

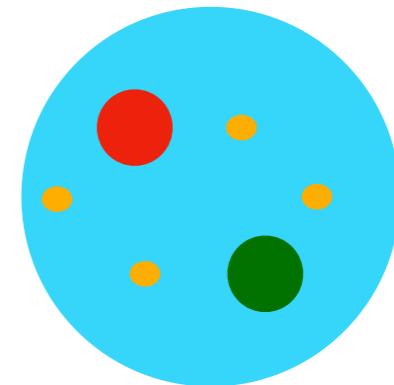
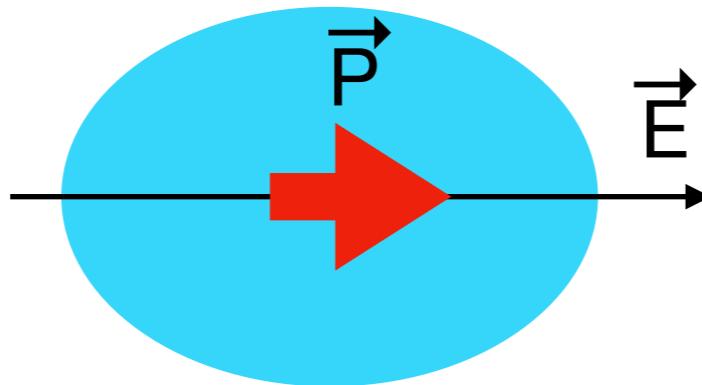
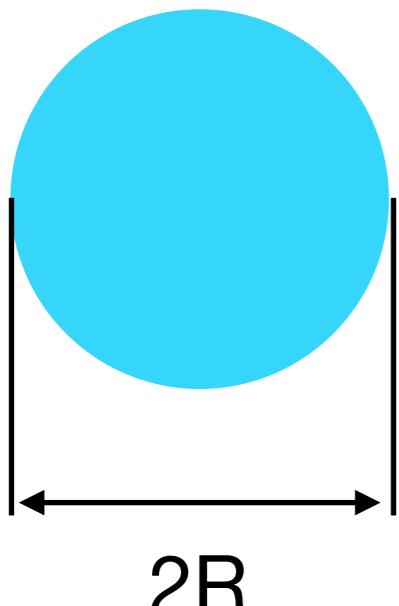


AMBER

Apparatus for Meson and Baryon  
Experimental Research

*Primakoff Reactions  
and  
Prompt Photons Production  
with  
AMBER*

# Hadronic matter



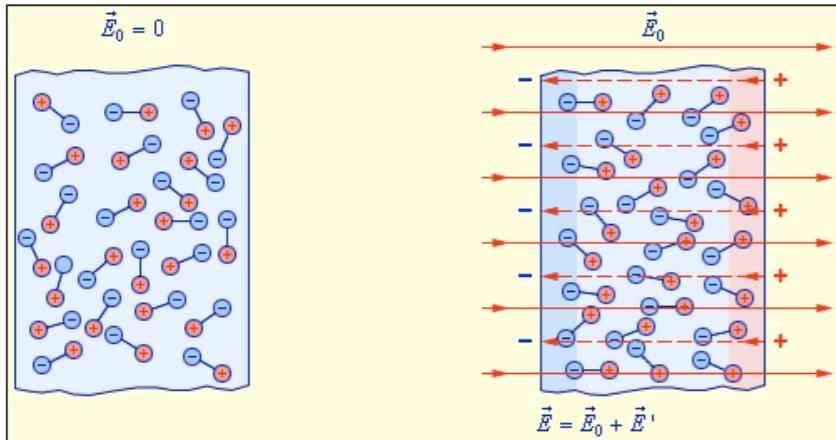
Existence  
of nuclear matter  
and its  
self-organization

Rigidity  
of nuclear matter

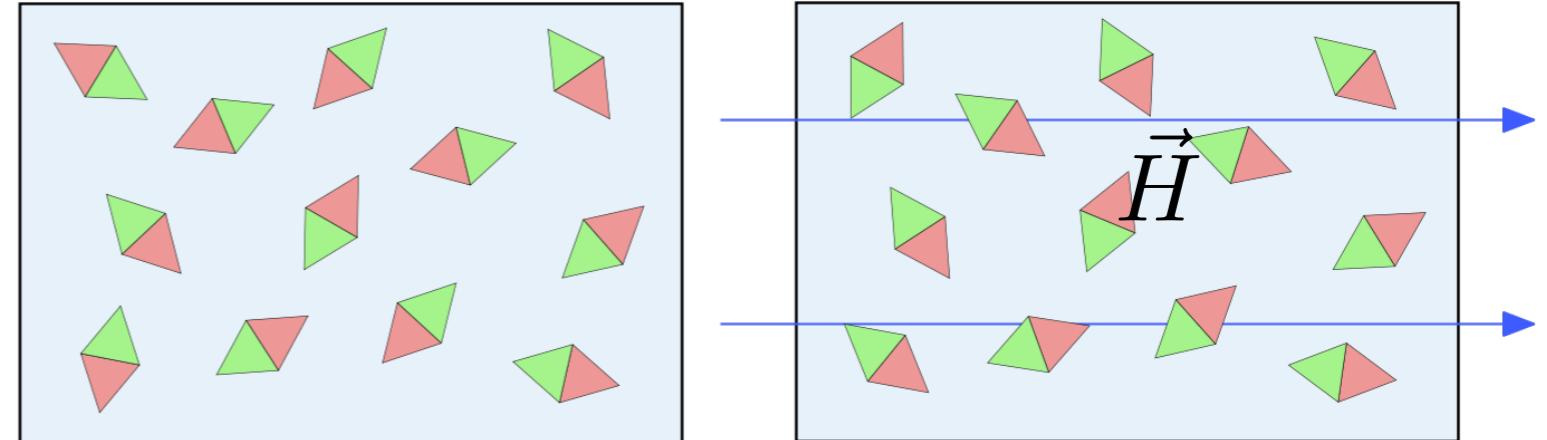
Structure  
of nuclear matter

# Polarizabilities: from medium to particles

Electric



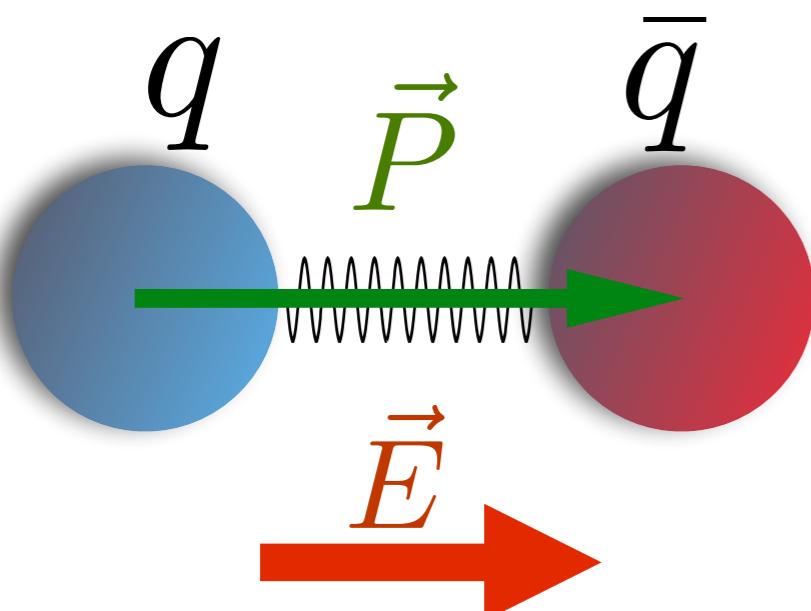
Magnetic



Polarizabilities:

$$\vec{P} = \alpha_X \vec{E}$$

$$\vec{\mu} = \beta_X \vec{H}$$



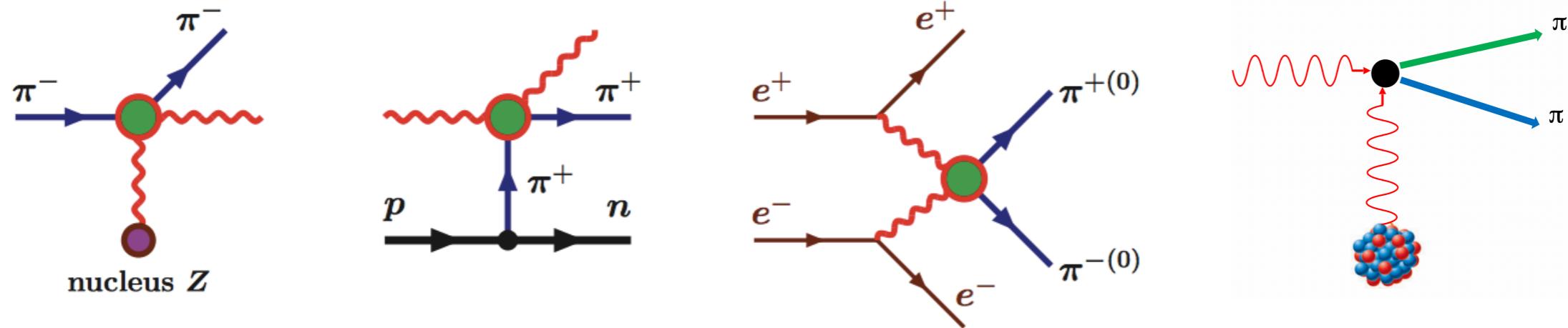
Compton amplitude:

$$A(\gamma X \rightarrow \gamma X) = (-\frac{\alpha}{m} \delta_{o\pm} + \alpha_X \omega_1 \omega_2) \hat{e}_1 \cdot \hat{e}_2 + + \beta_X \omega_1 \omega_2 (\hat{e}_1 \times \hat{q}_1) (\hat{e}_2 \times \hat{q}_2) + \dots$$

$$H = \dots - (\alpha_X E^2 + \beta_X H^2)/2$$

The electric and magnetic polarizabilities of a hadron are the quantities characterizing the rigidity of QCD system

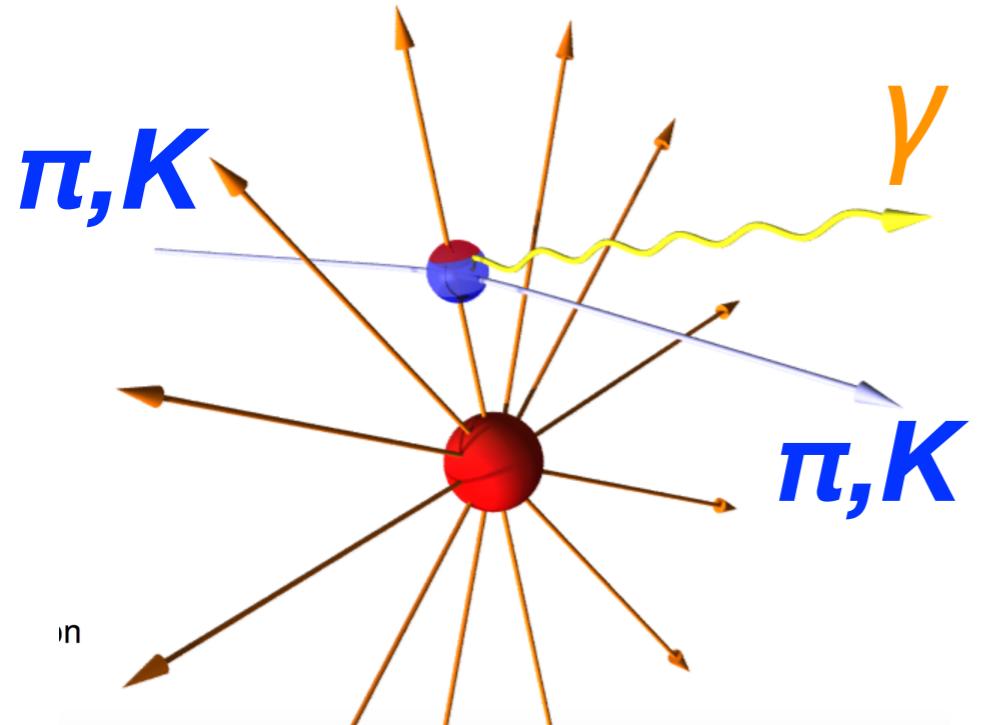
# Polarizability of hadrons



	$\alpha_x, 10^{-4} \text{ fm}^3$	$\beta_x, 10^{-4} \text{ fm}^3$	Comments	Chiral theory	$\alpha_x/r^3 x, 10^{-3}$
p	<b><math>11.2 \pm 0.4</math></b>	<b><math>2.5 \pm 0.4</math></b>		$\alpha=10.8, \beta=4.0 (\pm 0.7)$	1.9
n	<b><math>11.8 \pm 1.1</math></b>	<b><math>3.7 \pm 1.2</math></b>			
$\pi^\pm$	<b><math>2.0 \pm 0.9</math></b>	<b><math>-2.0 \mp 0.9</math></b>	assuming $\alpha = -\beta$	$\alpha=2.9, \beta=2.7 (\pm 0.5)$	1
$\pi^0$	$0 \pm 2$	$1 \mp 2$		$\alpha=-0.4, \beta=1.5 (\pm 0.3)$	
K $^\pm$	<b>&lt;200</b>		from kaonic atom spectra	$\alpha = -\beta = 0.6$	0.34
Hydrogen atom					4 500

