



SIDIS longitudinal-spin-dependent asymmetries at COMPASS

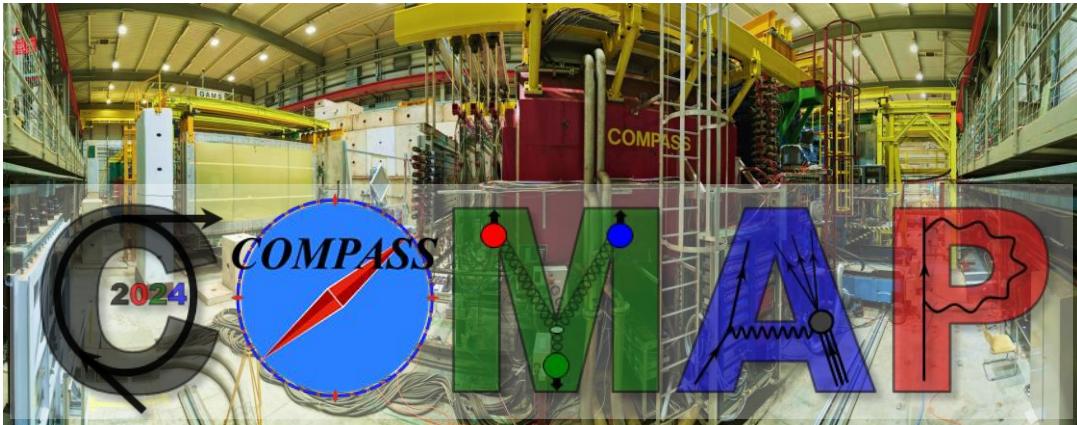


Bakur Parsamyan

AANL(Yerevan), CERN
and
INFN (Torino)



6th COMPASS Analysis Phase
mini-workshop (COMAP-VI)
January 24th, 2024, CERN



B. Parsamyan

COMPASS collaboration



Common Muon and Proton Apparatus for Structure and Spectroscopy



25 institutions from 13 countries
– nearly 200 physicists (in 2022)

- CERN SPS north area
- Fixed target experiment
- Approved in 1997 (**25 years**)
- Taking data since 2002 (**20 years**)

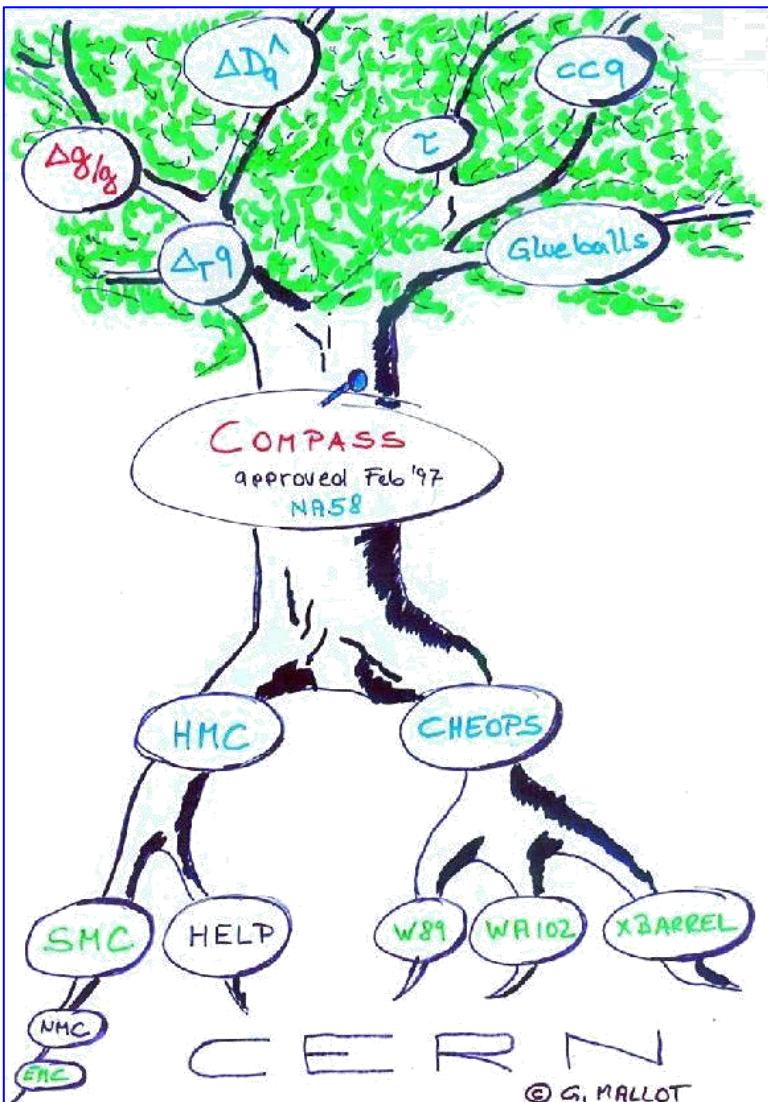
International Workshop on Hadron Structure and Spectroscopy
IWHSS-2022 workshop (**anniversary edition**)

CERN Globe, August 29-31, 2022



<https://indico.cern.ch/e/IWHSS-2022>

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COMPASS collaboration

Common Muon and Proton Apparatus for Structure and Spectroscopy



28 institutions from 14 countries

– nearly 210 physicists (in 2023: start of the Analysis Phase)

- CERN SPS north area
- Fixed target experiment
- Approved in 1997 (25 years)
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Wide physics program

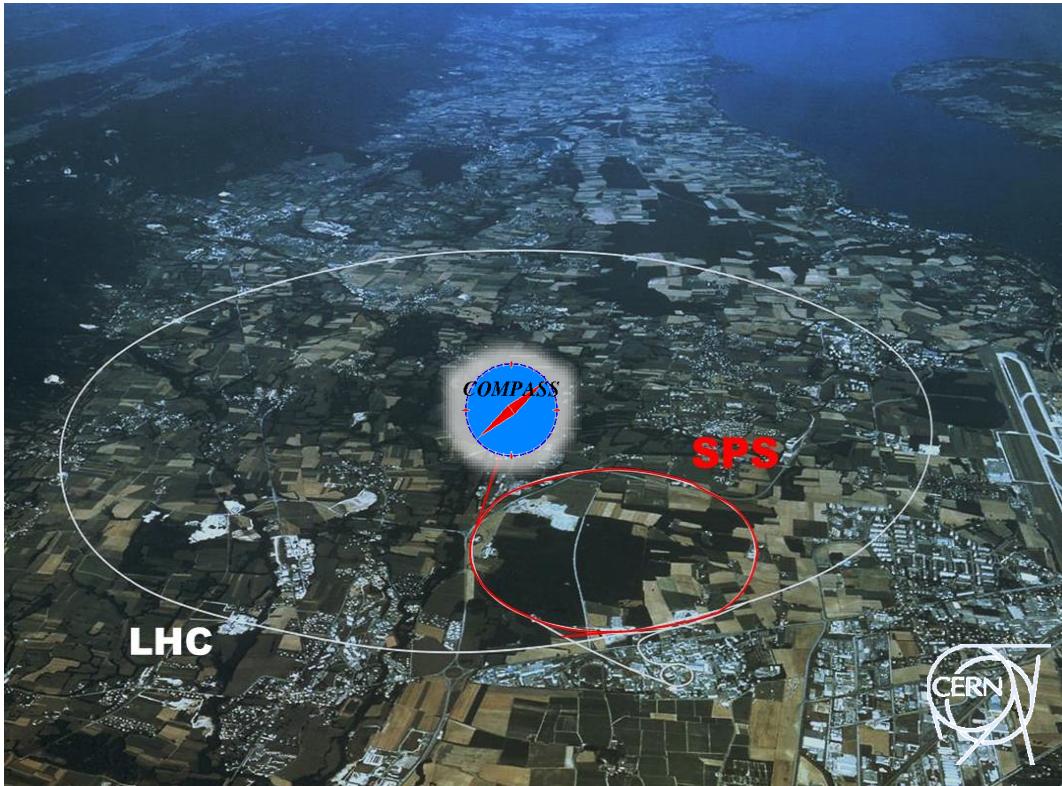
COMPASS-I

- Data taking 2002-2011
- Muon and hadron beams
- Nucleon spin structure
- Spectroscopy

COMPASS-II

- Data taking 2012-2022
- Primakoff
- DVCS (GPD+SIDIS)
- Polarized Drell-Yan
- Transverse deuteron SIDIS 2022

3 new groups joined the COMPASS collaboration in 2023
UCon (US), AANL (Armenia), NCU (Taiwan)



COMPASS web page: <http://wwwcompass.cern.ch>

COMPASS experimental setup: Phase I (muon program)

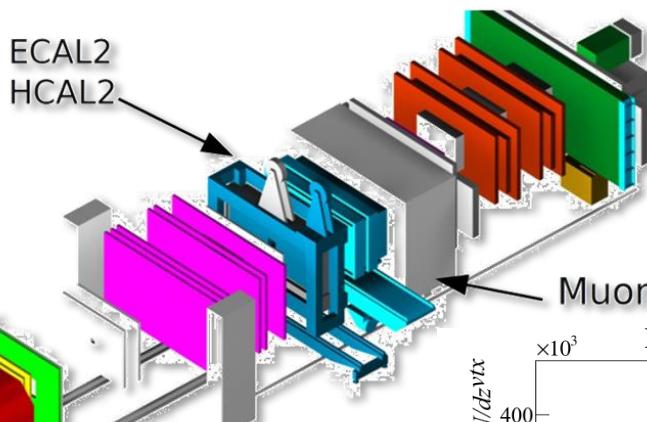
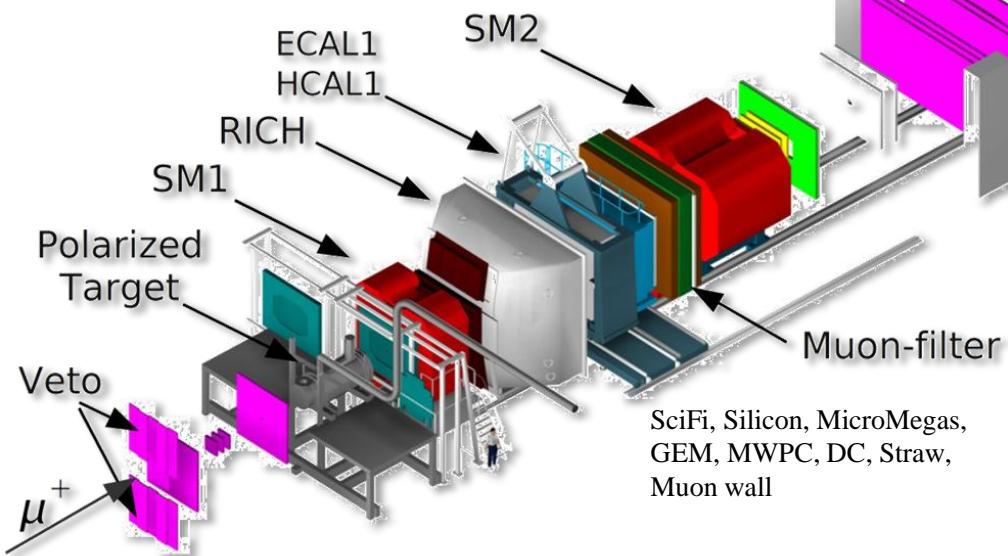


COmmon Muon Proton Apparatus for Structure and Spectroscopy

CERN SPS North Area.

Two stages spectrometer LAS+SAS

- Large Angle Spectrometer (SM1 magnet)
- Small Angle Spectrometer (SM2 magnet)



Longitudinally polarized (80%) μ^+ beam:

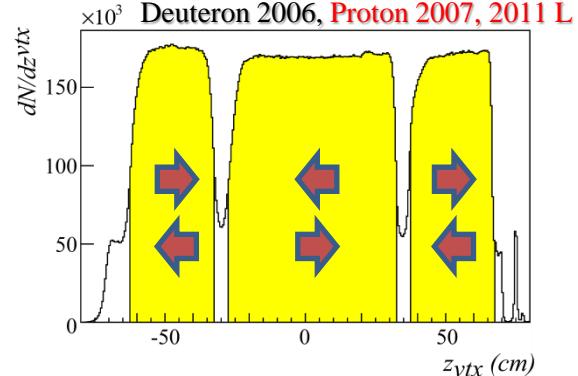
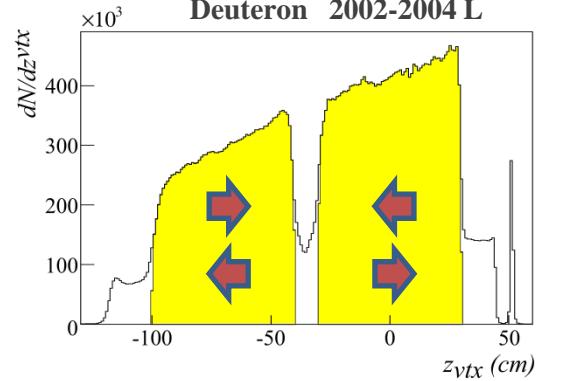
Energy: 160/200 GeV/c, Intensity: $2 \cdot 10^8 \mu^+$ /spill (4.8s).

Target: Solid state (${}^6\text{LiD}$ or NH_3)

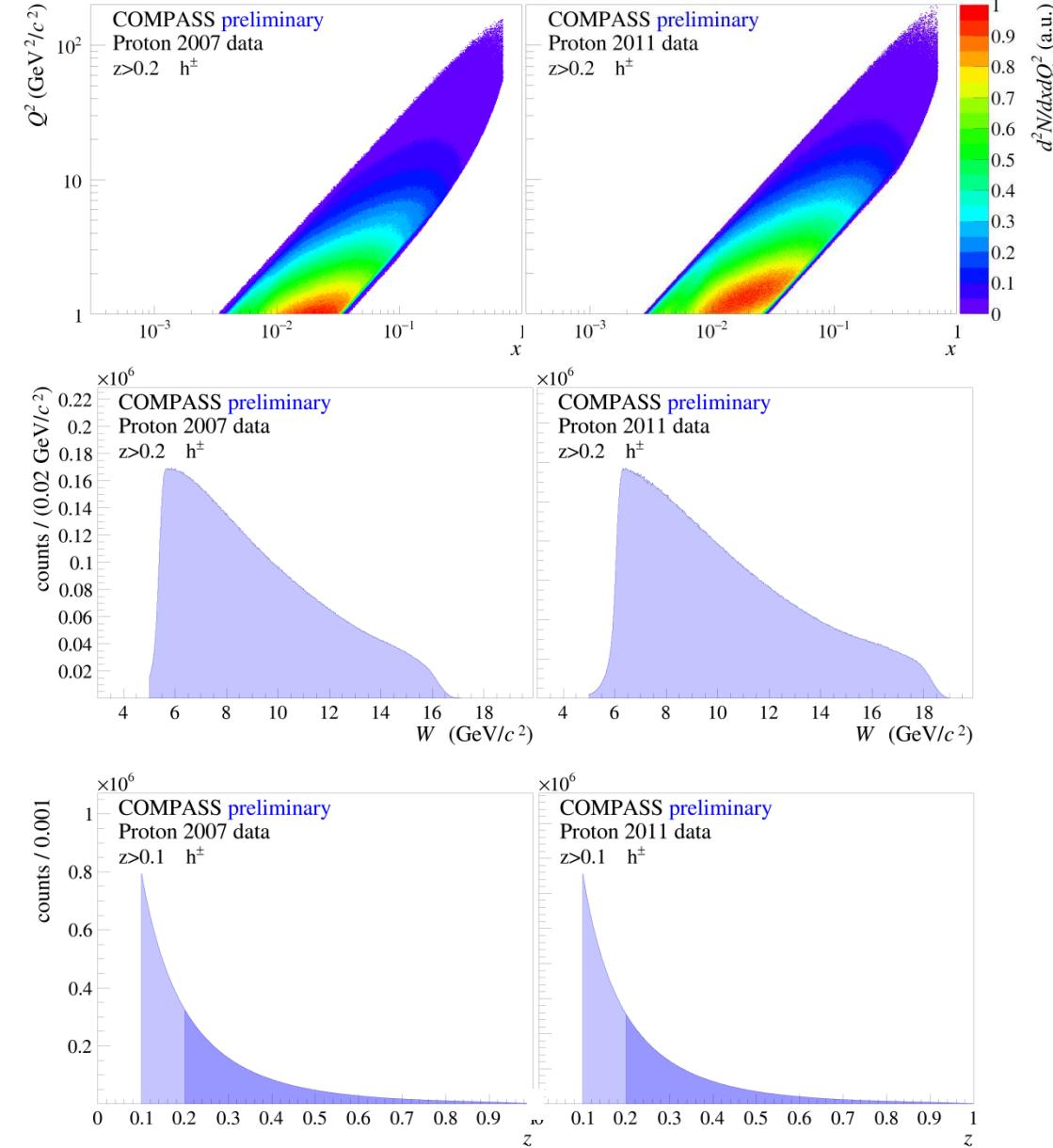
- ${}^6\text{LiD}$ 2-cell configuration. Polarization (L & T) $\sim 50\%$, f ~ 0.38
- NH_3 3-cell configuration. Polarization (L & T) $\sim 80\%$, f ~ 0.14

