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# A Blueprint to Understand the MC Top Mass Parameter

This talk reports on new work Oliver Jin,  
Simon Plätzer and Daniel Samitz

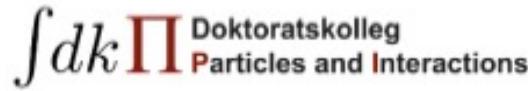
arXiv:1807.06617

arXiv:2404.09856

arXiv:2405.xxxxx

André H. Hoang

University of Vienna

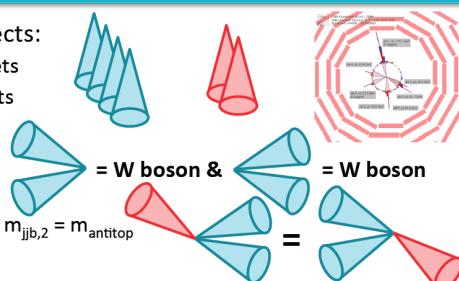


# Most Precise Top Mass Measurements Method

## LHC+Tevatron: Direct top mass measurements

### Kinematic Fit

- Selected objects:
  - 4 untagged jets
  - 2 b-tagged jets

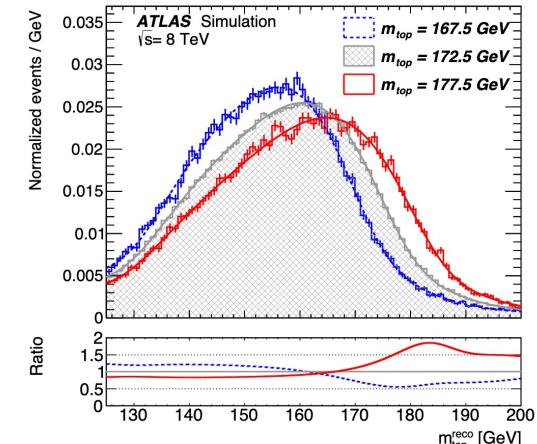
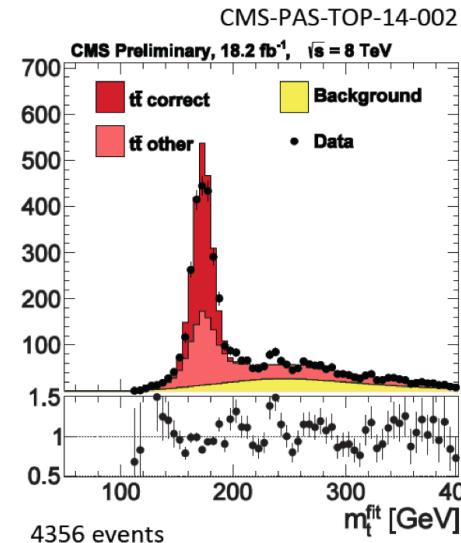


11 Eike Schlieckau - Universität Hamburg September 30th 2014

kinematic mass determination

based on the picture of a top quark particle

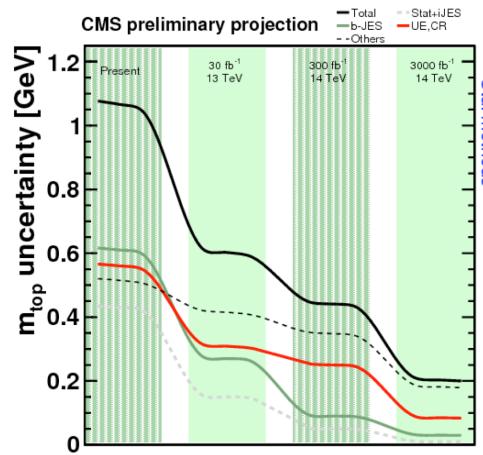
Determination of the best-fit value of the Monte-Carlo top quark mass parameter



$$m_t^{\text{MC}} = 171.77 \pm 0.37 \text{ GeV}$$

CMS collaboration. arXiv: 2302.01967

→ talk by Mark Owen



⊕ High top mass sensitivity

- ⊖ Precision of MC ?
- ⊖ Meaning of  $m_t^{\text{MC}}$  ?

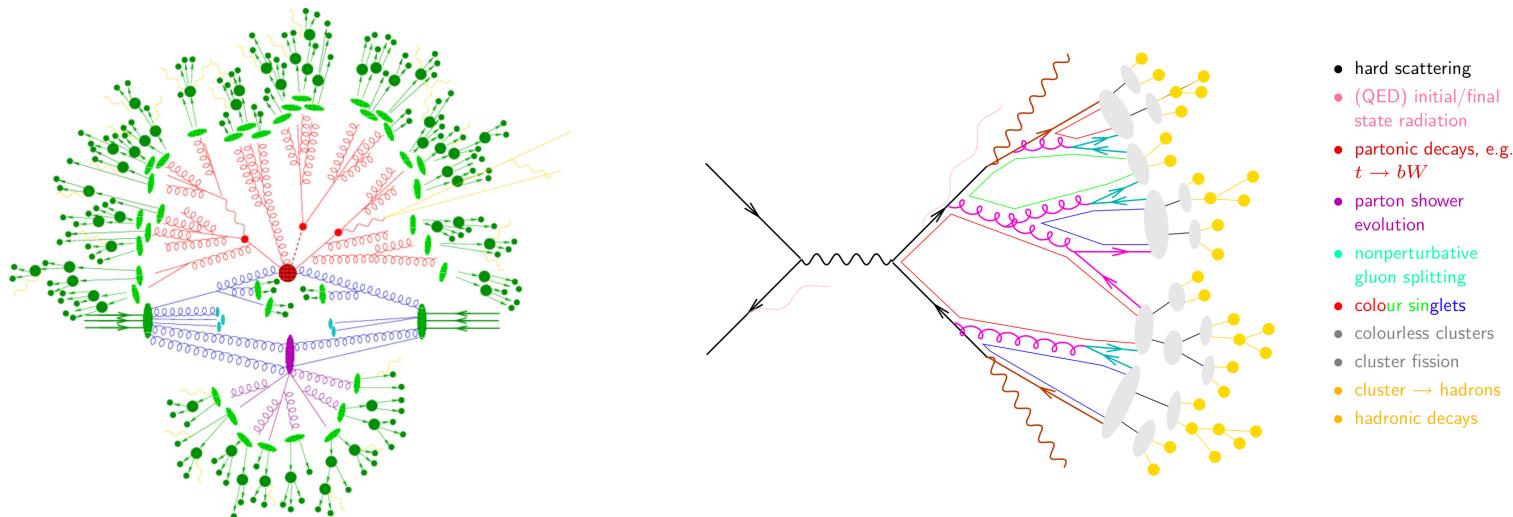
←  $\Delta m_t \sim 200 \text{ MeV}$  (projection)

# What is $m_t^{\text{MC}}$ ?

What does the question mean in the first place?

→ It means that we can provide the relation  $m_t^{\text{MC}} = m_t^{\text{scheme}}(\mu) + \frac{\alpha_s(\mu)}{\pi} \delta m^{\text{scheme}} + \dots$   
where  $\delta m^{\text{scheme}}$  can be computed in pQCD

The issue is complicated as we must understand and control the interplay of the different components of MC event generators.



→ Aim: Define and quantify a “MC top mass scheme”

- Defined in pQCD ( $\rightarrow$  parton shower)
- Controlled at the observable hadron level. ( $\rightarrow$  hadron level)

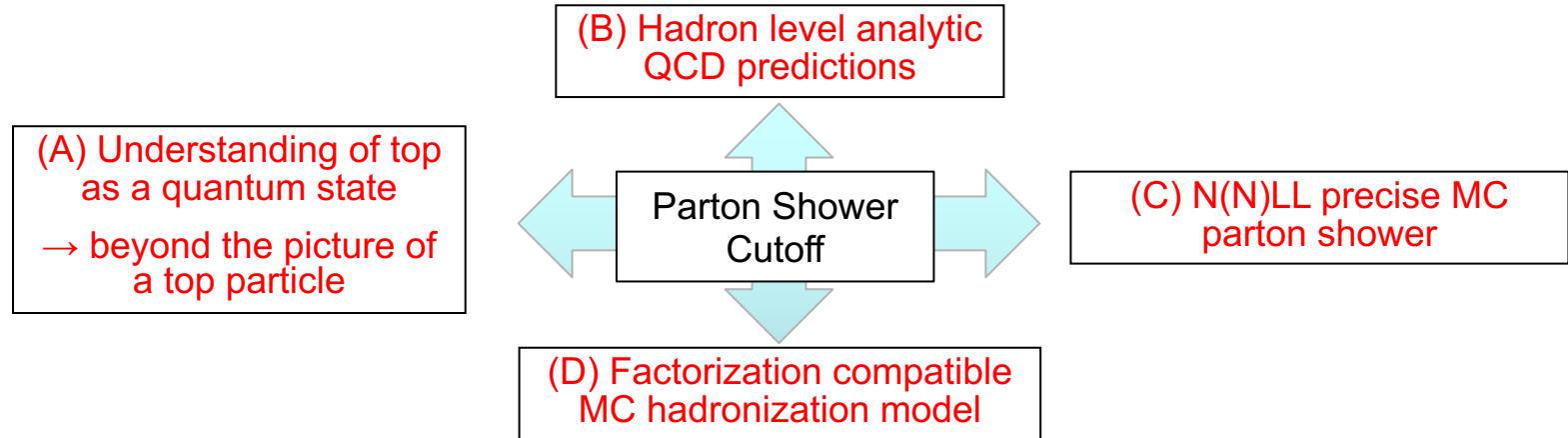
# Approaches to remedy the $m_t^{\text{MC}}$ problem

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- Indirect top quark mass measurements → ATLAS/CMS e.g. arXiv:2403.01313
  - Unfold data to parton level top-anti top on-shell particle distributions (e.g.  $m_{tt}$ ) to be compared to N(N)LO fixed order calculations for on-shell top quarks
  - MC modelling aspects now contained in the hadron-to-parton unfolding carried out with the MC generator (no “theory of unfolding”, but different systematics)
  - Uncertainties not yet as small as for direct determinations as observables are of more inclusive character
- ‘Hadron’ level analytic QCD predictions for top mass determinations (ongoing work)
  - Fat top jets with soft drop grooming  
→ MPI currently provides a practical limitation for LHC Mantry, Pathak, Stewart (2017)  
Mantry, Pathak, Stewart (2019)
  - Energy correlators  
→ new type of top mass sensitivity related to decay opening angle Holguin, Moult, Pathak, Procura (2022)  
Holguin, Moult, Pathak, Procura, Schöfbeck (2023)
- This talk is about work to truly understand and control the MC top quark mass parameter  $m_t^{\text{MC}}$  → Improve MCs so that direct measurements can (eventually) be interpreted reliably.

# What is $m_t^{\text{MC}}$ ?

There are 4 essential ingredients to resolve the problem from first principles:



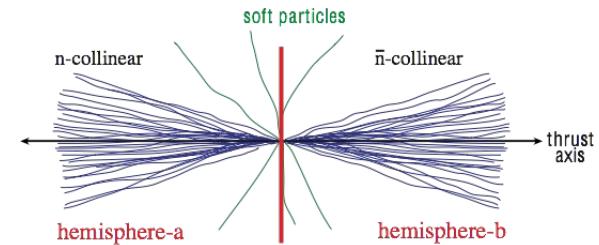
Currently there is only 1 observable class where all 4 ingredients are available and controlled.

## Event-shape observables in $e^+e^-$ collisions

for boosted top pair production:

2-jettiness, thrust, ... (decay insensitive)

(builds on sequence of work since 2007)



## Aim of this talk:

- Discuss interplay of (A) – (D) provide conceptual and practical basis to determine and control  $m_t^{\text{MC}}$  for MC event generators
- Review (A) – (C) from previous work. New development for (D)
- Explicit realization for  $e^+e^-$  event-shape top resonance distribution (e.g. 2-jettiness) for Herwig 7.2

# (A) Beyond the picture of a top particle

The top quark does not hadronize due to its large width  $\Gamma_t \gg \Lambda_{\text{QCD}}$ . It therefore has some characteristics of a physical particle (hadron).

BUT: If we stick to the picture of a physical top particle the only mass that is ever relevant is the pole mass = pole of the top propagator.

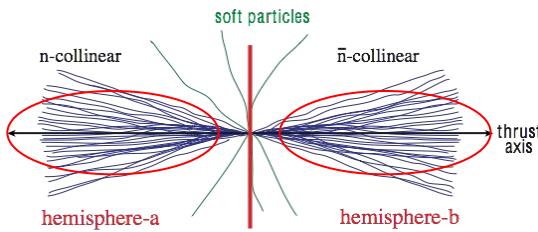
Due to the top quarks color charge, however, this picture is too restricted when we want to understand the MC top quark mass.

What we mean by a top quark is however related to

well known aspect

- a particular experimental measurement prescription (of a color singlet state)
  - calculations/simulations must properly account color neutralization effects
  - implies that we need accurate hadron level QCD predictions/simulations
- the way how we treat soft gluons in the top rest frame
  - MC simulations impose an IR cut  $Q_0$  of the parton shower gluon radiation
  - the shower cutoff  $Q_0$  act as a resolution scale
  - changes the physical meaning of the top quark (and its mass) in the simulation
  - impact of the shower cutoff needs to be quantified and controlled accurately

# (B) Boosted top eventshapes



$$\tau = 1 - \max_{\vec{n}} \frac{\sum_i |\vec{n} \cdot \vec{p}_i|}{Q} \underset{\tau \rightarrow 0}{\approx} \frac{M_1^2 + M_2^2}{Q^2}$$

$Q = E_{\text{c.m.}}$

In insensitive to details of top decay

Hadron level:

$$\frac{d\sigma}{d\tau}(\tau, Q, m, \delta m) = \int_0^{Q\tau} d\ell \frac{d\hat{\sigma}_s}{d\tau}\left(\tau - \frac{\ell}{Q}, Q, m, \delta m\right) S_{\text{mod}}(\ell)$$

Parton cross section

Shape function

First principles prediction of QCD and NOT A MODEL !!

