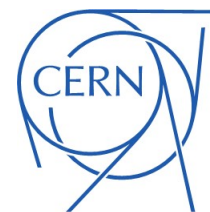


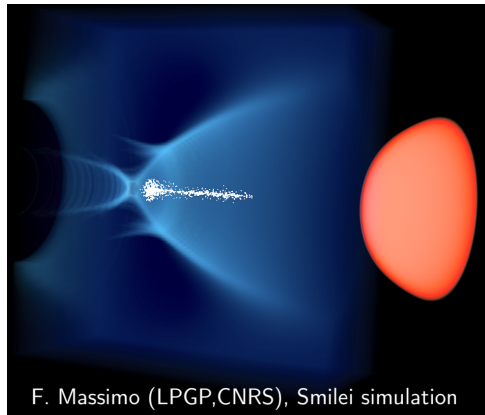
# Developing Expectations with Plasma Simulations

February 2024  
John Farmer, MPP



# State-of-the-art Simulations

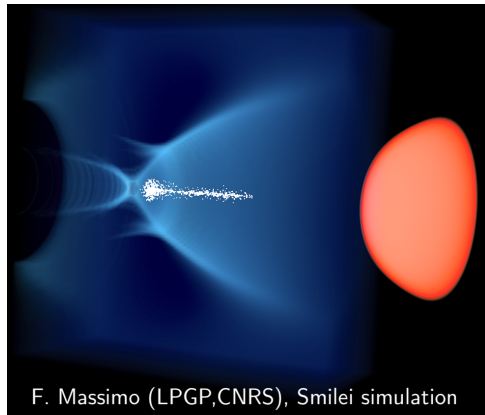
## Laser-driven wakefield acceleration (EARLI)



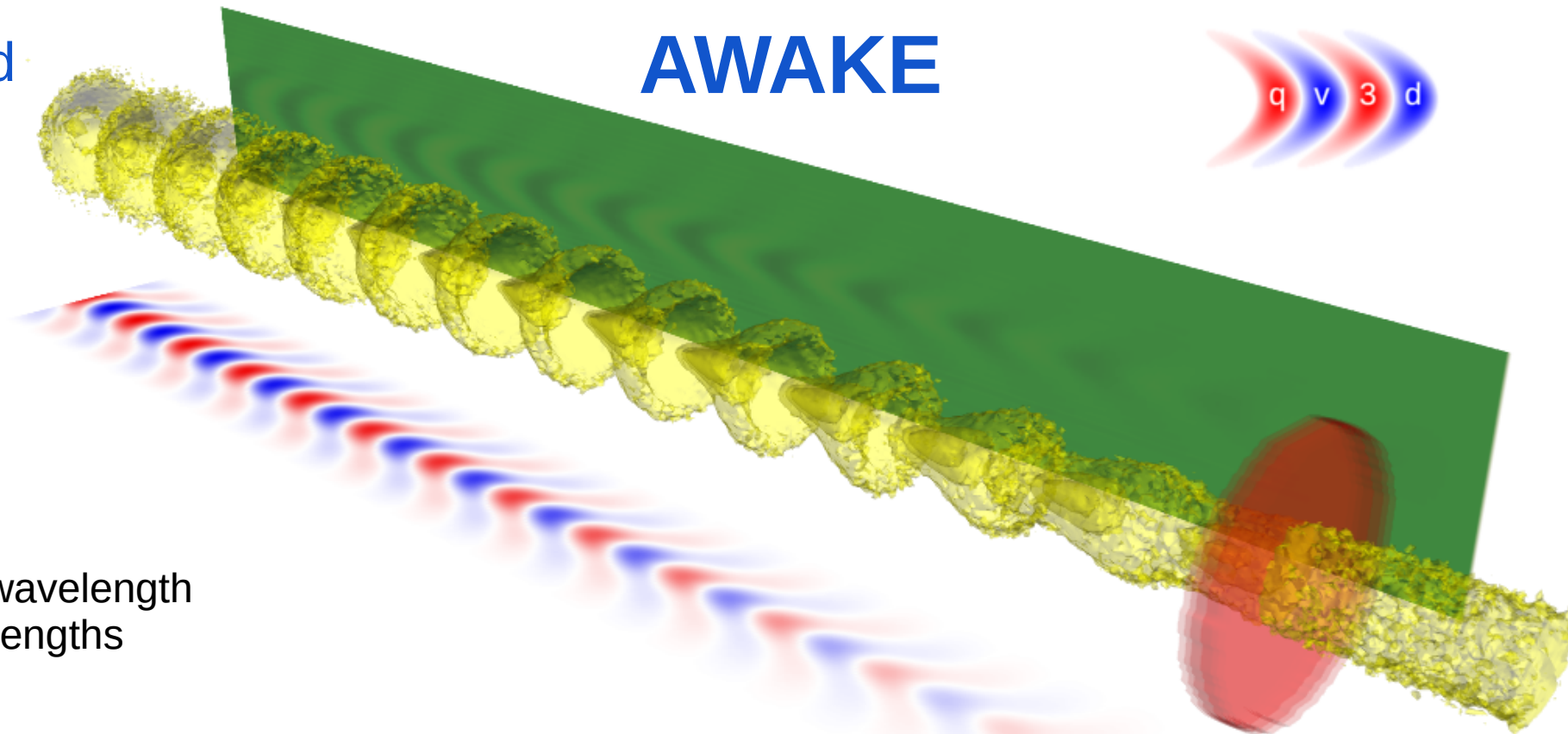
- wakefield structure  $\sim 1$  plasma wavelength
- propagate  $\sim 1000$  plasma wavelengths

# State-of-the-art Simulations

## Laser-driven wakefield acceleration (EARLI)



- wakefield structure  $\sim 1$  plasma wavelength
- propagate  $\sim 1000$  plasma wavelengths



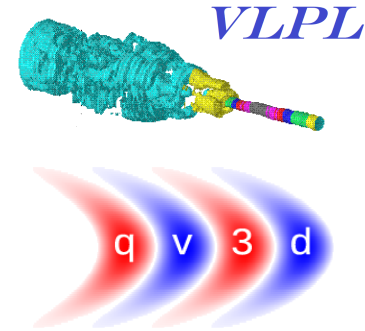
- wakefield structure 100s of plasma wavelengths
- propagate  $\sim 10,000$  plasma wavelengths
- $\sim 5$ Mch with conventional codes

Moschuering *et al.* (2019)

# State-of-the-art Simulations



IST Lisbon  
Full EM-PIC  
in 2D and 3D



HHU Düsseldorf  
Full EM-PIC in 3D  
Quasistatic PIC in 3D

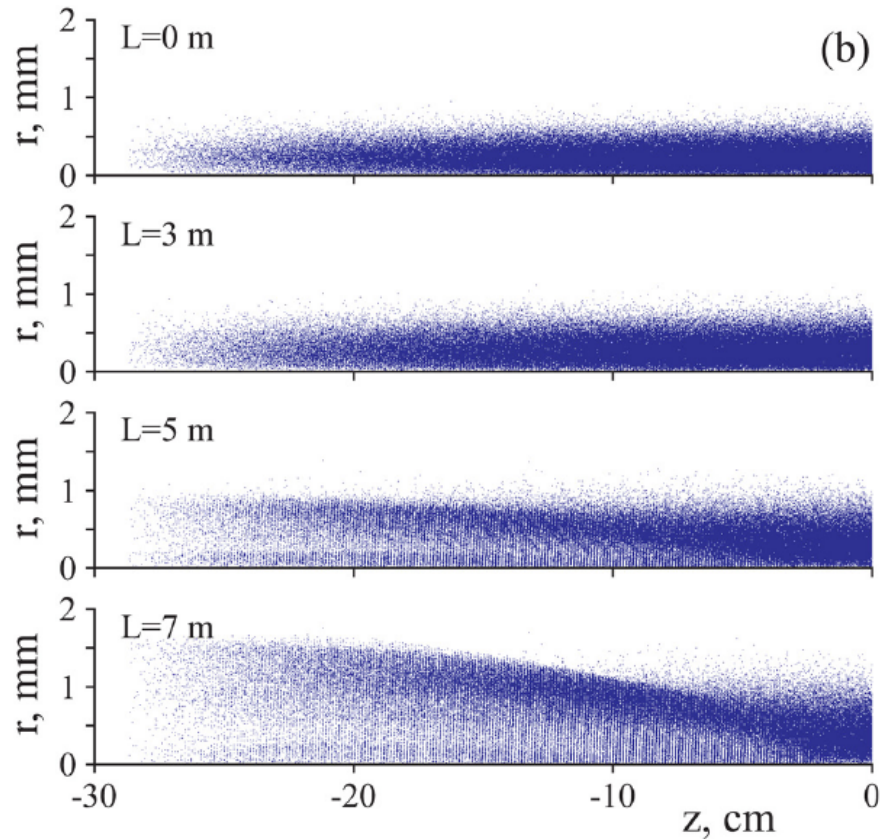
***LCODE***

BINP Novosibirsk  
Quasistatic PIC in 2D

Broad collaboration of institutes and simulation tools

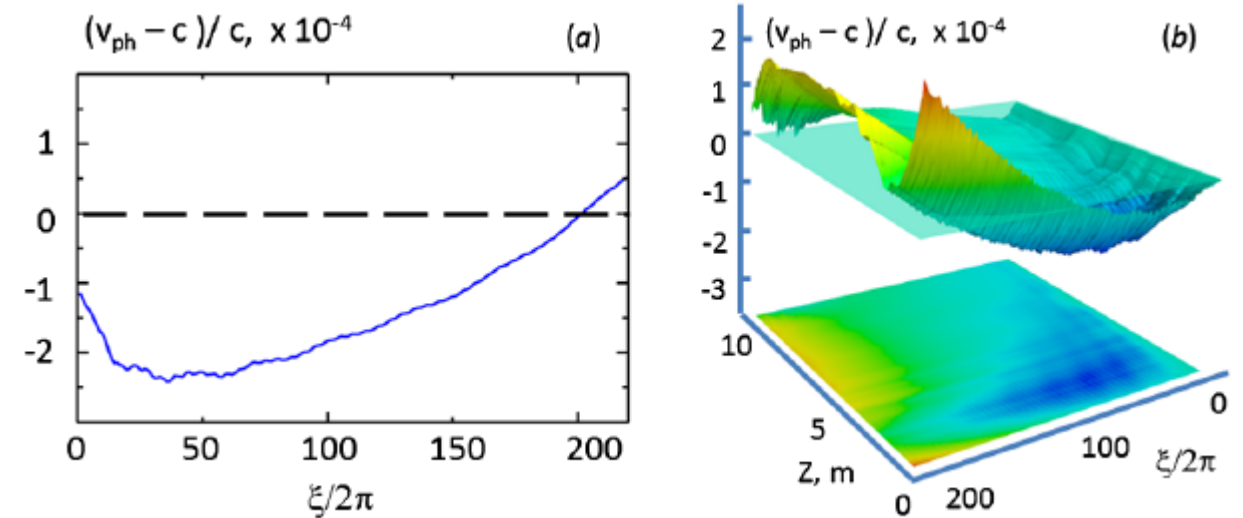
# Prediction

## Self modulation for acceleration Caldwell and Lotov, PoP (2011)



Demonstrated 2017

## Controlling SMI with density gradients Pukhov *et al.*, PRL (2011)

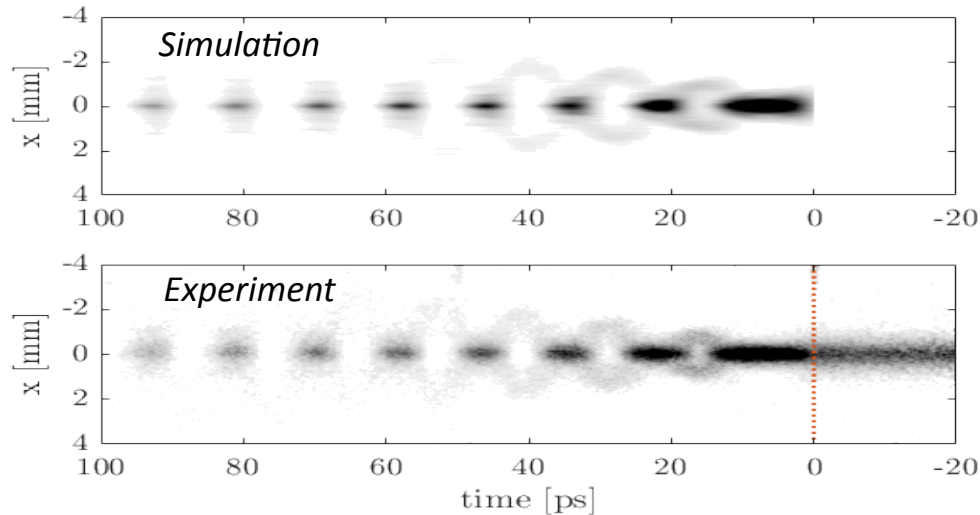
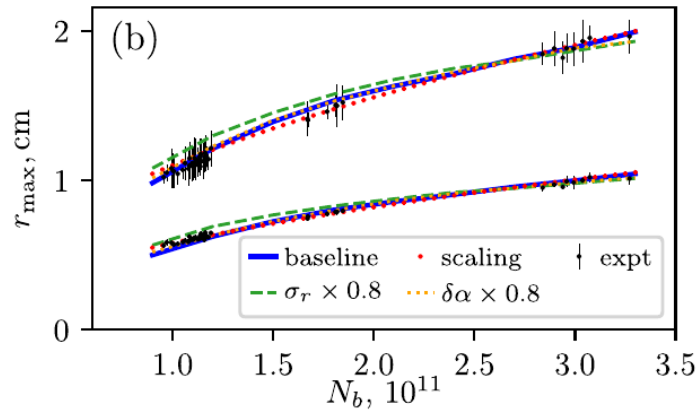