Data-taking years: 2002-2011

Data is collected simultaneously for the two target spin orientations
Polarization reversal after each $\sim 1\text{-}2$ days



Kinematics 2007(160 GeV/c), 2011 (200 GeV/c)



Two years of longitudinal data
with NH₃ target:
2007: 160 GeV μ^+ – beam
2011: 200 GeV μ^+ – beam

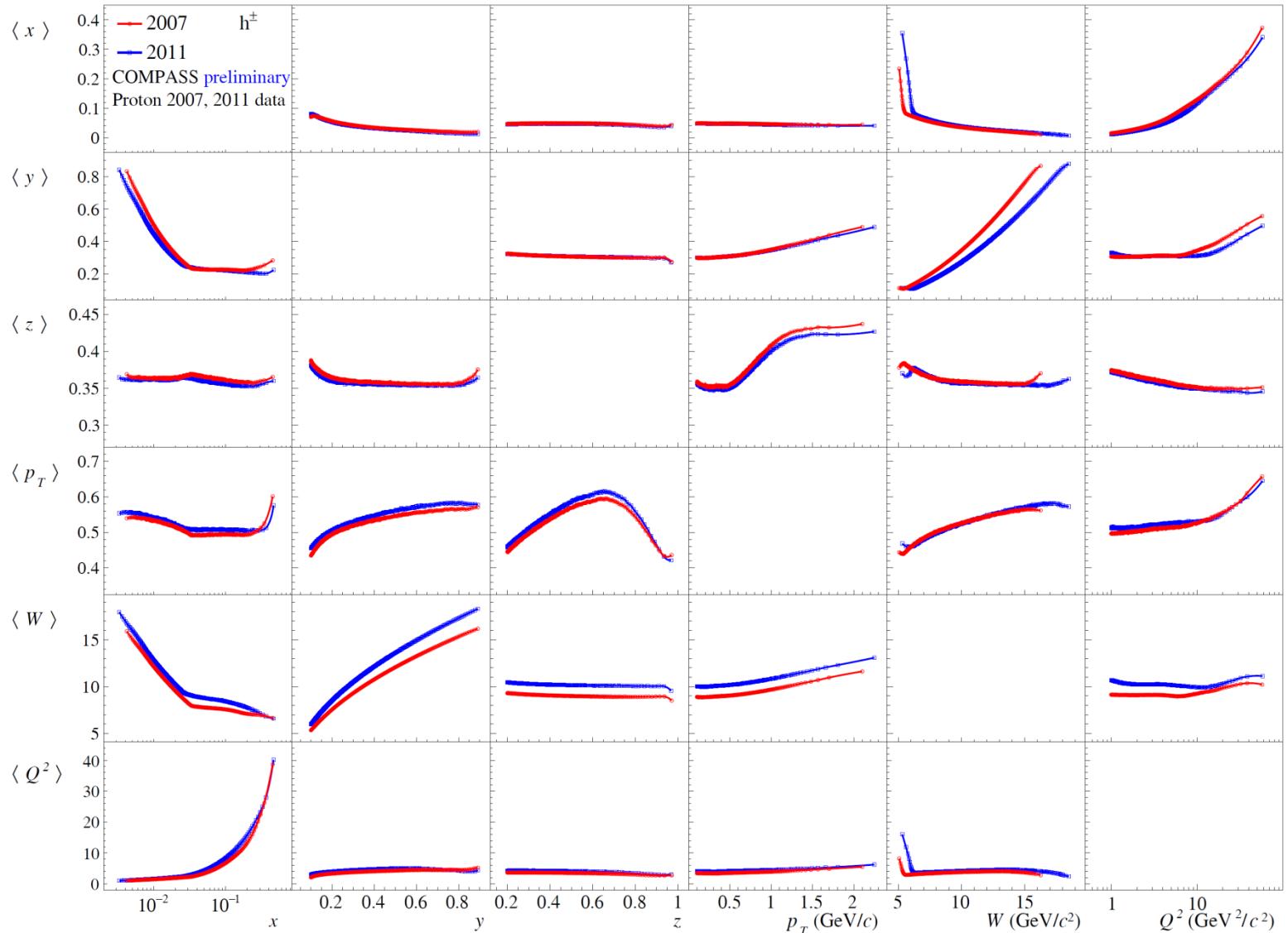
Kinematic cuts

DIS variables:
 $Q^2 > 1$ (GeV/c) 2
 $0.0025 < x < 0.7$
 $0.1 < y < 0.9$
 $W > 5$ GeV/c 2

Hadronic cuts:
 $z > 0.2, 0.1 < z < 0.2$
 $p_T > 0.1$ GeV/c

Comparable kinematic distributions

Kinematics 2007(160 GeV/c), 2011 (200 GeV/c)



Comparable kinematic distributions

Only results from merged 2007+2011 sample are shown

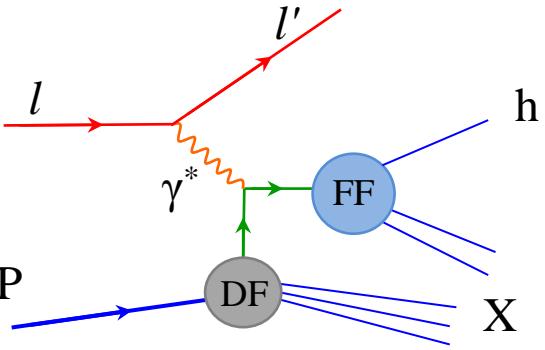
SIDIS x-section and TMDs at twist-2

$$\frac{d\sigma}{dxdydzdp_T^2d\phi_h d\phi_s} =$$

All measured by COMPASS

$$\left[\frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L})$$

$$1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ + \lambda \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin\phi_h} \sin\phi_h \\ + S_L \left[\sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h \right] \\ + S_L \lambda \left[\sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\phi_h} \cos\phi_h \right] \\ \times \left[\begin{array}{l} A_{UT}^{\sin(\phi_h-\phi_s)} \sin(\phi_h-\phi_s) \\ + \varepsilon A_{UT}^{\sin(\phi_h+\phi_s)} \sin(\phi_h+\phi_s) \\ + \varepsilon A_{UT}^{\sin(3\phi_h-\phi_s)} \sin(3\phi_h-\phi_s) \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_s} \sin\phi_s \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h-\phi_s)} \sin(2\phi_h-\phi_s) \end{array} \right] \\ + S_T \lambda \left[\begin{array}{l} \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h-\phi_s)} \cos(\phi_h-\phi_s) \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\phi_s} \cos\phi_s \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h-\phi_s)} \cos(2\phi_h-\phi_s) \end{array} \right]$$



Quark Nucleon	U	L	T
U	number density		Boer-Mulders
L		helicity	worm-gear L
T	Sivers	Kotzinian- Mulders worm-gear T	transversity pretzelosity
	spin of the nucleon	spin of the quark	k_T

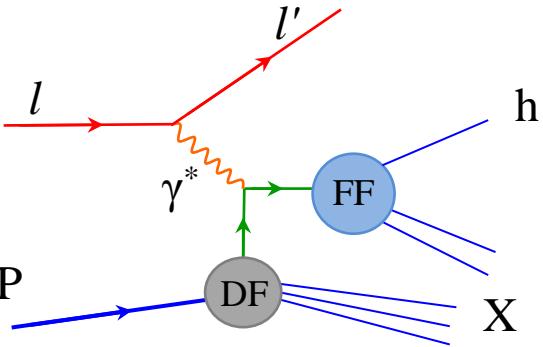
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Quark Nucleon	U	L	T
U	$f_1^q(x, \mathbf{k}_T^2)$ number density		$h_1^{\perp q}(x, \mathbf{k}_T^2)$ Boer-Mulders
L		$g_1^q(x, \mathbf{k}_T^2)$ helicity	$h_{1L}^{\perp q}(x, \mathbf{k}_T^2)$ worm-gear L
T	$f_{1T}^{\perp q}(x, \mathbf{k}_T^2)$ Sivers	$g_{1T}^q(x, \mathbf{k}_T^2)$ Kotzinian- Mulders worm-gear T	$h_{1T}^{\perp q}(x, \mathbf{k}_T^2)$ pretzelosity

+ two FFs: $D_{1q}^h(z, P_\perp^2)$ and $H_{1q}^{\perp h}(z, P_\perp^2)$

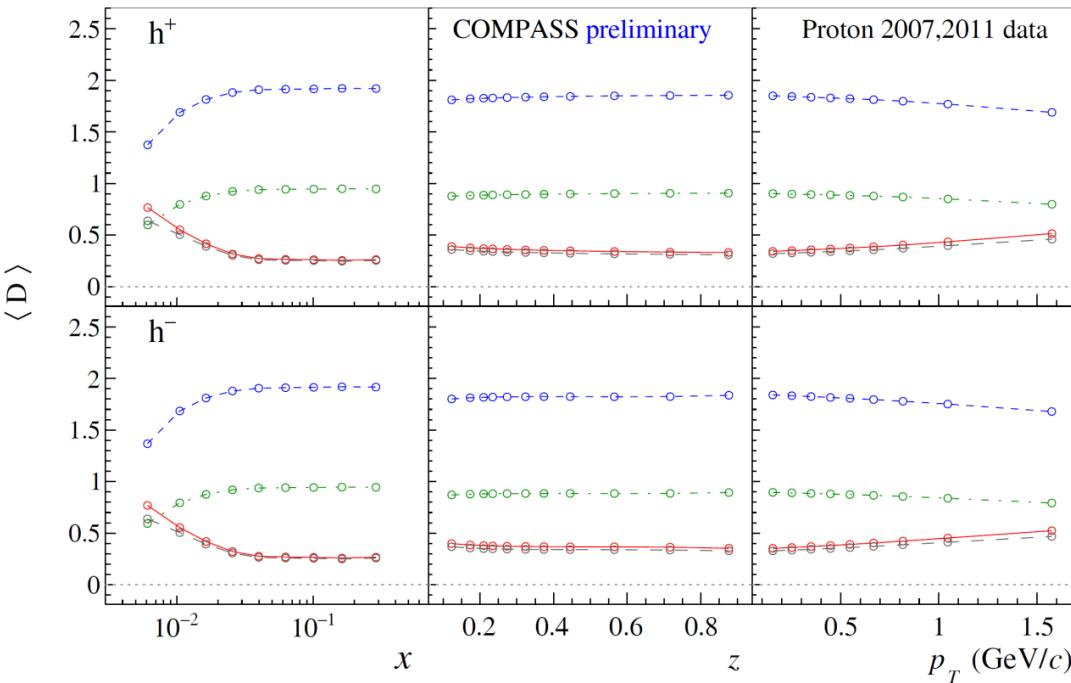


SIDIS: target longitudinal spin dependent asymmetries

$$\frac{d\sigma}{dxdydzdp_T^2d\phi_hd\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots \right.$$

$$+ S_L \left[\sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h \right] \left\} \right.$$

$$+ S_L \lambda \left[\sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\phi_h} \cos\phi_h \right] \left. \right\}$$



$$D^{\sin(\phi_h)} = \sqrt{2\varepsilon(1+\varepsilon)} \approx \frac{2(2-y)\sqrt{1-y}}{1+(1-y)^2}$$

$$D^{\sin(2\phi_h)} = \varepsilon \approx \frac{2(1-y)}{1+(1-y)^2}$$

$$D^1 = \sqrt{(1-\varepsilon^2)} \approx \frac{y(2-y)}{1+(1-y)^2}$$

$$D^{\cos(\phi_h)} = \sqrt{2\varepsilon(1-\varepsilon)} \approx \frac{2y\sqrt{1-y}}{1+(1-y)^2}$$

SIDIS: target longitudinal spin dependent asymmetries

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$$A_{UL}^{\sin \phi_h} \stackrel{WW}{\propto} Q^{-1} \left(h_{1L}^{\perp q} \otimes H_{1q}^{\perp h} + \dots \right) \leftarrow \begin{cases} A_{UT}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h \\ A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h} \end{cases}$$

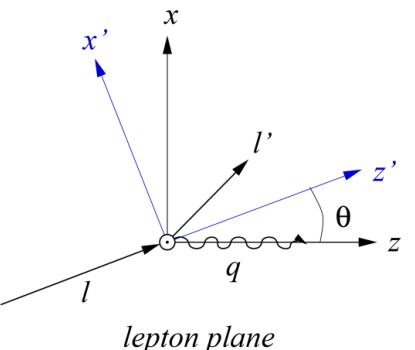
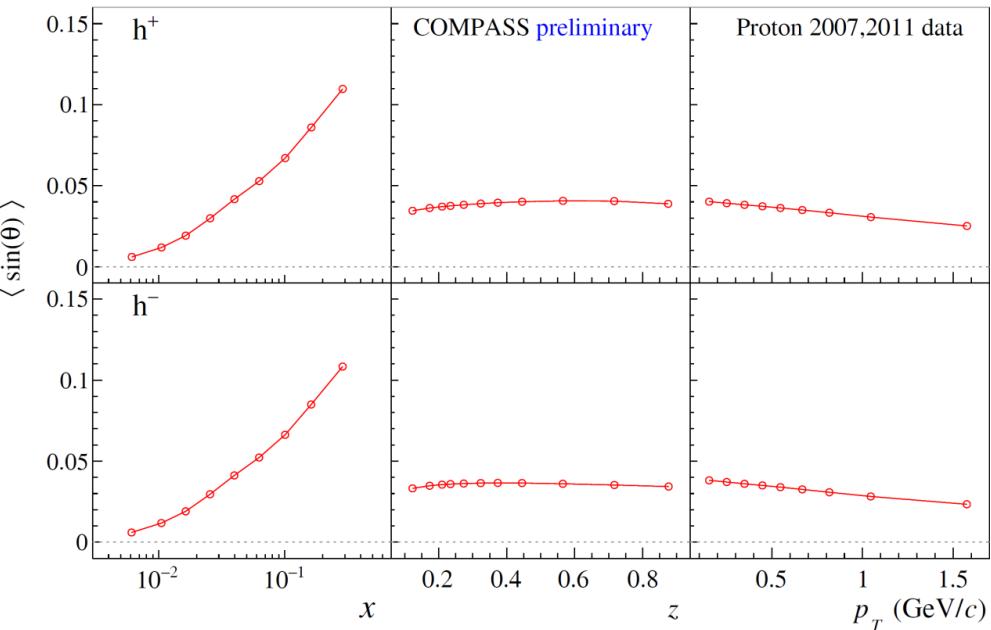
$$A_{UL}^{\sin 2\phi_h} \propto h_{1L}^{\perp q} \otimes H_{1q}^{\perp h} \leftarrow \begin{cases} A_{UT}^{\sin(2\phi_h - \phi_s)} \stackrel{WW}{\propto} Q^{-1} \left(h_1^q \otimes H_{1q}^{\perp h} + \dots \right) \end{cases}$$

$$A_{UL}^{\sin 3\phi_h} \leftrightarrow A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

$$A_{LL} \propto g_{1L}^q \otimes D_{1q}^h \leftarrow \begin{cases} A_{LT}^{\cos(\phi_s)} \stackrel{WW}{\propto} Q^{-1} \left(g_{1T}^q \otimes D_{1q}^h + \dots \right) \end{cases}$$

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$$\sin \theta = \gamma \sqrt{\frac{1-y - \frac{1}{4}\gamma^2 y^2}{1+\gamma^2}}, \quad \gamma = \frac{2Mx}{Q};$$

$\theta \xrightarrow{\text{Bjorken limit}} 0 \Rightarrow S_T \approx P_T, S_L \approx P_L$