Magnetic moment of proton induced by atomic magnetic fields is  $\sim 10^{-14} \mu_N$

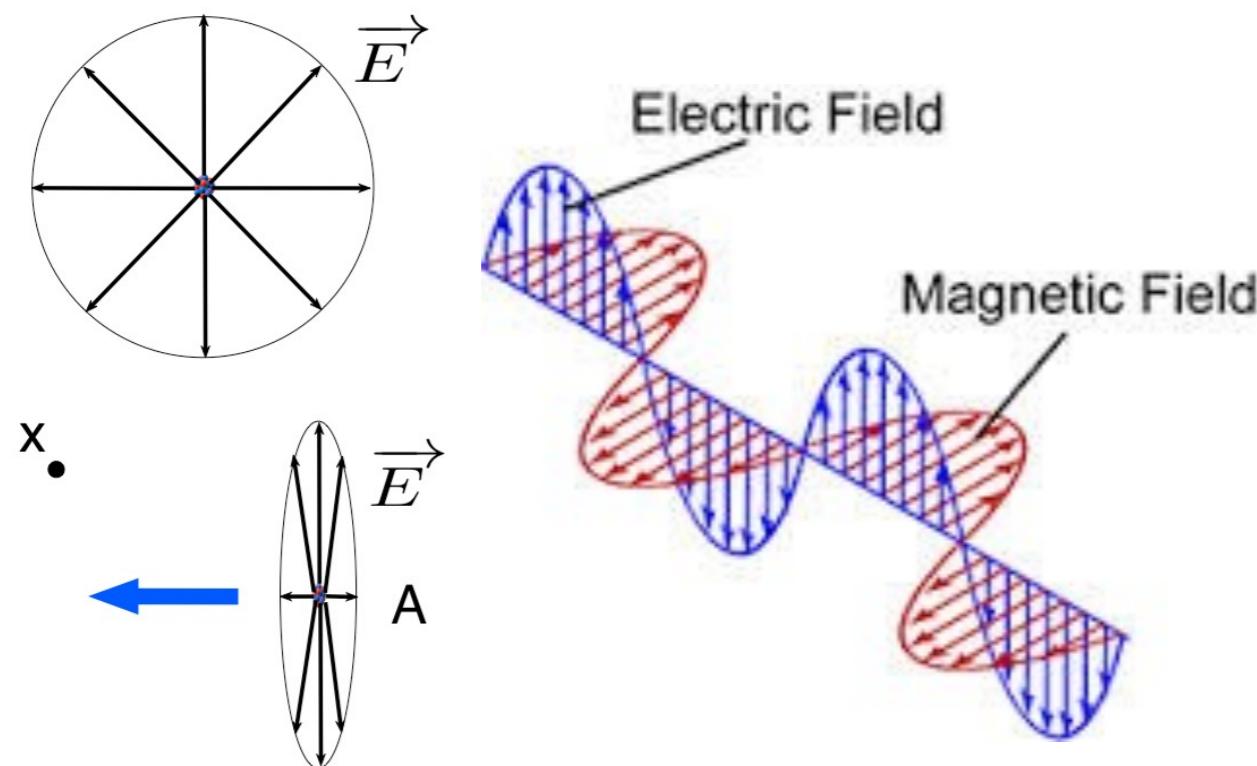
# Primakoff reactions



$$\sigma_{x\gamma} \sim 1/m_x^2$$

$$\sigma_{x\gamma}(\omega, Q^2) \rightarrow \sigma_{x\gamma}(\omega, 0)$$

$$d\sigma_{xz} = \int n_\gamma(\omega) d\sigma_{x\gamma}(\omega) d\omega$$



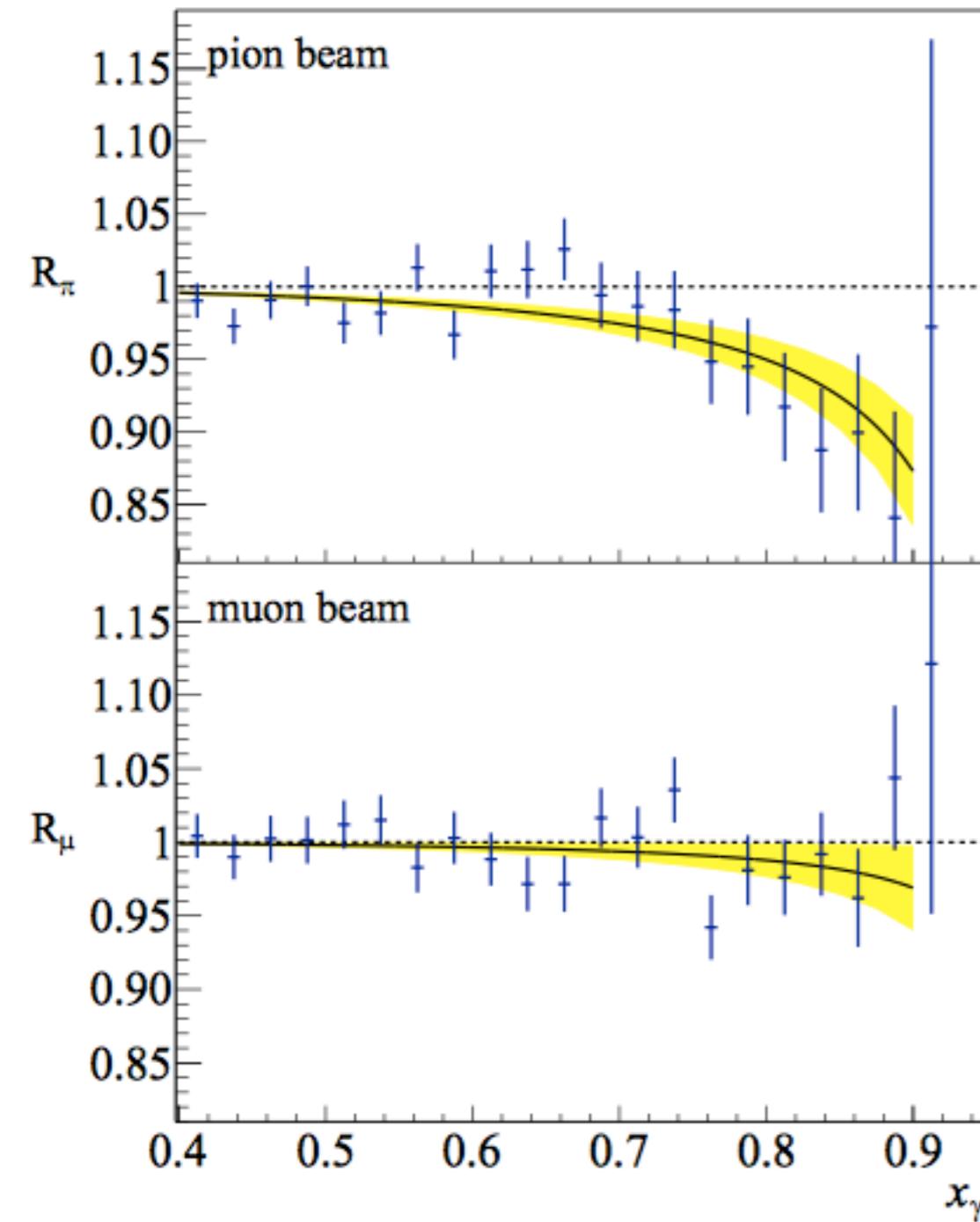
$$n_\gamma(\omega) \sim \frac{Z^2 \alpha}{\omega} \ln \frac{E}{\omega}$$

density of equivalent photons

# Pion polarizability at COMPASS



$$R_X = \frac{\sigma}{\sigma_{p.l.}} = 1 - \frac{3}{2} \times \frac{x_\gamma^2}{1-x_\gamma} \times \frac{m_X^3}{\alpha} \times \alpha_X$$



Source of uncertainty	Estimated magnitude [ $10^{-4}$ fm $^3$ ]
Determination of tracking detector efficiency	0.5
Treatment of radiative corrections	0.3
Subtraction of $\pi^0$ background	0.2
Strong interaction background	0.2
Pion-electron elastic scattering	0.2
Contribution of muons in the beam	0.05
Quadratic sum	0.7

***Under assumption  $\alpha_\pi = -\beta_\pi$ :***

$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3$

***Phys. Rev. Lett. 114 (2015) 06002***

# Kaon polarisability via Primakoff scattering

*Theoretical predictions:*  
 $\chi PT$  prediction  $O(p^4)$ :

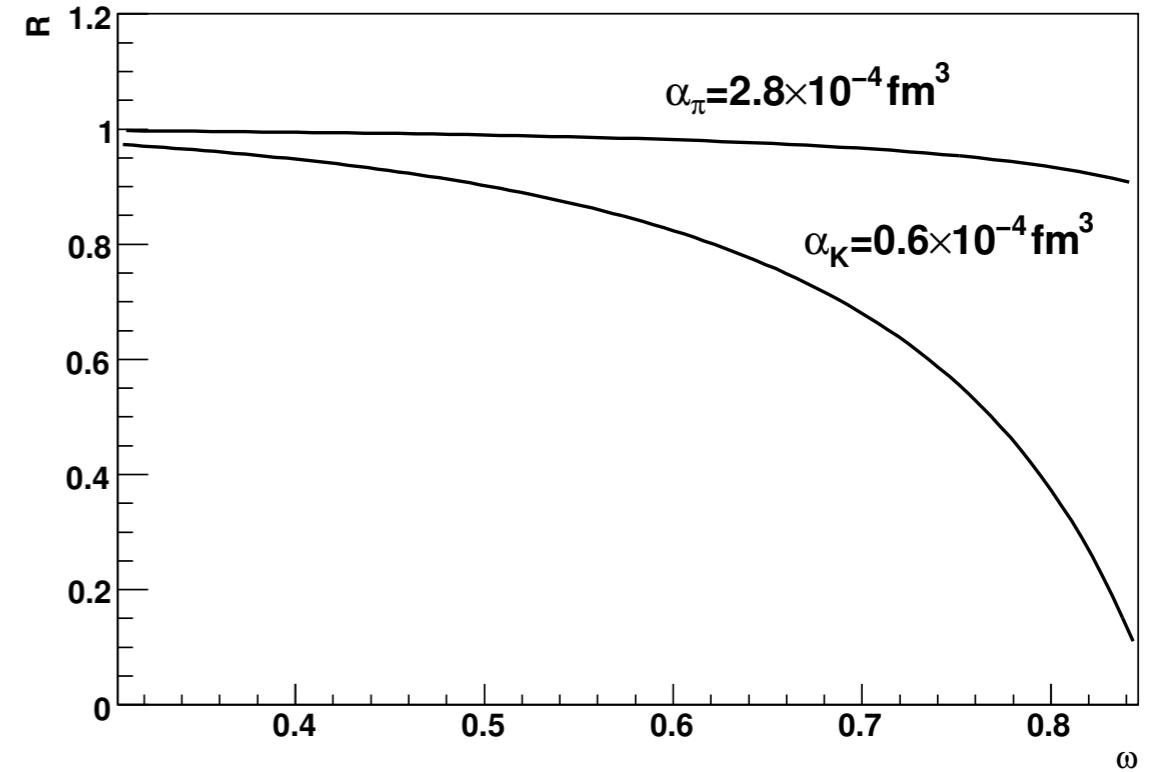
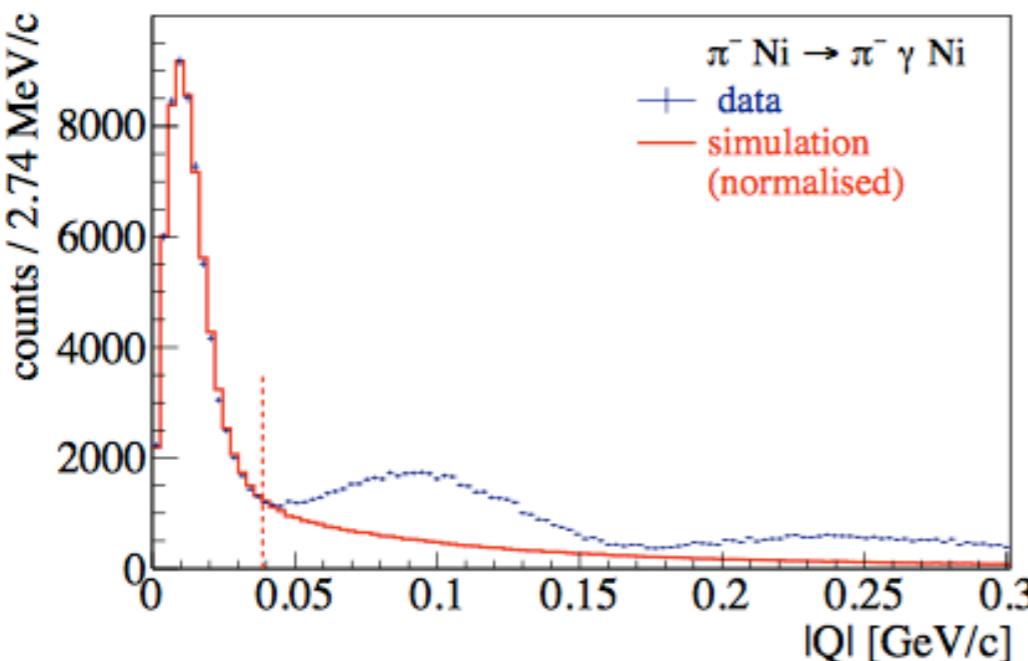
$$\alpha_K + \beta_K = 0$$

$$\alpha_K = \alpha_\pi \times \frac{m_\pi F_\pi^2}{m_K F_K^2} \approx \frac{\alpha_\pi}{5} \approx 0.6 \times 10^{-4} \text{ fm}^3$$

