

# Complete NLO corrections to top-quark pair production with isolated photons

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In collaboration with: Malgorzata Worek

Based on [JHEP 08 \(2023\) 179](#)

[JHEP 07 \(2024\) 091](#)

[arXiv: 2410.xxxxx \[hep-ph\]](#)

Collaborative Research Center TRR 257

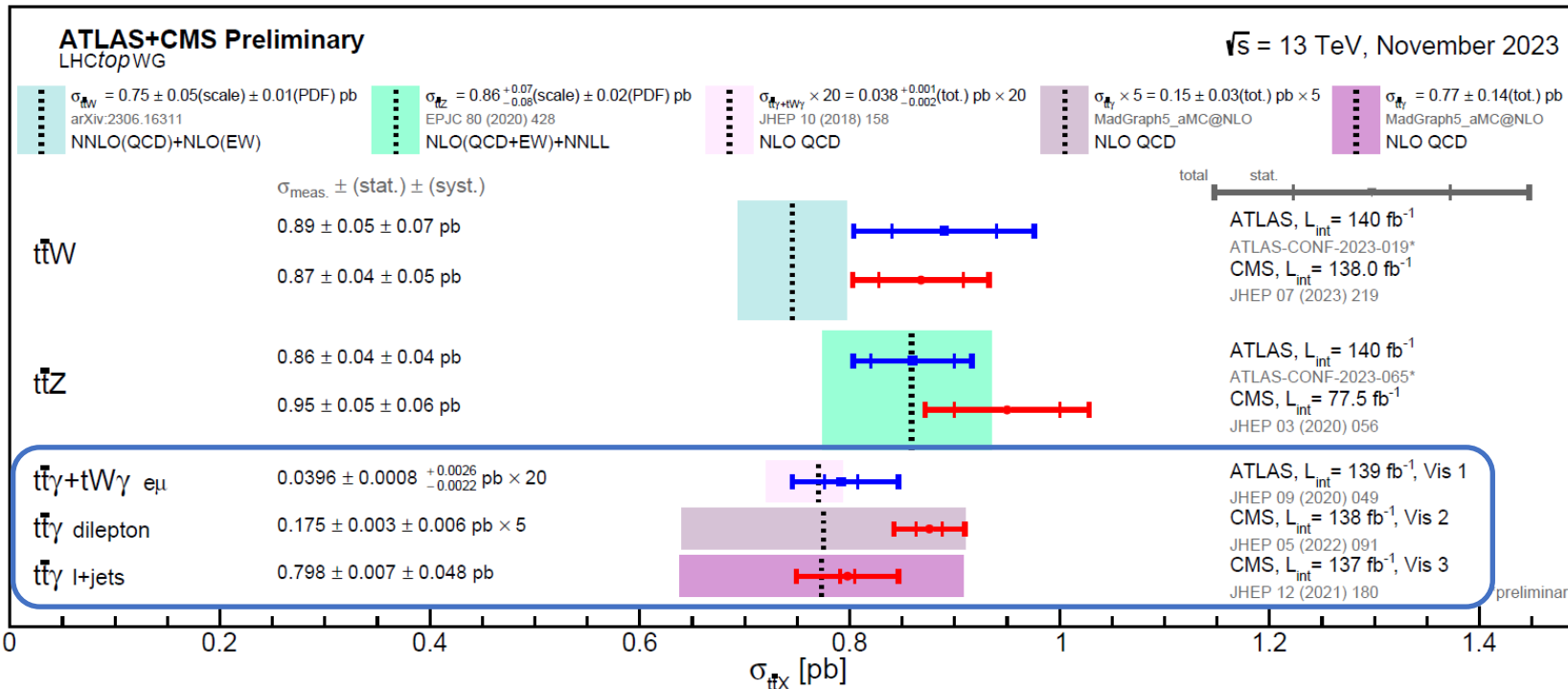


Particle Physics Phenomenology after the Higgs Discovery

*TOP2024, Saint-Malo, France, 23 September 2024*

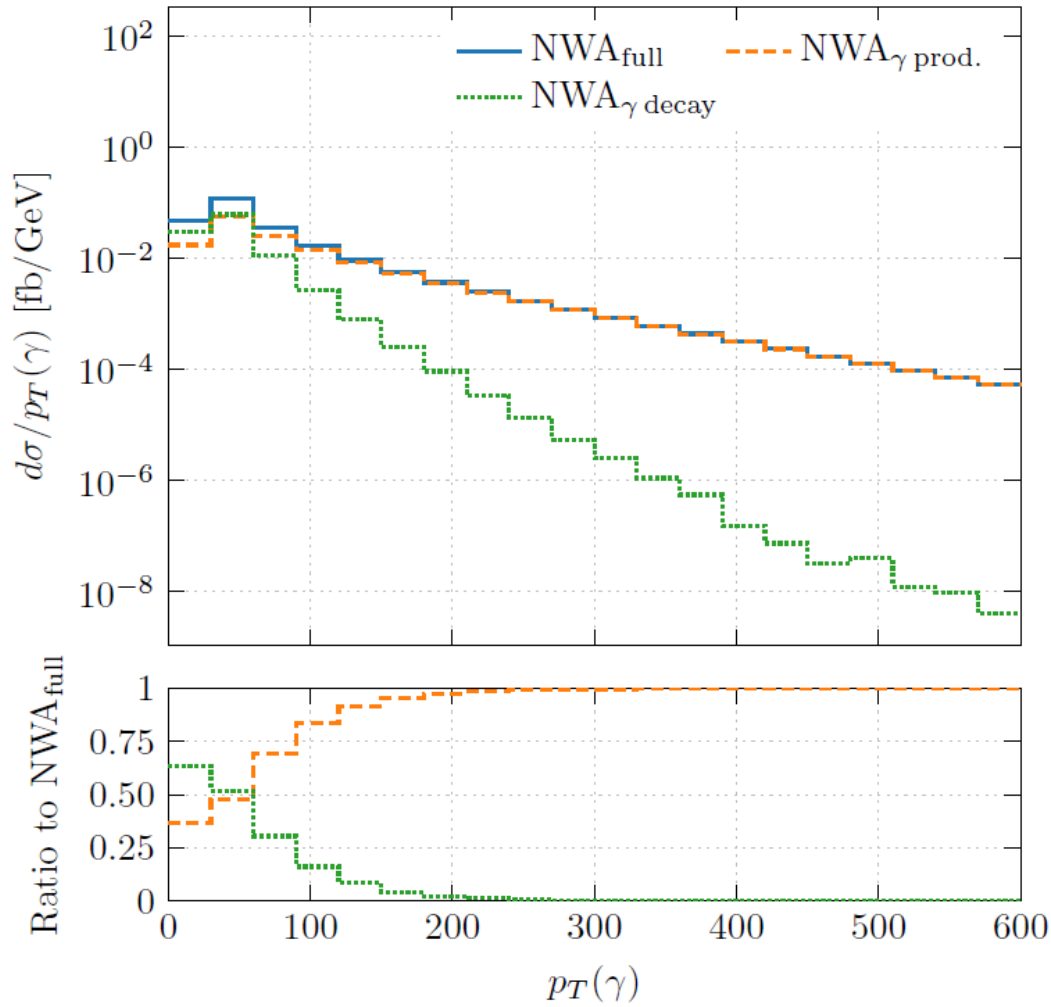
# Motivation - $pp \rightarrow t\bar{t}\gamma$

- Unique features with respect to other associated  $pp \rightarrow t\bar{t}$  processes:
  - Large fraction of photon radiation from top-quark decays ( $t\bar{t}\gamma$ :  $\sim 50\%$ )  
→ Difficult modeling
  - Secondary photon production due to fragmentation processes and hadron decays ( $\pi^0 \rightarrow \gamma\gamma$ )  
→ Use of photon isolation criteria in measurements to suppress secondary photons
- Probe  $t - \gamma$  coupling
- $pp \rightarrow t\bar{t}\gamma$  first observed by ATLAS at 7 TeV *Phys.Rev.D 91 (2015) 7, 072007*

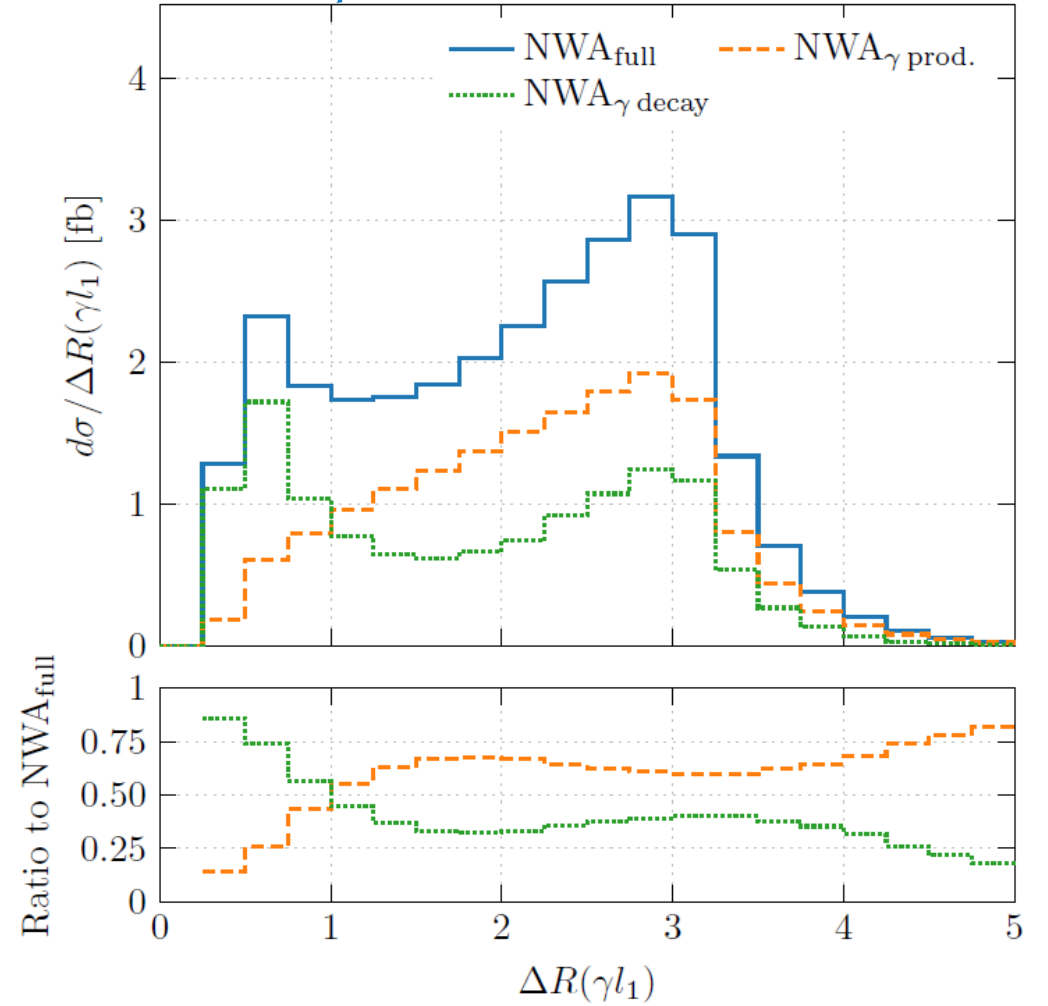


Current status:

# Prompt photon distribution in $pp \rightarrow t\bar{t}\gamma$ in di-lepton channel



*Bevilacqua, Hartanto, Kraus, Weber, Worek '20*

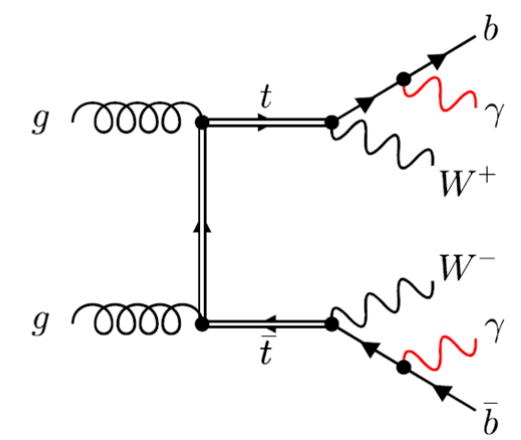
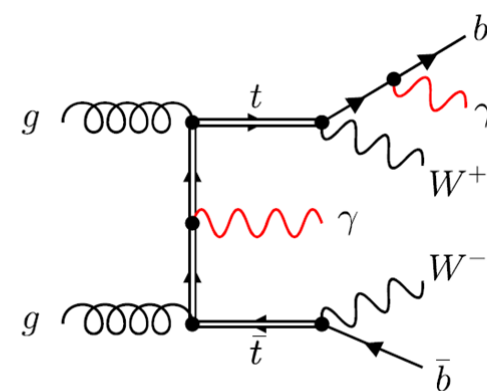
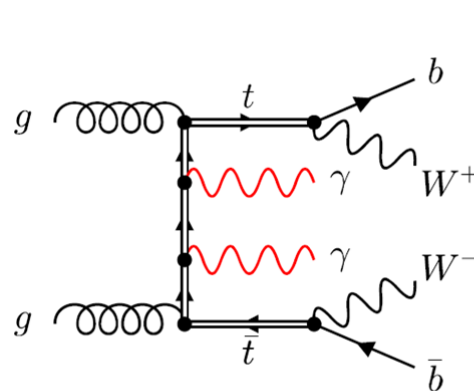
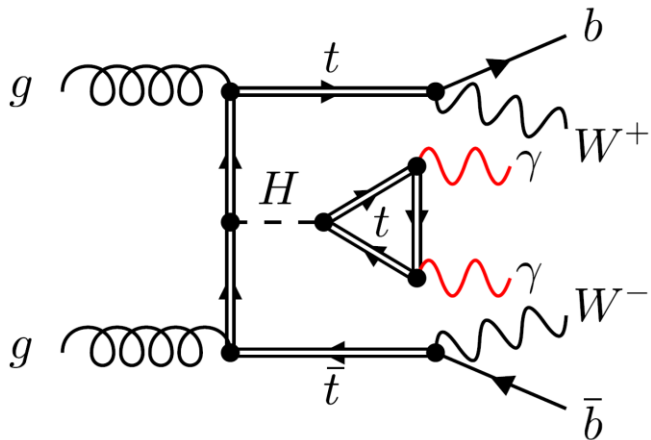
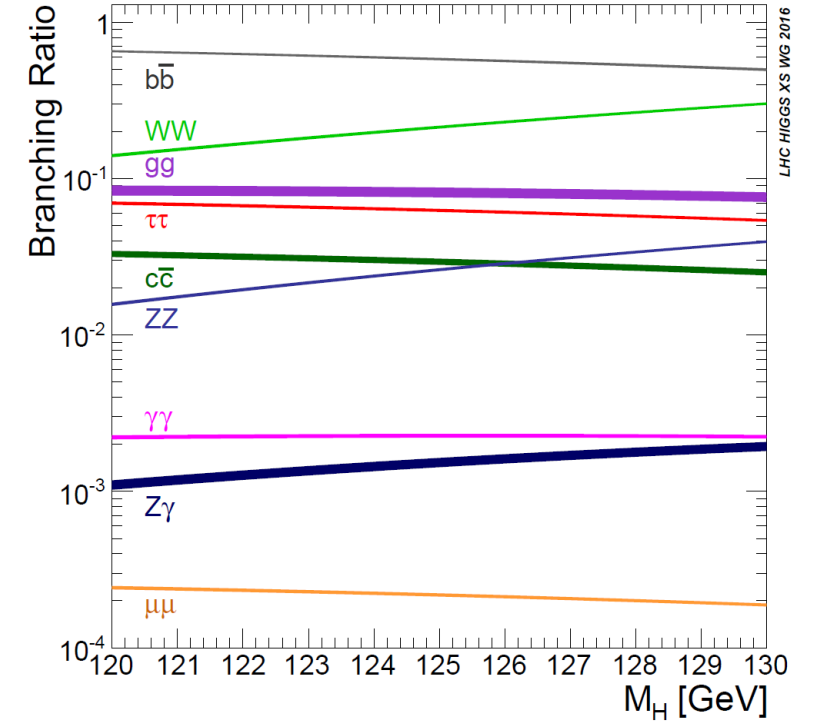