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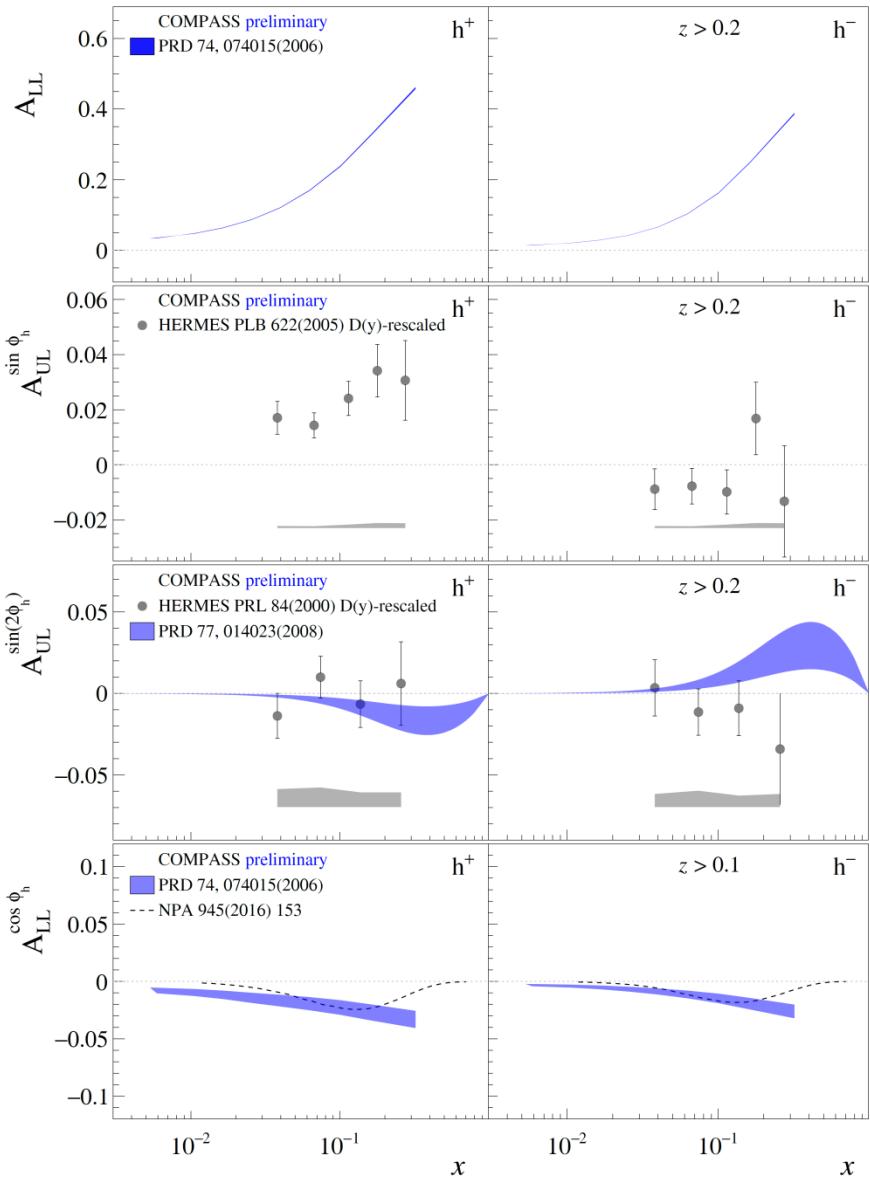
$$+ S_L \lambda \left[\sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos \phi_h} \cos \phi_h \right]$$

$$F_{LL}^1 = \mathcal{C} \left\{ g_{1L}^q D_{1q}^h \right\}$$

$$F_{UL}^{\sin \phi_h} = \frac{2M}{Q} \mathcal{C} \left\{ -\frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M_h} \left(x h_L^q H_{1q}^{\perp h} + \frac{M_h}{M} g_{1L}^q \frac{\tilde{G}_q^{\perp h}}{z} \right) \right. \\ \left. + \frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M} \left(x f_L^{\perp q} D_{1q}^h - \frac{M_h}{M} h_{1L}^{\perp q} \frac{\tilde{H}_q^h}{z} \right) \right\}$$

$$F_{UL}^{\sin 2\phi_h} = \mathcal{C} \left\{ -\frac{2(\hat{\mathbf{h}} \cdot \mathbf{p}_T)(\hat{\mathbf{h}} \cdot \mathbf{k}_T) - \mathbf{p}_T \cdot \mathbf{k}_T}{MM_h} h_{1L}^{\perp q} H_{1q}^{\perp h} \right\}$$

$$F_{LL}^{\cos \phi_h} = \frac{2M}{Q} \mathcal{C} \left\{ -\frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M_h} \left(x e_L^q H_{1q}^{\perp h} + \frac{M_h}{M} g_{1L}^q \frac{\tilde{D}_q^{\perp h}}{z} \right) \right. \\ \left. + \frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M} \left(x g_L^{\perp q} D_{1q}^h - \frac{M_h}{M} h_{1L}^{\perp q} \frac{\tilde{E}_q^h}{z} \right) \right\}$$



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COMPASS collected large amount of L-SIDIS data
Unprecedented precision for some amplitudes!

$A_{UL}^{\sin \phi_h}$

- Q-suppression, Various different “twist” ingredients
- Sizable TSA-mixing
- Significant h^+ asymmetry, clear z -dependence
- h^- compatible with zero

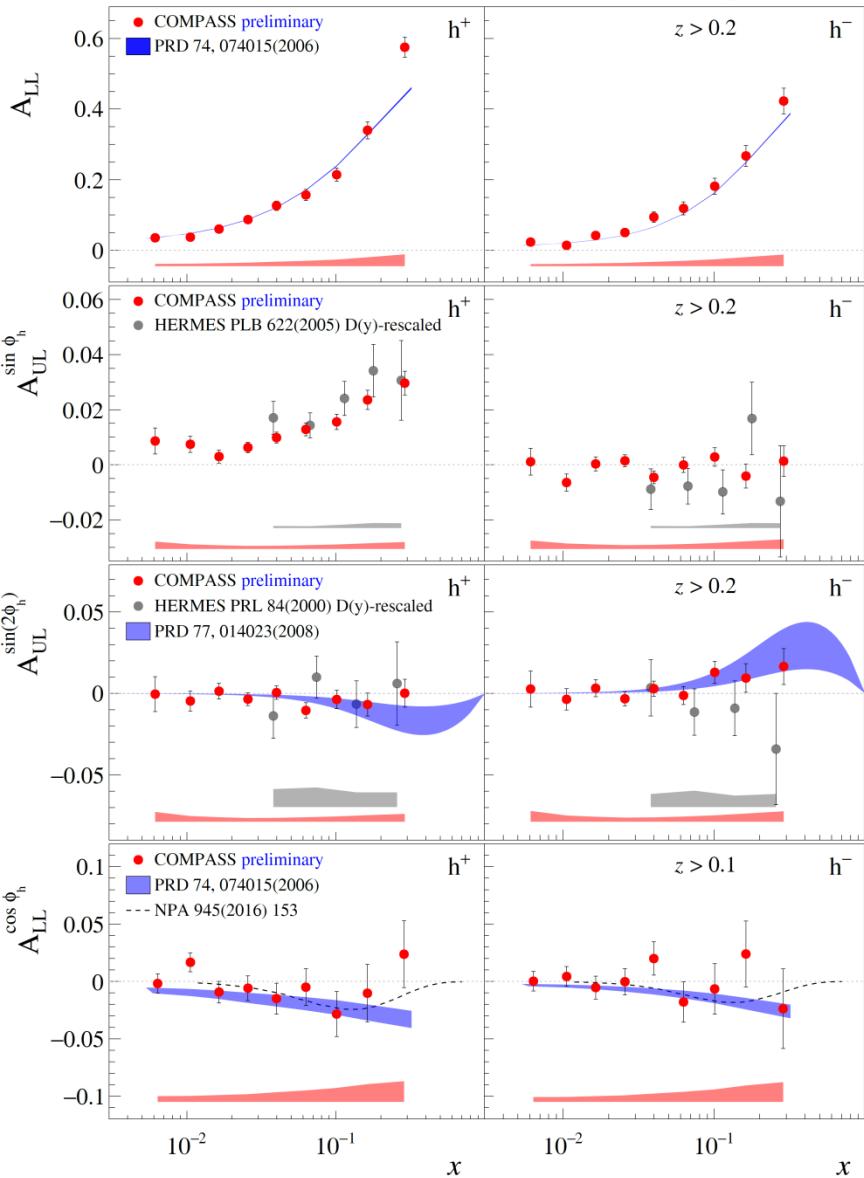
$A_{UL}^{\sin 2\phi_h}$

- Only “twist-2” ingredients
- Additional p_T -suppression
- Compatible with zero, in agreement with models
- Collins-like behavior?

$A_{LL}^{\cos \phi_h}$

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B. Parsamyan (for COMPASS) [arXiv:1801.01488 \[hep-ex\]](https://arxiv.org/abs/1801.01488)



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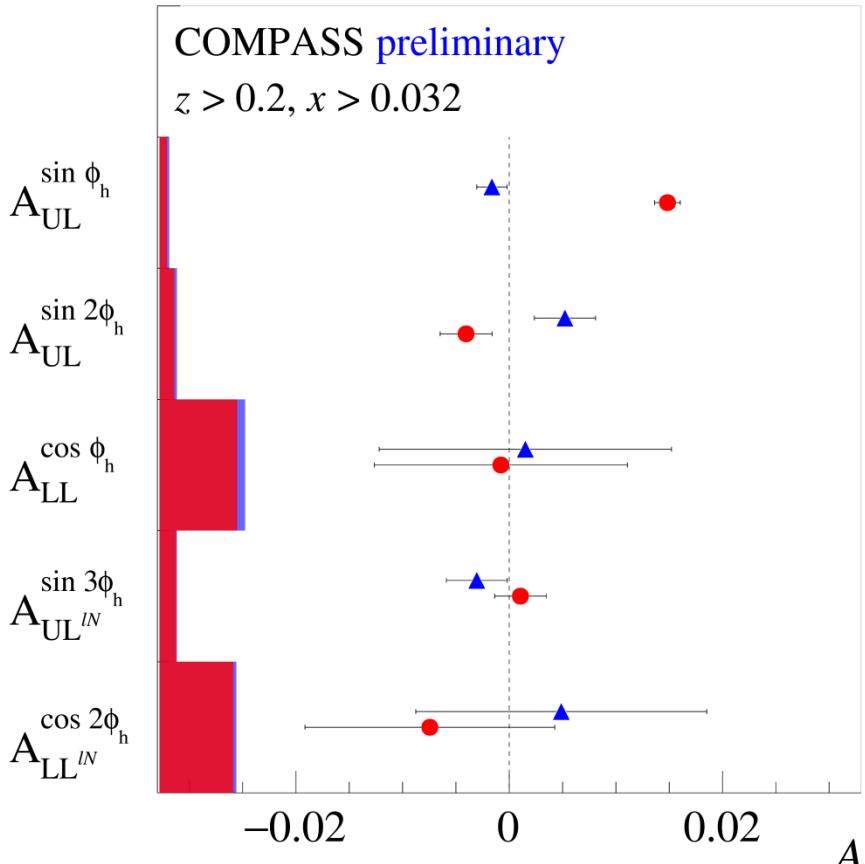
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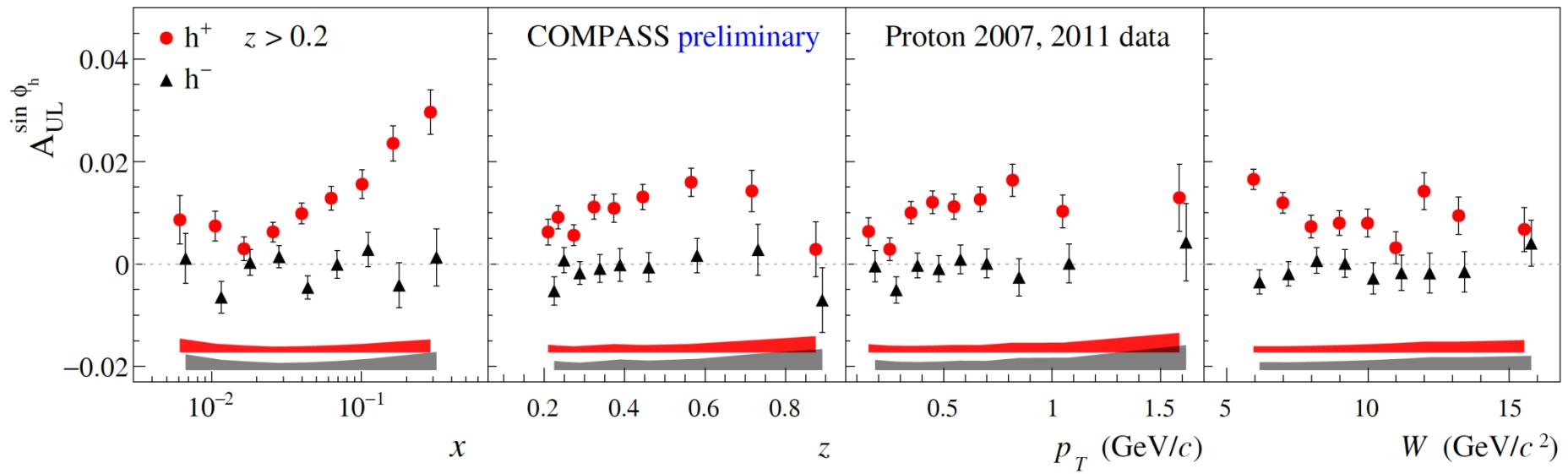
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The $A_{UL}^{\sin\phi_h}$ asymmetry

$$\frac{d\sigma}{dxdydzdp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_L \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \dots \right\}$$

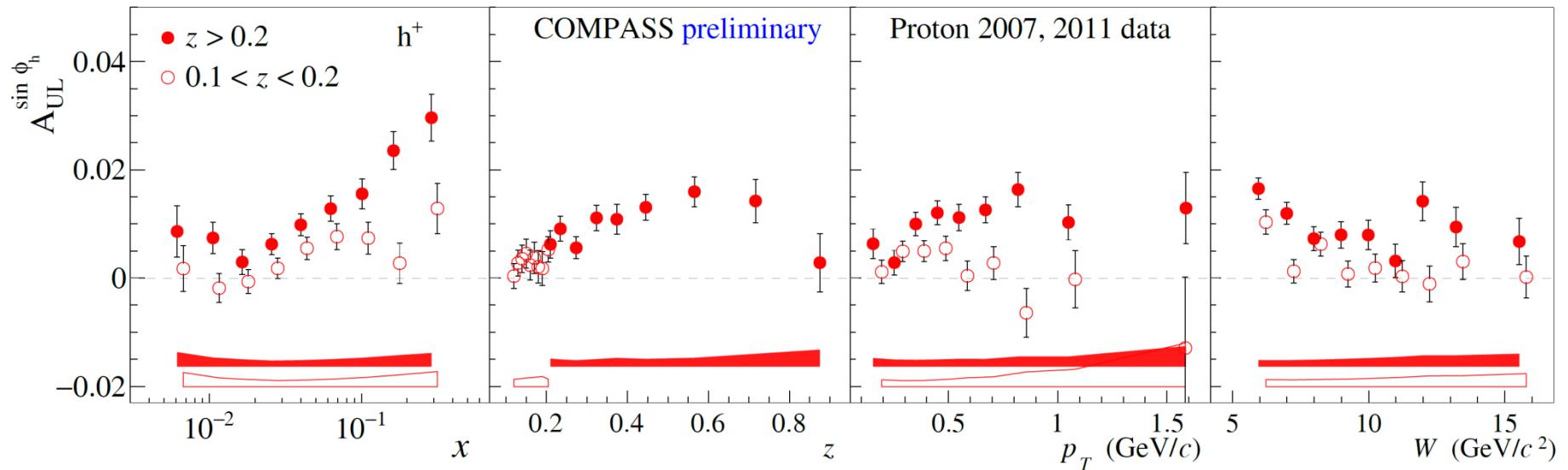
$$F_{UL}^{\sin\phi_h} = \frac{2M}{Q} \mathcal{C} \left\{ -\frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M_h} \left(x h_L^q H_{1q}^{\perp h} + \frac{M_h}{M} g_{1L}^q \frac{\tilde{G}_q^{\perp h}}{z} \right) \right. \\ \left. + \frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M} \left(x f_L^{\perp q} D_{1q}^h - \frac{M_h}{M} h_{1L}^{\perp q} \frac{\tilde{H}_q^h}{z} \right) \right\}$$