*Quark confinement model:*

$$\alpha_K + \beta_K = 1.0 \times 10^{-4} \text{ fm}^3$$

$$\alpha_K = 2.3 \times 10^{-4} \text{ fm}^3$$



$$R_K \approx \frac{\sigma}{\sigma_{p.l.}} = 1 - \frac{3}{2} \cdot \frac{x_\gamma^2}{1 - x_\gamma} \cdot \frac{m_K^3}{\alpha} \cdot \alpha_K$$

**1-st experimental problem:**

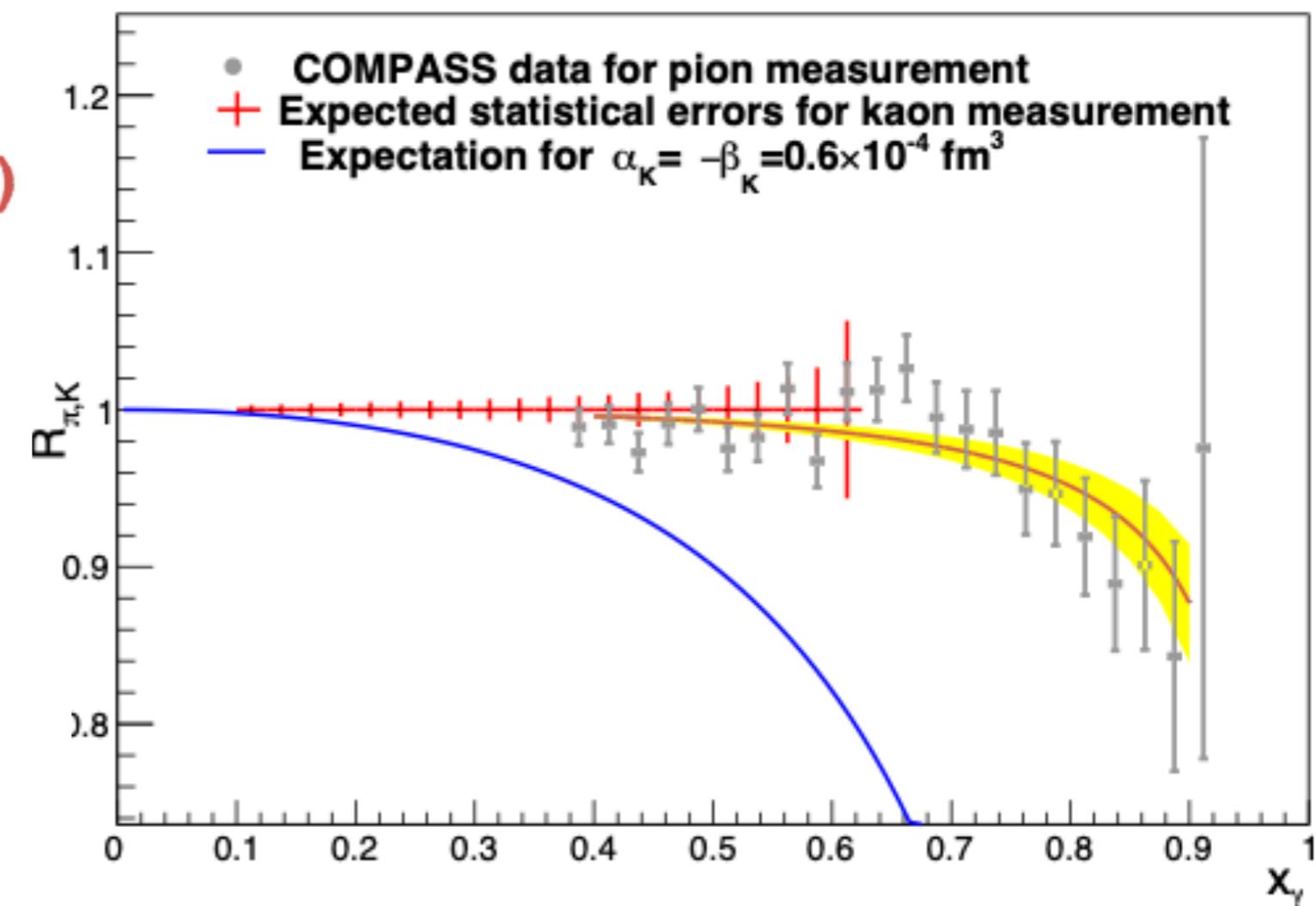
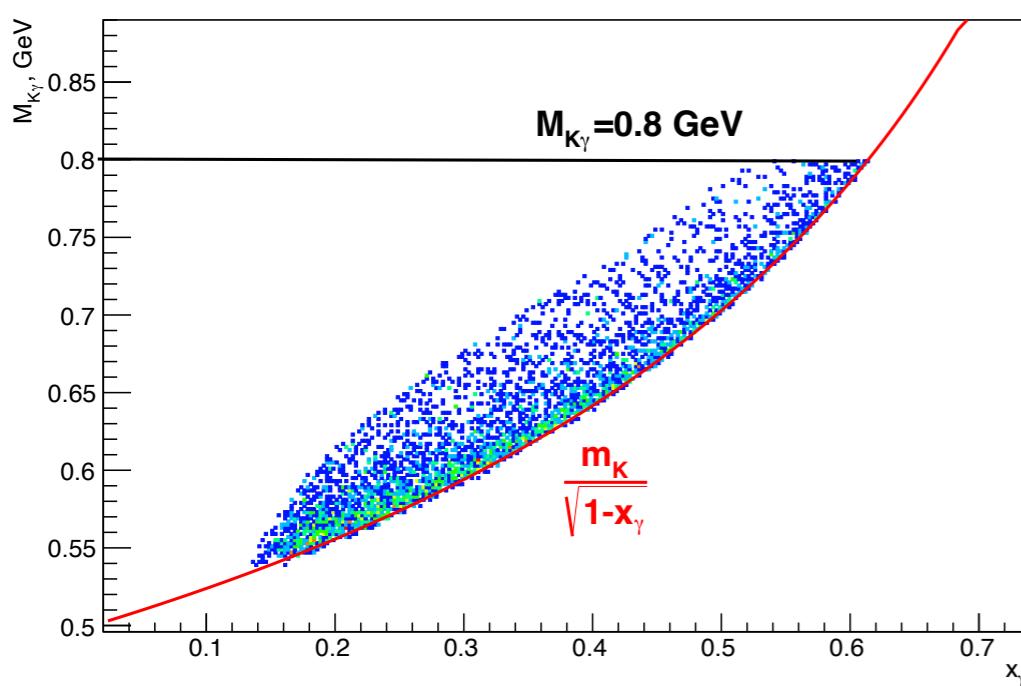
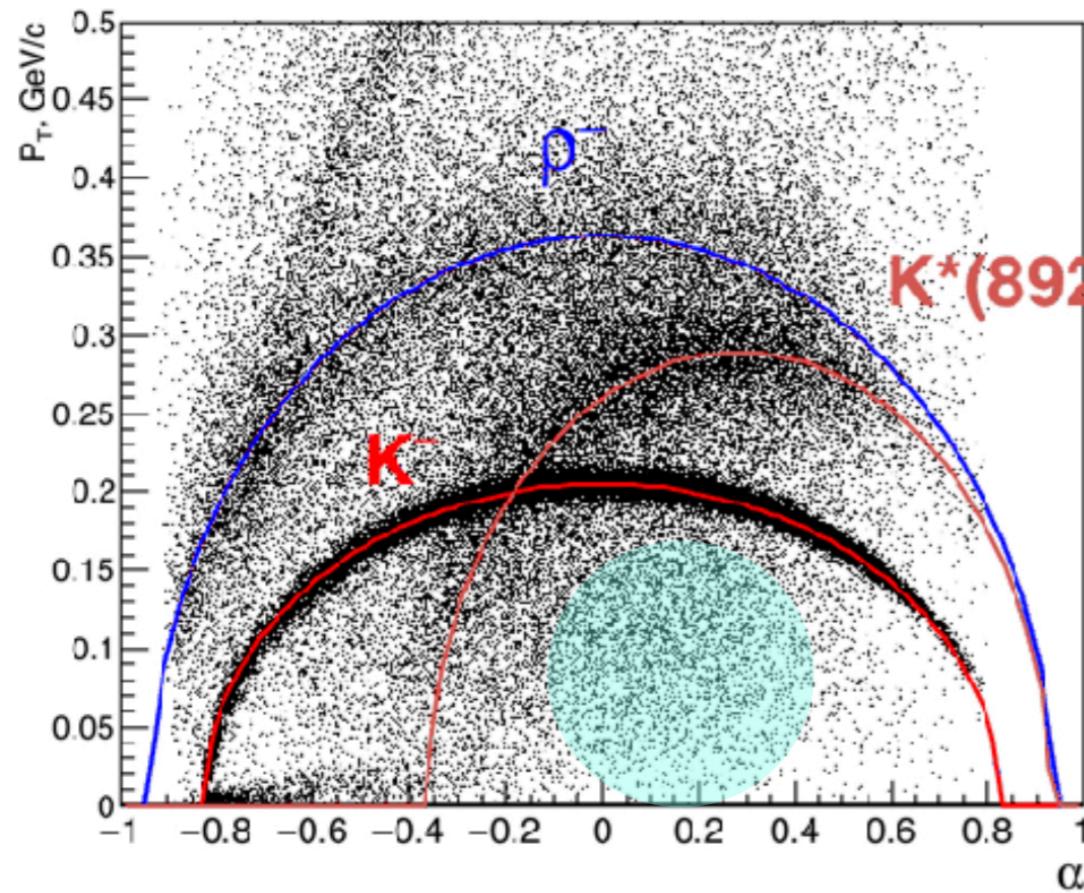
$$\sigma_{x\gamma} \sim 1/m_x^2$$

Primakoff peak for kaon is 10 times lower than for pion

Higher Z for target?