Partonic cross section (uses effective theories SCET, bHQET):

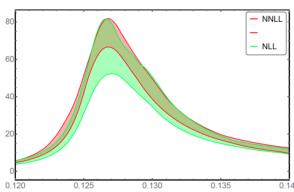
nonpert. large angle soft

$$\left( \frac{d^2\sigma}{dM_t^2 d\bar{M}_t^2} \right)_{\text{hemi}} = \sigma_0 H_Q(Q, \mu_m) H_m\left(m, \frac{Q}{m}, \mu_m, \mu\right) \times \int_{-\infty}^{\infty} d\ell^+ d\ell^- B_+\left(\hat{s}_t - \frac{Q\ell^+}{m}, \Gamma, \mu\right) B_-\left(\hat{s}_{\bar{t}} - \frac{Q\ell^-}{m}, \Gamma, \mu\right) S_{\text{hemi}}(\ell^+, \ell^-, \mu)$$

pert. ultra-collinear soft

(hard-collinear for massless quarks)

pert. large-angle soft

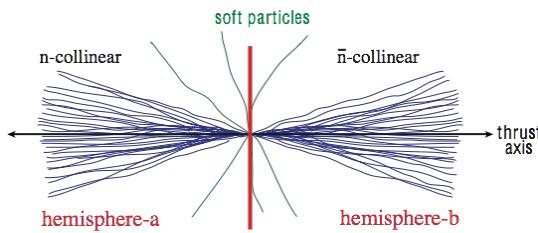


Known at NNNLL order

Fleming, Mantry, Stewart, AHH (2007)

Bachu, Mateu, Pathak, Stewart, AHH (2022)

## (B) Boosted top eventshapes



$$\tau = 1 - \max_{\vec{n}} \frac{\sum_i |\vec{n} \cdot \vec{p}_i|}{Q} \underset{\tau \rightarrow 0}{\approx} \frac{M_1^2 + M_2^2}{Q^2}$$

$Q = E_{\text{c.m.}}$

Insensitive to details of top decay

Hadron level:

$$\frac{d\sigma}{d\tau}(\tau, Q, m, \delta m) = \int_0^{Q\tau} d\ell \frac{d\hat{\sigma}_s}{d\tau}\left(\tau - \frac{\ell}{Q}, Q, m, \delta m\right) S_{\text{mod}}(\ell)$$

- $S_{\text{mod}}$  leading nonperturbative corrections only from large-angle soft radiation: linear sensitive to  $\Lambda_{\text{QCD}}$
- Any top mass renormalization scheme can be implemented  $m_t^{\text{pole}} = m + \delta m$
- Can be calculated with a finite IR cutoff  $Q_0$  for the parton cross section
- **IR cutoff  $Q_0$  = factorization scale** for parton-level vs. hadronization corrections
  - ▶ Defines scheme for  $S_{\text{mod}}$  (large-angle soft radiation):  $S_{\text{mod}}(I) \rightarrow S_{\text{mod}}(I, Q_0)$
  - ▶ Defines scheme for parton distribution:  $\frac{d\hat{\sigma}}{d\tau}(\tau, Q, m) \rightarrow \frac{d\hat{\sigma}}{d\tau}(\tau, Q, m, Q_0)$

# (C) Angular ordered parton shower (Herwig)

→ Coherent Branching algorithm (default Herwig shower):

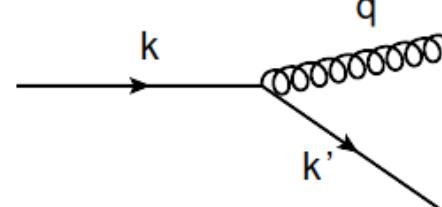
$$k'^\mu = zk^- \frac{n^\mu}{2} + \frac{k'^2 - q_\perp^2}{zk^-} \frac{\bar{n}^\mu}{2} - q_\perp^\mu$$

$$q^\mu = (1-z)k^- \frac{n^\mu}{2} + \frac{q^2 - q_\perp^2}{(1-z)k^-} \frac{\bar{n}^\mu}{2} + q_\perp^\mu$$

momentum conservation:

$$k^2 = \frac{k'^2}{z} + \frac{q^2}{1-z} + \frac{q_\perp^2}{z(1-z)}$$

Dokshitzer, Fadin, Khoze (1982)  
 Bassetto, Ciafaloni, Marchesini (1983)  
 Catani, Marchesini, Webber (1991)  
 Gieseke, Stephens, Webber (2003)



evolution variables:  $z$ ,  $\tilde{q} = \frac{q_\perp^2}{z^2(1-z)^2}$

color coherence of soft gluon emissions → angular ordering:  $z_i^2 \tilde{q}_i^2 > \tilde{q}_{i+1}^2$

probabilities from  
splitting functions and  
Sudakov form factors

→ analytic jet mass distribution (inv. mass generated from CB from one boosted quark)

$k^2 \approx$  hemisphere mass (does not account for out of cone radiation)

$$J(Q^2, k^2 - m^2, m^2) = \delta(k^2 - m^2)$$

→

$$+ \int_0^{Q^2} \frac{d\tilde{q}^2}{\tilde{q}^2} \int_0^1 dz P_{QQ} [\alpha_s(z(1-z)\tilde{q}), z, m] \theta\left(\tilde{q}^2 - \frac{Q_0^2 + m^2(1-z)^2}{z^2(1-z)^2}\right)$$

$$\times \left[ z J(z^2 \tilde{q}^2, z(k^2 - m^2) - z^2(1-z)\tilde{q}^2) - J(\tilde{q}^2, k^2 - m^2) \right]$$

# (C) Angular ordered parton shower (Herwig)

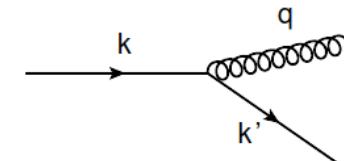
Partonic level cross section

Catani, Trentadue, Turnock Webber (1993)

$$\frac{d\hat{\sigma}}{d\tau} = \int dk^2 dk'^2 \delta\left(\tau - \frac{k^2 + k'^2}{Q^2}\right) J(Q^2, k^2) J(Q^2, k'^2)$$

AHH, Plätzer, Samitz (2018)

- Agrees exactly with partonic cross section obtained from analytic factorized calculations at NLL!
- CB is NLL precise for inclusive event shapes.
- For massless quarks and massive quarks
- Analytic calculation: for vanishing shower cutoff  $Q_0=0$ :  $m_t^{\text{MC}} = m_t^{\text{pole}}$   
(one-shell self energy contribution does not arise in CB!)



BUT: Parton showers in MC generators have an finite shower cutoff  $Q_0$  to prevent infinite multiplicities → acts as finite resolution scale that is physical for the MC

- We have to track (at least) the dominant linear dependence on  $Q_0$  from large-angle soft and ultra-collinear radiation
- Matches analogous calculations for analytic calculations
- Realized accurately by Herwig's shower

$$q_\perp > Q_0$$

# Linear Shower Cutoff Dependence

Massless quarks:

AHH, Jin, Plätzer, Samitz (2024)

$$\begin{aligned}\frac{d\hat{\sigma}}{d\hat{\tau}}(\hat{\tau}, Q, Q_0) &= \frac{d\hat{\sigma}}{d\hat{\tau}}(\hat{\tau}, Q) + \frac{1}{Q} \Delta_{\text{soft}}(Q_0) \frac{d^2\hat{\sigma}}{d\hat{\tau}^2}(\hat{\tau}, Q) \\ &= \frac{d\hat{\sigma}}{d\hat{\tau}}\left(\hat{\tau} + \frac{1}{Q} \Delta_{\text{soft}}(Q_0), Q\right)\end{aligned}$$

$$\Delta_{\text{soft}}(Q_0) = 16 Q_0 \frac{\alpha_s(Q_0) C_F}{4\pi} + \mathcal{O}(\alpha_s^2(Q_0))$$

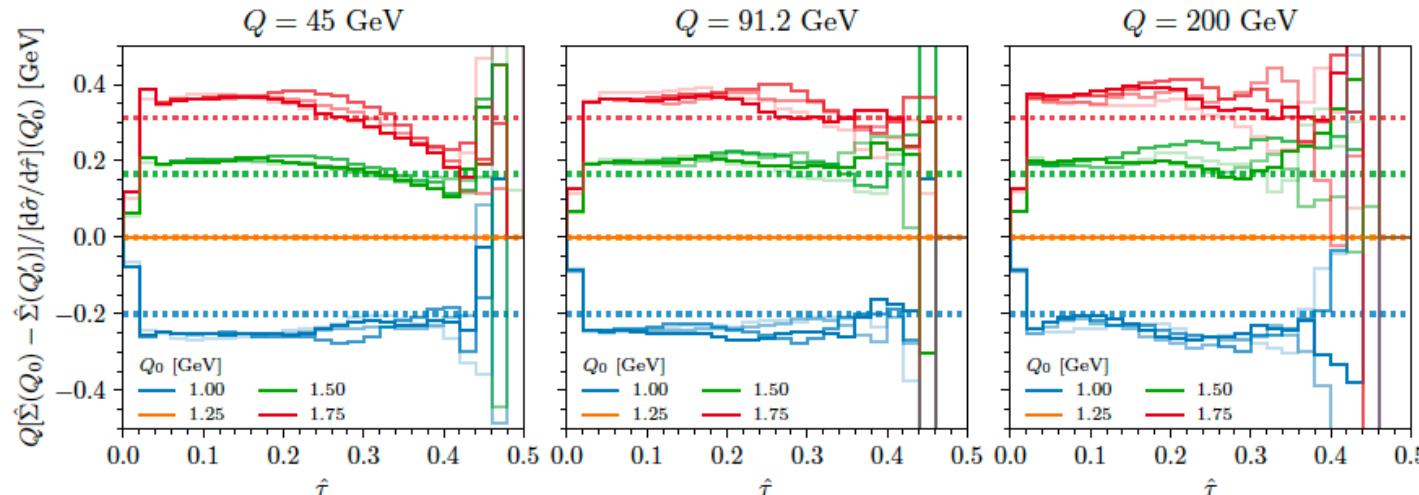
$$Q \frac{\hat{\Sigma}(\hat{\tau}, Q, Q_0) - \hat{\Sigma}(\hat{\tau}, Q, Q'_0)}{\frac{d\hat{\sigma}}{d\hat{\tau}}(\hat{\tau}, Q, Q'_0)} = \Delta_{\text{soft}}(Q_0, Q'_0)$$

→ 2-jettiness cumulant distribution:

Herwig CB shower versus pQCD:

→ Herwig 'true' parton level had to be added.

$$\Delta_{\text{soft}}(Q_0, Q'_0) = 16 \int_{Q'_0}^{Q_0} dR \left[ \frac{\alpha_s(R) C_F}{4\pi} \right]$$



Different lines: different matrix element and matching schemes

# Linear Shower Cutoff Dependence

Massive quarks:

→ 2-jettiness resonance position:

AHH, Plätzer, Samitz (2018)

$Q_0$ -dependent self-energy absorbed in mass:

Modifies pole of top propagator away from  $m_t^{\text{pole}}$ :

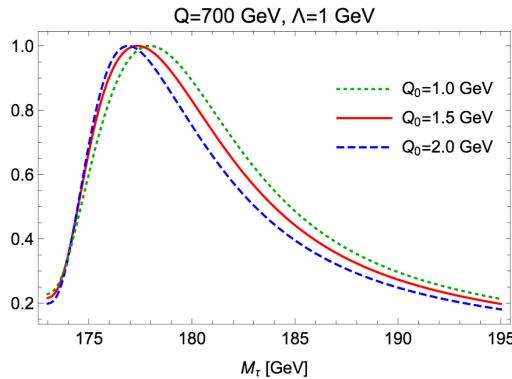
$$m_t^{\text{pole}} \rightarrow m_t(Q_0) = m_t^{\text{pole}} - \delta m(Q_0), \quad \delta m(Q_0) = 2/3 \alpha_s(Q_0) Q_0 + \dots$$

$$\frac{d}{d \ln Q_0} \tau_{\text{peak}}^{\text{parton}}(Q_0) = \frac{C_F \alpha_s(Q_0)}{4\pi} \frac{Q_0}{Q} \left[ 16 - 8\pi \frac{m_t}{Q} \right]$$

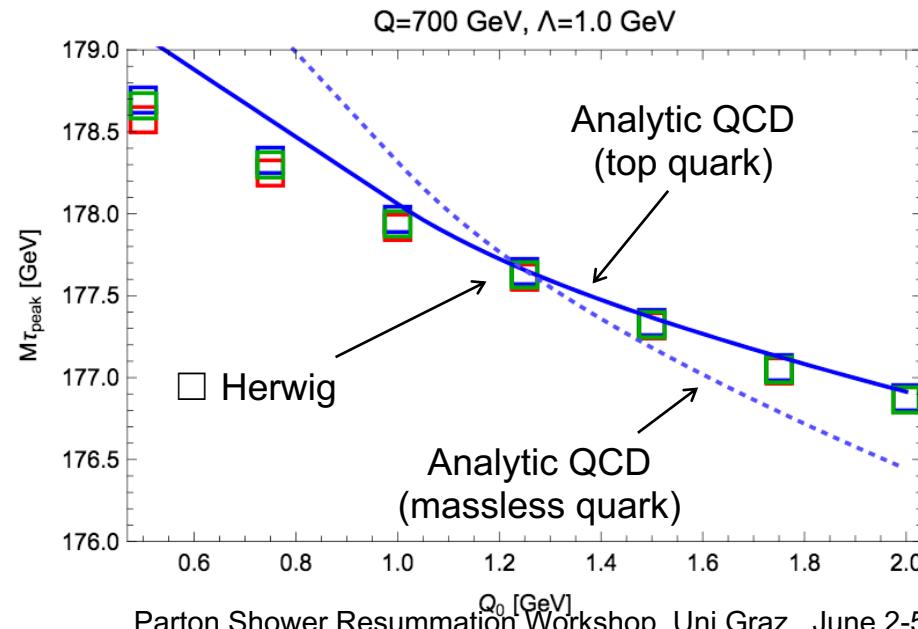
both linear  $Q_0$ -contributions cancel

large-angle soft

Must be compensated  
by hadronization  
corrections in  $S_{\text{mod}}$



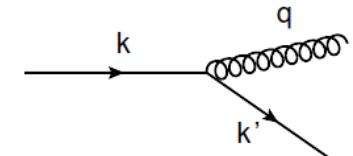
ultra-collinear (from all radiation except self-energy)



# (C) Angular ordered parton shower (Herwig)

For inclusive jet-mass-related event shapes the Herwig top mass parameter represents a  $Q_0$ -dependent mass scheme that can be related to other mass schemes at NLO:

AHH, Plätzer, Samitz (2018)



$$m_t^{\text{CB}}(Q_0) = m_t^{\text{pole}} - \frac{2}{3} Q_0 \alpha_s(Q_0) + \mathcal{O}(\alpha_s(Q_0)^2)$$

$$m_t^{\text{CB}}(Q_0) = m_t^{\text{MSR}}(Q_0) - \frac{2}{3} \left(1 - \frac{2}{\pi}\right) Q_0 \alpha_s(Q_0) + \mathcal{O}(\alpha_s^2(Q_0))$$

$$q_\perp > Q_0$$

(1) Does this survive the hadronization model?