→ Essential to include photon radiation in top-quark decays

# Motivation - $pp \rightarrow t\bar{t}\gamma\gamma$

- Observation of  $pp \rightarrow t\bar{t}H$  in 2018 by ATLAS and CMS  
*Phys.Lett.B 784 (2018) 173-191*  
*Phys.Rev.Lett. 120 (2018) 23, 231801*
- Direct probe of  $Y_t$  at tree level
- $H \rightarrow \gamma\gamma$  small branching ratio with  $\sim 0.2\%$
- $pp \rightarrow t\bar{t}H(H \rightarrow \gamma\gamma)$  first single-channel observation of  $pp \rightarrow t\bar{t}H$   
*Phys.Rev.Lett. 125 (2020) 6, 061801*  
*Phys.Rev.Lett. 125 (2020) 6, 061802*
- Irreducible background from direct photon production  $pp \rightarrow t\bar{t}\gamma\gamma$
- No observation of  $pp \rightarrow t\bar{t}\gamma\gamma$  yet

LHC HIGGS XS WG 2016



# Theory status ( $pp \rightarrow t\bar{t}\gamma$ )

- Stable top quarks

- NLO QCD
- NLO EW
- Complete NLO
- aNNLO QCD

*Duan, Ma, Zhang, Han, Guo, Wang '09 '11  
Maltoni, Pagani, Tsirikos '16*

*Duan, Zhang, Wang, Song, Li '17*

*Pagani, Shao, Tsirikos, Zaro '21*

*Kidonakis, Tonerio, '21*

- Matched to Parton showers at NLO QCD

- POWHEL/POWHEG

*Kardos, Trócsányi '15*

- Higher order corrections and photon radiation in decays

- NLO QCD in NWA
- NLO QCD with full off-shell effects

*Melnikov, Schulze, Scharf '11*

*Bevilacqua, Hartanto, Kraus, Weber, Worek '20*

*Bevilacqua, Hartanto, Kraus, Weber, Worek '18*

- Complete NLO in NWA

*Stremmer, Worek '24*

- All calculations based on smooth-cone isolation *Frixione '98*

# Theory status ( $pp \rightarrow t\bar{t}\gamma\gamma$ )

- Stable top quarks at NLO QCD

- NLO QCD
- NLO QCD+EW

*Alwall, Frederix, Frixione, Hirschi, Maltoni,  
Mattelaer, Shao, Stelzer, Torrielli, Zaro '14  
Maltoni, Pagani, Tsinikos '16*

*Pagani, Shao, Tsinikos, Zaro '21*

- Matched to Parton Showers at NLO QCD

- POWHEL/POWHEG
- MC@NLO

*Kardos, Trócsányi '15*

*van Deurzen, Frederix, Hirschi, Luisoni, Mastrolia '16*

- Higher order corrections and photon radiation in decays

- NLO QCD in NWA
- Complete NLO in NWA

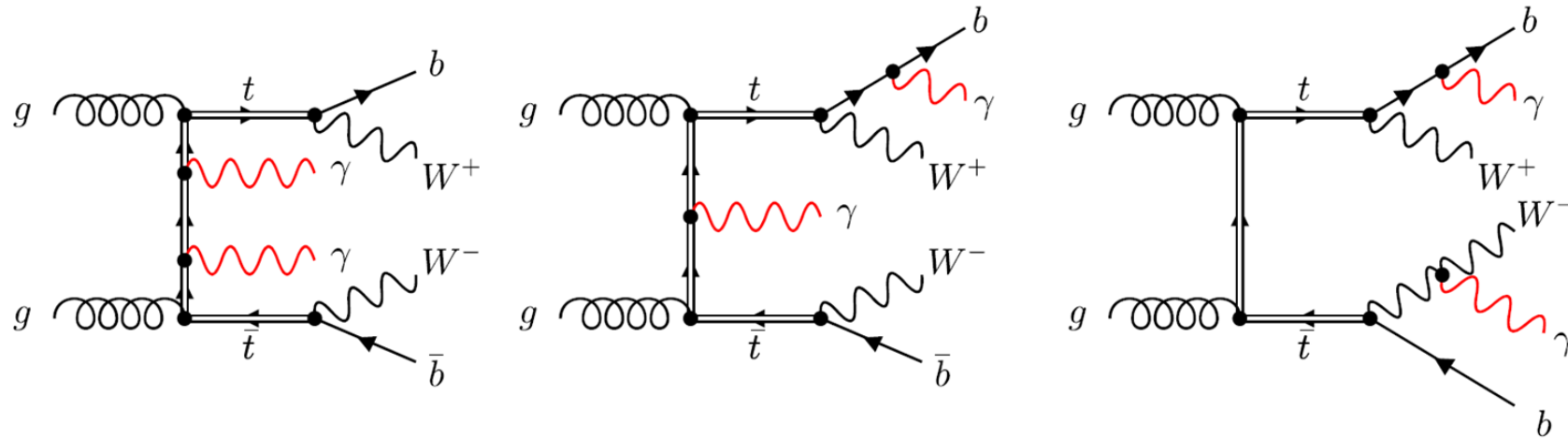
*Stremmer, Worek '23*

*Stremmer, Worek '24*

- All calculations based on smooth-cone isolation *Frixione '98*

# Process definition

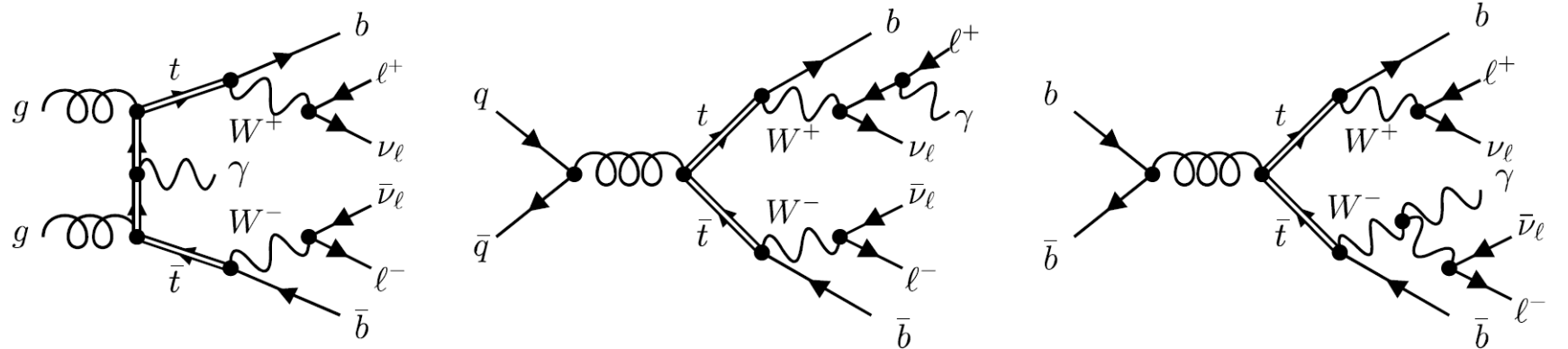
$$d\sigma_{\text{Full}}^{\text{LO}} = \Gamma_t^{-2} \left( \underbrace{d\sigma_{t\bar{t}\gamma\gamma}^{\text{LO}} d\Gamma_{t\bar{t}}^{\text{LO}}}_{\text{Prod.}} + \underbrace{d\sigma_{t\bar{t}\gamma}^{\text{LO}} d\Gamma_{t\bar{t}\gamma}^{\text{LO}}}_{\text{Mixed}} + \underbrace{d\sigma_{t\bar{t}}^{\text{LO}} d\Gamma_{t\bar{t}\gamma\gamma}^{\text{LO}}}_{\text{Decay}} \right)$$



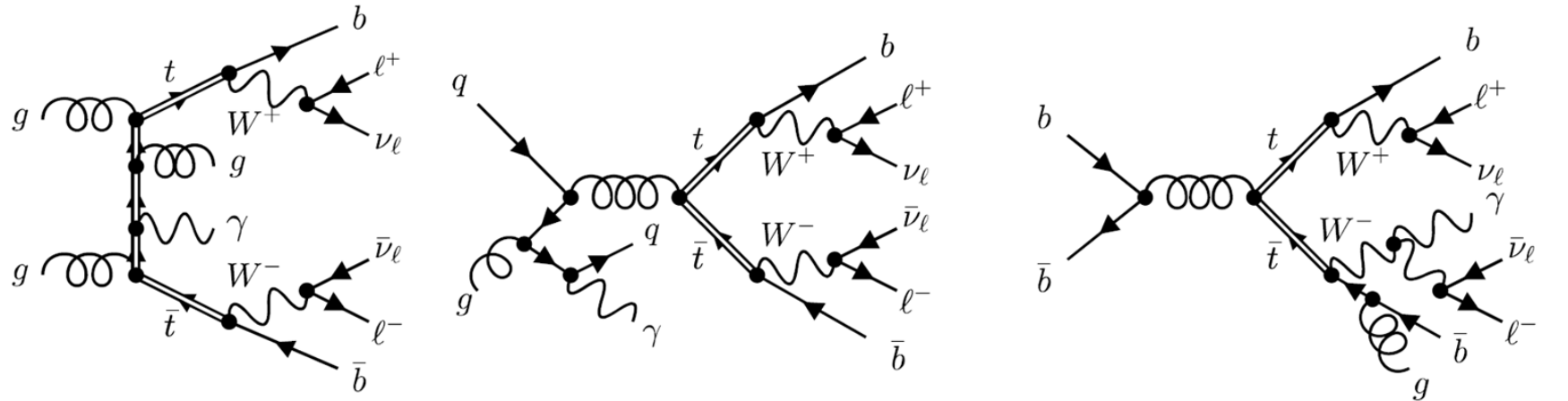
- Calculation performed in **NWA** preserving spin correlations
- Full calculation divided into three resonant contributions: **Prod.**, **Mixed** and **Decay**
- **Photon bremsstrahlung** and **NLO** corrections included in  $t\bar{t}$  production and decays
- NLO QCD corrections calculated for each resonant structure separately
- Mixing of resonant contributions in subleading NLO corrections

# NLO QCD

LO<sub>1</sub> at  $\mathcal{O}(\alpha_s^2 \alpha^{4+n_\gamma})$



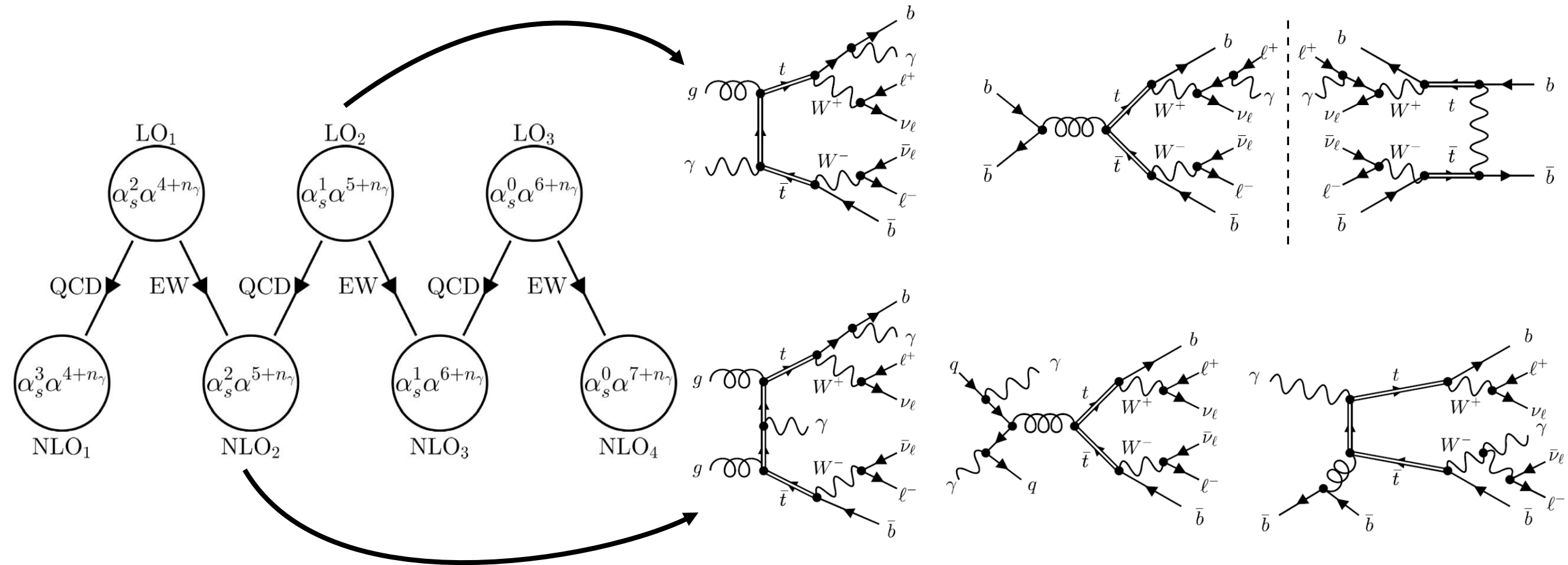
NLO<sub>1</sub> at  $\mathcal{O}(\alpha_s^3 \alpha^{4+n_\gamma})$



$$\text{NLO}_{\text{QCD}} = \text{LO}_1 + \text{NLO}_1$$



# Complete NLO



$$\text{LO} = \text{LO}_1 + \text{LO}_2 + \text{LO}_3$$

$$\text{NLO} = \text{LO}_1 + \text{LO}_2 + \text{LO}_3 + \text{NLO}_1 + \text{NLO}_2 + \text{NLO}_3 + \text{NLO}_4$$

# Computational framework

## Virtual Corrections with **Recola** (*Actis, Denner, Hofer, Lang, Scharf, Uccirati '17*) + **Collier** (*Denner, Hofer, Dittmaier, Hofer '17*)