# Expectations

2-nd experimental problem:  $\pi^0$  - background

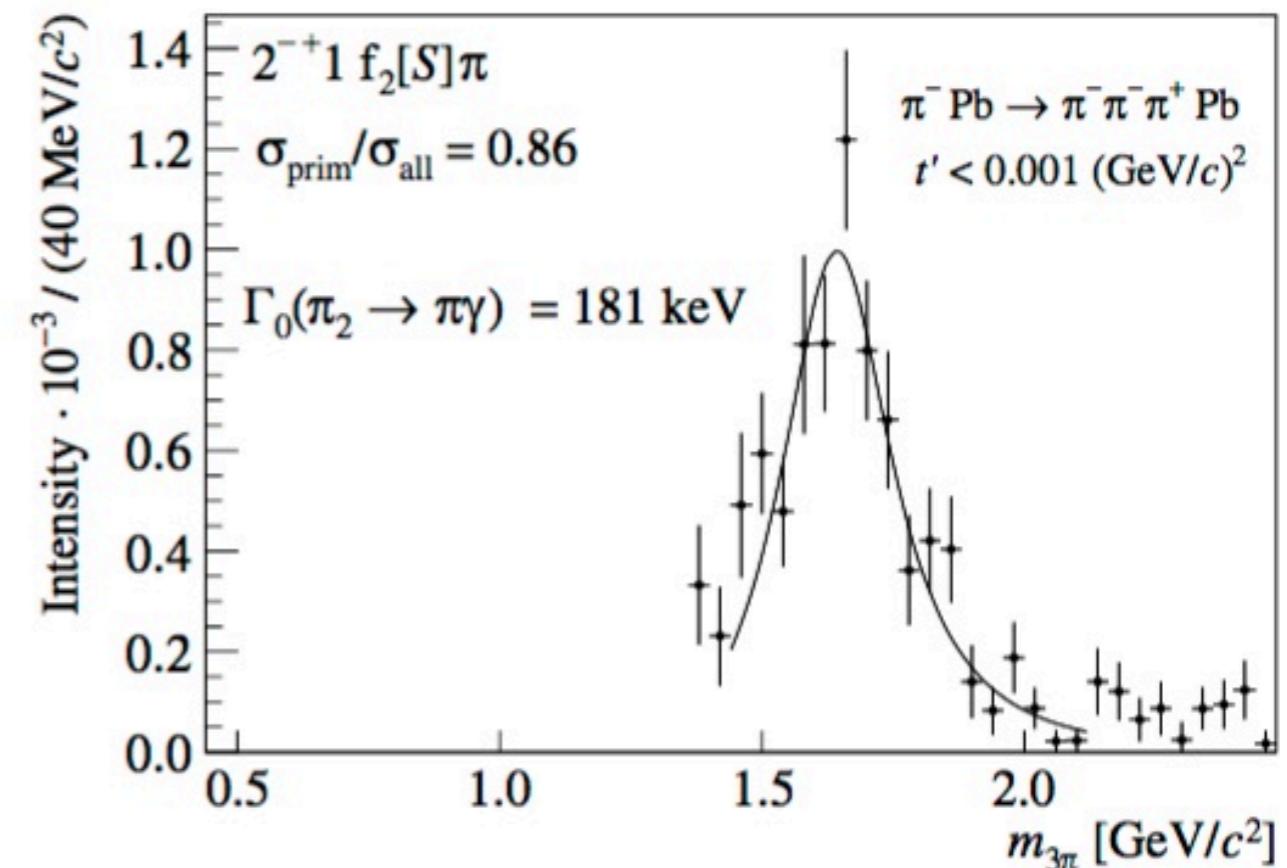
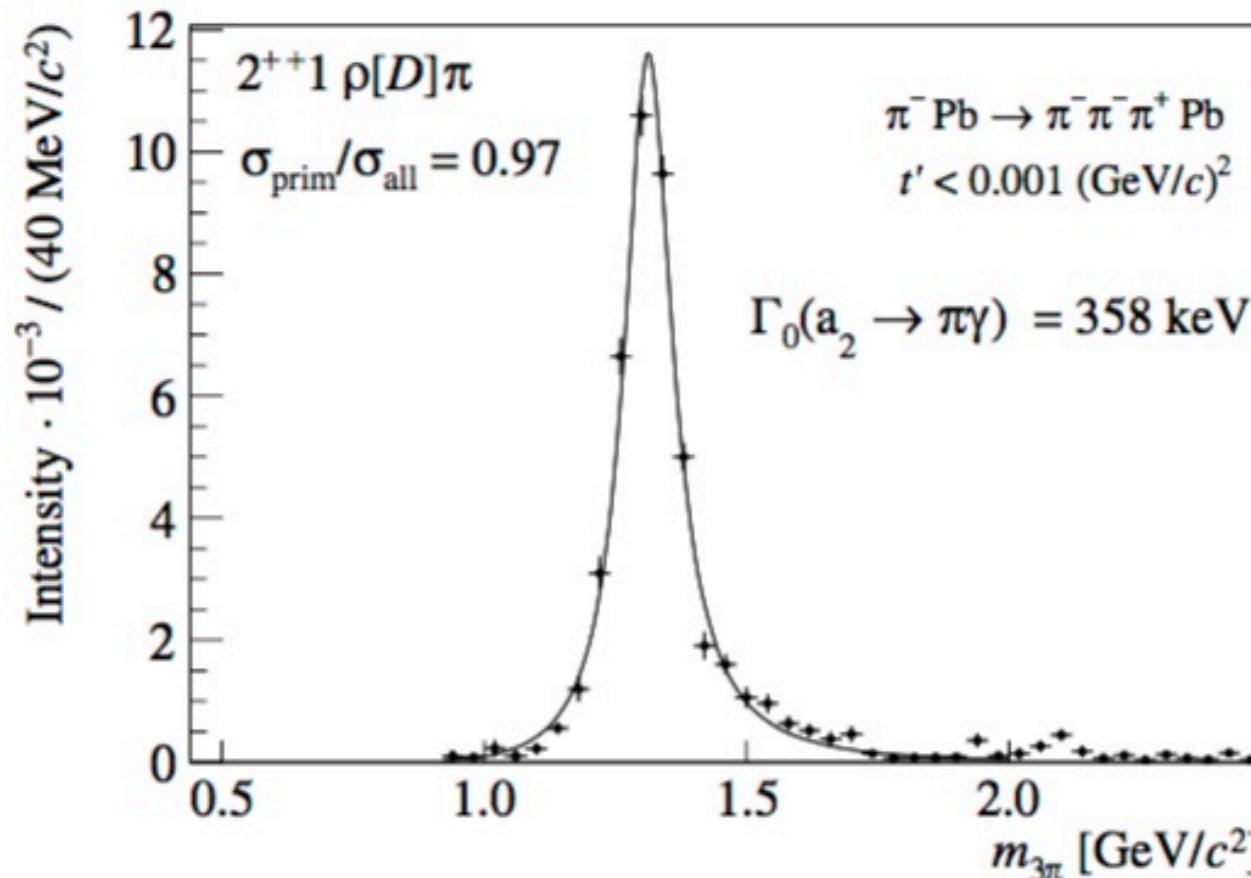


$$5 \times 10^{12} K^- \rightarrow 6 \times 10^5 K\gamma \text{ events}$$

$$\sigma_{\alpha_K \text{ stat}} = 0.03 \times 10^{-4} \text{ fm}^3$$

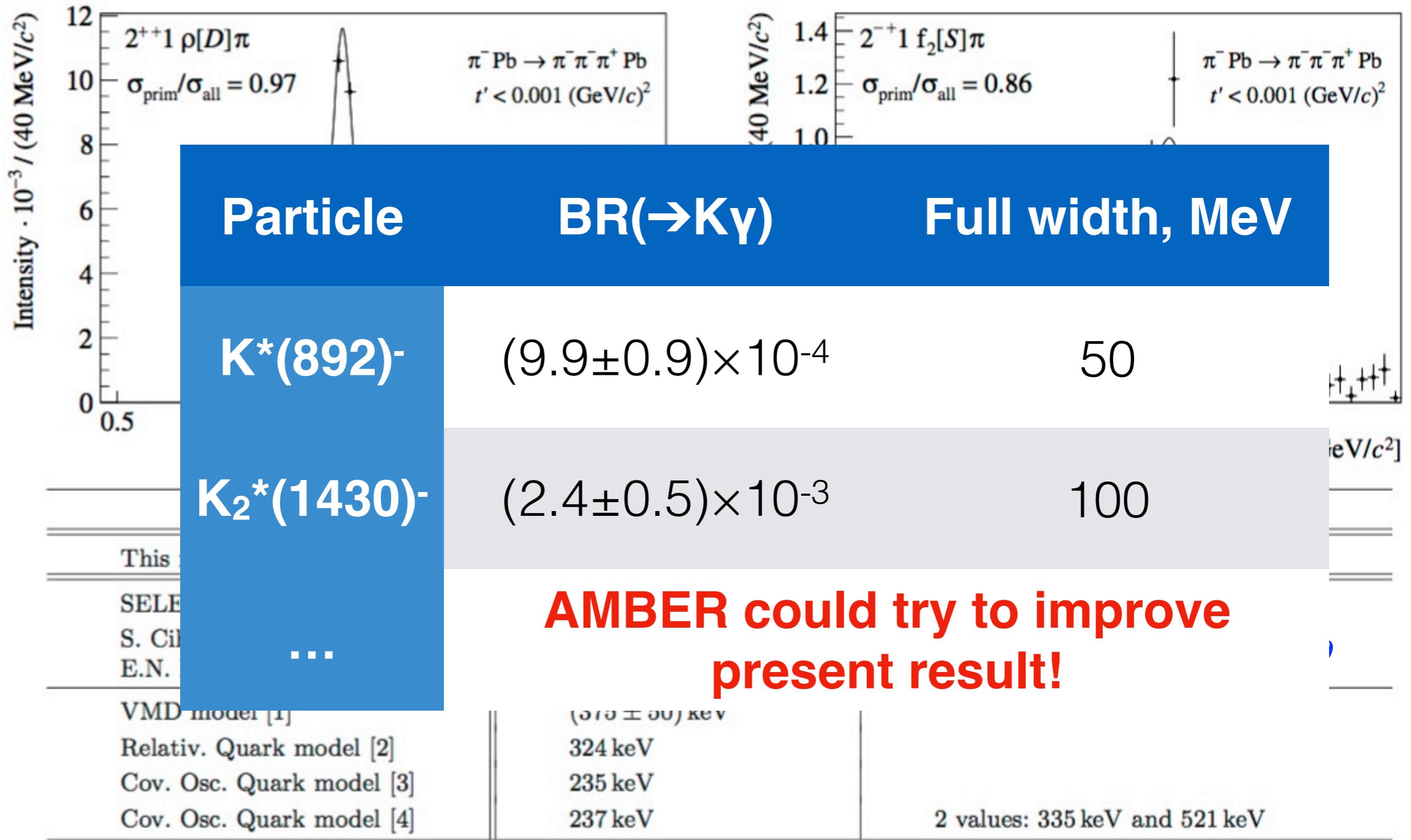


# Radiative widths of mesons



	$a_2(1320)$	$\pi_2(1670)$
This measurement	$(358 \pm 6 \pm 42) \text{ keV}$	$(181 \pm 11 \pm 27) \text{ keV} \cdot (0.56/\text{BR}_{f_2\pi})$
SELEX [21]	$(284 \pm 25 \pm 25) \text{ keV}$	
S. Cihangir <i>et al.</i> [24]	$(295 \pm 60) \text{ keV}$	
E.N. May <i>et al.</i> [25]	$(0.46 \pm 0.11) \text{ MeV}$	<b><i>EPJA 50 (2014) 79</i></b>
VMD model [1]	$(375 \pm 50) \text{ keV}$	
Relativ. Quark model [2]	324 keV	
Cov. Osc. Quark model [3]	235 keV	
Cov. Osc. Quark model [4]	237 keV	2 values: 335 keV and 521 keV

