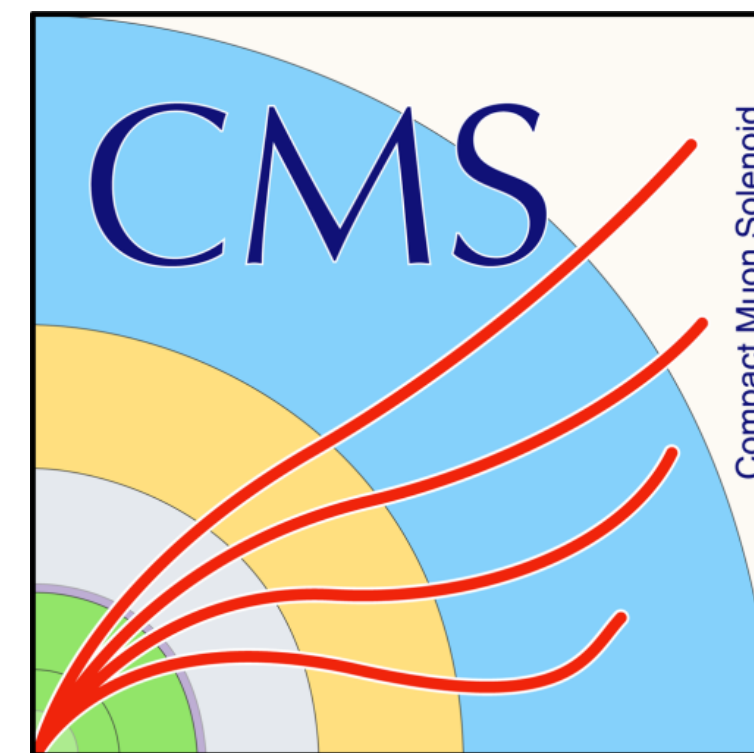


TOP Differential Cross Sections

Top Workshop, Saint-Malo, 23 Sep 2024

Olaf Behnke, DESY 

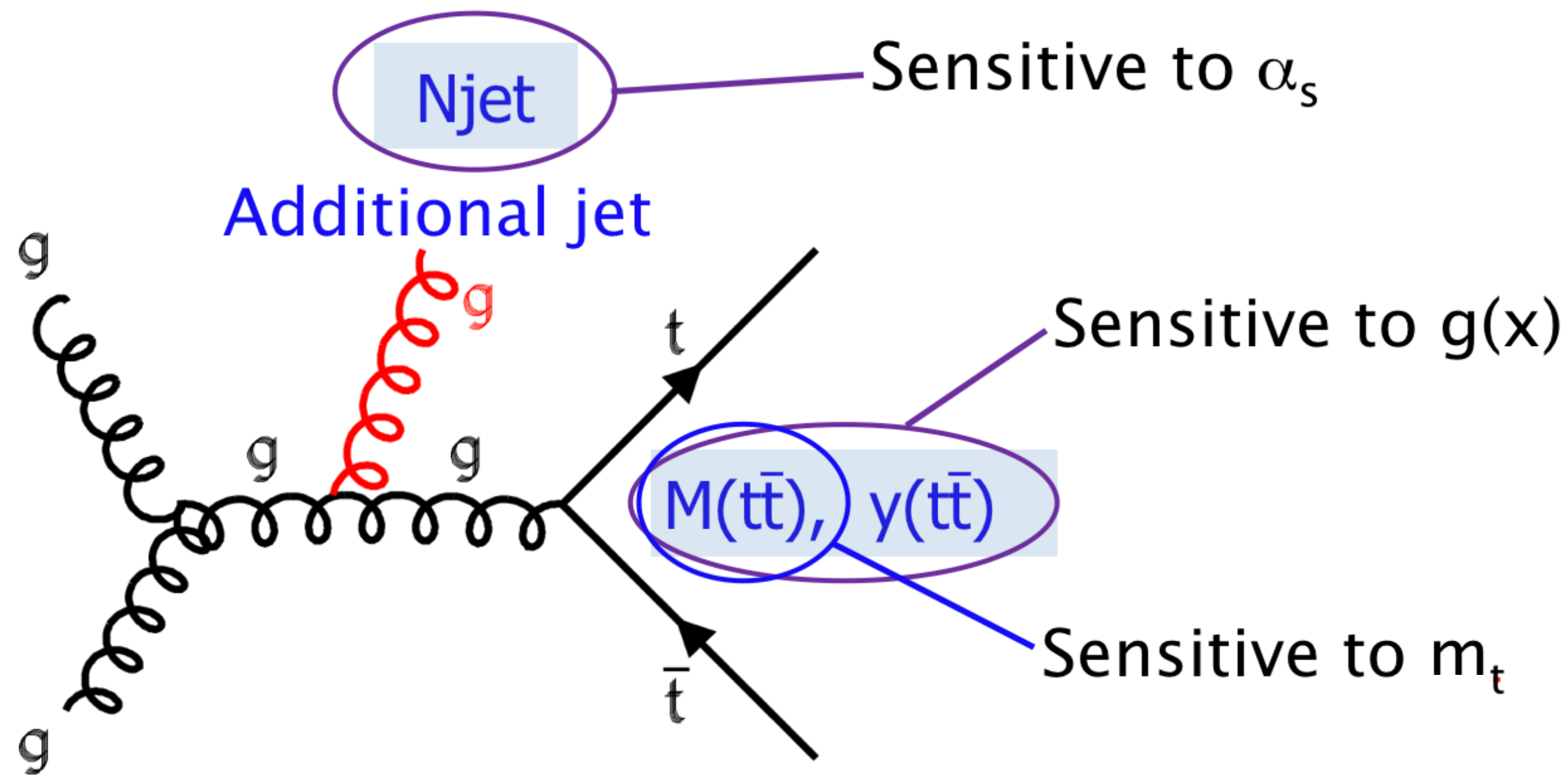
on behalf of the ATLAS and CMS Collaborations



Will focus on top pair production, single top differential results
are covered in talk by [Javier Del Riego Badas](#)

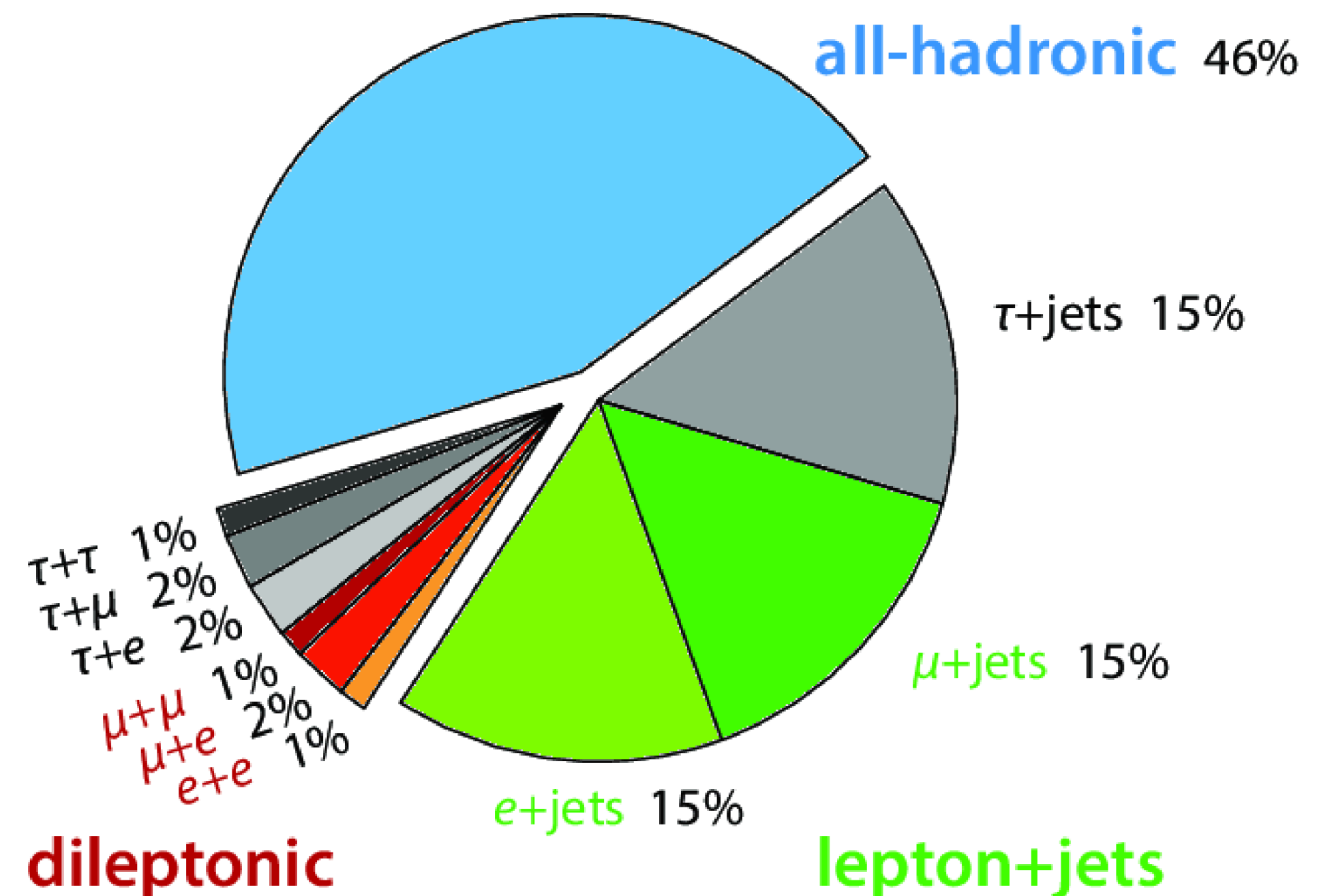
Differential $t\bar{t}$ production at the LHC

- study kinematical & topological distributions:
- ✓ QCD+EW Test
- ✓ Sensitive to theory parameters



tt Events in ATLAS and CMS	
Run 2	Run 3 till now
~100M	~100M

No differential $t\bar{t}$ results yet



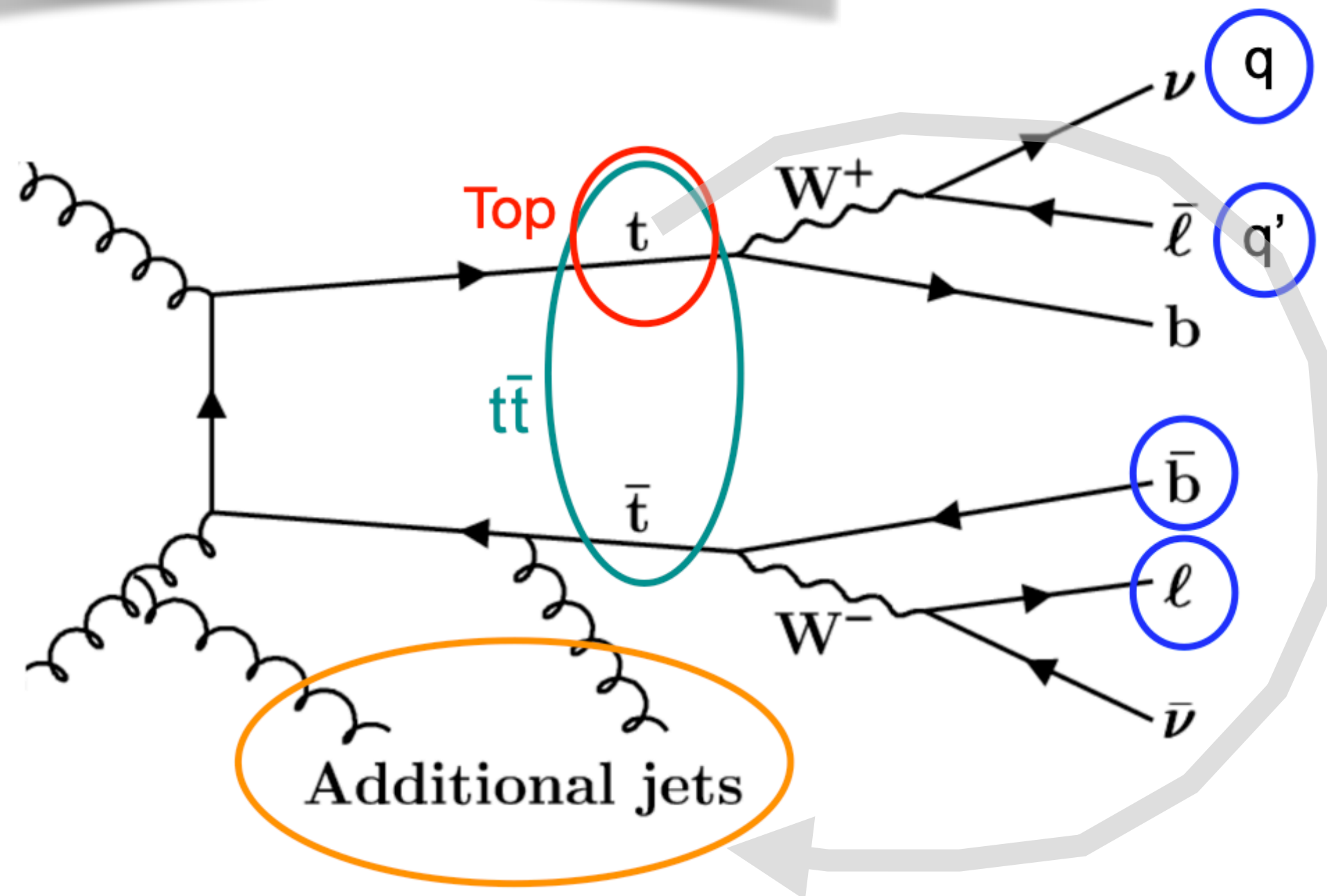


Today's Menu: review of RUN 2 results

- Make a round trip through the observable systems and kinematic distributions
- Compare most comprehensive ATLAS and CMS results with state-of-the-art predictions

Observable systems

Decay particles: l, b, q, q'



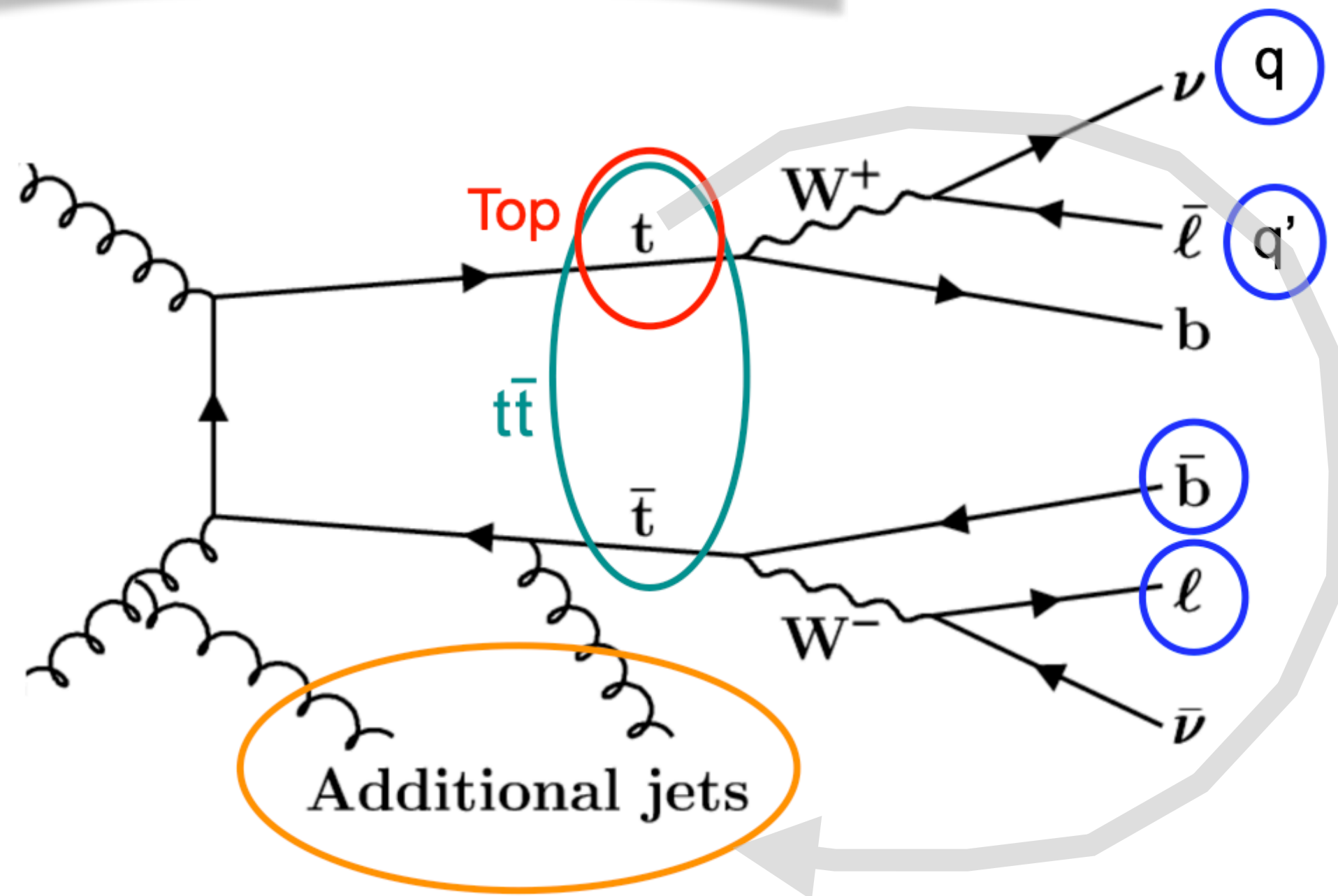


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Featured Analyses

Exp.	Journal or arXiv:	Channel	Lumi fb-1	Phase space	Unfolding	Top	tt	Decay particle	Additional Jets	Largest Syst.
CMS	2402.08486	Dilepton	138	Resolved	TUnfold	✓	✓	✓	✓	JES/R
CMS	PRD 104 (2021) 092013	l+jets	137	Resolved +Boosted	MLE	✓	✓	✓	✓	JES/R
CMS	PRD 97.112003 (2018)	l+jets	36	Resolved	D'Agostini	✓	✓	✓	✓	JES/R
ATLAS	JHEP 08 (2024) 182	l+jets	140	Resolved	D'Agostini			✓	✓	JES/R
ATLAS	JHEP07 (2023) 141	emu	140	Resolved	Bin-by-bin			✓		tt - tW interf. s and b modeling
ATLAS	JHEP 04 (2023) 080	All had	139	Both tops Boosted	D'Agostini	✓	✓			Top tagging
ATLAS	JHEP 06 (2022)063	l+jets	139	Boosted	D'Agostini	✓	✓		✓	JES/R, tt modeling
ATLAS	EPJC 79 (2019) 2018	l+jets	36	Resolved +Boosted	D'Agostini	✓	✓		✓	JES/R

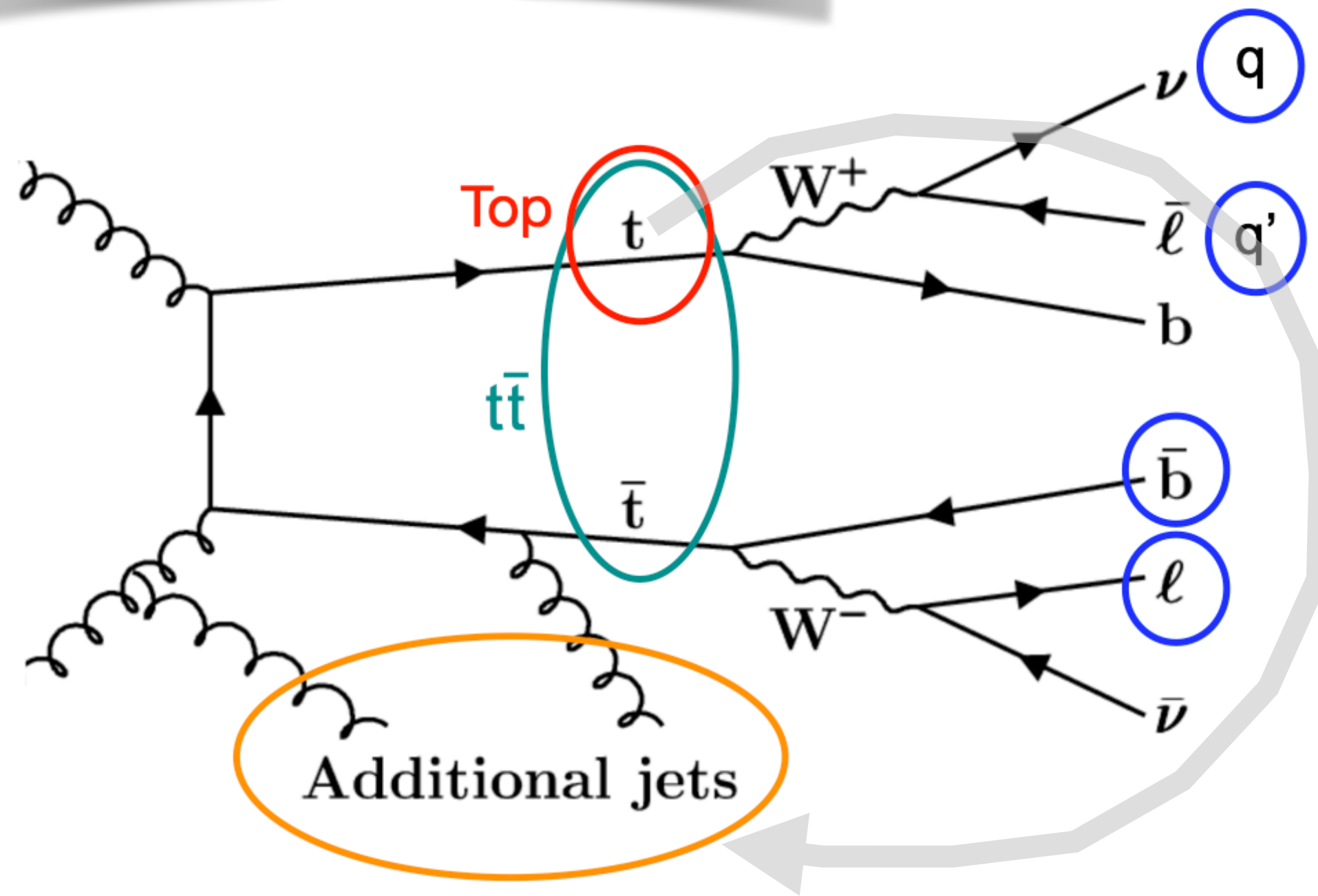


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ATLAS	EPJC 79 (2019) 2018	l+jets	36	Resolved +Boosted	D'Agostini	✓	✓		✓	JES/R

Key questions:

- Phase space coverage, precisions, sensitivities?
- Which systems are well or not so well described by NLO+PS or NNLO?

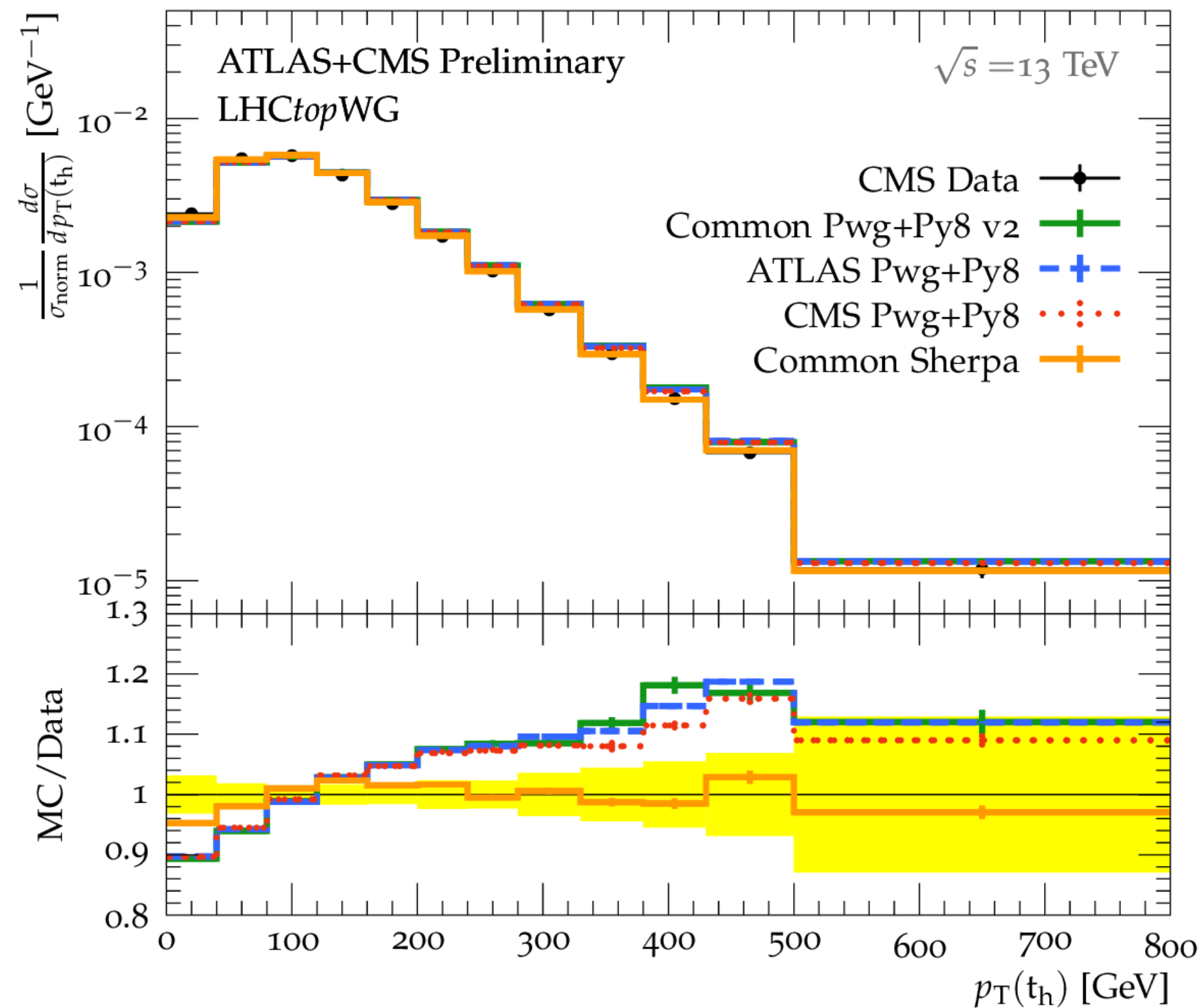
Previous Review in 2020 by M. Romano and O.B.

