



Fundamental physics with radioactive atoms and molecules at CERN-ISOLDE

Mia Au and Michail Athanasakis-Kaklamanakis

Low energy observables for BSM physics

eEDM

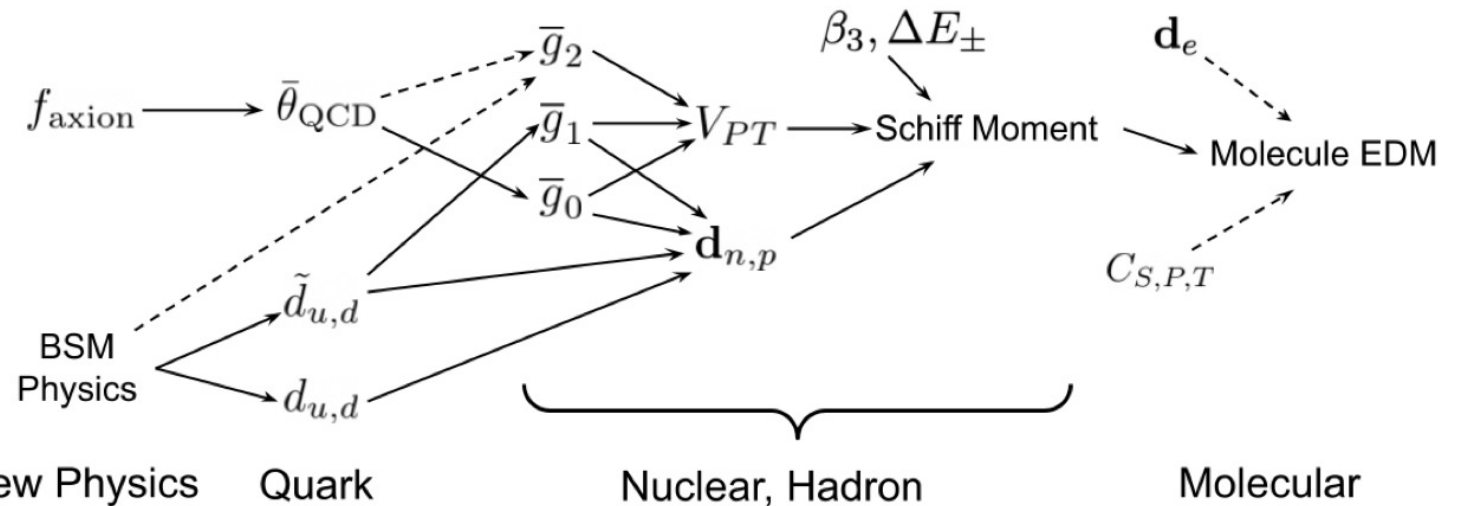
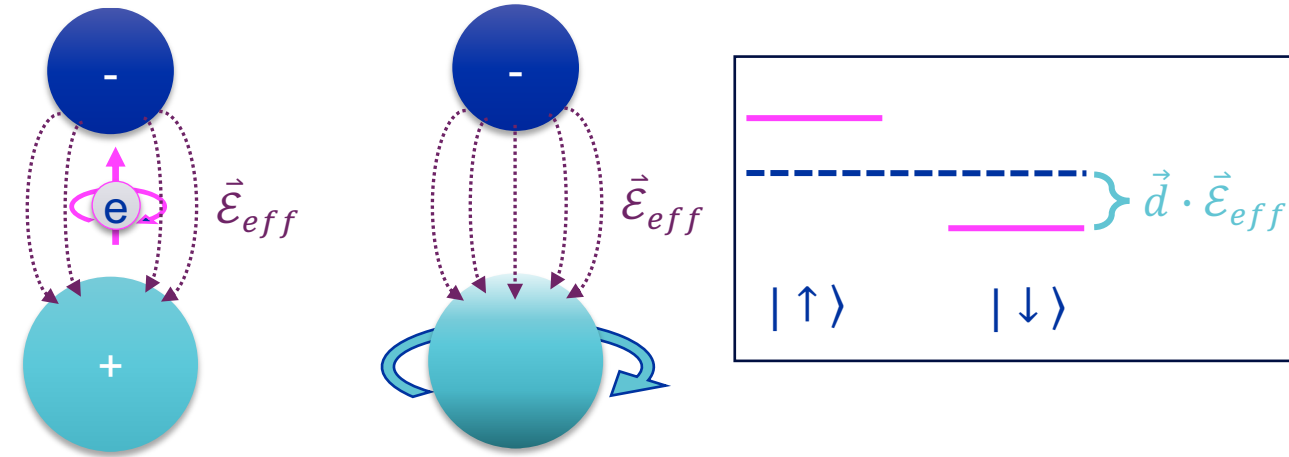
- Sensitive to electron-coupled CPV

Nuclear MQM

- Sensitive to nuclear CPV
- Enhanced in heavy nuclei
- Enhanced in quadrupole-deformed nuclei

Nuclear Schiff moment

- Sensitive to nuclear CPV
- Enhanced in heavy nuclei
- Enhanced in octupole-deformed nuclei



[1] Contribution to Snowmass 2021: *EDMs and the search for new physics*, arXiv 2203.08103 (2021)

[2] Safronova et al. (2018) *Rev. Mod. Phys.* 90. 2

[3] *Opportunities for Fundamental Physics Research with Radioactive Molecules*, arXiv 2302.02165 (2023), *Rep. Prog. Phys.* (2024) doi: 10.1088/1361-6633/ad1e39

Low energy observables for BSM physics

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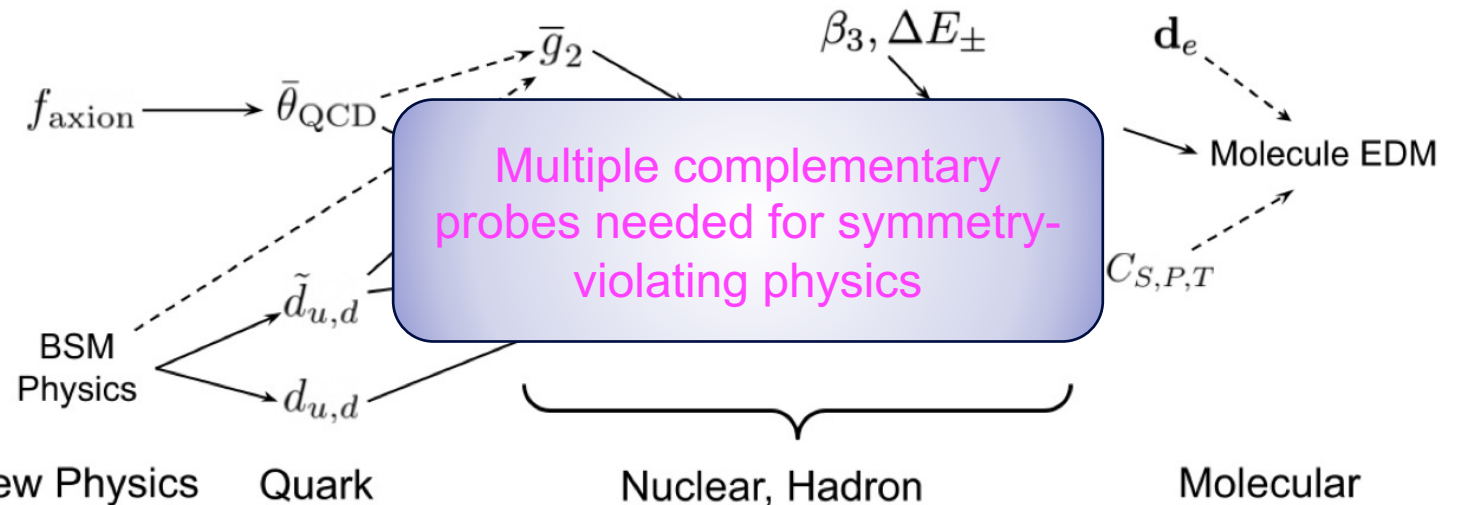
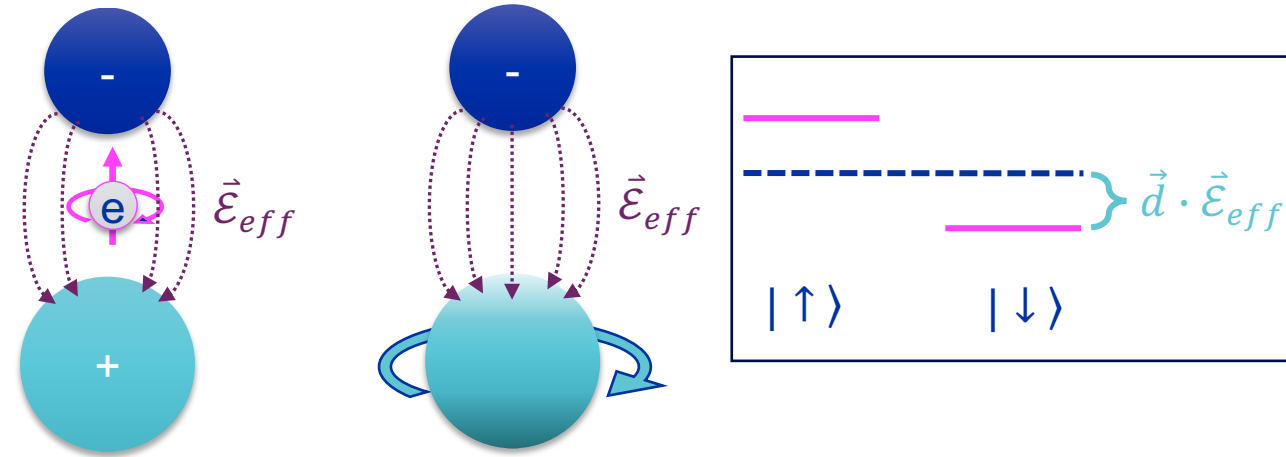
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EDM searches

The existence of a finite permanent EDM of a particle or atom would violate time reversal (T) and parity (P) symmetry, or equivalently charge conjugation and parity symmetry (CP), needed to solve baryon asymmetry

nEDM $|d_n|$

- 2006 ILL UCNs: $|d_n| < 2.9 \times 10^{-26}$ e cm
- 2020 PSI [1]: $|d_n| < 1.8 \times 10^{-26}$ e cm

eEDM $|d_e|$

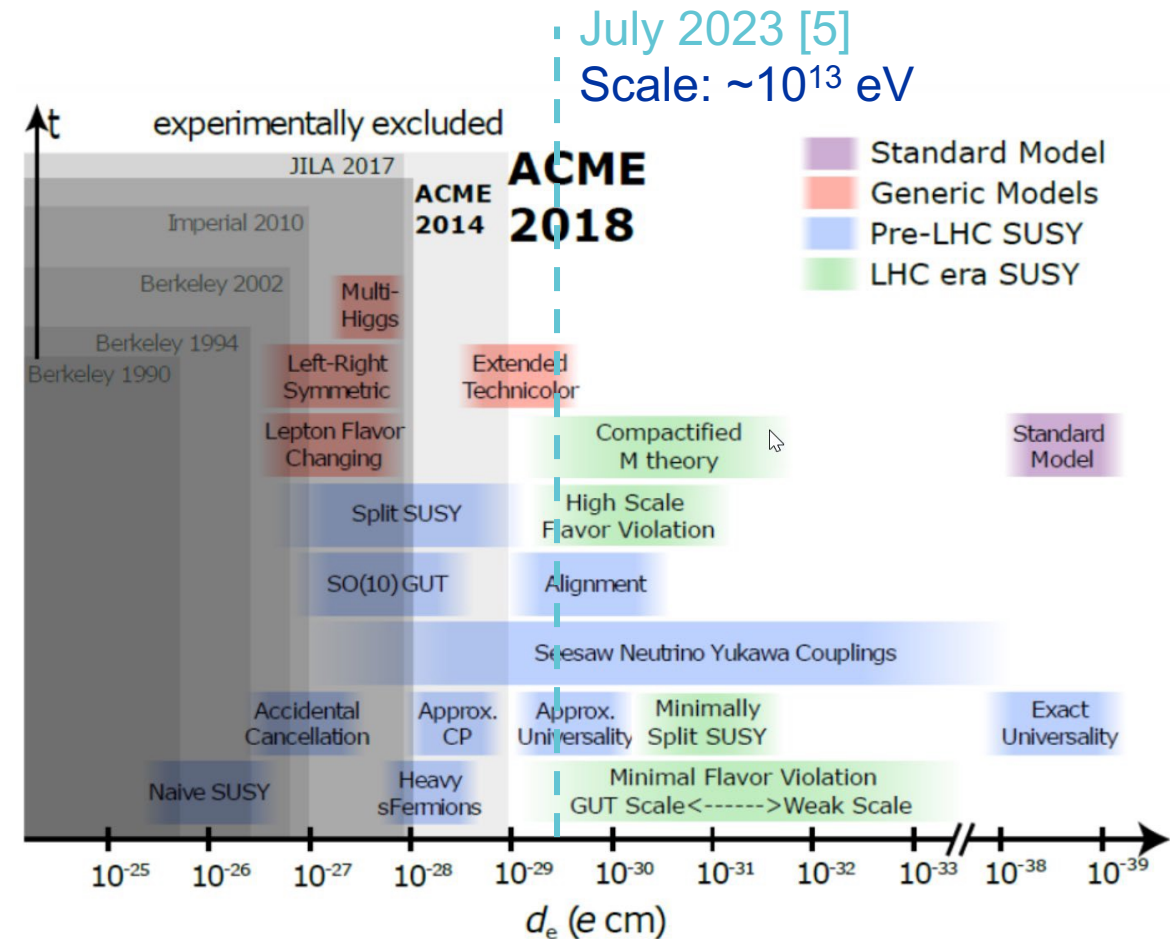
- 2011 Imperial $^{174}\text{Yb}^{19}\text{F}$ [2]: $|d_e| < 2 \times 10^{-28}$ e cm
- 2018, 2013 ACME $^{232}\text{Th}^{16}\text{O}$ [3,4]: $|d_e| < 1 \times 10^{-29}$ e cm
- 2023, 2017 JILA $^{180}\text{Hf}^{19}\text{F}^+$ [5]: $|d_e| < 4.1 \times 10^{-30}$ e cm

Atomic EDM

- 2009, ^{199}Hg : $|d| < 3.1 \times 10^{-29}$ e cm
- 2015, ^{225}Ra [6]: $|d| < 5 \times 10^{-22}$ e cm
- 2020, ^{171}Yb [7]: $|d| < 1.5 \times 10^{-26}$ e cm

[1] PRL 124, 081803 (2020)
 [2] Nature 473, 493 (2011)
 [3] Science 343, 269 (2014)
 [4] Nature 562, 355 (2018)

[5] Science 381, 46 (2023)
 [6] PRC 94, 025501 (2016)
 [7] PRL 129, 083001 (2020)



