

Collider constraints on massive gravitons coupling to photons

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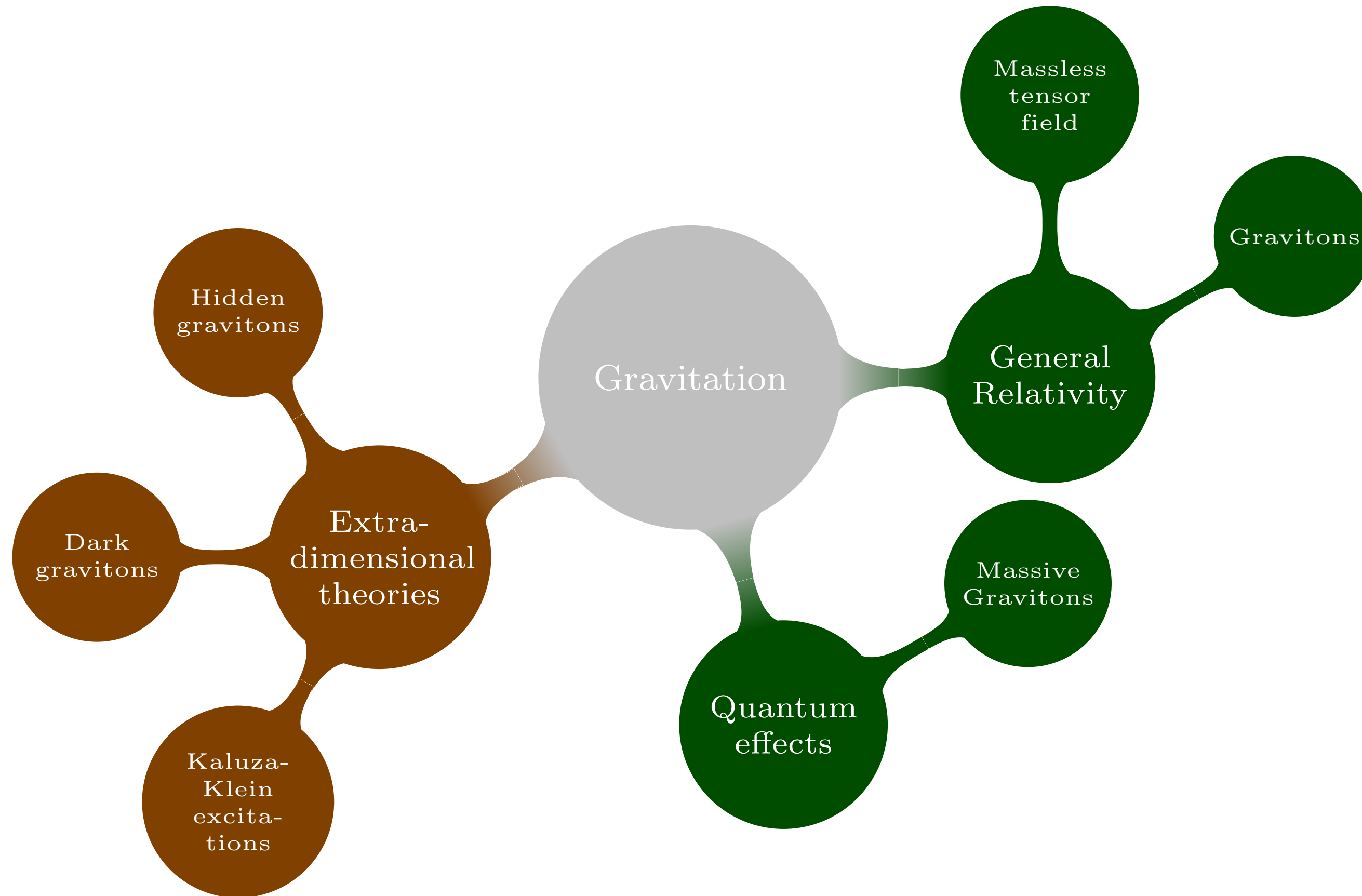
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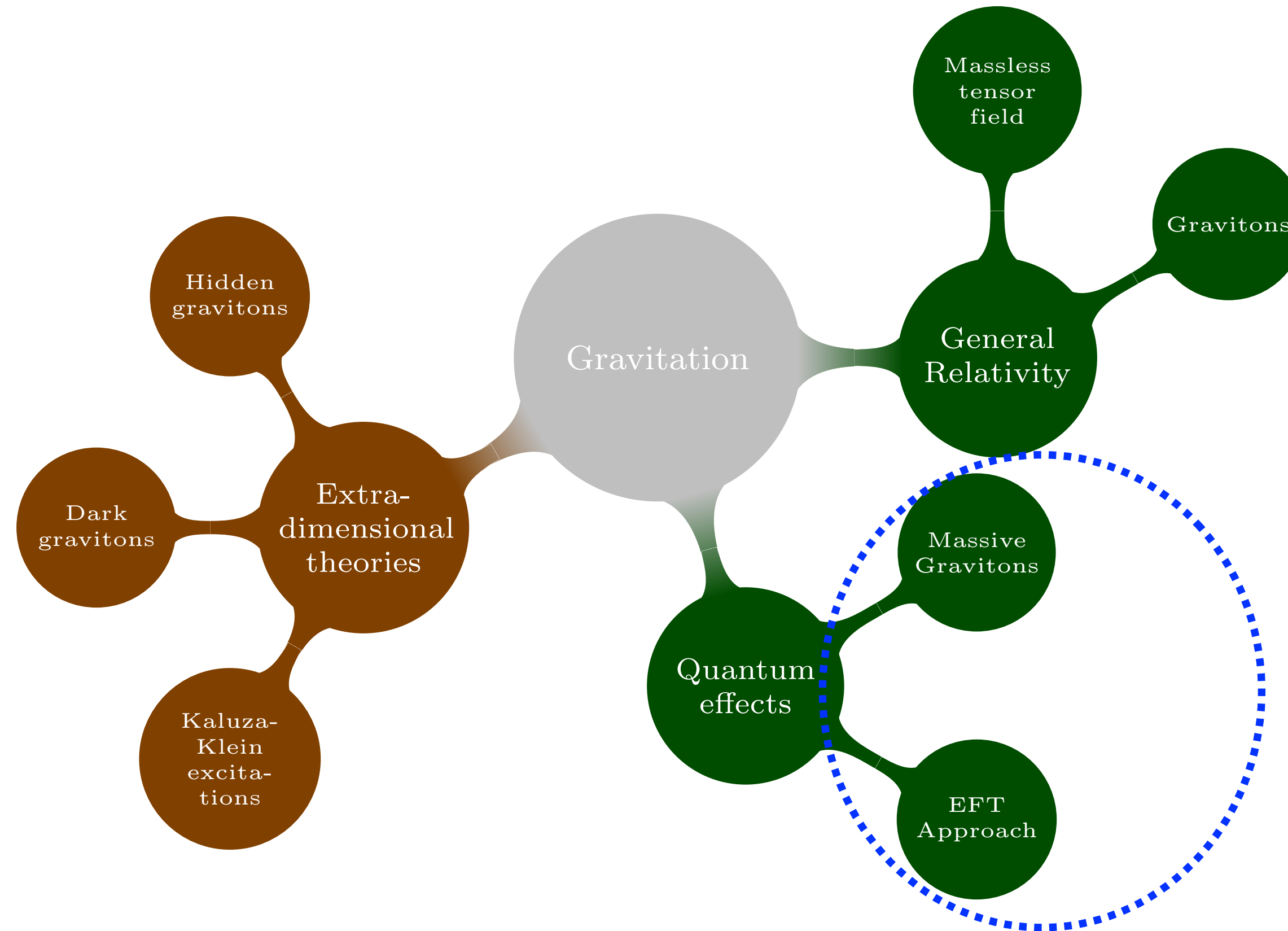
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Phys.Lett.B 846 (2023) 138237 (<https://arxiv.org/abs/2306.15558>)