Models to compare to

All references provided in the ATLAS/CMS papers

- NLO+PS Reference model: POWHEG+PYTHIA (POW)
- Effort towards common ATLAS/CMS $t\bar{t}$ MC settings

ATL-PHYS-PUB-2022-052



- For results today: ATLAS and CMS POW settings different
- ATLAS **also** uses POW with $P_T(t)$ reweighted to NNLO

- Other predictions shown today:

NLO+PS
 $\mathcal{O}(\alpha_s^3)$ or higher

- POWHEG+HERWIG
- MCatNLO+PYTHIA
- MCatNLO+HERWIG
- FFX (based on MC@NLO)
- SHERPA

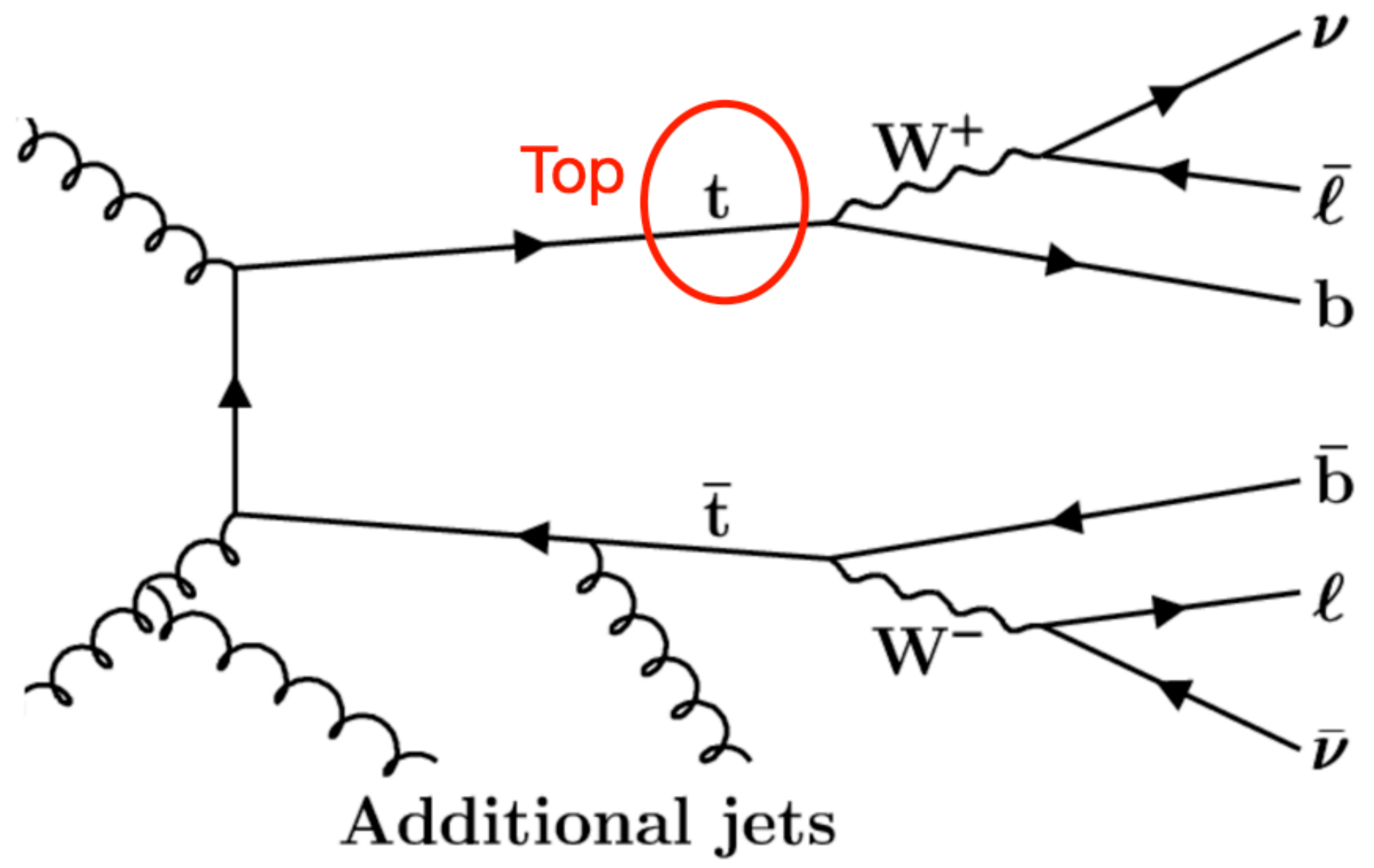
NNLO
 $\mathcal{O}(\alpha_s^4)$ or higher

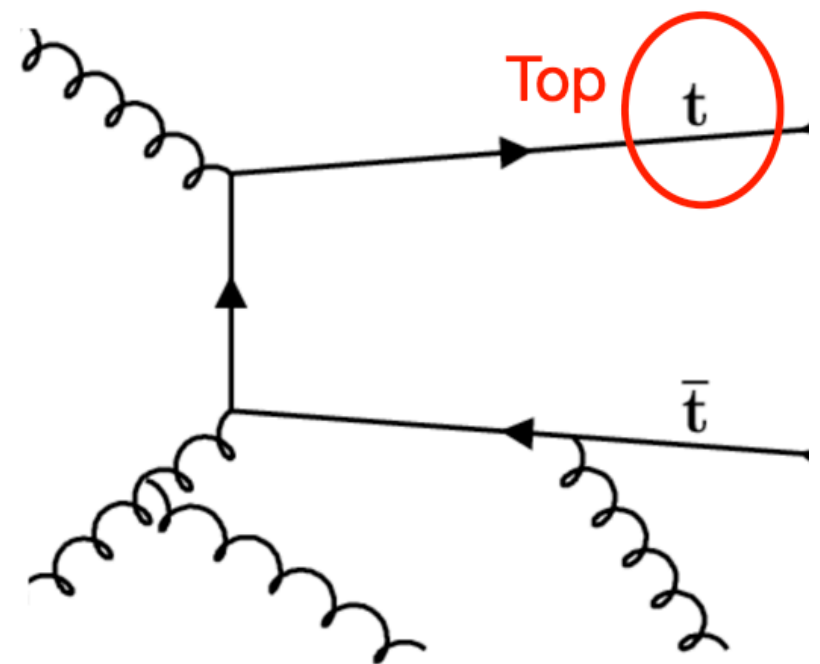
- NNLO (Czakon et al.)
- Stripper (Czakon et al.)
- Matrix (Grazzini et al.)

NNLO+PS
 $\mathcal{O}(\alpha_s^4)$ or higher

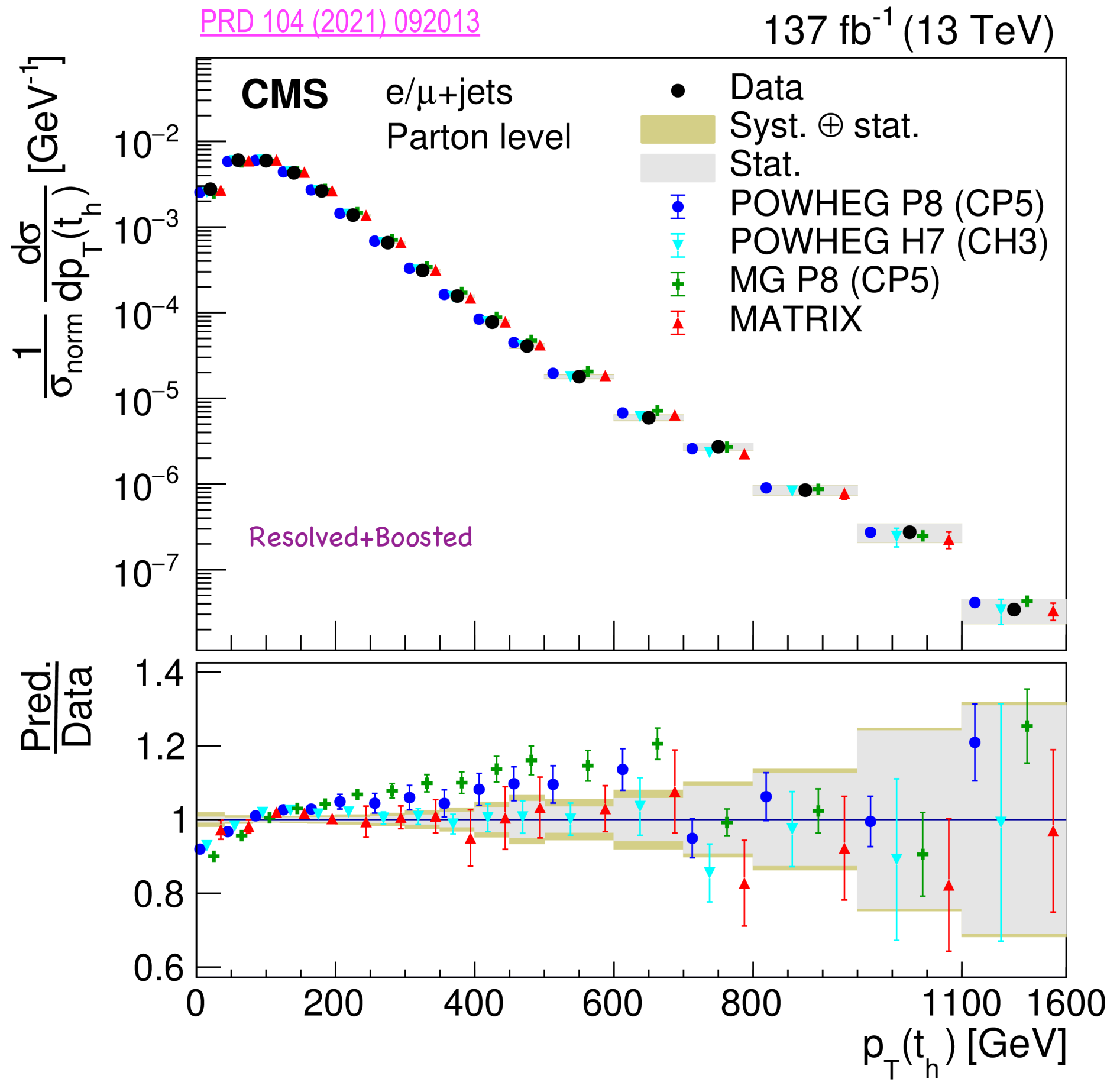
- MINNLOPS (Monni et al.)

Results:





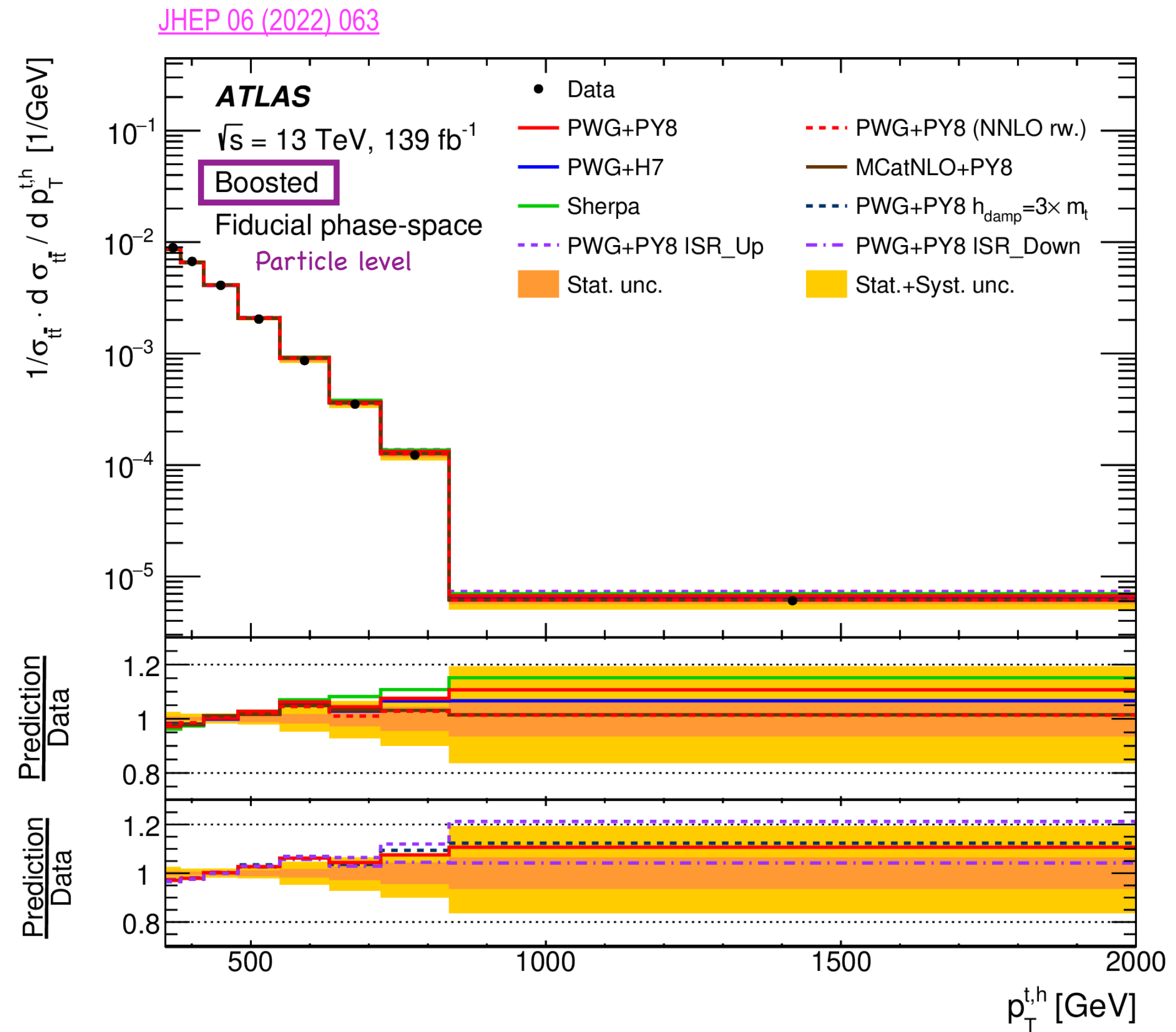
$p_T(t)$



POW/CMS:

NNLO/CMS:

I+jets

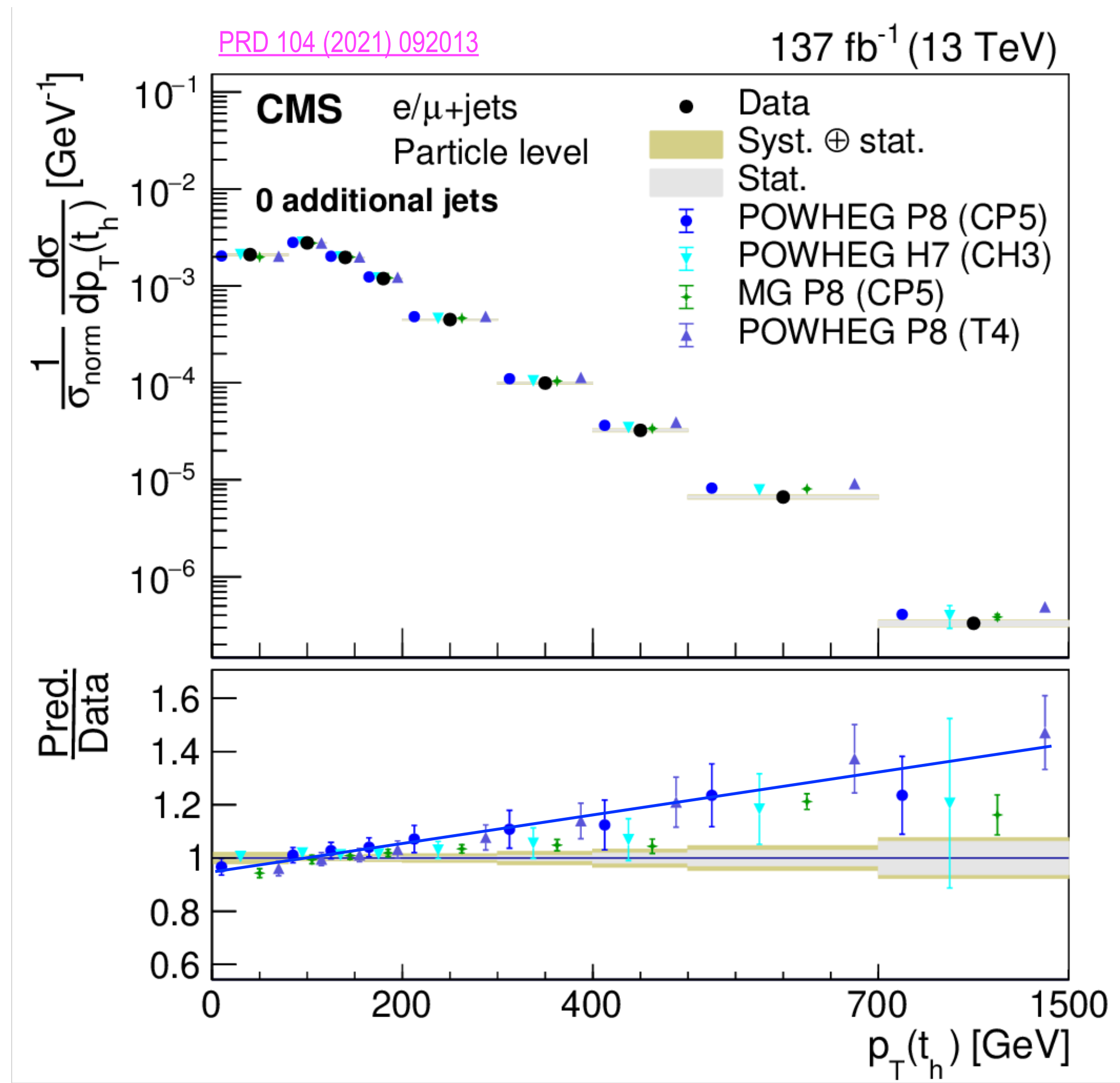


POW/ATLAS:

NNLO rw. POW/ATLAS:

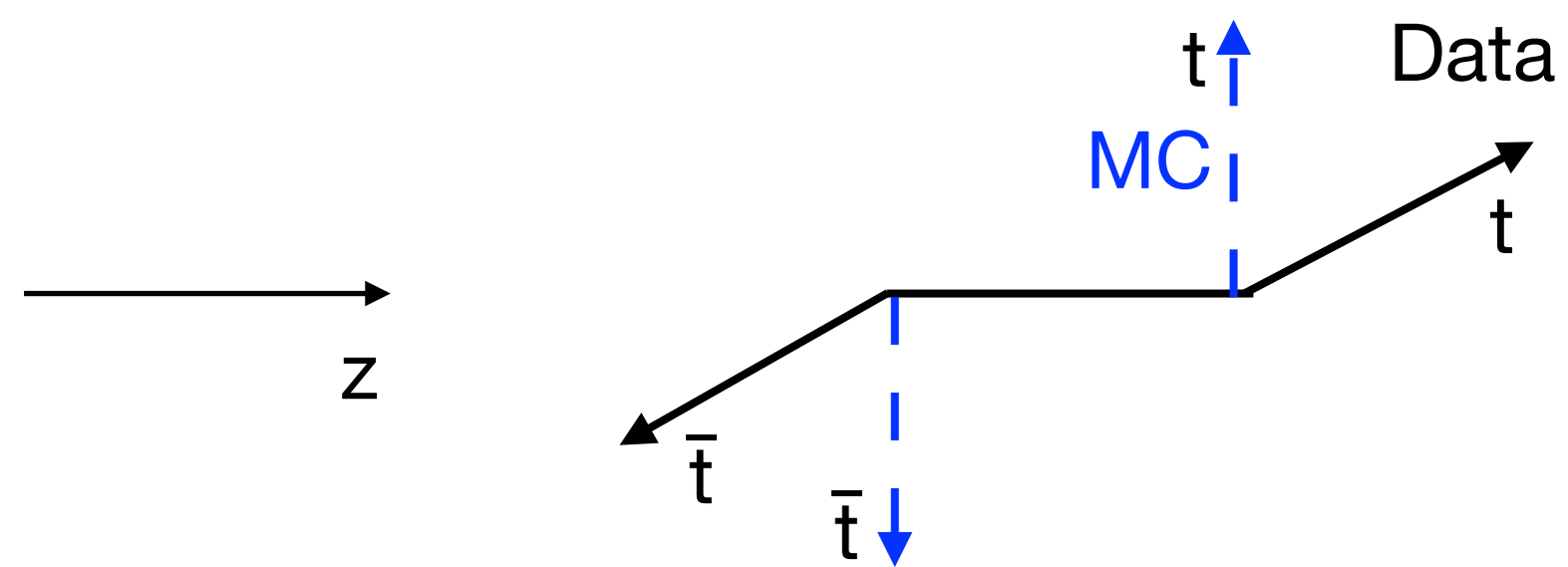
⇒ Known since long time: NNLO improves $p_T(t)$ prediction

“NLO+PS $p_T(t)$ problem” - learn from multi-differential studies



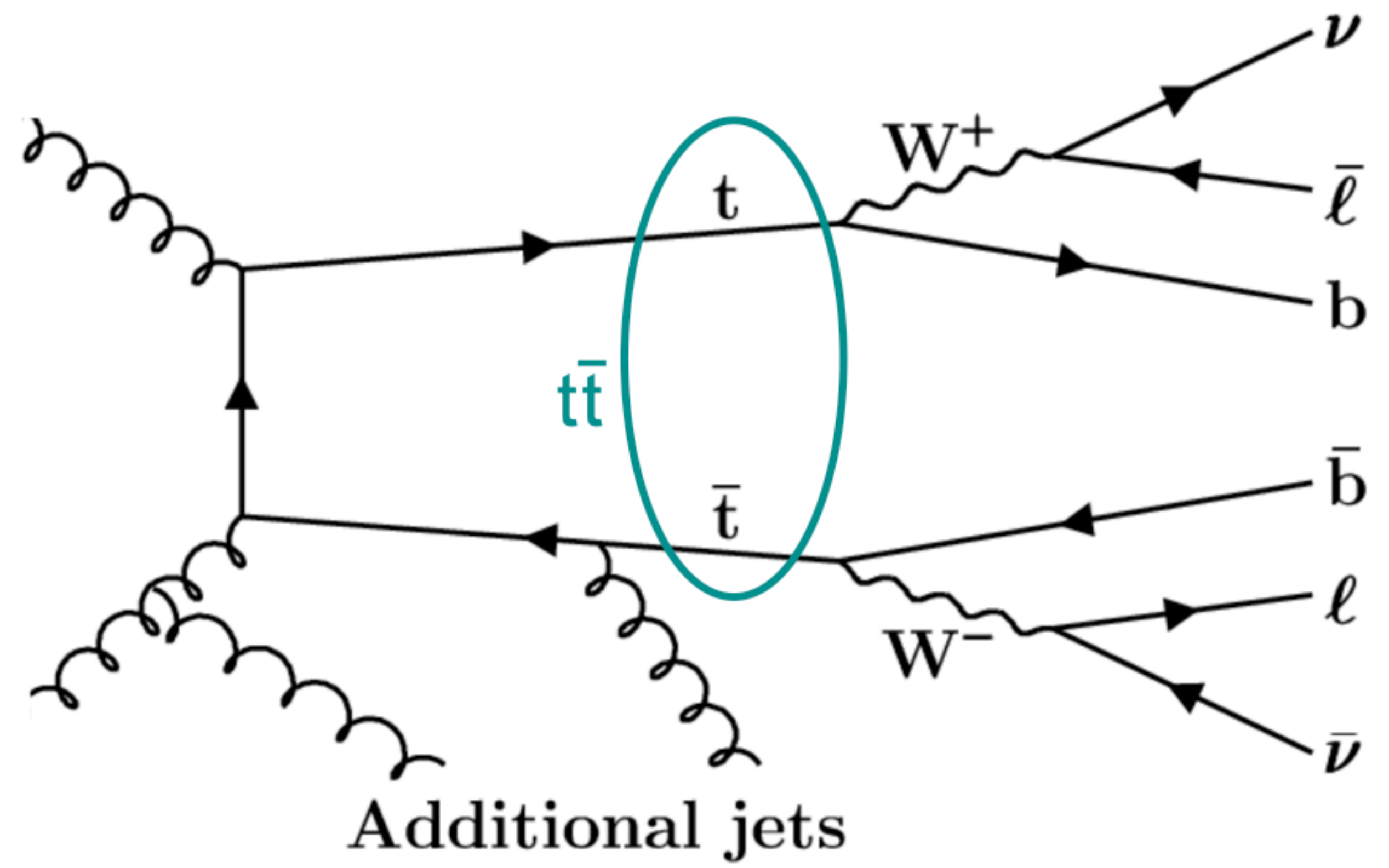
Observations:

- POW/Data $p_T(t)$ slope is
 - Mostly visible for 0 or 1 additional jets, see left Plot
 - Increases with $m(tt)$, see Plot
 - At high $m(tt)$: $\Delta\eta(t, \bar{t})$ larger in data than in MC, see Plot

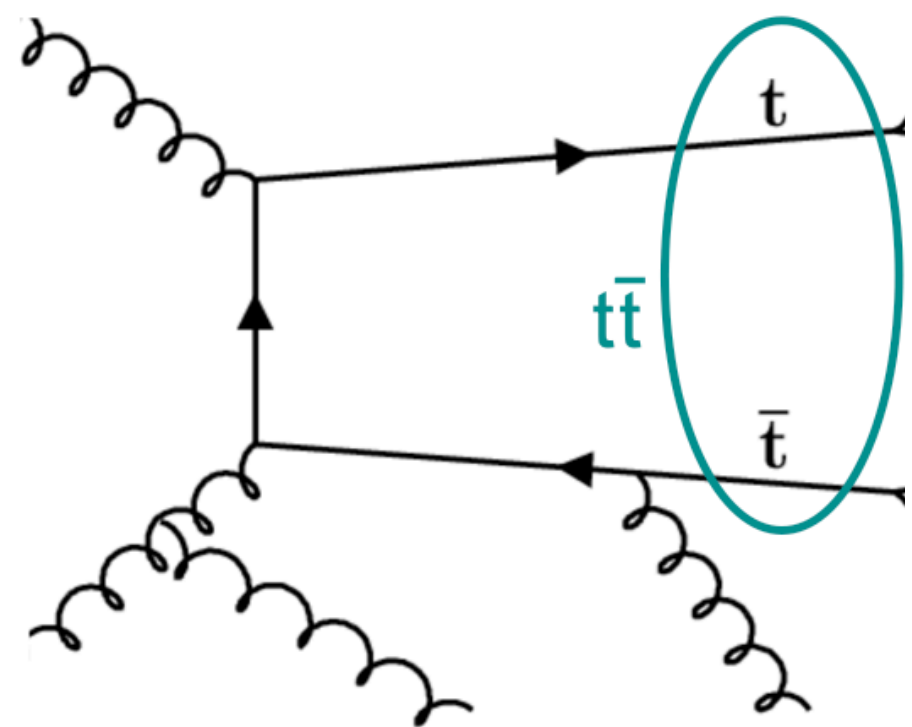


⇒ Do we need further studies?

