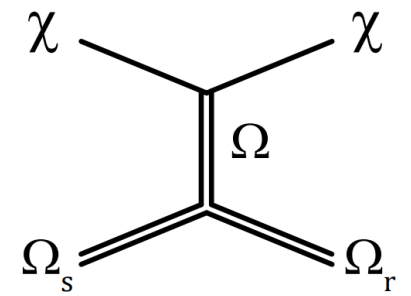


Optomechanical detection

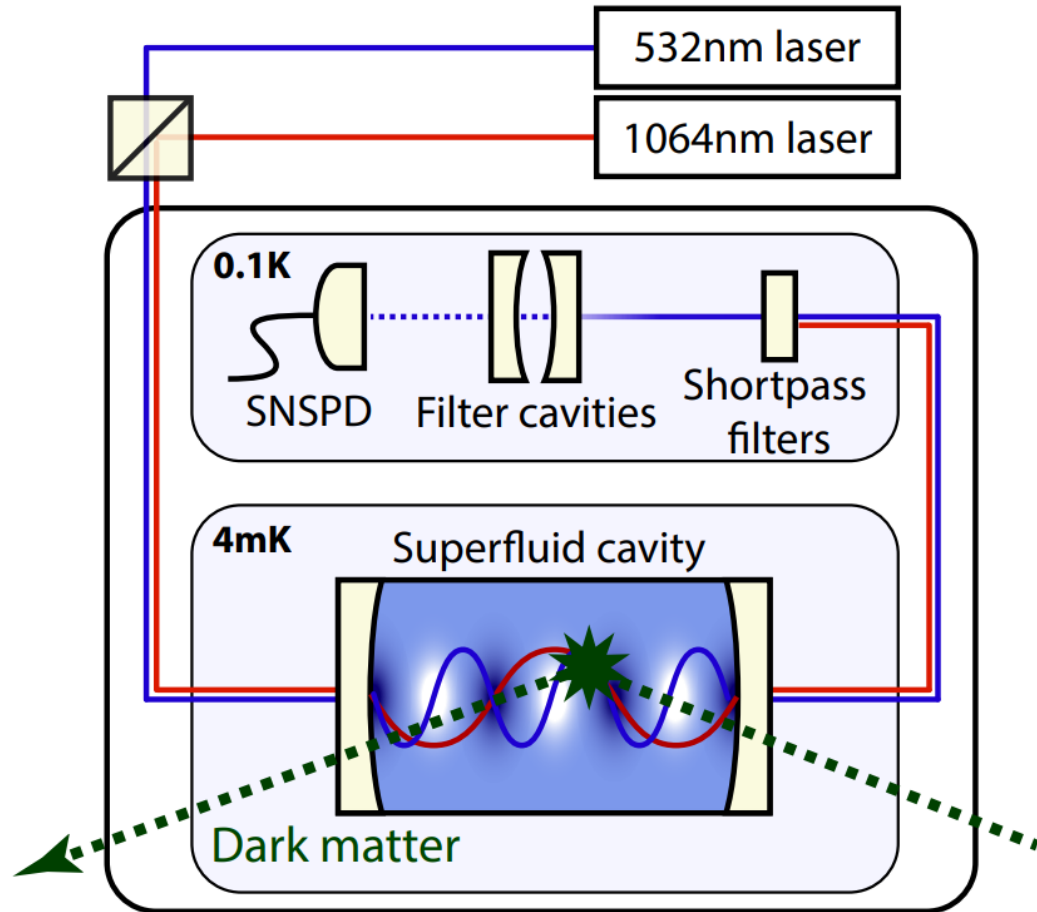
4

Detection

Photon detected by single photon detector (SNSPD)

