

# Proton Radius measurements at MAMI/MESA

Miha Mihovilovic for A1 Collaboration  
U Ljubljana and JSI

# Laurel and Hardy dilemma?!

---

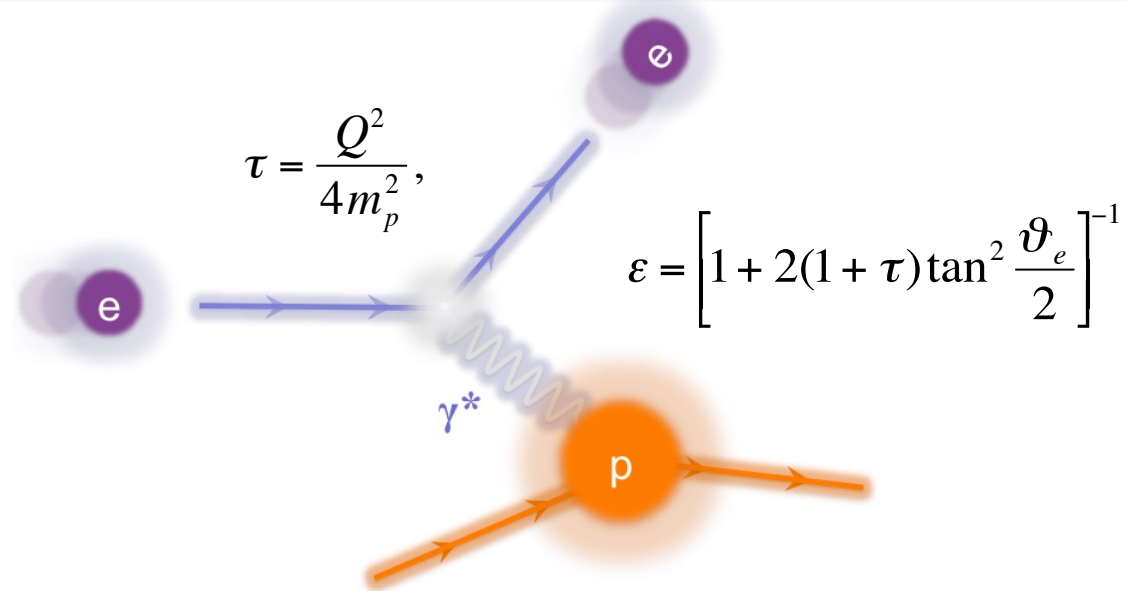


0.84 fm ?



0.88 fm ?

# Radius via Cross-section measurement

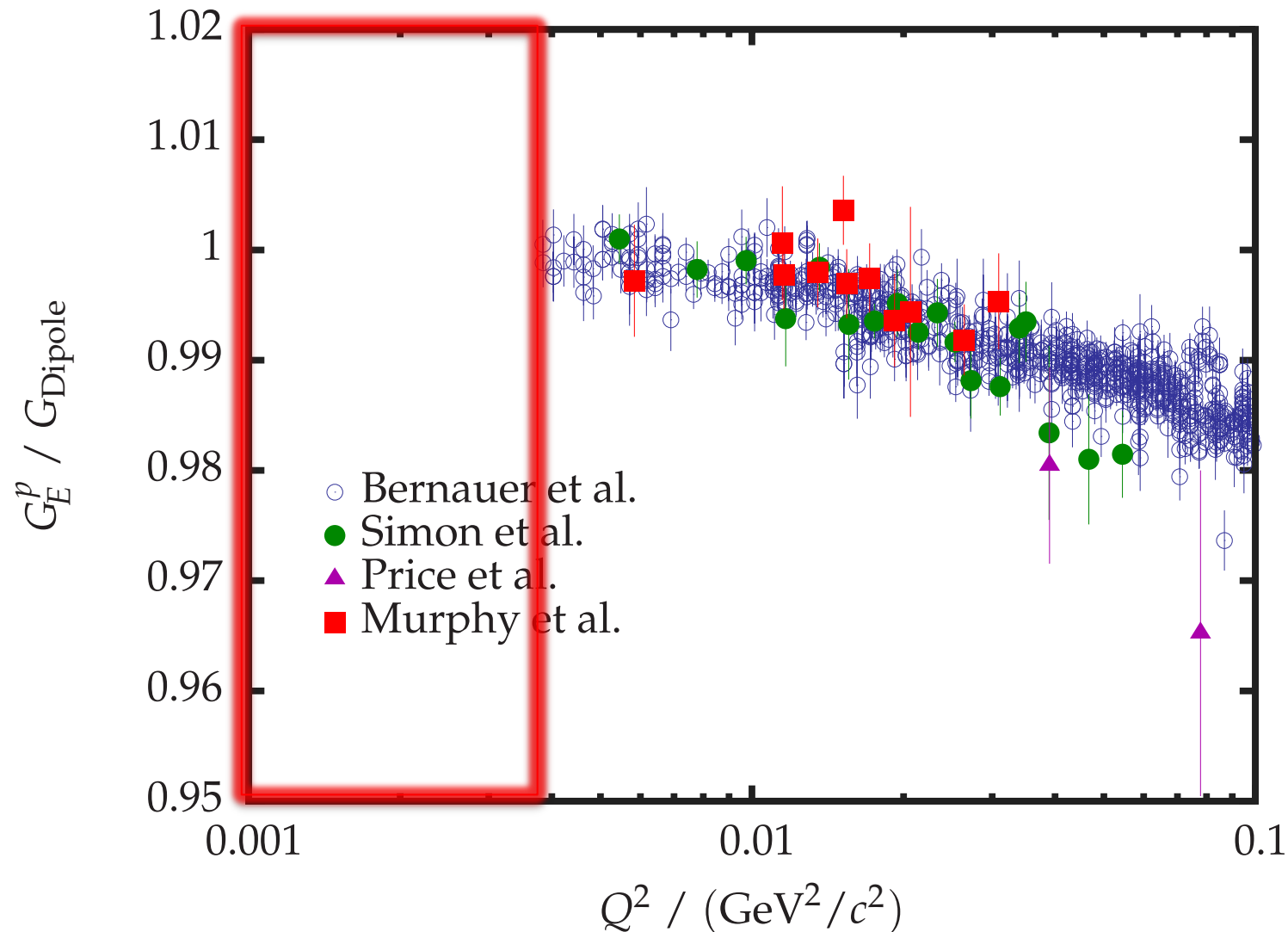


$$\frac{d\sigma}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_{Mott} \frac{1}{1 + \tau} \left[ G_E^2(Q^2) + \frac{\tau}{\epsilon} G_M^2(Q^2) \right]$$

- Extraction of FF via Rosenbluth Separation.
- Best estimate for radius:

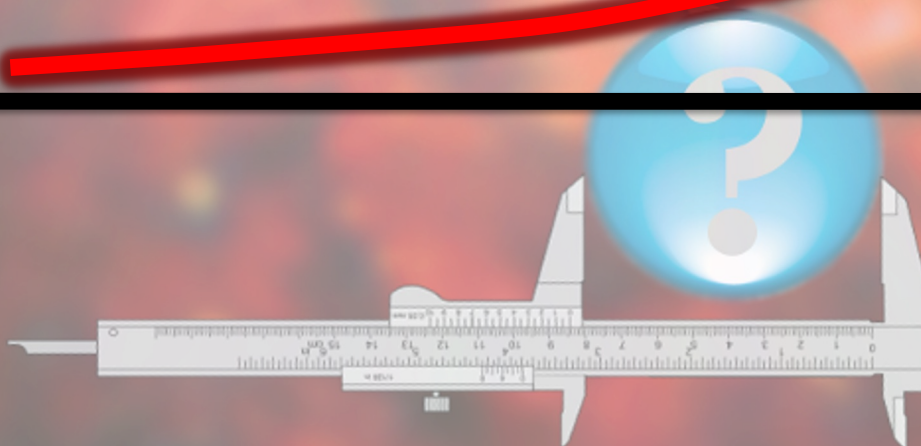
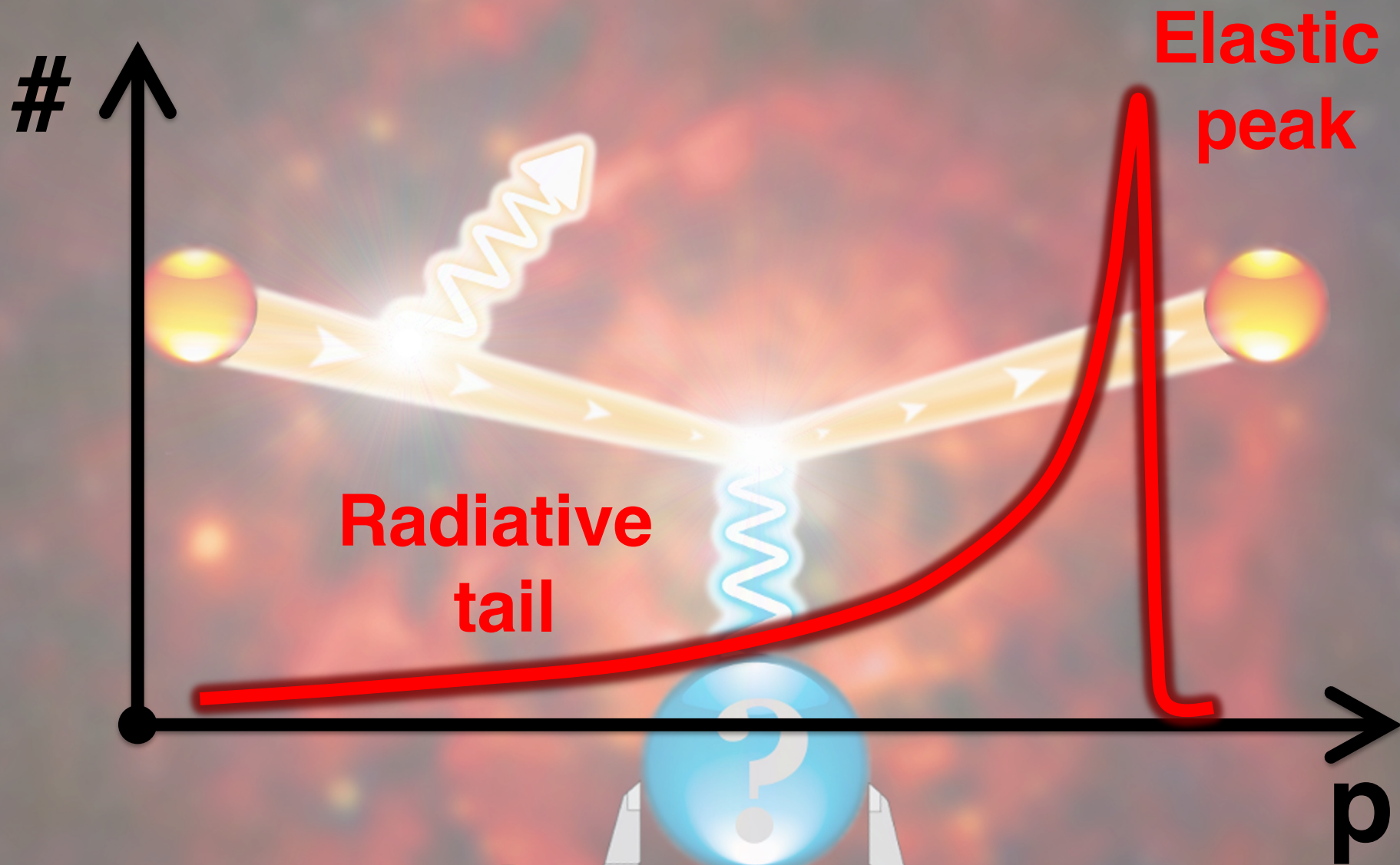
$$r_E^2 = -6\hbar^2 \left. \frac{d}{dQ^2} G_E(Q^2) \right|_{Q^2=0}$$

# Proton's charge form-factor



- **Data available only for  $Q^2 > 0.004 \text{ (GeV/c)}^2$ .**
- **Extrapolations to zero are needed!**

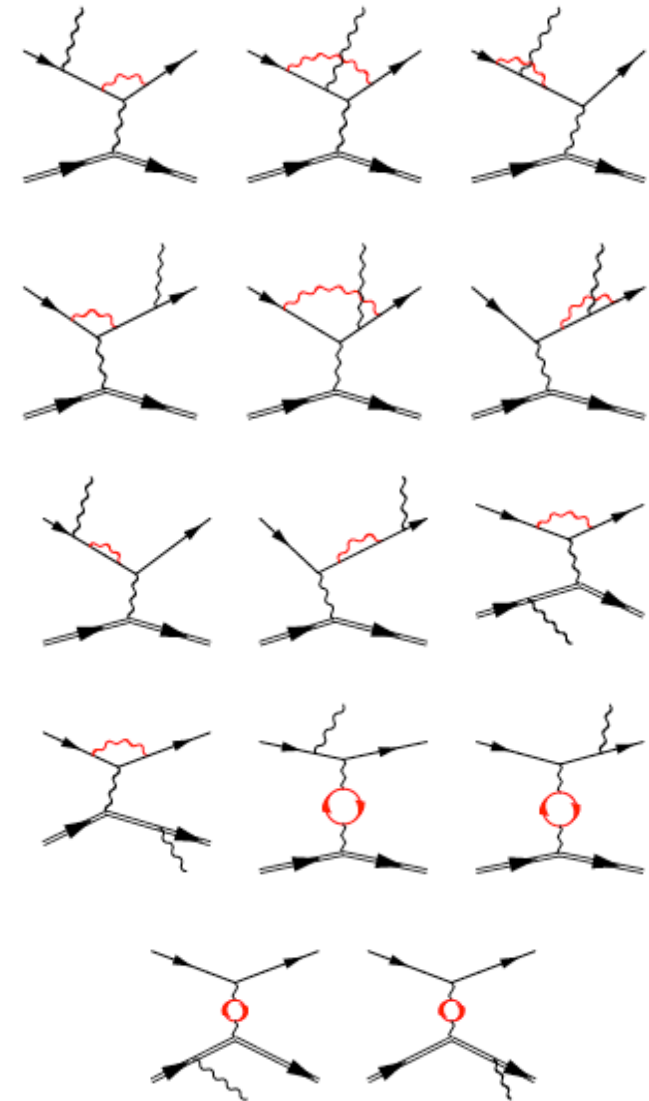
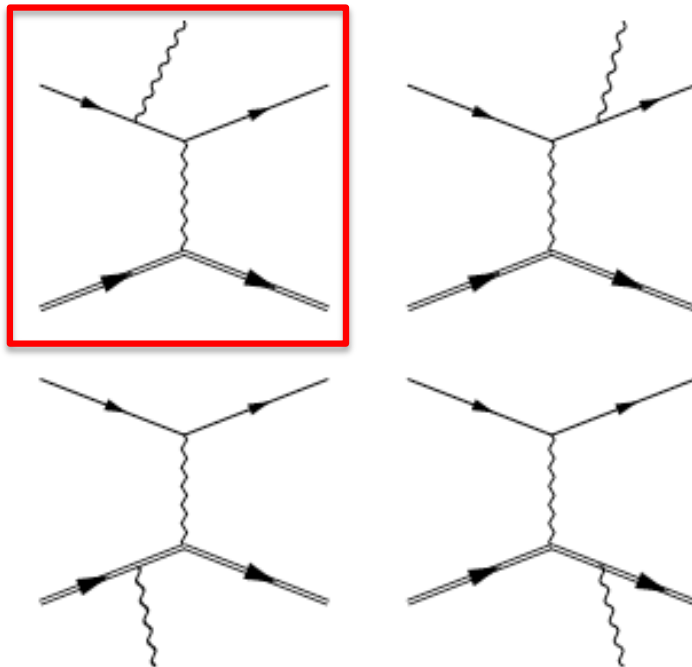
# The idea of ISR Experiment



# The ISR Simulation

- Based on standard A1 framework.
- Detailed description of apparatus.
- Exact calculation of the leading order diagrams:

ISR



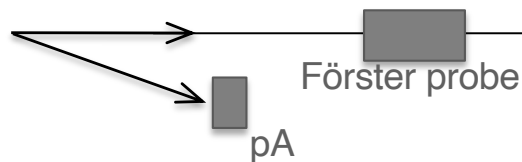
- The NL-order **virtual and real** corrections included via effective corrections to the cross-section.

# The ISR experiment

- Full experiment done in August 2013 + additional beam time in 2017.