### ■ Further Modifications in Recola

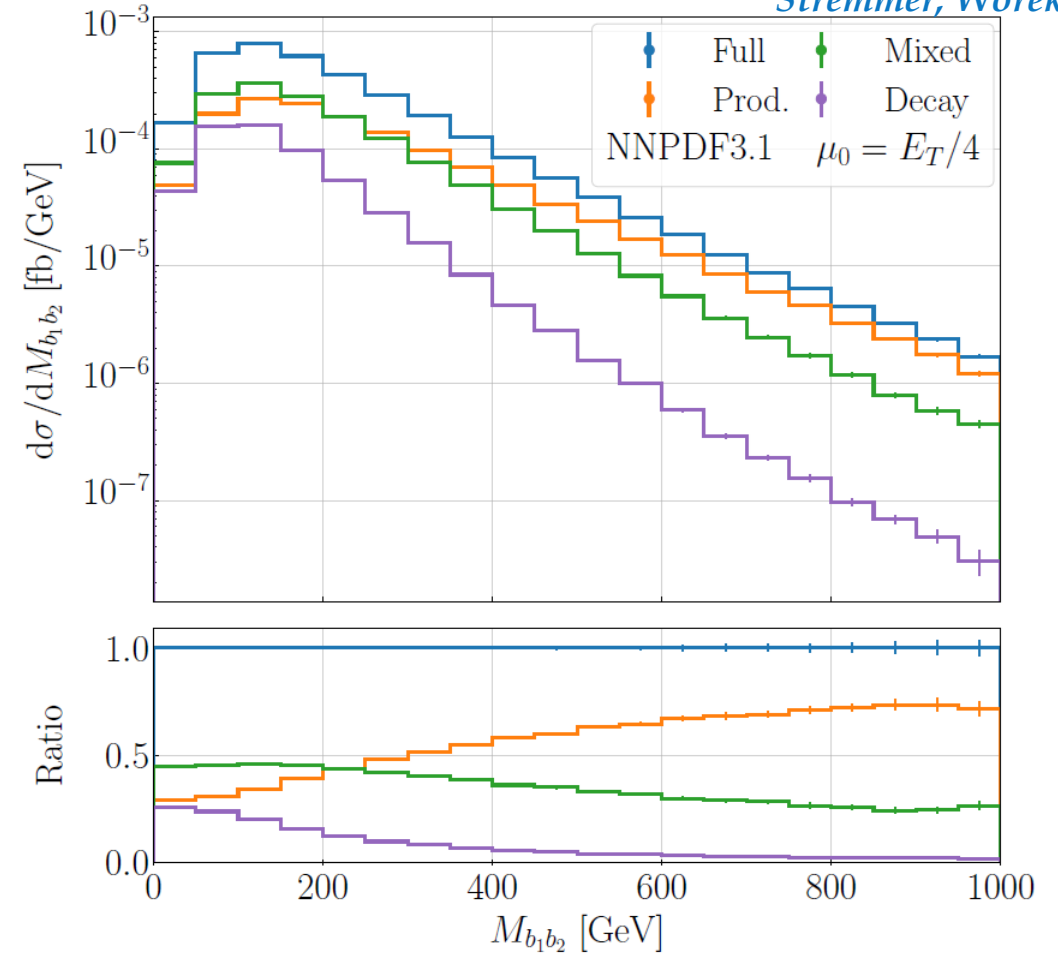
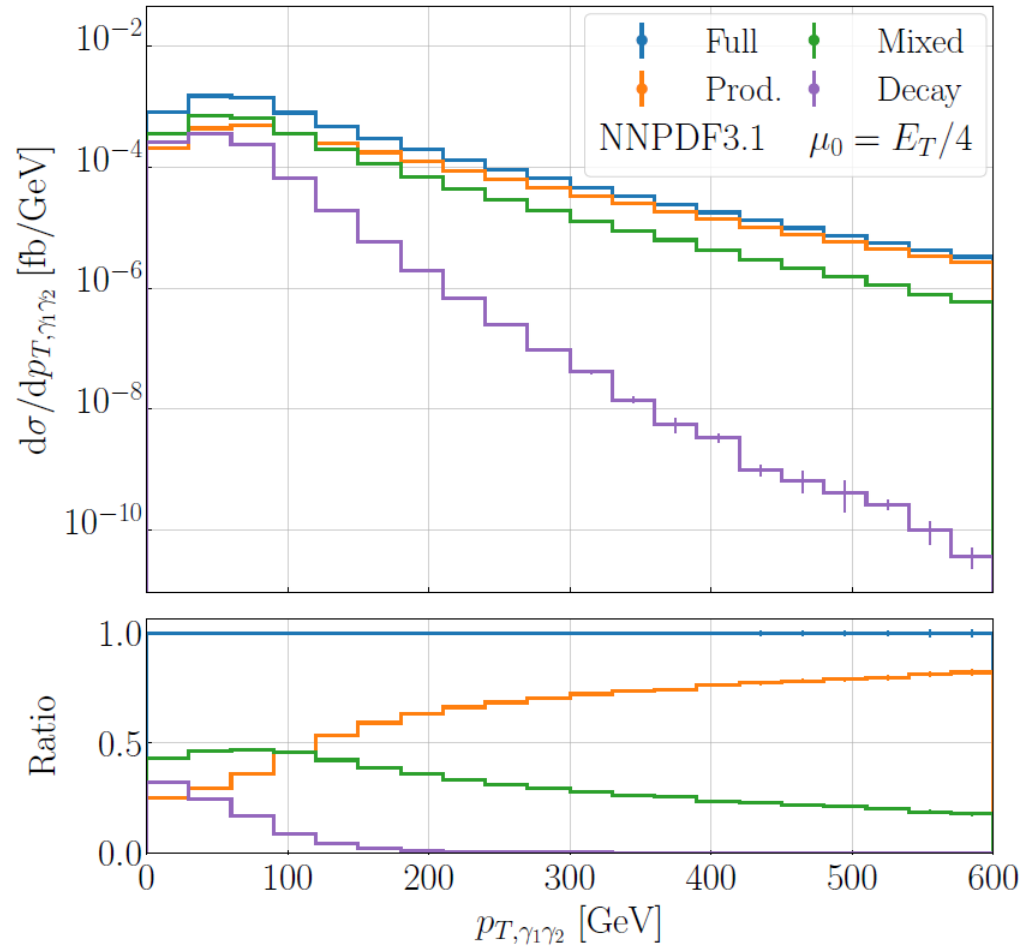
- Random polarisation method  $\sum_{\lambda} |\mathcal{M}_{\lambda}|^2 = \frac{1}{2\pi} \int_0^{2\pi} d\phi |\mathcal{M}_{\phi}|^2$
- Alternative reduction to scalar integrals with **CutTools** (*Ossola, Papadopoulos, Pittau '09*) and **OneLoop** (*van Hameren '11*)
- Mixed renormalisation of  $\alpha$ :  $\alpha^n = \alpha_{G_{\mu}}^{n-n_{\gamma}} \alpha(0)^{n_{\gamma}}$

## Real Corrections in Helac-Dipoles

- Nagy-Soper subtraction *Bevilacqua, Czakon, Kubocz, Worek '13*
  - Extended to QCD and QED-like subtraction in nested decay chains with massive/massless emitters
- Partially cross-checked with Catani-Seymour subtraction *Catani, Seymour '97* *Catani, Dittmaier, Seymour, Trocsanyi '02*
- Theoretical prediction are stored in modified **Les Houches Event Files (LHEFs)** *Bern, Dixon, Febres Cordero, Hoeche, Ita, Kosower, Maitre '14*
- Reweighting to different renormalisation/factorisation scales, PDF sets and observables

# Prompt photon distribution in $pp \rightarrow t\bar{t}\gamma\gamma$ in di-lepton channel at NLO QCD

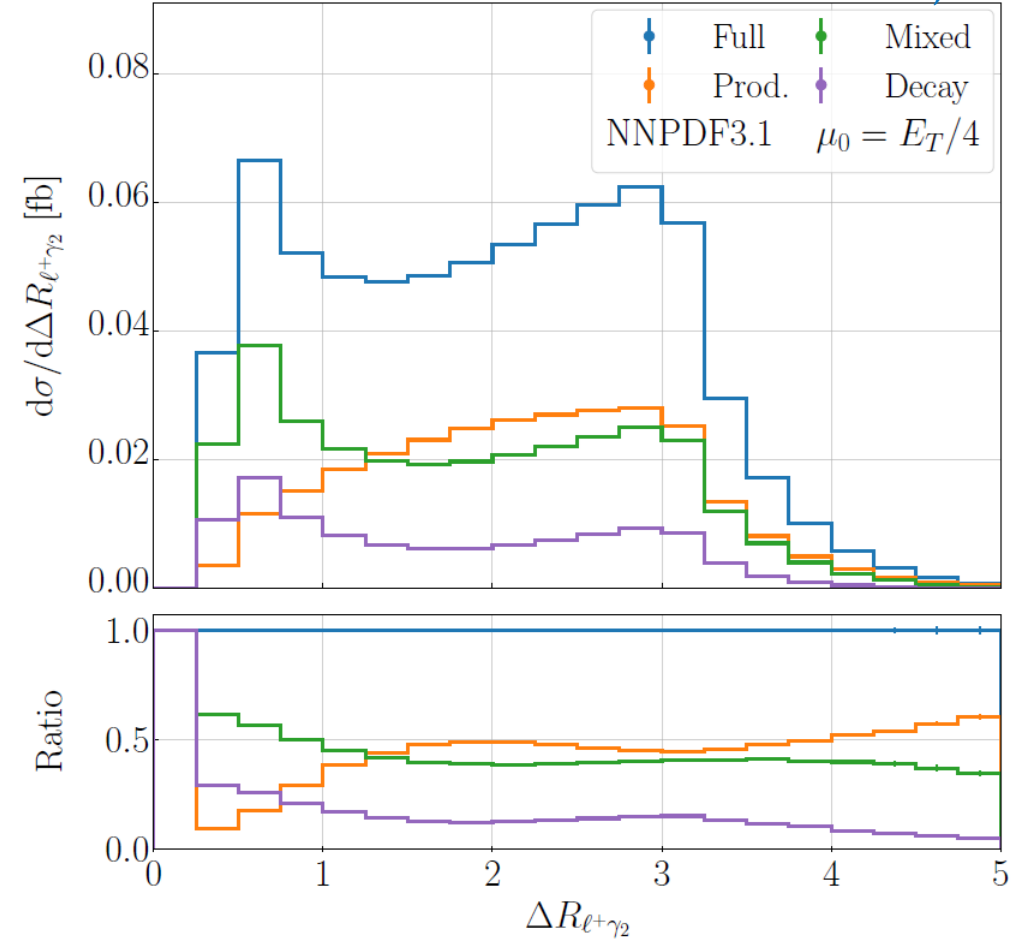
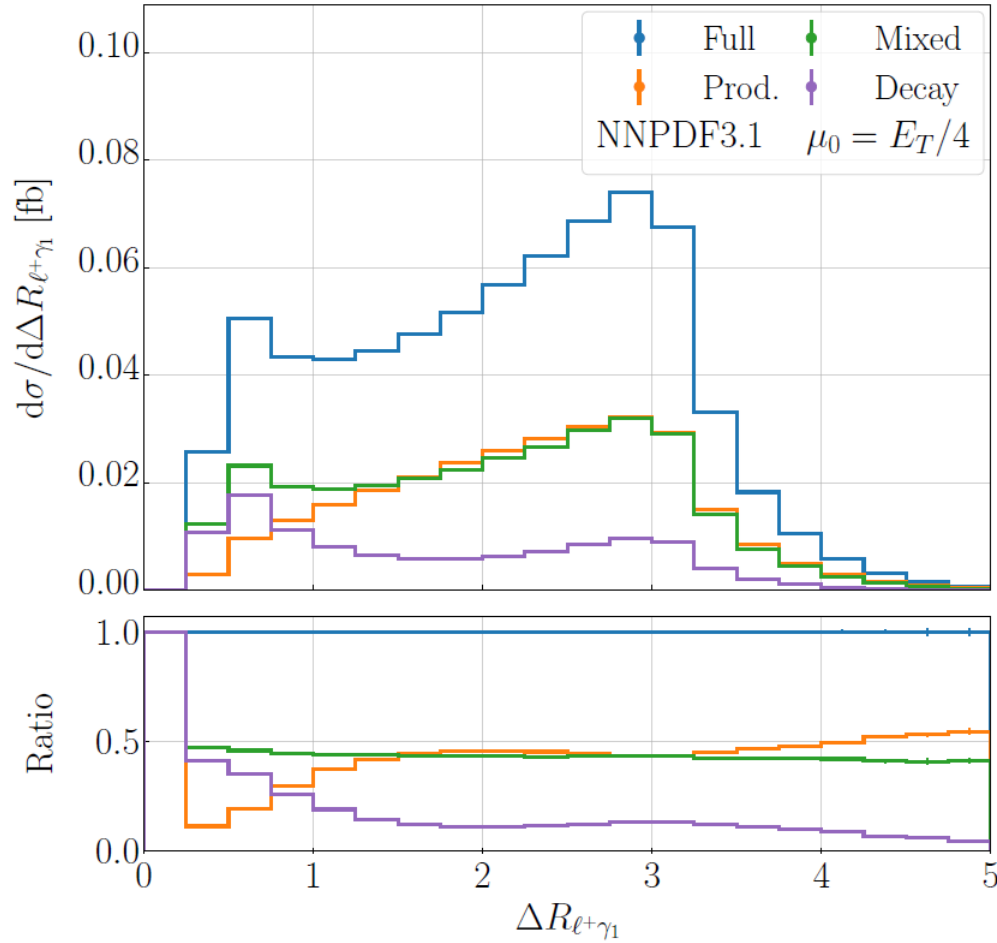
*Stremmer, Worek '23*



- Integrated level: **Full = Prod. (40%) + Mixed (44%) + Decay (16%)**
- Large contributions from photon emission in decays in bulk of distribution
- Tails dominated by **Prod. (79 – 82% of Full)**

# Prompt photon distribution in $pp \rightarrow t\bar{t}\gamma\gamma$ in di-lepton channel at NLO QCD

*Stremmer, Worek '23*

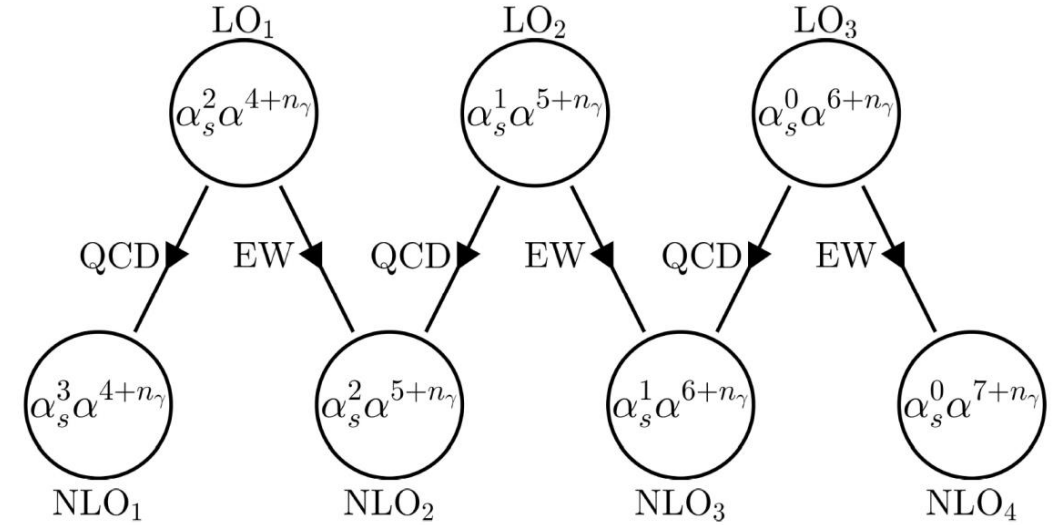


- Different peak structures for **Prod.**, **Mixed** and **Decay**
- Only sum leads to reliable predictions
- Similar conclusions in **lepton + jet** top-quark decay channel