D. DeMille, *The ACME Experiment*, (2023)

<https://cfp.physics.northwestern.edu/gabrielse-group/acme-electron-edm.html>

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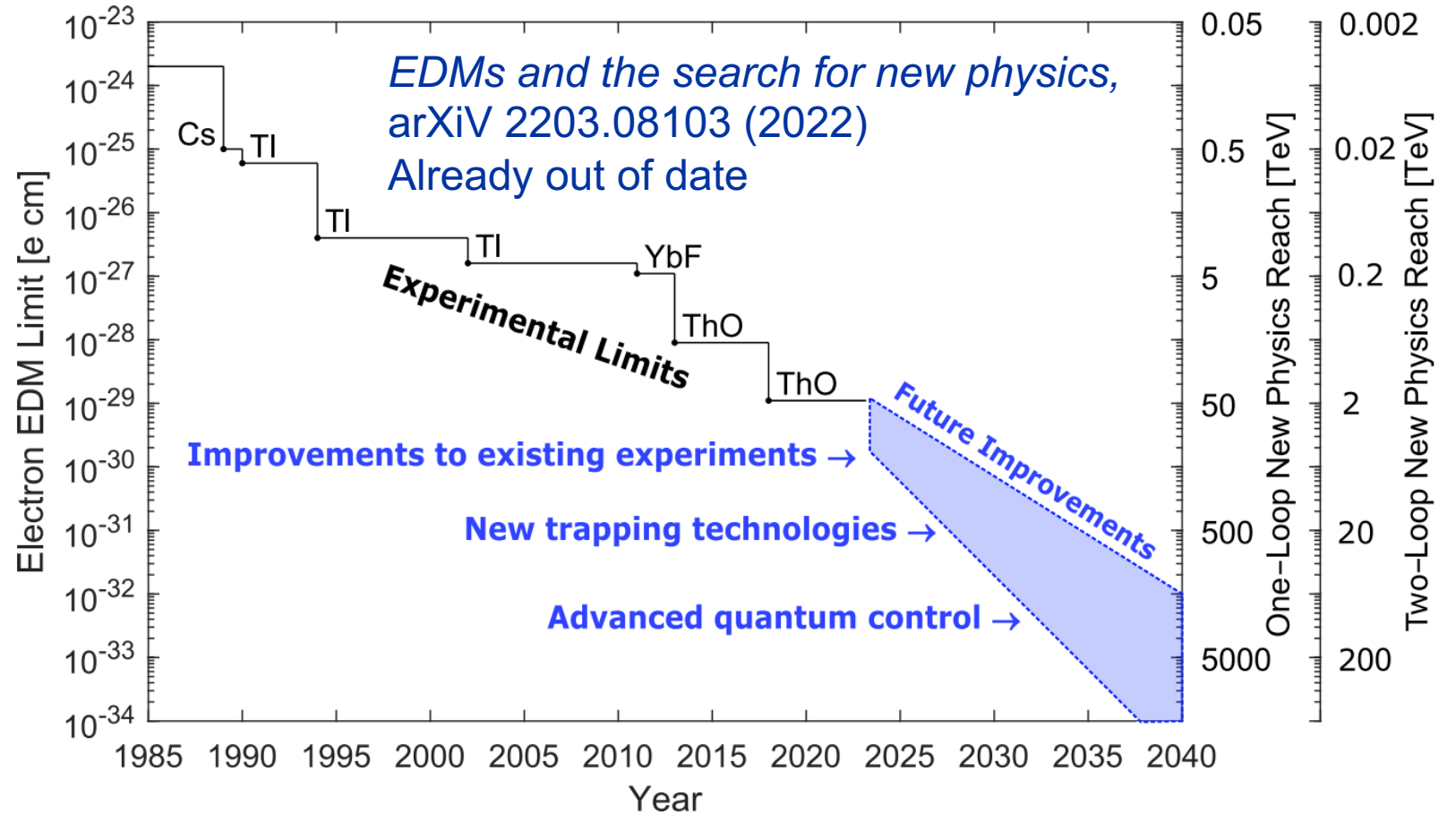
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CPV in molecules

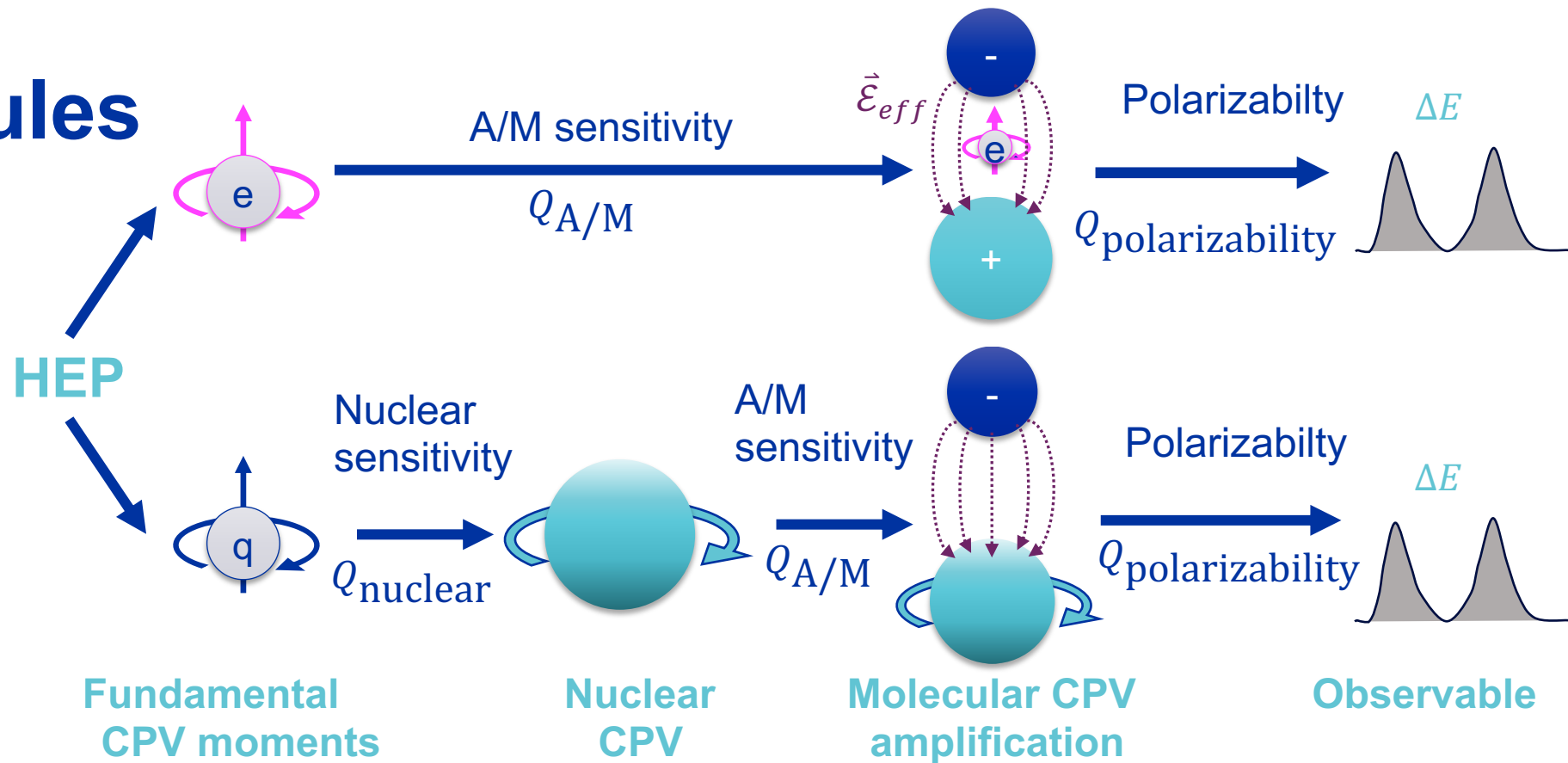
CPV searches (EDM searches)

- using a strong electric field and looking for spin precession

Molecular enhancement

- $\vec{\epsilon}_{eff}$ along molecular axis
~GV / cm
- Polar molecules can be aligned with lab axis with weak fields (~V / cm)

→ Molecular searches are exceptionally sensitive to leptonic, hadronic, and nuclear EDMs



Statistical uncertainty scales as

$$\frac{1}{Q_{eff} \tau \sqrt{N}}$$

Sensitivity
Extremely large for polar radioactive molecules

Spin precession time


Number of particles

Pathway to improved limits on EDMs

Statistical uncertainty scales as

$$\frac{1}{Q_{\text{eff}} \tau \sqrt{N}}$$

Efficiently produced and trapped radioactive molecules

$$\sqrt{N}$$


$$\tau$$

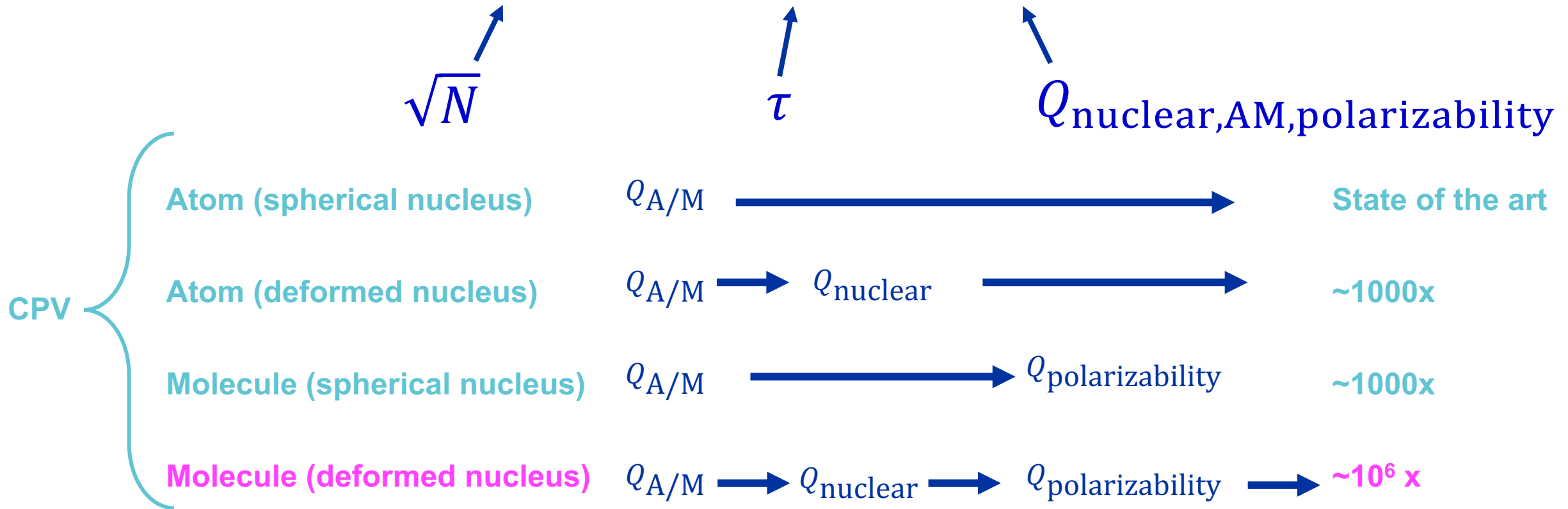

$$Q_{\text{nuclear,AM,polarizability}}$$


Pathway to improved limits on EDMs

Statistical uncertainty scales as

$$\frac{1}{Q_{\text{eff}} \tau \sqrt{N}}$$

Efficiently produced and trapped radioactive molecules



Conceptualization courtesy of N. Hutzler (2024)

Pathway to improved limits on EDMs

Statistical uncertainty scales as

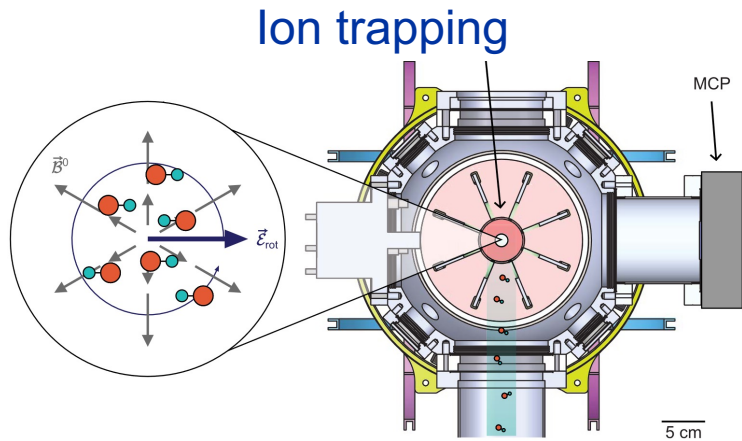
$$\frac{1}{Q_{\text{eff}} \tau \sqrt{N}}$$

Efficiently produced and trapped radioactive molecules

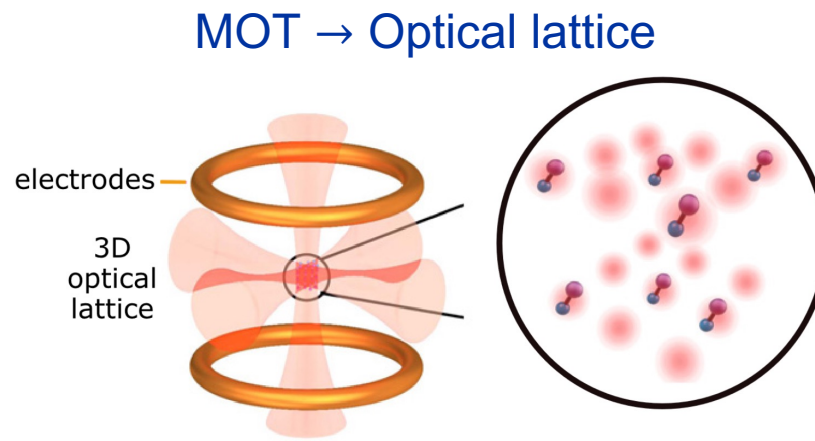
\sqrt{N}

τ

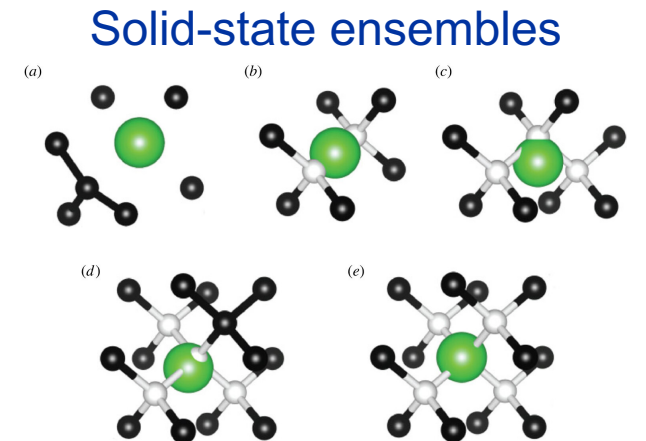
$Q_{\text{nuclear,AM,polarizability}}$



Roussy et al., *Science* 381, 46 (2023)



Fitch et al., *Q.Sci.T.* 6, 014006 (2021)



Morris et al., *Phil. Trans. R. Soc. A.* 3822 (2023)

Pathway to improved limits on EDMs

Statistical uncertainty scales as

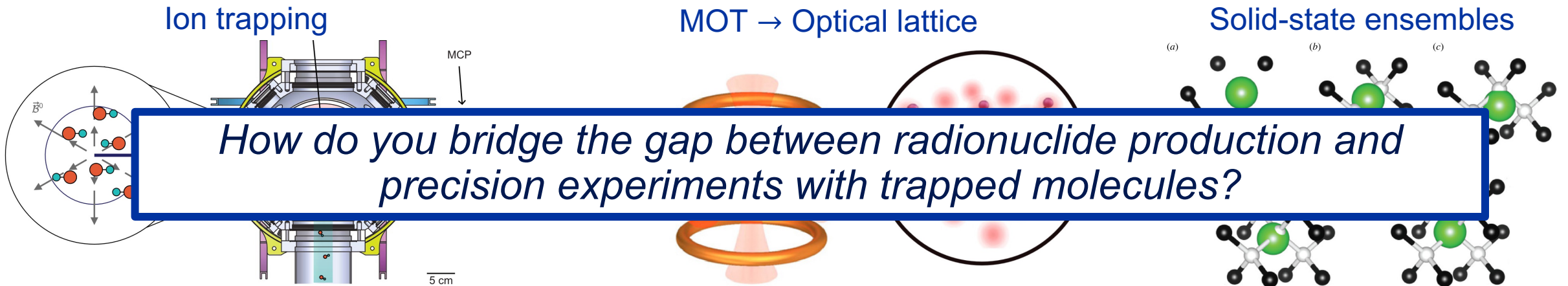
$$\frac{1}{Q_{\text{eff}} \tau \sqrt{N}}$$