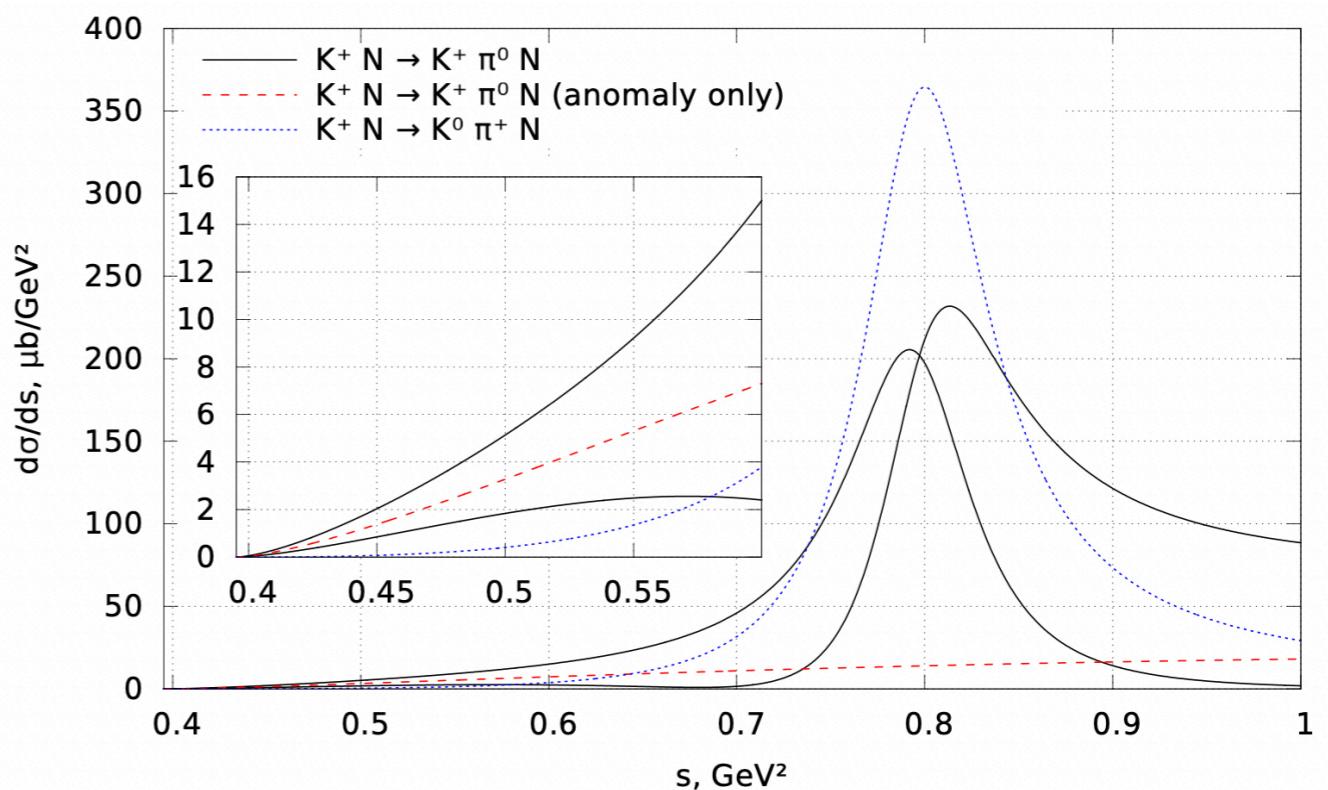
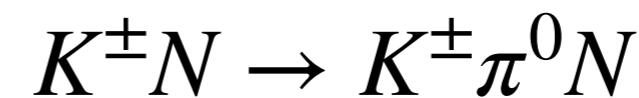
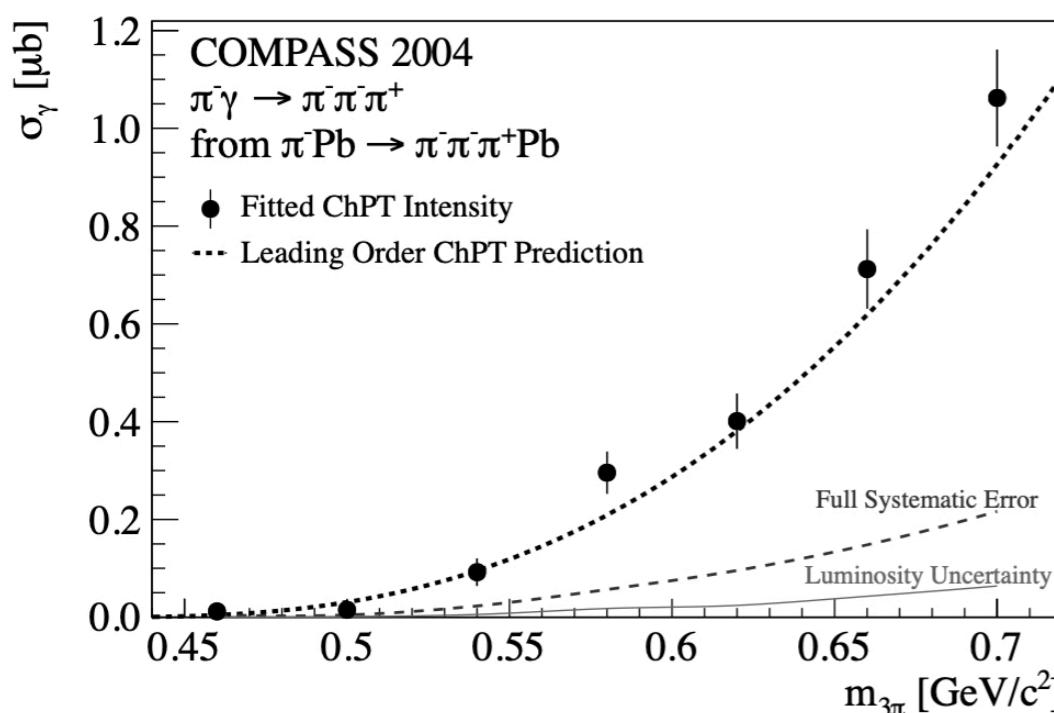
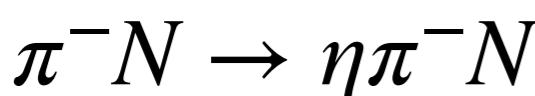
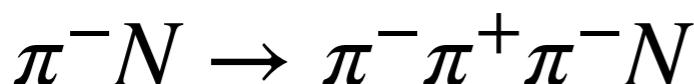
# Radiative widths of mesons



# Chiral anomaly and Primakoff cross sections near threshold

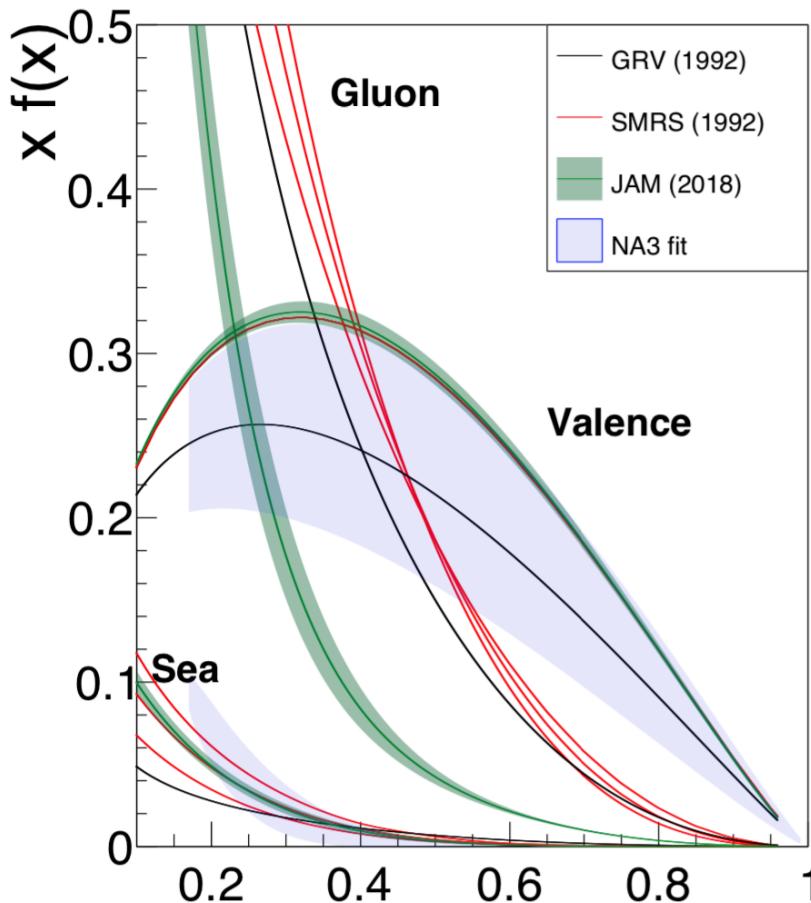


Chiral anomaly,  $F_{3\pi}$  constant



...

# Meson PDFs

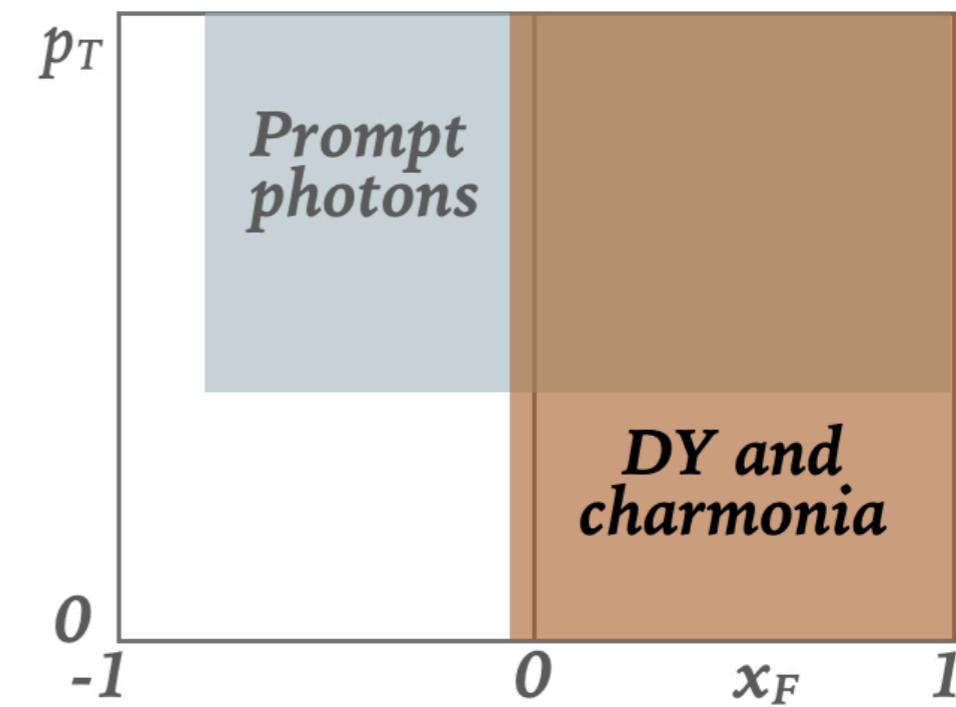
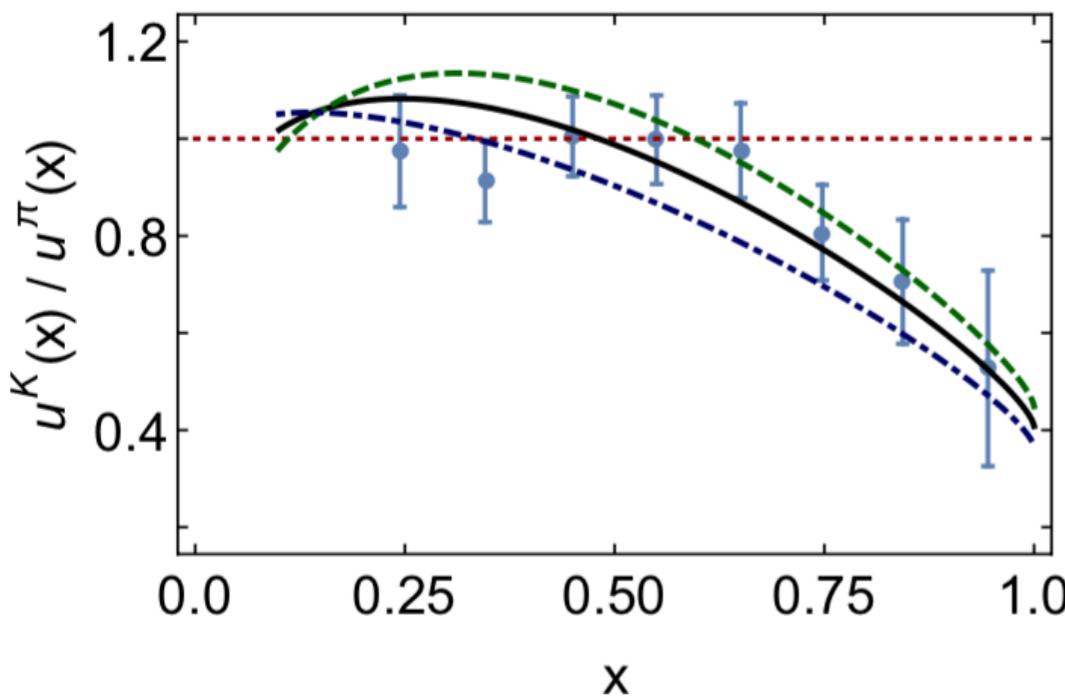


**GRV (1992)** set of pion PDFs: Drell-Yan, charmonia and prompt photon production experiments (**E615, NA10, WA70, NA24**).

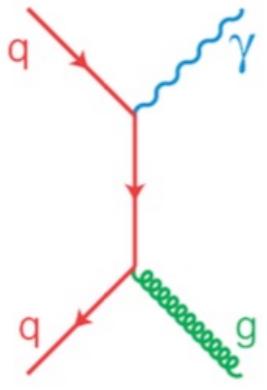
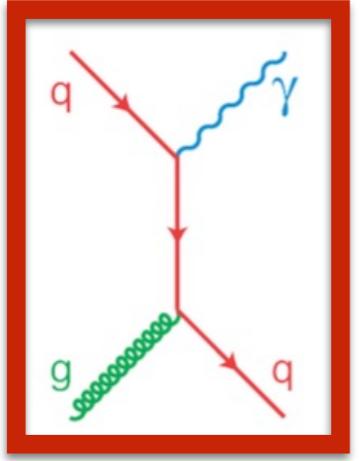
**SMRS (1992)**: basically the same old data.