INTRODUCTION



INTRODUCTION



Massive Gravitons in EFT

- In the EFT framework, the interaction of the gravitons with SM field is given by the following **Fierz-Pauli Lagrangian density**:

The diagram shows the Fierz-Pauli Lagrangian density $\mathcal{L}_{V,f}^G$ with callouts for its components:

- The strength of the coupling**: points to the coefficient $k_{V,f}$.
- Energy-Momentum tensor**: points to $T_{\mu\nu}^{V,f}$.
- Energy scale**: points to the denominator Λ .
- The spin-2 quantum field**: points to $G^{\mu\nu}$.

$$\mathcal{L}_{V,f}^G = \frac{k_{V,f}}{\Lambda} T_{\mu\nu}^{V,f} G^{\mu\nu}$$

- For gravitons coupling to photons:

The diagram shows the graviton-photon interaction Lagrangian \mathcal{L}_γ^G with a callout for the coupling constant $g_{G\gamma}$:

- Graviton-Photon coupling**: points to $g_{G\gamma}$.

$$\mathcal{L}_\gamma^G = g_{G\gamma} \left(-F_{\mu\rho} F_\nu^\rho + \frac{1}{4} \eta_{\mu\nu} (F_{\rho\sigma})^2 \right) G^{\mu\nu}$$

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Graviton-Photon coupling

The Goal of this work is to derive constraints on this coupling

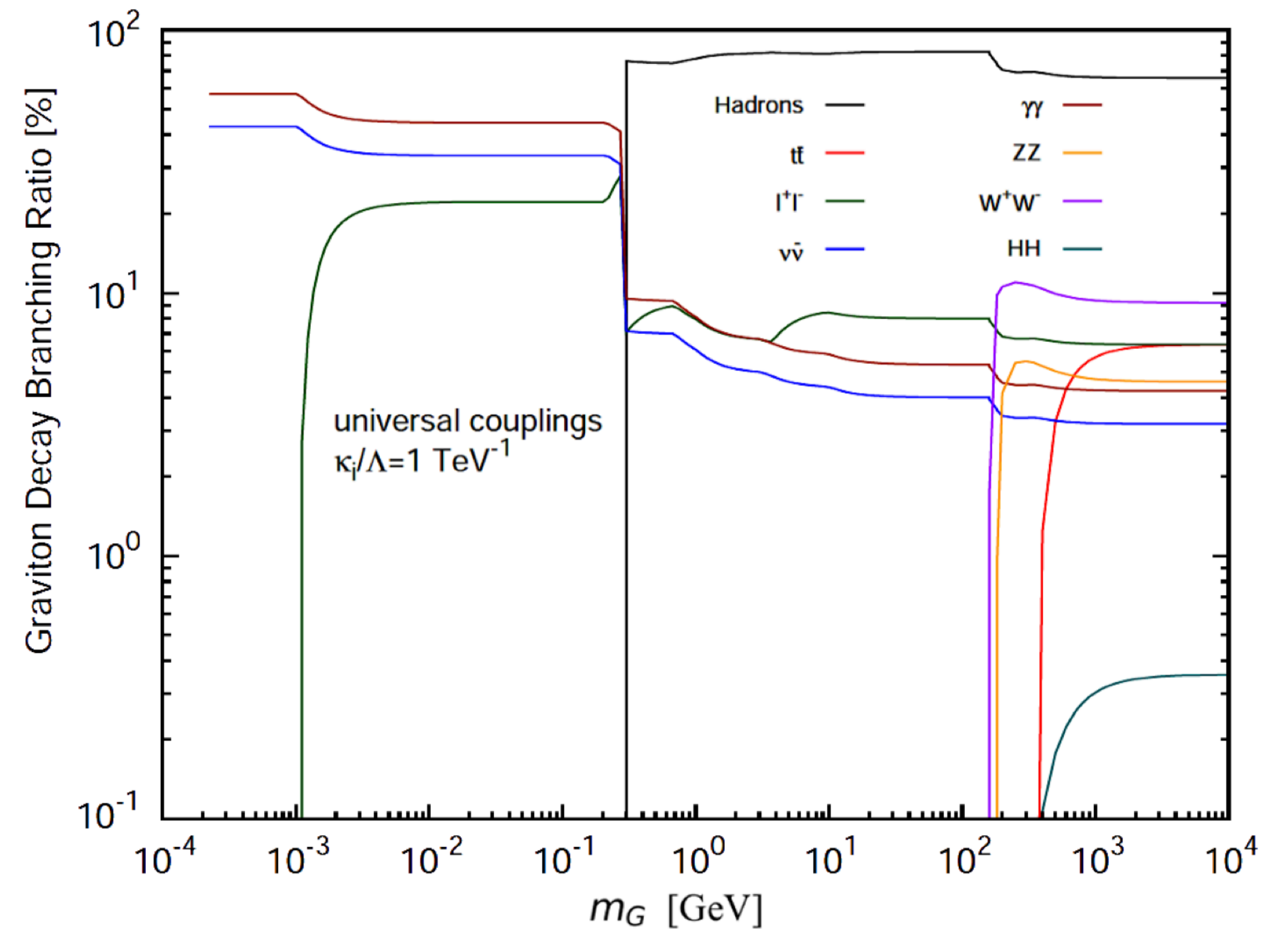
Graviton couplings

- Graviton without universal coupling , the simplified approach $\text{Br}(G \rightarrow \gamma\gamma) = 1$

- Graviton with universal coupling to all standard Model particles, it can decay with different modes, the $\text{Br}(G \rightarrow XX)$ depends on the graviton mass m_G