Efficiently produced and trapped radioactive molecules

$$\sqrt{N}$$

$$\tau$$

$$Q_{\text{nuclear,AM,polarizability}}$$



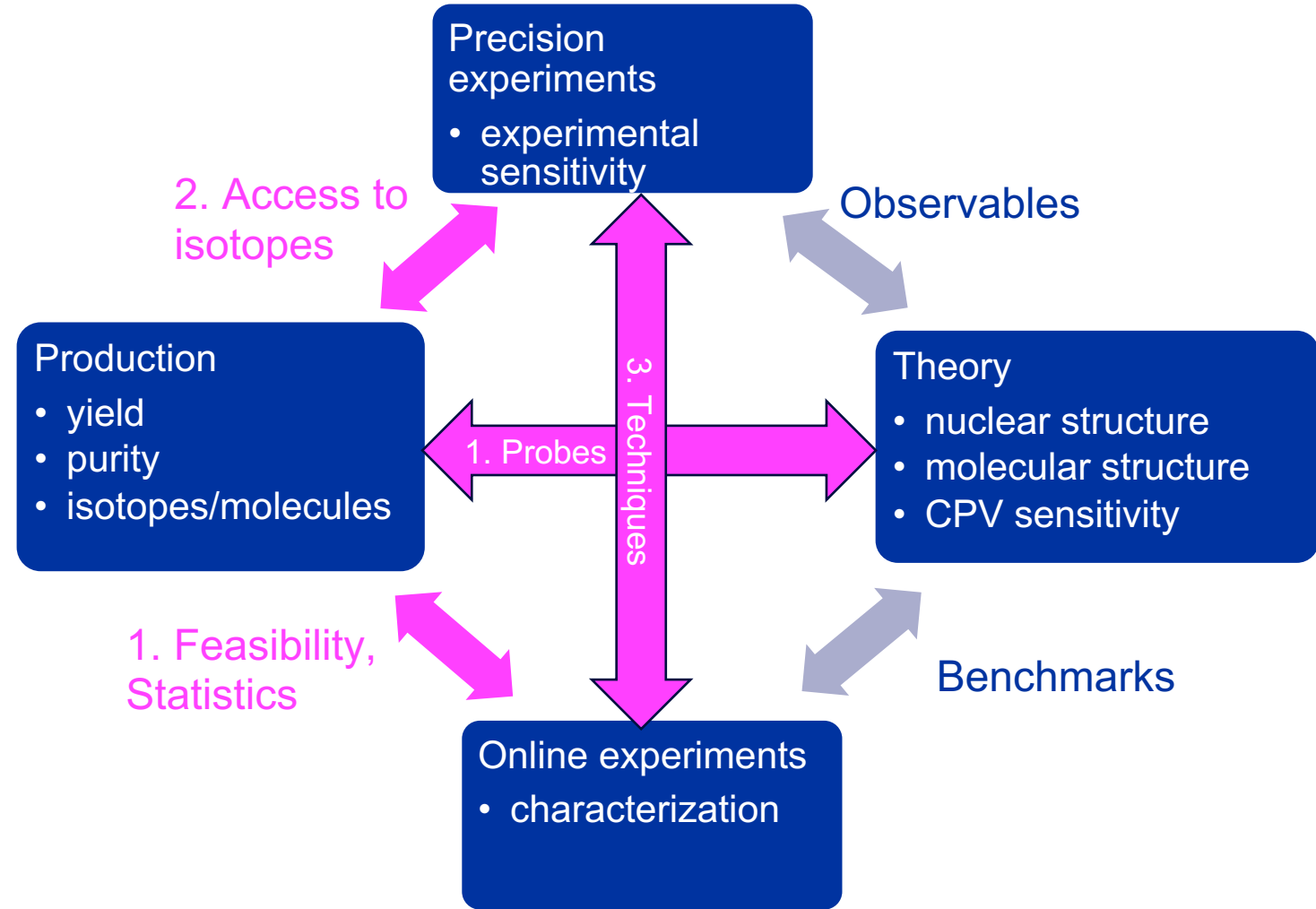
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Morris et al., *Phil. Trans. R. Soc. A.* 3822 (2023)

Proposal

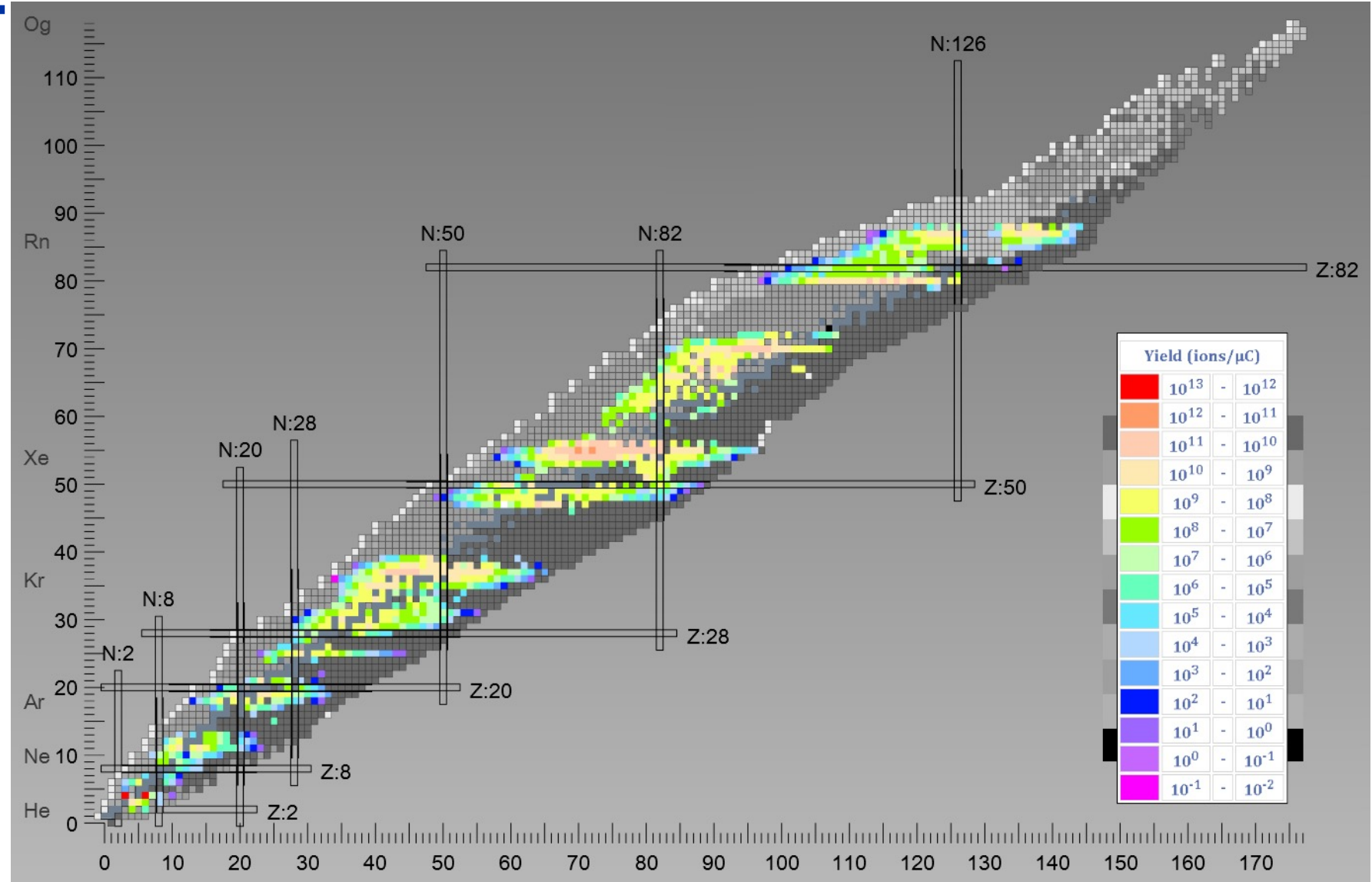
- 1 Access to new probes for online experiments
- 2 Production for offline experiments
- 3 Precision for online experiments
- 4 Towards precision measurements with radioactive molecules



CERN-ISOLDE

>1000
isotopes and
isomers

74 elements



www.nucleonica.com, Dataset:
JEFF-3.1 Nuclear Data Library,
NEA (2023)

Ballof *et.al*, (2020) *NIM B* **463**, 211-
215

cern.ch/isolde-yields



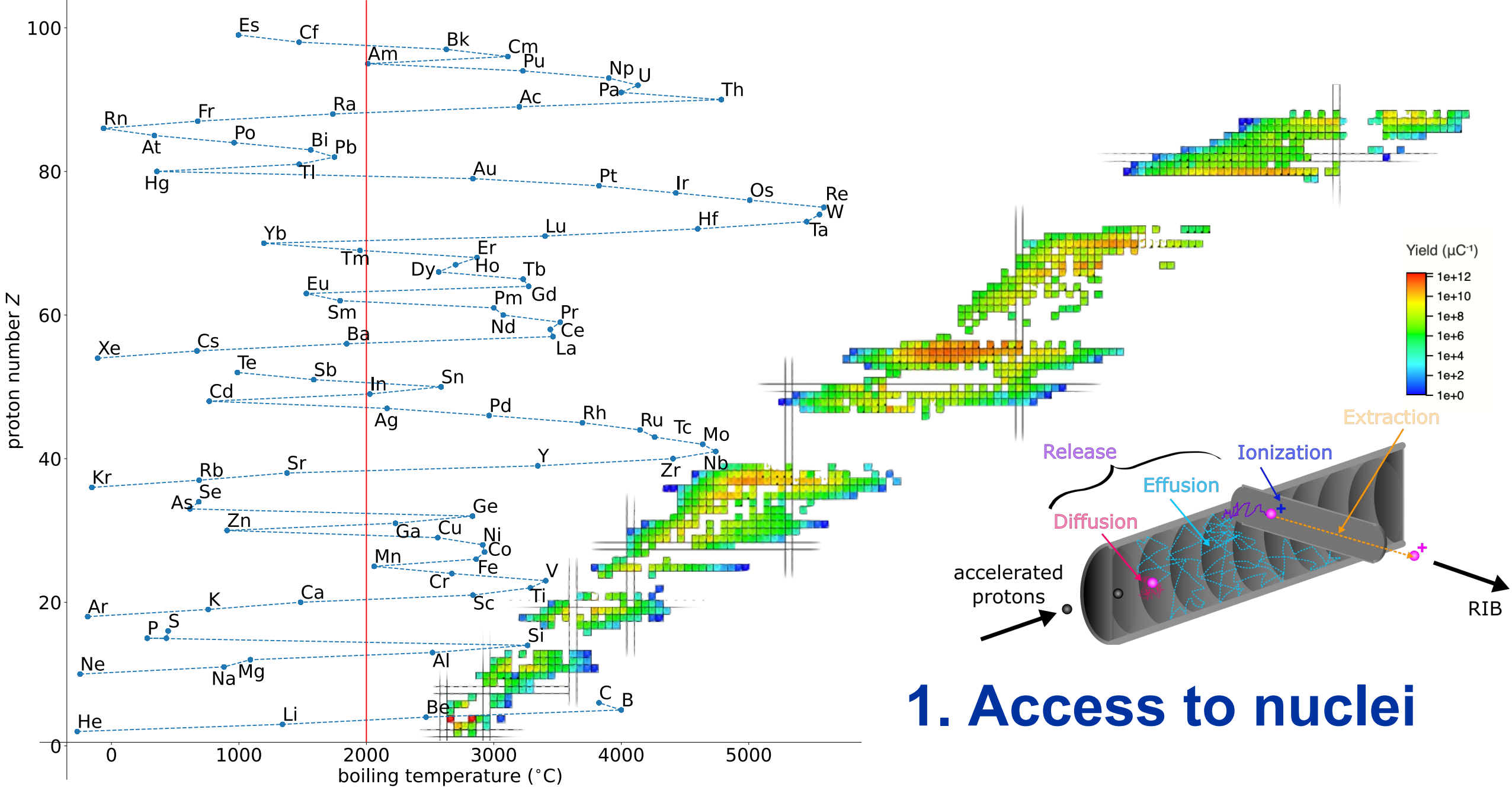
SY
Accelerator Systems

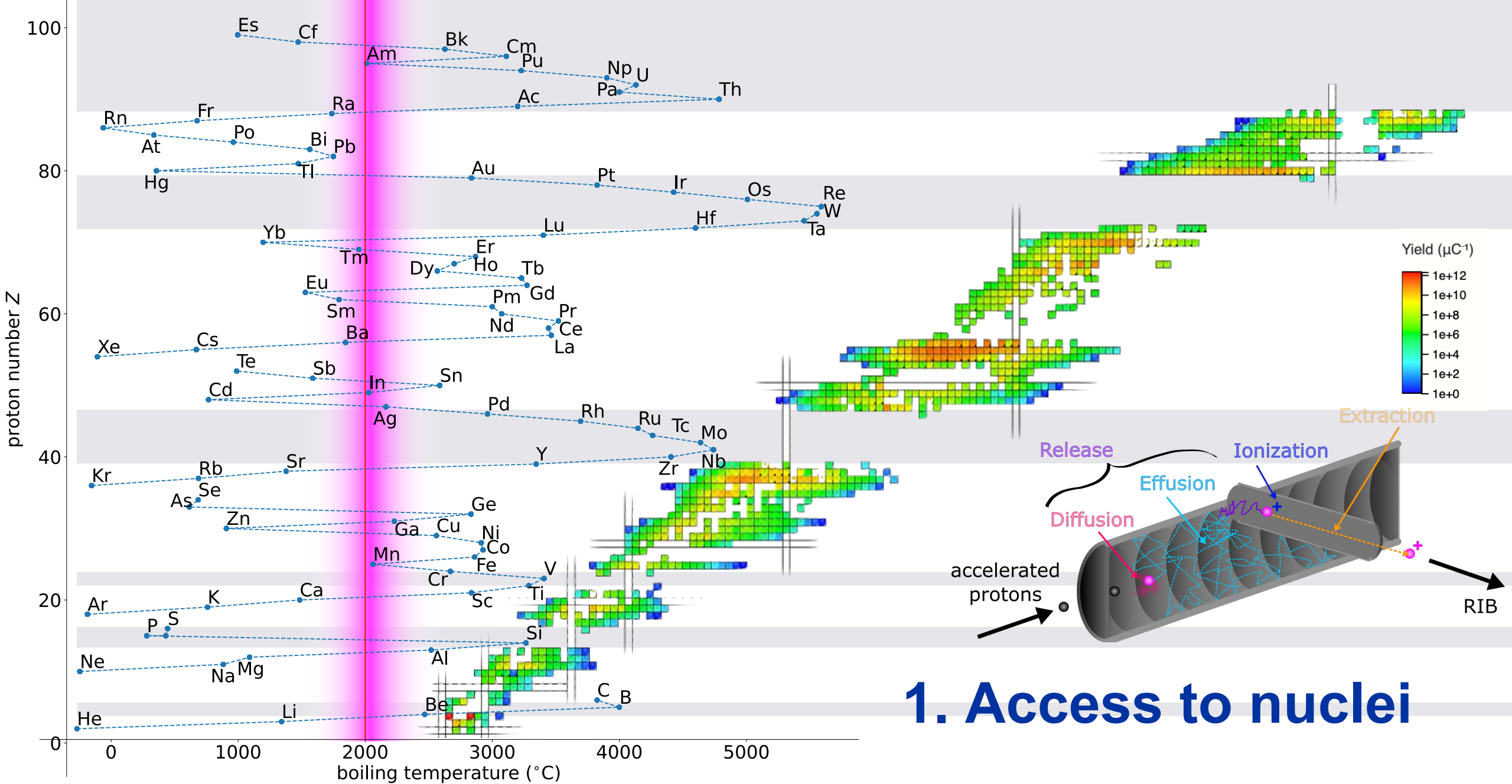


26.03.24

M. Au, M. Athanasakis-Kaklamanakis | Physics Beyond Colliders

7





1. Access to nuclei

2. Production of radioactive molecules for offline experiments

Facilities for ISOLDE TISD

- MEDICIS, GLM, LA1, YOL

Proposal

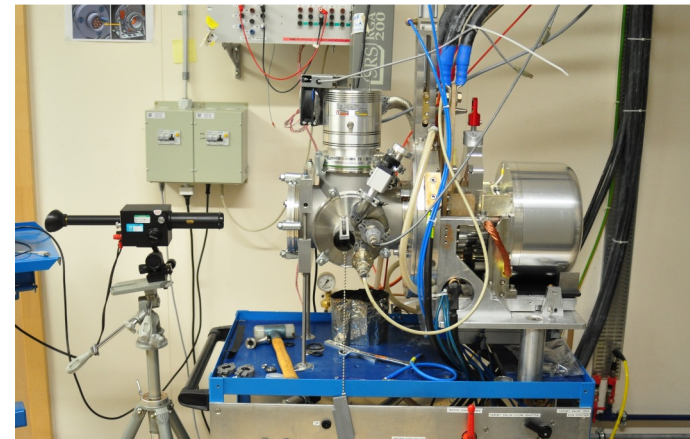
- Feasibility studies, efficiency characterization of isotope collection and transport

Extension and collaboration

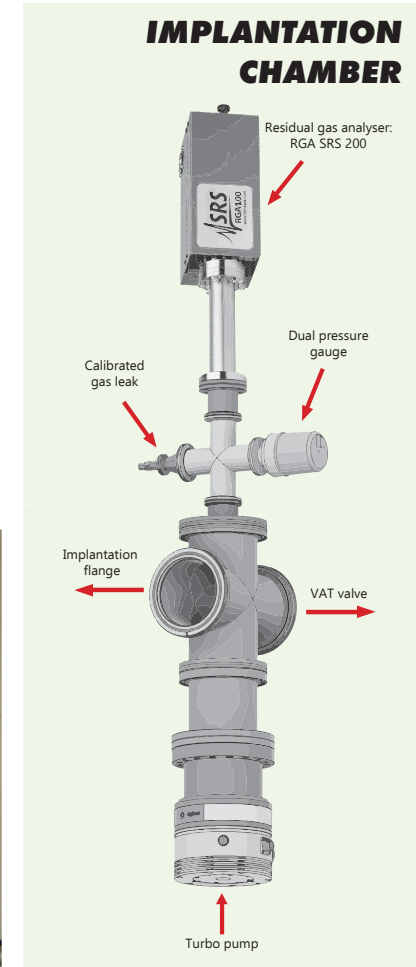
- Ablation and measurement:
- Imperial College London, Hutzler lab (Caltech), EMA (MIT), RAFICI (University of Edinburgh)