Demonstrated in 2018

# Agreement

Beam radius  
after SMI at  
Imaging Station 2

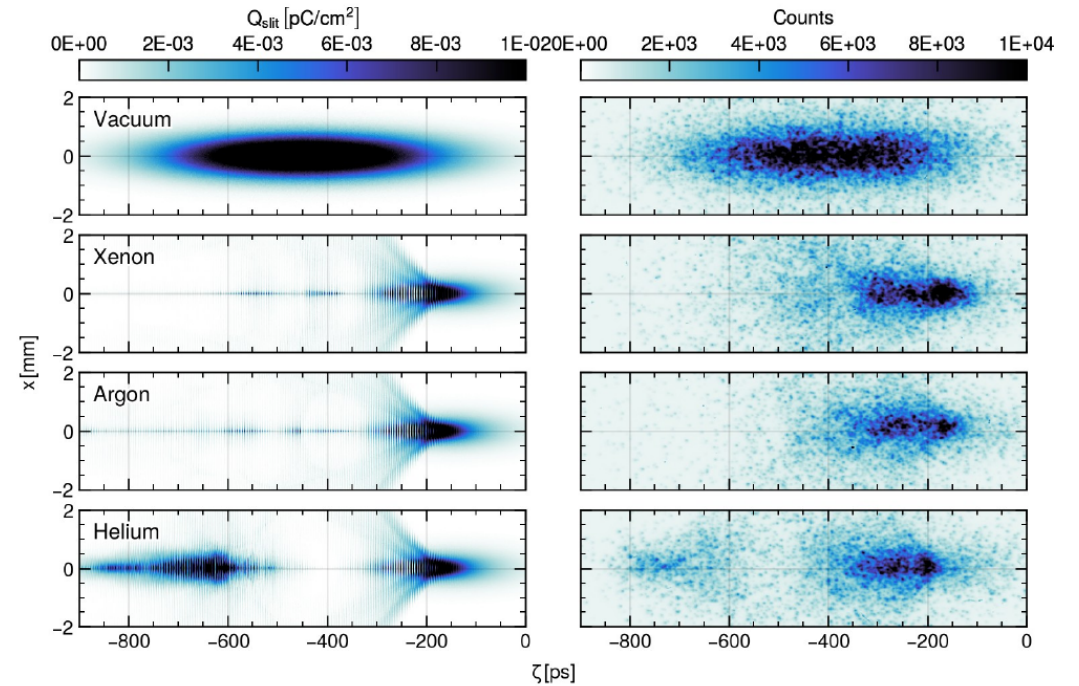
A. Gorn, PPCF (2020)



Microbunch structure at streak camera

A.-M. Bachmann, PhD thesis (2021)

Impact of ion motion on SMI  
imaged at streak camera

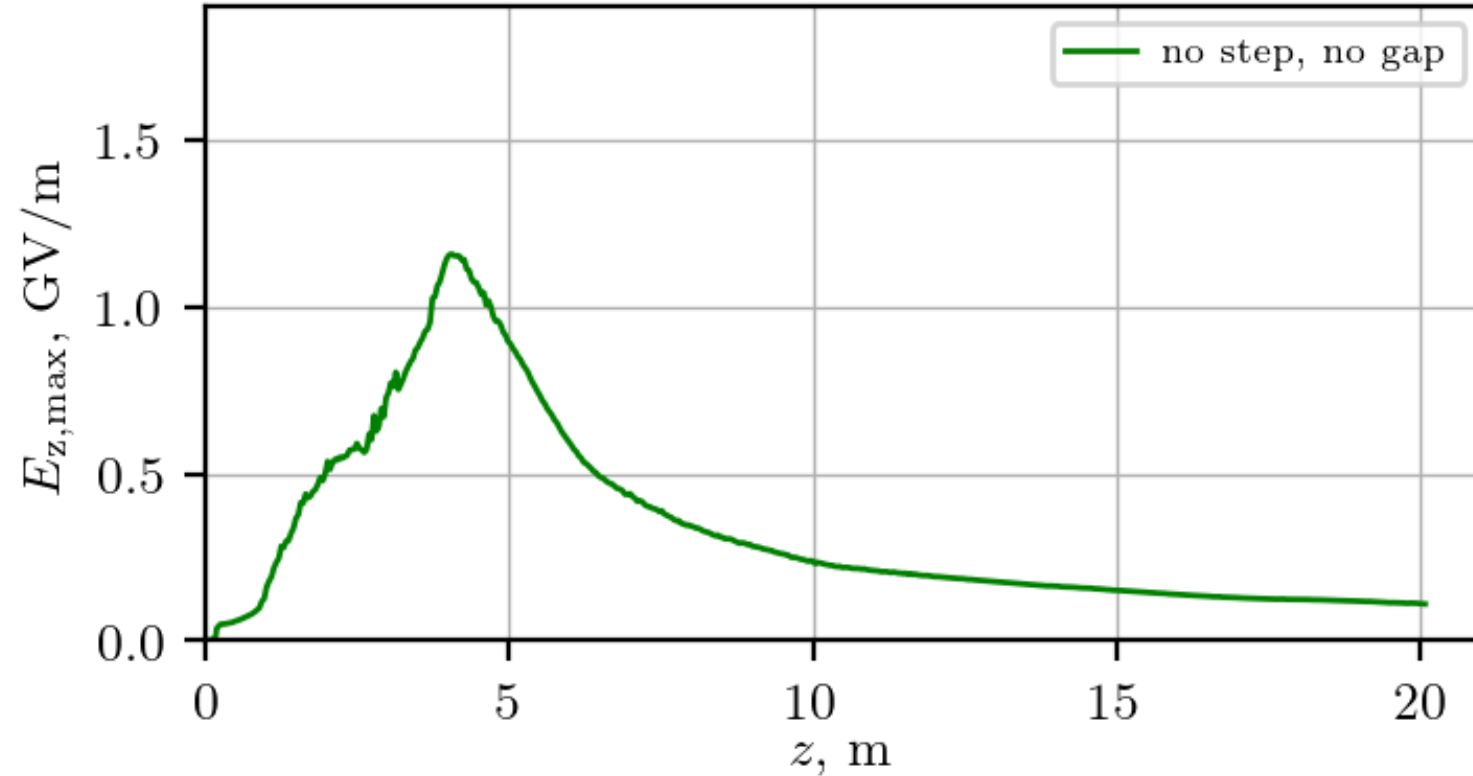


E. Walter,  
*in preparation*

M. Turner,  
*in preparation*

# Controlling Self-modulation

Wakefields initially grow, before decaying.

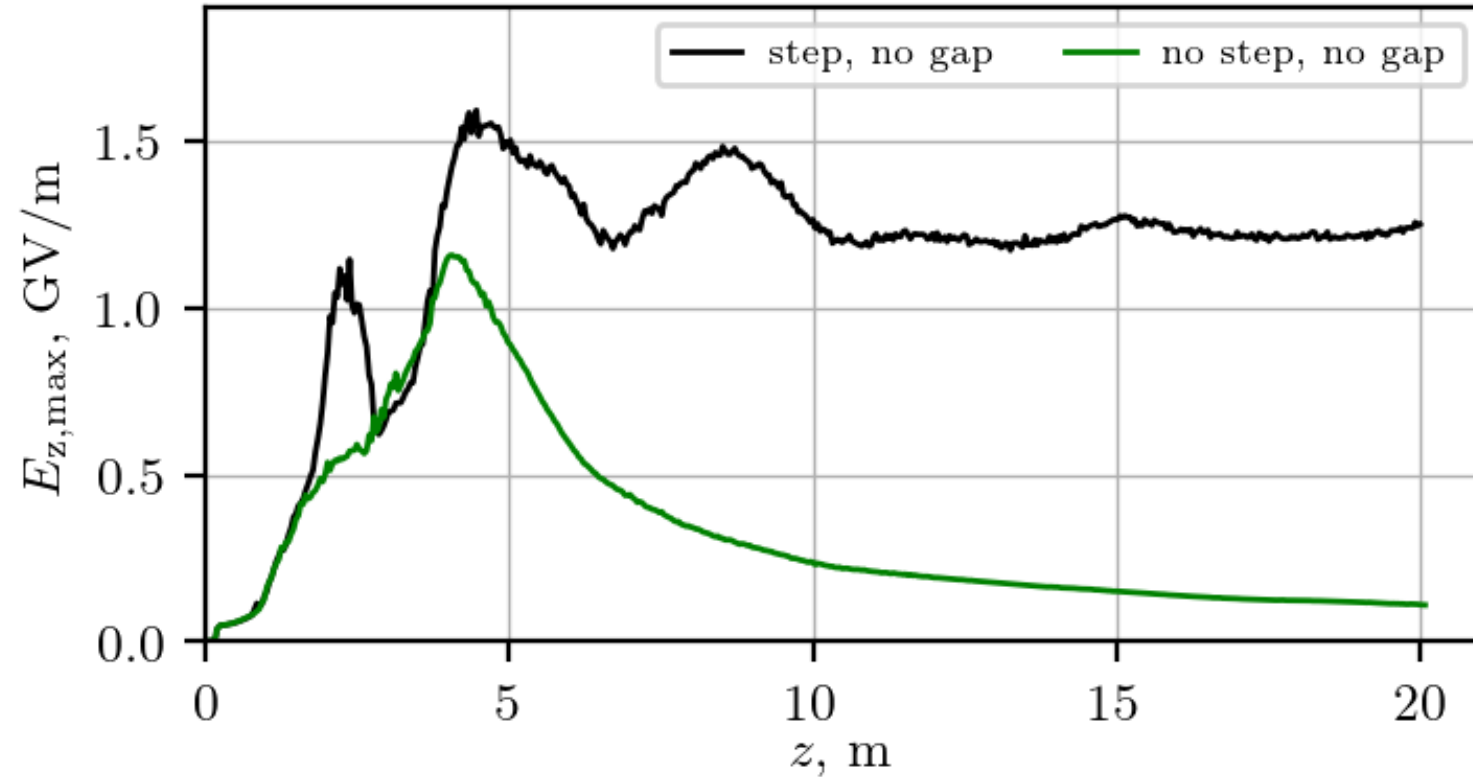


AWAKE Collaboration,  
Symmetry (2022)

# Controlling Self-modulation

Wakefields initially grow, before decaying.

Plasma density step allows self-modulation to be controlled



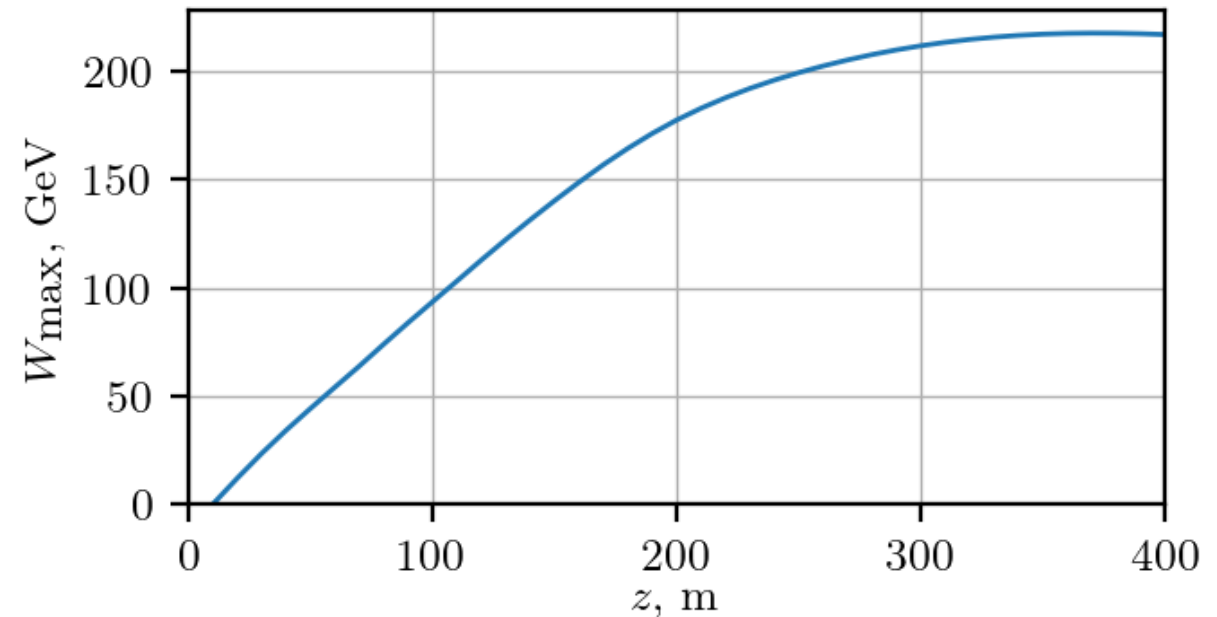
AWAKE Collaboration,  
Symmetry (2022)



# Controlling Self-modulation

Density step allows high wakefield amplitude over hundreds of metres.