Results:

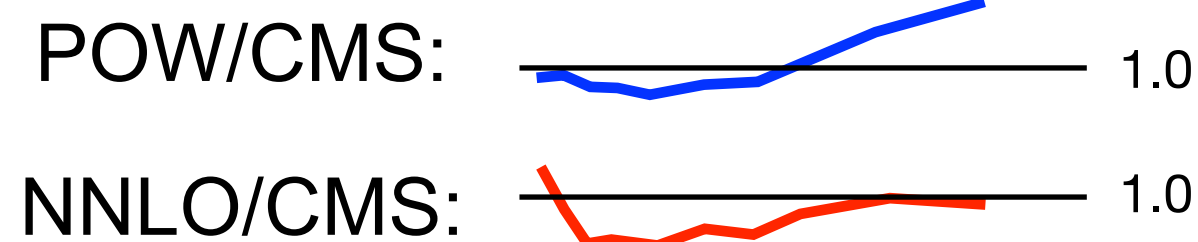
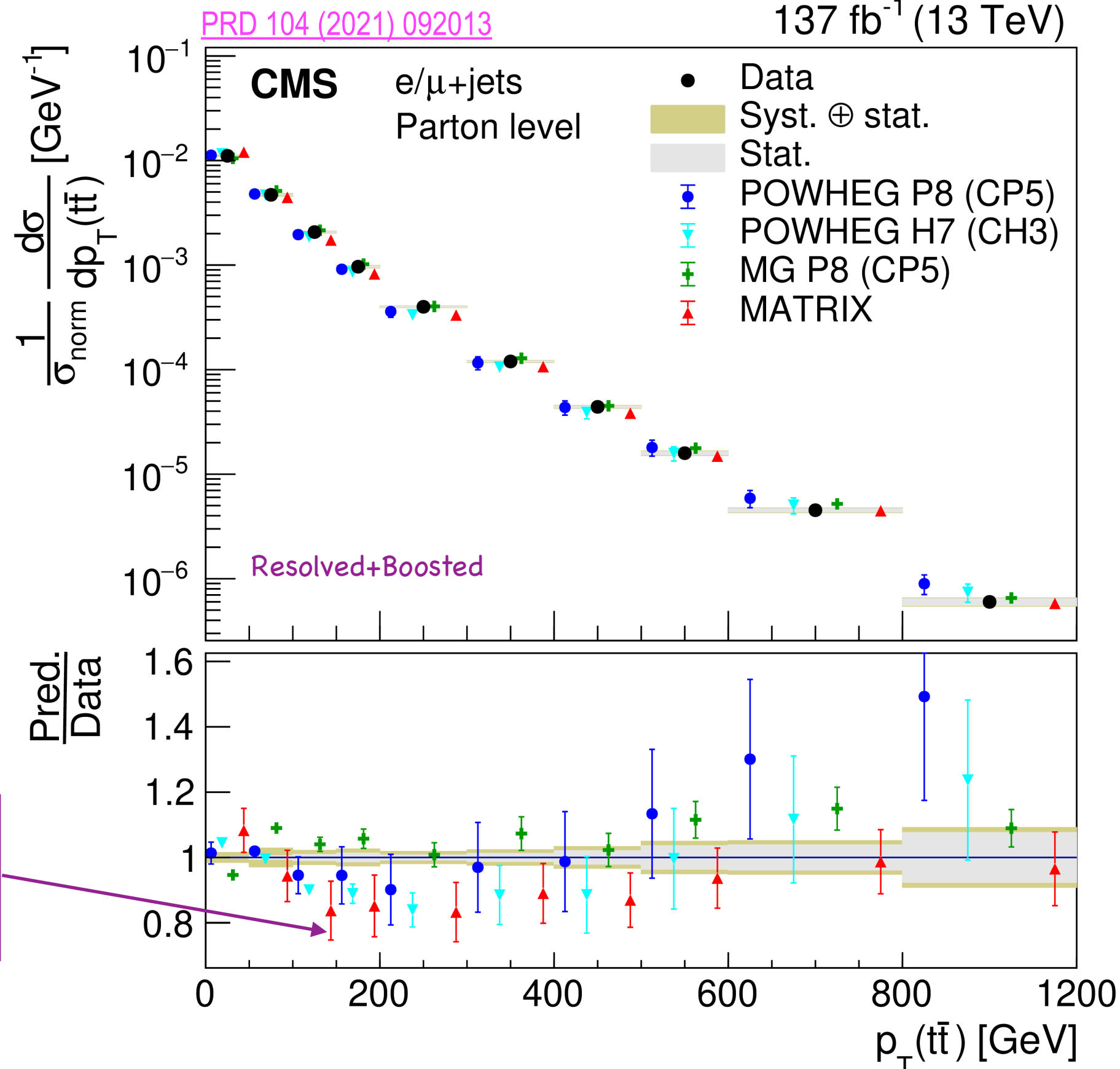


$p_T(t\bar{t})$

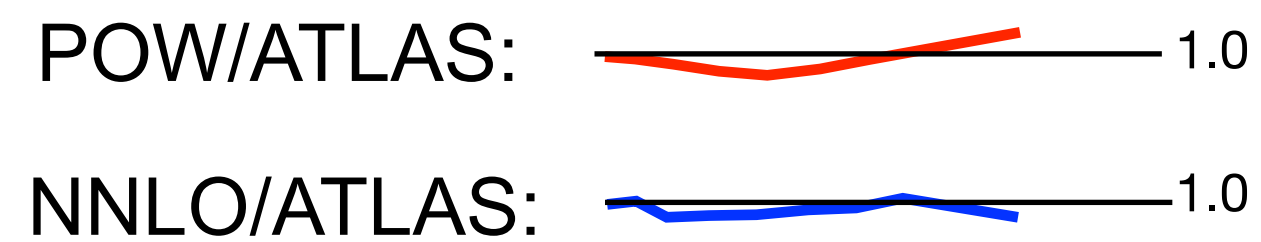
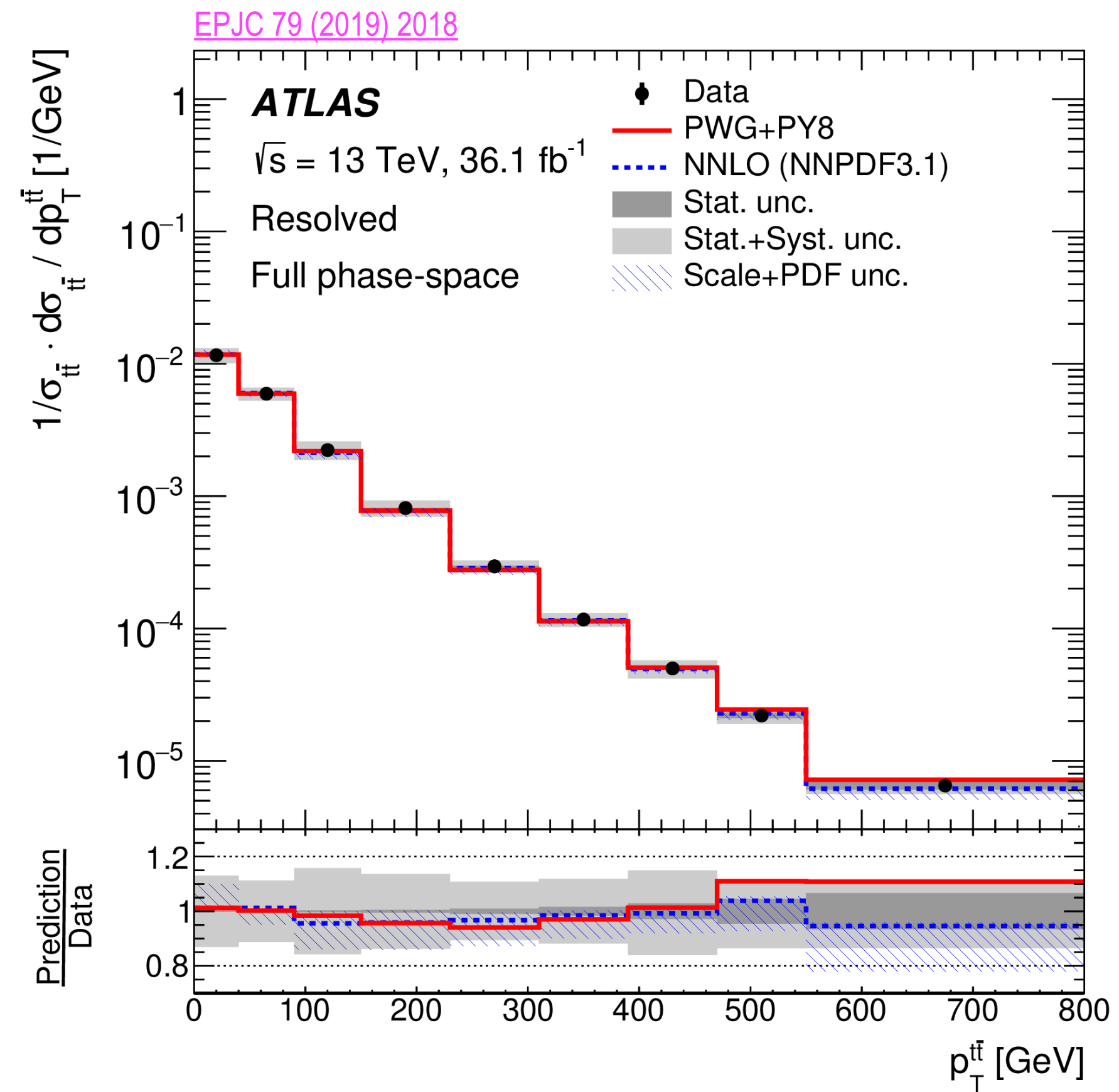


Non-zero $p_T(t\bar{t})$ directly sensitive to NLO QCD

⇒ Large theory scale Uncertainties

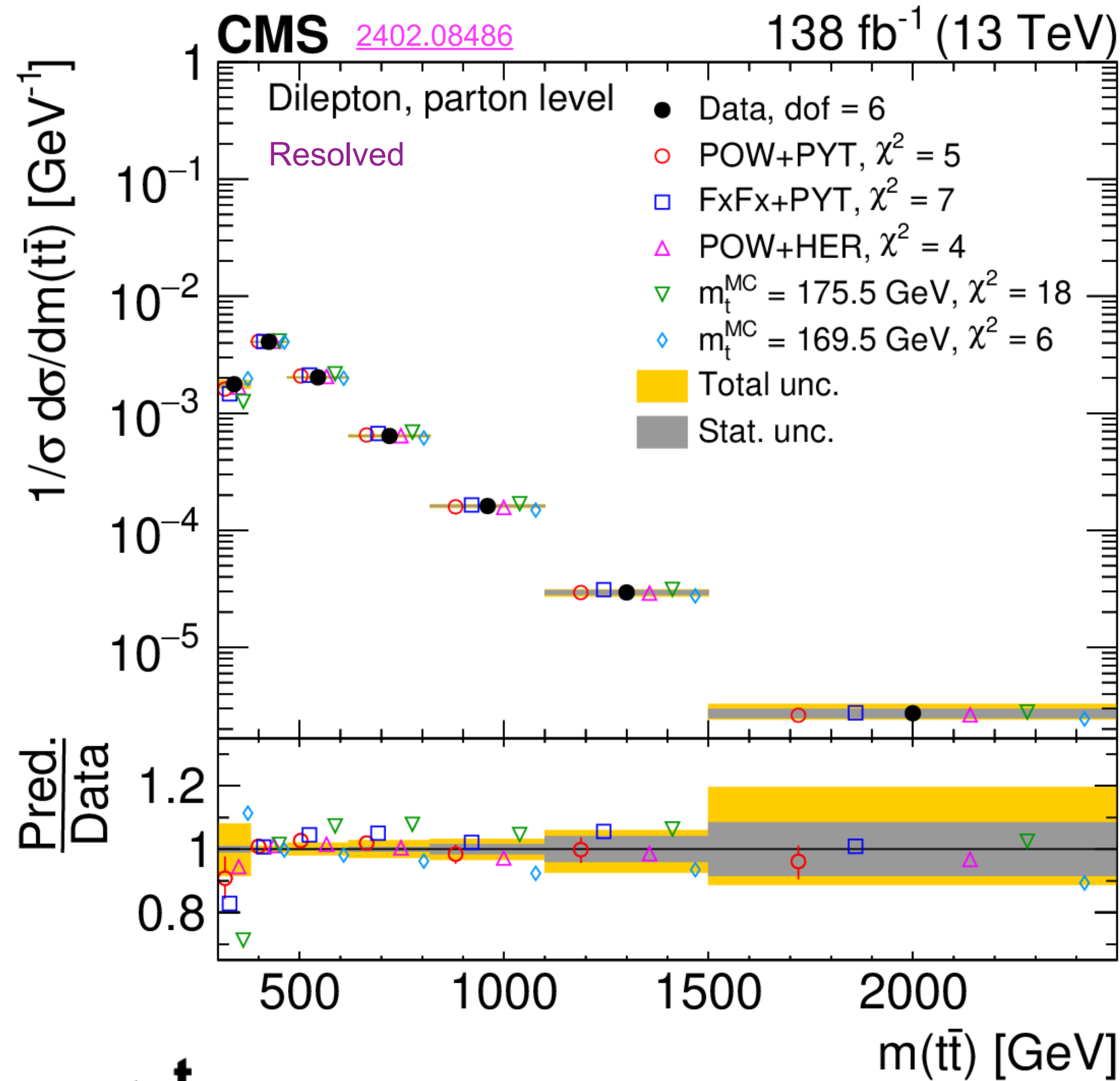


I+jets, Parton level

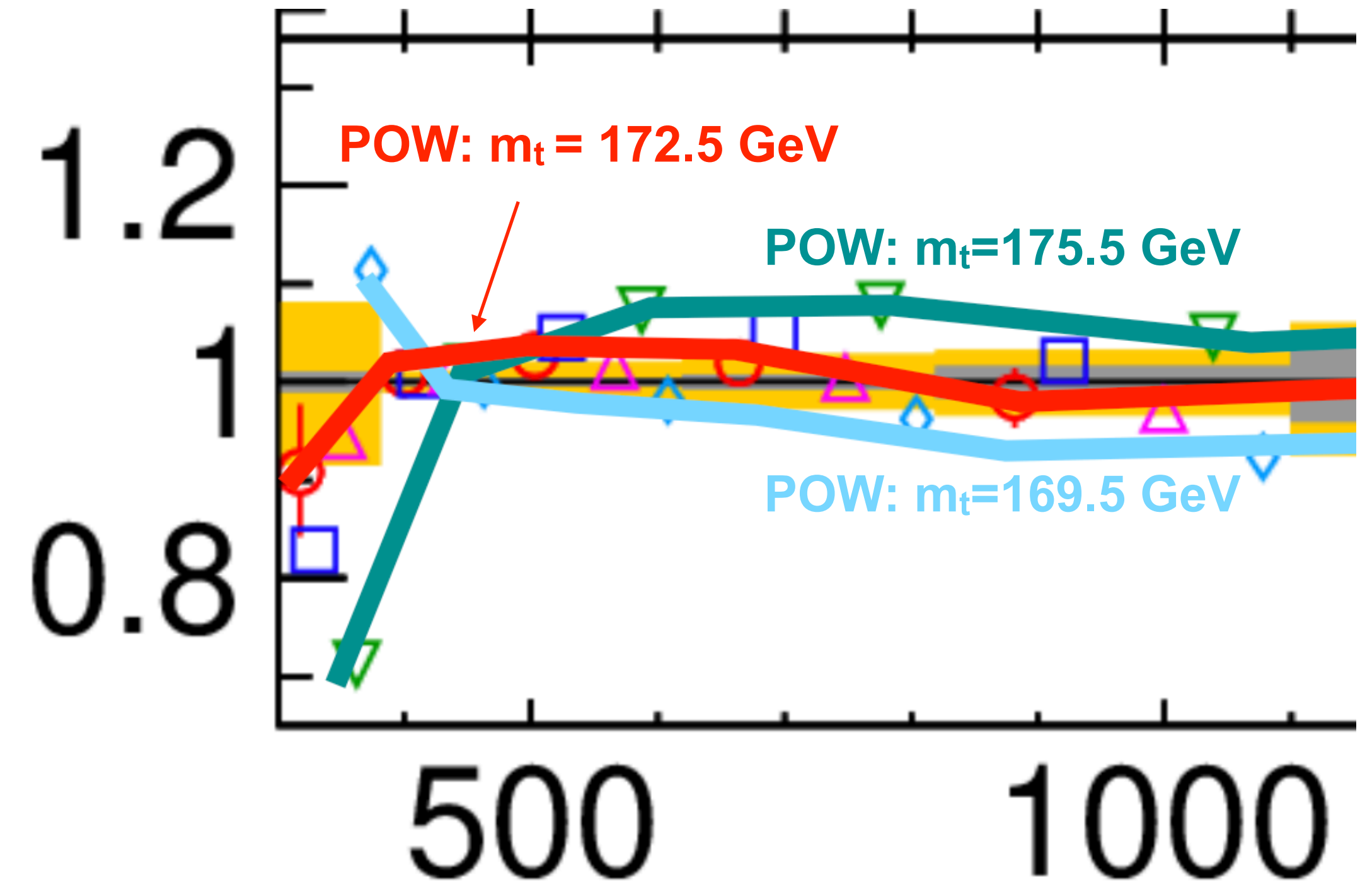


⇒ Both NNLO and POW exhibit some wiggles around the data
⇒ **Need NNNLO**

$m(t\bar{t})$

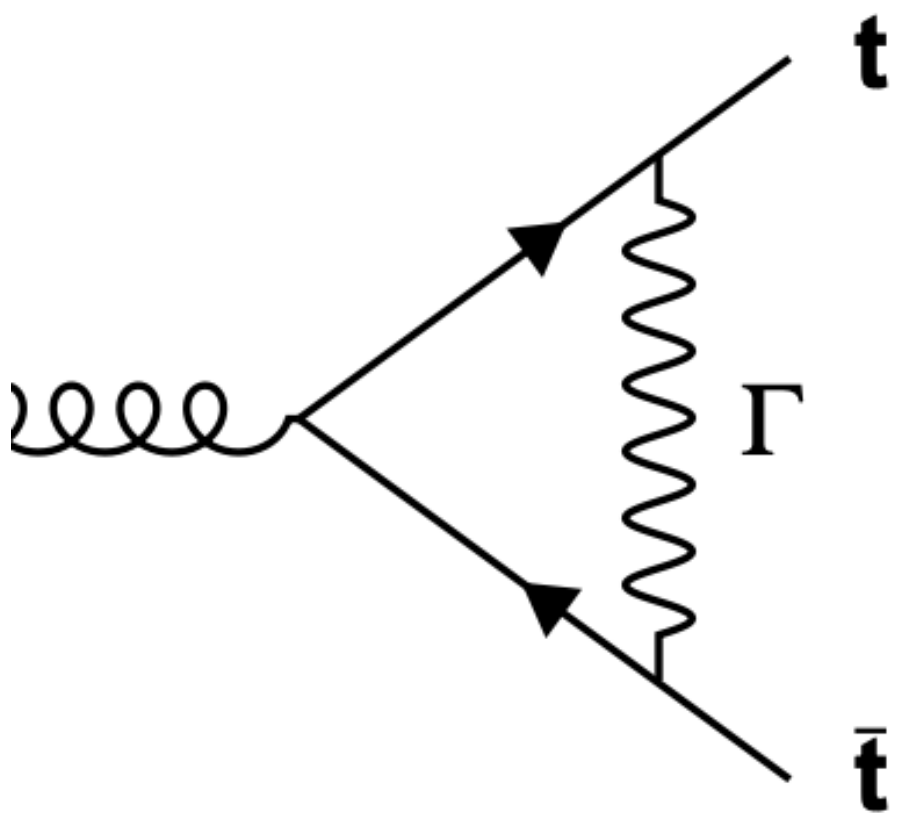


Zoom in $m(t\bar{t})$ threshold Region:



$\Rightarrow \sim \mathcal{O}(1 \text{ GeV})$ sensitivity to top quark mass

See [2403.01313](#) for an overview of m_t measurement techniques



$m(t\bar{t})$ near $2 \cdot m_t$ threshold sensitive to:

- m_t ← Let's focus on
- Top Yukawa coupling
- Soft/virtual gluons
- Toponium



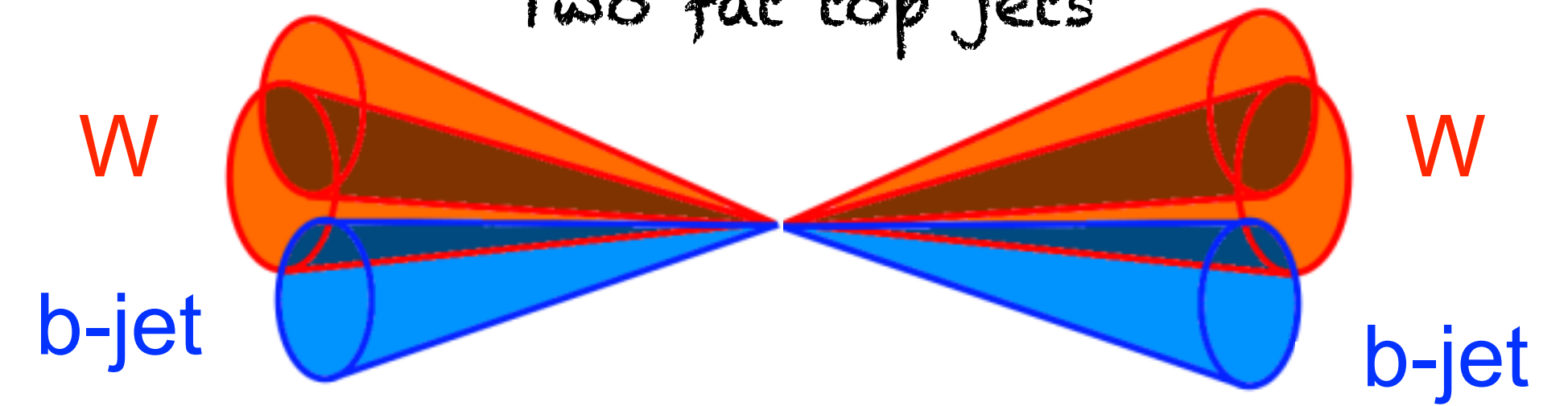
ATLAS



$m(t\bar{t})$

All had, Boosted
 $P_T(t_1) > 500$ GeV, $P_T(t_2) > 350$ GeV

Two fat top jets



⇒ Exploring masses up to 4 TeV
⇒ Reasonable description by NLO+PS MCs

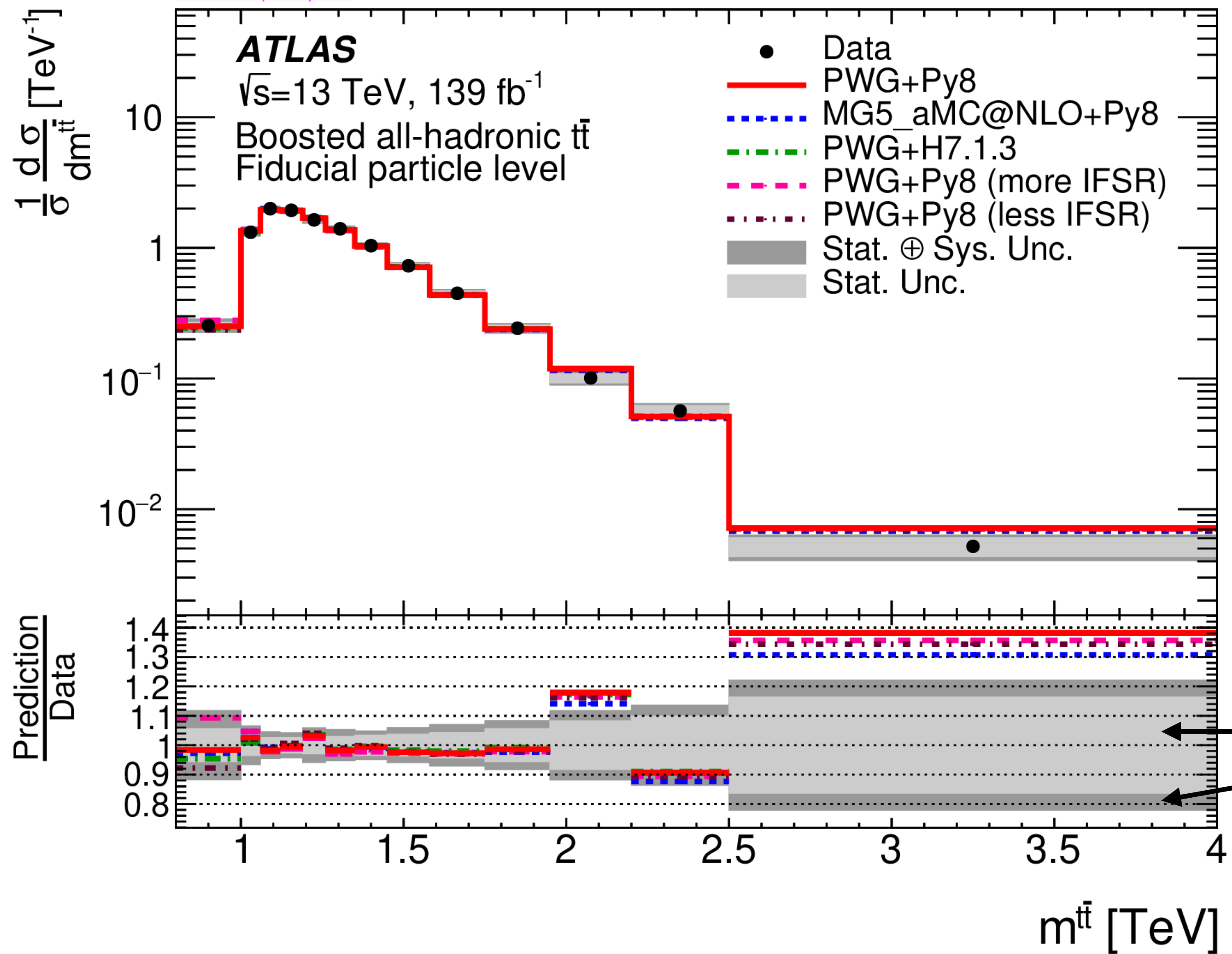
Dominant uncertainties:
• Statistical
• Boosted Top Tagger efficiencies

JHEP 04 (2023) 080

ATLAS

$\sqrt{s} = 13$ TeV, 139 fb⁻¹
Boosted all-hadronic $t\bar{t}$
Fiducial particle level

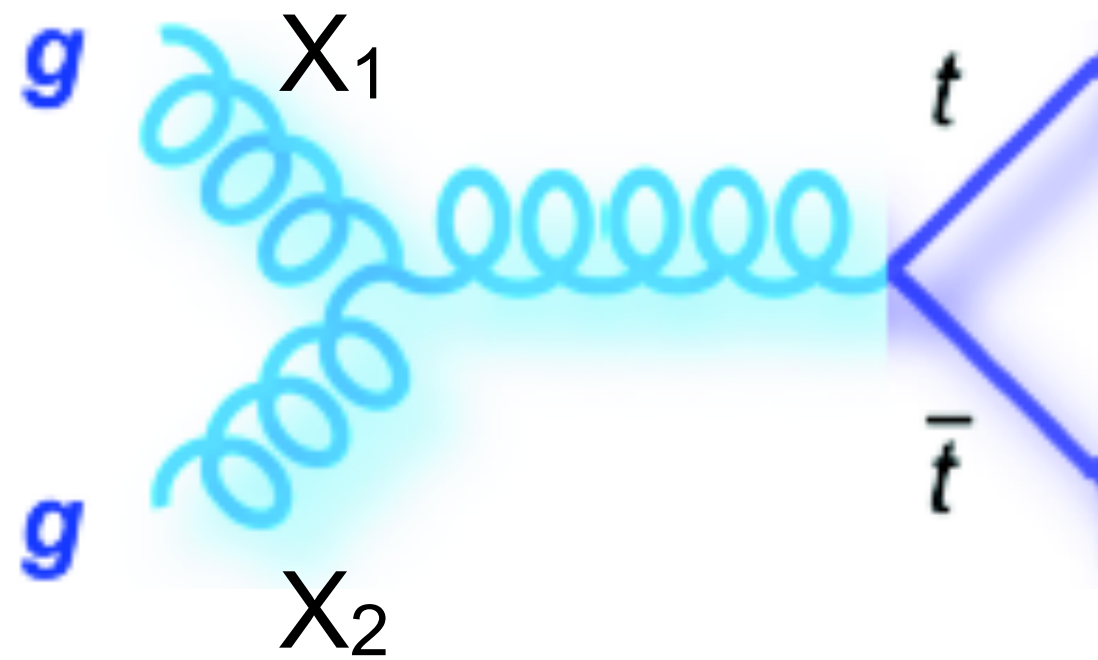
- Data
- PWG+Py8
- - - MG5_aMC@NLO+Py8
- · - · PWG+H7.1.3
- · - · PWG+Py8 (more IFSR)
- · - · PWG+Py8 (less IFSR)
- Stat. ⊕ Sys. Unc.
- Stat. Unc.