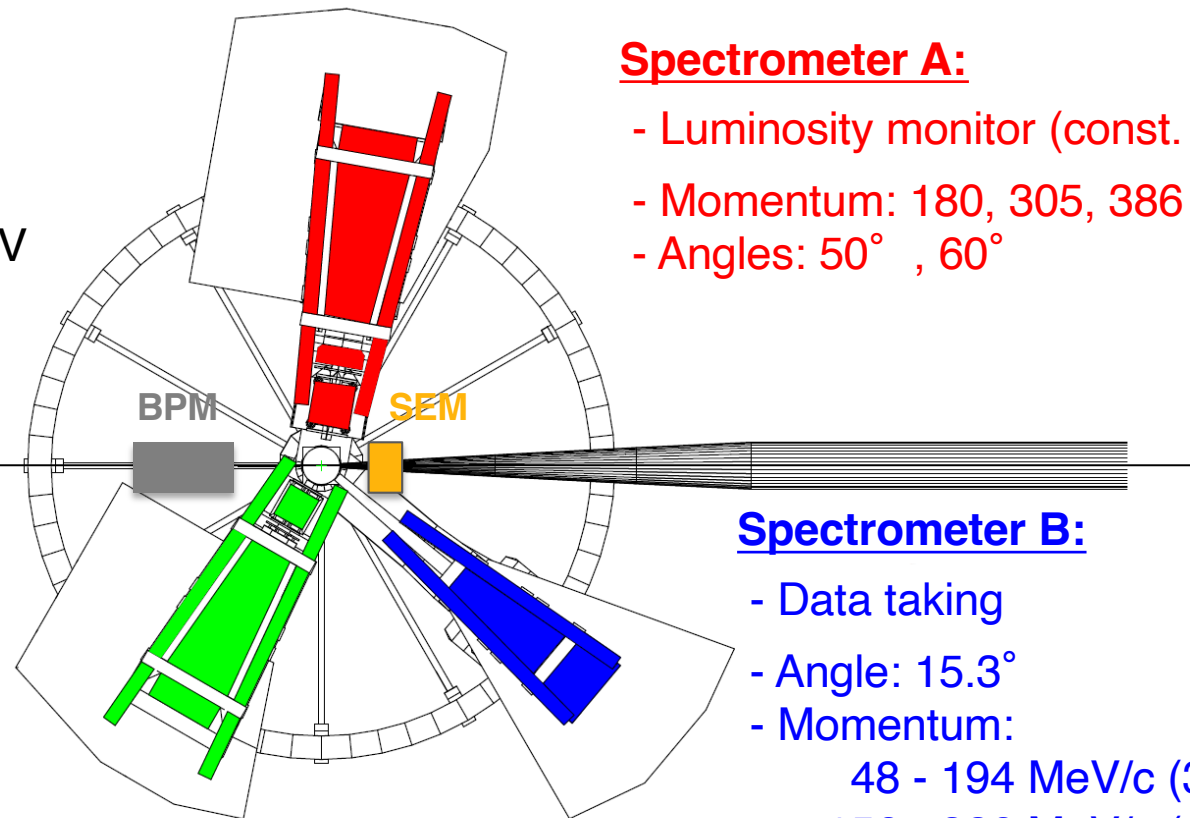
## Electron Beam:

- Energy: 195, 330, 495 MeV
- Current: 10nA – 1 $\mu$ A
- Rastered beam



## Luminosity monitors:

- pA-meter
- Förster probe
- **SEM**



## Spectrometer A:

- Luminosity monitor (const. setting)
- Momentum: 180, 305, 386 MeV/c
- Angles: 50° , 60°

## Spectrometer B:

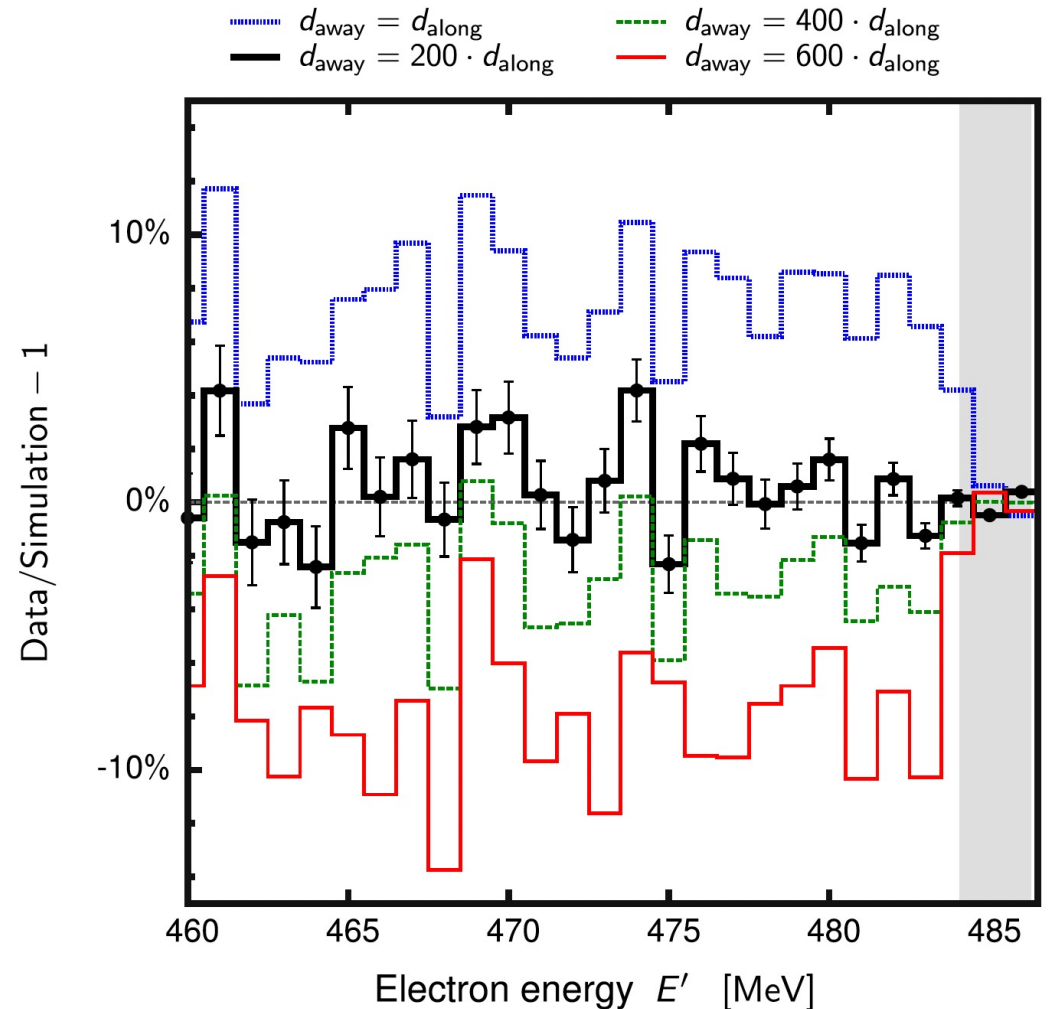
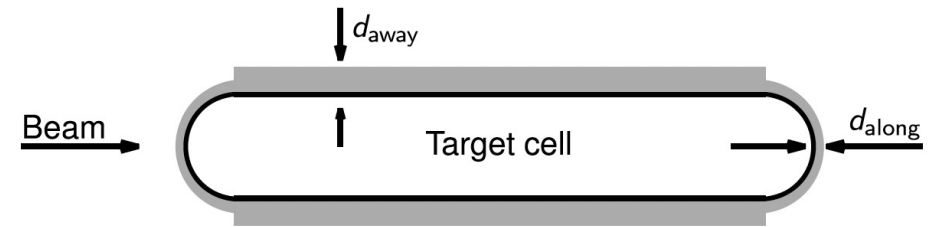
- Data taking
- Angle: 15.3°
- Momentum:
  - 48 - 194 MeV/c (35 setups)
  - 156 - 326 MeV/c (12 setups)
  - 289 - 486 MeV/c (9 setups)