- The graviton coupling to di-photons is dominant only at low masses

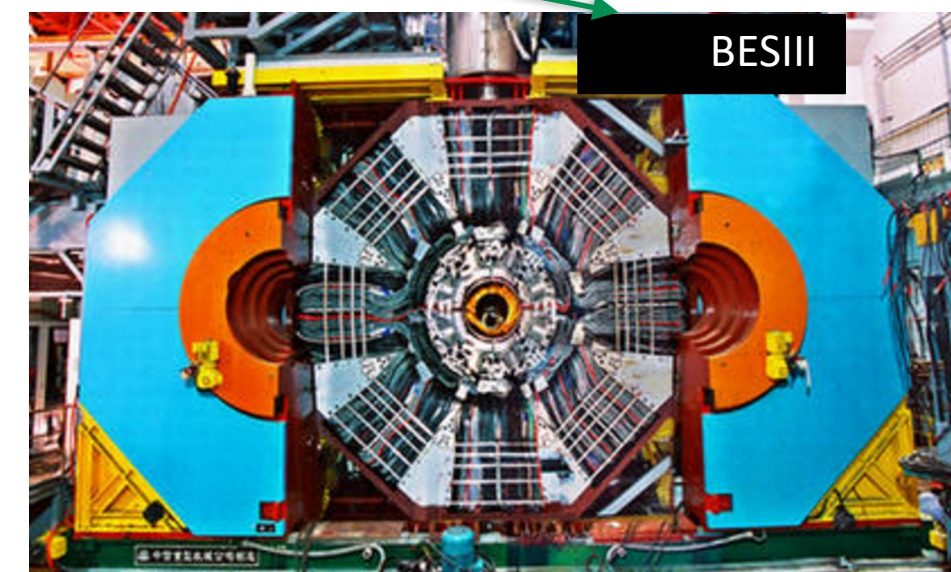
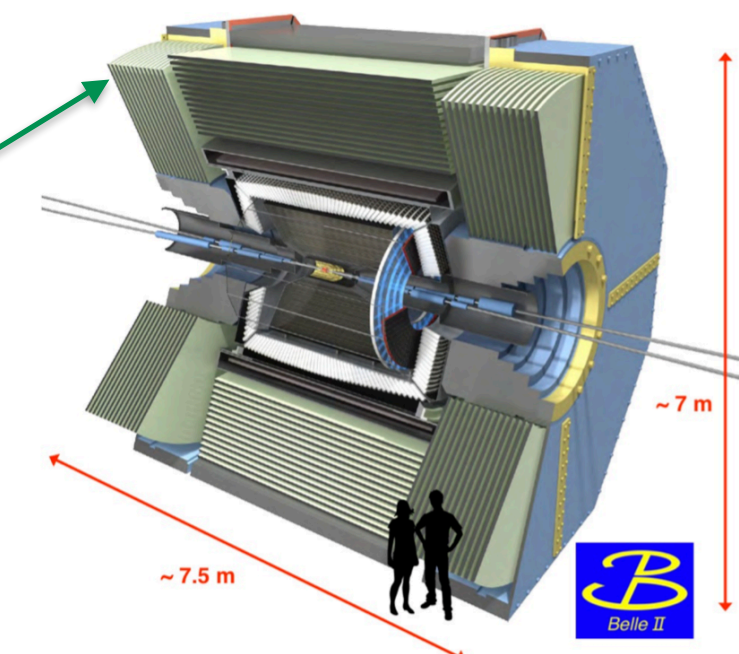
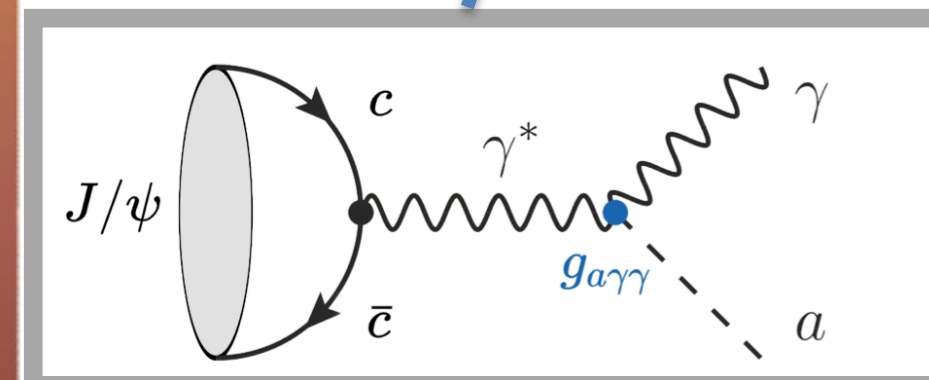
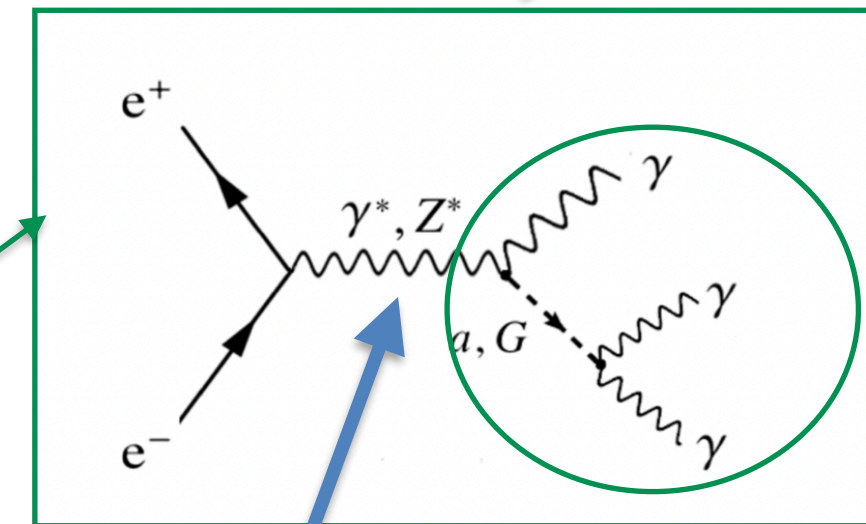
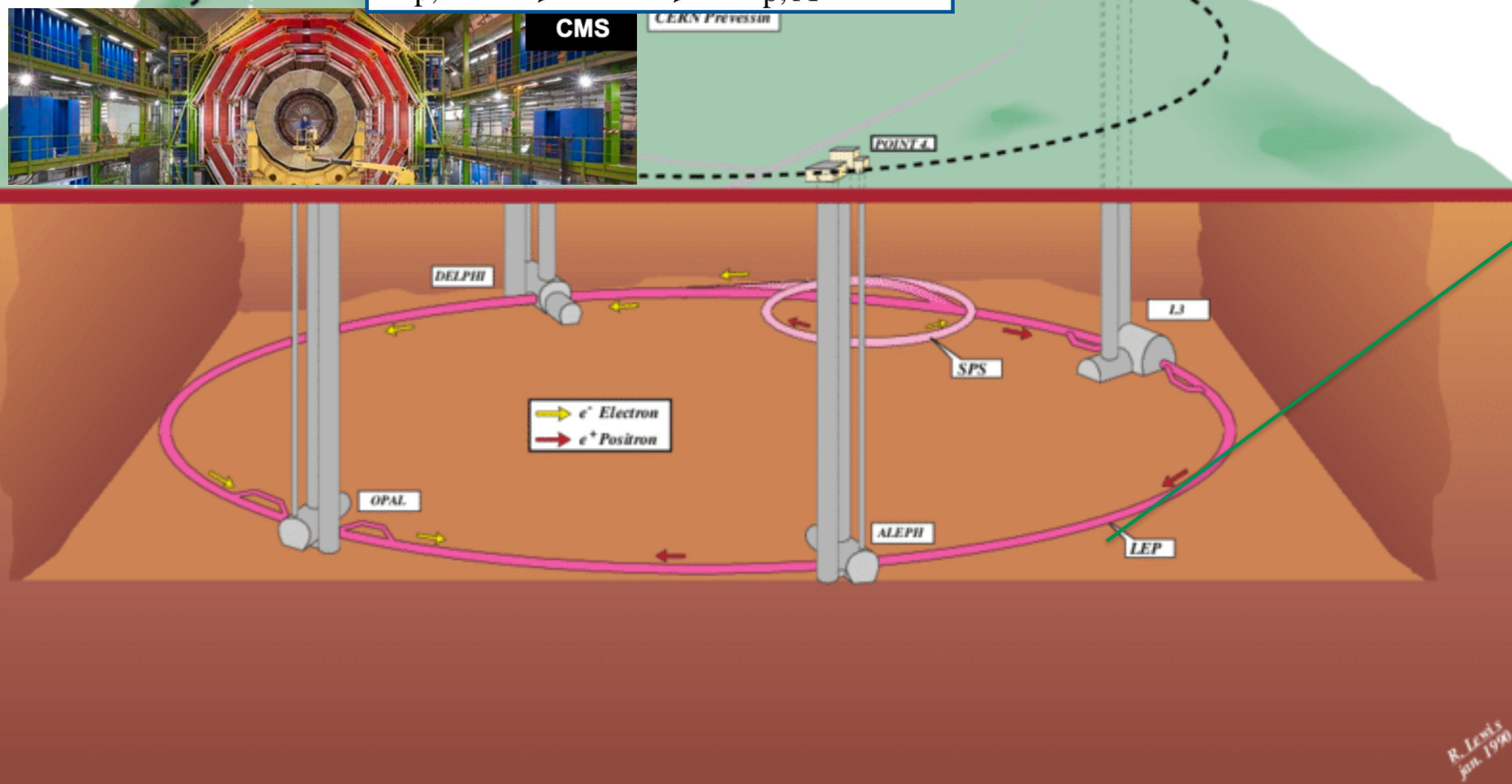
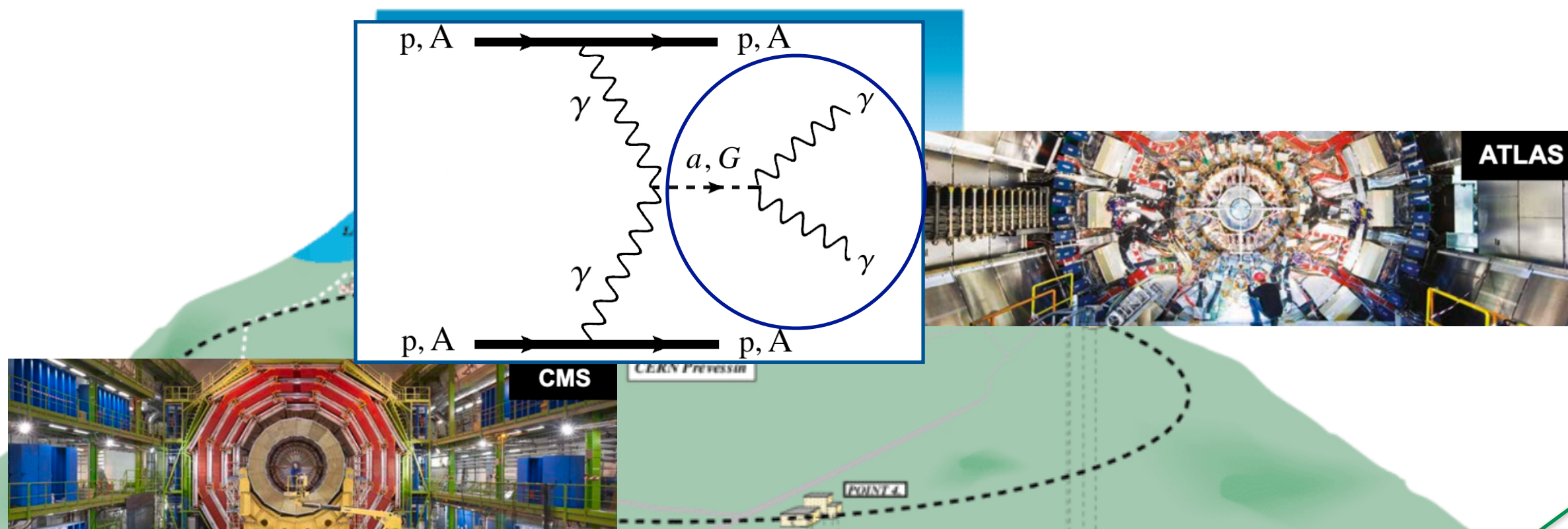
- Above a few GeV, $\text{Br}(G \rightarrow \gamma\gamma) \approx 0.05$