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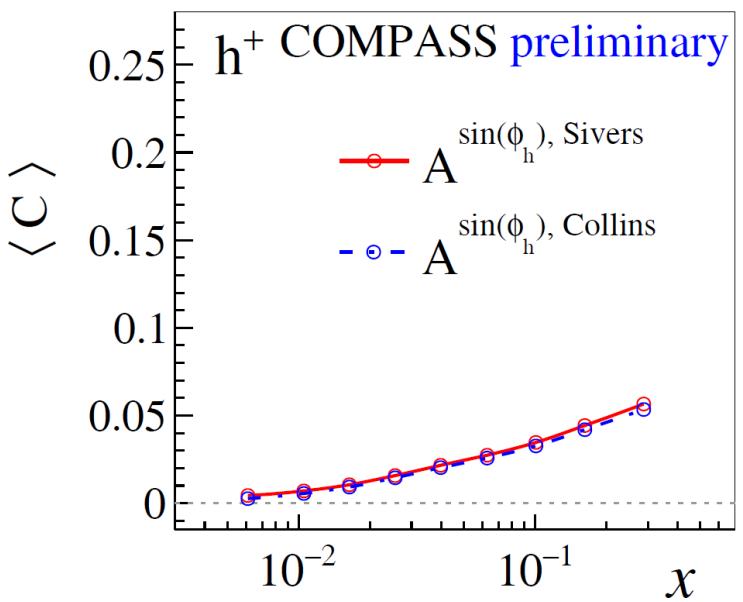


- Q-suppression, TSA-mixing
- Various different “twist” ingredients
- Non-zero trend for h^+, h^- compatible with zero, clear z -dependence

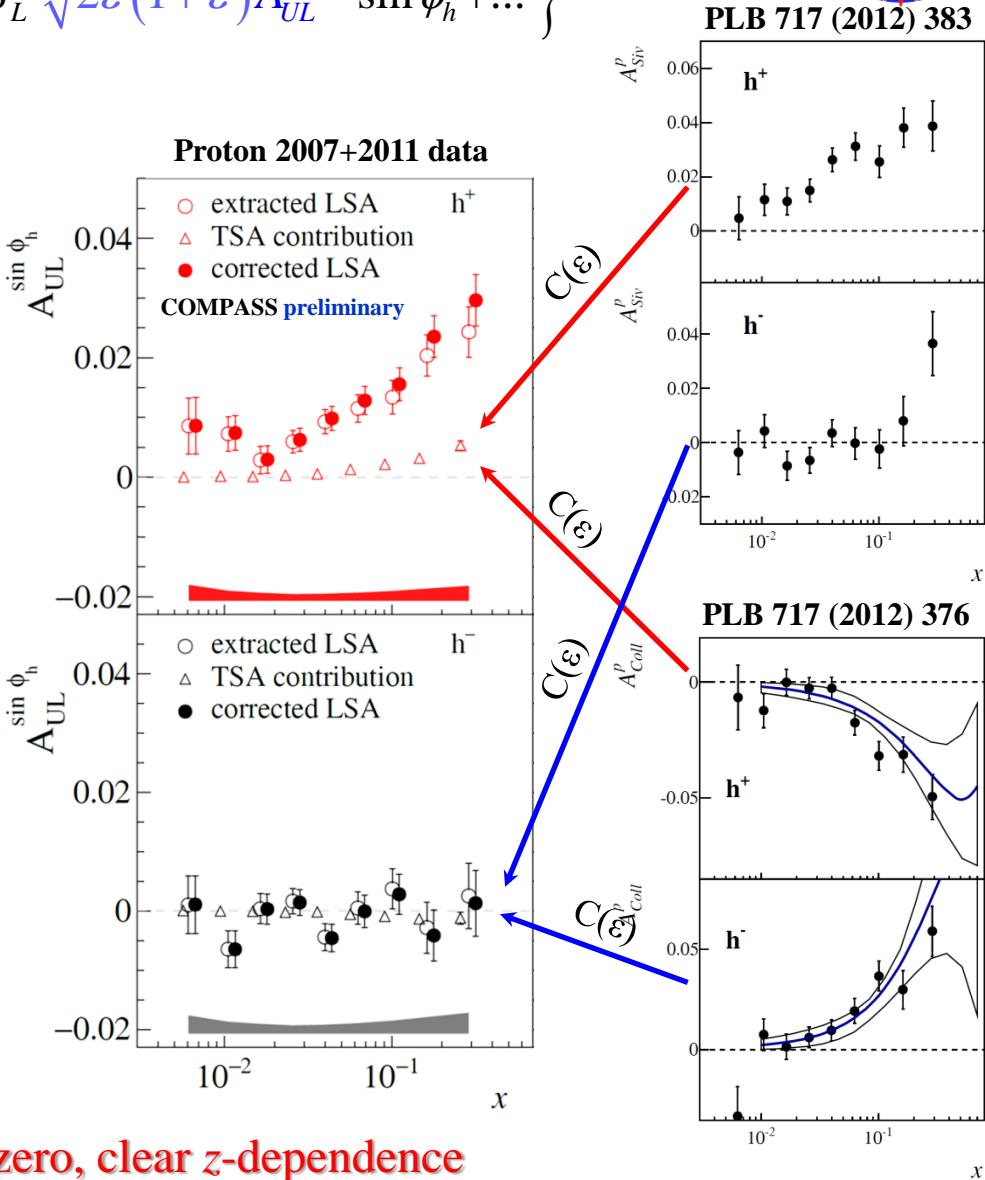
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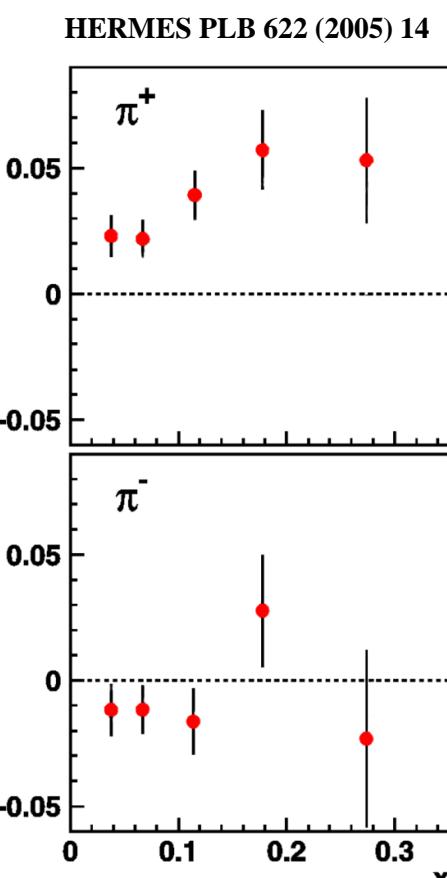
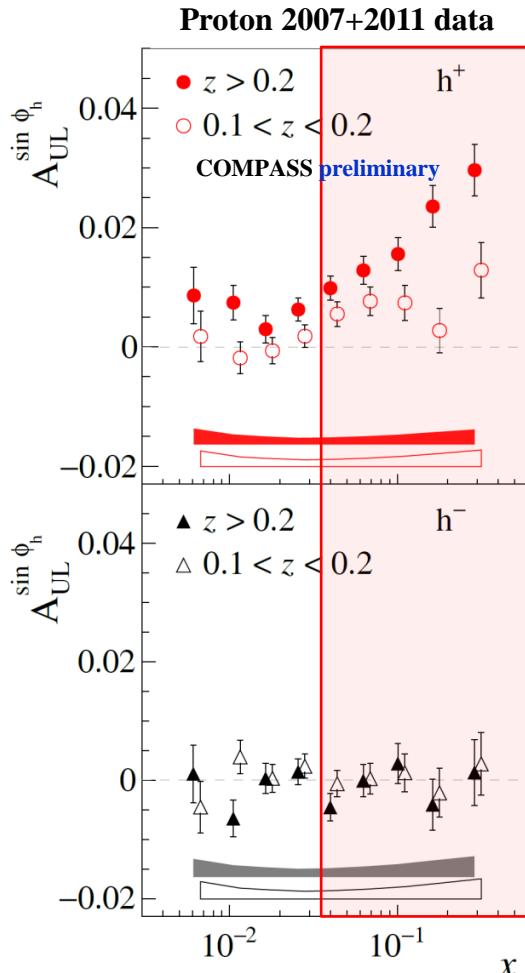
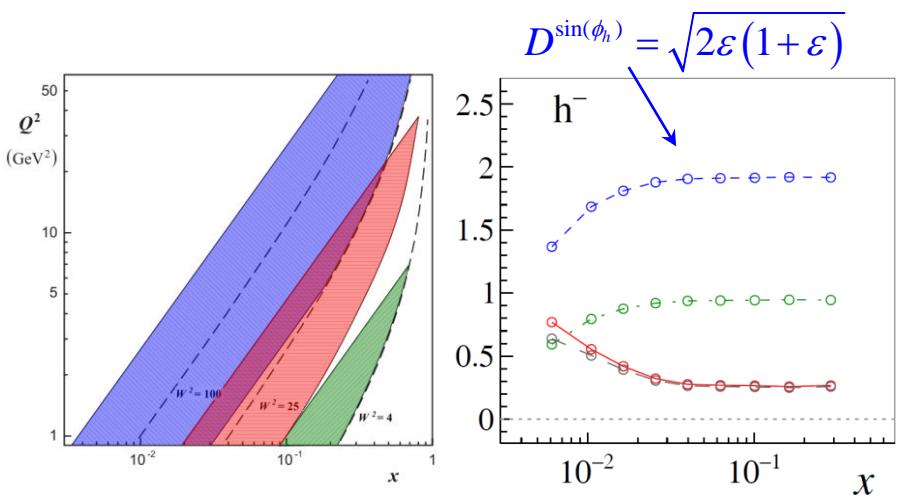
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$$F_{UL}^{\sin\phi_h} = \frac{2M}{Q} \mathcal{C} \left\{ -\frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M_h} \left(x h_L^q H_{1q}^{\perp h} + \frac{M_h}{M} g_{1L}^q \frac{\tilde{G}_q^{\perp h}}{z} \right) + \frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M} \left(x f_L^{\perp q} D_{1q}^h - \frac{M_h}{M} h_{1L}^{\perp q} \frac{\tilde{H}_q^h}{z} \right) \right\}$$



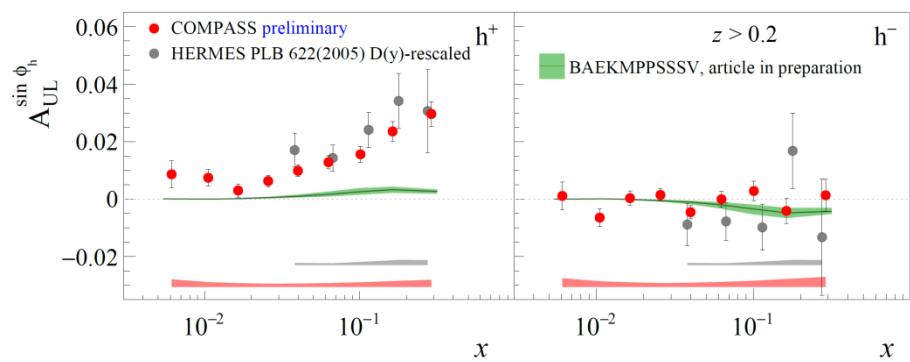
- Q-suppression, TSA-mixing
- Various different “twist” ingredients
- Non-zero trend for h^+, h^- compatible with zero, clear z -dependence

SIDIS: target longitudinal spin dependent asymmetries

$$\frac{d\sigma}{dxdydzdp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_L \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \dots \right\}$$

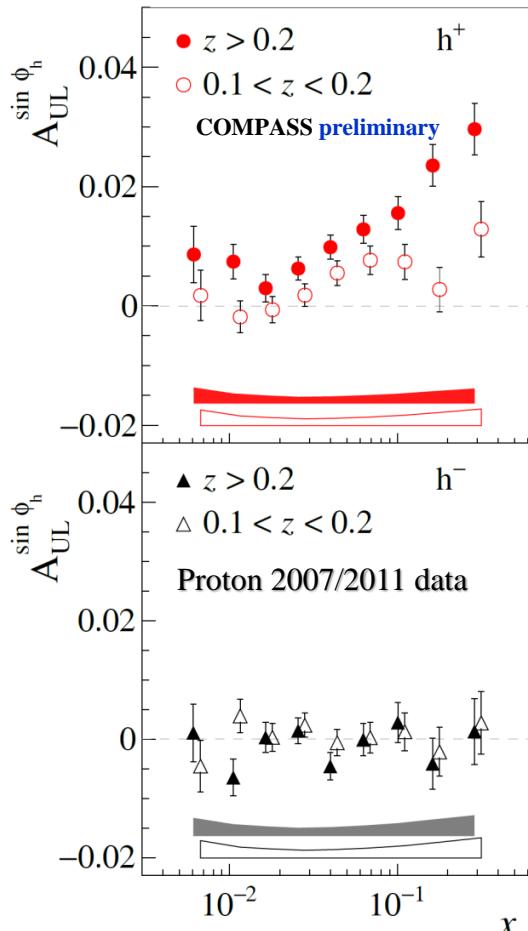
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S. Bastami et al. JHEP 1906 (2019) 007:
“SIDIS in Wandzura-Wilczek-type approximation”



- Q-suppression, TSA-mixing
- Various different “twist” ingredients
- Non-zero trend for h^+ , h^- compatible with zero, clear z -dependence

B. Parsamyan (for COMPASS)
[arXiv:1801.01488 \[hep-ex\]](https://arxiv.org/abs/1801.01488)



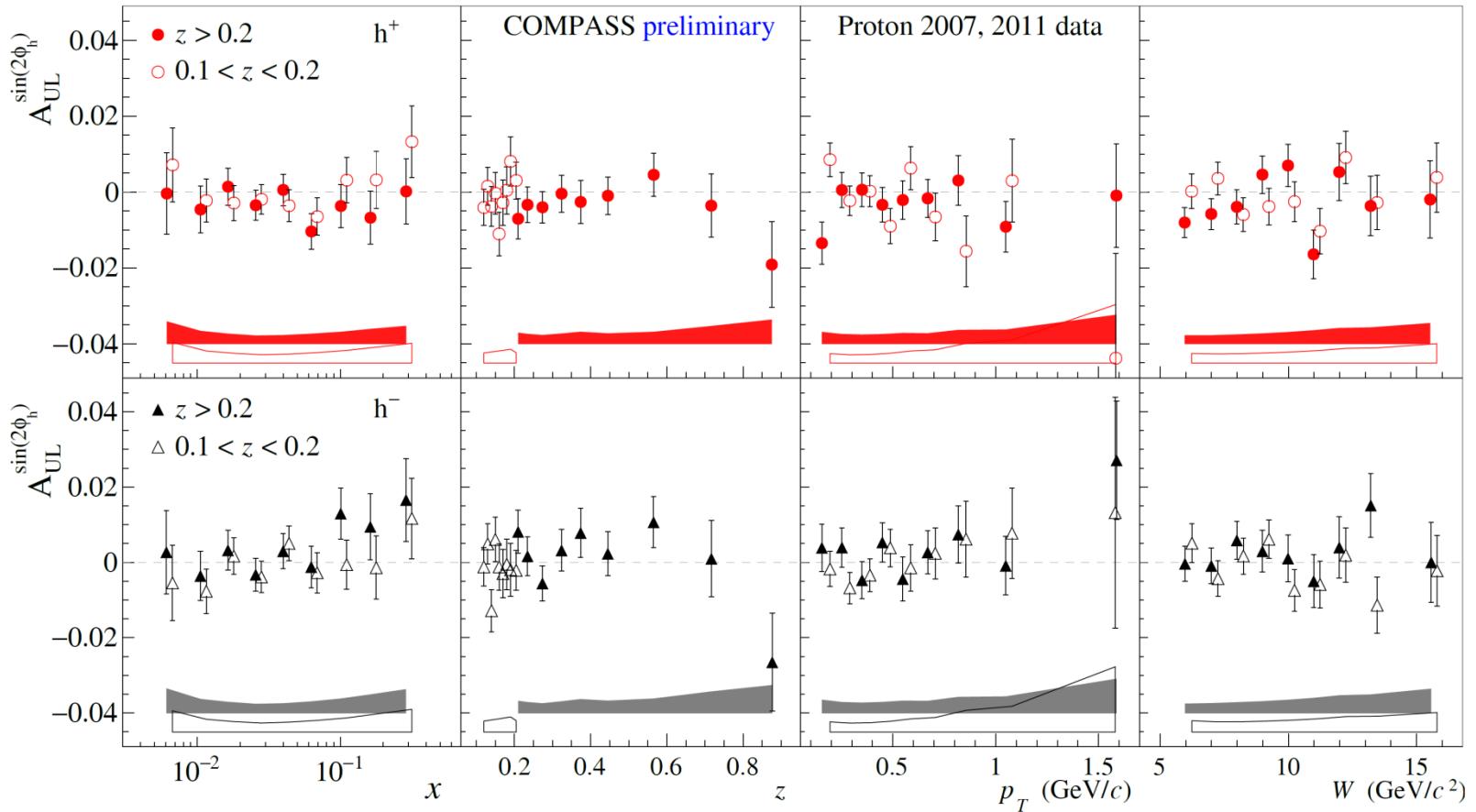
Zhun Lu
Phys. Rev. D 90, 014037(2014)