- Hadron level simulations should be  $Q_0$ -independent → Simon's talk yesterday
- Shower cut has to be considered as a factorization scale and its proper control in QCD is essential to control parton level and hadronization separately.

(2) How universal is the result? → Needs careful additional work

# (D) Factorization compatible hadronization model

AHH, Jin, Plätzer, Samitz arXiv:2404.09856

Standard shower cut treatment for all MC generators:

- Shower-cutoff scale  $Q_0$  = one of many hadronization model parameters

BUT: To gain control over the shower's top mass parameter:

Plätzer arXiv:2204.06956

- The shower-cutoff scale  $Q_0$  must be promoted to a factorization scale, such that hadron level descriptions are shower-cut independent.
- The parton-level to hadron-level migration matrix must behave like a shape function!

$$\frac{d\sigma}{d\tau}(\tau, Q) = \int d\hat{\tau} \frac{d\hat{\sigma}}{d\hat{\tau}}(\hat{\tau}, Q) \underbrace{T(\tau, \hat{\tau}, \{Q, Q_0\})}_{}$$

Migration matrix should have the property

$$T(\tau, \hat{\tau}, Q, Q_0) = T(\tau - \hat{\tau}, Q_0) = Q S_{\text{mod}}\left(\frac{\tau - \hat{\tau}}{Q}\right)$$

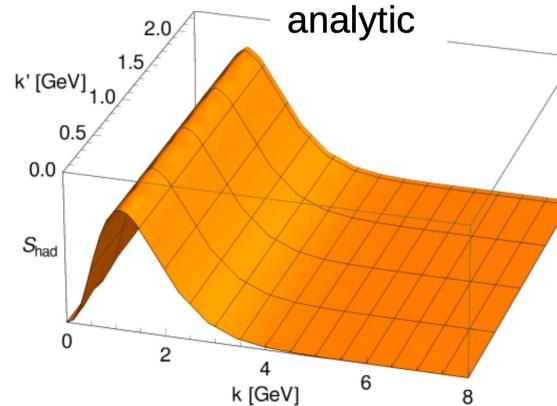
# (D) Factorization compatible hadronization model

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This implies non-trivial QCD constraints on the properties of the migration matrix:

$$T\left(\frac{k}{Q} = \tau - \hat{\tau}, \frac{k'}{Q} = \hat{\tau}, \{Q, Q_0\}\right)$$

(1) Transfer matrix should have this form:



$$T(\tau, \hat{\tau}, Q, Q_0) = T(\tau - \hat{\tau}, Q_0) = Q S_{\text{mod}}\left(\frac{\tau - \hat{\tau}}{Q}\right)$$

(2)  $Q_0$ -dependence of the first moment constrained at NLO QCD:

$$\Omega_1(Q_0) \equiv \frac{1}{2} \int d\ell \ell S_{\text{had}}(\ell, Q_0)$$

$$\Omega_1(Q_0') = \frac{1}{2} \Delta_{\text{soft}}(Q_0', Q_0) + \Omega_1(Q_0)$$

# **$Q_0$ -dependent tuning analyses**

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Tuning software: APPRENTICE

AHH, Jin, Plätzer, Samitz  
arXiv:2404.09856

Reference tune = standard  $e^+e^-$  tune (Z-pole LEP data [3180 observable bins])

Reference data = simulated data for  $Q_0 = 1.25$  GeV for

- Z-pole LEP data [3180]
- Z-pole 2-jettiness [peak region]
- ttbar 2-jettiness at  $E_{cm} = 700$  and 1000 GeV [peak region]

$Q_0$ -dependent tunes: tunes to reference data for different shower cut  $Q_0$  values

Tuned parameters: 6 tuning parameters +  $m_t^{MC}$

Default model

- $m_g$  (force gluon splitting)
- PSplit (cluster fission, mass distr.)
- $Cl_{max}$  (cluster fission, condition)
- $Cl_{pow}$  (cluster fission, condition)
- PwtSquark (cluster hadronization)
- PwtDIquark (cluster hadronization)

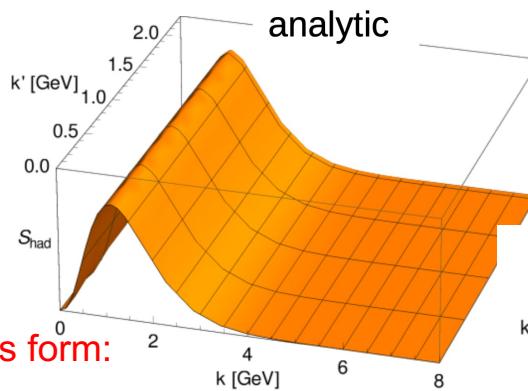
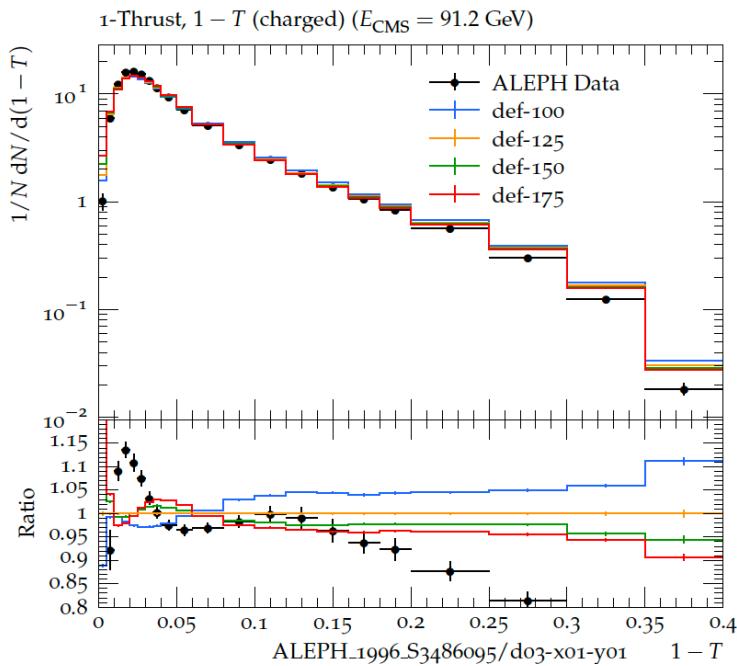
Interpolation grids: cubic and quartic polynomials

# (D) Factorization compatible hadronization model

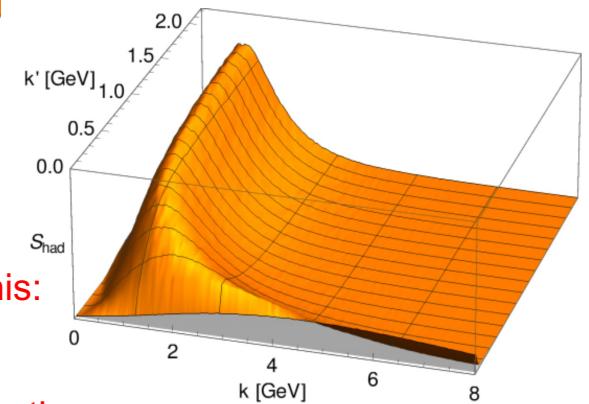
Results from  $Q_0$ -tuned MC simulations: Default model

$$T \left( \frac{k}{Q} = \tau - \hat{\tau}, \frac{k'}{Q} = \hat{\tau}, \{Q, Q_0\} \right)$$

migration matrix should have this form:



AHH, Jin, Plätzer, Samitz  
arXiv:2404.09856



But it actually looks like this:

Peak region hadronization  
inconsistent with QCD  
factorization!

Description of observables at hadron level not  
quite shower-cutoff independent (Thrust at  $Q=M_z$ )

$$Q_0 = (1.00, 1.25, 1.50, 1.75) \text{ GeV}$$

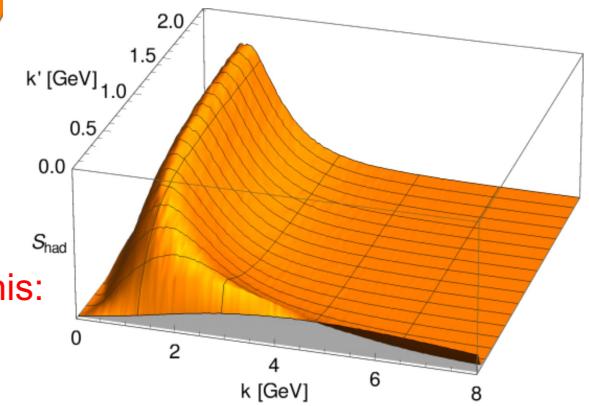
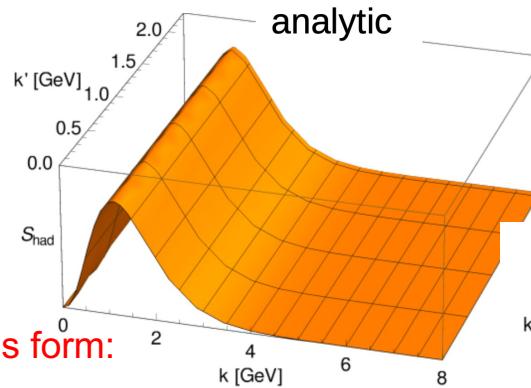
(Reference data for tune: Simulation for  $Q_0=1.25$  GeV)

# (D) Factorization compatible hadronization model

Results from  $Q_0$ -tuned MC simulations: Default model

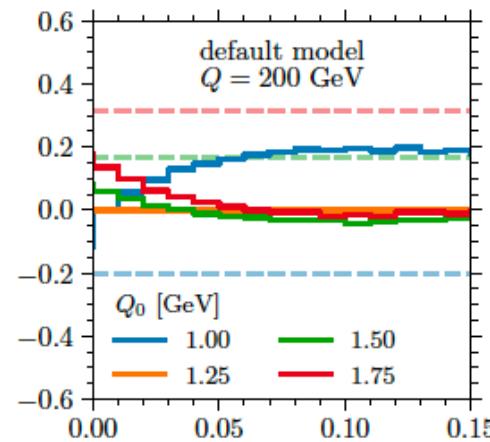
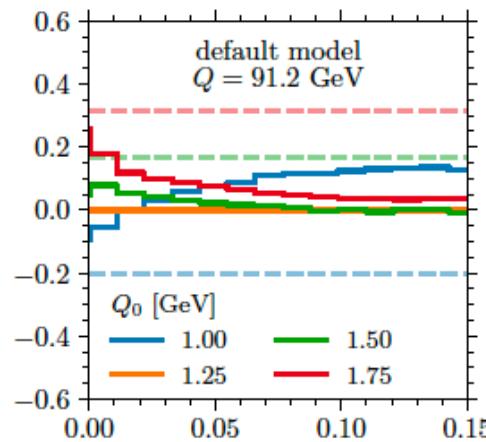
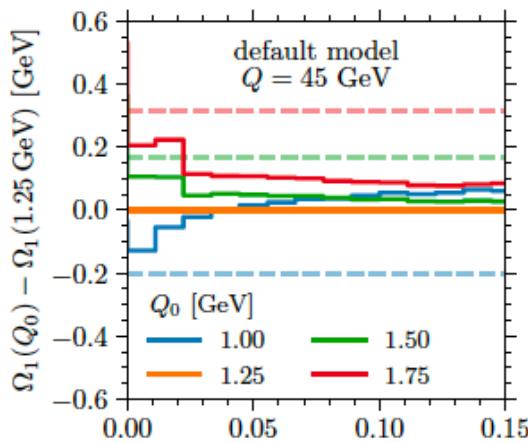
$$T \left( \frac{k}{Q} = \tau - \hat{\tau}, \frac{k'}{Q} = \hat{\tau}, \{Q, Q_0\} \right)$$

migration matrix should have this form:



But it actually looks like this:

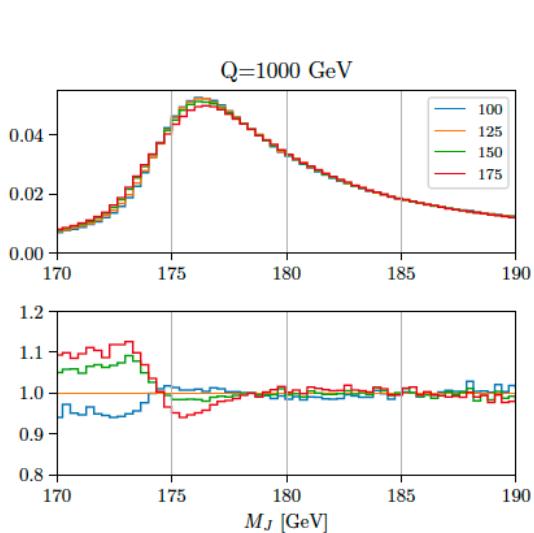
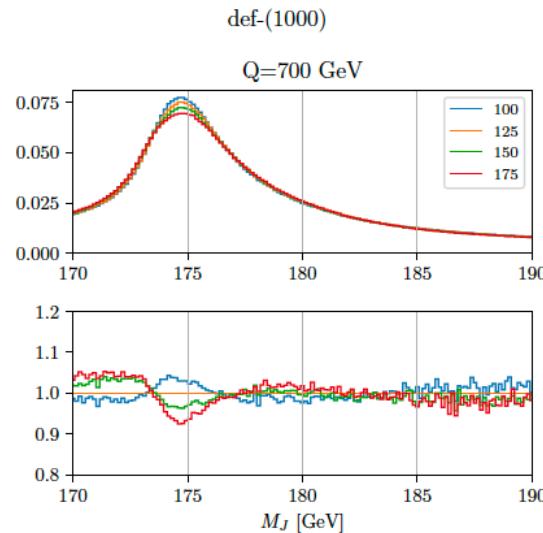
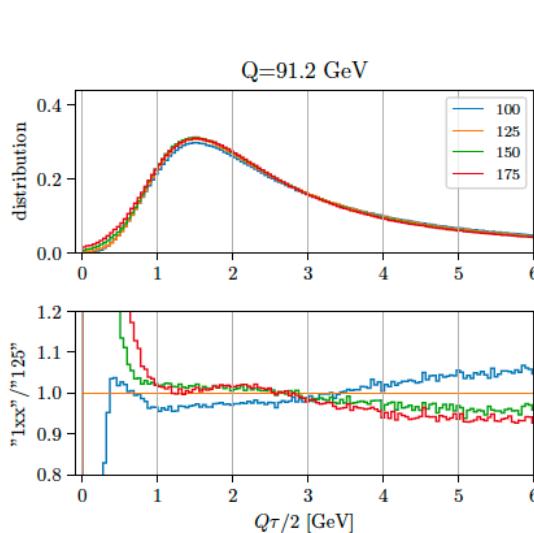
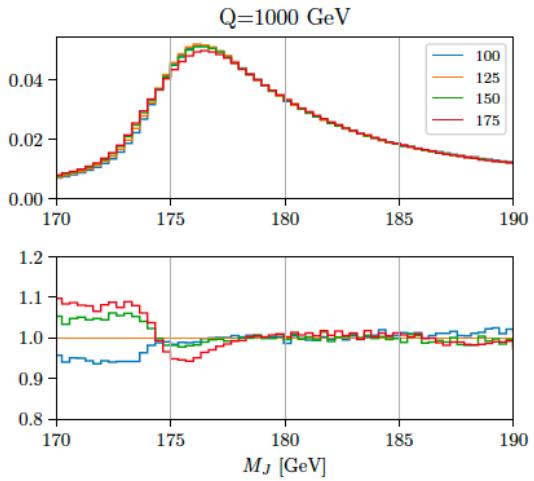
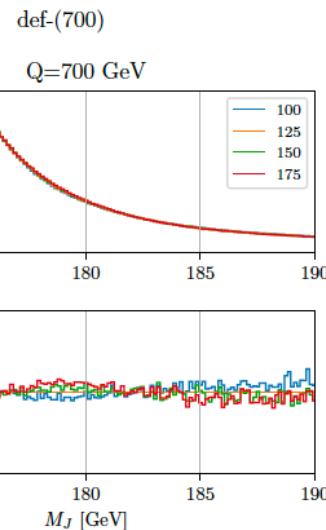
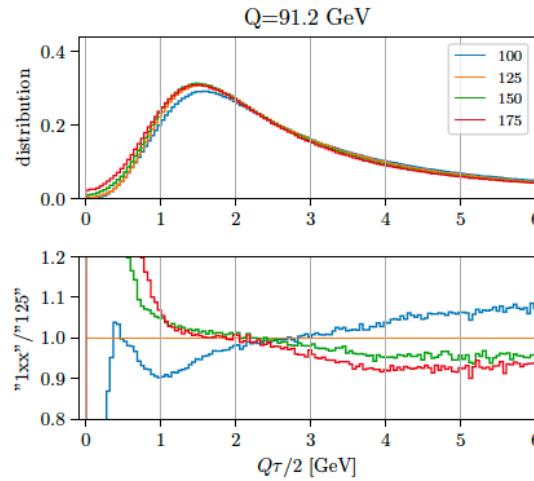
First moment does not satisfy the NLO QCD  $Q_0$ - evolution well