$y(t\bar{t})$

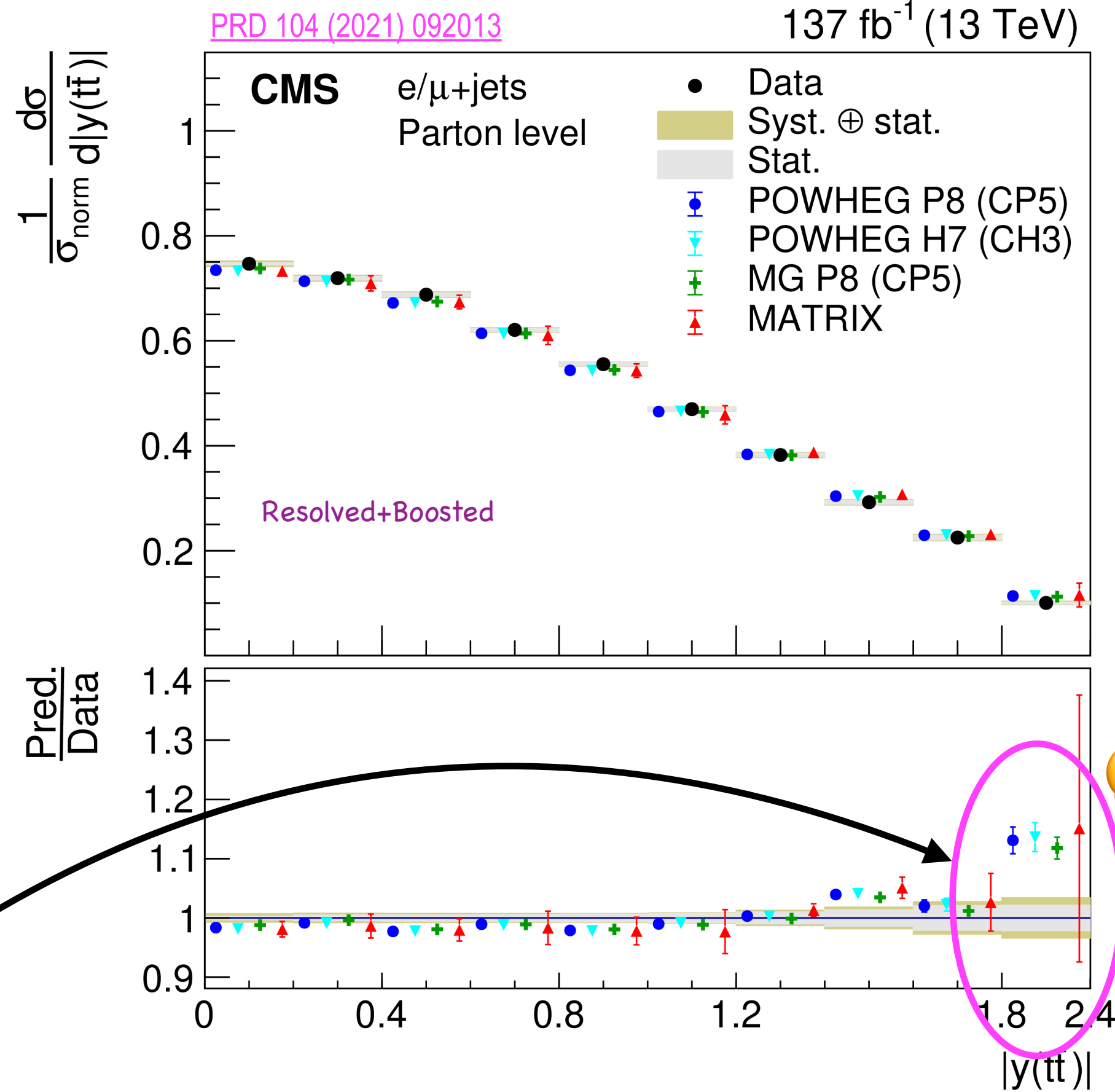
I+jets, Parton level

LO picture:

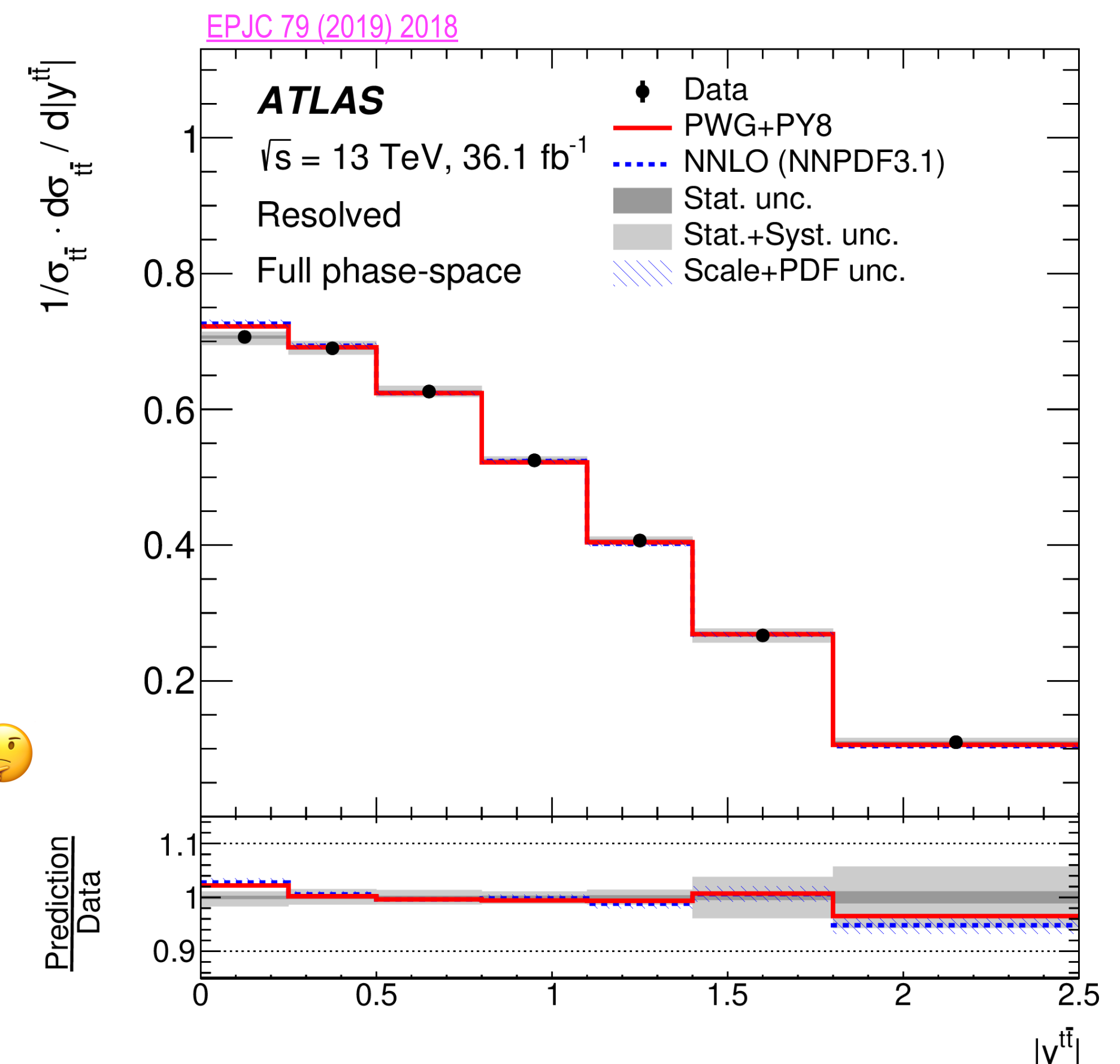
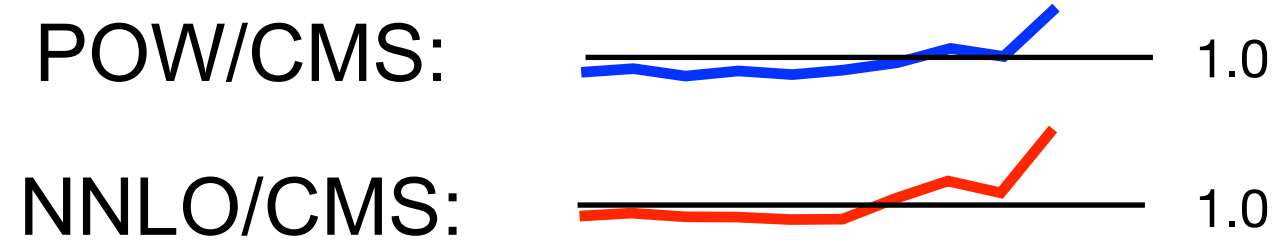


$$\ln\left(\frac{x_1}{x_2}\right) = 2 \cdot y(t\bar{t})$$

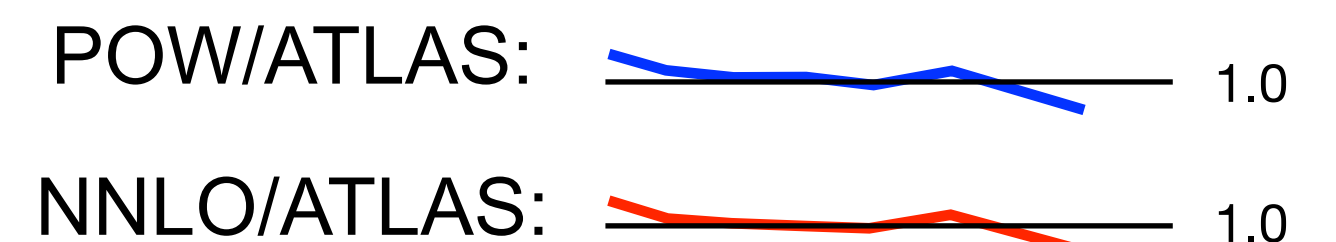
→ at high positive $y(t\bar{t})$
 probing large x_1
 ⇒ sensitive to $g(x)$



Pred.
Data



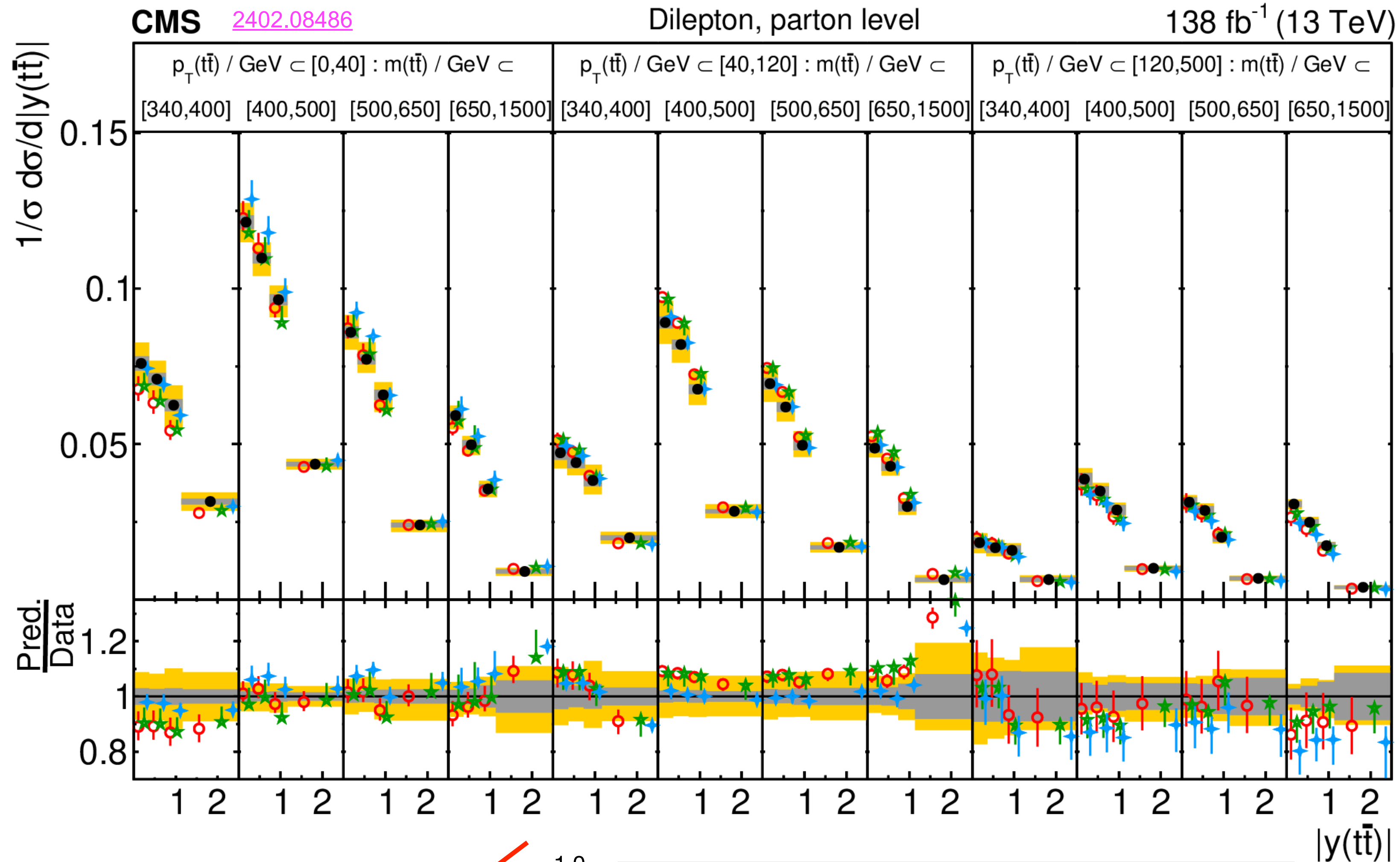
Prediction
Data



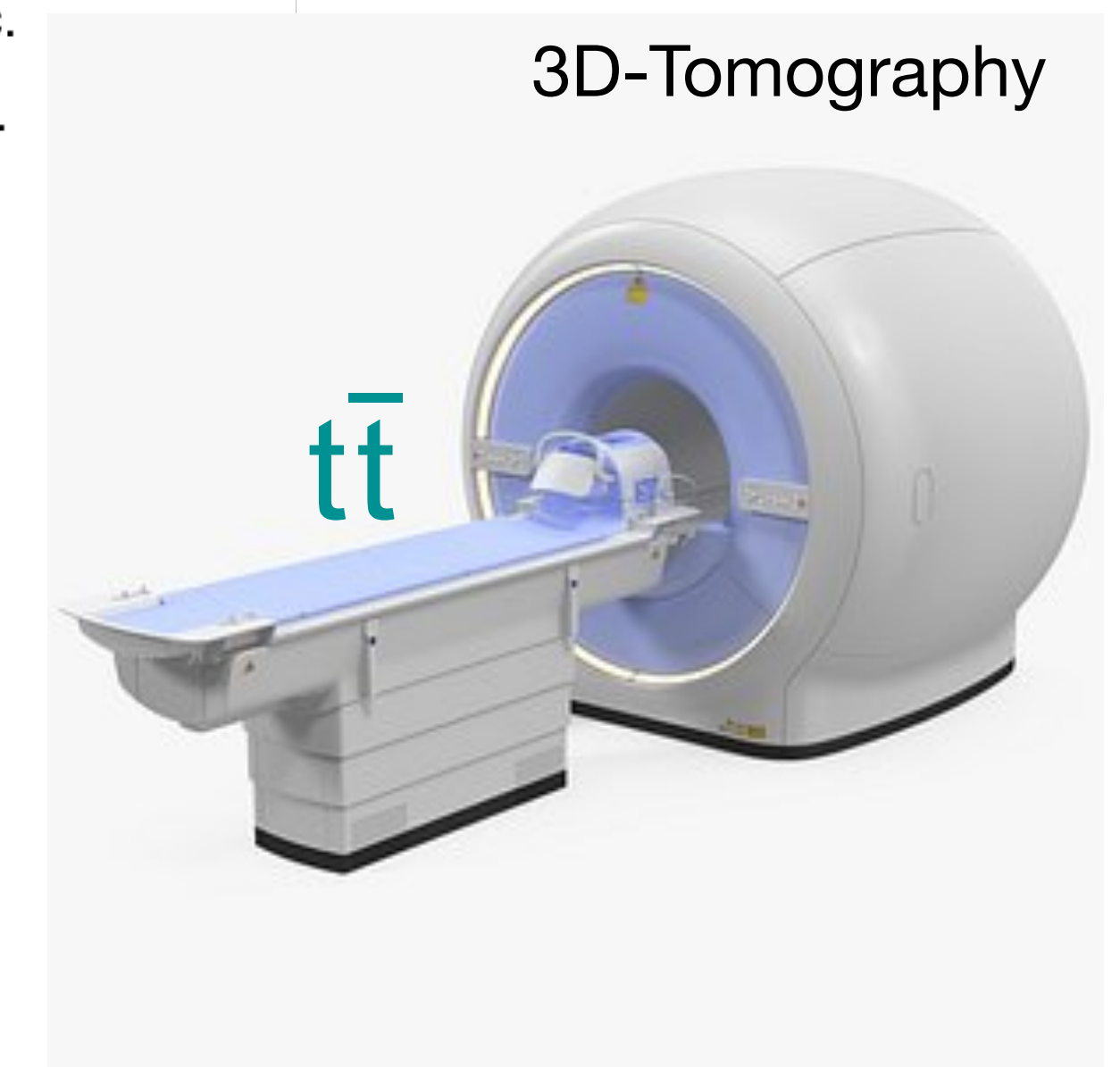
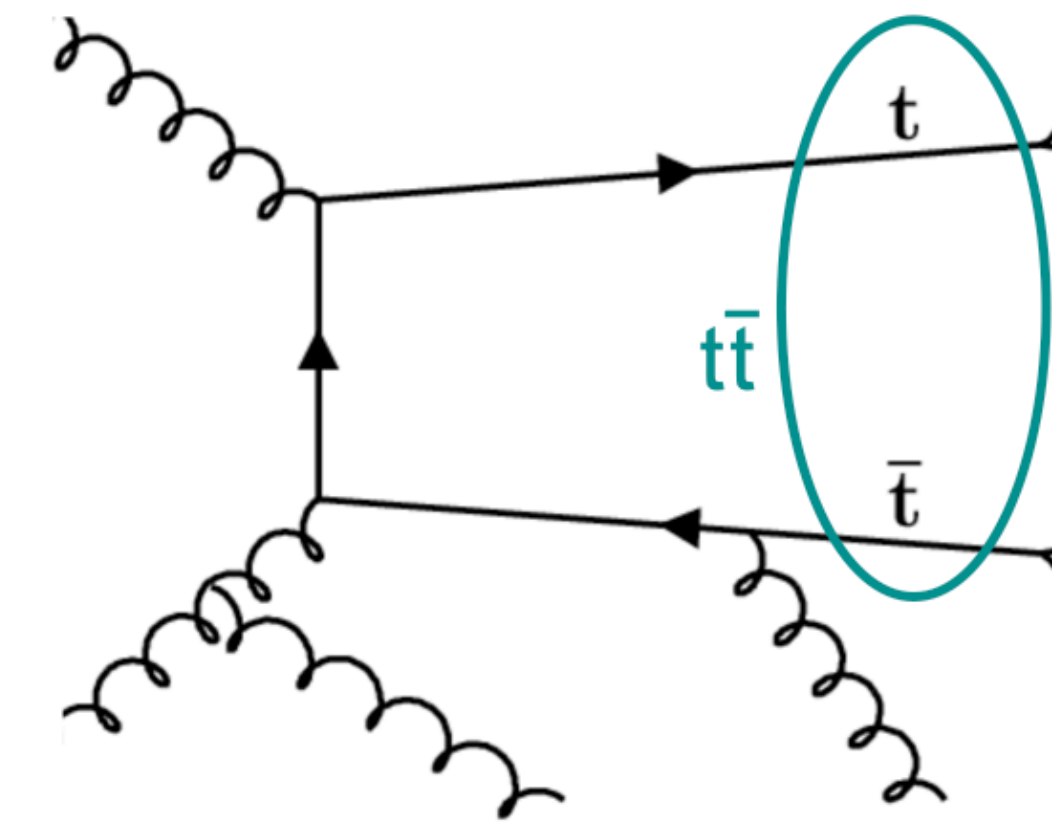
⇒ POW/NNLO describe Data mostly within 2% ⇒ Reasonable description

Dilepton,
Parton level,
Resolved

$y(t\bar{t})$ vs $m(t\bar{t})$ vs $p_T(t\bar{t})$



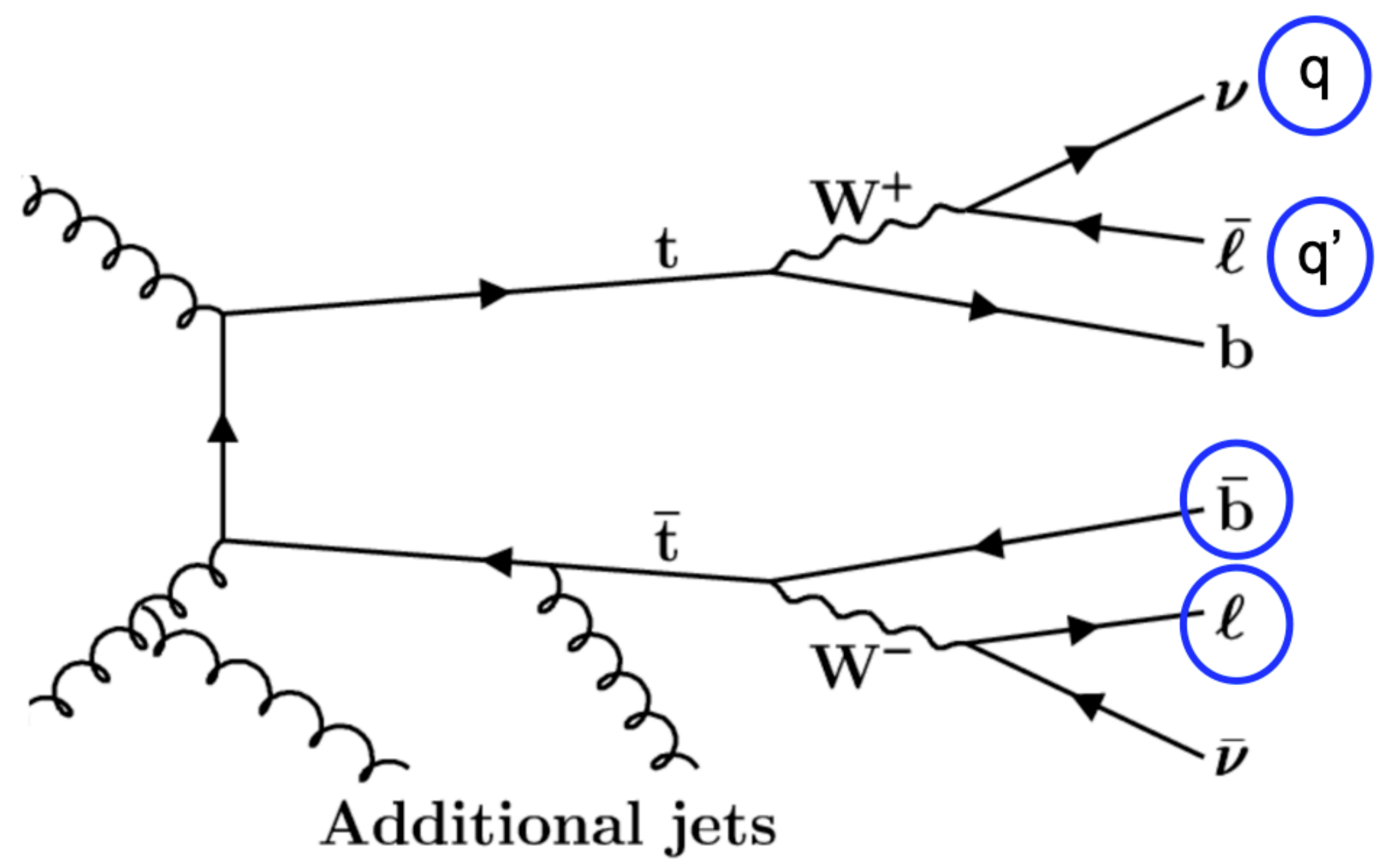
Example $y(t\bar{t})$ distribution at small $p_T(t\bar{t})$, large $m(t\bar{t})$
 POW/CMS positive slope