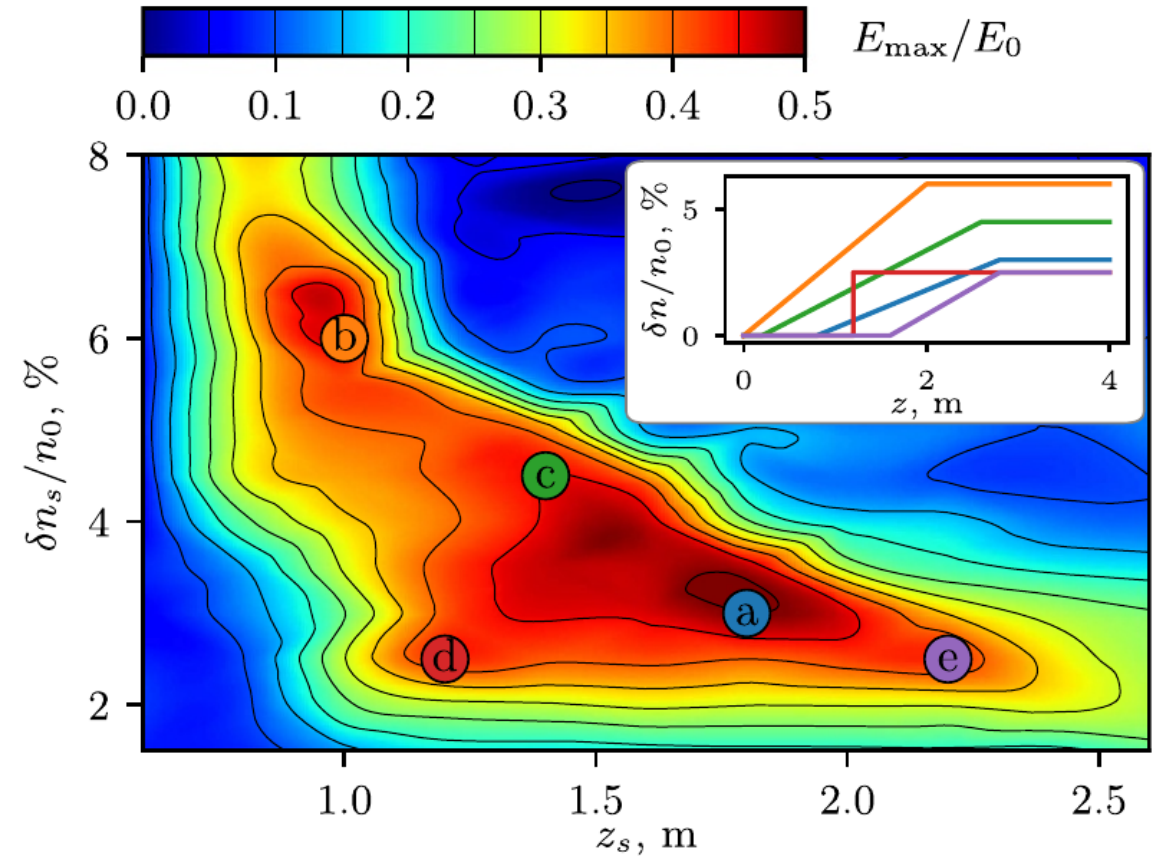
Energy gain of ~150 GeV in 200 m (after beamloading)



Lotov and Tuev, PPCF (2021)

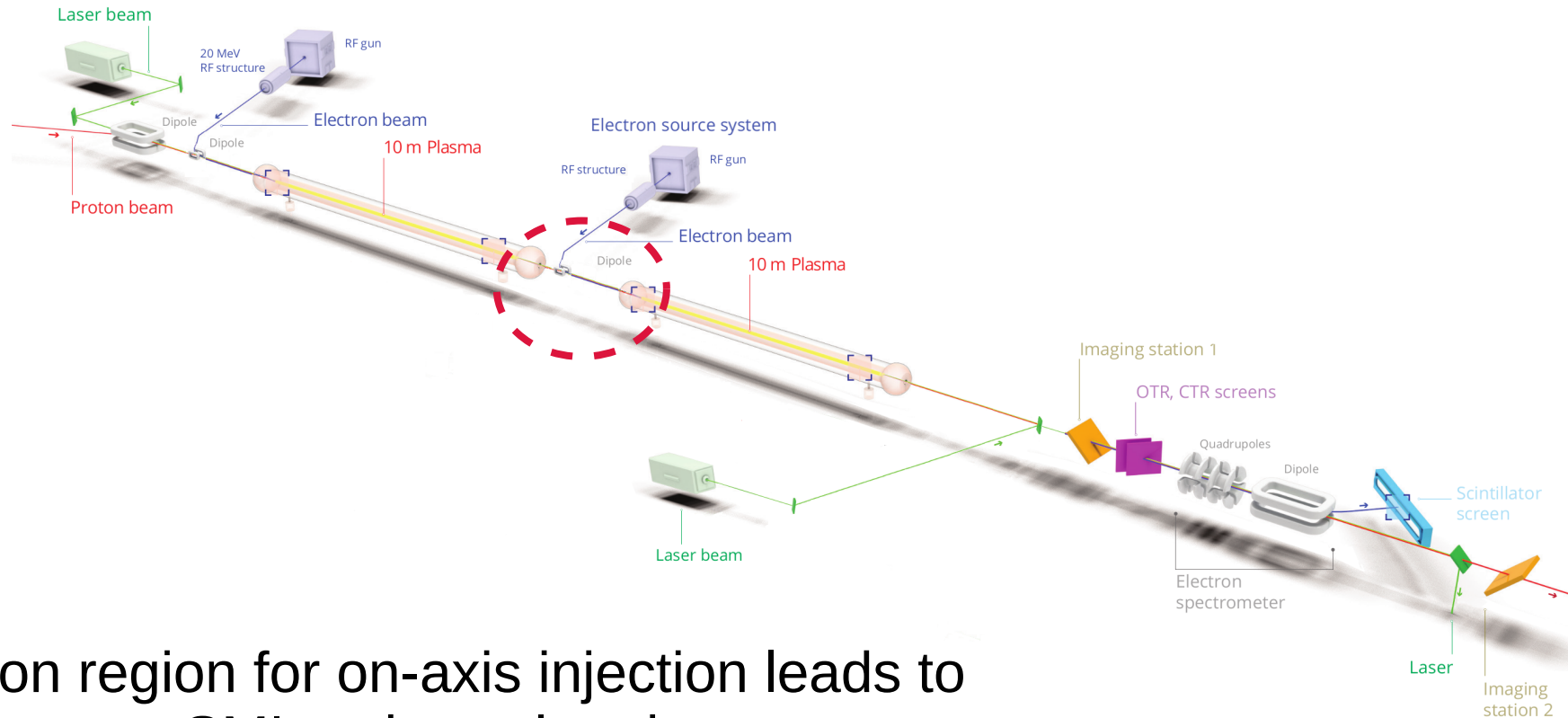
# Controlling Self-modulation

Wakefields after 20 metres show broad tolerances for step position and height.



Lotov and Tuev, PPCF (2021)

# Controlling Self-modulation



Integration region for on-axis injection leads to a gap between SMI and acceleration stages.

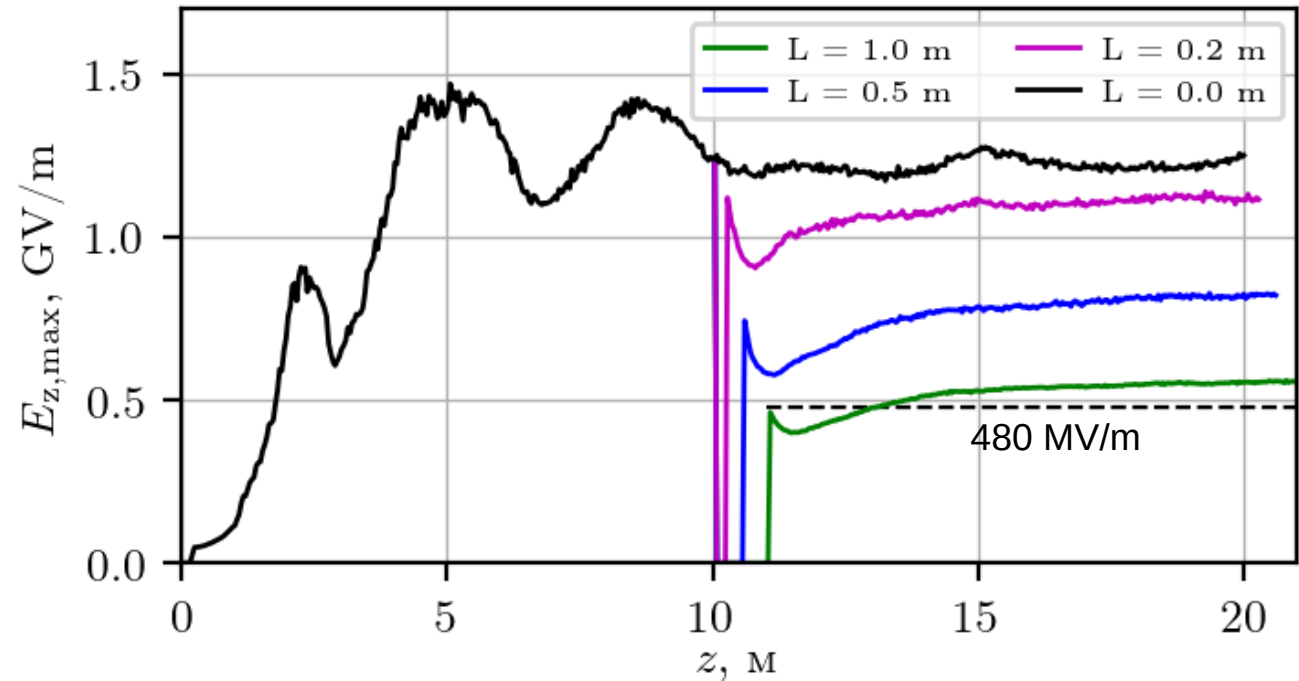
Modulated proton beam evolves in this gap.

# Injection Studies

Gap reduces wakefields,  
but amplitude remains stable.

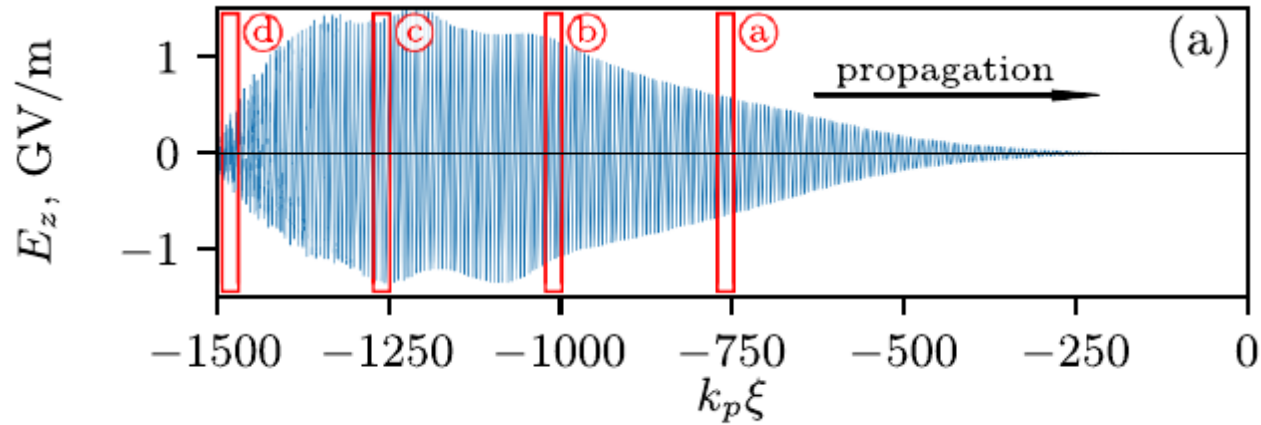
Accelerating gradient  
depends on gap length.

Assume 1 m gap (480 MV/m)  
as “worst case” scenario.