**JAM (2018)** set: production of leading neutrons in DIS at HERA (**ZEUS, H1**).

**Kaon PDFs**: just 700 kaon-induced DY events at **NA3**



# Prompt-photon production



$$data \rightarrow \sigma_{inclusive} \gamma(p_T, x_F) \rightarrow g_K(x_K)$$

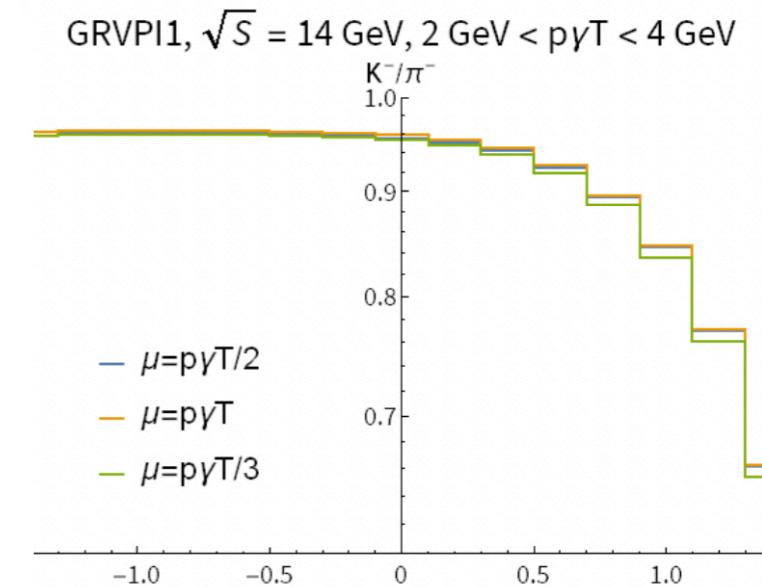
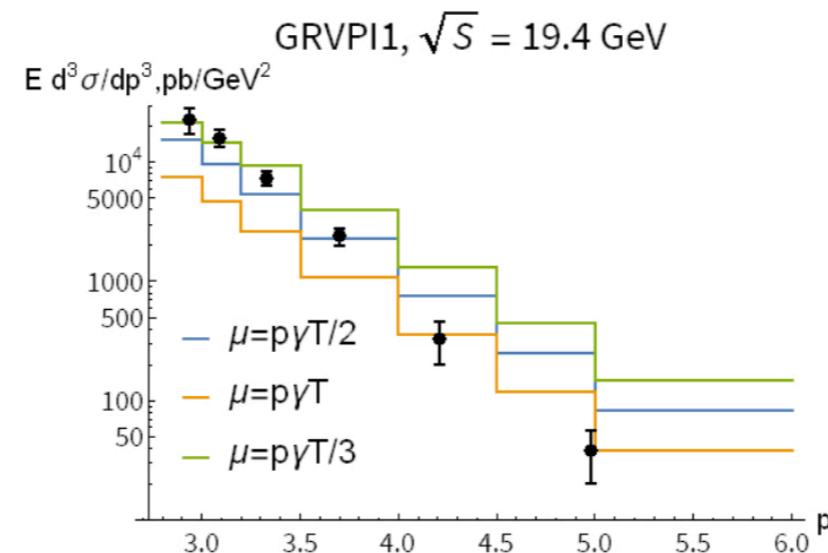
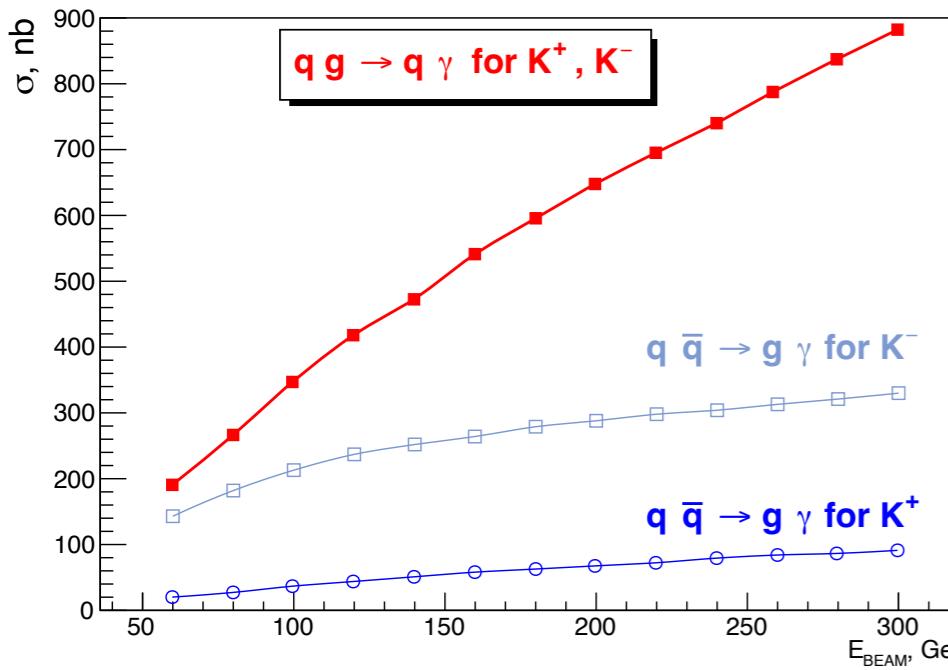
- separation of quark/gluon contribution in kaon ( $K^+$  vs  $K^-$ )
- pion as a reference!

$$x_{g \text{ min}} \approx x_{T \text{ min}}^2 = \frac{4p_T^2 \text{ min}}{s}$$

For  $p_T \text{ min} = 3 \text{ GeV}/c$  and  $P_{beam} = 190 \text{ GeV}$ :  $x_{g \text{ min}} = 0.1$

Observables:

$\sigma_K, \sigma_{K^+} - \sigma_{K^-}, \sigma_K/\sigma_\pi, (\sigma_{K^+} - \sigma_{K^-})/\sigma_\pi, \dots$



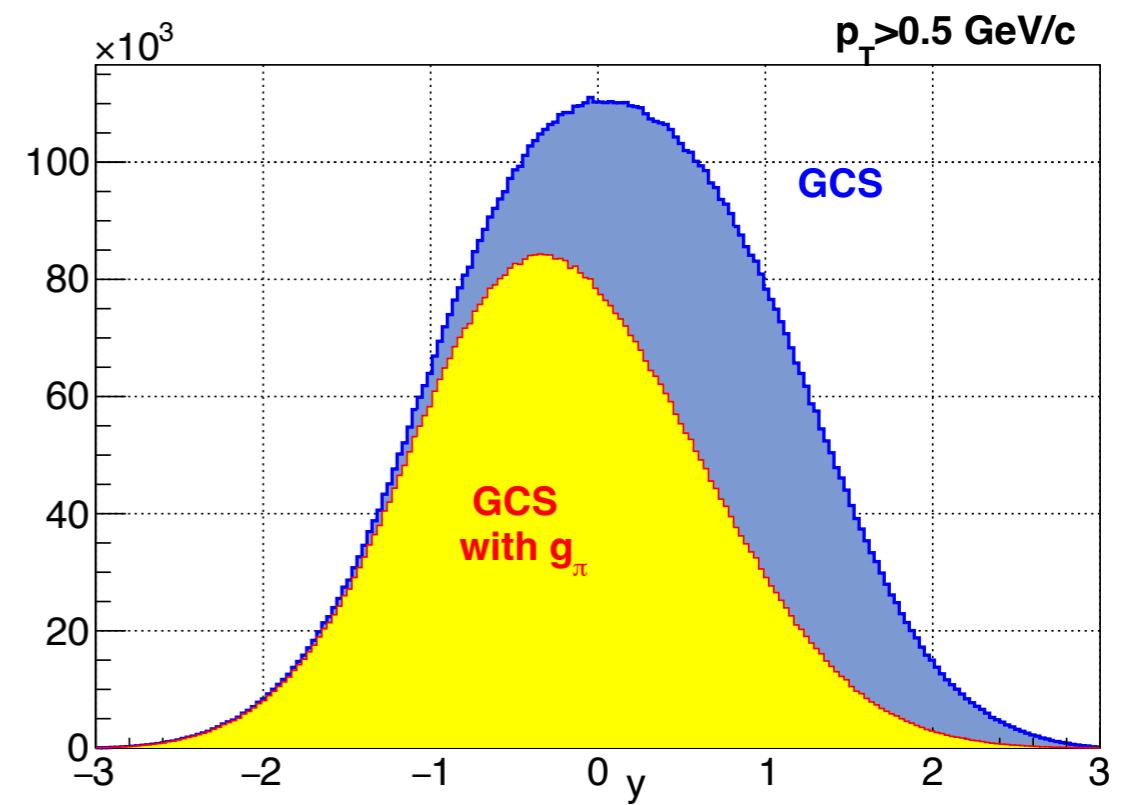
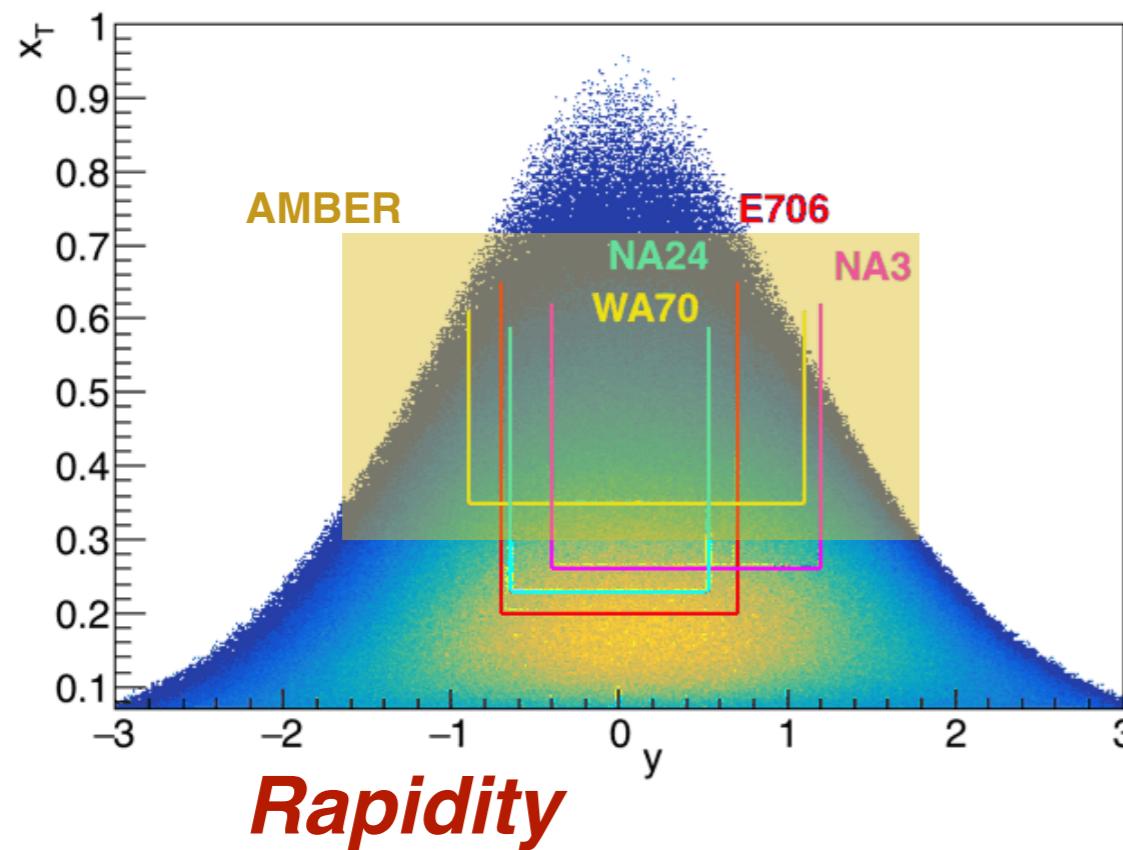
courtesy of A. Shipilova (Samara Univ.)