ISOLDE OFFLINE 1
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ISOLDE
PUMP STAND
© 2019-2022
CERN



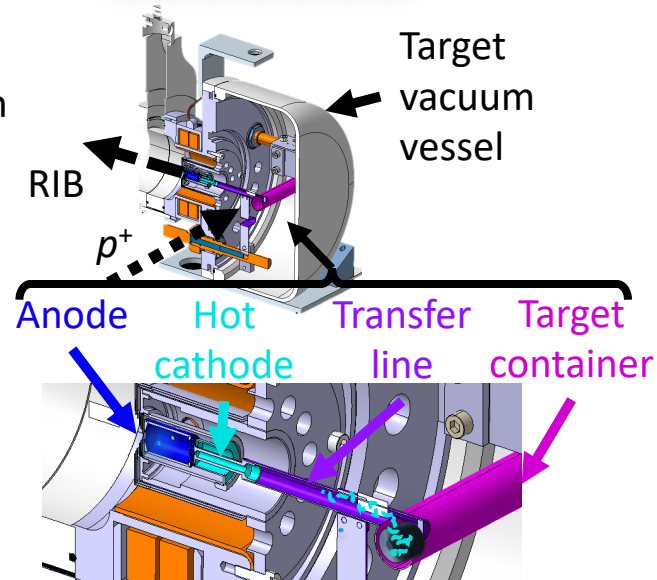
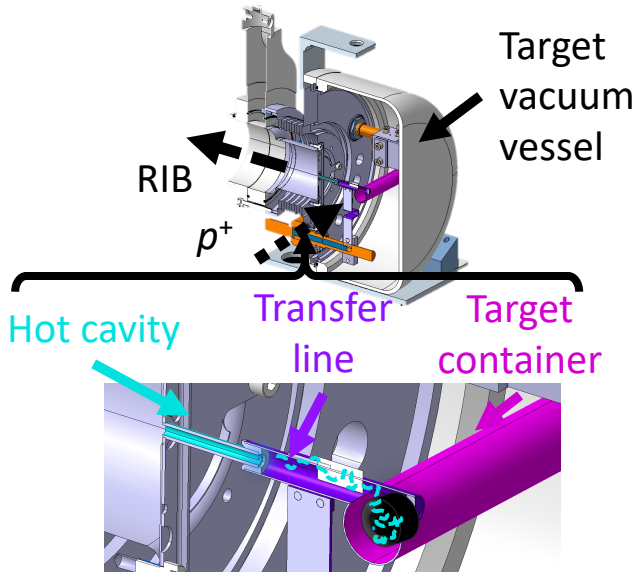
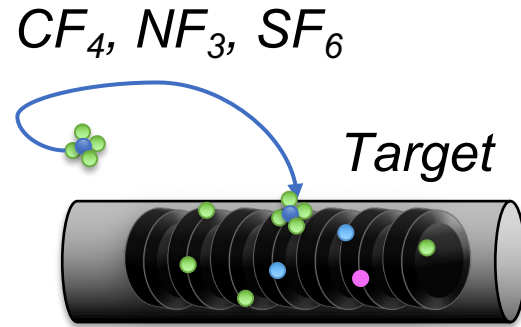
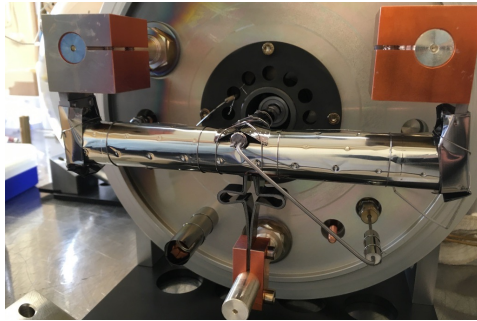
[1] Au et al. (2023) *NIM B.* **541** (144-147)

[2] Wojtaczka et al. (2023) *ICIS'23*, Victoria, Canada

3. Online experiments

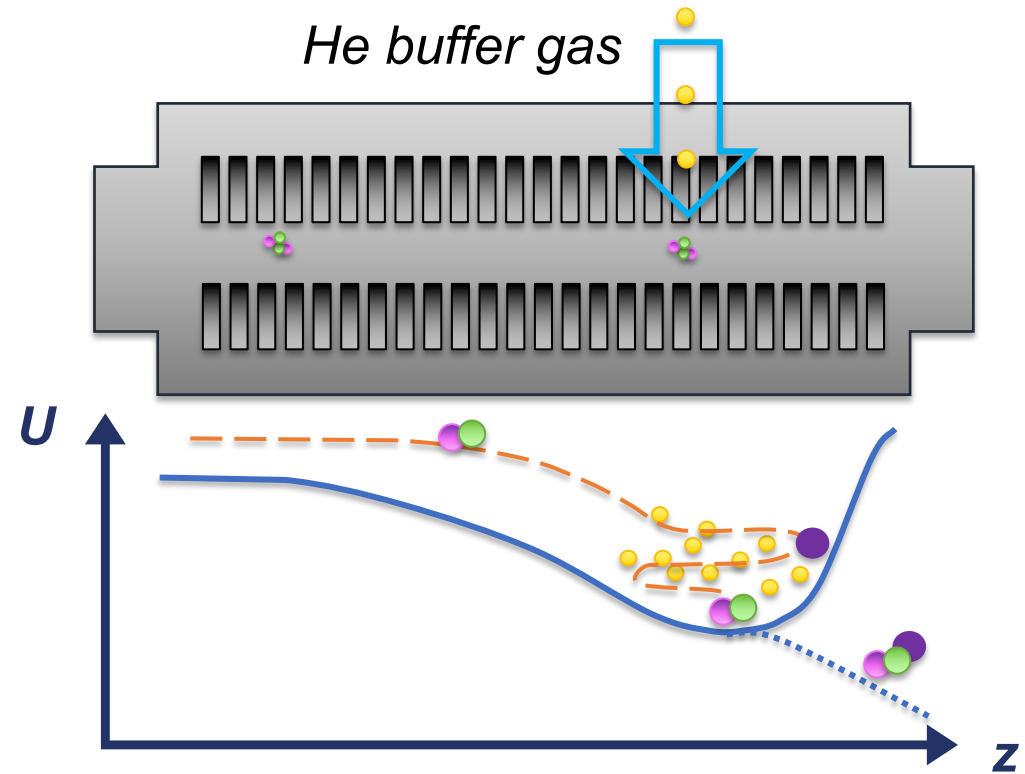
In-source

- Reactive gas



In-trap

- Radio-frequency quadrupole cooler-buncher (RFQ-cb)

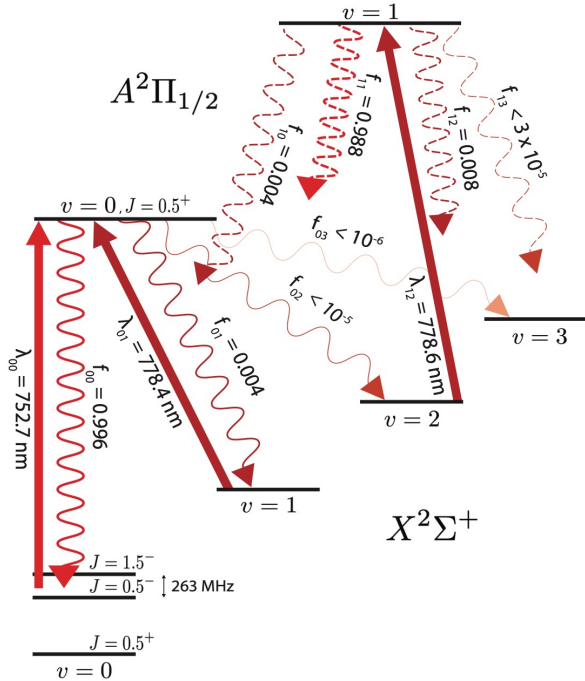


Au et al. (2023) *NIM B.* **541** (375-379)

RaF characterization at CERN-ISOLDE

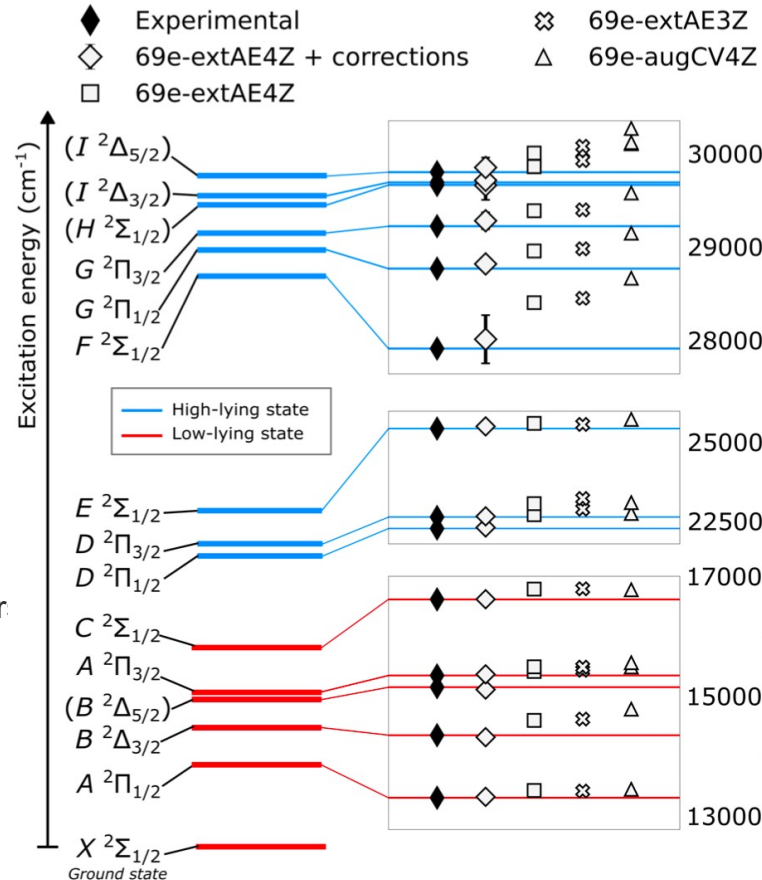


Laser cooling [1]



Excited states [2]

- agreement $\geq 99.64\%$ (~ 12 meV)

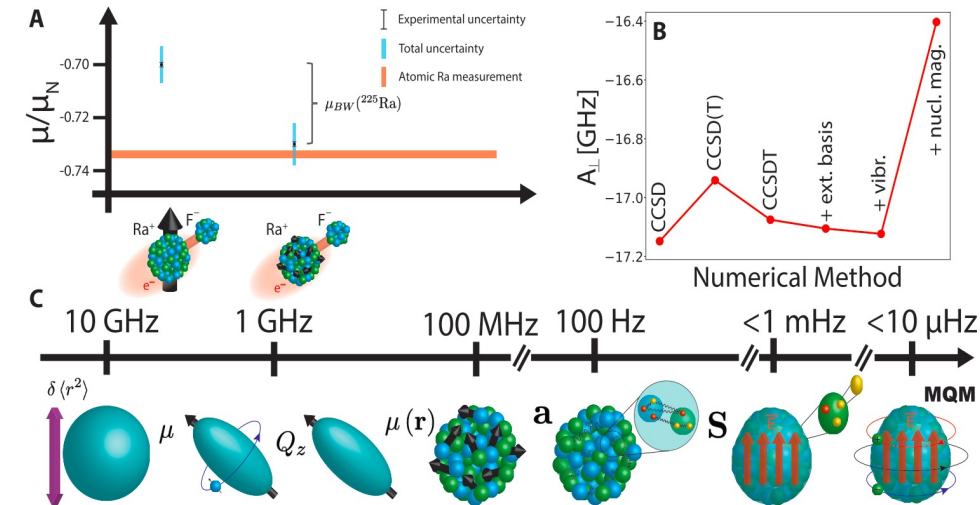


State lifetimes [3]

- Radiative lifetime of $A^2\Pi_{1/2}$ state

Nuclear magnetization effect [4]

- $\mu(^{225}\text{Ra})$

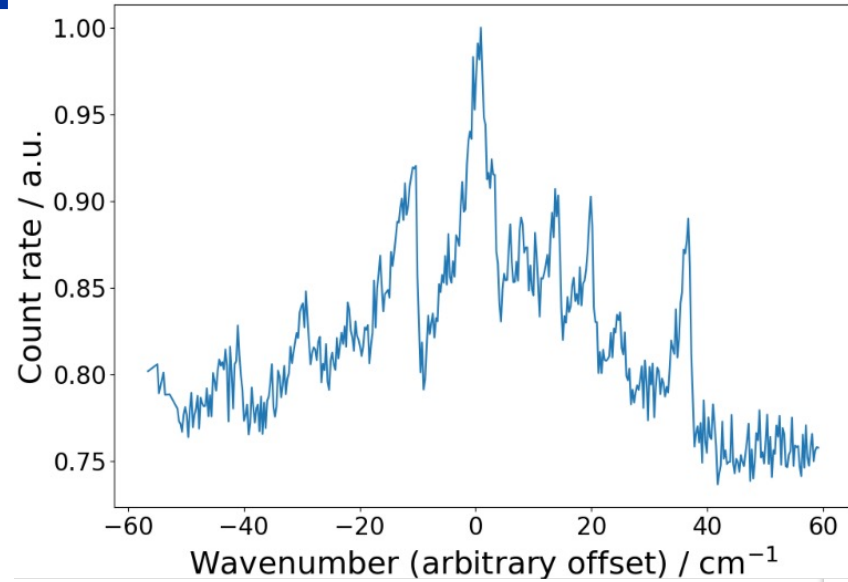


- [1] Udrescu et al., Research Square 10.21203/rs.3.rs.2648482/v1 accepted in Nat. Phys. (2023)
 [2] Athanasakis-Kaklamanakis et al., arXiv 2308.14862 submitted to PRL (2023)
 [3] Athanasakis-Kaklamanakis et al., arXiv 2403.09336 submitted to PRA (2024)
 [4] Wilkins et al., arXiv 2311.04121 submitted to Science (2024)

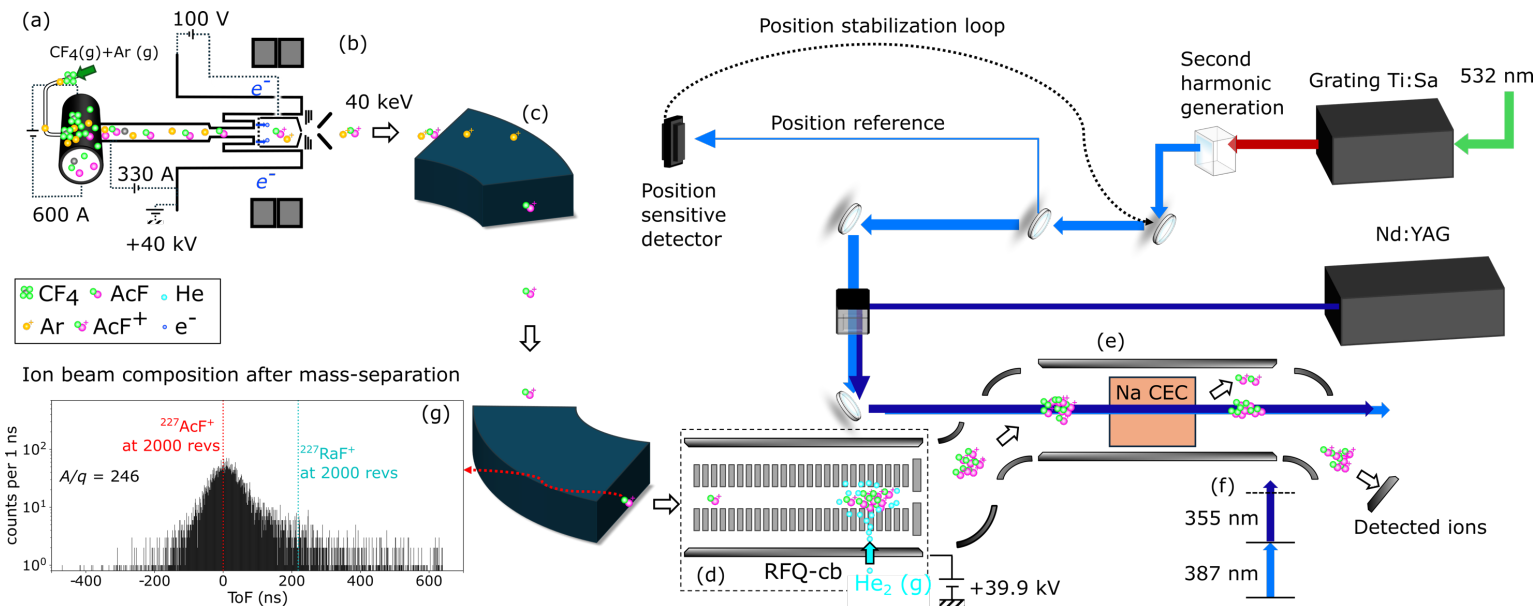
Multiple probes: AcF

Characterization

- $t_{1/2}$ and radioactivity challenging for offline setups
- 1 y proposal to beamtime



EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH
Proposal to the ISOLDE and Neutron Time-of-Flight Committee



Laser ionization spectroscopy of AcF

September 28, 2021

M. Athanasakis-Kaklamanakis^{1,2}, S.G. Wilkins³, M. Au^{4,5}, R. Berger⁶, A. Borschevsky⁷,
K. Chrysalidis⁸, T.E. Coccolios², R.P. de Groot², Ch.E. Düllmann^{5,9,10},
K.T. Flanagan^{11,12}, R.F. Garcia Ruiz³, S. Geldhof², R. Heinke⁸, T.A. Isaev¹³,
J. Johnson², A. Kiuberis⁷, Á. Kozzorús¹, L. Lalanne², M. Mougeot¹, G. Neyens²,
L. Nies^{1,14}, J. Reilly¹¹, S. Rothe⁴, L. Schweikhard¹⁴, A.R. Vernon³, X.F. Yang¹⁵

[1] Athanasakis-Kaklamanakis, Wilkins, Au *et al.*, (2021) <https://cds.cern.ch/record/2782407>, INTC-P-615

[2] Athanasakis-Kaklamanakis and Au, (2023) *CERN EP newsletter*

[3] Athanasakis-Kaklamanakis, Au, Kyuberis, Zülch, Wibowo, Skripnikov, Reilly, Lalanne *et al.*, in preparation 2024

Towards precision experiments at RIB facilities

Preparation of molecule

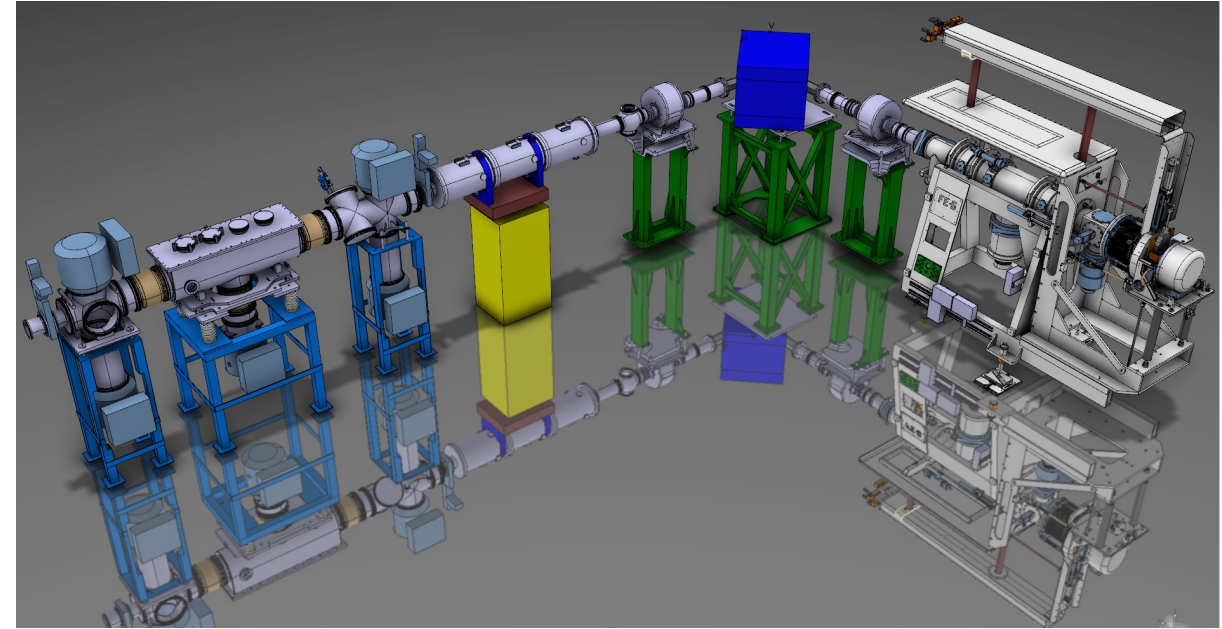
- Maximizing polarizability, inherent sensitivity
- Low-temperature molecular formation
- Control and selectivity of chemical reactions

Preparation of “science state”

- Deceleration from extraction energy
- Cooling
- Noise – E, B systematics

Proposal

- test feasibility of delivering cold, prepared ensembles for precision measurements
- initial upgrades to existing infrastructure

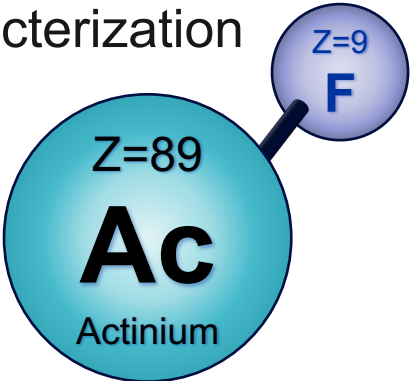


Photos: ISOLDE OFFLINE 2 © 2019-2022 CERN

Summary: radioactive molecules for PBC

1. Beam development at CERN-ISOLDE

- Provision of heavy, octupole deformed nuclei with sensitivity to symmetry violations
- Molecular formation techniques for delivery of sensitive, polarizable complementary probes for characterization



2. Radioactive species for offline precision experiments

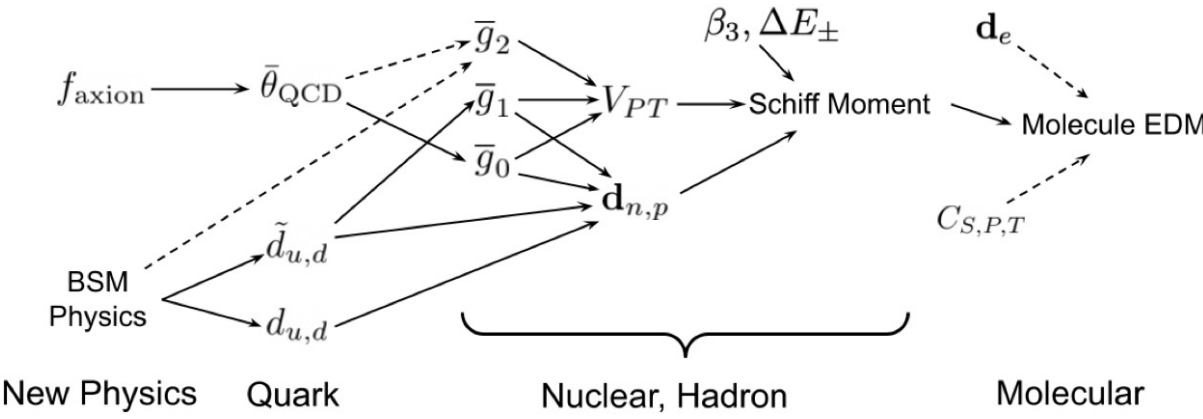
- Collection and transportation of radioactive nuclei to precision experiments



Image published in EP Newsletter, CERN (2020)

3. Beam preparation towards precision for online experiments

- Feasibility of delivering cold, prepared ensembles for precision measurements



Opportunities for Fundamental Physics Research with Radioactive Molecules, arXiv 2302.02165 (2023), Rep. Prog. Phys. (2024) doi: 10.1088/1361-6633/ad1e39

Conclusion: a tipping point

Community: rapidly growing, particle, nuclear, AMO physics, experimental and theory

- “In the next 10 years gains in sensitivity by several orders of magnitude over current bounds are possible and even likely for electrons, nucleons, atoms and molecules, with the very real chance of discovery.” – Snowmass contribution, 2021
- INT Program INT-24 (March 2024)
<https://www.int.washington.edu/programs-and-workshops/24-1>
- New Opportunities for Fundamental Physics Research with Radioactive Molecules, Virtual Meeting (2021)

Given the low relative cost of these experiments in terms of both funding (\lesssim \$10 M, and often \lesssim 1 M) and personnel (typically \lesssim 10 people), pursuing many simultaneously is feasible. However, advancing to the next generation will require increases in scale and complexity. Many of the new approaches discussed here require sustained R&D budgets, theory support, and access to facilities when working with exotic nuclei, continued over several experimental generations to fully realize their projected gains. The field is moving very rapidly and requires risk tolerance, but it has proven that it can deliver results from a variety of novel approaches.



European EDM community

- ECT*, Trento (March 2024)
- Outcome: Formation of Europe-wide matter EDM network where experiments with unstable nuclei will be a major aspect for future work

EDMs: complementary experiments and theory connections

Mar 4 – 8, 2024
ECT*
Europe/Rome timezone

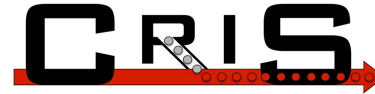
Enter your search



Thank you!

Acknowledgements

J. Ballof, R. Berger, A. Borschevsky, A. Breier, K. Chrysalidis, R.P. de Groote, Ch.E. Düllmann, C. Fajardo-Zambrano, P. Fischer, K. Flanagan, R.F. Garcia Ruiz, K. Gaul, P.F. Giesel, S. Gilardoni, R. Heinke, S. Hoekstra, N. Hutzler, Á. Koszorus, A. Kyuberis, D. Lange, B.A. Marsh, G. Neyens, L. Nies, E. Reis, S. Rothe, A. Oleynichenko, M. P. Reiter, P. Schmidt-Wellenburg, C. Schweiger, L. Skripnikov, M. Tarbutt, S. Wilkins, W. Wojtaczka, The CRIS collaboration, The ISOLDE collaboration



This project has received funding from the European's Union Horizon 2020 Research and Innovation Programme under grant agreement number 861198 project 'LISA' (Laser Ionization and Spectroscopy of Actinides) Marie Skłodowska-Curie Innovative Training Network (ITN)

Radioactive molecules community: growing every day



Funding request

Catalyst to solidify an active and rapidly growing community with expertise in fundamental symmetries, nuclear, atomic, molecular, and optical physics, experimentalists and theorists.

Beam development

- 1 postdoc, 2-3 years



Feasibility and precision techniques

- 1 postdoc, 2-3 years
- Collaboration with leaders in the European precision EDM community
 - S. Hoekstra (Precision Frontier, University of Groningen)
 - M. Tarbutt (Centre for Cold Matter, Imperial College London)
 - M. P. Reiter (The University of Edinburgh)
 - P. Schmidt-Wellenburg (PSI)



university of
 groningen

IMPERIAL



THE UNIVERSITY
of EDINBURGH

Infrastructure and consumables

- ~200k



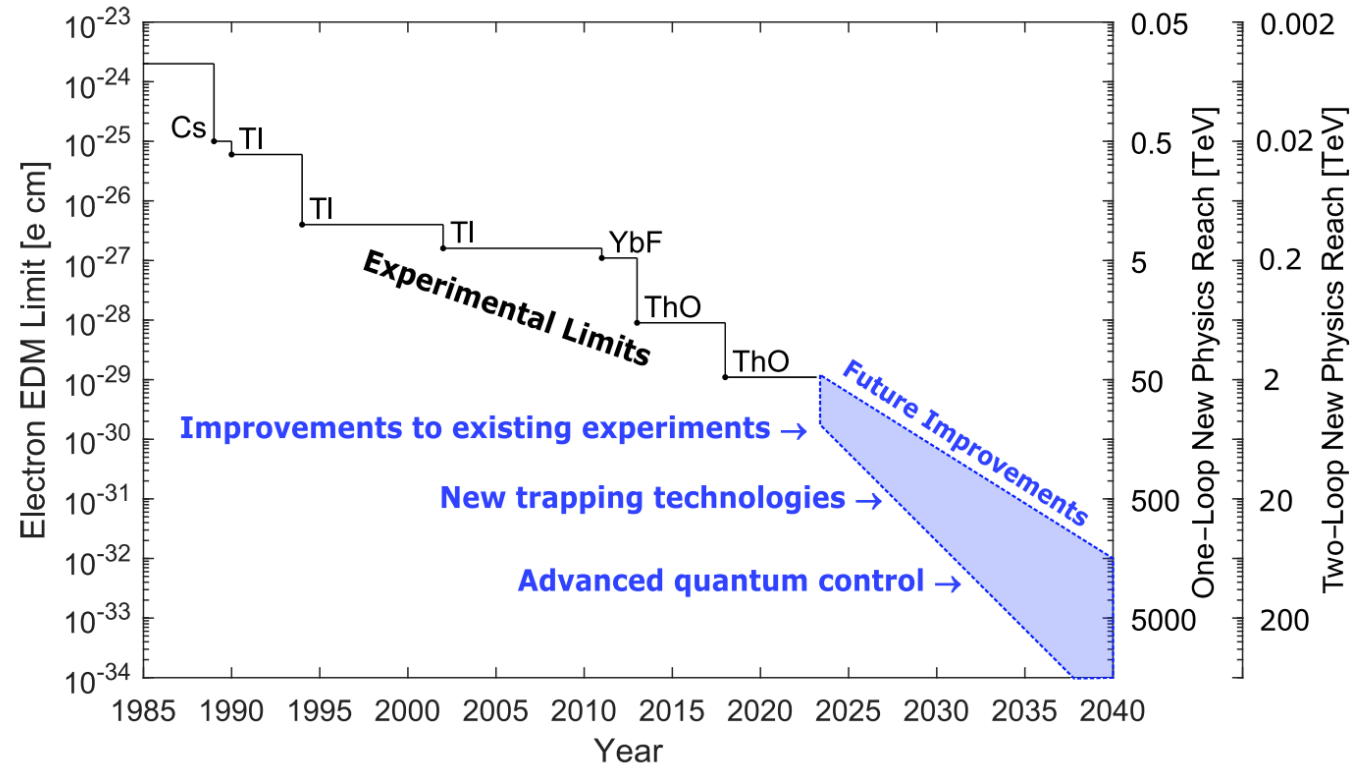
Existing and planned searches

Published:

- eEDM: Cs, TI, YbF (Imperial) [1], ThO (ACME) [2,3], HfF+ (JILA) [4]
- Schiff, MQM: ^{129}Xe , ^{199}Hg , ^{225}Ra [5], ^{171}Yb [6]

Planned / under development:

- ^{225}Ra , ^{223}Ra molecules, FrAg, $^{221/210}\text{Fr}$, RIKEN, ^{229}Pa , PaF $^{3+}$ MSU/FRIB, $^{225/227}\text{AcF}$, ^{229}Th , ^{175}Lu , Old Dominion, Grau, ^{181}Ta , UNLV, Zhou



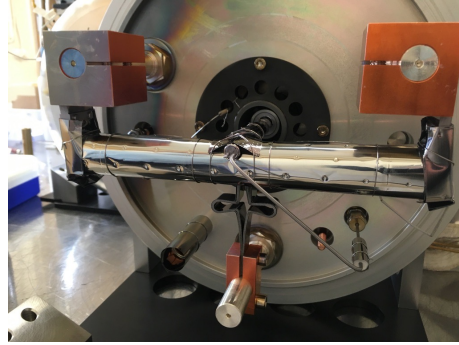
[1] Nature 473, 493 (2011)
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[3] Nature 562, 355 (2018)
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[5] PRC 94, 025501 (2016)
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Material developments