The $A_{UL}^{\sin 2\phi_h}$ asymmetry

$$\frac{d\sigma}{dxdydzdp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + \dots \right\}$$

$$F_{UL}^{\sin 2\phi_h} = C \left\{ -\frac{2(\hat{h} \cdot p_T)(\hat{h} \cdot k_T) - p_T \cdot k_T}{MM_h} h_{1L}^{\perp q} H_{1q}^{\perp h} \right\}$$

- Only “twist-2” ingredients
- Additional p_T -suppression

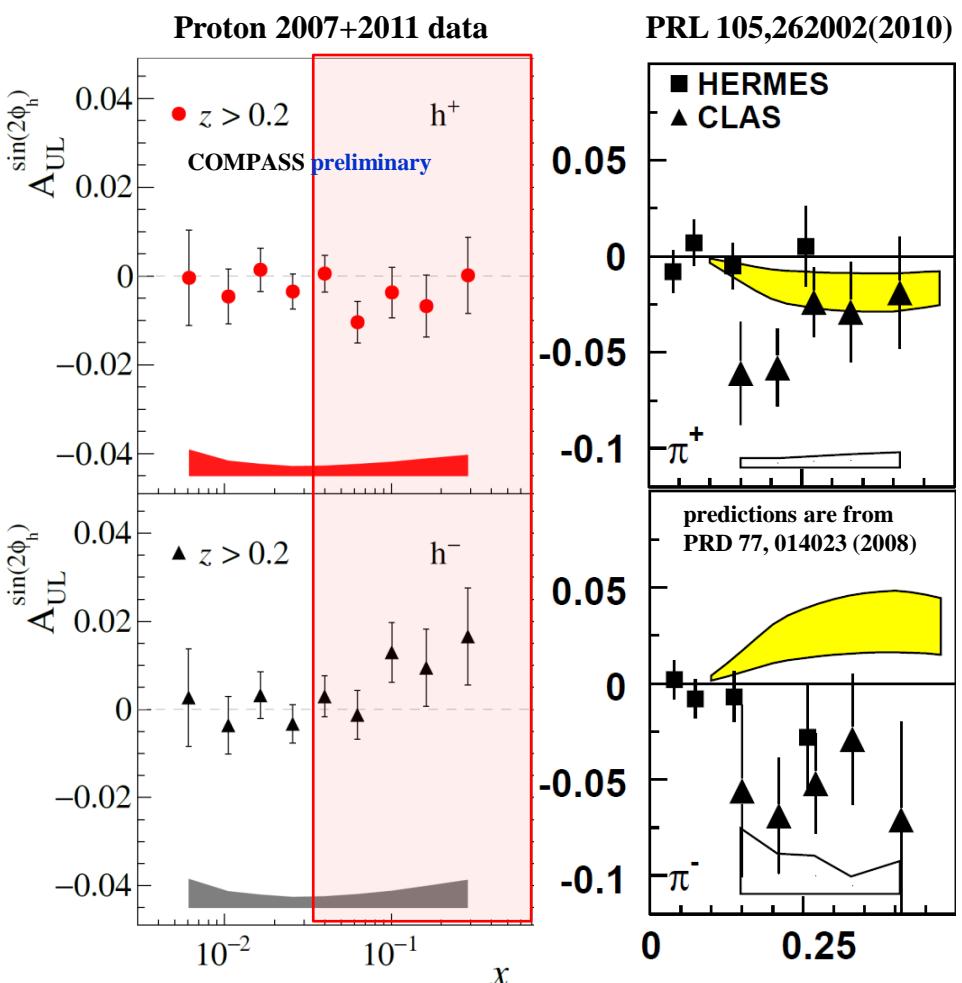


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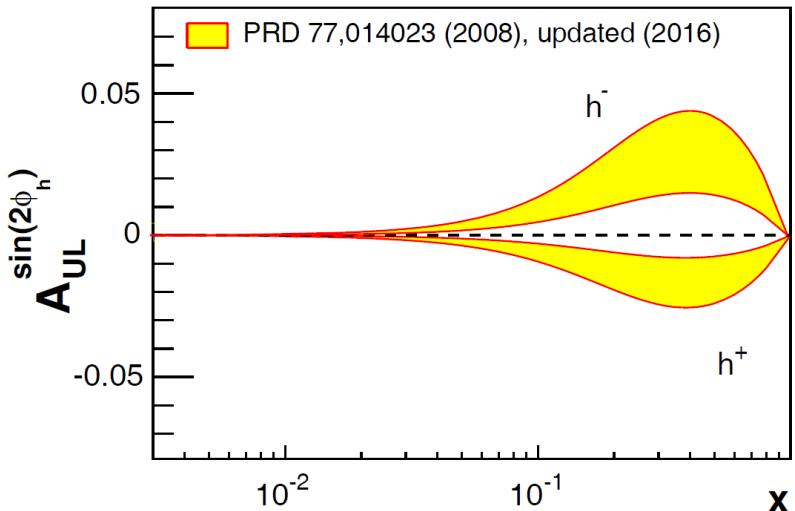
- Only “twist-2” ingredients
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- Collins-like behavior?
- In agreement with model predictions
- Discrepancy with HERMES and JLab?



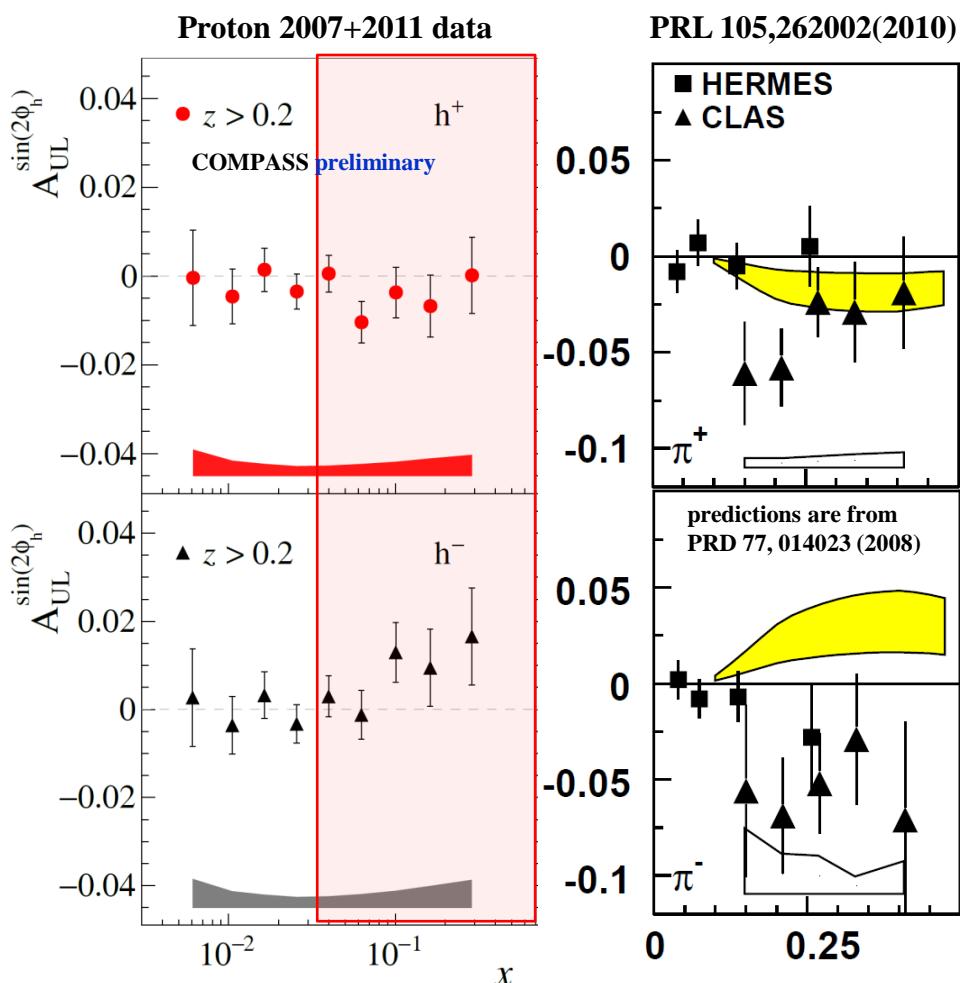
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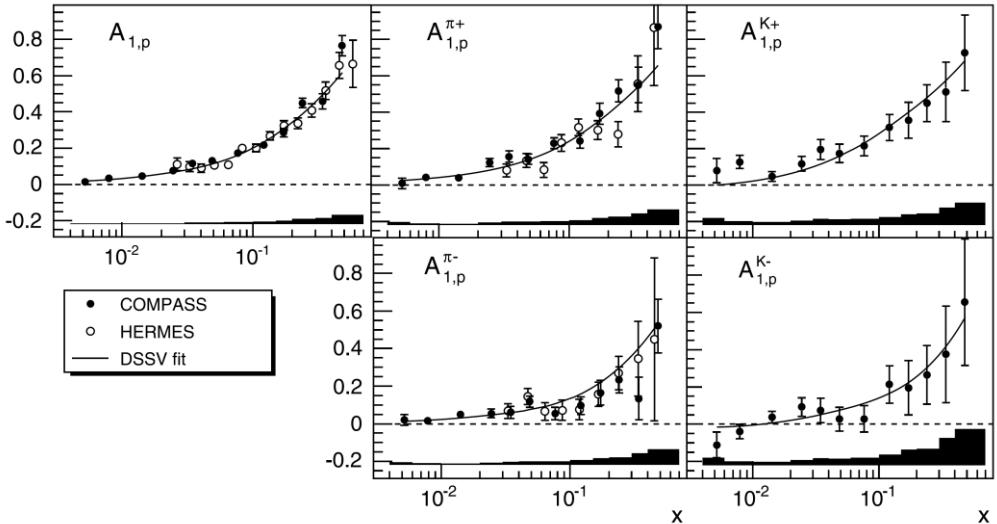
The A_{LL} asymmetry

$$\frac{d\sigma}{dxdydzdp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} + \dots \right\}$$

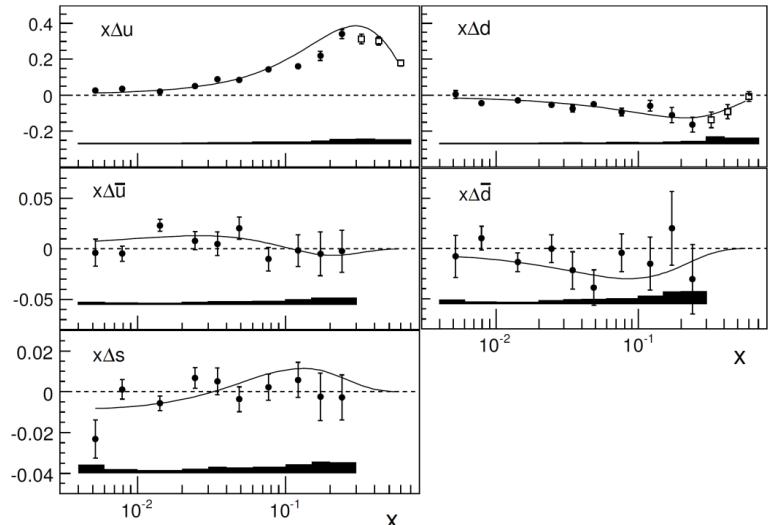
COMPASS: PLB 693 (2010) 227–235

$$F_{LL}^1 = C \left\{ g_{1L}^q D_{1q}^h \right\}$$

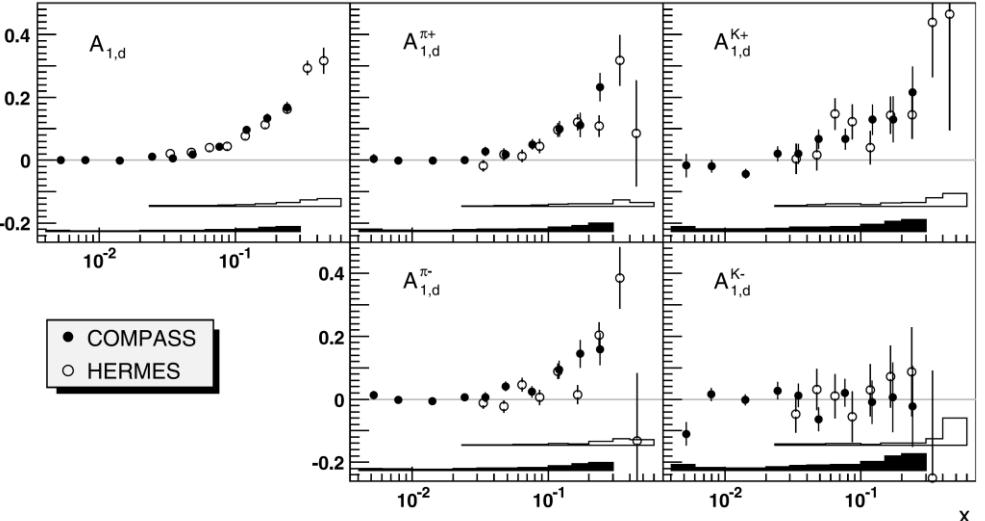
- Measurement of (semi-)inclusive $A_1(A_{LL})$ is one of the key physics topics of HERMES/COMPASS
- Large amount of P/D data
- No P_T -dependence observed



COMPASS: PLB 693 (2010) 227–235



COMPASS: PLB 680 (2009) 217–224

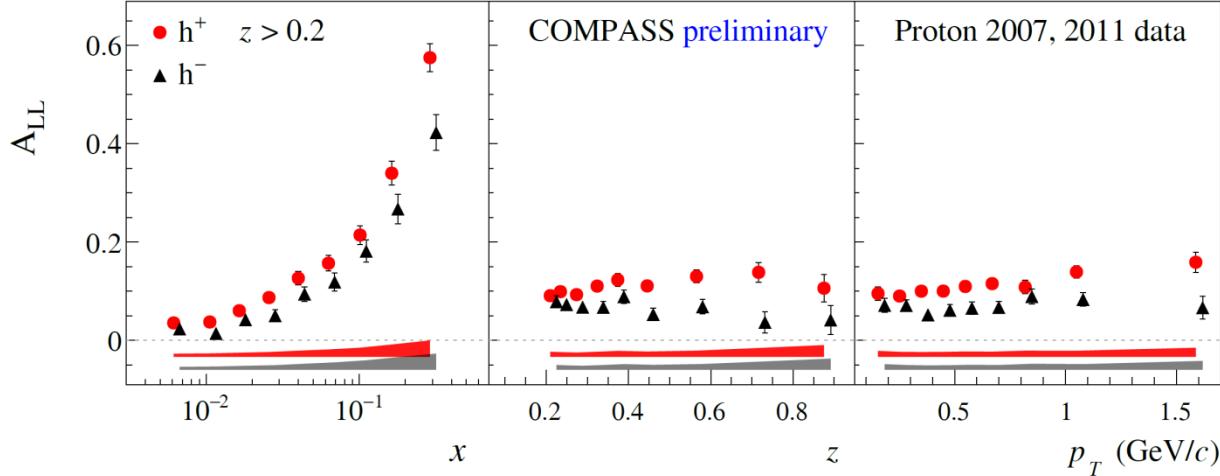


The A_{LL} asymmetry

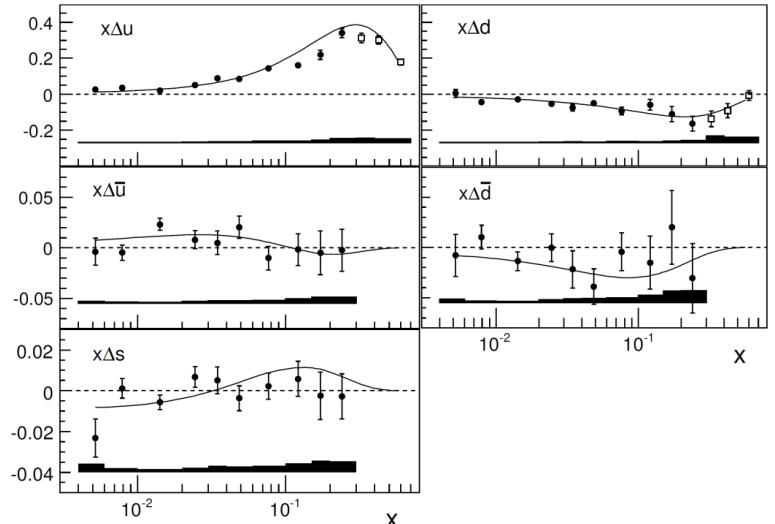
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PLB 693 (2010) 227–235