⇒ For all models: clearly some local trends visible vs Data

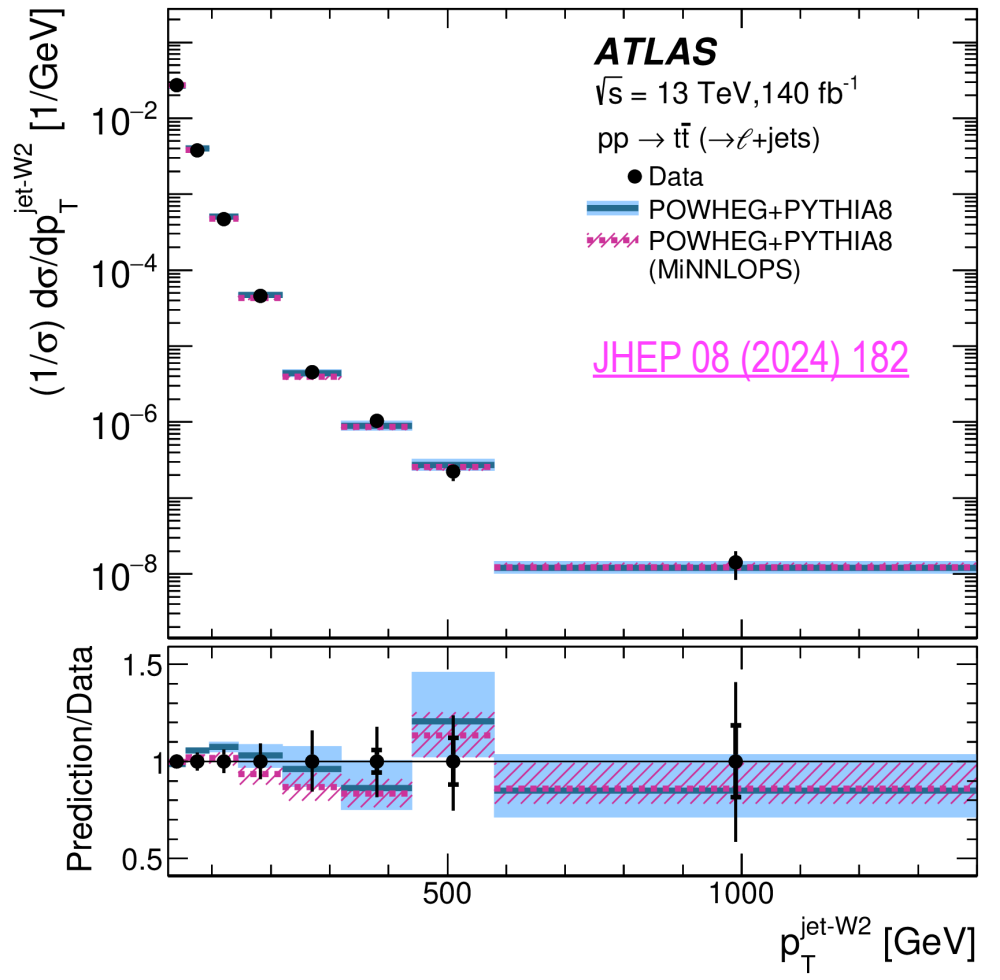
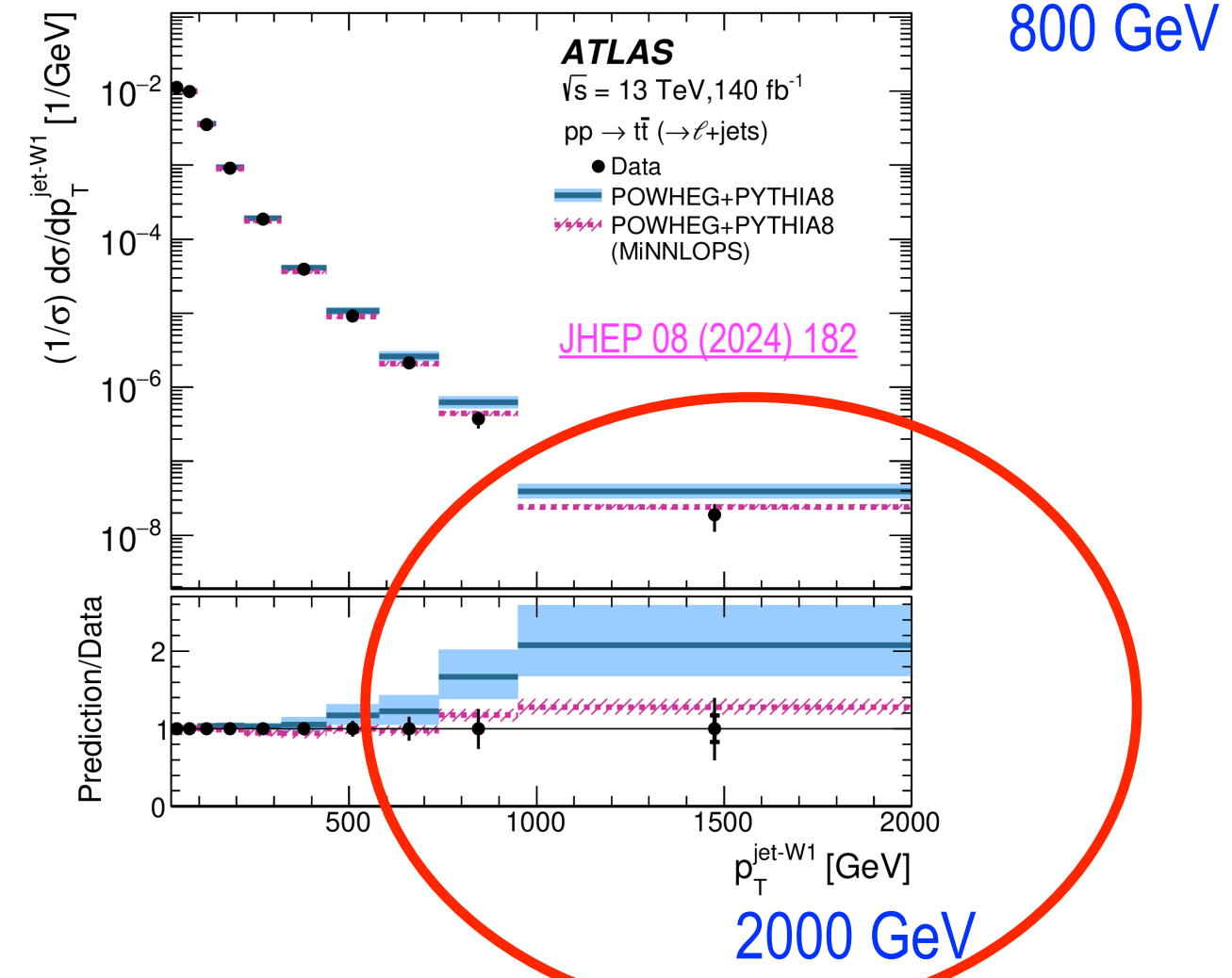
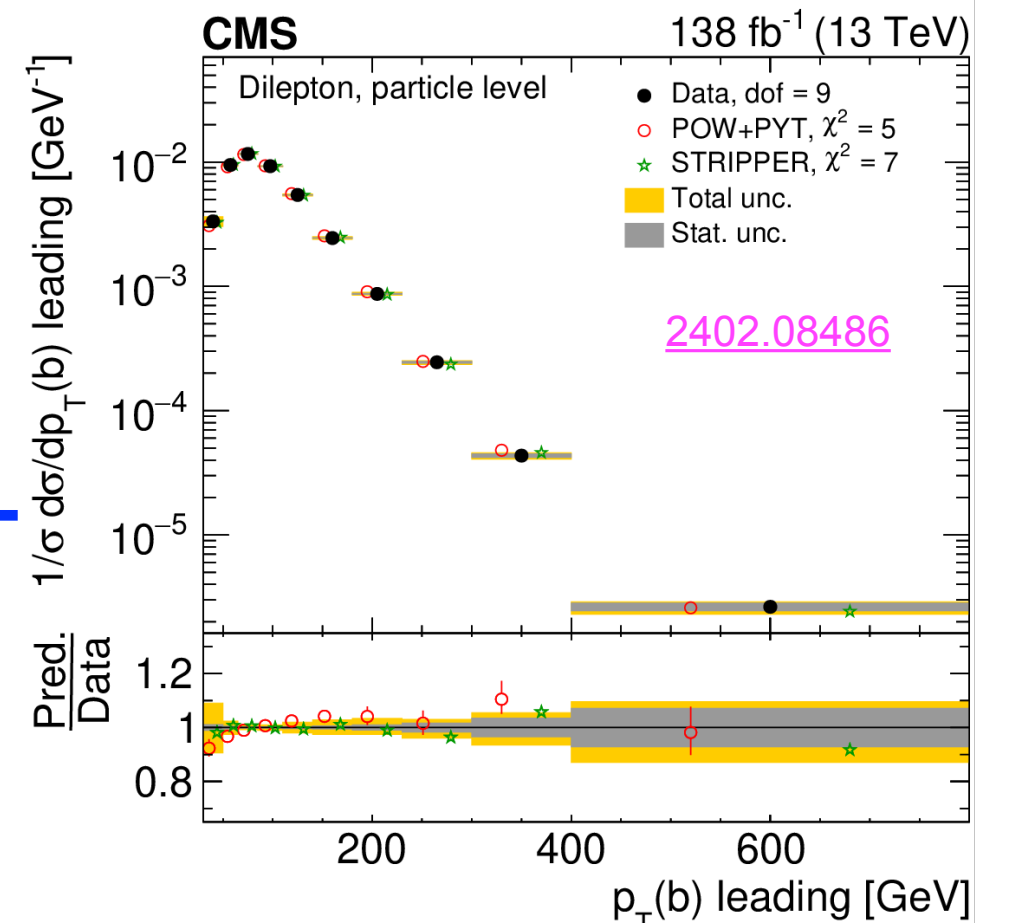
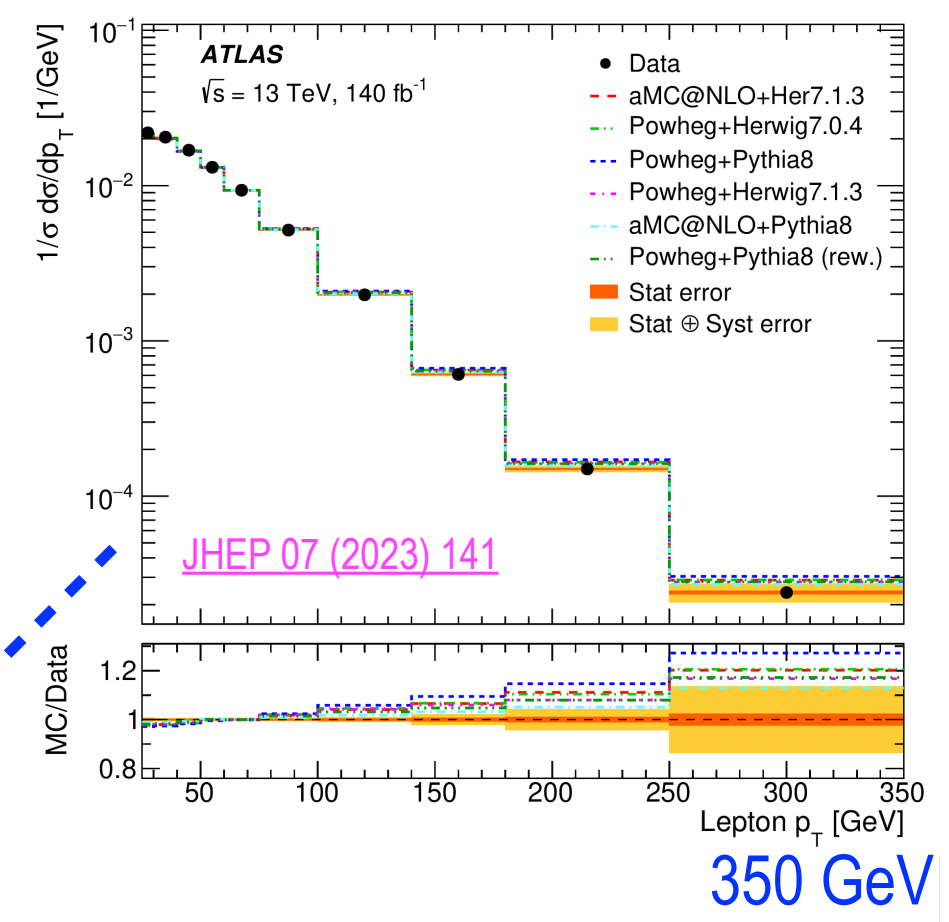
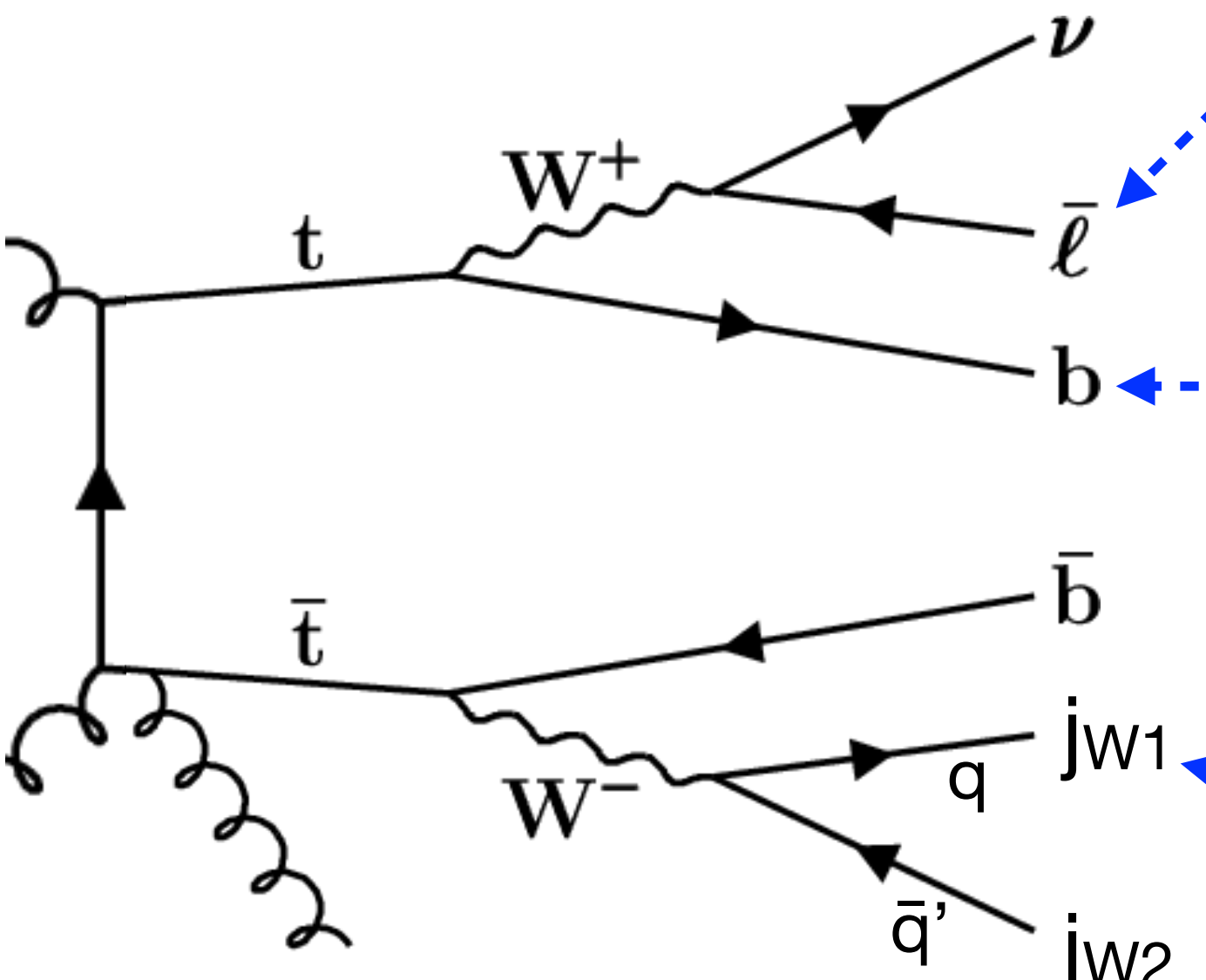
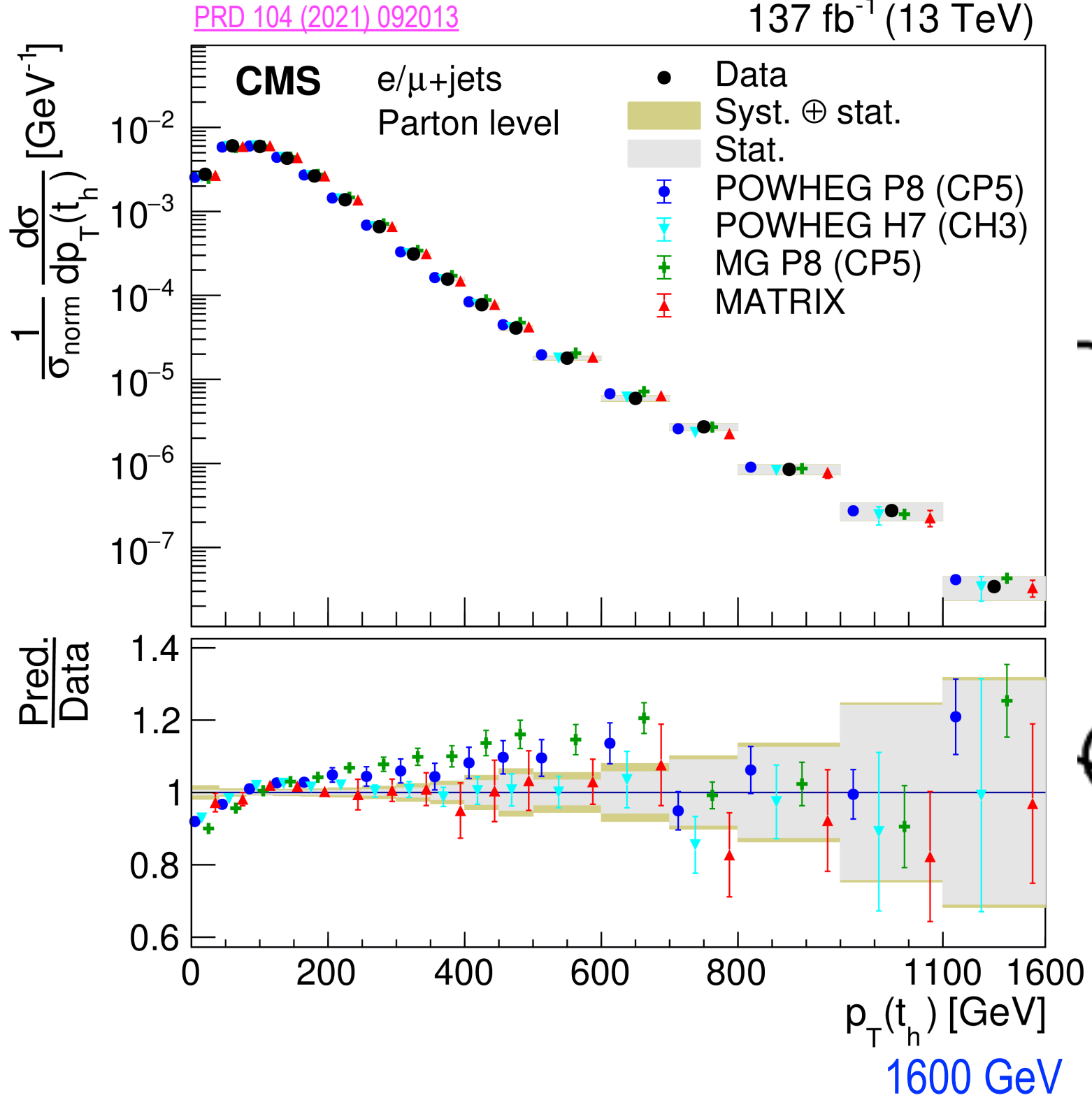
Results:

Decay particles: l, b, q, q'



Probing dynamics of $t\bar{t}$ production * decay

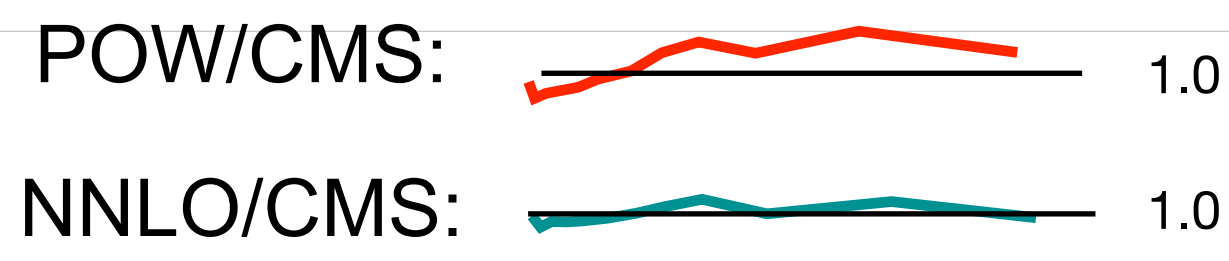
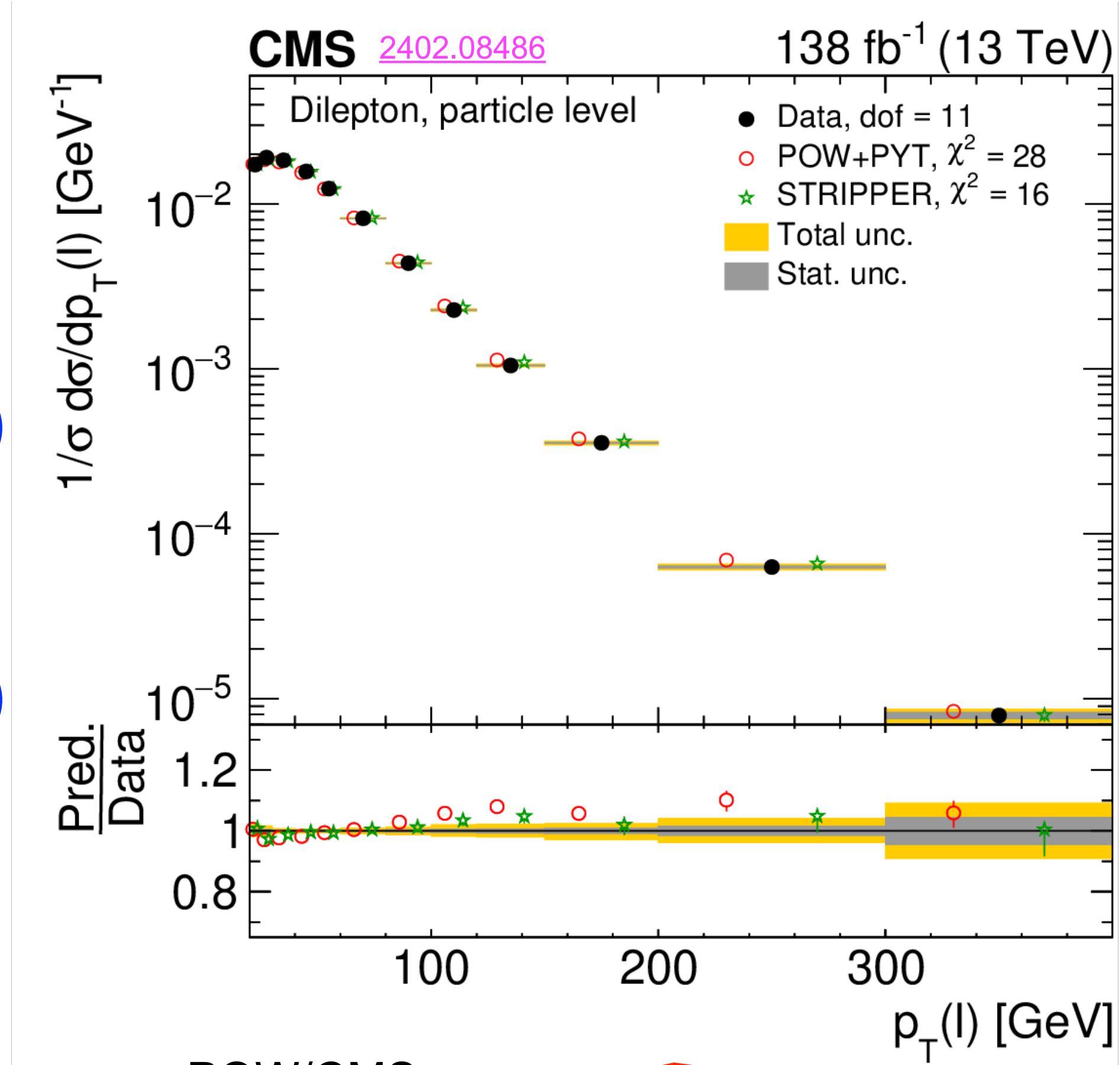
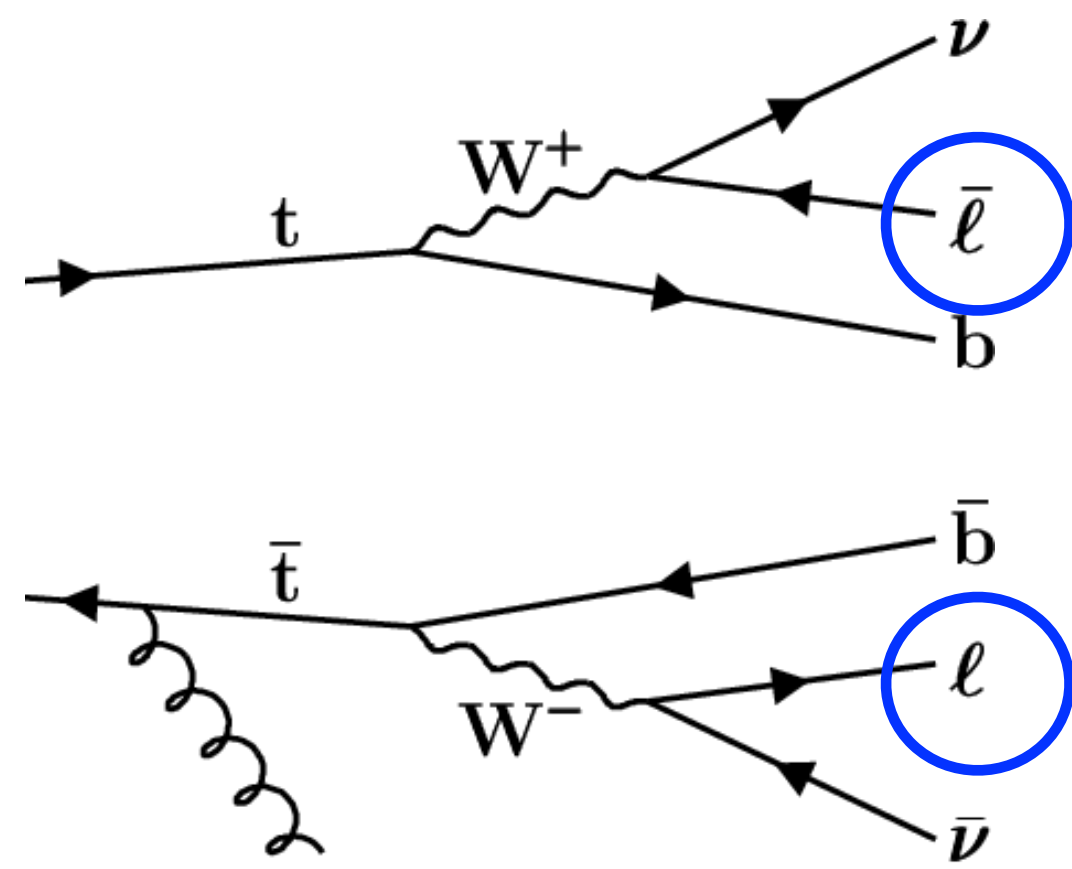
p_T of top and daughter particles



⇒ All particles inherit top **positive** Pow/data P_T slope except j_{W2}

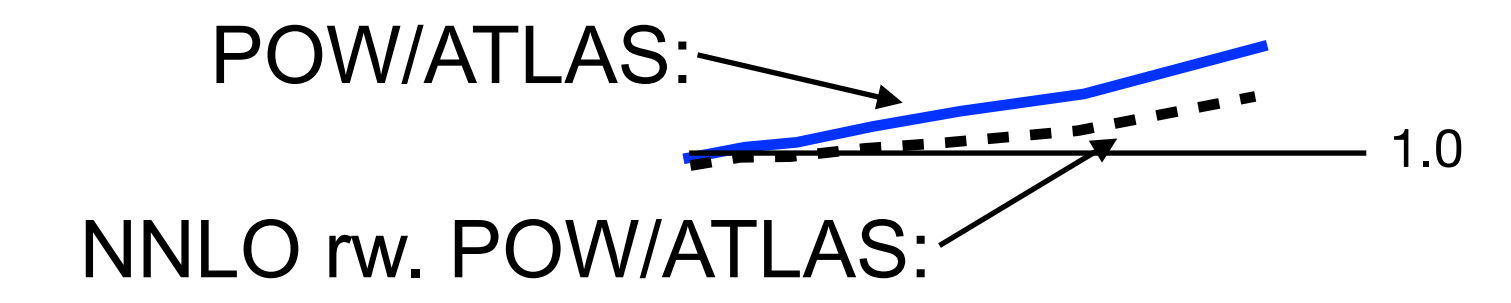
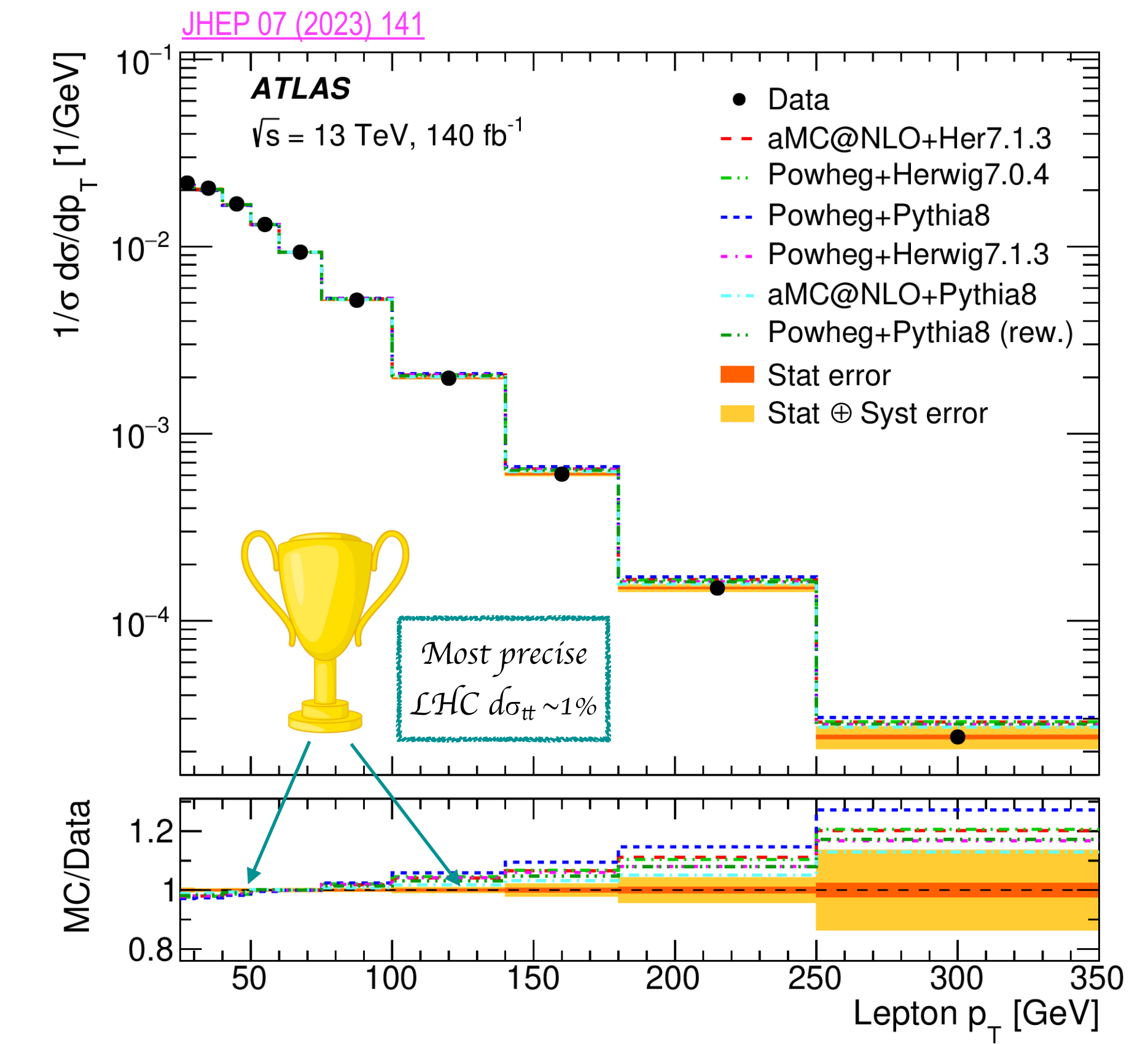
Should do more such high jet p_T analyses!