Motivation

- Photon-Photon collisions (Light-by-Light scattering: LbL) provide a clean environment to search for BSM particles (Axion-Like-Particle , spin0) and (gravitons, spin2)
- Recent searches for exclusive diphotons resonances produced in LbL at the **LHC** have allowed placing the most stringent constraints on **ALPs** over $m_a \approx 5 - 100$ GeV in PbPb UPCs [ATLAS](#), [CMS](#)
And $m_a \approx 0.5 - 2$ TeV in pp collisions [ATLAS](#), [CMS](#)
- There are also constraints from e^+e^- colliders : [BelleII](#), [BESIII](#), [LEP](#)
- The Goal of this work is **extracting new bounds on photon-graviton coupling by recasting the existing ALP constraints**
- Considering two cases for massive gravitons:
 - Without universal coupling: $\text{Br}(G \rightarrow \gamma\gamma) = 1$
 - With universal coupling : $\text{Br}(G \rightarrow \gamma\gamma) < 1$

Processes & Colliders



Methodology

- We generated the production of both ALP and Graviton using [gamma-UPC](#) code, in different processes and considering different colliders systems, for the same coupling factors

$$g_{a\gamma}^{Gen} = g_{G\gamma}^{Gen} = 1 \text{TeV}^{-1}$$

| Process | Colliding system | Energy | Mass Range |
|--|------------------|----------|-------------|
| $\gamma\gamma \rightarrow a, G \rightarrow \gamma\gamma$ | PbPb | 5.02 TeV | 5–100 GeV |
| $\gamma\gamma \rightarrow a, G \rightarrow \gamma\gamma$ | pp | 14 TeV | 0.15–2 TeV |
| $a, G\gamma \rightarrow \gamma\gamma\gamma$ | e^+e^- | 3–11 GeV | 0.16–10 GeV |

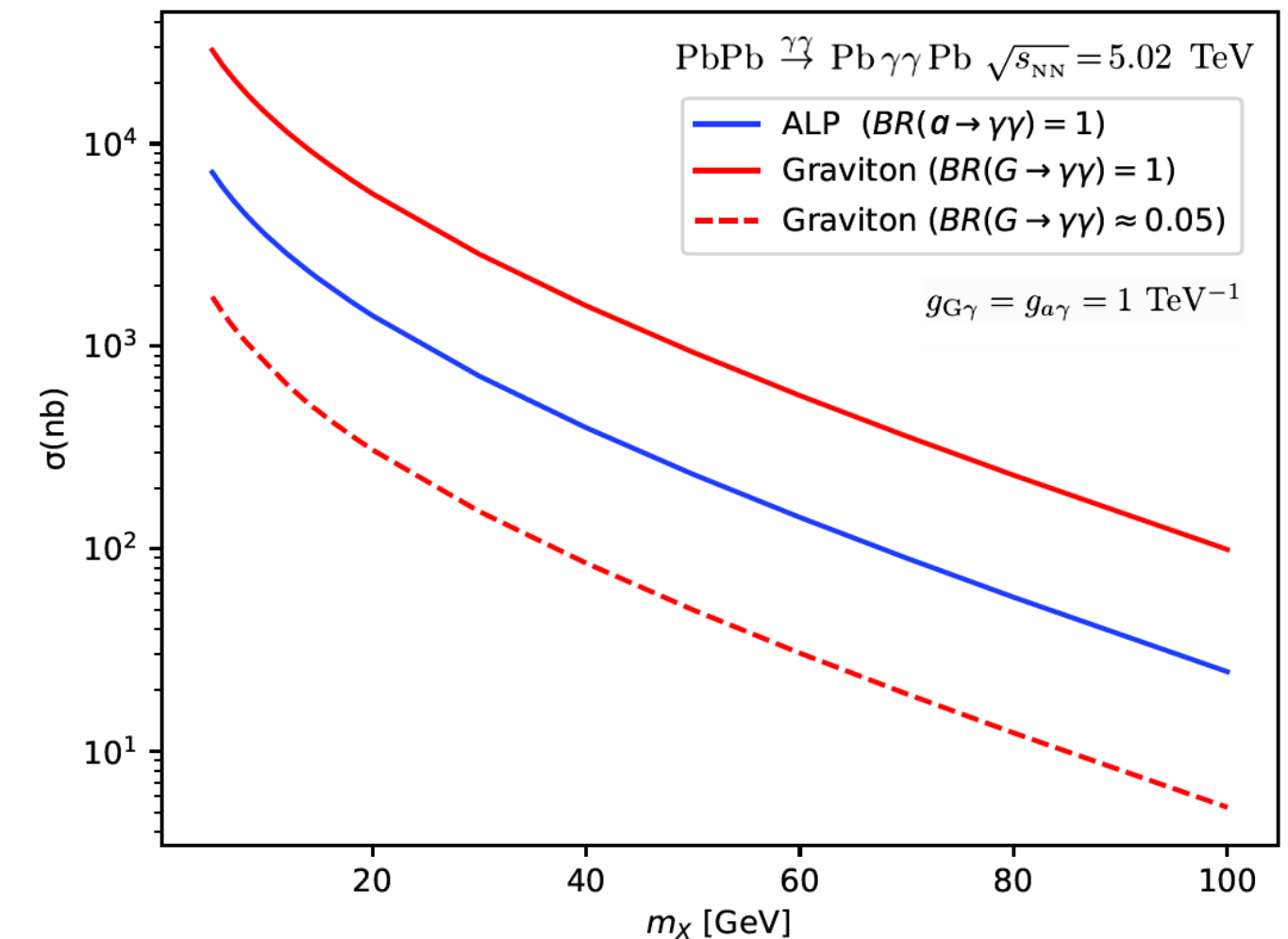
- We computed the total cross section of production in function of $m_{a,G}$