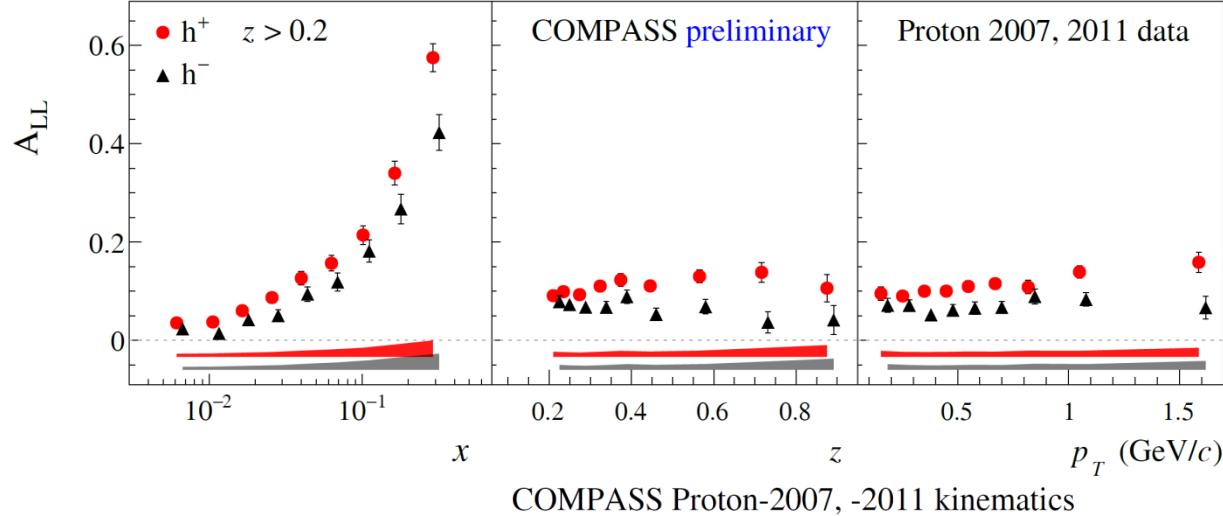


The A_{LL} asymmetry

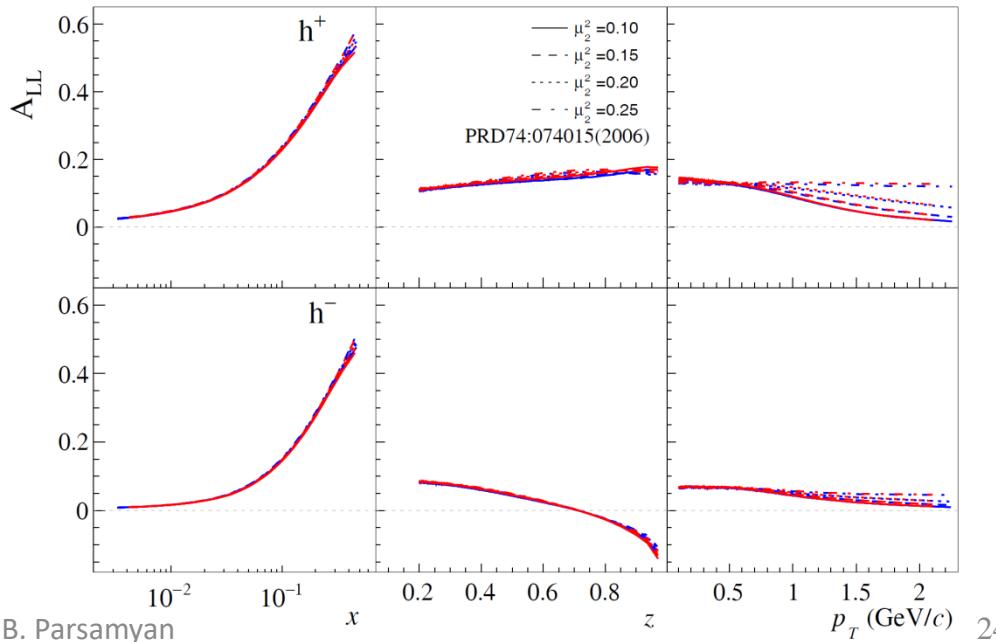
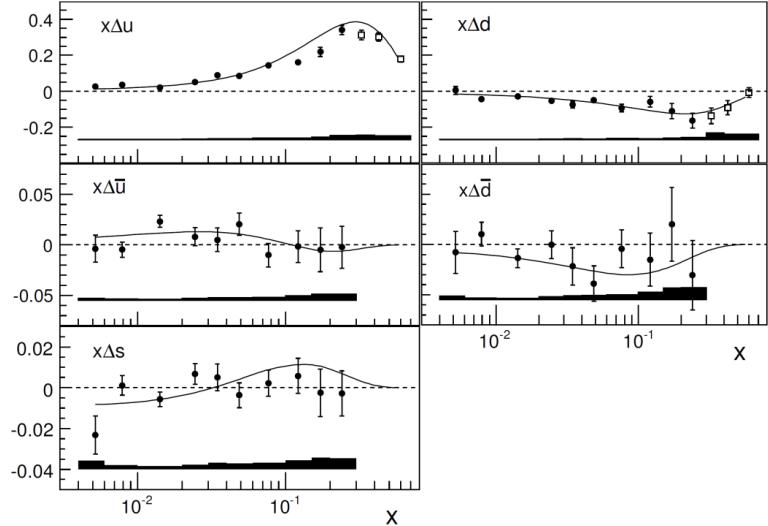
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PLB 693 (2010) 227–235

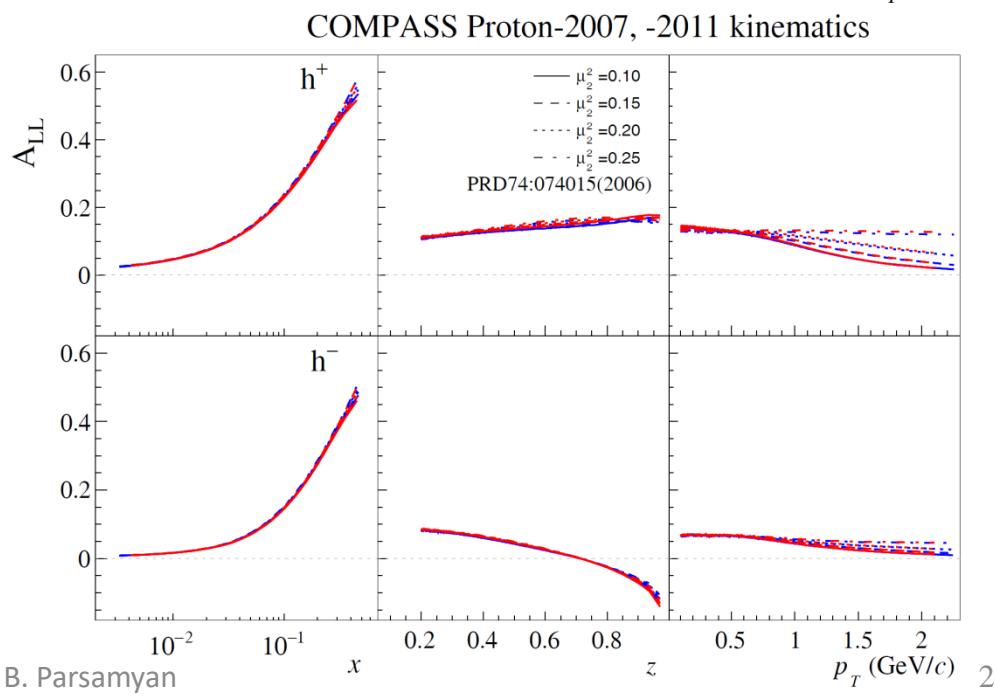
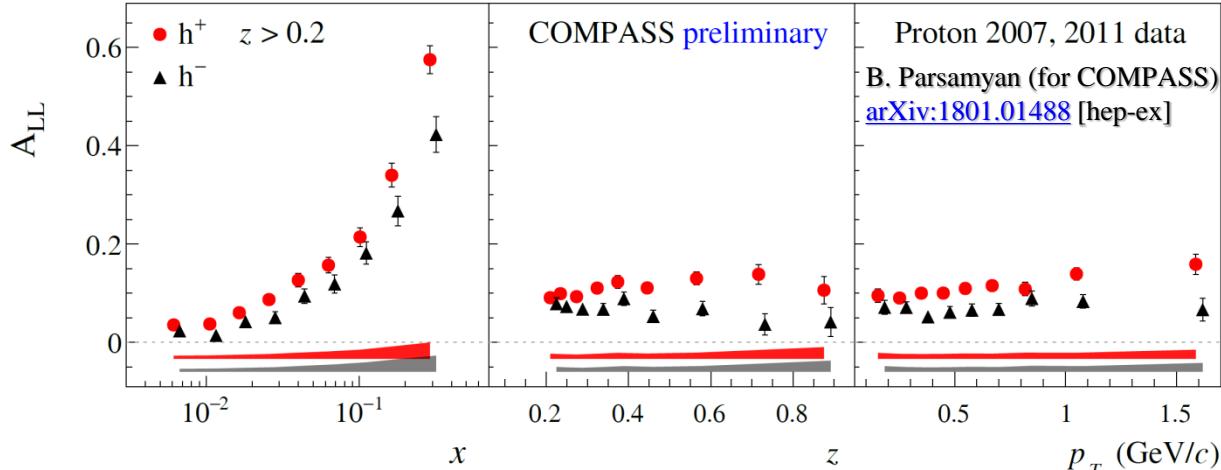
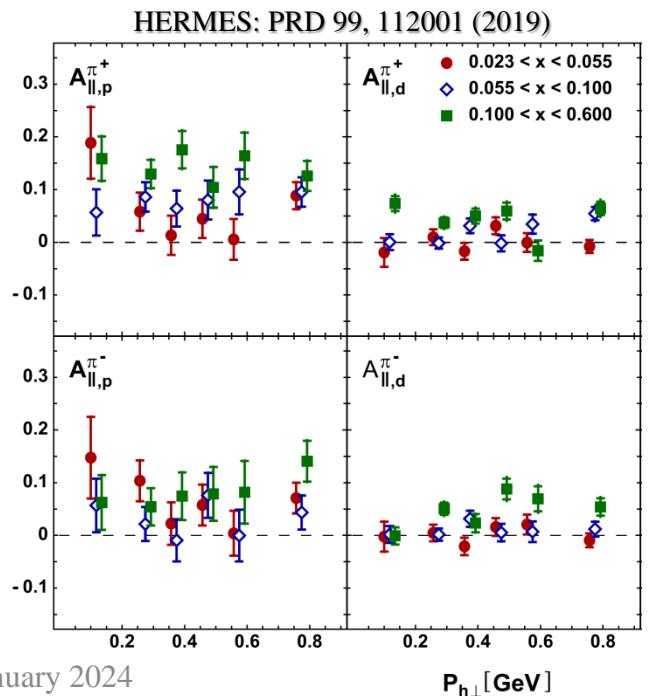


SIDIS: target longitudinal spin dependent asymmetries

$$\frac{d\sigma}{dxdydzdp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} + \dots \right\}$$

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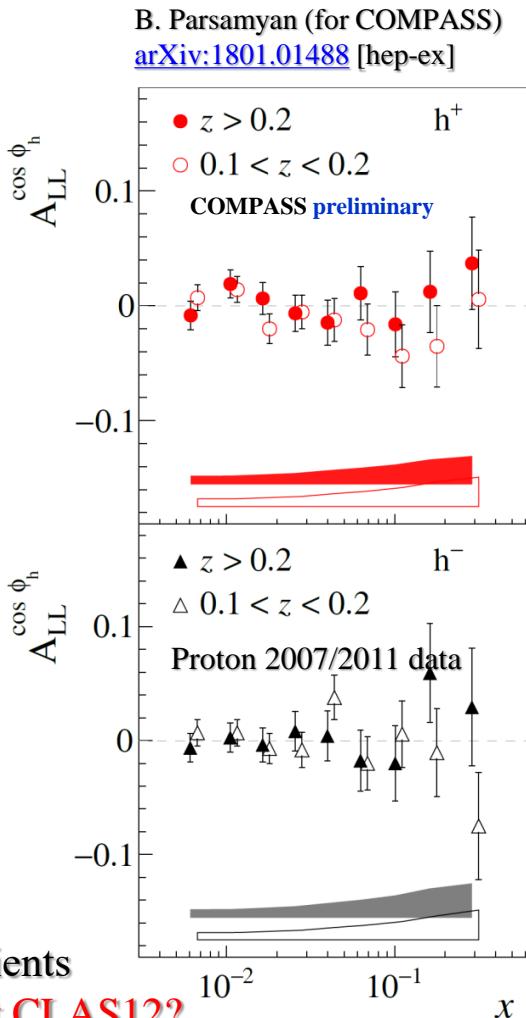
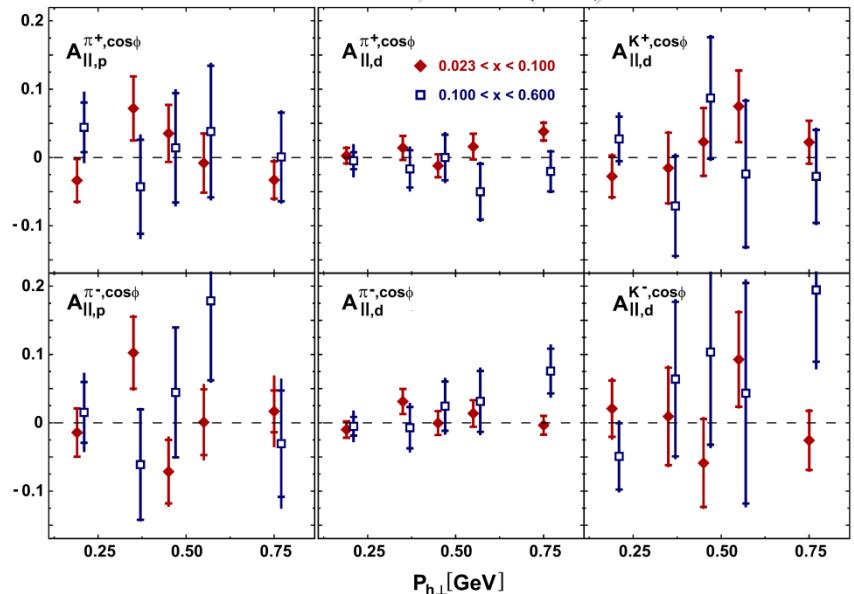


SIDIS: target longitudinal spin dependent asymmetries

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_L \lambda \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\phi_h} \cos\phi_h + \dots \right\}$$

$$F_{LL}^{\cos\phi_h} = \frac{2M}{Q} \mathcal{C} \left\{ -\frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M_h} \left(x e_L^q H_{1q}^{\perp h} + \frac{M_h}{M} g_{1L}^q \frac{\tilde{D}_q^{\perp h}}{z} \right) \right. \\ \left. + \frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M} \left(x g_L^{\perp q} D_{1q}^h - \frac{M_h}{M} h_{1L}^{\perp q} \frac{\tilde{E}_q^h}{z} \right) \right\}$$

HERMES: PRD 99, 112001 (2019)