# Complete NLO predictions for $pp \rightarrow t\bar{t}\gamma$ in di-lepton channel

		$\sigma_i$ [fb]	Ratio to LO <sub>1</sub>
LO <sub>1</sub>	$\mathcal{O}(\alpha_s^2 \alpha^5)$	55.604(8) <sup>+31.4%</sup> <sub>-22.3%</sub>	1.00
LO <sub>2</sub>	$\mathcal{O}(\alpha_s^1 \alpha^6)$	0.18775(5) <sup>+20.1%</sup> <sub>-15.4%</sub>	+0.34%
LO <sub>3</sub>	$\mathcal{O}(\alpha_s^0 \alpha^7)$	0.26970(4) <sup>+14.3%</sup> <sub>-16.9%</sub>	+0.49%
NLO <sub>1</sub>	$\mathcal{O}(\alpha_s^3 \alpha^5)$	+3.44(5)	+6.19%
NLO <sub>2</sub>	$\mathcal{O}(\alpha_s^2 \alpha^6)$	-0.1553(9)	-0.28%
NLO <sub>3</sub>	$\mathcal{O}(\alpha_s^1 \alpha^7)$	+0.2339(3)	+0.42%
NLO <sub>4</sub>	$\mathcal{O}(\alpha_s^0 \alpha^8)$	+0.001595(8)	+0.003%
LO		56.061(8) <sup>+31.2%</sup> <sub>-22.1%</sub>	1.0082
NLO <sub>QCD</sub>		59.05(5) <sup>+1.6%</sup> <sub>-5.9%</sub>	1.0620
NLO <sub>prd</sub>		59.08(5) <sup>+1.5%</sup> <sub>-5.9%</sub>	1.0626
NLO		59.59(5) <sup>+1.6%</sup> <sub>-5.9%</sub>	1.0717

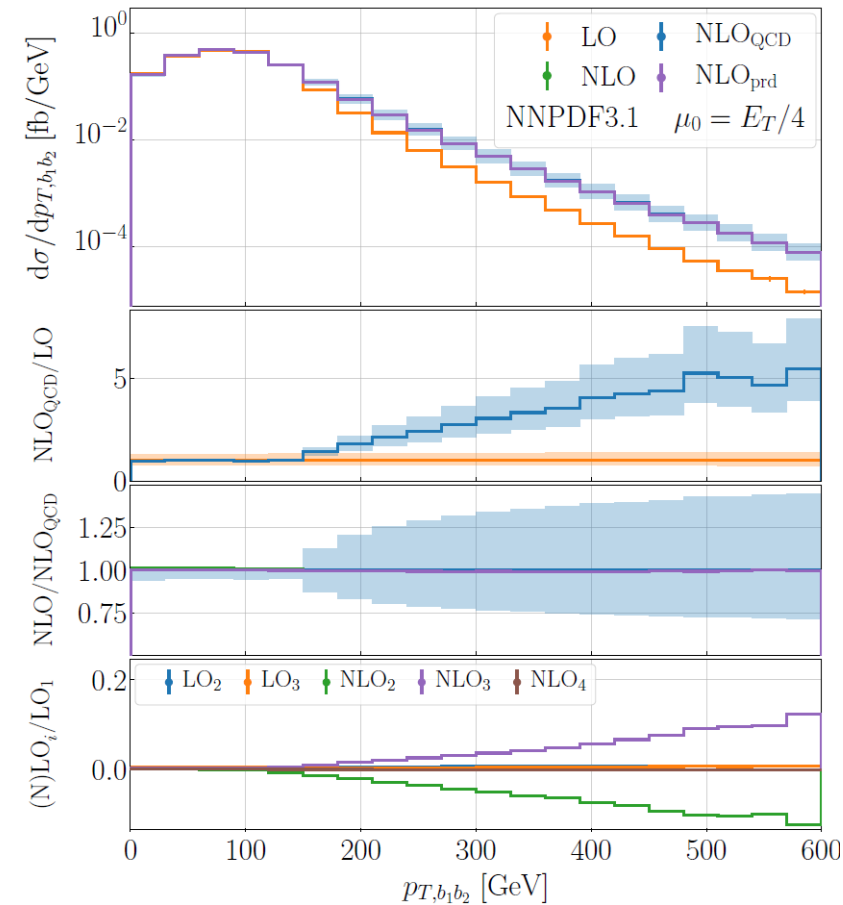
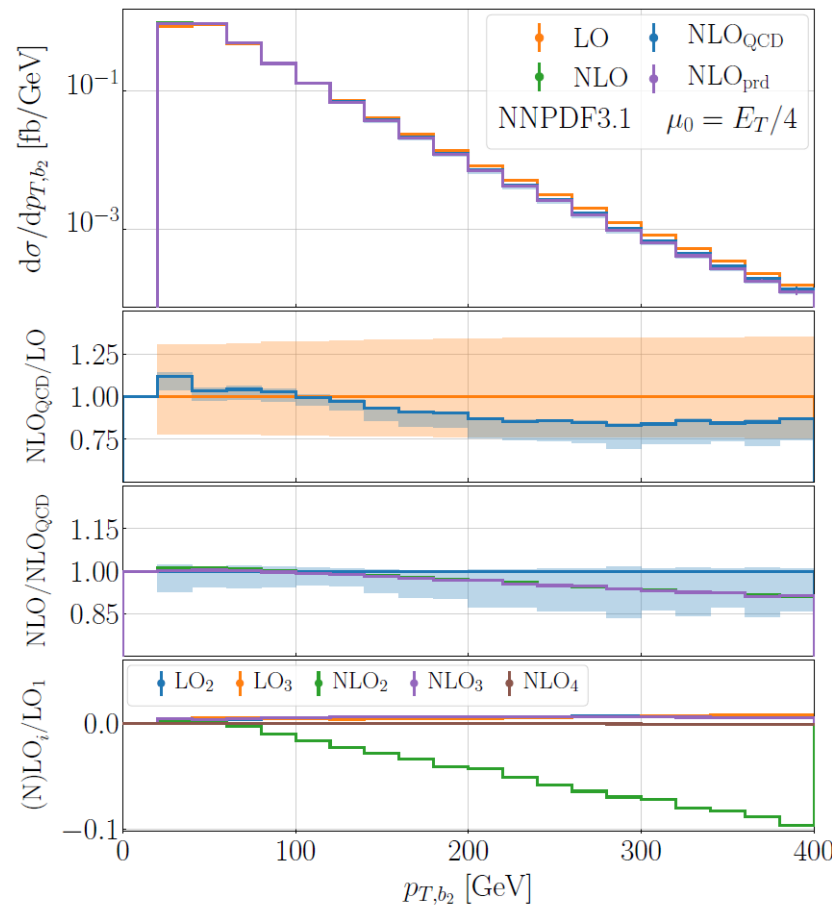
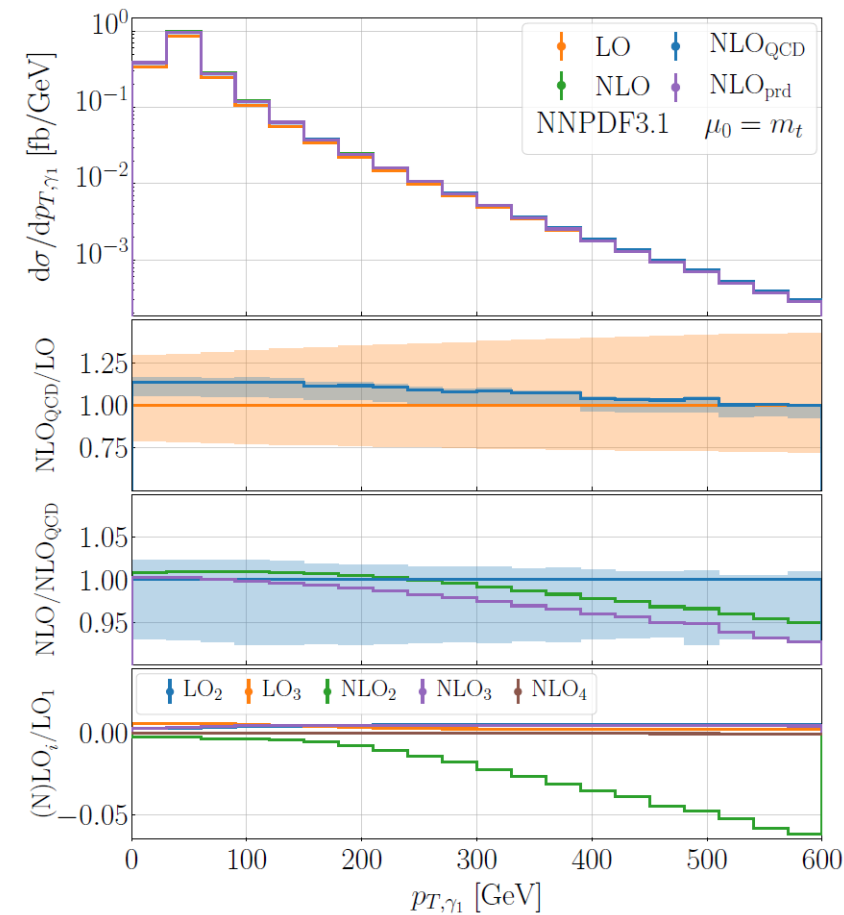
*Stremmer, Worek '24*



- Subleading LO contributions below **1%**
  - NLO corrections dominated by **NLO<sub>1</sub>**
  - Subleading NLO corrections below **1%**
  - Similar conclusions for  $pp \rightarrow t\bar{t}\gamma\gamma$
- $\text{NLO}_{\text{prd}} = \text{LO}_1 + \text{LO}_2 + \text{LO}_3 + \text{NLO}_1 + \text{NLO}_{2,\text{prd}} + \text{NLO}_{3,\text{prd}} + \text{NLO}_{4,\text{prd}}$
  - No photon radiation and higher-order corrections in top-quark decays in subleading NLO contributions

# Complete NLO predictions for $pp \rightarrow t\bar{t}\gamma$ in di-lepton channel

*Stremmer, Worek '24*

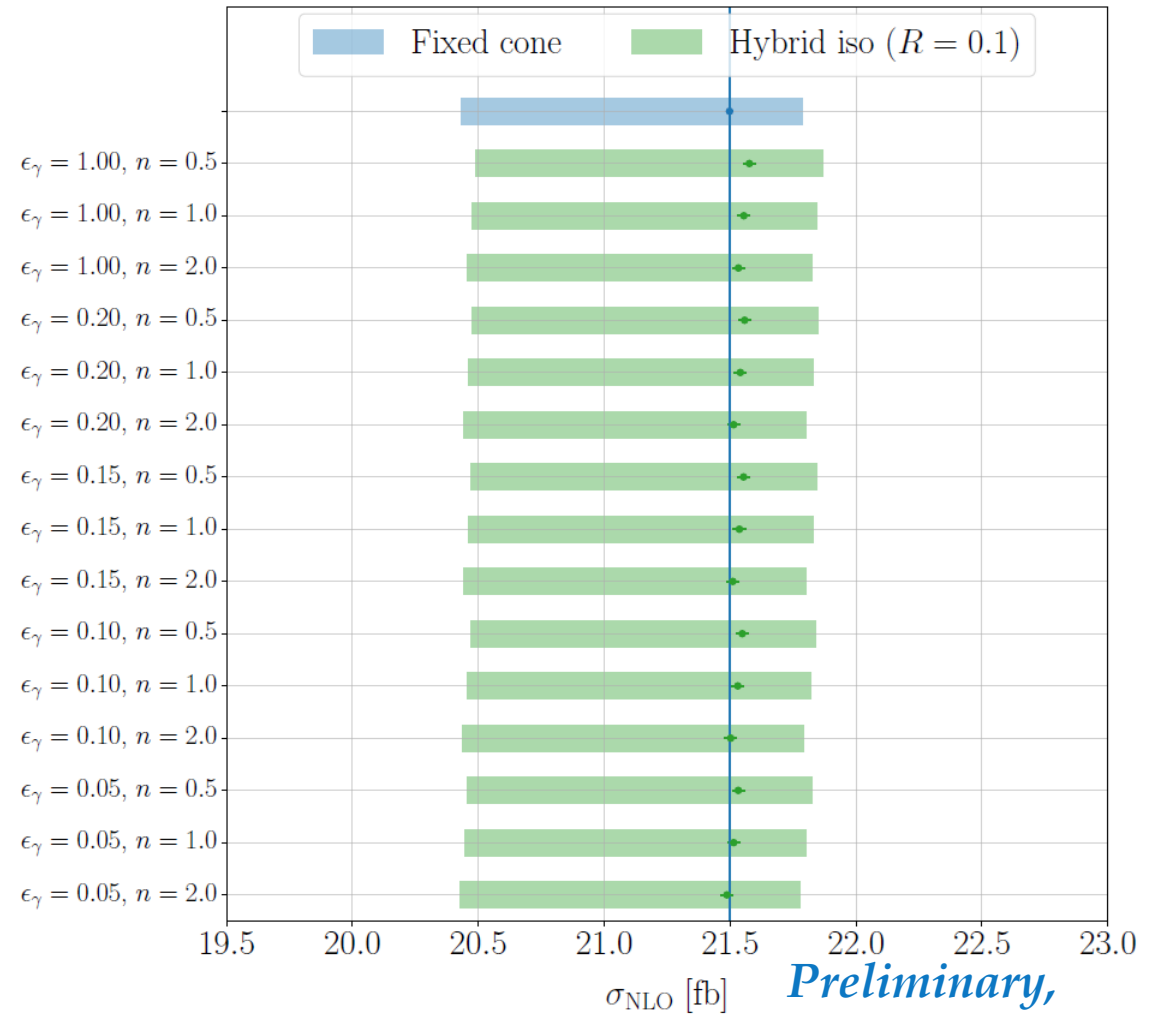
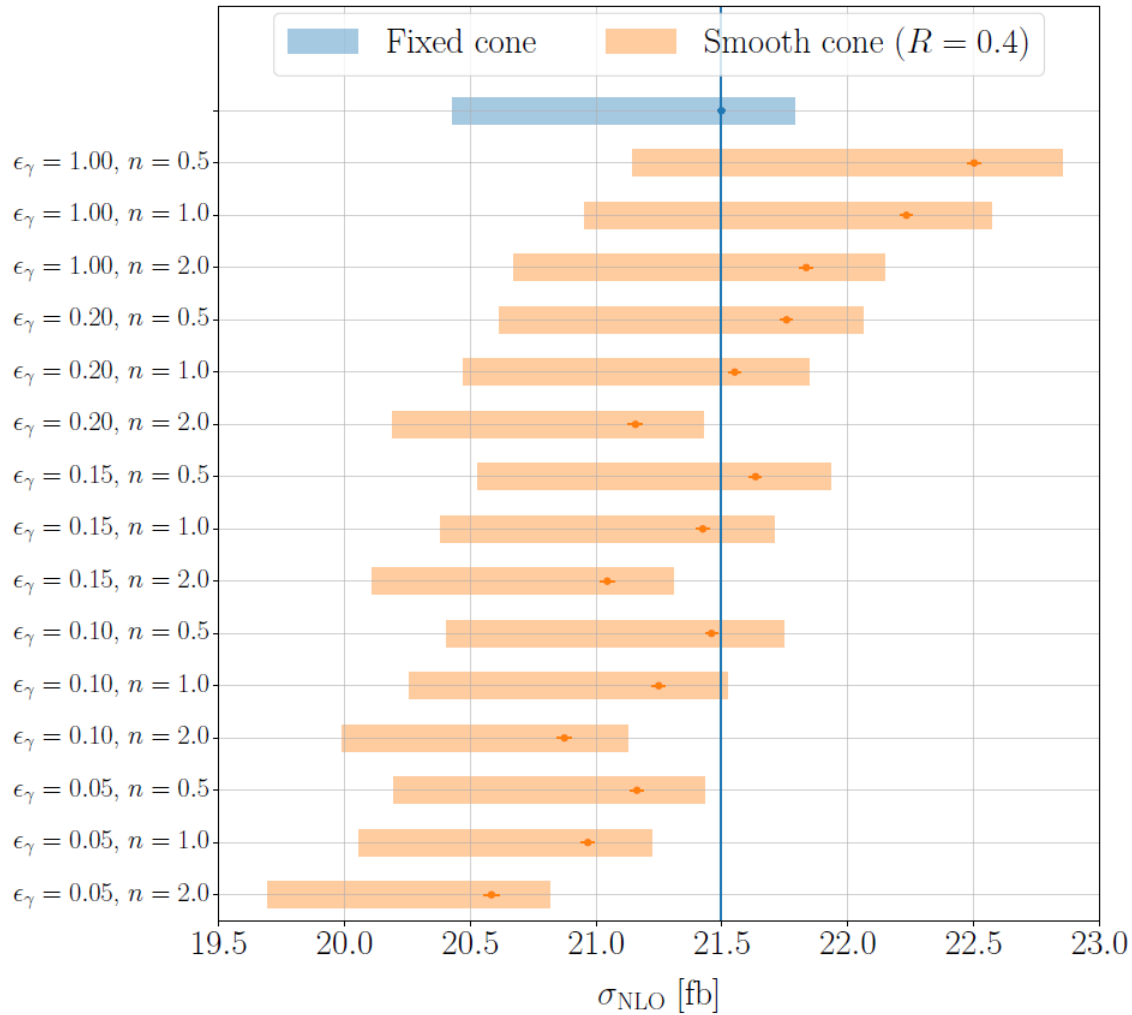