# (D) Factorization compatible hadronization model

Predictions from  $Q_0$ -tuned MC simulations: 2-jettiness

AHH, Jin, Plätzer, Samitz  
to appear

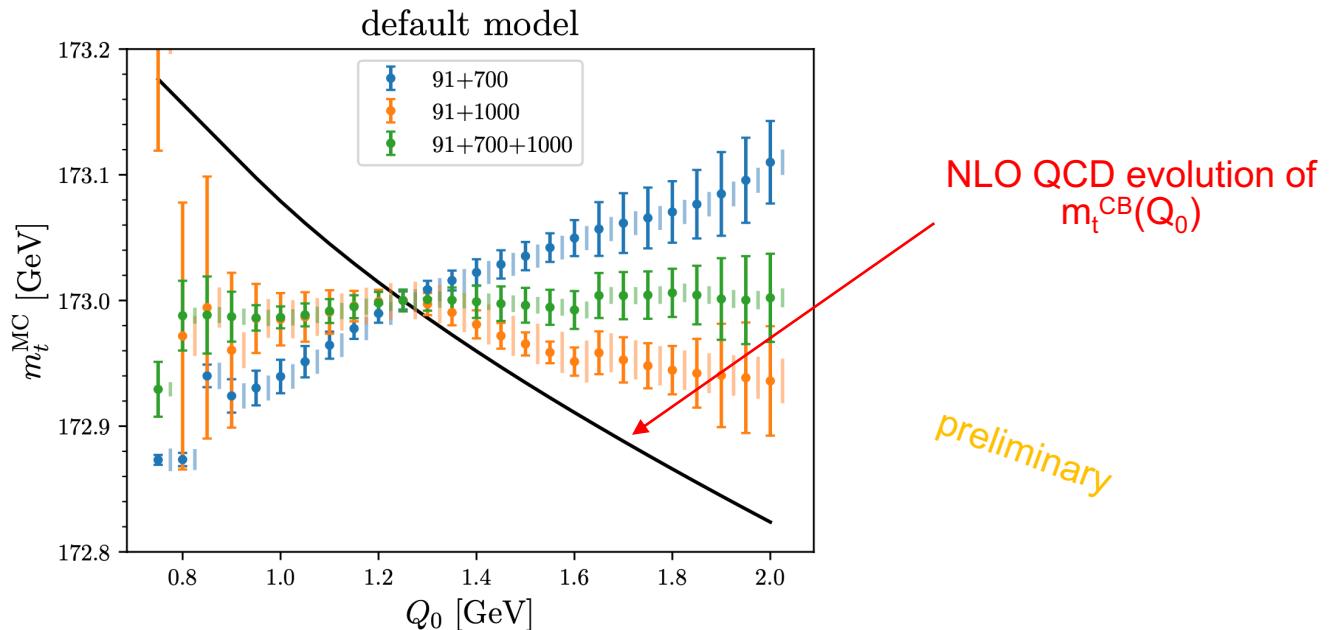


# (D) Factorization compatible hadronization model

AHH, Jin. Plätzer, Samitz to appear

$Q_0$ -dependent tunes  $m_t^{\text{MC}}$ :

- Also tune the top mass parameter  $m_t^{\text{MC}}$  for different  $Q_0$  values  
(to reference data generated for  $Q_0=1.25 \text{ GeV}$ )



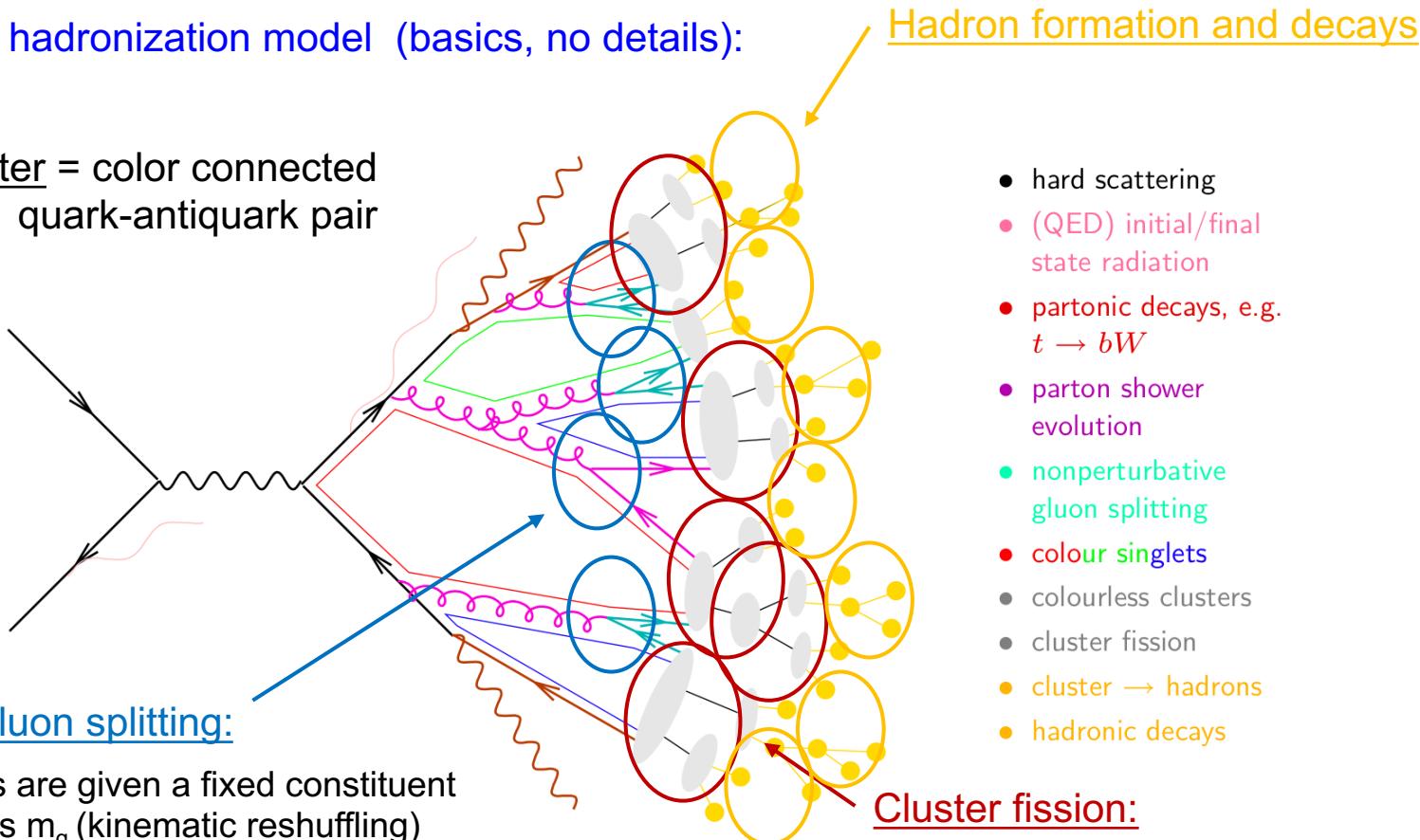
Default Herwig hadronization model modifies  $m_t^{\text{MC}}$  in an unphysical way incompatible with QCD factorization: uncertainty  $\sim 0.5 \text{ GeV}$

→  $m_t^{\text{Herwig}}(Q_0) \neq m_t^{\text{CB}}(Q_0)$  for the default hadronization model

# (D) Factorization compatible hadronization model

Cluster hadronization model (basics, no details):

Cluster = color connected quark-antiquark pair



Forced gluon splitting:

- Gluons are given a fixed constituent masses  $m_g$  (kinematic reshuffling)
- Isotropic decay into light  $q\bar{q}$  pair in gluon rest frame



Ad hoc modelling: not designed to adapt  $Q_0$

Hadron formation and decays

- hard scattering
- (QED) initial/final state radiation
- partonic decays, e.g.  $t \rightarrow bW$
- parton shower evolution
- nonperturbative gluon splitting
- colour singlets
- colourless clusters
- cluster fission
- cluster  $\rightarrow$  hadrons
- hadronic decays

Cluster fission:

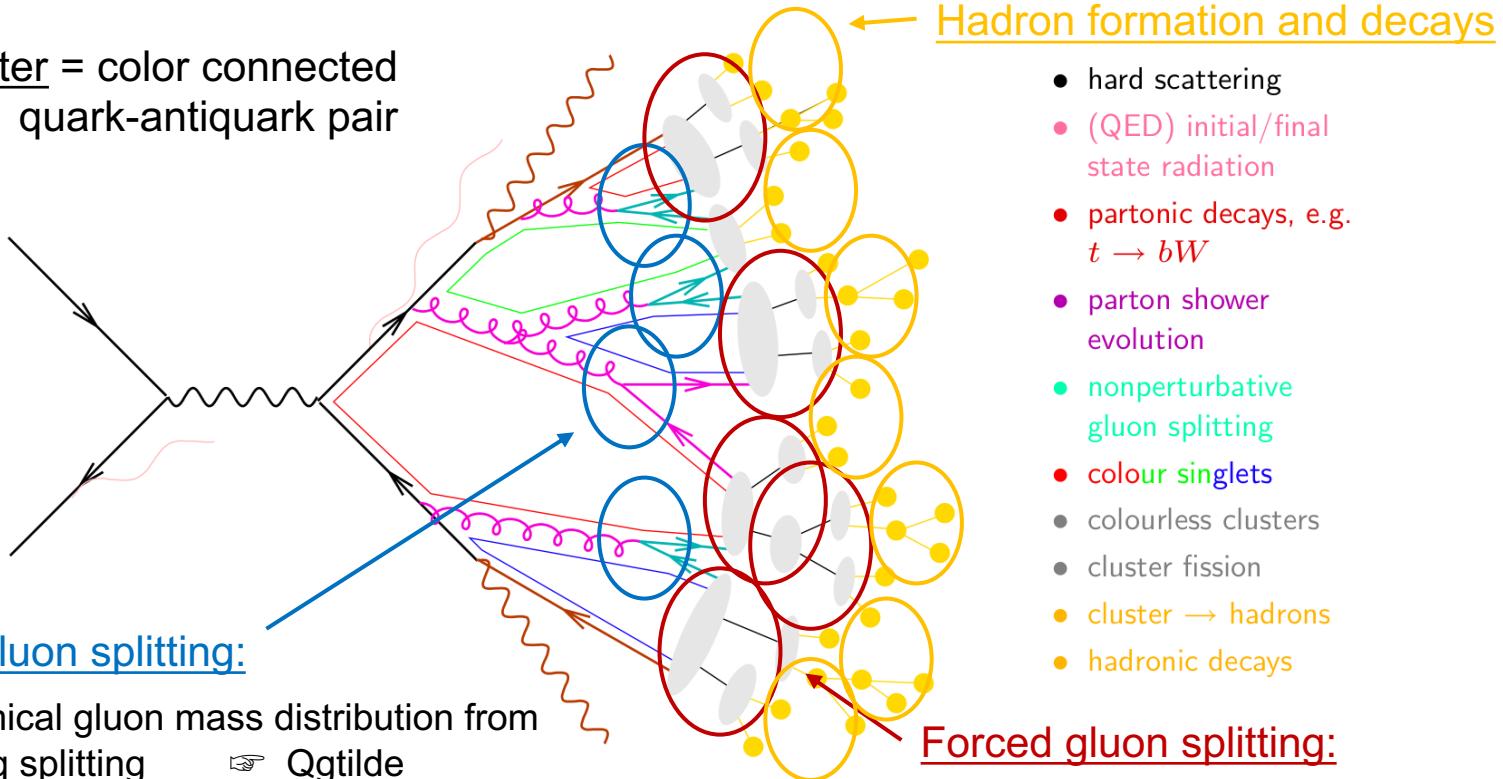
- Cluster fission as a 1-dim process along the  $q\bar{q}$  axis
- Adhoc functional ansatz for cluster mass distribution

# (D) Factorization compatible hadronization model

AHH, Jin. Plätzer, Samitz 2024.09856

Modified cluster hadronization that mimics aspects of parton shower dynamics:

Cluster = color connected quark-antiquark pair



Forced gluon splitting:

- Dynamical gluon mass distribution from  $g \rightarrow qq$  splitting  $\Rightarrow Q\tilde{}$
- Kinematics in analogy to parton shower

Model parameters can consistently adapt to changes of  $Q_0$

Forced gluon splitting:

- Cluster splitting from branching  $q \rightarrow q g$  and splitting  $g \rightarrow qq$   $\Rightarrow Q\tilde{}$
- Kinematics in analogy to the parton shower

# **$Q_0$ -dependent tuning analyses**

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Tuning software: APPRENTICE

AHH, Jin, Plätzer, Samitz  
arXiv:2404.09856

Reference tune = standard  $e^+e^-$  tune (Z-pole LEP data [3180 observable bins])

Reference data = simulated data for  $Q_0 = 1.25$  GeV for

- Z-pole LEP data [3180]
- Z-pole 2-jettiness [peak region]
- ttbar 2-jettiness at  $E_{cm} = 700$  and 1000 GeV [peak region]

$Q_0$ -dependent tunes: tunes to reference data for different shower cut  $Q_0$  values

Tuned parameters: 6 tuning parameters +  $m_t^{MC}$

## Default model

- $m_g$  (force gluon splitting)
- PSplit (cluster fission, mass distr.)
- $Cl_{max}$  (cluster fission, condition)
- $Cl_{pow}$  (cluster fission, condition)
- PwtSquark (cluster hadronization)
- PwtDIquark (cluster hadronization)

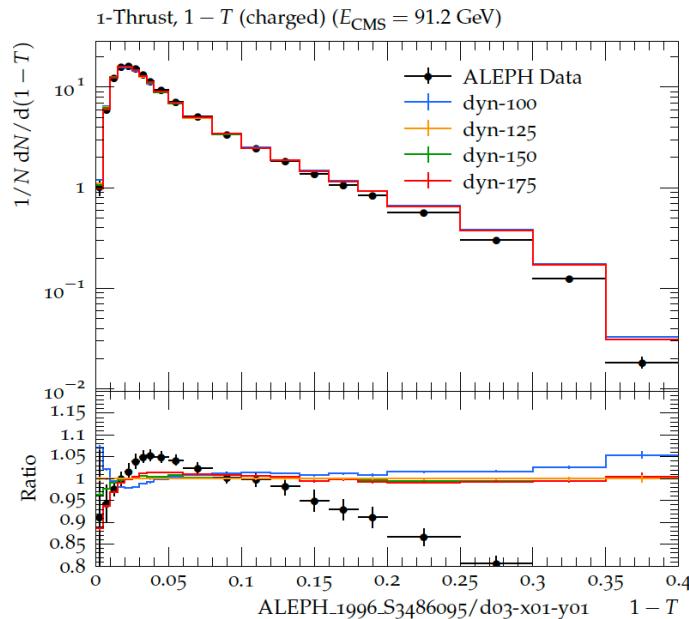
## Dynamic model

- $Q\tilde{g}$  (forced gluon splitting)
- $Q\tilde{q}$  (cluster fission splitting)
- $Cl_{max}$  (cluster fission, condition)
- $Cl_{pow}$  (cluster fission, condition)
- PwtSquark (cluster hadronization)
- PwtDIquark (cluster hadronization)

Interpolation grids: cubic and quartic polynomials

# (D) Factorization compatible hadronization model

Migration function much better consistent with QCD factorization



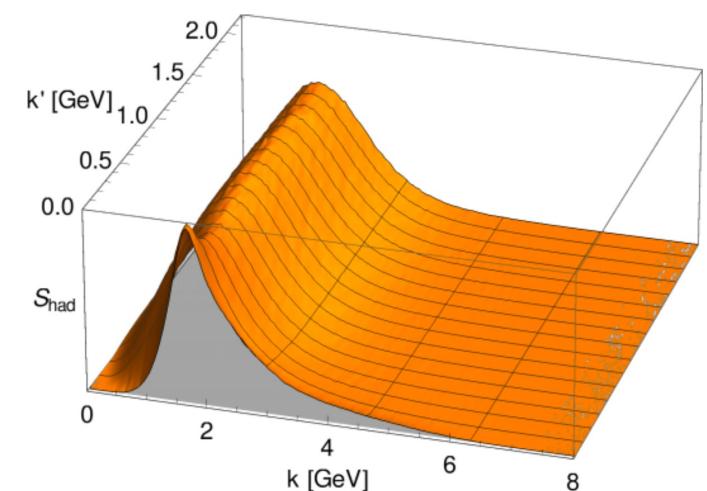
Tunes  $m_t^{\text{MC}}$  fully consistent with expectations from analytic QCD calculation

( “pseudo data” generated for  $Q_0=1.25 \text{ GeV}$  )

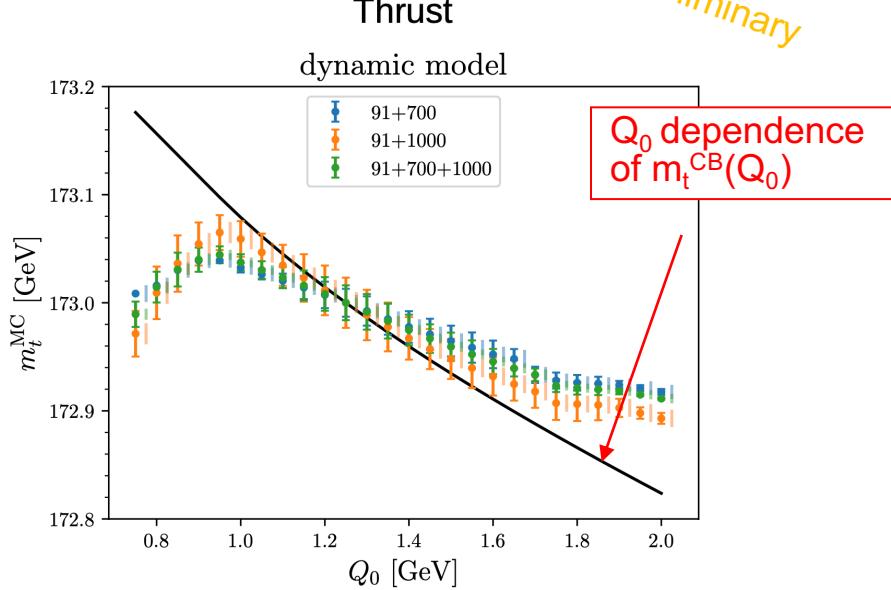
$$\Rightarrow m_t^{\text{Herwig}}(Q_0) = m_t^{\text{CB}}(Q_0)$$

within a precision of better than 50 MeV

AHH, Jin, Plätzer, Samitz to appear



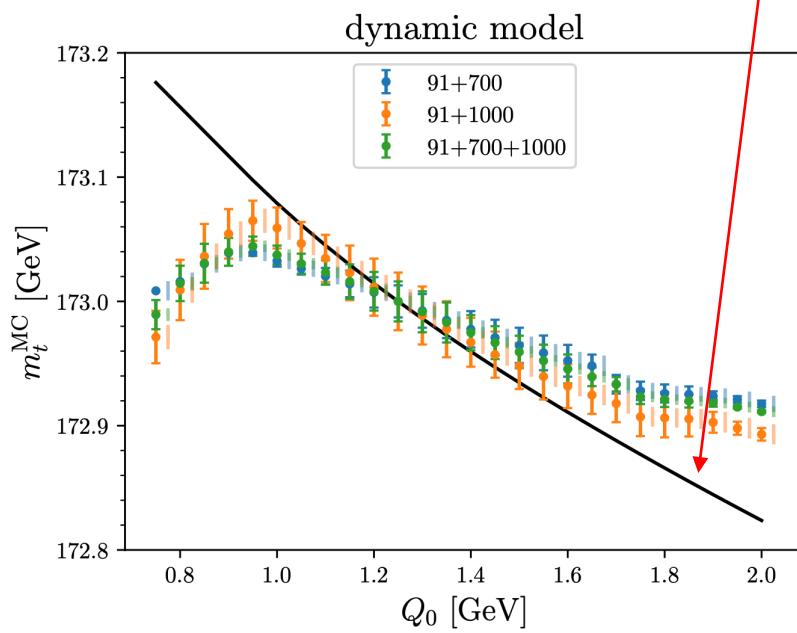
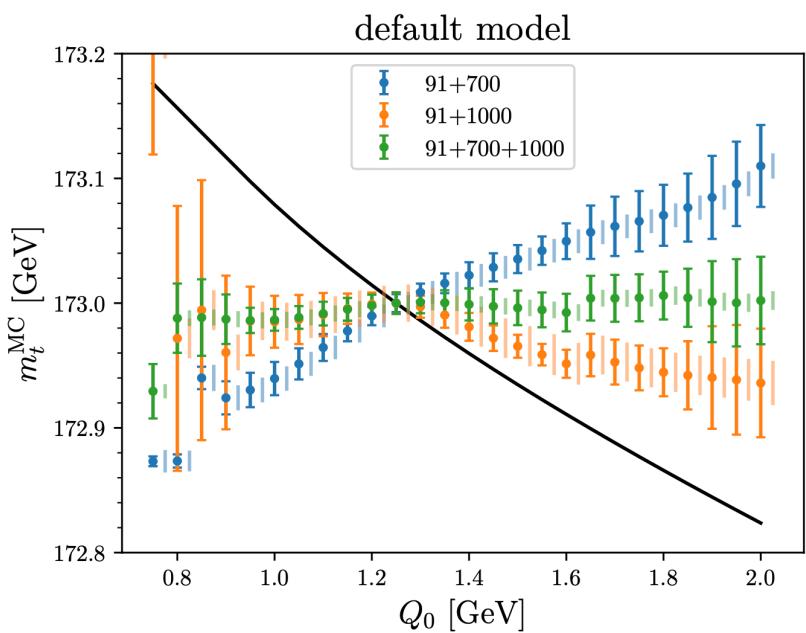
*preliminary*



# Old Default Model vs. New Dynamical Model

AHH, Jin. Plätzer, Samitz to appear

Shower cutoff dependence of tuned MC top quark mass to reference data including top quark 2-jettiness distributions at 700 and/or 1000 GeV



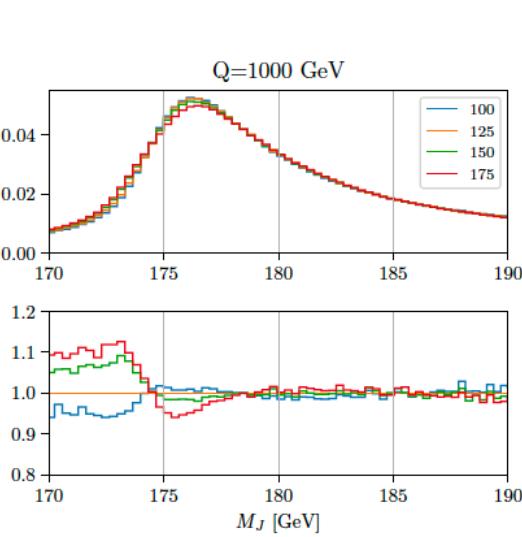
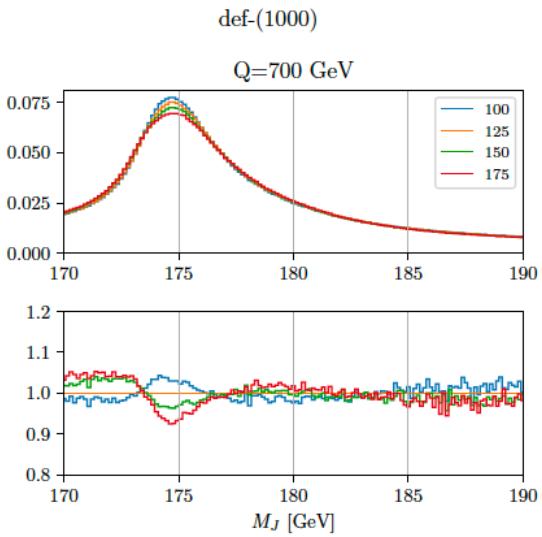
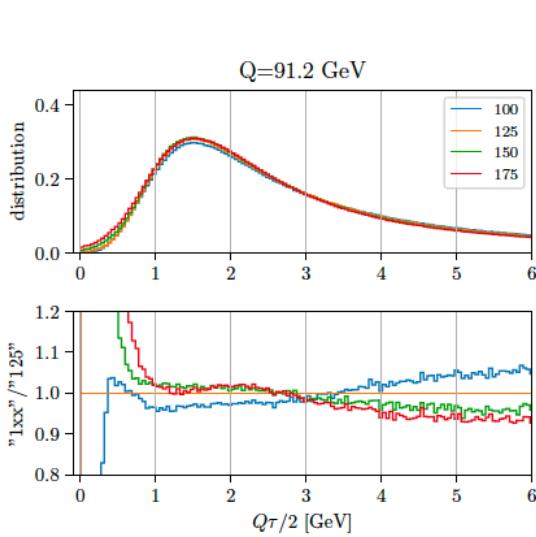
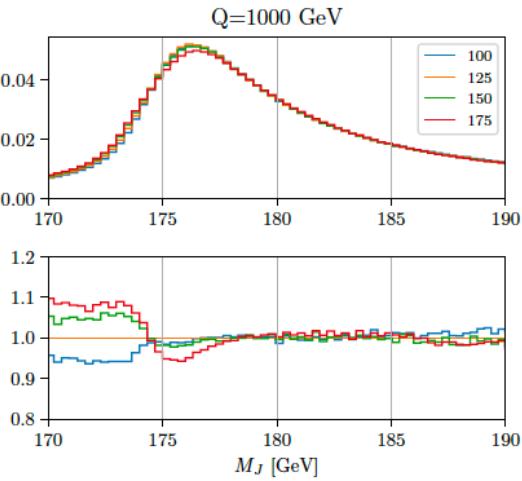
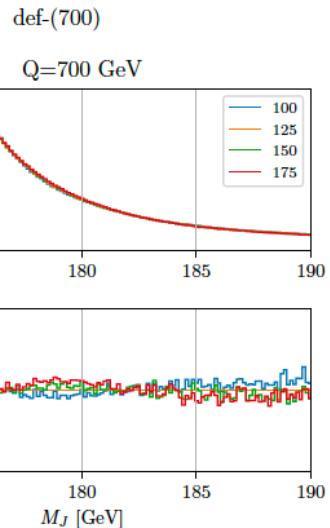
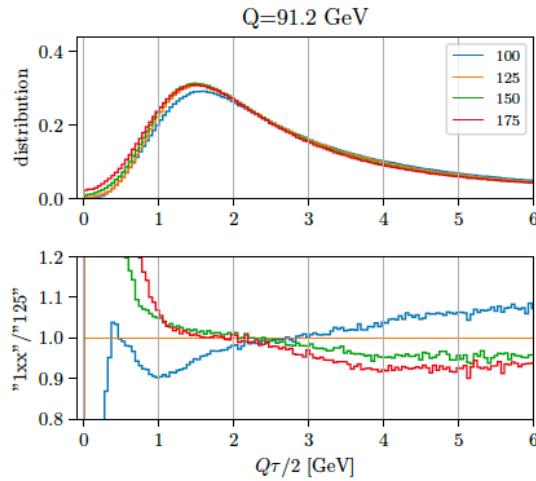
Q<sub>0</sub> dependence expected from  $m_t^{\text{CB}}(Q_0)$

Agreement of  $m_t^{\text{MC}}$  with  $m_t^{\text{CB}}(Q_0)$  within 50 MeV !