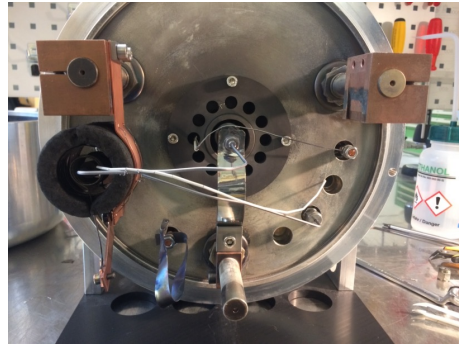
Gas injection

- Reactive/corrosive gases



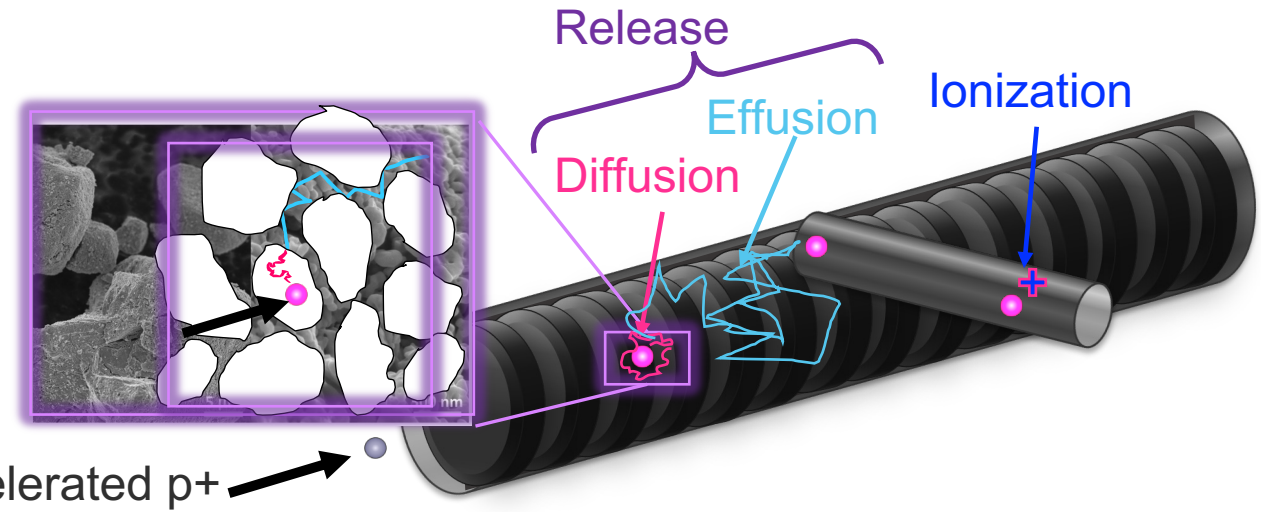
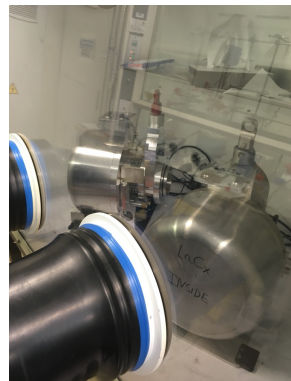
Reactants

- Mass markers



Target materials

- Particle size
- Open porosity



$$Beam\ Intensity = \sigma \cdot j \cdot N_t \cdot \varepsilon$$

N_t – Number of target atoms

j – Proton flux [cm^{-2}]

σ – Cross section [mb]

ε – Efficiency [%]

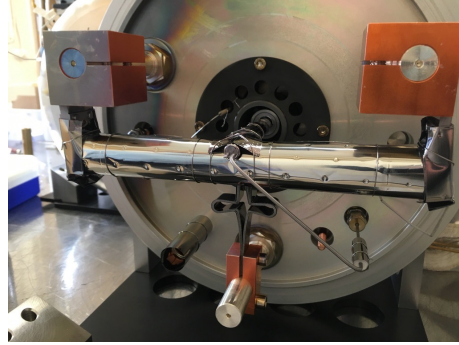
$$\varepsilon = \varepsilon_{diff} \varepsilon_{eff} \varepsilon_{is} \varepsilon_{ext} \varepsilon_{sep} \varepsilon_{trans}$$

Adapted from:
J.P. Ramos. EMIS XIII, CERN, Geneva, 2018.

Material developments

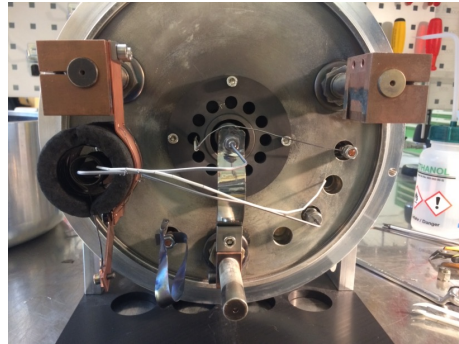
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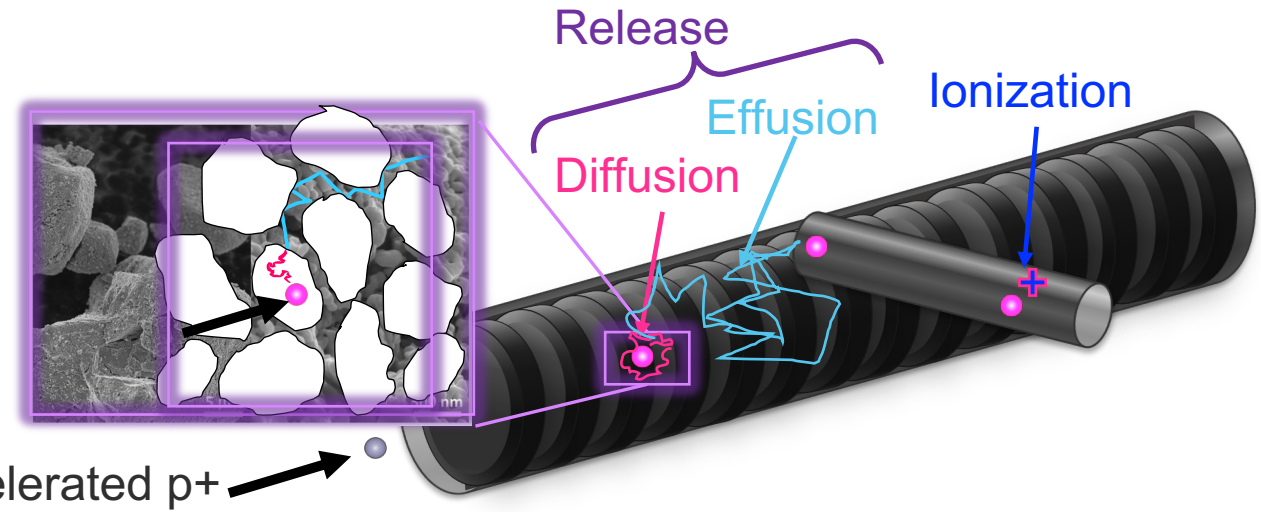
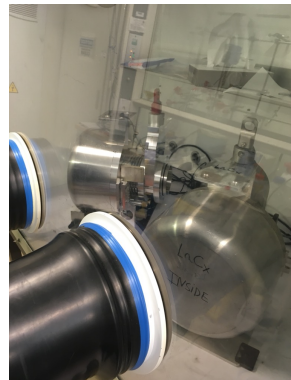
Reactants

- Mass markers



Target materials

- Particle size
- Open porosity



$$Beam\ Intensity = \sigma \cdot j \cdot N_t \cdot \varepsilon$$

N_t – Number of target atoms

j – Proton flux [cm⁻²]

σ – Cross section [mb]

ε – Efficiency [%]

μ – diffusion delay parameter

G – grain size

$$\varepsilon = \varepsilon_{diff} \varepsilon_{eff} \varepsilon_{is} \varepsilon_{ext} \varepsilon_{sep} \varepsilon_{trans}$$

$$\varepsilon_{diff} \propto \sqrt{\mu \cdot T_{1/2}} \propto \frac{1}{G}$$

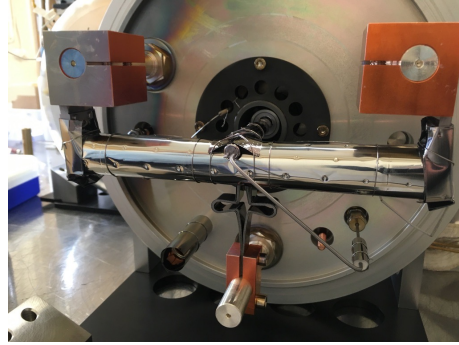
$$\mu = \frac{\pi^2 D}{G^2}$$

Adapted from:
J.P. Ramos. EMIS XIII, CERN, Geneva, 2018.

Material developments

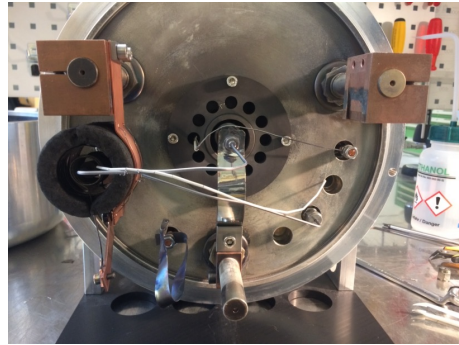
Gas injection

- Reactive/corrosive gases



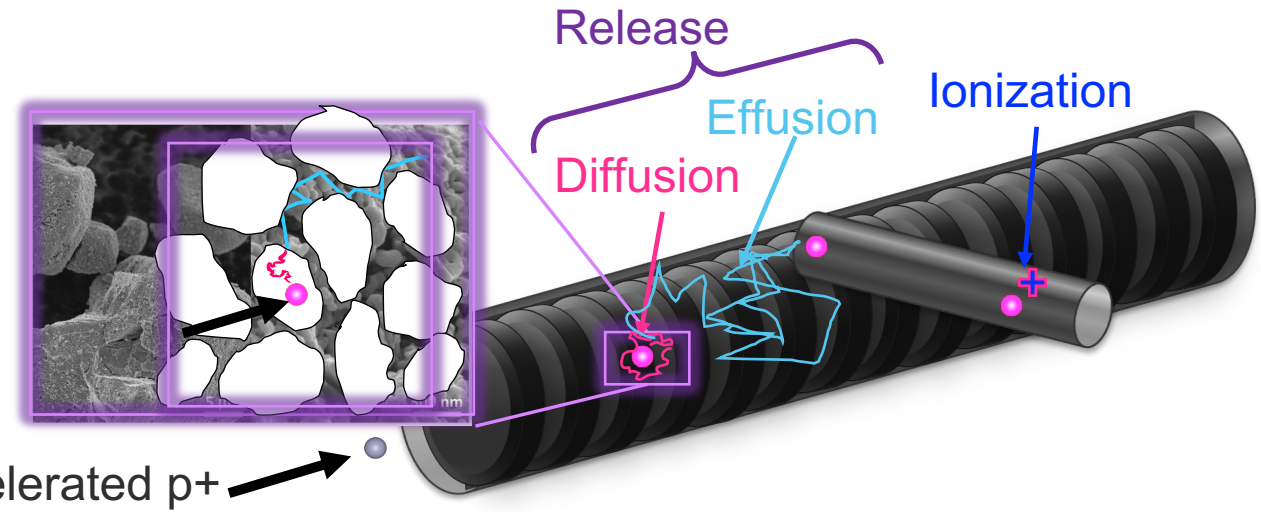
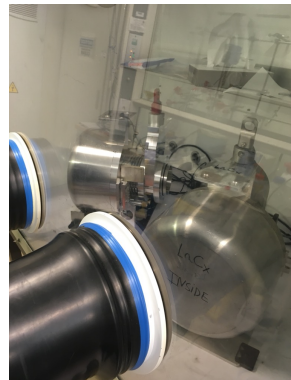
Reactants

- Mass markers



Target materials

- Particle size
- Open porosity



$$Beam\ Intensity = \sigma \cdot j \cdot N_t \cdot \varepsilon$$

N_t – Number of target atoms

j – Proton flux [cm⁻²]

σ – Cross section [mb]

ε – Efficiency [%]

μ – diffusion delay parameter

G – grain size

$$\varepsilon = \varepsilon_{diff} \varepsilon_{eff} \varepsilon_{is} \varepsilon_{ext} \varepsilon_{sep} \varepsilon_{trans}$$

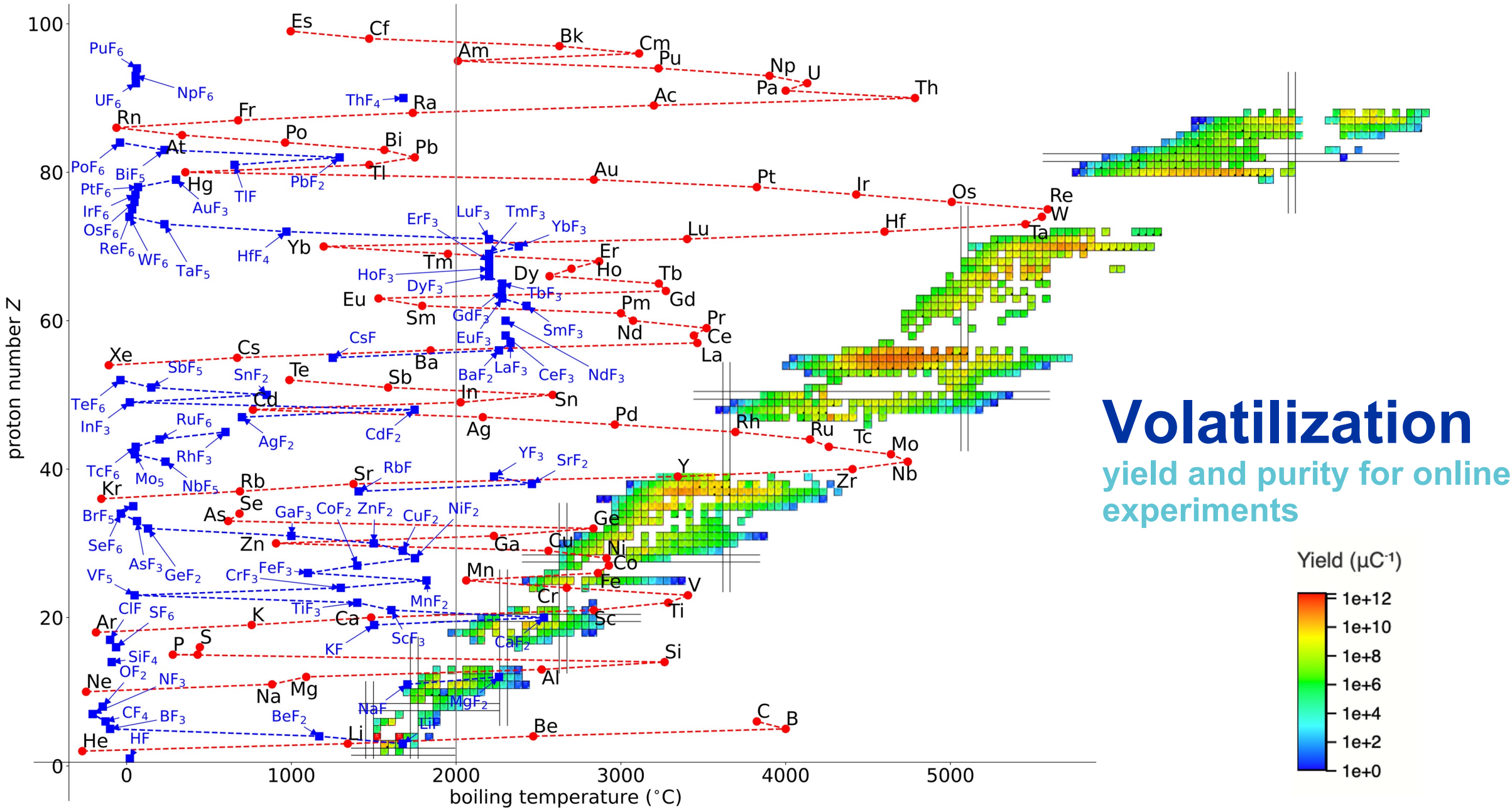
$$\varepsilon_{diff} \propto \sqrt{\mu \cdot T_{1/2}} \propto \frac{1}{G}$$