## Spectrometer C:

- Not used

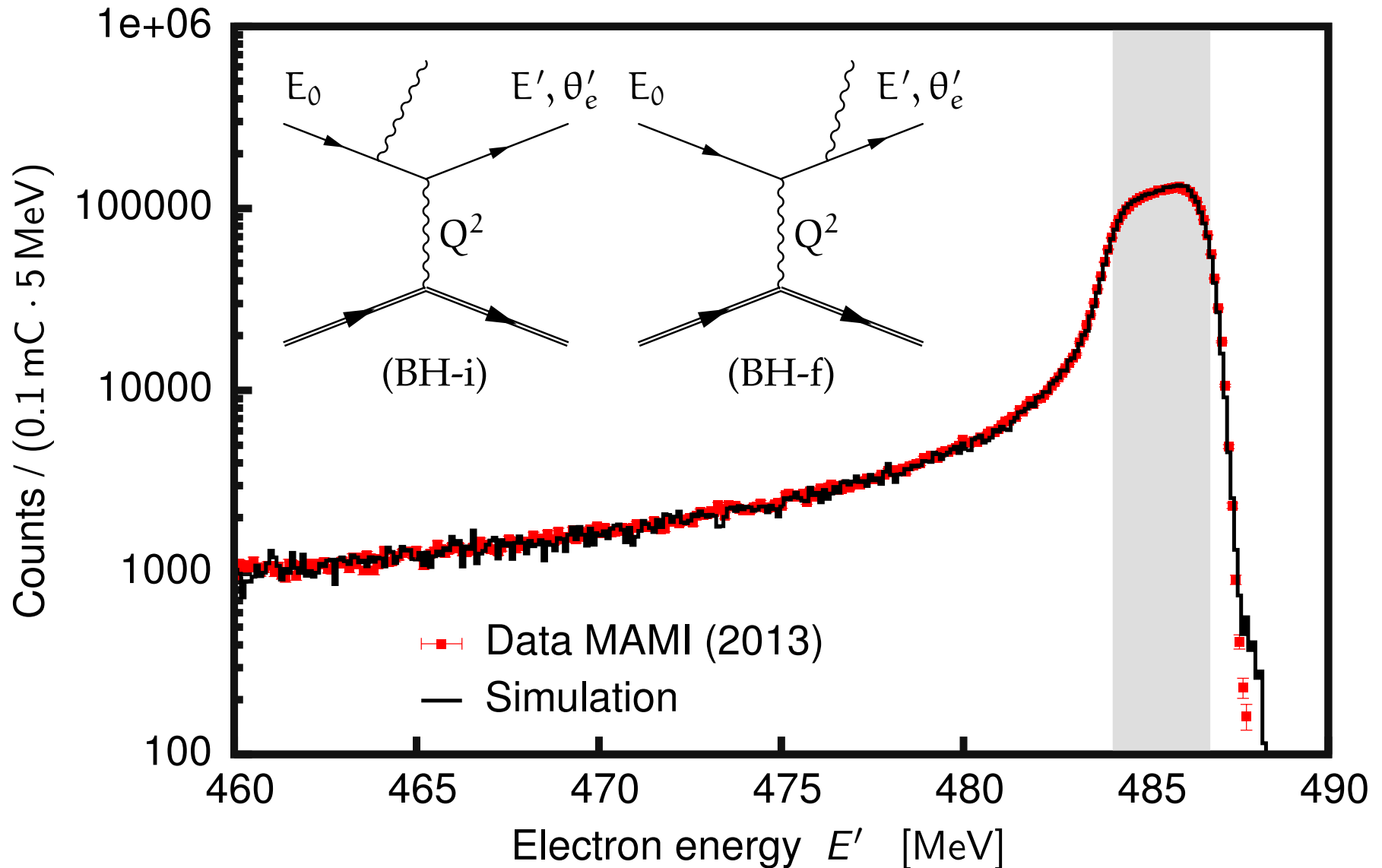
# Shortcomings of Cryogenic target

- Employed an extended cryogenic target.
- Backgrounds from target walls and supporting frame.
- Spectra distorted due to cryogenic depositions on the walls.
- Cryogenic layer on the sides much thicker than in the beam direction. Huge effect on the elastic data! **No control over the thickness of the layer.**





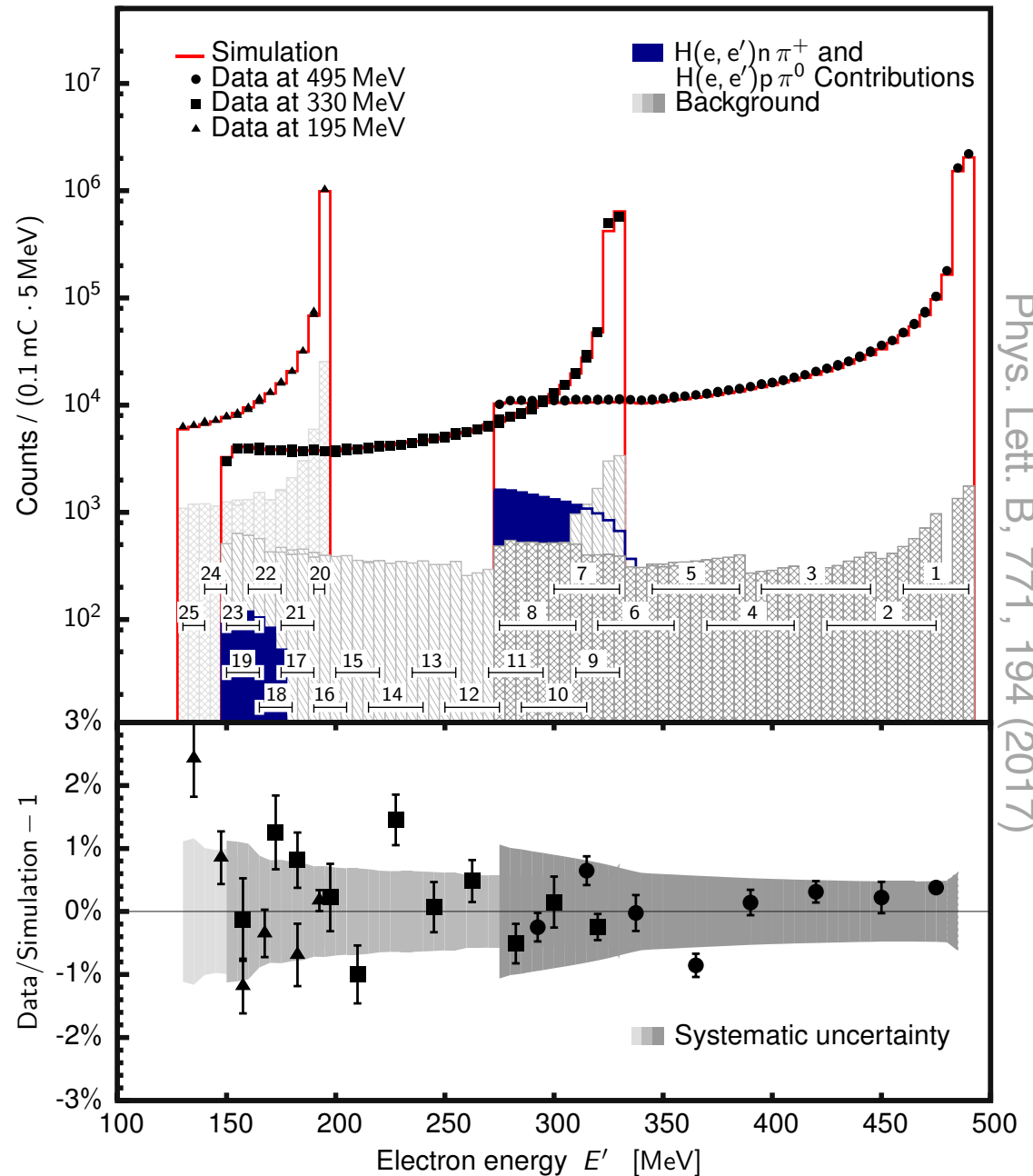
# The shape of the elastic peak



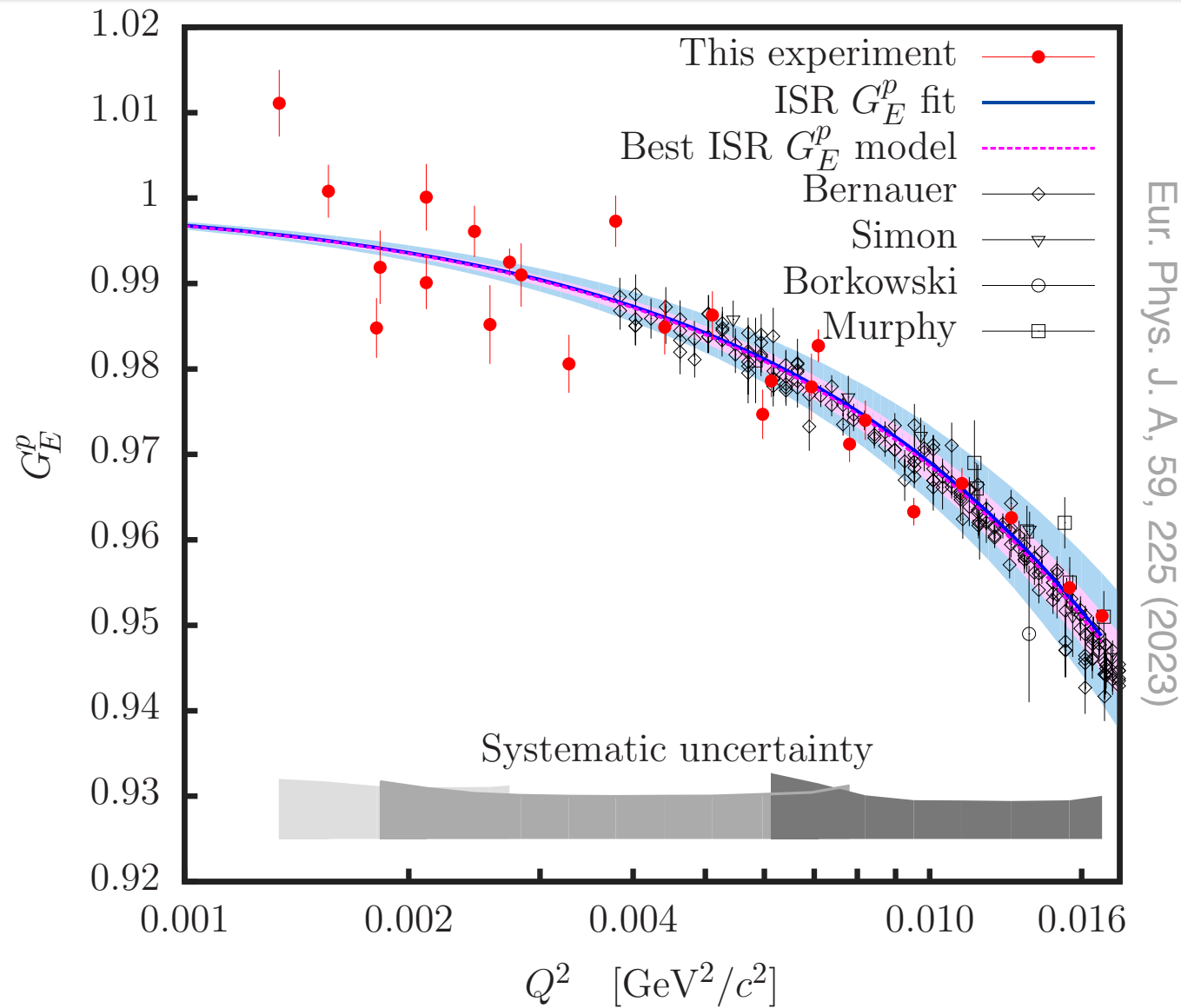
- This effects are important for all high precision experiments using cryogenic target.

# Results

- Existing apparatus limited reach of ISR experiment to  $E' \sim 130$  MeV.
- Elastic points included.
- Simulation performed with Bernauer parameterization of form factors.
- A percent agreement between the data and simulation demonstrates that the radiative corrections are well understood!



# ISR form-factors

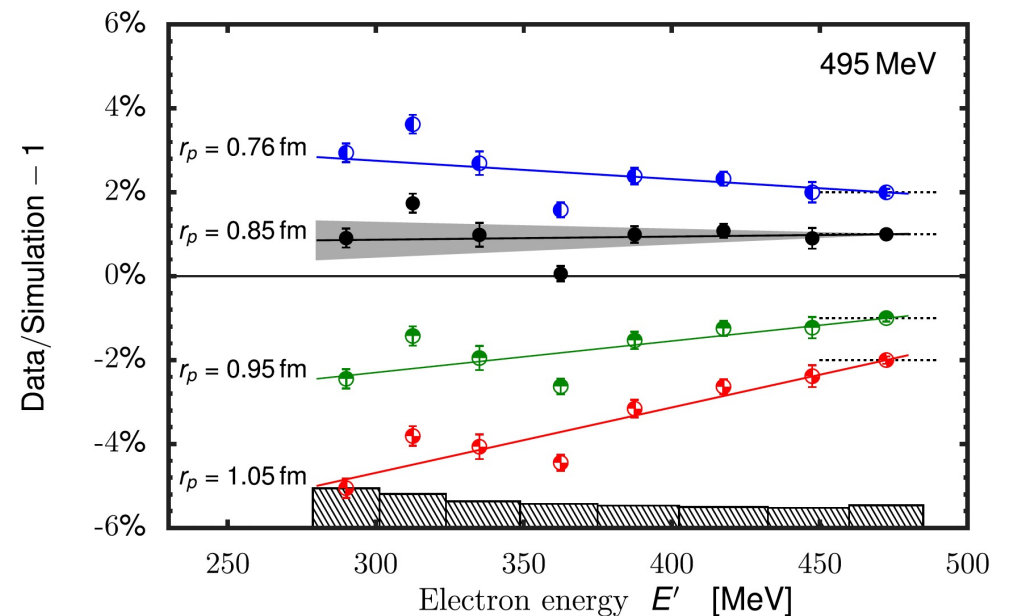
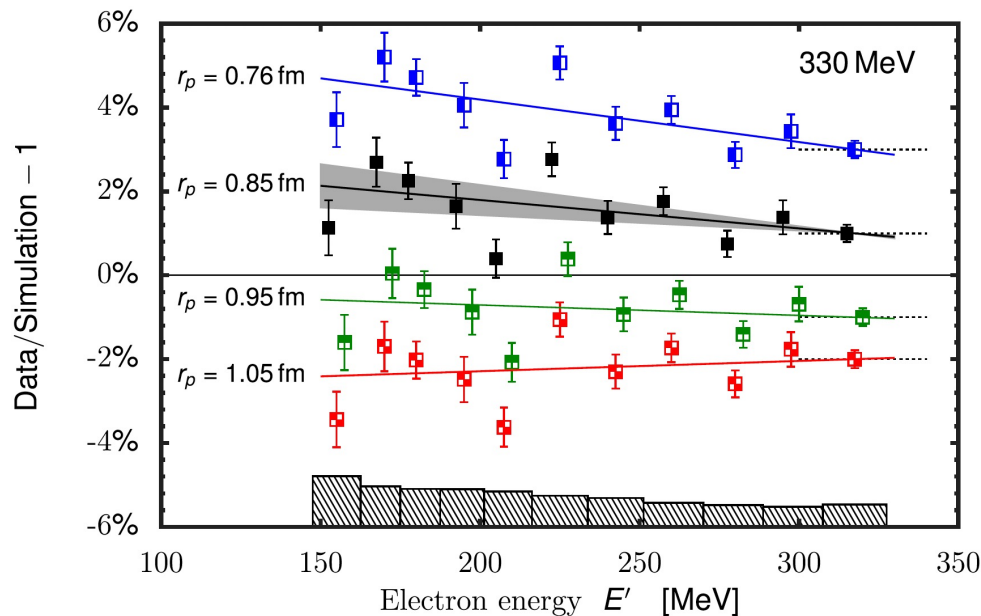


- Form-factors extracted from deviations of the measurements from the Bernauer model, assuming flawless description of radiative corrections.

# Analysis of cross-sections

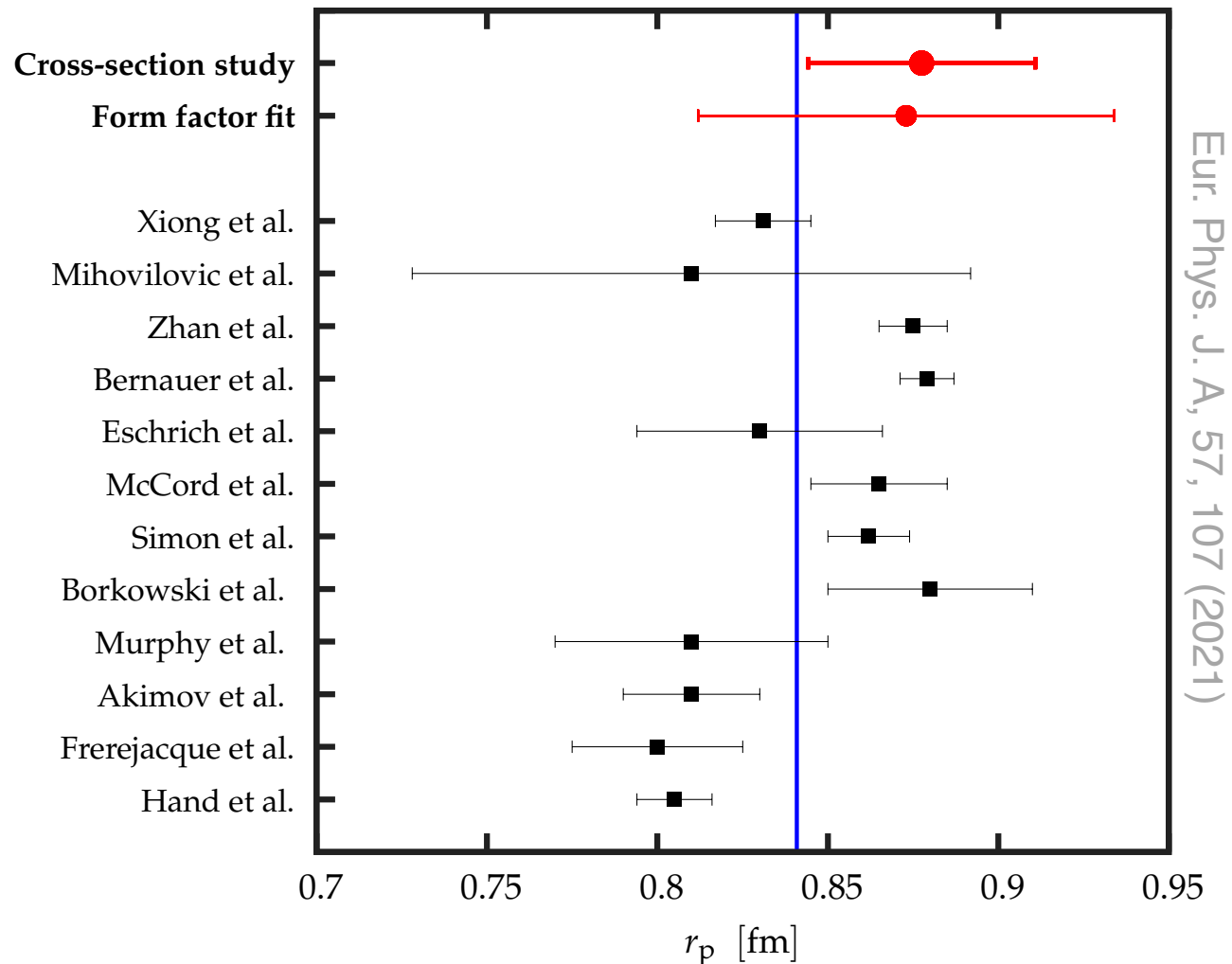
- Determination of the radius directly from the measured cross-sections.
- Small-energy data less sensitive to radius. 195 MeV data excluded.
- Analysis based on a specific form factor model.

$$G_E^p(Q^2) = n \left( 1 - \frac{\mathbf{r}_E^2}{6} Q^2 + \frac{a}{120} Q^4 - \frac{b}{5040} Q^6 \right)$$

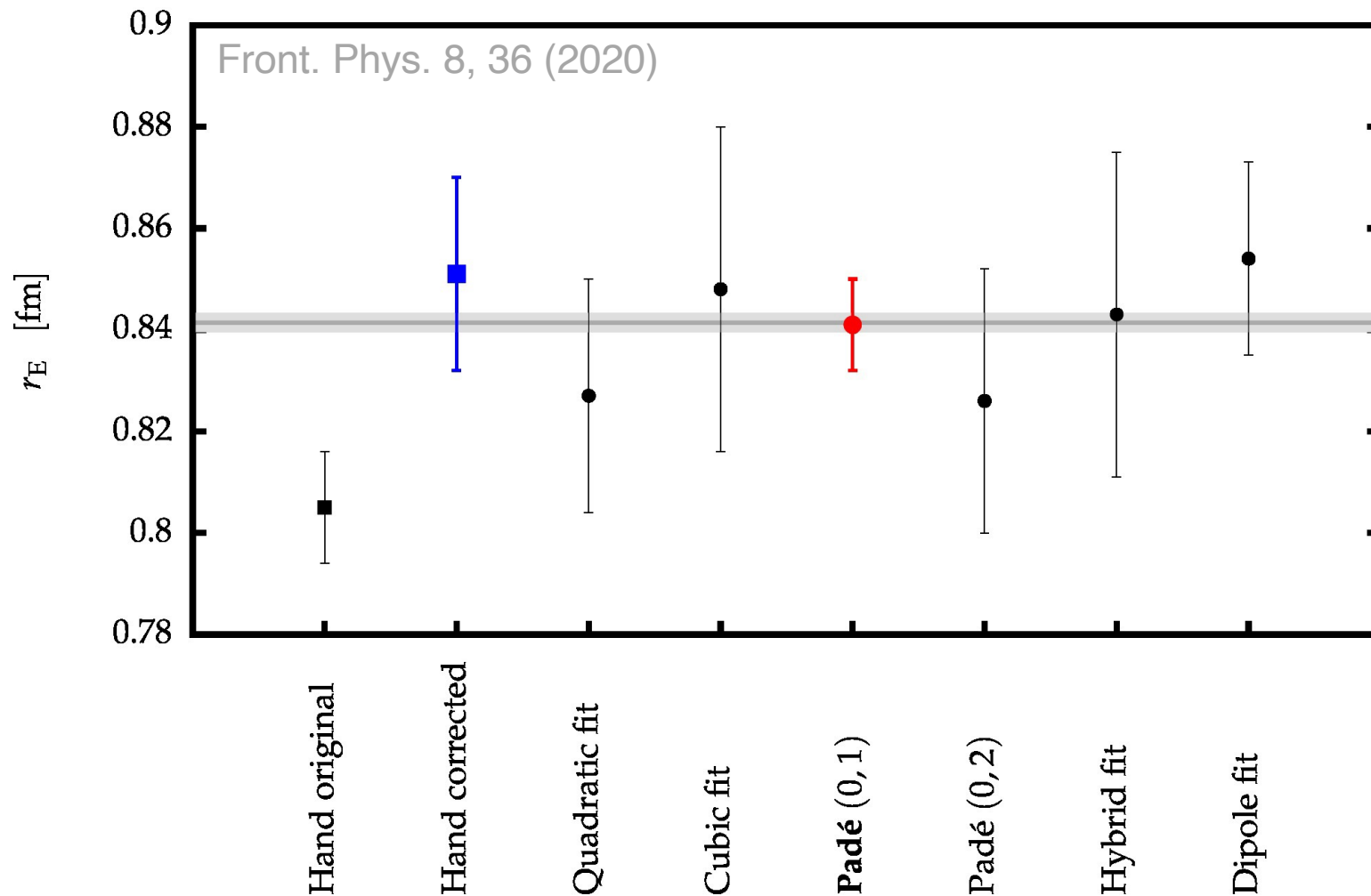


# The result of the ISR experiment

- The values from the direct analysis of cross-sections and fit of extracted form-factor.
- Uncertainty combines statistical and systematic uncertainty.

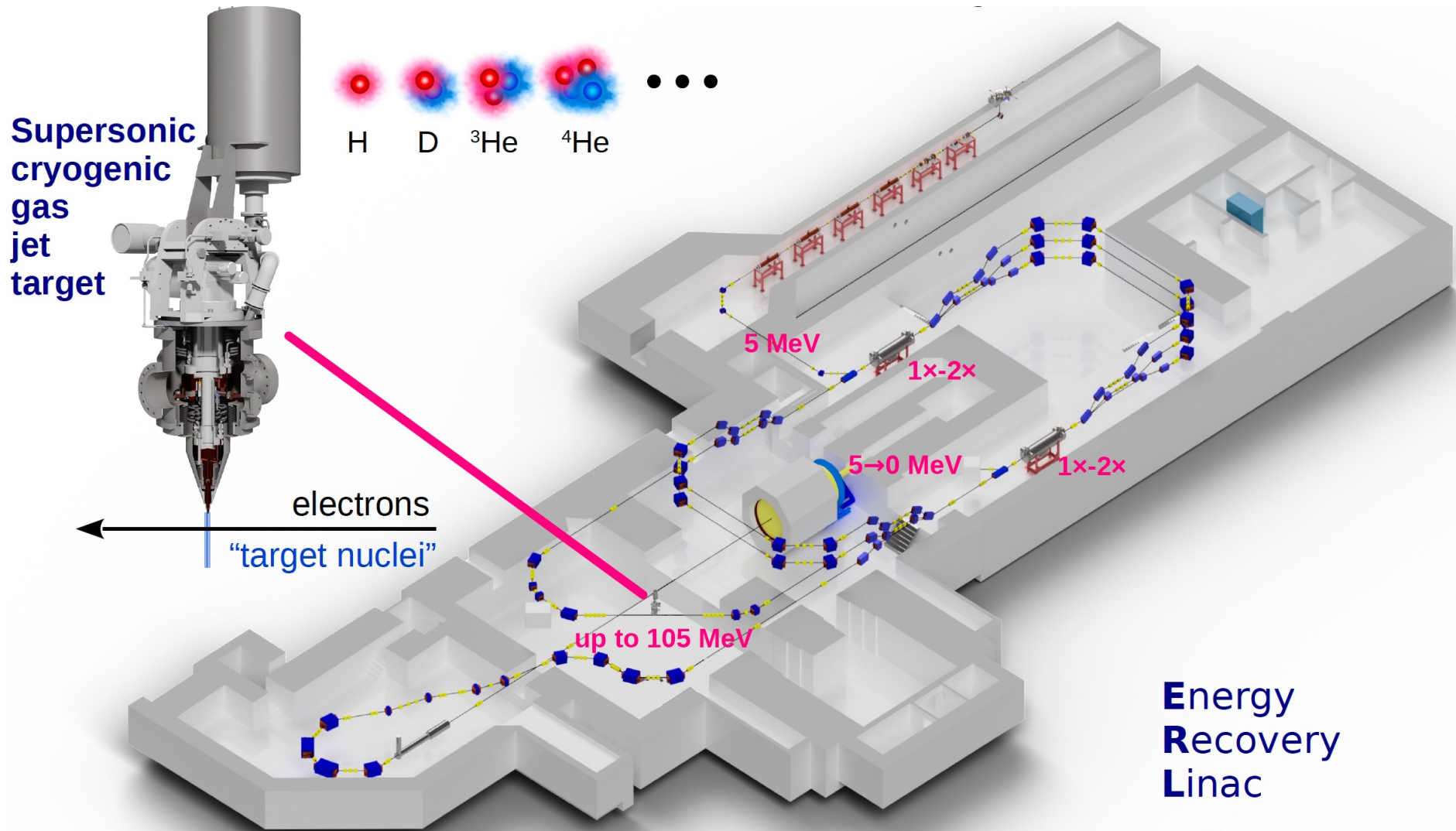


# Reinterpretation of first measurements



- Mistake in an analysis led Hand to too small value for the radius.
- Reanalysis of original measurements give results consistent with CODATA '18.

# Magix @ MESA

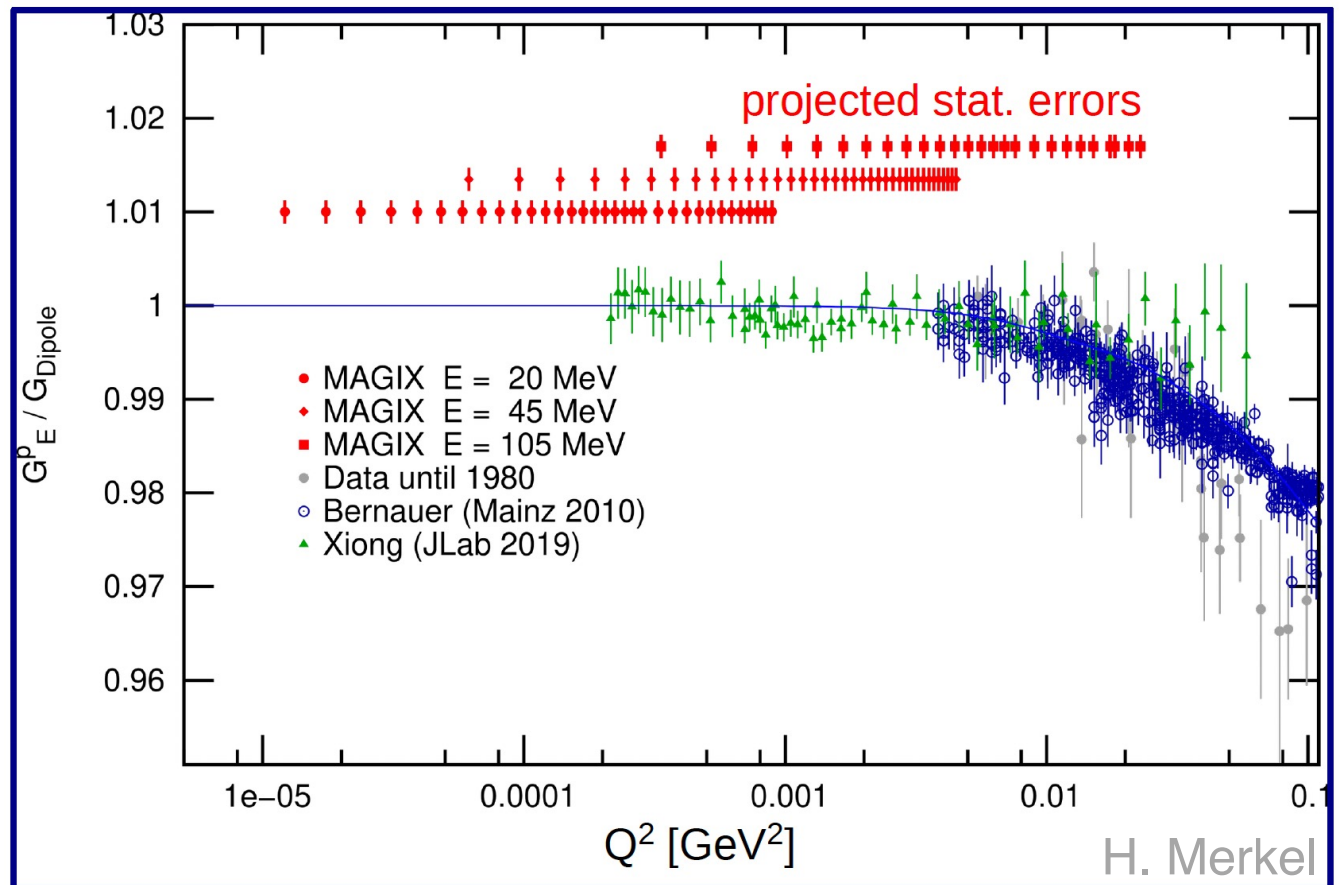


P2/DM-EB mode:	~155 MeV,	150 $\mu$ A
MX-EB mode:	20-105 MeV,	< 150 $\mu$ A
ERL mode:	30-105 MeV,	10000 $\mu$ A

# Radius measurements @ Magix

- Persistent discrepancy between different determinations of the proton radius persists demands further measurements.
- New measurement planned also at Magix @ MESA
- Measurement of  $G_E^p$  at  $Q^2$  between  $1 \cdot 10^{-5}$  and  $0.03 \text{ GeV}^2$

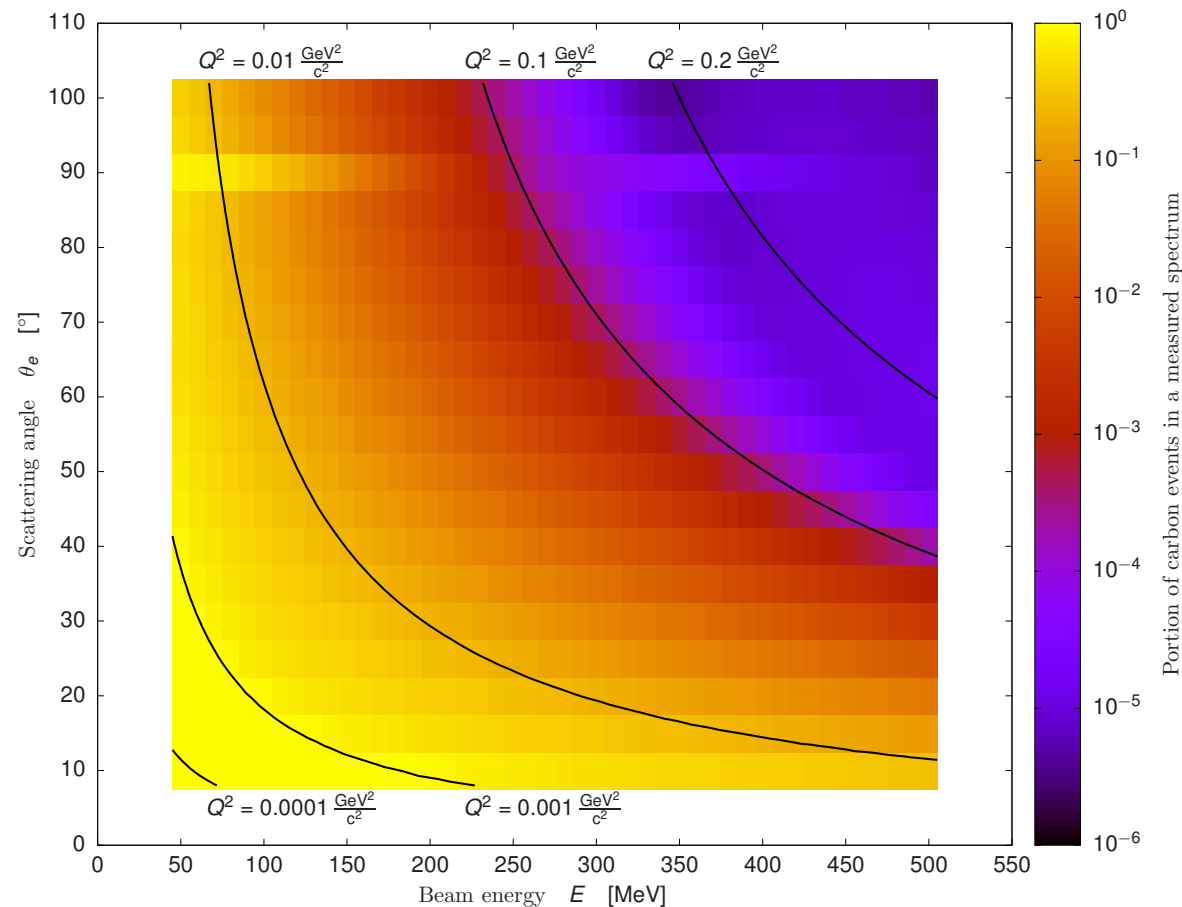
- Expected statistical uncertainty  $\sim 0.1 \%$ .
- Expected systematical uncertainty  $< 0.5 \%$ .
- Measurement of  $G_M^p$  using double-polarized experiments.