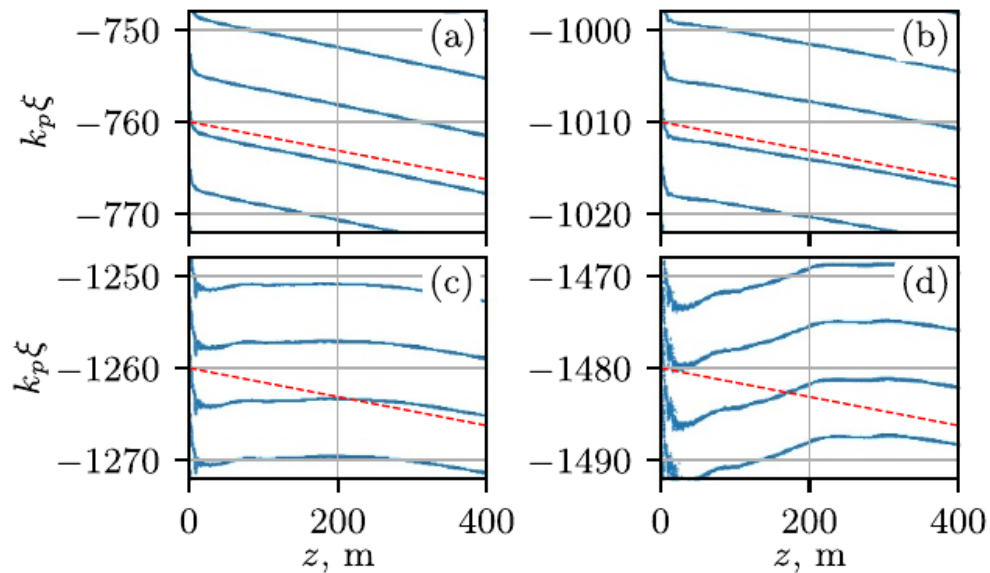
V. Yarygova (2023)

# Injection Studies



SMI growth allows wakefields with luminal phase.

Lotov and Tuv, 2021



Assume wakefield phase velocity equals proton velocity as “worst case” scenario

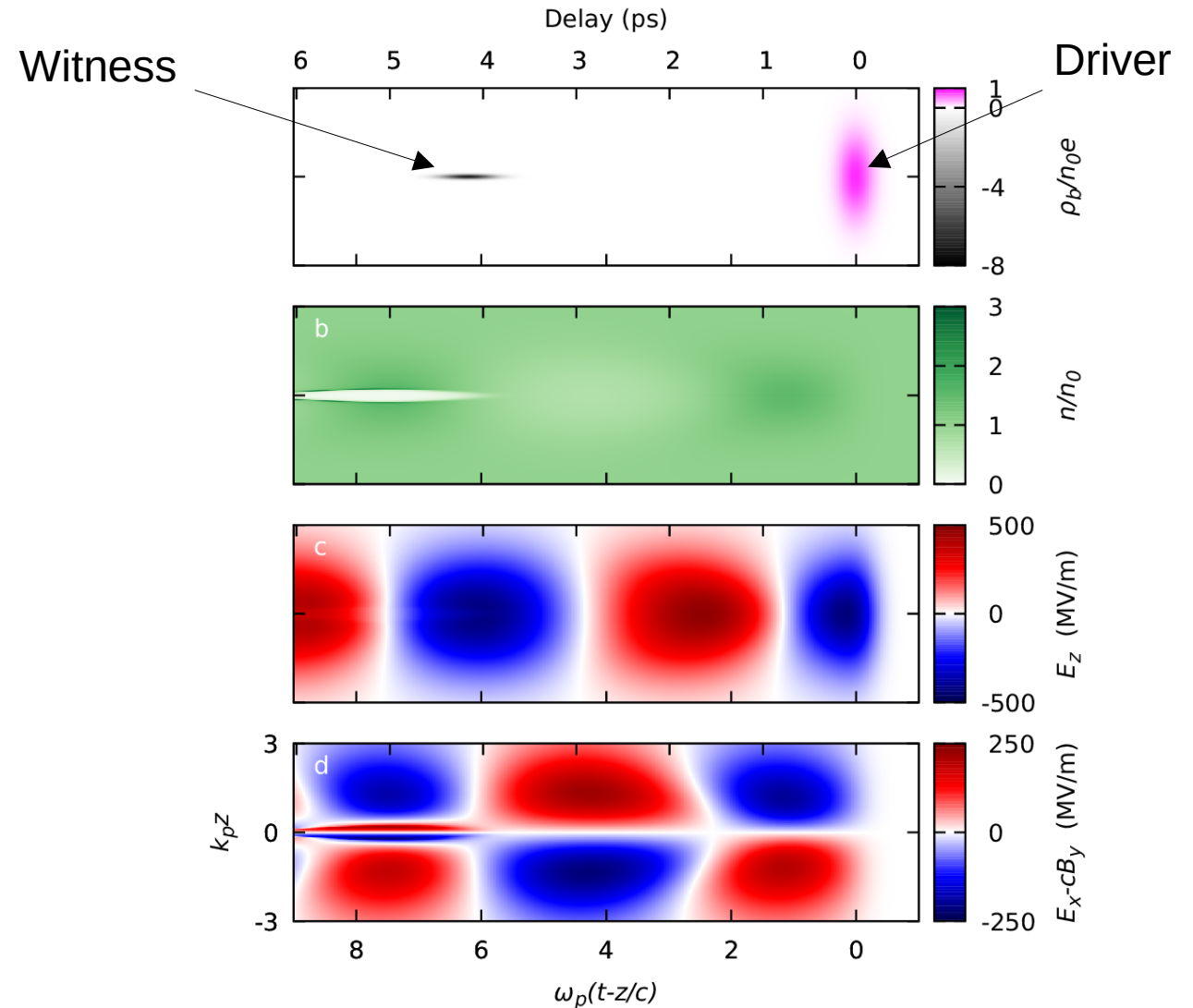
Blue – wakefield phase  
Red – driver velocity

# Injection Studies

These assumptions allow physics studies using “toy models”.

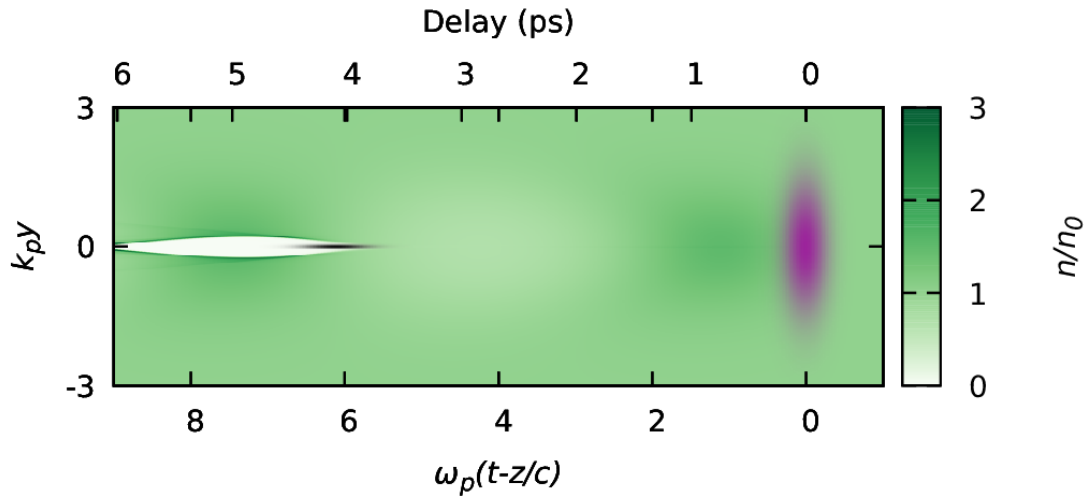
Short driver generates a quasilinear wake ( $E_z=480$  MV/m,  $\gamma_\phi=426$ ).

Allows rapid investigation of parameter space.



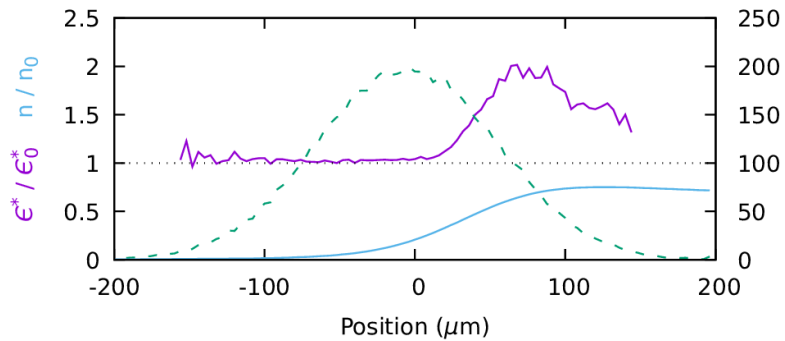
V. Olsen *et al.*, PRAB (2018)  
 J. Farmer *et al.*, *in preparation*

# Injection Studies



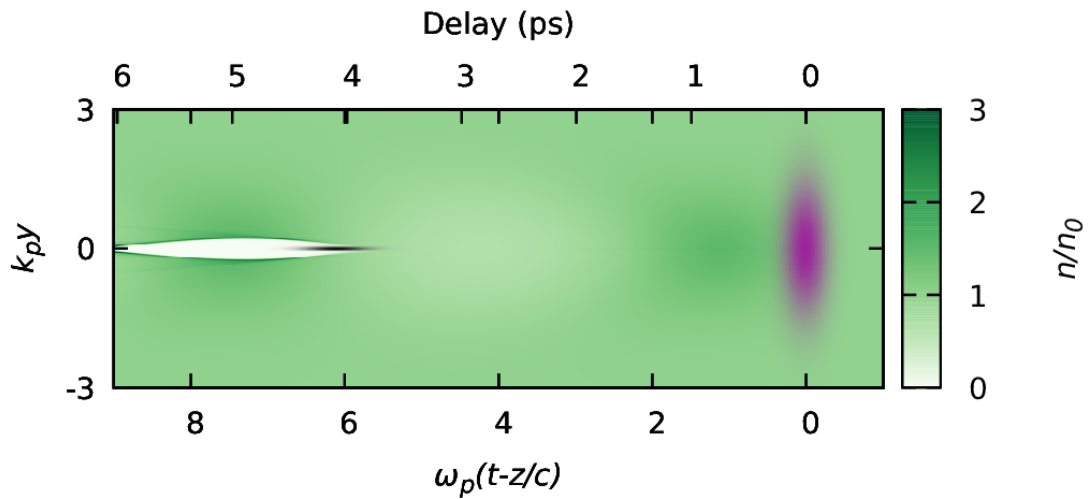
Conventional wisdom:  
need a blowout to conserve  
emittance.

Low-emittance witness  
drives its own!



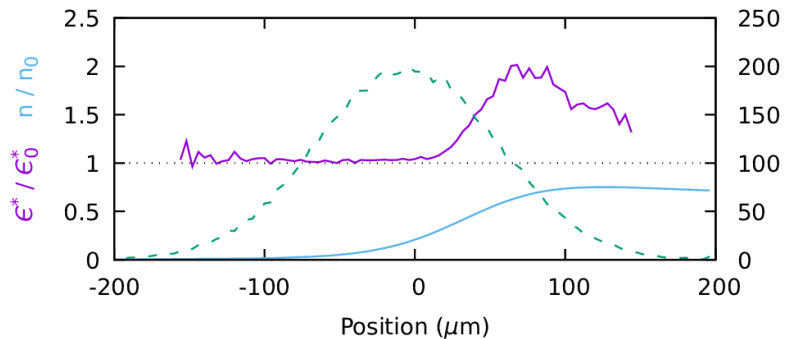
Witness slice emittance  
after 10m acceleration

# Injection Studies



Conventional wisdom:  
need a blowout to conserve  
emittance.

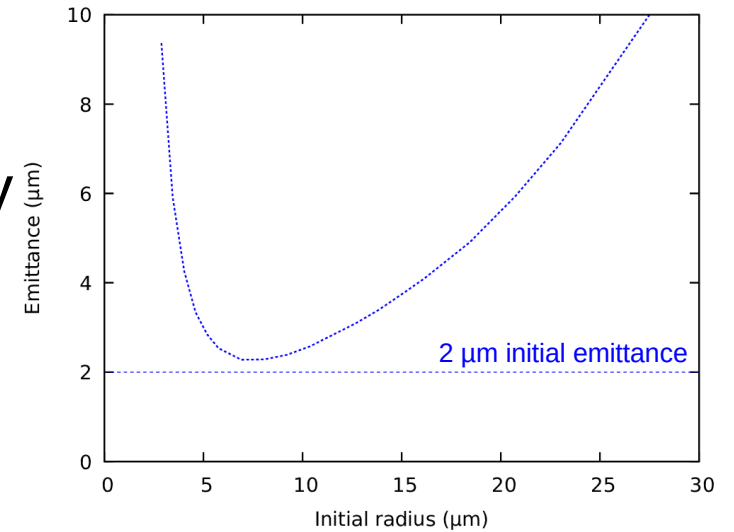
Low-emittance witness  
drives its own!