Case 1: $\text{Br}(G \rightarrow \gamma\gamma) = 1$

$$\sigma_G \approx 5\sigma_a$$

Case 2: $\text{Br}(G \rightarrow \gamma\gamma) \approx 0.05$

$$\sigma_G \approx \frac{1}{4}\sigma_a$$



- The factor $\frac{\sigma_a}{\sigma_G}$ will play a role in the extraction of $g_{G\gamma}$

Methodology

- Based on the simulated samples and by applying the following event selection criteria
- We calculated the difference of detector acceptance between ALP and graviton: $\frac{A_G}{A_a}$
- In this case, $\text{Br}(G \rightarrow \gamma\gamma)=1$, the formula (1) is used

$$g_{G\gamma} = g_{a\gamma} \times \sqrt{\frac{\sigma_a}{\sigma_G}} \times \frac{A_G}{A_a} \quad (1)$$

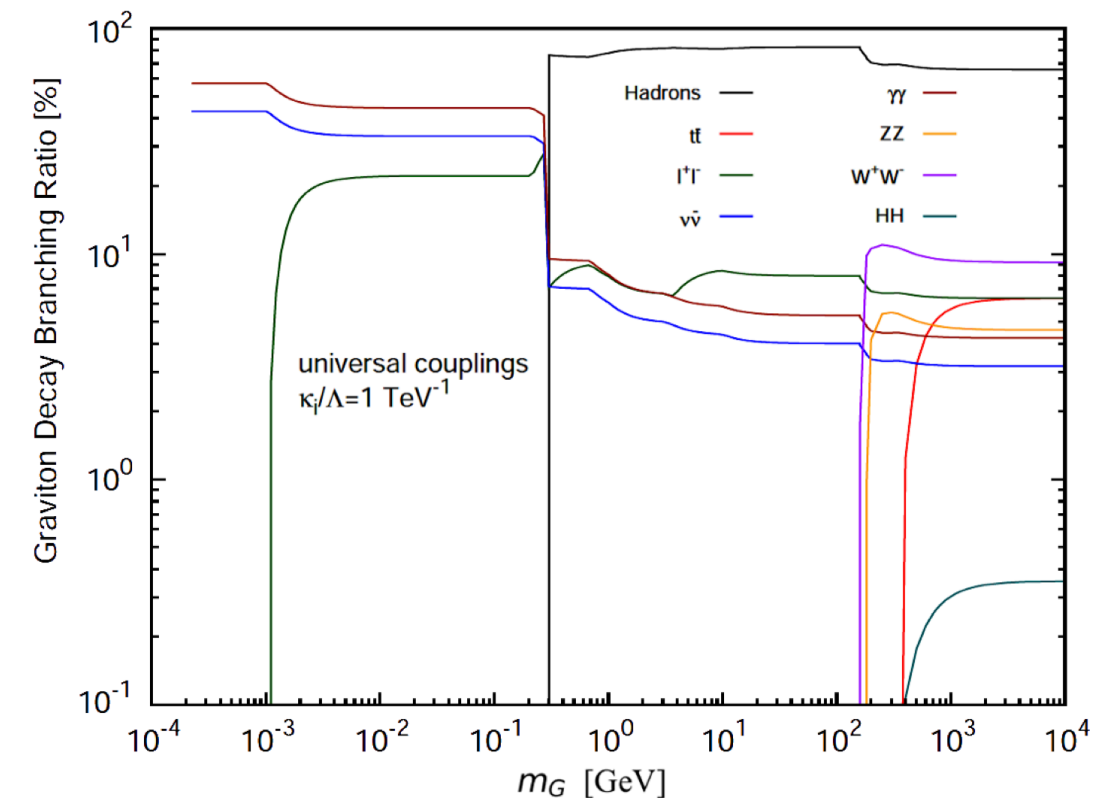
Selection criteria for ATLAS and CMS

| Variable | PbPb $\gamma\gamma \rightarrow \text{Pb}\gamma\gamma\text{Pb}$ | | pp $\gamma\gamma \rightarrow \text{p}\gamma\gamma\text{p}$ | |
|---|--|----------------------|--|----------------------|
| | ATLAS | CMS | ATLAS | CMS |
| $\sqrt{s_{\text{NN}}}$ energy (TeV) | 5.02 | 5.02 | 13.0 | 13.0 |
| Integrated luminosity \mathcal{L} | 2.2 nb ⁻¹ | 0.4 nb ⁻¹ | 14.6 fb ⁻¹ | 9.4 fb ⁻¹ |
| Exclusive number of photons | 2 | 2 | 2 | 2 |
| Single photon γ (GeV) | > 2.5 | > 2 | > 40 | > 100 |
| Single photon $ \eta^\gamma $ | < 2.37 | < 2.4 | < 2.37 | < 2.5 |
| Pair $\gamma\gamma$ (GeV) | < 1 | < 1 | < 1 | < 1 |
| Pair $m_{\gamma\gamma}$ (GeV) | > 5 | > 5 | > 150 | > 200 |
| Pair acoplanarity $A_\phi^{\gamma\gamma}$ | < 0.01 | < 0.01 | < 0.01 | < 0.01 |
| Rapidity gap range $ \eta^{\text{gap}} $ | < 5 | < 5 | – | – |
| Proton tagging | – | – | single | double |
| Proton energy loss ξ | – | – | [0.035–0.08] | [0.02–0.2] |

Methodology

- In this case, $\text{Br}(G \rightarrow \gamma\gamma) < 1$, the formula (2) is used