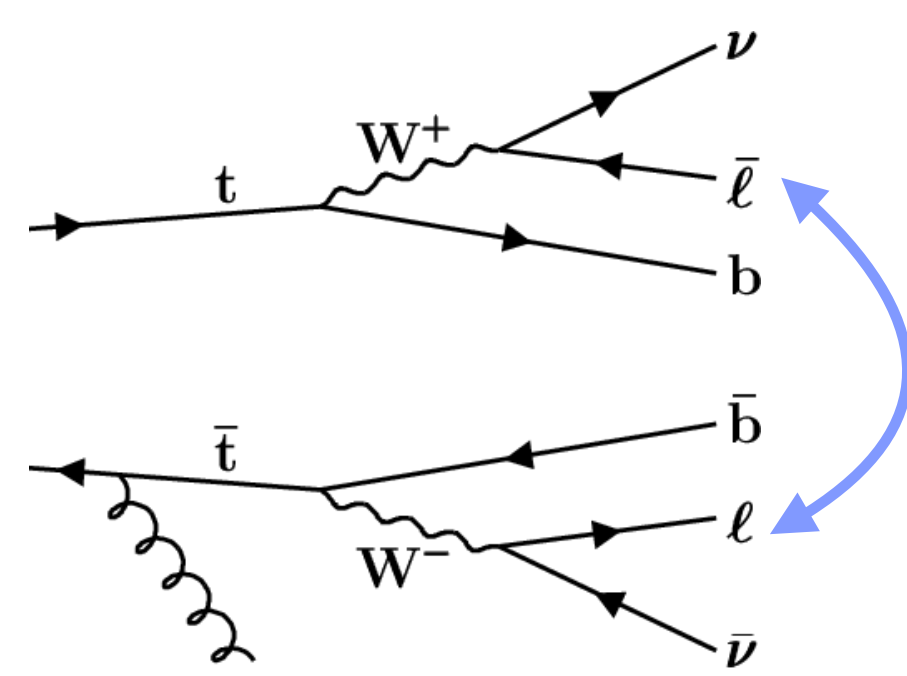
$p_T(l)$



⇒ NNLO seems to improve the description

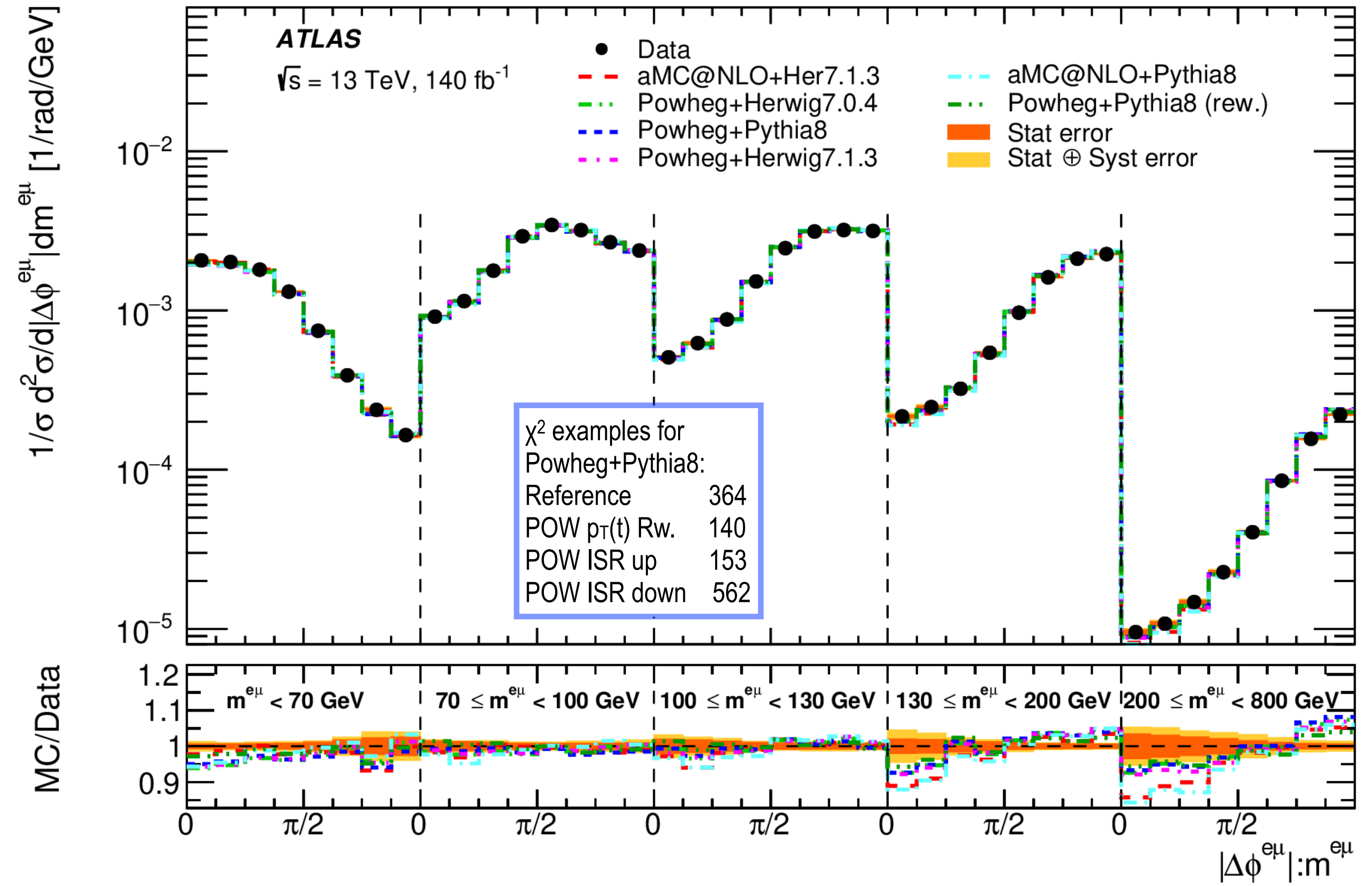
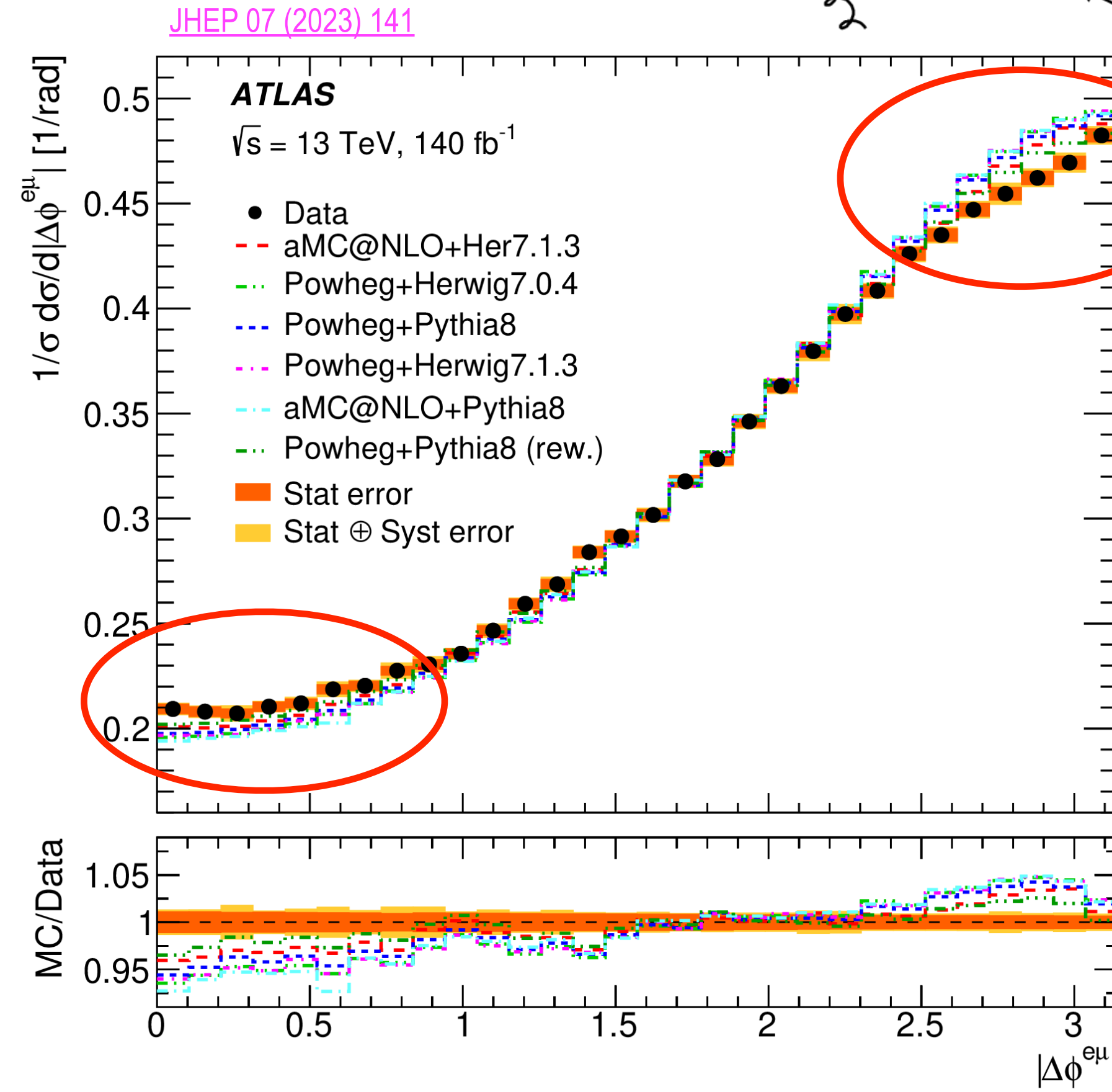
Dilepton, Particle level, Resolved





$$|\Delta\Phi^{e\mu}|$$

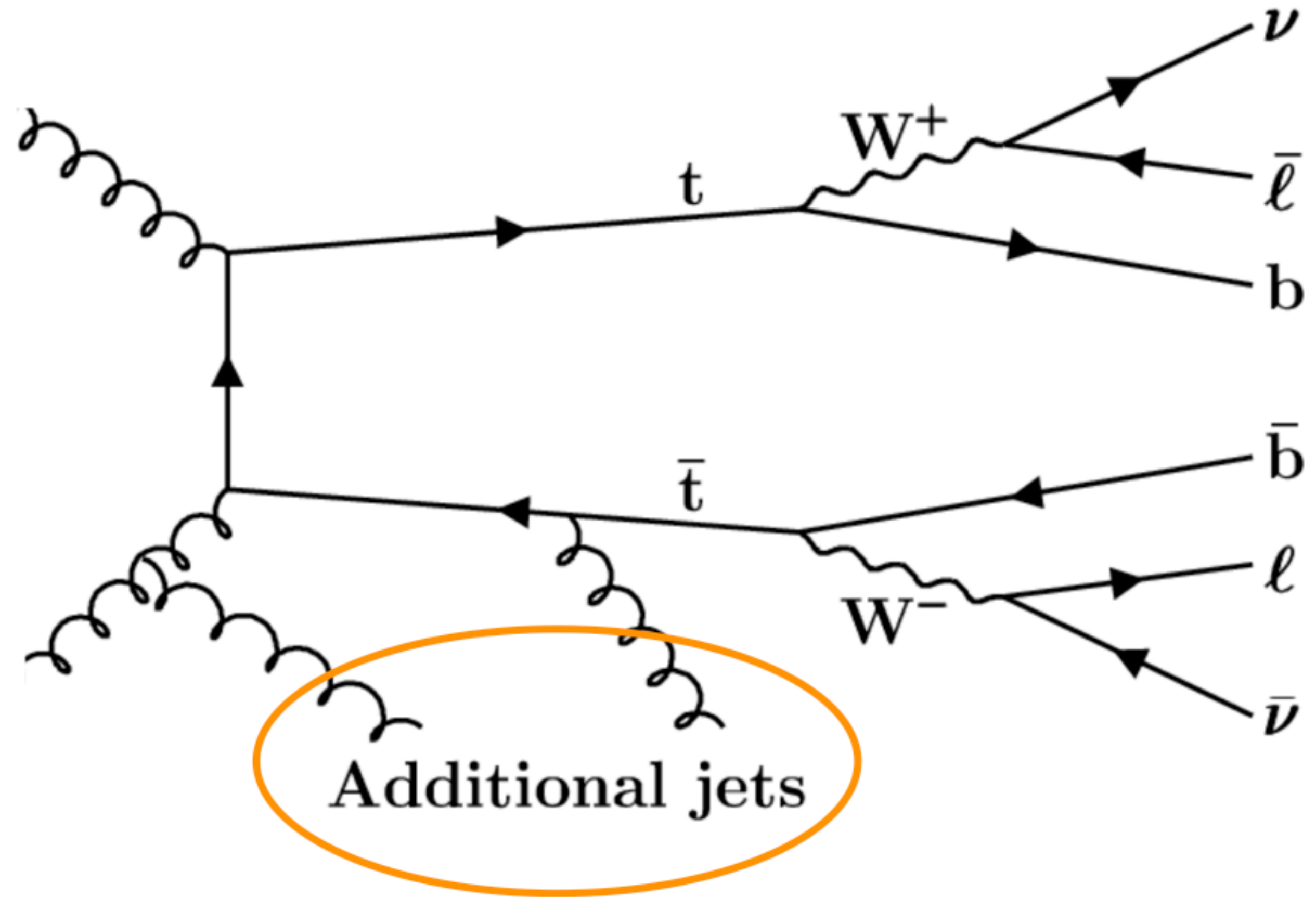
Dilepton, Particle level, Resolved



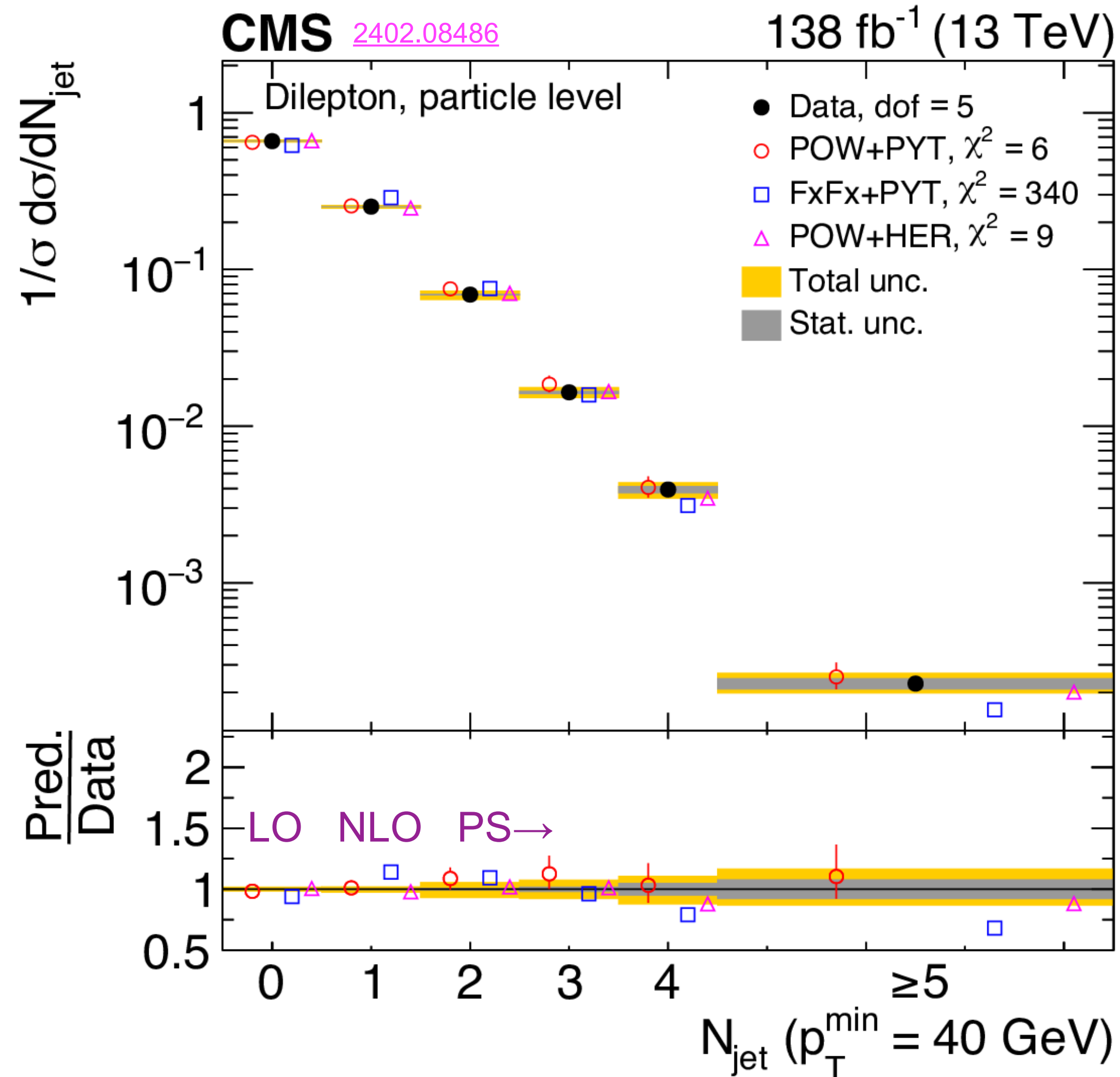
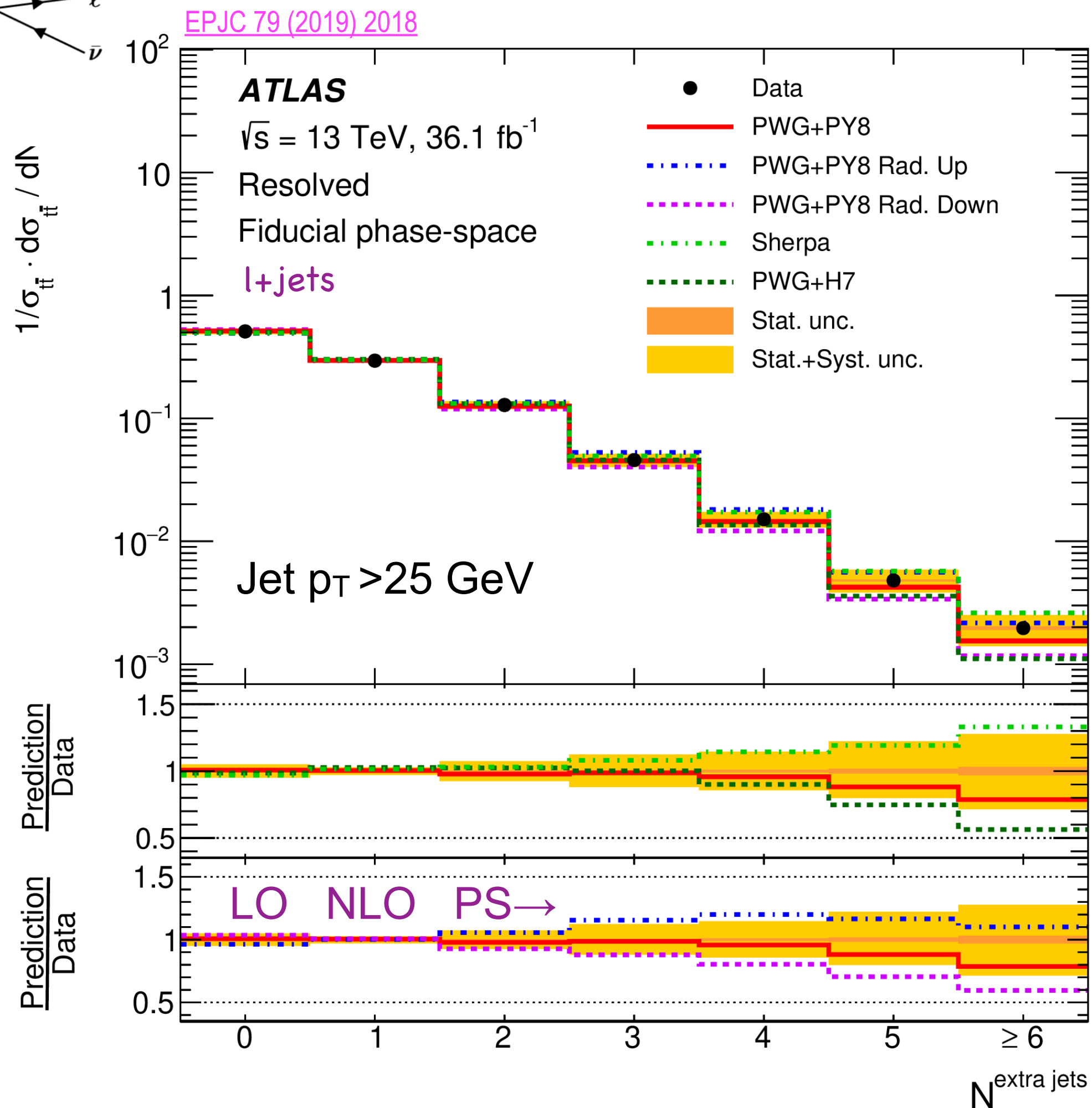
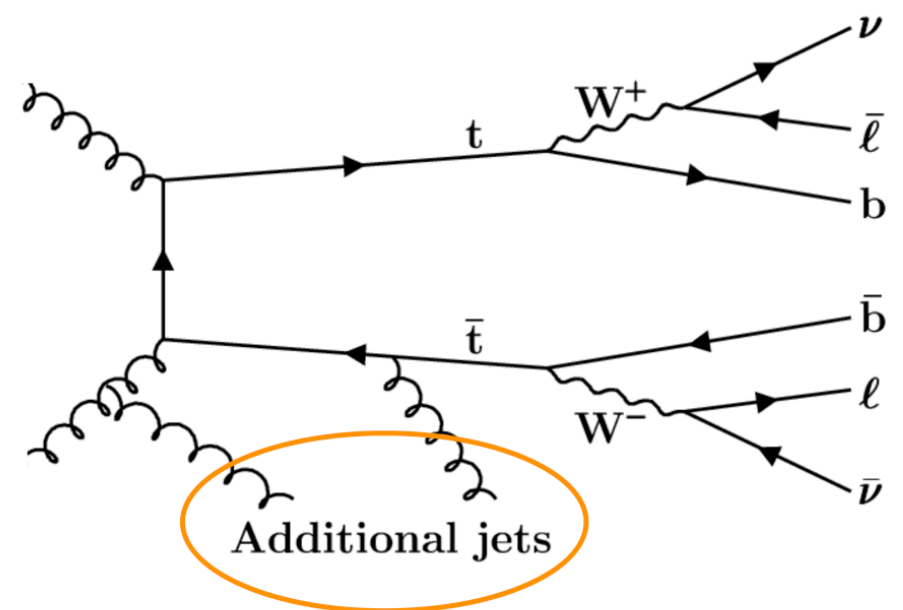
⇒ All models predict more back-to-back leptons than seen in data

⇒ Double differential xsec $|\Delta\Phi^{e\mu}| : m^{e\mu}$ is among the ones described worst → MC Tuning potential!