Witness slice emittance  
after 10m acceleration

Projected emittance after  
10m acceleration has only  
weak dependence on  
initial radius (5-15 $\mu\text{m}$ )

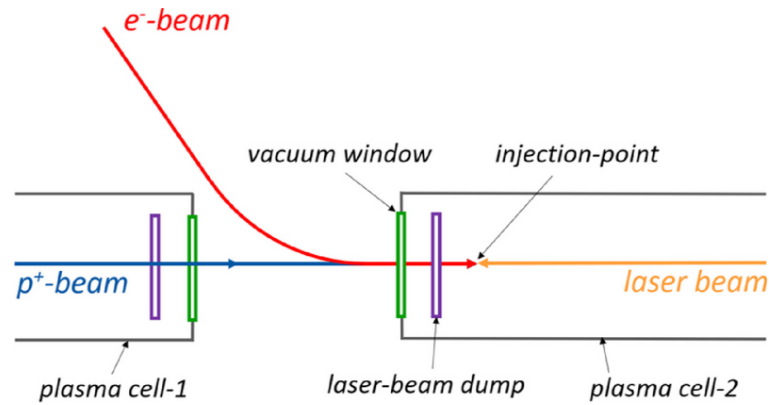
- broad tolerances



Witness projected emittance  
after 10m acceleration

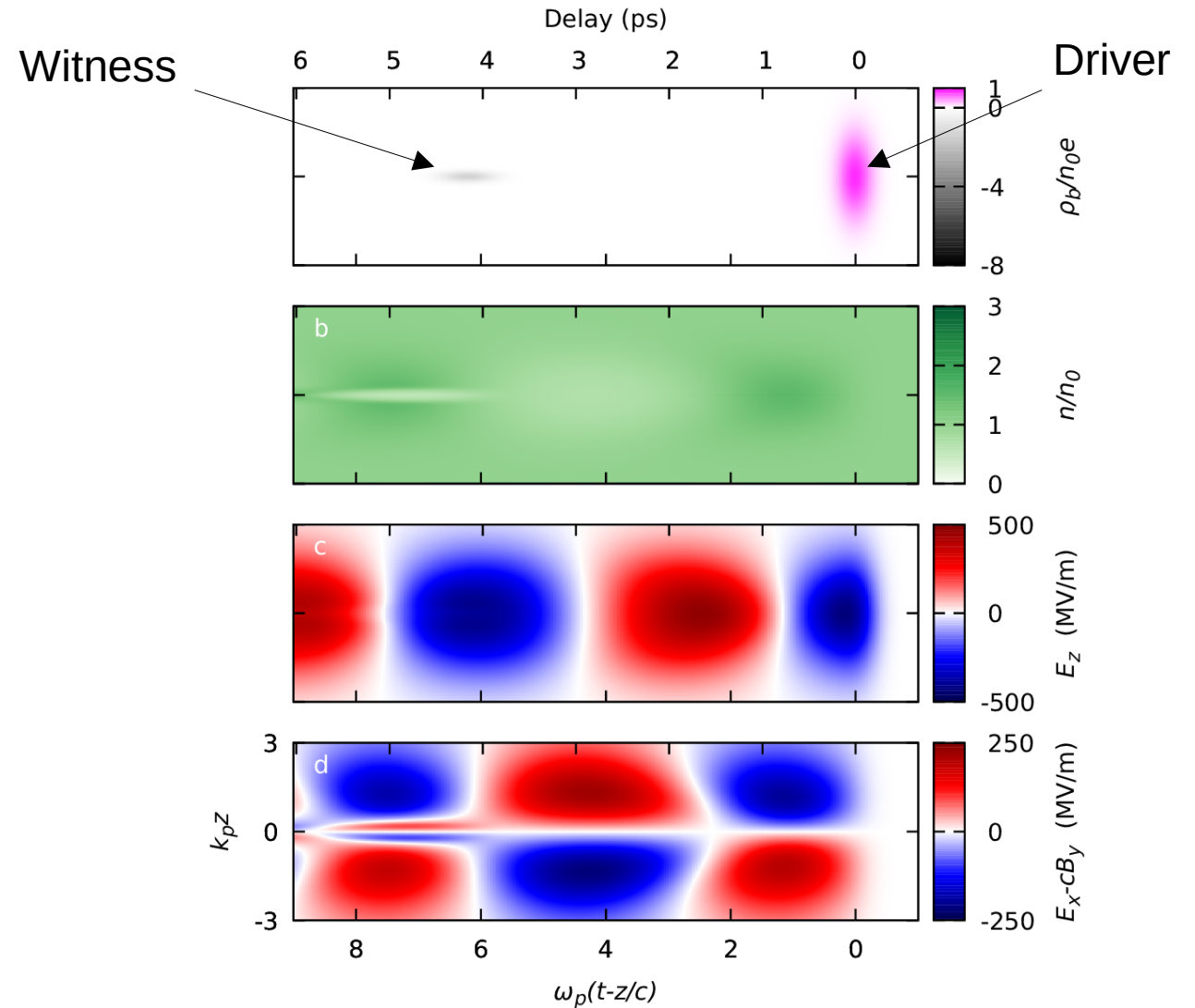


# Injection Studies



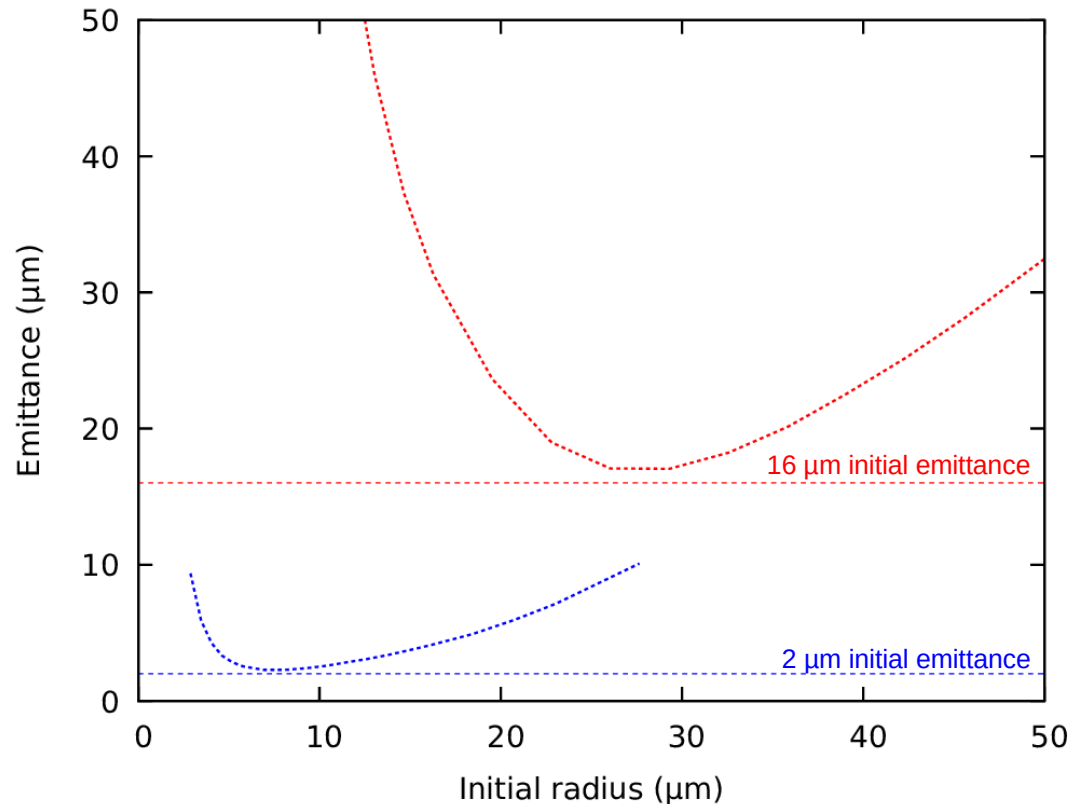
Technical constraints mean that it may be necessary to inject through the laser beam dump.

This will lower the charge density of the beam in the plasma, preventing the formation of a complete blowout.



J. Farmer *et al.*, *in preparation*

# Injection Studies



Projected normalized emittance after  
10m acceleration for different initial radii

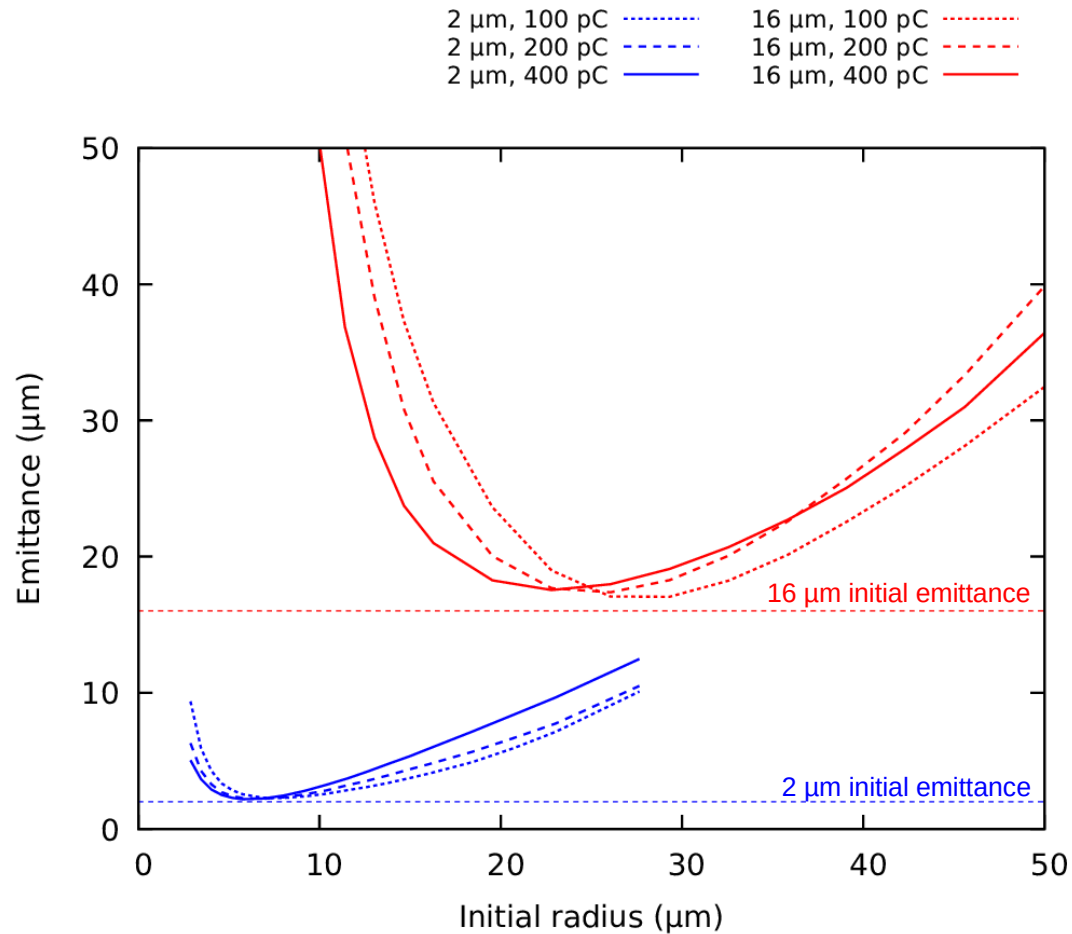
Emittance control *is* still possible  
with higher-emittance beams

- “quasi-matching” to  
nonlinear wakefield
- same broad tolerances

Similar schemes exist for  
positron beams

c.f. C. S. Hue *et al.* (2021)