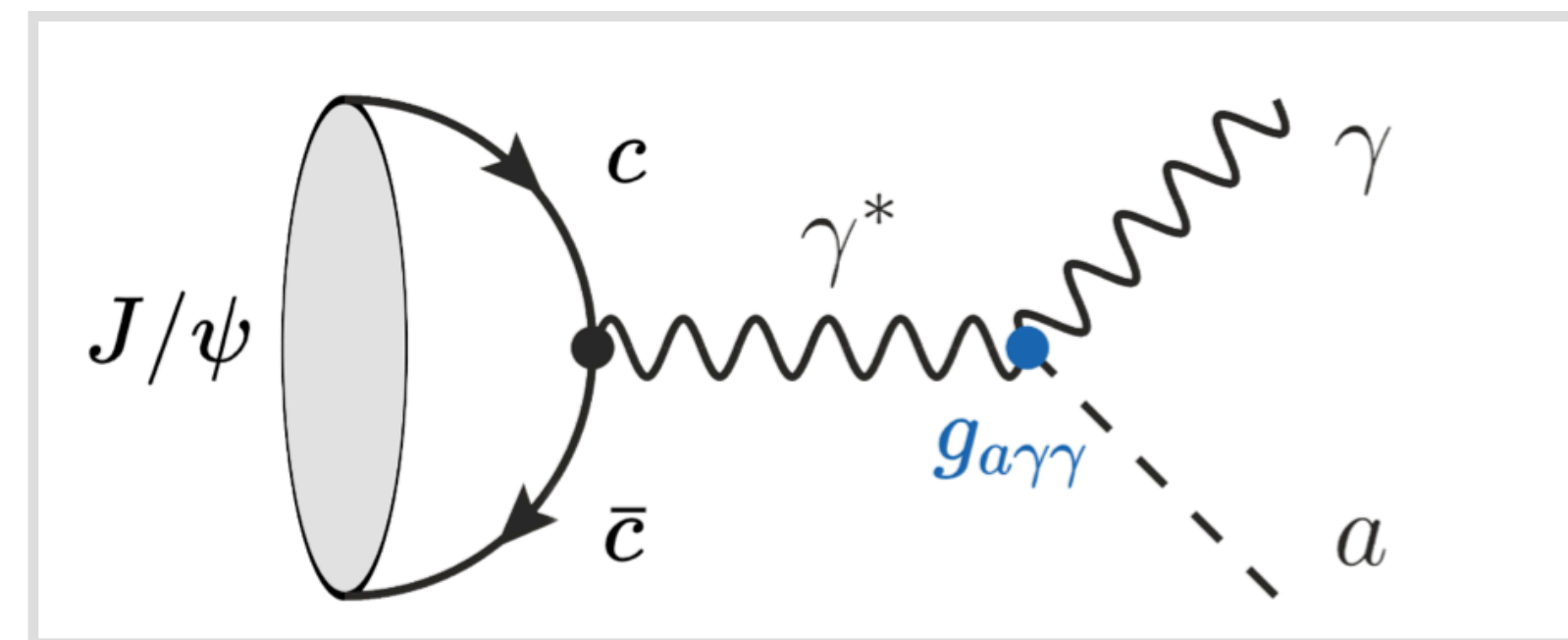
$$g_{G\gamma} = g_{a\gamma} \times \sqrt{\frac{\sigma_a}{\sigma_G}} \times \frac{A_G}{A_a} \times \text{Br}(G \rightarrow \gamma\gamma)$$



- We used this formula for both Pb-Pb, pp (ATLAS, CMS) and e^+e^- (LEP and BELLEII)

- For BES-III experiment, we use the following formula:

$$g_{G\gamma} = g_{a\gamma} \times \frac{m_{J/\Psi}^2 - m_G^2}{\sqrt{(4m_G^4 + 2m_G^2 m_{J/\Psi}^2 + \frac{2}{3}m_{J/\Psi}^4) B_{G \rightarrow \gamma\gamma}}}$$



$m_{J/\Psi}$: The mass of J/Ψ meson

m_G : The mass of the graviton

Results: $\text{Br}(G \rightarrow \gamma\gamma) = 1$

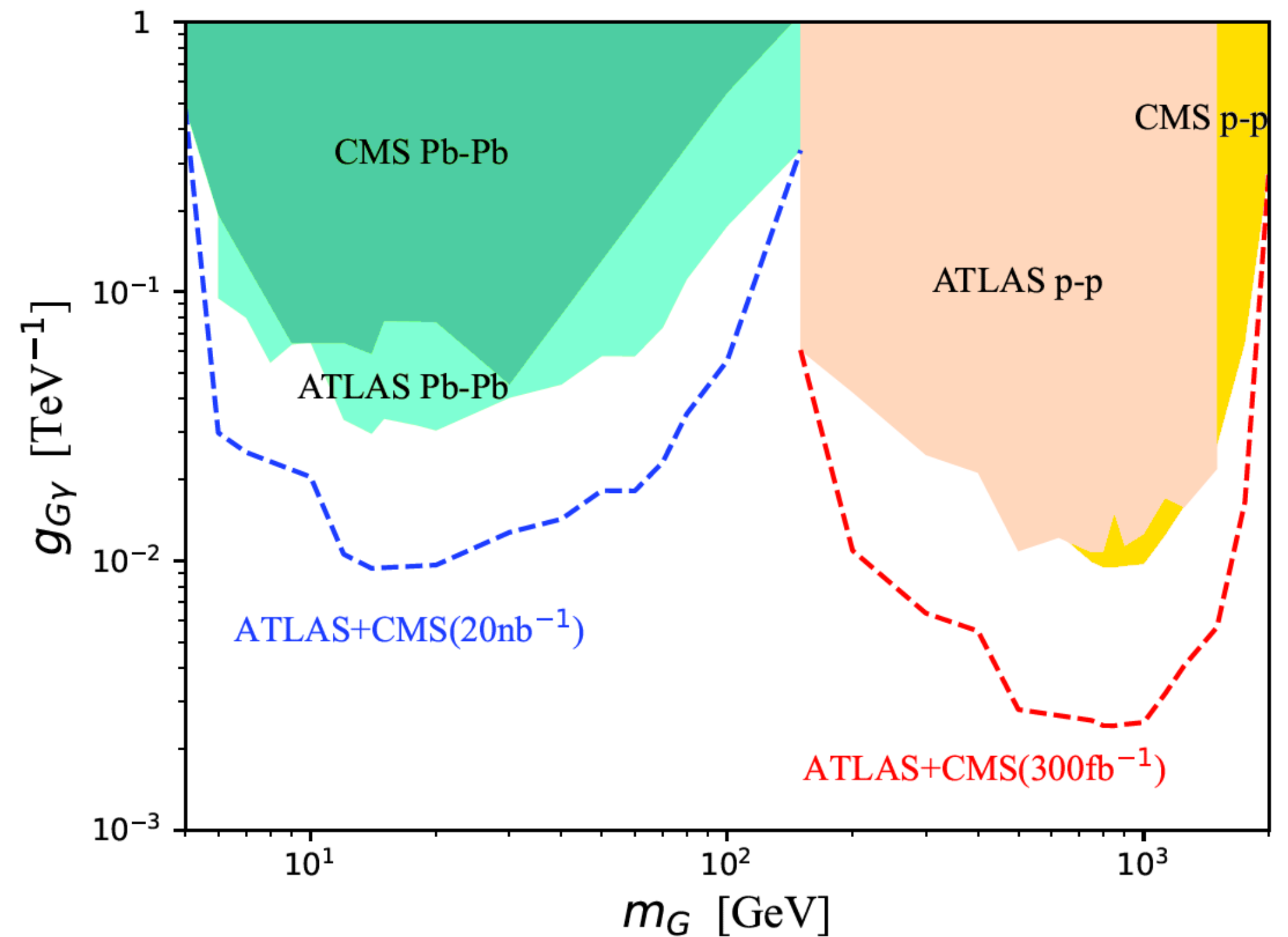
- In Pb-Pb , For $m_G=5$ GeV-100 GeV

$$g_{G\gamma} \approx 1 - 0.01 \text{ TeV}^{-1}$$

- In p-p, For $m_G= 150$ GeV- 2TeV

$$g_{G\gamma} \approx 0.5 - 0.002 \text{ TeV}^{-1}$$

- The dashed curves are obtained by extrapolating the results to the integrated luminosity of HL-LHC
 - The constraints on $g_{G\gamma}$ can be enhanced by **factor 4**