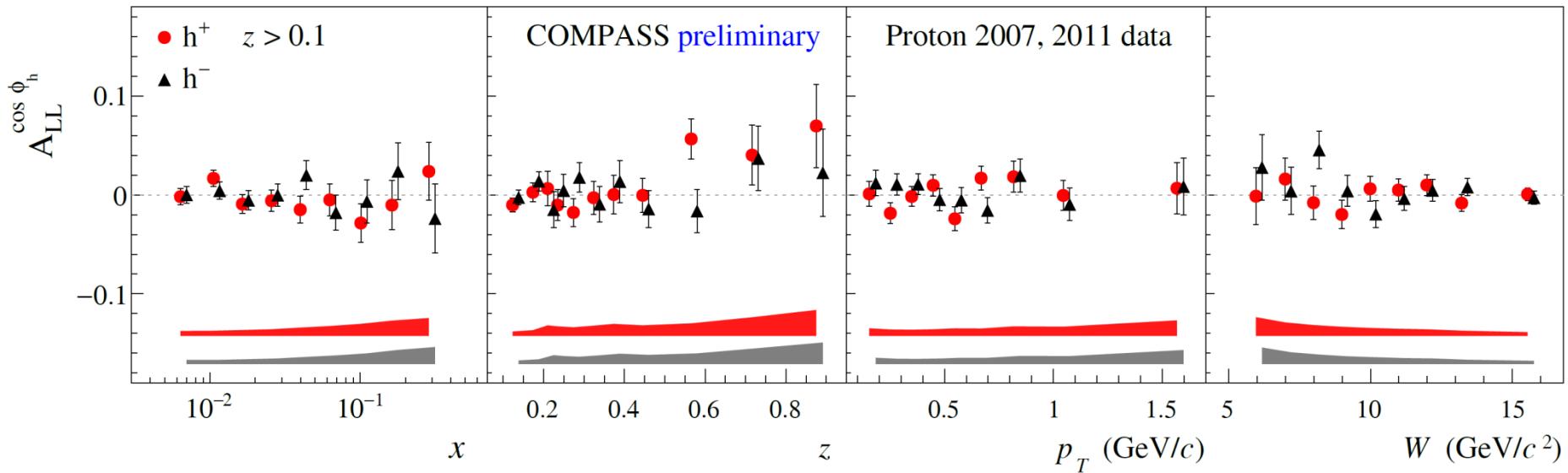


- Q-suppression, various different “twist” ingredients
- Measured to be non zero at CLAS6, what about CLAS12?
- HERMES/COMPASS - small and compatible with zero, in agreement with model predictions

The $A_{LL}^{\cos\phi_h}$ asymmetry

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$$F_{LL}^{\cos\phi_h} = \frac{2M}{Q} \mathcal{C} \left\{ -\frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M_h} \left(xe_L^q H_{1q}^{\perp h} + \frac{M_h}{M} g_{1L}^q \frac{\tilde{D}_q^{\perp h}}{z} \right) \right. \\ \left. + \frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M} \left(xg_L^{\perp q} D_{1q}^h - \frac{M_h}{M} h_{1L}^{\perp q} \frac{\tilde{E}_q^h}{z} \right) \right\}$$



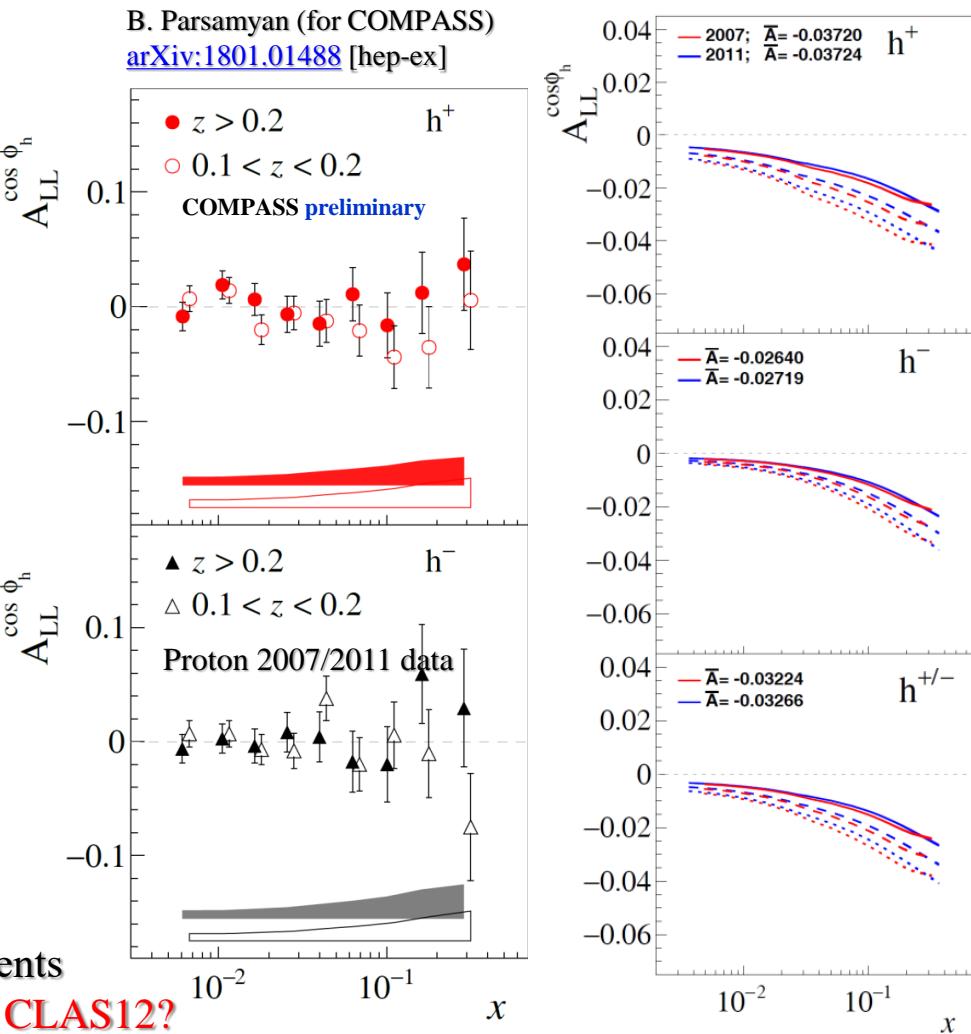
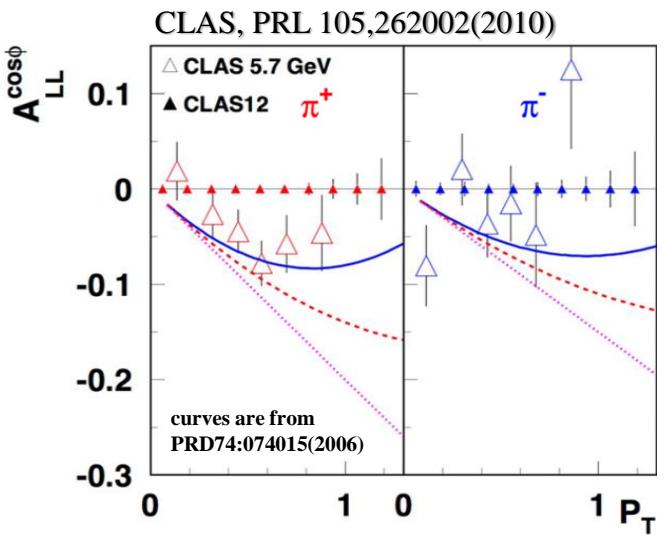
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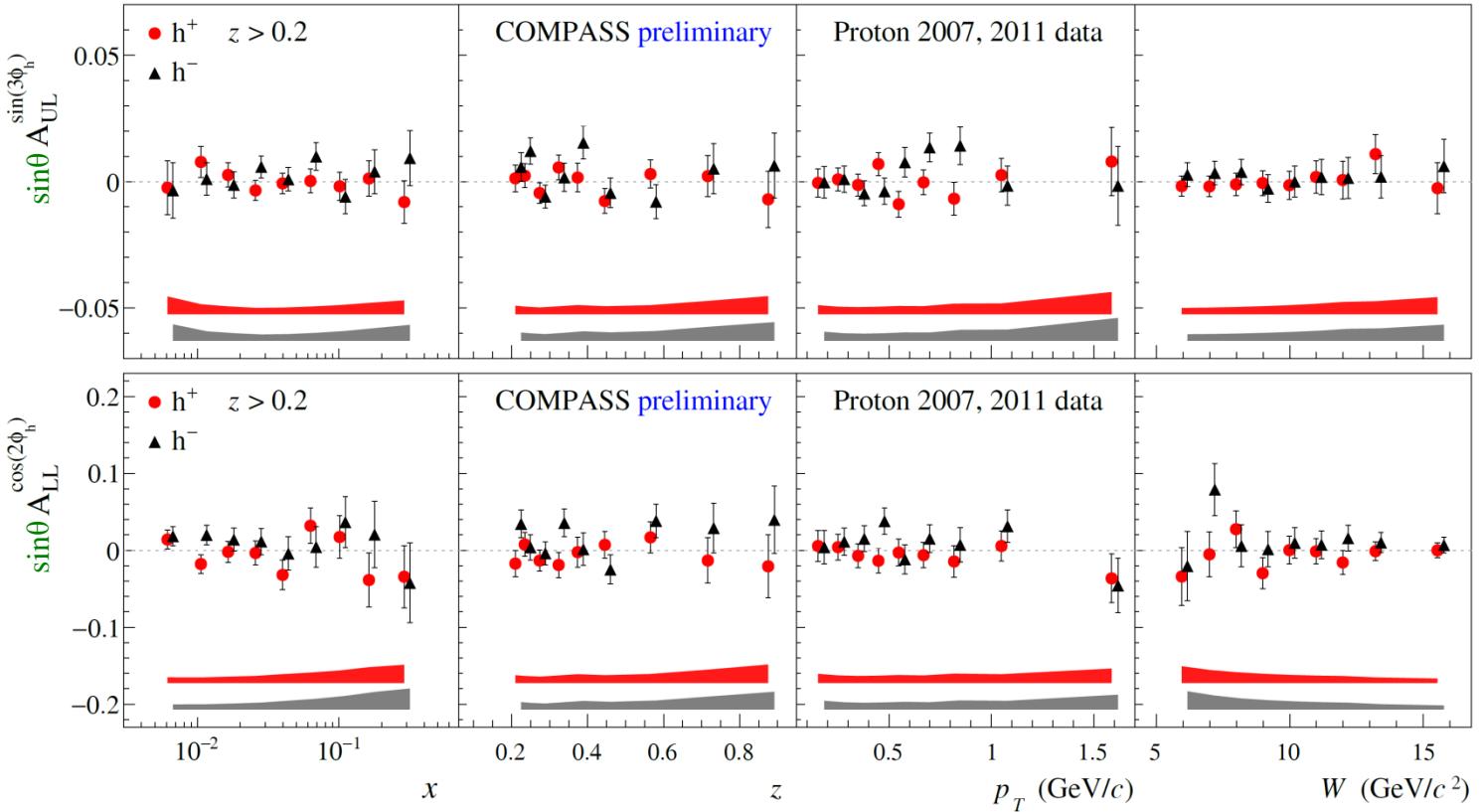


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COMPASS results for $A_{UL}^{\sin 3\phi_h}$ and $A_{LL}^{\cos 2\phi_h}$ asymmetries



$$\frac{d\sigma}{dxdydzdp_T^2 d\phi_h d\phi_s} \propto \left\{ 1 + \dots - \frac{\sin \theta \varepsilon A_{UL}^{\sin 3\phi_h} \sin 3\phi_h}{A_{LL}^{\cos 2\phi_h} \cos 2\phi_h} + P_L \lambda \left[-\sin \theta \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos 2\phi_h} \cos 2\phi_h + \dots \right] \right\}$$



- Alternative way to access corresponding TSAs
- $\sin(\theta)$ suppression
- Other suppressions at the “TSA”-level ($|p_T|^3$, Q^{-1})
- **Compatible with zero**

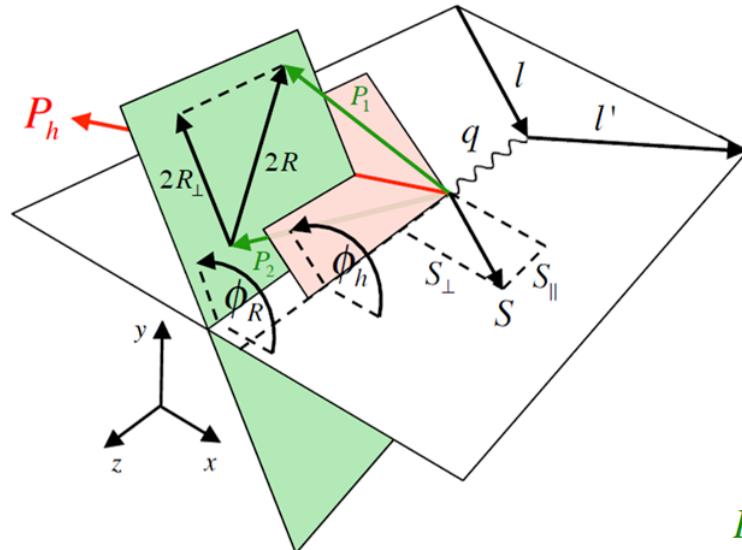
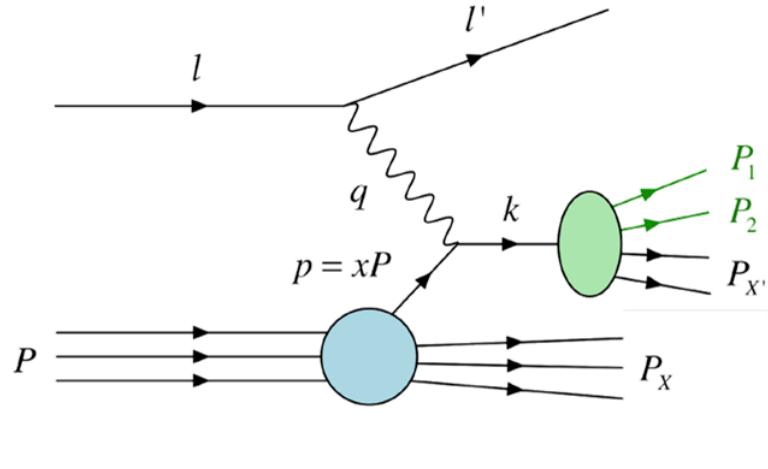
$$A_{UL}^{\sin 3\phi_h} \leftrightarrow A_{UT}^{\sin(3\phi_h - \phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

$$A_{LL}^{\cos 2\phi_h} \leftrightarrow A_{LT}^{\cos(2\phi_h - \phi_s)} \propto Q^{-1} (g_{1T}^q \otimes D_{1q}^h + \dots)$$

Theoretical Framework: Di-hadron SIDIS

$$\mu(l) + p(P) \rightarrow \mu(l') + h_1^+(P_1) + h_2^-(P_2) + X$$

Bacchetta & Radici: Phys. Rev. D69 094002
 Bacchetta & Radici & Gliske: Phys. Rev. D90 114027

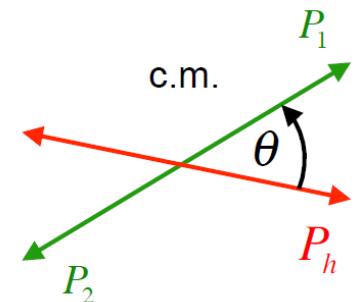


- X-section modulated in azimuthal angles ϕ_h and ϕ_R

$$\mathbf{R}_{\perp} \leftrightarrow \mathbf{R}_T = \frac{z_2 \mathbf{P}_{1\perp} - z_1 \mathbf{P}_{2\perp}}{z_1 + z_2} \quad \text{with} \quad z_i = \frac{E_i}{E - E'}$$

- Negligible transverse polarization mixing $S_{\perp} \approx 0$

- Partial wave expansion in θ , restricted to s- & p-waves



$$\langle \theta \rangle = \pi/2$$

θ is the emission angle between h^+ in the c.m. frame and the momentum of the di-hadron in the target rest frame



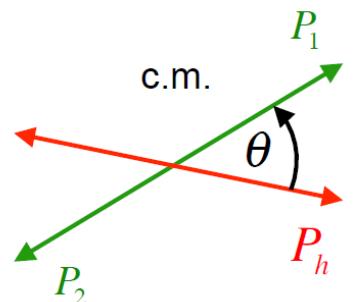
Theoretical Framework: Di-hadron SIDIS at twist-2

$$d\sigma = d\sigma_{UU} + \lambda d\sigma_{LU} + S_L (d\sigma_{UL} + \lambda d\sigma_{LL}) + S_L (d\sigma_{UT} + \lambda d\sigma_{LT})$$