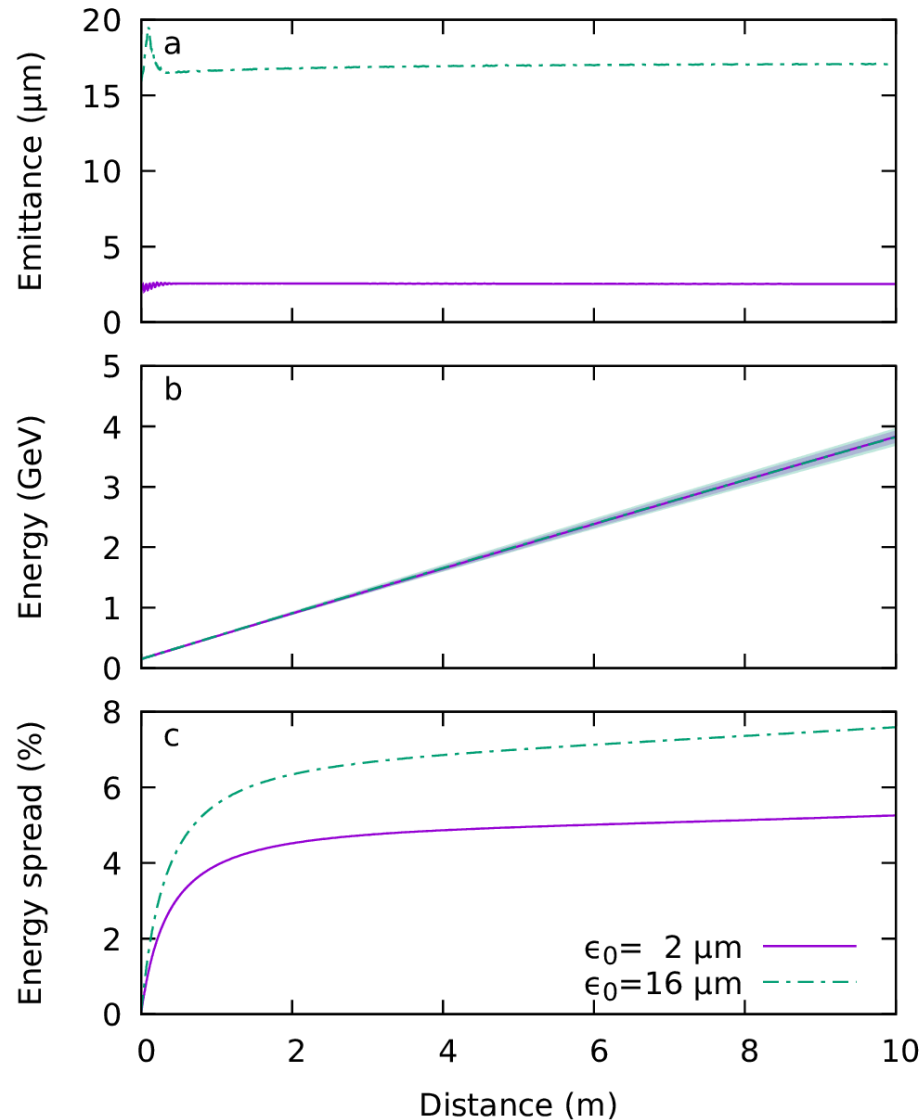
# Injection Studies



Further optimisation possible through tuning electron line or varying witness charge

Projected normalized emittance after 10m acceleration for different initial radii

# Injection Studies



Rapid initial evolution before reaching equilibrium.

- allows scaling to large distances/high energy.

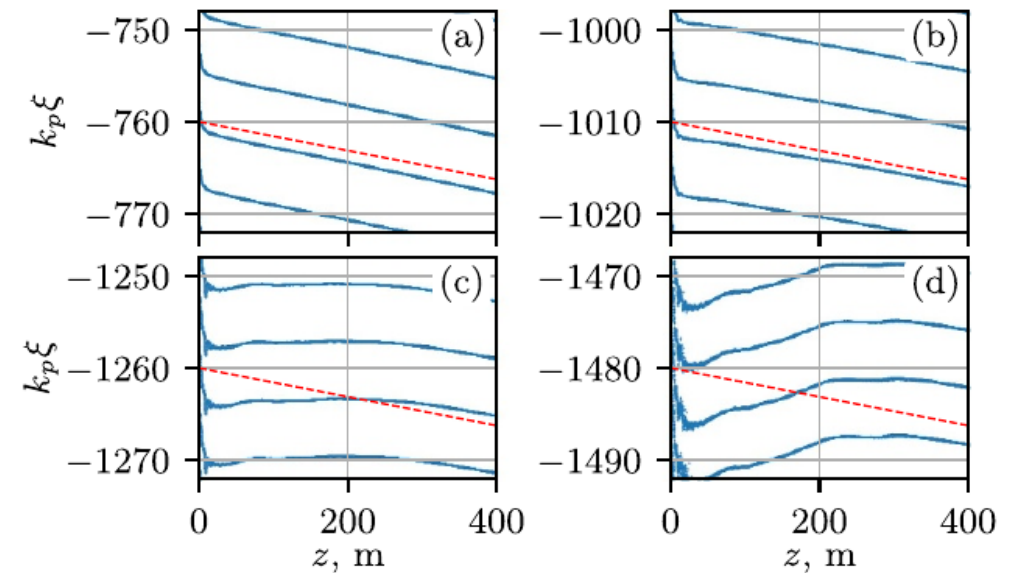
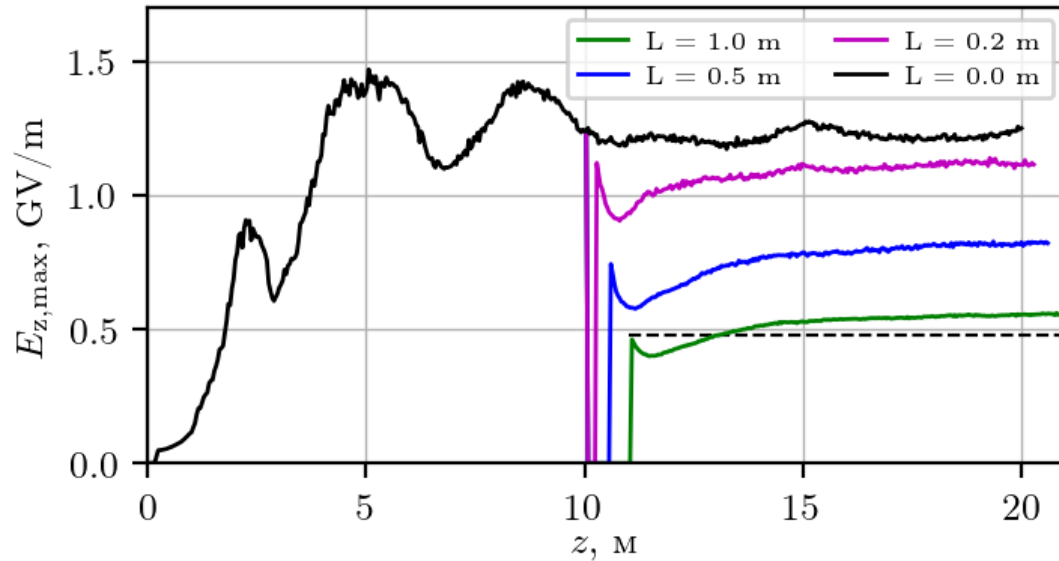
Over 10m:

- negligible emittance growth
- 4 GeV energy gain
- 5-8% energy spread

# Injection Studies

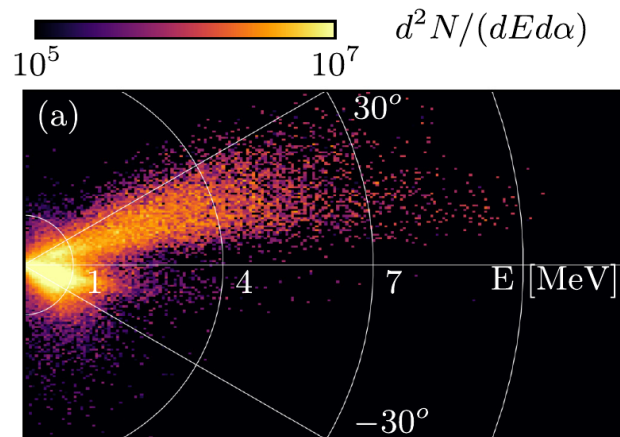
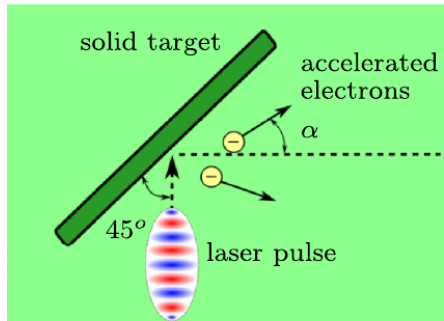
Clear paths to improve these values:

- smaller gap
- control wakefield phase



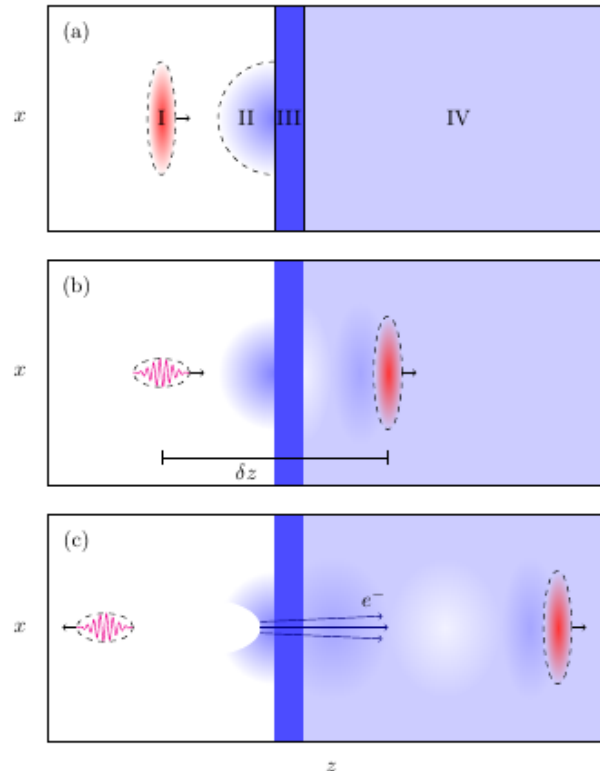
# Alternative Injection Schemes

## Laser-foil injector

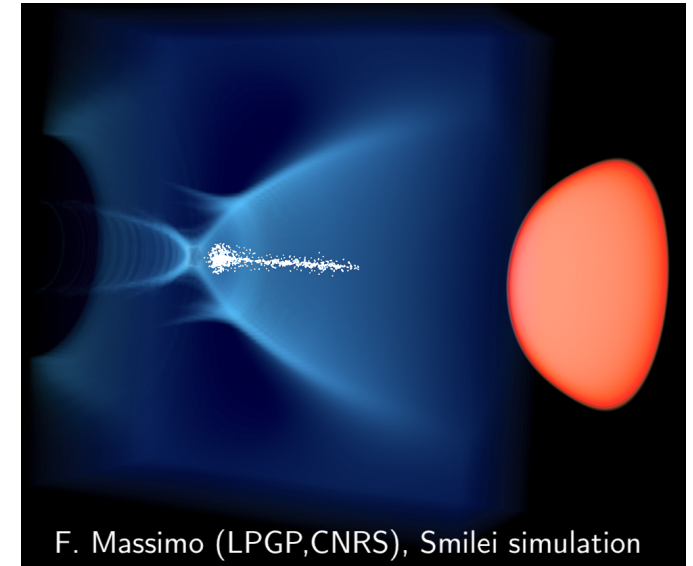


Khudiakov and Pukhov,  
PRE (2021)