- Subleading NLO corrections as large as **10%** due to EW Sudakov logarithms in **NLO<sub>2</sub>**
- Accidental cancellations between **NLO<sub>2</sub>** and **NLO<sub>3</sub>** → **Should be considered together**
- Negligible differences between **NLO<sub>prd</sub>** and **NLO** of less than **2%**

# Photon isolation criteria

- Smooth-cone isolation *Frixione '98*
  - $E_{T,\text{had}}(R) \leq \epsilon_\gamma E_{T,\gamma} \left( \frac{1 - \cos(R)}{1 - \cos(R_{\gamma j})} \right)^n$  for all  $R \leq R_{\gamma j}$
  - Removes collinear photon-quark configurations → Removes fragmentation contribution
  - Cannot directly be used in experiments
  - Input parameters  $\epsilon_\gamma$ ,  $n$  (and  $R_{\gamma j}$ ) are arbitrary
- Fixed-cone isolation
  - $E_{T,\text{had}}(R_{\gamma j}) \leq E_{T,\text{max}}(E_{T,\gamma})$
  - Collinear photon-quark configurations allowed
  - $d\hat{\sigma}^{\gamma+X,\text{NLO}} = d\hat{\sigma}_\gamma^{\text{NLO}} + \sum_p d\hat{\sigma}_p^{\text{LO}} \otimes D_{p \rightarrow \gamma} - \frac{\alpha}{2\pi} \sum_p d\hat{\sigma}_p^{\text{LO}} \otimes \mathbf{\Gamma}_{p \rightarrow \gamma}^{(0)}$
- Hybrid photon isolation
  - First use smooth-cone isolation to remove fragmentation contribution and then the fixed-cone isolation
  - Reduces dependence on (arbitrary) input parameters in smooth-cone isolation
- Setup based on recent ATLAS analysis: [arXiv: 2403.09452 \[hep-ex\]](https://arxiv.org/abs/2403.09452)
  - $E_{T,\text{had}}(R = 0.4) < 0.022 \cdot E_{T,\gamma} + 2.45 \text{ GeV}$  and  $E_{T,\text{had}}(R = 0.2) < 0.05 \cdot E_{T,\gamma}$
  - ALEPH LO quark-to-photon fragmentation function

# Photon isolation in $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ at $\sqrt{s} = 13.6$ TeV

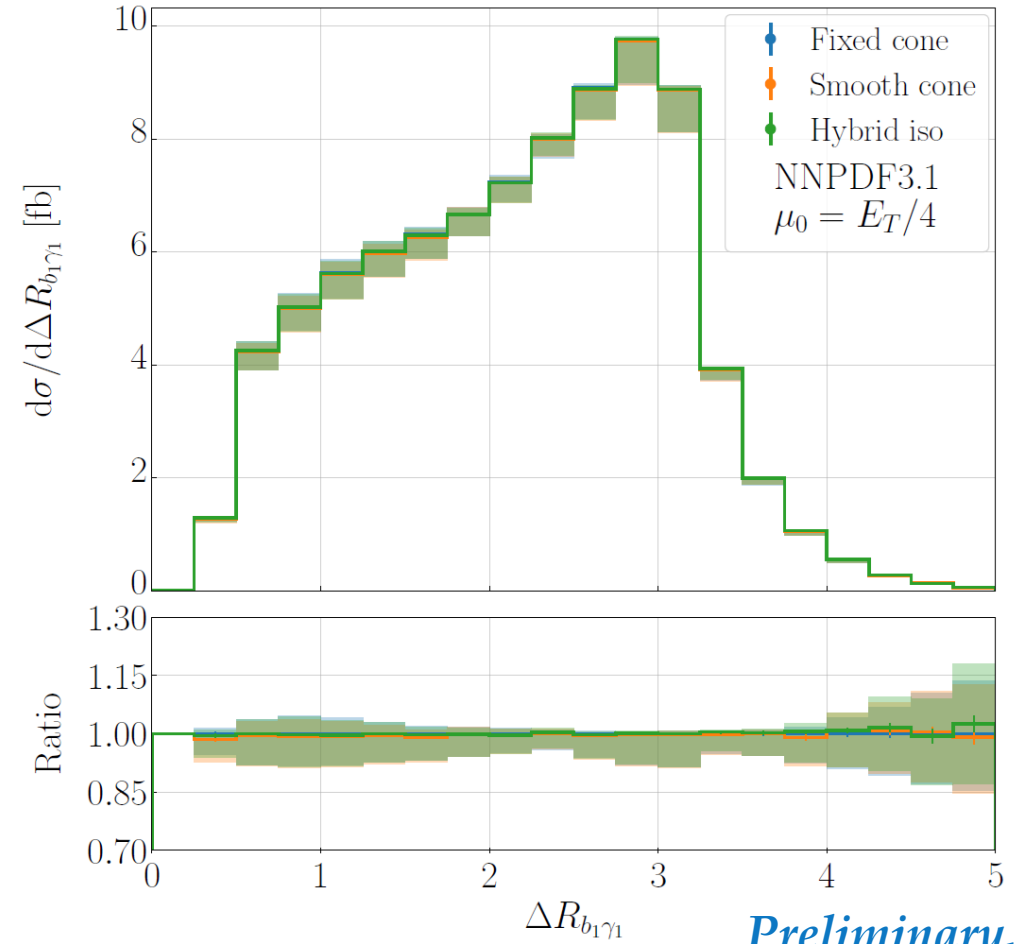
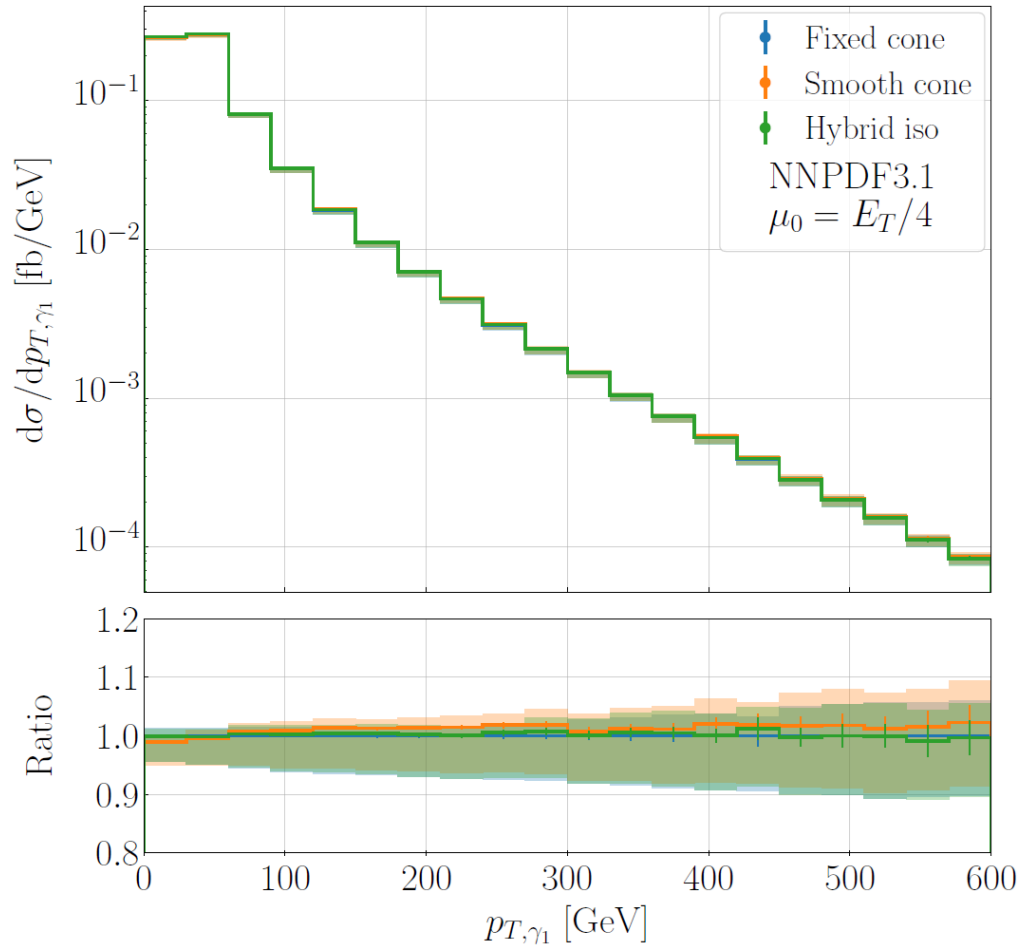


- Fragmentation contribution negligible small with  $\sim 0.2\%$
- Differences up to 5% between fixed-cone and smooth-cone isolation  $\rightarrow$  Similar to scale uncertainties
- Hybrid photon isolation reduces dependence on input parameters in (inner) smooth-cone isolation