$$\mu = \frac{\pi^2 D}{G^2}$$

Small G , high T → Increased ε_{diff}

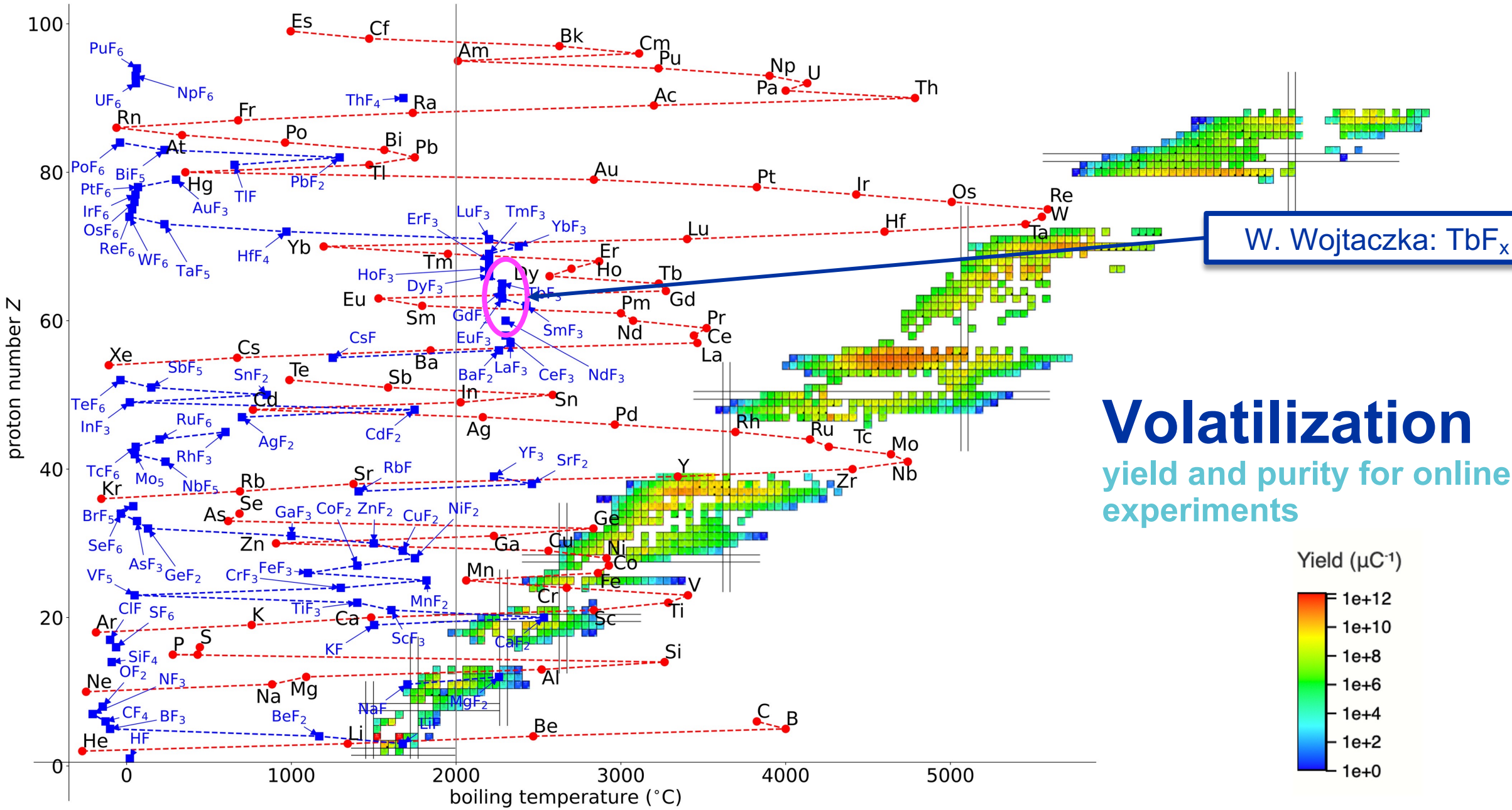
Increased ε_{diff} ↔ Increased sintering and grain growth

Adapted from:
J.P. Ramos. EMIS XIII, CERN, Geneva, 2018.



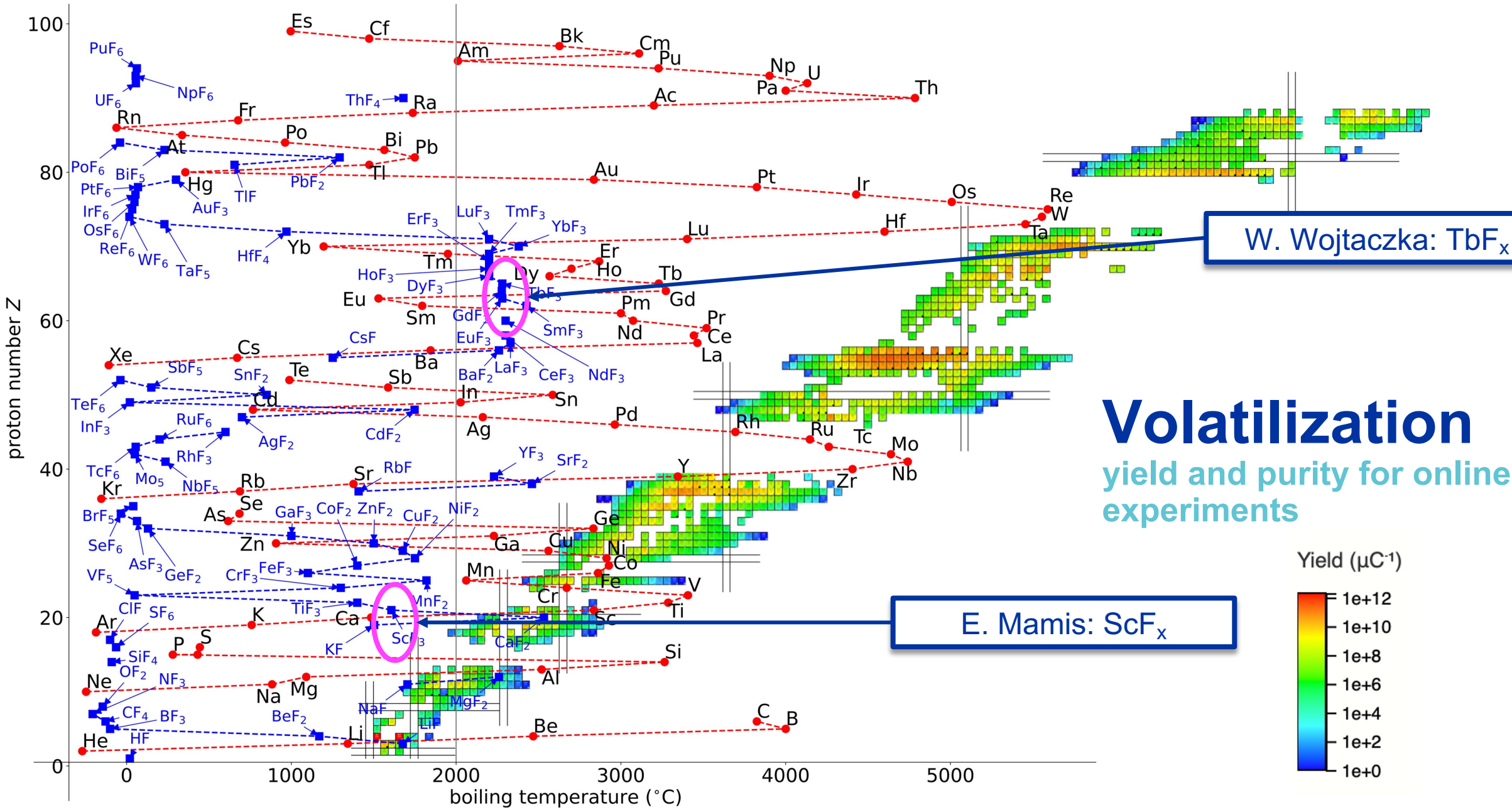
Volatilization

yield and purity for online experiments



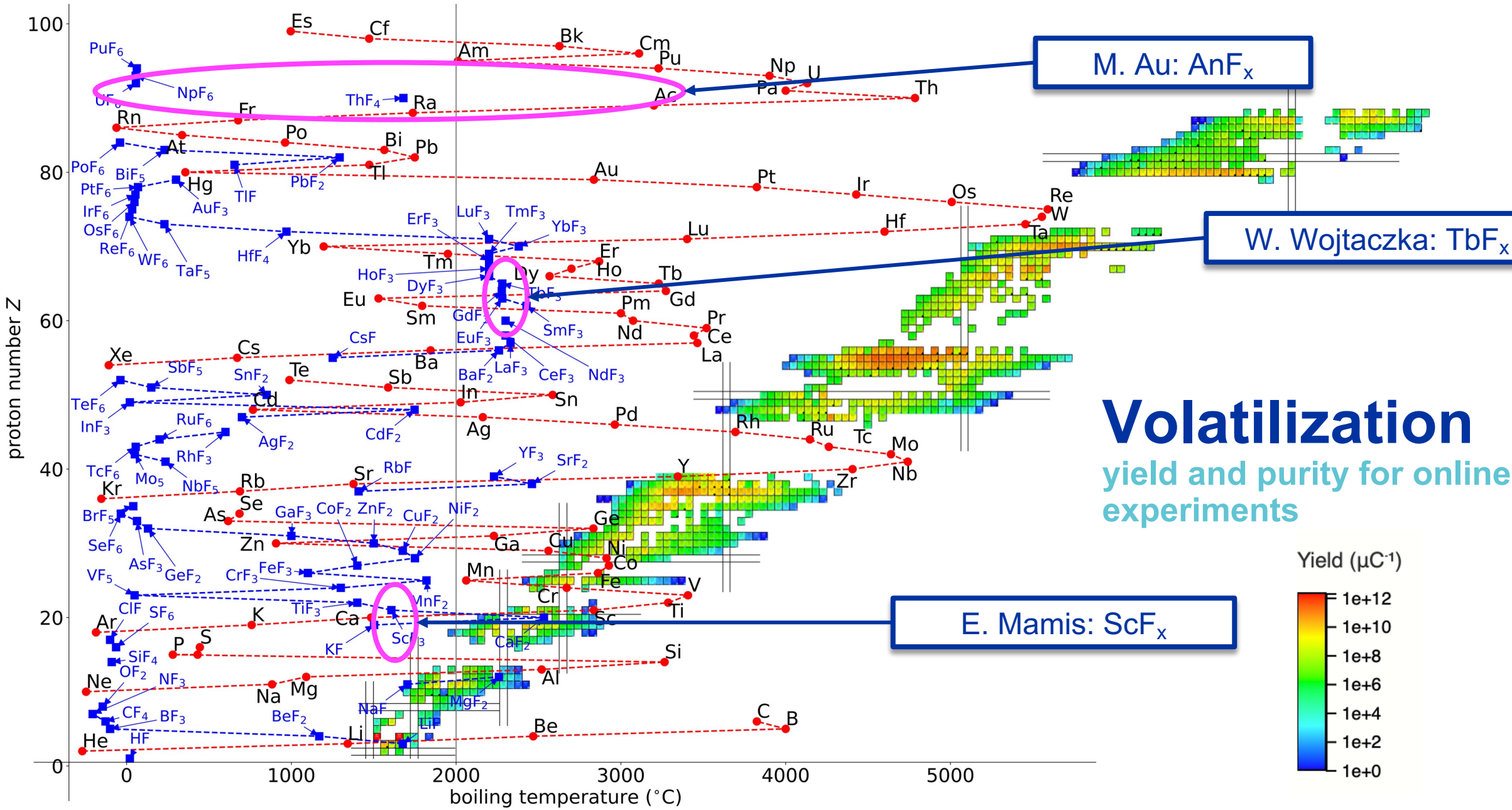
Volatilization

yield and purity for online experiments



Volatilization

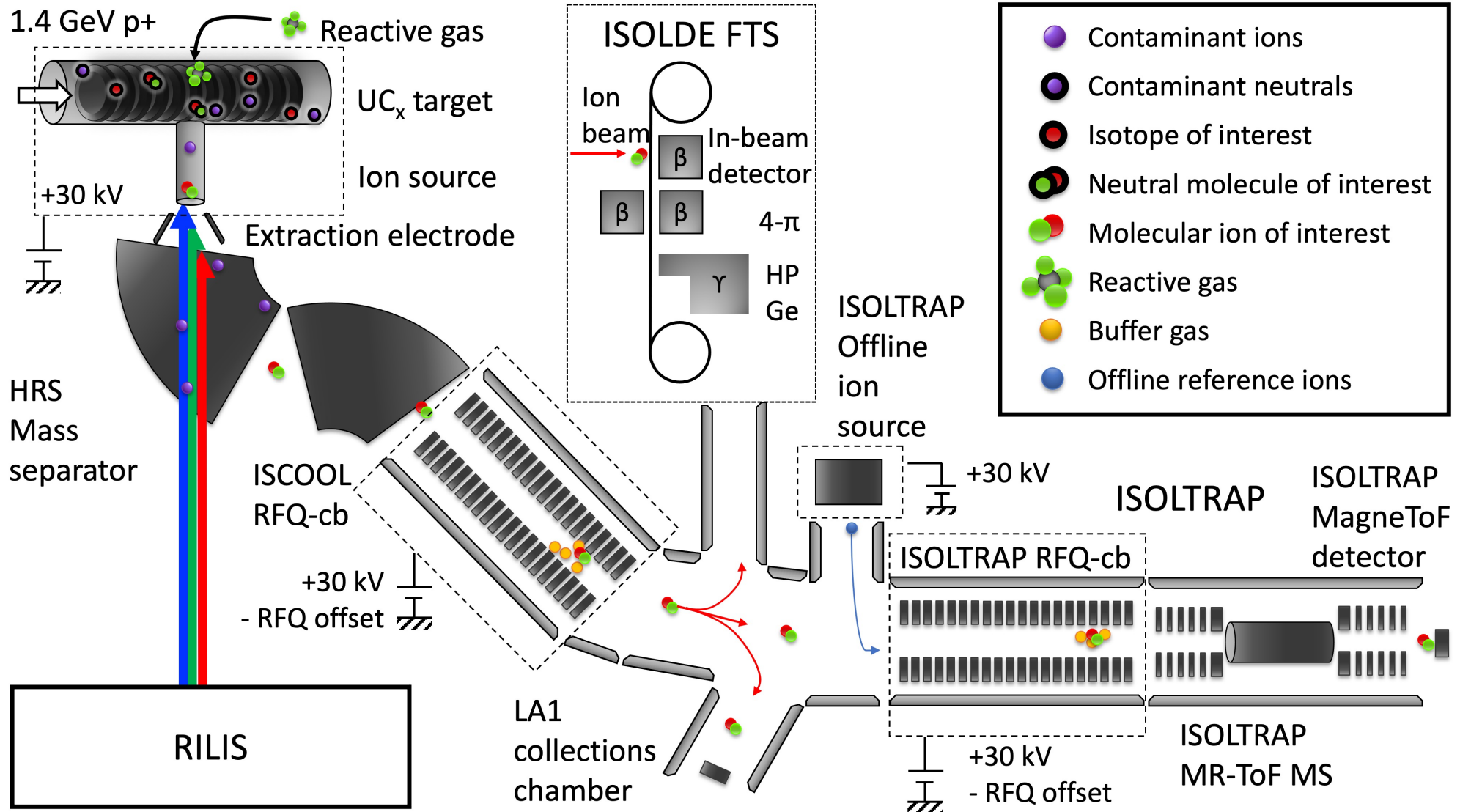
yield and purity for online experiments



Volatilization

yield and purity for online experiments

Detection and identification



Molecular structure

$$E = E_{el} + E_{vib} + E_{rot} + E_{hf}$$

Electronic

- $> 5000 \text{ cm}^{-1}$

Vibrational

- $300 - 3000 \text{ cm}^{-1}$

Rotational

- $1 - 100 \text{ cm}^{-1}$

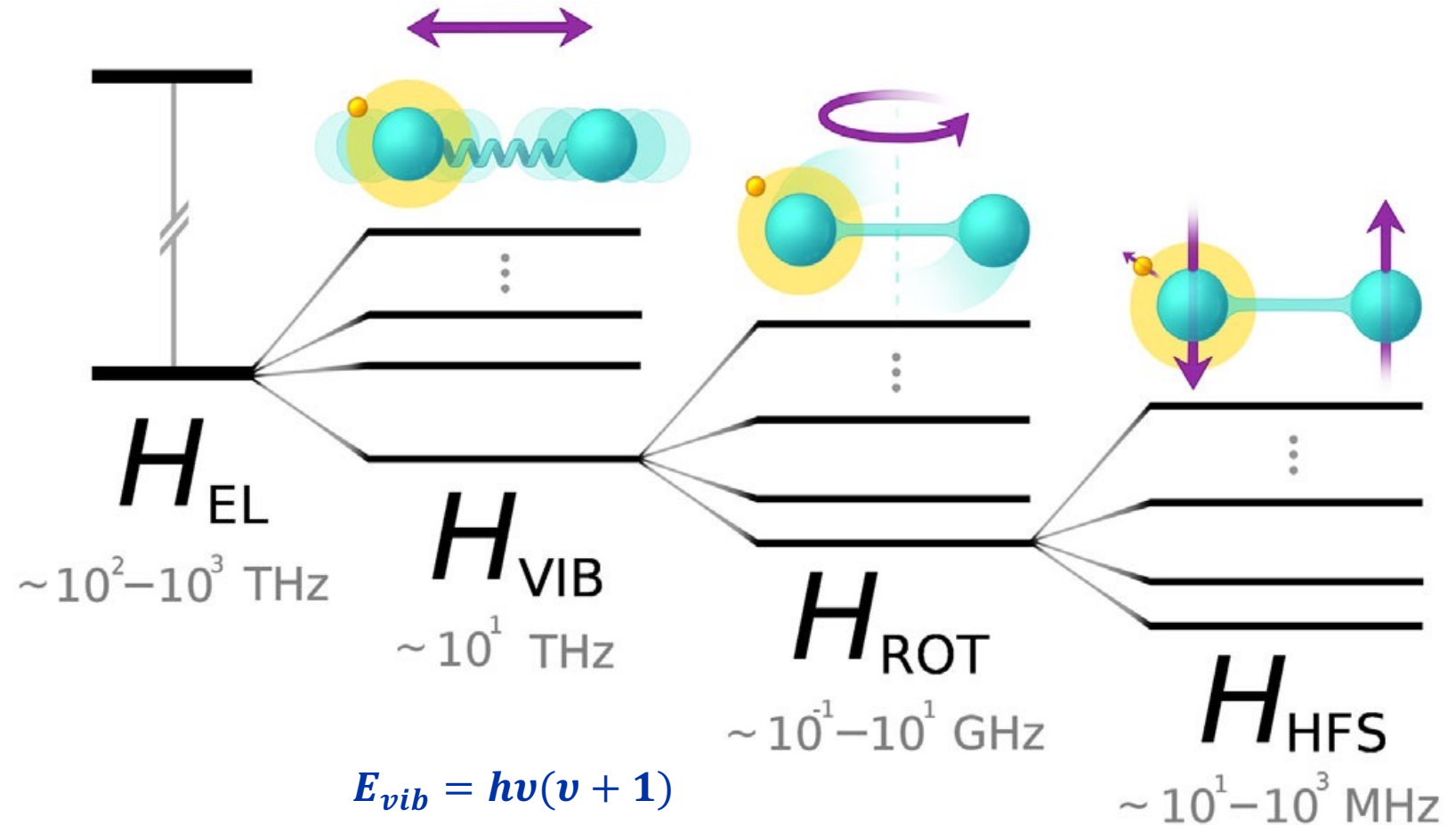


Figure published in [1]