Results:



Nextra jets

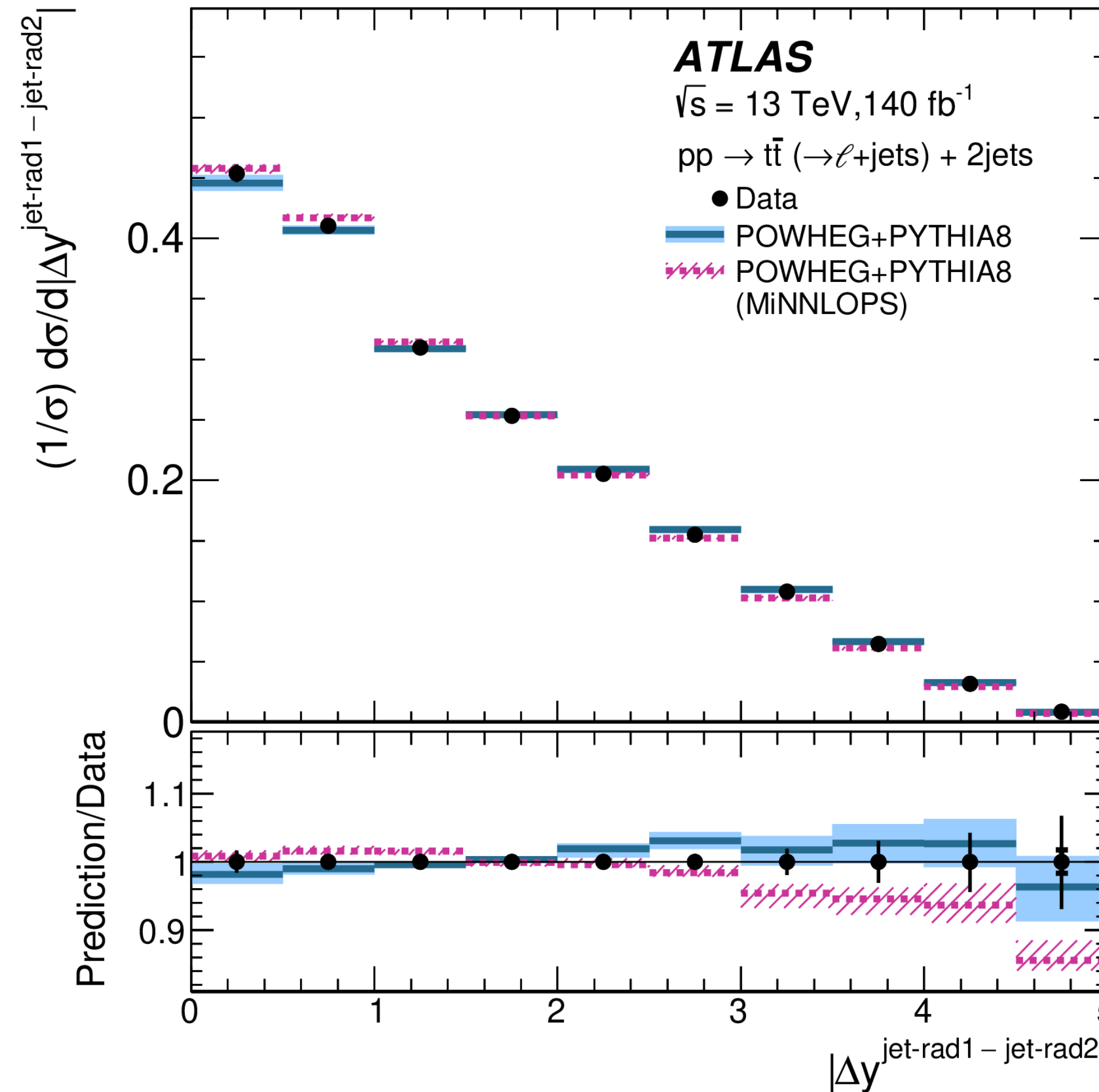
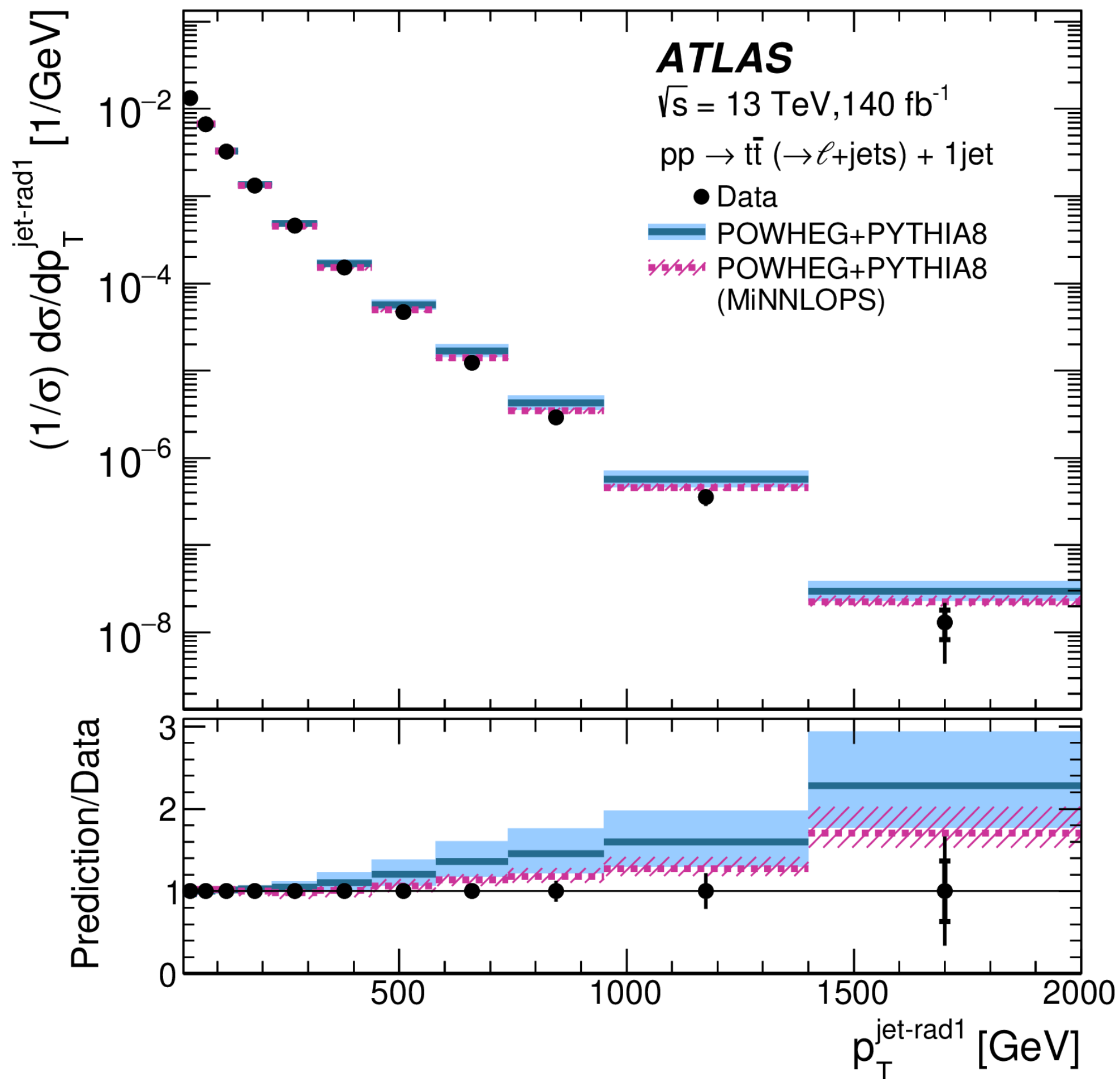


⇒ Excellent description by POW, maybe also because MC tunes were tested against earlier ATLAS & CMS $t\bar{t}$ +jet data?

$p_T^{\text{jet-rad1}}$

$|\Delta y^{\text{jet-rad1} - \text{jet-rad2}}|$

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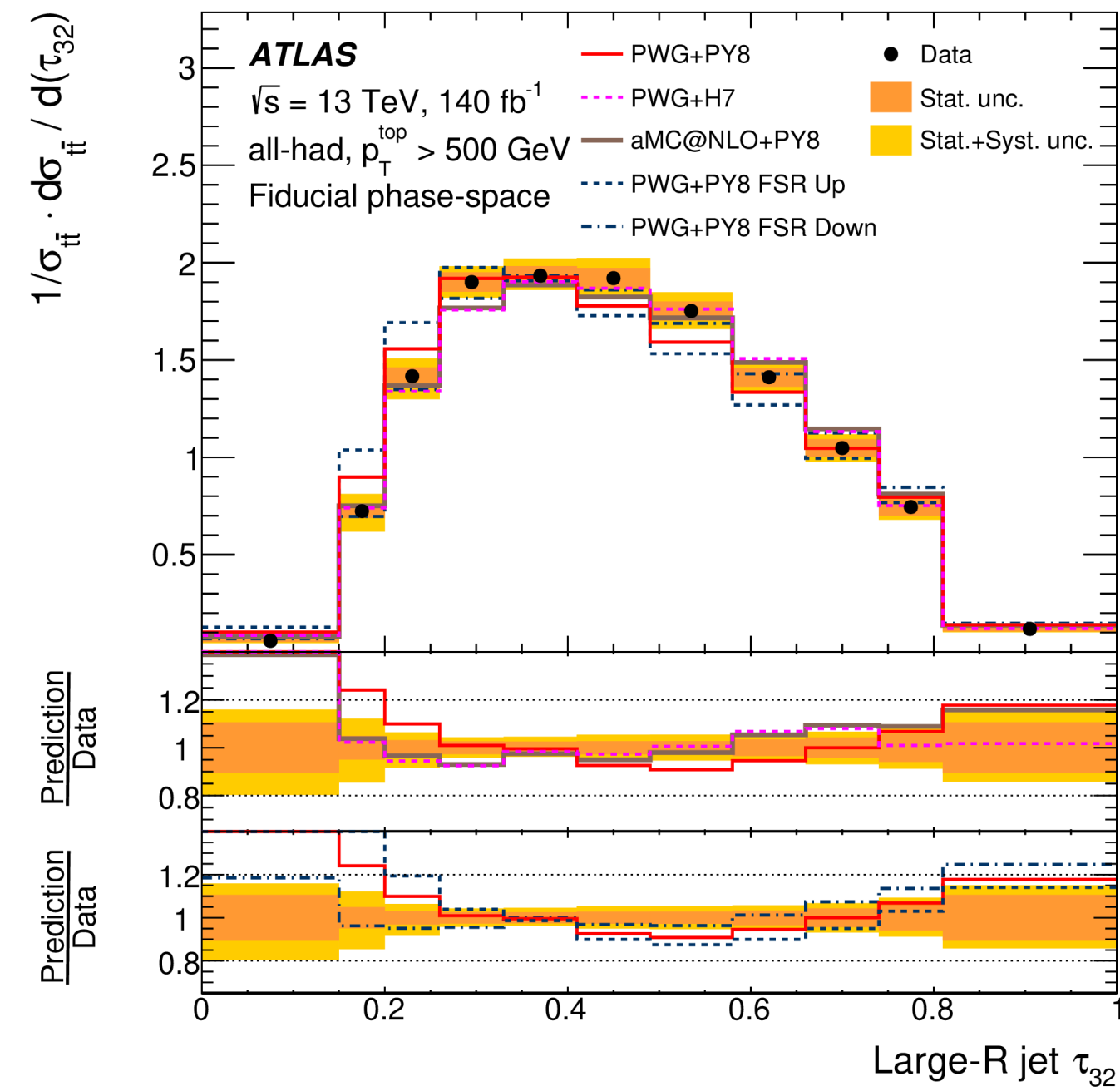
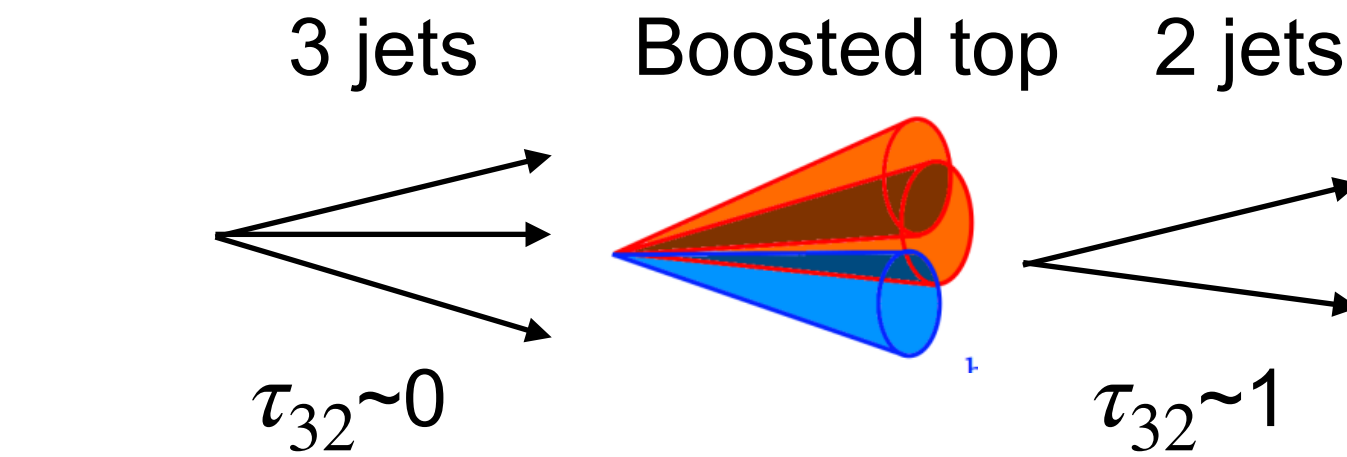


- ⇒ MiNNLOPS:
- improves leading jet p_T description
 - fails in the rapidity separation to the 2nd leading jet: that is an $\mathcal{O}(\alpha_s^4)$ observable

Looking even deeper into $t\bar{t}$ events: particle flow

PRD 109 (2024) 112016

Boosted top Jet-substructure I+jets, all had



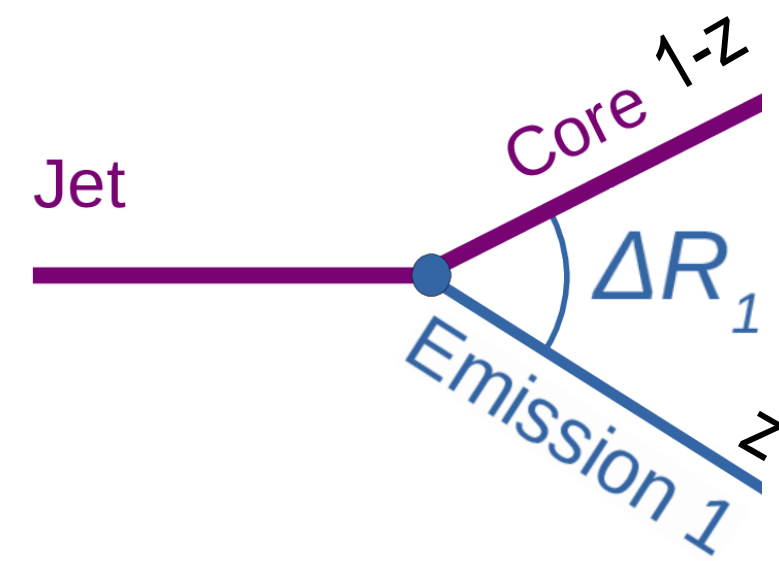
POW/ATLAS:  1.0

⇒ POW predicts more 3 jets like topologies

2407.10879

Measurement of the Lund jet plane I+jets

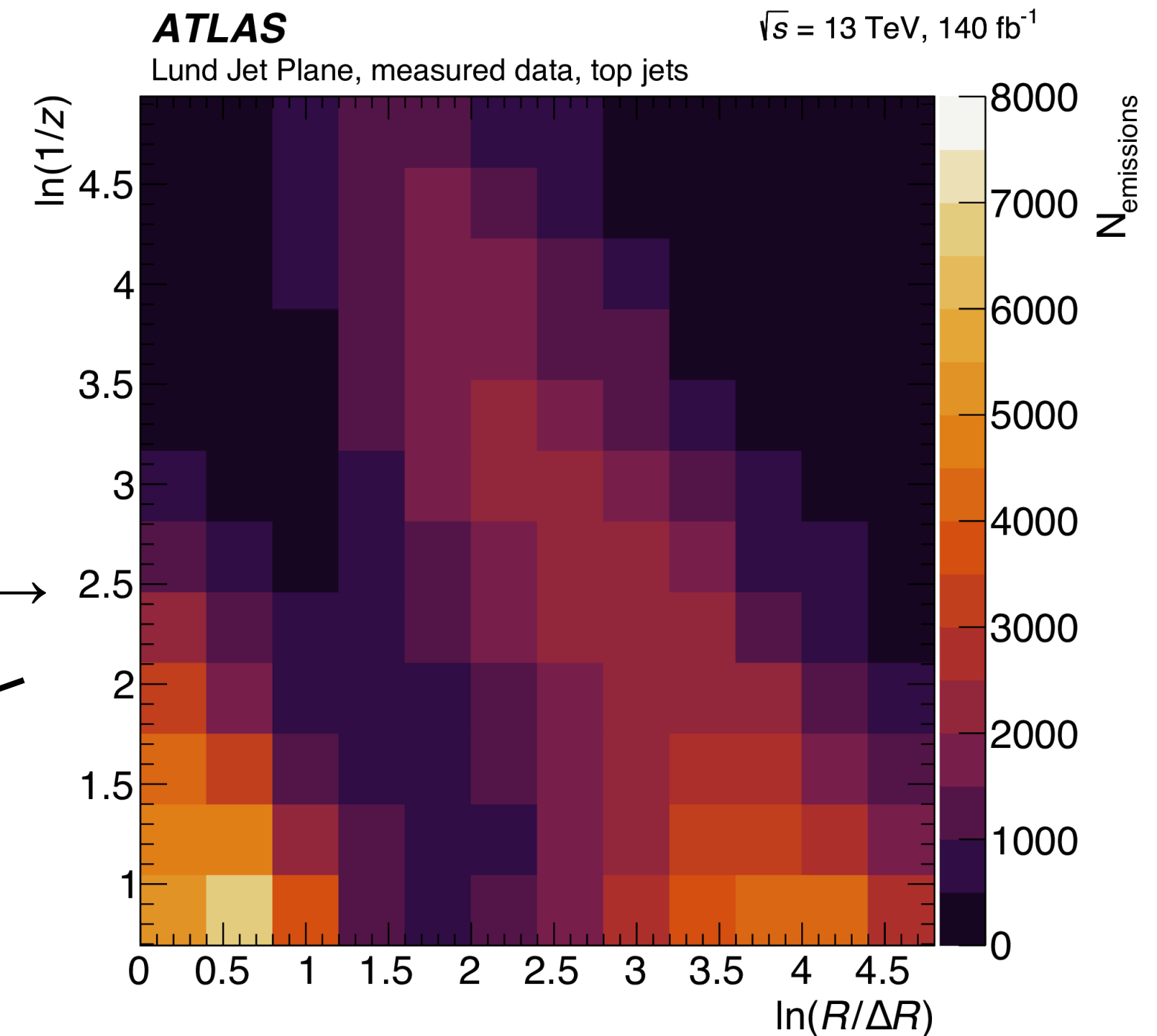
- Hadronically decaying top jets, $R=1$, $p_T > 350$ GeV, cluster from tracks
- Go backwards in the clustering, reinterpret mergings as emissions



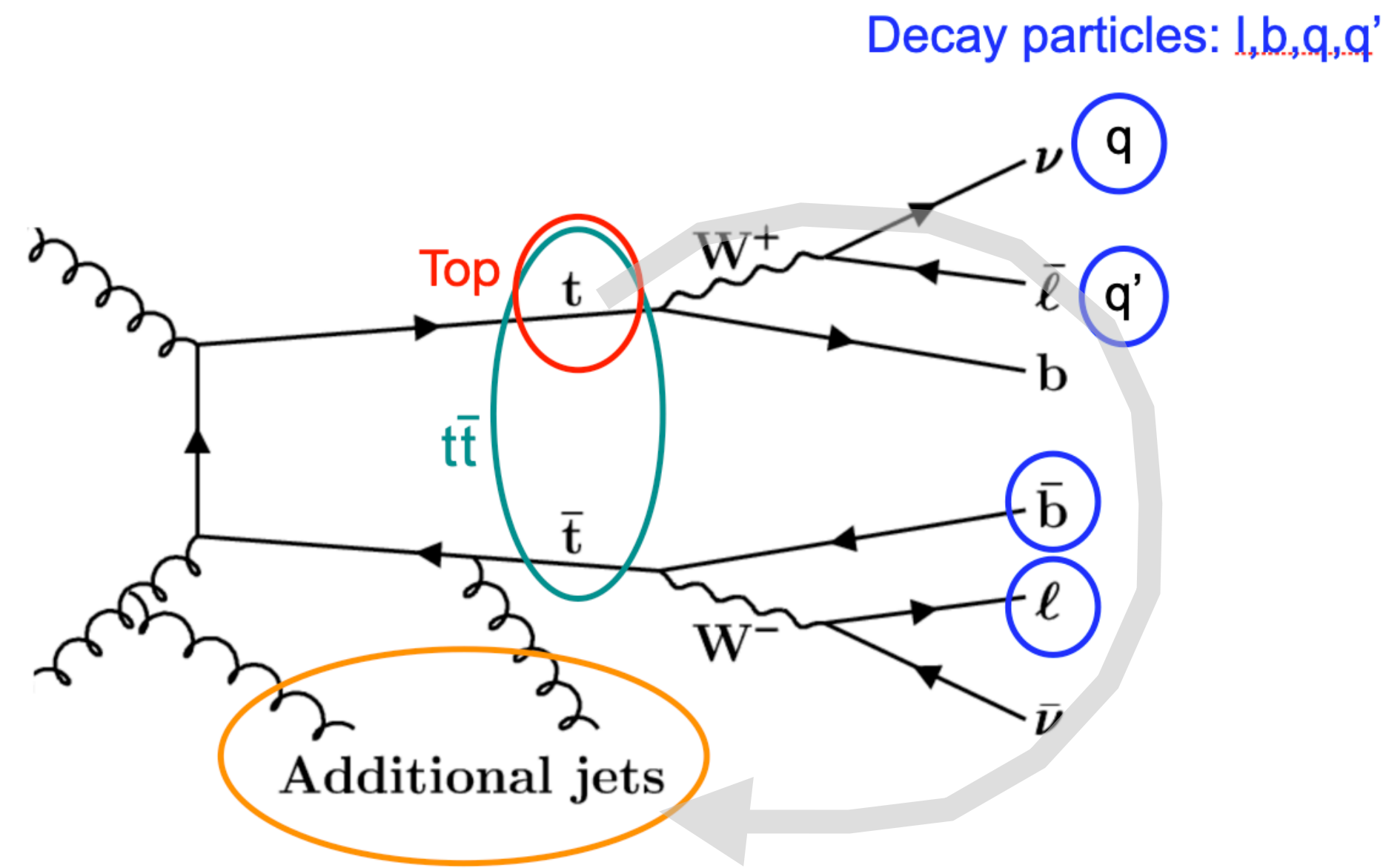
- Measure emission density →

Use data for:

- Tuning of MC generators
- Better modelling of heavy quarks and boson hadronic decays
- Improve performance of jet taggers

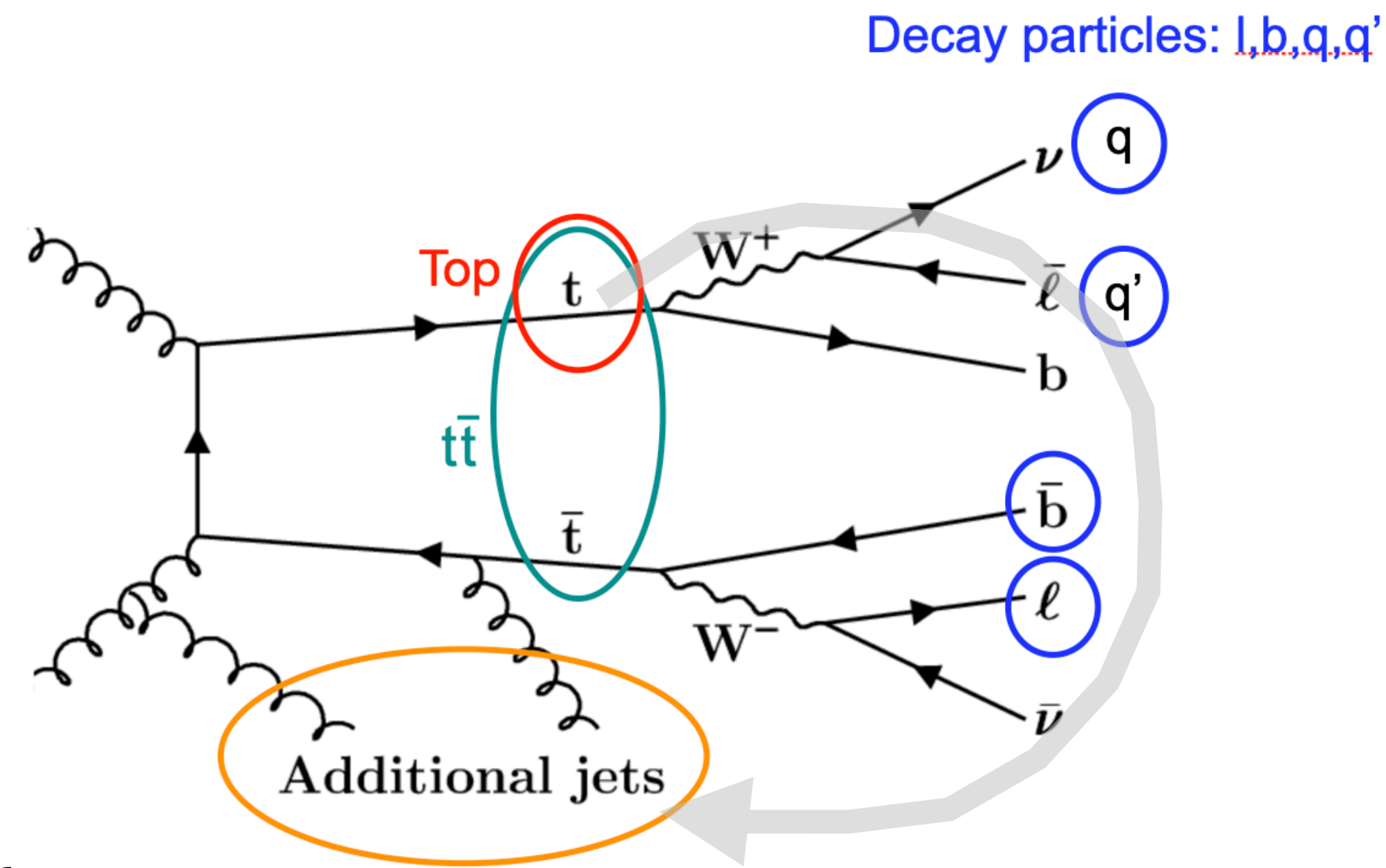


Conclusion



- **Broad wealth** of topologies and object kinematic distributions in $t\bar{t}$ events studied by ATLAS & CMS with RUN 2 Data, with total samples of $\mathcal{O}(10\text{M})$ $t\bar{t}$ events after event selections
- **No model** is able to describe all distributions
- **NNLO improves NLO+PS descriptions** for LO observables, e.g. $P_T(t)$, but not so much for higher order observables, e.g. $P_T(t\bar{t})$
- **Multi-differential distributions** seem less well described, example: the precise ATLAS measurements of $|\Delta\Phi^{e\mu}| : m^{e\mu}$