*Preliminary,  
Stremmer, Worek*



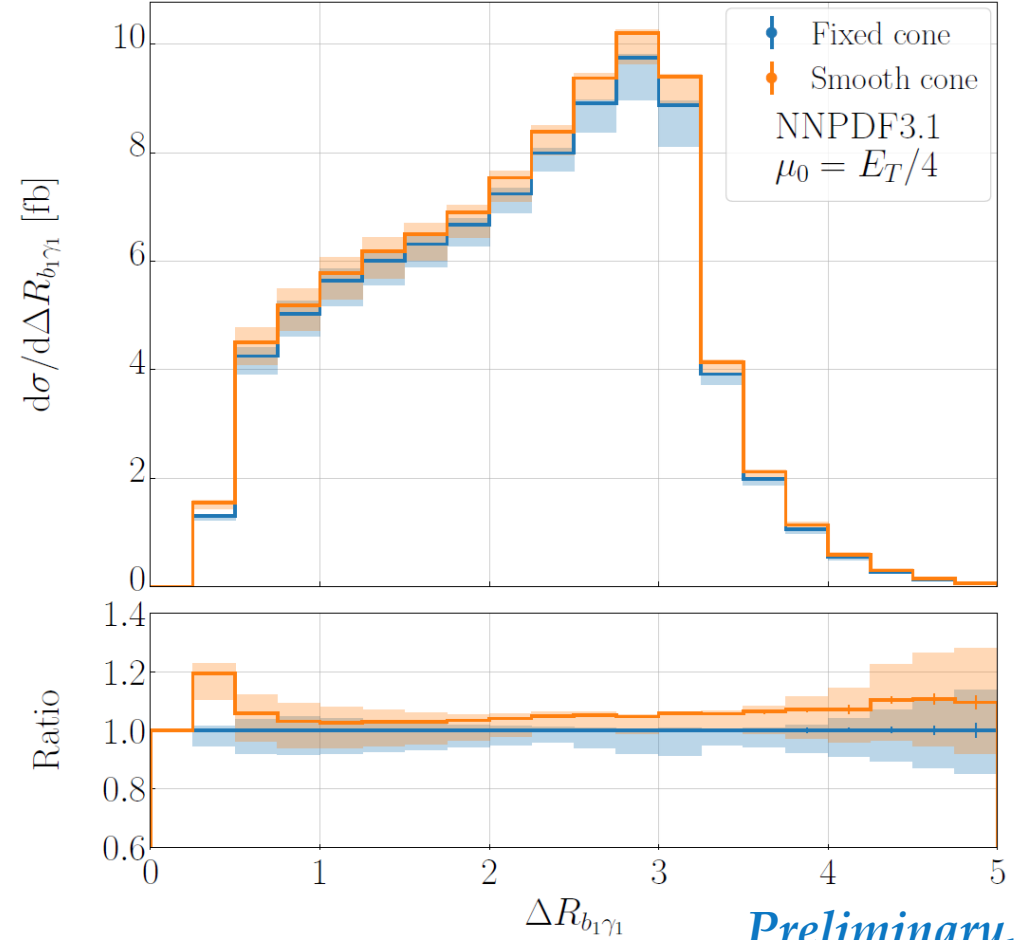
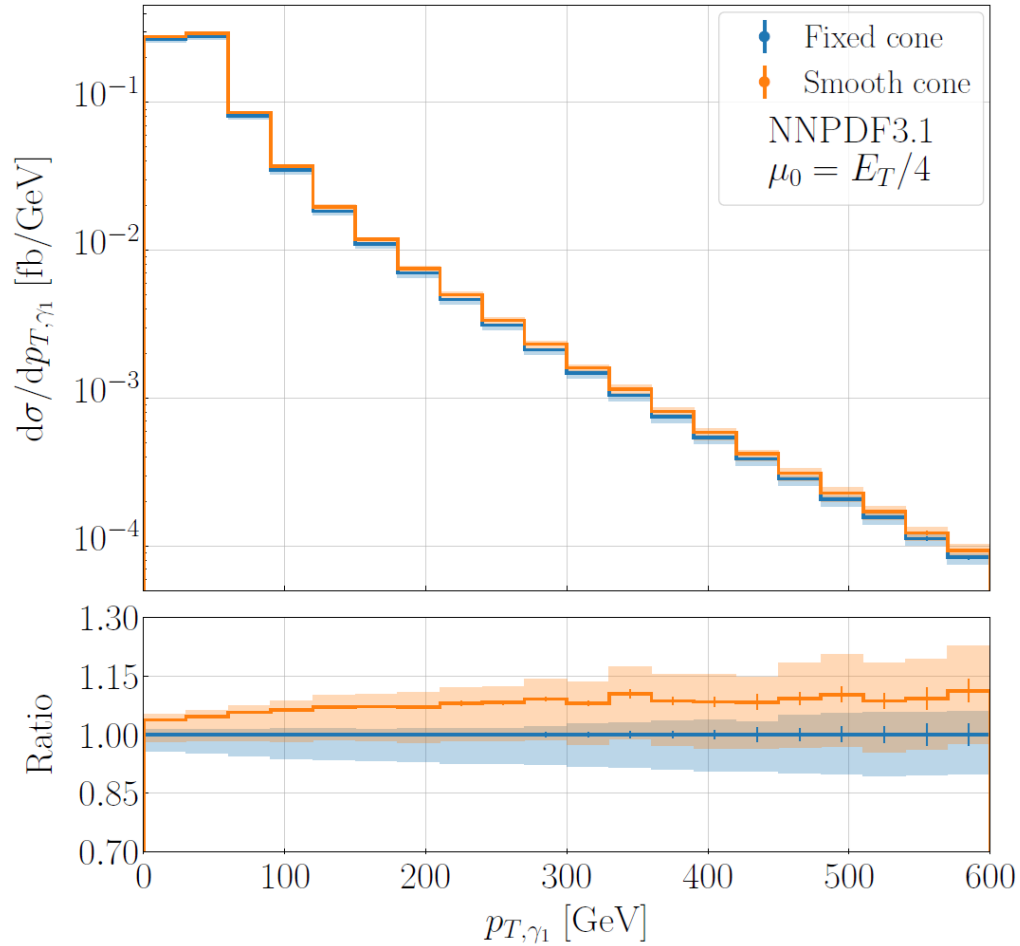
# Photon isolation in $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ at $\sqrt{s} = 13.6$ TeV



*Preliminary,  
Stremmer, Worek*

- Smooth cone isolation: ( $R = 0.4, \epsilon_\gamma = 0.10, n = 0.5$ )
- Hybrid photon isolation: ( $R = 0.1, \epsilon_\gamma = 0.10, n = 2.0$ )
- Negligible differences for tuned smooth-cone and hybrid photon isolation conditions

# Photon isolation in $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ at $\sqrt{s} = 13.6$ TeV



*Preliminary,  
Stremmer, Worek*

- Smooth cone isolation: ( $R = 0.4, \epsilon_\gamma = 1.00, n = 0.5$ )
- Significant and non-constant differences without tuning of parameters

# Conclusion

- Prompt photon distribution in  $pp \rightarrow t\bar{t}\gamma$  in the NWA
  - Only 40% of integrated fiducial cross section from Prod.
  - Only sum of all resonant contributions leads to accurate predictions
- Calculation of complete NLO corrections in  $pp \rightarrow t\bar{t}\gamma$  and  $pp \rightarrow t\bar{t}\gamma\gamma$  in the NWA
  - Enhancement of EW Sudakov logarithms in  $NLO_2 \rightarrow$  Reduction in tails up to 10%
  - Accidental cancellations between  $NLO_2$  and  $NLO_3 \rightarrow$  Should be considered together
  - $NLO_{\text{prd}}$  is good approximation  $\rightarrow$  Sufficient to include subleading NLO corrections in  $t\bar{t}\gamma(\gamma)$  production
- First calculation of  $pp \rightarrow t\bar{t}\gamma$  at NLO QCD with fixed-cone isolation
  - Small fragmentation contribution  $\sim 0.2\%$
  - Large dependence on input parameters in smooth-cone isolation  $\rightarrow$  Requires tuning of parameters
  - Basically no dependence on input parameters in hybrid photon isolation

# Outlook

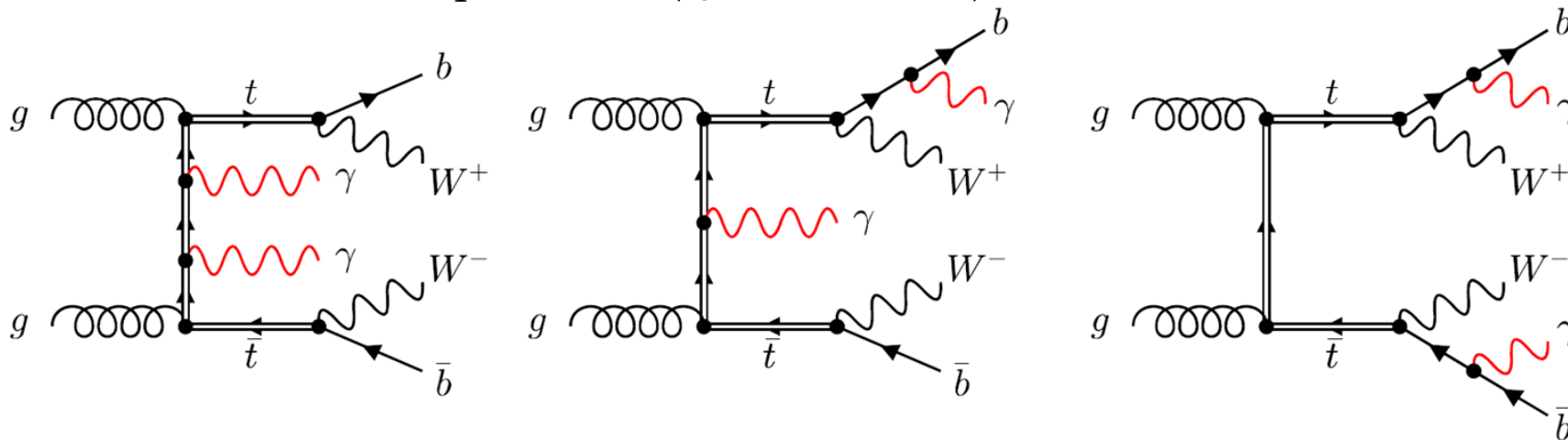
- Extend study of realistic photon isolation condition to  $pp \rightarrow t\bar{t}\gamma\gamma$  and lepton + jet top-quark decay channel
- Comparisons with experimental measurements

# Backup

# Setup

$$pp \rightarrow t\bar{t}(\gamma\gamma) \rightarrow W^+W^-b\bar{b}(\gamma\gamma) \rightarrow \begin{cases} l^+l^- \nu_e\bar{\nu}_e b\bar{b} \gamma\gamma \\ l^-\bar{\nu}_e jj b\bar{b} \gamma\gamma \end{cases} \quad l^\pm = e^\pm, \mu^\pm$$

- LHC with  $\sqrt{s} = 13$  TeV
- Calculation performed in [Narrow Width Approximation](#) preserving spin correlations
- [Photon bremsstrahlung](#) and [NLO QCD](#) corrections included in  $t\bar{t}$  production and decay
- Diagonal CKM matrix
- 5 flavour scheme ( $m_b = 0$ )
- Top-quark width treated as fixed parameter ( $\Gamma_t^{NLO}(\mu_R = m_t)$ )



# Setup of the calculation

- $G_\mu$  scheme:  $\alpha = \frac{\sqrt{2}}{\pi} G_\mu M_W^2 \left( 1 - \frac{M_W^2}{M_Z^2} \right)$
- External photon radiation with  $\alpha^{-1} = \alpha^{-1}(0) = 137.035999084$
- Renormalisation/Factorisation scale:  $\mu_R = \mu_F = \mu_0 = \frac{E_T}{4}$   $E_T = \sqrt{m_t^2 + p_{T,t}^2} + \sqrt{m_t^2 + p_{T,\bar{t}}^2} + p_{T,\gamma_1} + p_{T,\gamma_2}$
- NNPDF3.1(luxQED) NLO PDF set with  $\alpha_s(M_Z) = 0.118$

- Smooth-cone isolation *Frixione '98*

$$\sum_i E_{T,i} \Theta(R - R_{\gamma i}) \leq \epsilon_\gamma E_{T,\gamma} \left( \frac{1 - \cos(R)}{1 - \cos(R_{\gamma j})} \right)^n \quad \text{for all } R \leq R_{\gamma j}$$

- with  $R_{\gamma j} = 0.4$  and  $\epsilon_\gamma = n = 1$
- Anti- $k_T$  jet algorithm ( $R = 0.4$ ) *Cacciari, Salam, Soyez '08*

## Setup of the calculation (2)

- Exclusive in  $n_b = 2$

- Event selection:

$$p_{T,\ell} > 25 \text{ GeV}, \quad |y_\ell| < 2.5, \quad \Delta R_{\ell\ell} > 0.4,$$

$$p_{T,b} > 25 \text{ GeV}, \quad |y_b| < 2.5, \quad \Delta R_{bb} > 0.4,$$

$$p_{T,\gamma} > 25 \text{ GeV}, \quad |y_\gamma| < 2.5, \quad \Delta R_{\gamma\gamma} > 0.4,$$

$$\Delta R_{bl} > 0.4, \quad \Delta R_{\gamma l} > 0.4, \quad \Delta R_{\gamma b} > 0.4$$

- Additional cuts in lepton+jet channel:

$$p_{T,j} > 25 \text{ GeV}, \quad |y_j| < 2.5, \quad \Delta R_{jj} > 0.4,$$

$$\Delta R_{\ell j} > 0.4, \quad \Delta R_{bj} > 0.4, \quad \Delta R_{\gamma j} > 0.4$$

$$|m_W - M_{jj}| < 15 \text{ GeV}$$

- Modifications in fixed-cone isolation setup:

$$\text{▪ } n_b \geq 2, \quad p_{T,\gamma} > 20 \text{ GeV}, \quad |y_\gamma| < 2.37$$

# Integrated Fiducial cross section in di-lepton channel

$$pp \rightarrow t\bar{t}(\gamma\gamma) \rightarrow W^+W^-b\bar{b}(\gamma\gamma) \rightarrow \ell^+\ell^-\nu_e\bar{\nu}_e b\bar{b}\gamma\gamma$$

$\mu_0$		LO	NLO	$\mathcal{K} = \sigma_{\text{NLO}}/\sigma_{\text{LO}}$
	$\sigma_{\text{Full}}$ [fb]	0.13868(3) <sup>+31.2%</sup> <sub>-22.1%</sub>	0.1773(1) <sup>+1.8%</sup> <sub>-6.2%</sub>	1.28
$E_T/4$	$\sigma_{\text{Prod.}}$ [fb]	0.05399(2) <sup>+30.6%</sup> <sub>-21.7%</sub>	0.07130(6) <sup>+2.5%</sup> <sub>-7.2%</sub>	1.32
	$\sigma_{\text{Mixed}}$ [fb]	0.06022(2) <sup>+31.9%</sup> <sub>-22.5%</sub>	0.07733(8) <sup>+1.5%</sup> <sub>-6.2%</sub>	1.28
	$\sigma_{\text{Decay}}$ [fb]	0.024473(7) <sup>+30.9%</sup> <sub>-22.1%</sub>	0.02863(4) <sup>+0.9%</sup> <sub>-4.9%</sub>	1.17

*Stremmer, Worek '23*

- NLO QCD corrections  $\sim 30\%$
- Scale uncertainties reduced from 31% to 6%
- Relative size to Full: Prod. (40%), Mixed (44%) and Decay (16%)
- Internal PDF uncertainties: NNPDF3.1 1.0%, MSHT20 1.4%, CT18 2.0%



# Resonant contributions

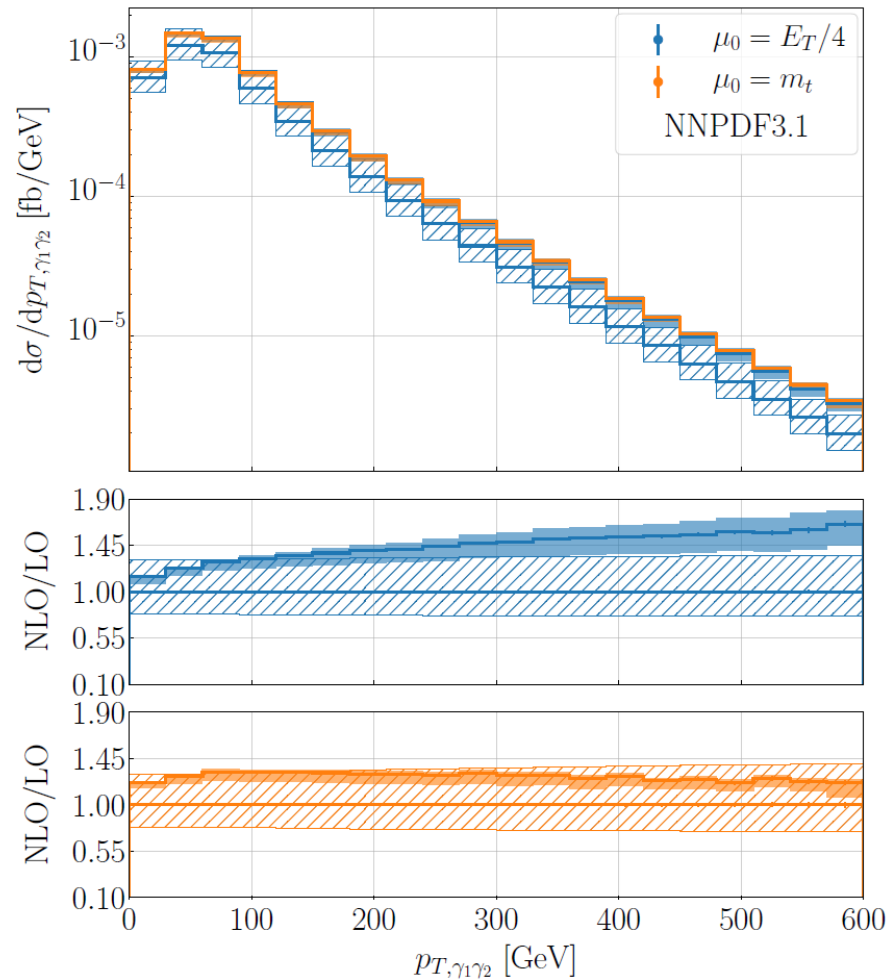
		$gg$	$gg/pp$	$q\bar{q}$	$q\bar{q}/pp$	$qg + \bar{q}g$	$(qg + \bar{q}g)/pp$
$\sigma_{\text{Full}}^{\text{NLO}}$	[fb]	0.0999(1)	56.4%	0.04307(4)	24.3%	0.03428(4)	19.3%
$\sigma_{\text{Prod.}}^{\text{NLO}}$	[fb]	0.02587(4)	36.3%	0.02672(4)	37.5%	0.01871(3)	26.2%
$\sigma_{\text{Mixed}}^{\text{NLO}}$	[fb]	0.04928(8)	63.7%	0.01408(2)	18.2%	0.01398(2)	18.1%
$\sigma_{\text{Decay}}^{\text{NLO}}$	[fb]	0.02476(4)	86.5%	0.002268(3)	7.9%	0.00160(2)	5.6%