# Old Default Model vs. New Dynamical Model

Predictions from  $Q_0$ -tuned MC simulations: 2-jettiness

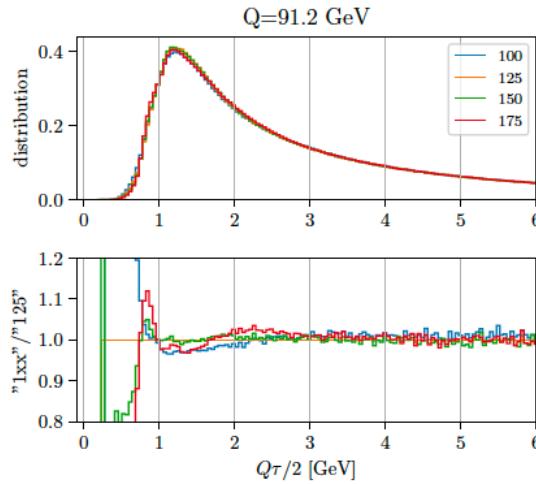
AHH, Jin, Plätzer, Samitz  
to appear



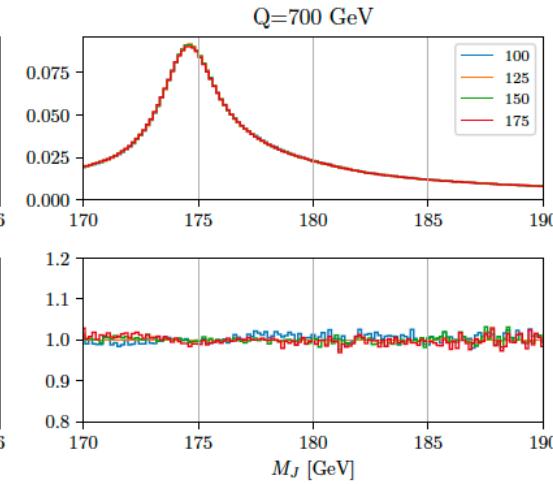
# Old Default Model vs. New Dynamical Model

Predictions from  $Q_0$ -tuned MC simulations: 2-jettiness

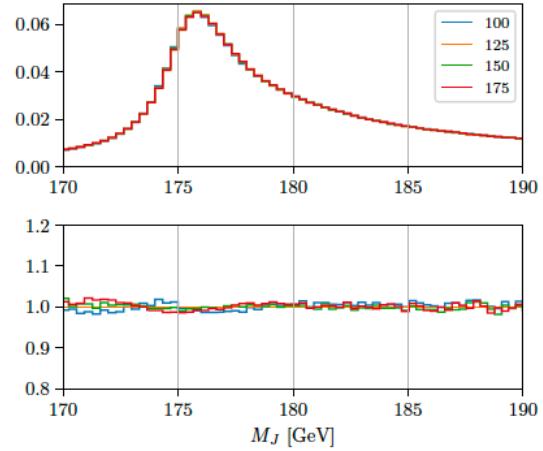
AHH, Jin, Plätzer, Samitz  
to appear



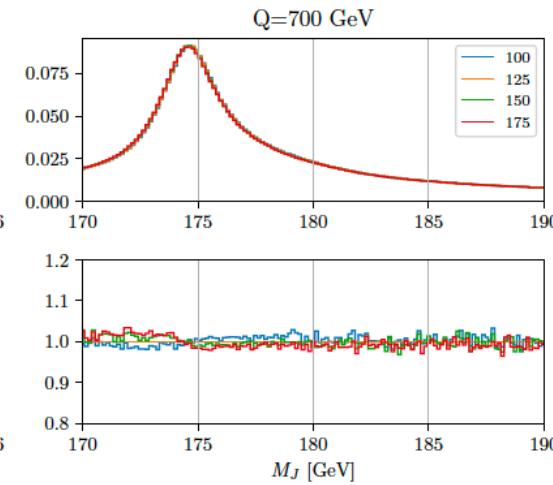
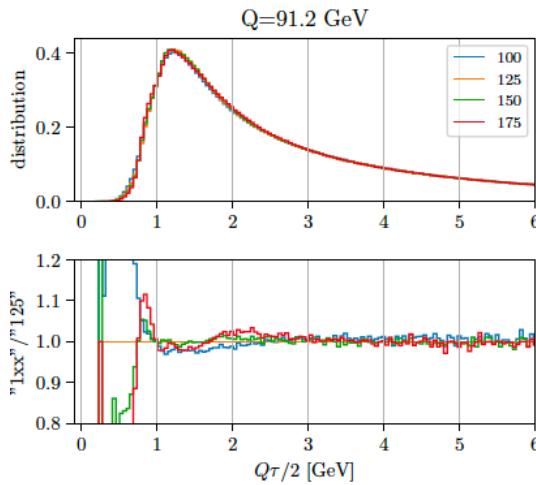
dyn-(700)



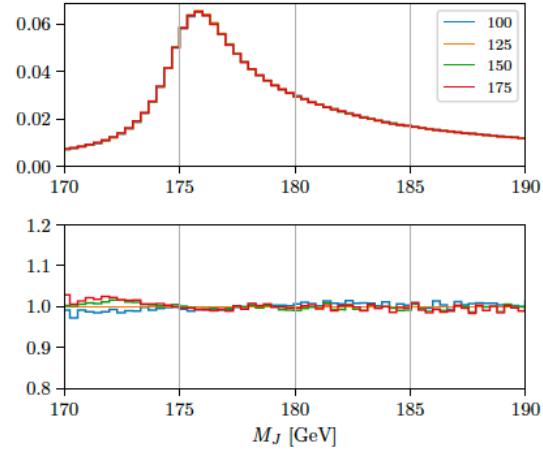
Q=1000 GeV



dyn-(1000)



Q=1000 GeV

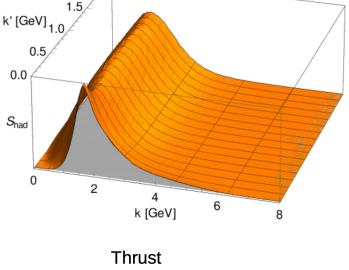
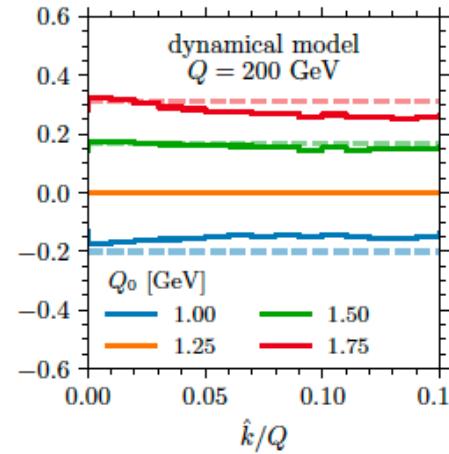
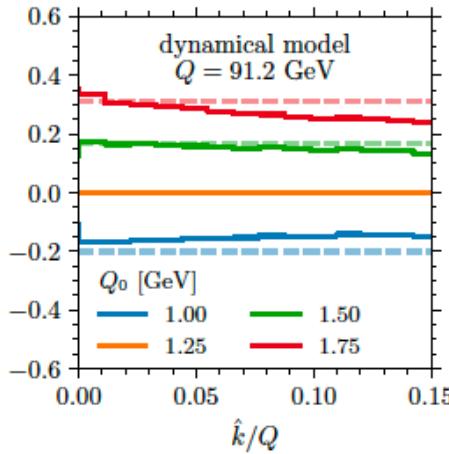
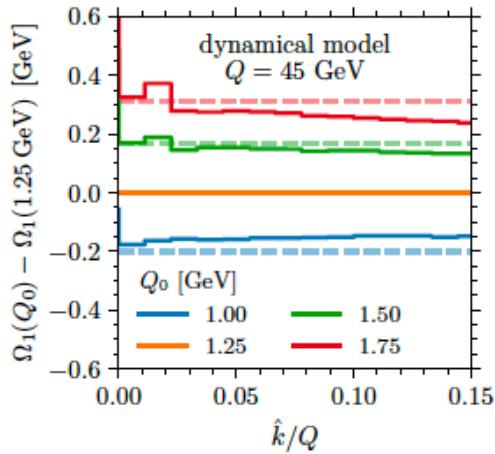
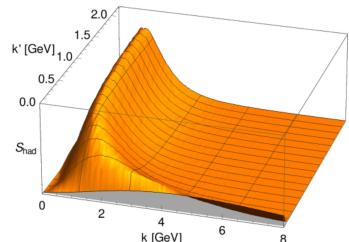
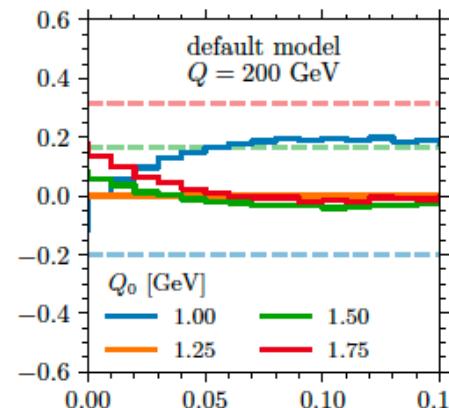
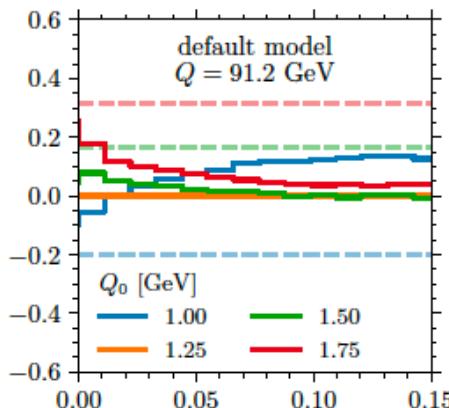
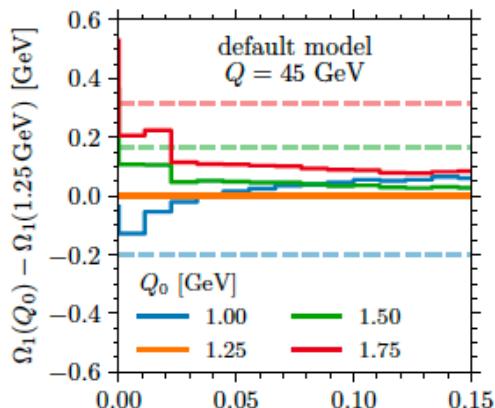


# Old Default Model vs. New Dynamical Model

AHH, Jin. Plätzer, Samitz 2404.09856

Shower cutoff dependence of first moment  $\Omega_1$  of migration matrix from simulations for 2-jettiness  $\rightarrow$  "MC scheme for hadronization correction"

$$\Omega_1^{\text{MC}}(\hat{k}, Q, Q_0) - \Omega_1^{\text{MC}}(\hat{k}, Q, Q_{0,\text{ref}} = 1.25 \text{ GeV})$$

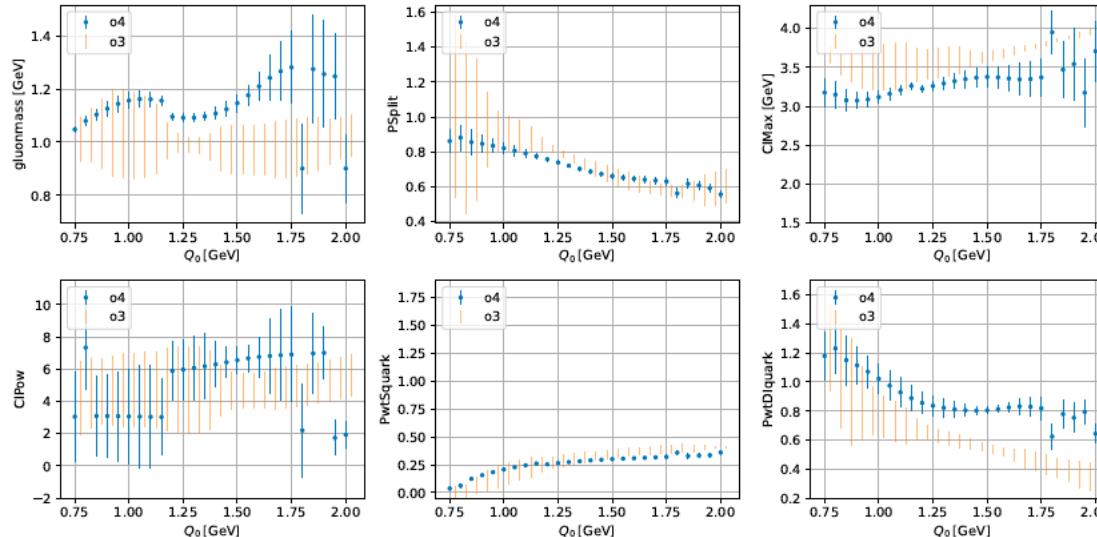


Thrust

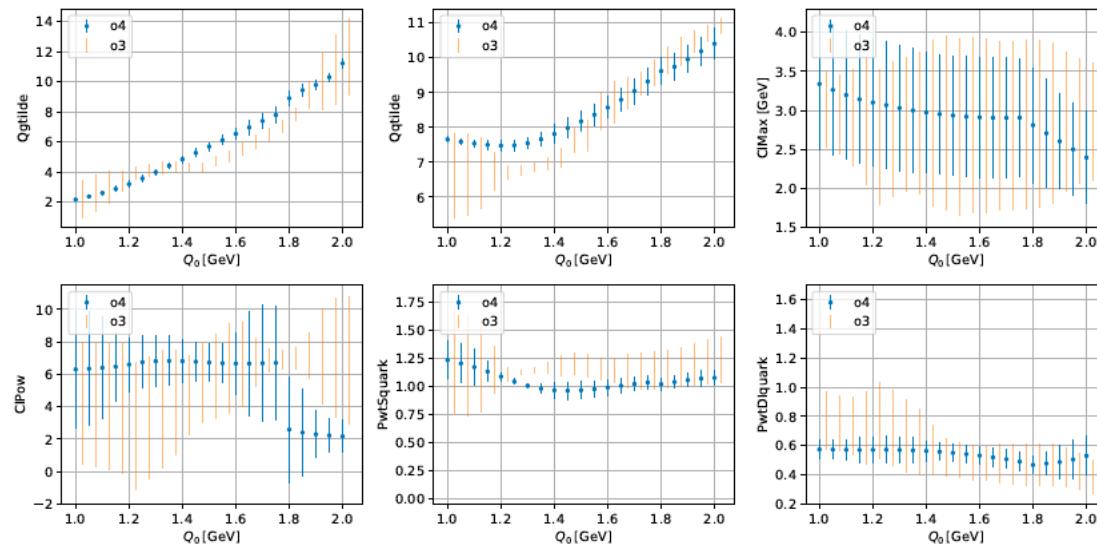
# Old Default Model vs. New Dynamical Model