# Previous measurements at low $\sqrt{s}$

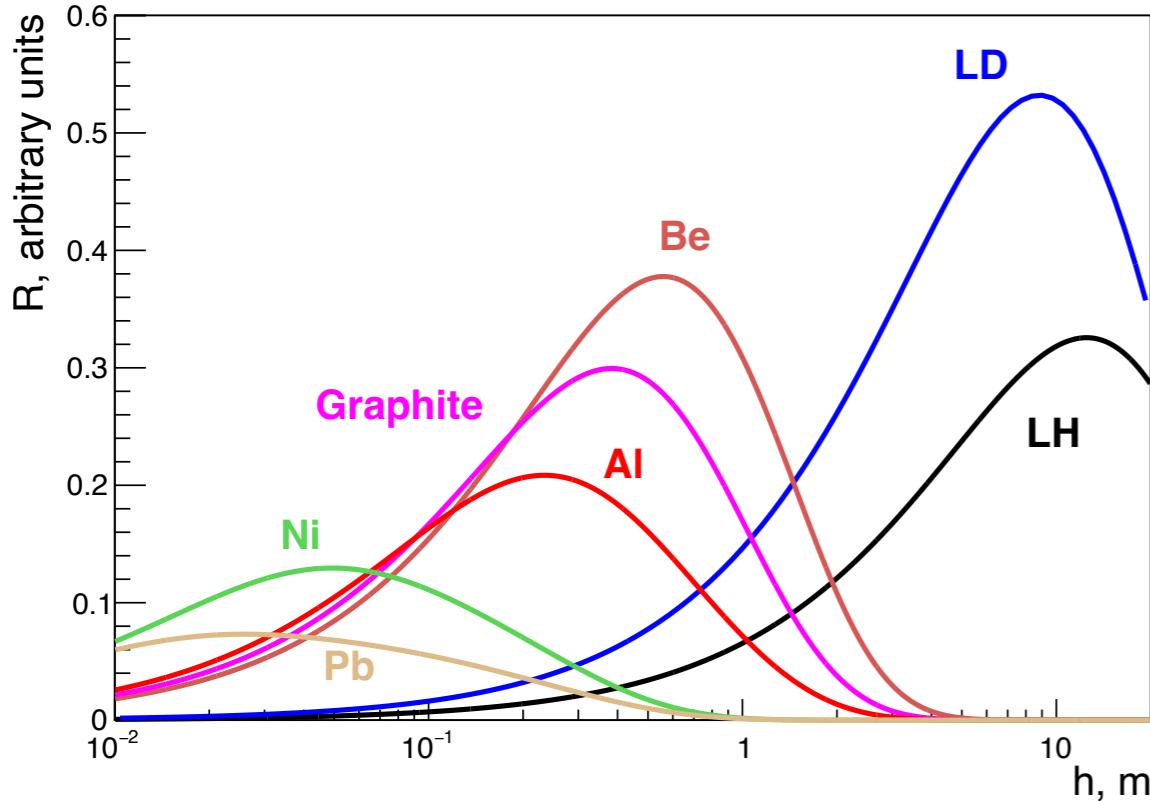
Experiment	Beam and target	$\sqrt{s}$ , GeV	$y$ range	$x_T$ range
E95 (1979)	p; Be	19.4, 23.75	-0.7 – 0.7	0.15 – 0.45
E629 (1983)	p, $\pi^+$ ; C	19.4	-0.75 – 0.2	0.22 – 0.52
NA3 (1986)	p, $\pi^+, \pi^-$ ; C	19.4	-0.4 – 1.2	0.26 – 0.62
NA24 (1987)	p, $\pi^+, \pi^-$ ; p	23.75	-0.65 – 0.52	0.23 – 0.59
WA70 (1988)	p, $\pi^+, \pi^-$ ; p	22.96	-0.9 – 1.1	0.35 – 0.61
E706 (1993)	p, $\pi^-$ ; Be	30.63	-0.7 – 0.7	0.20 – 0.65
E704 (1995)	p; p	19.4	<0.74	0.26 – 0.39
UA6 (1993,1998)	$\bar{p}$ ; p	24.3	-0.2 – 1.0	0.34 – 0.50

Fixed target  
measurements

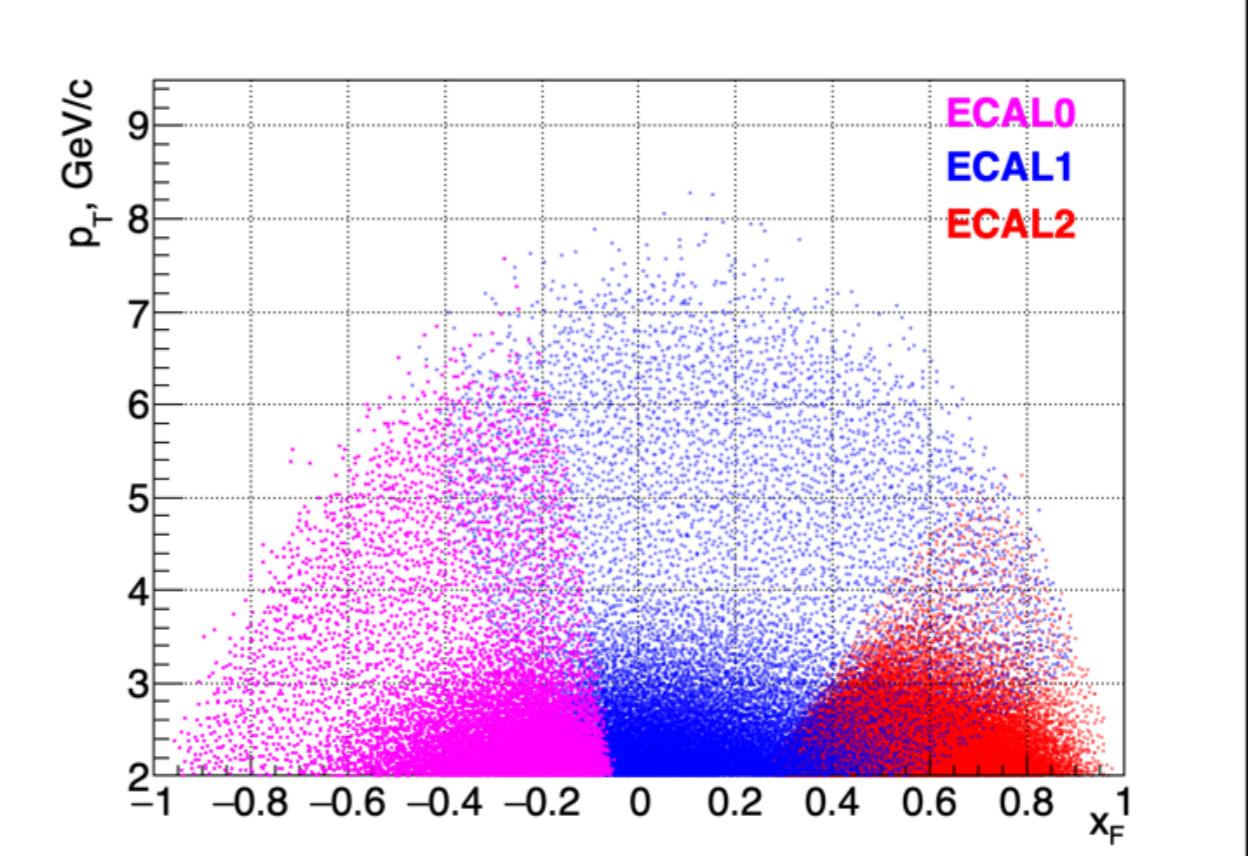
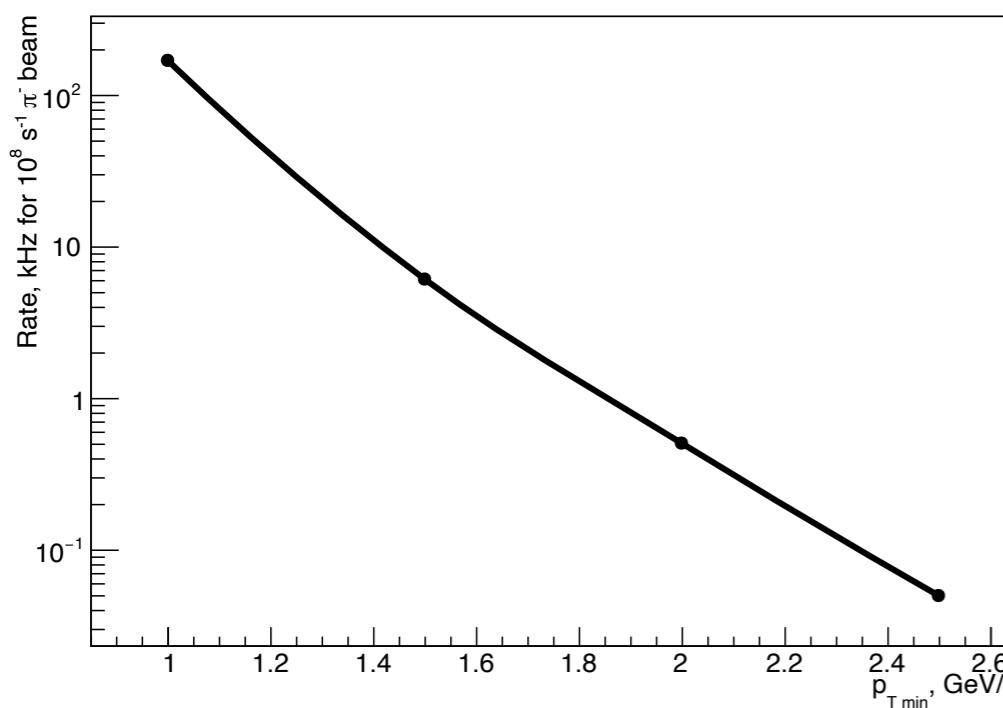
$$x_T = 2p_T/\sqrt{s}$$



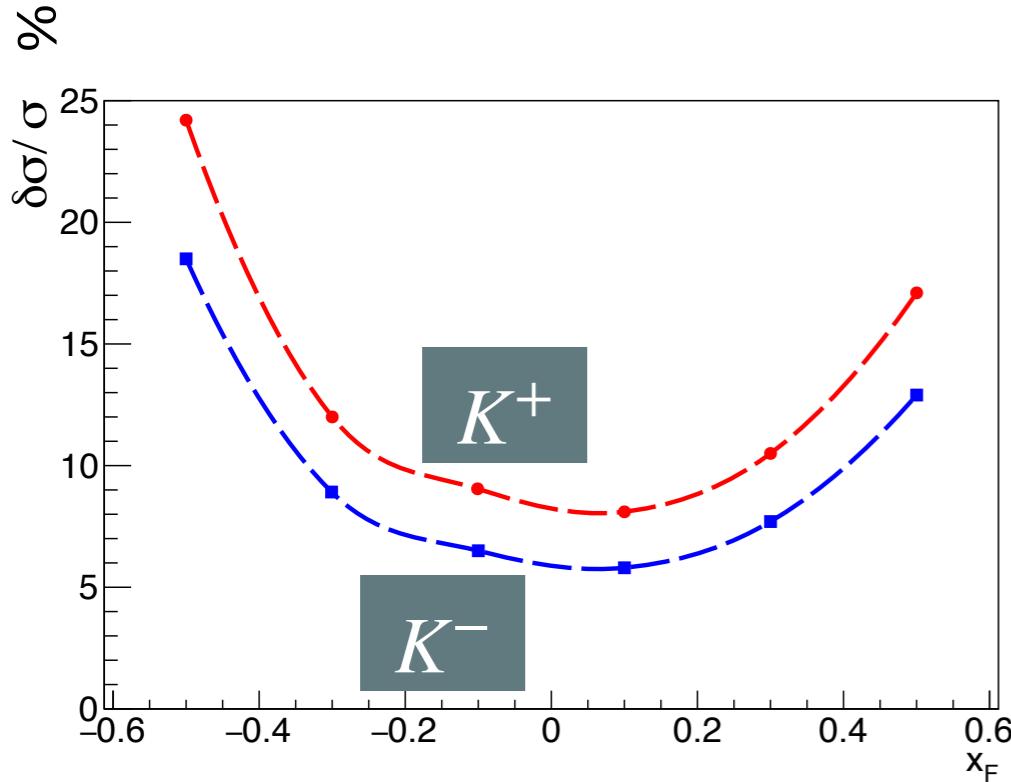
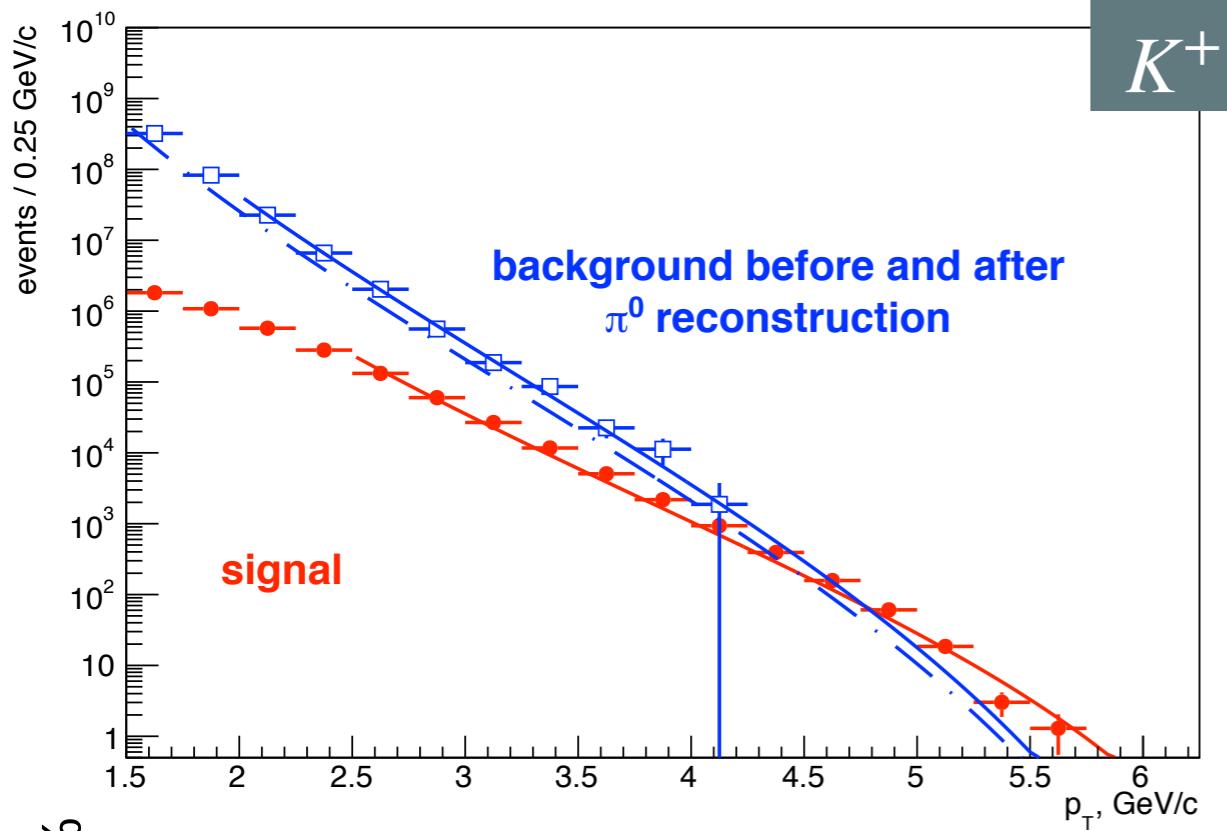
# Photons at AMBER