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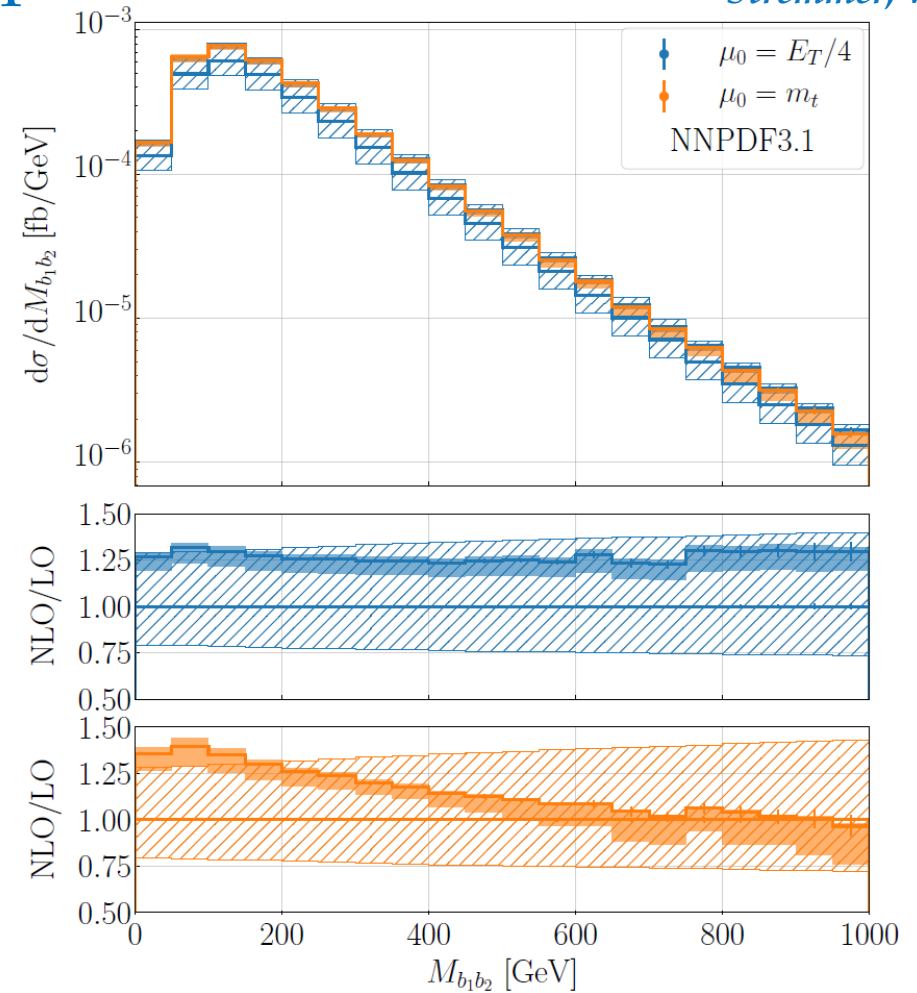
- Full dominated by  $gg$  with 56.4%
- $q\bar{q}$  channel decreases,  $gg$  channel increases in absolute size from Prod. to Mixed
- $gg$  channel suppressed for increasing number of photons in  $t\bar{t}$  production
- Conclusions also hold in lepton + jet top-quark decay channel

# Differential Fiducial cross section in di-lepton channel

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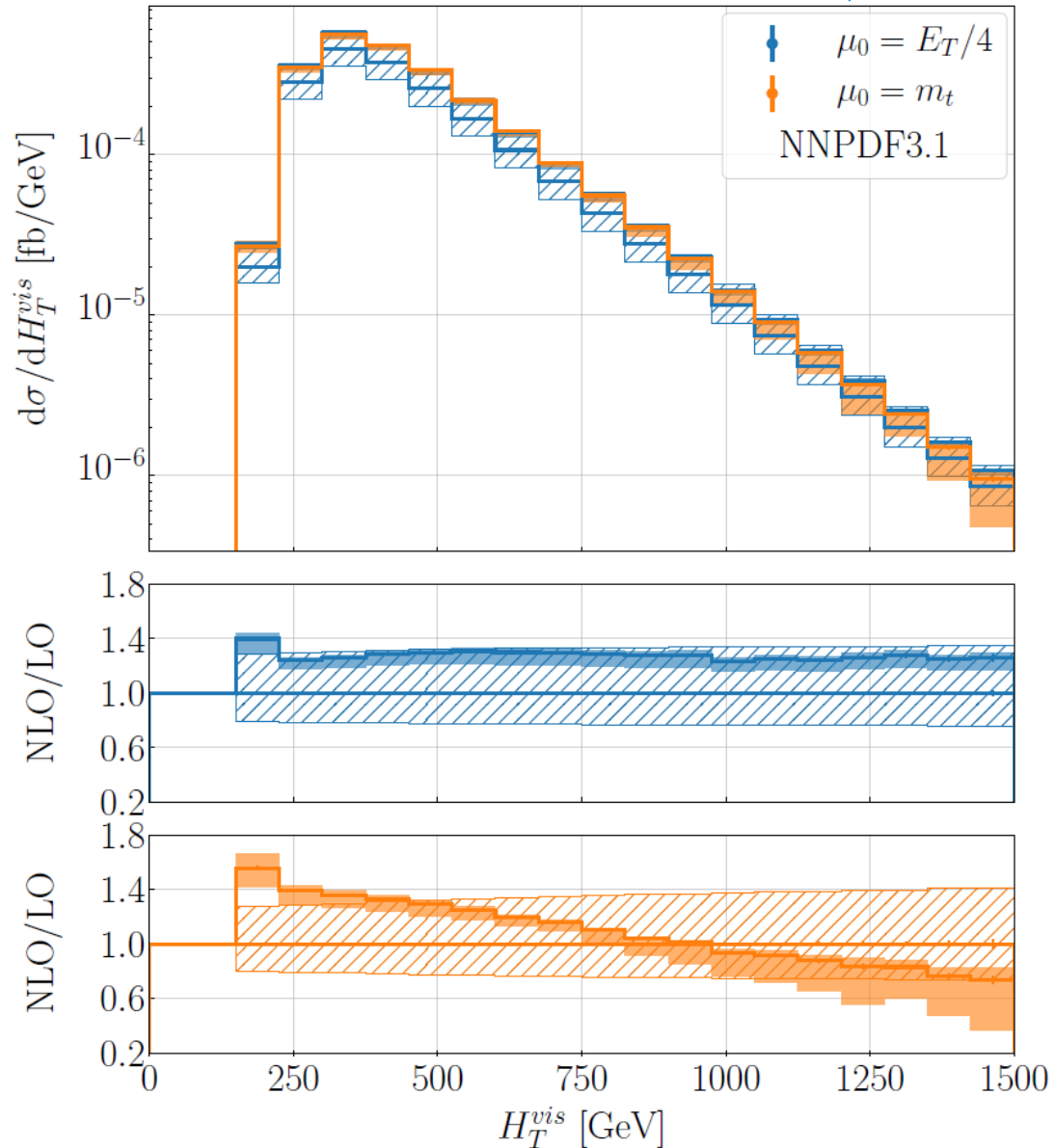
- NLO QCD corrections up to 65%
- Smaller corrections for  $\mu_0 = m_t$
- Scale uncertainties 5% – 13%



- NLO QCD corrections ~25% – 30%
- Scale uncertainties reduced from ~35% to 5% – 8%
- Increasing scale uncertainties in tails for  $\mu_0 = m_t$

# Differential Fiducial cross section in di-lepton channel

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$$H_T^{vis} = p_{T,\ell^+} + p_{T,\ell^-} + p_{T,b_1} + p_{T,b_2} + p_{T,\gamma_1} + p_{T,\gamma_2}$$

- Fixed scale unstable for general dimensionful observables:
  - Large shape distortions
  - NLO scale uncertainties, up to 50%, exceeding LO ones

→ Dynamical scale in general required

# Integrated Fiducial cross section in lepton + jet channel

$$|m_W - M_{jj}| < 15 \text{ GeV}$$

$\mu_0$		LO	NLO	$\mathcal{K} = \sigma_{\text{NLO}}/\sigma_{\text{LO}}$
$E_T/4$	$\sigma_{\text{Full}}$ [fb]	$0.24214(4)^{+31.1\%}_{-22.0\%}$	$0.2973(3)^{+1.9\%}_{-5.4\%}$	1.23
	$\sigma_{\text{Prod.}}$ [fb]	$0.11960(3)^{+30.5\%}_{-21.6\%}$	$0.1405(2)^{+2.1\%}_{-4.6\%}$	1.17
	$\sigma_{\text{Mixed}}$ [fb]	$0.09632(3)^{+31.9\%}_{-22.5\%}$	$0.1205(2)^{+1.5\%}_{-5.7\%}$	1.25
	$\sigma_{\text{Decay}}$ [fb]	$0.026230(9)^{+30.9\%}_{-22.1\%}$	$0.03629(7)^{+3.3\%}_{-7.7\%}$	1.38

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- NLO corrections  $\sim 23\%$ , scale uncertainties reduced from  $\sim 31\%$  to  $\sim 5\%$
- **Prod.** increased from  $40\%$  (**di-lepton**) to  $48\%$  (**lepton + jet**) because of by additional cut

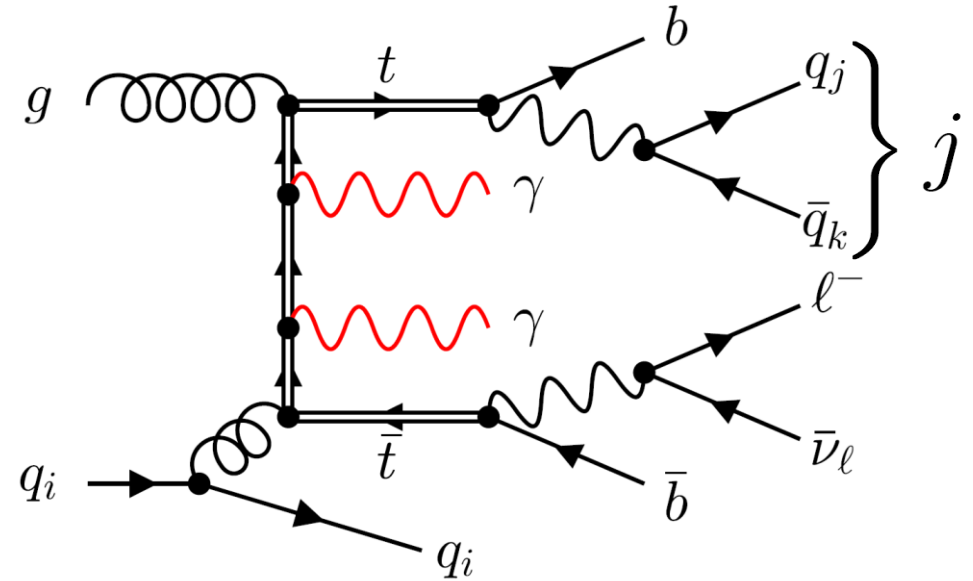
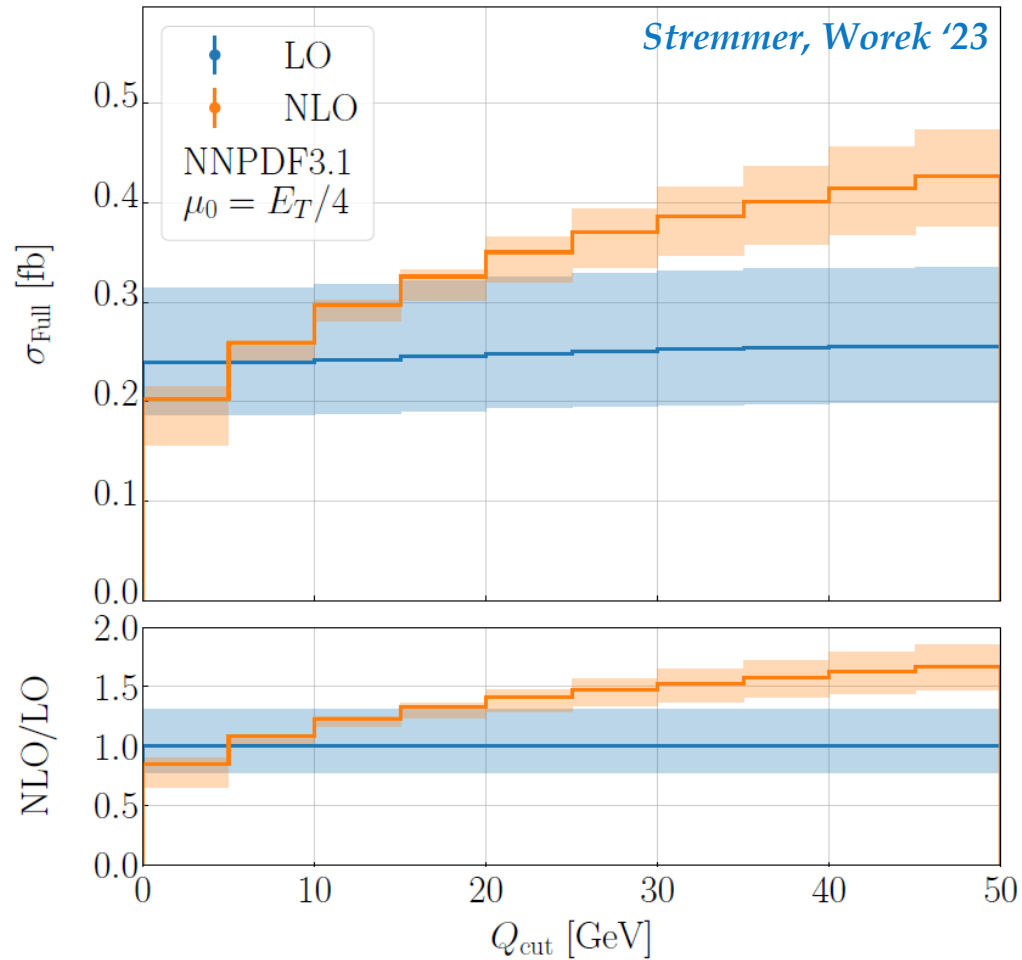
$$\sigma_{\text{Full}}^{\text{NLO}}(\epsilon_\gamma = 0.5) = 0.2832(7) \text{ fb}$$

$$\sigma_{\text{Full}}^{\text{NLO}}(E_{T\gamma} \epsilon_\gamma = 10 \text{ GeV}) = 0.2666(8) \text{ fb}$$

$$\sum_i E_{T_i} \Theta(R - R_{\gamma i}) \leq \epsilon_\gamma E_{T\gamma} \left( \frac{1 - \cos(R)}{1 - \cos(R_{\gamma j})} \right)^n$$