Tuned parameters for  $Q_0$ -dependent tuning analyses (apart from  $m_t^{\text{MC}}$ )

Default model



Dynamical model



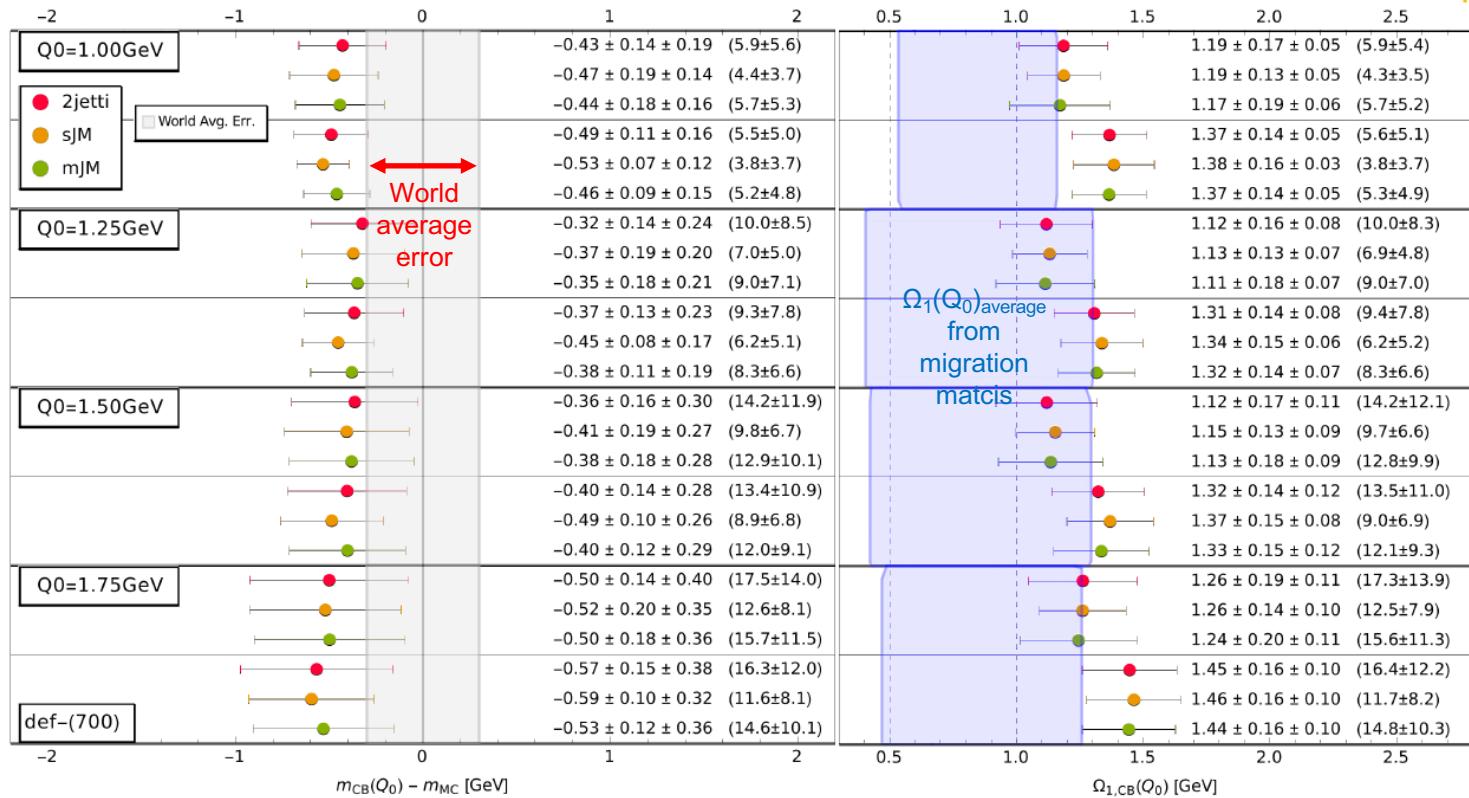
AHH, Jin, Plätzer,  
Samitz  
arXiv:2404.09856

# Old Default Model vs. New Dynamical Model

AHH, Jin. Plätzer, Samitz to appear

Cross check: apply top mass calibration to determine  $m_t^{\text{CB}}(Q_0)$

default model



Default:  $m_t^{\text{MC}}$  incompatible with  $m_t^{\text{CB}}(Q_0)$

First moment of migration matrix with large variations,  $Q_0$ -evolution not visible

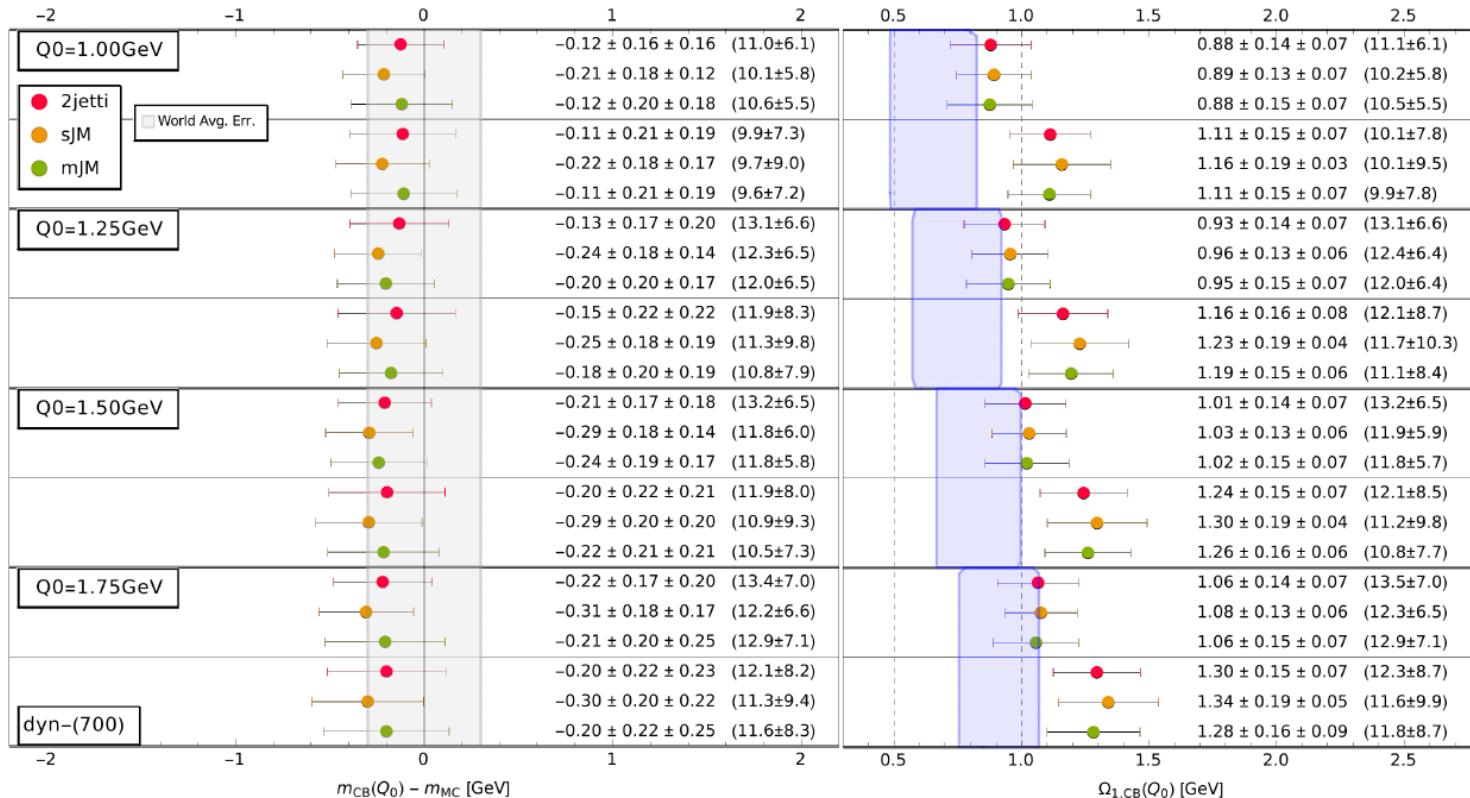
Dynamical:  $m_t^{\text{MC}}$  compatible with  $m_t^{\text{CB}}(Q_0)$

First moment of migration matrix with smaller variations,  $Q_0$ -evolution clearly visible

# Old Default Model vs. New Dynamical Model

AHH, Jin. Plätzer, Samitz to appear

Cross check: apply top mass calibration to determine  $m_t^{\text{CB}}(Q_0)$



dynamical  
model

Default:  $m_t^{\text{MC}}$  incompatible with  $m_t^{\text{CB}}(Q_0)$

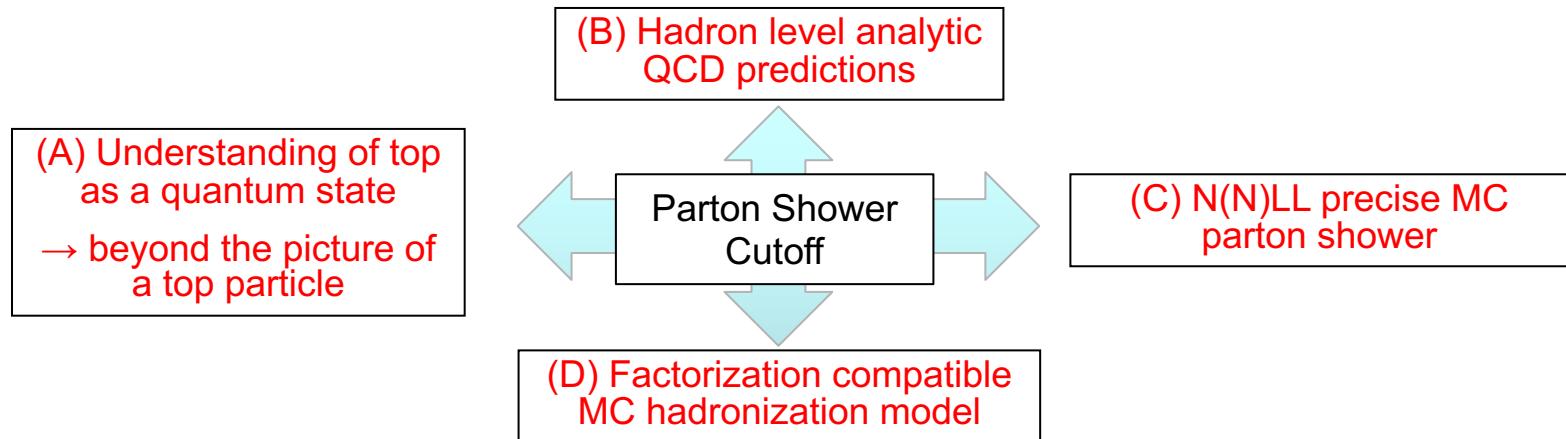
First moment of migration matrix with large variations,  $Q_0$ -evolution not visible

Dynamical:  $m_t^{\text{MC}}$  compatible with  $m_t^{\text{CB}}(Q_0)$

First moment of migration matrix with smaller uncertainties,  $Q_0$ -evolution clearly visible

# Final remarks and Outlook

- We have demonstrated: It is possible to promote the MC top mass parameter  $m_t^{\text{MC}}$  to a renormalization scheme so that its NLO relation to any other top mass renormalization scheme can be calculated.  
$$\rightarrow m_t^{\text{MC}} = m_t^{\text{CB}}(Q_0)$$
- Key aspect: Parton shower cutoff  $Q_0$  = Factorization scale separating pQCD and npQCD
- Currently: Concretely working machinery available only for  $e^+e^-$  event-shapes
- The realization of (A)-(D) in this work provides a concrete blueprint that can now be applied to other classes of observables more closely related to direct measurements.