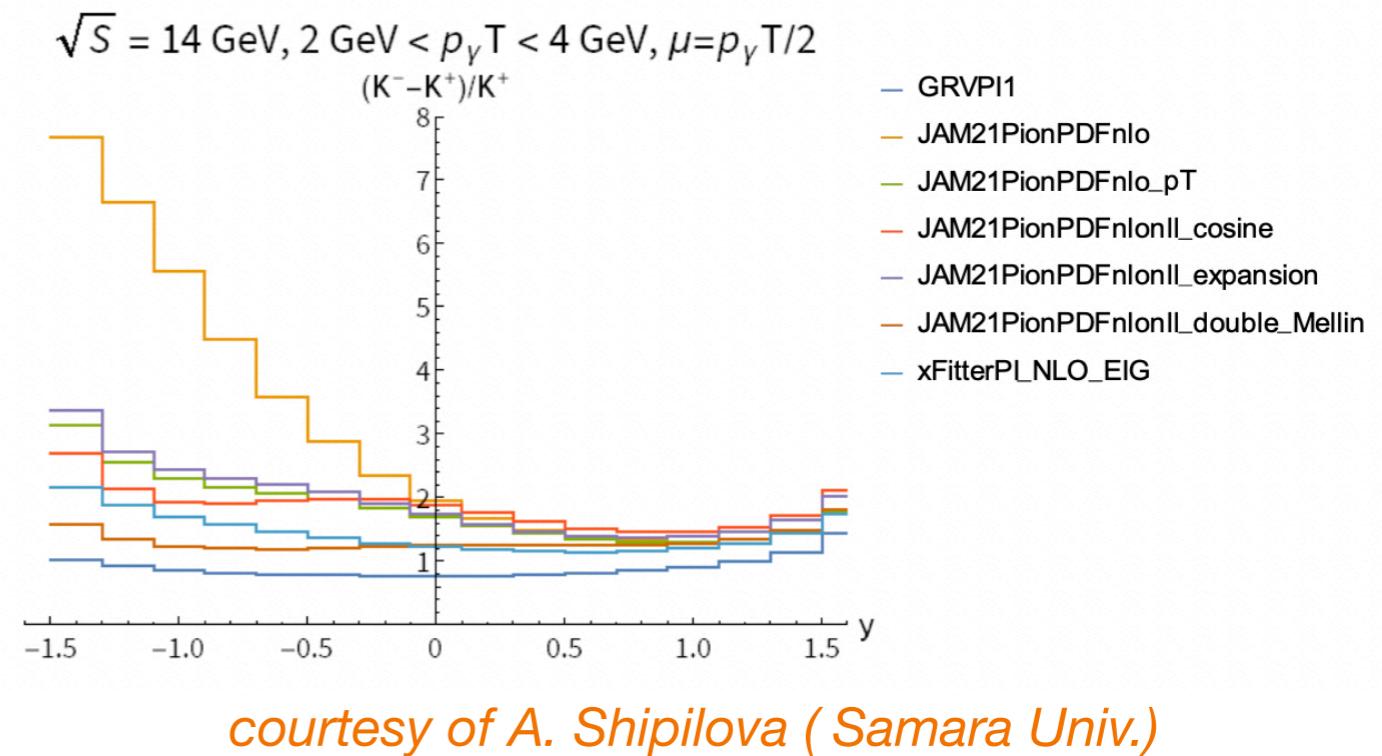
Target: 40 cm of graphite



# Expectations



Assuming the same gluon content for kaon as for pion



courtesy of A. Shipilova (Samara Univ.)

# Kaon-induced high-pT $\pi^0$ production

**LO**

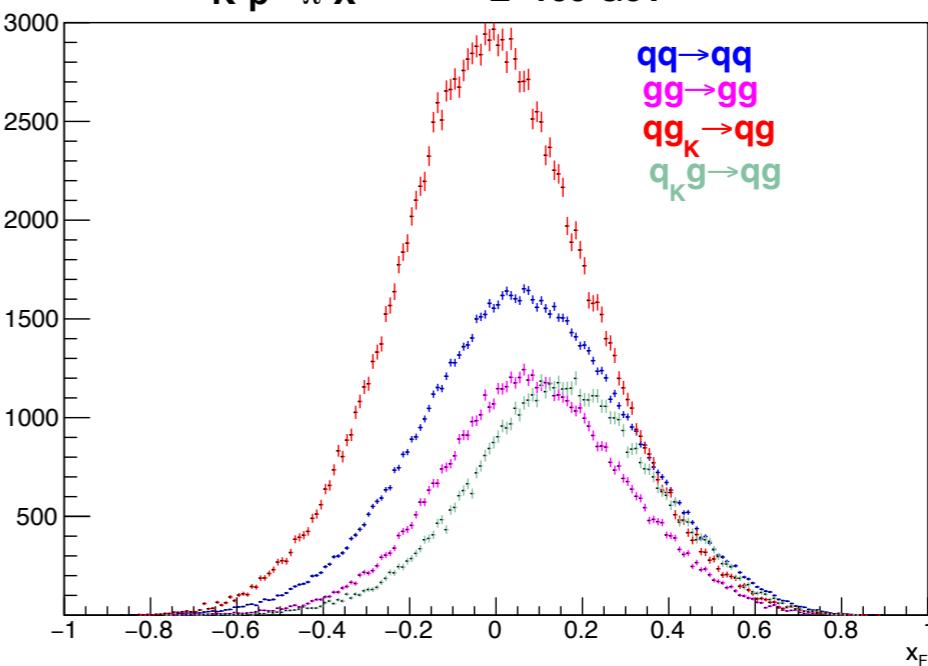
$qg \rightarrow qg$	51 %
$gg \rightarrow gg$	33 %
$qq \rightarrow qq$	15 %
$qq\bar{q}$	
$qq\bar{q}$	1 %
$gg \rightarrow qq$	

$p_T > 2 \text{ GeV}/c$

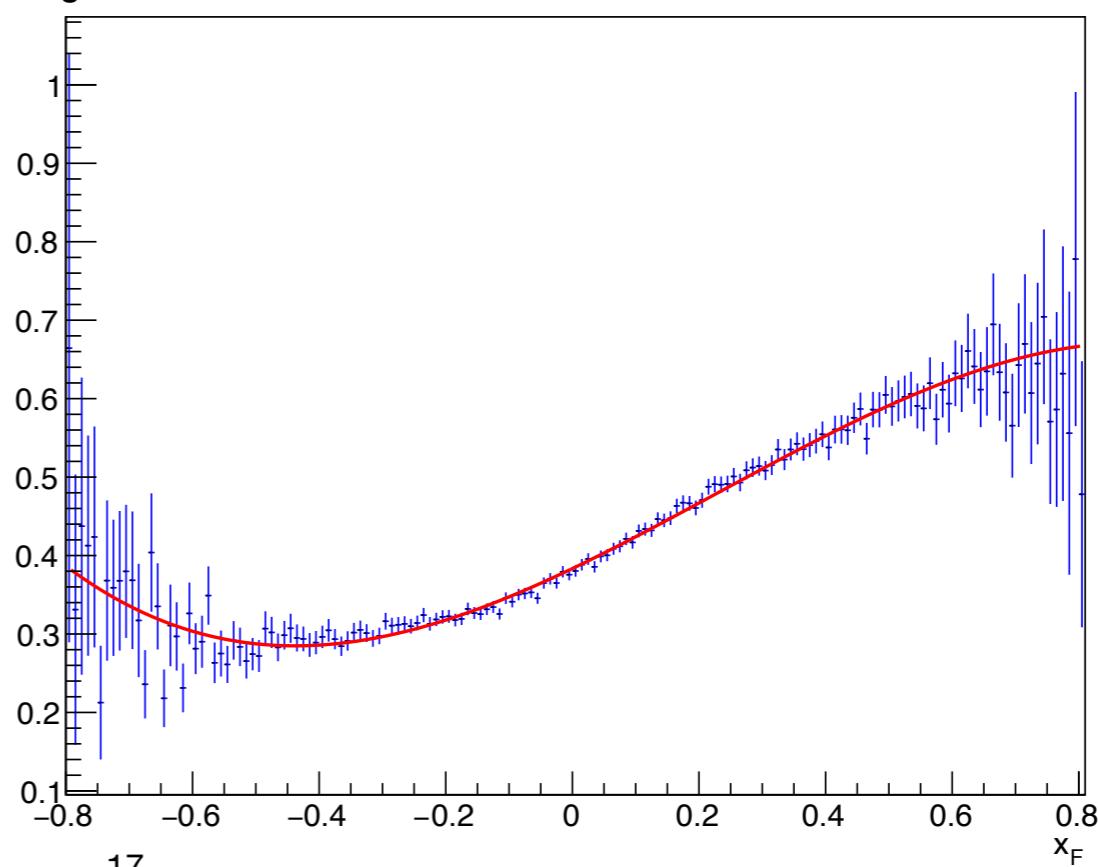
$p_T > 2 \text{ GeV}/c$

$K^+ p \rightarrow \pi^0 X$

$E = 100 \text{ GeV}$



$K_{\text{gluonless}}/K$



# Beam requirements

BEAM	Primakoff	High-pT photons
Beam particle	K-	K $^{+/-}$ , $\pi^{+/-}$
Beam momentum	>40 GeV	190 GeV
dP/P	1 %	not critical
Beam intensity	$\sim 5 \times 10^6$ kaons s $^{-1}$	$\sim 5 \times 10^6$ kaons s $^{-1}$
Beam spot on target	$\sim 5 \times 5$ mm	$\sim 5 \times 5$ mm
Beam time request	1 year	1 year
Particle ID by CEDAR	pion suppression $\sim 10^4$	pion suppression $\sim 10^3$
TARGET	> Ni $\sim 0.5 X_0$	$\sim C \sim 2 X_0$

# Summary

- AMBER as successor of COMPASS with its three calorimeters is a unique facility for the study of processes with photons in the final state.
- AMBER can perform sophisticated test of low-energy QCD models via kaon-induced Primakoff reactions:
  - first measurement of kaon polarizability
  - update the estimation of radiation width of kaon states
  - chiral anomaly study
  - investigation of Primakoff cross sections dynamics near threshold
- Measurement of the kaon-induced high-pT prompt photon and  $\pi^0$  production cross section can provide an important information about gluon content in kaon.