[1] Athanasakis-Kaklamanakis *et al.*, PRX **13** 011015 (2023)

AcF spectroscopy

Experimental [1]

- $(8)\Pi_1 \leftarrow X\ 1\Sigma_0$

Nuclear theory

- *previous values from scaling factors*
- $S_{\text{int}} \leftrightarrow Q_0^3$ [2]
- DFT: $S_{\text{int}}(^{227}\text{Ac}) = 37.1(16) \text{ e fm}^3$,
 $= 1.4 S_{\text{int}}(^{225}\text{Ra}) = 26.6(19) \text{ e fm}^3$ [3]

Molecular theory

- IH-FS-RCCSD
- IP = 48,866 cm^{-1}
- $D_e = 57,214 \text{ cm}^{-1}$

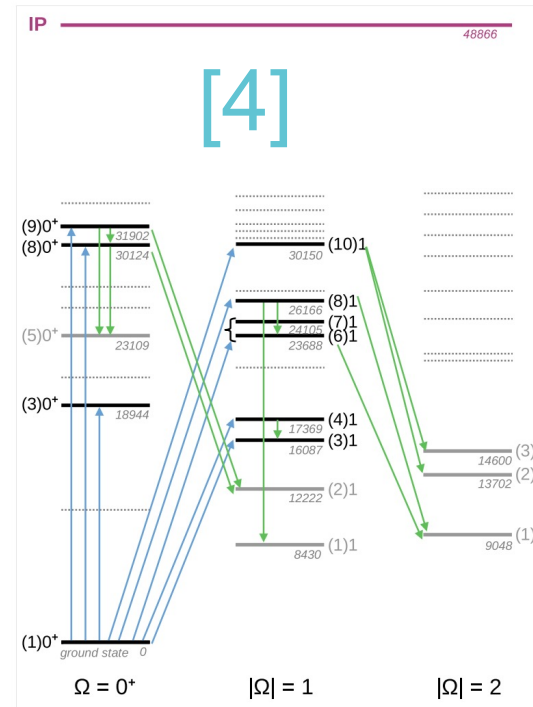


FIG. 3. The strongest transitions (blue arrows) from the $X(1)0^+$ ground state of AcF and the strongest transitions for stimulated emission (green arrows). Levels accessible with two-step excitations are shown with solid gray lines. Dotted lines depict electronic states that are hardly accessible from the ground state with either direct or two-step excitations. It is noted that all transitions to the $\Omega = 0^-$ states have low probabilities and are not shown here. T_e values (cm^{-1}) are shown.

CRIS

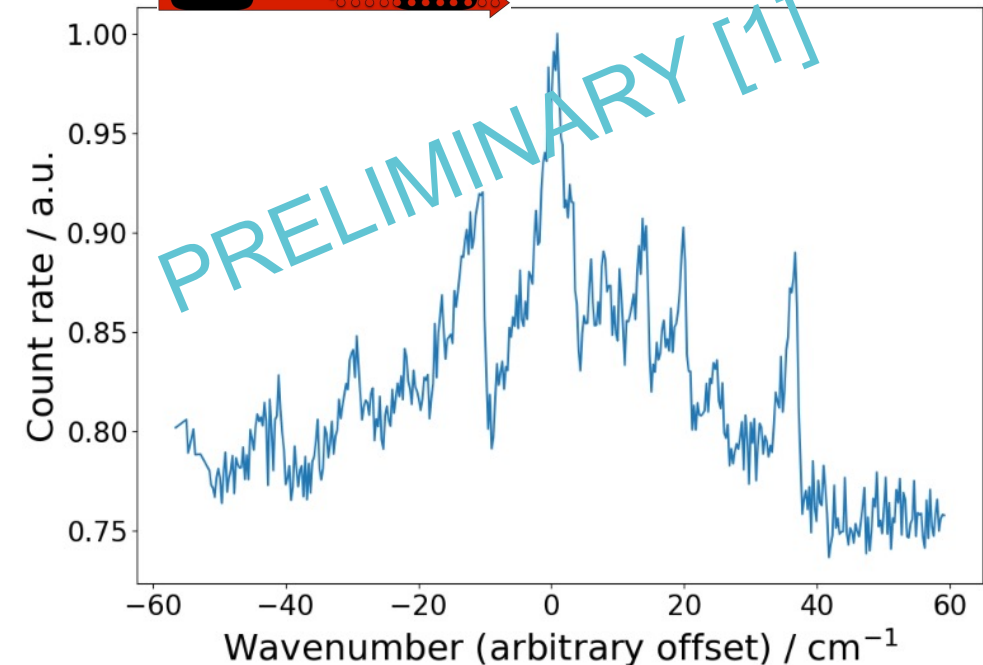


Table 2 Molecular constants X and $W_S^{(2)} = 6X/r^{5P}$ (e/a_B^4 , $a_B = 1$ Bohr) calculated at different levels of theory, given in square brackets

Mol.	State	X [HF]	X [CCSD]	X [CCSD(T)]	r^{5P}	$W_S^{(2)}$ [CCSD(T)]
AcF	$1\Sigma^+$	-2022	-1569	-1593	1.16	-8240
AcN	$1\Sigma^+$	-10 580	-9415	-8950	1.16	-46 295
AcO ⁺	$1\Sigma^+$	-13 362	-11 600	-11 302	1.16	-58 461
ThO	$1\Sigma^+$	-3965	-3187	-3332	1.17	-17 085
EuO ⁺	$(f^6)^a$	-2475 ^a	-2140 ^a	-2114 ^a	1.09	-11 677 ^a
EuN	$(f^6)^a$	-1975 ^a	-1847 ^a	-1890 ^a	1.09	-10 419 ^a
TlF	$1\Sigma^+$	9111	7262	7004	1.13	37 192

^a The spin-orbit part of the GRECP operator has been omitted in the calculation. Therefore, we give only the configuration of the molecular state.

[1] Athanasakis-Kaklamanakis and Au, (2023) *CERN EP newsletter*

[2] Dobaczewski, Engel, Kortelainen, Becker, *Phys. Rev. Lett.* **121**, 232501 (2018)

[3] Athanasakis-Kaklamanakis, Au, Kyuberis, Zülch, Wibowo, Skripnikov, Reilly, Lalanne *et al.*, *in prep.* (2024)

[4] Skripnikov *et al.*, *J. Chem. Phys.* **159** 124301 (2023)

[5] Skripnikov *et al.*, *Phys. Chem. Chem. Phys.* **22** 18374-18380 (2020)

Beam preparation

Molecular formation

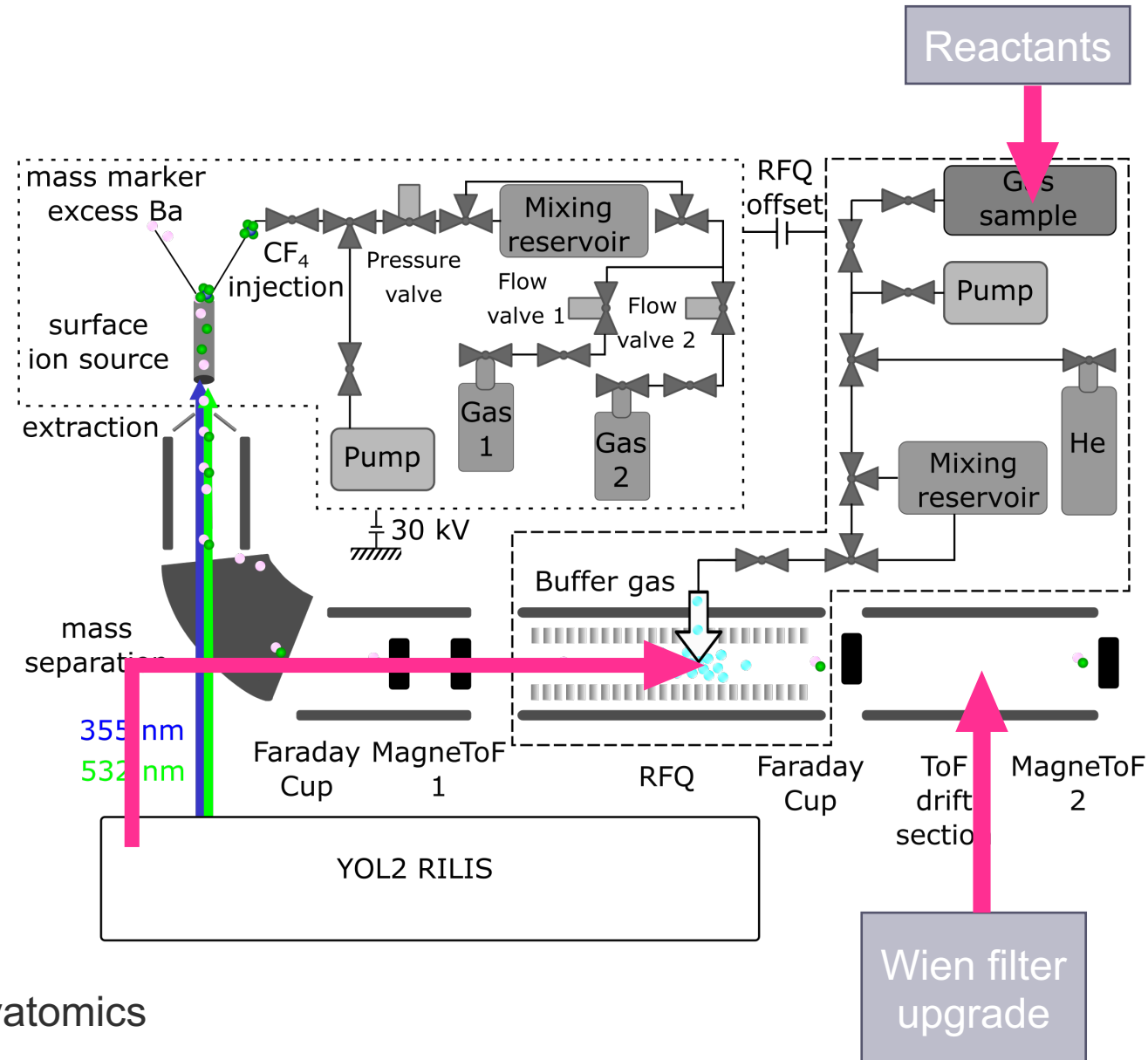
- Ion source developments:
 - FEBIAD, photocathode, LIST
- RFQ gas mixing and injection tests (+TRIUMF)
- Implantation/ablation (+KUL)

Laser setup

- YOL2 laser lab development (+KUL)
- New end of beamline
- Laser path to RFQ

Scheme development / spectroscopy

- In-source: Offline LIST – fluorides, oxides
- In-trap: pending molecular formation studies – polyatomics



Ion source developments

Molecular breakup and characterization studies

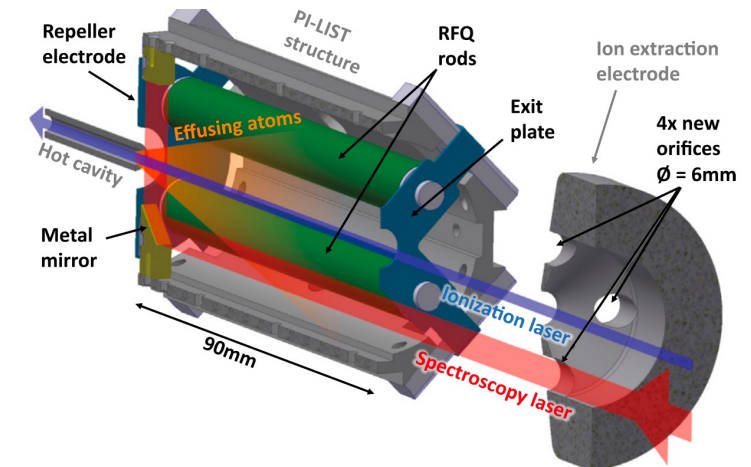
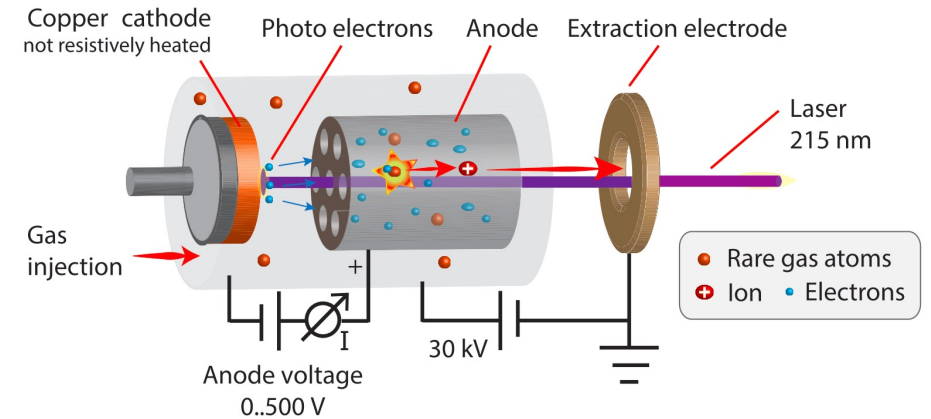
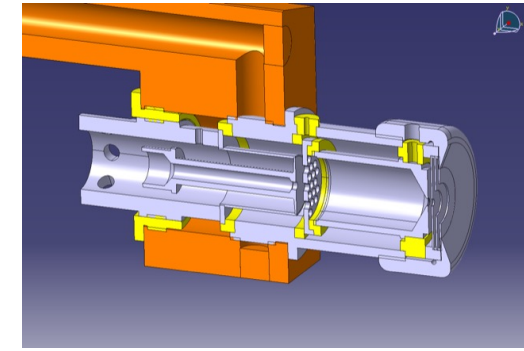
- FEBIAD-type ion sources [1,2]
- Electron energy and source optimization
- Ion source systematics

Photocathode ion sources [3]

- Cold (room-temperature) environments

In-source spectroscopy [4]

- PI-LIST: sub-Doppler hot-cavity in-source spectroscopy
- CERN-ISOLDE implementation



[1] Maldonado (2023) PhD thesis

[2] Martinez Palenzuela (2020) PhD thesis

[3] Ballof . et al., (2022) *J. Phys.: Conf. Ser.* **2244** 012072

[4] Heinke et al. (2023) *NIM B.* **541** (8-12)