Bacchetta & Radici: Phys. Rev. D69 094002

Bacchetta & Radici & Gliske: Phys. Rev. D90 114027

$$\begin{aligned}
 d\sigma_{UL} \propto & \sin(\phi_h - \phi_R) \left(A_{UL}^{\sin(\phi_h - \phi_R)\sin\theta} \sin\theta + A_{UL}^{\sin(\phi_h - \phi_R)\sin 2\theta} \sin 2\theta \right) \\
 & + \sin(2\phi_h - 2\phi_R) A_{UL}^{\sin(2\phi_h - 2\phi_R)\sin^2\theta} \sin^2\theta \\
 & + \varepsilon \left\{ \sin(2\phi_h) \left(A_{UL}^{\sin(2\phi_h)} + A_{UL}^{\sin(2\phi_h)\cos\theta} \cos\theta + A_{UL}^{\sin(2\phi_h)\frac{1}{3}(3\cos^2\theta-1)} \frac{1}{3}(3\cos^2\theta-1) \right) \right. \\
 & + \sin(\phi_h + \phi_R) \left(A_{UL}^{\sin(\phi_h + \phi_R)\sin\theta} \sin\theta + A_{UL}^{\sin(\phi_h + \phi_R)\sin 2\theta} \sin 2\theta \right) \\
 & + \sin(2\phi_R) A_{UL}^{\sin(2\phi_R)\sin^2\theta} \sin^2\theta \\
 & + \sin(3\phi_h - \phi_R) \left(A_{UL}^{\sin(3\phi_h - \phi_R)\sin\theta} \sin\theta + A_{UL}^{\sin(3\phi_h - \phi_R)\sin 2\theta} \sin 2\theta \right) \\
 & \left. + \sin(4\phi_h - 2\phi_R) A_{UL}^{\sin(4\phi_h - 2\phi_R)\sin^2\theta} \sin^2\theta \right\} \\
 d\sigma_{LL} \propto & \sqrt{1-\varepsilon^2} \left\{ A_{LL}^1 + A_{LL}^{\cos\theta} \cos\theta + A_{LL}^{\frac{1}{3}(3\cos^2\theta-1)} \frac{1}{3}(3\cos^2\theta-1) \right. \\
 & + \cos(\phi_h - \phi_R) \left(A_{LL}^{\cos(\phi_h - \phi_R)\sin\theta} \sin\theta + A_{LL}^{\cos(\phi_h - \phi_R)\sin 2\theta} \sin 2\theta \right) \\
 & \left. + \cos(2\phi_h - 2\phi_R) A_{LL}^{\cos(2\phi_h - 2\phi_R)} \right\}
 \end{aligned}$$

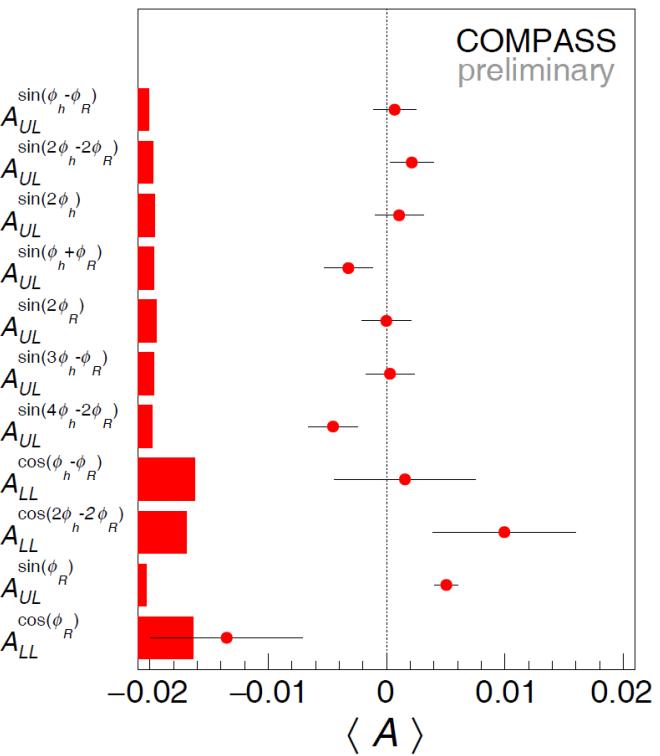
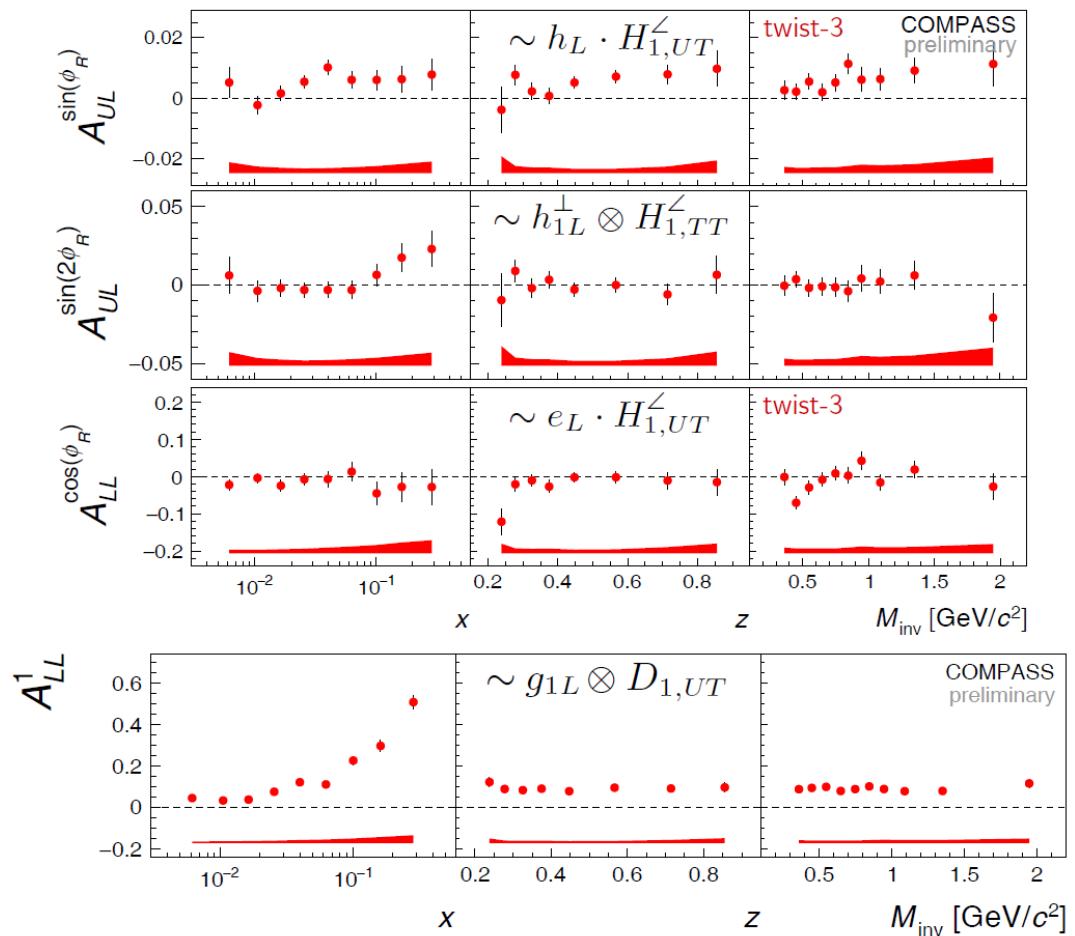


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θ is the emission angle between h^+ in the c.m. frame and the momentum of the di-hadron in the target rest frame

Selected results for di-hadron asymmetries

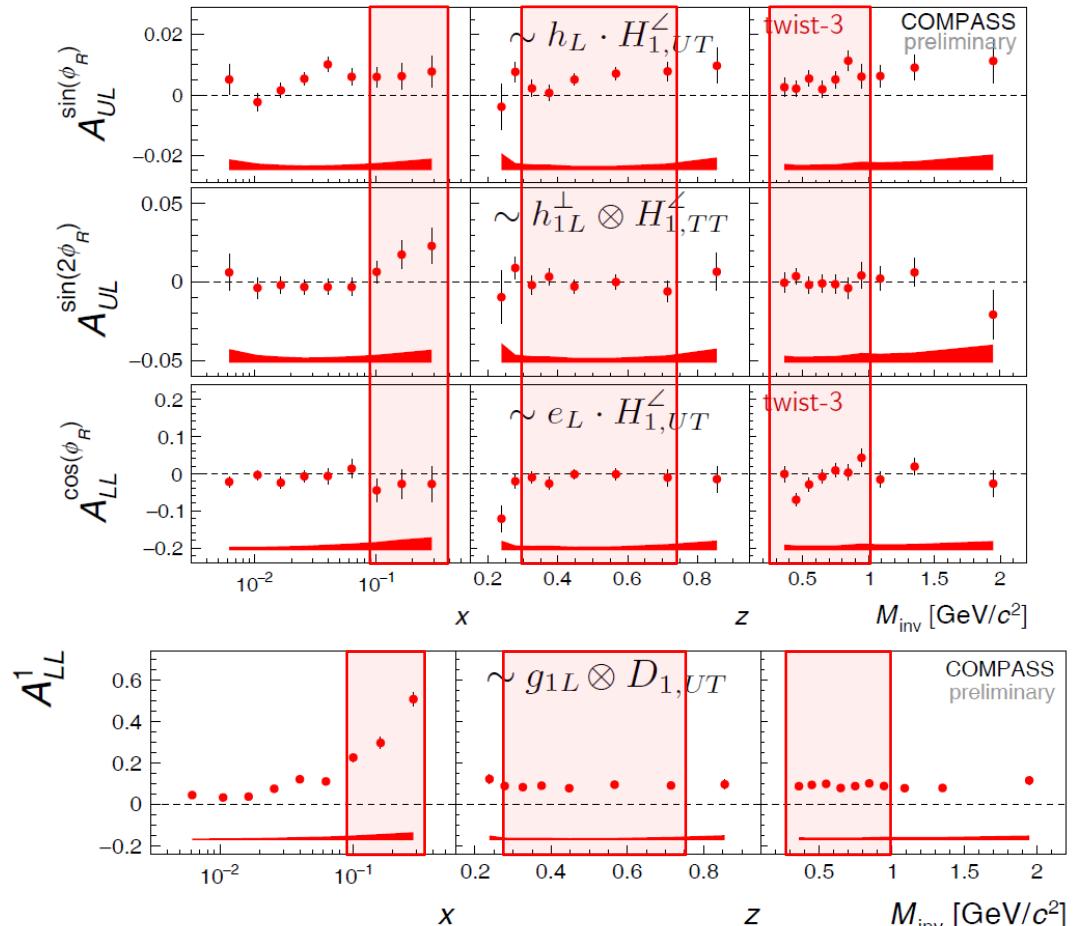
COMPASS (NH₃) 2007+2011 data: preliminary



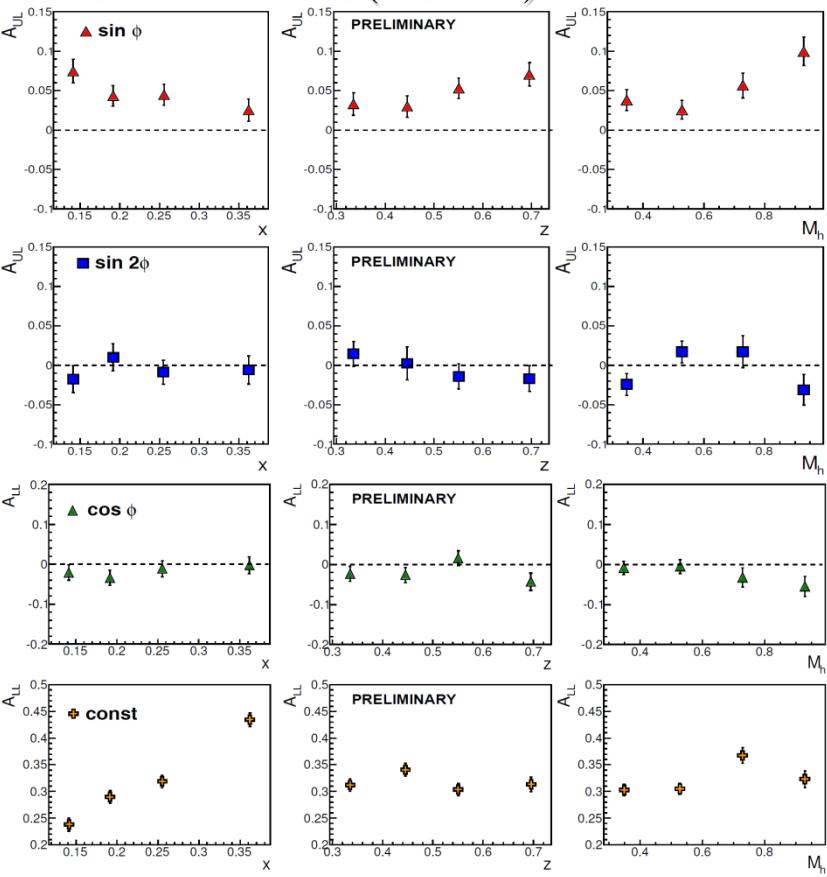
- Alternative way to access various twist-2/-3 distributions
- Non zero signal for $A_{UL}^{sin\phi_R}$ and A_{LL}^1

Selected results for di-hadron LSAs

COMPASS (NH₃) 2007+2011 data: preliminary

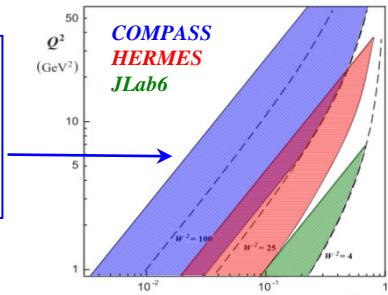


CLAS 6 GeV (NH₃)
S. A. Pereira: PoS (DIS 2014) 231



- Alternative way to access various twist-2/-3 distributions
- Non zero signal for $A_{UL}^{\sin\phi_R}$ and A_{LL}^1
- CLAS-COMPASS: different behavior for $A_{UL}^{\sin 2\phi_R}$ at large x?

$Q^2 > 1 (\text{GeV}/c)^2$
 $0.0025 < x < 0.7$
 $0.1 < y < 0.9$
 $W > 5 \text{ GeV}/c^2$

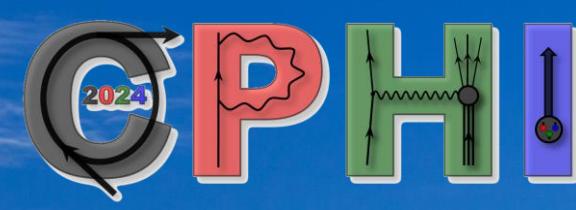




Conclusions

- COMPASS has measured all possible single-/di-hadron SIDIS LSAs from combined deuteron 2002-2006 and proton 2007/2011 data sample
- Together with existing measurements of proton TSAs these results complete the whole set of all possible proton SIDIS spin dependent azimuthal asymmetries
- This allowed us to evaluate the mixing between SIDIS LSAs and TSAs arising from the difference of target polarization components in lp and $\gamma*p$ systems
- Whereas azimuthal LSAs on deuteron appear to be compatible with zero, for some of the proton LSAs non-zero signals are observed
- A clear effect was observed for $A_{UL}^{sin\phi_h}$ with positive hadrons, while for negative hadrons the asymmetry is found to be compatible with zero
 - in agreement with HERMES observations
- The $A_{UL}^{sin2\phi_h}$ appear to exhibit opposite sign “Collins-like” behavior for h^+ and h^-
 - in agreement with model predictions
 - possible positive signal for negative hadrons appears to contradict HERMES and Jlab observations
- The $A_{LL}^{cos\phi_h}$ asymmetry is found to be small and compatible with zero within statistical accuracy which does not contradict available model predictions
- Non-zero signal was observed for $A_{UL}^{sin\phi_R}$ and A_{LL}^1 di-hadron asymmetries related to h_L and g_{1L} PDFs, correspondingly.

Thank you!



Joint XX-th International Workshop on *COMPASS* Hadron Structure and Spectroscopy



and 5-th Workshop on Correlations in
Partonic and Hadronic Interactions

<https://indico.cern.ch/e/IWHSS-CPHI-2024>

Yerevan, Armenia

30 September – 4 October, 2024