Results: $\text{Br}(G \rightarrow \gamma\gamma) < 1$

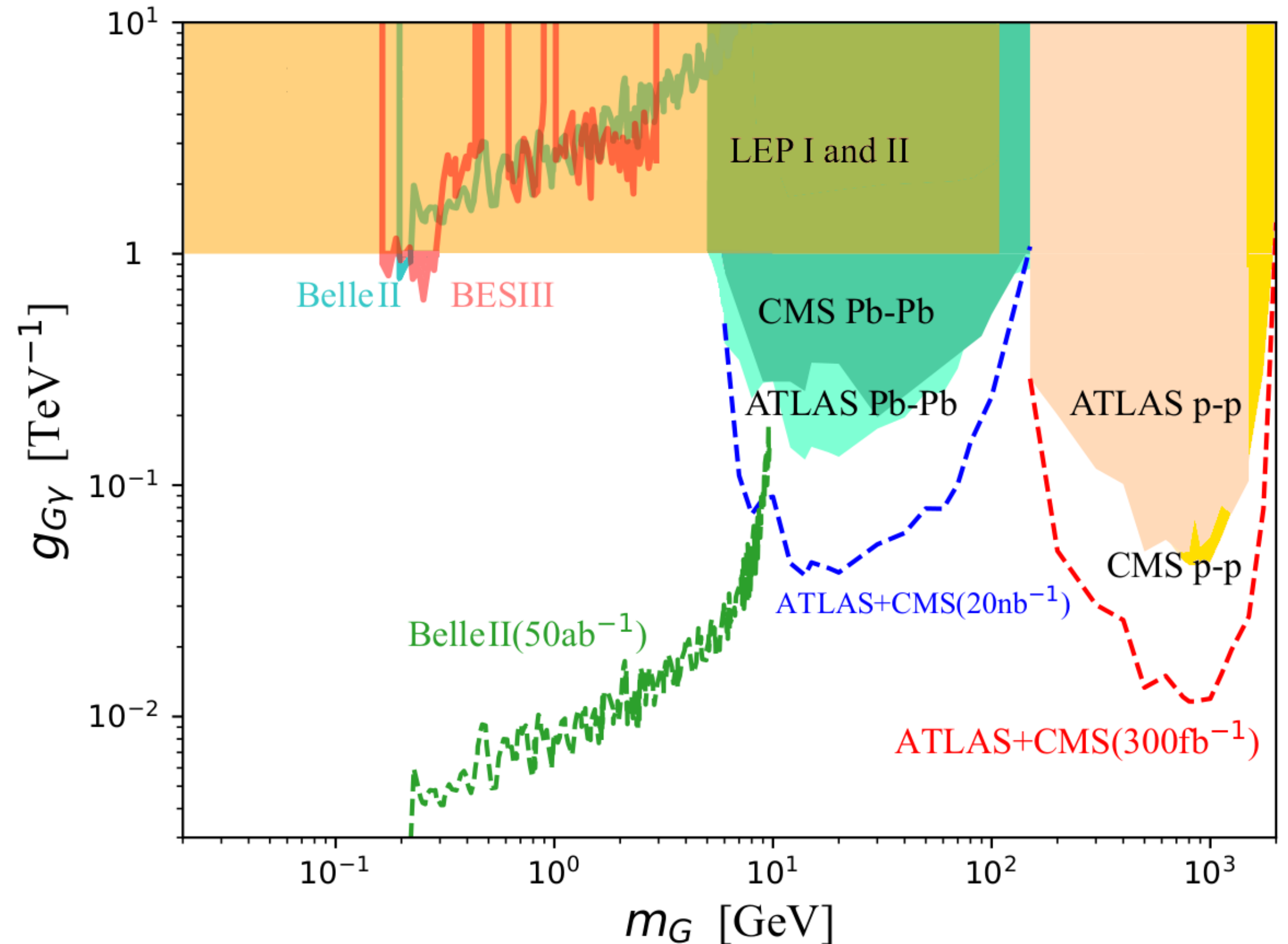
- In LHC, For $m_G = 5\text{GeV}$ to 1TeV

$$g_{G\gamma} \approx 1 - 0.01 \text{ TeV}^{-1}$$

- In e^+e^- colliders, For $m_G = 100\text{MeV} - 10\text{ GeV}$

$$g_{G\gamma} \approx 1 \text{ TeV}^{-1}$$

- For BelleII, the limit can be improved by a **factor 100** at low masses, for future luminosity



Exclusive Vs Inclusive searches

- Comparing the main backgrounds of the two searches:

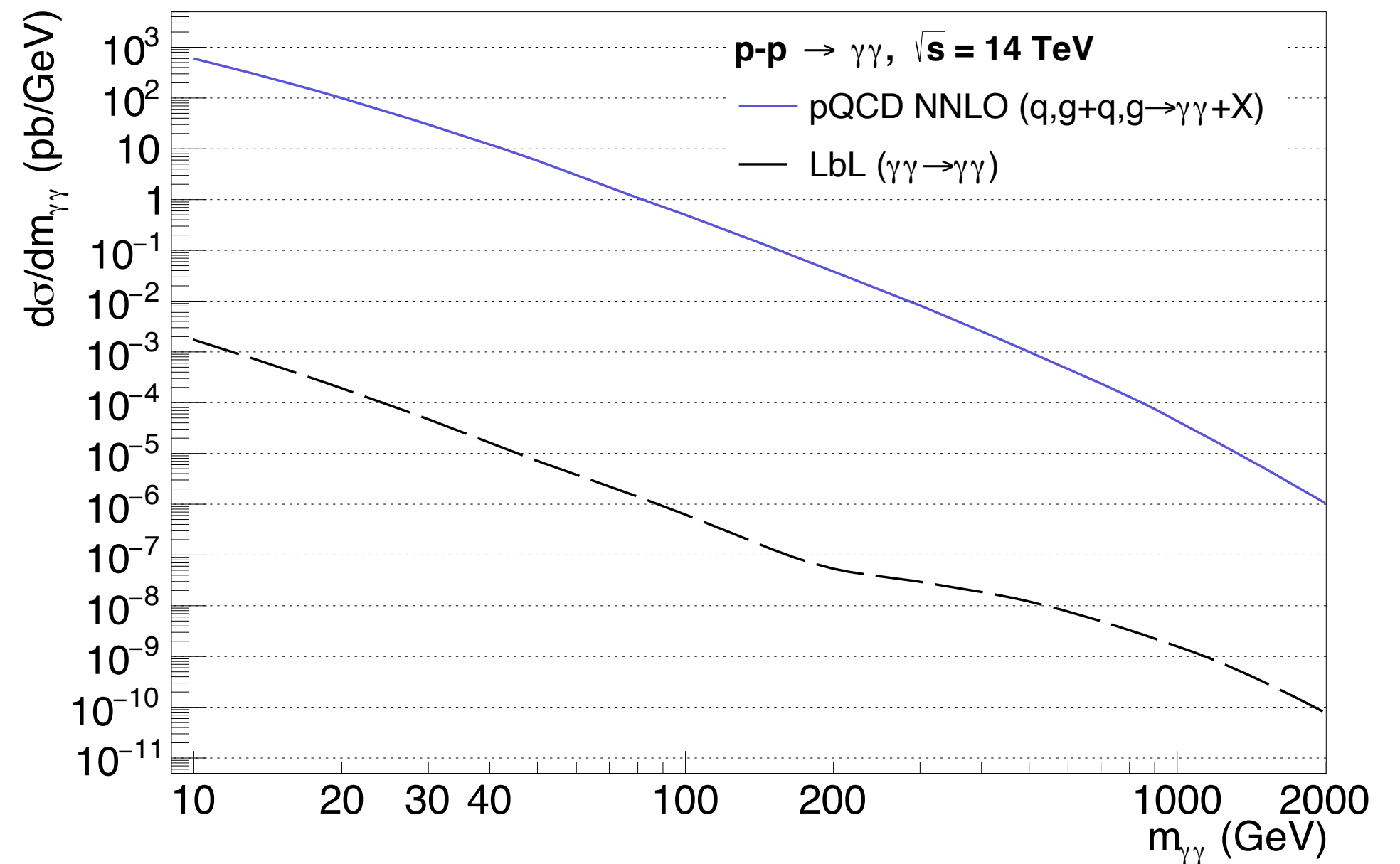
- **The exclusive LbL**

$$pp \xrightarrow{\gamma\gamma} p\gamma\gamma p$$

- **The inclusive pQCD**

$$pp \rightarrow \gamma\gamma + X$$

- The cross sections for inclusive $\gamma\gamma$ are up to 6 orders-of-magnitude larger than the exclusive $\gamma\gamma$ one



Summary

- Exploring the possibility of detecting massive spin-2 (graviton) particles using EFT and via :
 - Two photons processes: $PbPb(pp) \rightarrow Pb(p)G(\gamma\gamma)Pb(p)$
 - Three-photons final states: $e^+e^- \rightarrow G(\gamma\gamma)\gamma$
- The universal-coupling scenario, maintaining consistency with perturbative unitarity principles enabling consideration of a free $G\text{-}\gamma$ coupling in e^+e^- collisions
- The Exclusive studies showed, set $G\text{-}\gamma$ coupling constraints that are more competitive than conventional inclusive LHC searches: UPC final states gain from reduced pileup backgrounds , negligible SM irreducible backgrounds
- The work presented is published in Physics Letters B journal:

Phys.Lett.B 846 (2023) 138237 (<https://arxiv.org/abs/2306.15558>)

THANK YOU FOR YOUR ATTENTION

BACKUP SLIDES

Cross section for photon-photon collisions

- The kinetic term for the graviton field of mass m_G in photon-photon collisions :

$$\mathcal{L}_{\text{FP}} = -\frac{1}{2}(\partial_\rho G_{\mu\nu})^2 + \partial_\mu G_{\nu\rho} \partial^\nu G^{\mu\rho} - \partial_\mu G^{\mu\nu} \partial_\nu G + \frac{1}{2}(\partial_\rho G)^2 - \frac{1}{2}m_G^2 ((G_{\mu\nu})^2 - G^2)$$

- The propagator for the graviton field can be computed by

$$T^{\mu\nu\rho\sigma} = \frac{i}{p^2 - m_G^2 + i\epsilon} \left(\frac{1}{2}(P_{\mu\rho}P_{\nu\sigma} + P_{\mu\sigma}P_{\nu\rho}) - \frac{1}{3}P_{\mu\nu}P_{\rho\sigma} \right)$$

$$P_{\mu\nu} = \eta_{\mu\nu} + p_\mu p_\nu / m_G^2$$

Cross section for e^+e^- collisions

- The inclusive cross section for gravitons in e^+e^- collisions, $\text{Br}(G \rightarrow \gamma\gamma)=1$

$$\sigma(e^+e^- \rightarrow G\gamma \rightarrow \gamma\gamma\gamma) = \frac{\alpha}{36} \left(\frac{k_\gamma}{\Lambda}\right)^2 \frac{(s - m_G^2)^3}{s^3} \frac{s^2 + 3sm_G^2 + 6m_G^4}{m_G^4} \mathcal{B}_{G \rightarrow \gamma\gamma}$$

- This cross section has an asymptotic form:

$$\lim_{s \gg m_G^2} \sigma(e^+e^- \rightarrow G\gamma \rightarrow \gamma\gamma\gamma) = \frac{\alpha}{36} \left(\frac{k_\gamma}{\Lambda}\right)^2 \frac{s^2}{m_G^4} \mathcal{B}_{G \rightarrow \gamma\gamma}$$

- It is divergent in limit : $m_G^2/s \rightarrow 0$

Cross section for e^+e^- collisions

- The inclusive cross section for gravitons with universal coupling in e^+e^- collisions:

$$\sigma(e^+e^- \rightarrow G\gamma \rightarrow \gamma\gamma\gamma) = \frac{\alpha}{24} \left(\frac{k_U}{\Lambda}\right)^2 \frac{(s - m_G^2)^3}{s^3} \mathcal{B}_{G \rightarrow \gamma\gamma}$$

- Considering gravitons coupling only to photons and electrons: $K_U = K_e = K_\gamma$

- The asymptotic cross section for $s \gg m_G^2$: $\sigma \approx \frac{\alpha}{6} \left(\frac{k_U}{\Lambda}\right)^2 \mathcal{B}_{G \rightarrow \gamma\gamma}$

- For $m_G \ll 2m_e$, $Br(G \rightarrow \gamma\gamma) = 1$
- For $m_G \gg 2m_e$, $Br(G \rightarrow \gamma\gamma) = \frac{2}{3}$

The assumption $Br(G \rightarrow \gamma\gamma) = 1$ would be incorrect for e^+e^- colliders

Decay widths

- **Photon-Photon collisions:**

$$\Gamma(G \rightarrow \gamma\gamma) = \left(\frac{k_\gamma}{\Lambda}\right)^2 \frac{m_G^3}{80\pi}$$

- e^+e^- collisions (BelleII , LEP I&II):

$$\Gamma(G \rightarrow e^+e^-) = \left(\frac{k_e}{\Lambda}\right)^2 \frac{m_G^3}{160\pi} \left(1 - \frac{4m_e^2}{m_G^2}\right)^{3/2} \left(1 + \frac{8m_e^2}{3m_G^2}\right)$$

- e^+e^- collisions (BES-III):

$$\Gamma(J/\psi \rightarrow a\gamma \rightarrow \gamma\gamma\gamma) = \frac{\alpha}{81} g_{a\gamma}^2 \left(1 - \frac{m_a^2}{m_{J/\psi}^2}\right)^3 \langle O^{J/\psi} \rangle \mathcal{B}_{a \rightarrow \gamma\gamma}$$

$$\Gamma(J/\psi \rightarrow G\gamma \rightarrow \gamma\gamma\gamma) = \frac{2\alpha}{243} \left(\frac{k_U}{\Lambda}\right)^2 \left(1 - \frac{m_G^2}{m_{J/\psi}^2}\right) \left(1 + 3\frac{m_G^2}{m_{J/\psi}^2} + 6\frac{m_G^4}{m_{J/\psi}^4}\right) \langle O^{J/\psi} \rangle \mathcal{B}_{G \rightarrow \gamma\gamma} (16)$$

Statistical method

- The gravitons, could manifest as **resonances in shape** of the standard invariant mass spectrum of the two outgoing photons in **LbyL**
- An alternative statistical method could be used to extract the graviton-photon coupling :

Analyzing the distributions of the signal and backgrounds by varying m_G , and taking into account the experimental diphoton counts observed in each mass bin