## Laser-plasma injector



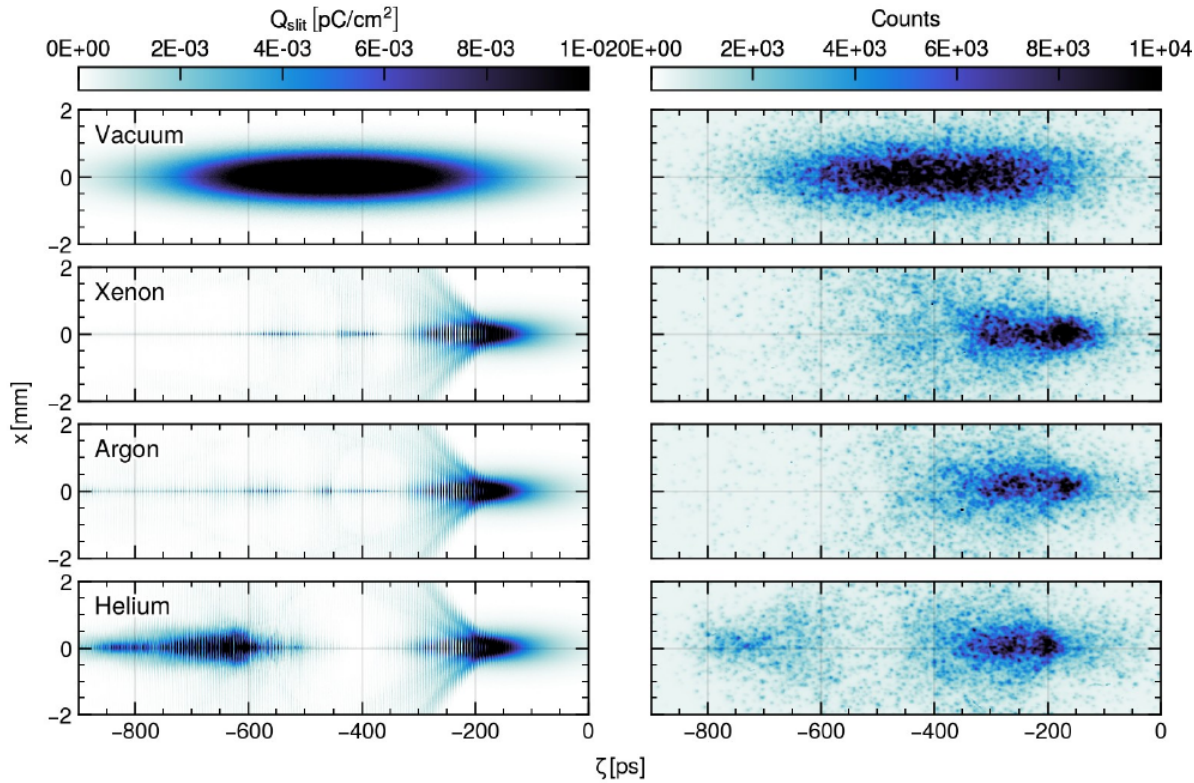
Wilson *et al.*  
*submitted.*



Minenna *et al.*  
(EARLI Collaboration),  
*submitted.*

# Associated Physics

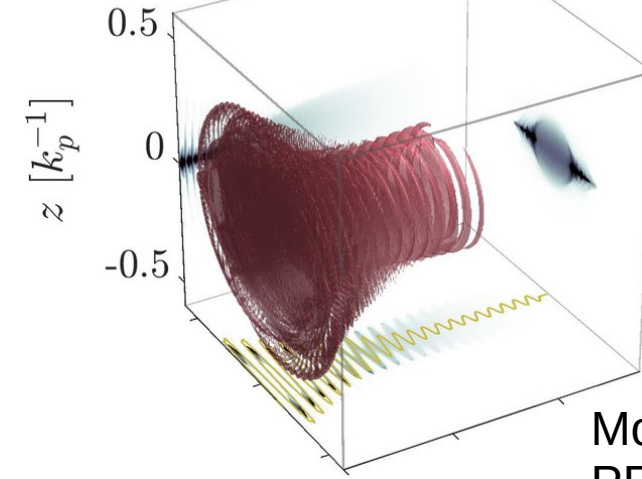
## Ion motion



E. Walter *et al.*,  
*in preparation*

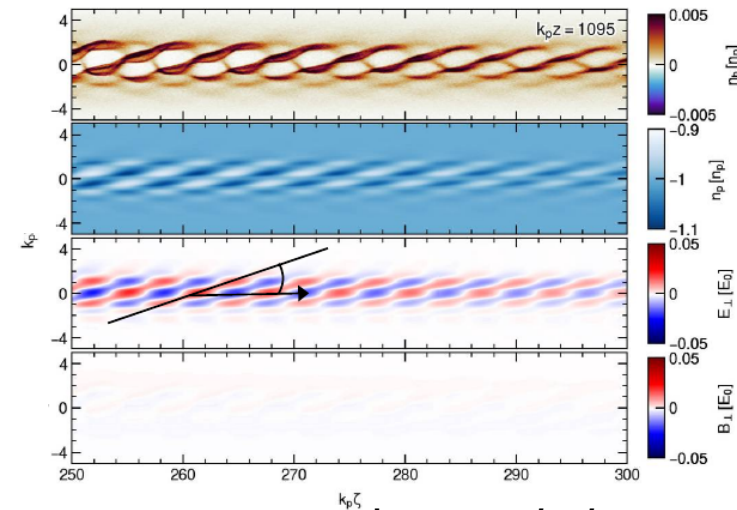
M. Turner *et al.*,  
*in preparation*

## Control of hosing



Moreira *et al.*,  
PRL (2023)

## Filamentation



Walter *et al.*, *in preparation*

# Impact Beyond AWAKE

Development and validation of simulation tools

Excellent test bed for global push towards  
High Performance Computing at the exascale

Tolerances for external injection in quasilinear wakes

- also relevant for positron acceleration



# Outlook

Comprehensive simulation programme ahead of Run 2c:

- integrated simulations, simultaneously resolving witness bunch emittance and full proton beam
- further optimisation to maximise gradients after the gap
- further optimisation of witness parameters at injection

# Conclusions

AWAKE simulations have proven ability to predict and reproduce experimental results.

Physics studies carried out with simulations show

- control of wakefield gradients over long distances
- control of witness emittance during acceleration
- broad tolerances in both cases

Provides confidence that the Run 2c/d goals are achievable

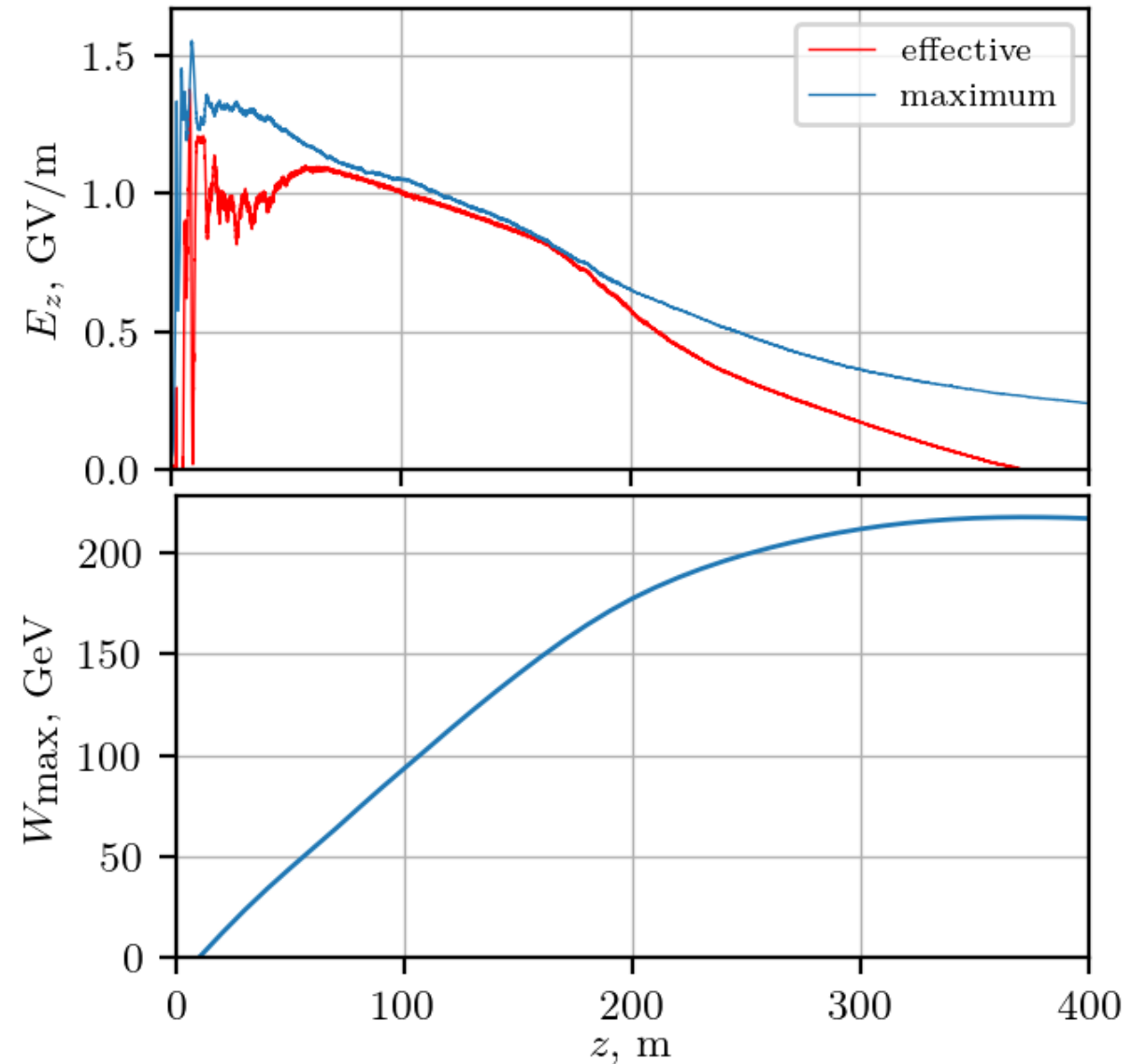
**Thank you**

# Bonus content

# Controlling Self-modulation

Density step allows high wakefield amplitude over hundreds of metres.

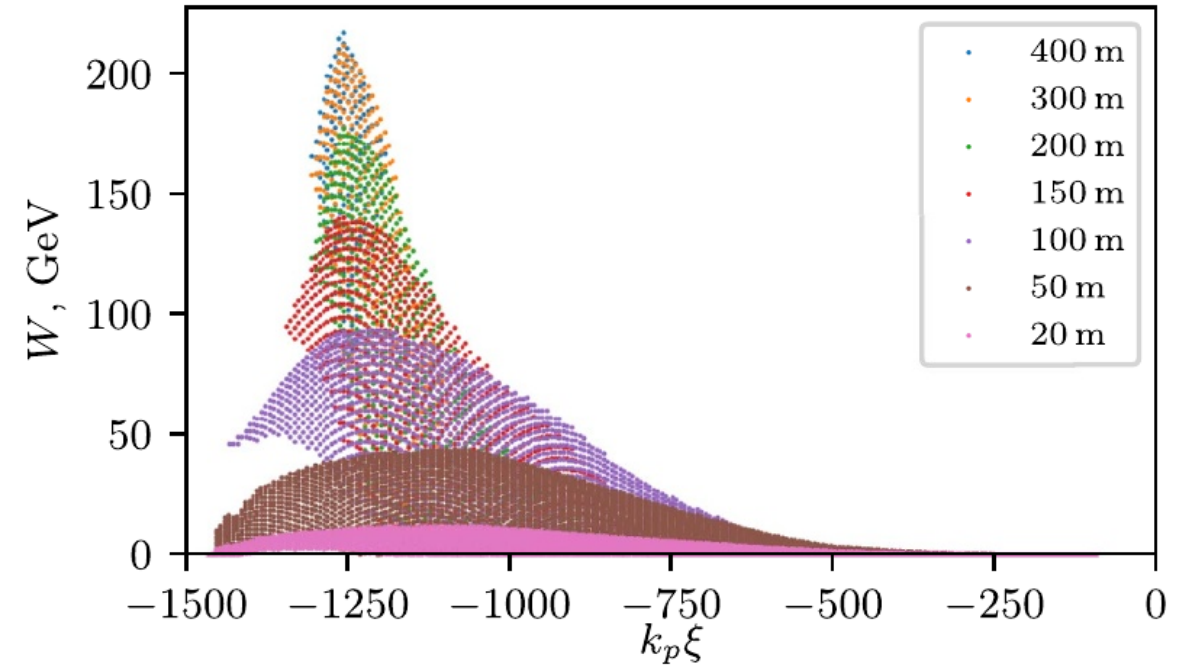
Energy gain of  
~150 GeV in 200 m  
(after beamloading)



# Controlling Self-modulation

What are the constraints for injection?

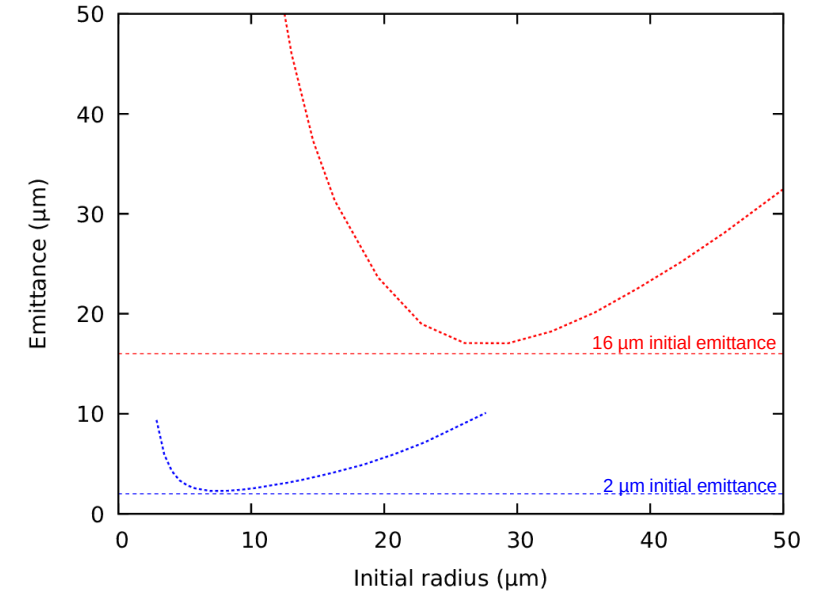
- For first 40 m acceleration, broad tolerances for witness delay



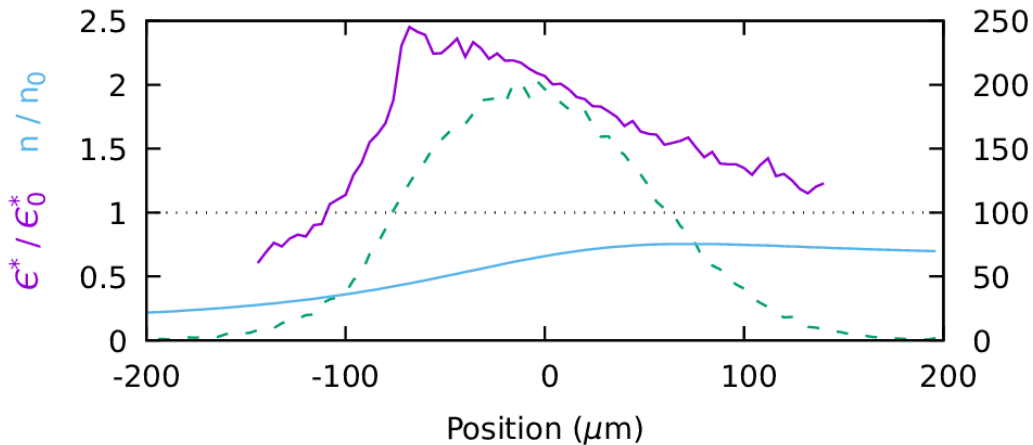
Lotov and Tsev,  
Plasma Phys. Control. Fusion (2021)

# Injection Studies

Emittance after 10 m acceleration for 16  $\mu\text{m}$  initial emittance.