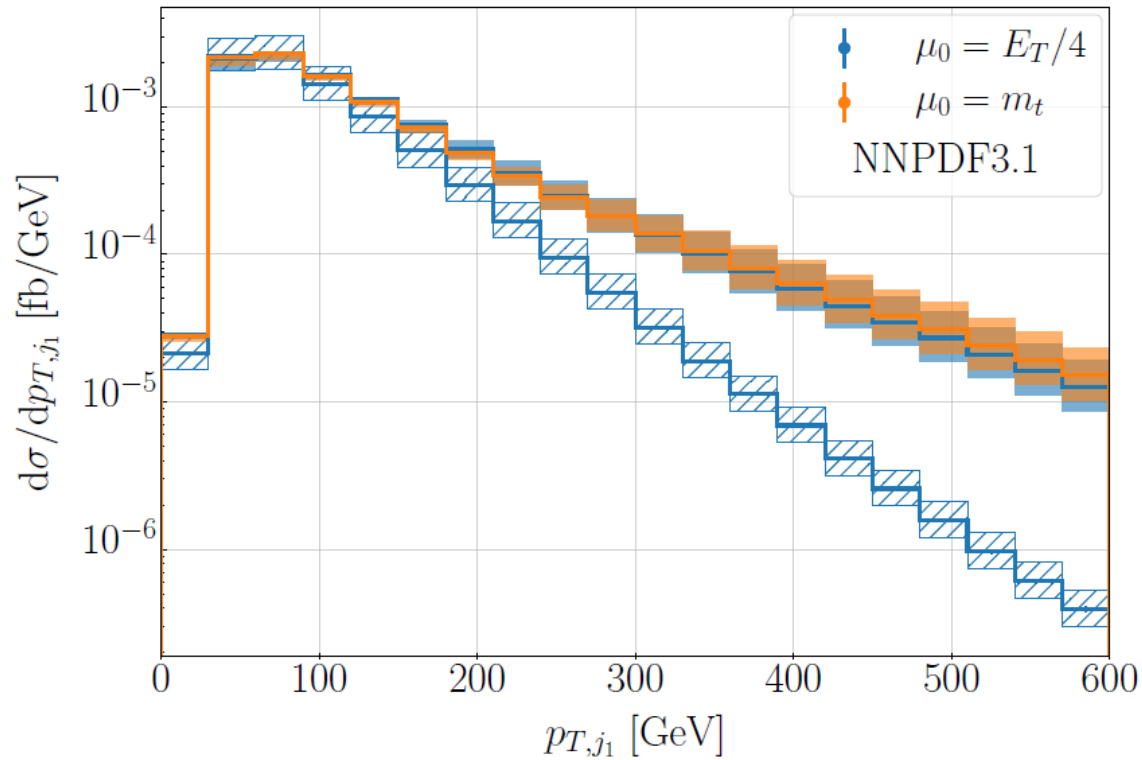
- Significant deviations ( $5\% - 10\%$ ) between different input parameters in Smooth photon isolation prescription

# Integrated Fiducial cross section in lepton + jet channel

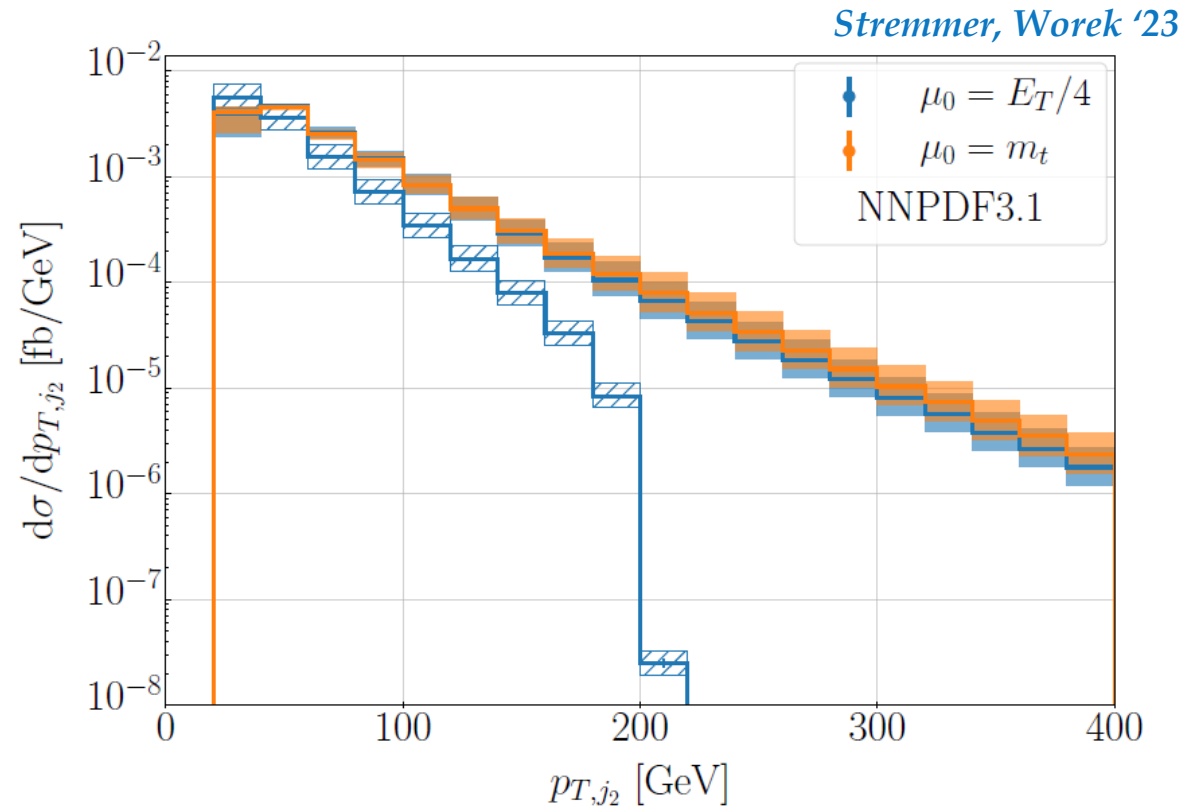


- Large NLO QCD corrections of  $\sim 140\%$  for  $Q_{\text{cut}} \rightarrow \infty$  caused by hard radiation in production stage
- NLO QCD corrections drastically reduced by additional  $|m_W - M_{jj}| < Q_{\text{cut}}$

# Differential Fiducial cross section in lepton + jet channel



- Huge NLO QCD corrections caused by hard jets in the production stage
- Scale uncertainties in tails  $\sim 50\%$

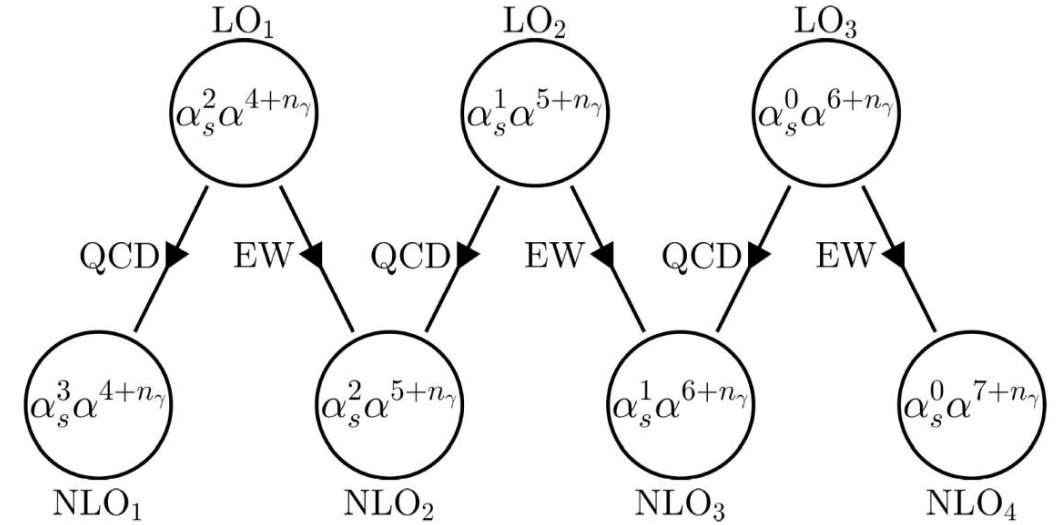


- LO spectrum limited by finite W boson mass  
 $p_{T,j_2,max} \sim m_W / \Delta R_{jj} \sim 203$  GeV
- Scale uncertainties in tails  $\sim 50\%$

# Complete NLO predictions for $pp \rightarrow t\bar{t}\gamma\gamma$ in di-lepton channel

		$\sigma_i$ [fb]	Ratio to LO <sub>1</sub>
LO <sub>1</sub>	$\mathcal{O}(\alpha_s^2\alpha^6)$	0.15928(3) <sup>+31.3%</sup> <sub>-22.1%</sub>	1.00
LO <sub>2</sub>	$\mathcal{O}(\alpha_s^1\alpha^7)$	0.0003798(2) <sup>+25.8%</sup> <sub>-19.2%</sub>	+0.24%
LO <sub>3</sub>	$\mathcal{O}(\alpha_s^0\alpha^8)$	0.0010991(2) <sup>+10.6%</sup> <sub>-13.1%</sub>	+0.69%
NLO <sub>1</sub>	$\mathcal{O}(\alpha_s^3\alpha^6)$	+0.0110(2)	+6.89%
NLO <sub>2</sub>	$\mathcal{O}(\alpha_s^2\alpha^7)$	-0.00233(2)	-1.46%
NLO <sub>3</sub>	$\mathcal{O}(\alpha_s^1\alpha^8)$	+0.000619(1)	+0.39%
NLO <sub>4</sub>	$\mathcal{O}(\alpha_s^0\alpha^9)$	-0.0000166(2)	-0.01%
LO		0.16076(3) <sup>+30.9%</sup> <sub>-21.9%</sub>	1.0093
NLO <sub>QCD</sub>		0.1703(2) <sup>+1.9%</sup> <sub>-6.2%</sub>	1.0690
NLO <sub>prd</sub>		0.1694(2) <sup>+1.7%</sup> <sub>-5.9%</sub>	1.0637
NLO		0.1700(2) <sup>+1.8%</sup> <sub>-6.0%</sub>	1.0674

*Stremmer, Worek '24*

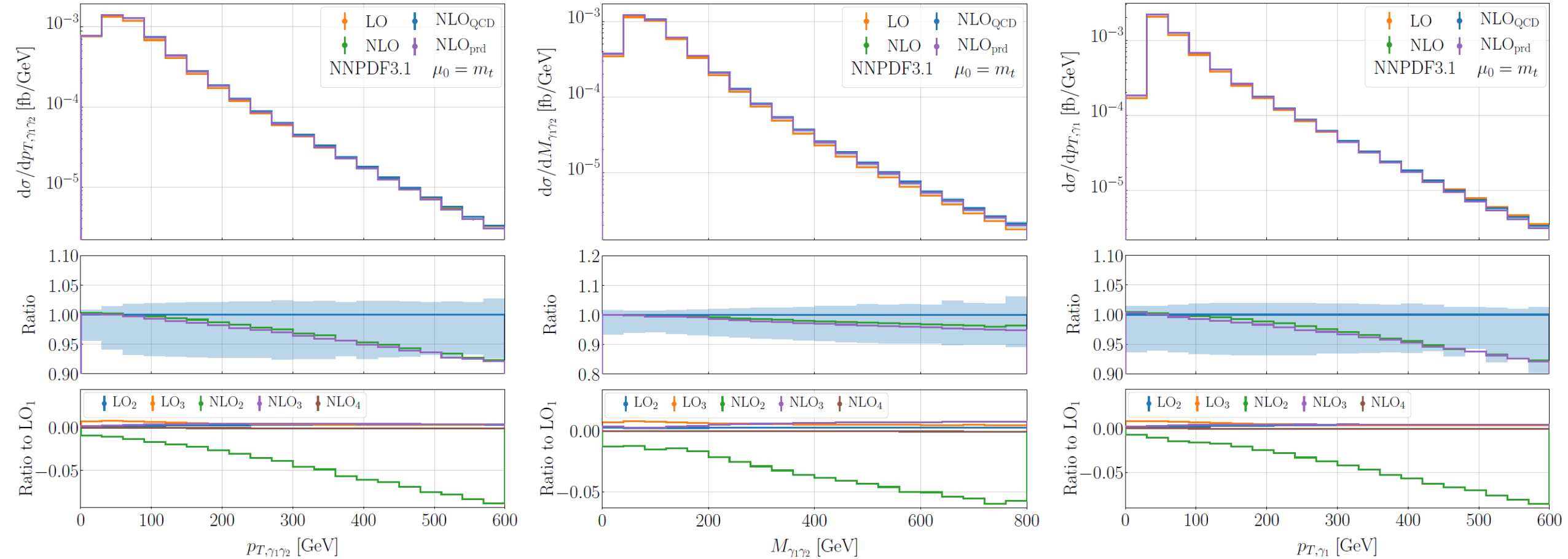


- Subleading LO contributions  $\sim 1\%$
- NLO corrections dominated by **NLO<sub>1</sub>**
- Subleading NLO corrections  $\sim 1\%$

- **$\text{NLO}_{\text{prd}} = \text{LO}_1 + \text{LO}_2 + \text{LO}_3 + \text{NLO}_1 + \text{NLO}_{2,\text{prd}} + \text{NLO}_{3,\text{prd}} + \text{NLO}_{4,\text{prd}}$**
- No photon radiation and higher-order corrections in top-quark decays in subleading NLO contributions

# Complete NLO predictions for $pp \rightarrow t\bar{t}\gamma\gamma$ in di-lepton channel

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- Subleading NLO corrections as large as **10%** due to EW Sudakov logarithms in **NLO<sub>2</sub>**
- Accidental cancellations between **NLO<sub>2</sub>** and **NLO<sub>3</sub>**
- Negligible differences between **NLO<sub>prcd</sub>** and **NLO** of less than **2%**