Outlook



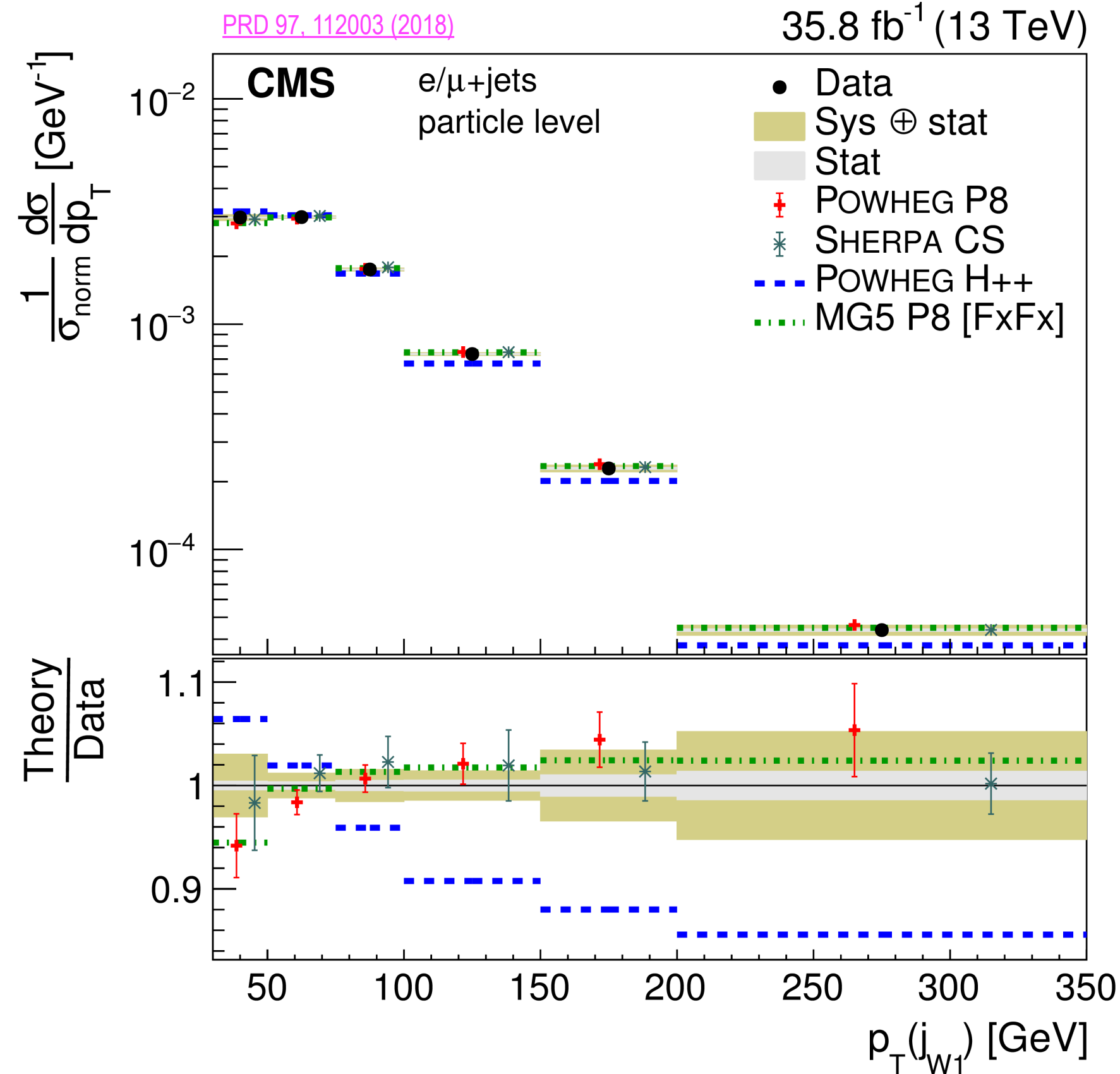
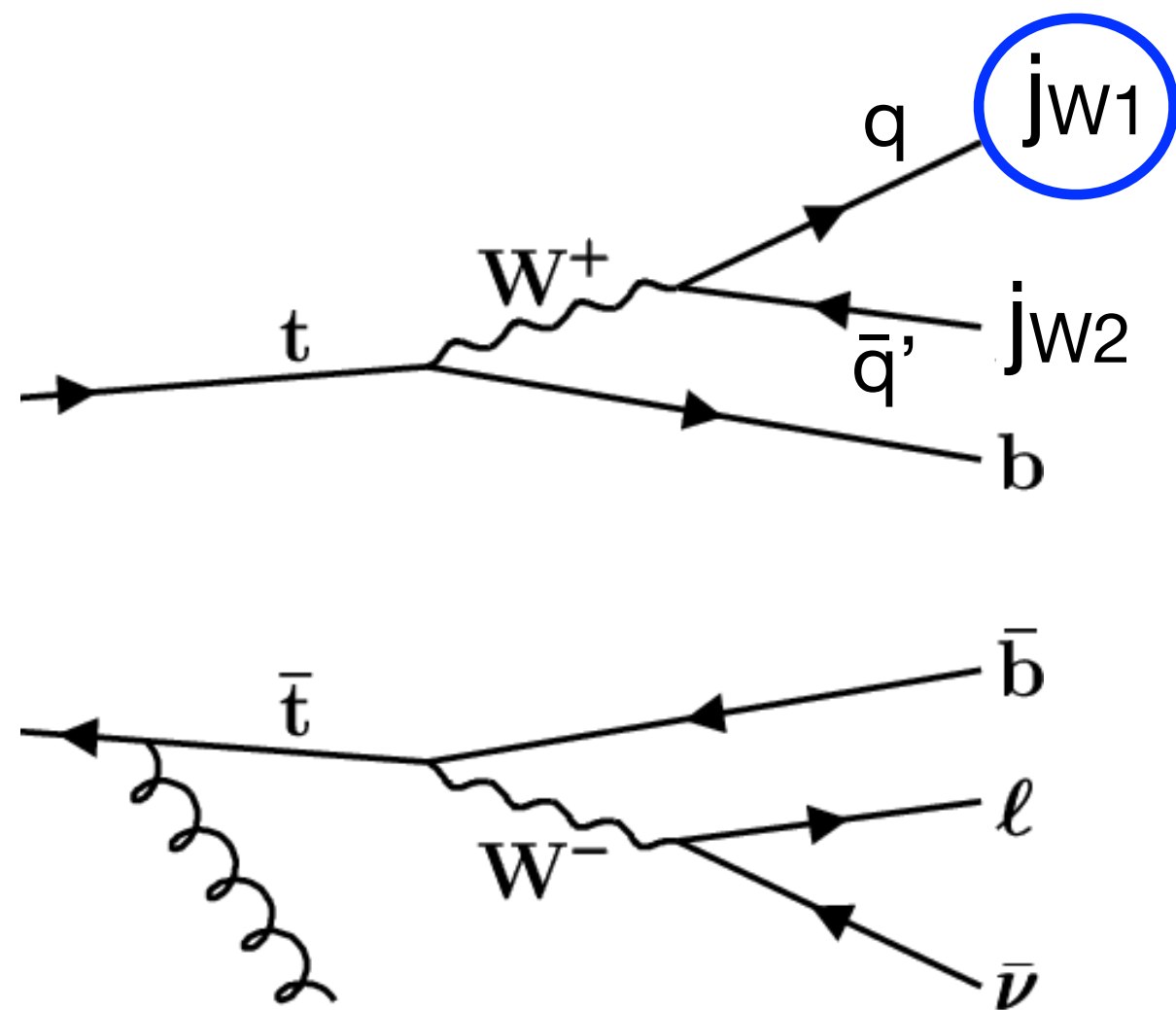
- **Run 3:**
 - Awaiting first differential $\sigma_{t\bar{t}}$ results
 - Expect to collect $\sim 200\text{M}+$ $t\bar{t}$ events per experiment (end 2025)
- **Exciting new methodic avenues ahead:**
 - $d^m\sigma_{t\bar{t}}/dx^m$ using Machine Learning (ML) unfolding, example:
ATLAS Z+jets [2405.20041](#) with $m=24$; [Find here recent overview talk on ML Unfolding](#)
 - Providing deep tomography, perhaps even anomaly detection
 - Compete with/complementary to profile likelihood fit unfolding?
 - **ML based improved top tagging and kinematic reconstructions**
 - rapidly growing field \Rightarrow measure more accurately and in finer bins



Backup

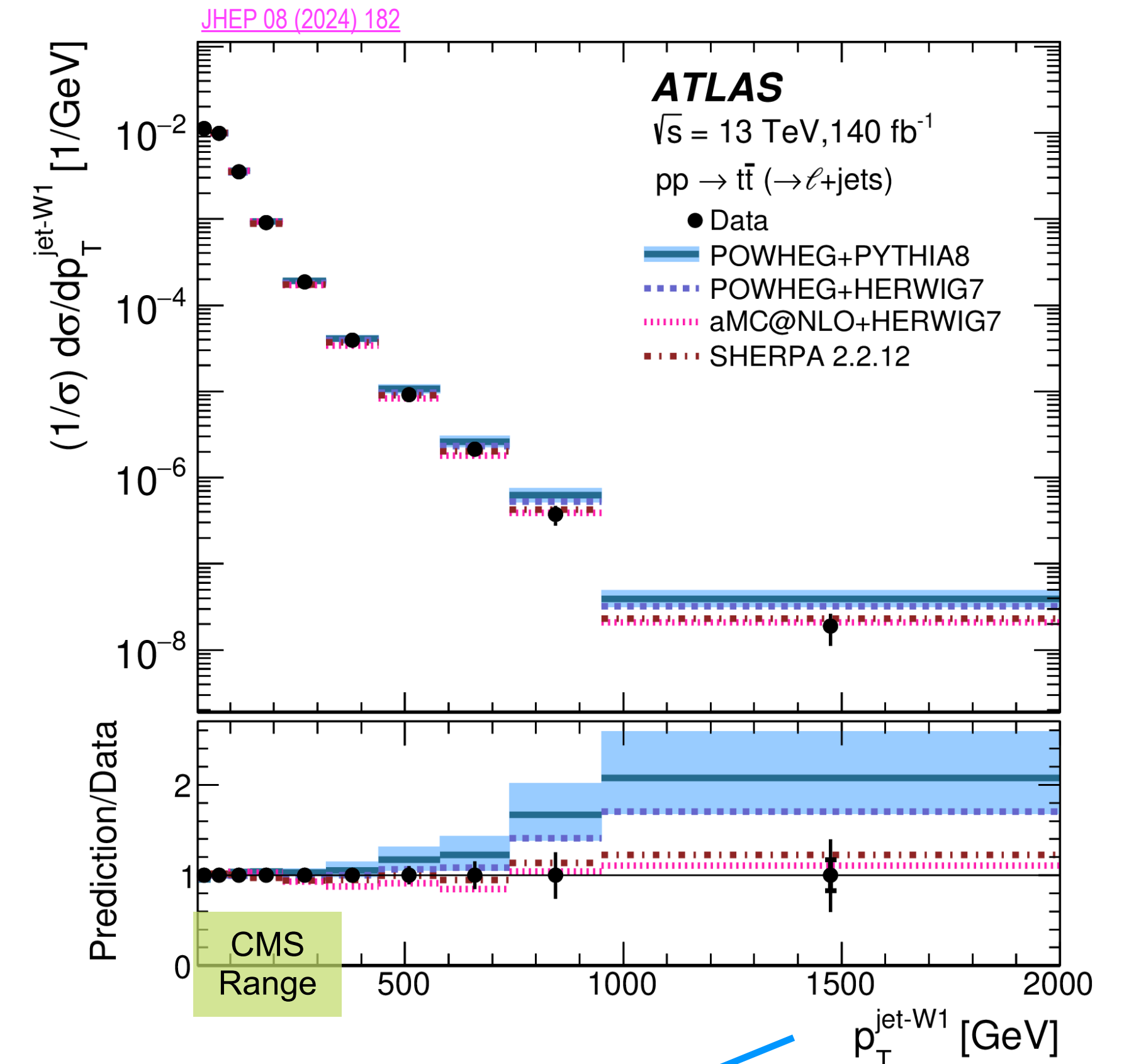
$p_T(j_{W1})$

I+jets, Particle level, Resolved



POW/CMS: 1.0

SHERPA/CMS: 1.0



POW/ATLAS: 1.0

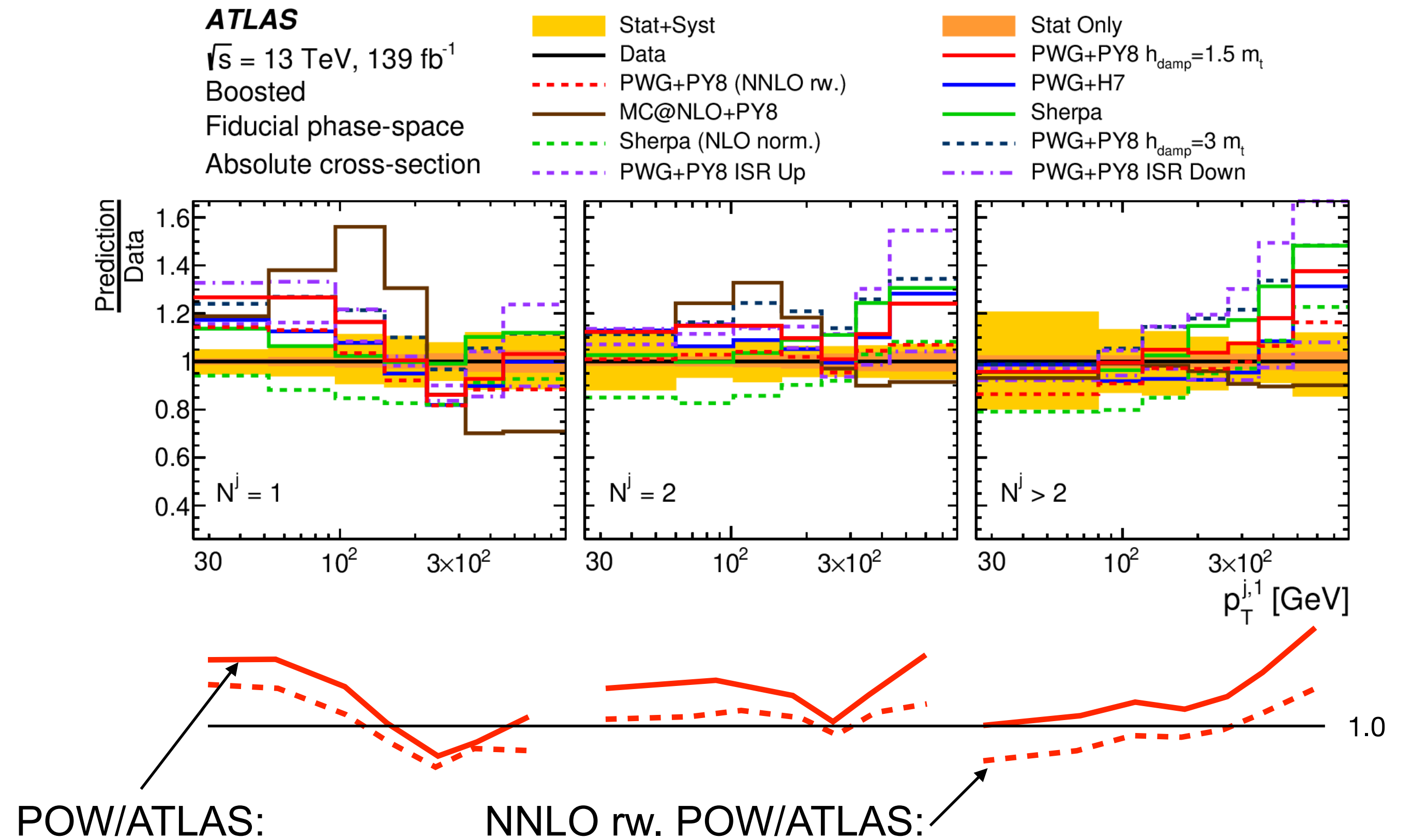
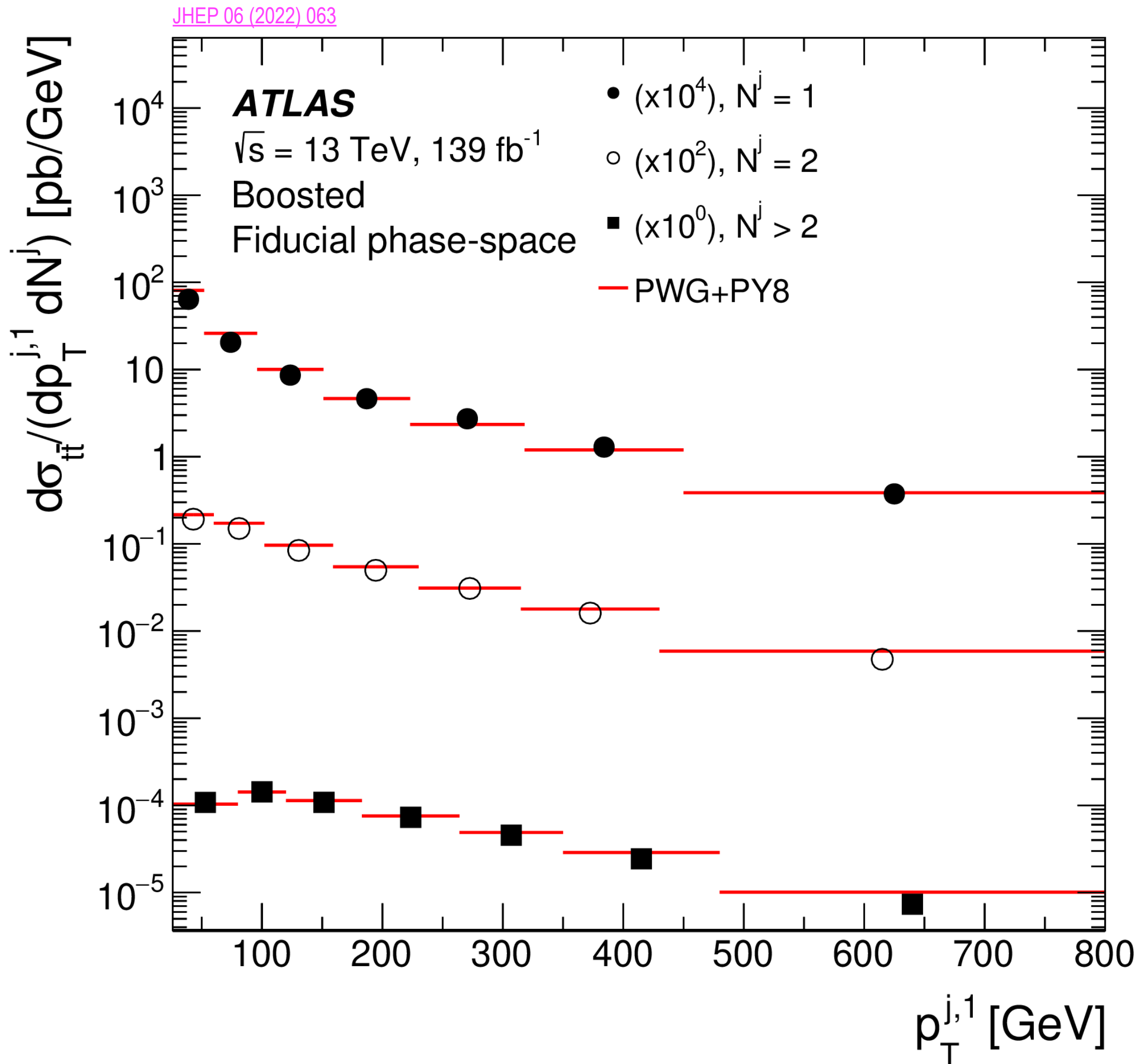
SHERPA/ATLAS: 1.0

⇒ ATLAS expands jet p_T to **2 TeV!**

⇒ SHERPA provides improved description

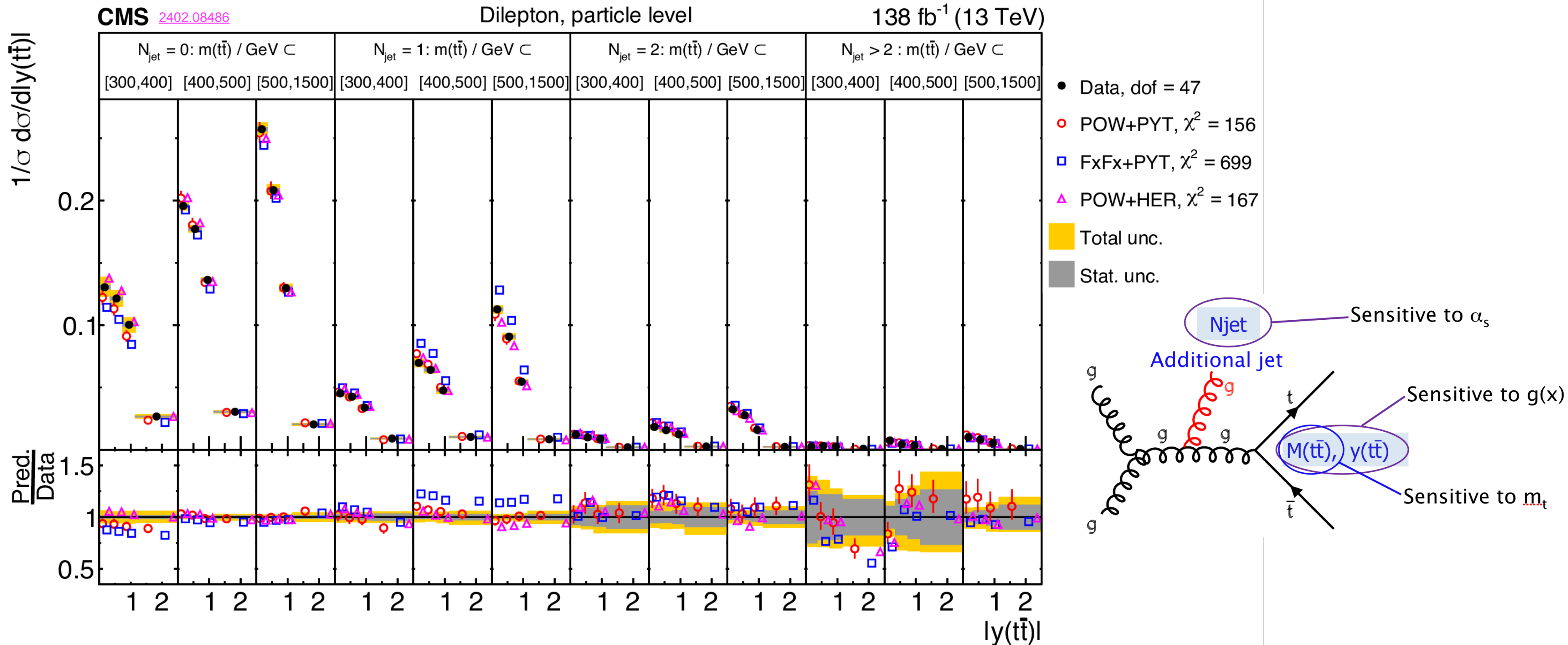
$p_{T}(j, 1)$

Particle level, with 1 boosted top quark



⇒ POW with problems for leading additional jet p_T distribution, for various $N_{\text{extra jets}}$
 NNLO reweighting helps!

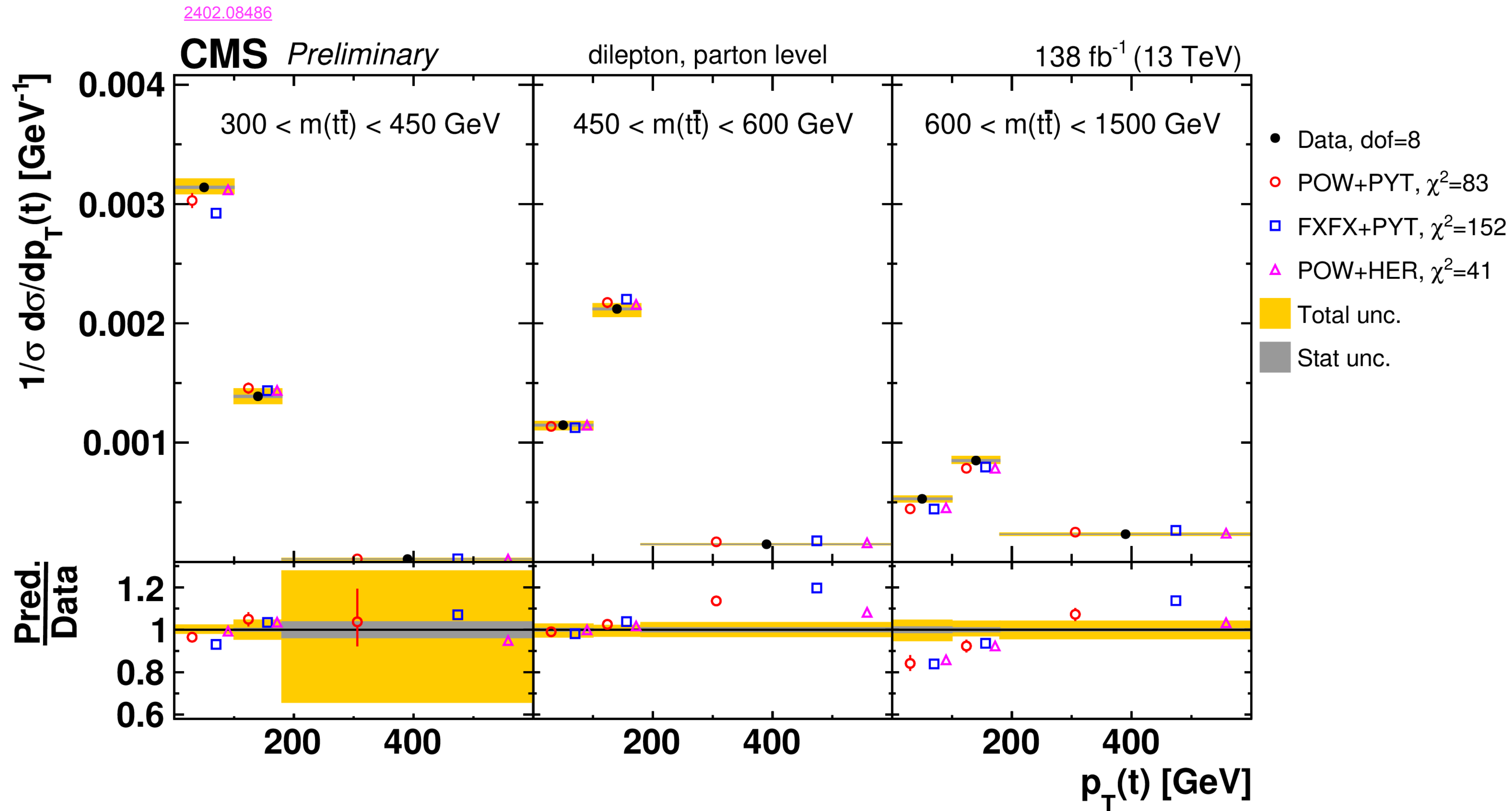
$y(tt)$ vs $m(tt)$ in bins of $N_{\text{extra jet}}$



⇒ Known from 1904.05237 to provide simultaneous sensitivity to m_t , α_s and $g(x)$
 Could still explore a great variety of not yet measured triple differential σ_{tt} , e.g. $y(t):p_T(t):m(tt)$

$p_T(t)$ in bins of $m(t\bar{t})$

Dilepton, Parton level

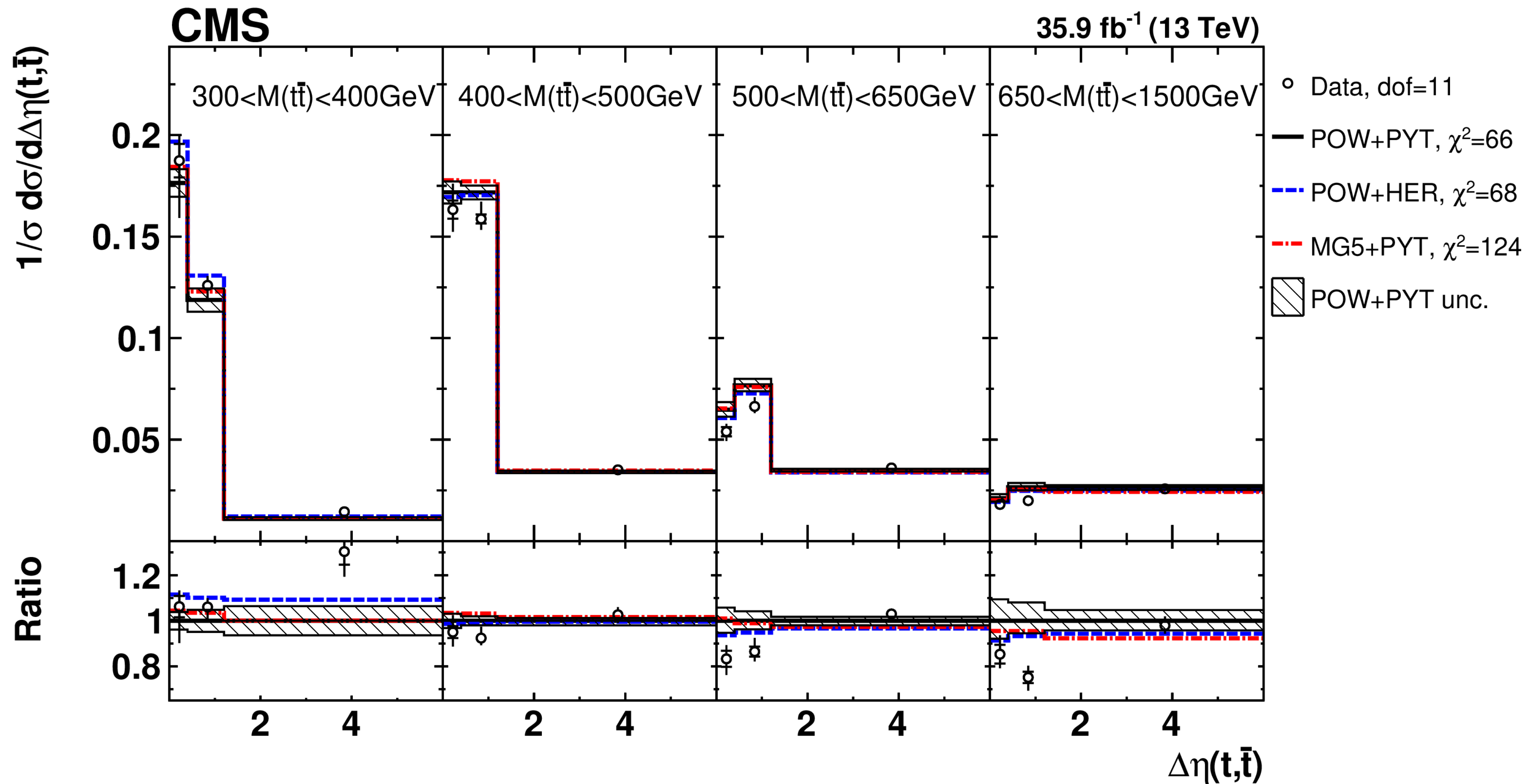


⇒ $p_T(t)$ distribution: POW/Data positive slope increasing with $m(t\bar{t})$

$\Delta\eta(t, \bar{t})$ in bins of $m(t\bar{t})$

Dilepton, Parton level

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⇒ $\Delta\eta(t, \bar{t})$ distribution: Data/POW positive slope increasing with $m(t\bar{t})$