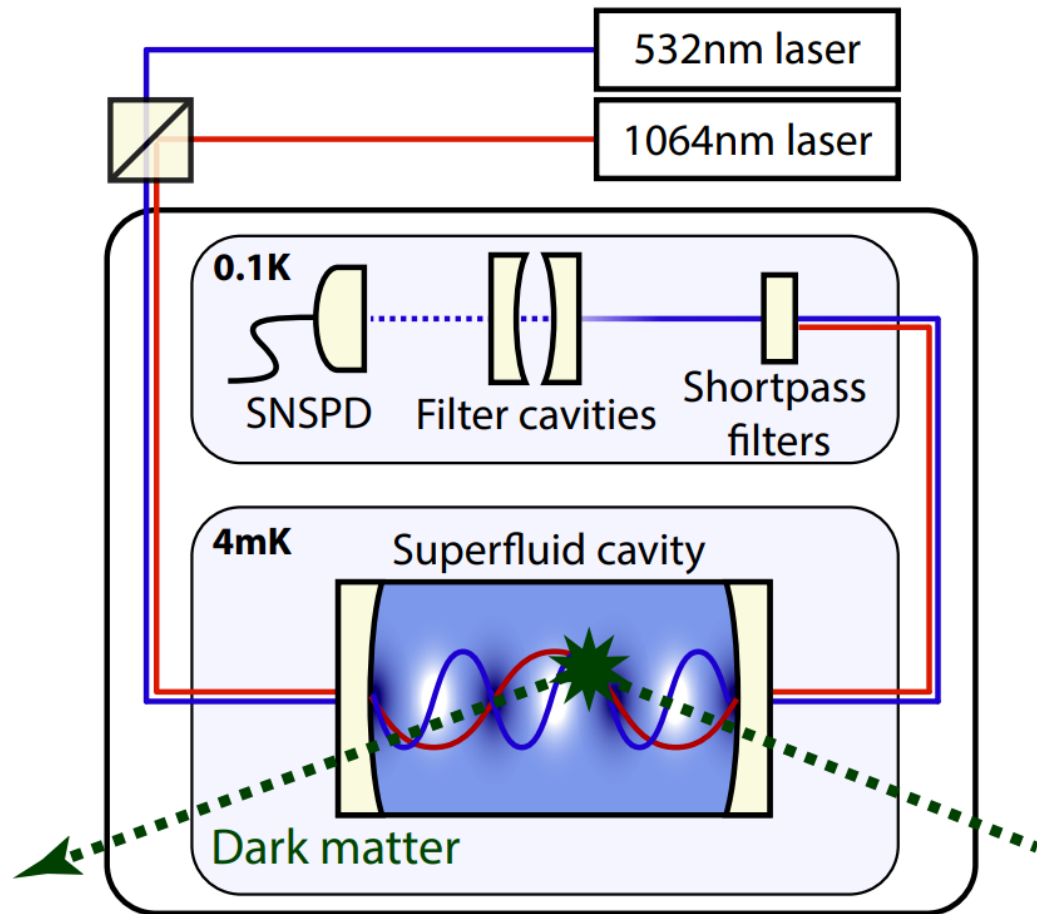


ODIN: Optomechanical Dark-matter INstrument



cavity dimensions $\sim 30\text{cm} \times 0.7\text{mm}$

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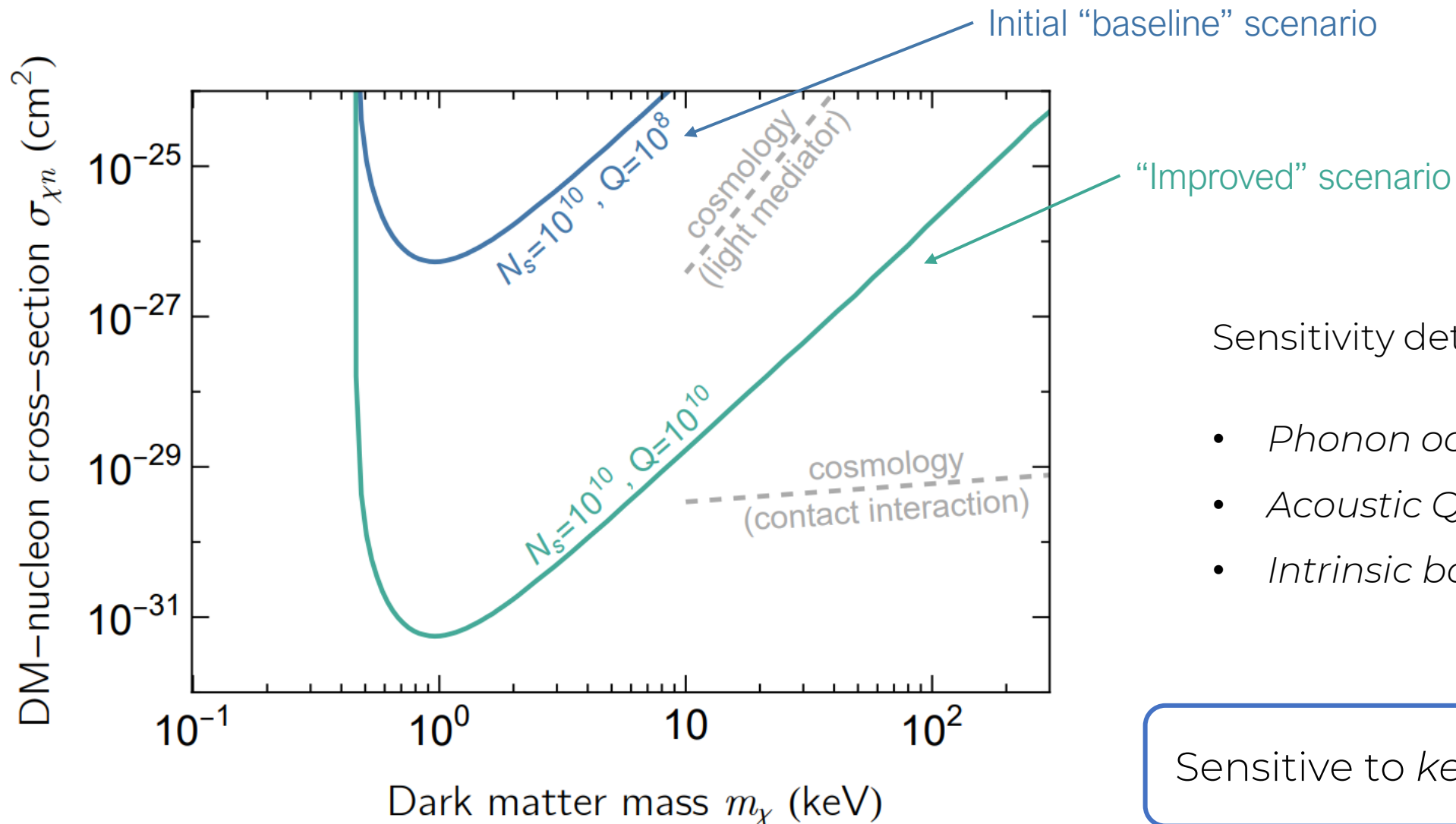
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Main detector backgrounds:

- *Thermal phonons*
(10^{-5} Hz at $T = 4\text{mK}$ and $Q = 10^{10}$)
- *SNSPD dark counts*
($\sim 6 \times 10^{-6}$ Hz)
- *Incomplete filtering of pump lasers*
(especially 532nm, suppressed with filter cavities)

Expected background rate ~ 1 event/day

ODIN: Projected Sensitivity



Sensitivity determined by:

- *Phonon occupation*
- *Acoustic Q-factor (phonon width)*
- *Intrinsic background rate*

Sensitive to keV-scale dark matter

Summary

- Superfluid He is a promising target for light dark matter searches
- Optomechanical detection uses conversion of $\sim\mu\text{eV}$ phonons to $\sim\text{eV}$ photons
- ODIN will be sensitive to $\sim\text{keV}$ mass dark matter
- Currently exploring improvements to sensitivity – signal modulation?
- Potential application to high frequency gravitational waves
- Proposals to also use optomechanical detectors for ultralight DM [Manley+ '19, Manley+ '22, Brady+ '22, Murgui+'22].

Backup

Optical asymmetry

Optical mode spacing (FSR) can be engineered to select amplification/cooling of acoustic modes:

