

Strange hadrons spectroscopy at LHCb

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University of Milano Bicocca and INFN



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Château de Bossey, 19.03.2024

Outline

The LHCb Experiment

Strange Hadrons at LHCb

Recent Results

- Amplitude analysis of $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$ decays ([JHEP 02 \(2019\) 126](#))
- Studies of the resonance structure in $D^0 \rightarrow K^\mp \pi^\pm \pi^\pm \pi^\mp$ decays ([Eur. Phys. J. C78 \(2018\) 443](#))
- Study of charmonium decays to $K^0_s K \pi$ in the $B \rightarrow (K^0_s K \pi) K$ channels ([Phys. Rev. D 108, 032010 \(2023\)](#))

Summary



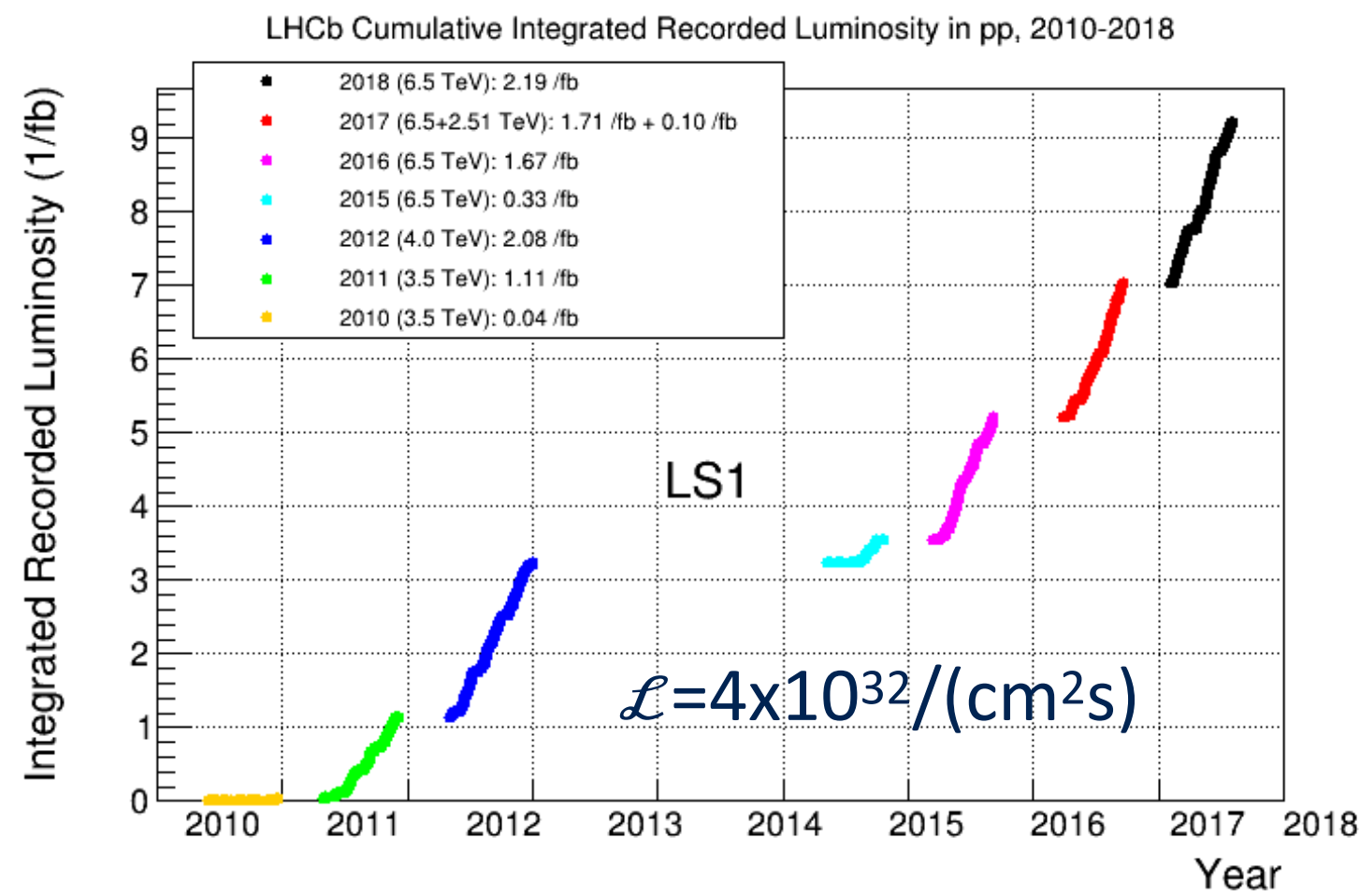
The LHCb Experiment



The LHCb Experiment

JINST 3 (2008) S08005

Charm quarks produced in high η at LHC
 $\sigma(pp \rightarrow c\bar{c}) \sim 20\sigma(pp \rightarrow b\bar{b})$



$\epsilon_{\text{VELO}} \approx 98\%$

$\delta t/t = 45 \text{fs}$

$\sigma(\text{IP}) \approx 20 \mu\text{m}$

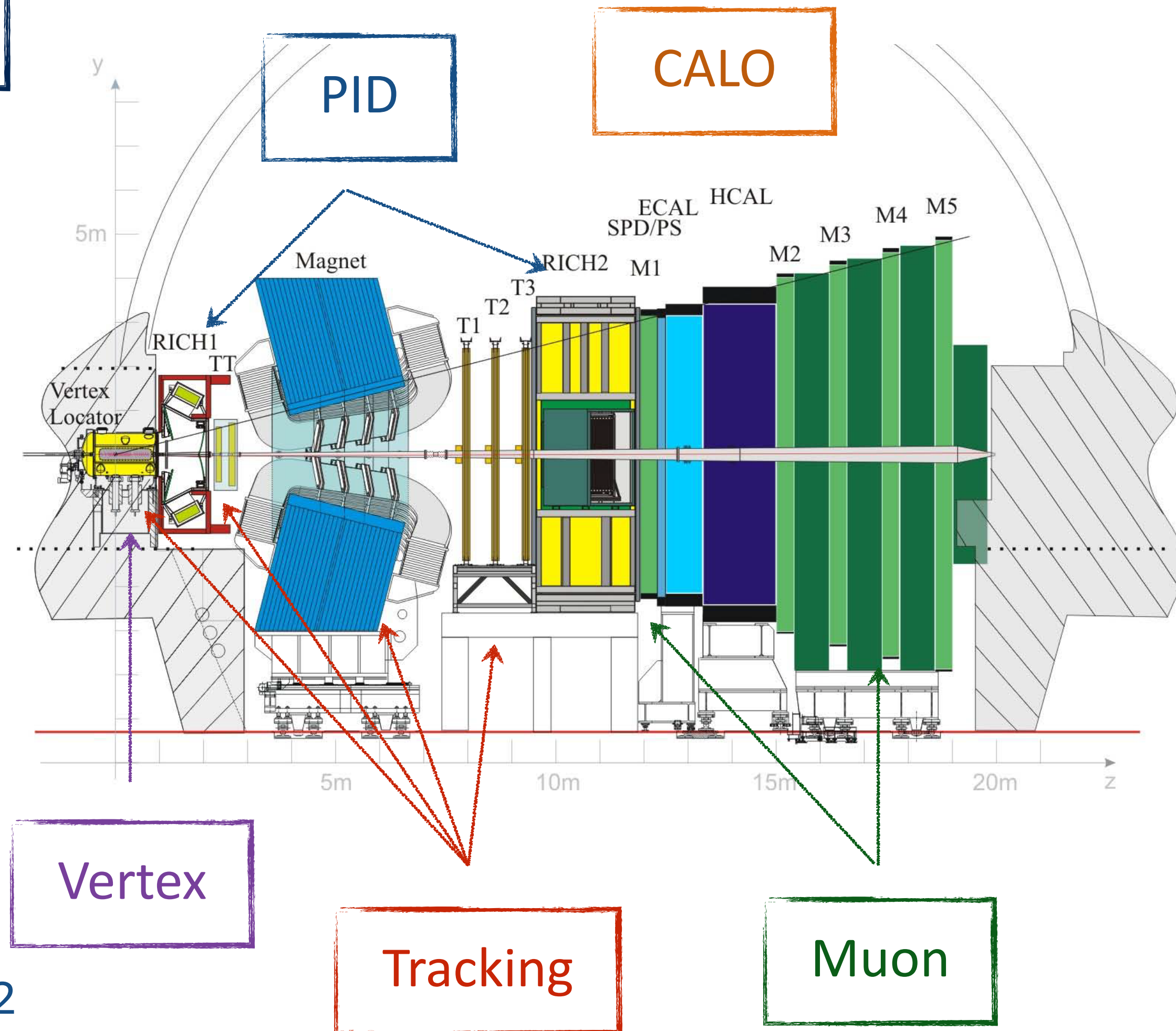
$\delta p/p \approx 0.5\%$

$\epsilon_{\text{Track}} \approx 95\%$

$\epsilon_{\text{PID(K)}} \approx 95\%$

$\epsilon_{\text{PID}(\mu)} \approx 97\%$

$\epsilon_{\text{PID}(e)} \approx 90\%$



Int.J.Mod.Phys. A30 (2015) no.07, 1530022

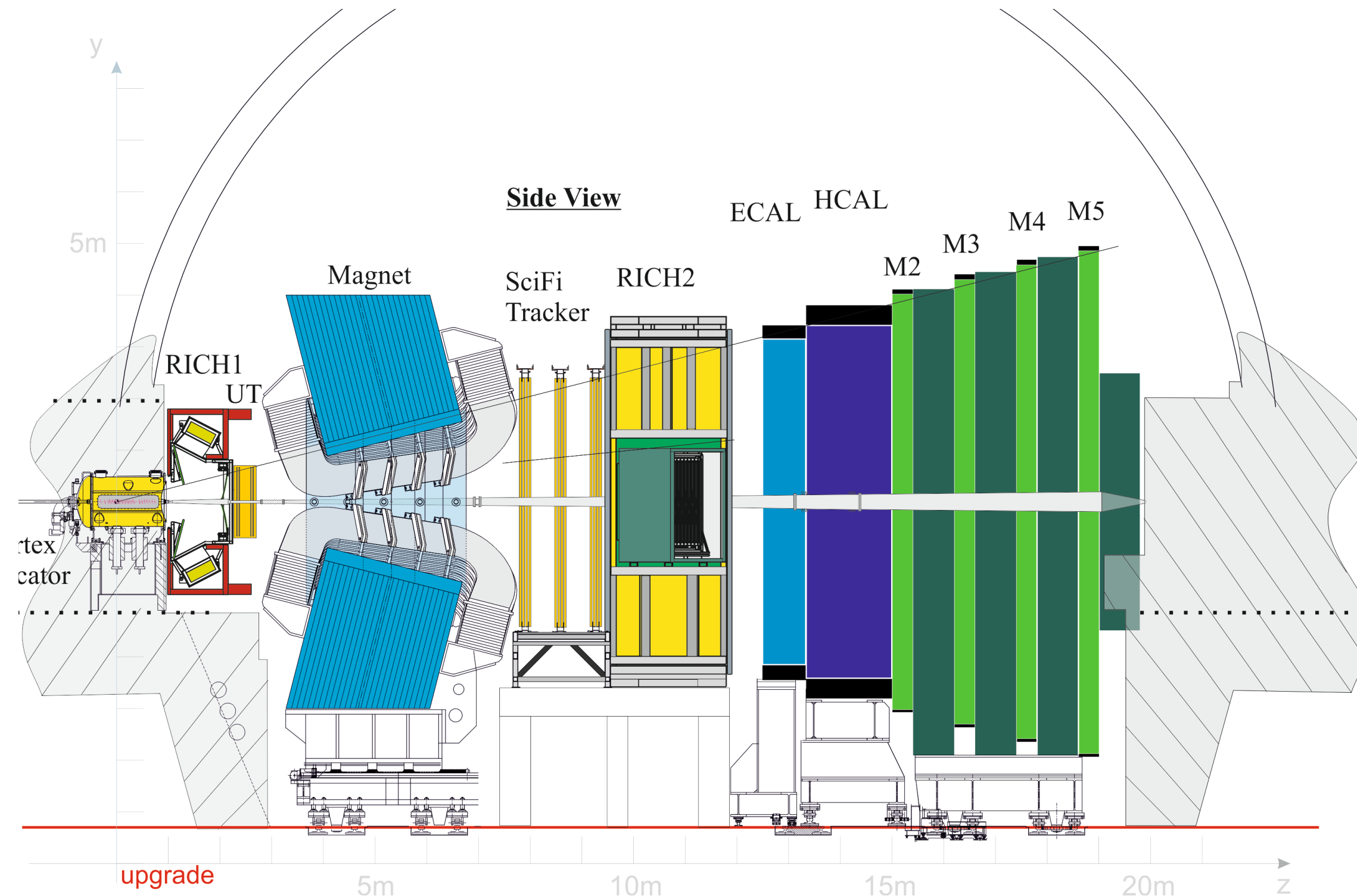
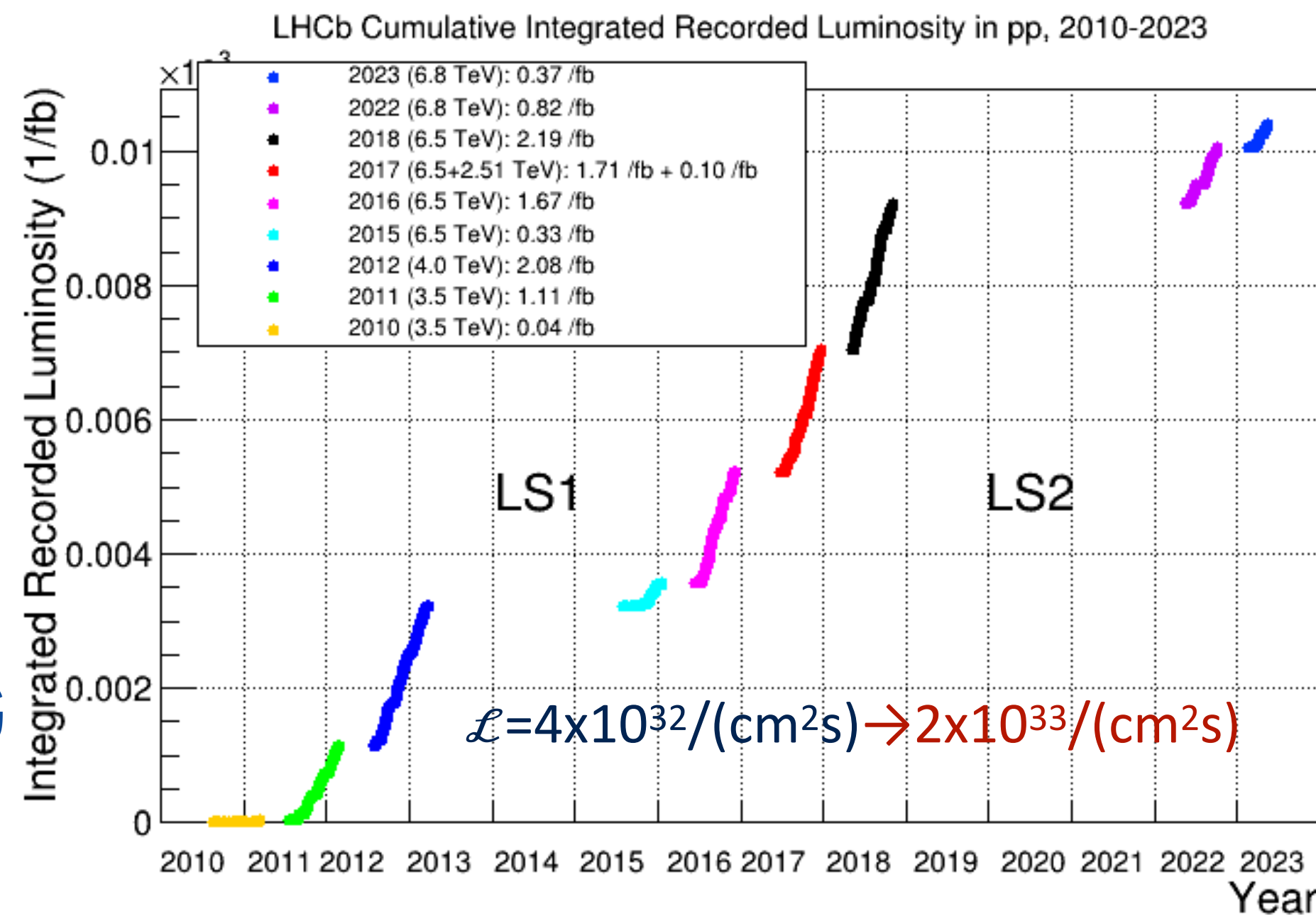


A New Detector for Run3 (2022-ongoing)

LHCb-DP-2022-002

LHCb Upgrade

- New Vertex Locator
- New Tracking Stations
- New RICH Electronics
- Fully Software Trigger



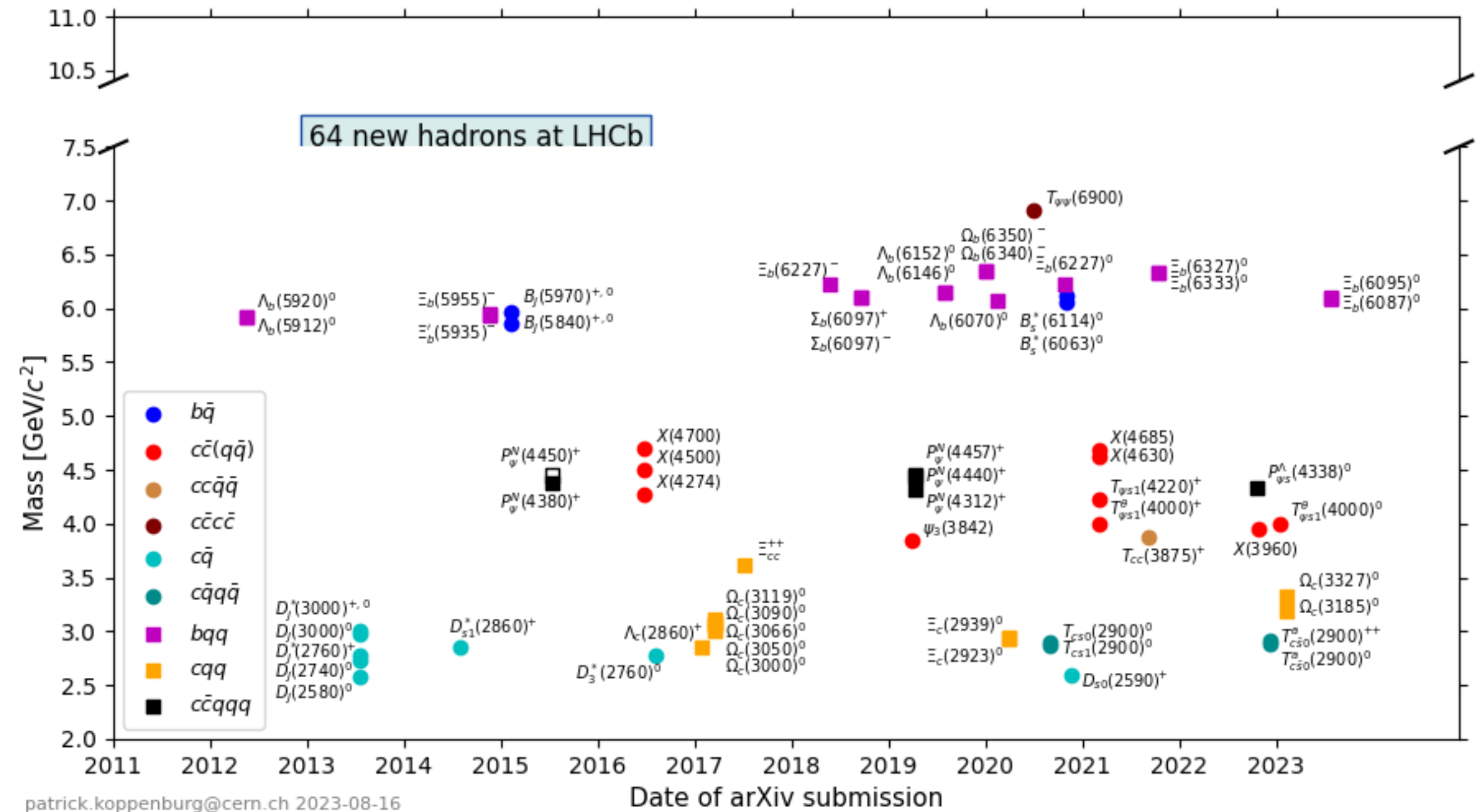
Strange Hadrons at LHCb



Spettroscopia at LHCb

Hadrons of Any Kind

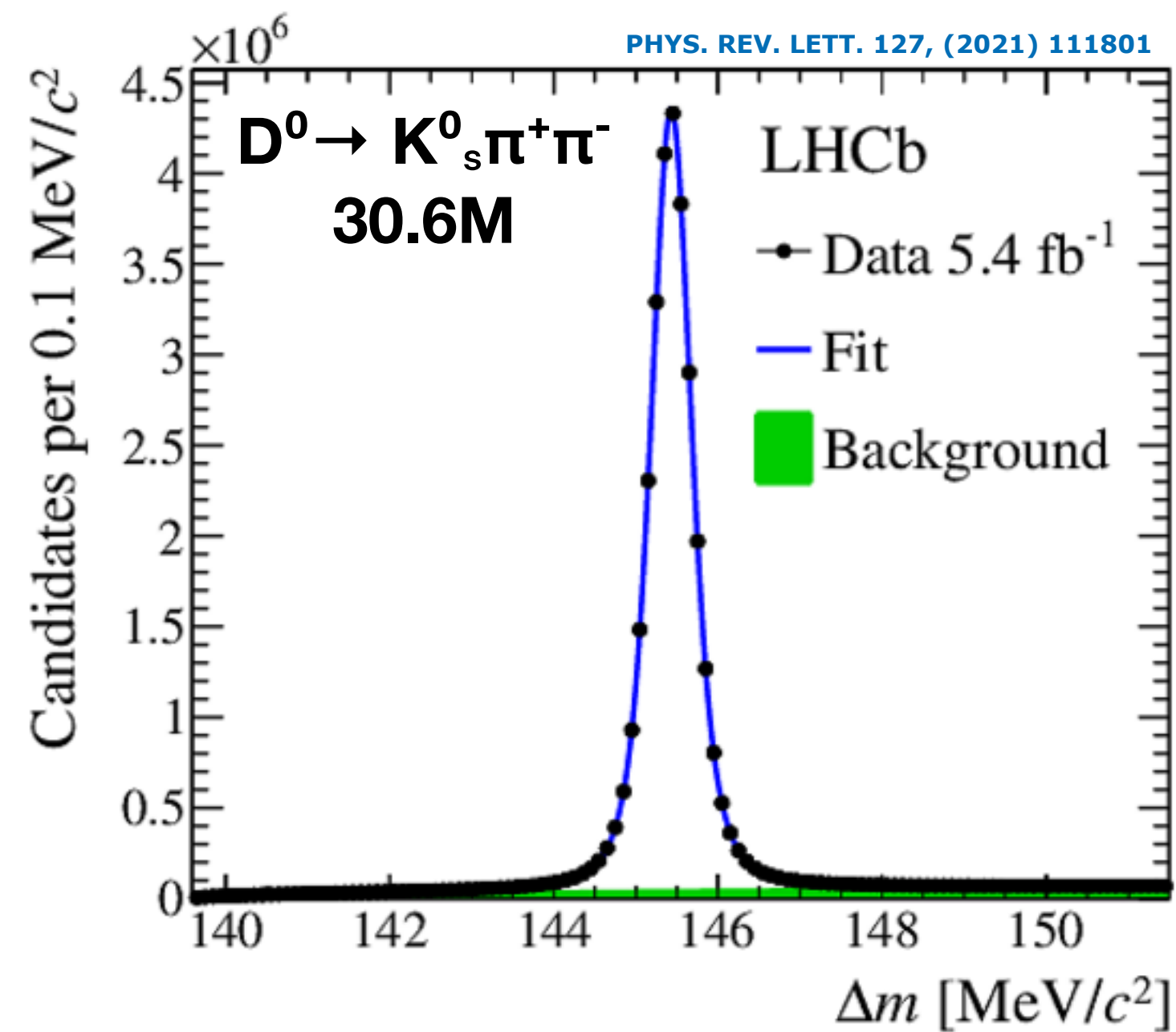
- Mesons, Baryons, Tetraquarks, Pentaquarks
- Excellent PID performance
- Flexibility of the Trigger system



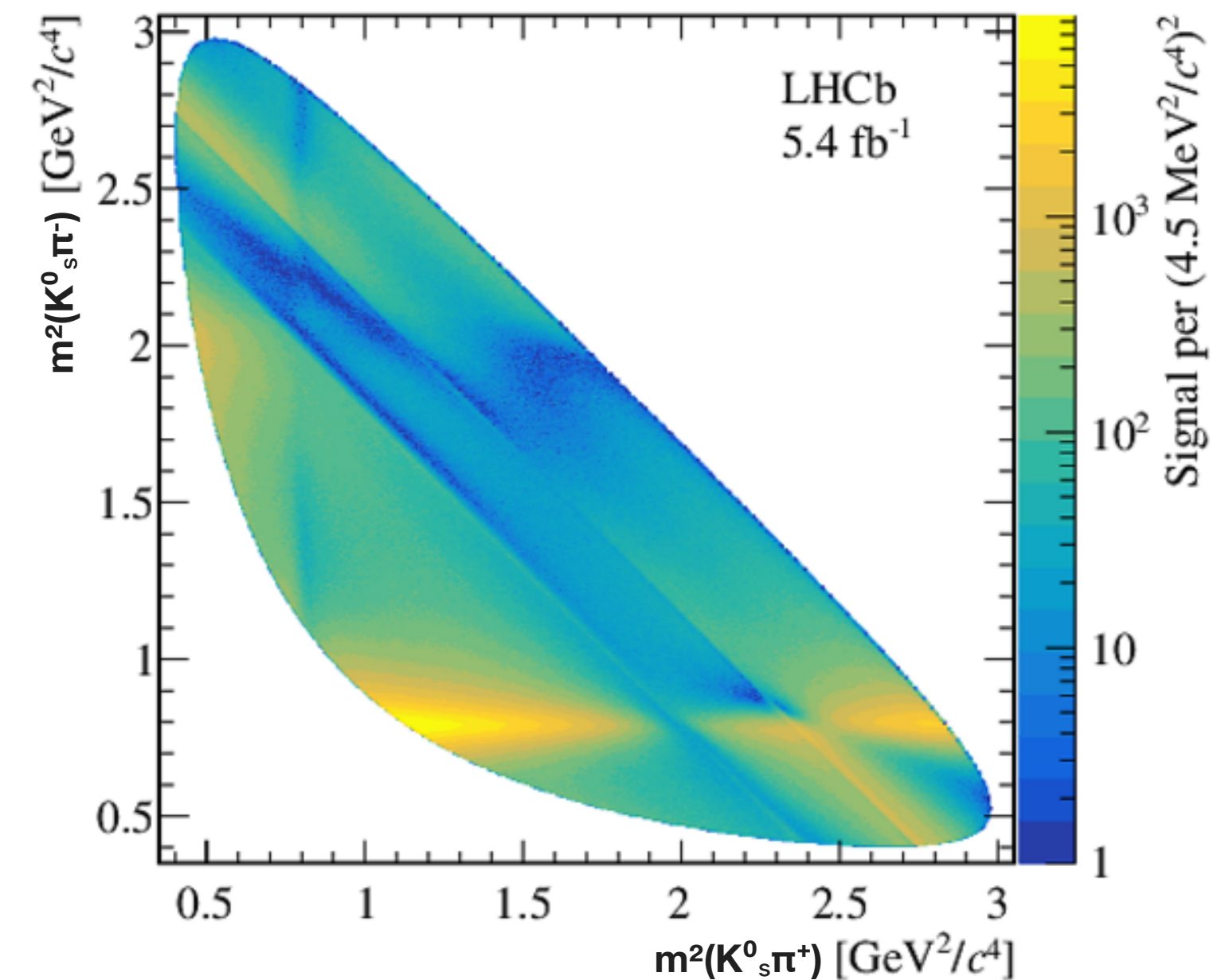
Light-Hadrons Spectroscopy at LHCb

Amplitude Analyses

- Direct production of light hadrons obviously happens but the multiplicity of tracks is so large that they are covered by large background
- Rather study resonances in heavy flavored particle decays (D, B, baryons)
- Allowed by clean signals and good understanding of detector efficiency



Dalitz
Plot
→



Recent Results



Strange Spectroscopy in D^0 Decays

Amplitude Analysis of 4-Body Charm Decays

- 4-Body Charm decays have a rich resonant structure, especially at low masses ($<1.7\text{GeV}/c^2$)
- Good knowledge of the resonant substructure of the decay is important for other studies (i.e. CP Violation)
- With pseudoscalars only, 5D phase space

Amplitude Analysis of 4-Body D^0 Decays

B-tagged Decays

- D^0 mesons reconstructed from $B \rightarrow D^{*+} \mu^- X$ with $D^{*+} \rightarrow D^0 \pi^+$, or $B \rightarrow D^0 \mu^- X$
Trigger selection on μ to improve efficiency determination
Requirements on decay chain improve signal purity

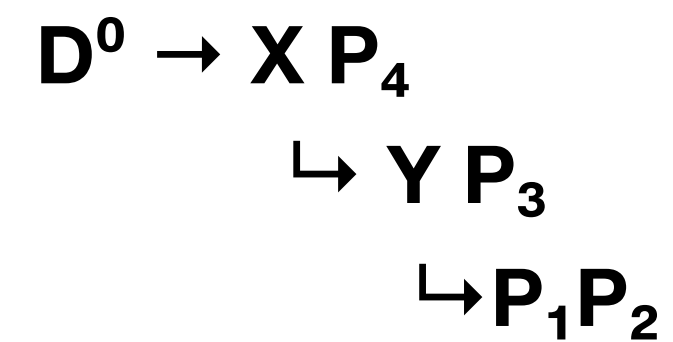
Efficiency

- Determined from simulation reconstructed as data
- Included in the fit by performing all the normalisation integrals over the simulated data - *integration sample*
- Normalisation integrals independent from integration sample, but their uncertainty is \rightarrow use approximation of model to generate the integration sample - *importance sampling*

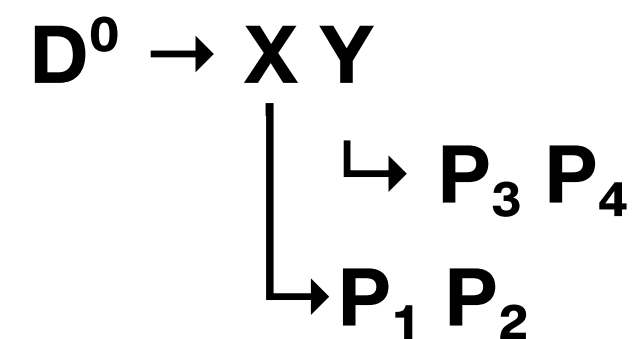
Amplitude Analysis of 4-Body D^0 Decays

Isobar Model

- Cascade decays



- Quasi two-body decays



- Amplitudes are product of dynamical functions for each isobar and a spin factor

Dynamical functions: Breit-Wigner; K-matrix

Spin factor from Covariant tensors

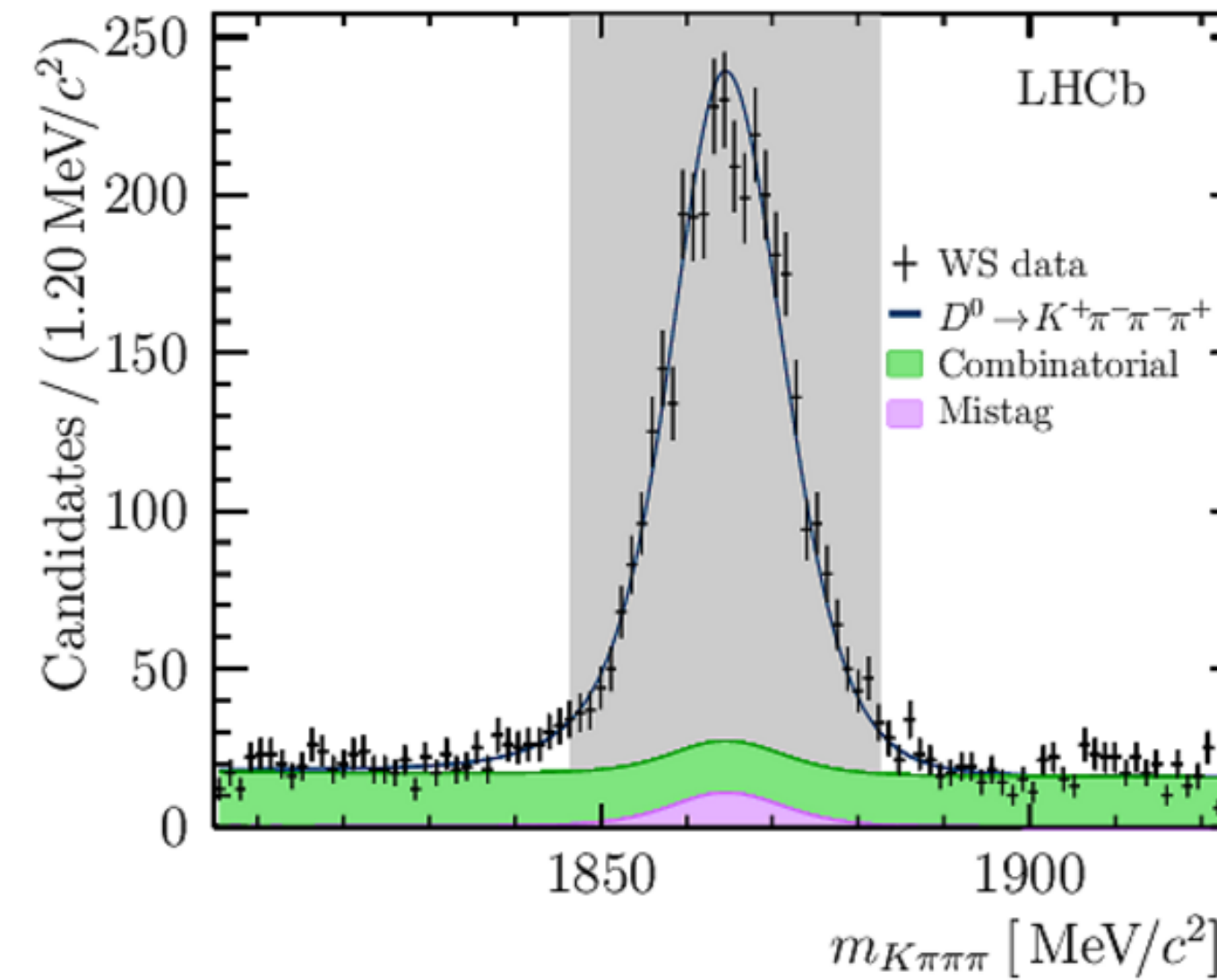
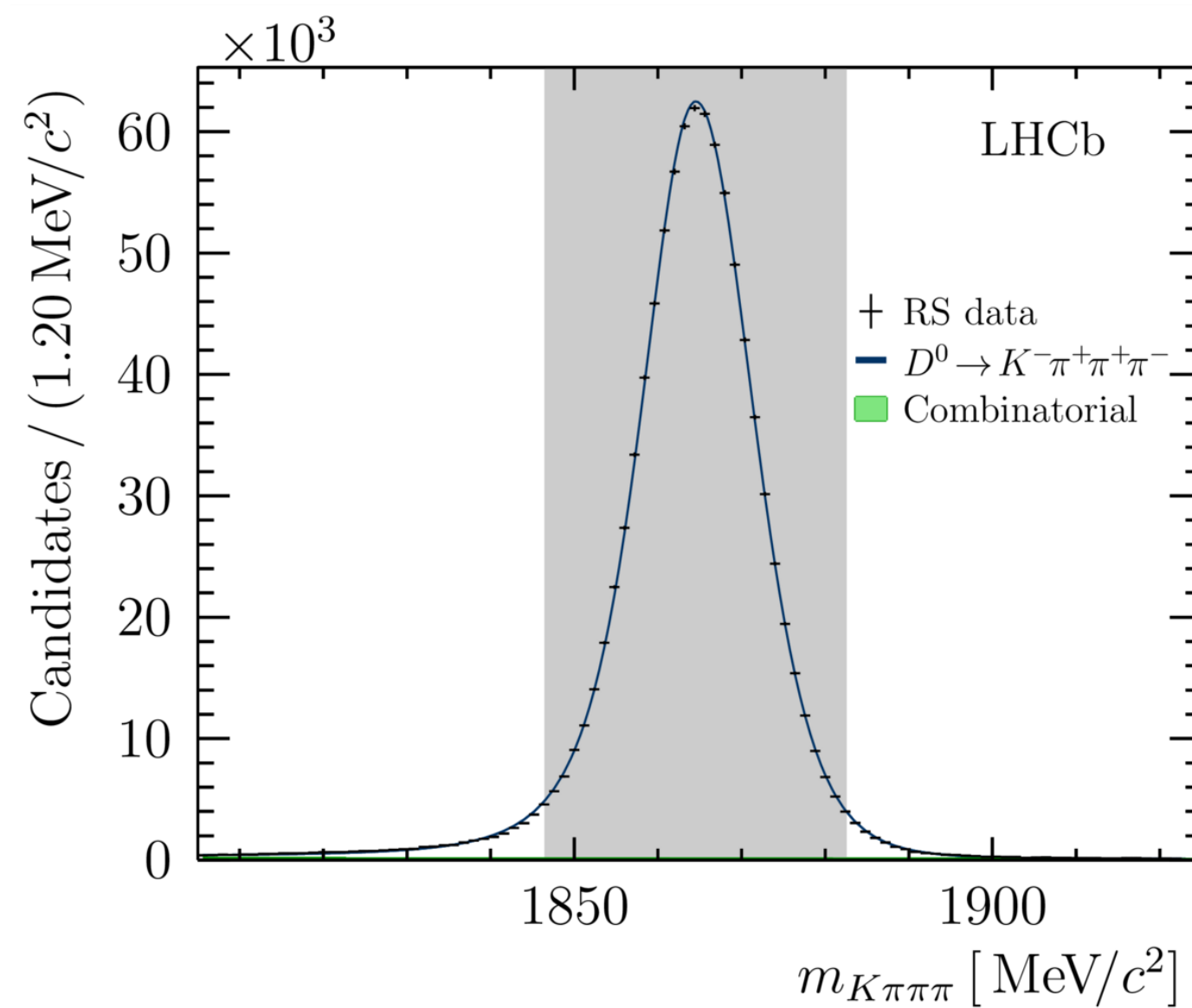
$$\text{BW: } \mathcal{T}(s) = \frac{\sqrt{k} B_L(q, 0)}{m_0^2 - s - i m_0 \Gamma(s)}$$

Signal Yields of $D^0 \rightarrow K^\mp \pi^\pm \pi^\mp \pi^\pm$

EUR. PHYS. J. C78 (2018) 443

RS and WS samples

- Right-Sign: Cabibbo favoured $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$ ($N_s=891k$, $P=99.6\%$ in 2011/12)
- Wrong-Sign: Doubly Cabibbo suppressed $D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$ ($N_s=3k$, $P=82.4\%$ in 2011/12)
- Contamination of RS in WS (Mistag)

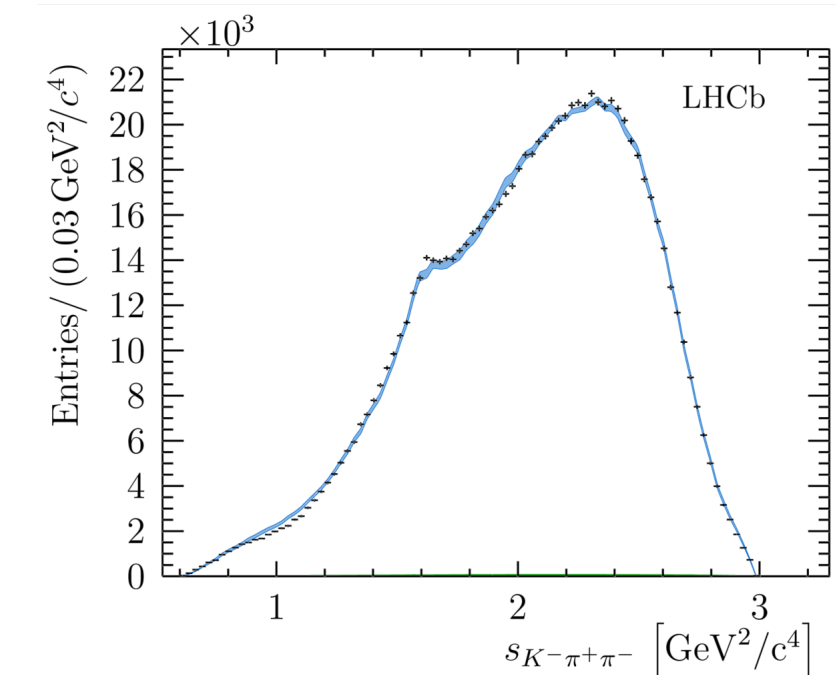
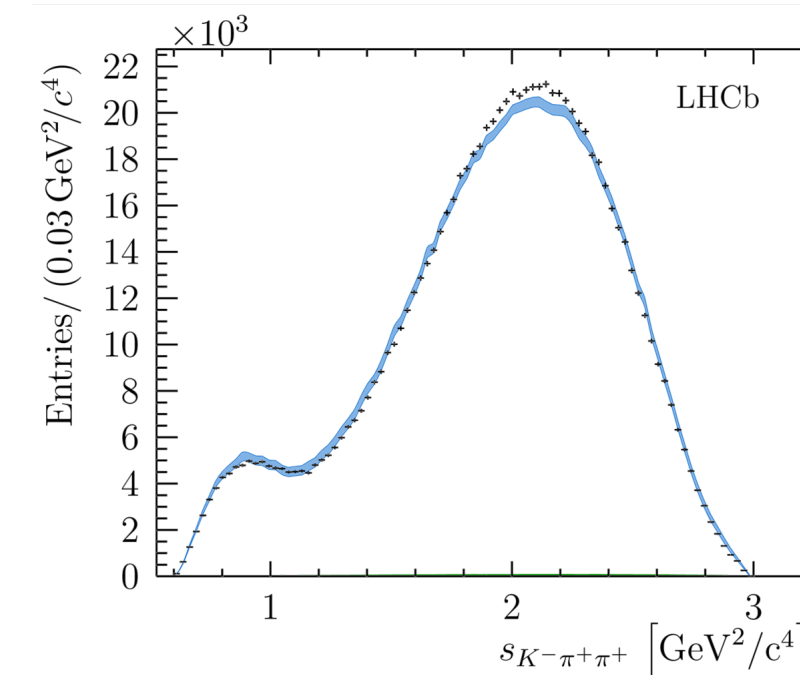
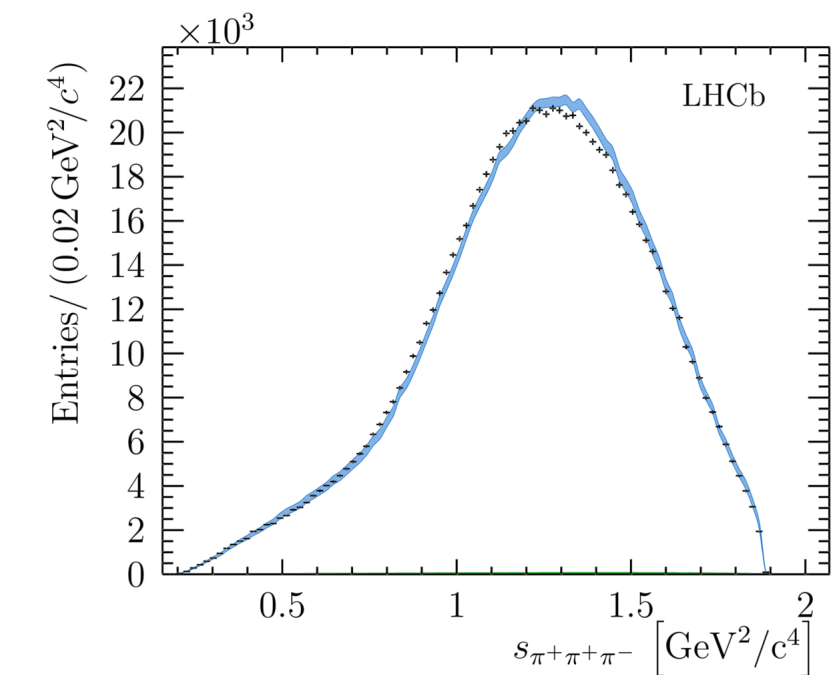
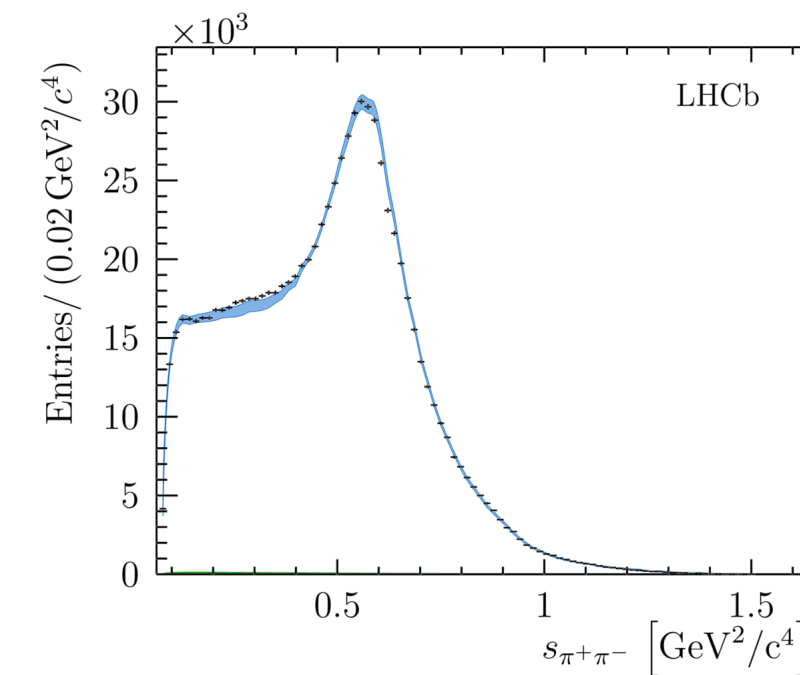
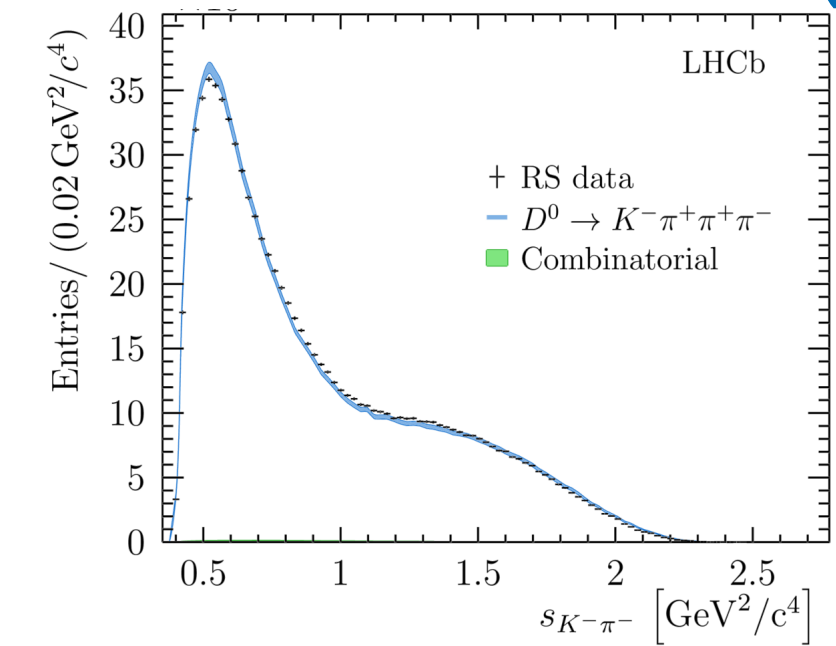
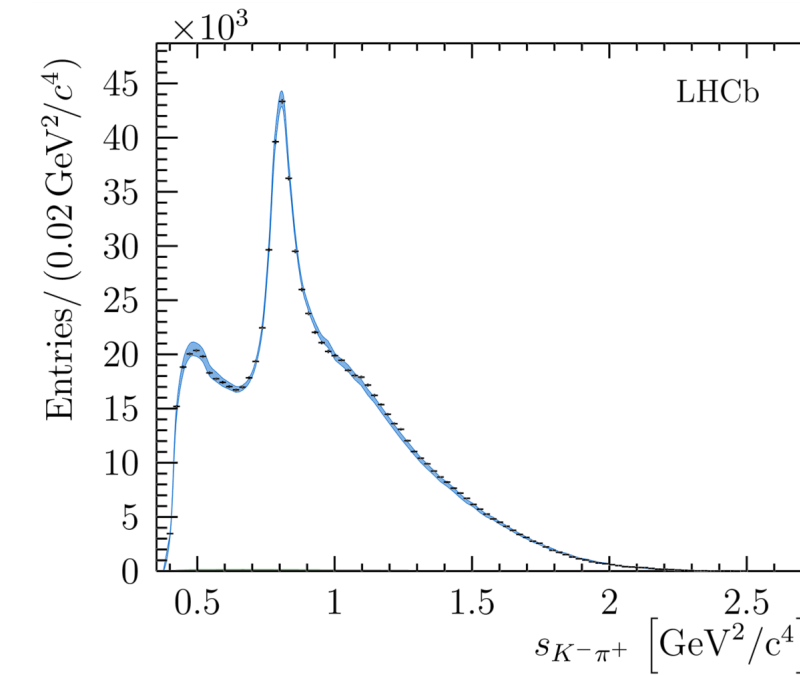


Resonant Structure of $D^0 \rightarrow K^\mp \pi^\pm \pi^\mp \pi^\pm$

EUR. PHYS. J. C78 (2018) 443

Fit Results $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$

	Fit Fraction [%]	$ g $	$\arg(g)[^\circ]$
$[\bar{K}^*(892)^0 \rho(770)^0]^{L=0}$	$7.34 \pm 0.08 \pm 0.47$	$0.196 \pm 0.001 \pm 0.015$	$-22.4 \pm 0.4 \pm 1.6$
$[\bar{K}^*(892)^0 \rho(770)^0]^{L=1}$	$6.03 \pm 0.05 \pm 0.25$	$0.362 \pm 0.002 \pm 0.010$	$-102.9 \pm 0.4 \pm 1.7$
$[\bar{K}^*(892)^0 \rho(770)^0]^{L=2}$	$8.47 \pm 0.09 \pm 0.67$		
$[\rho(1450)^0 \bar{K}^*(892)^0]^{L=0}$	$0.61 \pm 0.04 \pm 0.17$	$0.162 \pm 0.005 \pm 0.025$	$-86.1 \pm 1.9 \pm 4.3$
$[\rho(1450)^0 \bar{K}^*(892)^0]^{L=1}$	$1.98 \pm 0.03 \pm 0.33$	$0.643 \pm 0.006 \pm 0.058$	$97.3 \pm 0.5 \pm 2.8$
$[\rho(1450)^0 \bar{K}^*(892)^0]^{L=2}$	$0.46 \pm 0.03 \pm 0.15$	$0.649 \pm 0.021 \pm 0.105$	$-15.6 \pm 2.0 \pm 4.1$
$\rho(770)^0 [K^- \pi^+]^{L=0}$	$0.93 \pm 0.03 \pm 0.05$	$0.338 \pm 0.006 \pm 0.011$	$73.0 \pm 0.8 \pm 4.0$
$\alpha_{3/2}$		$1.073 \pm 0.008 \pm 0.021$	$-130.9 \pm 0.5 \pm 1.8$
$\bar{K}^*(892)^0 [\pi^+ \pi^-]^{L=0}$	$2.35 \pm 0.09 \pm 0.33$		
$f_{\pi\pi}$		$0.261 \pm 0.005 \pm 0.024$	$-149.0 \pm 0.9 \pm 2.7$
β_1		$0.305 \pm 0.011 \pm 0.046$	$65.6 \pm 1.5 \pm 4.0$
$a_1(1260)^+ K^-$	$38.07 \pm 0.24 \pm 1.38$	$0.813 \pm 0.006 \pm 0.025$	$-149.2 \pm 0.5 \pm 3.1$
$K_1(1270)^- \pi^+$	$4.66 \pm 0.05 \pm 0.39$	$0.362 \pm 0.004 \pm 0.015$	$114.2 \pm 0.8 \pm 3.6$
$K_1(1400)^- [\bar{K}^*(892)^0 \pi^-] \pi^+$	$1.15 \pm 0.04 \pm 0.20$	$0.127 \pm 0.002 \pm 0.011$	$-169.8 \pm 1.1 \pm 5.9$
$K_2^*(1430)^- [\bar{K}^*(892)^0 \pi^-] \pi^+$	$0.46 \pm 0.01 \pm 0.03$	$0.302 \pm 0.004 \pm 0.011$	$-77.7 \pm 0.7 \pm 2.1$
$K(1460)^- \pi^+$	$3.75 \pm 0.10 \pm 0.37$	$0.122 \pm 0.002 \pm 0.012$	$172.7 \pm 2.2 \pm 8.2$
$[K^- \pi^+]^{L=0} [\pi^+ \pi^-]^{L=0}$	$22.04 \pm 0.28 \pm 2.09$		
$\alpha_{3/2}$		$0.870 \pm 0.010 \pm 0.030$	$-149.2 \pm 0.7 \pm 3.5$
$\alpha_{K\eta'}$		$2.614 \pm 0.141 \pm 0.281$	$-19.1 \pm 2.4 \pm 12.0$
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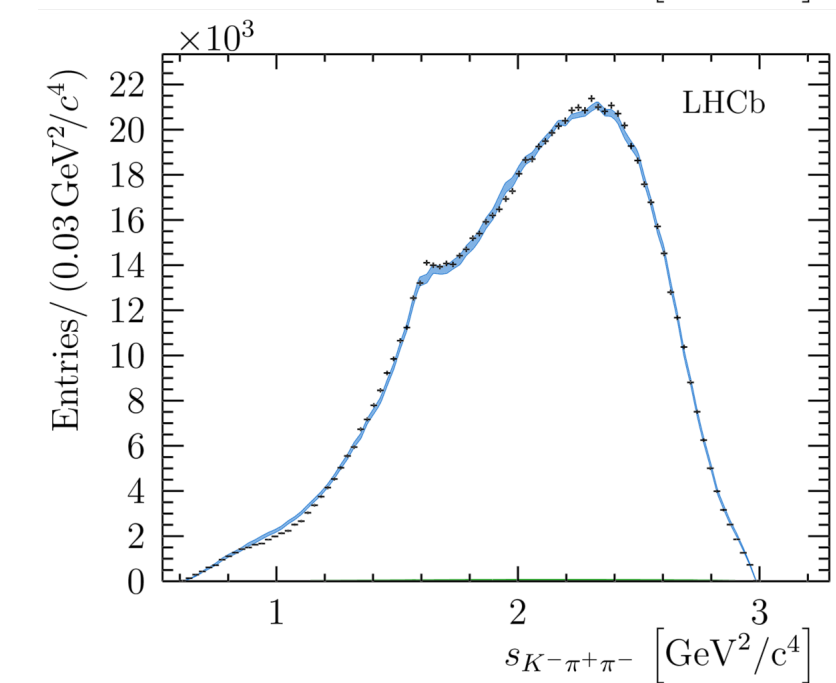
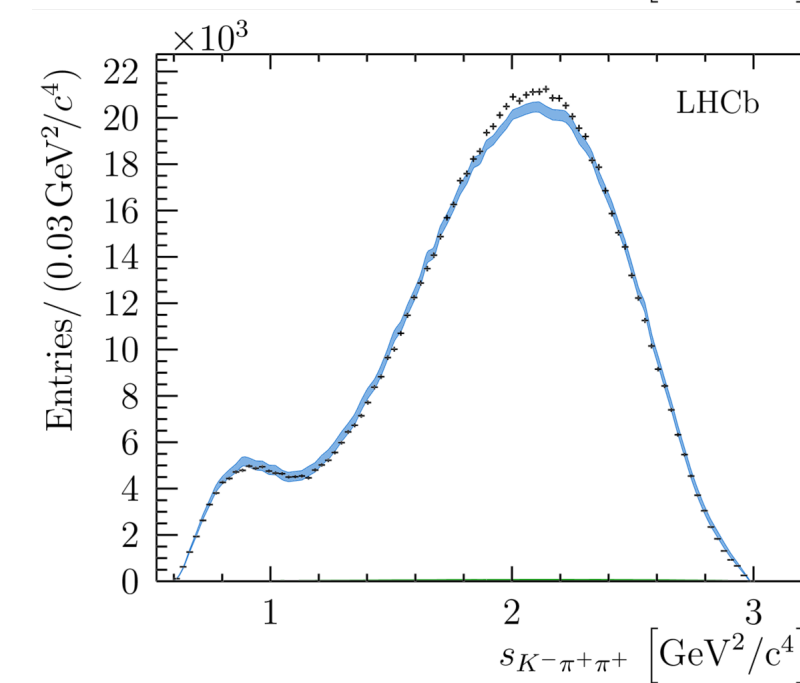
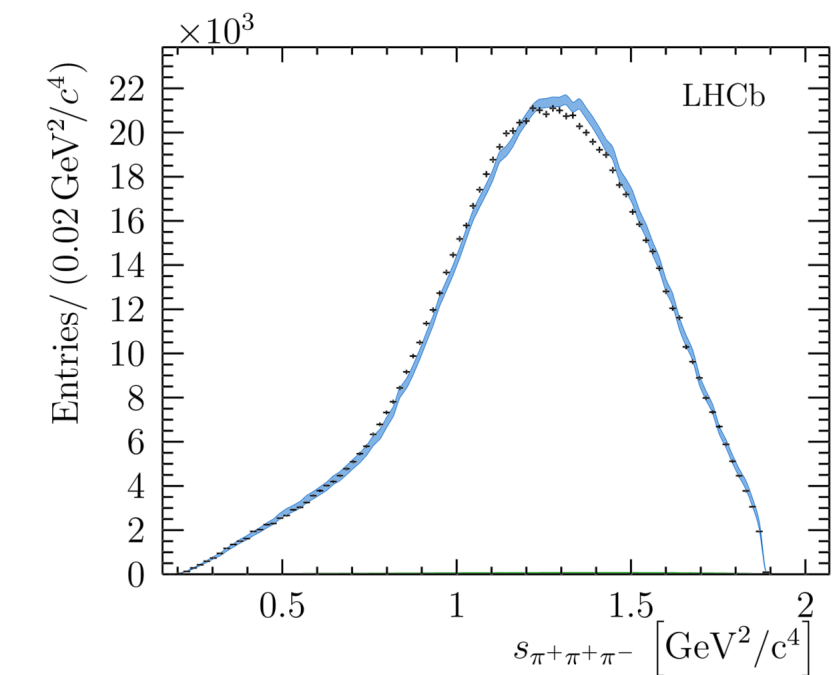
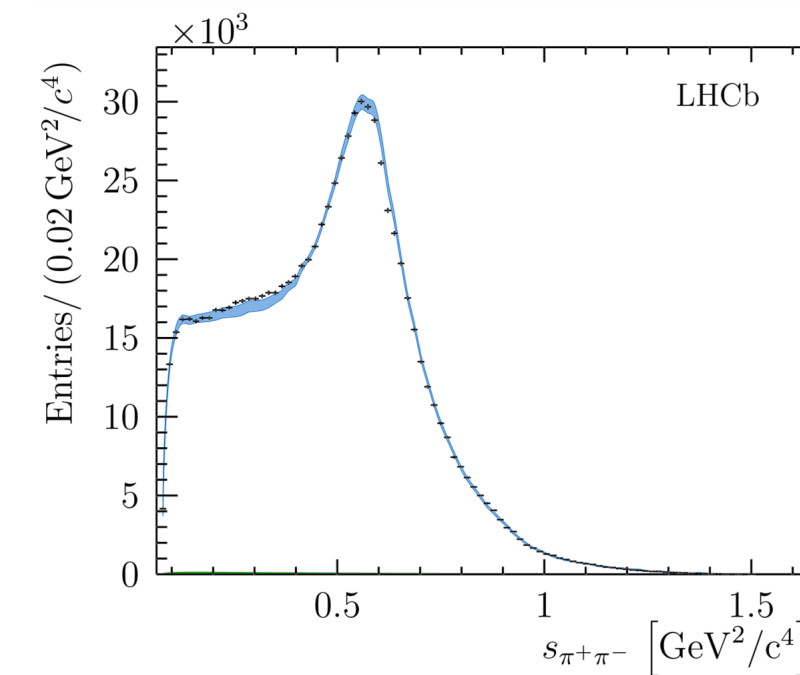
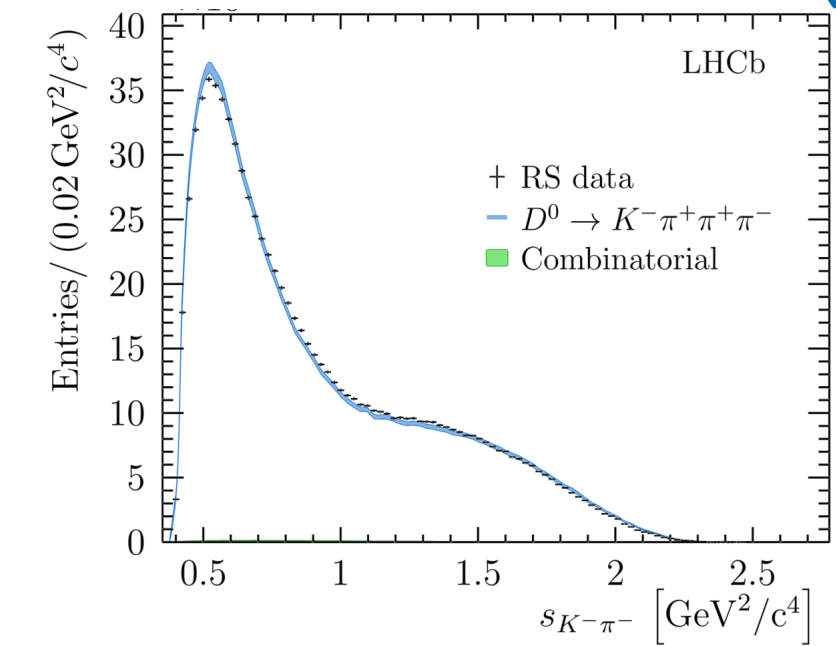
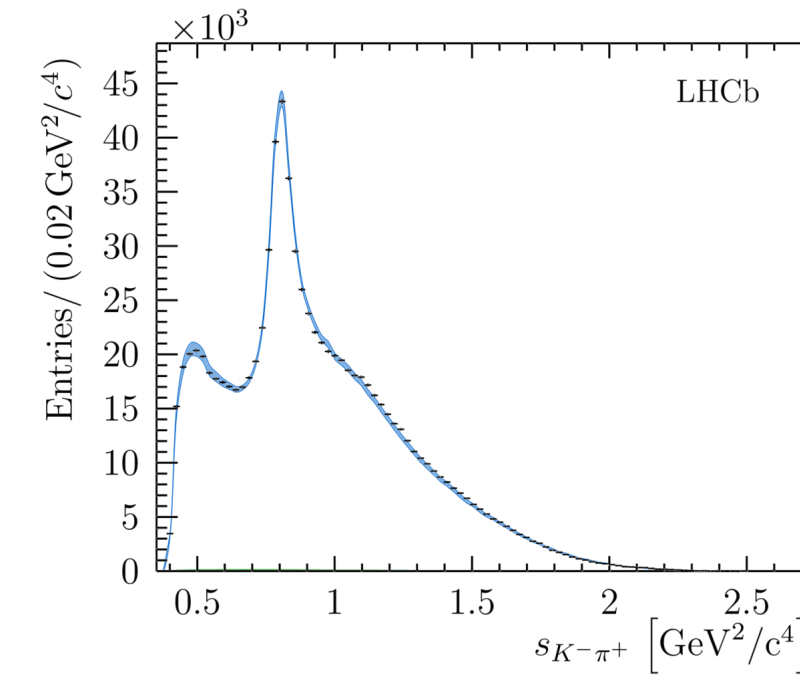


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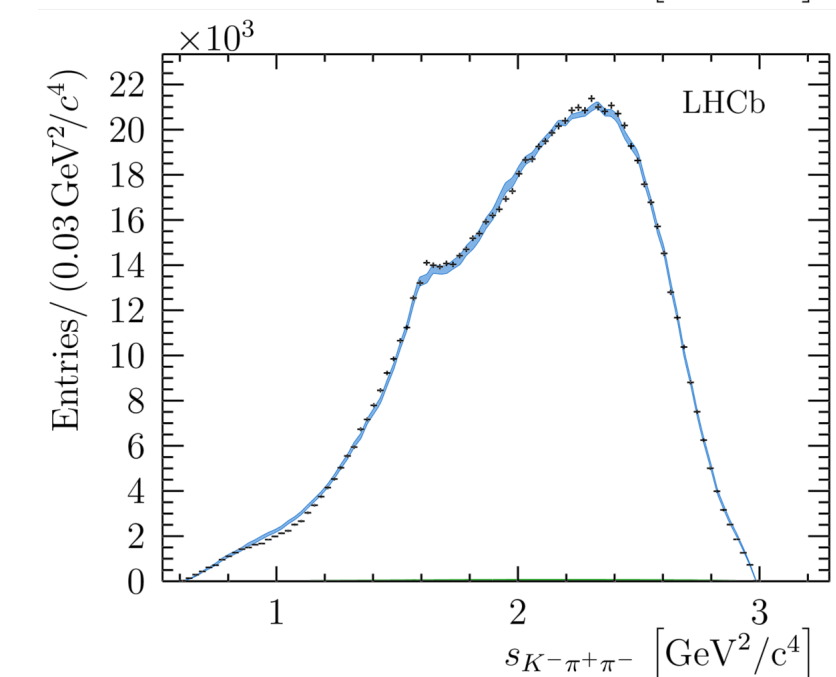
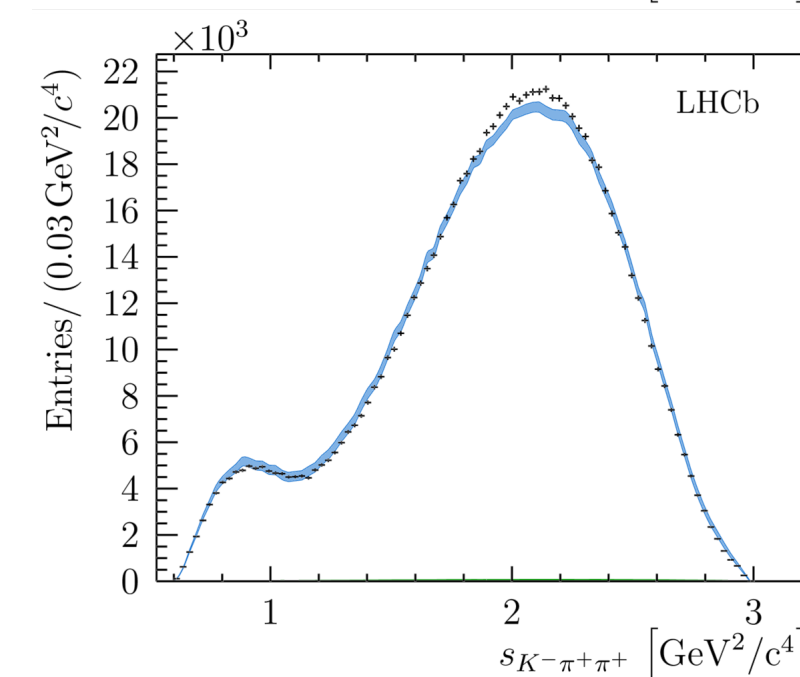
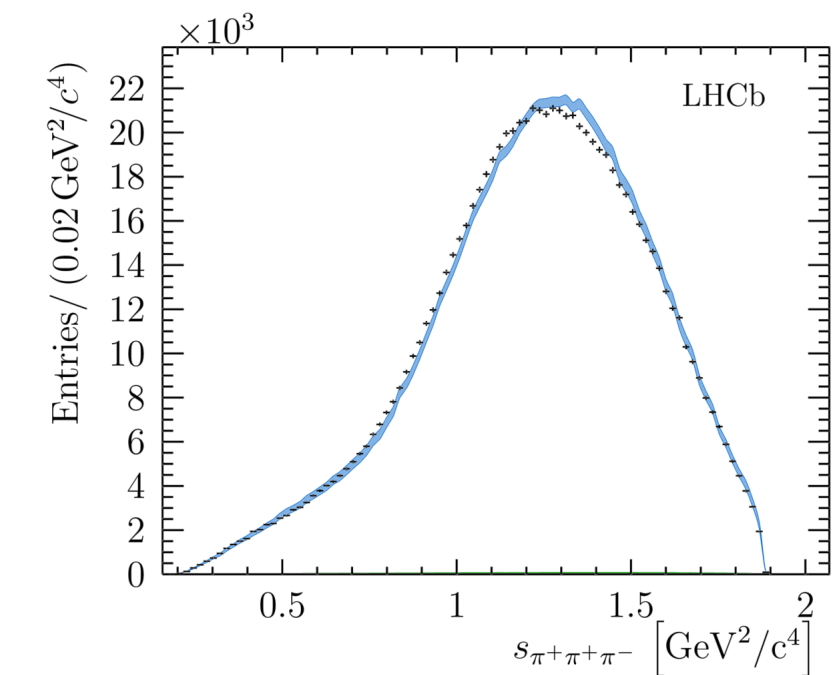
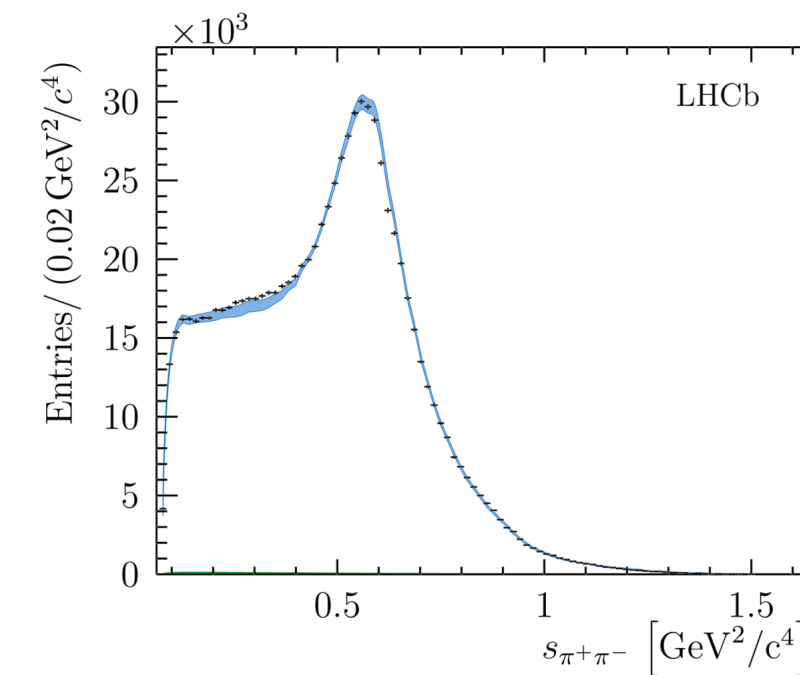
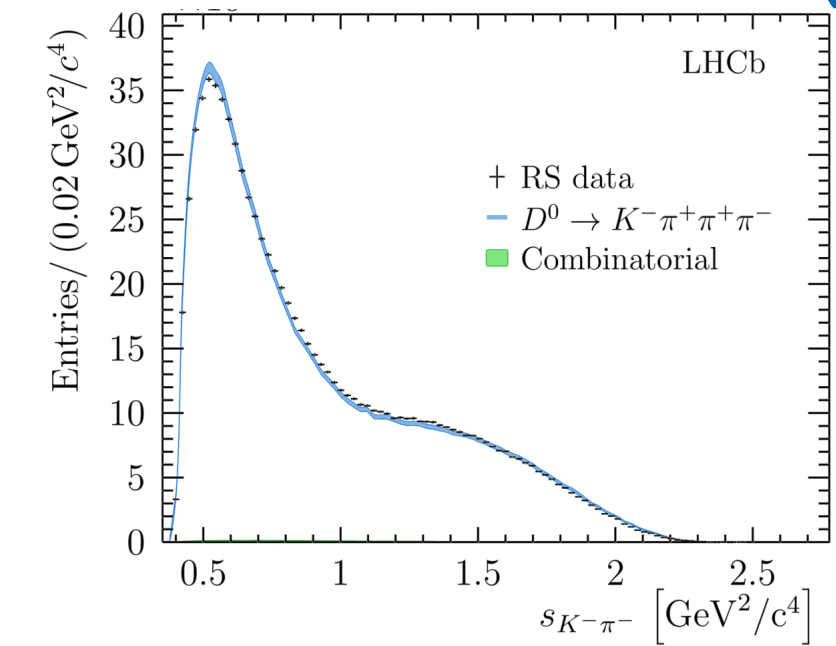
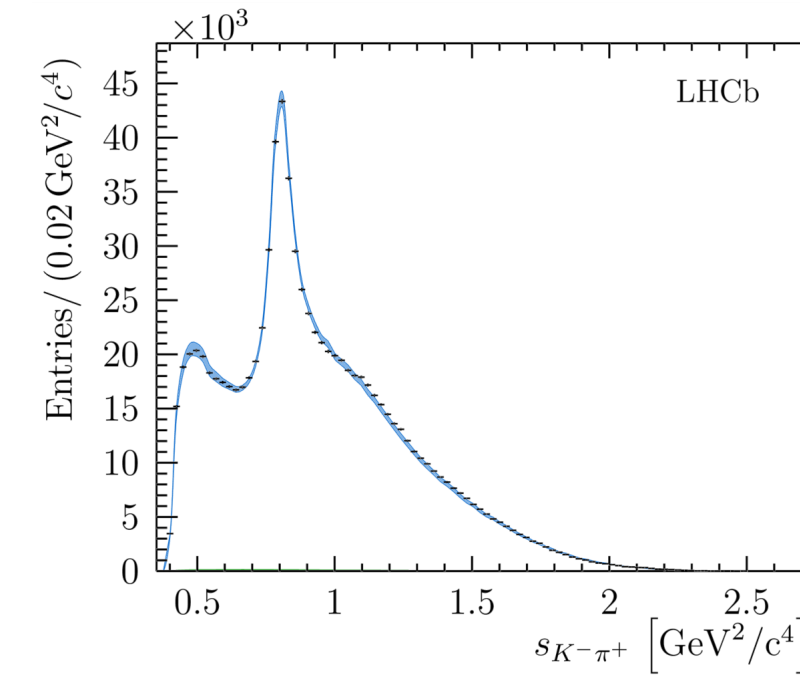


Resonant Structure of $D^0 \rightarrow K^\mp \pi^\pm \pi^\mp \pi^\pm$

EUR. PHYS. J. C78 (2018) 443

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Strange Resonances in $D^0 \rightarrow K^\mp \pi^\pm \pi^\mp \pi^\pm$

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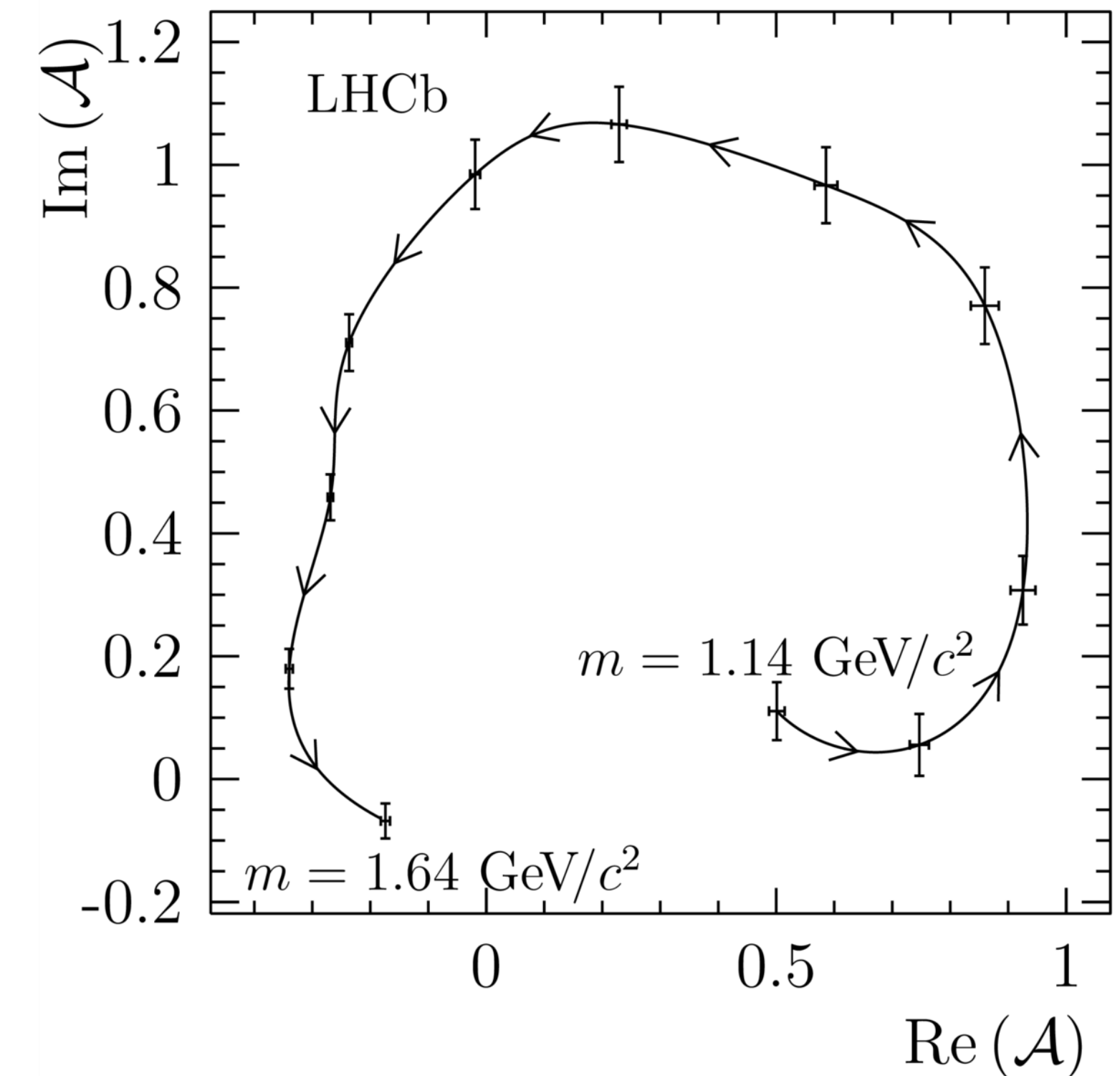
$K_1(1270)^-$

$K_1(1270)^- \quad m_0 = 1289.81 \pm 0.56 \pm 1.66 \text{ MeV}/c^2; \Gamma_0 = 116.11 \pm 1.65 \pm 2.96 \text{ MeV}/c^2$			
	Partial Fractions [%]	$ g $	$\arg(g)[^\circ]$
$\rho(770)^0 K^-$	$96.30 \pm 1.64 \pm 6.61$		
$\rho(1450)^0 K^-$	$49.09 \pm 1.58 \pm 11.54$	$2.016 \pm 0.026 \pm 0.211$	$-119.5 \pm 0.9 \pm 2.3$
$\bar{K}^*(892)^0 \pi^-$	$27.08 \pm 0.64 \pm 2.82$	$0.388 \pm 0.007 \pm 0.033$	$-172.6 \pm 1.1 \pm 6.0$
$[K^- \pi^+]^{L=0} \pi^-$	$22.90 \pm 0.72 \pm 1.89$	$0.554 \pm 0.010 \pm 0.037$	$53.2 \pm 1.1 \pm 1.9$
$[\bar{K}^*(892)^0 \pi^-]^{L=2}$	$3.47 \pm 0.17 \pm 0.31$	$0.769 \pm 0.021 \pm 0.048$	$-19.3 \pm 1.6 \pm 6.7$
$\omega(782) [\pi^+ \pi^-] K^-$	$1.65 \pm 0.11 \pm 0.16$	$0.146 \pm 0.005 \pm 0.009$	$9.0 \pm 2.1 \pm 5.7$

$K(1460)^-$

- The presence of this resonance is further justified by the Argand diagram from the Model Independent Partial Wave Analysis

$K(1460)^- \quad m_0 = 1482.40 \pm 3.58 \pm 15.22 \text{ MeV}/c^2; \Gamma_0 = 335.60 \pm 6.20 \pm 8.65 \text{ MeV}/c^2$			
	Partial Fractions [%]	$ g $	$\arg(g)[^\circ]$
$\bar{K}^*(892)^0 \pi^-$	$51.39 \pm 1.00 \pm 1.71$		
$[\pi^+ \pi^-]^{L=0} K^-$	$31.23 \pm 0.83 \pm 1.78$		
f_{KK}		$1.819 \pm 0.059 \pm 0.189$	$-80.8 \pm 2.2 \pm 6.6$
β_1		$0.813 \pm 0.032 \pm 0.136$	$112.9 \pm 2.6 \pm 9.5$
β_0		$0.315 \pm 0.010 \pm 0.022$	$46.7 \pm 1.9 \pm 3.0$



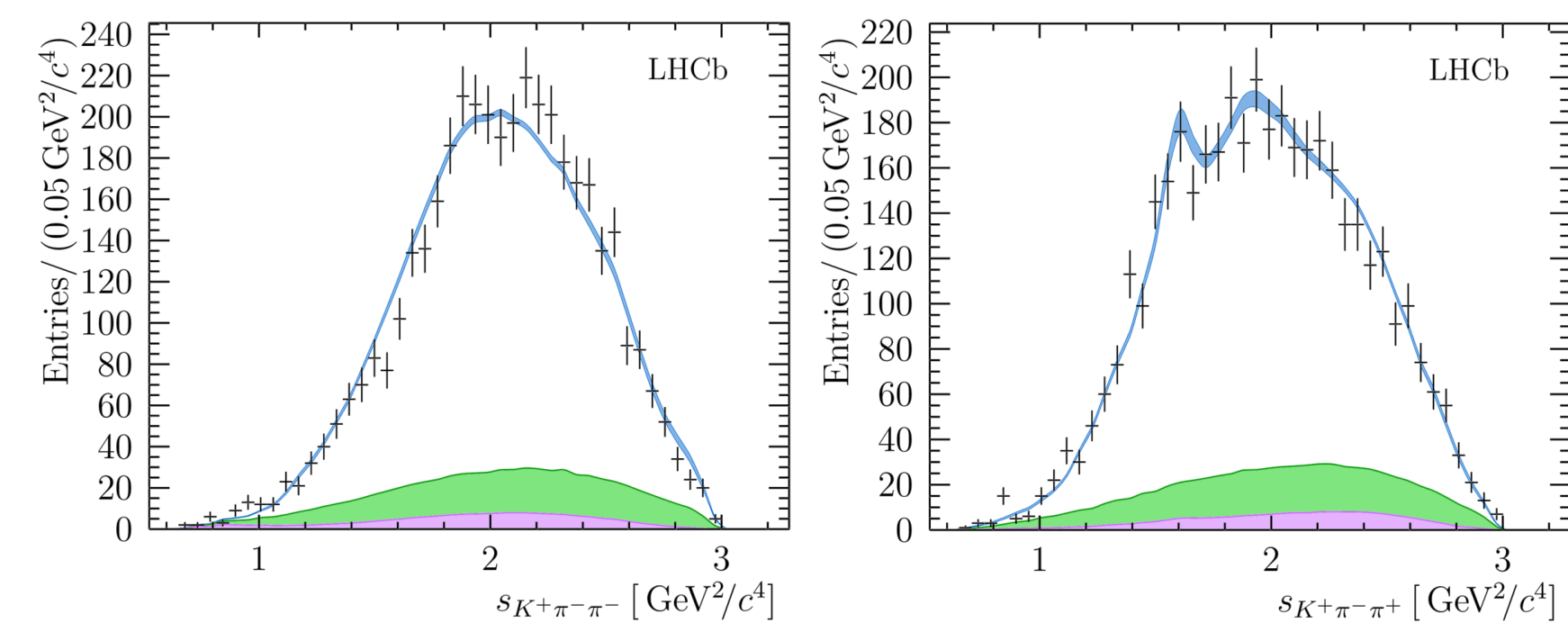
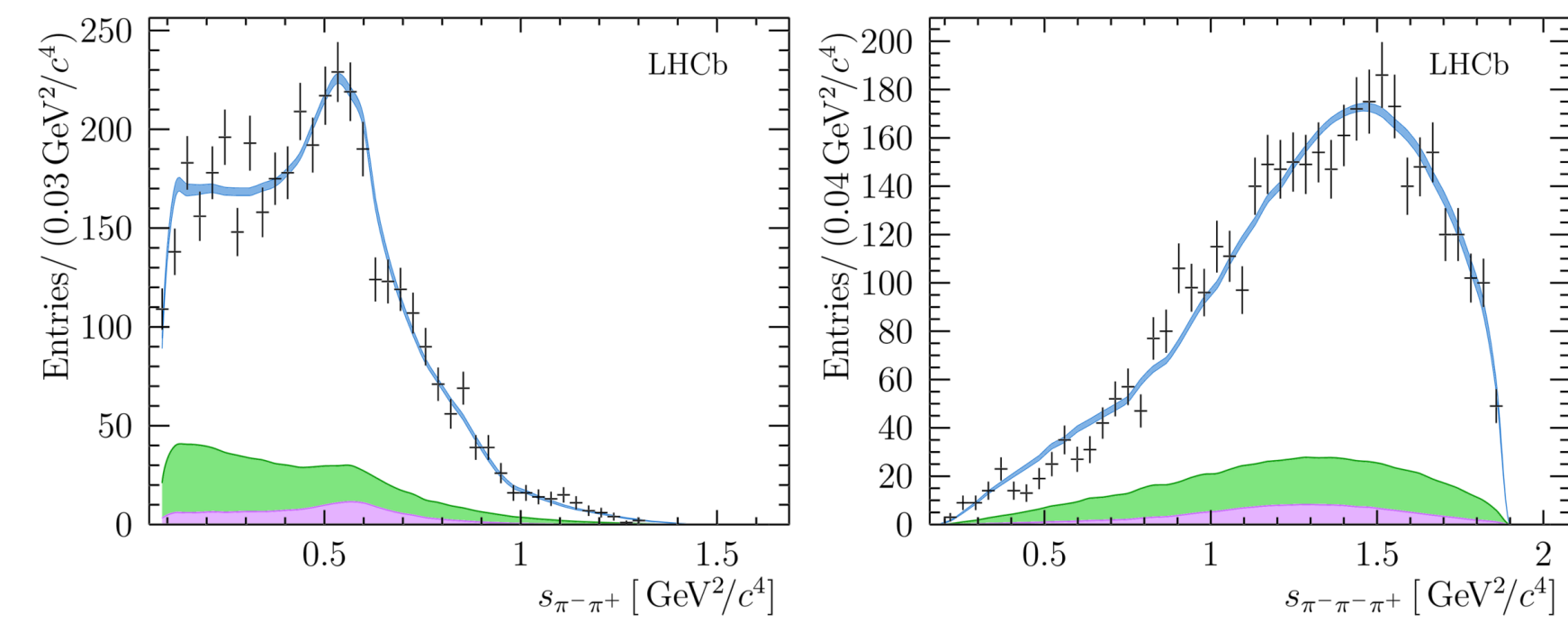
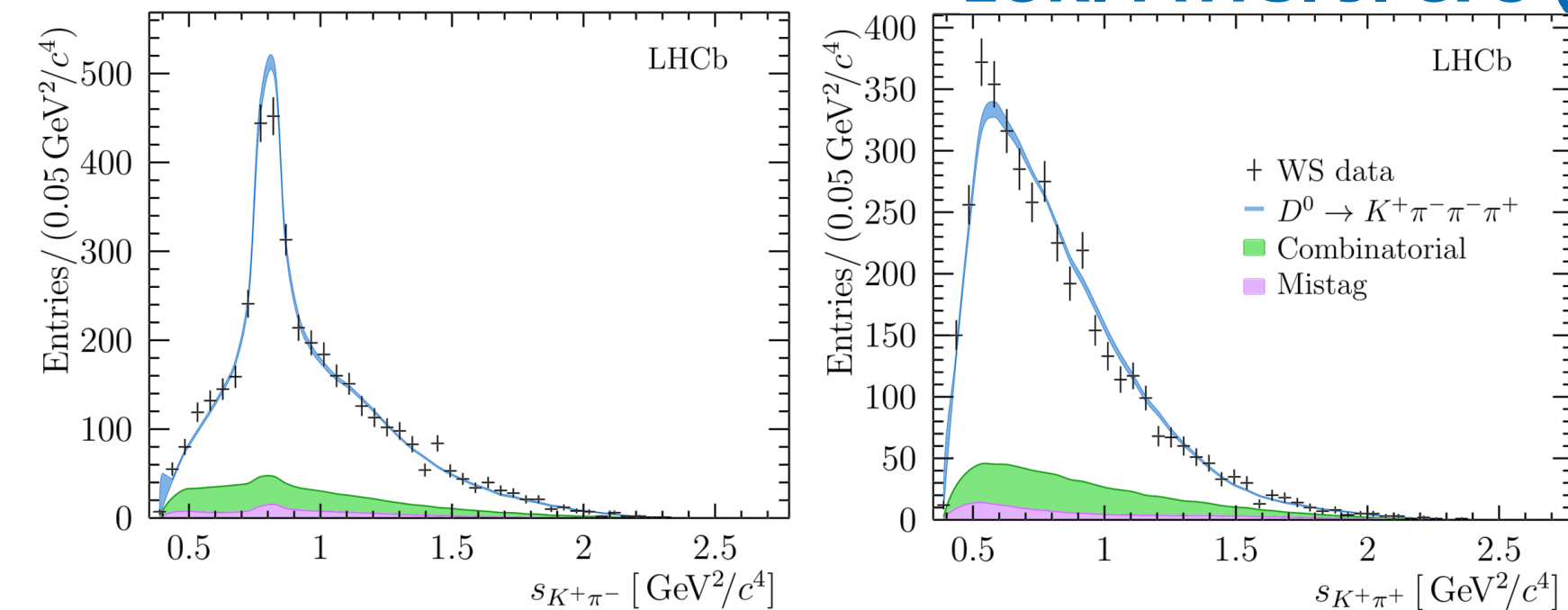
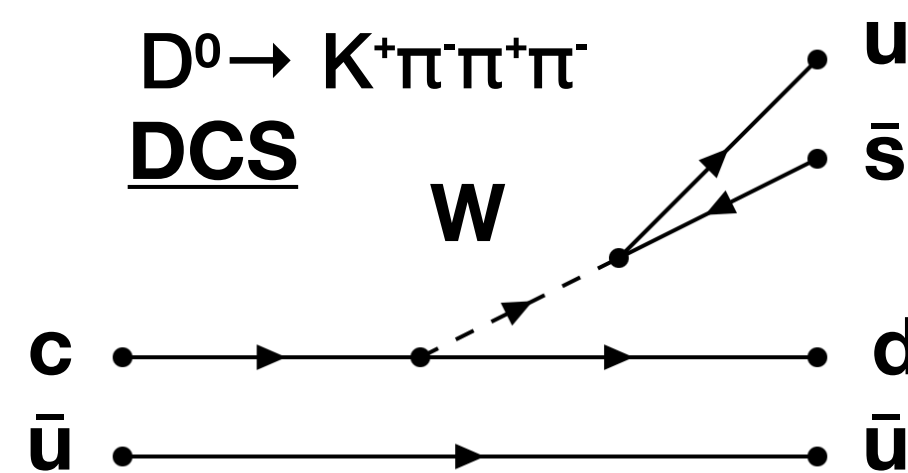
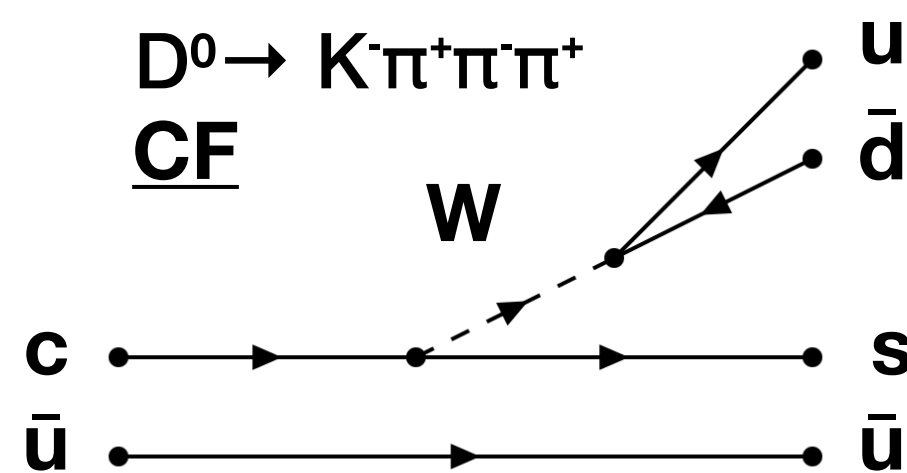
Resonant Structure of $D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$

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Fit Results $D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$

- 3-Body resonance parameters fixed to RS fit
- Largest fraction from $K_1 \pi$ (colour-favoured W emission)

	Fit Fraction [%]	$ g $	$\arg(g)[^\circ]$
$[K^*(892)^0 \rho(770)^0]^{L=0}$	$9.62 \pm 1.58 \pm 1.03$	$0.205 \pm 0.019 \pm 0.010$	$-8.5 \pm 4.7 \pm 4.4$
$[K^*(892)^0 \rho(770)^0]^{L=1}$	$8.42 \pm 0.83 \pm 0.57$	$0.390 \pm 0.029 \pm 0.006$	$-91.4 \pm 4.7 \pm 4.1$
$[K^*(892)^0 \rho(770)^0]^{L=2}$	$10.19 \pm 1.03 \pm 0.79$		
$[\rho(1450)^0 K^*(892)^0]^{L=0}$	$8.16 \pm 1.24 \pm 1.69$	$0.541 \pm 0.042 \pm 0.055$	$-21.8 \pm 6.5 \pm 5.5$
$K_1(1270)^+ \pi^-$	$18.15 \pm 1.11 \pm 2.30$	$0.653 \pm 0.040 \pm 0.058$	$-110.7 \pm 5.1 \pm 4.9$
$K_1(1400)^+ [K^*(892)^0 \pi^+] \pi^-$	$26.55 \pm 1.97 \pm 2.13$	$0.560 \pm 0.037 \pm 0.031$	$29.8 \pm 4.2 \pm 4.6$
$[K^+ \pi^-]^{L=0} [\pi^+ \pi^-]^{L=0}$	$20.90 \pm 1.30 \pm 1.50$		
$\alpha_{3/2}$		$0.686 \pm 0.043 \pm 0.022$	$-149.4 \pm 4.3 \pm 2.9$
β_1		$0.438 \pm 0.044 \pm 0.030$	$-132.4 \pm 6.5 \pm 3.0$
$f_{\pi\pi}$		$0.050 \pm 0.006 \pm 0.005$	$74.8 \pm 7.5 \pm 5.3$
Sum of Fit Fractions	$101.99 \pm 2.90 \pm 2.85$		
χ^2/ν	$350/239 = 1.463$		

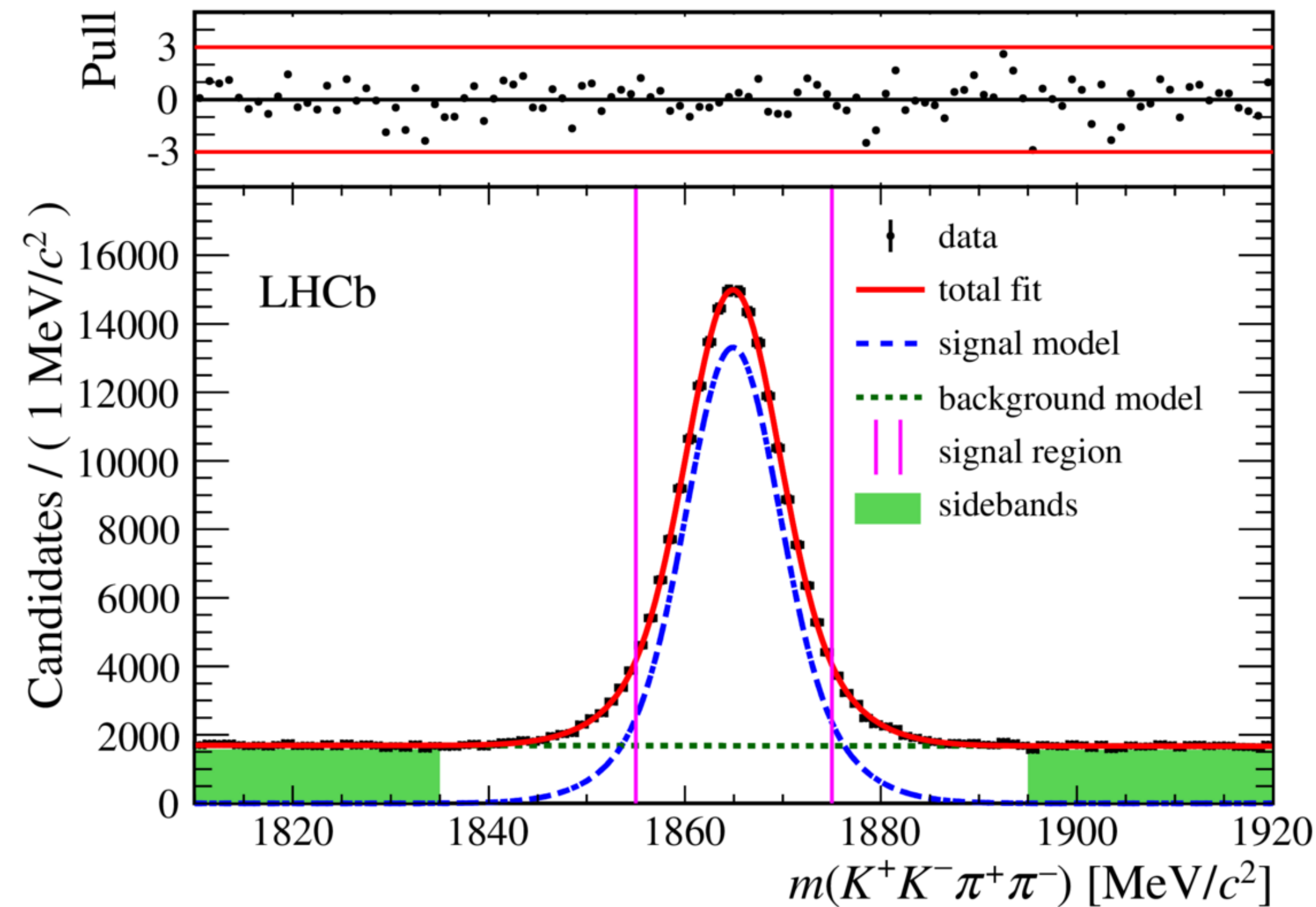


Signal Yield of $D^0 \rightarrow K^+K^-\pi^+\pi^-$

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Run1 Sample (2011/12)

- Cabibbo suppressed $D^0 \rightarrow K^+K^-\pi^+\pi^-$ ($N_S=160k$, $P=82.8\%$)
- Mass fit used to extract fraction of signal decays and background in $\pm 2\sigma$ region

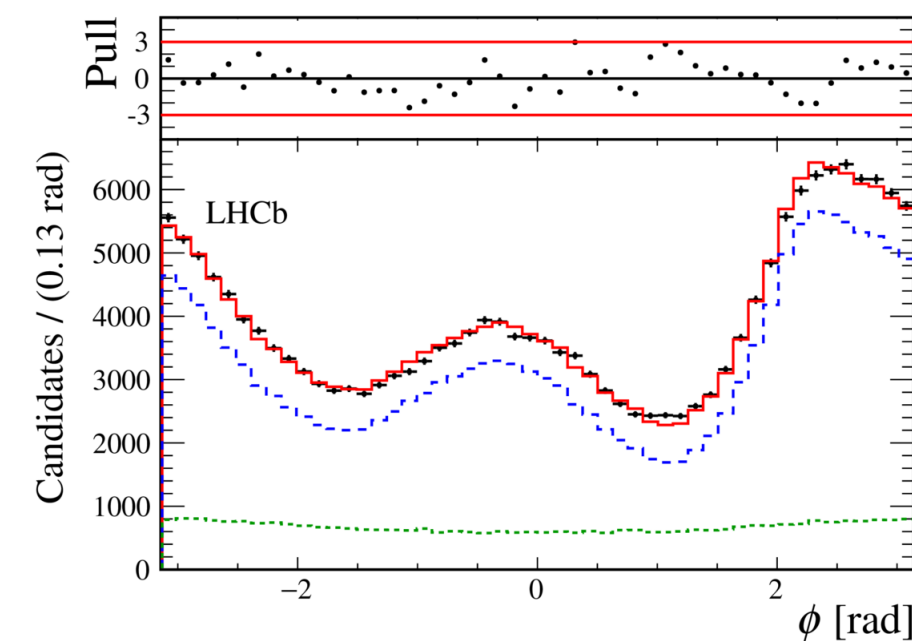
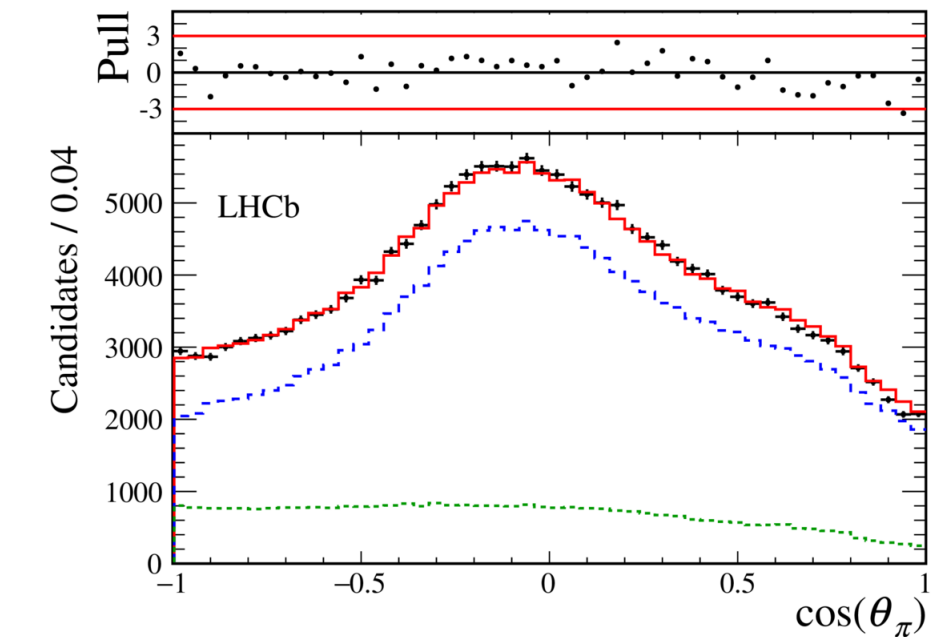
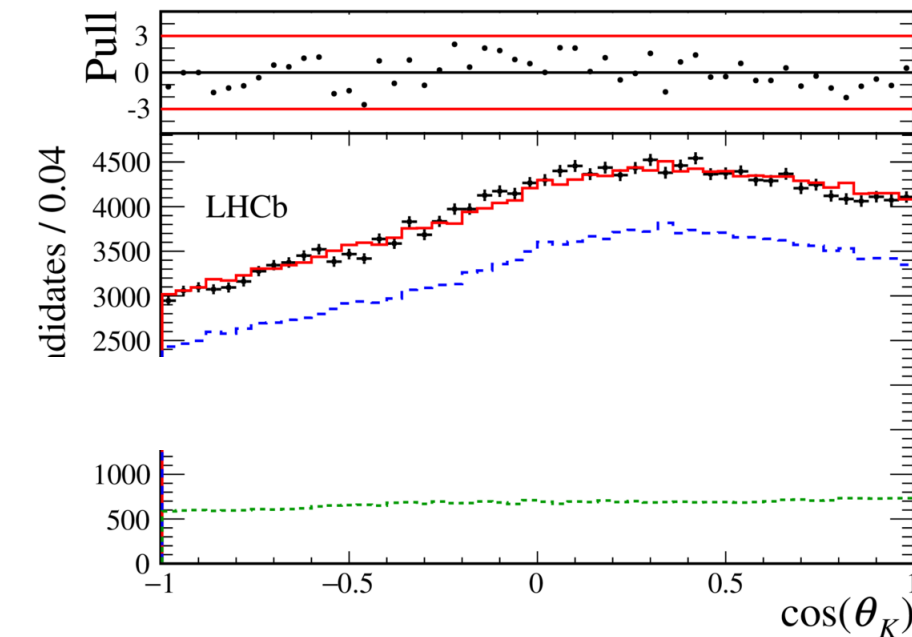
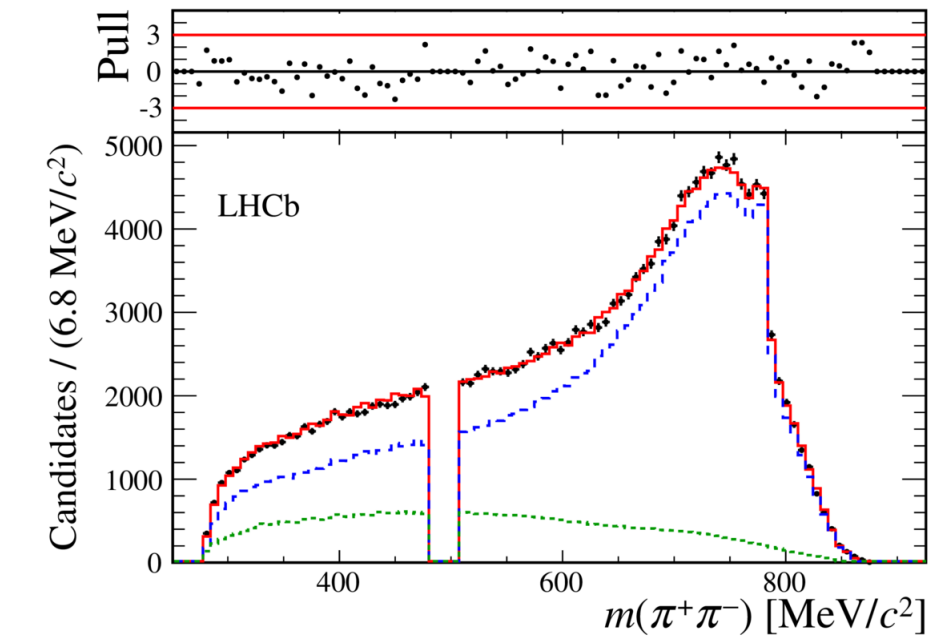
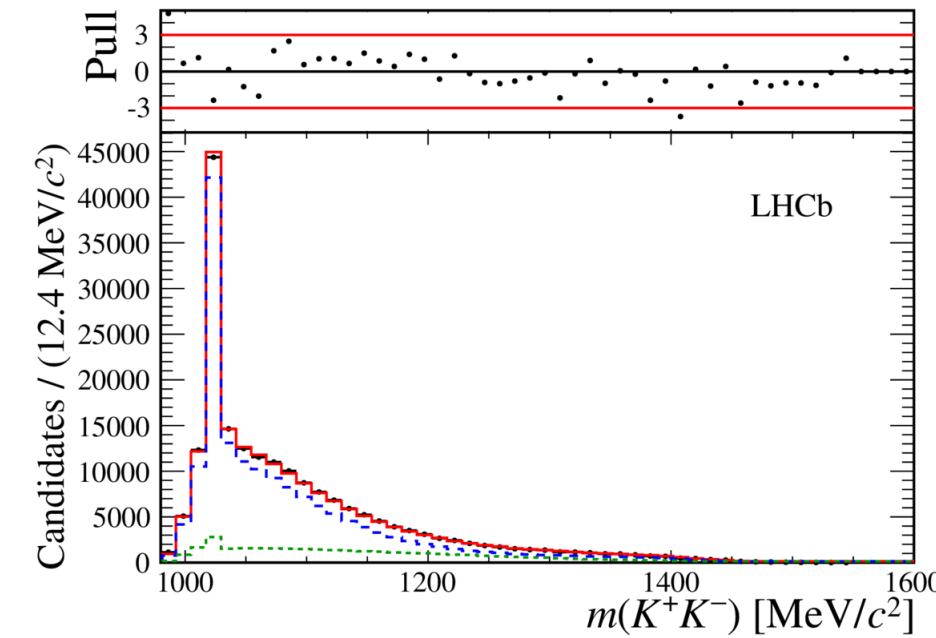


Resonant Structure of $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$

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Fit Results $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$

Amplitude	$ c_k $	$\arg(c_k)$ [rad]	Fit fraction [%]
$D^0 \rightarrow [\phi(1020)(\rho - \omega)^0]_{L=0}$	1 (fixed)	0 (fixed)	$23.82 \pm 0.38 \pm 0.50$
$D^0 \rightarrow K_1(1400)^+ K^-$	$0.614 \pm 0.011 \pm 0.031$	$1.05 \pm 0.02 \pm 0.05$	$19.08 \pm 0.60 \pm 1.46$
$D^0 \rightarrow [K^- \pi^+]_{L=0} [K^+ \pi^-]_{L=0}$	$0.282 \pm 0.004 \pm 0.008$	$-0.60 \pm 0.02 \pm 0.10$	$18.46 \pm 0.35 \pm 0.94$
$D^0 \rightarrow K_1(1270)^+ K^-$	$0.452 \pm 0.011 \pm 0.017$	$2.02 \pm 0.03 \pm 0.05$	$18.05 \pm 0.52 \pm 0.98$
$D^0 \rightarrow [K^*(892)^0 \bar{K}^*(892)^0]_{L=0}$	$0.259 \pm 0.004 \pm 0.018$	$-0.27 \pm 0.02 \pm 0.03$	$9.18 \pm 0.21 \pm 0.28$
$D^0 \rightarrow K^*(1680)^0 [K^- \pi^+]_{L=0}$	$2.359 \pm 0.036 \pm 0.624$	$0.44 \pm 0.02 \pm 0.03$	$6.61 \pm 0.15 \pm 0.37$
$D^0 \rightarrow [K^*(892)^0 \bar{K}^*(892)^0]_{L=1}$	$0.249 \pm 0.005 \pm 0.017$	$1.22 \pm 0.02 \pm 0.03$	$4.90 \pm 0.16 \pm 0.18$
$D^0 \rightarrow K_1(1270)^- K^+$	$0.220 \pm 0.006 \pm 0.011$	$2.09 \pm 0.03 \pm 0.07$	$4.29 \pm 0.18 \pm 0.41$
$D^0 \rightarrow [K^+ K^-]_{L=0} [\pi^+ \pi^-]_{L=0}$	$0.120 \pm 0.003 \pm 0.018$	$-2.49 \pm 0.03 \pm 0.16$	$3.14 \pm 0.17 \pm 0.72$
$D^0 \rightarrow K_1(1400)^- K^+$	$0.236 \pm 0.008 \pm 0.018$	$0.04 \pm 0.04 \pm 0.09$	$2.82 \pm 0.19 \pm 0.39$
$D^0 \rightarrow [K^*(1680)^0 \bar{K}^*(892)^0]_{L=0}$	$0.823 \pm 0.023 \pm 0.218$	$2.99 \pm 0.03 \pm 0.05$	$2.75 \pm 0.15 \pm 0.19$
$D^0 \rightarrow [\bar{K}^*(1680)^0 K^*(892)^0]_{L=1}$	$1.009 \pm 0.022 \pm 0.276$	$-2.76 \pm 0.02 \pm 0.03$	$2.70 \pm 0.11 \pm 0.09$
$D^0 \rightarrow \bar{K}^*(1680)^0 [K^+ \pi^-]_{L=0}$	$1.379 \pm 0.029 \pm 0.373$	$1.06 \pm 0.02 \pm 0.03$	$2.41 \pm 0.09 \pm 0.27$
$D^0 \rightarrow [\phi(1020)(\rho - \omega)^0]_{L=2}$	$1.311 \pm 0.031 \pm 0.018$	$0.54 \pm 0.02 \pm 0.02$	$2.29 \pm 0.08 \pm 0.08$
$D^0 \rightarrow [K^*(892)^0 \bar{K}^*(892)^0]_{L=2}$	$0.652 \pm 0.018 \pm 0.043$	$2.85 \pm 0.03 \pm 0.04$	$1.85 \pm 0.09 \pm 0.10$
$D^0 \rightarrow \phi(1020) [\pi^+ \pi^-]_{L=0}$	$0.049 \pm 0.001 \pm 0.004$	$-1.71 \pm 0.04 \pm 0.37$	$1.49 \pm 0.09 \pm 0.33$
$D^0 \rightarrow [K^*(1680)^0 \bar{K}^*(892)^0]_{L=1}$	$0.747 \pm 0.021 \pm 0.203$	$0.14 \pm 0.03 \pm 0.04$	$1.48 \pm 0.08 \pm 0.10$
$D^0 \rightarrow [\phi(1020)\rho(1450)^0]_{L=1}$	$0.762 \pm 0.035 \pm 0.068$	$1.17 \pm 0.04 \pm 0.04$	$0.98 \pm 0.09 \pm 0.05$
$D^0 \rightarrow a_0(980)^0 f_2(1270)^0$	$1.524 \pm 0.058 \pm 0.189$	$0.21 \pm 0.04 \pm 0.19$	$0.70 \pm 0.05 \pm 0.08$
$D^0 \rightarrow a_1(1260)^+ \pi^-$	$0.189 \pm 0.011 \pm 0.042$	$-2.84 \pm 0.07 \pm 0.38$	$0.46 \pm 0.05 \pm 0.22$
$D^0 \rightarrow a_1(1260)^- \pi^+$	$0.188 \pm 0.014 \pm 0.031$	$0.18 \pm 0.06 \pm 0.43$	$0.45 \pm 0.06 \pm 0.16$
$D^0 \rightarrow [\phi(1020)(\rho - \omega)^0]_{L=1}$	$0.160 \pm 0.011 \pm 0.005$	$0.28 \pm 0.07 \pm 0.03$	$0.43 \pm 0.05 \pm 0.03$
$D^0 \rightarrow [K^*(1680)^0 \bar{K}^*(892)^0]_{L=2}$	$1.218 \pm 0.089 \pm 0.354$	$-2.44 \pm 0.08 \pm 0.15$	$0.33 \pm 0.05 \pm 0.06$
$D^0 \rightarrow [K^+ K^-]_{L=0} (\rho - \omega)^0$	$0.195 \pm 0.015 \pm 0.035$	$2.95 \pm 0.08 \pm 0.29$	$0.27 \pm 0.04 \pm 0.05$
$D^0 \rightarrow [\phi(1020) f_2(1270)^0]_{L=1}$	$1.388 \pm 0.095 \pm 0.257$	$1.71 \pm 0.06 \pm 0.37$	$0.18 \pm 0.02 \pm 0.07$
$D^0 \rightarrow [K^*(892)^0 \bar{K}^*(1430)^0]_{L=1}$	$1.530 \pm 0.086 \pm 0.131$	$2.01 \pm 0.07 \pm 0.09$	$0.18 \pm 0.02 \pm 0.02$
	Sum of fit fractions		$129.32 \pm 1.09 \pm 2.38$
	χ^2/ndf		$9242/8121 = 1.14$

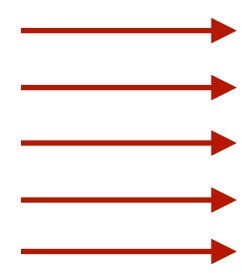


- \bullet Data
- Total fit
- - - Signal model
- ... Background model

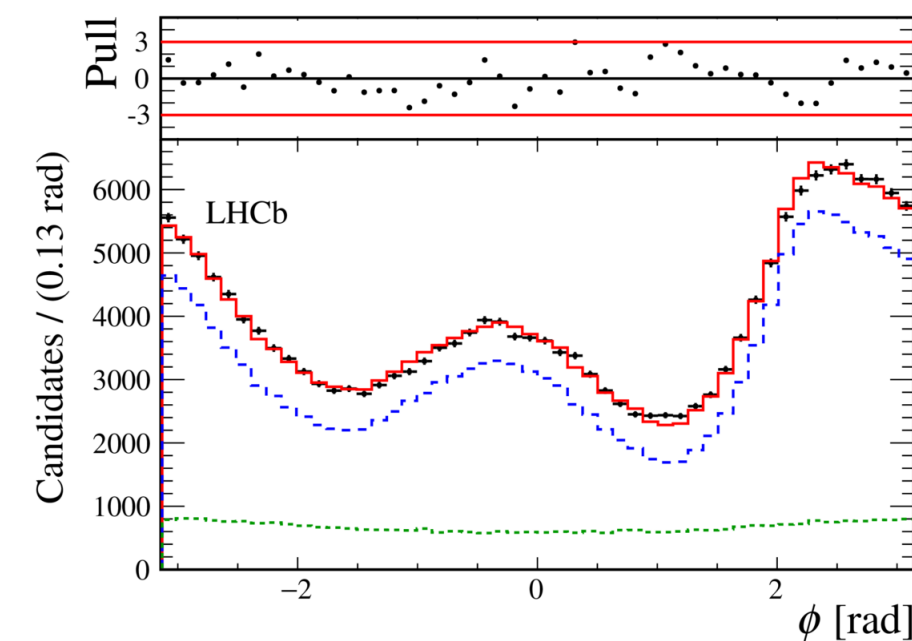
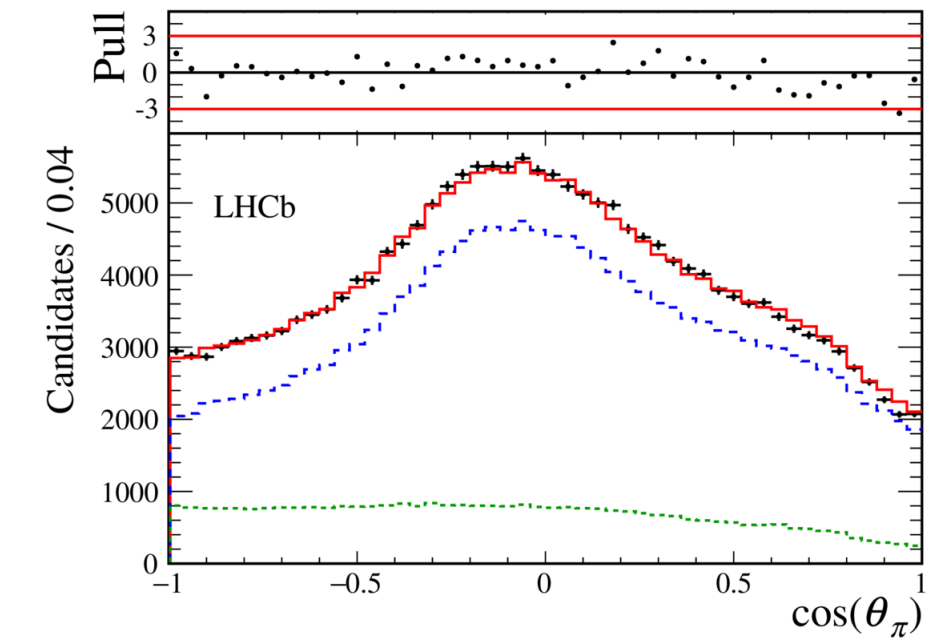
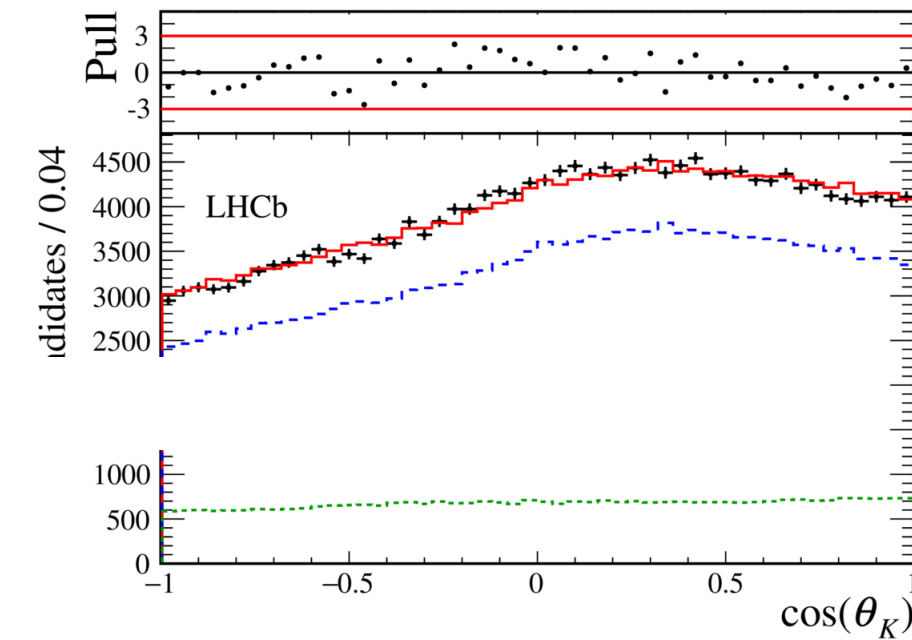
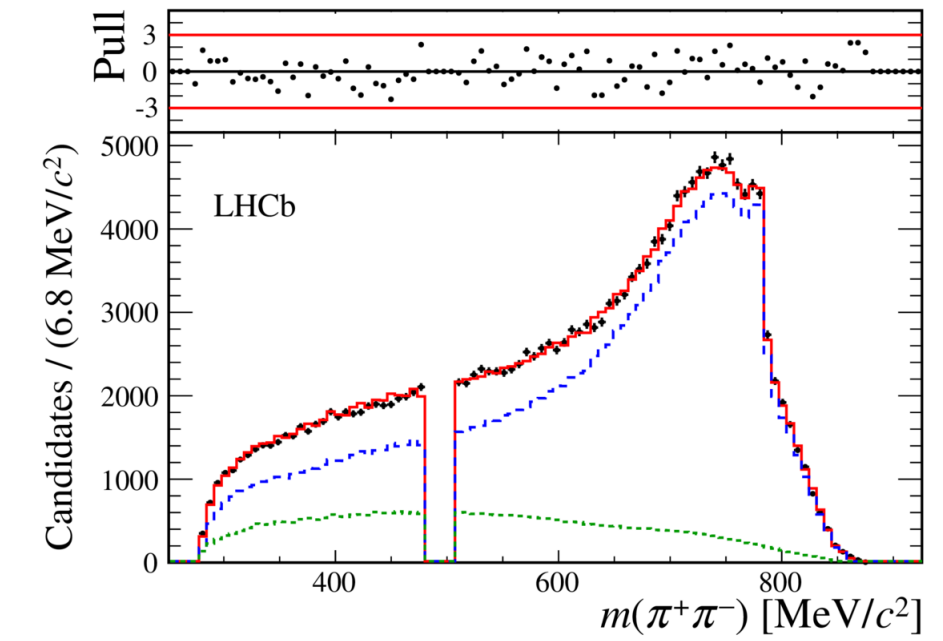
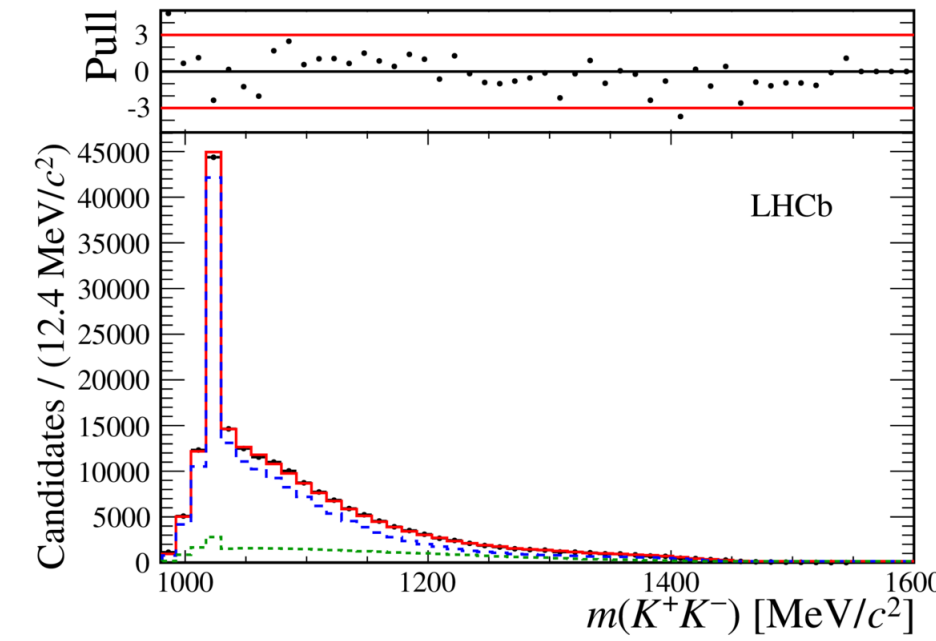
Resonant Structure of $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$

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Fit Results $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$



Amplitude	$ c_k $	$\arg(c_k)$ [rad]	Fit fraction [%]
$D^0 \rightarrow [\phi(1020)(\rho - \omega)^0]_{L=0}$	1 (fixed)	0 (fixed)	$23.82 \pm 0.38 \pm 0.50$
$D^0 \rightarrow K_1(1400)^+ K^-$	$0.614 \pm 0.011 \pm 0.031$	$1.05 \pm 0.02 \pm 0.05$	$19.08 \pm 0.60 \pm 1.46$
$D^0 \rightarrow [K^- \pi^+]_{L=0} [K^+ \pi^-]_{L=0}$	$0.282 \pm 0.004 \pm 0.008$	$-0.60 \pm 0.02 \pm 0.10$	$18.46 \pm 0.35 \pm 0.94$
$D^0 \rightarrow K_1(1270)^+ K^-$	$0.452 \pm 0.011 \pm 0.017$	$2.02 \pm 0.03 \pm 0.05$	$18.05 \pm 0.52 \pm 0.98$
$D^0 \rightarrow [K^*(892)^0 \bar{K}^*(892)^0]_{L=0}$	$0.259 \pm 0.004 \pm 0.018$	$-0.27 \pm 0.02 \pm 0.03$	$9.18 \pm 0.21 \pm 0.28$
$D^0 \rightarrow K^*(1680)^0 [K^- \pi^+]_{L=0}$	$2.359 \pm 0.036 \pm 0.624$	$0.44 \pm 0.02 \pm 0.03$	$6.61 \pm 0.15 \pm 0.37$
$D^0 \rightarrow [K^*(892)^0 \bar{K}^*(892)^0]_{L=1}$	$0.249 \pm 0.005 \pm 0.017$	$1.22 \pm 0.02 \pm 0.03$	$4.90 \pm 0.16 \pm 0.18$
$D^0 \rightarrow K_1(1270)^- K^+$	$0.220 \pm 0.006 \pm 0.011$	$2.09 \pm 0.03 \pm 0.07$	$4.29 \pm 0.18 \pm 0.41$
$D^0 \rightarrow [K^+ K^-]_{L=0} [\pi^+ \pi^-]_{L=0}$	$0.120 \pm 0.003 \pm 0.018$	$-2.49 \pm 0.03 \pm 0.16$	$3.14 \pm 0.17 \pm 0.72$
$D^0 \rightarrow K_1(1400)^- K^+$	$0.236 \pm 0.008 \pm 0.018$	$0.04 \pm 0.04 \pm 0.09$	$2.82 \pm 0.19 \pm 0.39$
$D^0 \rightarrow [K^*(1680)^0 \bar{K}^*(892)^0]_{L=0}$	$0.823 \pm 0.023 \pm 0.218$	$2.99 \pm 0.03 \pm 0.05$	$2.75 \pm 0.15 \pm 0.19$
$D^0 \rightarrow [\bar{K}^*(1680)^0 K^*(892)^0]_{L=1}$	$1.009 \pm 0.022 \pm 0.276$	$-2.76 \pm 0.02 \pm 0.03$	$2.70 \pm 0.11 \pm 0.09$
$D^0 \rightarrow \bar{K}^*(1680)^0 [K^+ \pi^-]_{L=0}$	$1.379 \pm 0.029 \pm 0.373$	$1.06 \pm 0.02 \pm 0.03$	$2.41 \pm 0.09 \pm 0.27$
$D^0 \rightarrow [\phi(1020)(\rho - \omega)^0]_{L=2}$	$1.311 \pm 0.031 \pm 0.018$	$0.54 \pm 0.02 \pm 0.02$	$2.29 \pm 0.08 \pm 0.08$
$D^0 \rightarrow [K^*(892)^0 \bar{K}^*(892)^0]_{L=2}$	$0.652 \pm 0.018 \pm 0.043$	$2.85 \pm 0.03 \pm 0.04$	$1.85 \pm 0.09 \pm 0.10$
$D^0 \rightarrow \phi(1020) [\pi^+ \pi^-]_{L=0}$	$0.049 \pm 0.001 \pm 0.004$	$-1.71 \pm 0.04 \pm 0.37$	$1.49 \pm 0.09 \pm 0.33$
$D^0 \rightarrow [K^*(1680)^0 \bar{K}^*(892)^0]_{L=1}$	$0.747 \pm 0.021 \pm 0.203$	$0.14 \pm 0.03 \pm 0.04$	$1.48 \pm 0.08 \pm 0.10$
$D^0 \rightarrow [\phi(1020)\rho(1450)^0]_{L=1}$	$0.762 \pm 0.035 \pm 0.068$	$1.17 \pm 0.04 \pm 0.04$	$0.98 \pm 0.09 \pm 0.05$
$D^0 \rightarrow a_0(980)^0 f_2(1270)^0$	$1.524 \pm 0.058 \pm 0.189$	$0.21 \pm 0.04 \pm 0.19$	$0.70 \pm 0.05 \pm 0.08$
$D^0 \rightarrow a_1(1260)^+ \pi^-$	$0.189 \pm 0.011 \pm 0.042$	$-2.84 \pm 0.07 \pm 0.38$	$0.46 \pm 0.05 \pm 0.22$
$D^0 \rightarrow a_1(1260)^- \pi^+$	$0.188 \pm 0.014 \pm 0.031$	$0.18 \pm 0.06 \pm 0.43$	$0.45 \pm 0.06 \pm 0.16$
$D^0 \rightarrow [\phi(1020)(\rho - \omega)^0]_{L=1}$	$0.160 \pm 0.011 \pm 0.005$	$0.28 \pm 0.07 \pm 0.03$	$0.43 \pm 0.05 \pm 0.03$
$D^0 \rightarrow [K^*(1680)^0 \bar{K}^*(892)^0]_{L=2}$	$1.218 \pm 0.089 \pm 0.354$	$-2.44 \pm 0.08 \pm 0.15$	$0.33 \pm 0.05 \pm 0.06$
$D^0 \rightarrow [K^+ K^-]_{L=0} (\rho - \omega)^0$	$0.195 \pm 0.015 \pm 0.035$	$2.95 \pm 0.08 \pm 0.29$	$0.27 \pm 0.04 \pm 0.05$
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	Sum of fit fractions		$129.32 \pm 1.09 \pm 2.38$
	χ^2/ndf		$9242/8121 = 1.14$



Data
 Total fit
 Signal model
 Background model

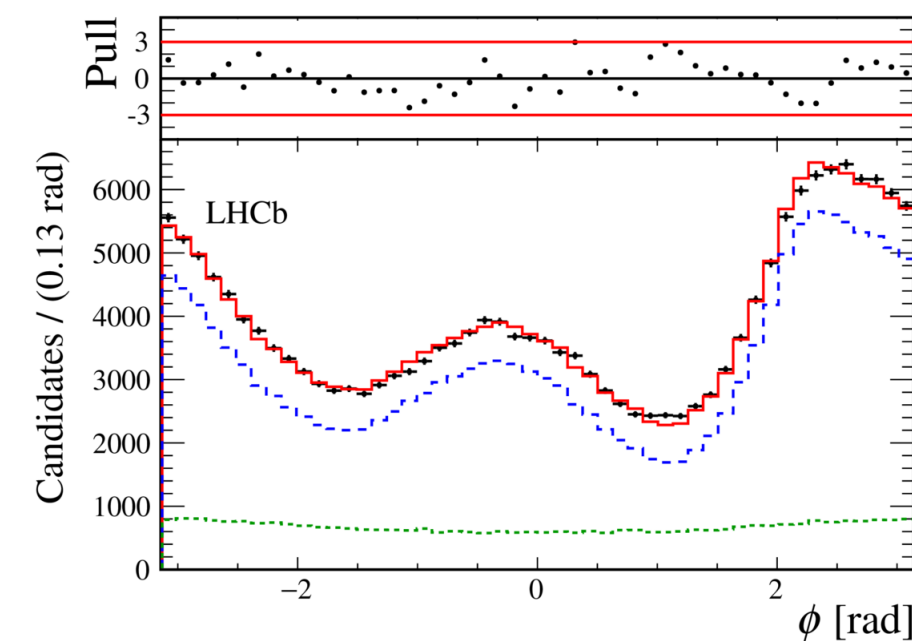
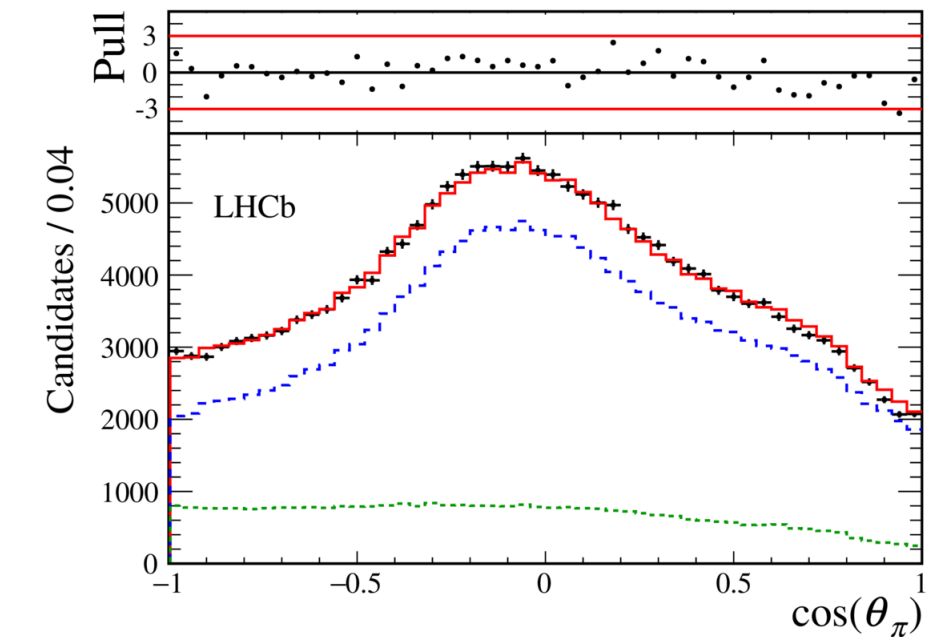
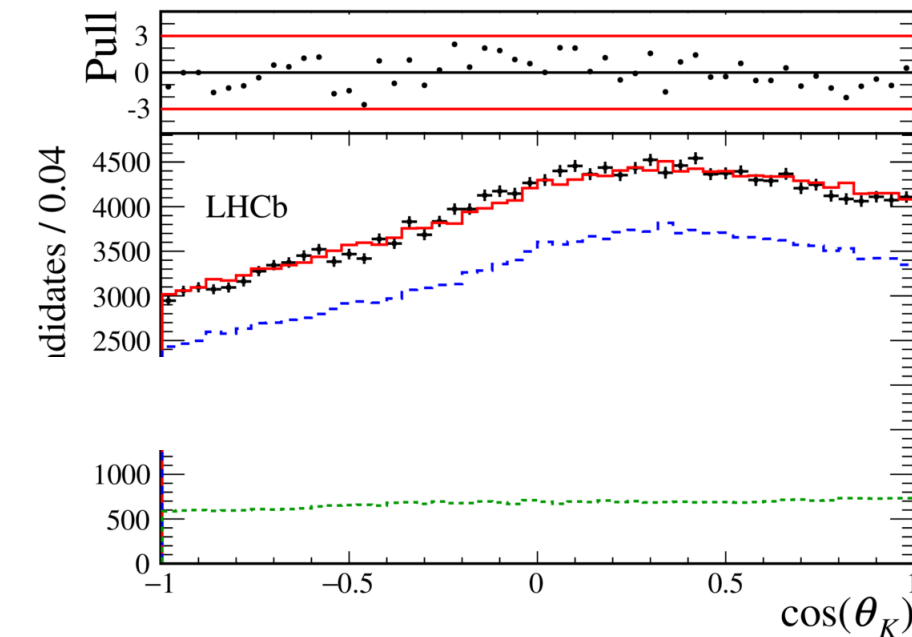
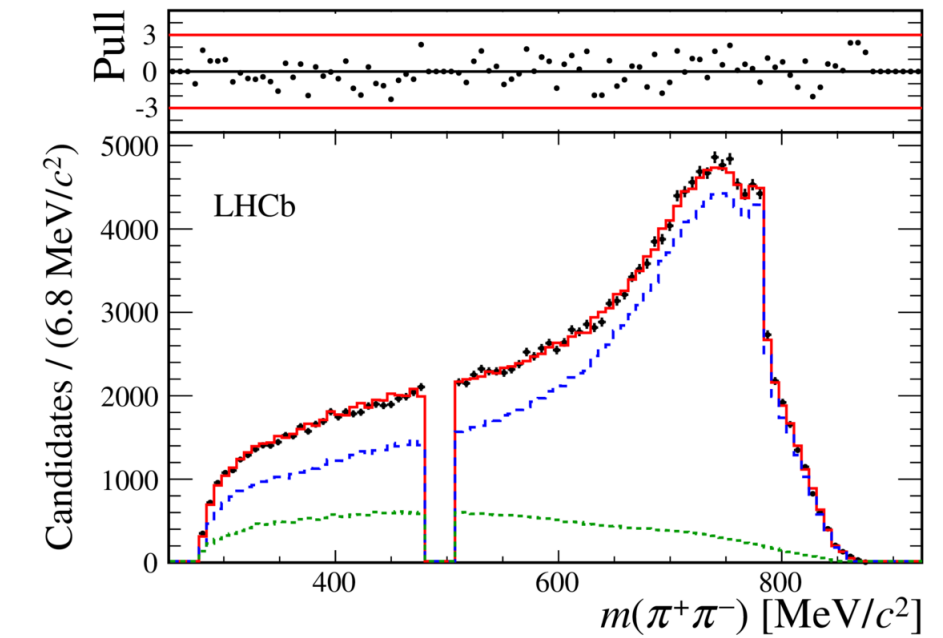
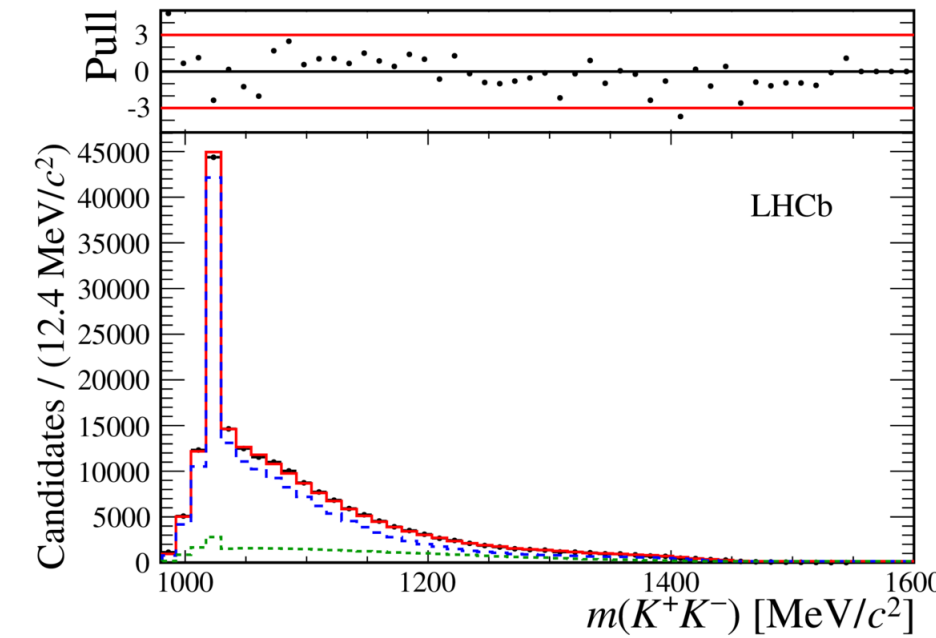


Resonant Structure of $D^0 \rightarrow K^+K^-\pi^+\pi^-$

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Fit Results $D^0 \rightarrow K^+K^-\pi^+\pi^-$

Amplitude	$ c_k $	$\arg(c_k)$ [rad]	Fit fraction [%]
$D^0 \rightarrow [\phi(1020)(\rho - \omega)^0]_{L=0}$	1 (fixed)	0 (fixed)	$23.82 \pm 0.38 \pm 0.50$
$D^0 \rightarrow K_1(1400)^+K^-$	$0.614 \pm 0.011 \pm 0.031$	$1.05 \pm 0.02 \pm 0.05$	$19.08 \pm 0.60 \pm 1.46$
$D^0 \rightarrow [K^-\pi^+]_{L=0}[K^+\pi^-]_{L=0}$	$0.282 \pm 0.004 \pm 0.008$	$-0.60 \pm 0.02 \pm 0.10$	$18.46 \pm 0.35 \pm 0.94$
$D^0 \rightarrow K_1(1270)^+K^-$	$0.452 \pm 0.011 \pm 0.017$	$2.02 \pm 0.03 \pm 0.05$	$18.05 \pm 0.52 \pm 0.98$
$D^0 \rightarrow [K^*(892)^0\bar{K}^*(892)^0]_{L=0}$	$0.259 \pm 0.004 \pm 0.018$	$-0.27 \pm 0.02 \pm 0.03$	$9.18 \pm 0.21 \pm 0.28$
$D^0 \rightarrow K^*(1680)^0[K^-\pi^+]_{L=0}$	$2.359 \pm 0.036 \pm 0.624$	$0.44 \pm 0.02 \pm 0.03$	$6.61 \pm 0.15 \pm 0.37$
$D^0 \rightarrow [K^*(892)^0\bar{K}^*(892)^0]_{L=1}$	$0.249 \pm 0.005 \pm 0.017$	$1.22 \pm 0.02 \pm 0.03$	$4.90 \pm 0.16 \pm 0.18$
$D^0 \rightarrow K_1(1270)^-K^+$	$0.220 \pm 0.006 \pm 0.011$	$2.09 \pm 0.03 \pm 0.07$	$4.29 \pm 0.18 \pm 0.41$
$D^0 \rightarrow [K^+K^-]_{L=0}[\pi^+\pi^-]_{L=0}$	$0.120 \pm 0.003 \pm 0.018$	$-2.49 \pm 0.03 \pm 0.16$	$3.14 \pm 0.17 \pm 0.72$
$D^0 \rightarrow K_1(1400)^-K^+$	$0.236 \pm 0.008 \pm 0.018$	$0.04 \pm 0.04 \pm 0.09$	$2.82 \pm 0.19 \pm 0.39$
$D^0 \rightarrow [K^*(1680)^0\bar{K}^*(892)^0]_{L=0}$	$0.823 \pm 0.023 \pm 0.218$	$2.99 \pm 0.03 \pm 0.05$	$2.75 \pm 0.15 \pm 0.19$
$D^0 \rightarrow [\bar{K}^*(1680)^0K^*(892)^0]_{L=1}$	$1.009 \pm 0.022 \pm 0.276$	$-2.76 \pm 0.02 \pm 0.03$	$2.70 \pm 0.11 \pm 0.09$
$D^0 \rightarrow \bar{K}^*(1680)^0[K^+\pi^-]_{L=0}$	$1.379 \pm 0.029 \pm 0.373$	$1.06 \pm 0.02 \pm 0.03$	$2.41 \pm 0.09 \pm 0.27$
$D^0 \rightarrow [\phi(1020)(\rho - \omega)^0]_{L=2}$	$1.311 \pm 0.031 \pm 0.018$	$0.54 \pm 0.02 \pm 0.02$	$2.29 \pm 0.08 \pm 0.08$
$D^0 \rightarrow [K^*(892)^0\bar{K}^*(892)^0]_{L=2}$	$0.652 \pm 0.018 \pm 0.043$	$2.85 \pm 0.03 \pm 0.04$	$1.85 \pm 0.09 \pm 0.10$
$D^0 \rightarrow \phi(1020)[\pi^+\pi^-]_{L=0}$	$0.049 \pm 0.001 \pm 0.004$	$-1.71 \pm 0.04 \pm 0.37$	$1.49 \pm 0.09 \pm 0.33$
$D^0 \rightarrow [K^*(1680)^0\bar{K}^*(892)^0]_{L=1}$	$0.747 \pm 0.021 \pm 0.203$	$0.14 \pm 0.03 \pm 0.04$	$1.48 \pm 0.08 \pm 0.10$
$D^0 \rightarrow [\phi(1020)\rho(1450)^0]_{L=1}$	$0.762 \pm 0.035 \pm 0.068$	$1.17 \pm 0.04 \pm 0.04$	$0.98 \pm 0.09 \pm 0.05$
$D^0 \rightarrow a_0(980)^0f_2(1270)^0$	$1.524 \pm 0.058 \pm 0.189$	$0.21 \pm 0.04 \pm 0.19$	$0.70 \pm 0.05 \pm 0.08$
$D^0 \rightarrow a_1(1260)^+\pi^-$	$0.189 \pm 0.011 \pm 0.042$	$-2.84 \pm 0.07 \pm 0.38$	$0.46 \pm 0.05 \pm 0.22$
$D^0 \rightarrow a_1(1260)^-\pi^+$	$0.188 \pm 0.014 \pm 0.031$	$0.18 \pm 0.06 \pm 0.43$	$0.45 \pm 0.06 \pm 0.16$
$D^0 \rightarrow [\phi(1020)(\rho - \omega)^0]_{L=1}$	$0.160 \pm 0.011 \pm 0.005$	$0.28 \pm 0.07 \pm 0.03$	$0.43 \pm 0.05 \pm 0.03$
$D^0 \rightarrow [K^*(1680)^0\bar{K}^*(892)^0]_{L=2}$	$1.218 \pm 0.089 \pm 0.354$	$-2.44 \pm 0.08 \pm 0.15$	$0.33 \pm 0.05 \pm 0.06$
$D^0 \rightarrow [K^+K^-]_{L=0}(\rho - \omega)^0$	$0.195 \pm 0.015 \pm 0.035$	$2.95 \pm 0.08 \pm 0.29$	$0.27 \pm 0.04 \pm 0.05$
$D^0 \rightarrow [\phi(1020)f_2(1270)^0]_{L=1}$	$1.388 \pm 0.095 \pm 0.257$	$1.71 \pm 0.06 \pm 0.37$	$0.18 \pm 0.02 \pm 0.07$
$D^0 \rightarrow [K^*(892)^0\bar{K}^*(1430)^0]_{L=1}$	$1.530 \pm 0.086 \pm 0.131$	$2.01 \pm 0.07 \pm 0.09$	$0.18 \pm 0.02 \pm 0.02$
	Sum of fit fractions		$129.32 \pm 1.09 \pm 2.38$
	χ^2/ndf		$9242/8121 = 1.14$



● Data
— Total fit
- - - Signal model
. . . Background model

Strange Resonances in $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$

$K_1(1270)^+$ and $K_1(1400)$

- It is interesting to notice that in this analysis the contributions of $K^* \pi$ and $(\rho - \omega)K$ are more balanced wrt to $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$
- Interference is also much lower in this analysis
- No evidence of $K(1460)$ is found

Amplitude	$ c_k $	$\arg(c_k)$ [rad]	Fit fraction [%]
$a_1(1260)^+ \rightarrow [\phi(1020)\pi^+]_{L=0}$	1 (fixed)	0 (fixed)	100
$K_1(1270)^+ \rightarrow [K^*(892)^0 \pi^+]_{L=0}$	$0.584 \pm 0.016 \pm 0.040$	$0.63 \pm 0.03 \pm 0.05$	$51.22 \pm 1.06 \pm 3.21$
$K_1(1270)^+ \rightarrow [(\rho - \omega)^0 K^+]_{L=0}$	1 (fixed)	0 (fixed)	$49.58 \pm 1.99 \pm 4.35$
$K_1(1270)^+ \rightarrow [K^+ \pi^-]_{L=0} \pi^+$	$0.612 \pm 0.027 \pm 0.094$	$-1.94 \pm 0.04 \pm 0.08$	$6.27 \pm 0.48 \pm 1.66$
$K_1(1270)^+ \rightarrow [K^*(892)^0 \pi^+]_{L=2}$	$0.859 \pm 0.044 \pm 0.060$	$-2.53 \pm 0.04 \pm 0.05$	$2.03 \pm 0.17 \pm 0.20$
$K_1(1270)^+ \rightarrow [\rho(1450)^0 K^+]_{L=0}$	$0.482 \pm 0.068 \pm 0.187$	$-2.37 \pm 0.10 \pm 0.45$	$1.50 \pm 0.47 \pm 1.04$
Sum of fit fractions			$110.60 \pm 2.20 \pm 5.76$
$K_1(1400)^+ \rightarrow [K^*(892)^0 \pi^+]_{L=0}$	1 (fixed)	0 (fixed)	100

$D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$

$K_1(1270)^- \quad m_0 = 1289.81 \pm 0.56 \pm 1.66 \text{ MeV}/c^2; \Gamma_0 = 116.11 \pm 1.65 \pm 2.96 \text{ MeV}/c^2$			
	Partial Fractions [%]	$ g $	$\arg(g)$ [°]
$\rho(770)^0 K^-$	$96.30 \pm 1.64 \pm 6.61$		
$\rho(1450)^0 K^-$	$49.09 \pm 1.58 \pm 11.54$	$2.016 \pm 0.026 \pm 0.211$	$-119.5 \pm 0.9 \pm 2.3$
$\bar{K}^*(892)^0 \pi^-$	$27.08 \pm 0.64 \pm 2.82$	$0.388 \pm 0.007 \pm 0.033$	$-172.6 \pm 1.1 \pm 6.0$
$[K^- \pi^+]^{L=0} \pi^-$	$22.90 \pm 0.72 \pm 1.89$	$0.554 \pm 0.010 \pm 0.037$	$53.2 \pm 1.1 \pm 1.9$
$[\bar{K}^*(892)^0 \pi^-]^{L=2}$	$3.47 \pm 0.17 \pm 0.31$	$0.769 \pm 0.021 \pm 0.048$	$-19.3 \pm 1.6 \pm 6.7$
$\omega(782) [\pi^+ \pi^-] K^-$	$1.65 \pm 0.11 \pm 0.16$	$0.146 \pm 0.005 \pm 0.009$	$9.0 \pm 2.1 \pm 5.7$

Strange Spectroscopy in B decays

Charmonium Decays

- Multibody B decays offer a large spectrum of resonant states, but their Dalitz plots are typically more populated at the borders
- A circumscription of the phase space is possible by studying charmonium resonances, which are abundantly produced in the process $B^+ \rightarrow (c\bar{c})K^+$
- Charmonium in turn decays to light hadrons (π, K) and provides a favourable ground for studying strange mesons resonances
- These studies are also conducted by other experiments

$B^+ \rightarrow K^0_s K^+ K^\pm \pi^\mp$ Decays

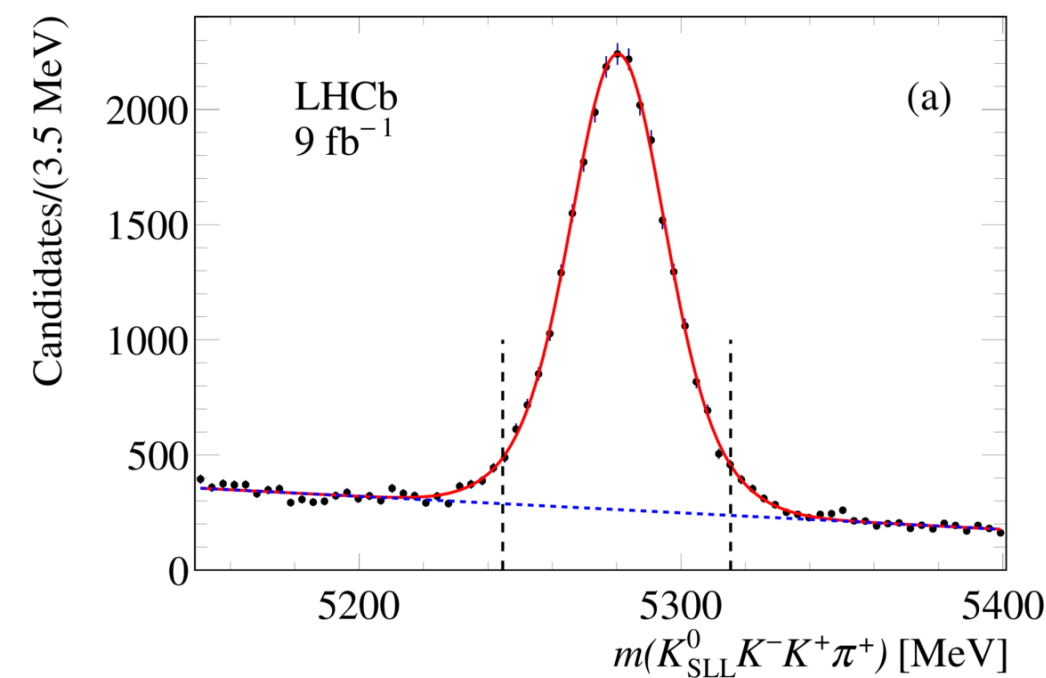
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Lots of Physics

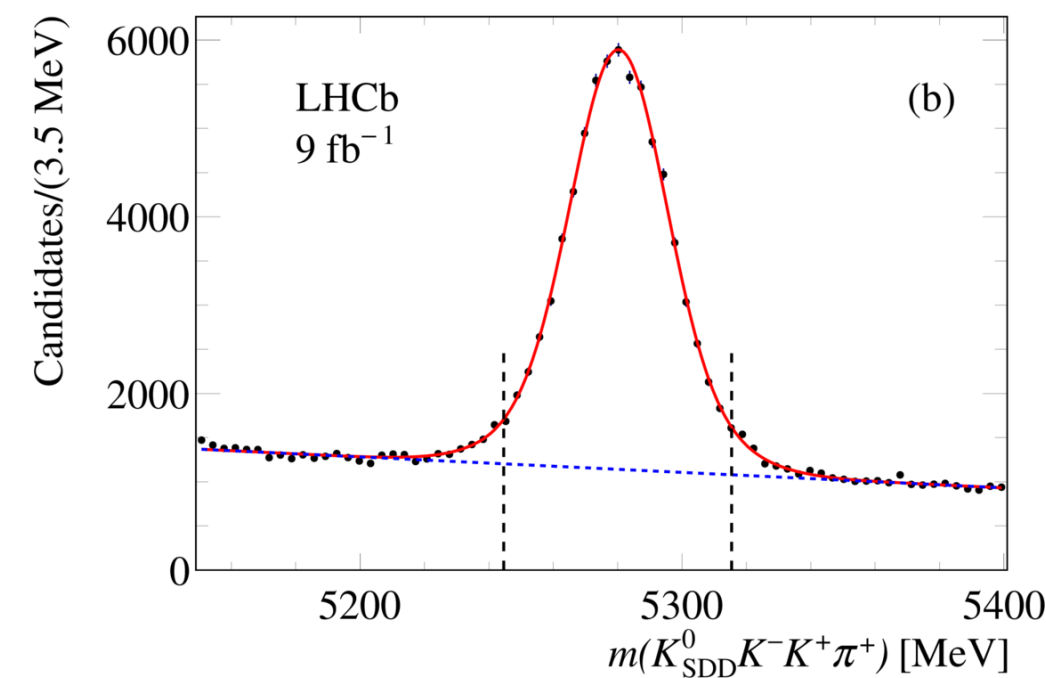
- Branching fractions of $B^+ \rightarrow (c\bar{c})K^+$ decays (not covered in this talk)
- Amplitude analysis of charmonium resonances

Sample

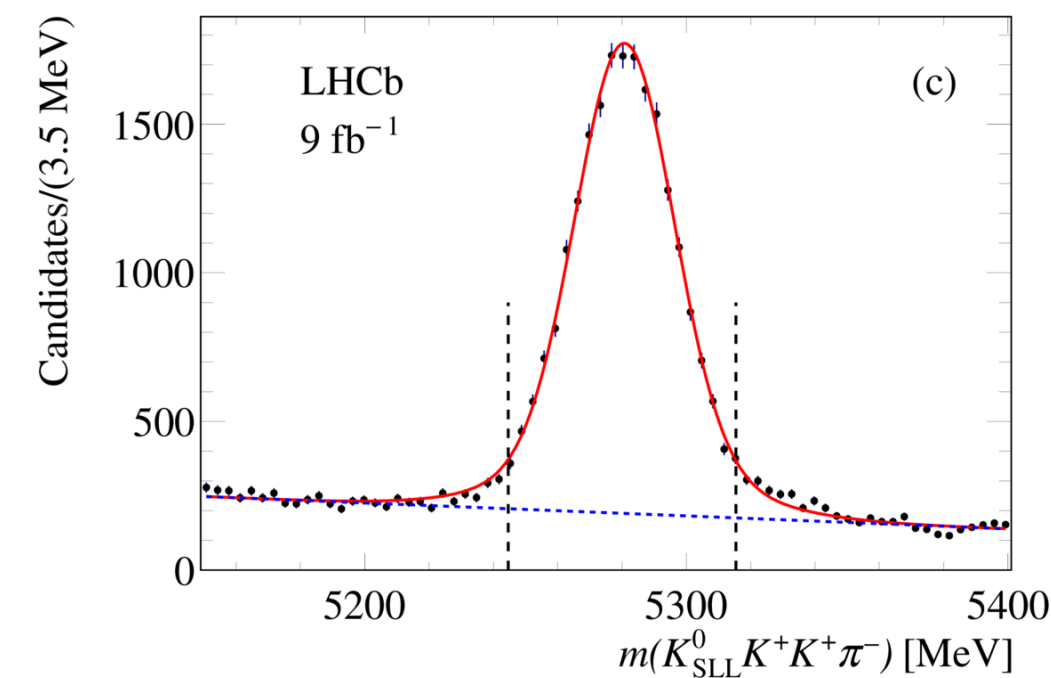
- Full LHCb dataset (2011-2018): 9/fb
- KS candidates reconstructed when decaying inside (LL) and outside (DD) the VELO



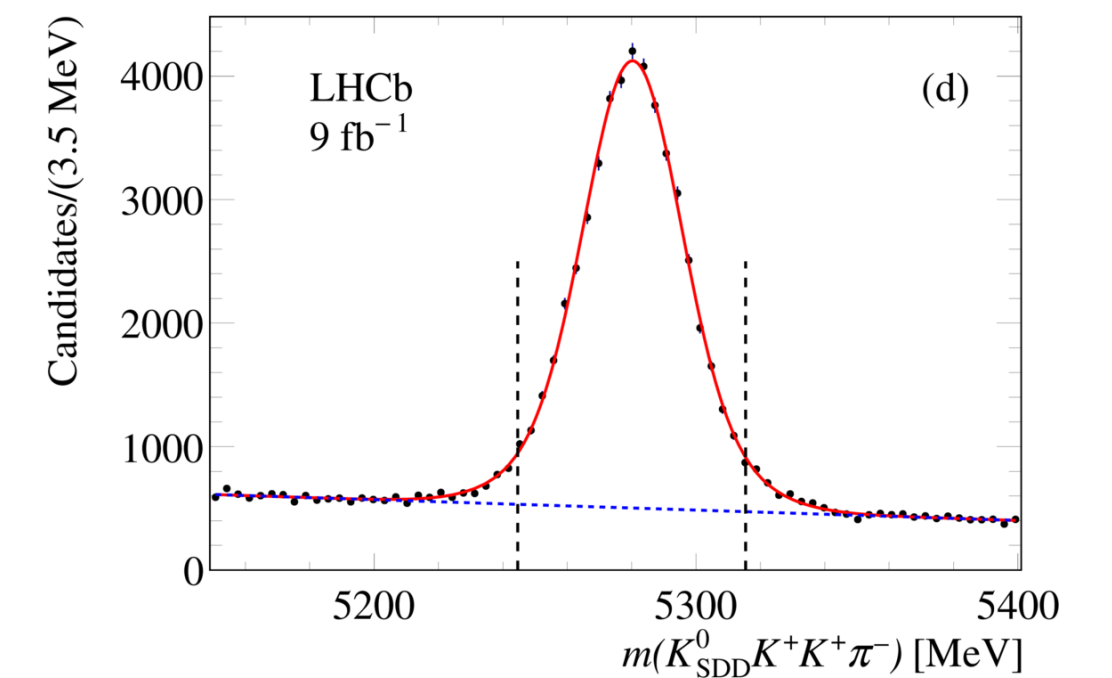
$N_S=21k$
 $P=80.0\%$



$N_S=53k$
 $P=69.5\%$



$N_S=18k$
 $P=82.3\%$

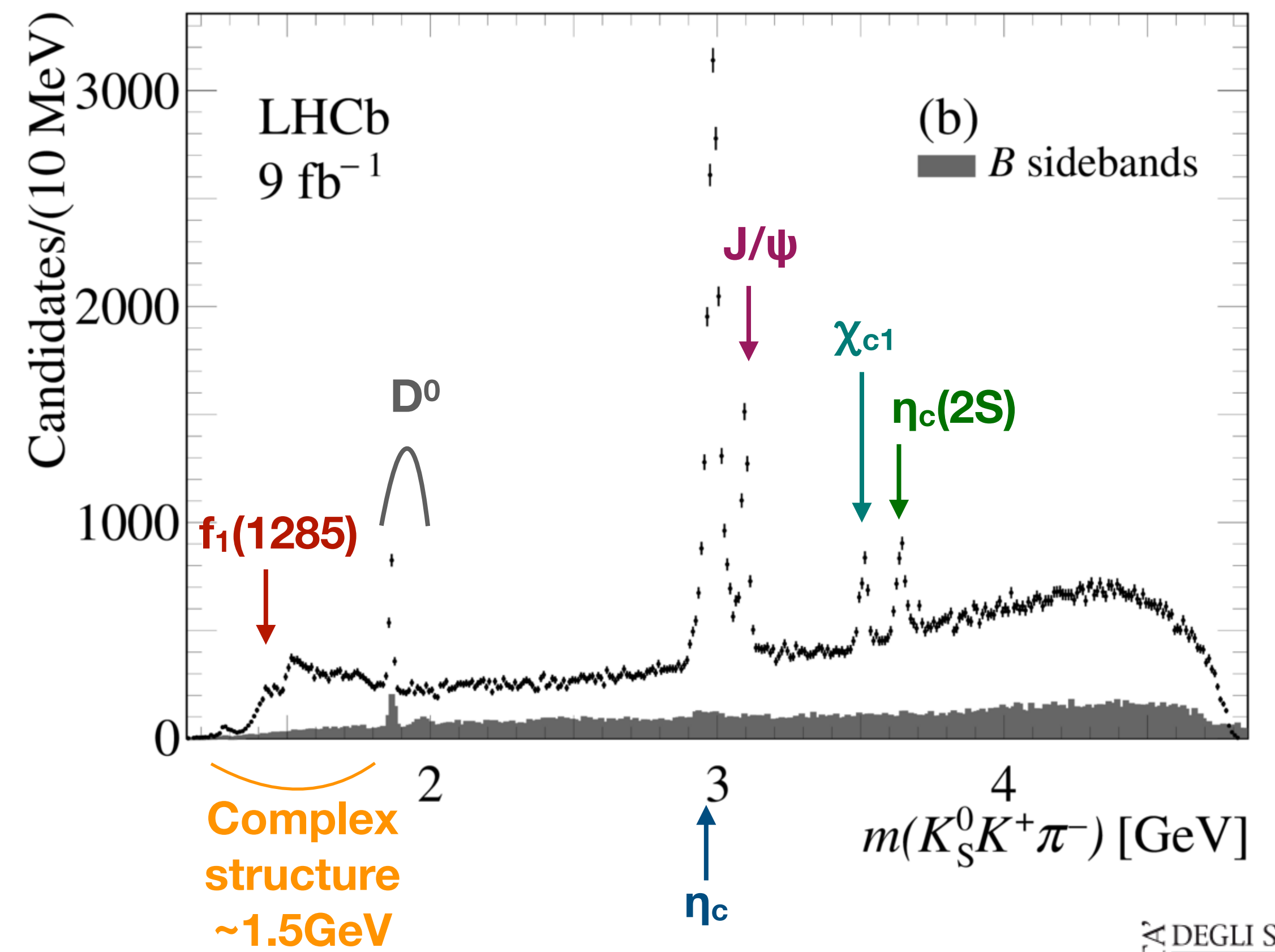
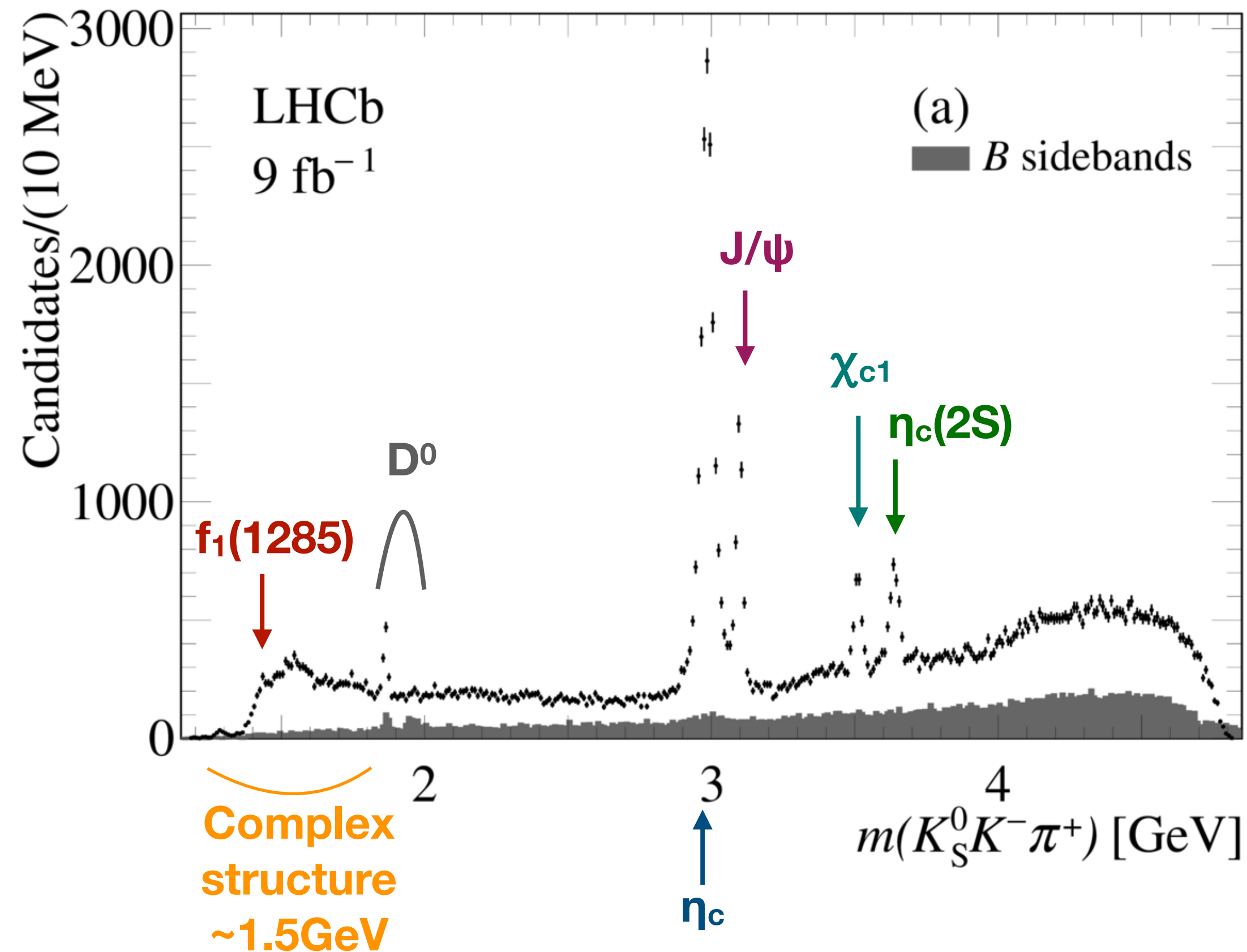


$N_S=40k$
 $P=79.9\%$

$B^+ \rightarrow K_s^0 K^- \pi^+ K^+$ and $B^+ \rightarrow K_s^0 K^+ \pi^- K^+$

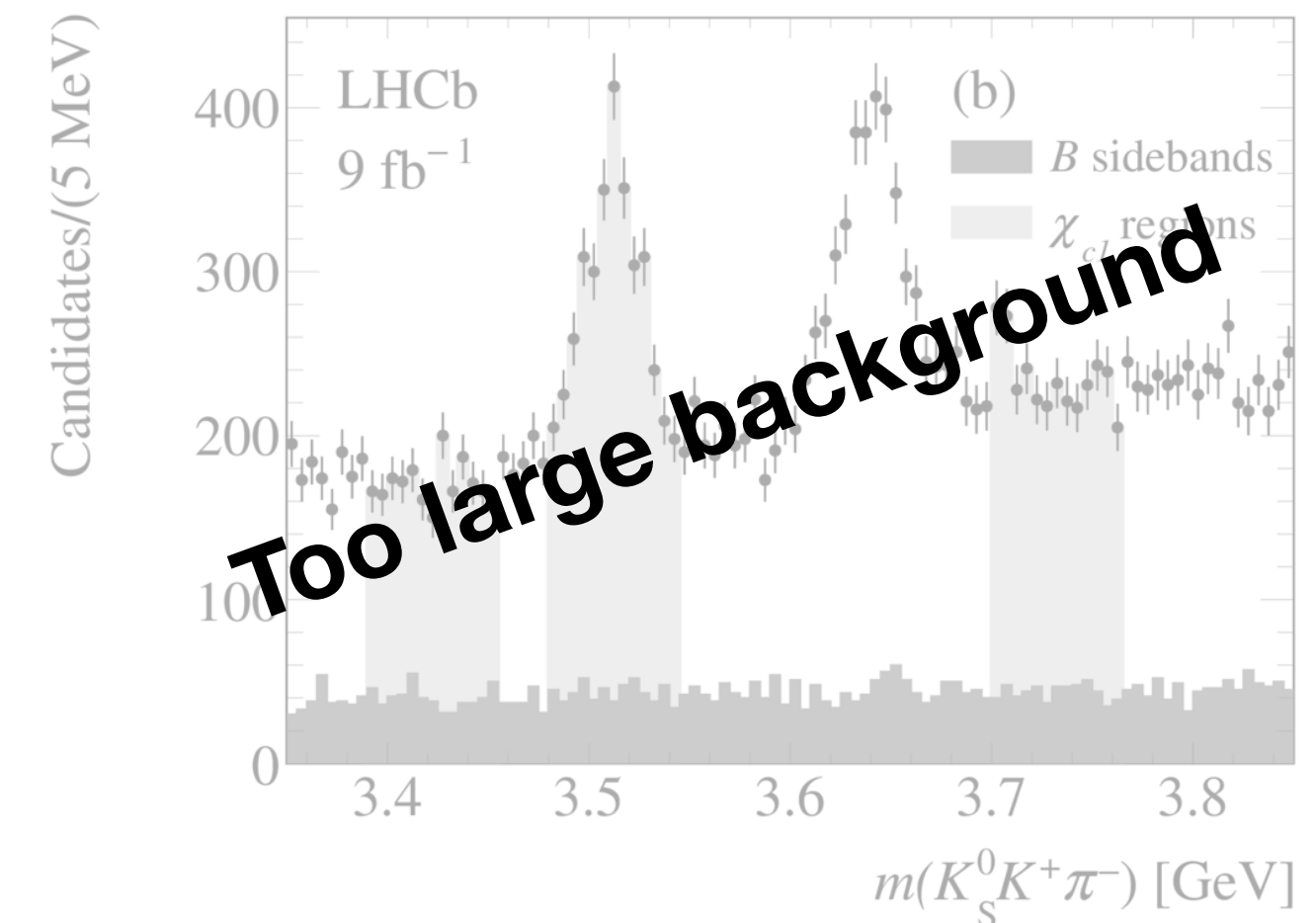
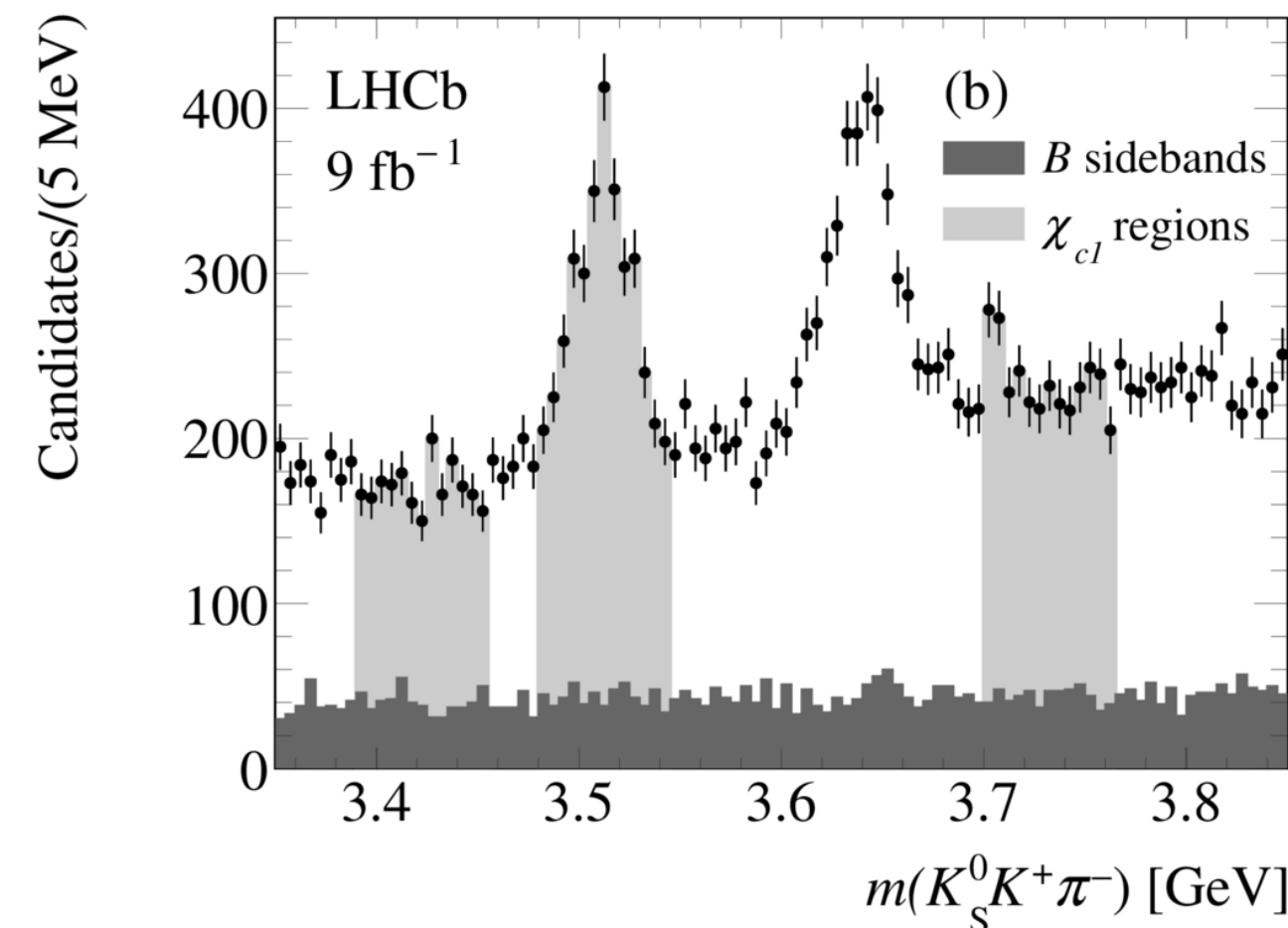
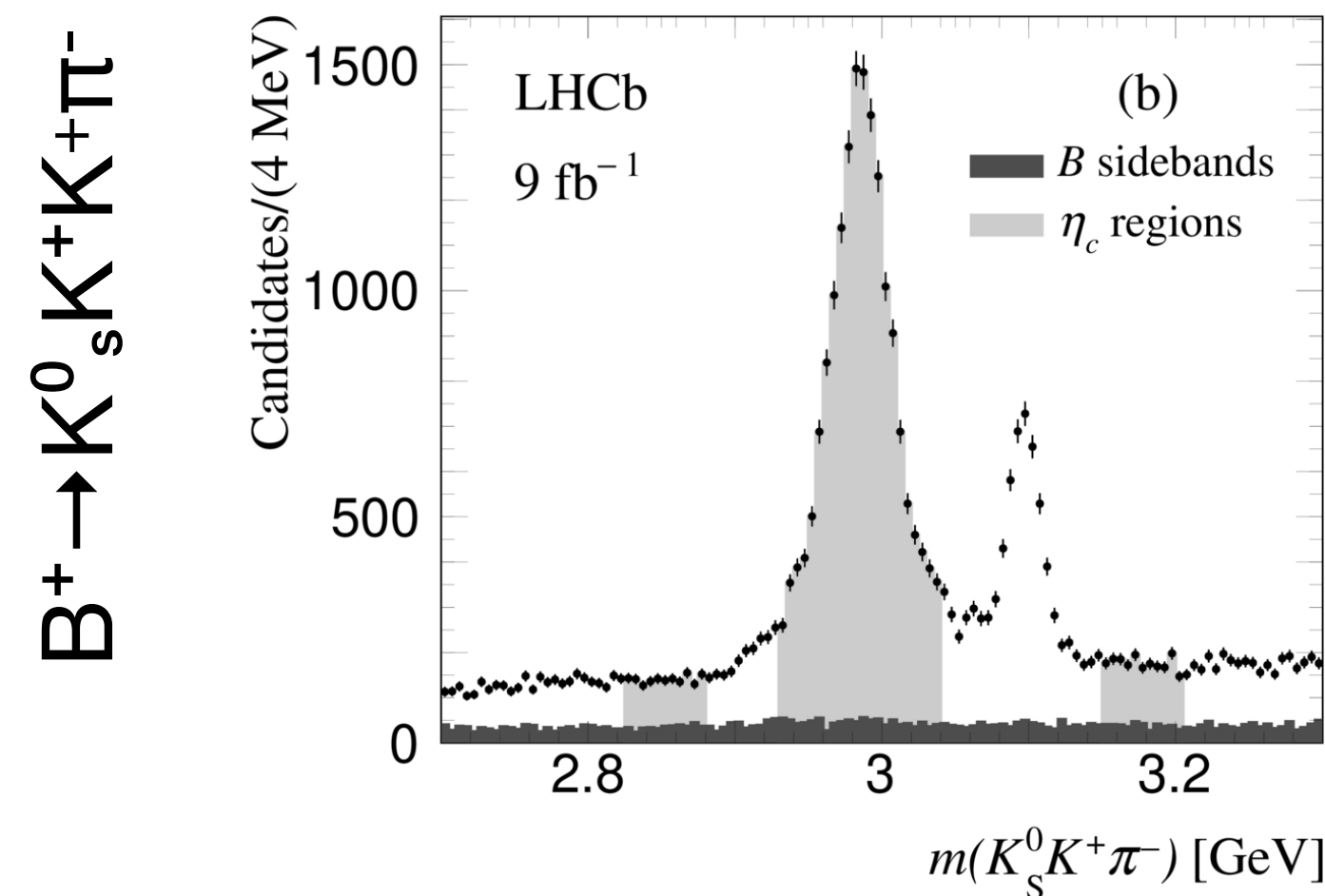
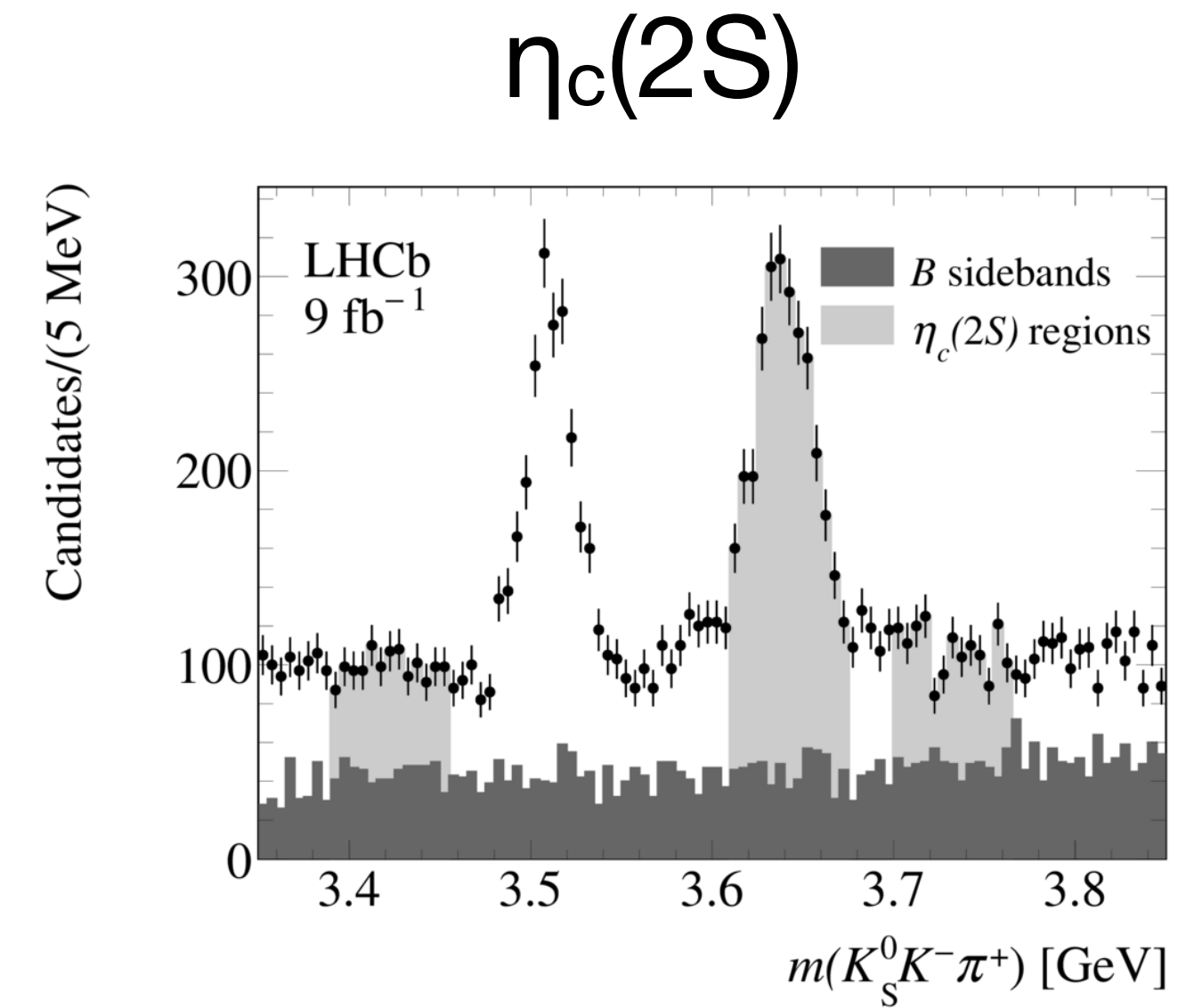
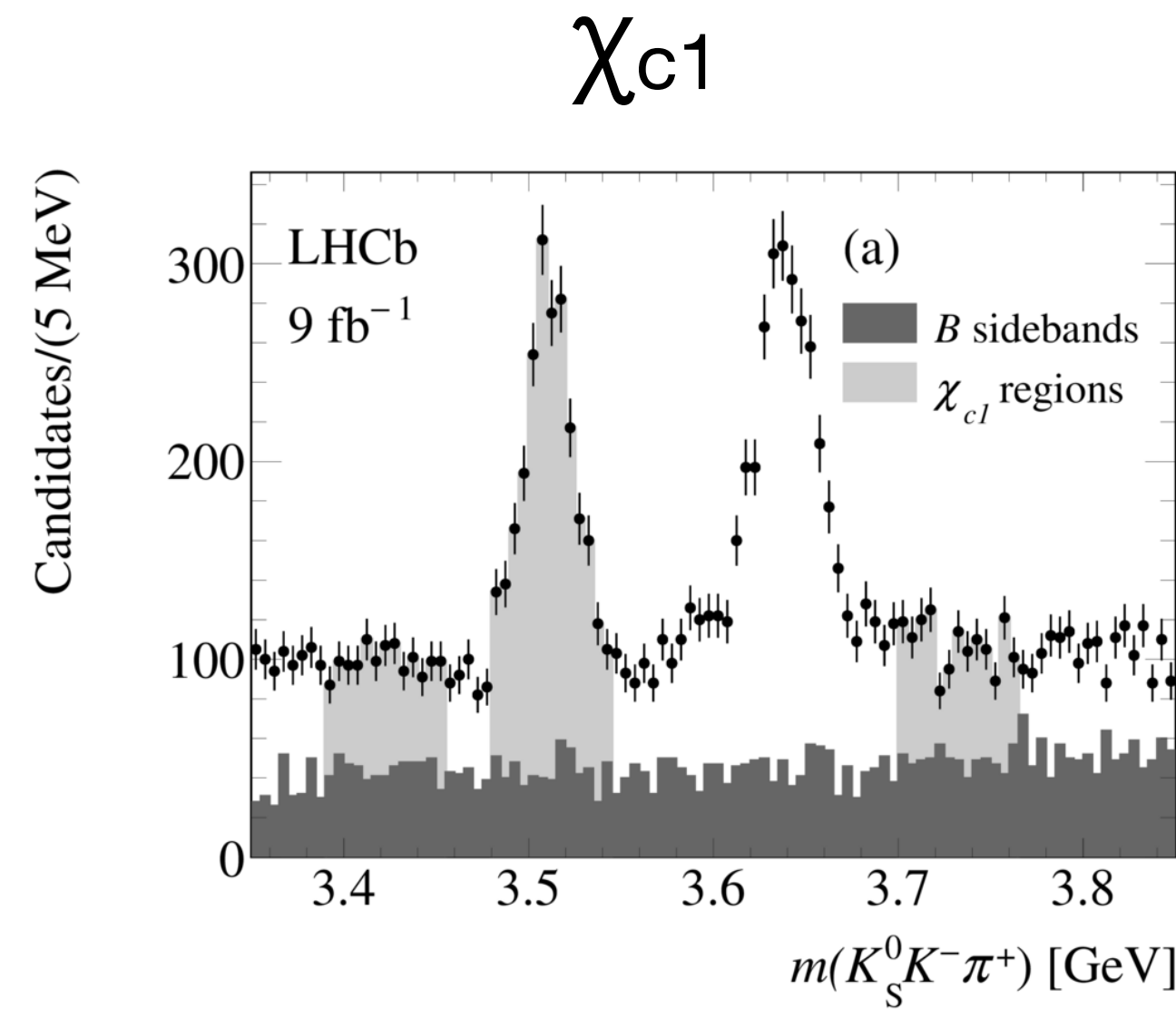
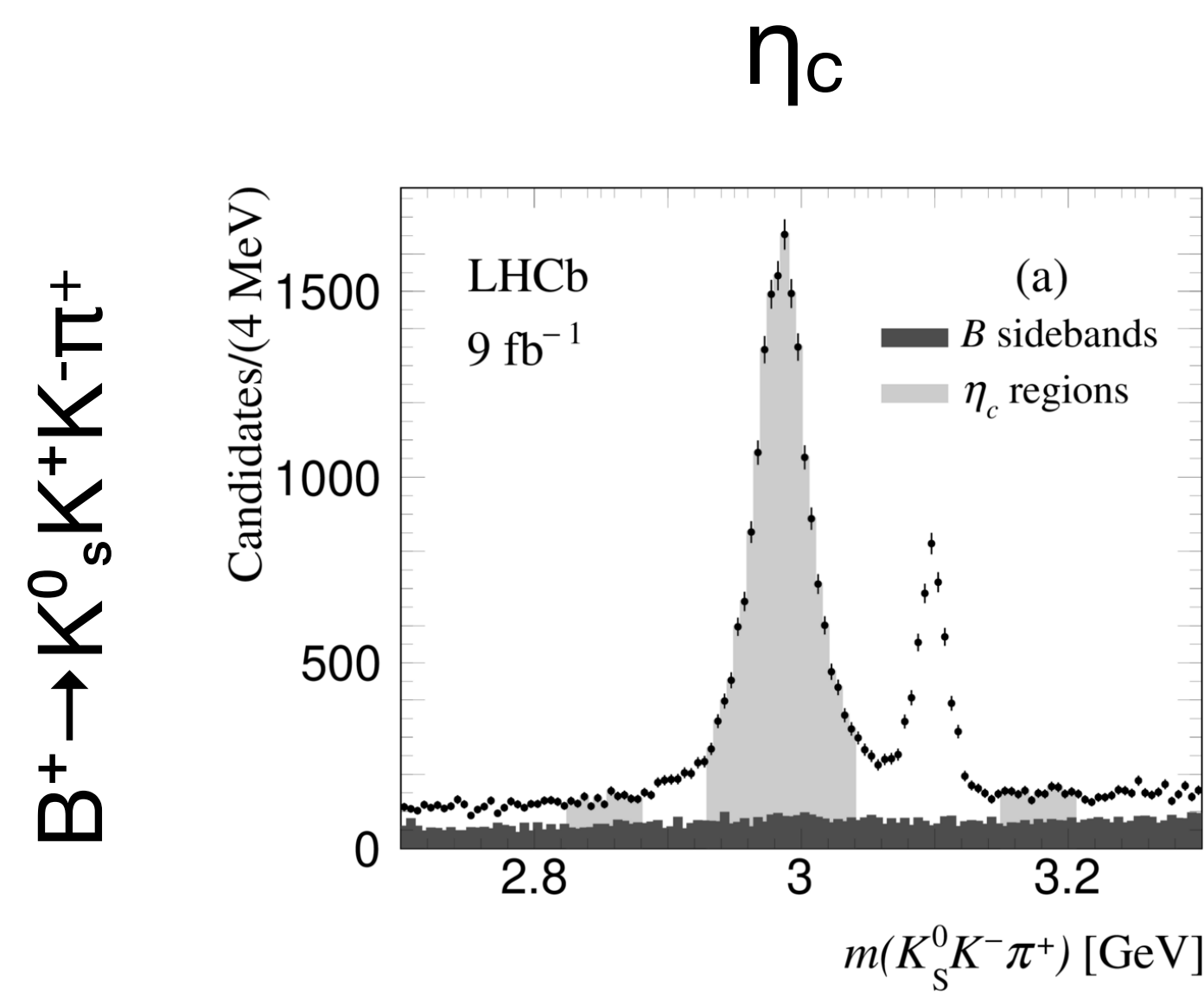
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Charmonium with Good Purity



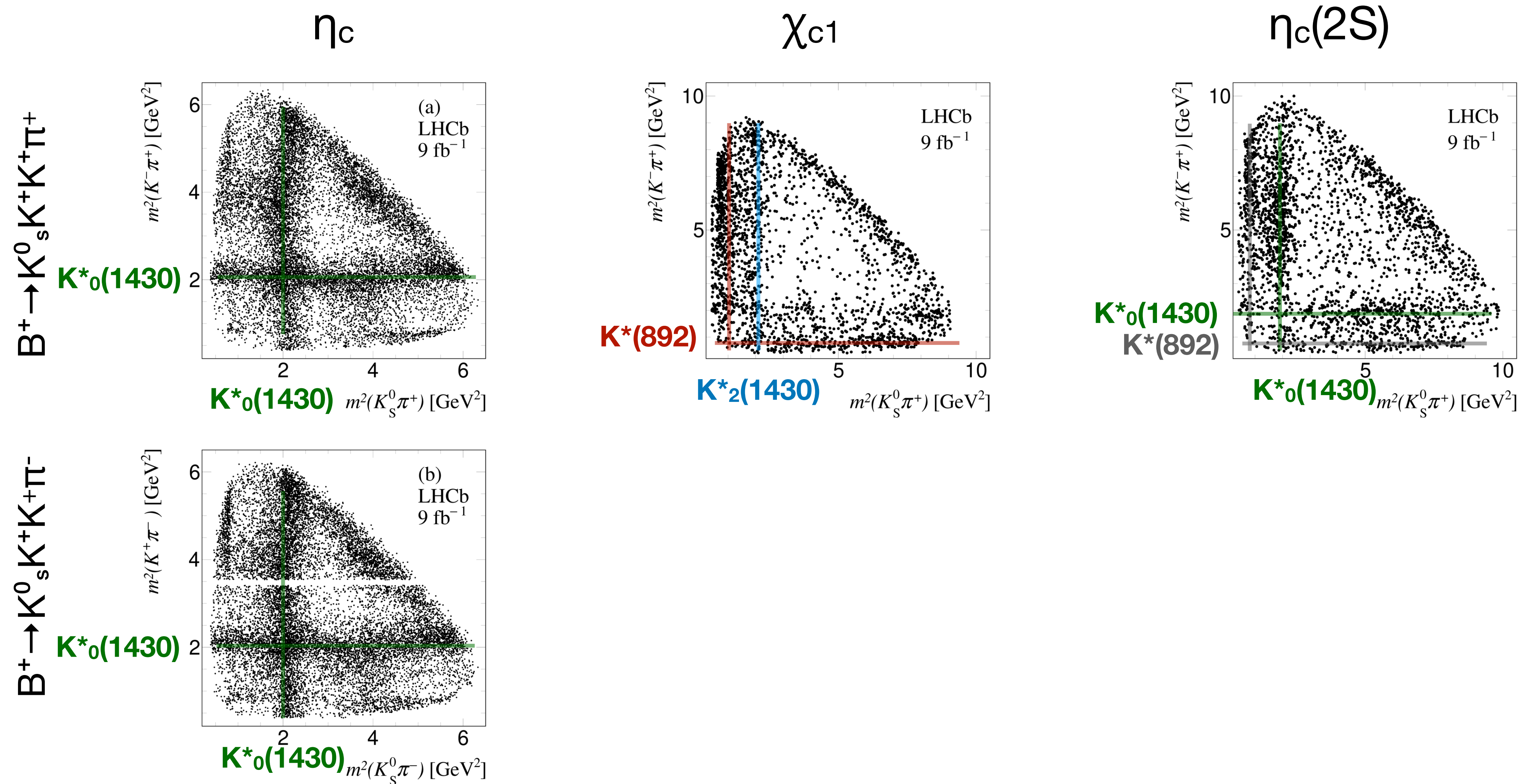
Selection of Charmonium Resonances

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Dalitz Plot of Charmonium Resonances

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Dalitz Plot Analysis of $\eta_c \rightarrow K^0_s K \pi$ Decays

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2D Dalitz

- Approximately 15k signal candidates per channel
- $m^2(K^0\pi)$ vs. $m^2(K\pi)$
- Efficiency parametrised as function of $m^2(K^0\pi)$ and $\cos\theta_\pi$
- Two analyses: Quasi Model Independent and Isobar to gain insights of the $K\pi$ S-wave

QMI: amplitude and phase of S-wave fitted at equally spaced intervals of 50 MeV

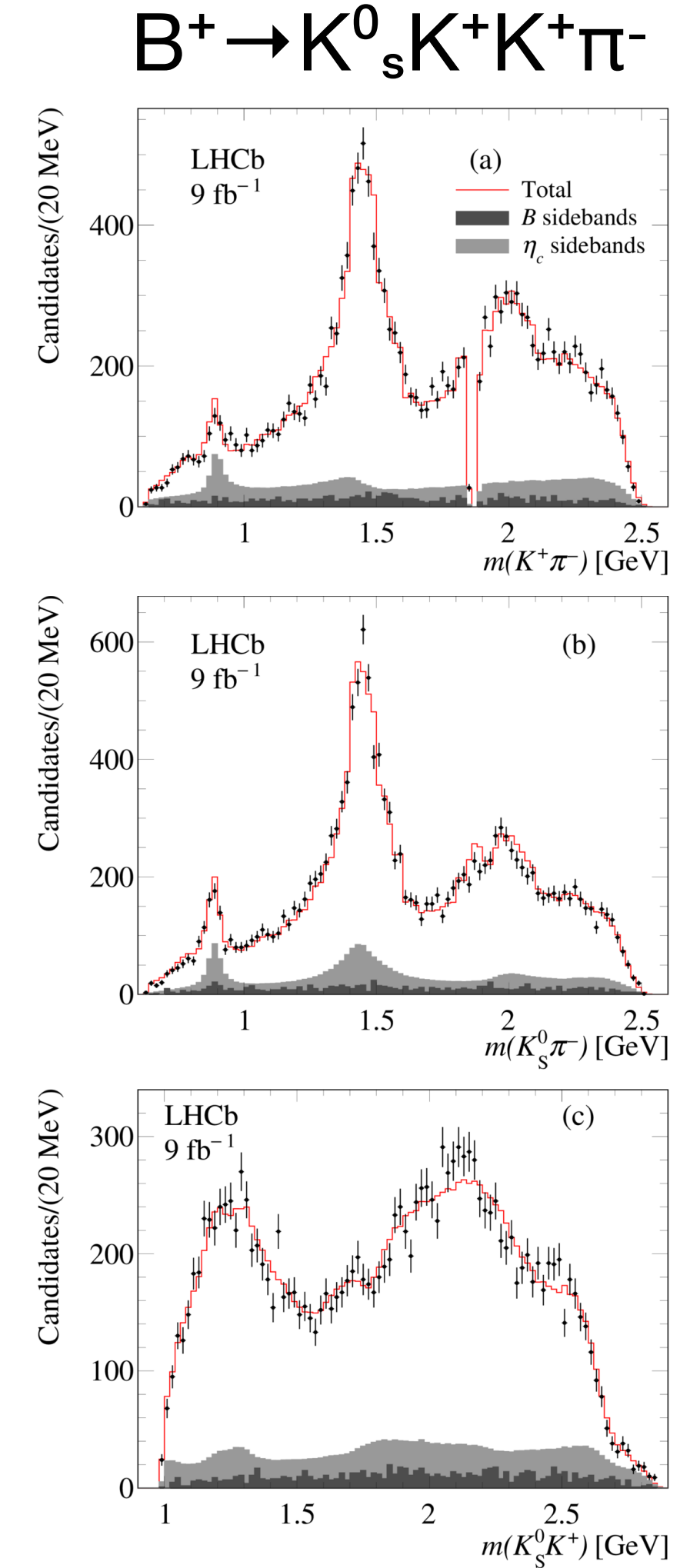
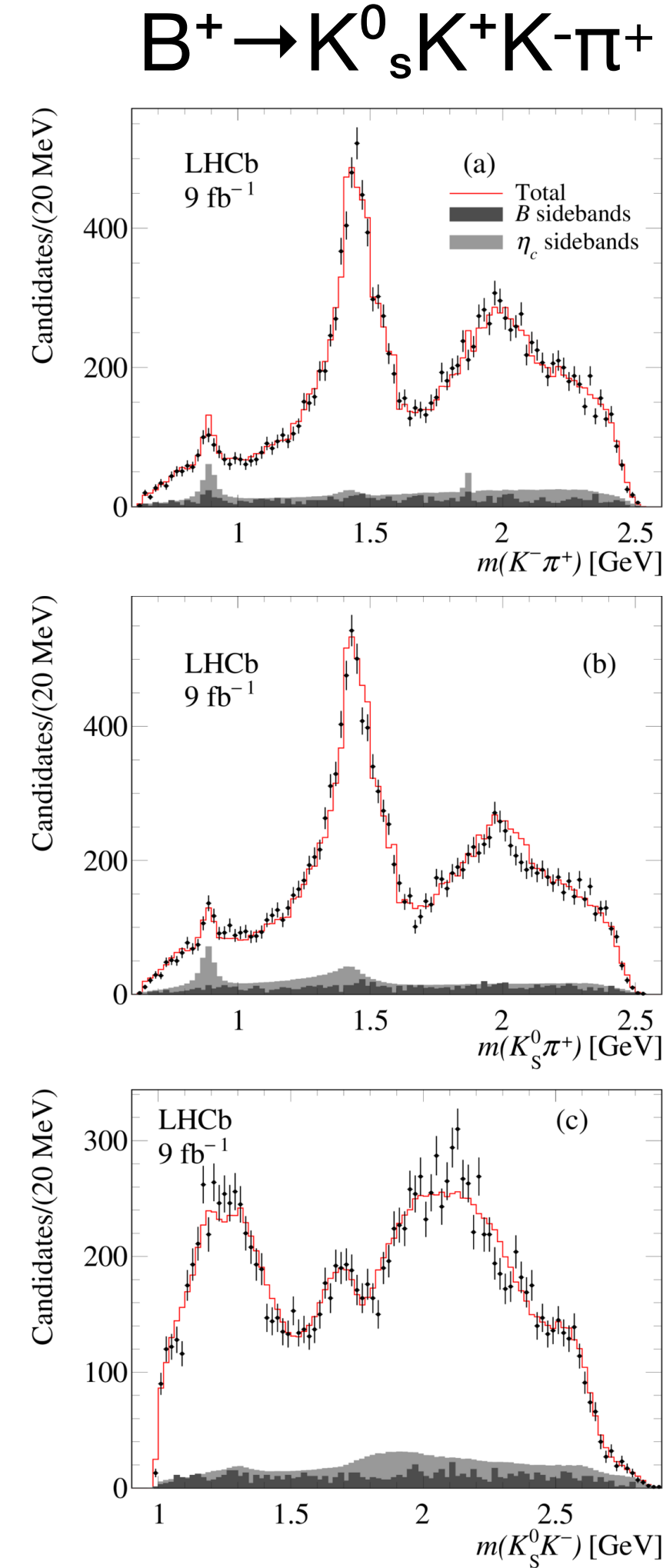
$$A_j = \frac{1}{\sqrt{2}} \left(a_j^{K\pi} e^{i\varphi_j^{K\pi}} + a_j^{K^0\pi} e^{i\varphi_j^{K^0\pi}} \right), a_j^{K\pi} = a_j^{K^0\pi} \text{ and } \varphi_j^{K\pi} = \varphi_j^{K^0\pi}$$

Isobar: Fit data with superposition of known and poorly known resonances

Quasi Model Independent $K\pi$ S-wave Fit

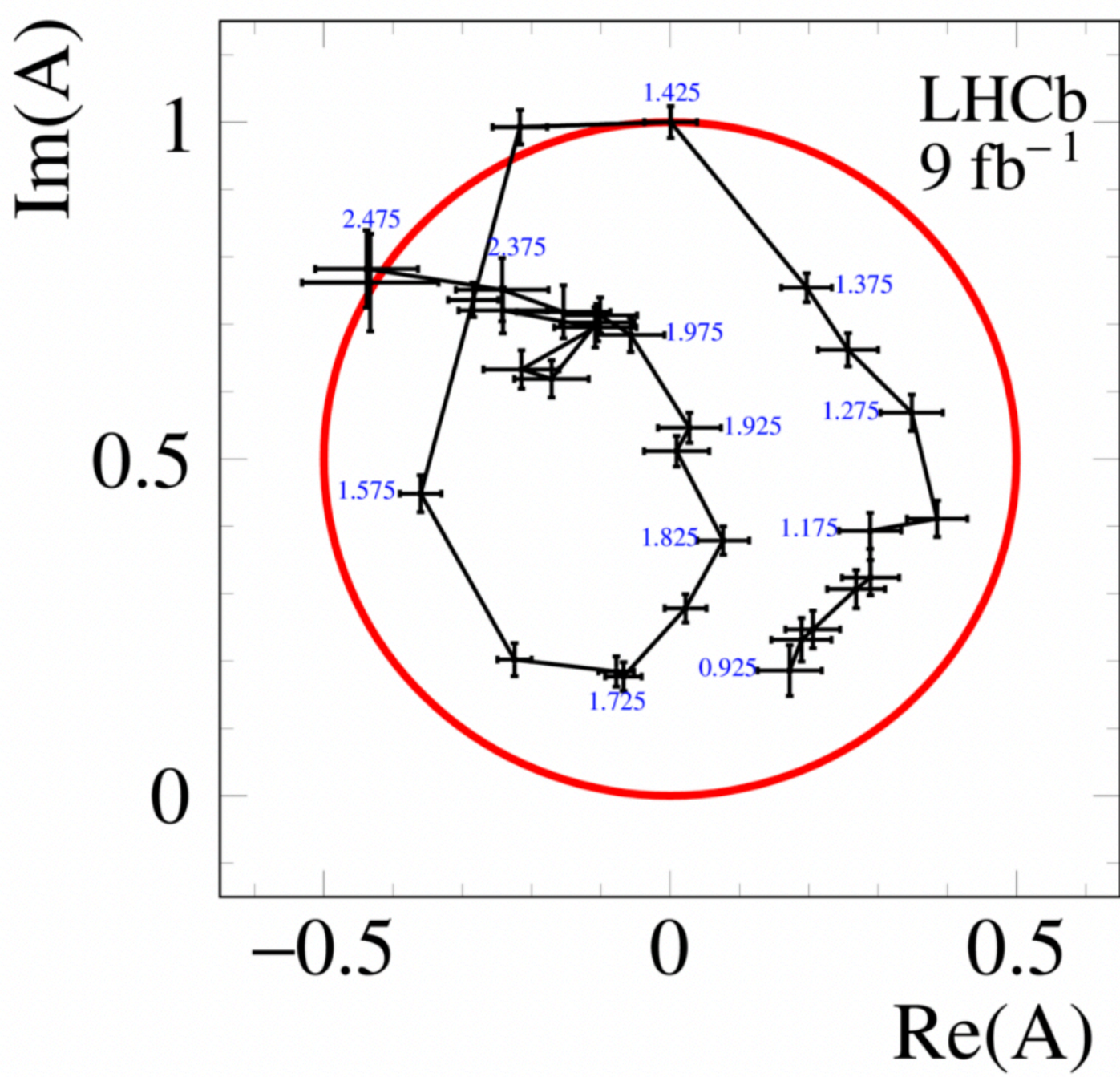
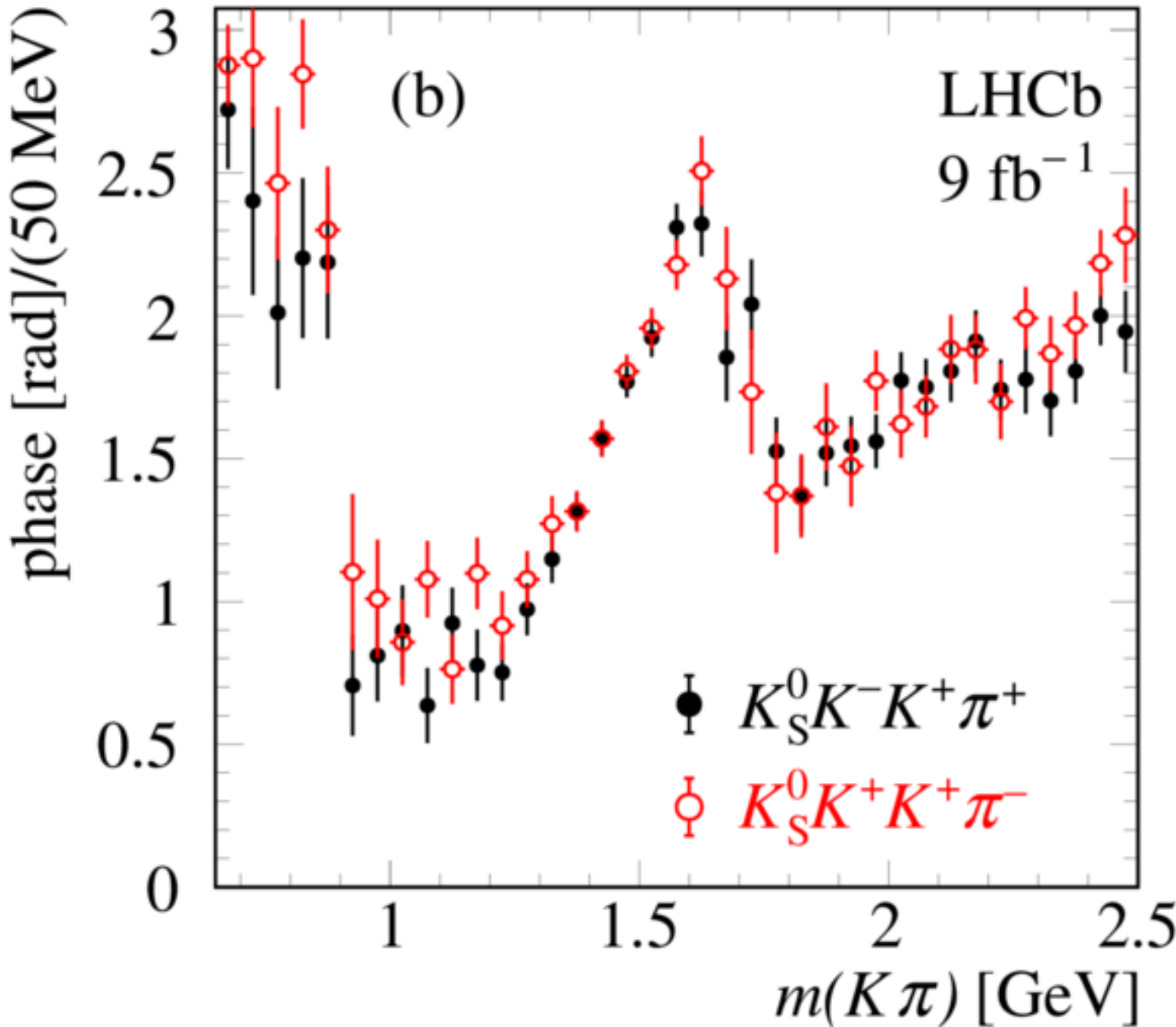
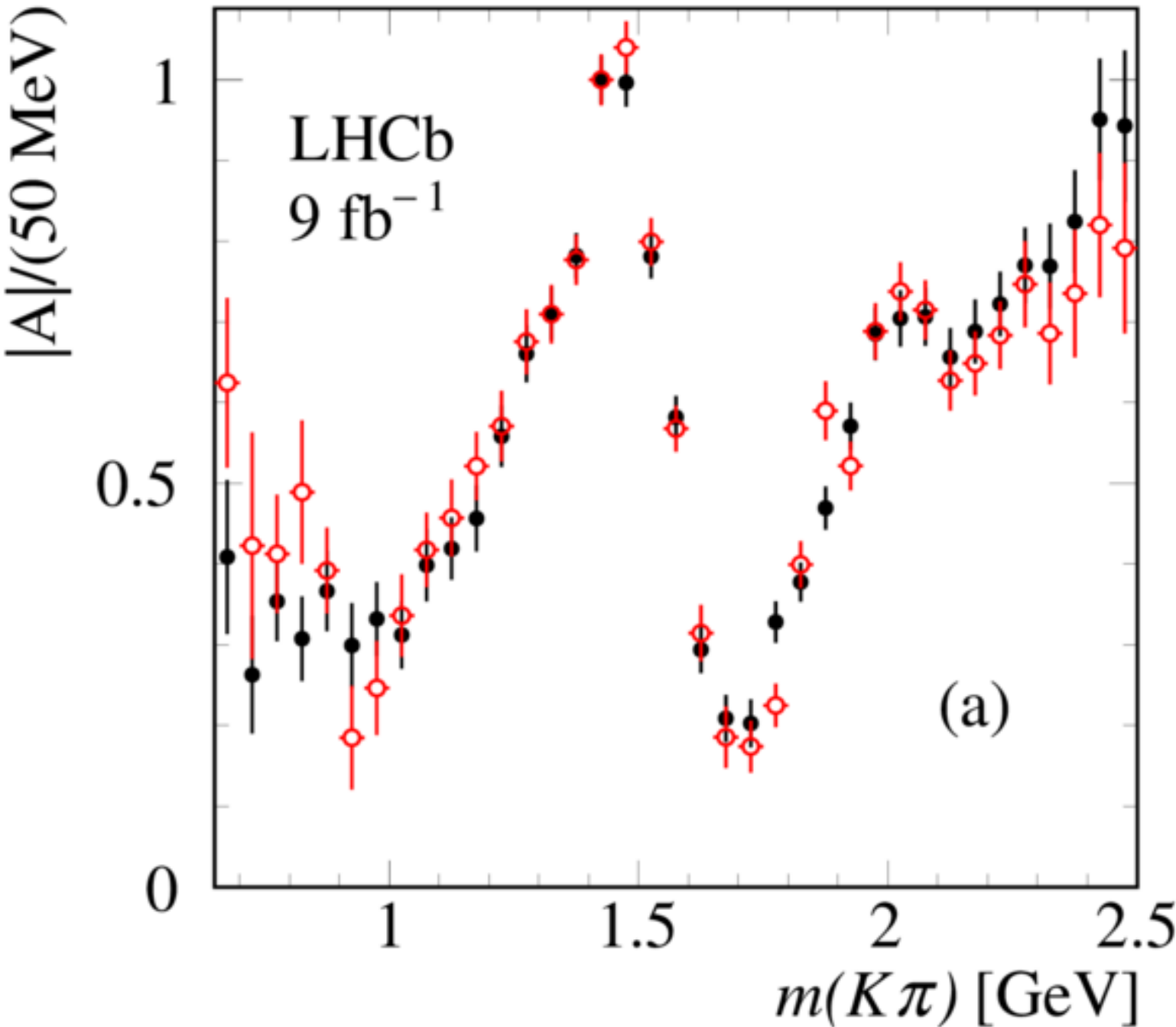
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Final state	Fraction [%]	Phase [rad]
$B^+ \rightarrow K_S^0 K^+ K^- \pi^+$		
$(K\pi)_S K$	$120.6 \pm 2.4 \pm 5.4$	0.
$a_0(1450)\pi$	$2.4 \pm 0.4 \pm 0.8$	$2.48 \pm 0.07 \pm 0.09$
$K_2^*(1430)K$	$16.6 \pm 0.8 \pm 0.9$	$4.31 \pm 0.03 \pm 0.11$
$a_2(1320)\pi$	$0.7 \pm 0.2 \pm 0.5$	$4.18 \pm 0.10 \pm 0.27$
$a_0(980)\pi$	$11.3 \pm 0.6 \pm 0.9$	$-2.93 \pm 0.03 \pm 0.03$
$a_0(1700)\pi$	$1.5 \pm 0.2 \pm 0.2$	$2.00 \pm 0.08 \pm 0.14$
$K_2^*(1980)K$	$2.8 \pm 0.3 \pm 1.0$	$-0.08 \pm 0.07 \pm 0.14$
$a_2(1750)\pi$	$0.2 \pm 0.1 \pm 0.1$	$-3.56 \pm 0.20 \pm 0.24$
Sum	$156.1 \pm 2.7 \pm 11.4$	
$\chi^2/\text{ndf} = 1706/(1597 - 17) = 1.08$		
$B^+ \rightarrow K_S^0 K^+ K^+ \pi^-$		
$(K\pi)_S K$	$106.0 \pm 2.8 \pm 8.5$	0.
$a_0(1450)\pi$	$0.8 \pm 0.3 \pm 0.4$	$1.64 \pm 0.14 \pm 0.47$
$K_2^*(1430)K$	$17.8 \pm 0.9 \pm 1.0$	$4.32 \pm 0.03 \pm 0.13$
$a_2(1320)\pi$	$0.7 \pm 0.2 \pm 0.5$	$4.22 \pm 0.11 \pm 0.93$
$a_0(980)\pi$	$9.7 \pm 0.6 \pm 0.3$	$-3.02 \pm 0.04 \pm 0.05$
$a_0(1700)\pi$	$0.8 \pm 0.2 \pm 0.2$	$2.10 \pm 0.11 \pm 0.24$
$K_2^*(1980)K$	$6.3 \pm 0.6 \pm 1.9$	$0.13 \pm 0.05 \pm 0.08$
$a_2(1750)\pi$	$0.2 \pm 0.2 \pm 0.3$	$-3.87 \pm 0.22 \pm 0.16$
Sum	$143.7 \pm 2.9 \pm 8.8$	
$\chi^2/\text{ndf} = 1686/(1589 - 17) = 1.07$		
$B \rightarrow K_S^0 K K \pi$		
$(K\pi)_S K$	$114.4 \pm 1.8 \pm 4.6$	0.
$a_0(1450)\pi$	$1.4 \pm 0.2 \pm 0.4$	$2.31 \pm 0.06 \pm 0.09$
$K_2^*(1430)K$	$17.1 \pm 0.6 \pm 0.7$	$4.32 \pm 0.02 \pm 0.08$
$a_2(1320)\pi$	$0.7 \pm 0.1 \pm 0.4$	$4.20 \pm 0.08 \pm 0.26$
$a_0(980)\pi$	$10.5 \pm 0.4 \pm 0.4$	$-2.97 \pm 0.02 \pm 0.03$
$a_0(1700)\pi$	$1.0 \pm 0.1 \pm 0.1$	$2.04 \pm 0.06 \pm 0.12$
$K_2^*(1980)K$	$3.5 \pm 0.3 \pm 0.9$	$0.06 \pm 0.04 \pm 0.07$
$a_2(1750)\pi$	$0.2 \pm 0.1 \pm 0.1$	$-3.69 \pm 0.15 \pm 0.16$
Sum	$148.8 \pm 2.0 \pm 4.8$	



Quasi Model Independent $K\pi$ S-wave Fit

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Isobar Model Fit

PHYS. REV. D108 032010 (2023)

$\kappa(2600)$

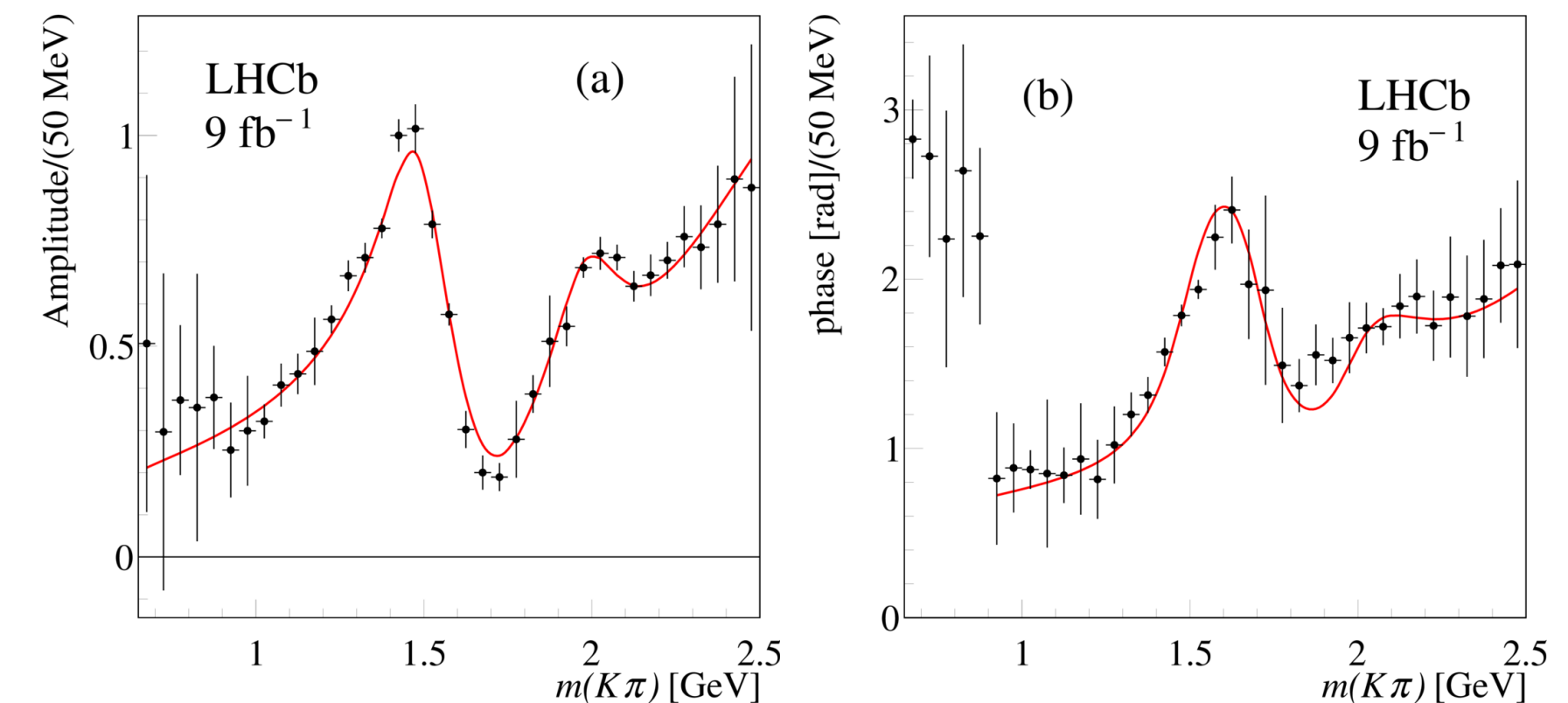
- A large S-wave amplitude is required for the model to fit

Low mass $\kappa/K^*_0(700)$

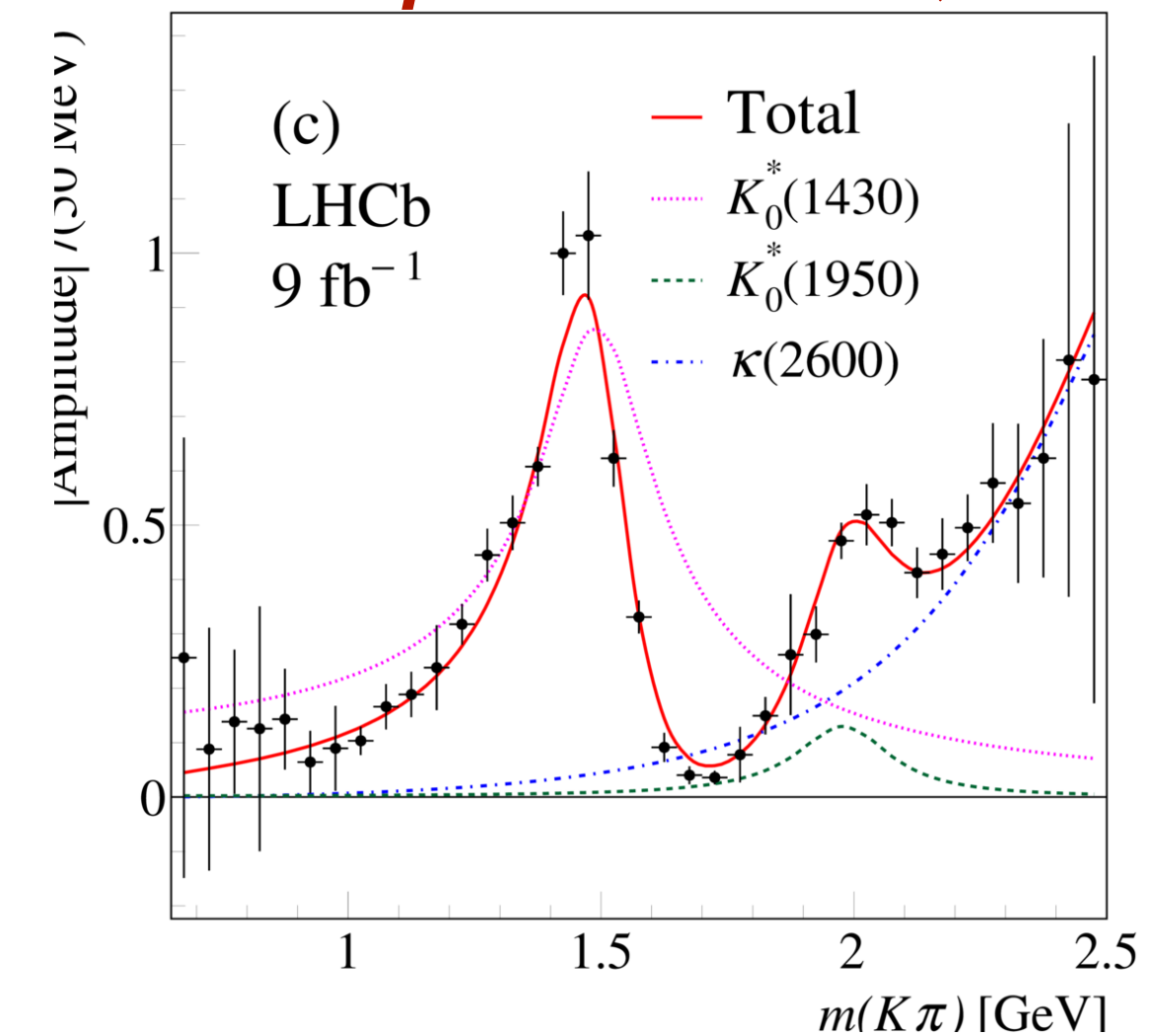
- Tested, non-significant improvement to the fit

Poorly known resonances

- $K^*_2(1980)$ consistent with zero
- $K^*_0(1430)$, $K^*_0(1950)$, $a_0(1700)$



Comparison with QM1



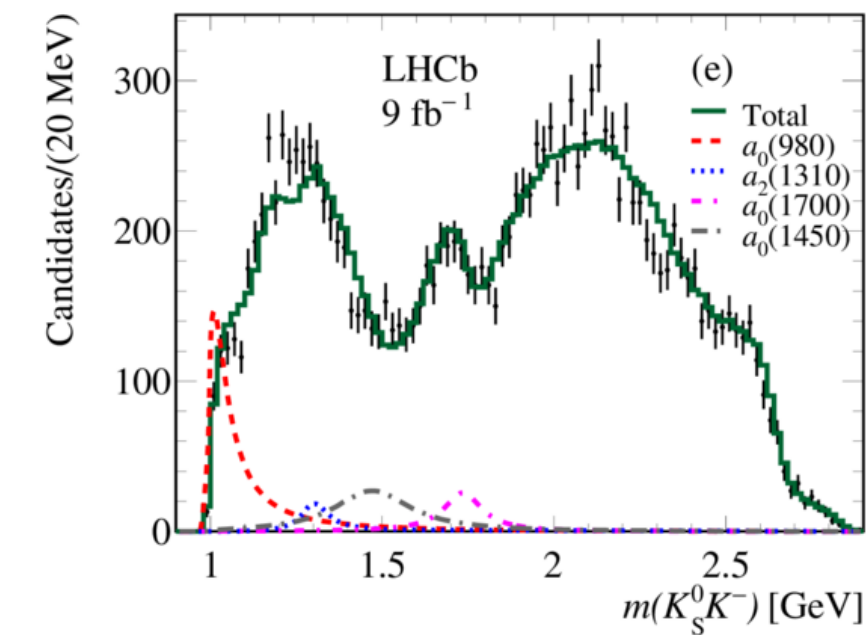
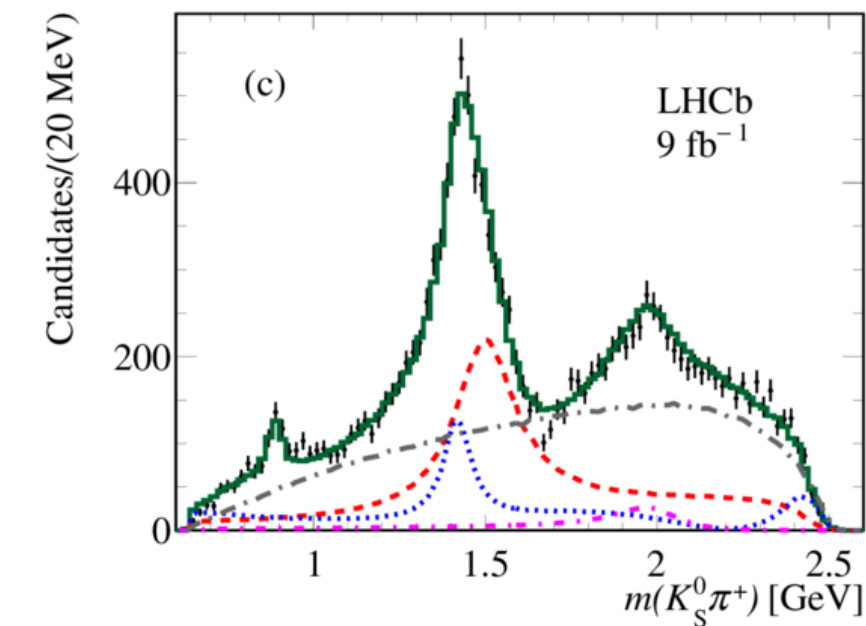
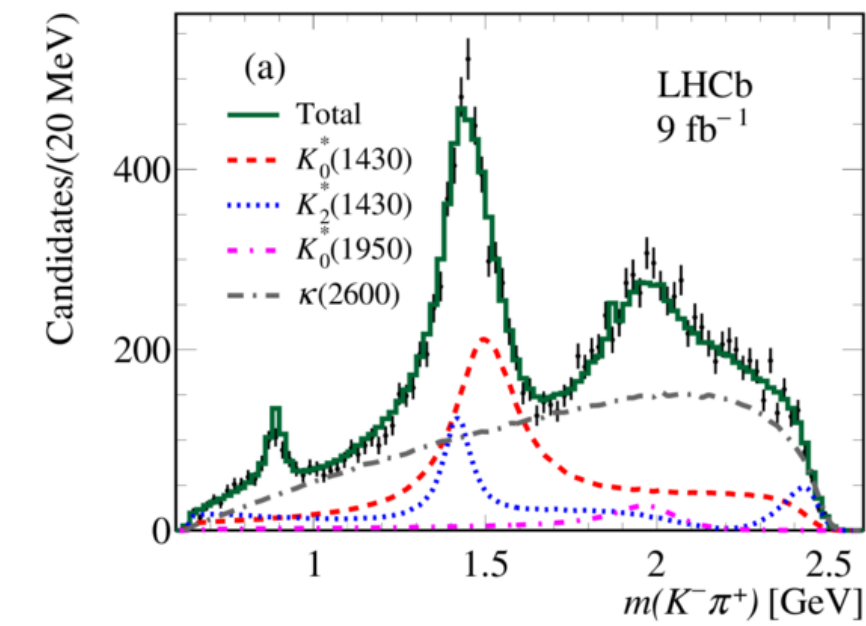
Resonance	Mass [MeV]	Γ [MeV]	$\Delta(2 \log \mathcal{L})$	Significance
$K^*_0(1430)$	$1493 \pm 4 \pm 7$	$215 \pm 7 \pm 4$	-	-
$K^*_0(1950)$	$1980 \pm 14 \pm 19$	$229 \pm 26 \pm 16$	316	17.8σ
$a_0(1700)$	$1736 \pm 10 \pm 12$	$134 \pm 17 \pm 61$	161	12.7σ
$\kappa(2600)$	$2662 \pm 59 \pm 201$	$480 \pm 47 \pm 72$	1338	36.6σ

Isobar Model Fit

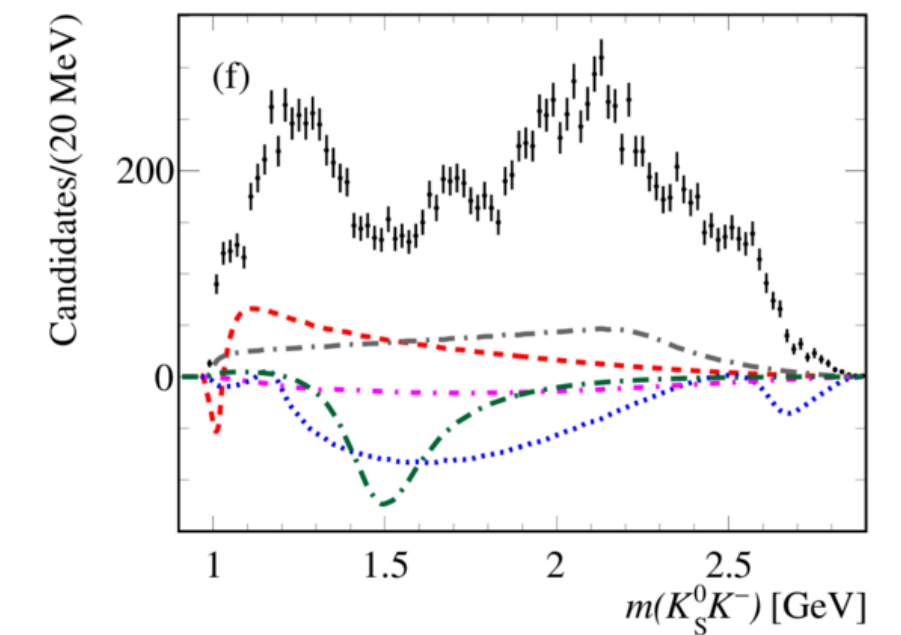
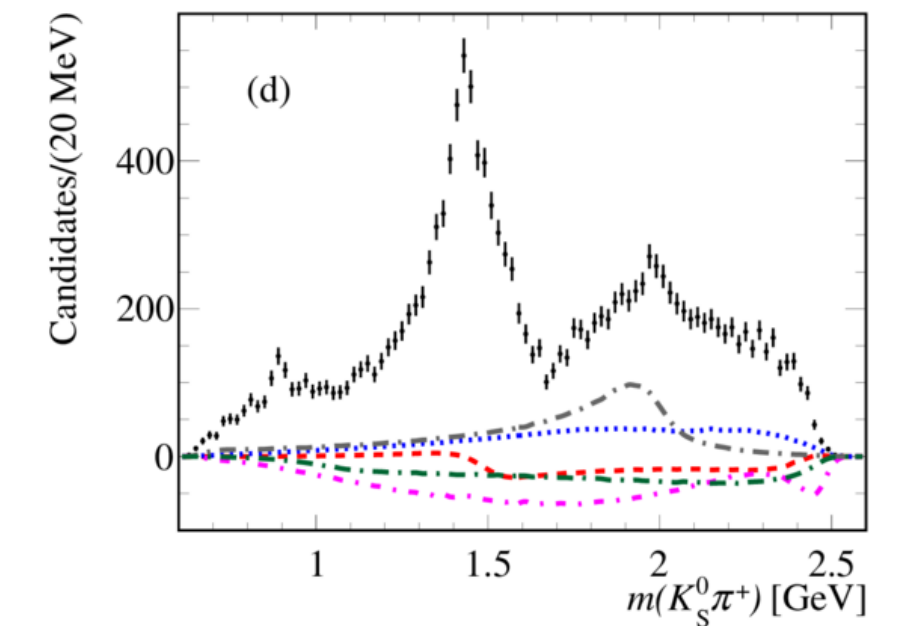
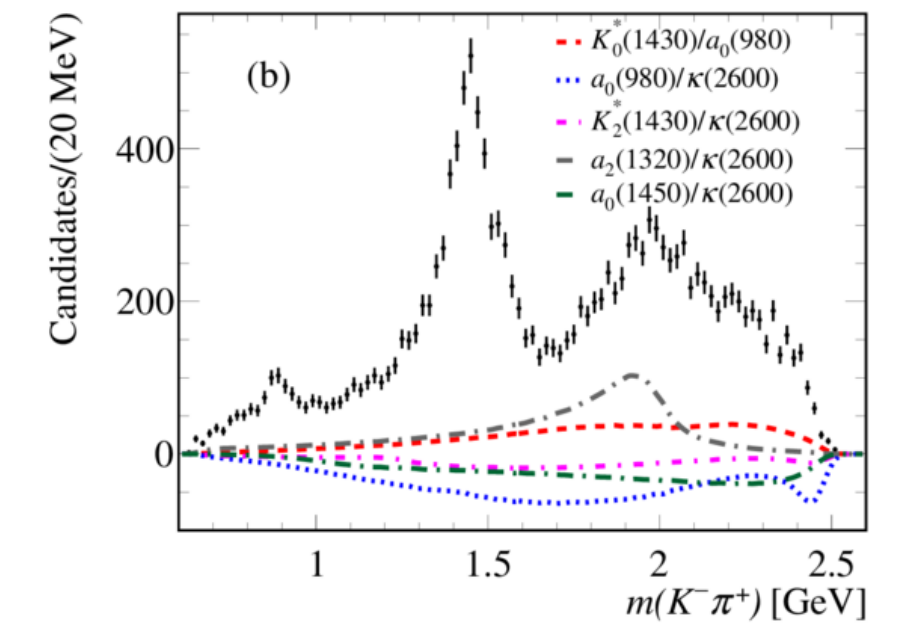
PHYS. REV. D108 032010 (2023)

Final state	Fraction [%]	Phase [rad]
$B^+ \rightarrow K_S^0 K^+ K^- \pi^+$		
$K_0^*(1430)K$	$35.1 \pm 1.3 \pm 2.9$	0.
$a_0(980)\pi$	$5.6 \pm 0.8 \pm 1.6$	$-3.39 \pm 0.08 \pm 0.13$
$K_2^*(1430)K$	$15.4 \pm 1.0 \pm 1.1$	$3.53 \pm 0.03 \pm 0.10$
$a_2(1320)\pi$	$1.1 \pm 0.2 \pm 0.3$	$-2.90 \pm 0.11 \pm 0.26$
$K_0^*(1950)K$	$3.9 \pm 0.4 \pm 0.3$	$-0.46 \pm 0.06 \pm 0.63$
$a_0(1700)\pi$	$1.7 \pm 0.3 \pm 0.4$	$1.00 \pm 0.08 \pm 0.17$
$a_0(1450)\pi$	$3.4 \pm 0.5 \pm 0.8$	$-4.78 \pm 0.08 \pm 0.17$
$a_2(1750)\pi$	$0.3 \pm 0.1 \pm 0.1$	$2.43 \pm 0.17 \pm 0.17$
$\kappa(2600)K$	$63.9 \pm 3.4 \pm 8.1$	$-0.42 \pm 0.05 \pm 0.14$
Sum	$130.5 \pm 4.0 \pm 8.9$	
$\chi^2/\text{ndf} = 1798/(1589 - 19) = 1.15$		
$B^+ \rightarrow K_S^0 K^+ K^+ \pi^-$		
$K_0^*(1430)K$	$32.0 \pm 1.2 \pm 2.8$	0.
$a_0(980)\pi$	$4.9 \pm 0.6 \pm 1.0$	$-3.37 \pm 0.08 \pm 0.11$
$K_2^*(1430)K$	$13.8 \pm 1.0 \pm 1.2$	$3.56 \pm 0.03 \pm 0.11$
$a_2(1320)\pi$	$1.2 \pm 0.2 \pm 0.3$	$-2.82 \pm 0.11 \pm 0.24$
$K_0^*(1950)K$	$3.4 \pm 0.4 \pm 0.3$	$-0.42 \pm 0.06 \pm 0.64$
$a_0(1700)\pi$	$0.7 \pm 0.2 \pm 0.2$	$1.18 \pm 0.11 \pm 0.28$
$a_0(1450)\pi$	$2.0 \pm 0.4 \pm 0.7$	$-4.86 \pm 0.10 \pm 0.22$
$a_2(1750)\pi$	$0.3 \pm 0.1 \pm 0.1$	$2.24 \pm 0.18 \pm 0.17$
$\kappa(2600)K$	$59.8 \pm 3.4 \pm 7.3$	$-0.32 \pm 0.05 \pm 0.12$
Sum	$118.1 \pm 2.7 \pm 8.0$	
$\chi^2/\text{ndf} = 1738/(1584 - 21) = 1.11$		
$B \rightarrow K_S^0 K K \pi$		
$K_0^*(1430)K$	$33.4 \pm 0.9 \pm 2.0$	0.
$a_0(980)\pi$	$5.1 \pm 0.5 \pm 0.8$	$-3.38 \pm 0.06 \pm 0.08$
$K_2^*(1430)K$	$14.6 \pm 0.7 \pm 0.8$	$3.54 \pm 0.02 \pm 0.07$
$a_2(1320)\pi$	$1.1 \pm 0.1 \pm 0.2$	$-2.89 \pm 0.08 \pm 0.18$
$K_0^*(1950)K$	$3.7 \pm 0.3 \pm 0.2$	$-0.44 \pm 0.04 \pm 0.45$
$a_0(1700)\pi$	$1.1 \pm 0.2 \pm 0.2$	$1.05 \pm 0.06 \pm 0.15$
$a_0(1450)\pi$	$2.6 \pm 0.3 \pm 0.5$	$-4.82 \pm 0.06 \pm 0.13$
$a_2(1750)\pi$	$0.3 \pm 0.1 \pm 0.1$	$2.33 \pm 0.12 \pm 0.11$
$\kappa(2600)K$	$61.8 \pm 2.4 \pm 5.4$	$-0.37 \pm 0.03 \pm 0.09$
Sum	$123.7 \pm 2.7 \pm 4.7$	

Amplitudes



Interference



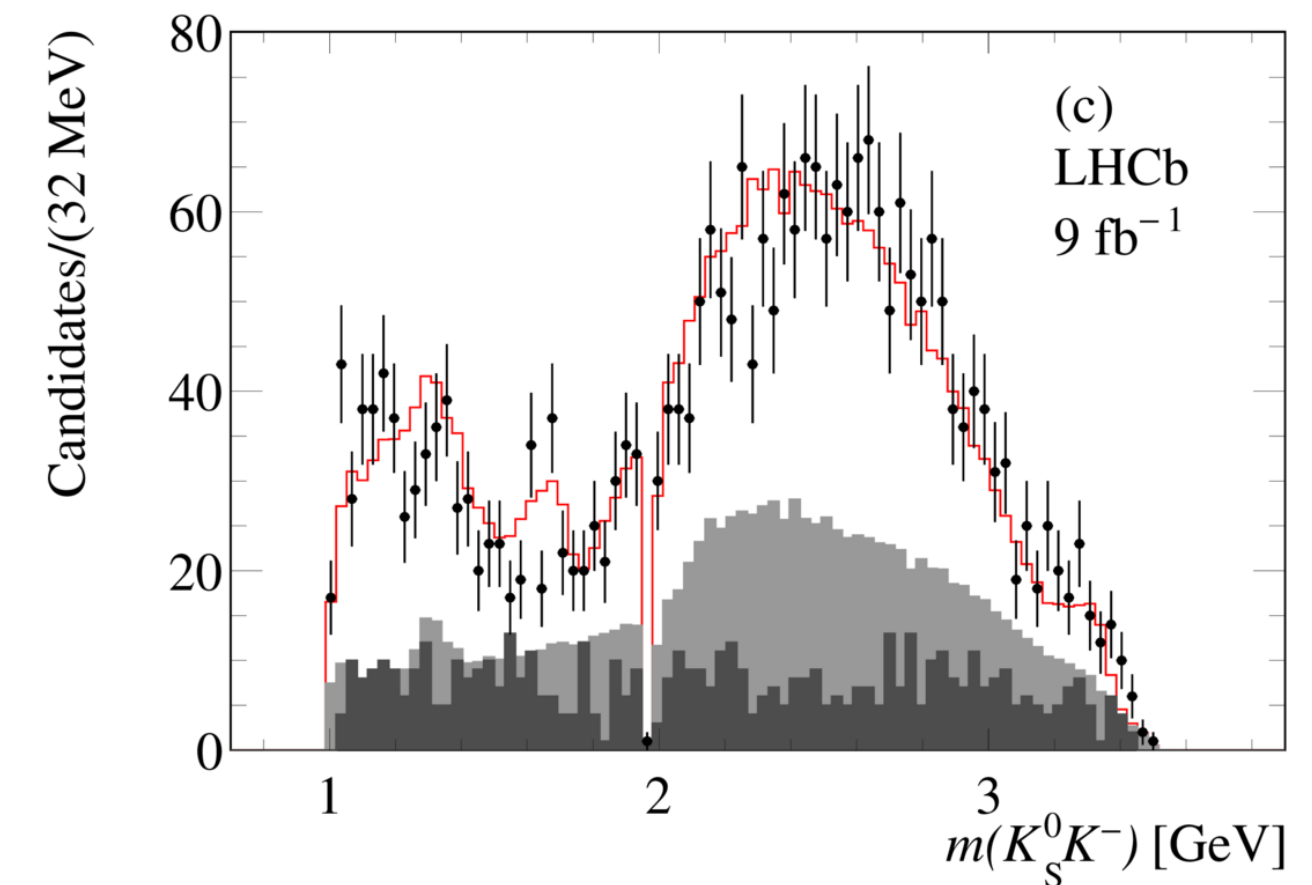
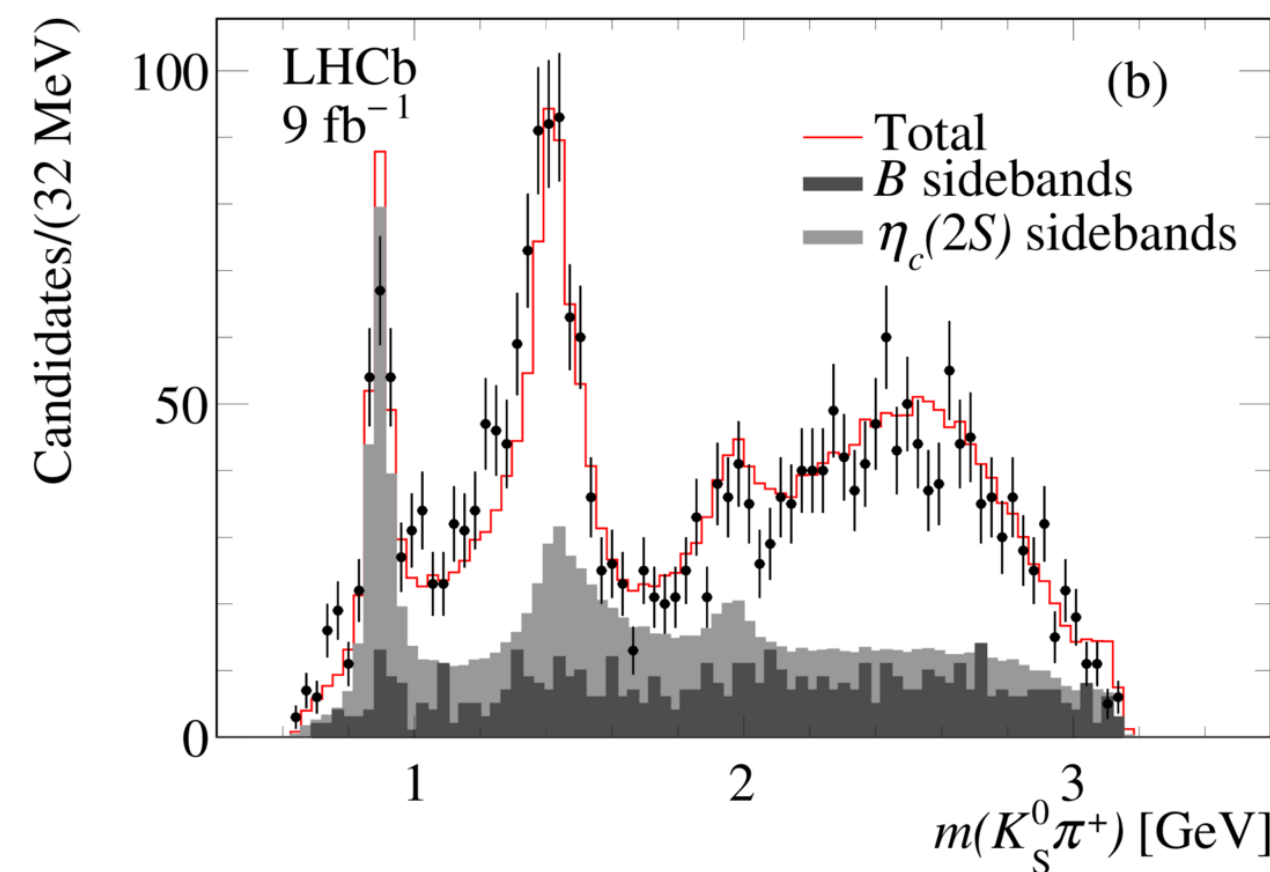
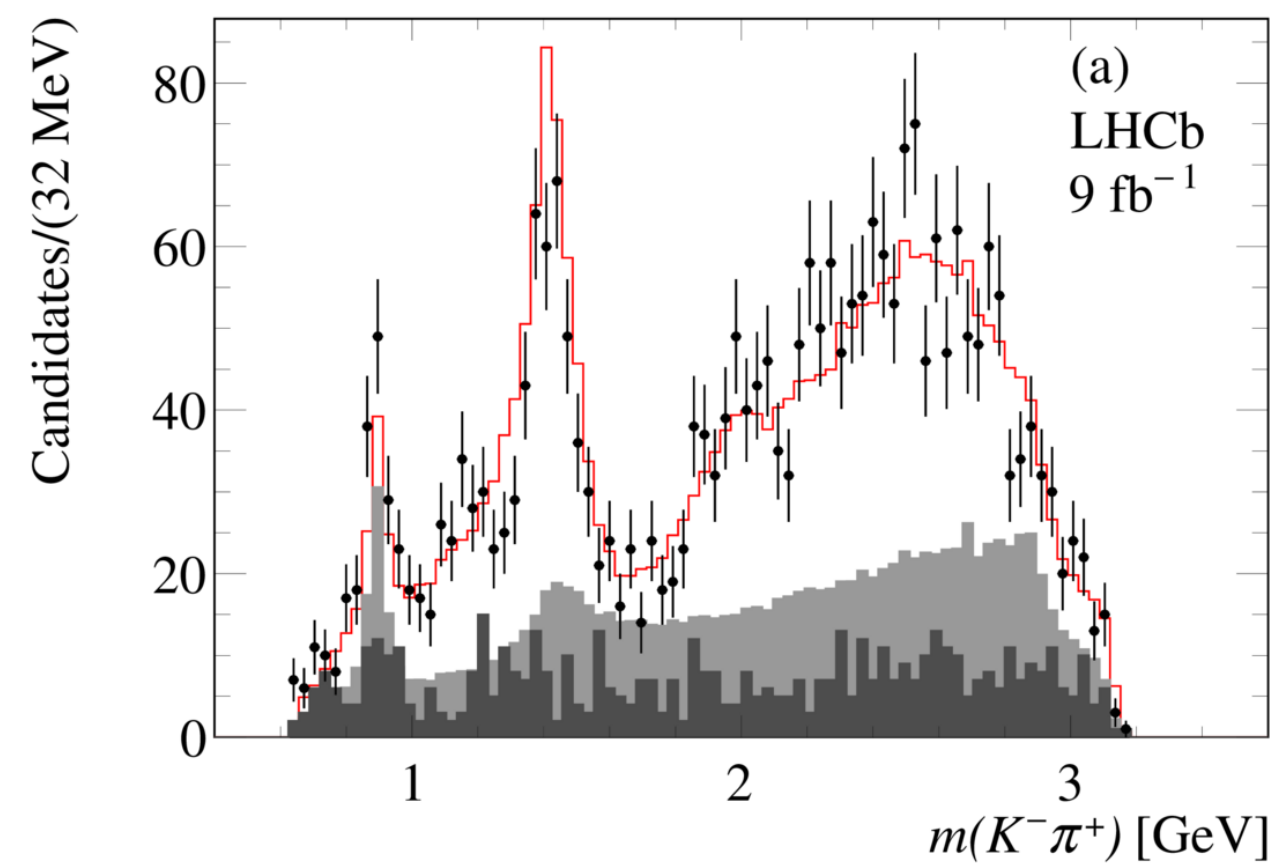
Dalitz Plot Analysis of $\eta_c(2S) \rightarrow K_s^0 K \pi$ Decays

PHYS. REV. D108 032010 (2023)

Much Lower Data

- Approximately 2800 decays in $B^+ \rightarrow K_s^0 K^+ K^- \pi^+$
- Using the same model of η_c (Isobar only)
- Very large interference

Final state	Fraction [%]	Phase [rad]
$K_0^*(1430)K$	$25.5 \pm 3.3 \pm 4.1$	0.
$K_2^*(1430)K$	$24.5 \pm 3.3 \pm 4.4$	$3.10 \pm 0.11 \pm 0.08$
$K_0^*(1950)K$	$3.7 \pm 1.3 \pm 1.1$	$-0.82 \pm 0.17 \pm 0.24$
$a_0(1700)^- \pi^+$	$1.7 \pm 1.1 \pm 0.5$	$1.22 \pm 0.32 \pm 0.90$
$a_0(1450)^- \pi^+$	$7.8 \pm 1.9 \pm 1.0$	$1.86 \pm 0.14 \pm 0.56$
$a_2(1750)^- \pi^+$	$4.9 \pm 1.4 \pm 1.1$	$-1.75 \pm 0.15 \pm 0.39$
$\kappa(2600)K$	$124.2 \pm 9.0 \pm 7.7$	$-0.91 \pm 0.10 \pm 0.08$
Sum	$192.3 \pm 10.9 \pm 10.0$	
$\chi^2/\text{ndf} = 578/(591-13) = 1.00$		



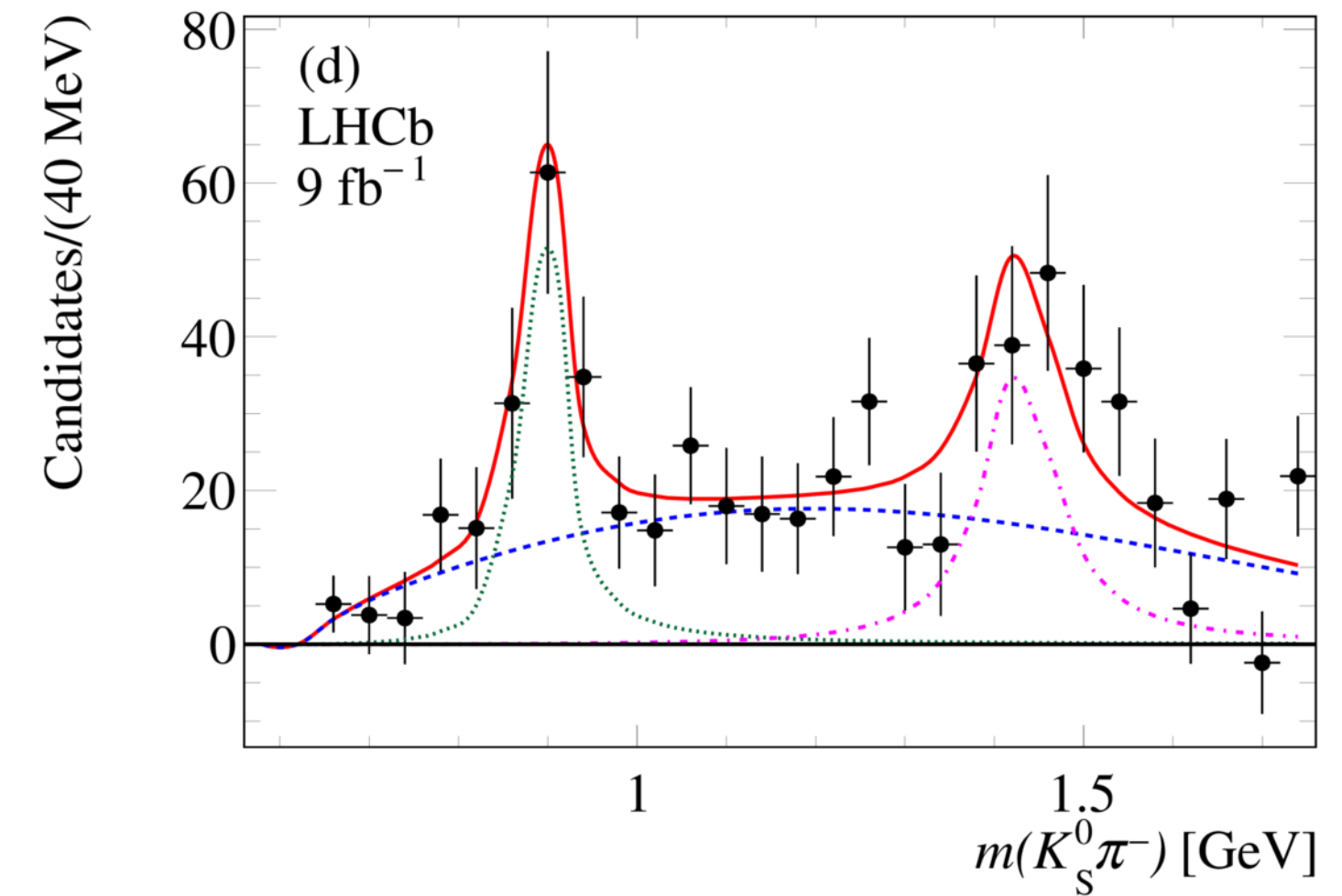
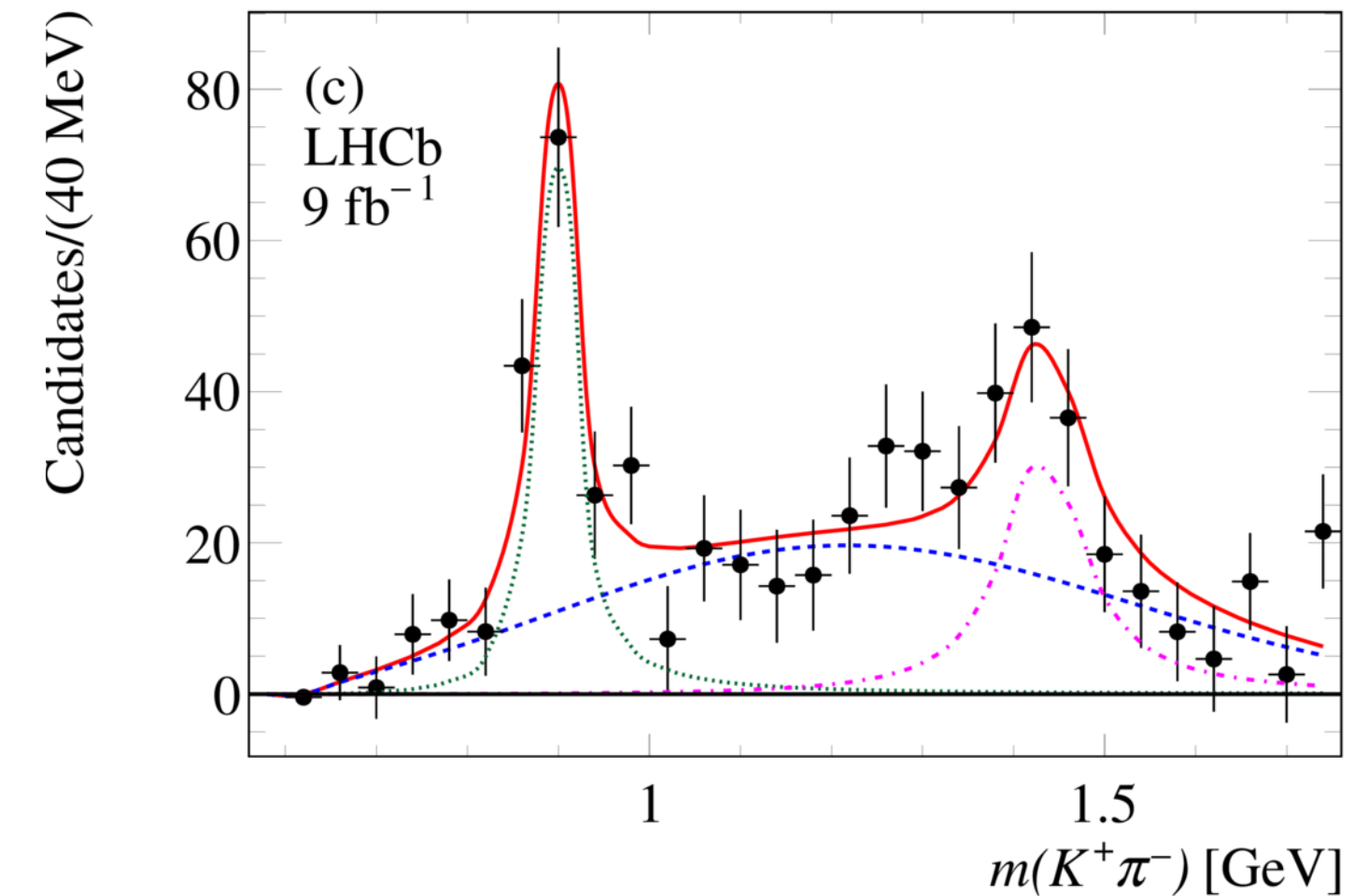
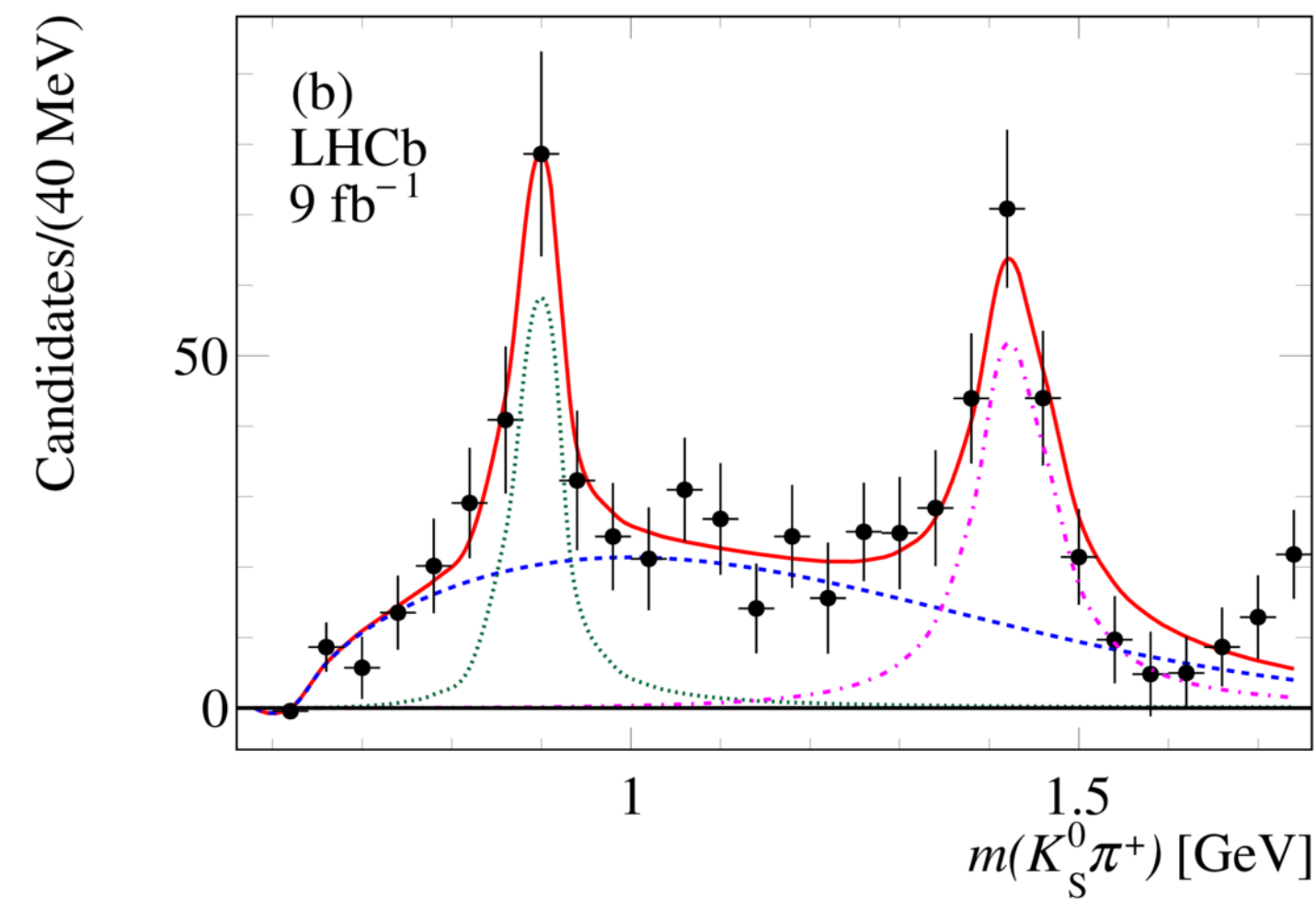
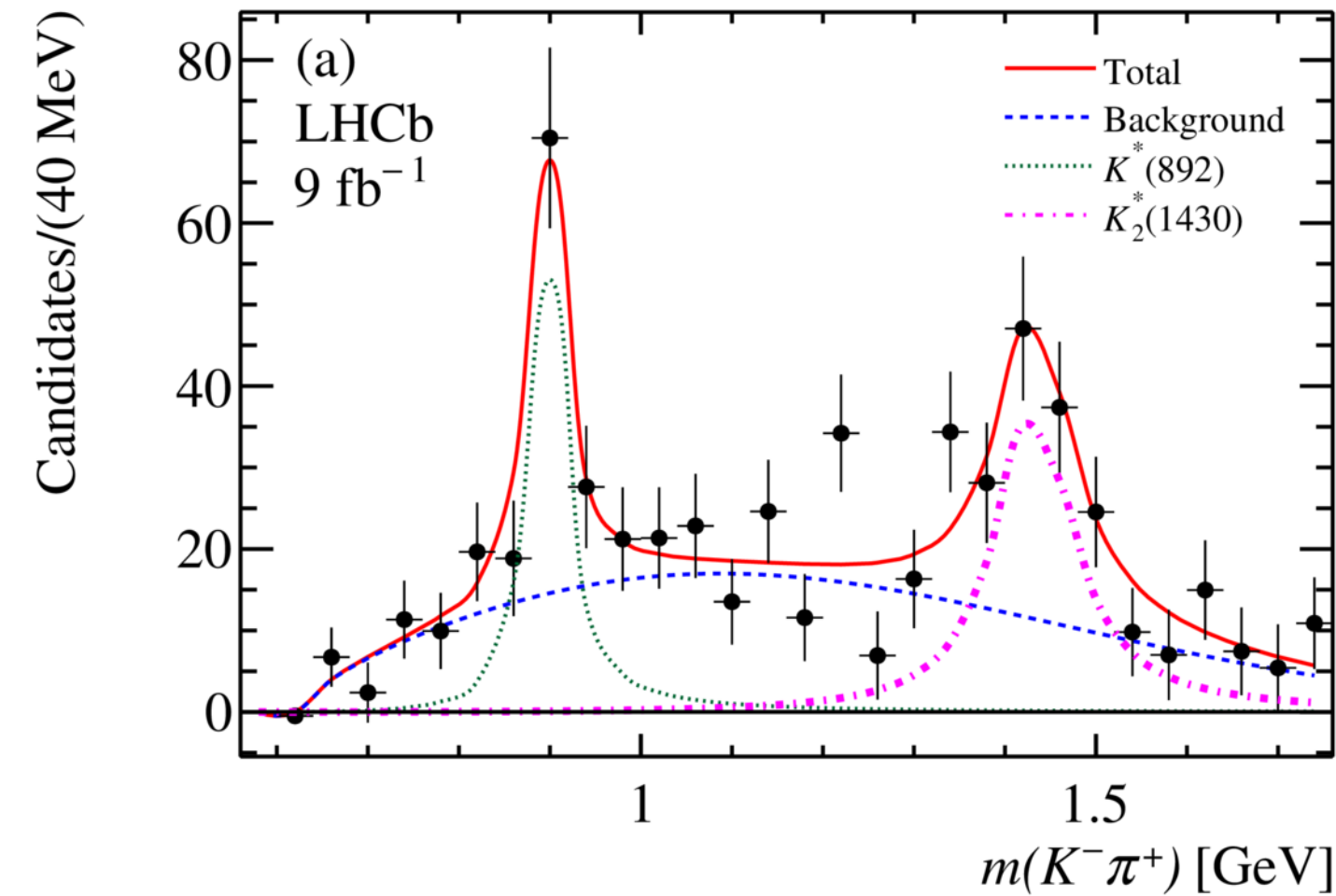
Dalitz Plot Analysis of $\chi_{c1} \rightarrow K^0_s K \pi$ Decays

PHYS. REV. D108 032010 (2023)

High Background

- Dalitz plot not feasible in this case
- Simplified approach: fit only the $m(K\pi)$ and $m(K^0\pi)$ distributions
- Efficiency corrected

Decay mode	Fraction	Branching fraction ($\times 10^{-3}$)
$\mathcal{B}(\chi_{c1} \rightarrow K^*(892)^0 \bar{K}^0)$	$0.099 \pm 0.012 \pm 0.004$	$1.04 \pm 0.13 \pm 0.04 \pm 0.09$
$\mathcal{B}(\chi_{c1} \rightarrow K_2^*(1430)^0 \bar{K}^0)$	$0.111 \pm 0.015 \pm 0.005$	$1.17 \pm 0.16 \pm 0.05 \pm 0.10$
$\mathcal{B}(\chi_{c1} \rightarrow K^*(892)^+ K^-)$	$0.112 \pm 0.016 \pm 0.013$	$1.18 \pm 0.17 \pm 0.14 \pm 0.10$
$\mathcal{B}(\chi_{c1} \rightarrow K_2^*(1430)^+ K^-)$	$0.143 \pm 0.018 \pm 0.006$	$1.61 \pm 0.19 \pm 0.19 \pm 0.14$



Summary

Summary

Strange Hadrons Spectroscopy at LHCb

- A byproduct of amplitude analyses of B and D decays
- (Relatively) Large yields with high purity
- Many interesting results can be extracted
 - $K^*_0(1950)$ established
 - New parametrisation of the $K\pi$ S-wave including $K^*_0(1430)$, $K^*_0(1950)$, and $\kappa(2600)$
- **KK and $K\pi$ S-waves can be studied**

*Spare*s

Systematic Uncertainties $D^0 \rightarrow K^\mp \pi^\pm \pi^\mp \pi^\pm$

Tested With PseudoExperiments

- Size of Integration Sample (Resampling)
- Background description in WS fit
- Flavour Misidentification
- Detection Asymmetry
- Alternative Models

Tested With Alternative Fits

- Background Description
- Selection Efficiency
- Resonance Shapes

Tested With Multiple Fits of Resampled Data

- Background Description
- Uncertainties of the Fixed Parameters

Systematic Uncertainties $D^0 \rightarrow K^+K^-\pi^+\pi^-$

Tested With PseudoExperiments

- Fit Bias
- Background description
- Flavour Misidentification
- Detection Asymmetry
- Alternative Models

Tested With Alternative Fits

- Background Description
- Selection Efficiency
- Resonance Shapes

Tested With Multiple Fits of Resampled Data

- Background Description
- Uncertainties of the Fixed Parameters

Systematic Uncertainties $\eta_c \rightarrow K_S^0 K \pi$

Sources of Uncertainties

- **Efficiency Correction**
 $\epsilon(m(K_S^0 K), \cos\theta_\pi) \rightarrow \epsilon_1(m(K_S^0 K))\epsilon_2(\cos\theta_\pi)$
- **Trigger Selection**
 TOS vs. No-TOS
- **Uncertainty on Signal Purity**
 $\pm 5\%$ change in BDT selection
- **Radius of the Blatt-Weisskopf factor (1.5/GeV)**
 Varied in (0.5 ÷ 2.5)/GeV range
- **Background Model**
 Random variations of background model

Negligible

- Fit Bias
- Sidebands

Amplitudes

Final state	Eff	Trig	Pur	r	Back	Tot	Eff	Trig	Pur	r	Back	Tot
$(K\pi)_S K$	3.27	0.89	1.03	4.01	0.48	5.37	-	-	-	-	-	-
$a_0(1450)\pi$	0.65	0.29	0.24	0.16	0.06	0.77	0.04	0.07	0.03	0.00	0.03	0.09
$K_2^*(1430)K$	0.02	0.17	0.04	0.86	0.48	1.00	0.08	0.06	0.03	0.05	0.01	0.11
$a_2(1320)\pi$	0.38	0.10	0.34	0.04	0.08	0.53	0.21	0.08	0.14	0.05	0.01	0.27
$a_0(980)\pi$	0.70	0.05	0.47	0.12	0.34	0.92	0.01	0.02	0.02	0.00	0.02	0.04
$a_0(1700)\pi$	0.12	0.05	0.05	0.08	0.01	0.16	0.10	0.08	0.02	0.00	0.00	0.14
$K_2^*(1980)K$	0.04	0.08	0.19	0.96	0.16	1.00	0.10	0.06	0.04	0.08	0.01	0.14
$a_2(1750)\pi$	0.05	0.01	0.05	0.03	0.03	0.09	0.04	0.14	0.05	0.11	0.06	0.20

Phases

Final state	Eff	Trig	Pur	r	Back	Tot	Eff	Trig	Pur	r	Back	Tot
$(K\pi)_S K$	6.06	2.94	2.80	4.39	0.20	8.52	-	-	-	-	-	-
$a_0(1450)\pi$	0.30	0.12	0.24	0.14	0.06	0.43	0.31	0.35	0.08	0.01	0.01	0.47
$K_2^*(1430)K$	0.32	0.08	0.30	0.88	0.54	1.13	0.09	0.07	0.04	0.06	0.01	0.13
$a_2(1320)\pi$	0.32	0.09	0.30	0.08	0.11	0.47	0.27	0.13	0.19	0.05	0.86	0.93
$a_0(980)\pi$	0.01	0.17	0.02	0.22	0.26	0.46	0.02	0.02	0.03	0.02	0.02	0.06
$a_0(1700)\pi$	0.12	0.00	0.08	0.08	0.01	0.17	0.18	0.15	0.03	0.00	0.01	0.24
$K_2^*(1980)K$	0.46	0.11	0.43	1.77	0.22	1.89	0.04	0.01	0.06	0.05	0.01	0.08
$a_2(1750)\pi$	0.21	0.10	0.13	0.02	0.03	0.27	0.09	0.02	0.06	0.11	0.19	0.25

Systematic Uncertainties $\eta_c(2S) \rightarrow K^0_s K \pi$

Sources of Uncertainties

- **Efficiency Correction**
Use 2D-binned map
- **Trigger Selection**
TOS vs. No-TOS
- **Uncertainty on Signal Purity**
 $\pm 5\%$ change in BDT selection
- **Radius of the Blatt-Weisskopf factor (1.5/GeV)**
Varied in (0.5 ÷ 2.5)/GeV range
- **Background Model**
Random variations of background model

Final state	Amplitudes						Phases					
	Pur	Par	r	Back	Eff	Tot	Pur	Par	r	Back	Eff	Tot
$K_0^*(1430)K$	1.92	1.25	0.17	0.91	3.26	4.1	-	-	-	-	-	-
$K_2^*(1430)K$	2.47	0.43	1.24	0.86	3.30	4.4	0.06	0.02	0.04	0.02	0.01	0.08
$K_0^*(1950)K$	0.60	0.22	0.37	0.18	0.74	1.1	0.03	0.09	0.08	0.21	0.01	0.24
$a_0(1700)^-\pi^+$	0.32	0.05	0.29	0.13	0.02	0.45	0.18	0.05	0.11	0.87	0.12	0.90
$a_0(1450)^-\pi^+$	0.94	0.04	0.19	0.32	0.19	1.03	0.10	0.04	0.09	0.53	0.09	0.56
$a_2(1750)^-\pi^+$	0.53	0.15	0.42	0.11	0.79	1.05	0.03	0.04	0.08	0.38	0.03	0.39
$\kappa(2600)K$	4.33	3.28	4.97	0.01	2.40	7.74	0.04	0.05	0.04	0.02	0.01	0.08

Negligible

- Fit Bias
- Sidebands

Systematic Uncertainties $\chi_{c1} \rightarrow K^0_s K \pi$

Sources of Uncertainties

- **Decay Modes**
Difference between separate results
- **Uncertainty on Signal Purity**
 $\pm 5\%$ change in BDT selection
- **Radius of the Blatt-Weisskopf factor (1.5/GeV)**
Varied in (0.5 ÷ 2.5)/GeV range

Amplitude Analysis of 4-Body D^0 Decays

Software: AmpGen

- C++ and ROOT based with multithreading (OpenMP)
- Isobar model
 - coherent sum of amplitudes
 - polarised sum of amplitudes for particles carrying spin
 - incoherent sum of amplitudes for background description
- Spin Formalism
 - Covariant Tensors (Rarita-Schwinger)
 - Canonical helicity formalism
- Quasiparticles
 - Fictional decaying particles to describe for example S-wave with K-matrix

Modelling 3-Body Resonances

3-Body Running Width

- The width of 2-body resonances is typically given by

$$\Gamma(s) = \frac{\Gamma_0 q m_0}{q_0 \sqrt{s}} \left(\frac{q}{q_0} \right)^{2L} B_L(q, q_0)^2$$

- In 3-body resonances one must account for the dynamics of the intermediate decay process
- We decided to express it in terms of the spin-averaged matrix element of the decay integrated over the phase space of the three-particle final state

$$\Gamma(s) \propto \frac{1}{s} \int ds_{ab} ds_{bc} \left| \mathcal{M}_{R \rightarrow abc} \right|^2, \Gamma(m_0^2) = \Gamma_0$$

3-Body Amplitude

$$\mathcal{T}(s) = \frac{\sqrt{k} F(q)}{m_0^2 - s - im_0 \Gamma(s)}, F(q) = e^{-r^2 q^2 / 2}$$