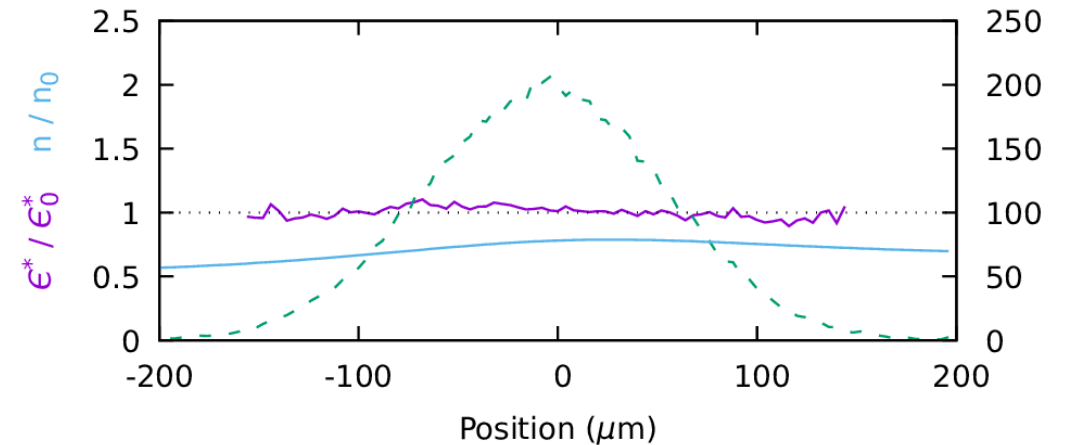


## Blowout-matched radius



$$\epsilon_0^* = 16 \mu\text{m}, \sigma_0 = 16 \mu\text{m}$$

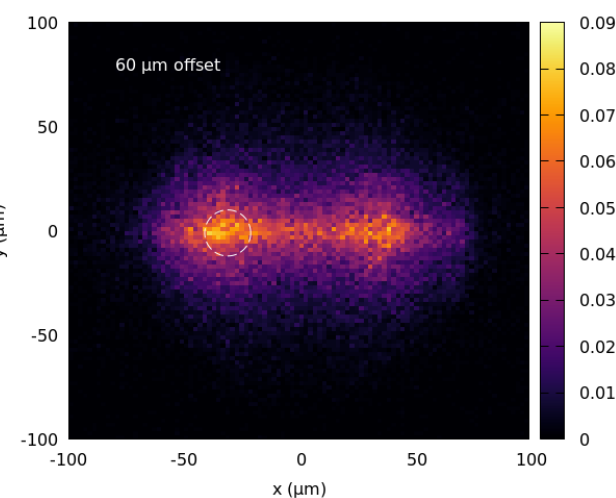
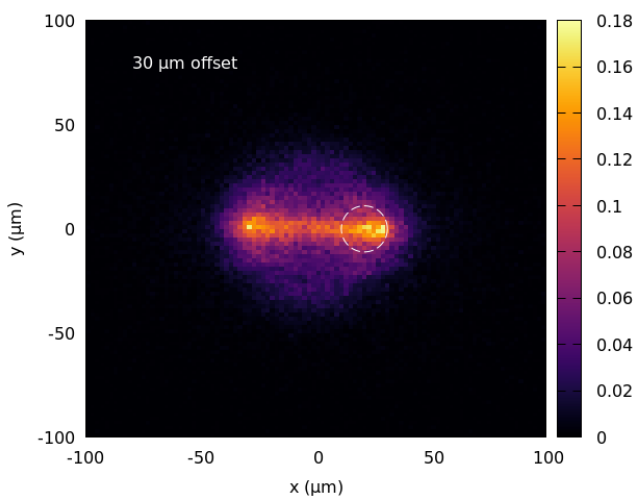
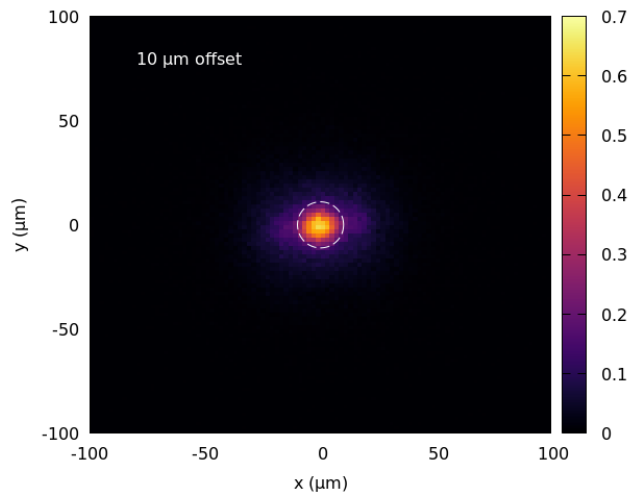
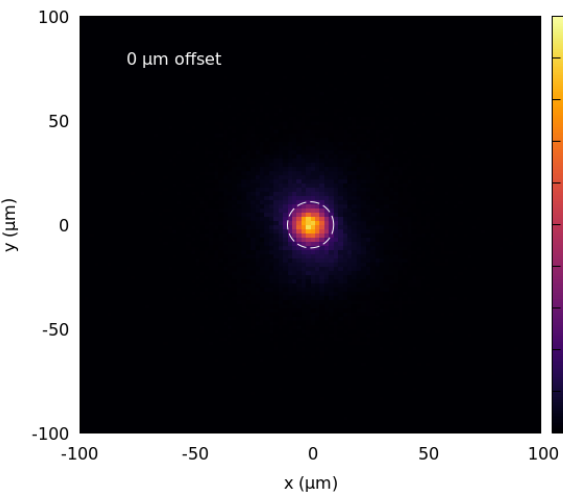
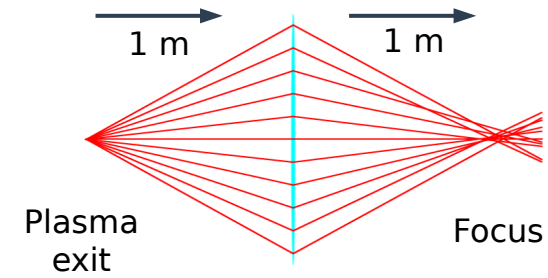
## Optimal radius (self-matching)



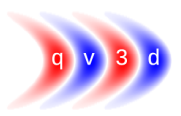
$$\epsilon_0^* = 16 \mu\text{m}, \sigma_0 = 26 \mu\text{m}$$

# Injection Studies

Simulations for different transverse offsets show smeared-out bunch at focus.



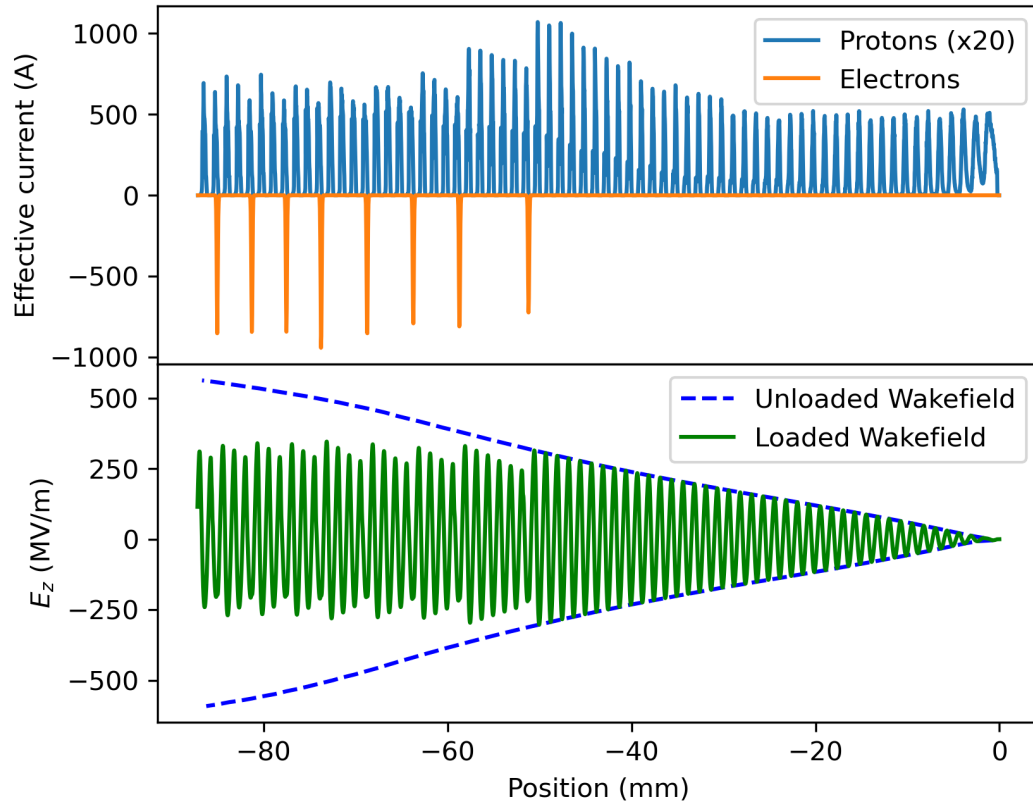
100 pC charge, 8  $\mu\text{m}$  initial emittance





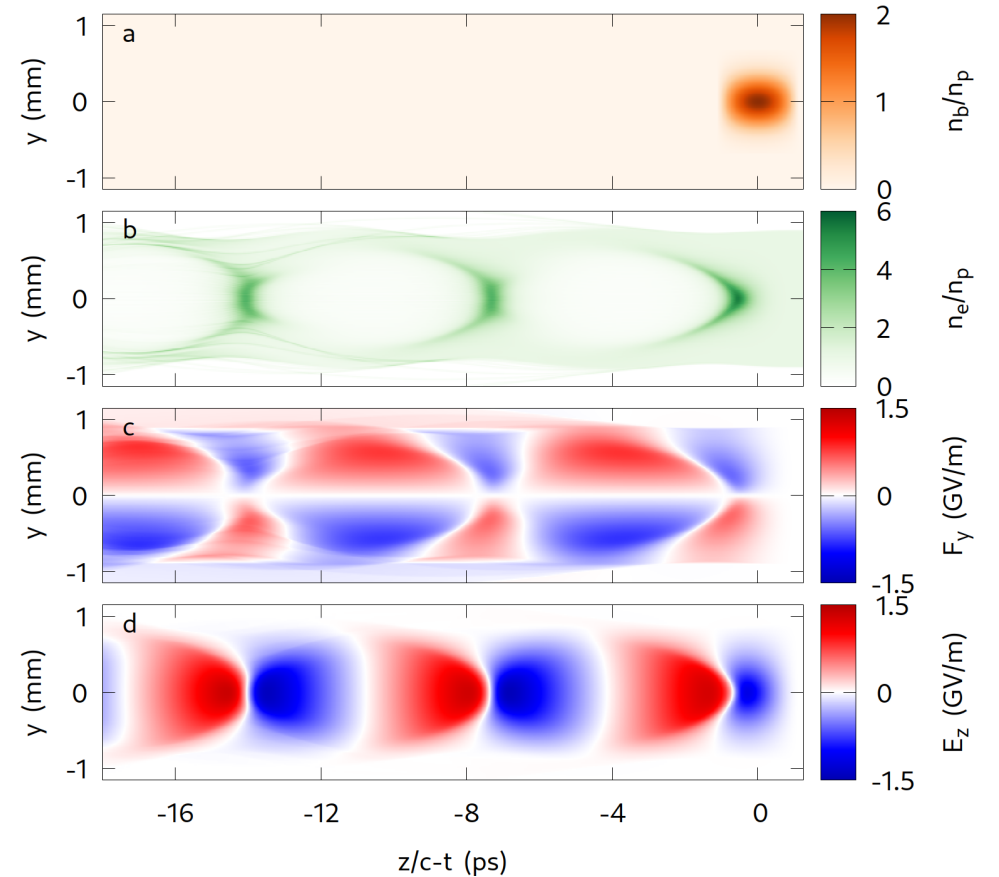
# Beyond Run 2

## Multi-bunch injection



Farmer and Zevi Della Porta  
*in preparation*

## Short-proton driver



Farmer, Caldwell and Pukhov,  
*in preparation*