# Final remarks and Outlook

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2-jettiness: top decay insensitive

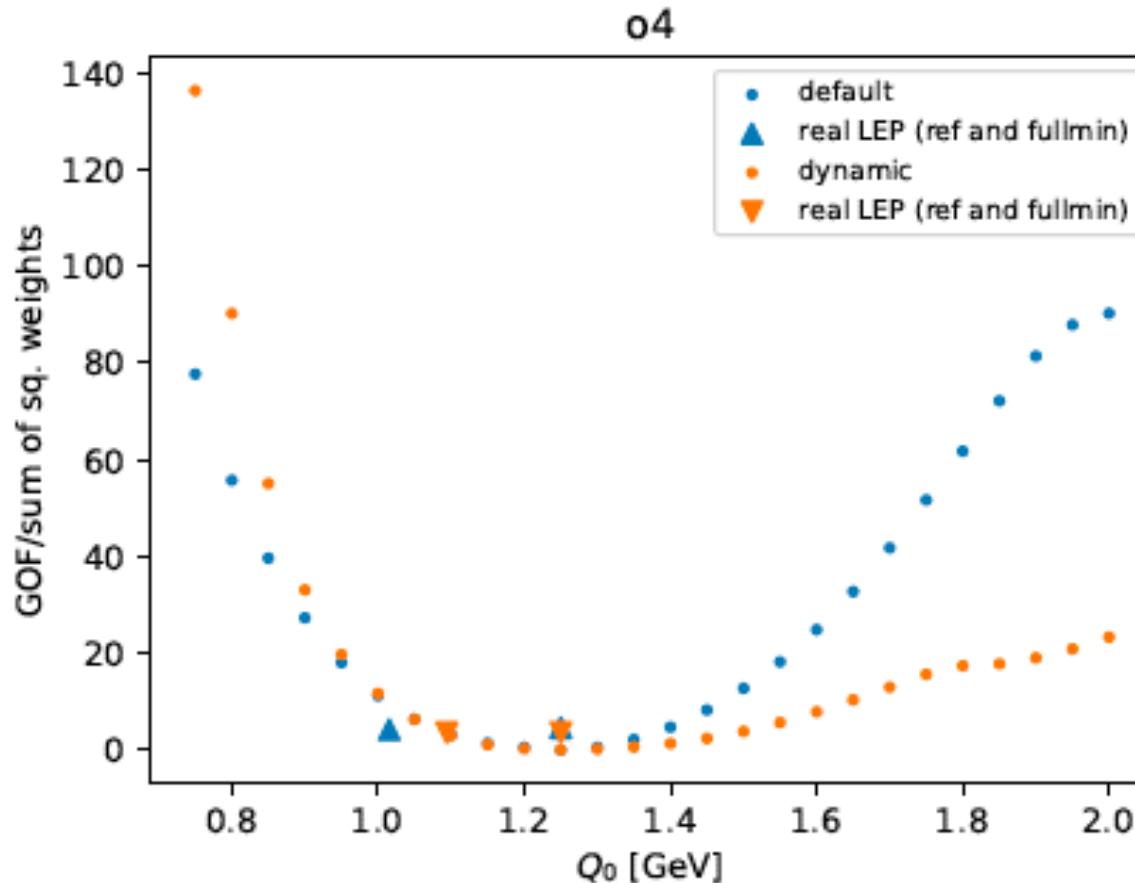


- Universality of the current insights
  - So far we have all theoretical ingredients to interpret  $m_t^{\text{MC}}$  only for  $e^+e^-$  eventshape distributions and the Herwig MC generator (coherent branching + cluster hadronization)
  - Novel dynamical hadronization model: public with Herwig 7.4 release
  - Recall: MC generators do not have the same precision for all observables
- Progress to generalize the current results will involve much more work because many theory tools need to be developed ( $\rightarrow$  e.g. differential in top decay)
- Future plans:
  - ▶ investigate dipole shower (NLL), string hadronization (Pythia)
  - ▶ investigate other shower cutoff prescriptions
  - ▶ universality: observables differential in top decay ( $\rightarrow$  e.g.  $M_{\text{b-jet lepton}}$ )
  - ▶ long-term aim: b-jets with small jet radius
  - ▶ establish a  $m_t^{\text{MC}}$  verification tool box
  - ▶ MC Hadronization corrections with controlled scheme dependence
- Cetero censeo: MPI and UE hadronization models still need to be better understood from the QCD perspective

# Old Default Model vs. New Dynamical Model

AHH, Jin, Plätzer, Samitz arXiv:2404.09856

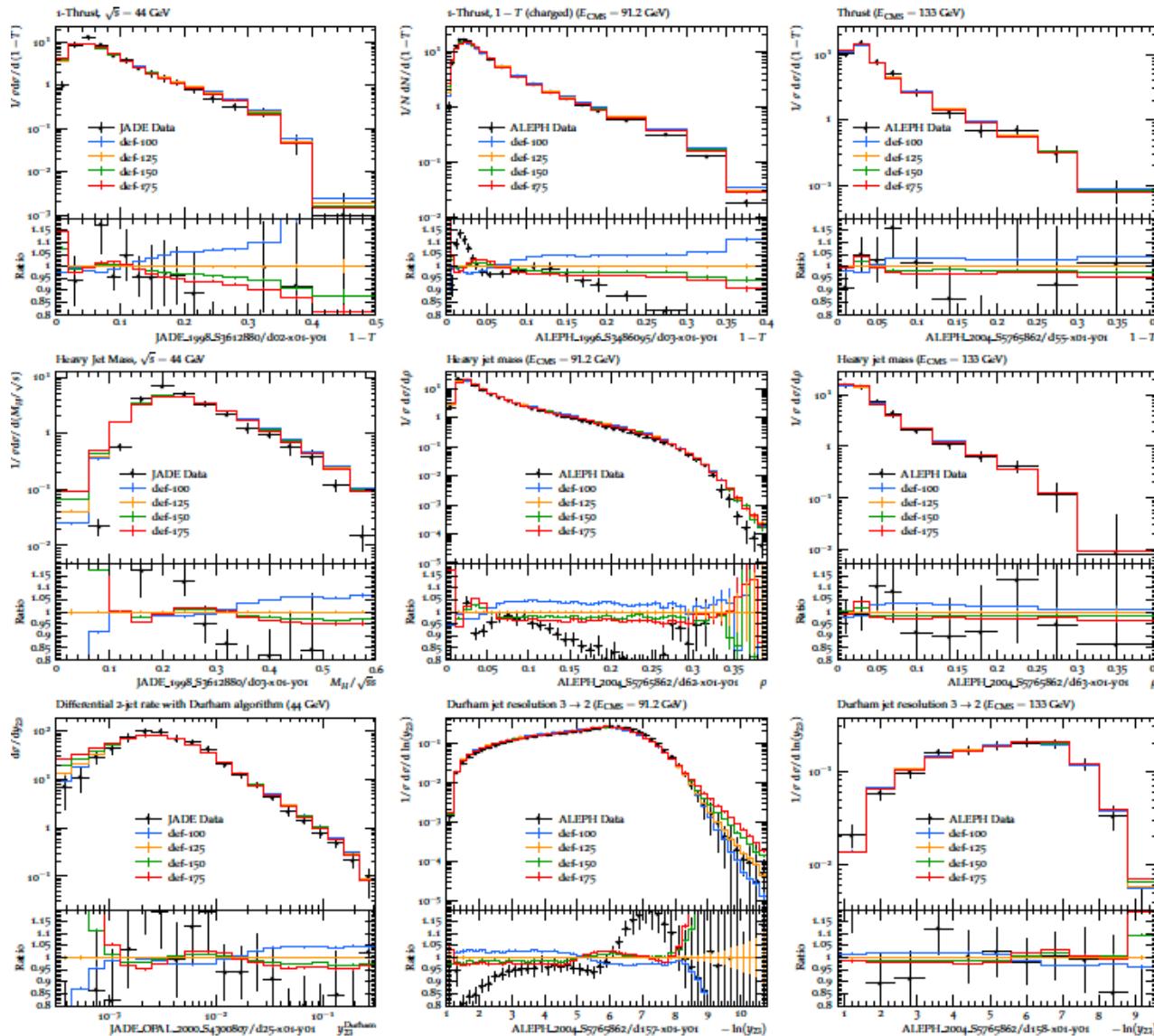
Shower cutoff  $Q_0$  minimal  $\chi^2$ -values obtained in the tuning fits



# Old Default Model vs. New Dynamical Model

AHH, Jin, Plätzer, Samitz arXiv:2404.09856

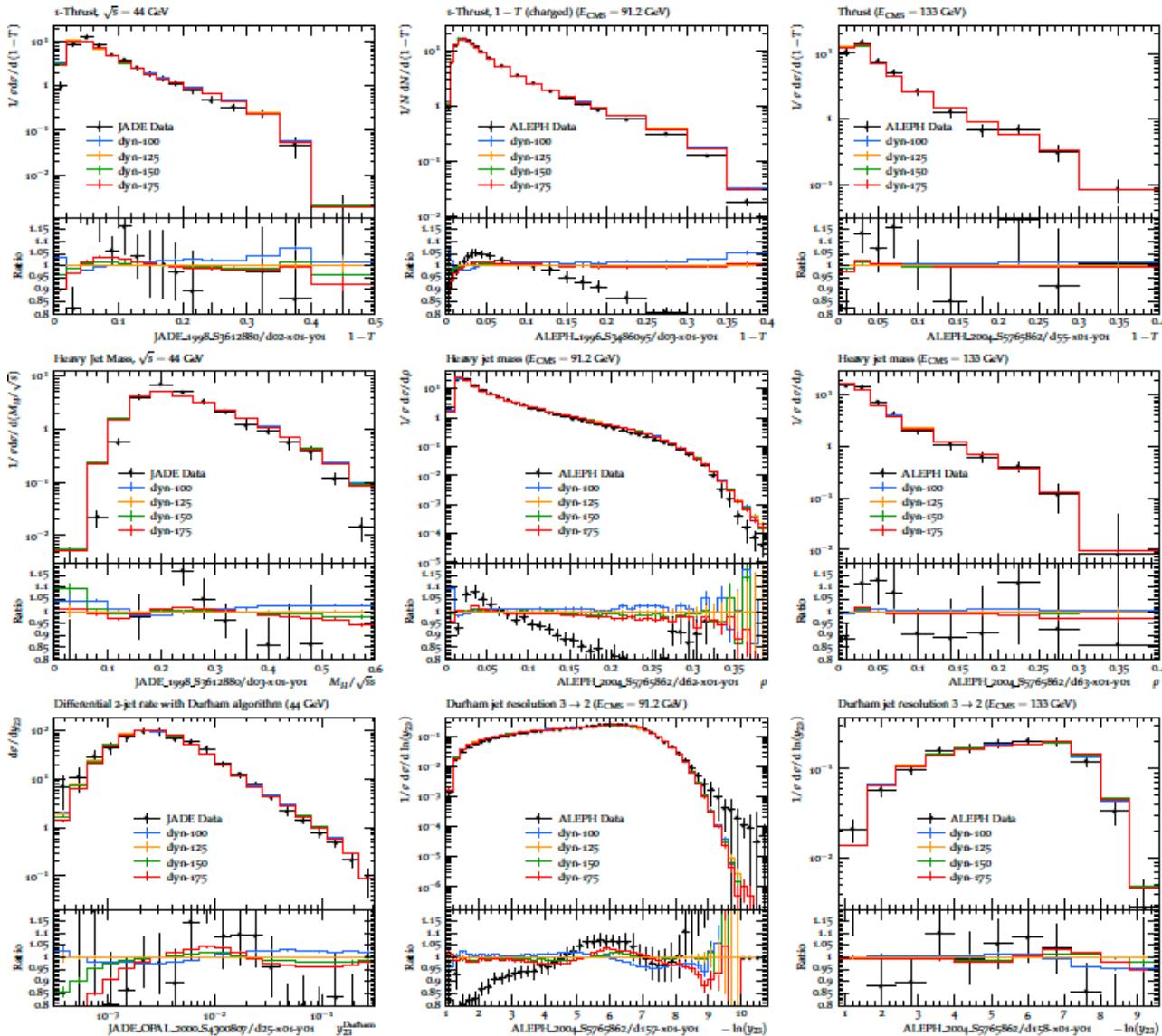
Default



# Old Default Model vs. New Dynamical Model

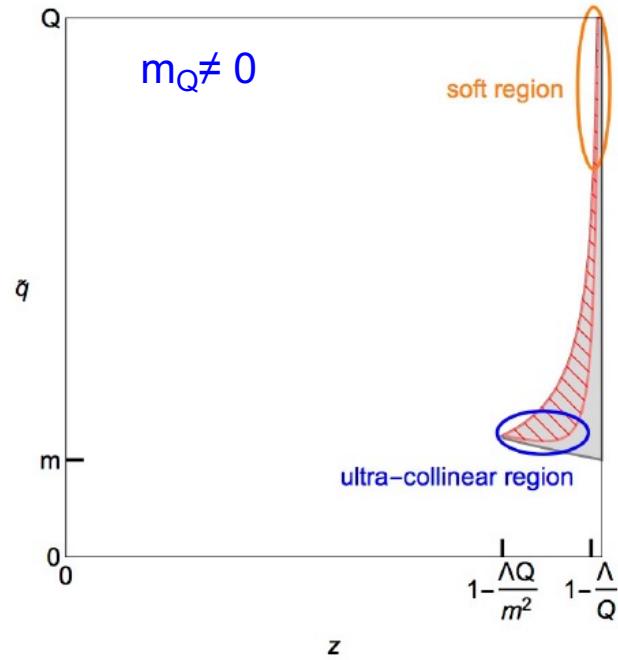
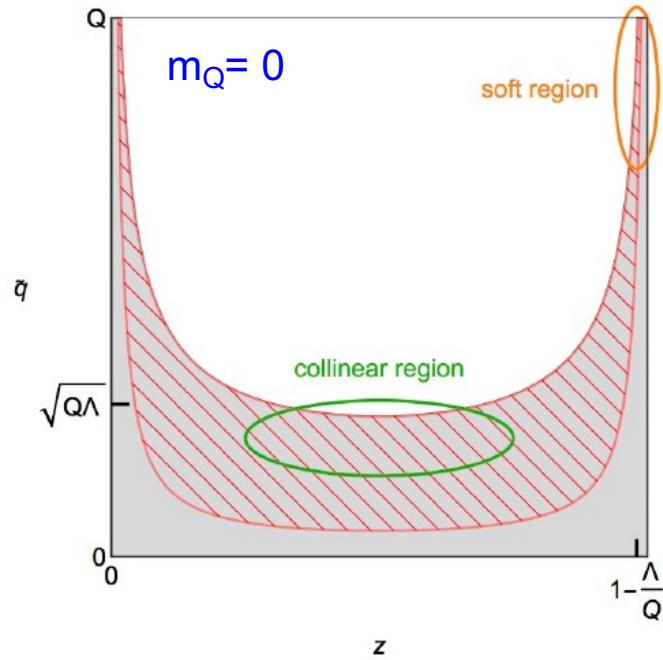
AHH, Jin, Plätzer, Samitz arXiv:2404.09856

Dynamical



# Phase Space and Power Counting ( $Q_0=0$ )

AHH, Plätzer, Samitz arXiv:1807.06617



phase space regions for $\tau_{\text{peak}} \sim \frac{\Lambda}{Q} \ll 1, m = 0$		
	coherent branching	QCD factorization
n-coll.	$z \sim (1-z) \sim 1$ $\tilde{q} \sim (Q\Lambda)^{\frac{1}{2}}$ $q_{\perp} \sim (Q\Lambda)^{\frac{1}{2}}$	$q^{\mu} \sim (\Lambda, Q, (Q\Lambda)^{\frac{1}{2}})$
soft	$1-z \sim \frac{\Lambda}{Q}, z \sim 1$ $\tilde{q} \sim Q$ $q_{\perp} \sim \Lambda$	$q^{\mu} \sim (\Lambda, \Lambda, \Lambda)$

phase space regions for $\tau_{\text{peak}} - \tau_{\min} \sim \frac{\Lambda}{Q} \ll 1, m \neq 0$		
	coherent branching	QCD factorization
u. coll.	$1-z \sim \frac{Q\Lambda}{m^2}, z \sim 1$ $\tilde{q} \sim m$ $q_{\perp} \sim \frac{Q}{m}\Lambda$	$q^{\mu} \sim (\Lambda, \frac{Q^2}{m^2}\Lambda, \frac{Q}{m}\Lambda)$
soft	$1-z \sim \frac{\Lambda}{Q}, z \sim 1$ $\tilde{q} \sim Q$ $q_{\perp} \sim \Lambda$	$q^{\mu} \sim (\Lambda, \Lambda, \Lambda)$