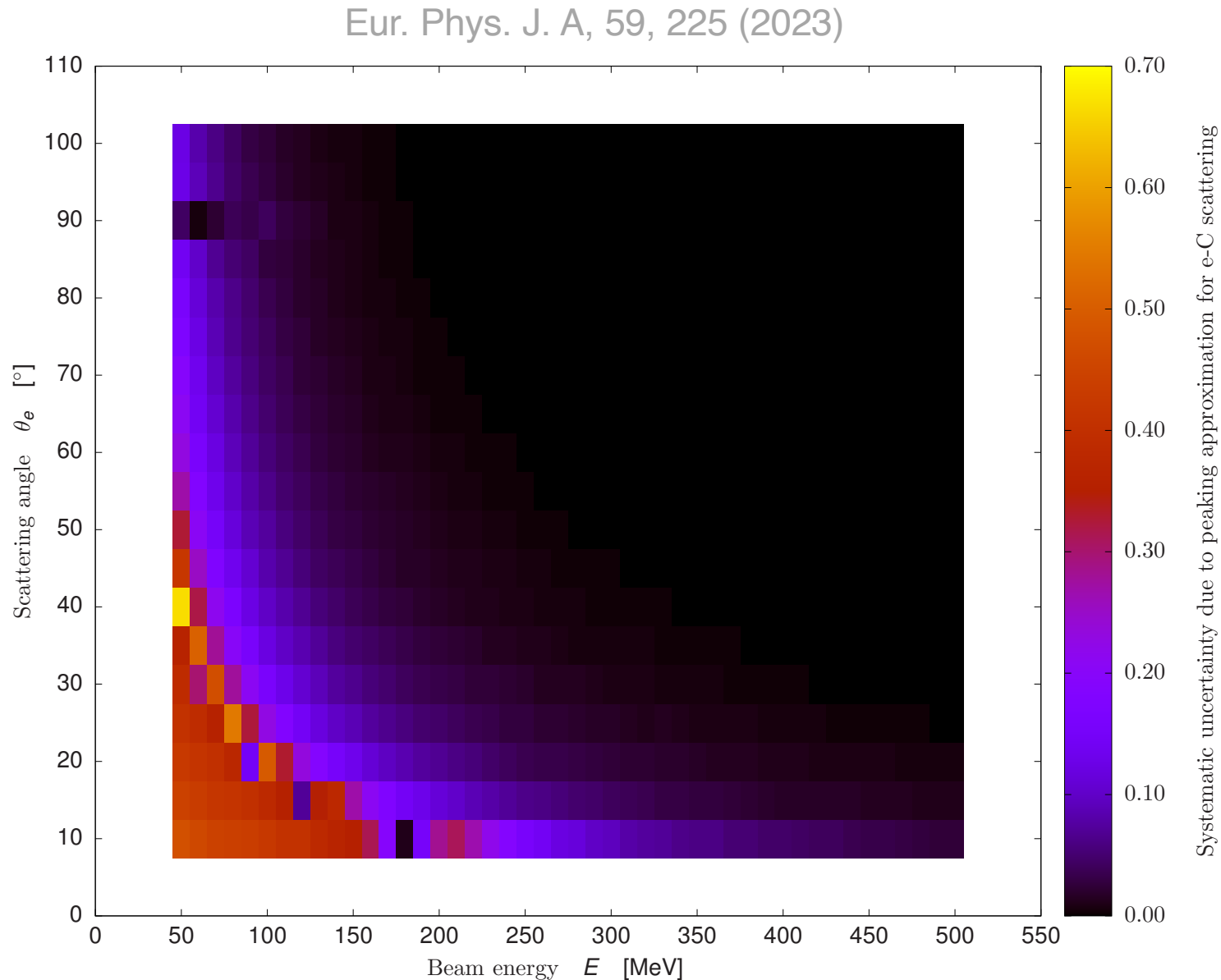
# Potential experiments with plastic targets

- Uncertainty of experiments dominated by the target-related systematics.
- Desired target is **thin** with **known and constant density** and **background**, that can be clearly **subtracted**.
- Plastic (-CH<sub>2</sub>-) target an effective hydrogen target with carbon background.

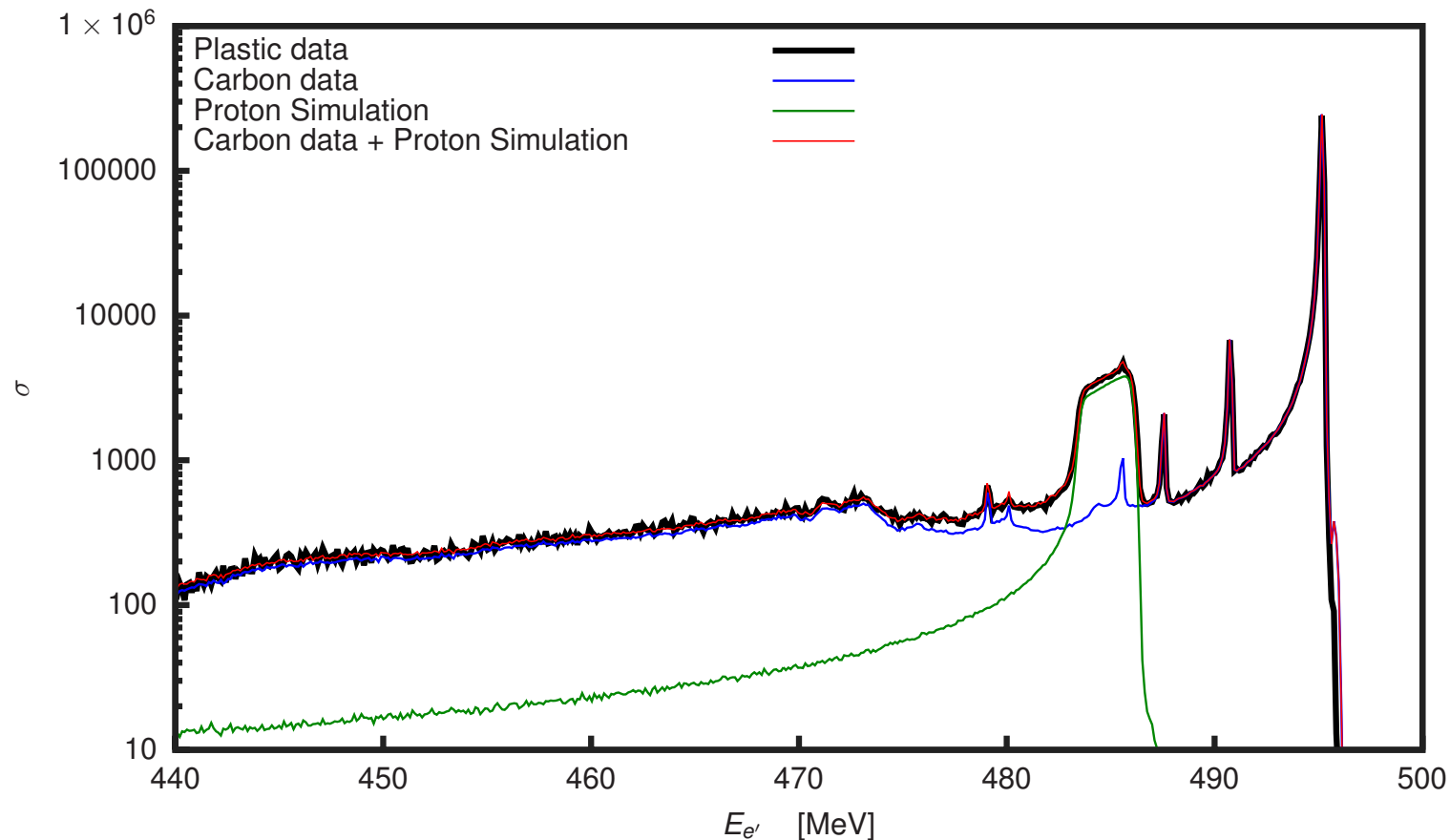


# Findings of tests with plastic target

- Peaking approximations **insufficient** for describing carbon background.



# Findings of tests with plastic target



- Peaking approximations insufficient for describing carbon background.
- Measurements with thin carbon targets are necessary due to the presence of inelastic contributions for adequate background description.
- External radiative corrections need to be applied to match plastic spectra.

# Summary

---

- The ISR experiment used a new experimental technique for determination of the proton form-factors at very small  $Q^2$ .
- **Validated radiative corrections far away from elastic settings.**
- Experimental result dominated by the systematic uncertainties arising from the use of  $\text{LH}_2$  target.
- Extracted  $G_E^p$  at very low  $Q^2$  and the charge radius, but with the limited precision.
- Further measurements with thin windowless targets are needed – **Magix experiment with Hypersonic gas jet target!**
- **Plastic targets are also an option.**
- **Find consensus on how to fit / interpret the nuclear scattering data.**

**Thank you!**